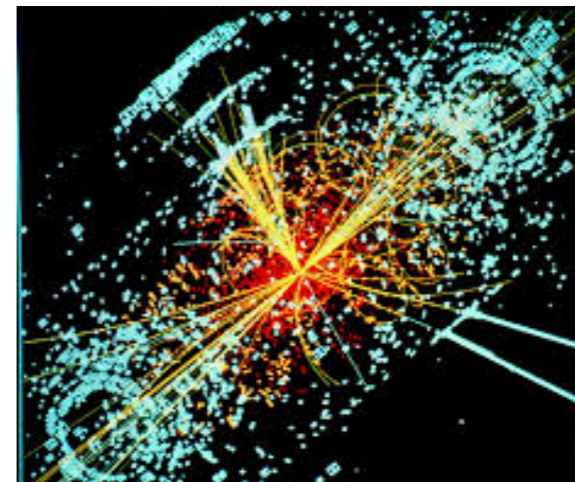


# Physics beyond the Standard Model in the LHC13 era

Howard Baer

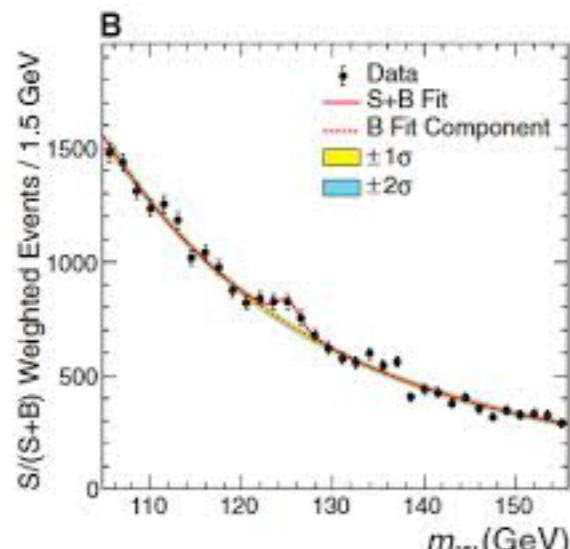
University of Oklahoma

DIS2015 meeting, SMU, Dallas, April 2015



# LHC7-8 era a grand success

- Standard Model vigorously confirmed in both QCD and EW sectors
- discovery of Higgs boson  $m(h) \sim 125.1$  GeV: looks highly SM-like: no significant deviations from SM
- Standard Model reigns supreme! Or does it?



And yet: critical problems remain

# Standard Model

Higgs mass  
unstable:  
Big  
Hierarchy

Strong CP

neutrino mass:

astro:  
DM,  
DE,  
baryogenesis

# an abundance of theoretical proposals!

- many new ideas to address various marginal/transient anomalies or partial solutions to theoretical problems
- House of Cards constructs:  
the further one strays from the SM, the more likely one is to be wrong
- more serious paths:  
SUSY, PQ/axions, see-saw neutrinos =>  
solutions to astro problems



Let data be the guide!

## The Higgs puzzle: scalar fields in QFT:

- quadratic mass divergence causes mass to blow up to highest scale in theory:
  - hard to understand unless

Higgs is composite or protected by some symmetry

so far, newly discovered  $h$  looks fundamental

then SUSY seems likely answer: protects  $m(h)$  to all orders in perturbation theory:  
does the job, once-and-for-all!

mantra: need SUSY at weak scale:  
but no sign of SUSY at LHC!

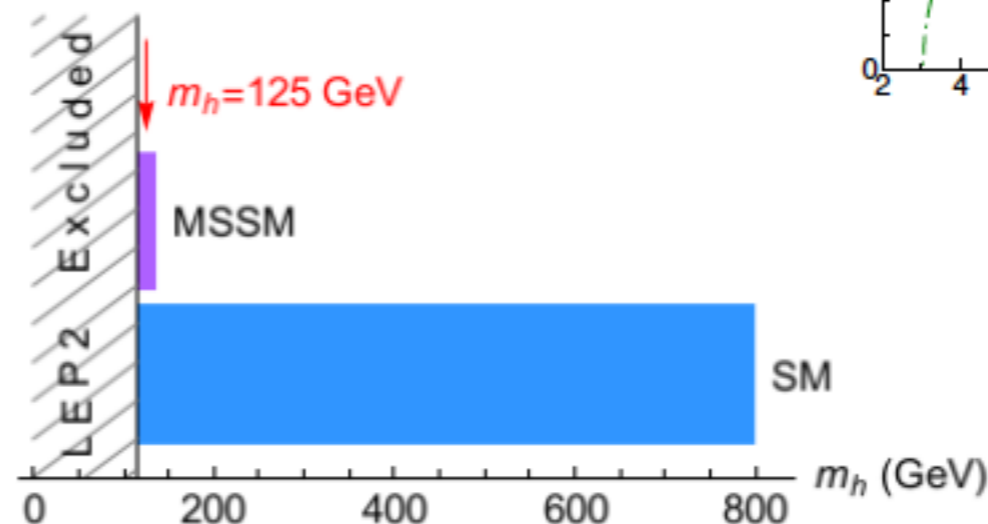
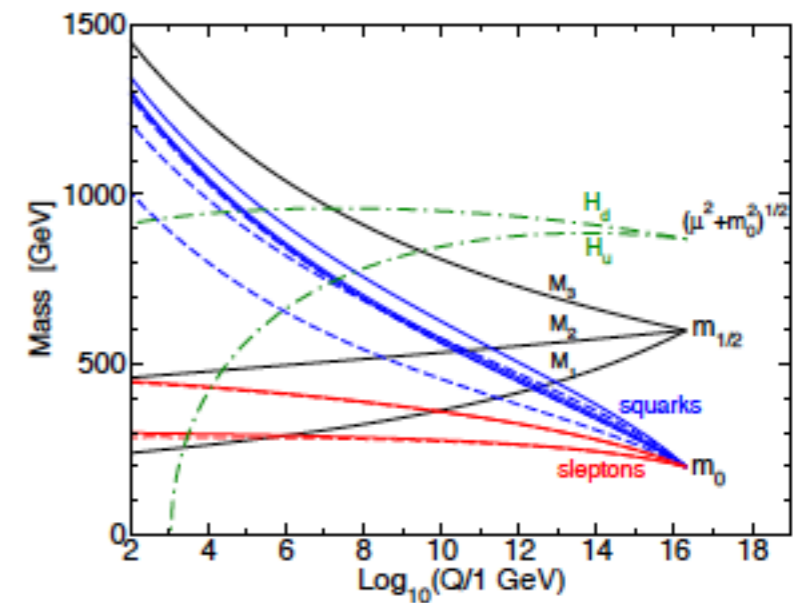
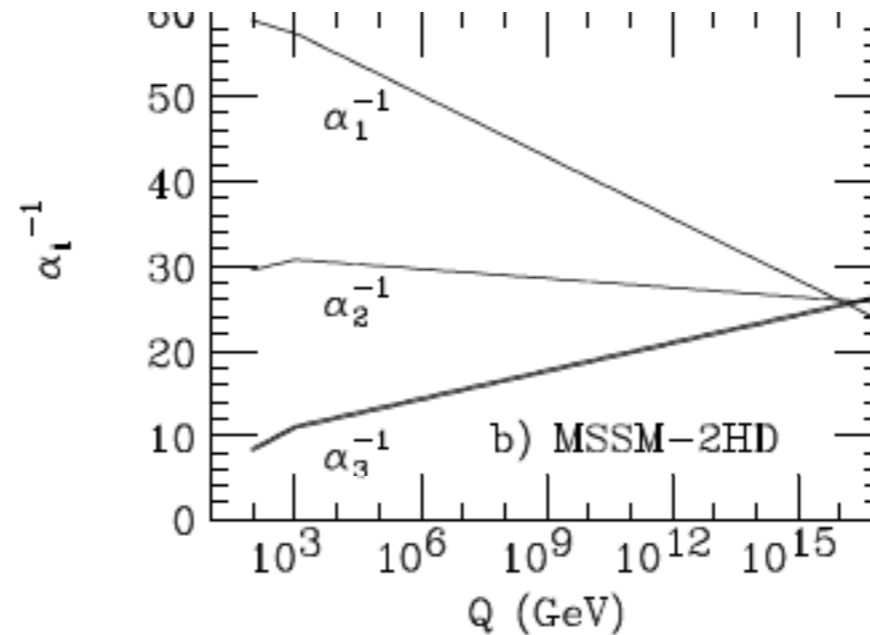
SUSY not as know it?

# Reminder: SUSY/MSSM success stories-match to data!

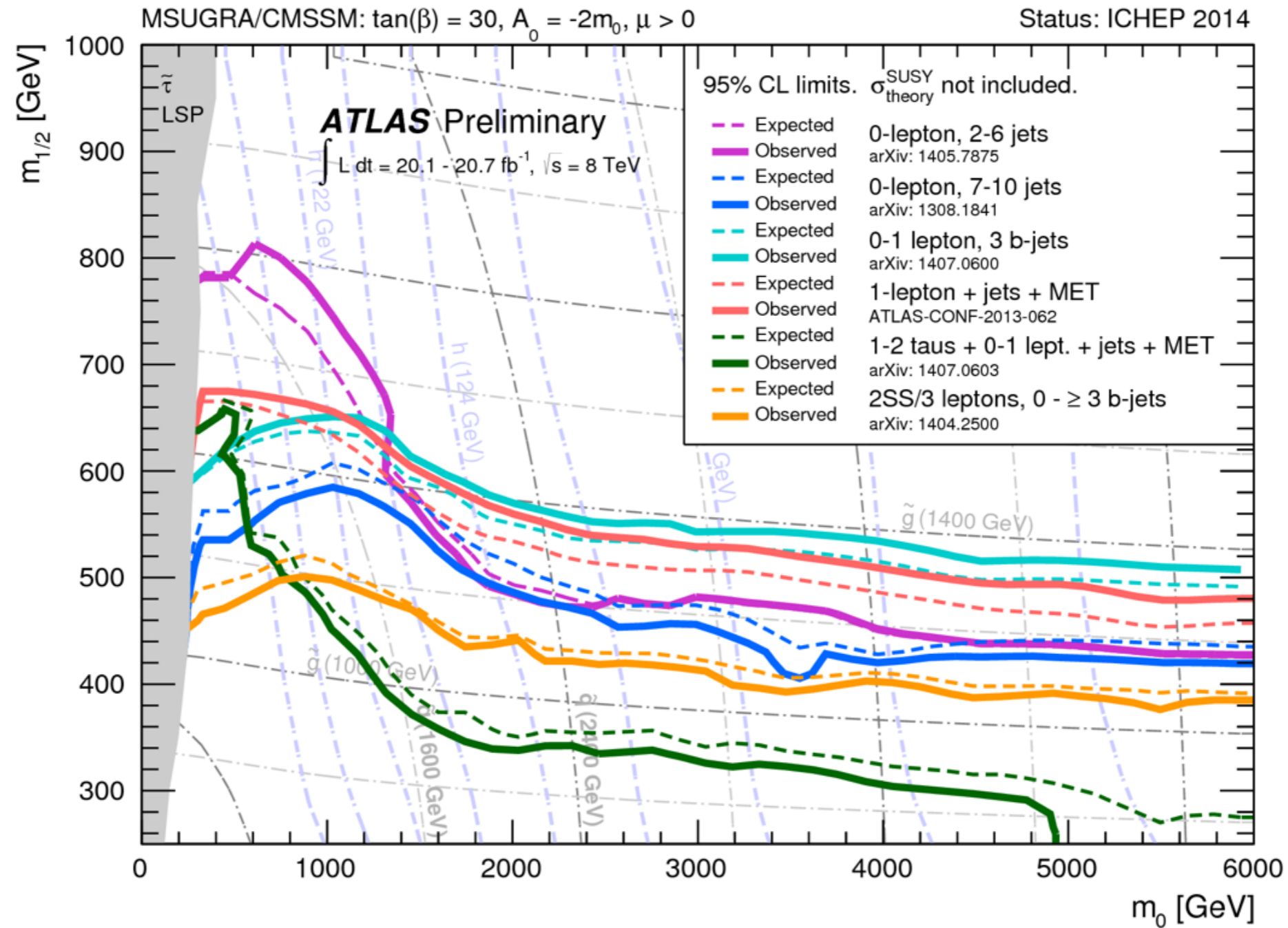
gauge  
coupling  
unification

require  
 $m(t) \sim 150-200$   
GeV for EWSB

predict  
 $m(h) < \sim 130$  GeV



# Where are the sparticles?



$$m_{\tilde{g}} > 1.3 \text{ TeV} \quad (m_{\tilde{q}} \gg m_{\tilde{g}})$$

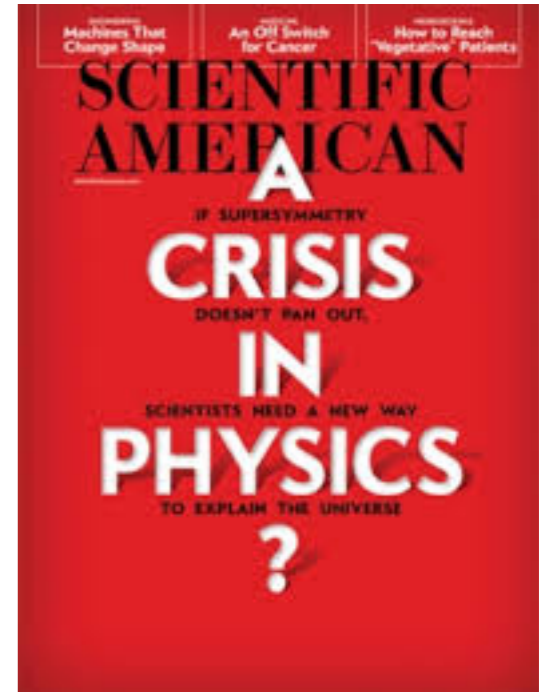
$$m_{\tilde{g}} > 1.8 \text{ TeV} \quad (m_{\tilde{q}} \sim m_{\tilde{g}})$$

$$m_h \simeq 125.1 \text{ GeV} \Rightarrow m_{\tilde{t}_{1,2}} \sim \text{TeV}$$

# Is there a **crisis** in physics?

We have heard for a long time that  
(natural) SUSY requires  
superpartners at the weak scale

Also claim is naturalness requires  
3 third generation squarks  $< 600$  GeV



## Where are the WIMPs “predicted” by WIMP miracle?

*This unshakable fidelity to supersymmetry is widely shared. Particle theorists do admit, however, that the idea of natural supersymmetry is already in trouble and is headed for the dustbin of history unless superpartners are discovered soon...*

Lykken & Spiropolu

It's great to see such a high-profile public discussion of the implications of the collapse of the paradigm long-dominant in some circles which sees SUSY extensions of the Standard Model as the way forward for the field.

Peter Woit blog,  
April 15, 2014

**Sensational claims deserve scrutiny!**



# Three measures of fine-tuning:



But first:

Is observable  $\mathcal{O}$  fine-tuned?

$$\mathcal{O} = \mathcal{O} + b - b$$

Prime directive on fine-tuning:

“Thou shalt not claim fine-tuning of **dependent** quantities one against another!”

HB, Barger, Mickelson, Padeffke-Kirkland, PRD89 (2014) 115019

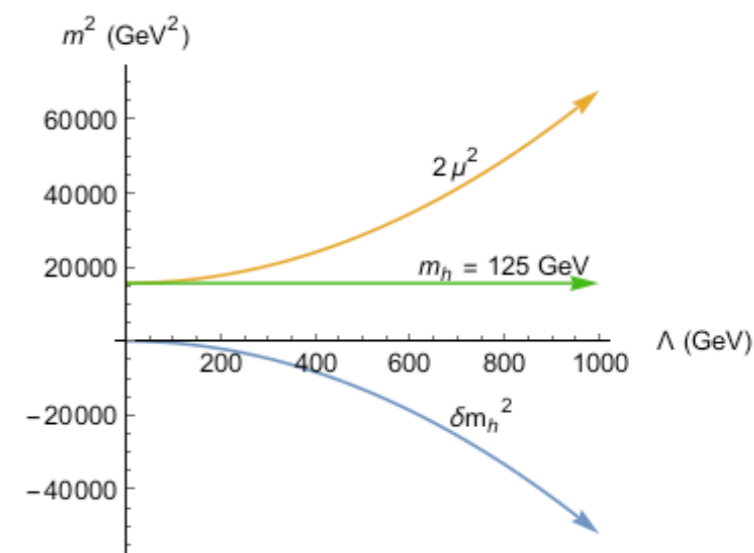


# Naturalness in the Standard Model

SM case: a single Higgs doublet

$$V = -\mu^2 \phi^\dagger \phi + \lambda (\phi^\dagger \phi)^2$$

$$m_h^2 = m_h^2|_{tree} + \delta m_h^2|_{rad}$$



$$m_h^2|_{tree} = 2\mu^2 \quad \delta m_h^2|_{rad} \simeq \frac{3}{4\pi^2} \left( -\lambda_t^2 + \frac{g^2}{4} + \frac{g^2}{8 \cos^2 \theta_W} + \lambda \right) \Lambda^2$$

$m_h^2|_{tree}$  and  $\delta m_h^2|_{rad}$  are independent,

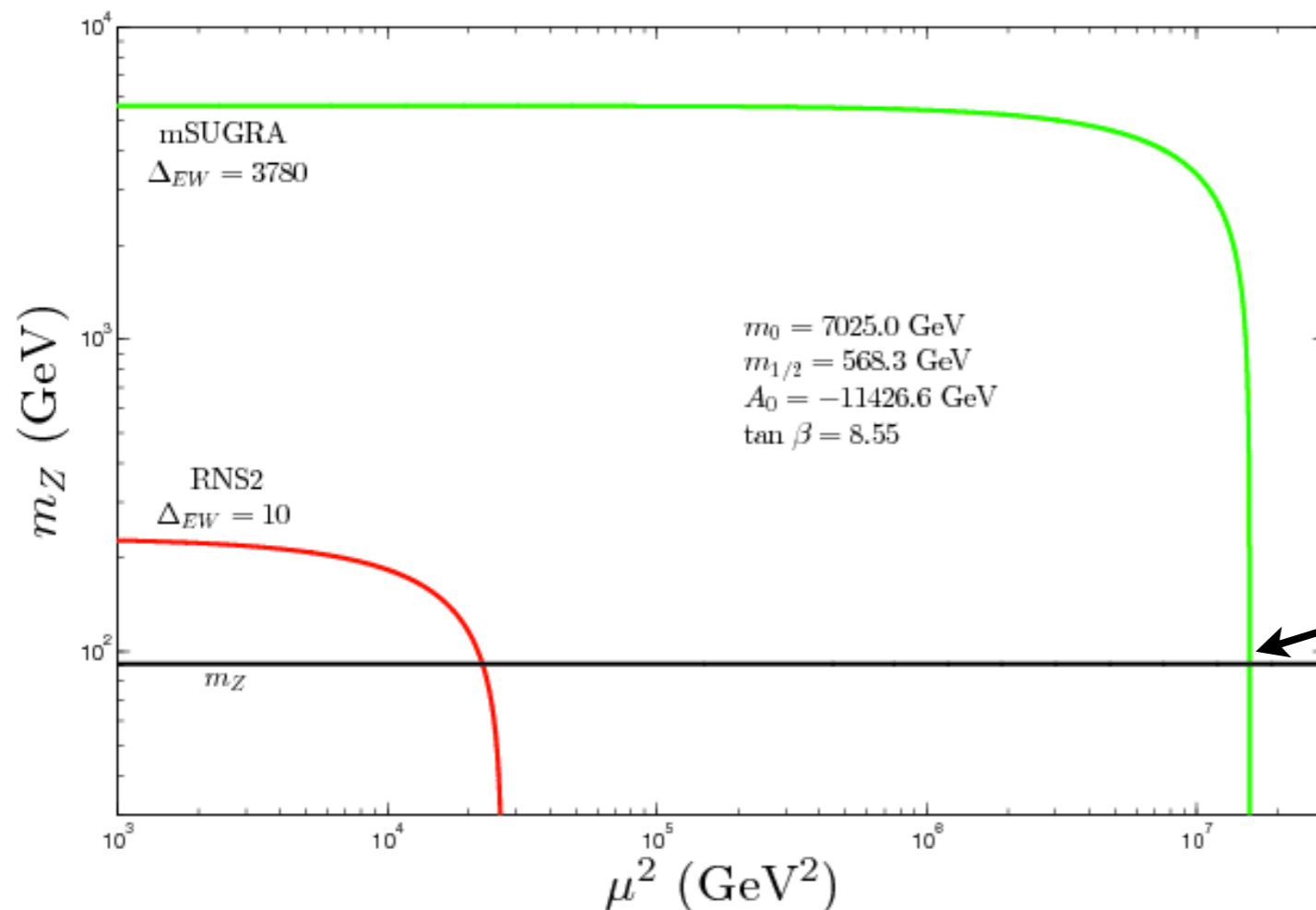
If  $\delta m_h^2$  blows up, can freely adjust (tune)  $2\mu^2$  to maintain  $m_h = 125.5$  GeV

$$\Delta_{SM} \equiv \delta m_h^2|_{rad} / (m_h^2/2)$$

$$\Delta_{SM} < 1 \Rightarrow \Lambda \sim 1 \text{ TeV}$$

First: simple electroweak fine-tuning in MSSM:  
 dial the value of  $\mu$  so that Z mass comes out right:  
 everybody does it, but it is hidden inside spectra codes  
 (Isajet, SuSpect, SoftSUSY, Spheno, SSARD)

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2 \simeq -m_{H_u}^2 - \Sigma_u^u - \mu^2$$



e.g. in CMSSM/  
 mSUGRA:  
 one then concludes  
 nature  
 gives this:

# #1: Simplest SUSY measure: $\Delta_{EW}$

Working only at the weak scale, minimize scalar potential: calculate  $m(Z)$  or  $m(h)$

No large uncorrelated cancellations in  $m(Z)$  or  $m(h)$

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2 \sim -m_{H_u}^2 - \Sigma_u^u - \mu^2$$

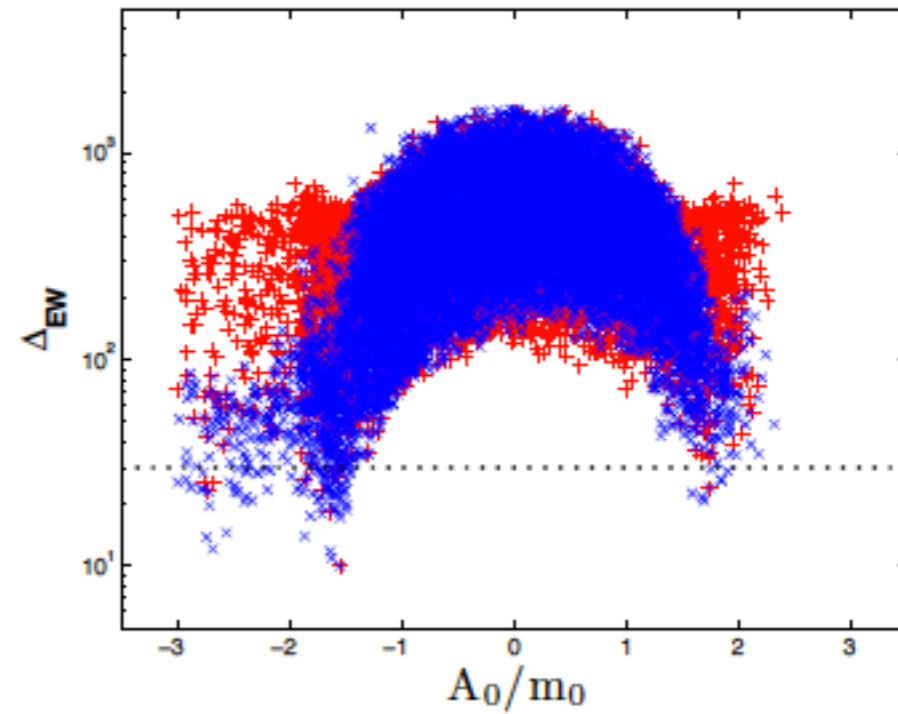
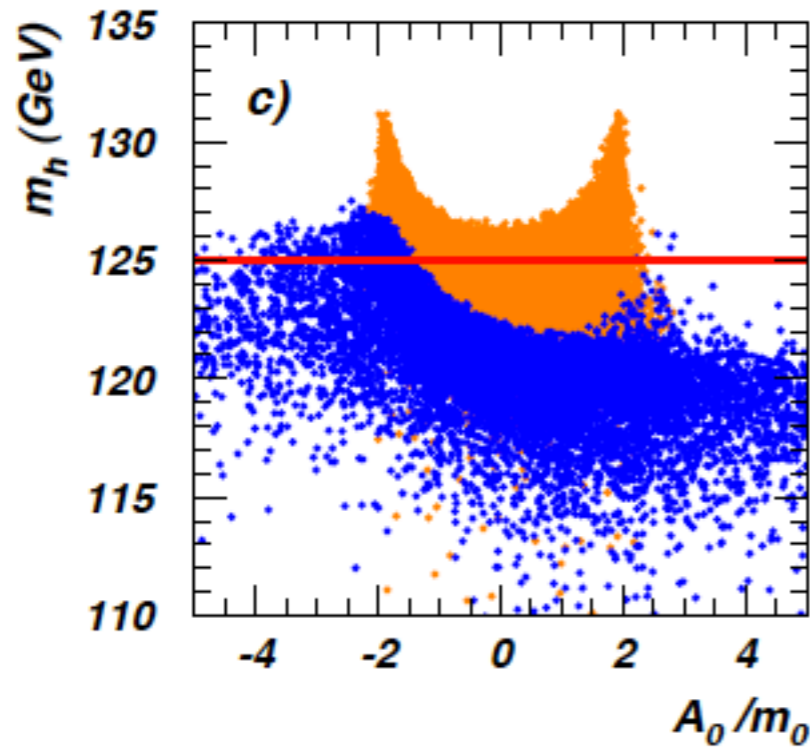
$$\Delta_{EW} \equiv \max_i |C_i| / (m_Z^2/2) \quad \text{with} \quad C_{H_u} = -m_{H_u}^2 \tan^2 \beta / (\tan^2 \beta - 1) \quad \text{etc.}$$

simple, direct, unambiguous interpretation:

- $|\mu| \sim m_Z \sim 100 - 200 \text{ GeV}$
- $m_{H_u}^2$  should be driven to small negative values such that  $-m_{H_u}^2 \sim 100 - 200 \text{ GeV}$  at the weak scale and
- that the radiative corrections are not too large:  $\Sigma_u^u \lesssim 100 - 200 \text{ GeV}$

Radiative natural SUSY with a 125 GeV Higgs boson (with V. Barger, P. Huang, A. Mustafayev and X. Tata), Phys. Rev. Letters **109** 161802 (2012).

Large value of  $A_t$  reduces  $\Sigma_u^u(\tilde{t}_{1,2})$  contributions to  $\Delta_{EW}$  while uplifting  $m_h$  to  $\sim 125$  GeV



$$\Sigma_u^u(\tilde{t}_{1,2}) = \frac{3}{16\pi^2} F(m_{\tilde{t}_{1,2}}^2) \left[ f_t^2 - g_Z^2 \mp \frac{f_t^2 A_t^2 - 8g_Z^2 \left(\frac{1}{4} - \frac{2}{3}x_W\right) \Delta_t}{m_{\tilde{t}_2}^2 - m_{\tilde{t}_1}^2} \right]$$

$$\Delta_t = (m_{\tilde{t}_L}^2 - m_{\tilde{t}_R}^2)/2 + M_Z^2 \cos 2\beta \left(\frac{1}{4} - \frac{2}{3}x_W\right)$$

$$F(m^2) = m^2 \left( \log \frac{m^2}{Q^2} - 1 \right) \quad Q^2 = m_{\tilde{t}_1} m_{\tilde{t}_2}$$

## #2: Higgs mass or large-log fine-tuning

 $\Delta_{HS}$ 

$$m_h^2 \simeq \mu^2 + m_{H_u}^2 + \delta m_{H_u}^2|_{rad}$$

$$\frac{dm_{H_u}^2}{dt} = \frac{1}{8\pi^2} \left( -\frac{3}{5}g_1^2 M_1^2 - 3g_2^2 M_2^2 + \frac{3}{10}g_1^2 S + 3f_t^2 X_t \right) \quad X_t = m_{Q_3}^2 + m_{U_3}^2 + m_{H_u}^2 + A_t^2$$

neglect gauge pieces, S,  $m_{H_u}$  and running;  
then we can integrate from  $m(\text{SUSY})$  to  $\Lambda$

$$\delta m_{H_u}^2|_{rad} \sim -\frac{3f_t^2}{8\pi^2} (m_{Q_3}^2 + m_{U_3}^2 + A_t^2) \ln(\Lambda^2/m_{\text{SUSY}}^2)$$

$$\Delta_{HS} \sim \delta m_h^2 / (m_h^2/2) < 10 \quad \text{then} \quad m_{\tilde{t}_{1,2}, \tilde{b}_1} < 500 \text{ GeV}$$

$$m_{\tilde{g}} < 1.5 \text{ TeV}$$

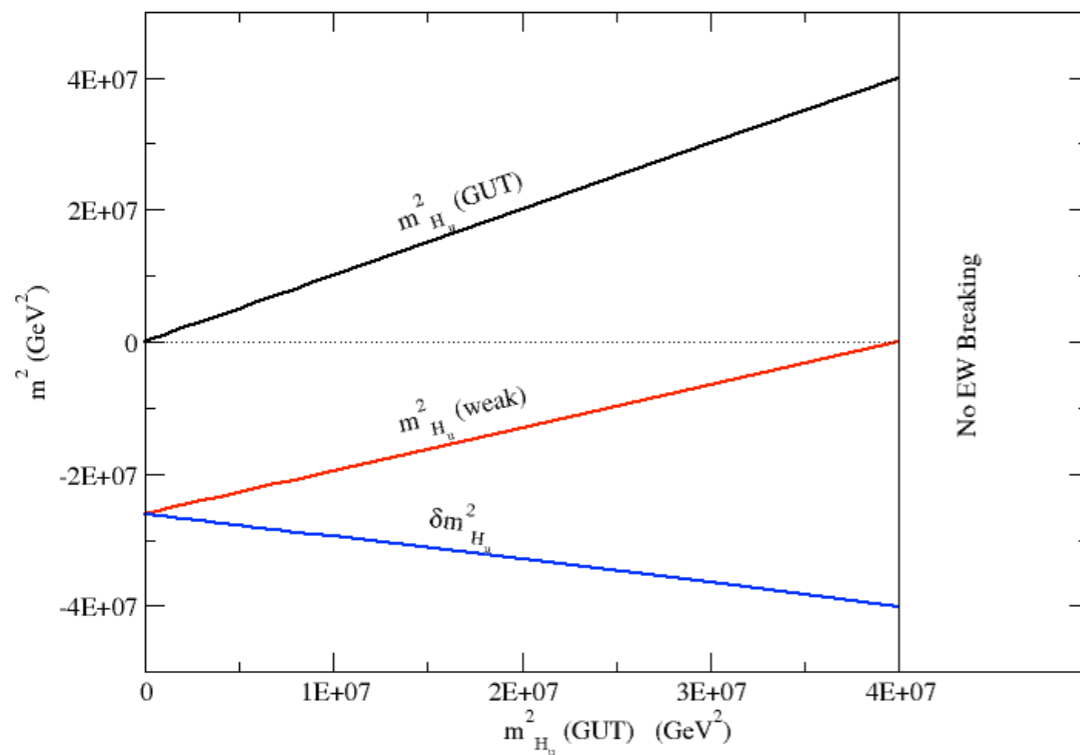
$A_t$  can't be too big

old natural SUSY

What's wrong with this argument?  
 In zeal for simplicity, have made several simplifications: most **egregious** is that one sets  $m(H_u)^2=0$  at beginning to simplify

$m_{H_u}^2(\Lambda)$  and  $\delta m_{H_u}^2$  are *not* independent!

**violates prime directive!**



The larger  $m_{H_u}^2(\Lambda)$  becomes, then the larger becomes the cancelling correction!



To fix: combine dependent terms:

$m_h^2 \simeq \mu^2 + (m_{H_u}^2(\Lambda) + \delta m_{H_u}^2)$  where now both  $\mu^2$  and  $(m_{H_u}^2(\Lambda) + \delta m_{H_u}^2)$  are  $\sim m_Z^2$

After re-grouping:  $\Delta_{HS} \simeq \Delta_{EW}$

Instead of: the radiative correction  $\delta m_{H_u}^2 \sim m_Z^2$   
we now have: the radiatively-corrected  $m_{H_u}^2 \sim m_Z^2$

### #3: EENZ/BG traditional measure $\Delta_{BG}$

Such a re-grouping is properly used  
in the EENZ/BG measure:

$$\Delta_{BG} \equiv \max_i [c_i], \quad \text{where } c_i = \left| \frac{\partial \ln m_Z^2}{\partial \ln p_i} \right| = \left| \frac{p_i}{m_Z^2} \frac{\partial m_Z^2}{\partial p_i} \right|$$

the  $p_i$  constitute the fundamental parameters of the model.

for pMSSM, obviously  $\Delta_{BG} \simeq \Delta_{EW}$

What about models defined at high scale?

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 - m_{H_u}^2 \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2 \simeq -m_{H_u}^2 - \mu^2$$

express **weak scale value** in terms of high scale parameters

Express  $m(Z)$  in terms of GUT scale parameters:

$$m_Z^2 \simeq -2m_{H_u}^2 - 2\mu^2 \quad (\text{weak scale relation})$$

$$-2\mu^2(m_{SUSY}) = -2.18\mu^2$$

$$\begin{aligned} -2m_{H_u}^2(m_{SUSY}) = & 3.84M_3^2 + 0.32M_3M_2 + 0.047M_1M_3 - 0.42M_2^2 \\ & + 0.011M_2M_1 - 0.012M_1^2 - 0.65M_3A_t - 0.15M_2A_t \\ & - 0.025M_1A_t + 0.22A_t^2 + 0.004m_3A_b \\ & - 1.27m_{H_u}^2 - 0.053m_{H_d}^2 \\ & + 0.73m_{Q_3}^2 + 0.57m_{U_3}^2 + 0.049m_{D_3}^2 - 0.052m_{L_3}^2 + 0.053m_{E_3}^2 \\ & + 0.051m_{Q_2}^2 - 0.11m_{U_2}^2 + 0.051m_{D_2}^2 - 0.052m_{L_2}^2 + 0.053m_{E_2}^2 \\ & + 0.051m_{Q_1}^2 - 0.11m_{U_1}^2 + 0.051m_{D_1}^2 - 0.052m_{L_1}^2 + 0.053m_{E_1}^2, \end{aligned}$$

all GUT scale  
parameters

Ibanez, Lopez, Munoz;  
Lleyda, Munoz

Kane, King

Abe, Kobayashi, Omura;  
S. P. Martin

For generic parameter choices,  $\Delta_{BG}$  is large

But if:  $m_{Q_{1,2}} = m_{U_{1,2}} = m_{D_{1,2}} = m_{L_{1,2}} = m_{E_{1,2}} \equiv m_{16}(1,2)$  then  $\sim 0.007m_{16}^2(1,2)$

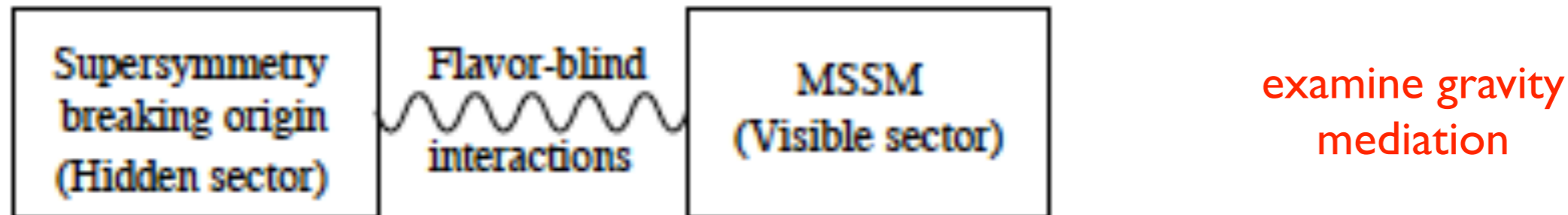
Even better:  $m_{H_u}^2 = m_{H_d}^2 = m_{16}^2(3) \equiv m_0^2 \Rightarrow -0.017m_0^2$

**For correlated parameters, EWFT collapses in 3rd gen. sector!**

- Usually  $\Delta_{BG}$  is applied to *multi-parameter effective theories* where multiple soft terms are adopted as parameter set.
- For these theories, the multiple soft terms parametrize our ignorance of details of the hidden sector SUSY breaking.
- But in supergravity, for any given hidden sector, soft terms are all *dependent* and can be computed as multiples of  $m_{3/2}$ .

Thus, the usual evaluation of  $\Delta_{BG}$  also **violates the prime directive!**

To properly apply BG measure, need to identify **independent** soft breaking terms



For any particular SUSY breaking hidden sector, each soft term is some multiple of gravitino mass  $m_{3/2}$

$$m_{H_u}^2 = a_{H_u} \cdot m_{3/2}^2,$$

$$m_{Q_3}^2 = a_{Q_3} \cdot m_{3/2}^2,$$

$$A_t = a_{A_t} \cdot m_{3/2},$$

$$M_i = a_i \cdot m_{3/2},$$

....

Soni, Weldon (1983);  
Kaplunovsky, Louis (1992);  
Brignole, Ibanez, Munoz (1993)

Since we don't know hidden sector, we impose parameters which parameterize our ignorance:

**but this doesn't mean each parameter is independent**

e.g. dilaton-dominated SUSY breaking:  $m_0^2 = m_{3/2}^2$  with  $m_{1/2} = -A_0 = \sqrt{3}m_{3/2}$

Writing each soft term as a multiple of  $m(3/2)$  then we allow for correlations/cancellations:

$$m_Z^2 = -2.18\mu^2 + a \cdot m_{3/2}^2$$

numerical co-efficient which depends on hidden sector

for naturalness, then

$$\mu^2 \sim m_Z^2 \quad \text{and} \quad a \cdot m_{3/2}^2 \sim m_Z^2$$

either  $m_{3/2} \sim m_Z$  or  $a$  is small

$$m_Z^2 \simeq -2\mu^2(\text{weak}) - 2m_{H_u}^2(\text{weak}) \simeq -2.18\mu^2(\text{GUT}) + a \cdot m_{3/2}^2$$

then

$$-m_{H_u}^2(\text{weak}) \sim a \cdot m_{3/2}^2 \sim m_Z^2$$

$$\lim_{n_{SSB} \rightarrow 1} \Delta_{BG} \rightarrow \Delta_{EW}$$

Thus, correctly applying these measures by first collecting dependent quantities, we find that— at tree level— all agree:

$$\Delta_{HS} \simeq \Delta_{BG} \simeq \Delta_{EW}$$

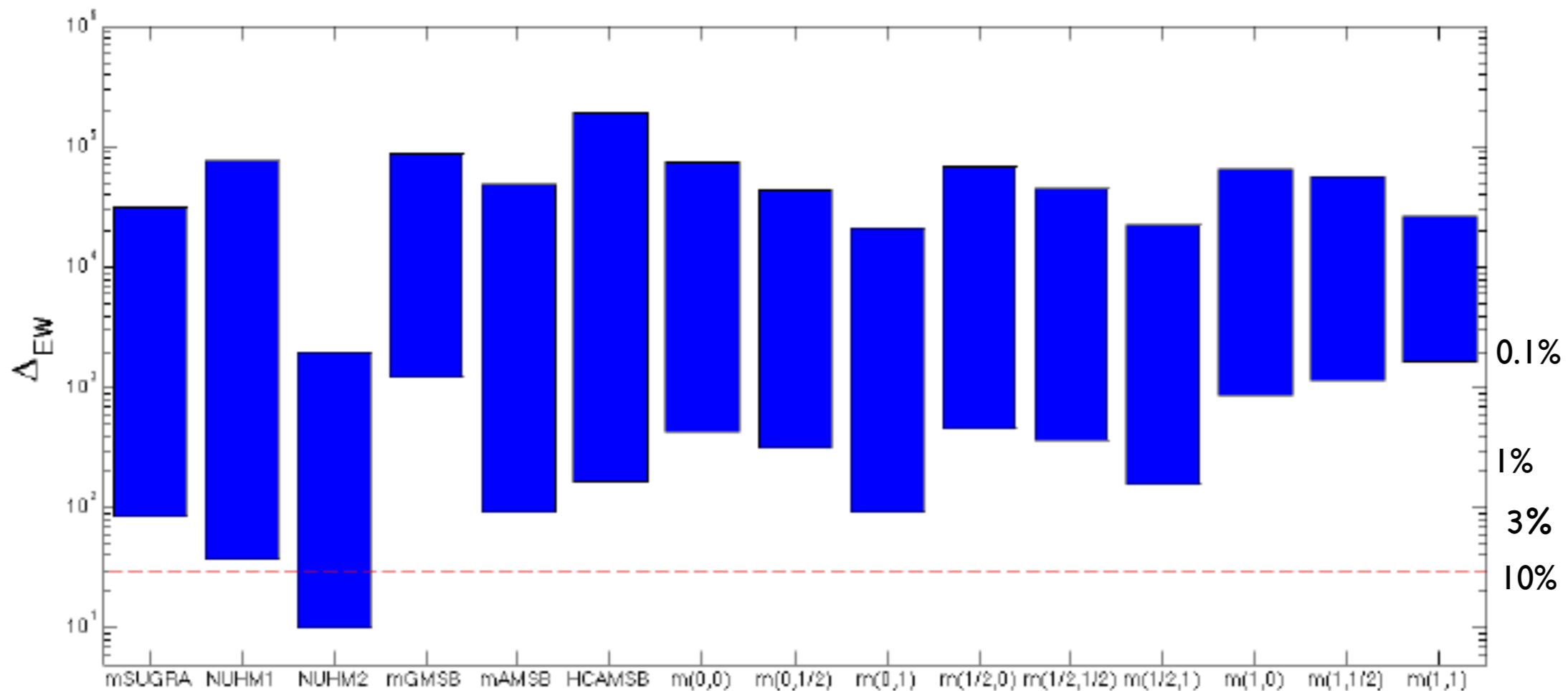
Due to ease of use and including radiative corrections, and due to its explicit model independence, we will use

$$\Delta_{EW}$$

for remainder of talk

Often claimed that  $\Delta_{EW}$  doesn't include high scale effects:  
 not true: it selects out high scale models which can  
 naturally produce  $m(W,Z,h) \sim 100$  GeV

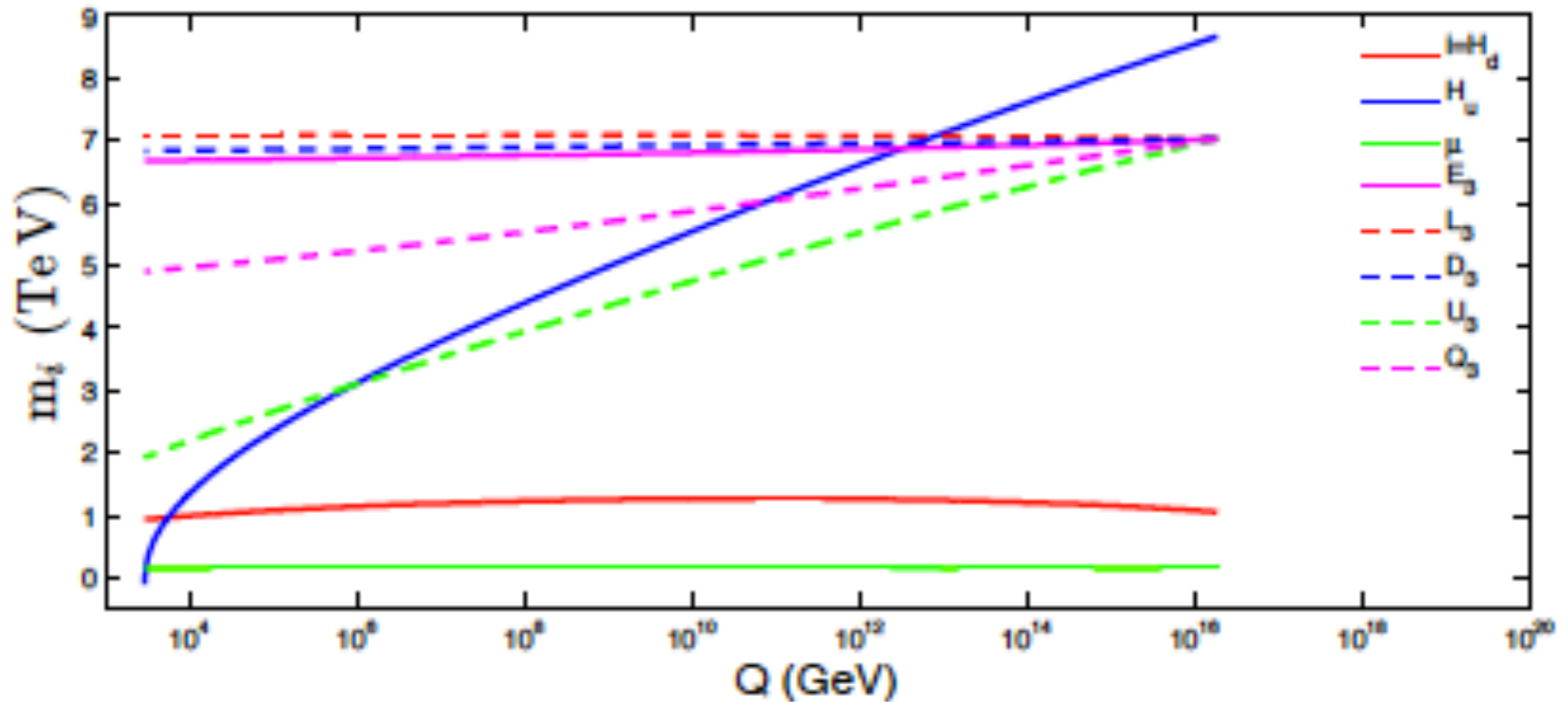
scan over p-space with  $m(h) = 125.5 \pm 2.5$  GeV:



need large  $A_t$  and some non-universality e.g. NUHM2 model



Applied properly, all three measures agree:  
**naturalness is unambiguous and highly predictive!**



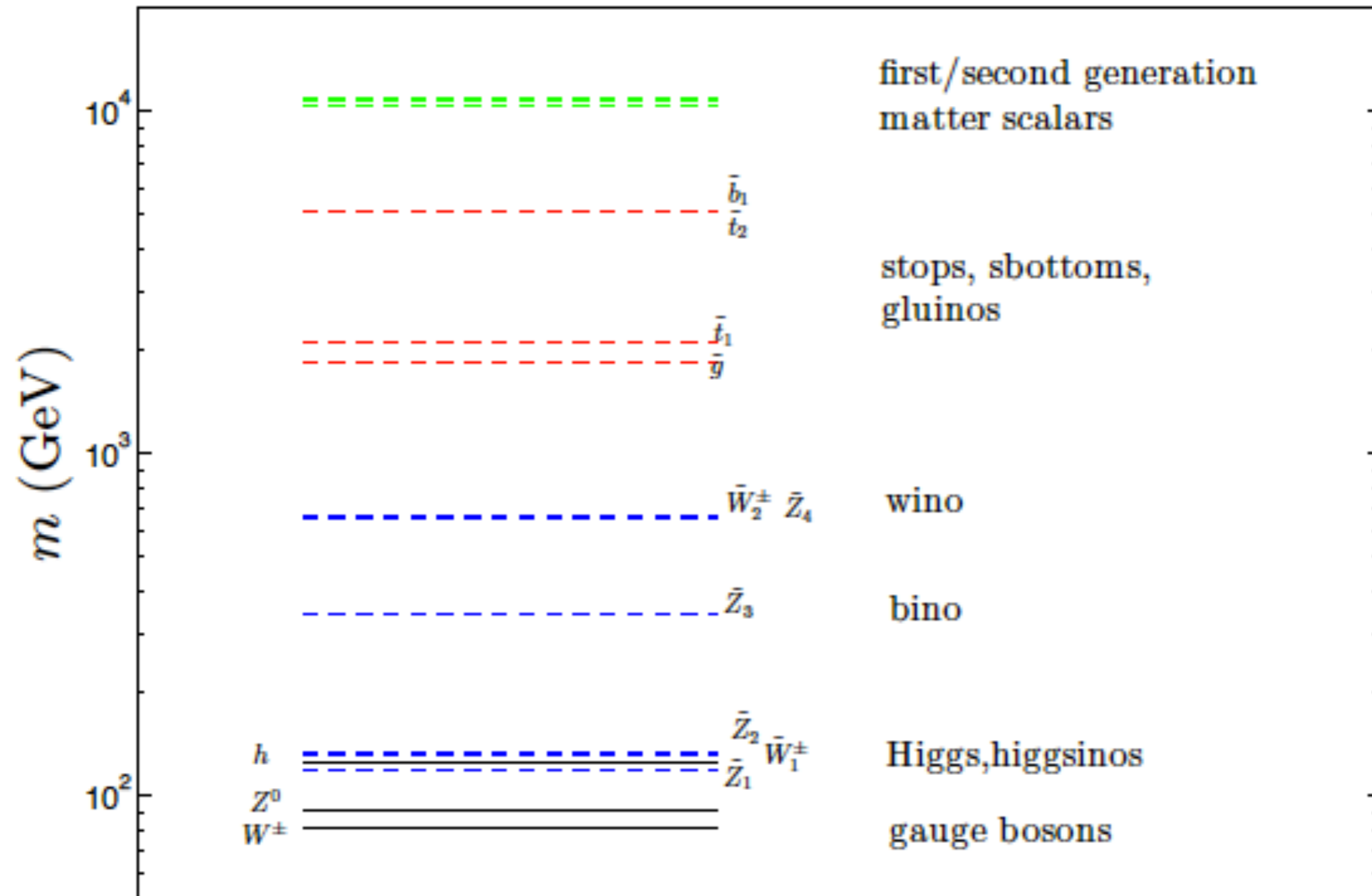
Radiatively-driven natural SUSY, or RNS:

(typically need  $m_{Hu} \sim 25\text{--}50\%$  higher than  $m_0$ )

H. Baer, V. Barger, P. Huang, A. Mustafayev and X. Tata, *Phys. Rev. Lett.* **109** (2012) 161802.

H. Baer, V. Barger, P. Huang, D. Mickelson, A. Mustafayev and X. Tata, *Phys. Rev. D* **87** (2013) 115028 [arXiv:1212.2655 [hep-ph]].

# Typical spectrum for low $\Delta_{EW}$ models

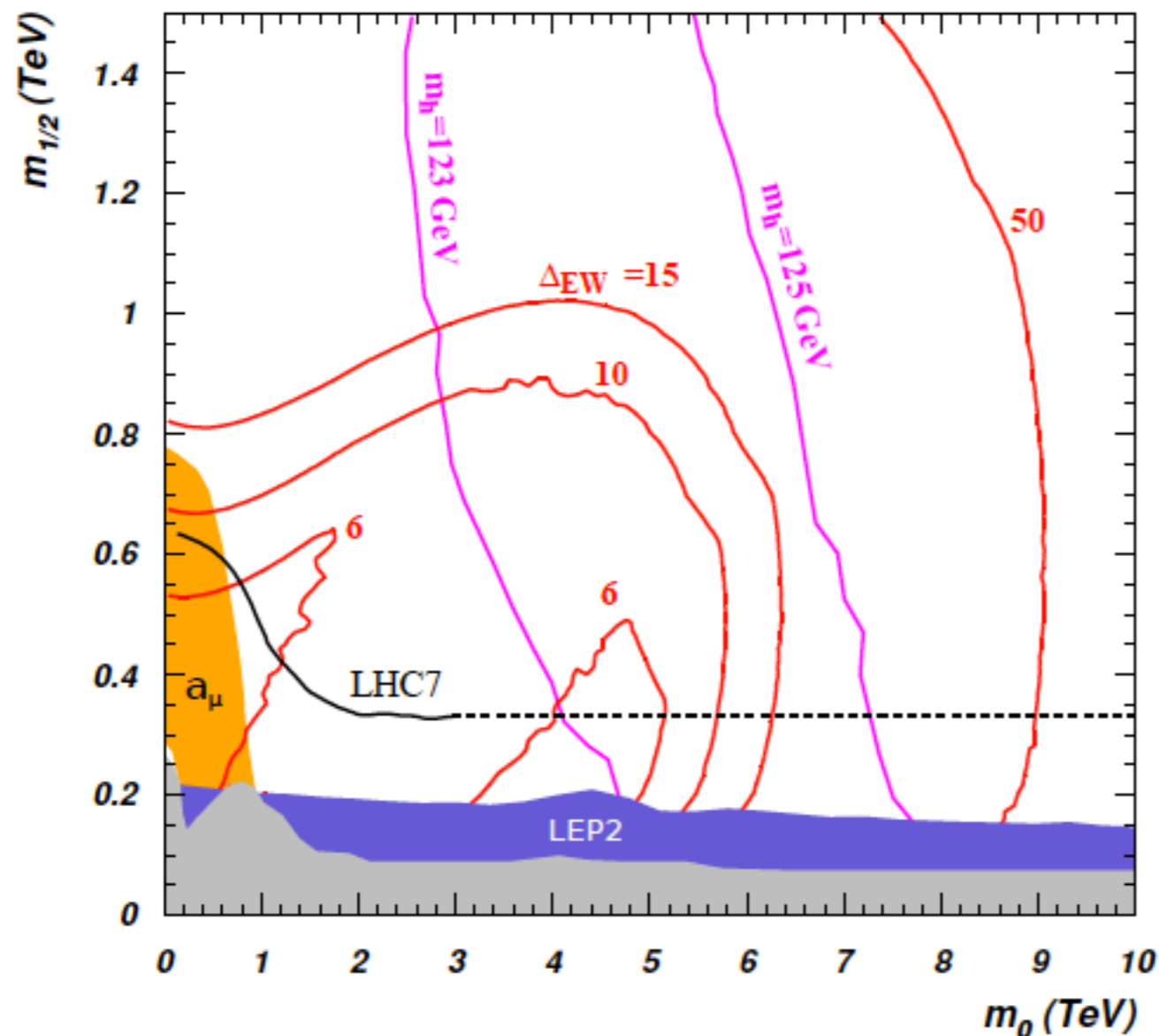


There is a Little Hierarchy, but it is **no problem**

$m_{H_u}^2$  is radiatively driven to natural values and  $\mu \ll m_{3/2}$

# Good old $m_0$ vs. $m_{1/2}$ plane still viable, but require low $\mu$ (NUHM2)

NUHM2:  $\tan\beta=10$ ,  $A_0=-1.6m_0$ ,  $\mu=150$  GeV,  $m_t=173.2$  GeV



$\mu = 150$  GeV throughout  
which is allowed for NUHM2

SUSY **mu problem**: mu term is SUSY, not SUSY breaking:  
expect  $\mu \sim M(\text{Pl})$  but phenomenology requires  $\mu \sim m(\text{Z})$

- NMSSM:  $\mu \sim m(3/2)$ ; beware singlets!
- Giudice–Masiero: mu forbidden by some symmetry:  
generate via Higgs coupling to hidden sector
- **Kim–Nilles**: invoke SUSY version of DFSZ axion  
solution to strong CP:

KN: PQ symmetry forbids mu term,  
but then it is generated via PQ breaking

Little Hierarchy due to mismatch between  
PQ breaking and SUSY breaking scales?

$$W_{DFSZ} \ni \lambda S^2 H_u H_d / M_P$$

$$\mu \sim \lambda f_a^2 / M_P$$

$$m_{3/2} \sim m_{hid}^2 / M_P$$

$$f_a \ll m_{hid}$$

**Higgs mass tells us where  
to look for axion!**

$$m_a \sim 6.2 \mu\text{eV} \left( \frac{10^{12} \text{ GeV}}{f_a} \right)$$

# Little Hierarchy from radiative PQ breaking? explore within context of MSY model

Murayama, Suzuki, Yanagida (1992);

Gherghetta, Kane (1995)

Choi, Chun, Kim (1996)

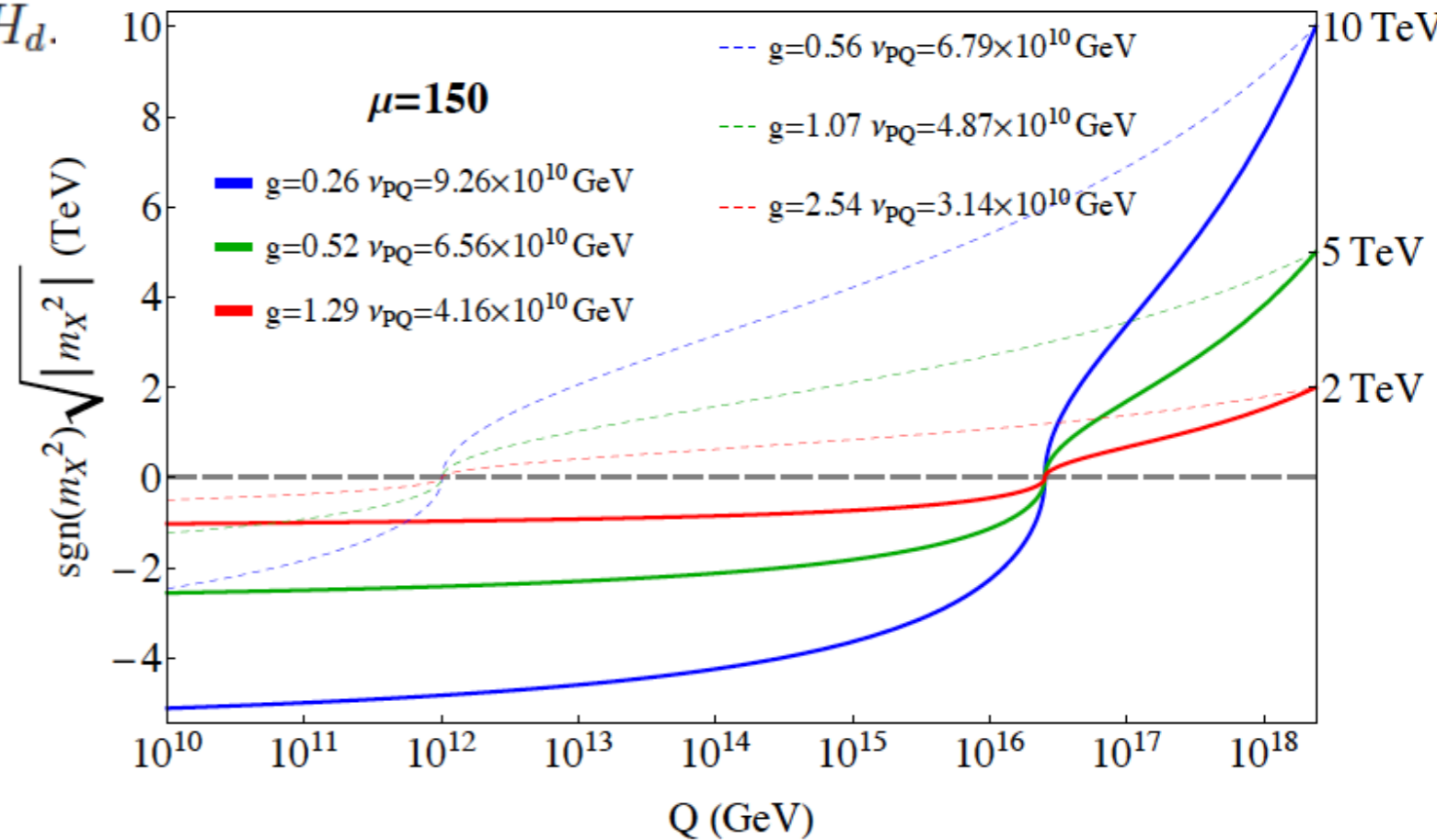
Bae, HB, Serce, PRD91 (2015) 015003

## augment MSSM with PQ charges/fields:

$$\hat{f}' = \frac{1}{2} h_{ij} \hat{X} \hat{N}_i^c \hat{N}_j^c + \frac{f}{M_P} \hat{X}^3 \hat{Y} + \frac{g}{M_P} \hat{X} \hat{Y} \hat{H}_u \hat{H}_d.$$

$$M_{N_i^c} = v_X h_i |_{Q=v_X}$$

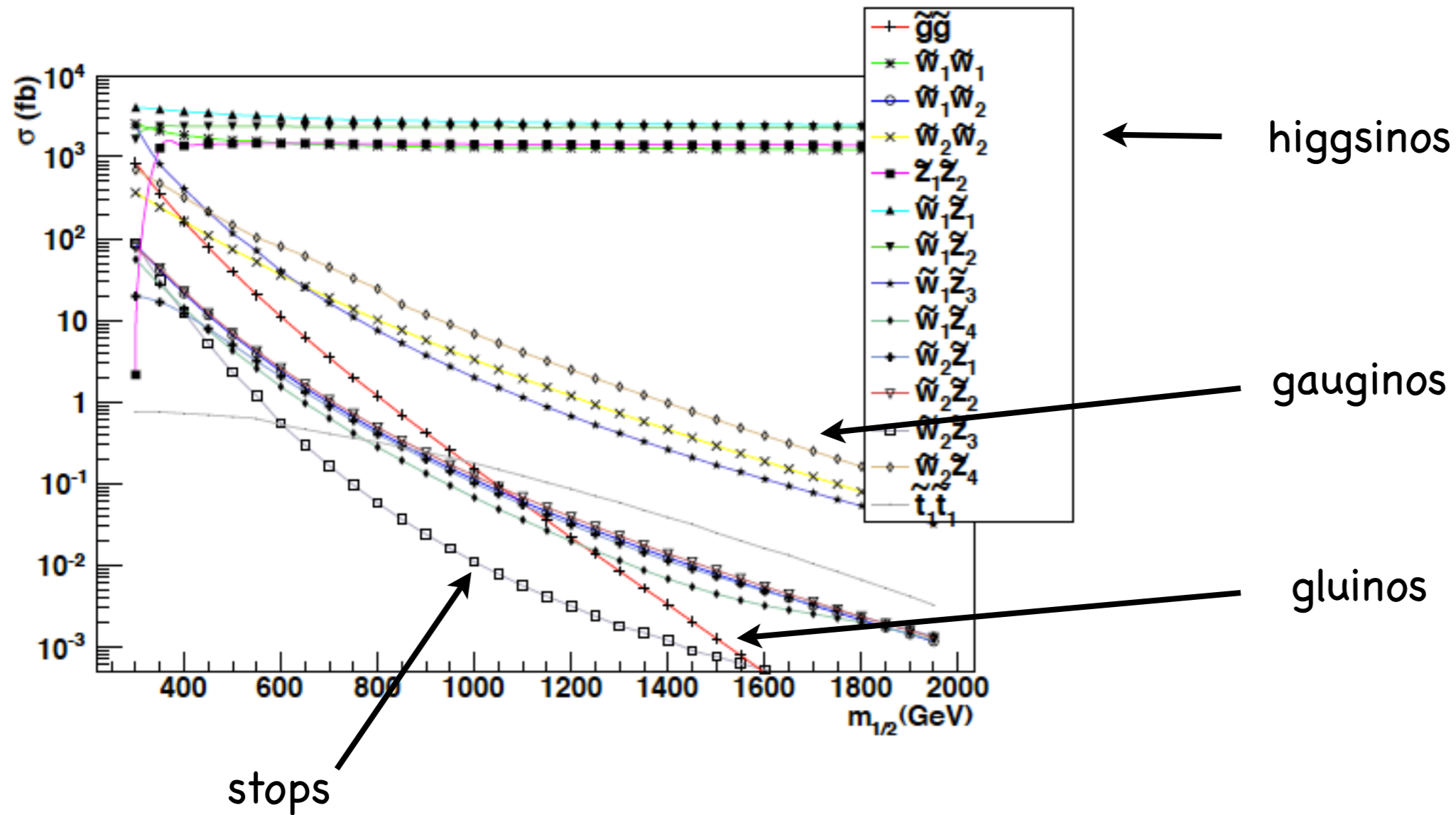
$$\mu = g \frac{v_X v_Y}{M_P}.$$



Large  $m_{3/2}$  generates small  $\mu \sim 100 - 200$  GeV!

# Prospects for discovering RNS at LHC and ILC

# Sparticle prod'n along RNS model-line at LHC14:



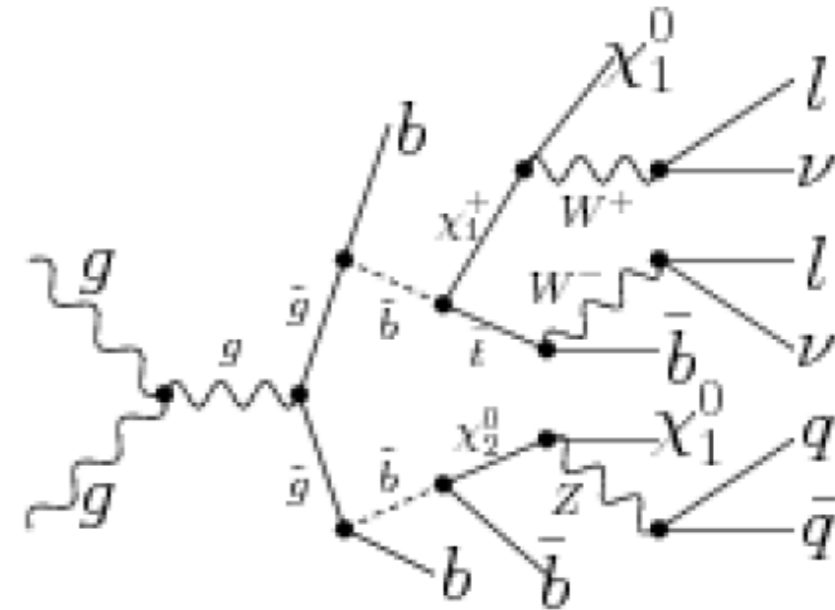
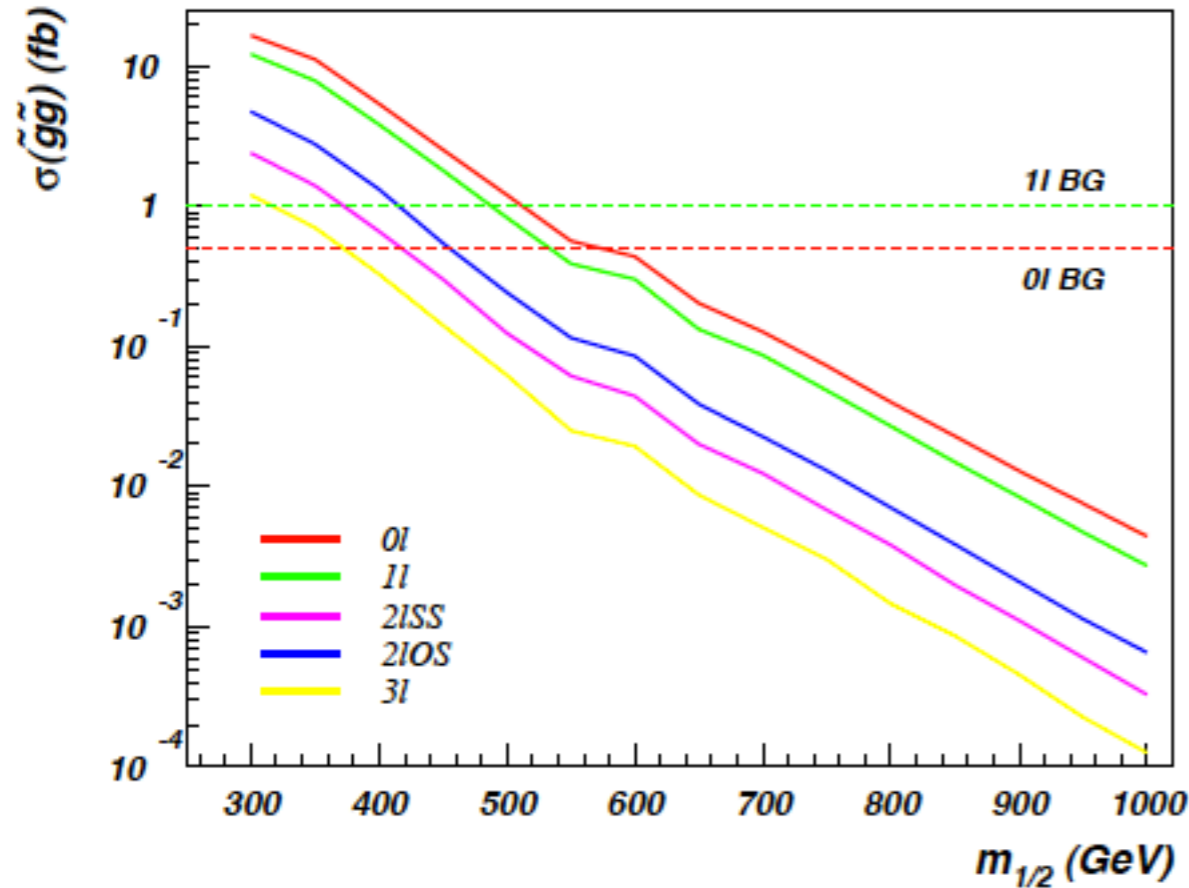
higgsino pair production dominant—but only soft visible energy release from higgsino decays

largest visible cross section: **wino pairs**

gluino pairs sharply dropping

# gluino pair cascade decay signatures

NUHM2:  $m_0=5\text{ TeV}$ ,  $A_0=-1.6m_0$ ,  $\tan\beta=15$ ,  $\mu=150\text{ GeV}$ ,  $m_A=1\text{ TeV}$



Particle	dom. mode	BF
$\tilde{g}$	$\tilde{t}_1 t$	$\sim 100\%$
$\tilde{t}_1$	$b\tilde{W}_1$	$\sim 50\%$
$\tilde{Z}_2$	$\tilde{Z}_1 f\bar{f}$	$\sim 100\%$
$\tilde{Z}_3$	$\tilde{W}_1^\pm W^\mp$	$\sim 50\%$
$\tilde{Z}_4$	$\tilde{W}_1^\pm W^\mp$	$\sim 50\%$
$\tilde{W}_1$	$\tilde{Z}_1 f\bar{f}'$	$\sim 100\%$
$\tilde{W}_2$	$\tilde{Z}_i W$	$\sim 50\%$

Table 1: Dominant branching fractions of various sparticles along the RNS model line for  $m_{1/2} = 1\text{ TeV}$ .

Int. lum. ( $\text{fb}^{-1}$ )	$\tilde{g}\tilde{g}$
10	1.4
100	1.6
300	1.7
1000	1.9

LHC14 reach  
in  $m(\text{gluino})$  (TeV)

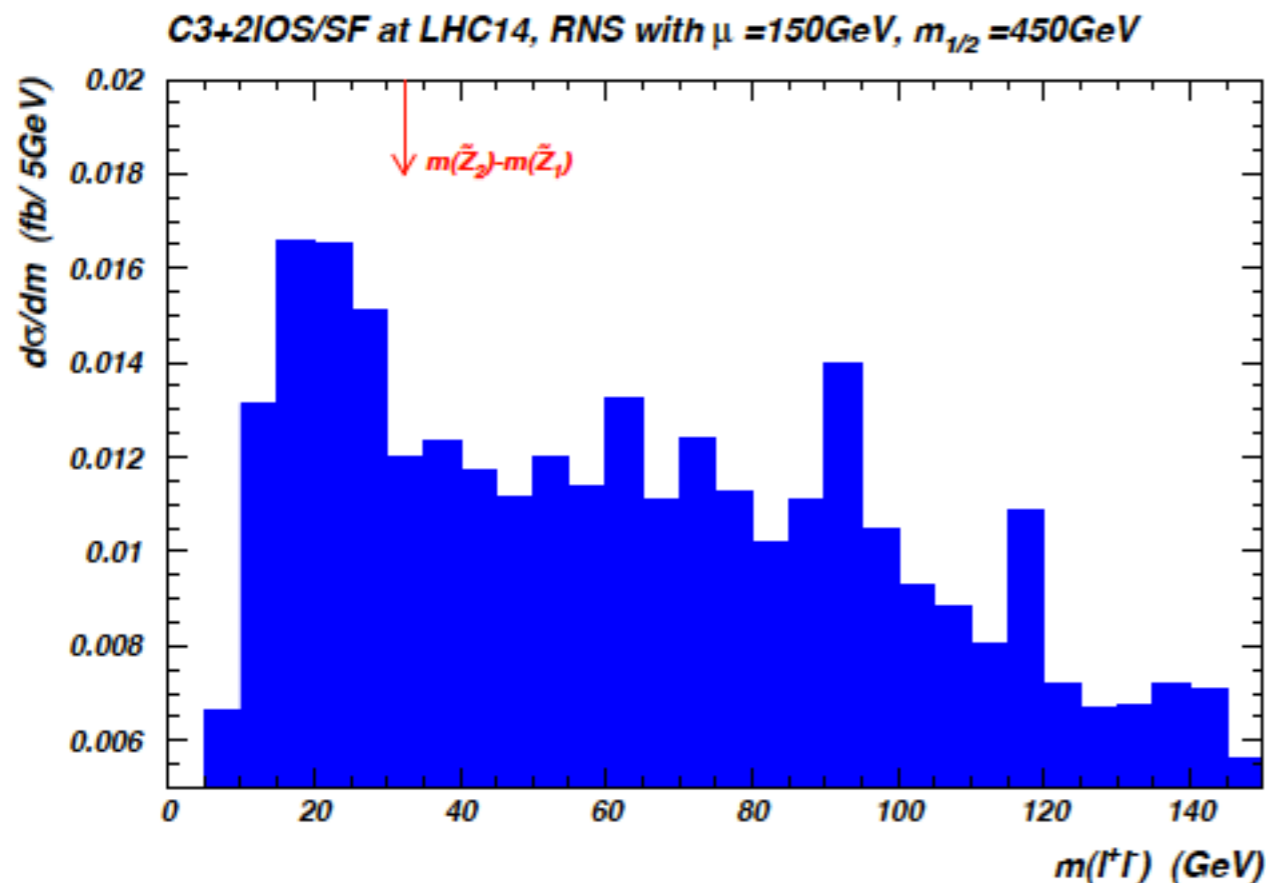
since  $m(\text{gluino})$  extends to  $\sim 5\text{ TeV}$ ,  
**LHC14 can see about half** the low EWFT  
parameter space in these modes



# LHC14 has some reach for RNS; if a signal is seen, should be characteristic

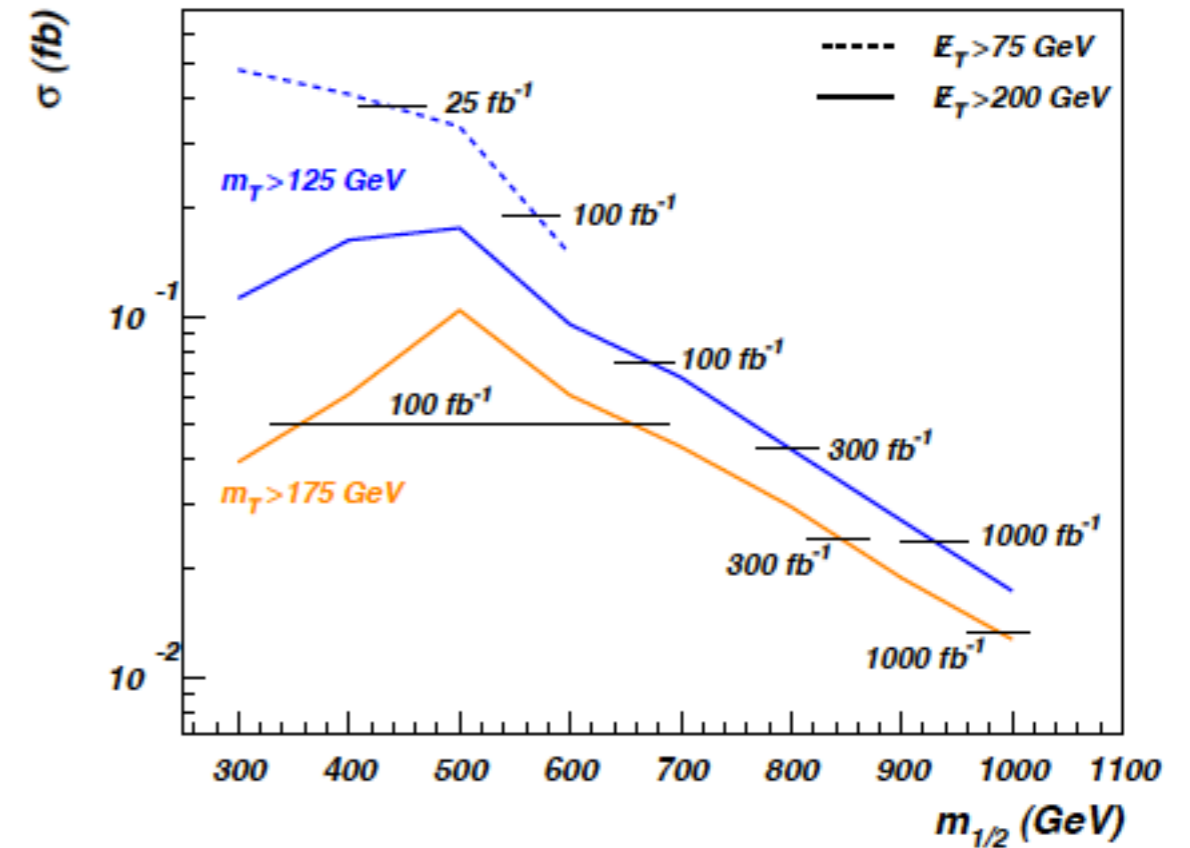
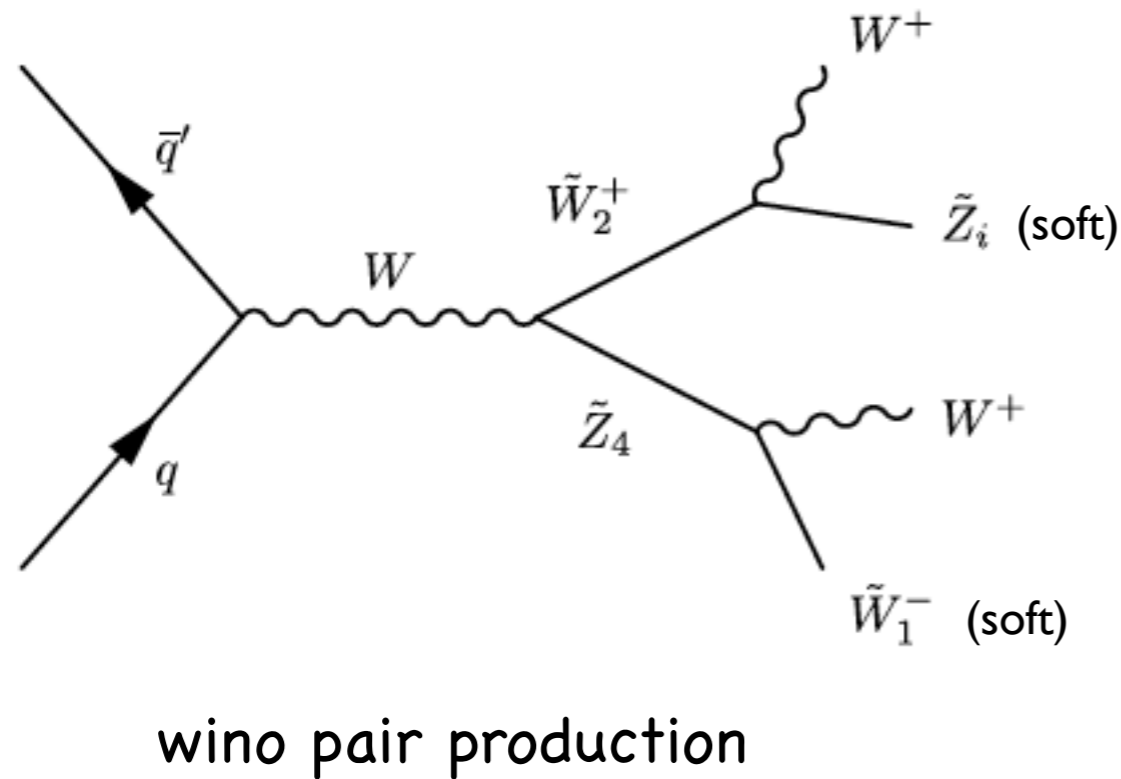
Int. lum. ( $\text{fb}^{-1}$ )	$\tilde{g}\tilde{g}$	SSdB	$WZ \rightarrow 3\ell$	$4\ell$
10	1.4	–	–	–
100	1.6	1.6	–	$\approx 1.2$
300	1.7	2.1	1.4	$\approx 1.4$
1000	1.9	2.4	1.6	$\approx 1.6$

$5\sigma$  reach of LHC14 in terms of  $m_{\tilde{g}}$  for various Int. Lum.



OS/SF dilepton mass  
edge apparent from  
cascade decays  
with  $z_2 \rightarrow z_1 + l + l\text{bar}$

# Characteristic same-sign diboson (SSdB) signature from SUSY models with light higgsinos!

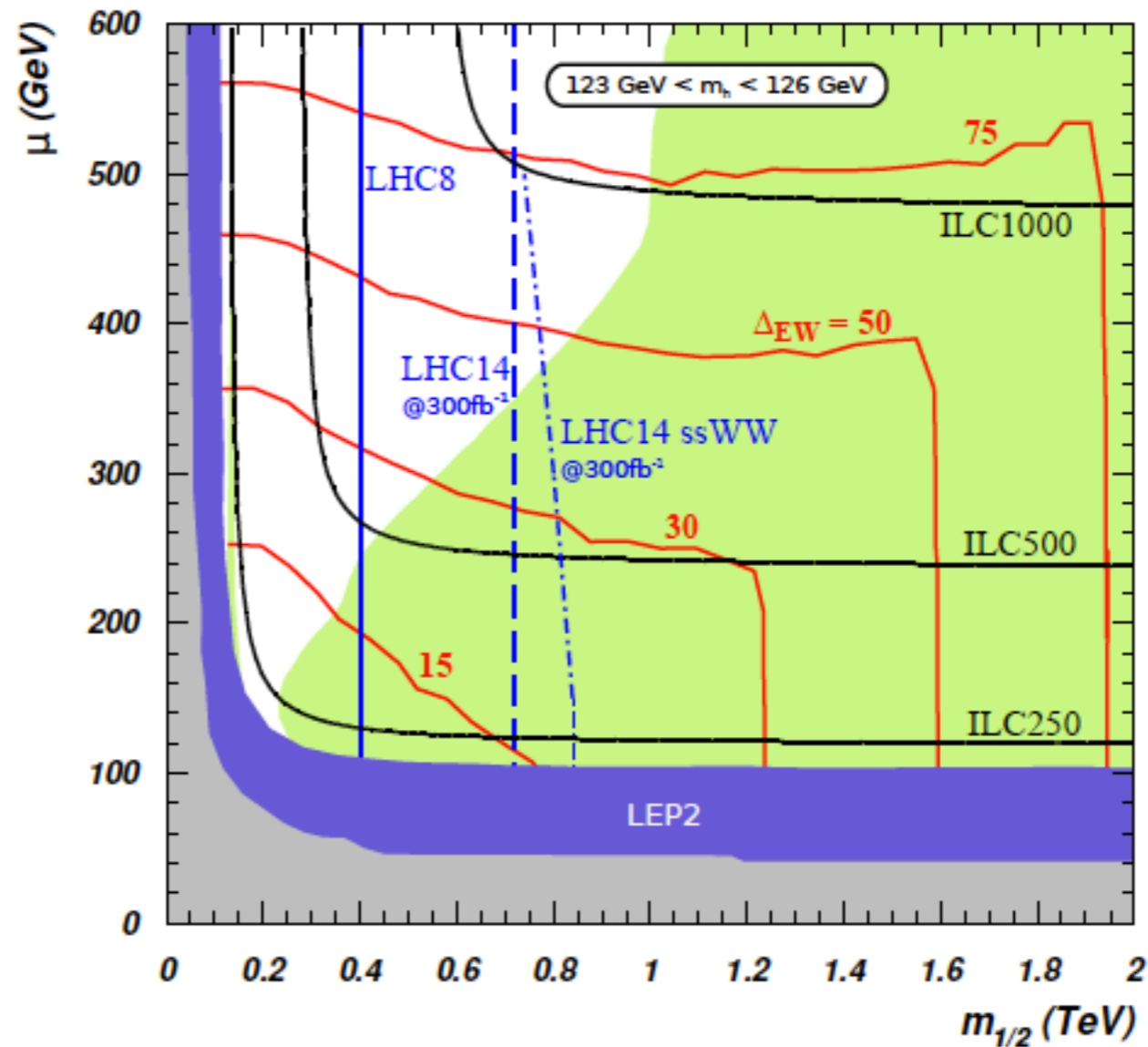


This channel offers best reach of LHC14 for RNS;  
it is also indicative of wino-pair prod'n  
followed by decay to higgsinos

H. Baer, V. Barger, P. Huang, D. Mickelson, A. Mustafayev, W. Sreethawong and X. Tata,  
*Phys. Rev. Lett.* **110** (2013) 151801.

# LHC/ILC complementarity

NUHM2:  $m_0=5$  TeV,  $\tan\beta=15$ ,  $A_0=-1.6m_0$ ,  $m_A=1$  TeV,  $m_t=173.2$  GeV

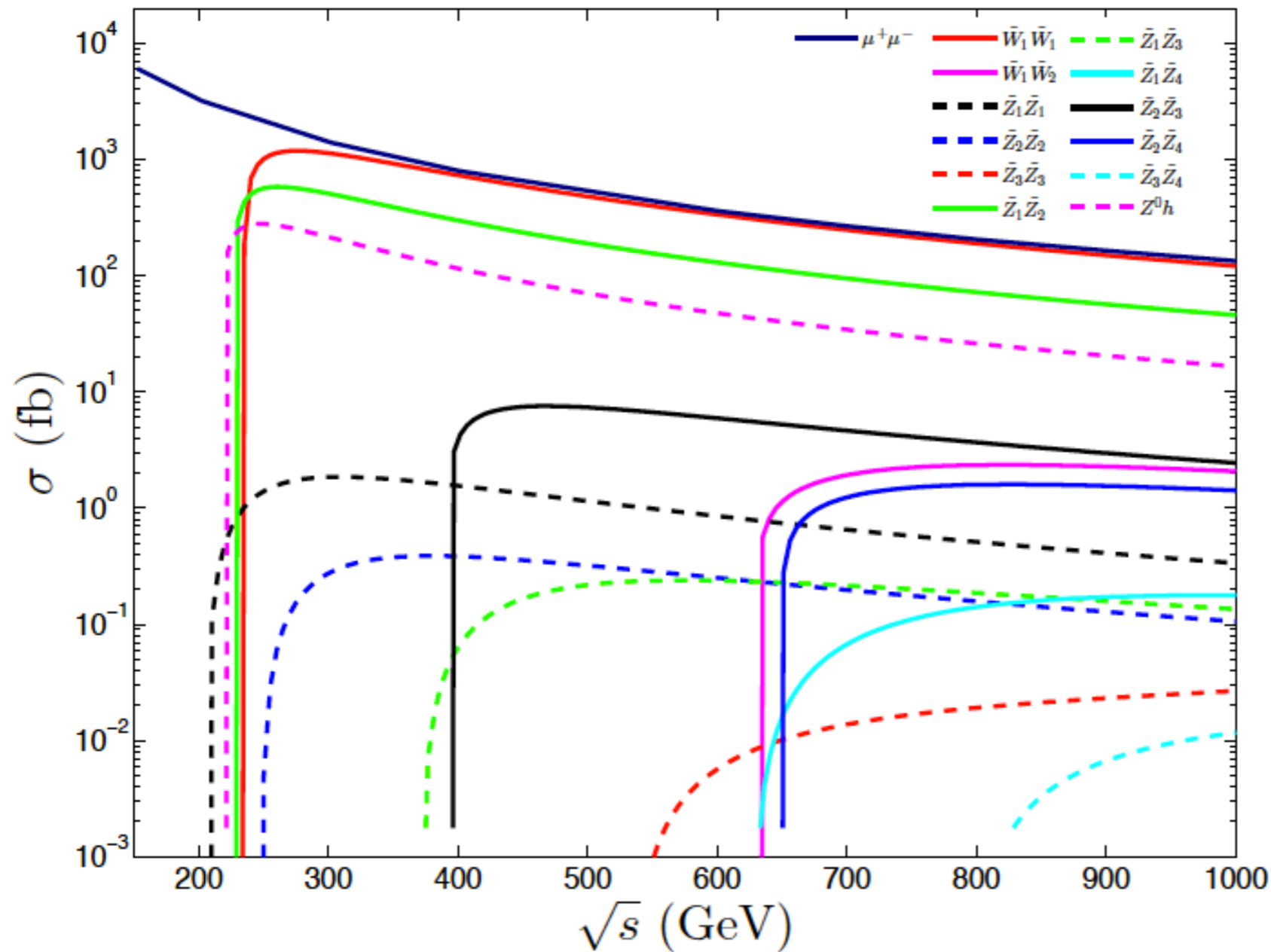


When to give up on naturalness in SUSY?  
If ILC(500–600 GeV) sees no light higgsinos

# Smoking gun signature: light higgsinos at ILC:

ILC is Higgs/higgsino factory!

ILC1:  $m_0 = 7025$  GeV,  $m_{1/2} = 568.3$  GeV,  $A_0 = -11426.6$  GeV,  $\tan\beta = 10$ ,  $\mu = 115$  GeV,  $m_A = 1000$  GeV



compressed higgsino spectrum very hard to see at LHC

10-20 GeV higgsino mass gaps are no problem in clean ILC environment

$$\sigma(\text{higgsino}) \gg \sigma(Zh)$$

HB, Barger, Mickelson, Mustafayev, Tata

ILC either sees light higgsinos or natural SUSY dead

But so far we have addressed only **Part 1**  
of fine-tuning problem:

In QCD sector, the term  $\frac{\bar{\theta}}{32\pi^2} F_{A\mu\nu} \tilde{F}_A^{\mu\nu}$  must occur

But neutron EDM says it is not there: strong CP problem  
(frequently ignored by SUSY types)

Best solution after 35 years:

PQWW/KSVZ/DFSZ **invisible axion**

In SUSY, axion accompanied by axino and saxion

Changes DM calculus:

expect mixed WIMP/axion DM (**2 particles**)

## Axion cosmology

★ Axion field eq'n of motion:  $\theta = a(x)/f_a$

$$- \ddot{\theta} + 3H(T)\dot{\theta} + \frac{1}{f_a^2} \frac{\partial V(\theta)}{\partial \theta} = 0$$

$$- V(\theta) = m_a^2(T) f_a^2 (1 - \cos \theta)$$

– Solution for  $T$  large,  $m_a(T) \sim 0$ :

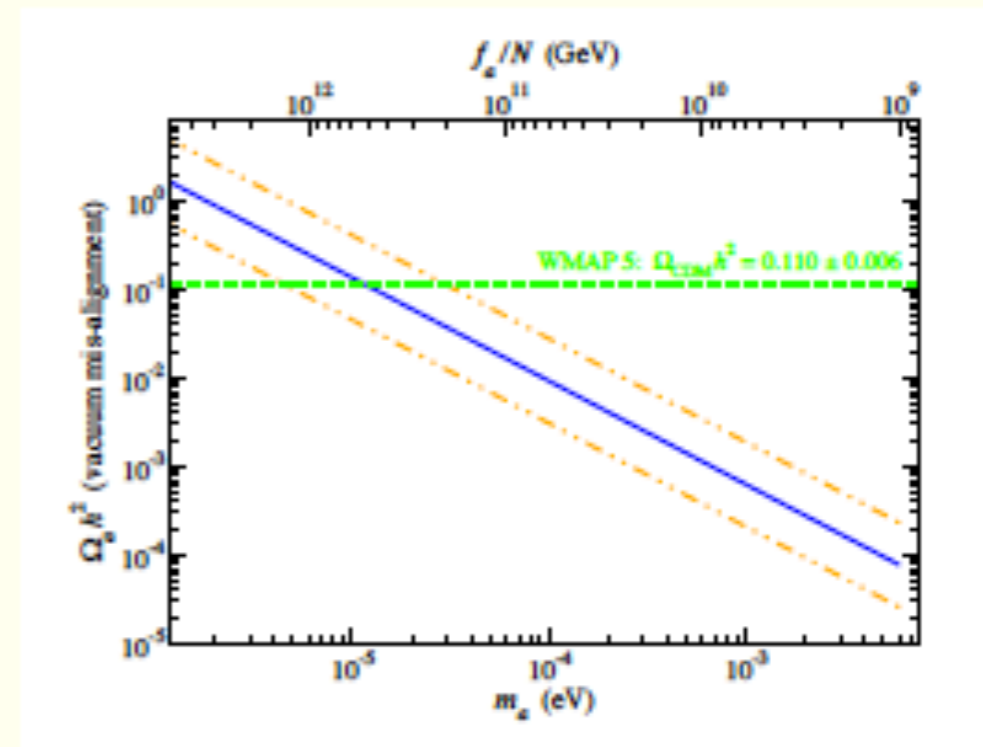
$$\theta = \text{const.}$$

–  $m_a(T)$  turn-on  $\sim 1$  GeV

★  $a(x)$  oscillates,  
creates axions with  $\vec{p} \sim 0$ :  
production via vacuum mis-alignment

$$\star \Omega_a h^2 \sim \frac{1}{2} \left[ \frac{6 \times 10^{-6} \text{ eV}}{m_a} \right]^{7/6} \theta_i^2 h^2$$

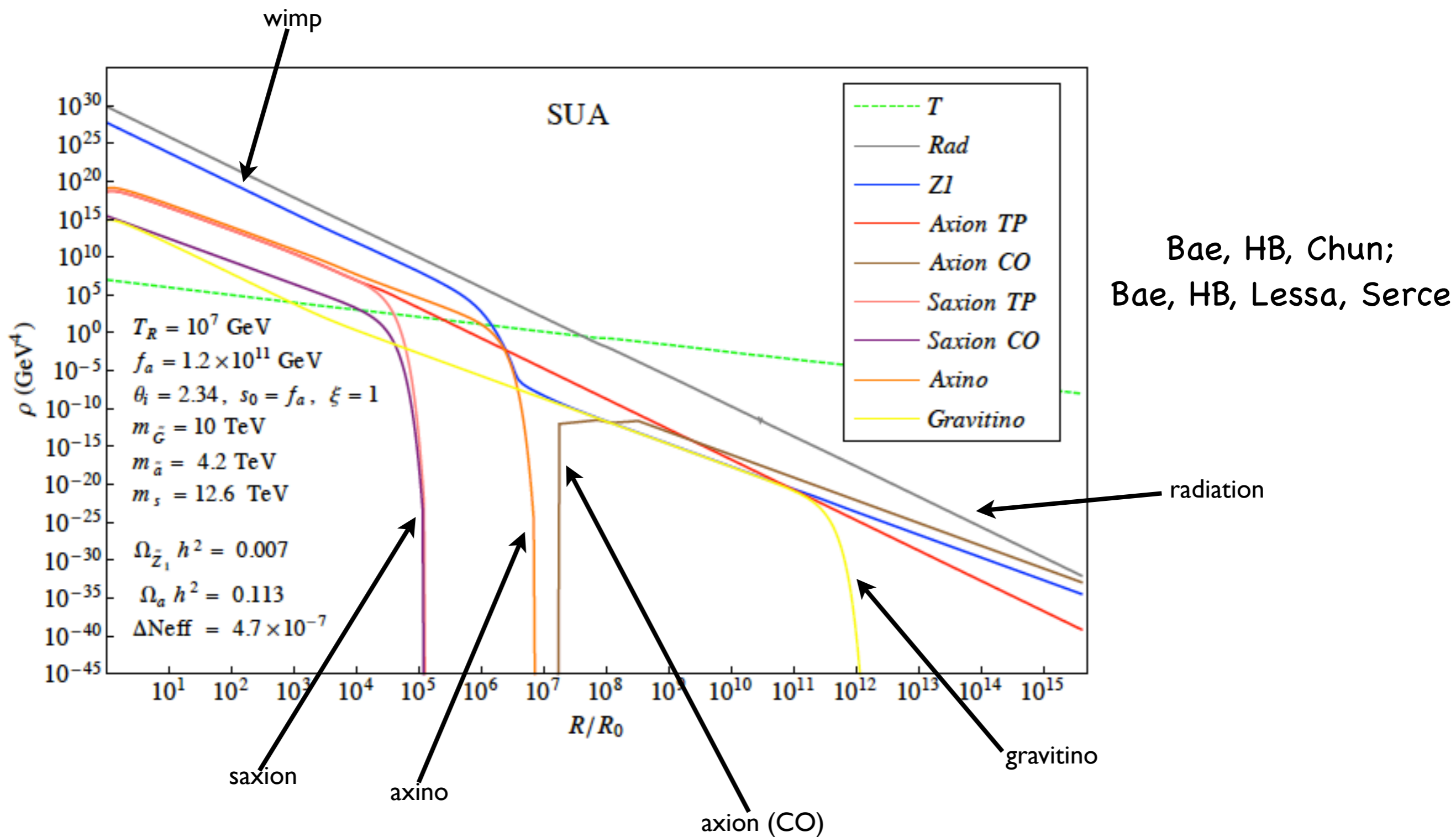
★ astro bound: stellar cooling  $\Rightarrow f_a \gtrsim 10^9 \text{ GeV}$



# mixed axion-neutralino production in early universe

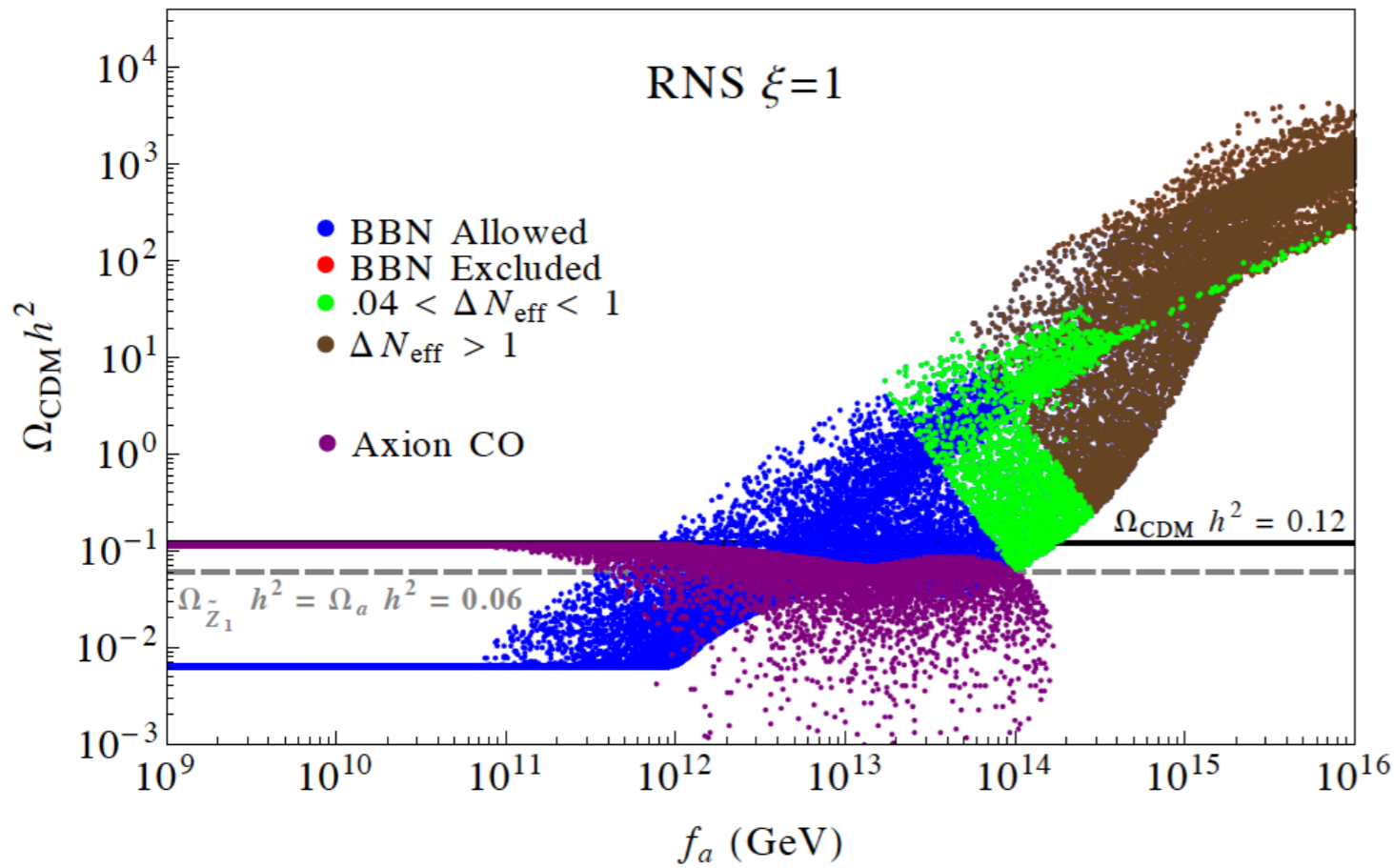
- neutralinos: thermally produced (TP) or NTP via  $\tilde{a}$ ,  $s$  or  $\tilde{G}$  decays
  - re-annihilation at  $T_D^{s,\tilde{a}}$
- axions: TP, NTP via  $s \rightarrow aa$ , bose coherent motion (BCM)
- saxions: TP or via BCM
  - $s \rightarrow gg$ : entropy dilution
  - $s \rightarrow SUSY$ : augment neutralinos
  - $s \rightarrow aa$ : dark radiation ( $\Delta N_{eff} < 1.6$ )
- axinos: TP
  - $\tilde{a} \rightarrow SUSY$  augments neutralinos
- gravitinos: TP, decay to SUSY

# DM production in SUSY DFSZ: solve eight coupled Boltzmann equations



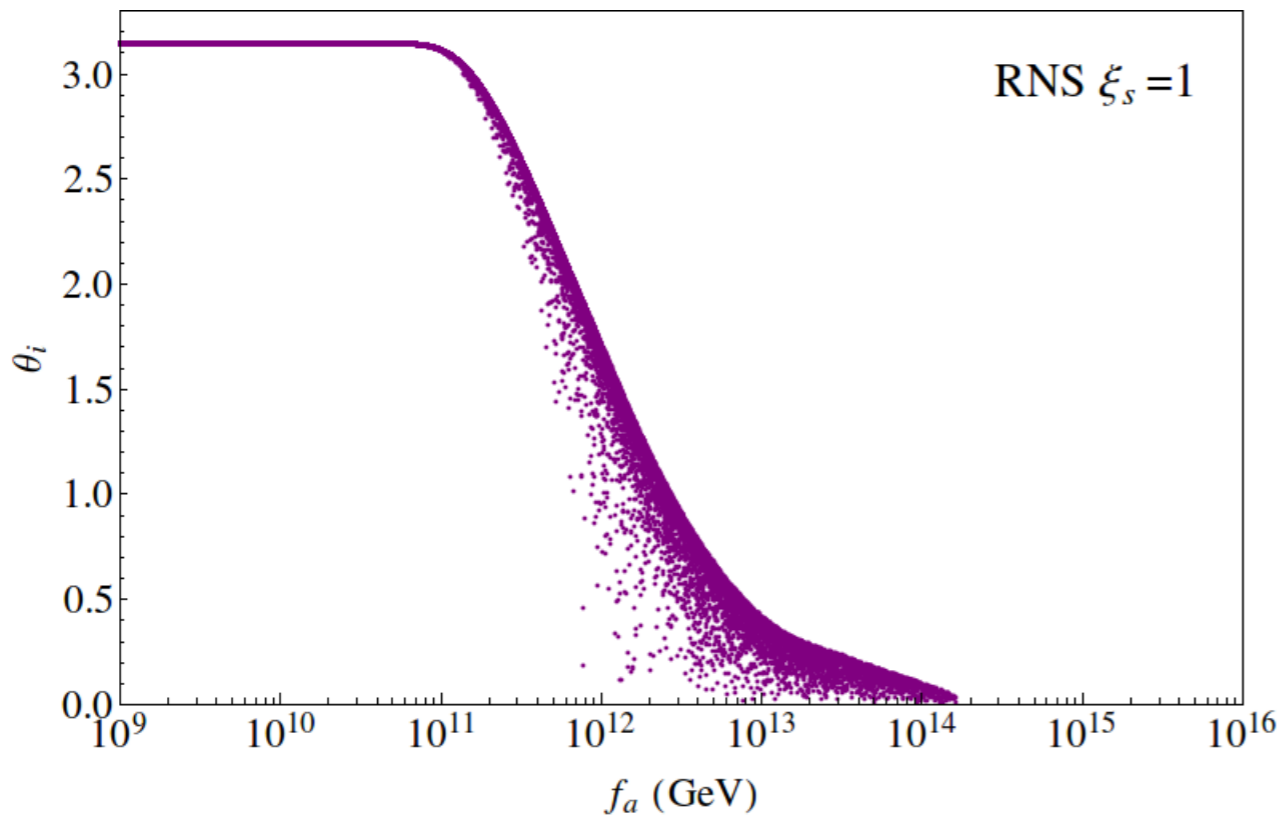
Bae, HB, Chun;  
Bae, HB, Lessa, Serce





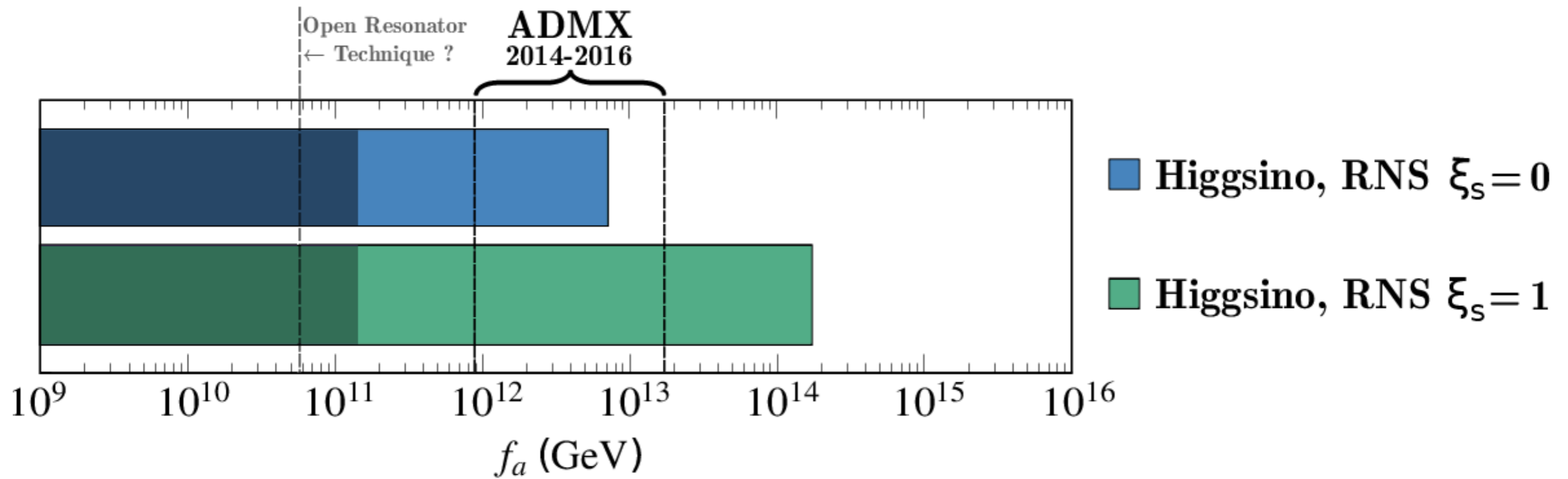
higgsino abundance

axion abundance



mainly axion CDM  
 for  $f_a < \sim 10^{12}$  GeV;  
 for higher  $f_a$ , then  
 get increasing wimp  
 abundance

Bae, HB, Lessa, Serce



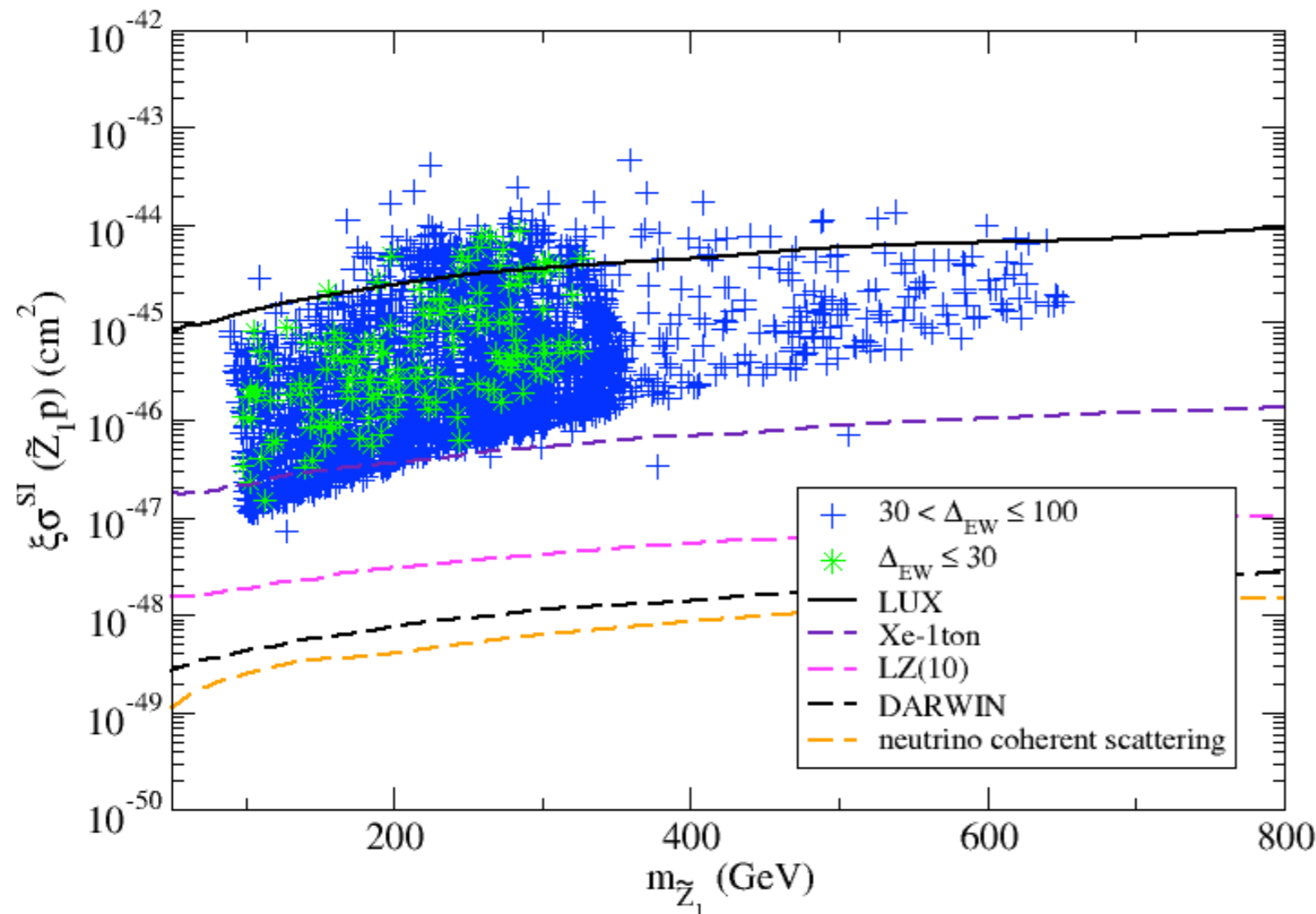
range of  $f_a$  expected from SUSY  
with radiatively-driven naturalness  
compared to ADMX axion reach

# Direct higgsino detection rescaled for minimal local abundance

Bae, HB, Barger, Savoy, Serce

$$\mathcal{L} \ni -X_{11}^h \bar{\tilde{Z}}_1 \tilde{Z}_1 h$$

$$X_{11}^h = -\frac{1}{2} (v_2^{(1)} \sin \alpha - v_1^{(1)} \cos \alpha) (g v_3^{(1)} - g' v_4^{(1)})$$



Deployment of Xe-1ton,  
LZ, SuperCDMS  
coming soon!

Can test completely with ton scale detector  
or equivalent (subject to minor caveats)

# Conclusions: status of SUSY post LHC8

- SUSY EWFT **non-crisis**: EWFT allowed at 10% level in radiatively-driven natural SUSY: SUGRA GUT paradigm is just fine in NUHM2 but CMSSM/others fine-tuned
- naturalness maintained for  $\mu \sim 100\text{--}200$  GeV;  $t_1 \sim 1\text{--}2$  TeV,  $t_2 \sim 2\text{--}4$  TeV, highly mixed;  $m(\tilde{g}, \tilde{u}) \sim 1\text{--}5$  TeV
- LHC14 w/  $300 \text{ fb}^{-1}$  can see about half of RNS parameter space
- **$e^+e^-$  collider with  $\sqrt{s} \sim 500\text{--}600$  GeV needed to find predicted light higgsino states**
- Discovery of and precision measurements of light higgsinos at ILC!
- RNS spectra characterized by mainly higgsino-like WIMP: standard relic underabundance
- SUSY DFSZ/MSY invisible axion model:  
solves strong CP and  $\mu$  problems while allowing for  $\mu \sim m(Z)$
- Expect mainly axion CDM with 5–10% higgsino-like WIMPs over much of p-space
- Ultimately detect **both axion and higgsino-like WIMP**