

Light Inflaton –
hunting for it from CMB through the Dark
Matter and down to the colliders

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Outline

- 1 Minimally extending the Standard Model
- 2 Inflation and cosmological constraints
 - ϕ^4 inflation and non-minimal coupling
 - Coupling to the SM and the model
 - Constraints from reheating and radiative corrections
- 3 Anything interesting in the laboratory?
 - Direct inflaton search
 - Is the Higgs compatible?
- 4 Dark Matter generation
 - Abundance
 - Warm or Cold

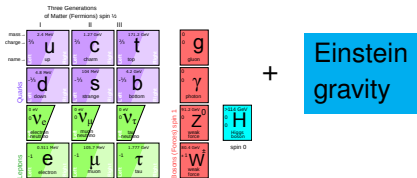
Standard Model of particle physics

Three Generations
of Matter (Fermions) spin $\frac{1}{2}$

	I	II	III		
mass →	2.4 MeV	1.27 GeV	171.2 GeV	0	0
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
name →	u up	c charm	t top	g gluon	
	Left Right	Left Right	Left Right		
				0	0
	4.8 MeV	104 MeV	4.2 GeV	0	0
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	γ photon	
Quarks	d down	s strange	b bottom		
	Left Right	Left Right	Left Right		
	0 eV	0 eV	0 eV	91.2 GeV	>114 GeV
	0	0	0	0	0
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	Z⁰ weak force	H Higgs boson
	Left Right	Left Right	Left Right		
	0.511 MeV	105.7 MeV	1.777 GeV	80.4 GeV	
	-1	-1	-1	± 1	
Leptons	e electron	μ muon	τ tau	W[±] weak force	spin 0
	Left Right	Left Right	Left Right		

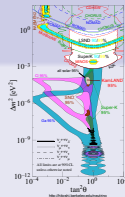
Bosons (Forces) spin 1

Standard Model – describes **nearly** everything



Experimental problems:

- Laboratory
 - ? Neutrino oscillations
- Cosmology
 - ? Baryon asymmetry of the Universe
 - ? Dark Matter

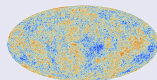


Describes

- all laboratory experiments – electromagnetism, nuclear processes, etc.
- all processes in the evolution of the Universe after the Big Bang Nucleosynthesis ($T < 1 \text{ MeV}$, $t > 1 \text{ sec}$)



? Inflation



? Dark Energy

Minimal extensions of the SM to account for everything

Should explain everything

- Neutrino oscillations
 - Baryon asymmetry of the Universe
 - Dark Matter
 - Inflation
- } ν MSM
} this talk

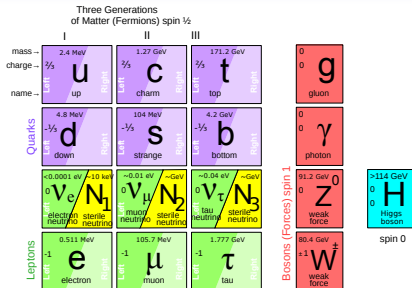
in a minimal way

- Introduce minimal amount of new particle/parameters
 - Simple
 - Predictive
- No new scales up to gravity/inflation
 - Allows to make relations between inflation and particle physics

Standard Model and nothing else above up to Planck scale?

- No heavy particles/scales
 - no physical high scale quadratic contributions to the Higgs boson mass
 - hierarchy problem is not that scary (however, the gravity should be generous enough not to give quadratically divergent contributions)
 - Processes at the highest energy (inflation) may be directly related to the low energy properties

Dark matter – ν MSM setup used



Role of sterile neutrinos

N_1 (Warm) Dark Matter, $M_1 = 7\text{keV}$
Already seen in X-rays!

$N_{2,3}$ Baryogenesis, $M_{2,3} \sim \text{several GeV}$

- Generation of DM abundance will be discussed later

Standard Model – extended for inflation

Some models that minimally expand the SM and have inflation

- Higgs inflation
 - No new particles, but: new scale M_P/ξ , UV corrections may mask inflation at $M_P/\sqrt{\xi}$ from particle physics
- R^2 inflation
 - purely gravitational solution, nothing interesting for the particle physics
- Light inflaton with non-minimal coupling
 - this talk, solution within renormalizable particle physics model

Important – the whole Universe evolution should be fully described within the model!

Standard Model – extended for inflation

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 - **this talk, solution within renormalizable particle physics model**

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“Standard” chaotic inflation

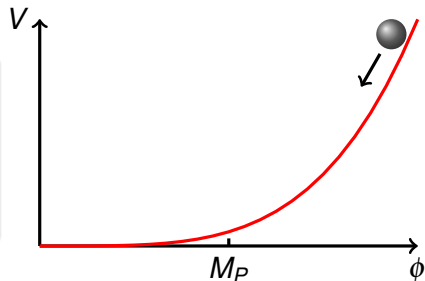
Scalar part of the action

$$S = \int d^4x \sqrt{-g} \left\{ -\frac{M_P^2}{2} R + \frac{\partial_\mu \phi \partial^\mu \phi}{2} - \frac{\beta}{4} \phi^4 \right\}$$

Required to get
 $\delta T/T \sim 10^{-5}$

$$\beta \sim 10^{-13}$$

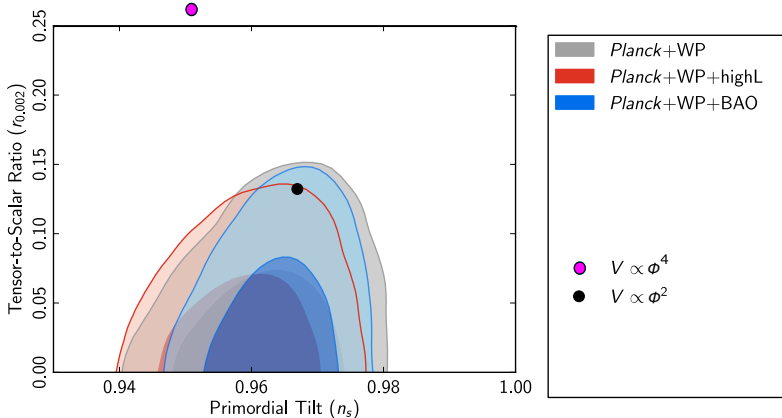
$$m \sim 10^{13} \text{ GeV}$$



Fields $\gtrsim M_P$, energy $\sim \lambda^{1/4} M_P$.



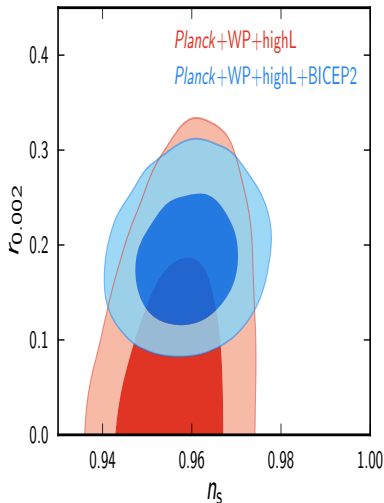
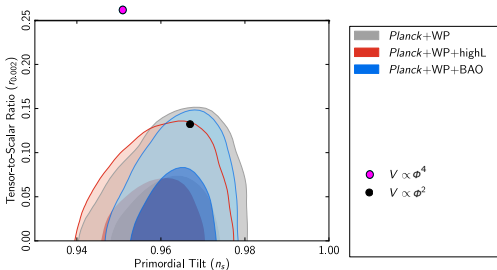
Planck results disfavor plain ϕ^4



Obligatory BICEP2 remark

$$U_{\text{inflation}}^{1/4} \sim 1.9 \times 10^{16} \text{ GeV} \left(\frac{r}{0.1}\right)^{1/4}$$

If BICEP2 measured anything – that would be fun!



Non-minimal coupling to gravity leads to good inflation

Scalar action with non-minimal coupling

$$S = \int d^4x \sqrt{-g} \left\{ -\frac{M_P^2}{2} R - \frac{\xi}{2} \phi^2 R + \frac{\partial_\mu \phi \partial^\mu \phi}{2} - \frac{\lambda}{4} \phi^4 \right\}$$

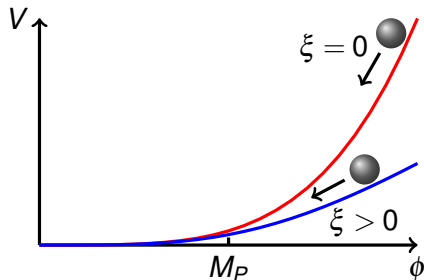
Conformal transformation to the Einstein frame

$$\hat{g}_{\mu\nu} = \sqrt{1 + \frac{\xi \phi^2}{M_P^2}} g_{\mu\nu},$$

flattens the potential

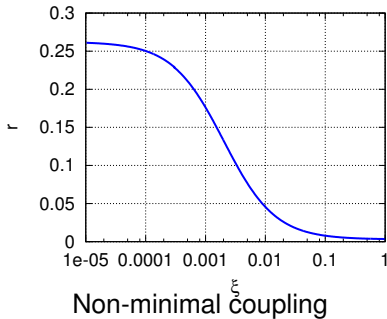
$$V(\phi) \rightarrow \hat{V}(\phi) = \frac{V(\phi)}{(1 + \xi \phi^2 / M_P^2)^2}$$

(Change of the field $\frac{d\chi}{d\phi} = \sqrt{\frac{1 + (\xi + 6\xi^2)\phi^2 / M_P^2}{(1 + \xi \phi^2 / M_P^2)^2}}$ is also needed)

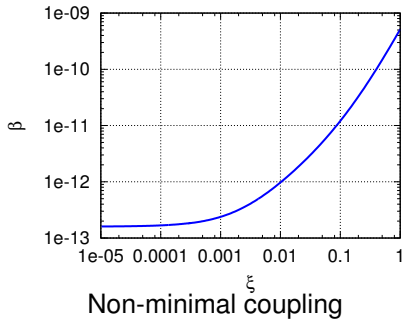


The tensor perturbations are suppressed, inflaton self-coupling β is increased

Tensor-to-Scalar Ratio

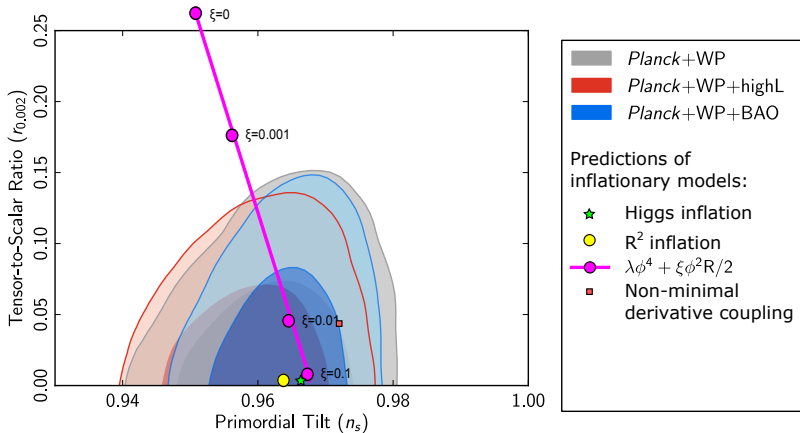


Inflaton Self-Coupling



- For each ξ the self-coupling β is fixed by $\delta T/T \simeq 10^{-5}$ requirement.
- Measurement of not-too-small r measures ξ !

Inflationary predictions are ok for $\xi \gtrsim 0.003$



Note: for small $\xi \lesssim 1$ no new scales in the model!

SM + Light Inflaton coupled in the Higgs sector only

$$\mathcal{L} = \mathcal{L}_{\text{SM}, M=0} + \alpha H^\dagger H \phi^2 +$$

Standard Model

Interaction

$$+ \frac{M_P^2}{2} R +$$

Einstein gravity

$$\frac{(\partial\phi)^2}{2} + \frac{\xi\phi^2}{2} R + \frac{\beta}{4}\phi^4 - \frac{\mu^2}{2}\phi^2$$

Inflationary sector

Main assumption for today

- The scale invariance breaking is manifest *only in the inflaton sector*

$$V(H, \phi) = \lambda \left(H^\dagger H - \frac{\alpha}{\lambda} \phi^2 \right)^2 + \frac{\beta}{4} \phi^4 - \frac{1}{2} \mu^2 \phi^2 + V_0$$

Inflaton gets a vev \rightarrow Higgs gets a vev

SM + Light Inflaton coupled in the Higgs sector only

$$\mathcal{L} = \mathcal{L}_{\text{SM}, M=0} + \alpha H^\dagger H \phi^2 +$$

Standard Model

Interaction

$$+ \frac{M_P^2}{2} R +$$

Einstein gravity

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Inflationary sector

Parameter counting:

- overall 5: λ , α , ξ , β , μ

Fix in SM: Higgs mass m_H and vev $v^2 = 1/2\sqrt{2}G_F$

Fix COBE normalization

- 2 free parameters: α and β , or:

inflaton mass $m_\chi = m_h \sqrt{\beta/2\alpha}$

Higgs-inflaton mixing $\theta^2 = 2\alpha/\lambda$

All constants of the model are bound from cosmology

CMB normalization: $\beta(\xi)$

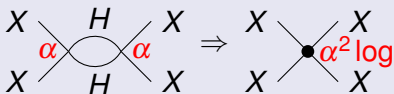
$$\beta = \frac{3\pi^2 \Delta_{\mathcal{R}}^2}{2} \frac{(1+6\xi)(1+6\xi+8(N+1)\xi)}{(1+8(N+1)\xi)(N+1)^3}$$

CMB tensor modes give ξ

$$r = \frac{16(1+6\xi)}{(N+1)(1+8(N+1)\xi)}$$

$\alpha^2 \lesssim \beta$ (mass lower bound)

Inflation is not spoiled by the radiative corrections



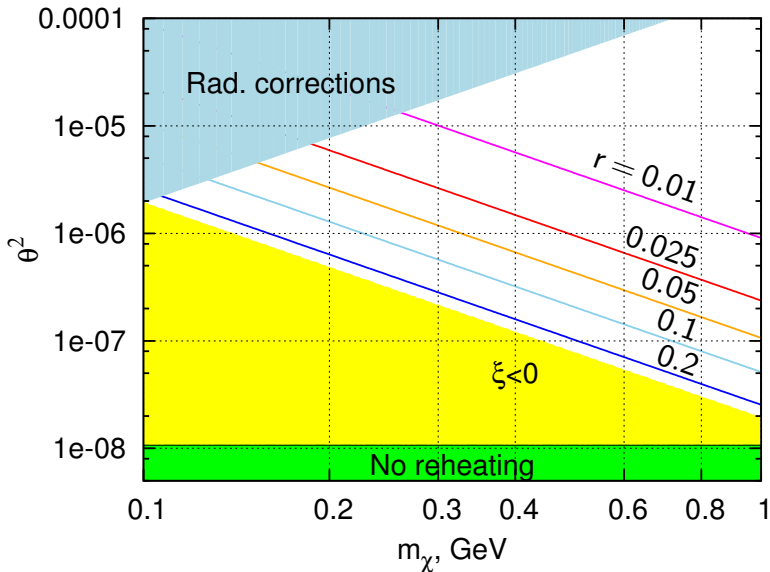
$\alpha > 10^{-7}$ (mass upper bound)

Sufficient reheating

- After inflation: empty & cold
- Needed: hot,
 $T_r \gtrsim 150$ GeV (to get baryogenesis)

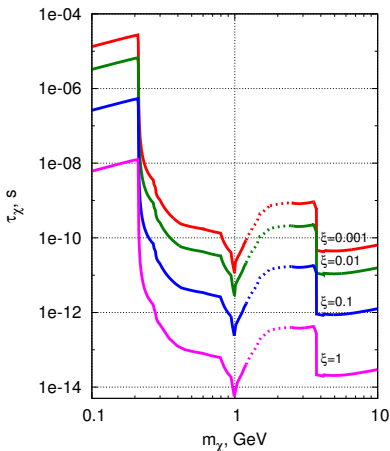
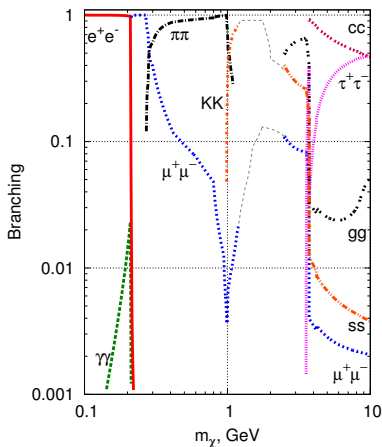


Parameter region is constraint from cosmology



Inflaton decays and lifetime

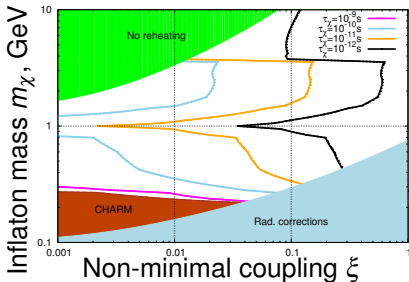
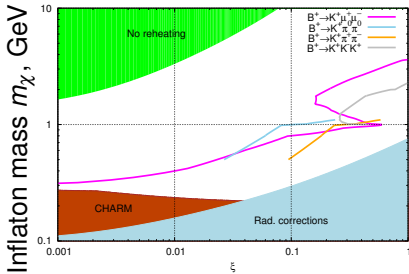
Coupled to everything proportional particle mass



Created in meson decays:

$$\text{Br}(B \rightarrow \chi X_s) \simeq 10^{-6} \frac{\beta(\xi)}{1.5 \times 10^{-13}} \frac{300 \text{ MeV}^2}{m_\chi}$$

Experimental searches are possible



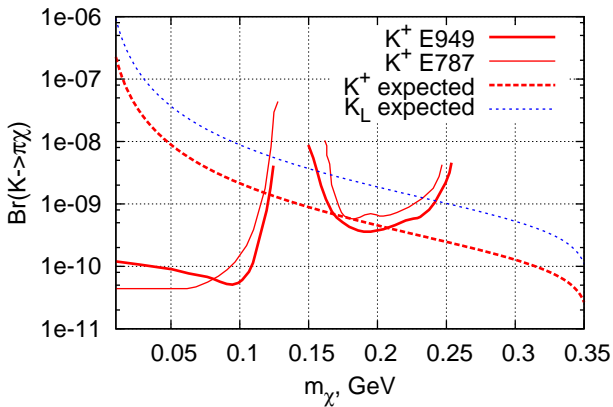
Behaves as light “Higgs” boson, suppressed by $\theta = \sqrt{2\beta} v / m_\chi$

- Created in meson decays
- Decays: KK , $\pi\pi$, $\mu\mu$, ee , ...
- Interacts with media: extremely weakly

Search (LHCb, Belle)

- Events with offset vertices in B decays
- Peaks in Dalitz plot of three body B decays

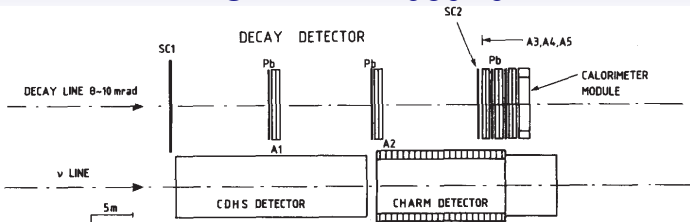
Production: bound from $K^+ \rightarrow \pi^+ + \text{nothing}$



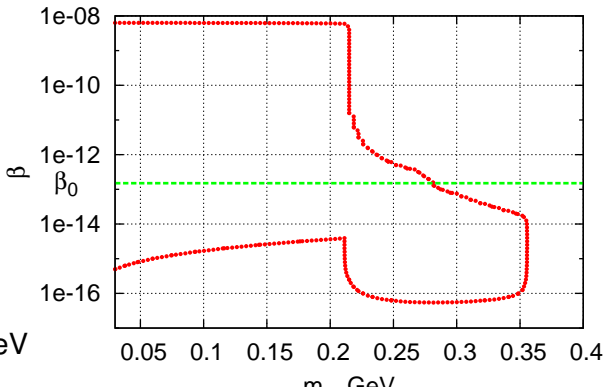
Excluded: $m_\chi \lesssim 120 \text{ MeV}$

Disfavoured: $170 \text{ MeV} \lesssim m_\chi \lesssim 205 \text{ MeV}$

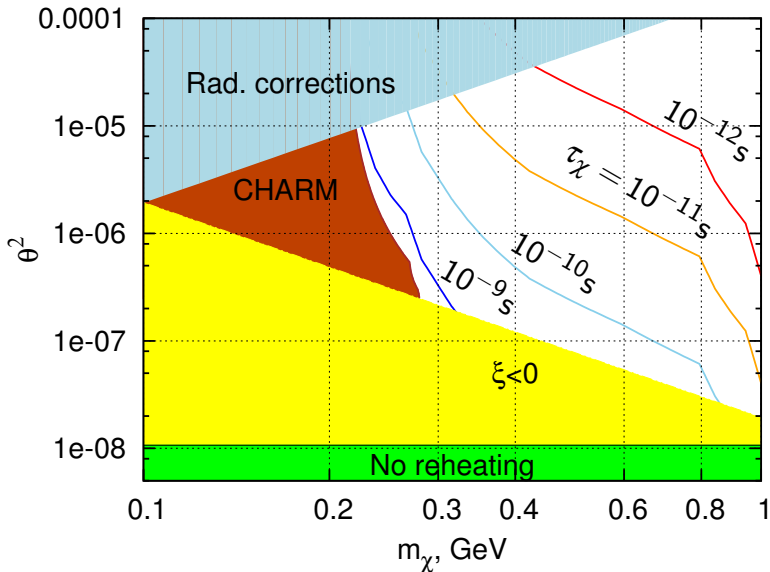
CHARM – bound



Search
for
decays of
something into
 $\gamma\gamma, e^+e^-,$
 $\mu^+\mu^- \implies$
 $m_\chi < 270 \text{ MeV}$



Longer lifetimes are excluded by CHARM



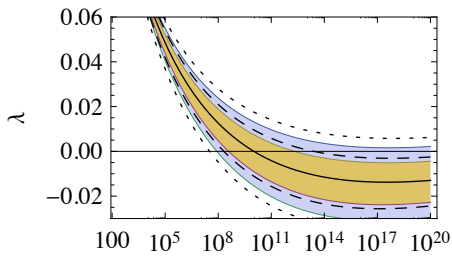
Future experimental searches

- For the longer lifetimes – SHIP
- For the shorter lifetimes – LHCb, BELLE (some constraints are there, just awaiting for proper analysis)

Another prediction: The Higgs boson can not be light

Inflation proceeds along $H^\dagger H = \frac{\alpha}{\lambda} X^2 \Rightarrow H$ is large at inflation

- The Higgs self-coupling λ : must be positive up to inflationary scales



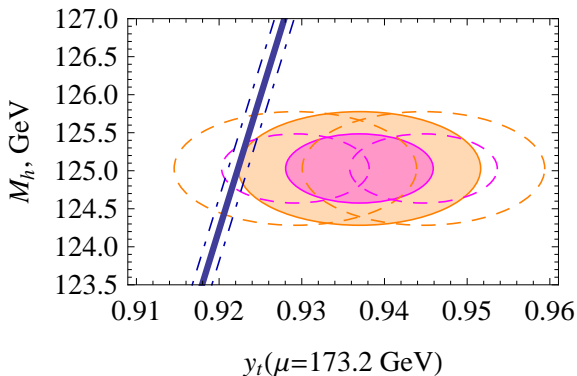
Higgs mass
 $m_H = 125.3 \text{ GeV}$

yScale μ , GeV

Current experimental value: $m_H = 125.7 \pm 0.4 \text{ GeV}$ (CMS)

[FB, Kalmykov, Kniehl,, Shaposhnikov'12,
 Degrassi, Di Vita, Elias-Miro, Espinosa, Giudice, Isidori,, Strumia'12]

Current top quark Yukawa is compatible with stable Higgs within experimental errors



DM and Baryogenesis: Adding sterile neutrinos N_I

$$\begin{aligned}
 \mathcal{L} = & \mathcal{L}_{\text{SM}, M=0} + \alpha H^\dagger H \phi^2 + \\
 & + \frac{M_P^2}{2} R + \frac{(\partial\phi)^2}{2} + \frac{\xi\phi^2}{2} R + \frac{\beta}{4}\phi^4 - \frac{\mu^2}{2}\phi^2 \\
 & + i\bar{N}_I \not{\partial} N_I - F_{\alpha I} \bar{L}_\alpha N_I H - \frac{f_I}{2} \bar{N}_I^c N_I \phi
 \end{aligned}$$

Standard Model
Interaction

Einstein gravity
Inflationary sector

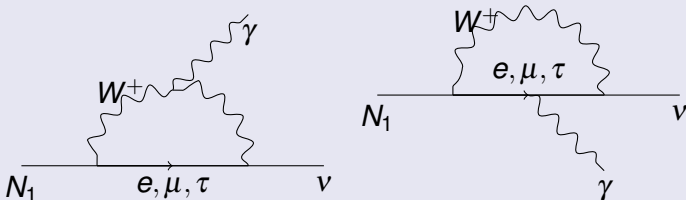
Dirac masses
Majorana masses

- f_I control both Majorana masses $M_I = f_I \langle \phi \rangle$ and inflaton-sterile neutrino coupling in the early Universe
- $F_{\alpha I}$ control active neutrino masses $m_i \sim m_D^2/M$ and sterile-active neutrino mixing $\theta_i \sim m_D^2/M_I^2$ (see-saw formula)

DM properties – Radiative decay

leads to constraints from the X-ray observations

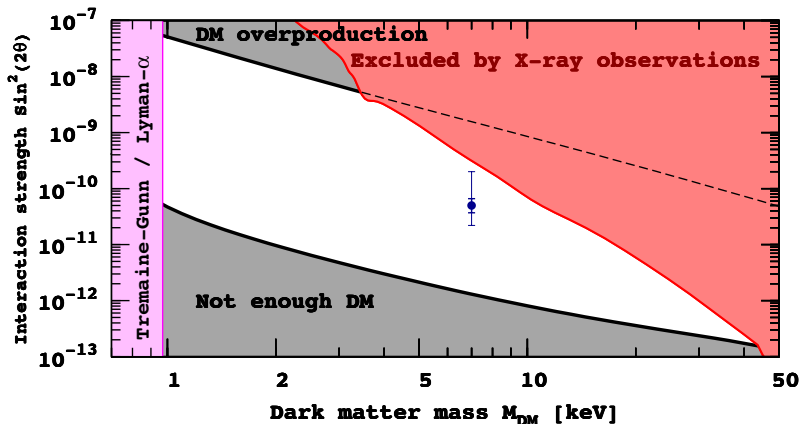
Second decay channel: $N_1 \rightarrow \nu \gamma$



$$\Gamma \simeq 5.5 \times 10^{-27} \left(\frac{\theta_1^2}{10^{-5}} \right) \left(\frac{M_1}{1\text{keV}} \right)^5 \text{s}^{-1}$$

- Monochromatic: $E_\gamma = M_1/2$
- We should see an X-ray ($\sim \text{keV}$) line coming from everywhere in the sky

Sterile-active mixing θ_1 is bound (discovered?!) in X-ray observations



3.5 keV X-ray hint—mixing θ_1^2 (Dirak Yukawa F) too small mixing to produce DM via non-resonantly enhanced oscillations

DM is produced in inflaton decays

- Light inflaton is in thermal equilibrium down to small temperature $T_f \ll m_\chi$ (reactions $\chi \leftrightarrow e^+ e^-, \mu^+ \mu^-,$ etc.)
- Maximal production happens at $T \simeq m_\chi$

$$\frac{\partial n}{\partial t} - \mathcal{H} p \frac{\partial n}{\partial p} = \frac{2m_\chi \Gamma_{\chi \rightarrow N_1 N_1}}{p^2} \int_{p+m_\chi^2/4p}^{\infty} n_\chi(E) dE$$

- Amount of DM produced

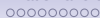
$$\Omega_{DM} \propto \frac{\Gamma_{\chi \rightarrow N_1 N_1} M_1}{m_\chi^2} \propto \frac{f_1^3 \theta^2}{m_\chi}$$

DM mass $M_1 = f_1 \langle \chi \rangle$ defines the inflaton-higgs mixing θ

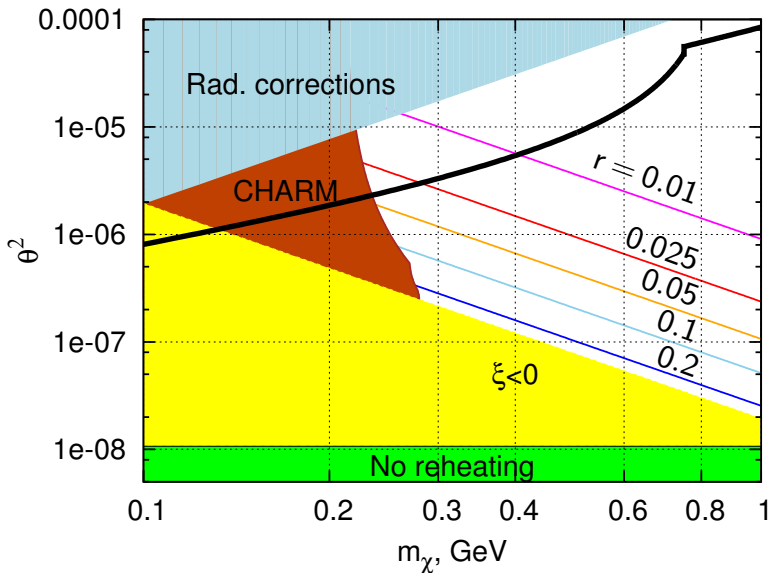
$$\theta^2 \simeq 2.7 \times 10^{-6} \left(\frac{7 \text{keV}}{M_1} \right)^3 \left(\frac{S}{1.5 f(m_\chi)} \right) \left(\frac{\Omega_N}{0.22} \right) \left(\frac{m_\chi}{250 \text{ MeV}} \right)$$

$f(m_\chi) \sim 1$ depends on d.o.f. around $T \sim m_\chi/3$

[Shaposhnikov, Tkachev'06, FB, Gorbunov'13]



Parameters are completely fixed after DM discovery and measurement of r



How cold is the Warm DM produced?

- Average momentum of the DM neutrino

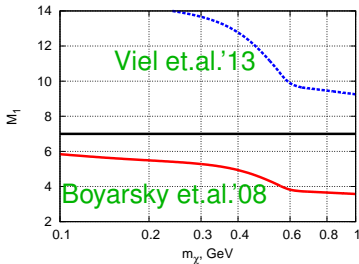
$$\langle p \rangle \simeq 2.45 T \left(\frac{10.75}{g_*(m_\chi/3)} \right)^{1/3}$$

- Average momentum of particles with temperature T (more or less that of non-resonantly produced sterile neutrinos)

$$p_T = 3.15 T$$

- On the edge!

Ly- α mass *lower* bounds



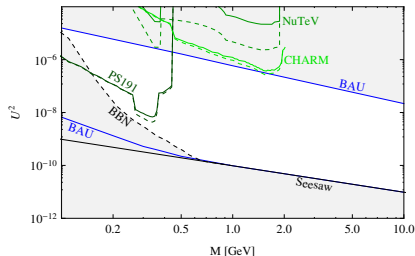
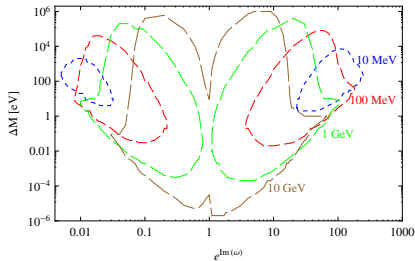
Constraints and searches for heavier sterile $N_{2,3}$

ν MSM with inflaton decay into DM

- Leptogenesis by $N_{2,3}$

$$\Delta M/M \sim 10^{-3}$$
- Experimental searches
 - $N_{2,3}$ production in hadron decays:
 - Missing energy in K decays
 - Peaks in Dalitz plot
 - $N_{2,3}$ decays into SM
 - Beam target experiments – SHIP

[Gorbunov, Shaposhnikov'07]



Caveats

- Why this specific pattern of scale symmetry breaking?
- Domain wall problem

Conclusions

- A minimal model without any new scales can
 - Fully describe the Universe
 - Can be constrained from *a combination* of cosmological and laboratory experiments
- Example model: light non-minimally coupled inflaton
 - Cosmology – essential measurement of r , search for DM decays in X-rays
 - Laboratory
 - Inflaton – search in rare decays of B (LHCb, SHIP)
 - Sterile neutrinos – no large neutrinoless double beta decay, search in rare decays, SHIP
- Invent a better model?

Backup slides

How to reheat the Universe after inflation?

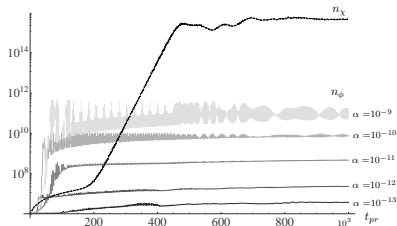
- After inflation: empty & cold
- Needed: hot, $T_r > 150 \text{ GeV}$ (to get baryogenesis, eg. via leptogenesis)

The estimate:

- Require, that at $T_r \sim 150 \text{ GeV}$ $\chi\chi \rightarrow HH$ process enters thermal equilibrium

$$\alpha \gtrsim 7 \times 10^{-10}$$

Parametric resonance?
Not so easy to create the Higgs



The large Higgs self interaction destroys coherence and spoils parametric resonance.

DM generation in the early Universe

Produced in $\bar{l}l \rightarrow \nu N_1$, $q\bar{q} \rightarrow \nu N_1$, etc.

Production is proportional to the effective active-sterile mixing angle

$$\theta_M^2(T) \simeq \frac{\theta_1^2}{\left(1 + \frac{2\rho}{M_1^2} (b(\rho, T) \pm c(T))\right)^2 + \theta_1^2}.$$

$$b(\rho, T) = \frac{16G_F^2}{\pi\alpha_W} \rho (2 + \cos^2 \theta_W) \frac{7\pi^2 T^4}{360}$$

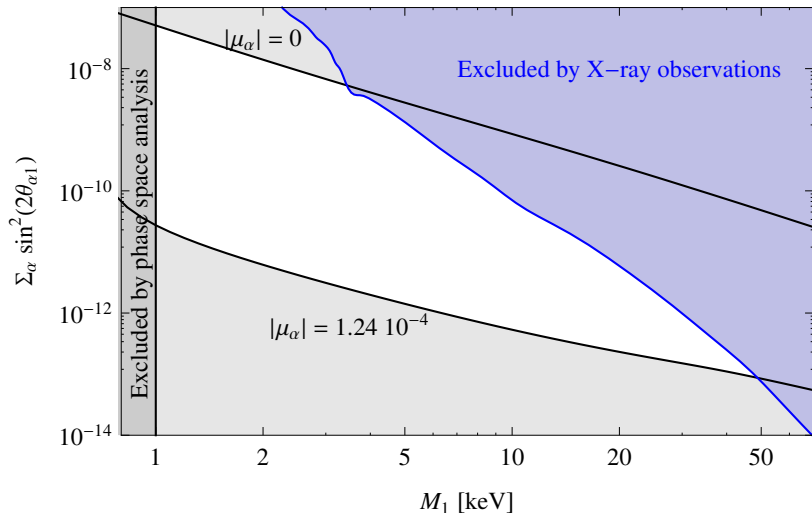
$$c(T) = 3\sqrt{2}G_F \left(1 + \sin^2 \theta_W\right) (n_{\nu_e} - n_{\bar{\nu}_e})$$

(θ_1 – vacuum mixing angle of N_1 and active ν)

Production can be

Non-resonant (b dominates) or **Resonant** ($c \sim b$)

Bounds for the N_1 – DM sterile neutrino



vMSM experimental consequences (DM)

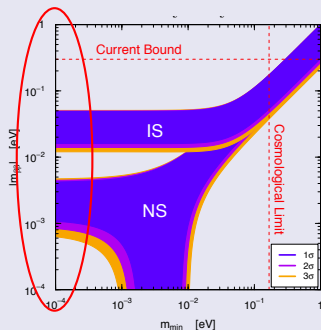
Active neutrino masses

- X-rays require very small N_1 mixing angle θ_1 , so
$$m_1 < 10^{-5} \text{ eV}$$

Neutrinoless double beta decay

- Additional contributions are negligible
 - N_1 – X-ray constraints
 - $N_{2,3}$ – mass $> 100 \text{ MeV}$
- Mass spectrum strongly hierarchical – X-ray constraints

$$m_{0\nu\beta\beta} < 50 \times 10^{-3} \text{ eV}$$



Low T and low M leptogenesis

CP violation present in Yukawa matrices F

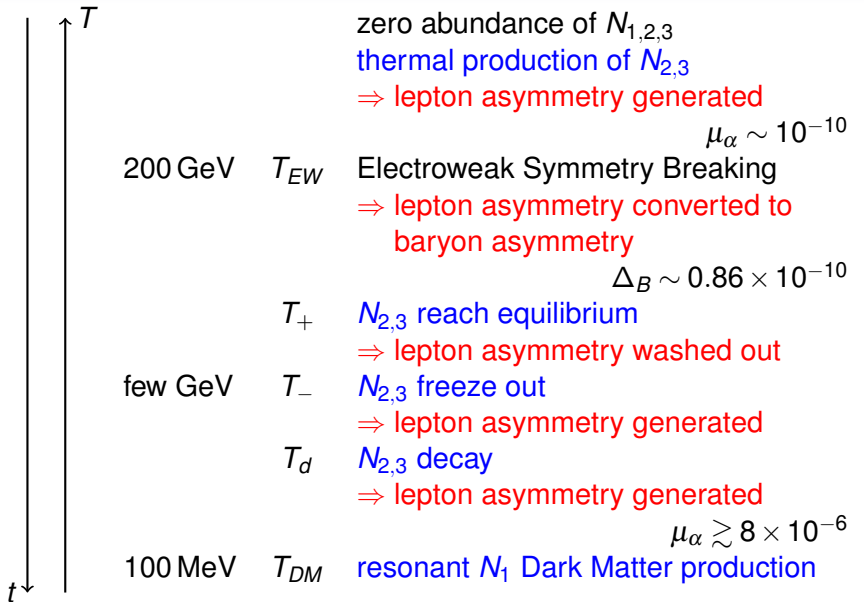
non-equilibrium process are for sterile neutrino N_I

- production
- freeze-out
- decay

Note – for $M_I/T \ll 1$ the asymmetries can be generated in active and sterile sectors with opposite signs

$$\begin{aligned}
 i \frac{d\rho_N}{dT} &= [H, \rho_N] - \frac{i}{2} \{ \Gamma_N, \rho_N - \rho^{eq} \} + \frac{i}{2} \mu_\alpha \tilde{\Gamma}_N^\alpha, \\
 i \frac{d\rho_{\bar{N}}}{dT} &= [H^*, \rho_{\bar{N}}] - \frac{i}{2} \{ \Gamma_N^*, \rho_{\bar{N}} - \rho^{eq} \} - \frac{i}{2} \mu_\alpha \tilde{\Gamma}_N^{\alpha*}, \\
 i \frac{d\mu_\alpha}{dT} &= -i \Gamma_L^\alpha \mu_\alpha + i \text{tr} \left[\tilde{\Gamma}_L^\alpha (\rho_N - \rho^{eq}) \right] \\
 &\quad - i \text{tr} \left[\tilde{\Gamma}_L^{\alpha*} (\rho_{\bar{N}} - \rho^{eq}) \right].
 \end{aligned}$$

Thermal history of the Universe





T. Asaka, S. Blanchet and M. Shaposhnikov *Phys. Lett.* **B631** (2005) 151–156, [hep-ph/0503065](#).



S. Tsujikawa and B. Gumjudpai *Phys. Rev.* **D69** (2004) 123523, [astro-ph/0402185](#).



F. L. Bezrukov [arXiv:0810.3165](#).



M. Shaposhnikov and I. Tkachev *Phys. Lett.* **B639** (2006) 414–417, [hep-ph/0604236](#).



A. Anisimov, Y. Bartocci and F. L. Bezrukov *Phys. Lett.* **B671** (2009) 211–215, [arXiv:0809.1097](#).



F. Bezrukov and D. Gorbunov *JHEP* **1307** (2013) 140, [arXiv:1303.4395](#).



F. Bezrukov, M. Kalmykov, B. Kniehl, and M. Shaposhnikov *JHEP* **1210** (2012) 140, [arXiv:1205.2893](#).



G. Degrassi, S. Di Vita, J. Elias-Miro, J. R. Espinosa, G. F. Giudice, G. Isidori, and A. Strumia *JHEP* **1208** (2012) 098, [arXiv:1205.6497](#).



D. Gorbunov and M. Shaposhnikov *JHEP* **10** (2007) 015, [arXiv:0705.1729](#).



L. Canetti, M. Drewes and M. Shaposhnikov *Phys.Rev.Lett.* **110** (2013) 061801, [arXiv:1204.3902](#).



F. Bezrukov *Phys. Rev.* **D72** (2005) 071303, [hep-ph/0505247](#).