

Measurement of semileptonic asymmetries at LHCb

- LHCb Collaboration, “Measurement of the flavour-specific CP-violating asymmetry a_{sl}^s in B_s^0 decays”, PLB 728C 607-615 (2014).
- LHCb Collaboration, “Measurement of the semileptonic CP asymmetry in $B^0 - \bar{B}^0$ mixing”, LHCb-PAPER-2014-053 (**NEW**)

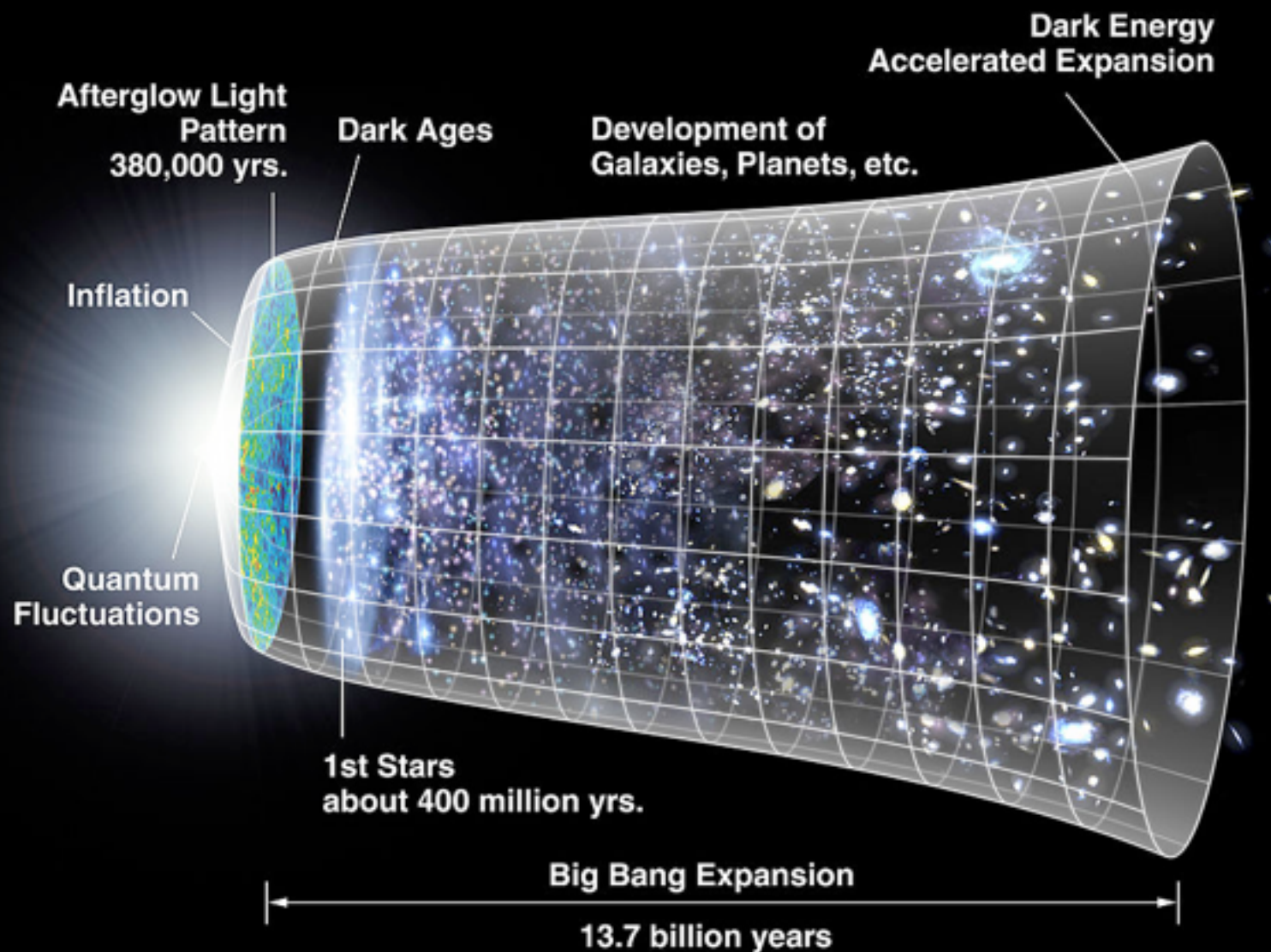
Mika Vesterinen

Physikalisches Institut Heidelberg
On behalf of the LHCb collaboration

CERN LHC seminar
30th September 2014

CP-violation

- Violation of symmetry under Charge and Parity
- Discovered in the weak interaction in 1964



- Baryon asymmetry of the universe: $n_b/n_\gamma \sim 10^{-10}$
- CP-violation in the Standard Model accounts for $\sim 10^{-20}$
- Must be new **new physics** and new sources of CP-violation.

Two ways to find new physics at the LHC

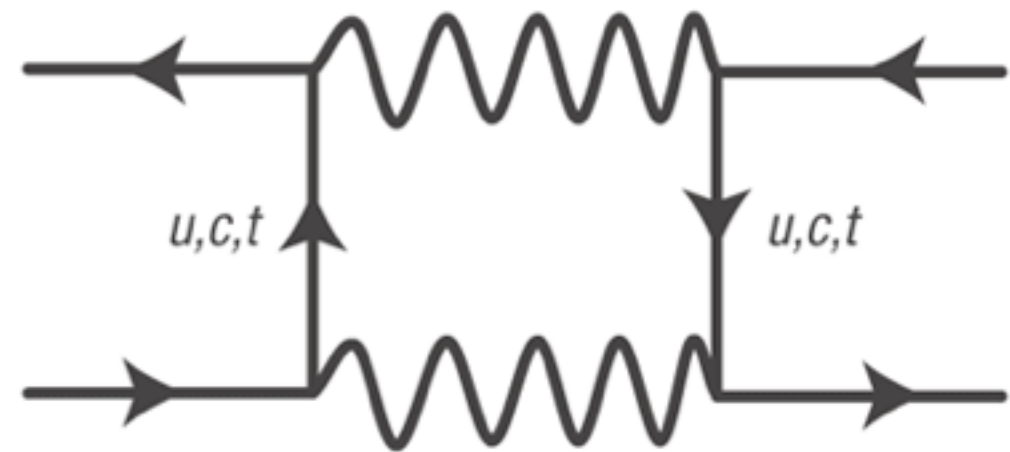
Direct observation



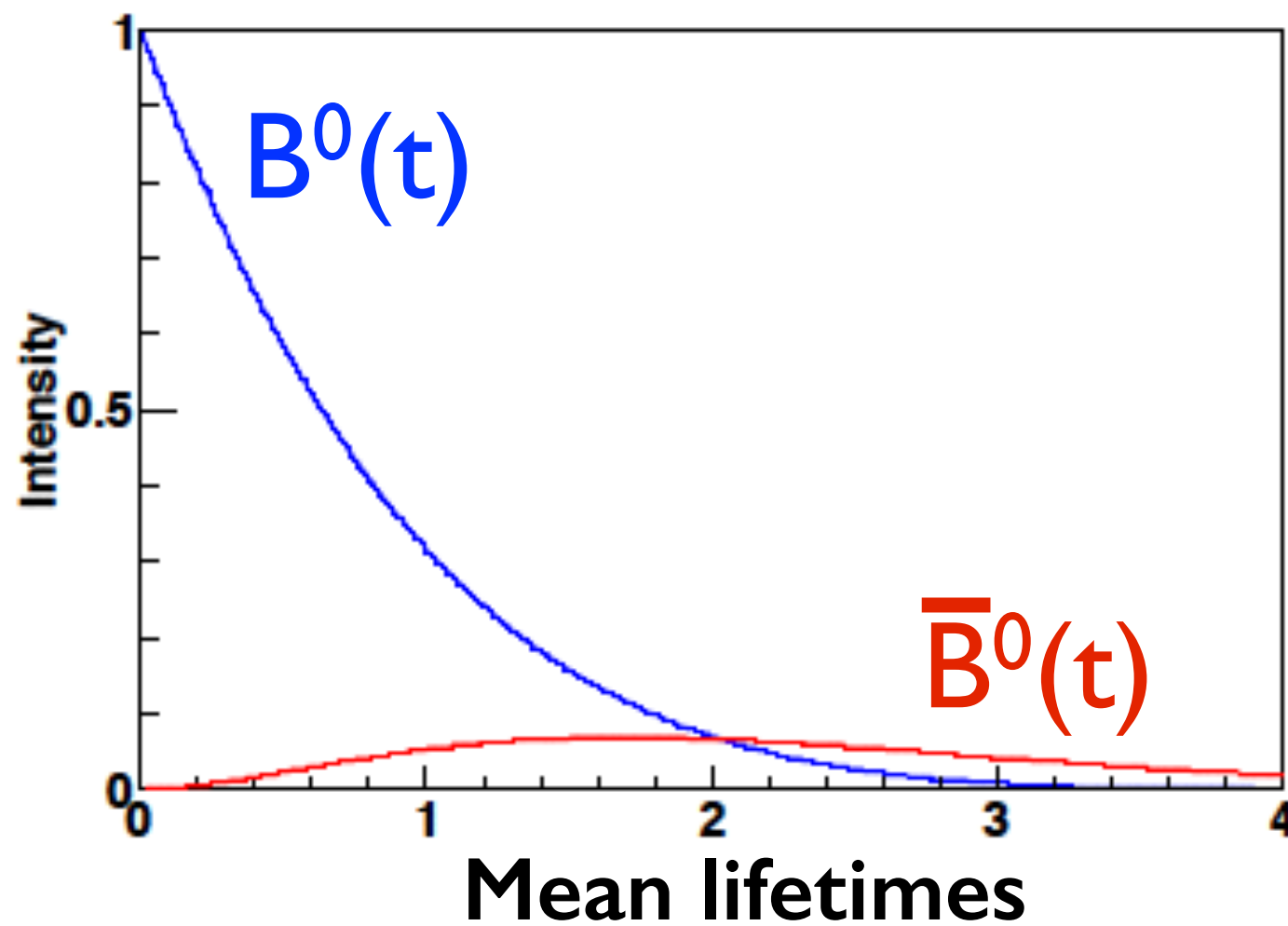
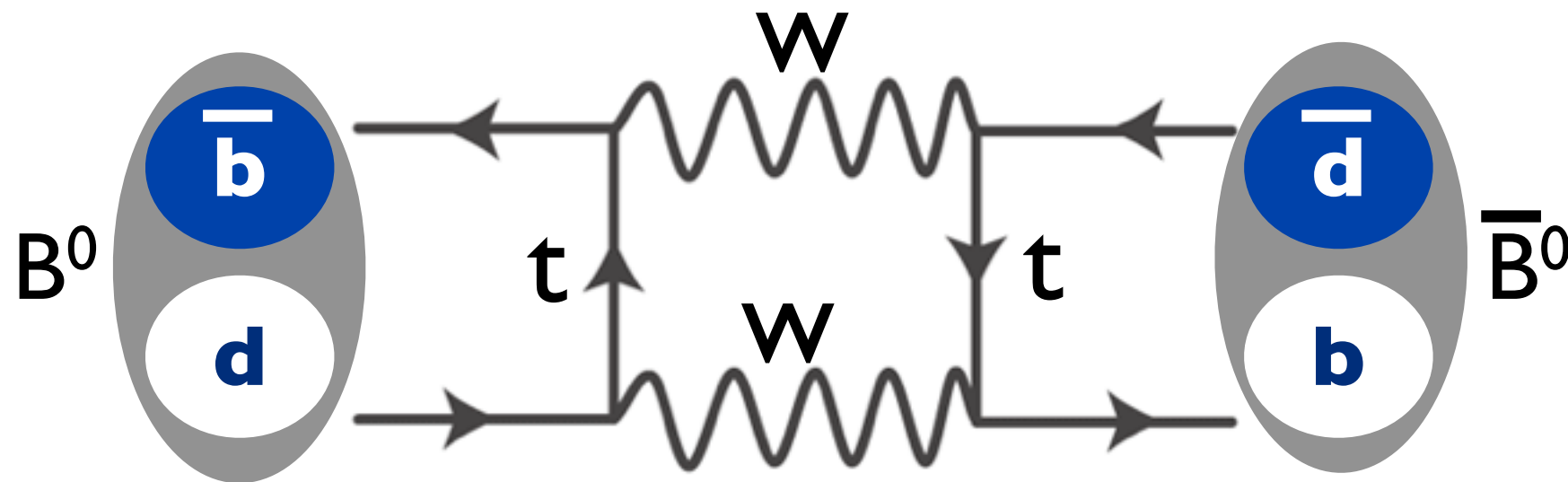
Note that particles with $MC^2 > E$ can't be produced directly...

Indirect effects

... but they can have an effect through quantum corrections



Neutral meson mixing



Neutral meson mixing

- Time evolution from Schrodinger's equation:

$$i \frac{d}{dt} \begin{pmatrix} |B^0(t)\rangle \\ |\bar{B}^0(t)\rangle \end{pmatrix} = \left(M - \frac{i}{2} \Gamma \right) \begin{pmatrix} |B^0(t)\rangle \\ |\bar{B}^0(t)\rangle \end{pmatrix}$$

- With “heavy” and “light” mass eigenstates:

$$|B_{H,L}\rangle = p|B^0\rangle \mp q|\bar{B}^0\rangle$$

- Which can have different masses and decay widths

$$\Delta m = m_H - m_L$$

$$\Delta \Gamma = \Gamma_L - \Gamma_H$$

Neutral meson mixing

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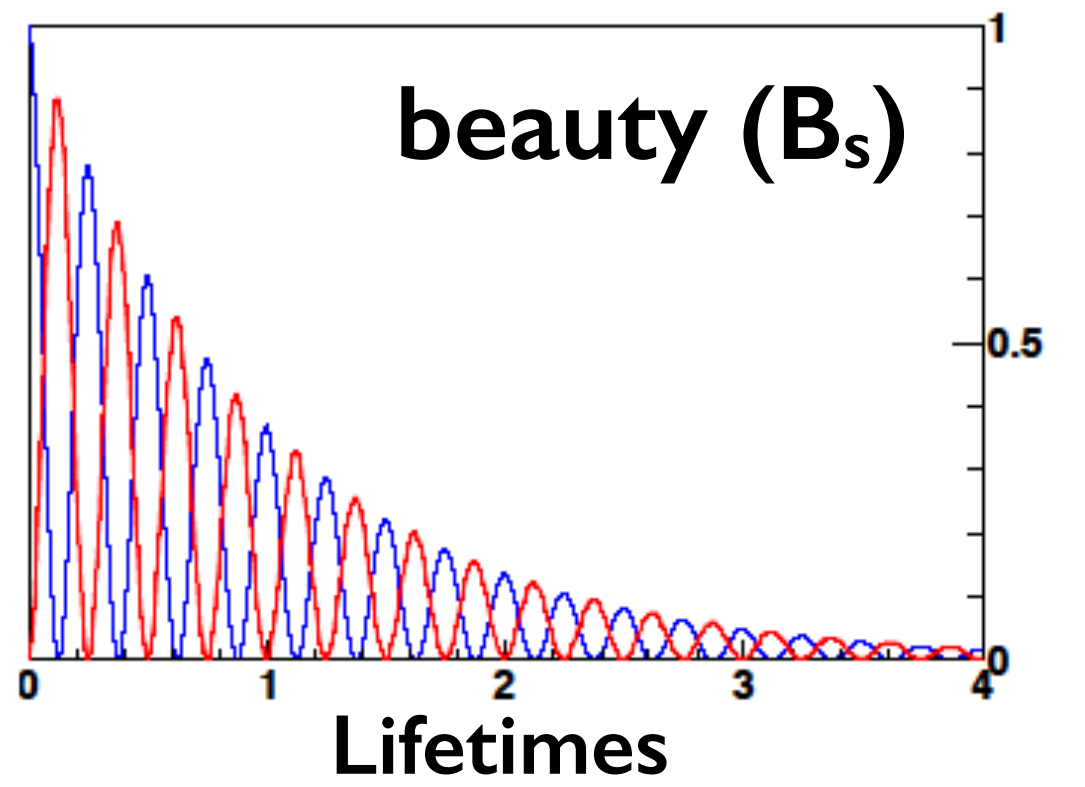
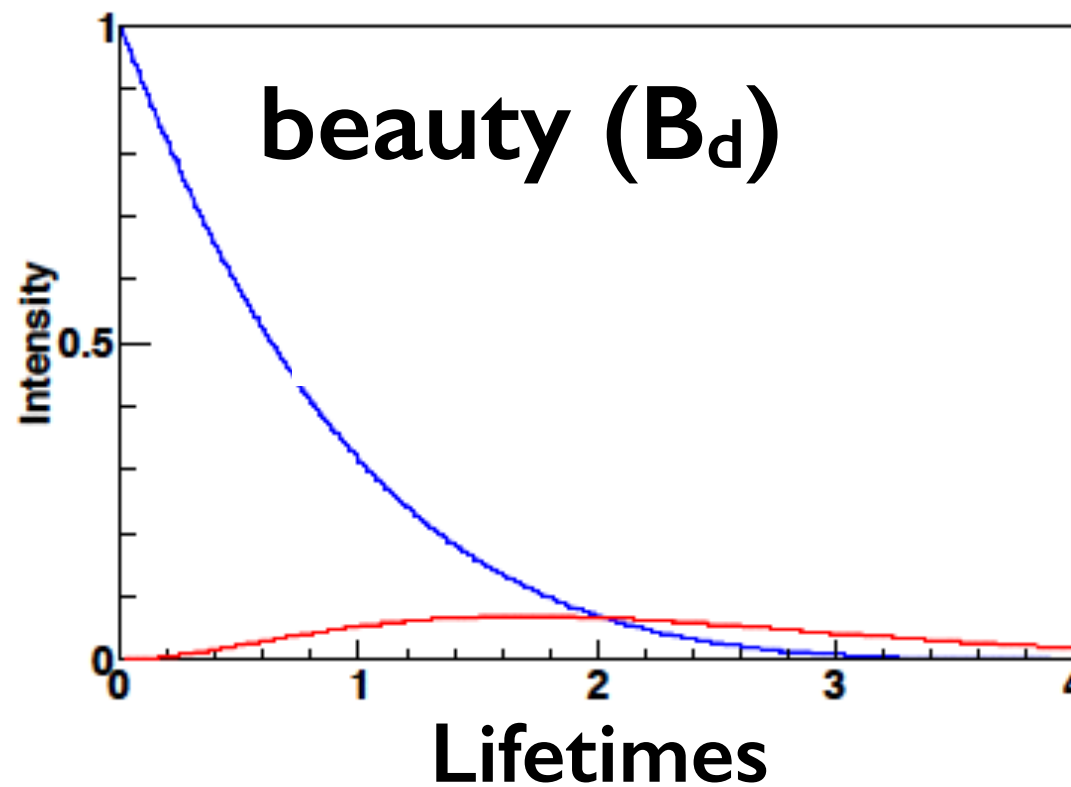
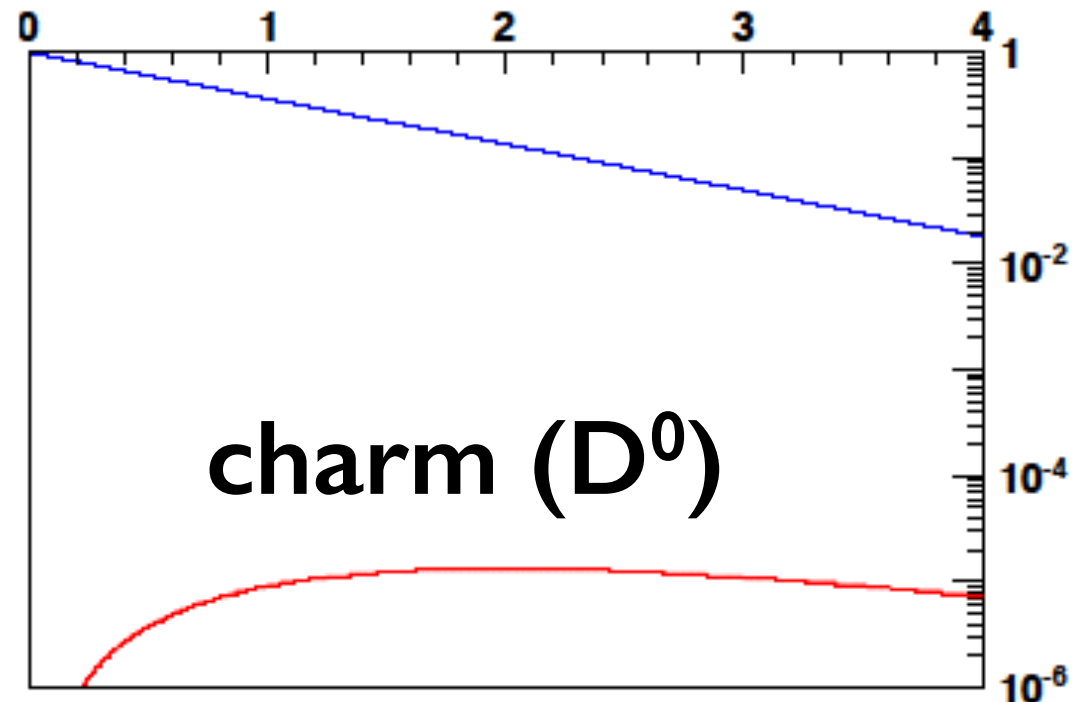
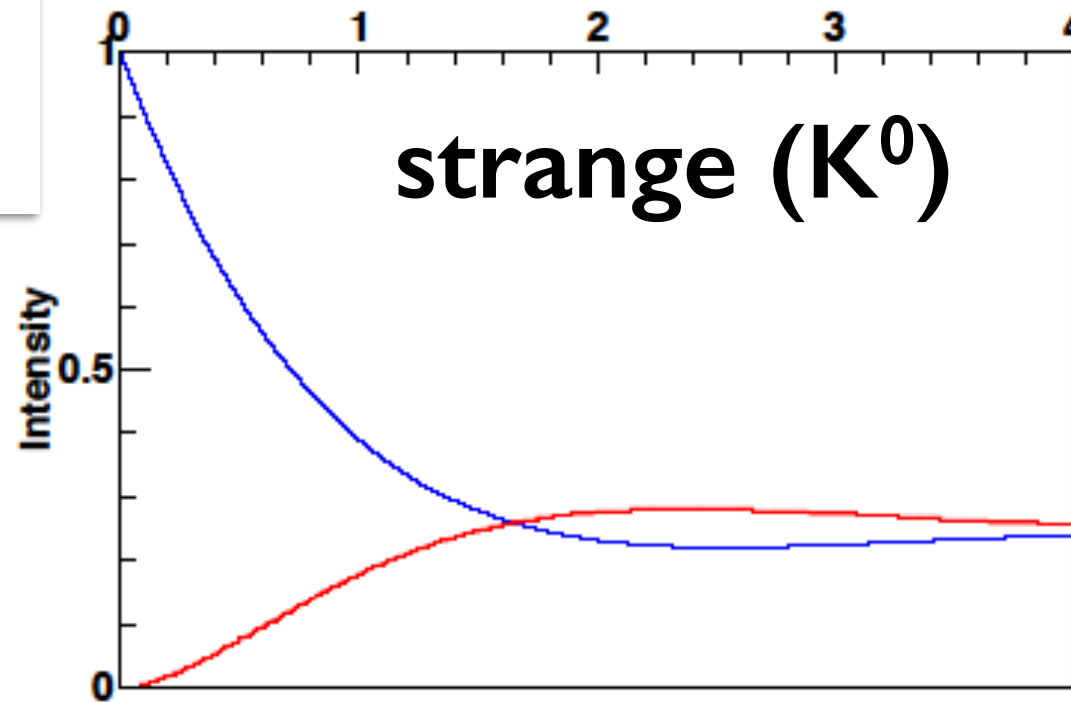
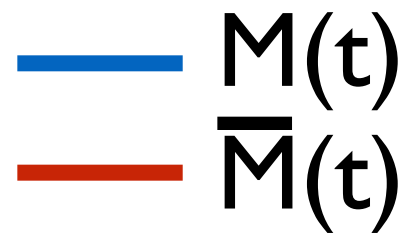
$$\Delta m = m_H - m_L$$

$$\Delta \Gamma = \Gamma_L - \Gamma_H$$

- Probability to find \bar{B} at time t in a B beam:

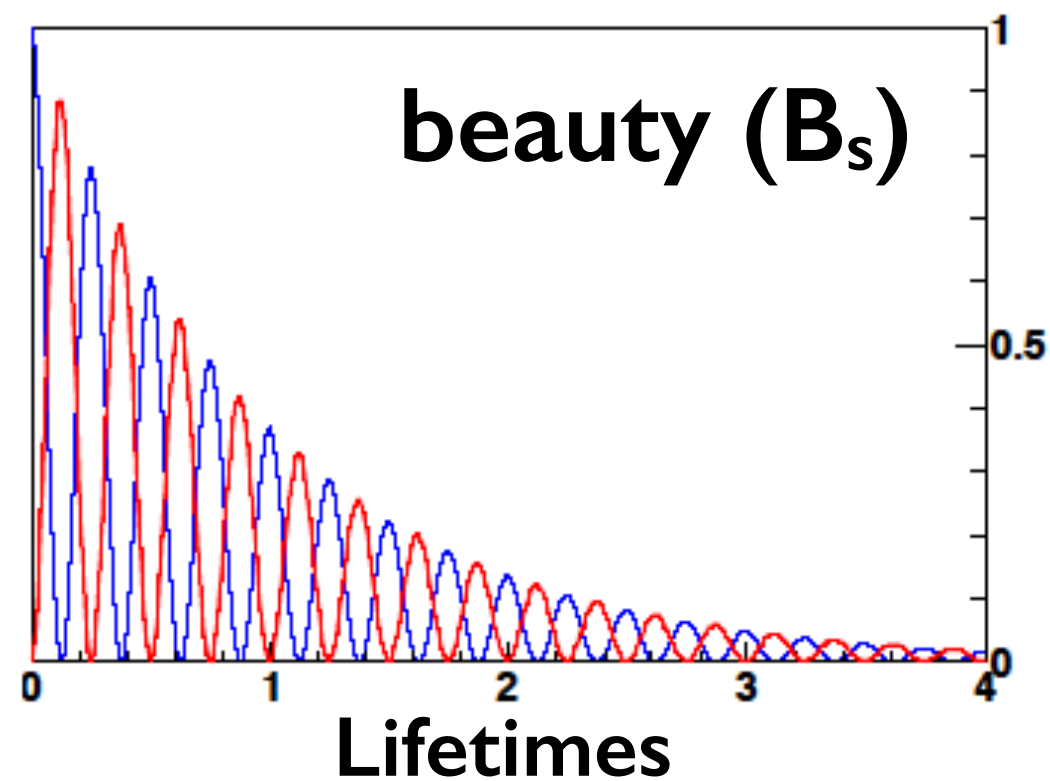
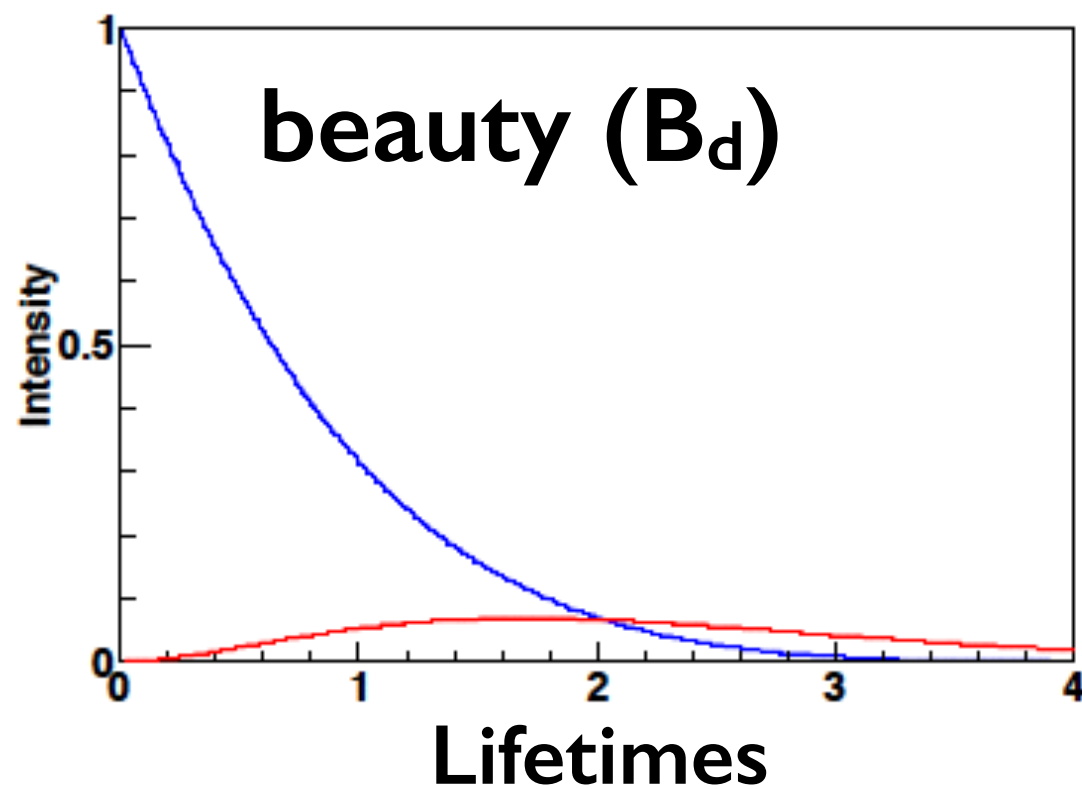
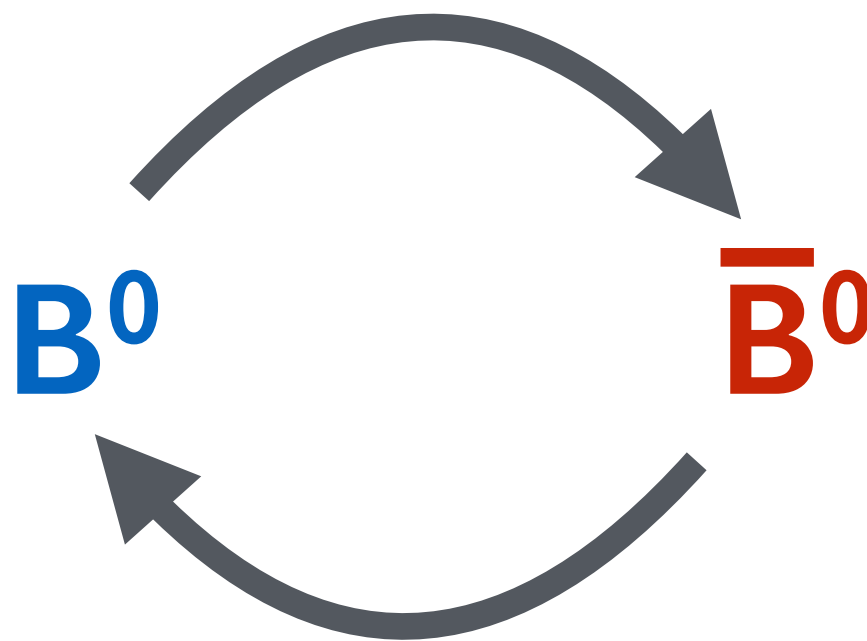
$$\propto e^{-\Gamma t} \left[\cosh \left(\frac{\Delta \Gamma}{2} t \right) - \cos (\Delta m t) \right]$$

Mixing phenomenology



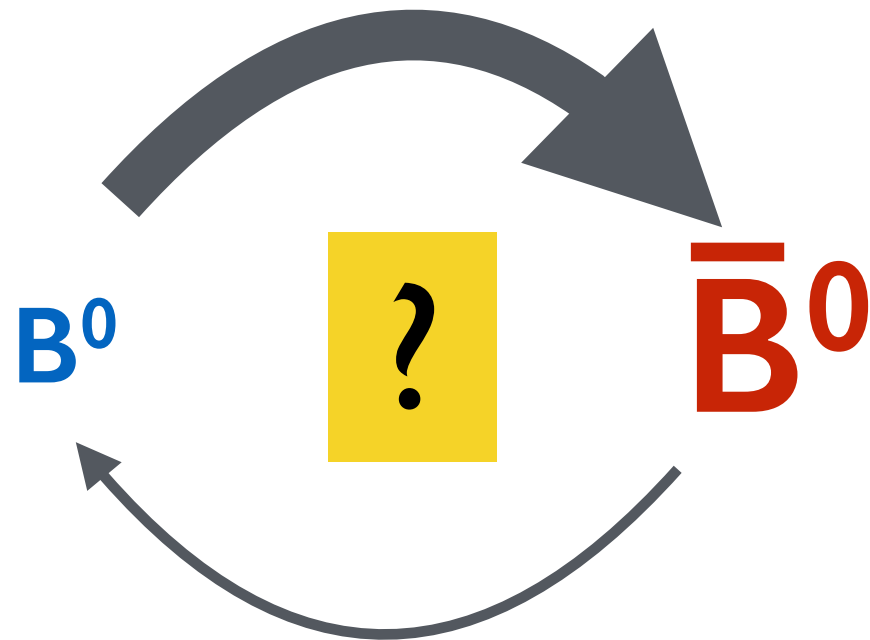
Mixing phenomenology

— $M(t)$
— $\bar{M}(t)$

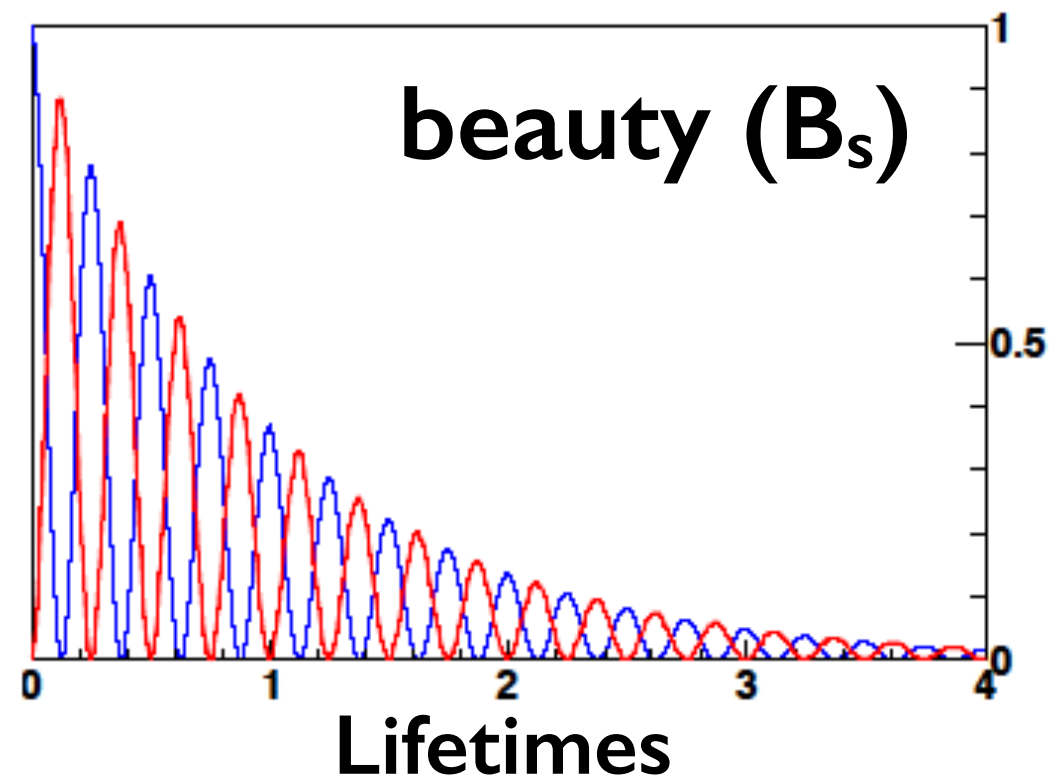
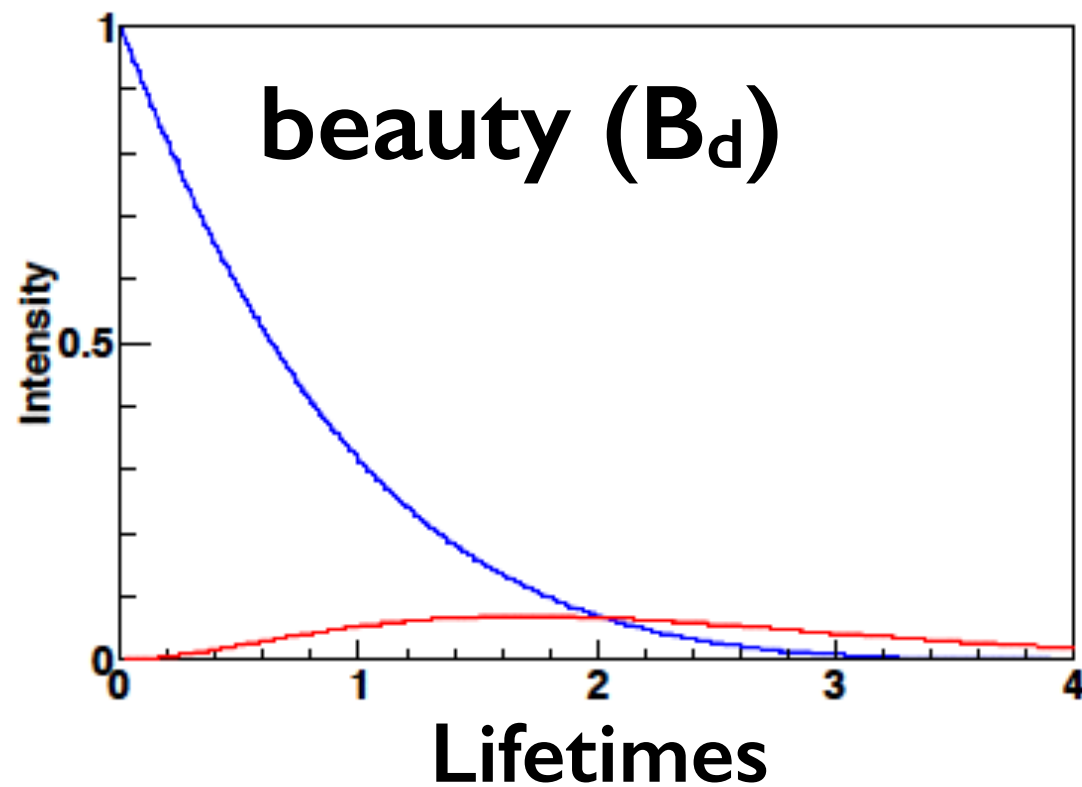


Mixing phenomenology

— $M(t)$
— $\bar{M}(t)$



CP-violation
in mixing

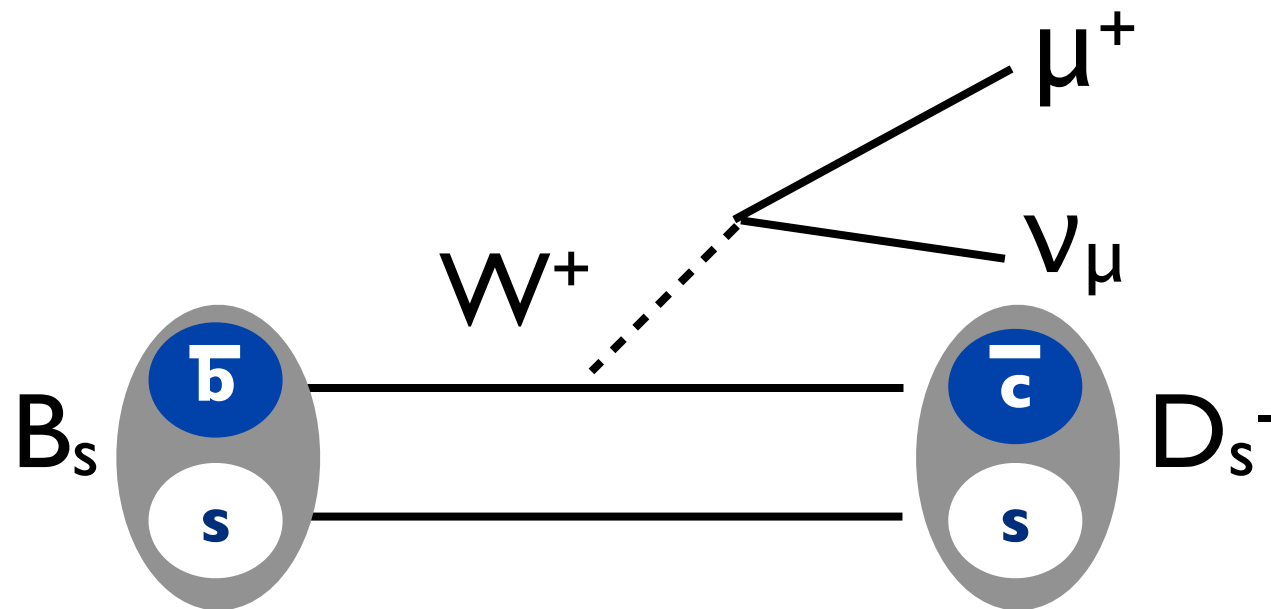


CP violation in mixing

- The CP-violating “semileptonic” asymmetry:

$$a_{sl} = \frac{\Gamma(\bar{B} \rightarrow B \rightarrow f) - \Gamma(B \rightarrow \bar{B} \rightarrow \bar{f})}{\Gamma(\bar{B} \rightarrow B \rightarrow f) + \Gamma(B \rightarrow \bar{B} \rightarrow \bar{f})}$$

- Semileptonic decays tag the flavour



CP violation in mixing

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In the Standard Model*:

$$a_{\text{sl}}^{\text{d}} = (-4.1 \pm 0.6) \times 10^{-4}$$

$$a_{\text{sl}}^{\text{s}} = (1.9 \pm 0.3) \times 10^{-5}$$

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In the Standard Model*:

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(Experimental precision: few $\times 10^{-3}$)

A little theory

- Time dependent Schrodinger equation

$$i \frac{d}{dt} \begin{pmatrix} |B^0(t)\rangle \\ |\bar{B}^0(t)\rangle \end{pmatrix} = \left[\begin{pmatrix} M_{11} & M_{12} \\ M_{12}^* & M_{22} \end{pmatrix} - \frac{i}{2} \begin{pmatrix} \Gamma_{11} & \Gamma_{12} \\ \Gamma_{12}^* & \Gamma_{22} \end{pmatrix} \right] \begin{pmatrix} |B^0(t)\rangle \\ |\bar{B}^0(t)\rangle \end{pmatrix}$$

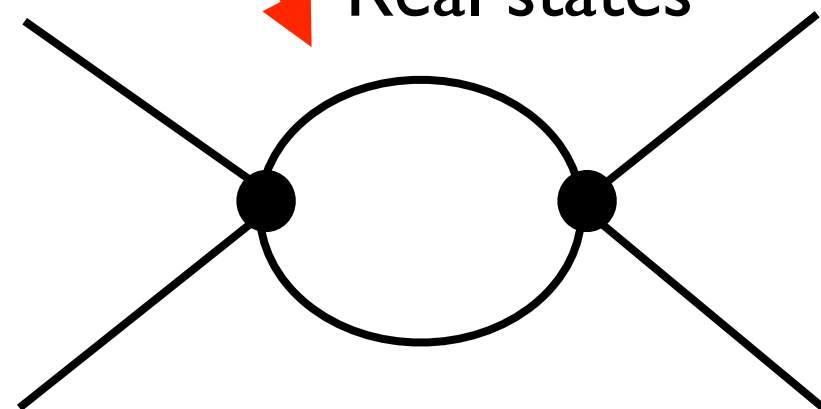
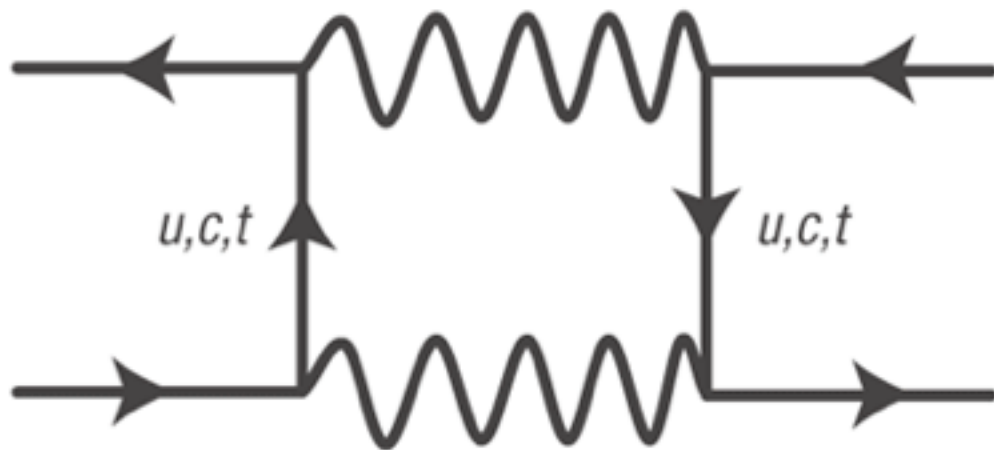
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Virtual states

Real states



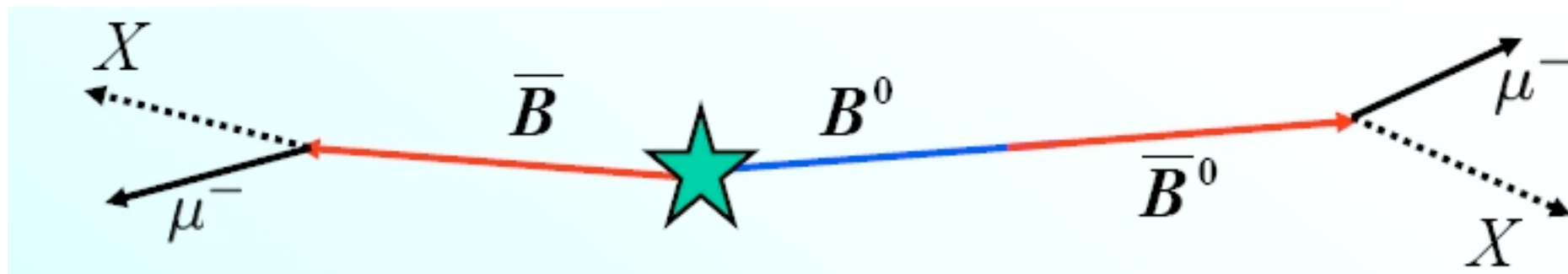
- CP-violation in mixing

$$a_{sl} = \text{Im}(M_{12}/\Gamma_{12})$$

How to measure?

$$a_{\text{sl}} = \frac{\Gamma(\bar{B} \rightarrow B \rightarrow f) - \Gamma(B \rightarrow \bar{B} \rightarrow \bar{f})}{\Gamma(\bar{B} \rightarrow B \rightarrow f) + \Gamma(B \rightarrow \bar{B} \rightarrow \bar{f})}$$

Method A: Inclusive like-sign dilepton asymmetry



$$A_{\ell\ell} \equiv \frac{\Gamma(\ell^+\ell^+) - \Gamma(\ell^-\ell^-)}{\Gamma(\ell^+\ell^+) + \Gamma(\ell^-\ell^-)} = a_{\text{sl}}$$

How to measure?

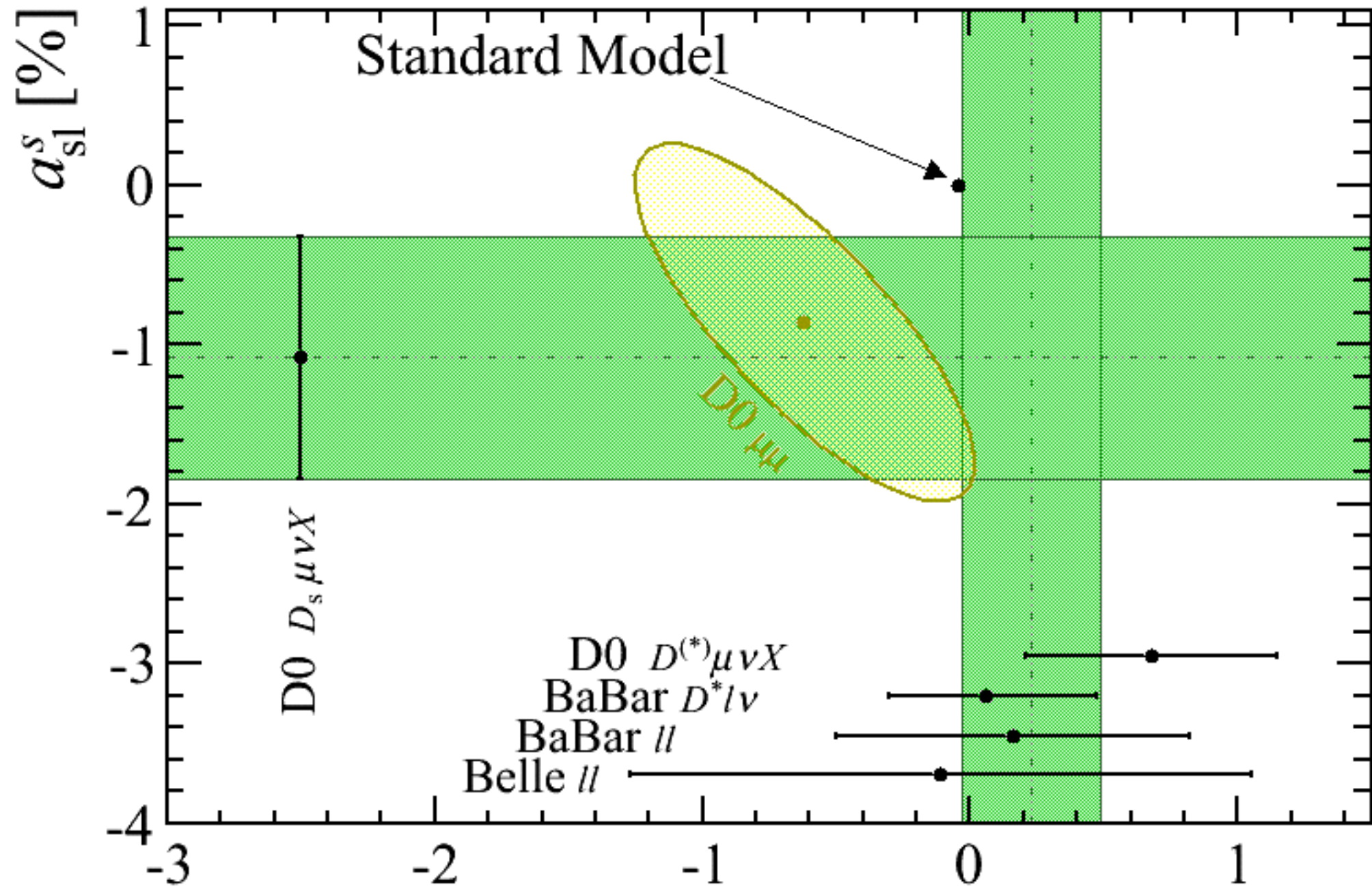
$$a_{\text{sl}} = \frac{\Gamma(\bar{B} \rightarrow B \rightarrow f) - \Gamma(B \rightarrow \bar{B} \rightarrow \bar{f})}{\Gamma(\bar{B} \rightarrow B \rightarrow f) + \Gamma(B \rightarrow \bar{B} \rightarrow \bar{f})}$$

Method B: Untagged asymmetry (used by LHCb)

$$\frac{N(B, t) - N(\bar{B}, t)}{N(B, t) + N(\bar{B}, t)} = \frac{a_{\text{sl}}}{2} \cdot \left[1 - \frac{\cos \Delta M t}{\cosh \frac{\Delta \Gamma t}{2}} \right]$$

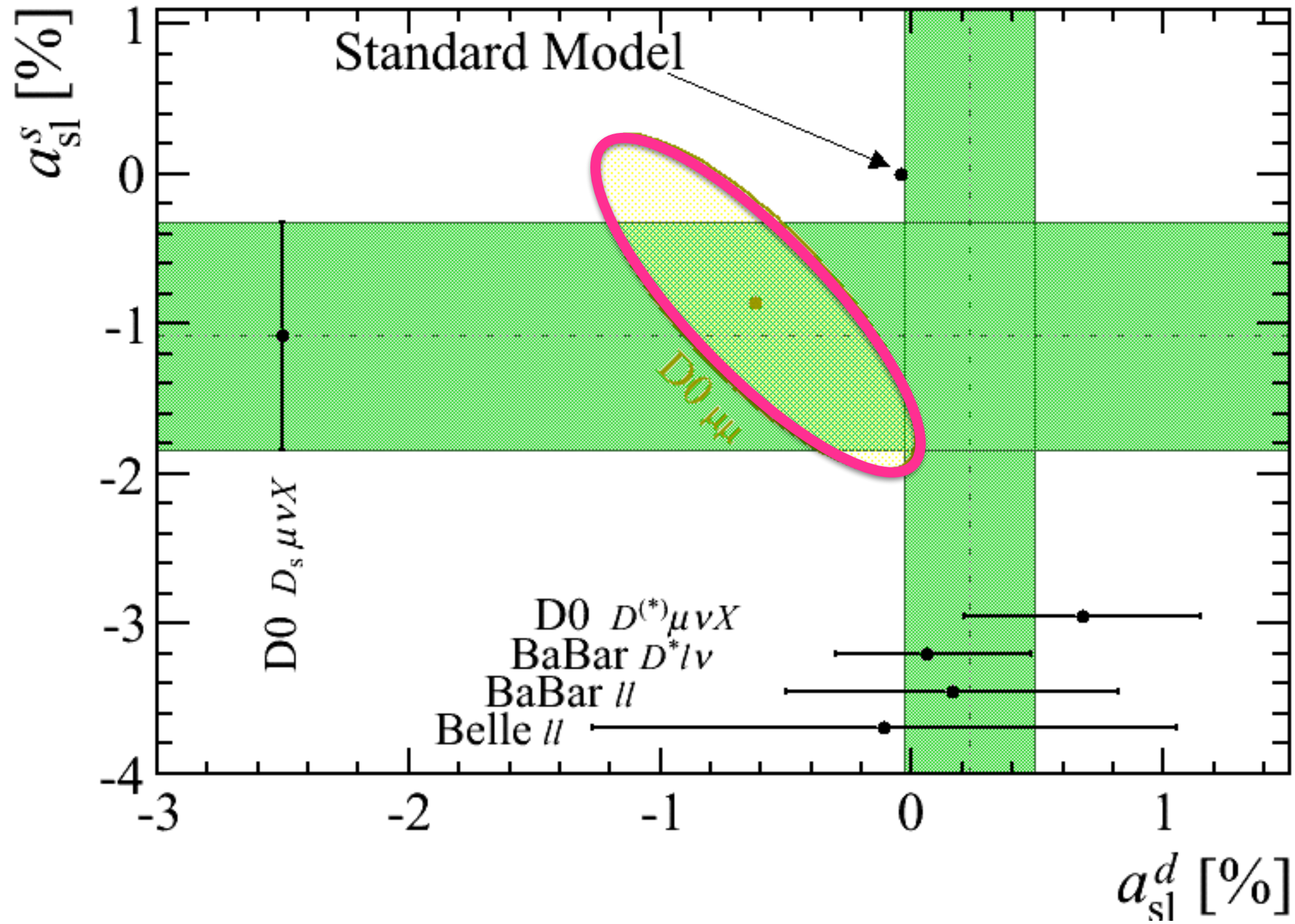
Look for an oscillating asymmetry as a function of decay time

Experimental landscape before LHCb



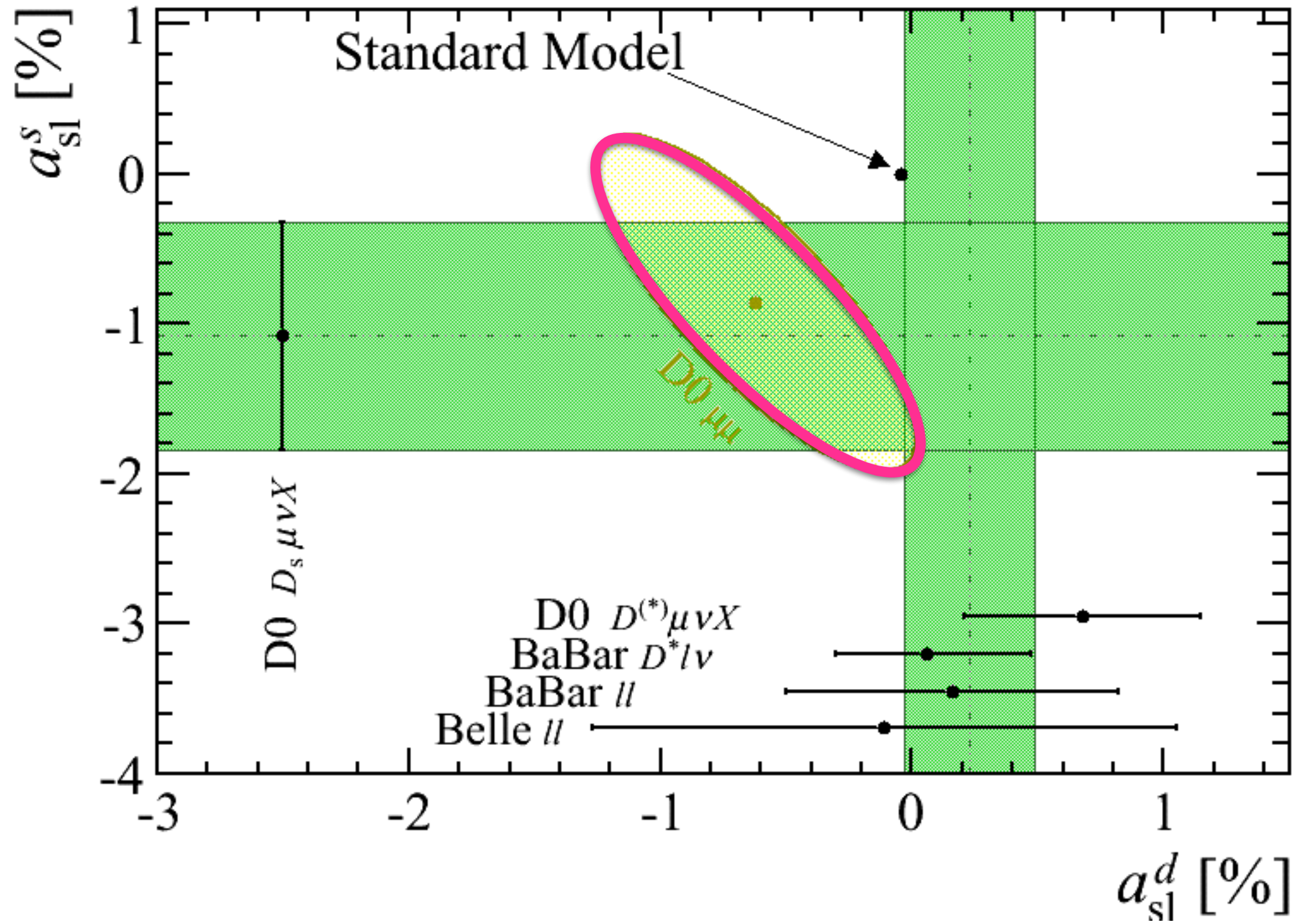
A preliminary measurement of $a_{sl}^d = (-3.9 \pm 3.5 \pm 1.9) \times 10^{-3}$, with inclusive dileptons was reported by BaBar at CKM 2014 (see [slides](#) of Chih-hsiang Cheng)

Experimental landscape before LHCb



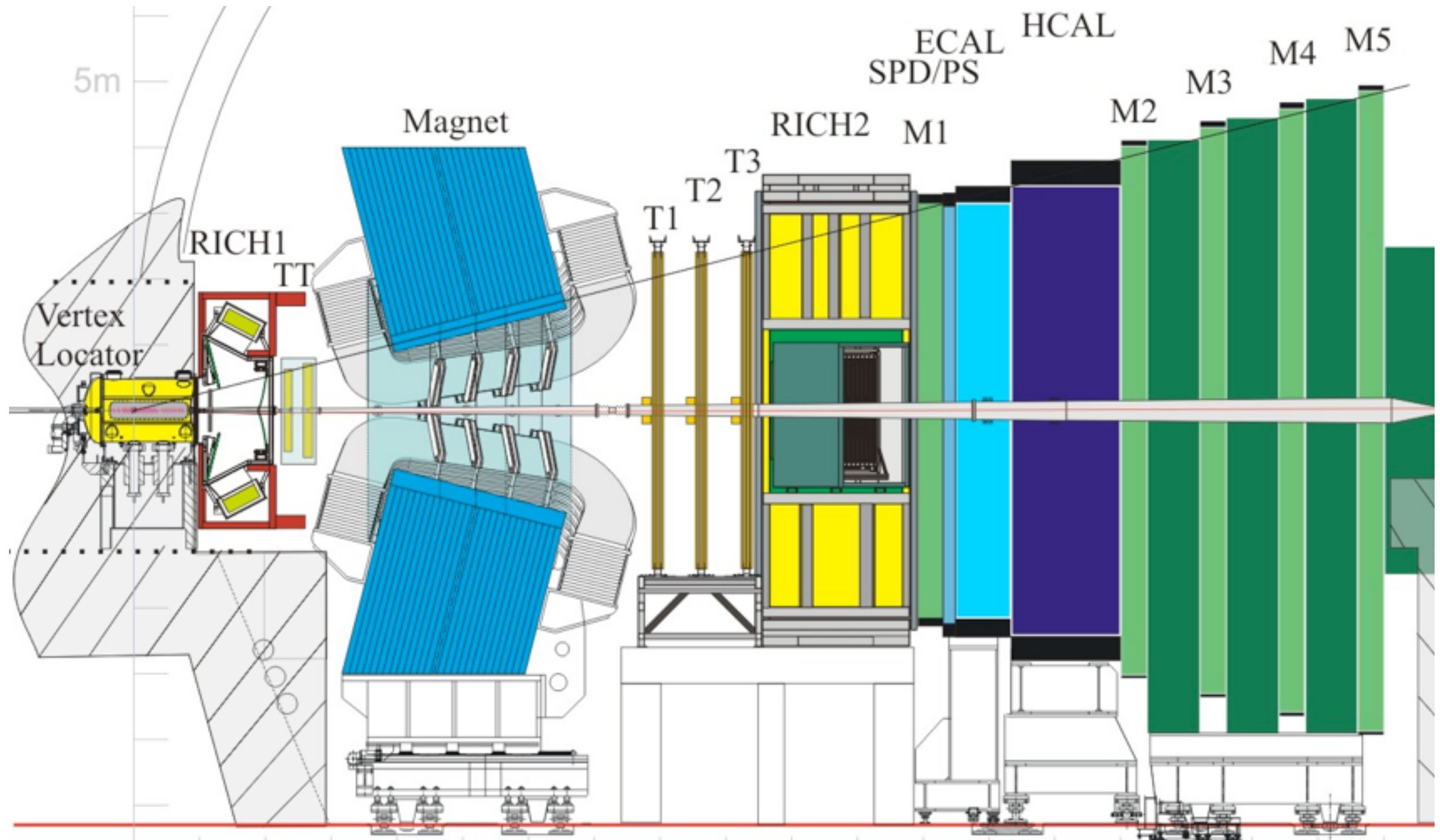
Dimuon asymmetry from D0 is 3.6σ from the SM

Experimental landscape before LHCb



New measurements urgently needed

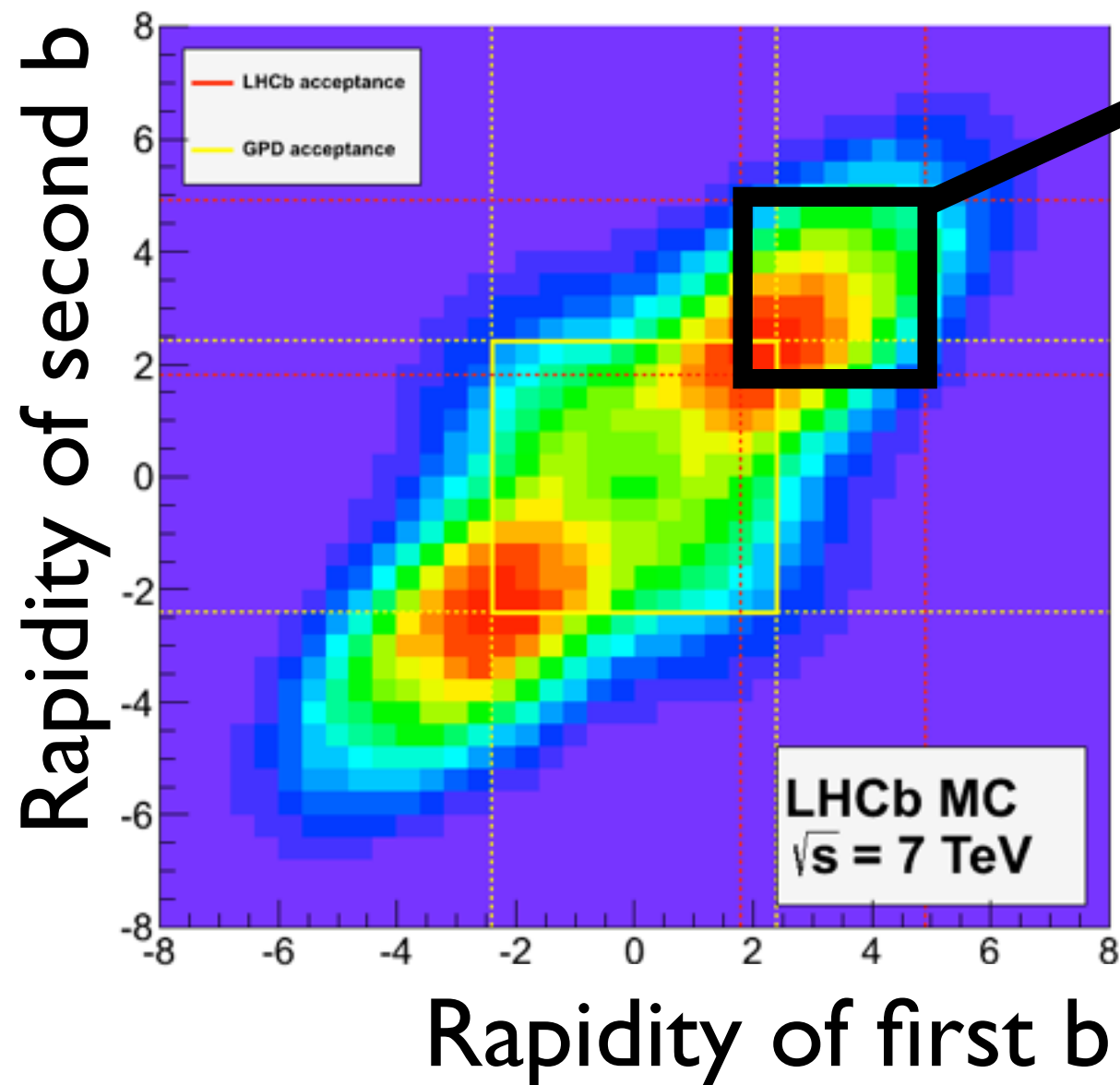
The LHC beauty experiment



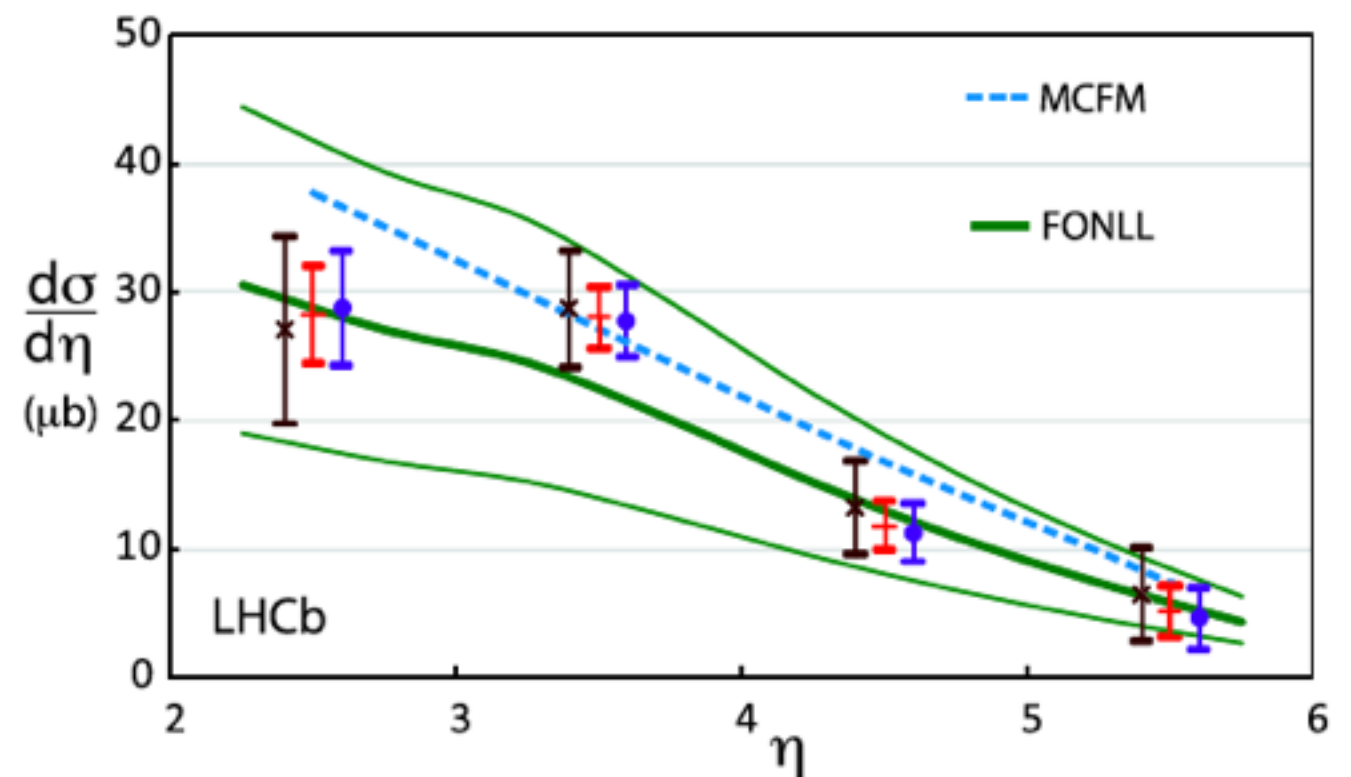
*LHCb reoptimized detector design and performance :Technical Design Report,
CERN-LHCC-2003-030*

The LHC beauty experiment

b production at the LHC is mostly in the forward direction



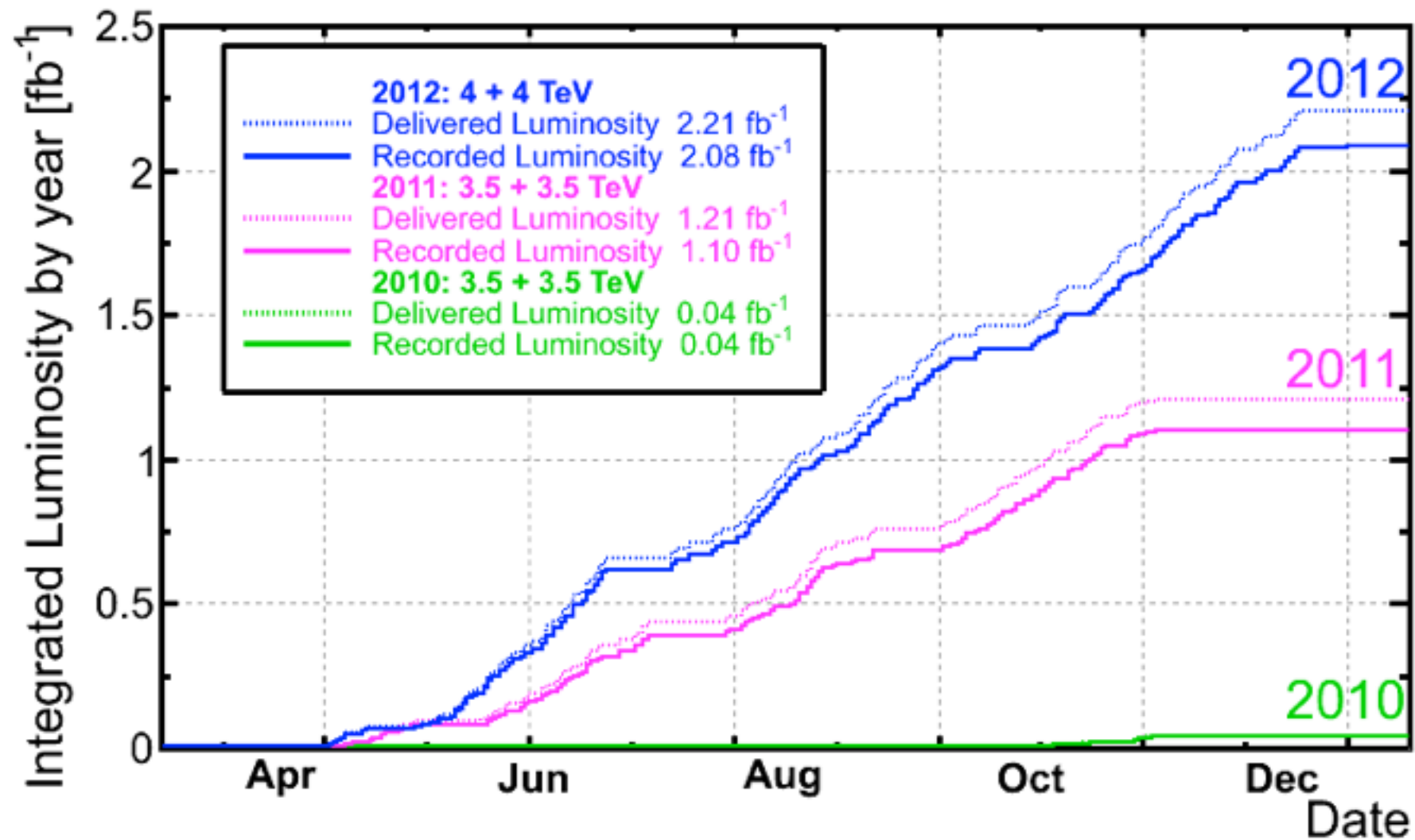
b cross section in LHCb:
 $(75 \pm 14) \mu\text{b} @ 7 \text{ TeV}$



LHCb, Phys Lett. B694 209-2016 (2010)

The LHC beauty experiment

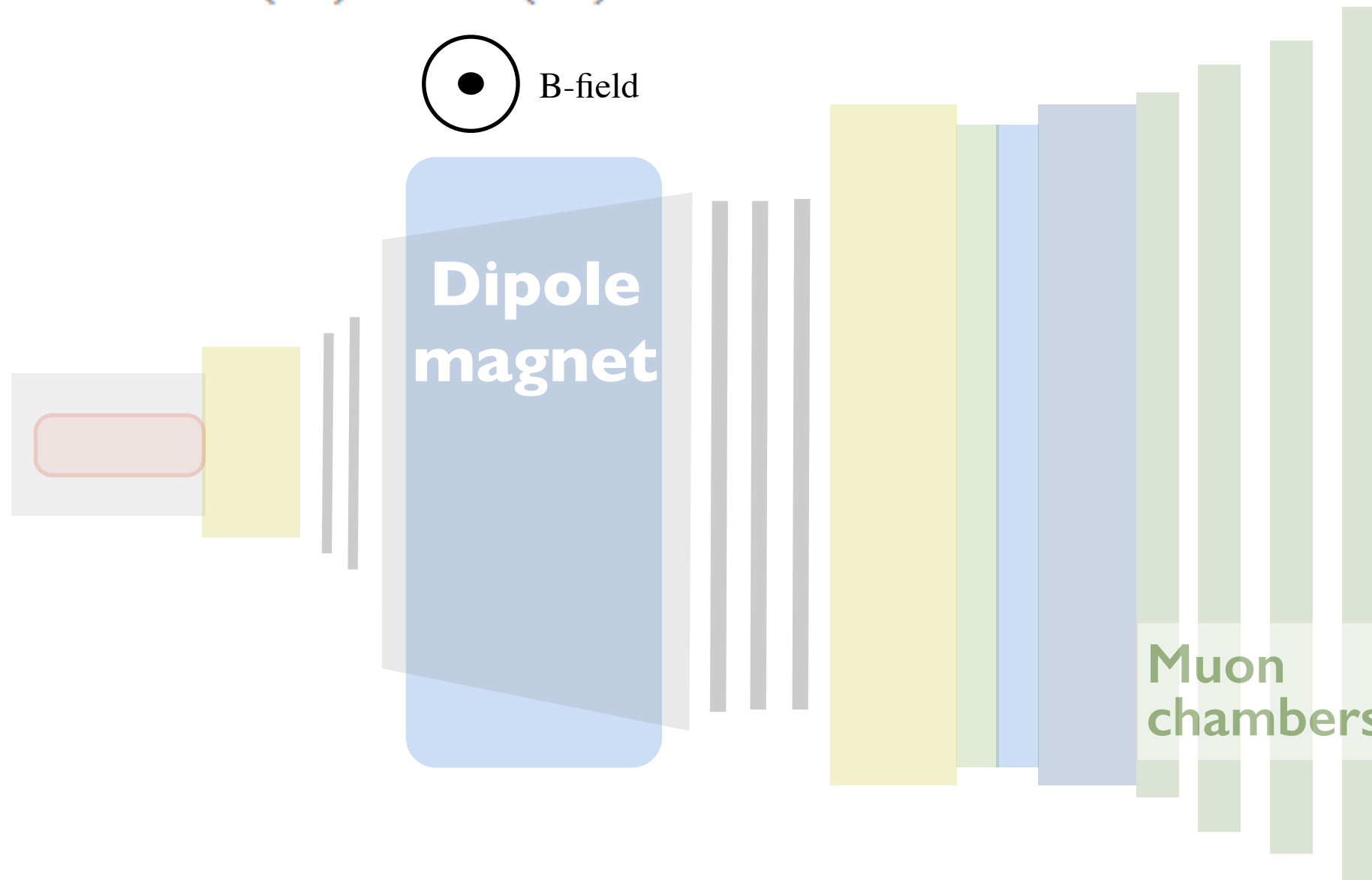
3 fb⁻¹ recorded in Run-I
Around 10¹² b hadrons!



Thanks to the machine people!
Also for delivering our two polarity scheme...

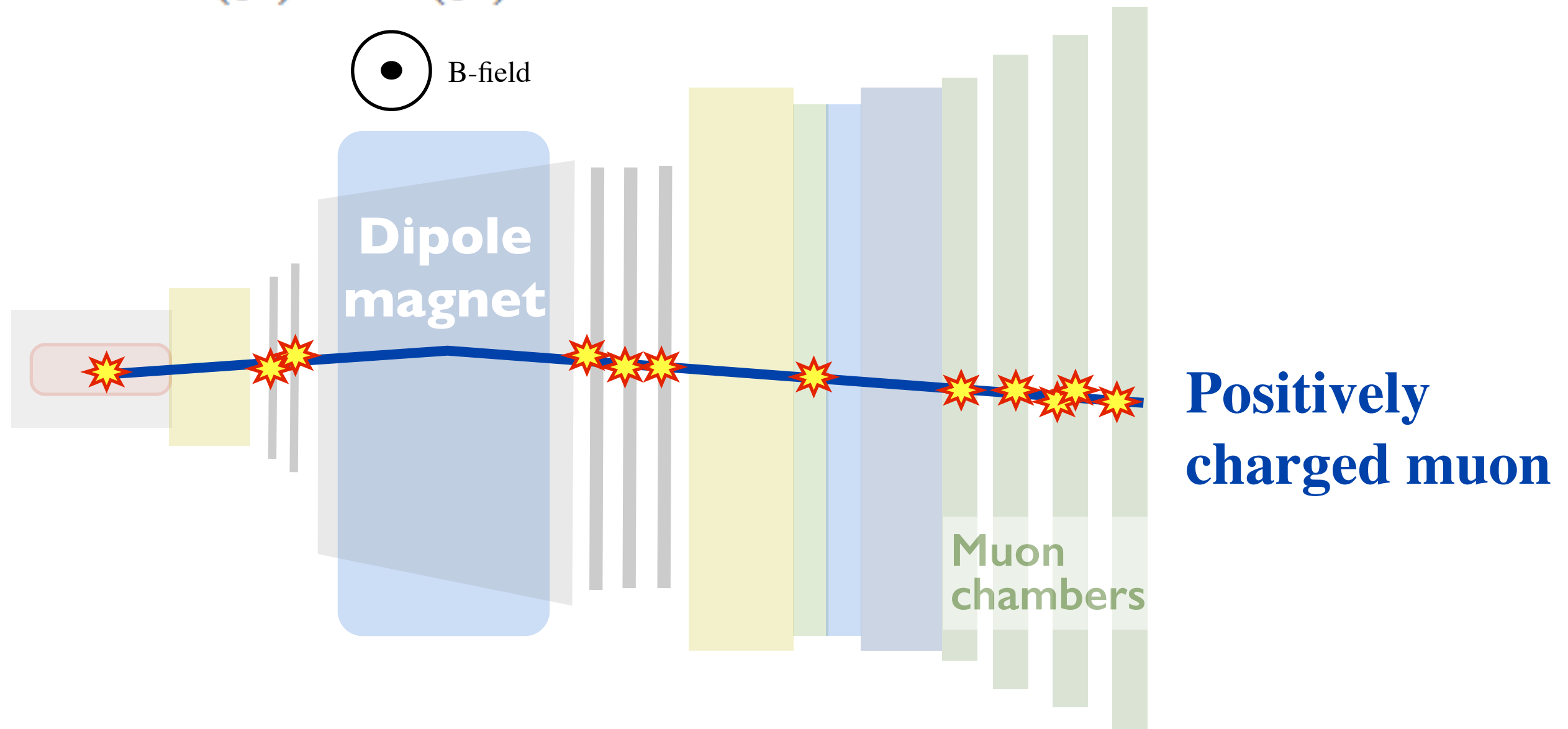
Detection asymmetries

$$A_D = \frac{\varepsilon(f) - \varepsilon(\bar{f})}{\varepsilon(f) + \varepsilon(\bar{f})}$$



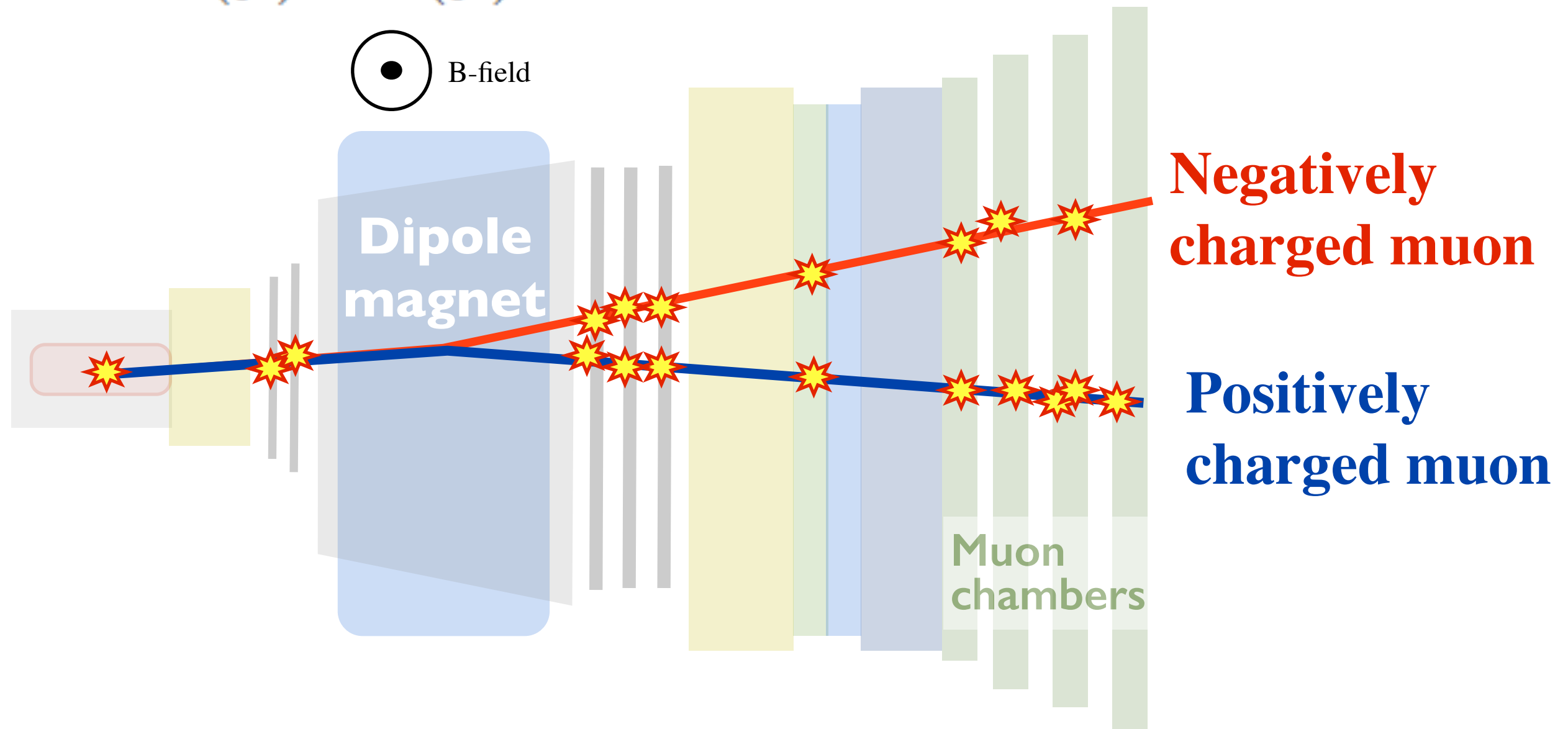
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Detection asymmetries

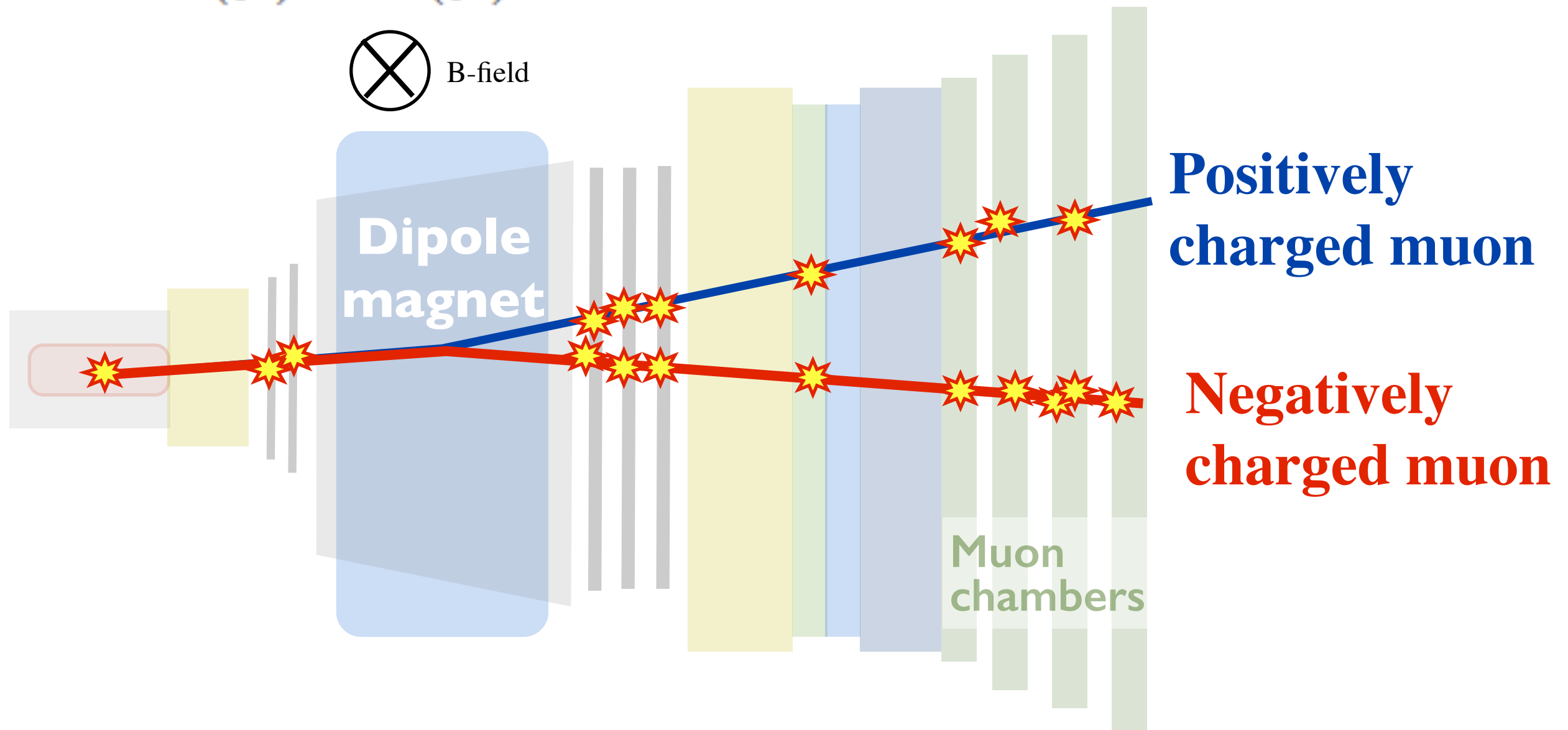
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Detection asymmetries

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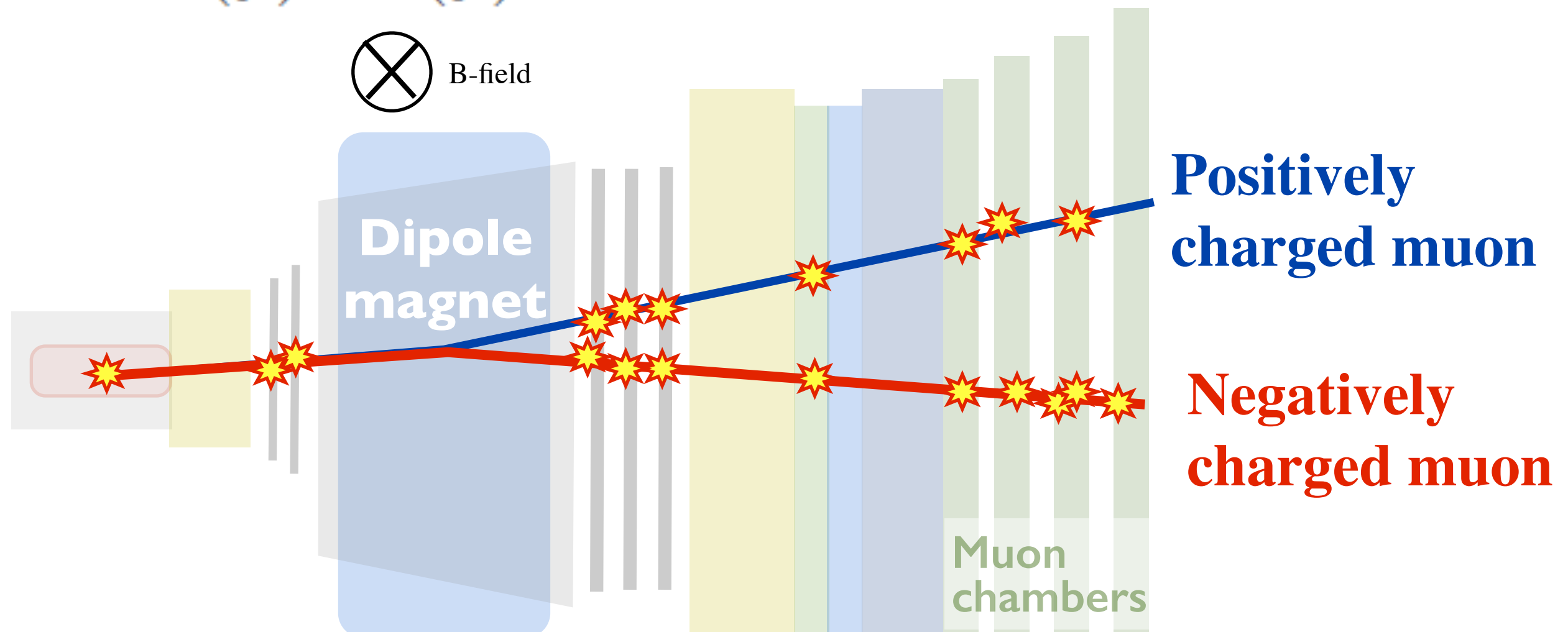
Reversed magnet polarity



Detection asymmetries

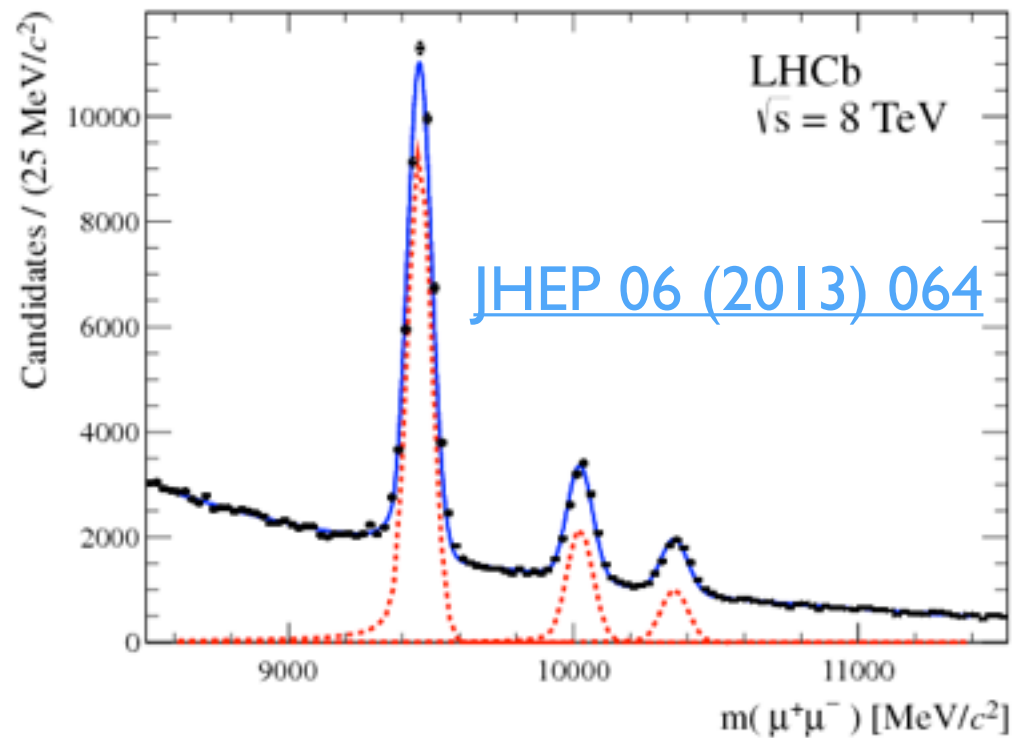
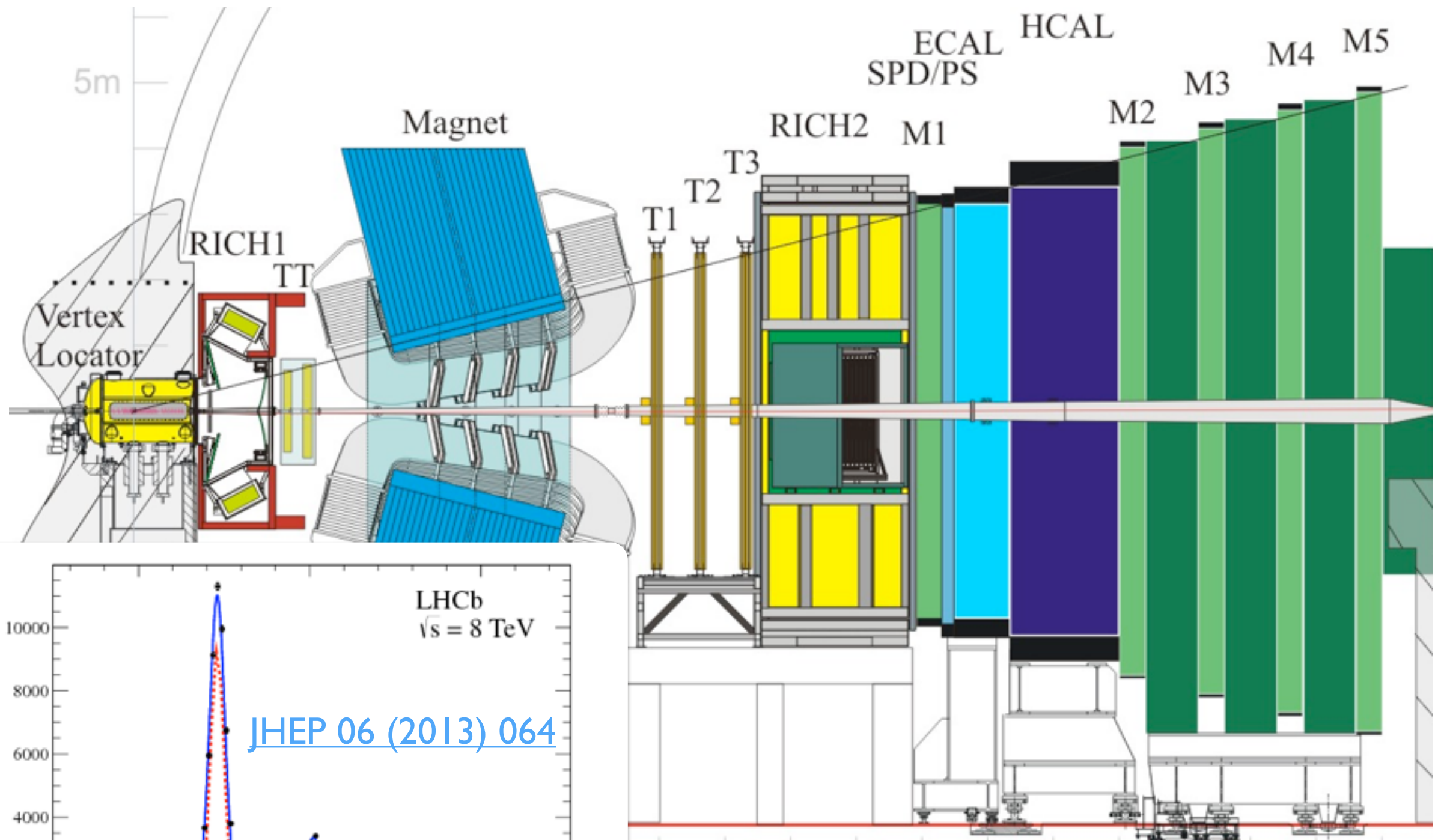
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Reversed magnet polarity



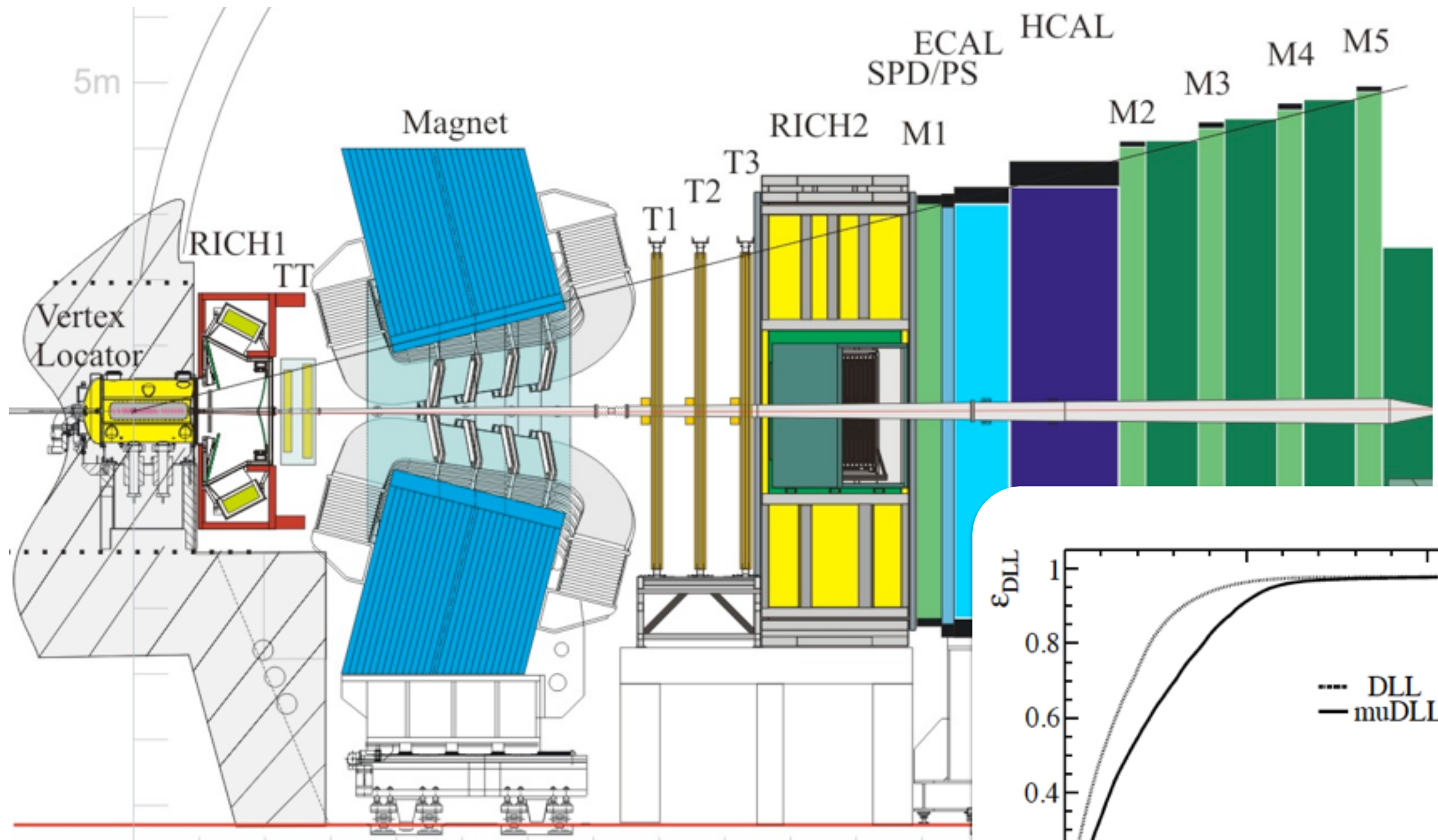
- Effectiveness depends on high frequency (2 week) of changes.
- Does not cancel asymmetries to 10^{-3} level, but crucial systematic check of result.

The LHC beauty experiment

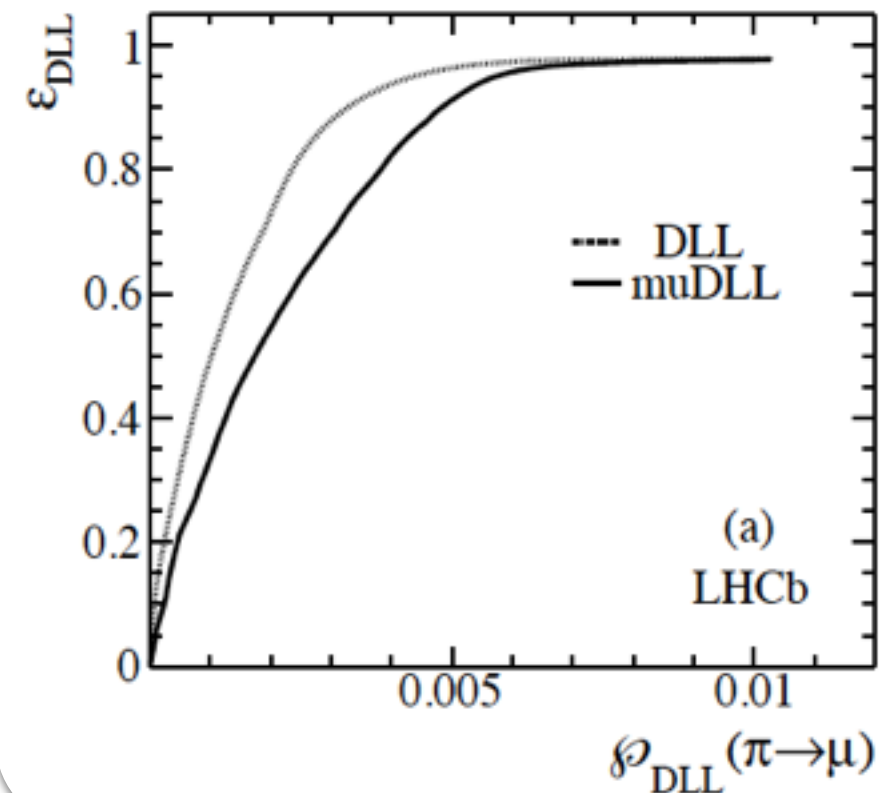


Excellent tracking

The LHC beauty experiment



Excellent muon-ID



Measuring a_{sl} at LHCb

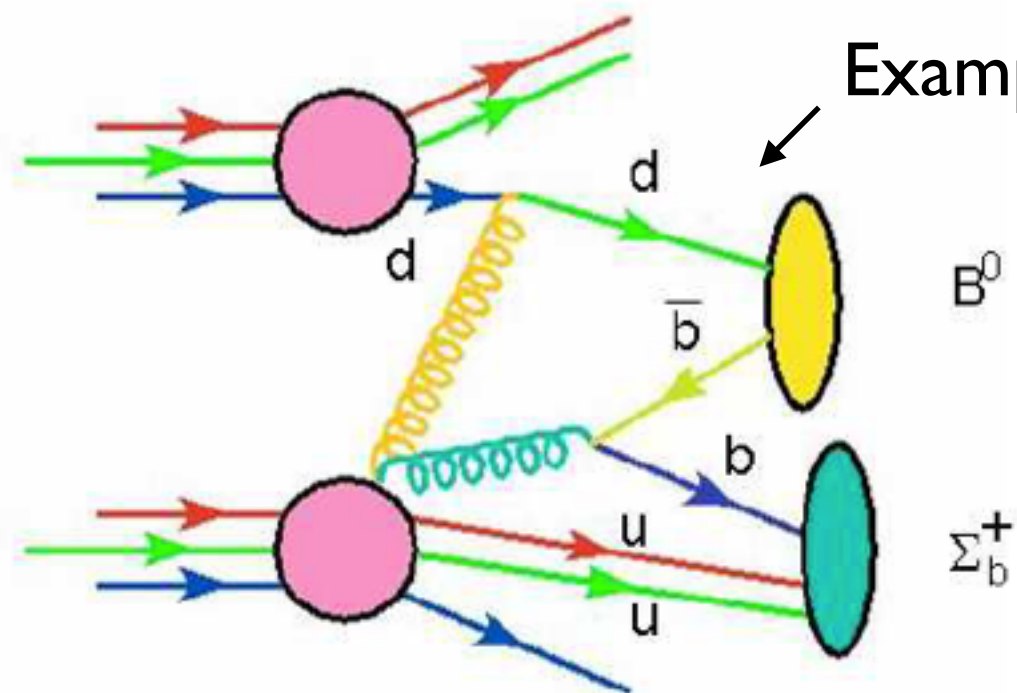
- This is what we need to measure

$$\frac{N(B, t) - N(\bar{B}, t)}{N(B, t) + N(\bar{B}, t)} = \frac{a_{sl}}{2} \cdot \left[1 - \frac{\cos \Delta M t}{\cosh \frac{\Delta \Gamma t}{2}} \right]$$

The problem...



Production asymmetries



Expected to be around 1%

$$a_P = \frac{\sigma(pp \rightarrow \bar{B}) - \sigma(pp \rightarrow B)}{\sigma(pp \rightarrow \bar{B}) + \sigma(pp \rightarrow B)}$$

Now need to measure:

$$\frac{N(B, t) - N(\bar{B}, t)}{N(B, t) + N(\bar{B}, t)} = \frac{a_{sl}}{2} - \left[a_P + \frac{a_{sl}}{2} \right] \cdot \frac{\cos \Delta M t}{\cosh \frac{\Delta \Gamma t}{2}}$$

Simpler for a_{sl}^s

Decay time integrated asymmetry

$$\frac{N(B_s^0) - N(\bar{B}_s^0)}{N(B_s^0) + N(\bar{B}_s^0)} = \frac{a_{sl}^s}{2} + \left[a_P - \frac{a_{sl}^s}{2} \right] \frac{\int_{t=0}^{\infty} e^{-\Gamma_s t} \cos(\Delta M_s t) \epsilon(t) dt}{\int_{t=0}^{\infty} e^{-\Gamma_s t} \cosh\left(\frac{\Delta\Gamma_s t}{2}\right) \epsilon(t) dt}$$

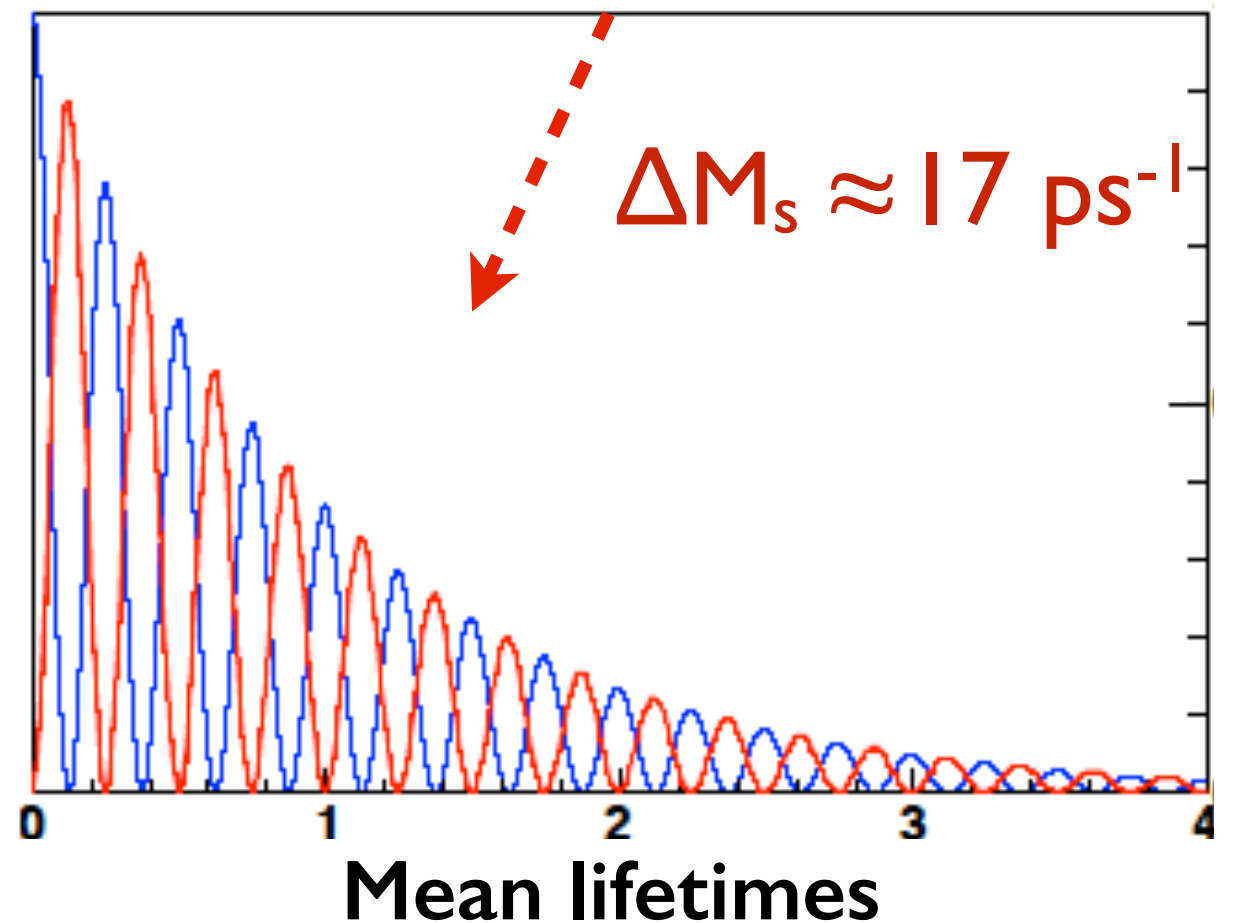
Simpler for a_{sl}^s

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$< 10^{-4}$

Effect of a_P is washed out
by the fast oscillations!



Simpler for a_{sl}^s

“Simply” need to measure:

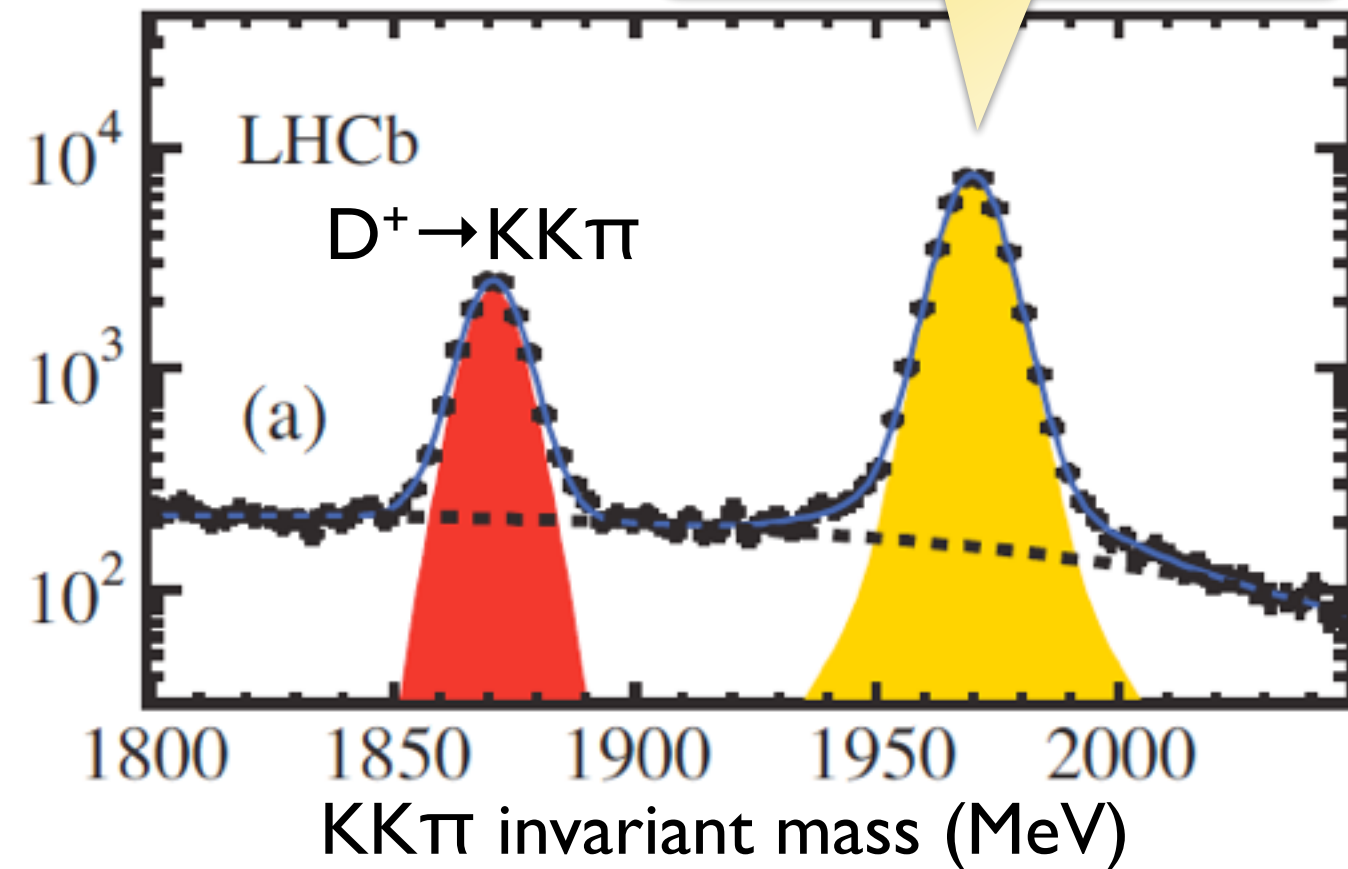
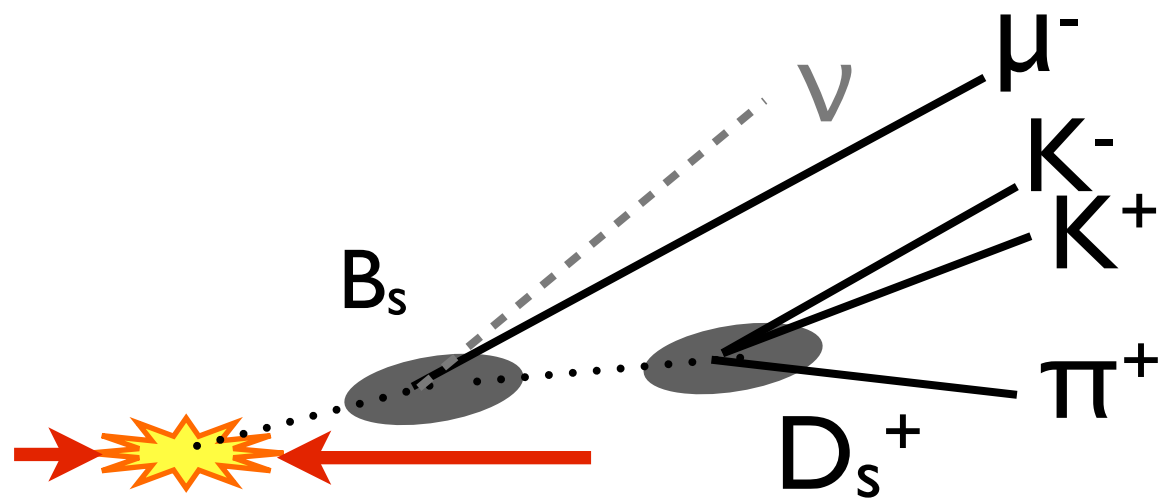
$$\frac{N(B_s^0) - N(\overline{B}_s^0)}{N(B_s^0) + N(\overline{B}_s^0)} = \frac{a_{sl}^s}{2}$$

Simpler for a_{sl}^s

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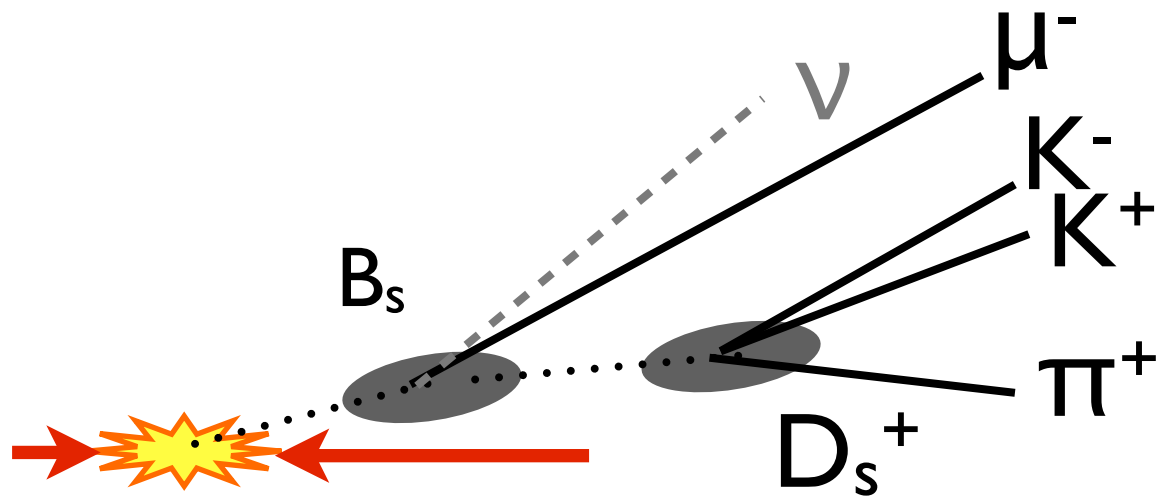
200k $B_s \rightarrow D_s \mu$
signal events in
2011



Simpler for a_{sl}^s

“Simply” need to measure:

$$\frac{N(B_s^0) - N(\bar{B}_s^0)}{N(B_s^0) + N(\bar{B}_s^0)} = \frac{a_{sl}^s}{2}$$



- The main problem is the detection asymmetry.
- Restricting to the $\phi \rightarrow KK$ resonance so only have a $\mu^\pm \pi^\mp$ asymmetry.

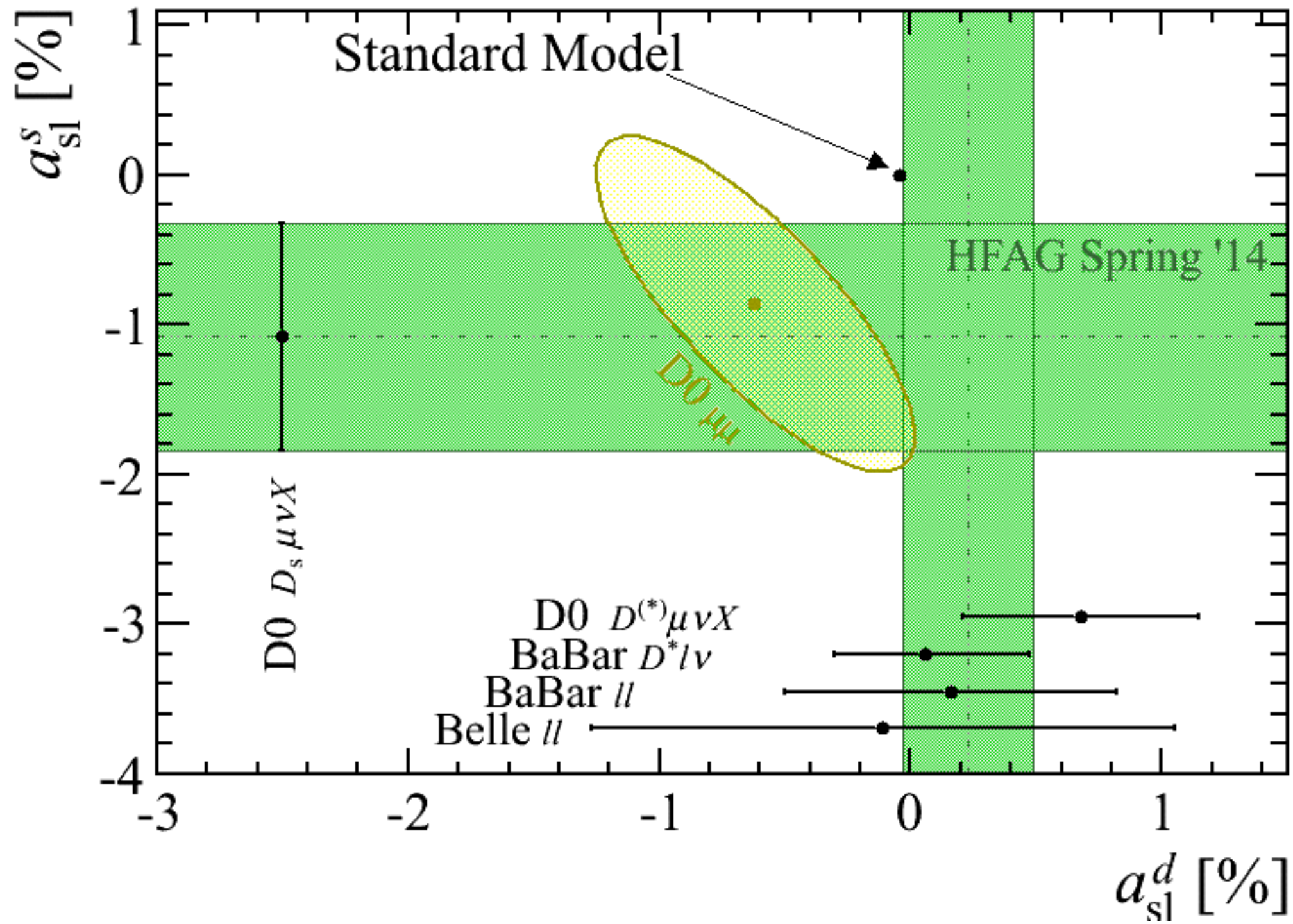
Result with 2011 dataset (1 fb⁻¹)

$$a_{sl^s} = (-0.06 \pm 0.50_{\text{stat}} \pm 0.36_{\text{syst}})\%$$

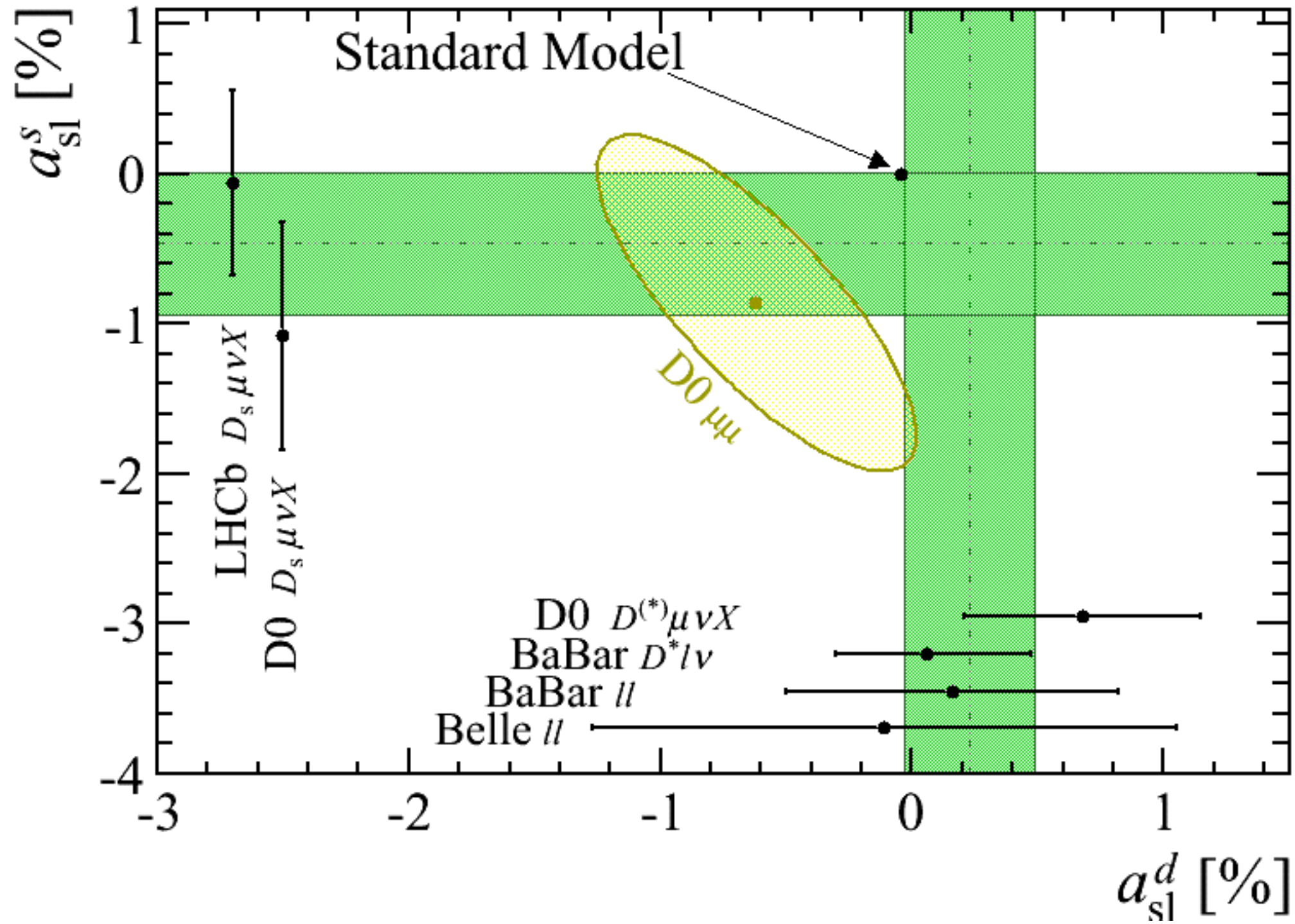
Source	δ (%)
Tracking asymmetries	0.26
Muon asymmetries	0.16
Fitting	0.15
Backgrounds	0.10
Quadratic sum	0.36

LHCb Collaboration, “Measurement of the flavour-specific CP-violating asymmetry a_{sl^s} in B_0 s decays”, PLB 728C 607-615 (2014).

Landscape before



Landscape after



LHCb measurement of a_{sl}

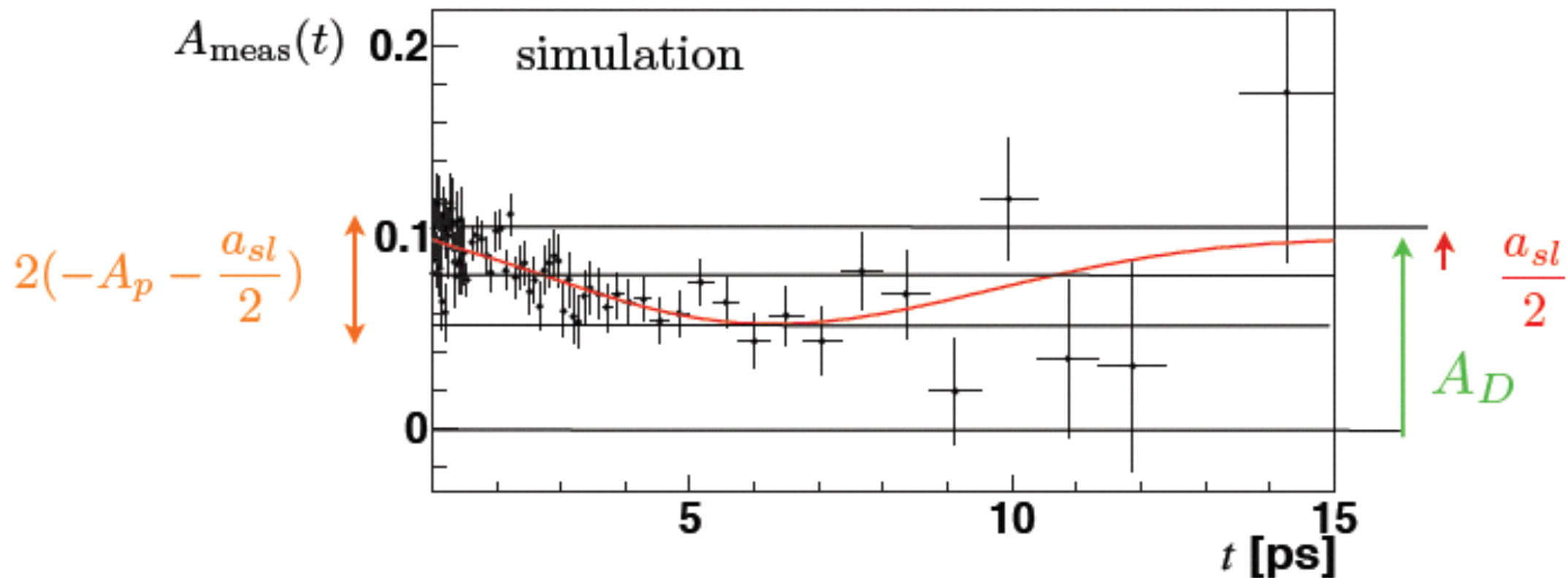
- B_d mesons oscillate too slowly
- Fit the asymmetry as a function of decay time, to disentangle a_P and a_{sl} .

$$\frac{N(B, t) - N(\bar{B}, t)}{N(B, t) + N(\bar{B}, t)} = \frac{a_{sl}}{2} - \left[a_P + \frac{a_{sl}}{2} \right] \cdot \frac{\cos \Delta M t}{\cosh \frac{\Delta \Gamma t}{2}}$$

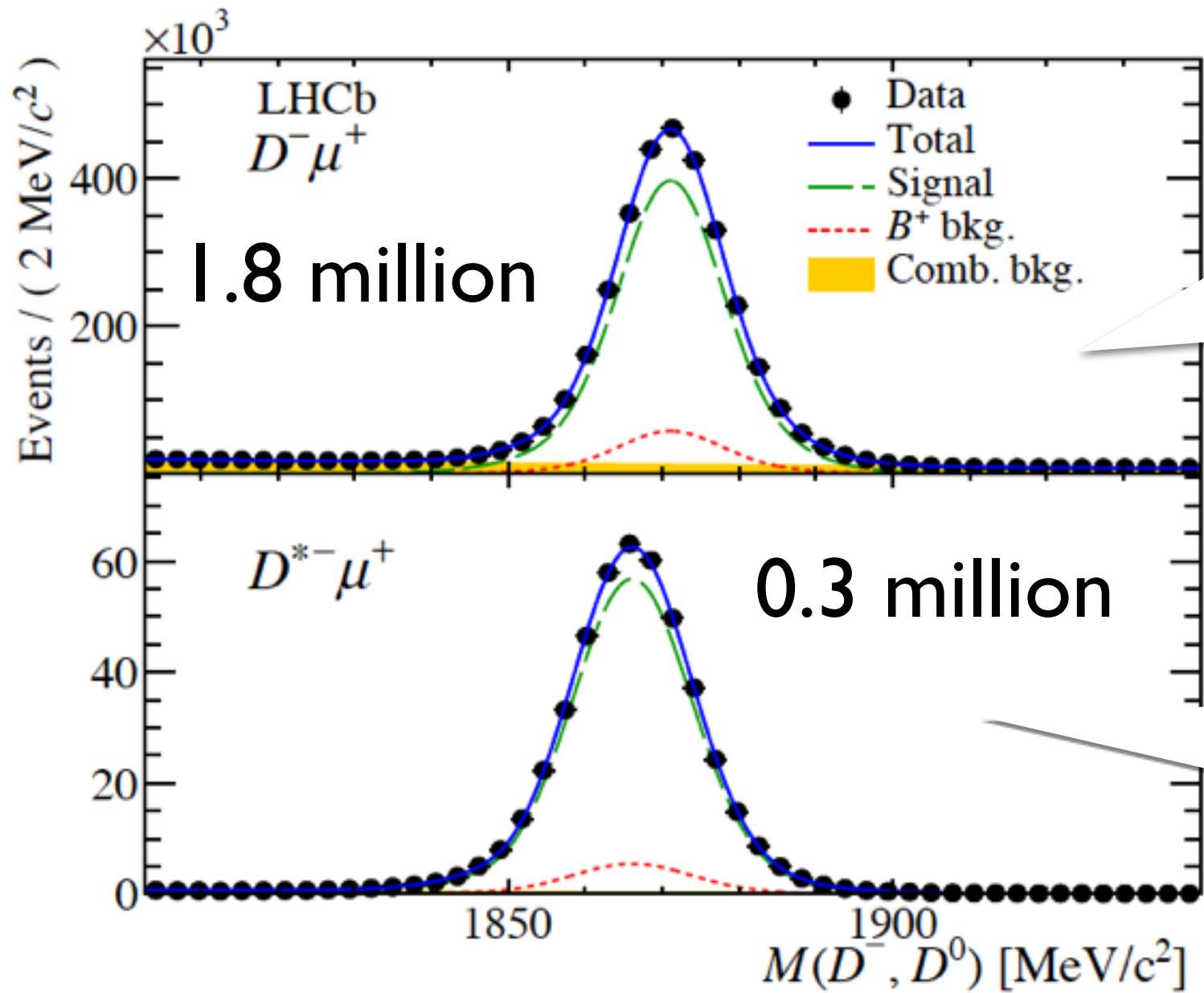
LHCb measurement of a_{sl}

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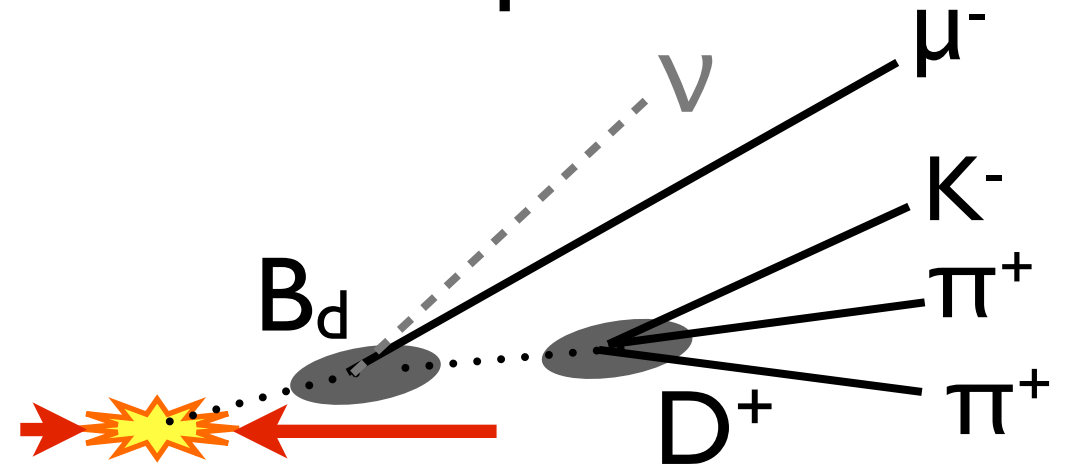
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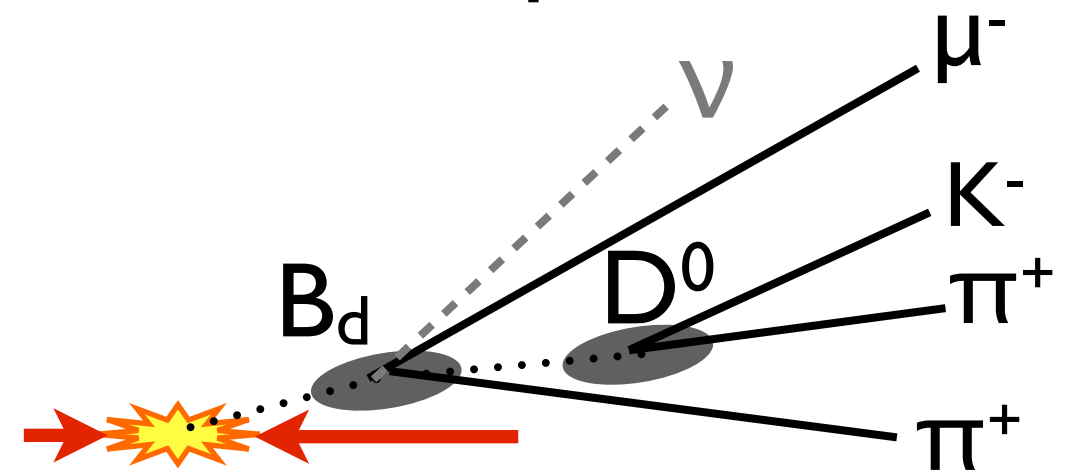
Our signals



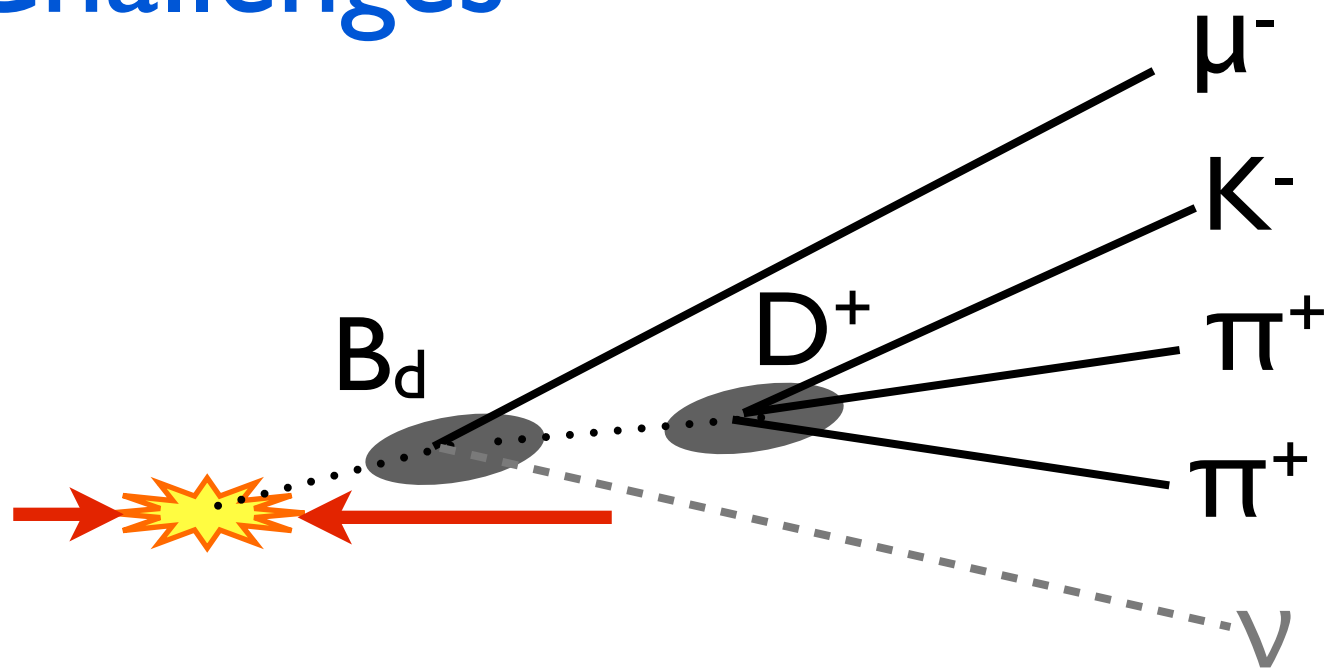
1. $B_d \rightarrow D^+ \mu \nu X$



2. $B_d \rightarrow D^{*+} \mu \nu X$



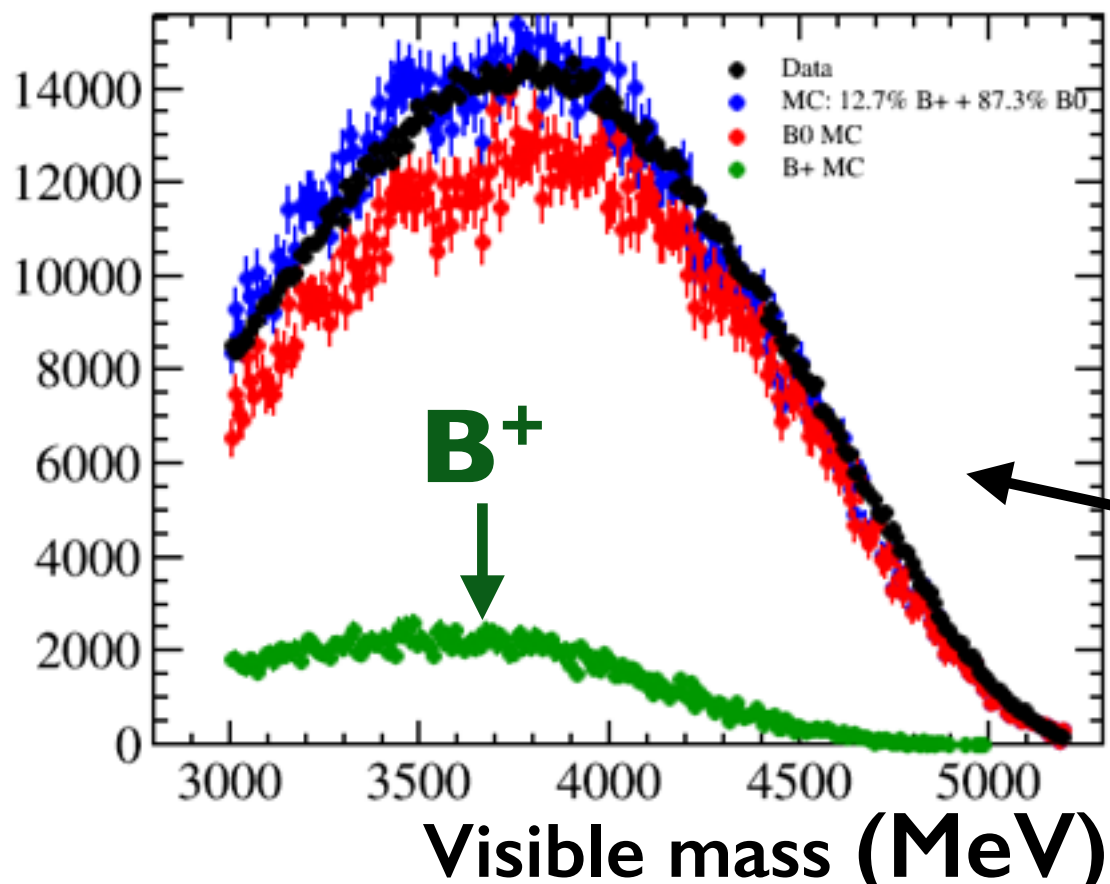
Challenges



1. The detection asymmetry for the $\mu^\pm \pi^\mp K^\pm \pi^\mp$ final state

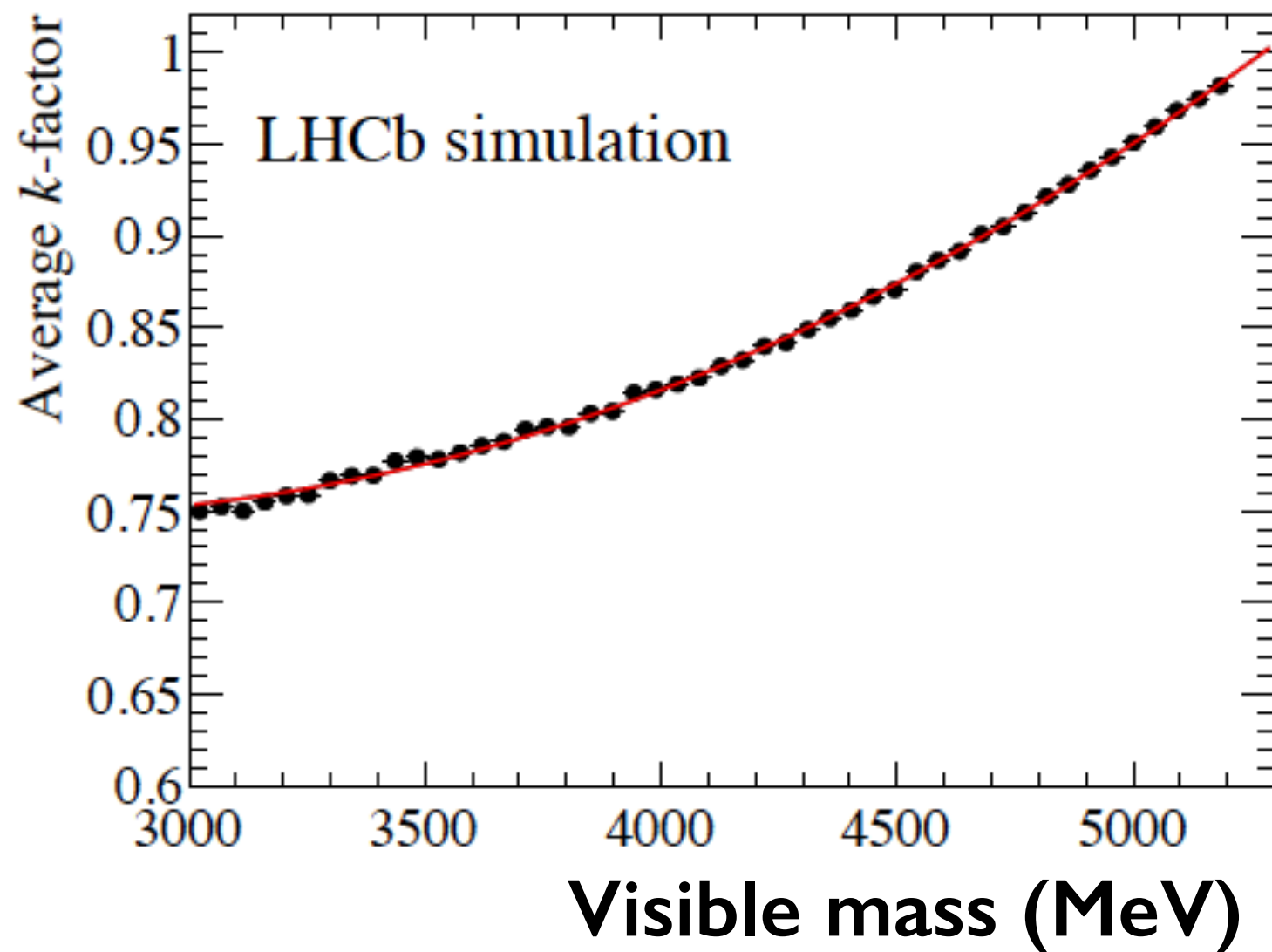
2. Don't know the B momentum

$$t = L \cdot \frac{M}{|p|}$$



3. No mass peak. Backgrounds!

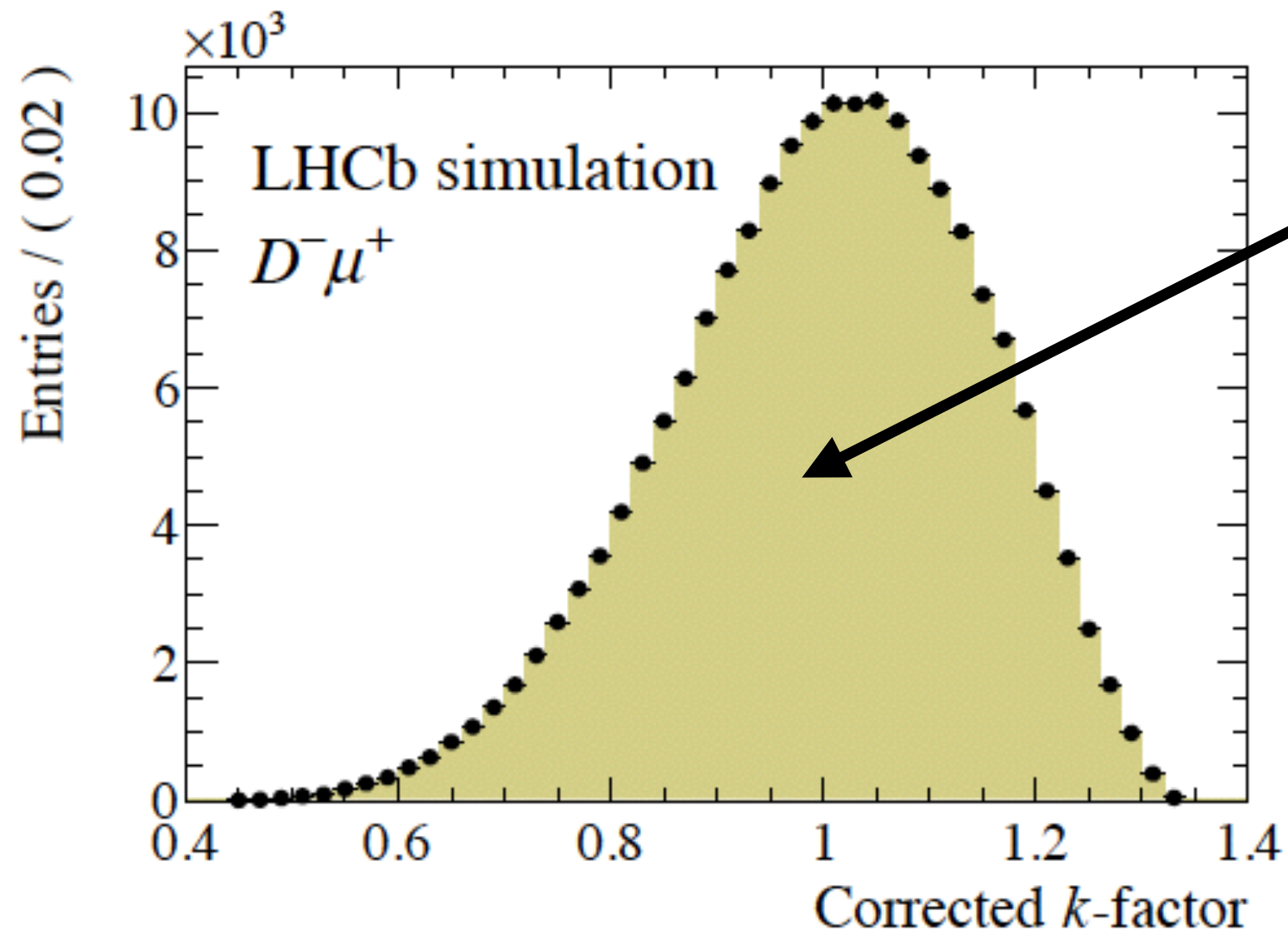
The K-factor method



Use to correct the decay time

$$t = \frac{L \cdot M_{\text{PDG}}}{|p_{\text{vis}}|} \cdot K(M_{\text{vis}})$$

The K-factor method



Resolution to be used in time dependent fit

- Simulate a “cocktail” of sub-decays.
- Systematic uncertainty on a_{sl} is 5×10^{-4} .

Backgrounds

- The $D^{+(*)}\mu\nu X$ final state is also fed by B^+ decays
- Also smaller backgrounds from Λ_b and B_s
- B^+ fractions estimated from simulation:

$$D^+\mu\nu X: (12.7 \pm 2.2)\%$$

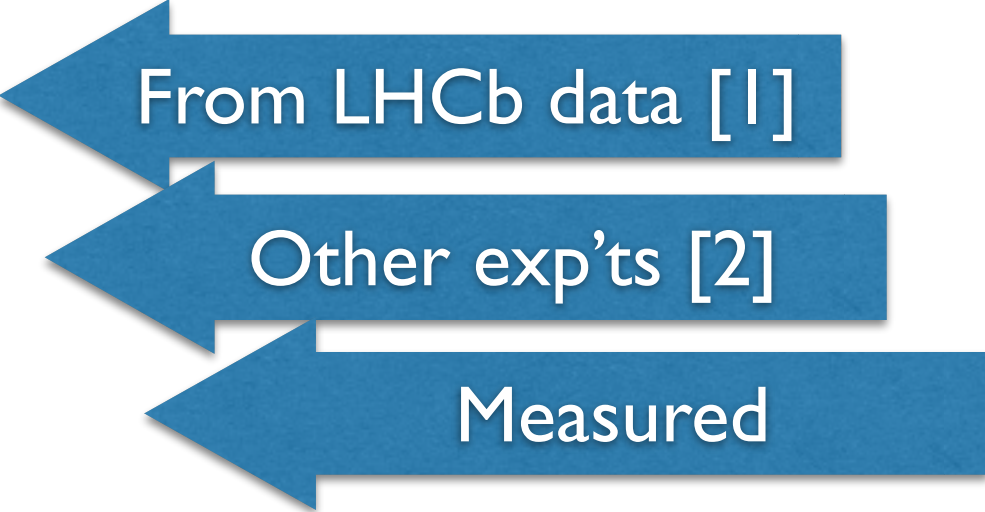
$$D^{*+}\mu\nu X: (8.8 \pm 2.2)\%$$

- Also need the B^+ production asymmetry...

$$a_P(B^+) = \frac{\sigma(\bar{B}^+) - \sigma(B^-)}{\sigma(\bar{B}^+) + \sigma(B^-)}$$

Backgrounds

- Determine the B^+ production asymmetry with

$$A_P(B^+) = A_{\text{raw}}(B^+ \rightarrow J/\psi K^+) - A_{\text{CP}}(B^+ \rightarrow J/\psi K^+) - A_{\text{det}}(K^+)$$


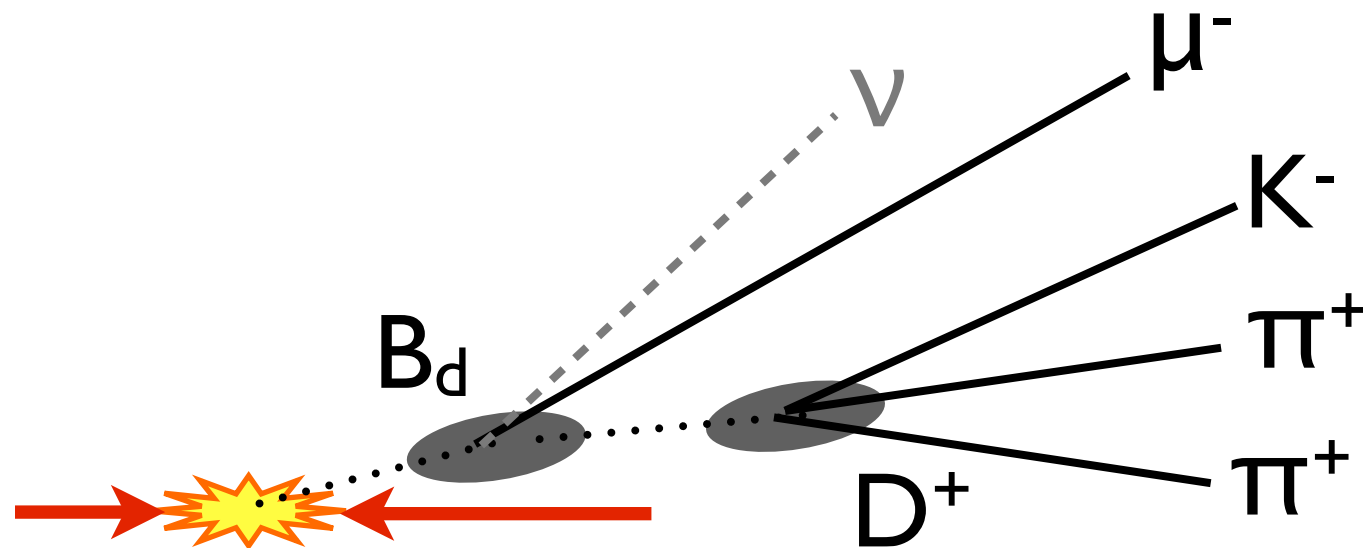
$$A_P(B^+) = (-0.6 \pm 0.6)\%$$

2nd largest systematic on a_{sl}^d

[1] <http://arxiv.org/abs/1408.0978>

[2] K.A. Olive et al. (Particle Data Group), Chin. Phys. C, 38, 090001 (2014).

The detection asymmetry



$$A_D = \frac{\varepsilon(f) - \varepsilon(\bar{f})}{\varepsilon(f) + \varepsilon(\bar{f})}$$

$$f = \mu^+ K^+ \pi^- \pi^-$$

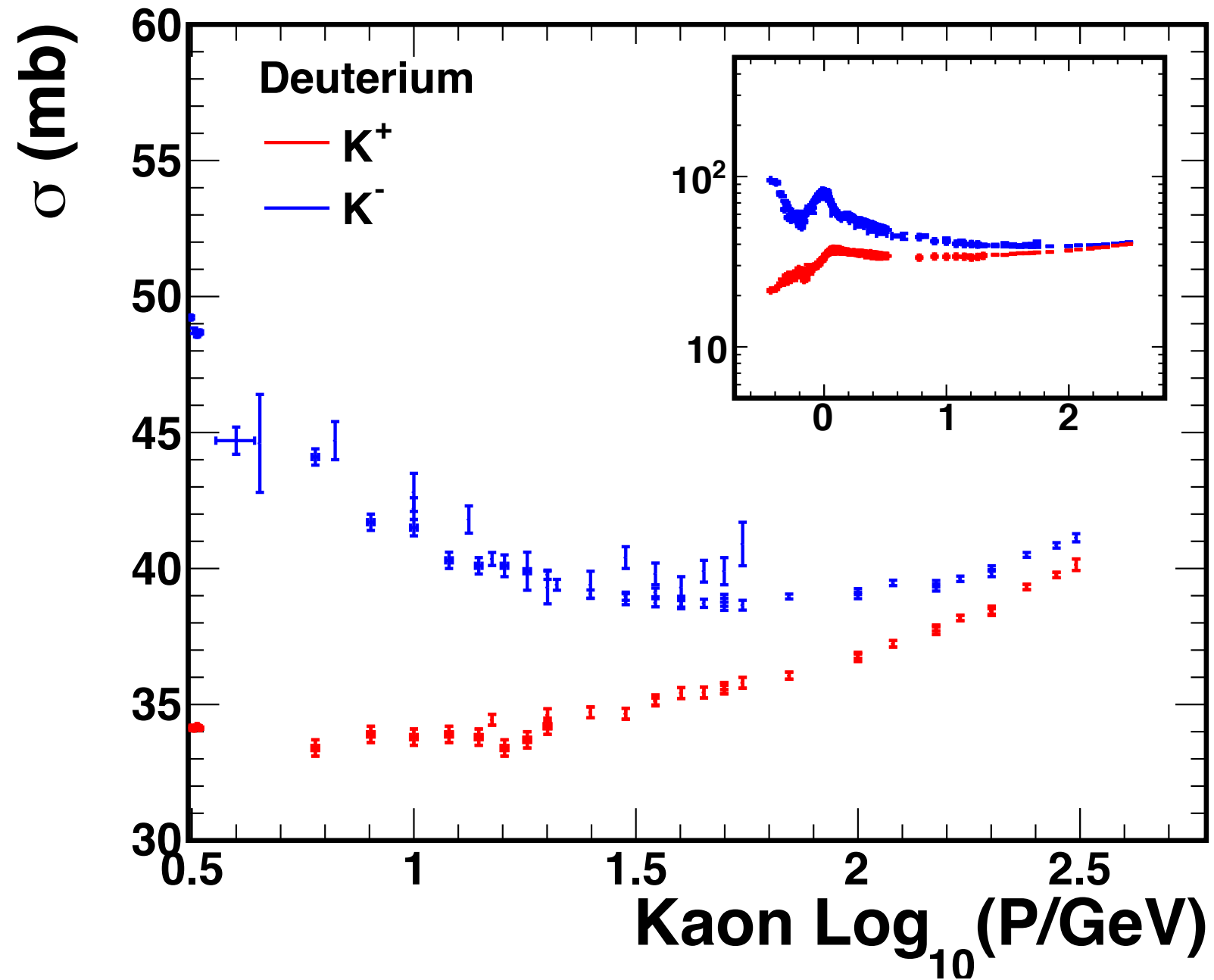


$$A_D(\mu^+ \pi^-), A_D(K^+ \pi^-)$$

- Sources of asymmetry:
 - Detector mis-alignments, and inhomogeneities
 - nuclear interactions...

The kaon asymmetry

K.A. Olive et al. (Particle Data Group),
Chin. Phys. C, 38, 090001 (2014).



Kaon detection asymmetry of $\sim 10^{-2}$

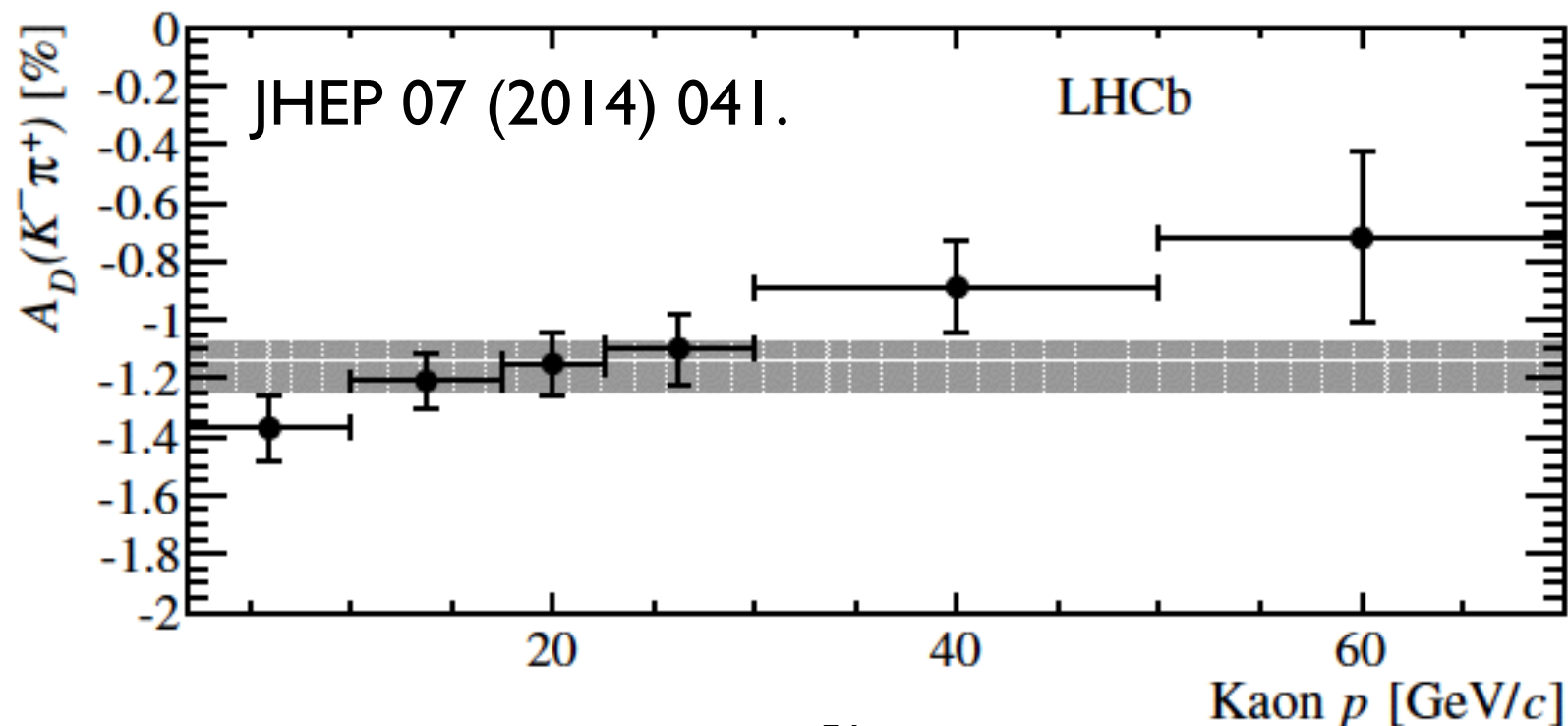
Measuring the $K\pi$ asymmetry

- Exploit the LHCb's huge charm signals

$$A_{K\pi} \equiv \frac{\epsilon(K^+\pi^-) - \epsilon(K^-\pi^+)}{\epsilon(K^+\pi^-) + \epsilon(K^-\pi^+)}$$

$$= A(D \rightarrow K\pi\pi) - A(D \rightarrow K_S\pi) - A(K_S)$$

Need two decay modes of the same D species to cancel the production asymmetry



Measuring the $K\pi$ asymmetry

- Exploit the LHCb's huge charm signals

$$\begin{aligned} A_{K\pi} &\equiv \frac{\epsilon(K^+\pi^-) - \epsilon(K^-\pi^+)}{\epsilon(K^+\pi^-) + \epsilon(K^-\pi^+)} \\ &= A(D \rightarrow K\pi\pi) \\ &\quad - A(D \rightarrow K_S\pi) \\ &\quad - A(K_S) \end{aligned}$$

Need two decay modes of the same D species to cancel the production asymmetry

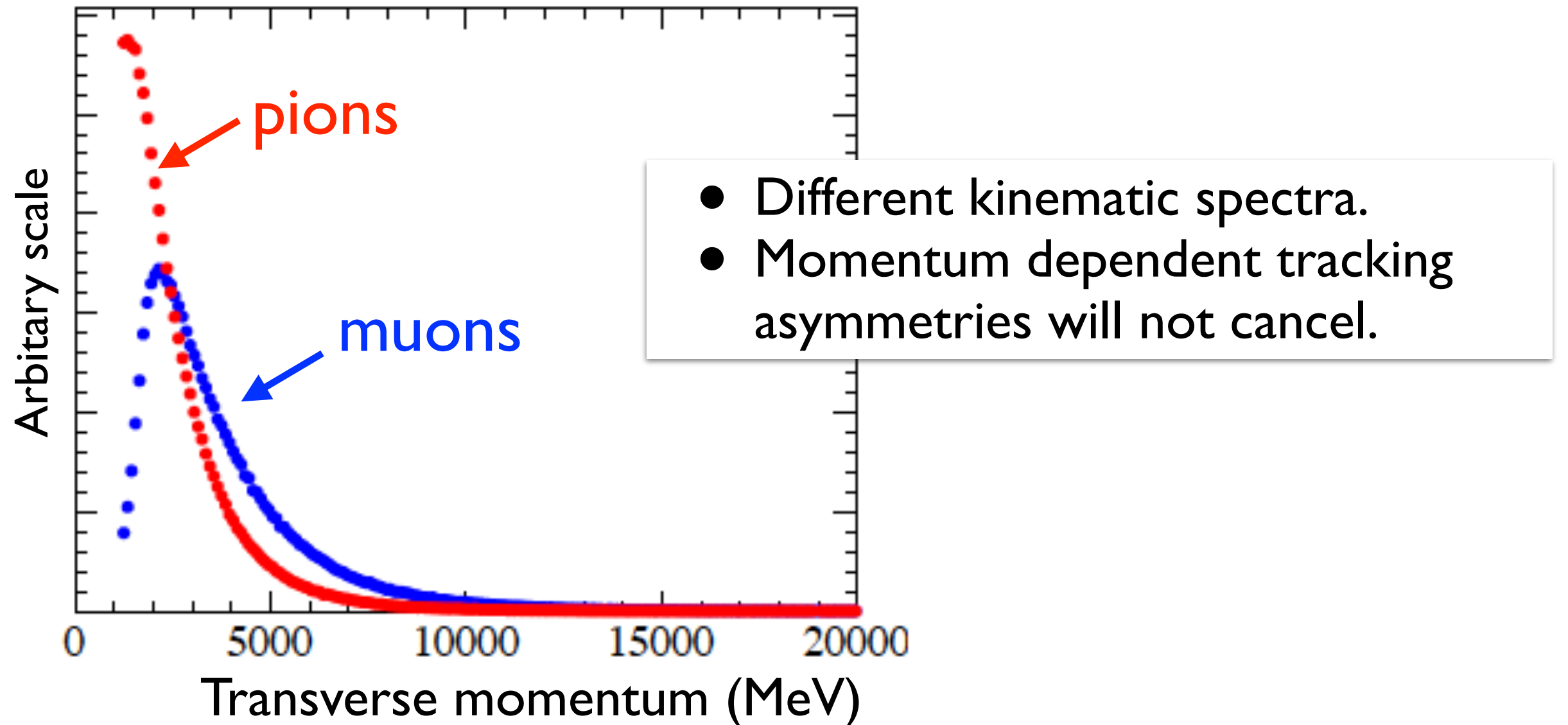
- After a weighting of the charm modes:

e.g., for $D^+\mu\nu$ mode:

$$A_{K\pi} = (1.15 \pm 0.08_{\text{stat}} \pm 0.07_{\text{syst}})\%$$

largest systematic uncertainty on a_{sl}^d

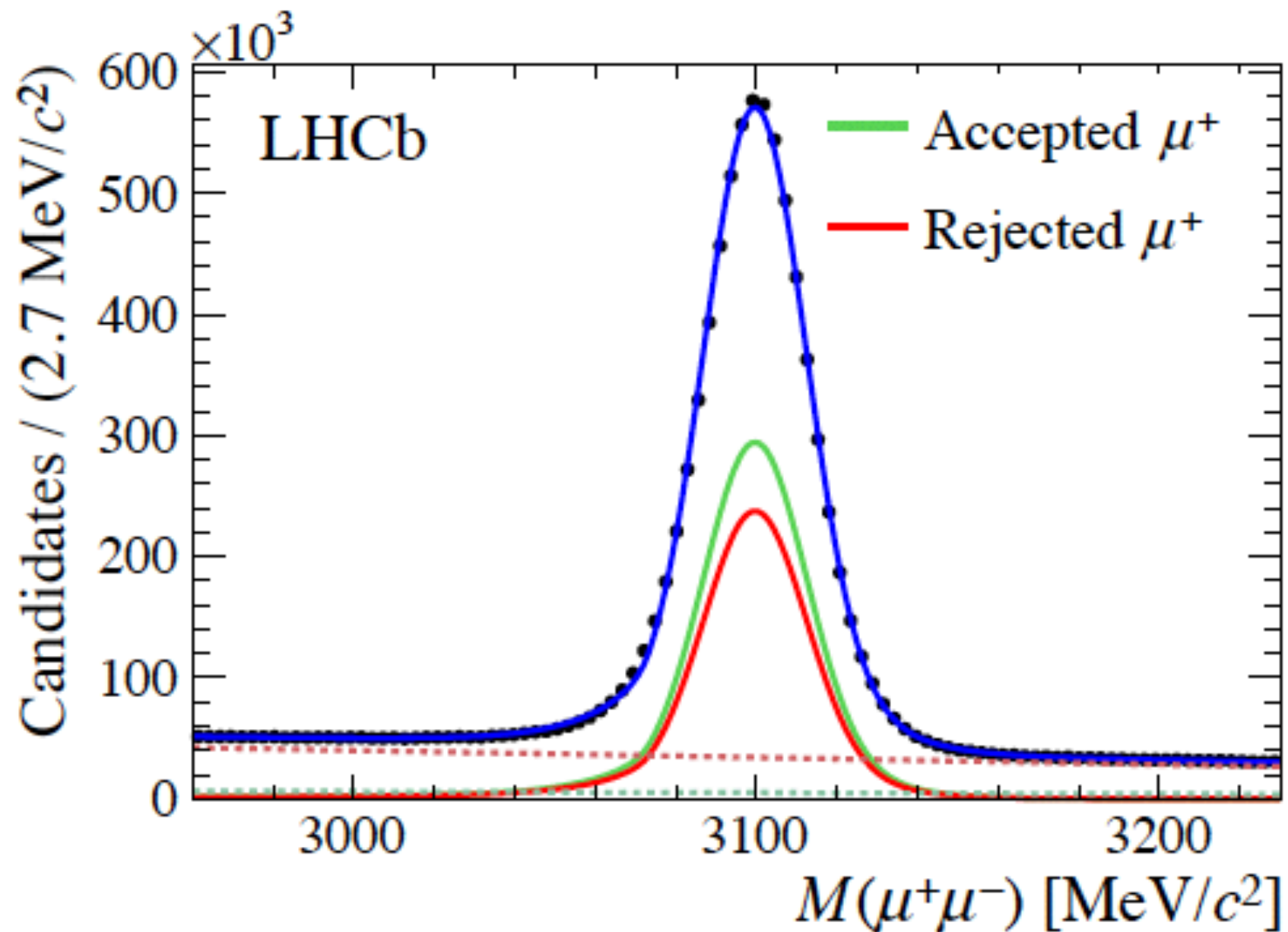
Measuring the $\mu\pi$ asymmetry



- Momentum dependent weighting to equalise their spectra.
- Effective sample size reduced by factor of ≈ 0.8

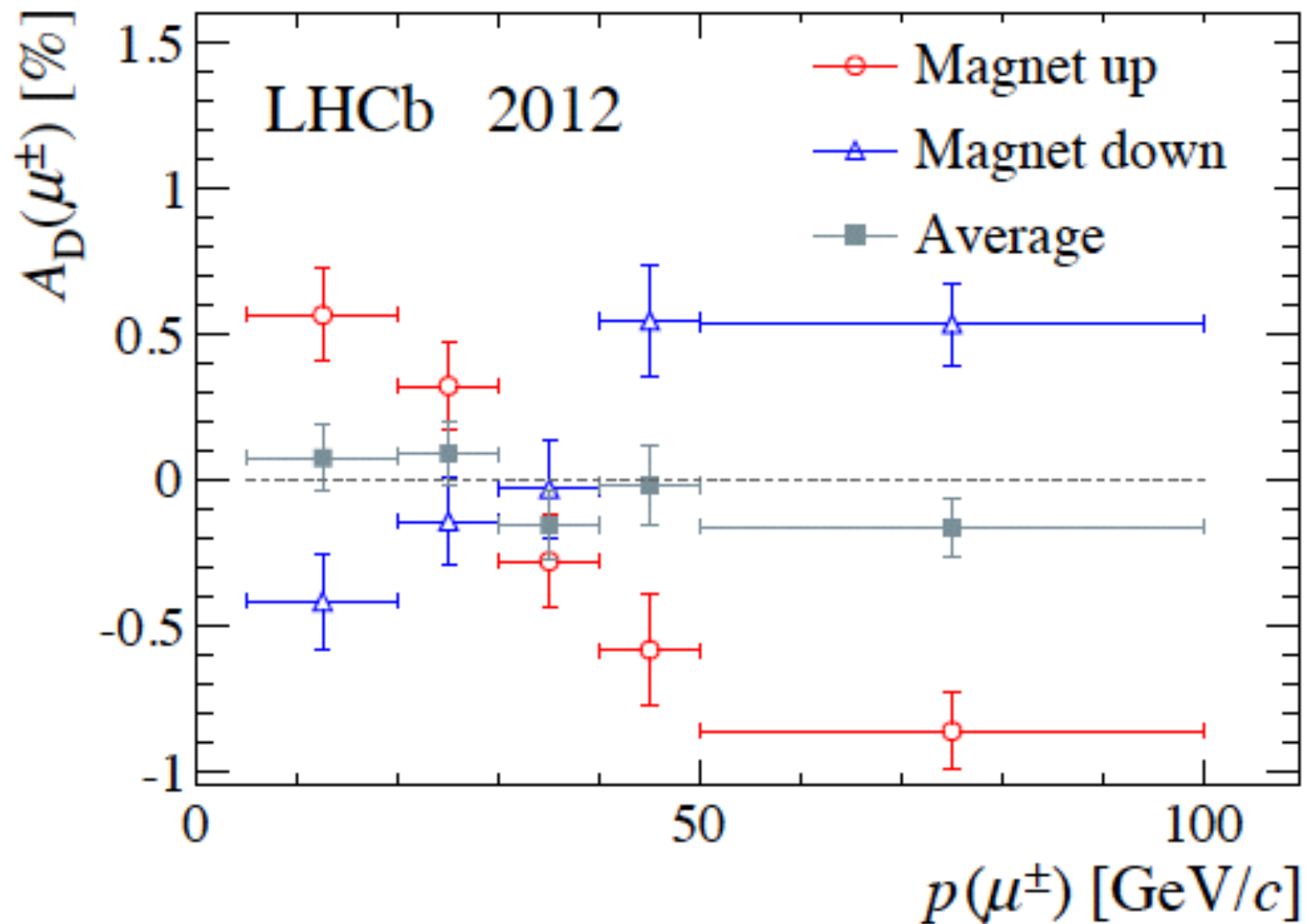
Measuring the $\mu\pi$ asymmetry

- Combine muon identification and trigger asymmetry measured with $J/\Psi \rightarrow \mu^+\mu^-$ decays.



Measuring the $\mu\pi$ asymmetry

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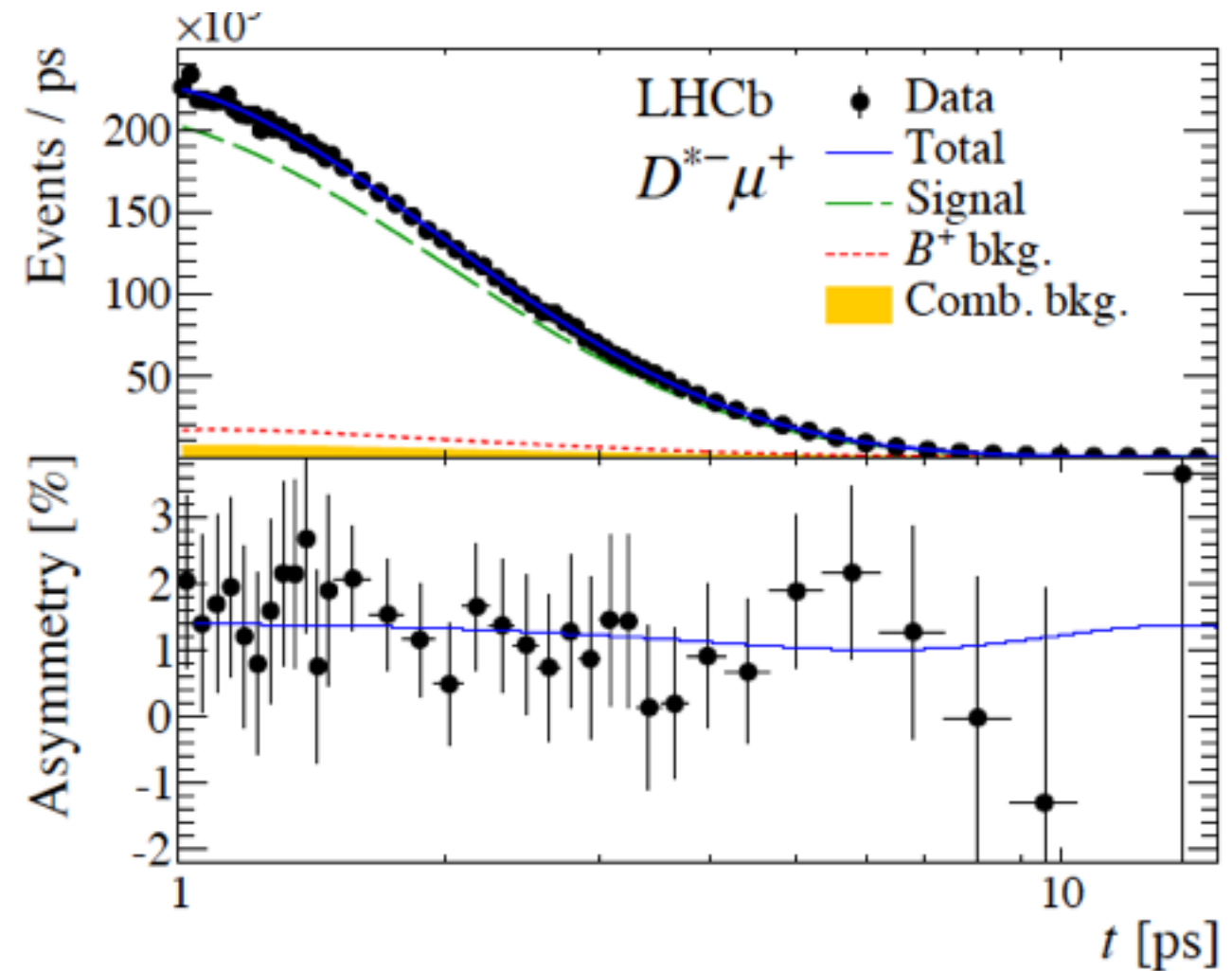
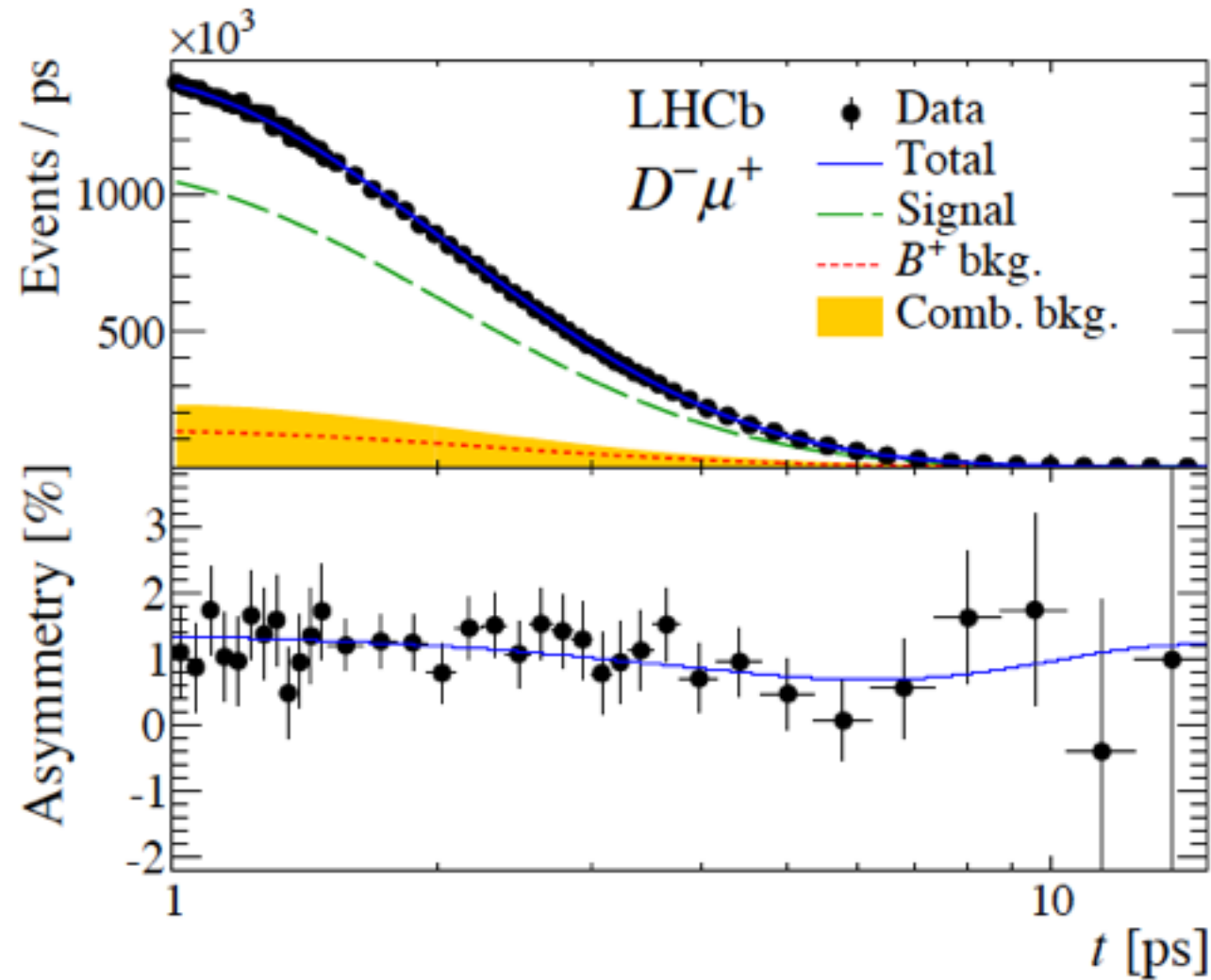


$\pm 0.5\%$ polarity dependent asymmetries caused by chamber mis-alignment and inefficiencies.

Only for illustrative purposes. Actually extract a single, kinematic weighted muon asymmetry.

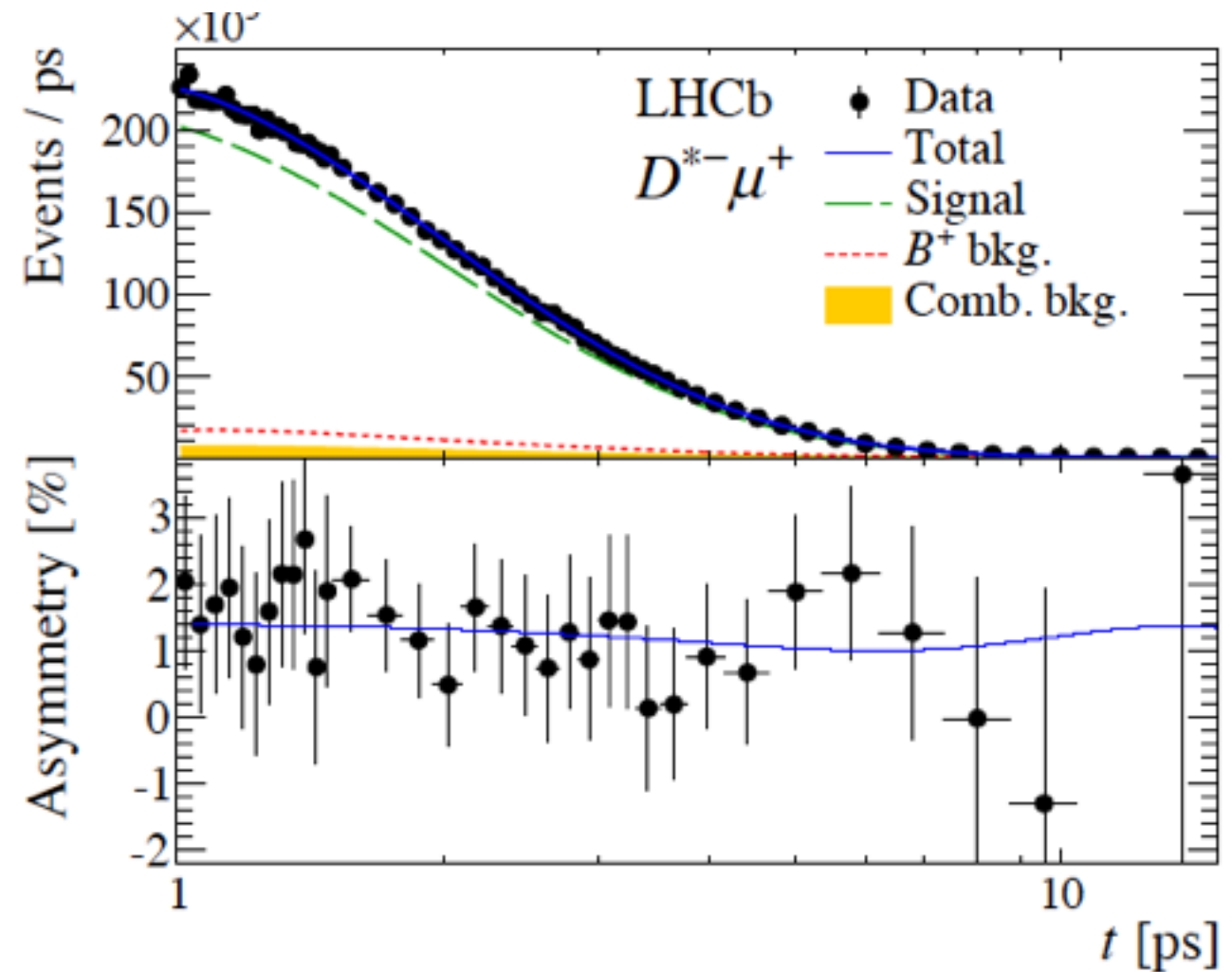
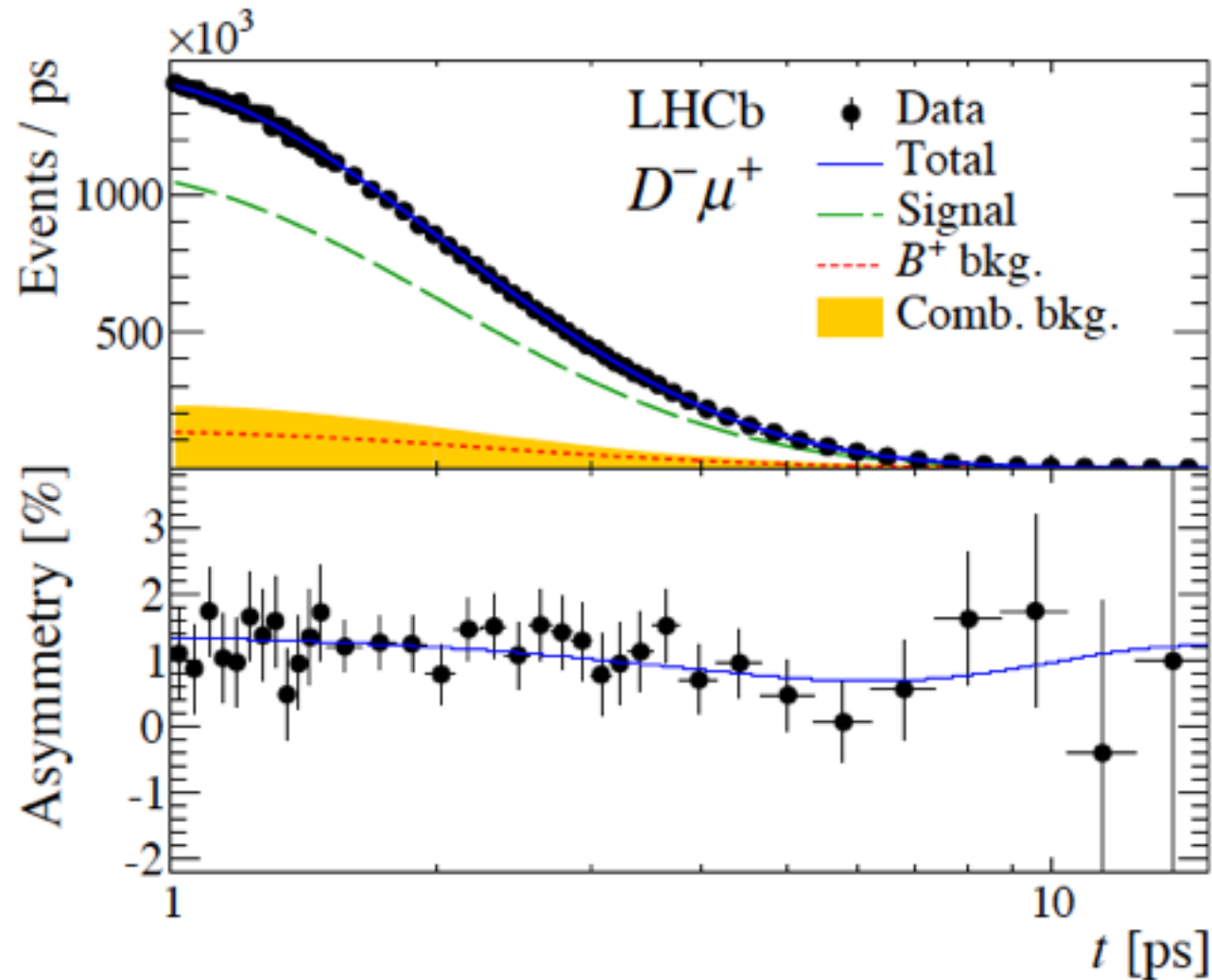
Fit results

$$N(f, t) \propto e^{-\Gamma_d t} \left[1 \pm A_D \pm \frac{a_{sl}^d}{2} \mp \left(A_p + \frac{a_{sl}^d}{2} \right) \cos \Delta m_d t \right]$$



Fit results

$$N(f, t) \propto e^{-\Gamma_d t} \left[1 \pm A_D \pm \frac{a_{sl}^d}{2} \mp \left(A_p + \frac{a_{sl}^d}{2} \right) \cos \Delta m_d t \right]$$



Also measure the B_d production asymmetry

$$a_p(B_d, 7 \text{ TeV}) = (-0.66 \pm 0.26 \pm 0.22)\%$$

$$a_p(B_d, 8 \text{ TeV}) = (-0.48 \pm 0.15 \pm 0.17)\%$$

Systematic uncertainties on a_{sl}

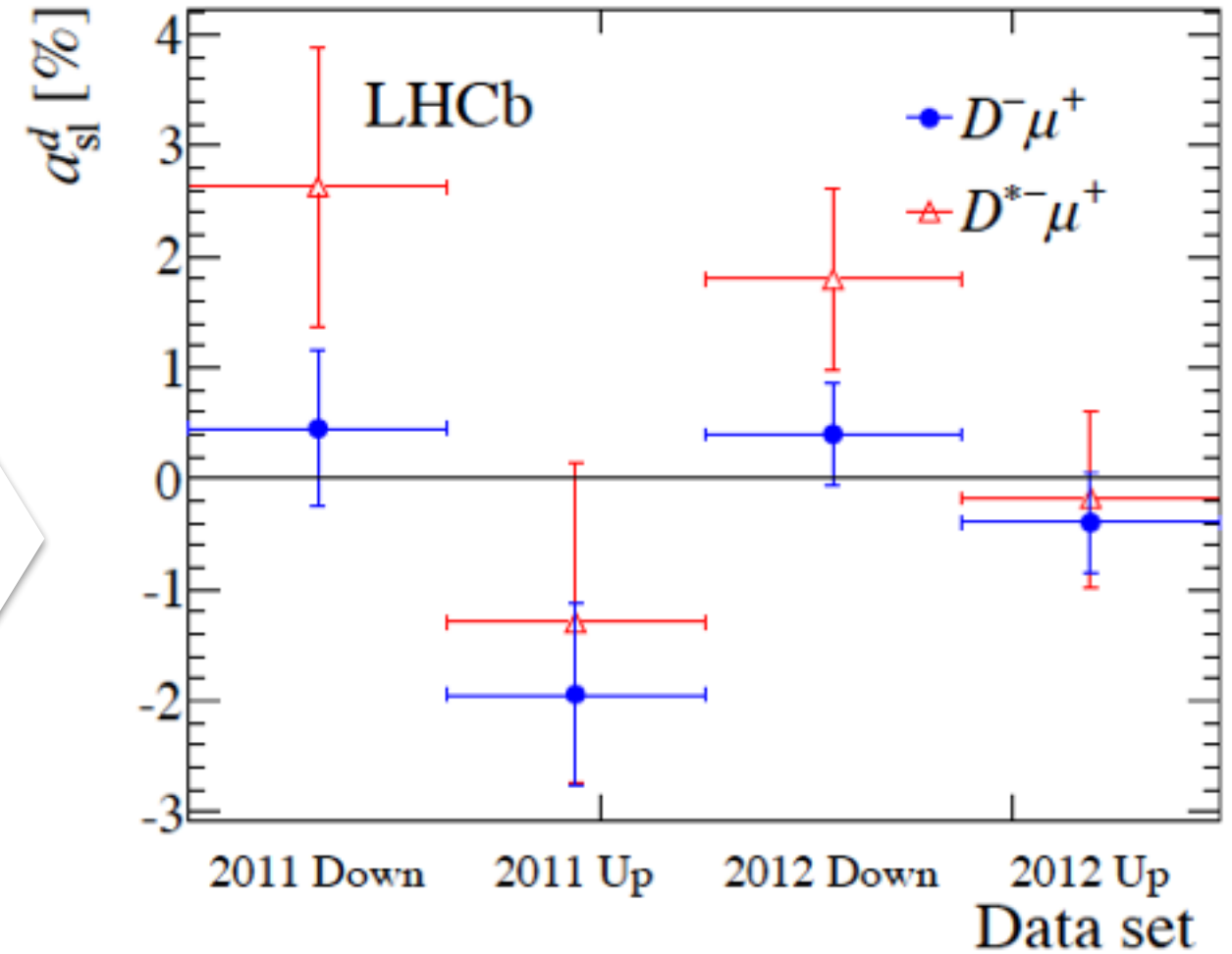
Source	δ (%)
Detection asymmetry	0.26
B plus	0.13
Baryonic background	0.07
Bs background	0.03
Fake D background	0.03
K-factor model	0.03
Decay time acceptance	0.03
Mixing frequency	0.02
Quadratic sum	0.30

Many of these are limited by control mode statistics

Results and checks

- Don't rely on the polarity reversal to cancel

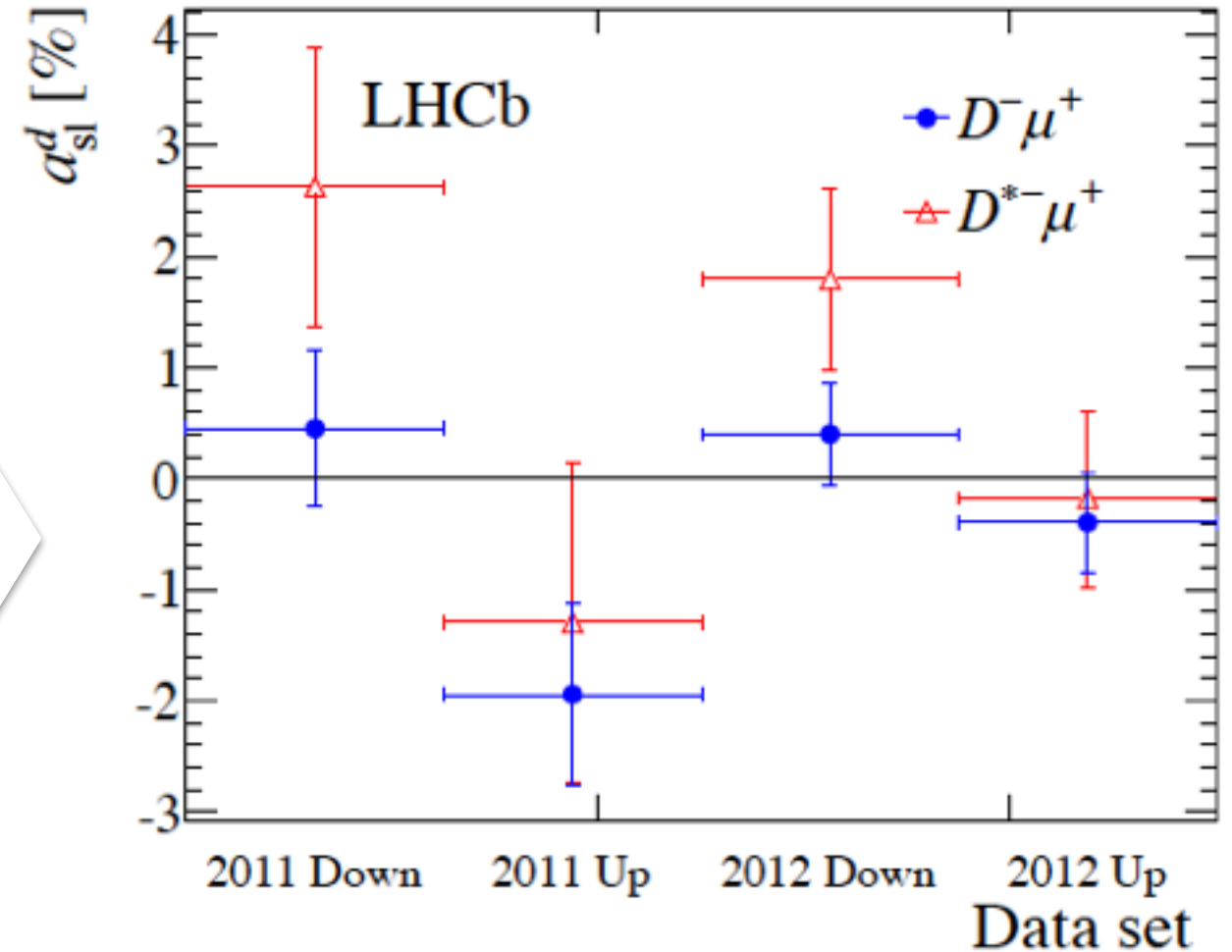
Can make independent with up/down and 2011/2012.



Results and checks

- Don't rely on the polarity reversal to cancel

Can make independent with up/down and 2011/2012.



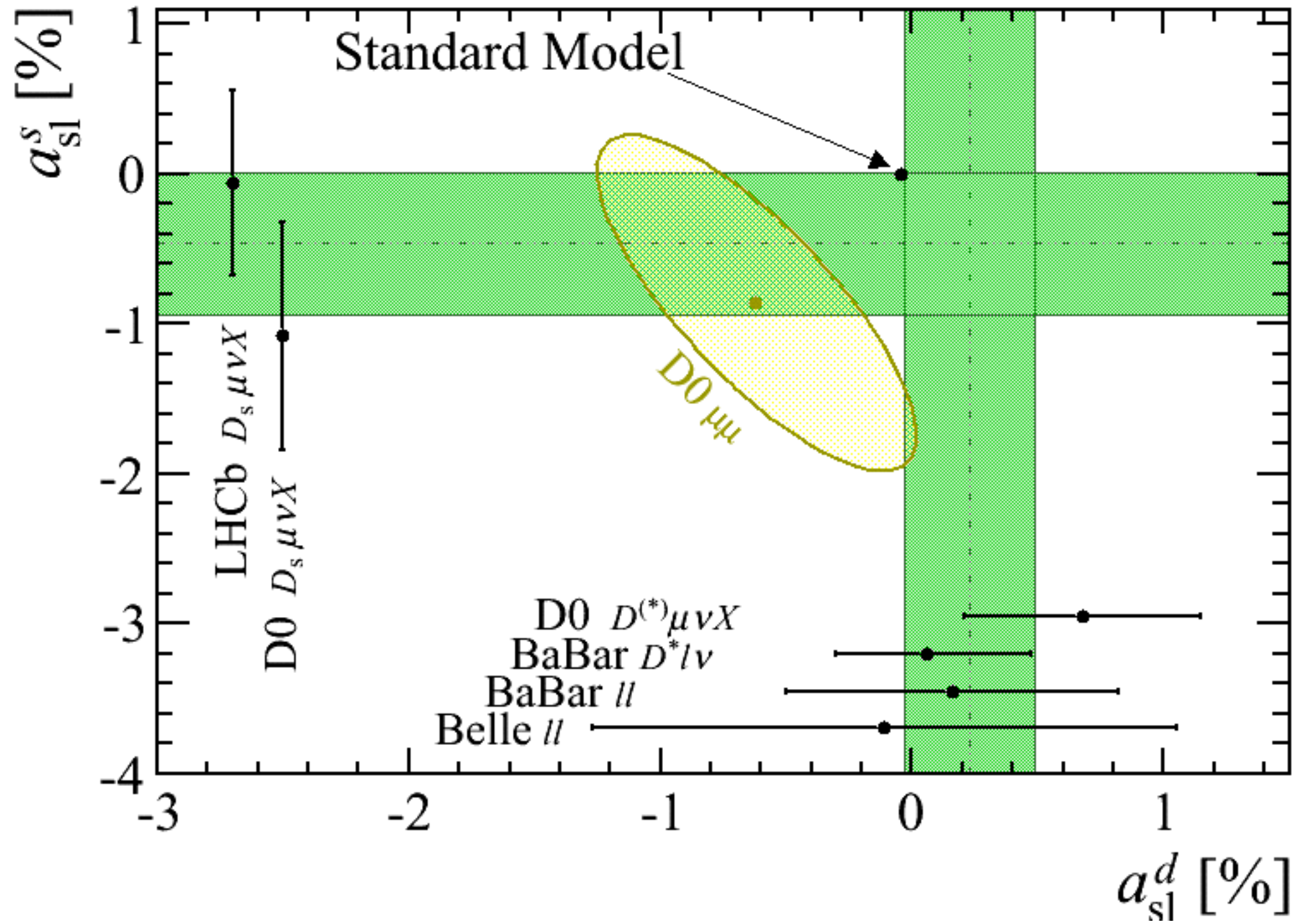
Final average:

1. Linear average of polarities: $[u+d]/2$
2. Weighted average of 2011 and 2012
3. Weighted average of D^+ and D^{*+}

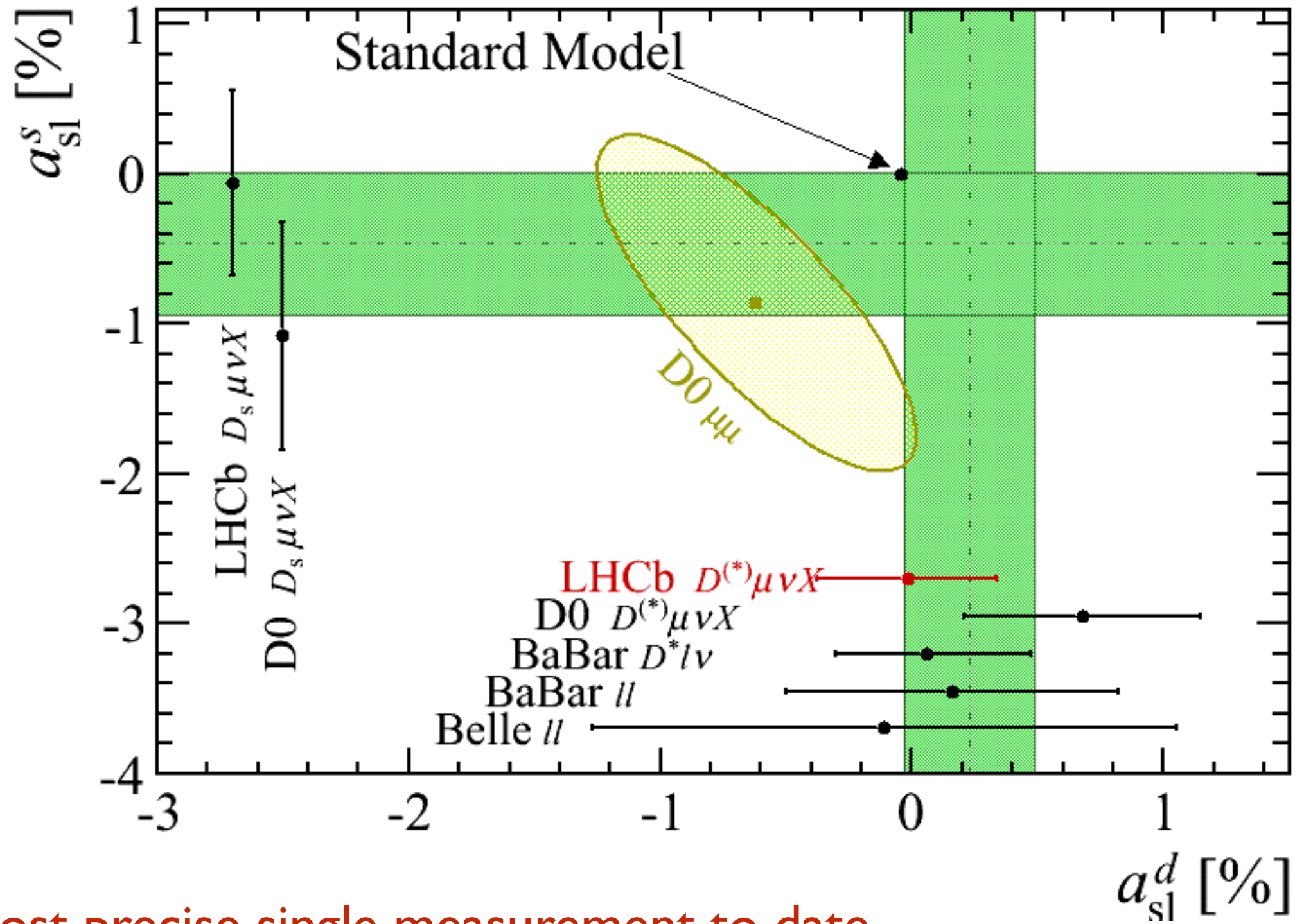
(taking into account correlations in the systematic uncertainties)

Result: $a_{sl}^d = (-0.02 \pm 0.19_{\text{stat}} \pm 0.30)\%$

Before

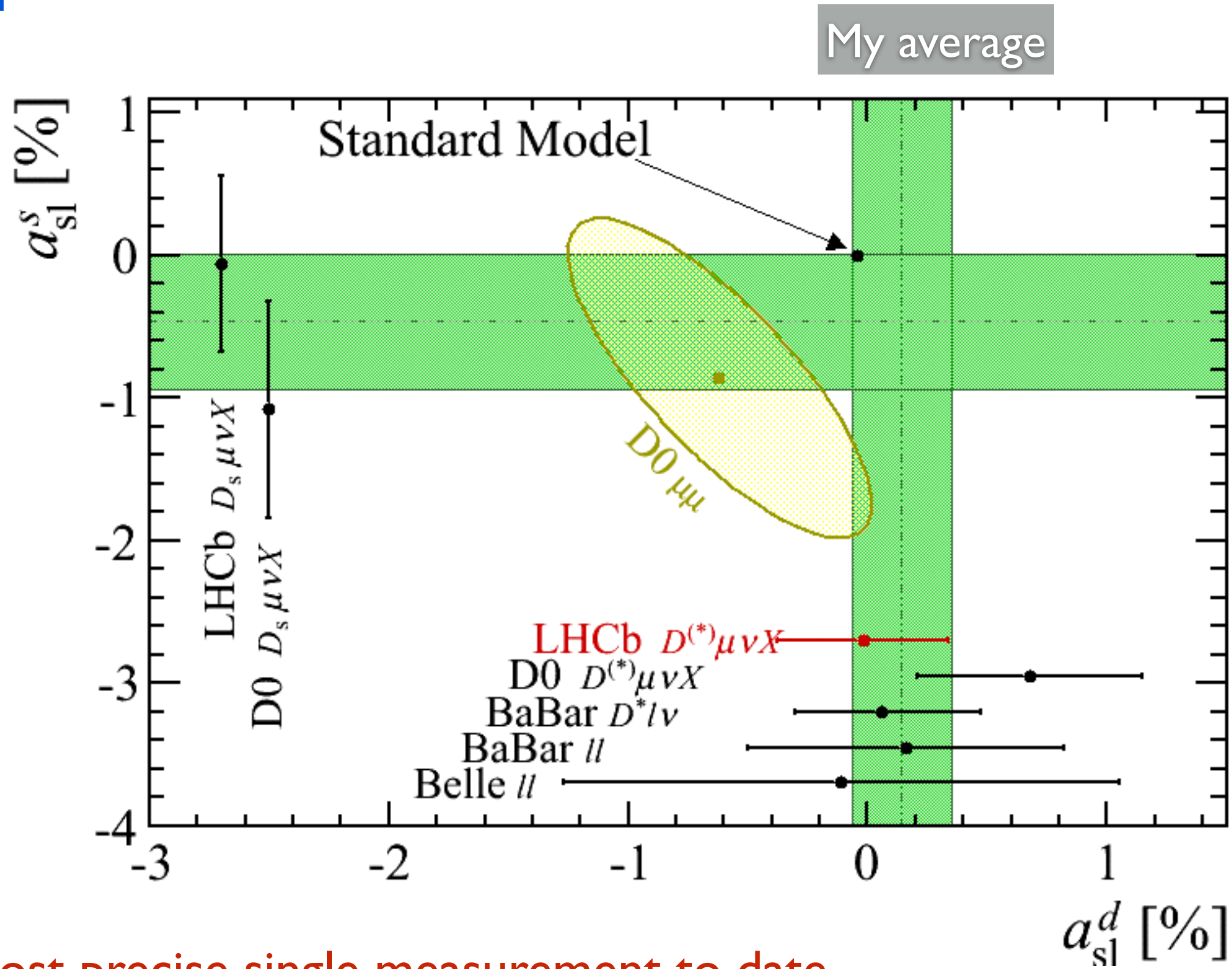


After



- Most precise single measurement to date.
- Do not see an anomalous asymmetry.

After



- Most precise single measurement to date.
- Do not see an anomalous asymmetry.

Conclusions

- First LHCb measurements of CP-violation in B_s and B_d mixing.

$$a_{sl}^d = (-0.02 \pm 0.19_{\text{stat}} \pm 0.30_{\text{syst}})\% \quad \text{PLB 728C 607-615 (2014)}$$

$$a_{sl}^s = (-0.06 \pm 0.50_{\text{stat}} \pm 0.36_{\text{syst}})\% \quad \text{LHCb-PAPER-2014-053}$$

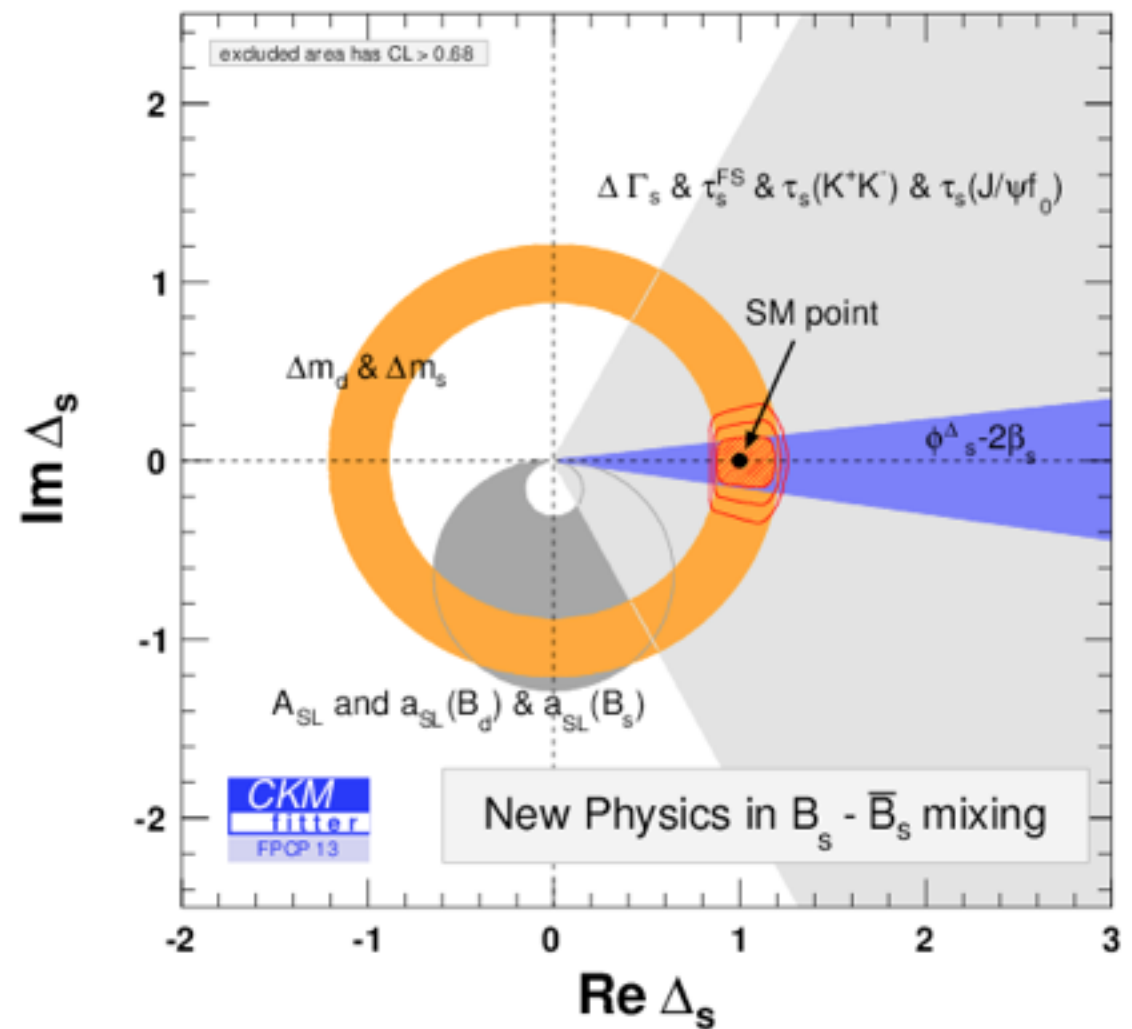
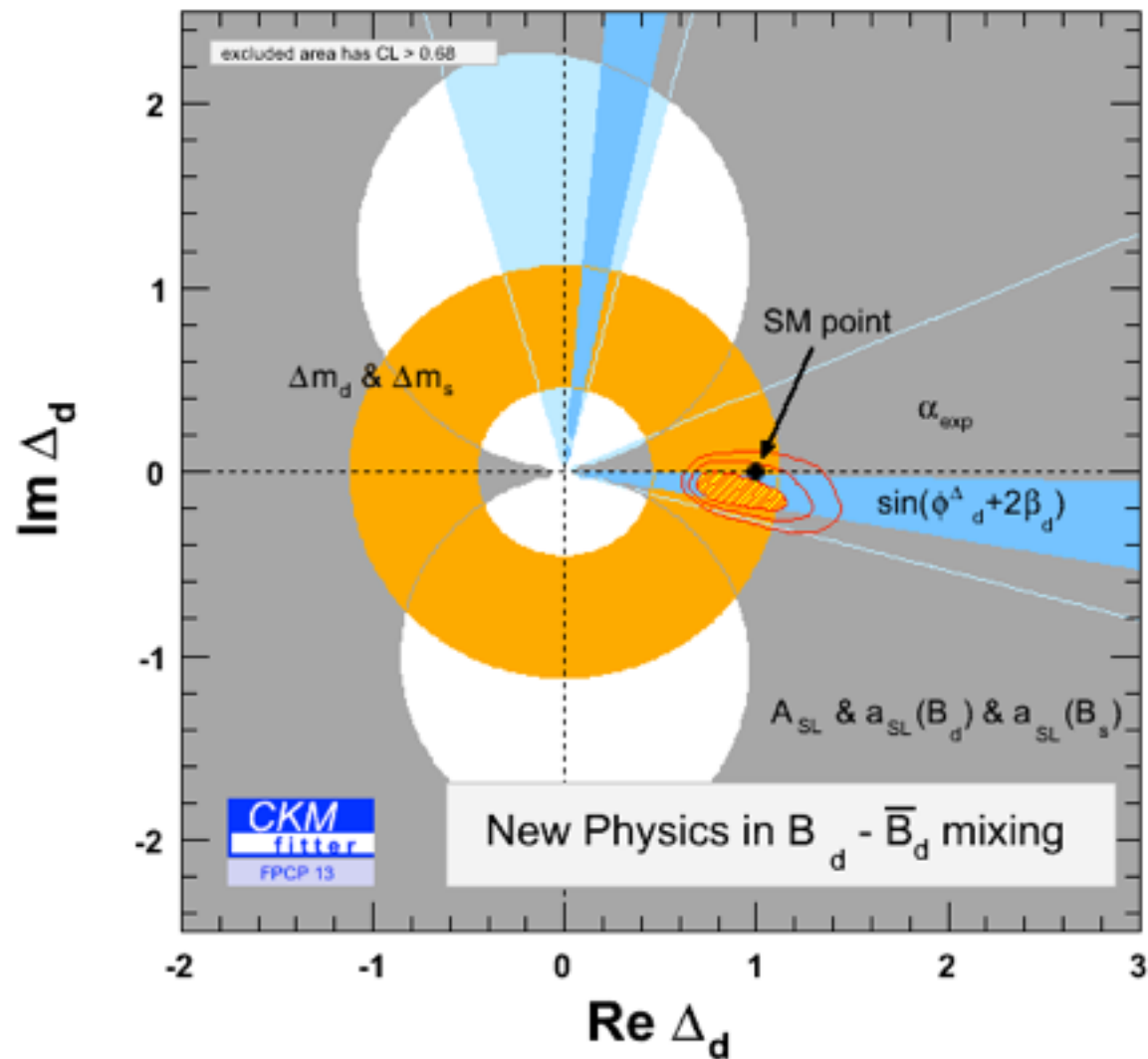
- 3 fb^{-1} update of a_{sl}^s is coming soon.
- Both are still statistically limited so exciting prospects for Run-II.

Backup slides

Model independent NP analysis

$$i \frac{\partial}{\partial t} \begin{pmatrix} |P^0(t)\rangle \\ |\bar{P}^0(t)\rangle \end{pmatrix} = \left[\begin{pmatrix} M_{11} & M_{12} \\ M_{12}^* & M_{22} \end{pmatrix} - \frac{i}{2} \begin{pmatrix} \Gamma_{11} & \Gamma_{12} \\ \Gamma_{12}^* & \Gamma_{22} \end{pmatrix} \right] \begin{pmatrix} |P^0(t)\rangle \\ |\bar{P}^0(t)\rangle \end{pmatrix}$$

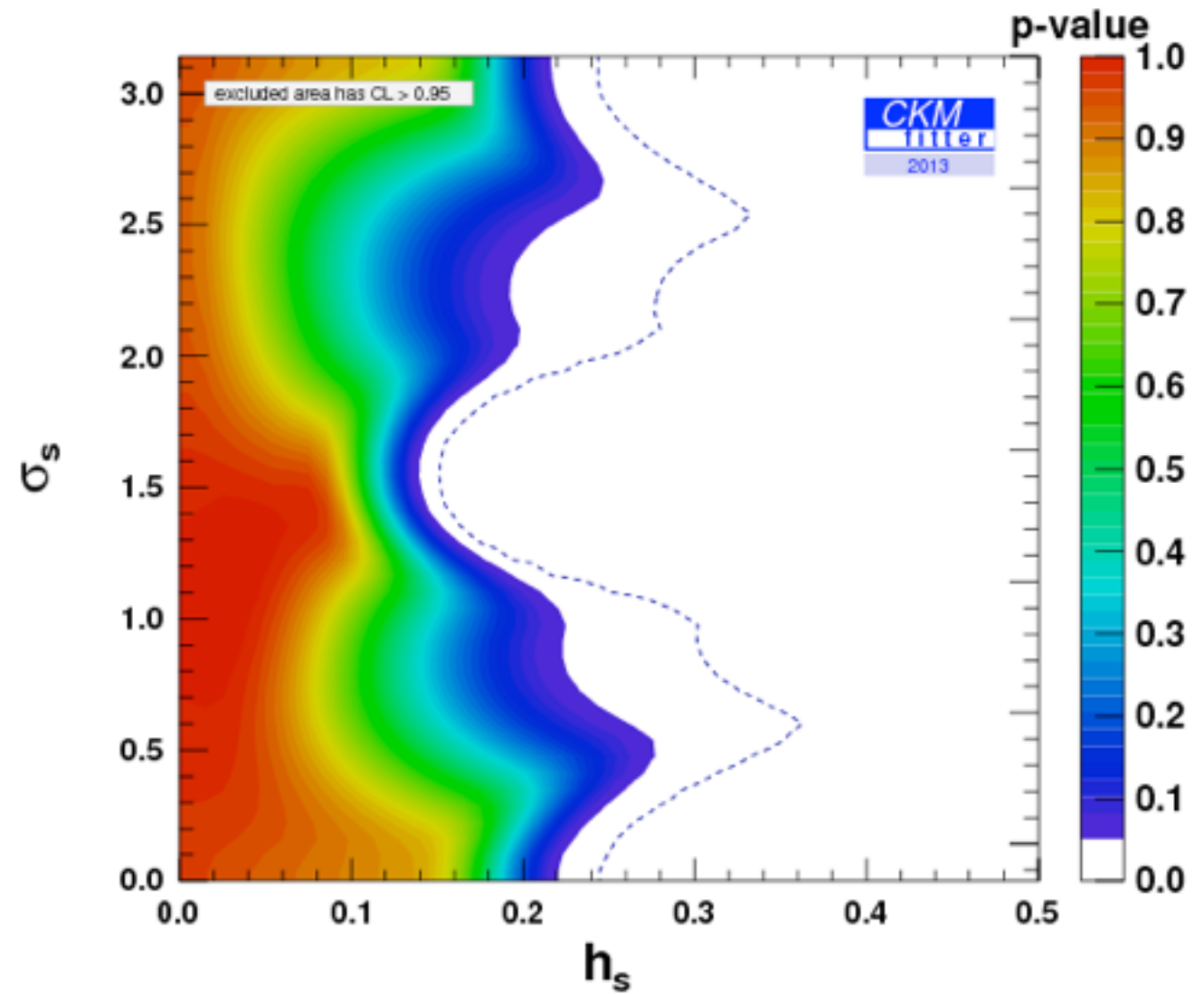
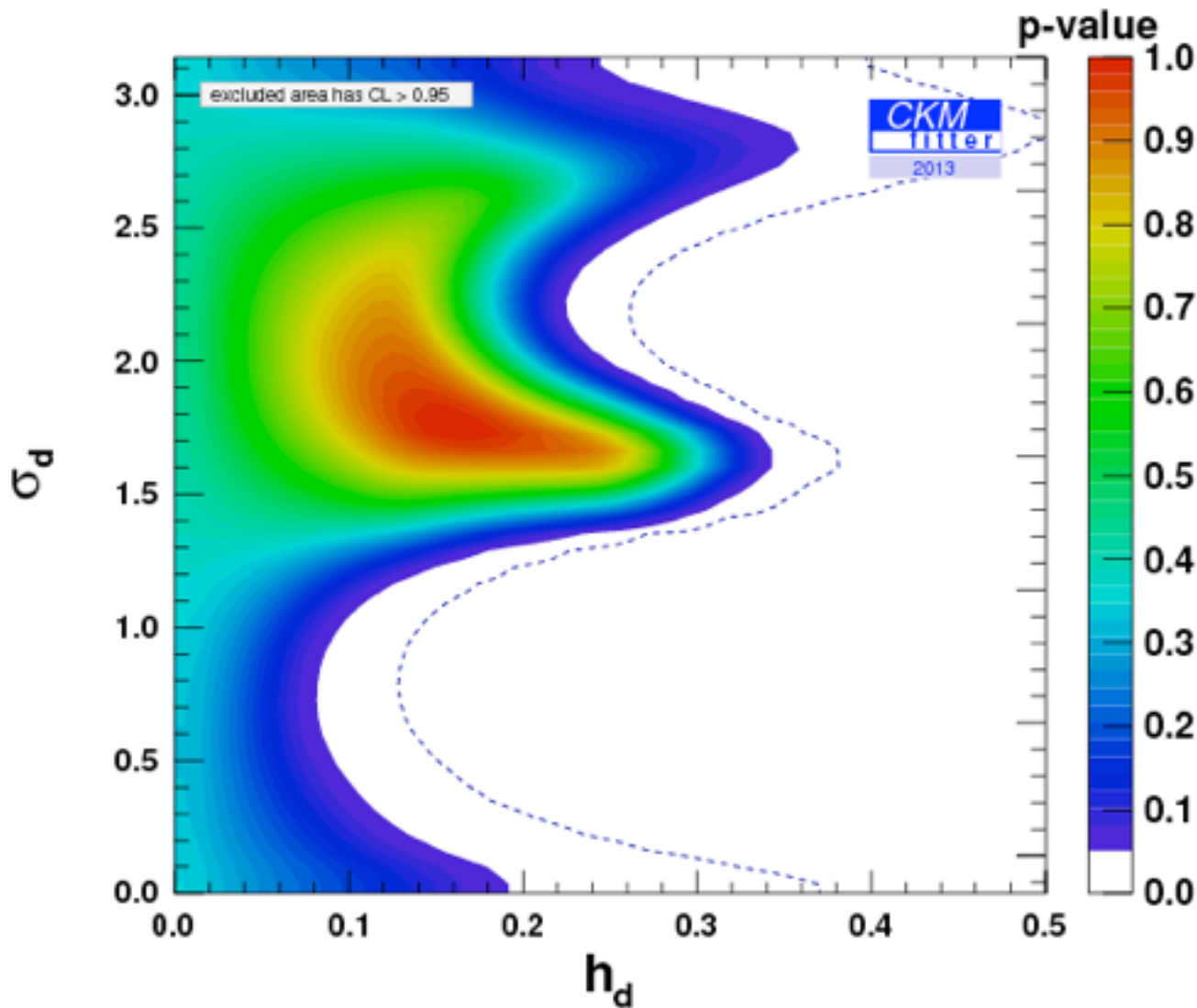
$$M_{12} \rightarrow M_{12}\Delta$$



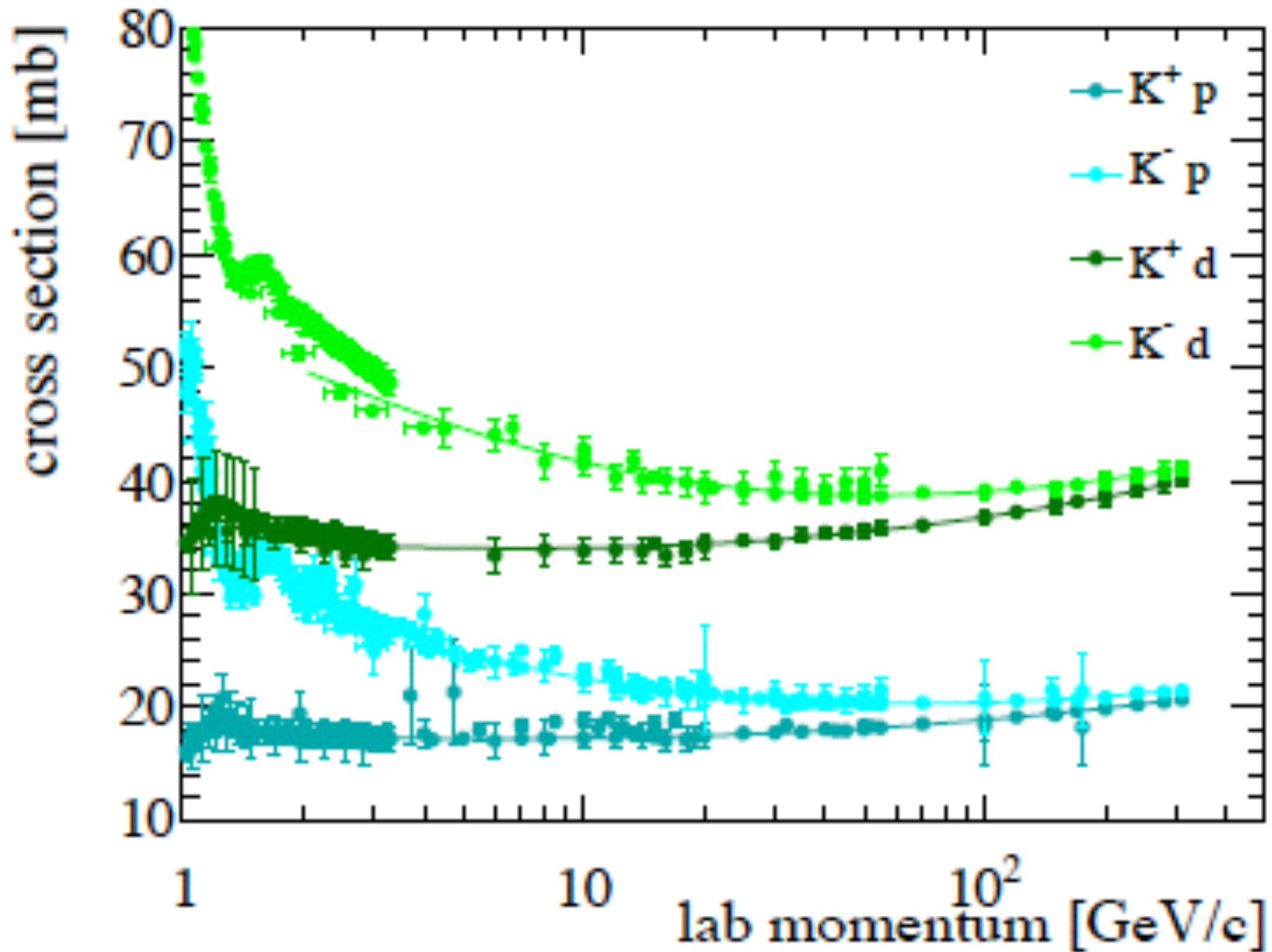
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$$M_{12} \rightarrow M_{12}(1 + h e^{i\phi})$$



Kaon asymmetry



K-factors

