

# Flavored U(1)s



Christopher Smith



- Outline

I. Introduction: MFV, global U(1)s, and anomalies

II. U(1) phases and CP violation

III. B violating attractors

IV. Baryonic axions?

V. Conclusion

# I. MFV, global U(1)s, anomalies

## A. Minimal Flavor Violation

The three generations of quarks/leptons have identical gauge interactions

→ flavor symmetry:  $G_F = U(3)^5 = U(3)_Q \times U(3)_U \times U(3)_D \times U(3)_L \times U(3)_E$

*Chivukula,  
Georgi '87*

- The only sources of breaking are the Yukawa couplings:

$$\mathcal{L}_{\text{Yukawa}} = U \mathbf{Y}_u Q H + D \mathbf{Y}_d Q H^\dagger + E \mathbf{Y}_e L H^\dagger$$

...but artificially invariant if  $\mathbf{Y}_{u,d} \rightarrow g_{U,D} \mathbf{Y}_{u,d} g_Q^\dagger$ ,  $\mathbf{Y}_e \rightarrow g_E \mathbf{Y}_e g_L^\dagger$ .  
*(= spurions)*

- New physics couplings/operators are assumed to be also invariant:

Example:  $d_L^I \rightarrow d_L^J \gamma^*$  from  $\mathcal{O}_\gamma \sim c^{IJ} \bar{Q}^I \gamma_\nu Q^J D_\mu F^{\mu\nu}$

MFV expansion:  $c^{IJ} \sim (1 + \mathbf{Y}_u^\dagger \mathbf{Y}_u + \mathbf{Y}_d^\dagger \mathbf{Y}_d + \dots)^{IJ}$

Background values:  $v \mathbf{Y}_u = m_u V_{CKM}$ ,  $v \mathbf{Y}_{d,e} = m_{d,e}$ .

## B. Flavor symmetry and anomalies

The three generations of quarks/leptons have identical gauge interactions

→ flavor symmetry:  $G_F = U(3)^5 = U(3)_Q \times U(3)_U \times U(3)_D \times U(3)_L \times U(3)_E$

But the U(1)s are chiral hence anomalous:

$$\begin{pmatrix} \partial_\mu J_Q^\mu \\ \partial_\mu J_U^\mu \\ \partial_\mu J_D^\mu \\ \partial_\mu J_L^\mu \\ \partial_\mu J_E^\mu \end{pmatrix} = -\frac{N_f}{16\pi^2} \begin{pmatrix} 1 & 3/2 & 1/6 \\ 1/2 & 0 & 4/3 \\ 1/2 & 0 & 1/3 \\ 0 & 1/2 & 1/2 \\ 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} g_s^2 G_{\mu\nu} \tilde{G}^{\mu\nu} \\ g^2 W_{\mu\nu} \tilde{W}^{\mu\nu} \\ g'^2 B_{\mu\nu} \tilde{B}^{\mu\nu} \end{pmatrix}$$

## B. Flavor symmetry and anomalies

The three generations of quarks/leptons have identical gauge interactions

→ flavor symmetry:  $G_F = U(3)^5 = U(3)_Q \times U(3)_U \times U(3)_D \times U(3)_L \times U(3)_E$

But the U(1)s are chiral hence anomalous:

$$\begin{pmatrix} \partial_\mu J_Y^\mu \\ \partial_\mu J_B^\mu \\ \partial_\mu J_L^\mu \\ \partial_\mu J_{PQ}^\mu \\ \partial_\mu J_E^\mu \end{pmatrix} = -\frac{N_f}{16\pi^2} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1/2 & -1/2 \\ 0 & 1/2 & -1/2 \\ 1 & 0 & 8/3 \\ 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} g_s^2 G_{\mu\nu} \tilde{G}^{\mu\nu} \\ g^2 W_{\mu\nu} \tilde{W}^{\mu\nu} \\ g'^2 B_{\mu\nu} \tilde{B}^{\mu\nu} \end{pmatrix}$$

$U(1)_{B-L}$  and  $U(1)_Y$  are anomaly-free.

### C. Strong but no weak CP puzzle

Could we use these U(1) transformations to get rid of CPV terms:

$$\mathcal{L}_{CP} = \theta_C \frac{\alpha_s}{8\pi} G_{\mu\nu} \tilde{G}^{\mu\nu} + \theta_L \frac{g^2}{16\pi^2} W_{\mu\nu} \tilde{W}^{\mu\nu} + \theta_Y \frac{g'^2}{16\pi^2} B_{\mu\nu} \tilde{B}^{\mu\nu}$$

with  $\theta_C \rightarrow \theta_C - N_f (2\alpha_Q + \alpha_U + \alpha_D)$

$$\theta_L \rightarrow \theta_L - N_f (3\alpha_Q + \alpha_L)$$

$$\theta_Y \rightarrow \theta_Y - N_f (1/3\alpha_Q + 8/3\alpha_U + 2/3\alpha_D + \alpha_L + 2\alpha_E)$$

### C. Strong but no weak CP puzzle

Could we use these U(1) transformations to get rid of CPV terms:

$$\mathcal{L}_{CP} = \theta_C \frac{\alpha_s}{8\pi} G_{\mu\nu} \tilde{G}^{\mu\nu} + \theta_L \frac{g^2}{16\pi^2} W_{\mu\nu} \tilde{W}^{\mu\nu} + \theta_Y \frac{g'^2}{16\pi^2} B_{\mu\nu} \tilde{B}^{\mu\nu}$$

with  $\theta_C \rightarrow \theta_C - \arg \det \mathbf{Y}_u - \arg \det \mathbf{Y}_d$

$$\theta_L \rightarrow \theta_L - N_f (3\alpha_Q + \alpha_L)$$

$$\theta_Y \rightarrow \theta_Y + N_f (3\alpha_Q + \alpha_L) - \frac{8}{3} \arg \det \mathbf{Y}_u - \frac{2}{3} \arg \det \mathbf{Y}_d - 2 \arg \det \mathbf{Y}_e$$

But  $U(3)^5$  is broken by the Yukawa couplings.

= Three  $U(1)$  are fixed to get to  $v \mathbf{Y}_u = m_u V_{CKM}$ ,  $v \mathbf{Y}_{d,e} = m_{d,e}$ .

$B_{\mu\nu} \tilde{B}^{\mu\nu}$ : removed by partial integration.

$W_{\mu\nu} \tilde{W}^{\mu\nu}$ : removed thanks to  $U(1)_{B+L}$  (choice for  $3\alpha_Q + \alpha_L$ ).

$G_{\mu\nu} \tilde{G}^{\mu\nu}$ : cannot be removed  $\rightarrow$  Strong CP puzzle.

## D. Flavor-blind multi-fermion transitions

t'Hooft '76

Instantons still induce  $U(1)$ -breaking but  $SU(3)^5$ -invariant transitions:

Singlet QCD anomaly:

$$\mathcal{H}_{\text{eff}}^{\text{axial}} \sim g_{\text{axial}} (\varepsilon^{IJK} Q^I Q^J Q^K)^2 (\varepsilon^{IJK} U^I U^J U^K) (\varepsilon^{IJK} D^I D^J D^K)$$

→ Mass for the eta prime.

B+L anomaly:

$$\mathcal{H}_{\text{eff}}^{B+L} \sim g_{B+L} (\varepsilon^{IJK} Q^I Q^J Q^K)^3 (\varepsilon^{IJK} L^I L^J L^K)$$

→ Sphalerons in leptogenesis.

So: MFV should be based on  $SU(3)^5$  instead of  $U(3)^5$ .

Four  $U(1)$  are necessarily fixed, only  $U(1)_{B-L}$  may remain.

## II. U(1) phases and CP-violation

## A. U(1) rotations and anomalous CP-violating phases

Flavor-blind anomalous couplings are naturally CP-violating

Singlet QCD anomaly:

$$\mathcal{H}_{\text{eff}}^{\text{axial}} \sim g_{\text{axial}} (\varepsilon^{IJK} Q^I Q^J Q^K)^2 (\varepsilon^{IJK} U^I U^J U^K) (\varepsilon^{IJK} D^I D^J D^K)$$

$$\begin{aligned} \text{Under } U(1)^5 : g_{\text{axial}} &\rightarrow |g_{\text{axial}}| \exp i(\underbrace{\delta_{\text{axial}} + N_f (2\alpha_Q + \alpha_U + \alpha_D)}_{}) \\ &= -\arg \det \mathbf{Y}_u - \arg \det \mathbf{Y}_d = \theta_{\text{eff}} - \theta_C \end{aligned}$$

B+L anomaly:

$$\mathcal{H}_{\text{eff}}^{B+L} \sim g_{B+L} (\varepsilon^{IJK} Q^I Q^J Q^K)^3 (\varepsilon^{IJK} L^I L^J L^K)$$

$$\begin{aligned} \text{Under } U(1)^5 : g_{B+L} &\rightarrow |g_{B+L}| \exp i(\underbrace{\delta_{B+L} + N_f (3\alpha_Q + \alpha_L)}_{}) \\ &= \theta_L \end{aligned}$$

Two additional free and CP-violating parameters in the SM?

## B. U(1) rotations and CP-violating B and/or L violating couplings

Simplest  $\Delta B$  or  $\Delta L$  operators allowed by the SM flavor structures:



$$\text{E.g.: } \varepsilon^{IJK} Q^{\dagger I} (U \mathbf{Y}_u)^J (D \mathbf{Y}_d)^K \rightarrow \exp iN_f \alpha_Q$$

$$~~~~~ \varepsilon^{IJK} L^{\dagger I} L^{\dagger J} (E \mathbf{Y}_e)^K \rightarrow \exp iN_f \alpha_L$$

$$\mathcal{H}_{eff} = \frac{1}{\Lambda^5} \left[ \underbrace{c_1 E L^{\dagger 2} U^3 + c_2 L^{\dagger 3} Q^{\dagger} U^2 + c_3 D^4 U^2 + c_4 D^3 U Q^{\dagger 2} + c_5 D^2 Q^{\dagger 4}}_{\Delta B, \Delta L = 1, 3} \right] \underbrace{\quad \quad \quad}_{\Delta B, \Delta L = 2, 0}$$

can induce proton decay!    can induce neutron oscillations!

## B. U(1) rotations and CP-violating B and/or L violating couplings

Simplest  $\Delta B$  or  $\Delta L$  operators allowed by the SM flavor structures:



$$\text{E.g.: } \epsilon^{IJK} Q^{\dagger I} (U \mathbf{Y}_u)^J (D \mathbf{Y}_d)^K \rightarrow \exp iN_f \alpha_Q$$

$$~~~~~ \epsilon^{IJK} L^{\dagger I} L^{\dagger J} (E \mathbf{Y}_e)^K \rightarrow \exp iN_f \alpha_L$$

$$\mathcal{H}_{eff} = \frac{1}{\Lambda^5} \left[ \underbrace{c_1 EL^{\dagger 2} U^3 + c_2 L^{\dagger 3} Q^{\dagger} U^2 + c_3 D^4 U^2 + c_4 D^3 U Q^{\dagger 2} + c_5 D^2 Q^{\dagger 4}}_{\Delta B, \Delta L = 1, 3} \right] \underbrace{\quad \quad \quad}_{\Delta B, \Delta L = 2, 0}$$

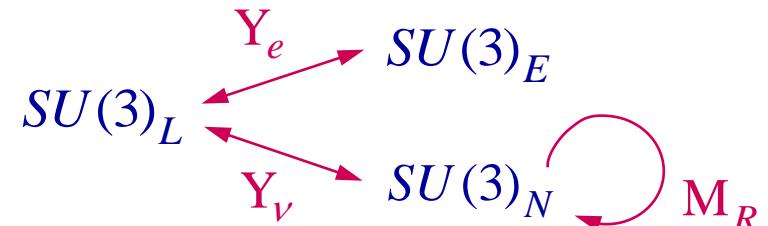
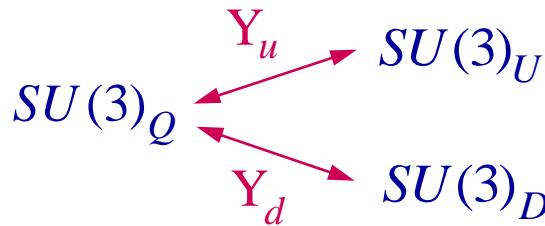
$$\rightarrow \exp iN_f (\alpha_Q + \alpha_L)$$

$$\rightarrow \exp iN_f (2\alpha_Q)$$

Both classes of operators cannot be made real at the same time.

## B. U(1) rotations and CP-violating B and/or L violating couplings

Weinberg operators are naturally CP-violating:



$$\text{E.g.: } \varepsilon^{IJK} Q^{\dagger I} (U \mathbf{Y}_u)^J (D \mathbf{Y}_d)^K$$

$$\varepsilon^{IJK} L^{\dagger I} (\underbrace{v \mathbf{Y}_v^T \mathbf{M}_R^{-1} \mathbf{Y}_v}_{m_v/v} \mathbf{Y}_e^\dagger \mathbf{Y}_e)^{JK}$$

Weinberg '79

$$\mathcal{H}_{eff} = H^2 L (\mathbf{Y}_v^T \mathbf{M}_R^{-1} \mathbf{Y}_v) L + \frac{1}{\Lambda^2} \left[ c_1 L Q^3 + c_2 E U^2 D + c_3 E U Q^{\dagger 2} + c_4 L Q D^\dagger U^\dagger \right]$$



$$c_i \rightarrow |c_i| \exp i(\delta_i + \underbrace{N_f (3\alpha_Q + \alpha_L)}_{= \theta_L})$$

Conventionally fixed:  $-2\alpha_L \equiv \arg(\mathbf{Y}_v^T \mathbf{M}_R^{-1} \mathbf{Y}_v)^{11}$

### C. Supersymmetry: MFV for R-parity violating couplings

1. Take the usual seesaw :  $-2\alpha_L \equiv \arg(\mathbf{Y}_v^T \mathbf{M}_R^{-1} \mathbf{Y}_v)^{11}$
2. Get rid of  $W_{\mu\nu} \tilde{W}^{\mu\nu} \Rightarrow 3\alpha_Q = \theta_L / N_f - \alpha_L$  : All 5 phases fixed!
3. Add  $\Delta B=1$  supersymmetric couplings:  $\mathcal{W}_{RPV} = \lambda''^{IJK} U^I D^J D^K$
4. Impose MFV, e.g.  $\lambda''^{IJK} = \lambda \epsilon^{LMN} Y_u^{IL} Y_d^{JM} Y_d^{KN}$  (Holomorphic MFV)
 

↑  
O(1) free parameter
5. The RPV coupling is then CP-violating, even when  $\lambda$  is assumed real:
 

$\lambda'' \rightarrow |\lambda''| \exp i(\delta_{\lambda''} + N_f \alpha_Q)$   
↑  
Small CKM-induced phase

### III. B violating attractors

## A. Flavored R-parity violation in the MSSM

Nikolidakis, CS '07

$$\mathcal{W}_{RPV} \supset \underbrace{\lambda^{IJK} L^I L^J E^K + \lambda'^{IJK} L^I Q^J D^K}_{\Delta L=1} + \underbrace{\lambda''^{IJK} U^I D^J D^K}_{\Delta B=1}$$

Violates selection rules:

 $\Delta L=3$  hierarchies $\oplus$  $\Delta L=2$  neutrino mass

Yukawa-induced hierarchies:

$$\lambda''^{IJK} \sim \varepsilon^{LJK} (Y_u Y_d^\dagger)^{IL}$$

Dominant, breaks  $U(1)_D$ 

$$\lambda'^{IJK} \sim \varepsilon^{ILM} \underbrace{(v Y_\nu^T M_R^{-1} Y_\nu)_{IJ}}_{m_\nu/v} (Y_e^\dagger Y_e)^{LM} Y_d^{KJ}$$

$$\lambda''^{IJK} \sim \varepsilon^{LMN} Y_u^{IL} Y_d^{JM} Y_d^{KN}$$

Holomorphic, breaks  $U(1)_Q$

## A. Flavored R-parity violation in the MSSM

Nikolidakis, CS '07

$$\mathcal{W}_{RPV} \supset \underbrace{\lambda^{IJK} L^I L^J E^K + \lambda'^{IJK} L^I Q^J D^K}_{\Delta L=1} + \underbrace{\lambda''^{IJK} U^I D^J D^K}_{\Delta B=1}$$

Violates selection rules:

 $\Delta L=3$  hierarchies $\oplus$  $\Delta L=2$  neutrino mass

$$\Rightarrow \begin{cases} \lambda^{IJK} < 10^{-13} \\ \lambda'^{IJK} < 10^{-17} \end{cases}$$

Yukawa-induced hierarchies:

Dominant :

$\lambda''$	$ds$	$sb$	$bd$	$x \equiv \mathcal{O}(10^{-x})$
$u$	5	5	5	
$c$	4	6	5	$\tan \beta = 5$
$t$	1	5	4	

Holomorphic:

Csaki, Grossman, Heidenreich '11

$\lambda''$	$ds$	$sb$	$bd$
$u$	13	8	10
$c$	10	6	7
$t$	6	5	6

Proton decay is slow enough even for TeV-scale squark masses!

## A. Flavored R-parity violation in the MSSM

Nikolidakis, CS '07

$$\mathcal{W}_{RPV} \supset \underbrace{\lambda^{IJK} L^I L^J E^K + \lambda'^{IJK} L^I Q^J D^K}_{\Delta L=1} + \underbrace{\lambda''^{IJK} U^I D^J D^K}_{\Delta B=1}$$

Violates selection rules:

 $\Delta L=3$  hierarchies $\oplus$  $\Delta L=2$  neutrino mass

$$\Rightarrow \begin{cases} \lambda^{IJK} < 10^{-12} \\ \lambda'^{IJK} < 10^{-14} \end{cases}$$

Yukawa-induced hierarchies:

Dominant :

$\lambda''$	$ds$	$sb$	$bd$
$u$	4	4	4
$c$	3	4	4
$t$	0	3	3

$x \equiv \mathcal{O}(10^{-x})$

$\tan \beta = 50$

Holomorphic:

Csaki, Grossman, Heidenreich '11

$\lambda''$	$ds$	$sb$	$bd$
$u$	11	6	8
$c$	8	4	5
$t$	4	3	4

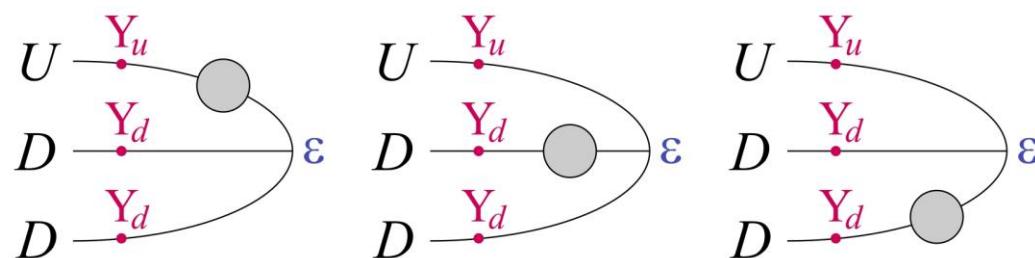
Proton decay is slow enough even for TeV-scale squark masses!

## B. Form non-renormalization of holomorphic MFV

Bernon, CS '14

At the high scale:  $\lambda''^{IJK} = \lambda_1 \epsilon^{LMN} Y_u^{IL} Y_d^{JM} Y_d^{KN}$

At the low scale?  $\lambda''^{IJK} = \lambda_1 \epsilon^{LMN} Y_u^{IL} Y_d^{JM} Y_d^{KN}$   
 $+ \lambda_2 \epsilon^{LMN} (Y_u Y_u^\dagger Y_u)^{IL} Y_d^{JM} Y_d^{KN}$   
 $+ \lambda_3 \epsilon^{LMN} Y_u^{IL} (Y_d Y_u^\dagger Y_u)^{JM} Y_d^{KN} + \dots$



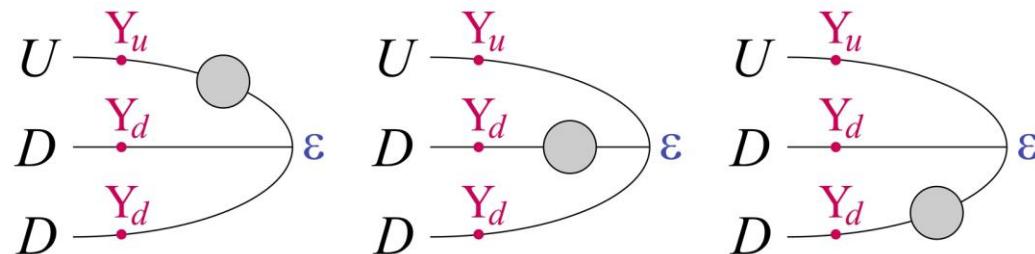
## B. Form non-renormalization of holomorphic MFV

Bernon, CS '14

At the high scale:  $\lambda''^{IJK} = \lambda_1 \epsilon^{LMN} Y_u^{IL} Y_d^{JM} Y_d^{KN}$

At the low scale?  $\lambda''^{IJK} = \lambda_1 \epsilon^{LMN} Y_u^{IL} Y_d^{JM} Y_d^{KN}$   
 $+ \lambda_2 \epsilon^{LMN} (Y_u Y_u^\dagger Y_u)^{IL} Y_d^{JM} Y_d^{KN}$   
 $+ \lambda_3 \epsilon^{LMN} Y_u^{IL} (Y_d Y_u^\dagger Y_u)^{JM} Y_d^{KN} + \dots$

Actually, these corrections precisely sum up, at all orders



$$\epsilon^{LJK} A^{LI} + \epsilon^{ILK} A^{LJ} + \epsilon^{IJL} A^{LK} = \epsilon^{IJK} \text{Tr}(A)$$

## B. Form non-renormalization of holomorphic MFV

Bernon, CS '14

At the high scale:  $\lambda''^{IJK} = \lambda_1 \epsilon^{LMN} Y_u^{IL} Y_d^{JM} Y_d^{KN}$

At the low scale?  $\lambda''^{IJK} = \lambda_1 \epsilon^{LMN} Y_u^{IL} Y_d^{JM} Y_d^{KN}$   
 $+ \lambda_2 \epsilon^{LMN} (Y_u Y_u^\dagger Y_u)^{IL} Y_d^{JM} Y_d^{KN}$   
 $+ \lambda_3 \epsilon^{LMN} Y_u^{IL} (Y_d Y_u^\dagger Y_u)^{JM} Y_d^{KN} + \dots$

Actually, these corrections precisely sum up, at all orders,

And holomorphy holds at all scales if it holds at some scale:

$$\lambda''^{IJK}[t] = \lambda_1[t] \epsilon^{LMN} Y_u^{IL}[t] Y_d^{JM}[t] Y_d^{KN}[t]$$

$$\frac{d\lambda_1}{dt} = -\lambda_1 (\gamma_{Q^P}^{Q^P} + \gamma_{H_2}^{H_2} + 2\gamma_{H_1}^{H_1})$$

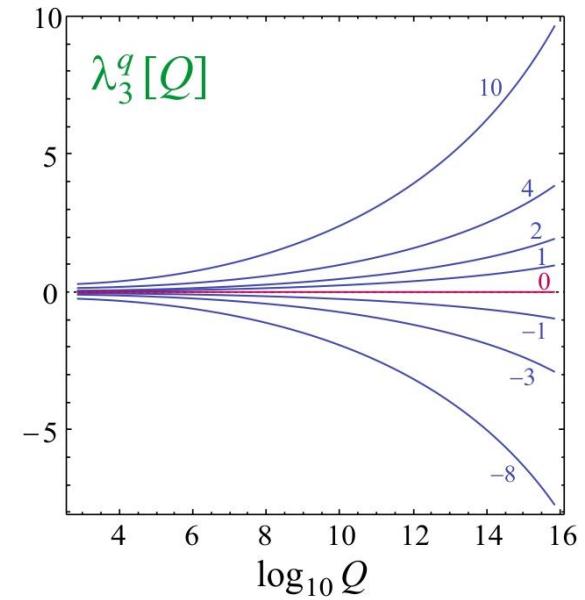
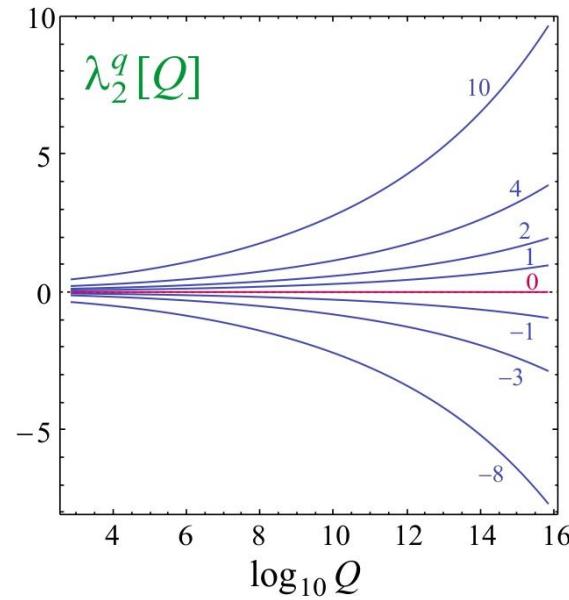
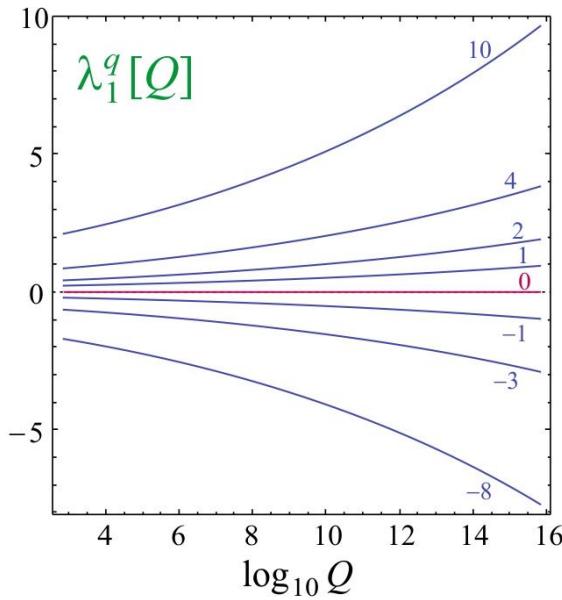
## B. Form non-renormalization of holomorphic MFV

Bernon, CS '14

At the high scale:  $\lambda''^{IJK} = \lambda_1 \epsilon^{LMN} Y_u^{IL} Y_d^{JM} Y_d^{KN}$

$$+ \lambda_2 \epsilon^{LMN} (Y_u Y_u^\dagger Y_u)^{IL} Y_d^{JM} Y_d^{KN}$$

$$+ \lambda_3 \epsilon^{LMN} Y_u^{IL} (Y_d Y_u^\dagger Y_u)^{JM} Y_d^{KN} + \dots$$

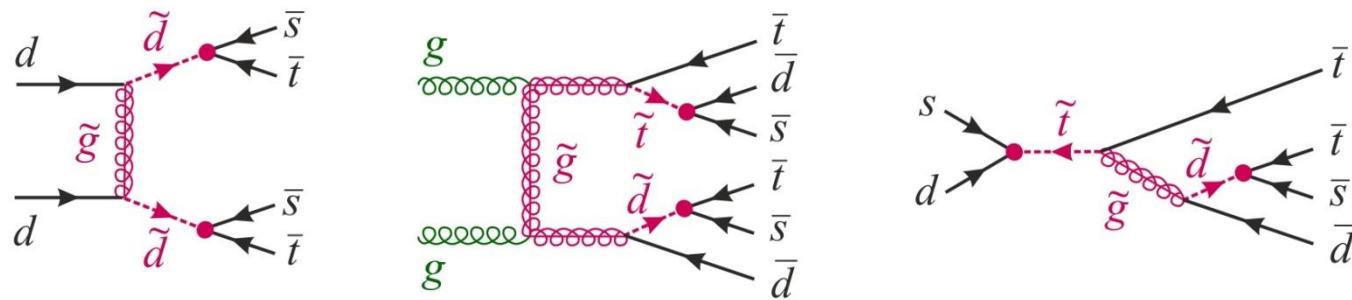


Holomorphy emerges at the low scale whenever only  $U(1)_Q$  is broken.

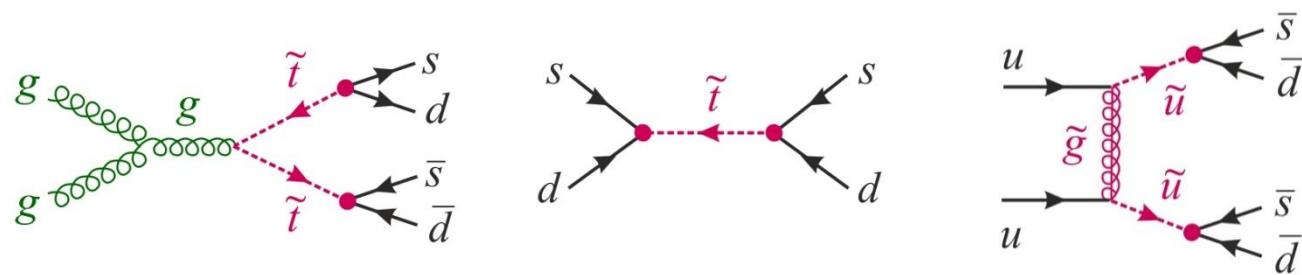
### C. Characteristic signatures of the B violating MSSM

Dominant B-violation through  $\lambda''_{312} \leq \mathcal{O}(1)$ :  $\tilde{t}_R d_R s_R$ ,  $t_R \tilde{d}_R s_R$ ,  $t_R d_R \tilde{s}_R$ .

- Same sign top pairs  $\rightarrow$  same sign lepton pairs.



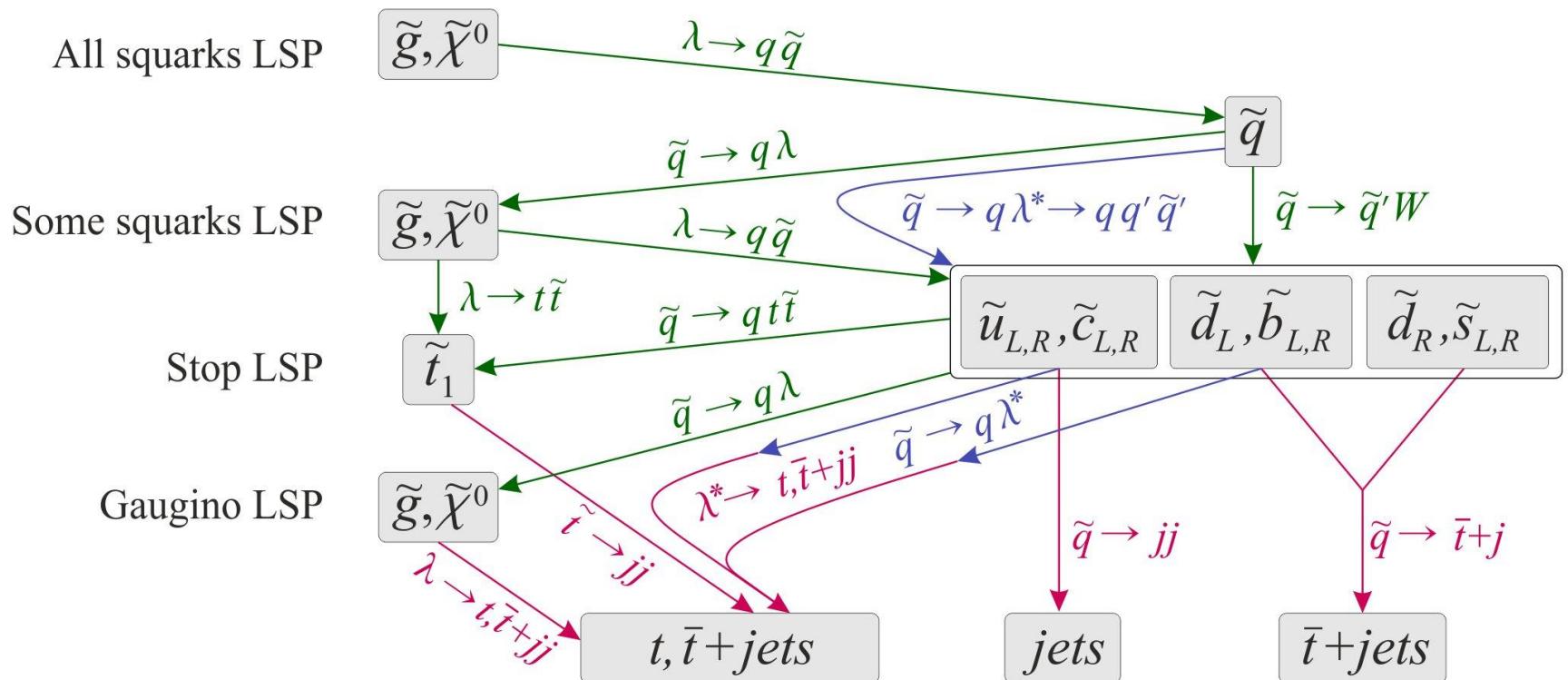
- Dijet resonances from intermediate up-type squarks.



- R-hadrons? Without large mass splitting, sparticles decay too quickly.

## C. Characteristic signatures of the B violating MSSM

Durieux, CS, '13

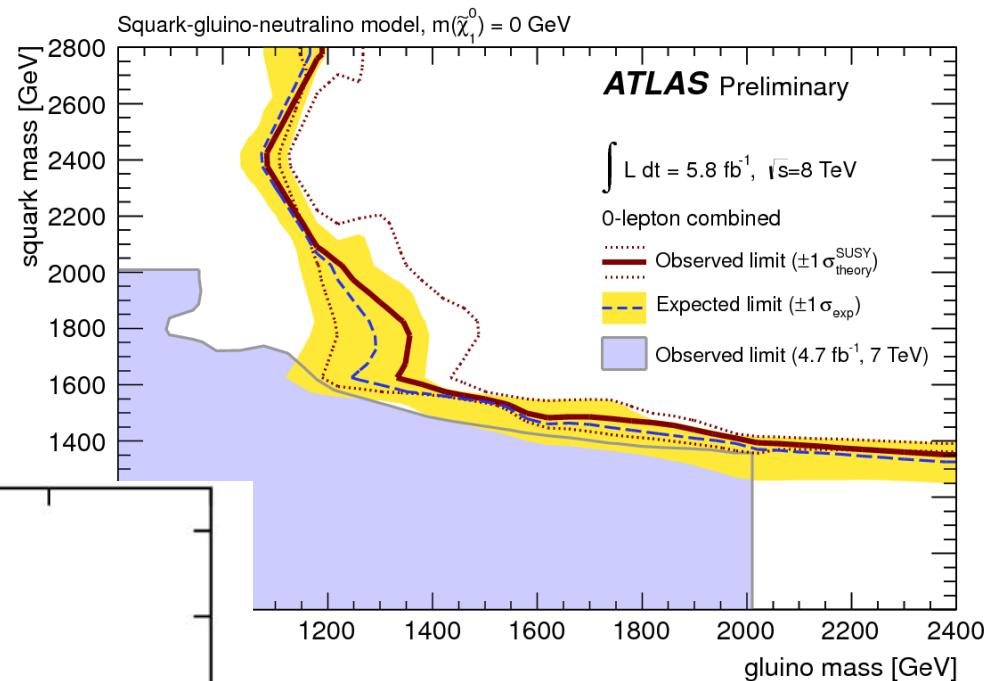
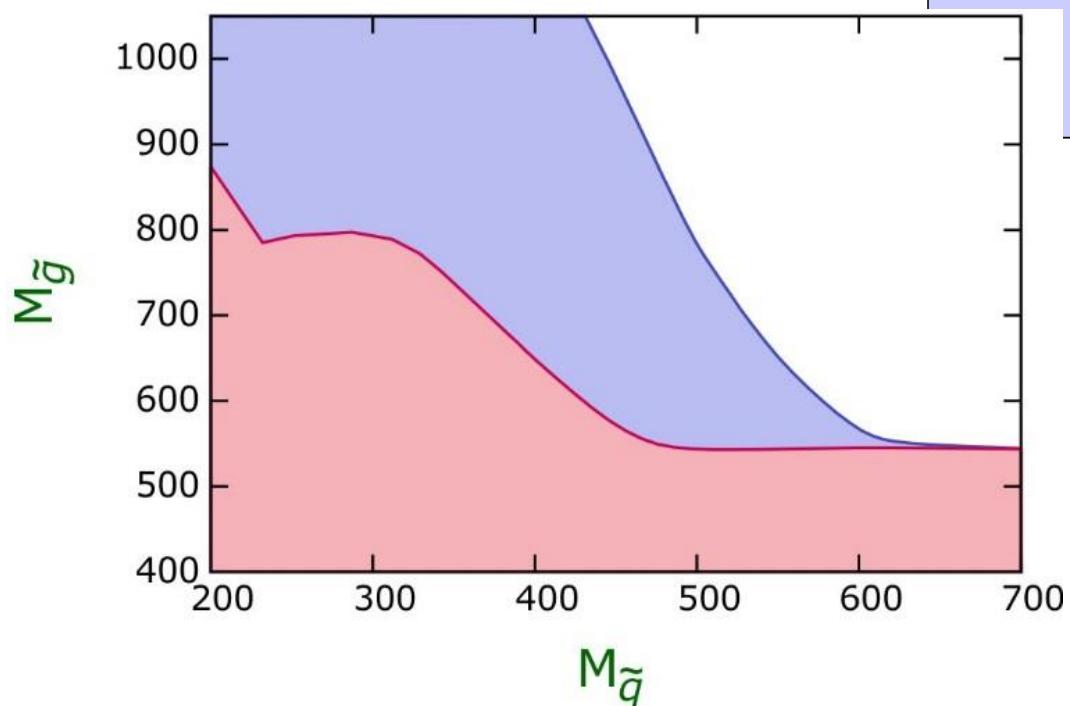


## C. Characteristic signatures of the B violating MSSM

Durieux, CS, '13

MSSM with R-parity

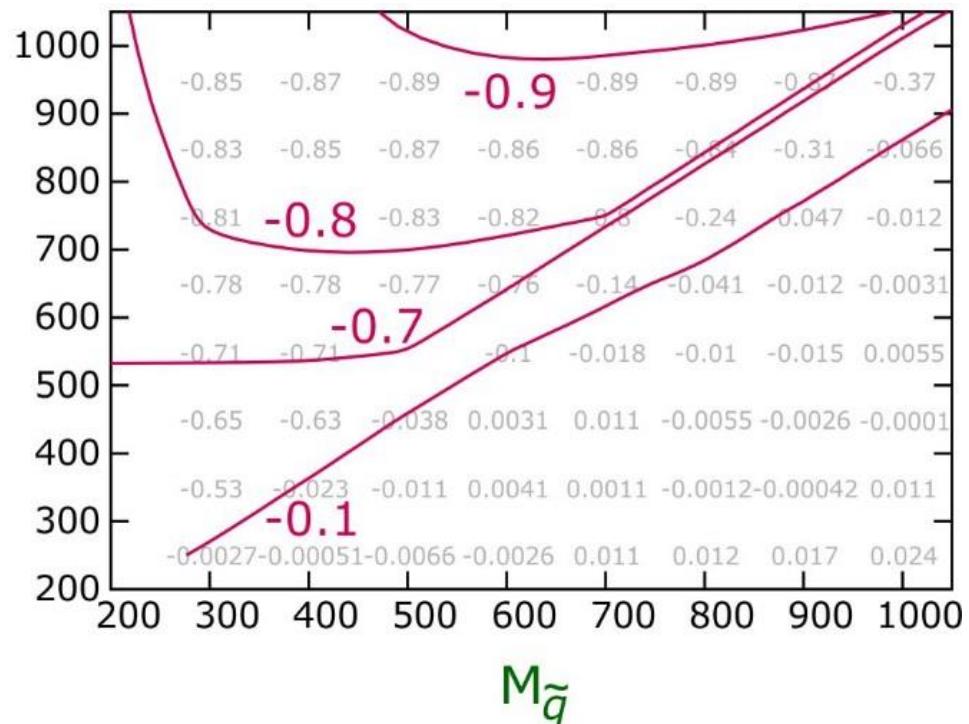
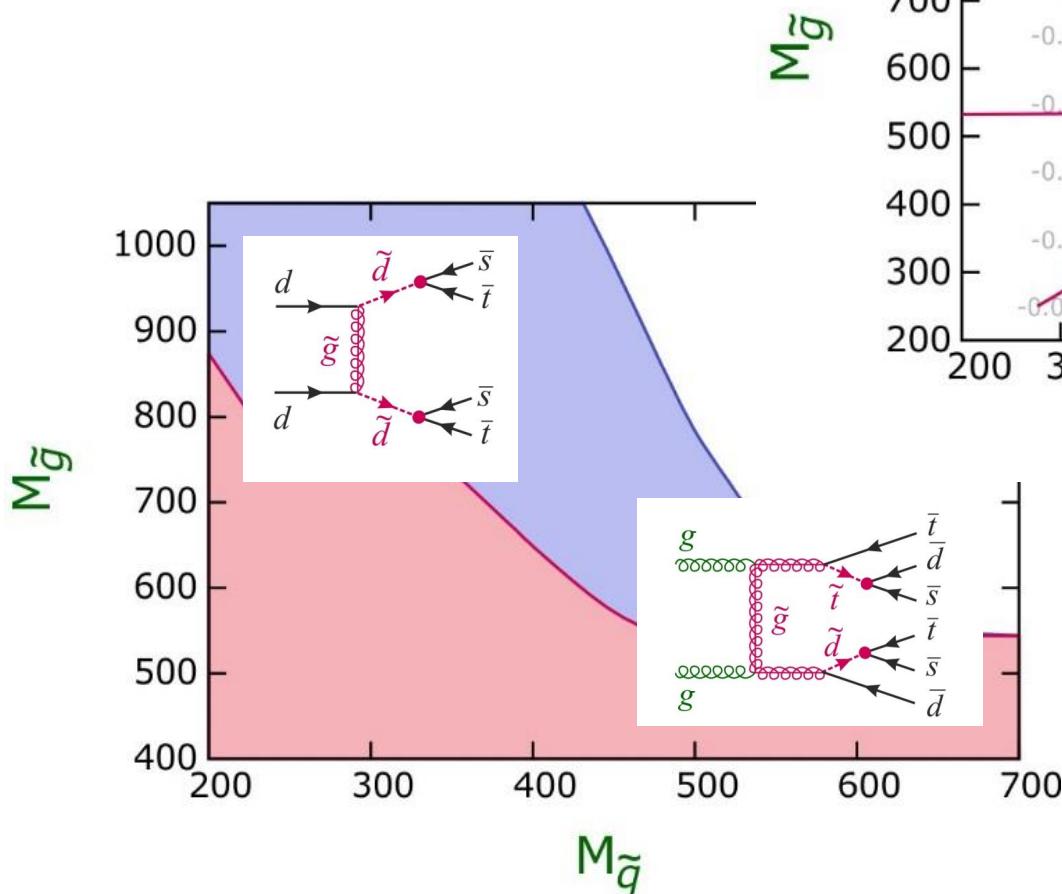
(from same sign lepton pairs)



## C. Characteristic signatures of the B violating MSSM

Durieux, CS, '13

Lepton charge asymmetry:



MSSM without R-parity

## IV. Baryonic Axions?

## A. Invisible axion as a solution to the strong CP puzzle

Introduce a new field to spontaneously relax  $\theta_C$  towards zero.

- Impose  $U(1)_{PQ}$  invariance (DFSZ):

$$\mathcal{L} = H_u U \mathbf{Y}_u Q + H_d D \mathbf{Y}_d Q + H_d E \mathbf{Y}_e L + V(H_u, H_d, \phi)$$

$$\supset H_u H_d \phi^2$$

$$e^{-i(X_u + X_d) \alpha_{PQ}}$$

- Break  $U(1)_{PQ}$  spontaneously  $\rightarrow$  Goldstone boson = axion
- $U(1)_{PQ}$  is a chiral symmetry  $\rightarrow$  explicitly broken by the anomaly.

These (not unique) charges are not always compatible with B violation!

(think about  $\lambda''^{IJK} U^I D^J D^K$  in SUSY)

Watamura & Yoshimura, '82

## B. Could the axion participate in B violating processes?

[Some very preliminary ideas!]

Proton decay to axions?

$$\mathcal{L}_{eff} = \phi \frac{LQQQ}{\Lambda^3} \rightarrow \phi = (v_{PQ} + \eta) e^{ia/v_{PQ}} \rightarrow \mathcal{L}_{eff} = \frac{v_{PQ} LQQQ}{\Lambda^3} + i \frac{a LQQQ}{\Lambda^3}$$

Even with MFV, the scale  $\Lambda$  must be close to  $v_{PQ}$ ,  
and the axion should stay invisible.

Supersymmetry? Naively, the couplings could sum up to

$$\mathcal{W}_{eff} = \left( \frac{v_{PQ}}{\Lambda} + i \frac{a}{\Lambda} \right) \lambda''^{IJK} U^I D^J D^K$$

With MFV, proton  
decay still ok even  
for large  $v_{PQ}/\Lambda \sim 10^5$ .

If  $m_{\tilde{a}} < m_{p^+}$ :  $p^+ \rightarrow K^+ \tilde{a} \Rightarrow \Lambda > 10^{3-5}$  TeV.

If  $m_{\tilde{a}} > m_{p^+}$ :  $pp \rightarrow \bar{t} + \tilde{a}$  at the LHC?

# Conclusion

## 1. MFV must allow for B and/or L violation

Since it occurs in the SM → Enforce MFV using  $SU(3)^5$  only.

## 2. Flavor U(1)-breakings are quite automatically CP-violating

In particular, the SM appears to have four CP-violating parameters!

$$\delta_{CKM}, \theta_L, \theta_C, \theta_{eff} = \theta_C - \arg \det \mathbf{Y}_u - \arg \det \mathbf{Y}_d$$

In supersymmetry, RPV should be CP-violating also.

## 3. In supersymmetry, large B-violation is natural and welcome!

With holomorphy, it even gives a unique IR stable parametrization.

Could a signals in same sign lepton pair searches be around the corner?

## 4. Axions and B-violation could be intimately linked.