

Lepton Non-Universality and Flavor in Rare Decays

$$R_K @ \text{LHCb} \neq 1$$

<http://journals.aps.org/prl/abstract/10.1103/PhysRevLett.113.151601>,
arXiv:1406.6482 [hep-ex]

physics highlight: <http://physics.aps.org/articles/v7/102>

based on works with Martin Schmaltz and Ivo de Medeiros Varzielas
arXiv:1408.1627, arXiv:1411.4773, arXiv:1503.01084 [hep-ph].

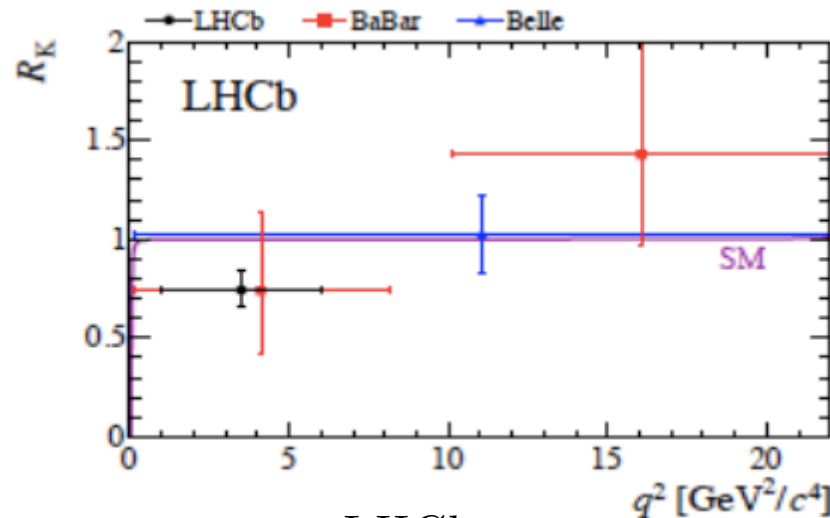
Gudrun Hiller, Dortmund

$$R_K = \frac{\mathcal{B}(\bar{B} \rightarrow \bar{K} \mu \mu)}{\mathcal{B}(\bar{B} \rightarrow \bar{K} e e)}$$

idea: $R_H^{\text{SM}} = 1 + \text{tiny}$ for $H = K, K^*, X_s, \dots$ GH, Krüger, hep-ph/0310219

refined, cuts, correlations, models: 0709.4174 Bobeth et al

early data: Belle 0904.0770, BaBar 1204.3933, consistent with SM



latest data: LHCb 1406.6482 $R_K^{\text{LHCb}} \simeq 3/4 \pm 0.1$: **2.6 σ , BSM huge!**

theory: 1406.6681 1407.7044 1408.1627 1408.4097 1409.0882

$B^\pm \rightarrow K^\pm ee$ and $B^\pm \rightarrow K^\pm \mu\mu$ events at LHCb. Full data set, 3fb^{-1} , from 7 and 8 TeV LHC run.

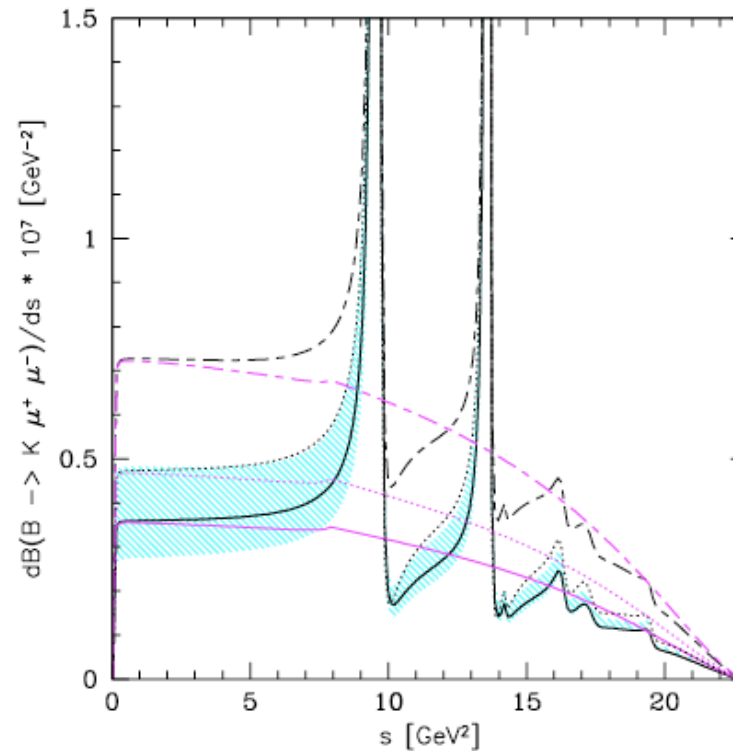


Fig from 9910221, solid: SM, dotted and dot-dashed: BSM scenario

Select low dilepton mass window: $1 \leq q^2 < 6 \text{ GeV}^2$ below J/Ψ .

situation for numerator $\mu\mu$ and denominator ee of R_K separately:

	LHCb ^a	SM ^b
$\mathcal{B}(B \rightarrow K\mu\mu)_{[1,6]}$	$(1.21 \pm 0.09 \pm 0.07) \cdot 10^{-7}$	$(1.75^{+0.60}_{-0.29}) \cdot 10^{-7}$
$\mathcal{B}(B \rightarrow Kee)_{[1,6]}$	$(1.56^{+0.19+0.06}_{-0.15-0.04}) \cdot 10^{-7}$	same
$R_K _{[1,6]}$	$0.745 \pm_{0.074}^{0.090} \pm 0.036$	$\simeq 1$

^a 1209.4284 (μ) and 1406.6482 (e) ^b Bobeth, GH, van Dyk '12, form factors from 1006.4945

Individual branching ratios make presently no case for new physics, although muons are a bit below SM. The ratio R_K is much cleaner.

Probing Lepton e vs μ universality with R_K

.. which was the idea behind R_K in first place:

Lepton-universal effects – including hadronic ones – drop out in ratios of branching fractions GH,Krüger'03

$$R_K = \frac{\mathcal{B}(\bar{B} \rightarrow \bar{K} \mu \mu)}{\mathcal{B}(\bar{B} \rightarrow \bar{K} e e)}$$

$R_K^{\text{SM}} = 1$ up to kinematic corrections $\mathcal{O}(m_\mu^2/m_b^2)$ and electromagnetic logs (depending on exp. cuts) $\mathcal{O}(\frac{\alpha_e}{4\pi} \text{Log}(m_e/m_b))$ at O(per mille) level.

$$R_K^{\text{LHCb}} = 0.745 \pm_{0.074}^{0.090} \pm 0.036, \quad \text{1406.6482 hep-ex}$$

2.6σ : if taken at face value this implies lepton-nonuniversal new physics in the flavor sector.

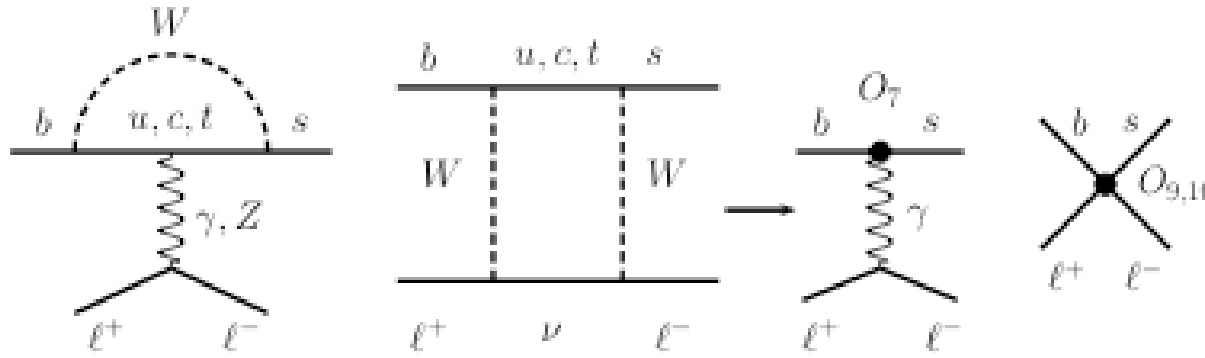
Probing Lepton e vs μ universality with R_K

Comments:

- $R_K = 0.745 \pm_{0.074}^{0.090} \pm 0.036 < 1$ implies suppressed muons and/or enhanced electrons, that is, BSM in electrons, or muons, or both.
- $R_K \simeq 3/4$ is almost an order 1 effect. Yet, it is not excluded by other data essentially because R_K is so clean and the effect, lepton-nonuniversality in $b \rightarrow s$, is quite specific.
- Ongoing precision fits in $B \rightarrow K^{(*)} \ell \ell$ decays (Babar, Belle, CDF, ATLAS, CMS, LHCb) [1307.5683](#), [1308.1501](#), [1310.2478](#) dominated from hadron colliders hence give essentially lepton-specific constraints for $\ell = \mu$.
- Electrons much more difficult for LHCb than muons:
 $B \rightarrow K \mu \mu$: ~ 1226 events, $B \rightarrow K e e$: $\sim O(200)$ events.

- 1) About R_K ✓
- 2) Model-independent interpretations (implications for Wilson coefficients)
- 3) Model-interpretations; Leptoquarks; mass scale for this?
- 4) Diagnosing with more ratios: R_K vs R_{K^*} vs R_φ vs R_{X_s} vs ..
- 5) Connecting to flavor; LFV and probing the origin

$b \rightarrow s\ell\ell$ FCNCs model-independently



Construct EFT $\mathcal{H}_{\text{eff}} = -4 \frac{G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i C_i(\mu) O_i(\mu)$ at dim 6

V,A operators $\mathcal{O}_9 = [\bar{s}\gamma_\mu P_L b] [\bar{\ell}\gamma^\mu \ell]$, $\mathcal{O}'_9 = [\bar{s}\gamma_\mu P_R b] [\bar{\ell}\gamma^\mu \ell]$

$\mathcal{O}_{10} = [\bar{s}\gamma_\mu P_L b] [\bar{\ell}\gamma^\mu \gamma_5 \ell]$, $\mathcal{O}'_{10} = [\bar{s}\gamma_\mu P_R b] [\bar{\ell}\gamma^\mu \gamma_5 \ell]$

S,P operators $\mathcal{O}_S = [\bar{s}P_R b] [\bar{\ell}\ell]$, $\mathcal{O}'_S = [\bar{s}P_L b] [\bar{\ell}\ell]$, **ONLY O_9, O_{10} are SM, all other BSM**

$\mathcal{O}_P = [\bar{s}P_R b] [\bar{\ell}\gamma_5 \ell]$, $\mathcal{O}'_P = [\bar{s}P_L b] [\bar{\ell}\gamma_5 \ell]$

and tensors $\mathcal{O}_T = [\bar{s}\sigma_{\mu\nu} b] [\bar{\ell}\sigma^{\mu\nu} \ell]$, $\mathcal{O}_{T5} = [\bar{s}\sigma_{\mu\nu} b] [\bar{\ell}\sigma^{\mu\nu} \gamma_5 \ell]$

lepton specific $C_i O_i \rightarrow C_i^\ell O_i^\ell$, $\ell = e, \mu, \tau$

Barring the presence of several different types of operators, hence allowing for tuning, there are the following model-independent explanations for R_K :

- i)* V,A operators with muons
- ii)* V,A operators with electrons
- iii)* S,P operators electrons (disfavored at 1σ and requires cancellations, testable with $\bar{B} \rightarrow \bar{K}ee$ angular distributions)

Tensors and S,P muons are excluded.

Model-independent interpretations with V,A interactions: [arXiv:1408.1627](#),

[1406.6681](#)

$$0.7 \lesssim \text{Re}[X^e - X^\mu] \lesssim 1.5 ,$$

$$X^\ell = C_9^{\text{NP}\ell} + C_9^{\prime\ell} - (C_{10}^{\text{NP}\ell} + C_{10}^{\prime\ell})$$

- The required NP is large $C_9^{\text{SM}} \simeq -C_{10}^{\text{SM}} \simeq 4.2$.
- Since the SM couples V-A-like, the leading constraints on X^ℓ from SM-NP-interference have V-A structure for the leptons; there is no sensitivity to V+A (right-handed) leptons at this level.

Lets use the chiral basis:

$$\begin{aligned}\mathcal{O}_{LL}^\ell &\equiv (\mathcal{O}_9^\ell - \mathcal{O}_{10}^\ell)/2, & \mathcal{O}_{LR}^\ell &\equiv (\mathcal{O}_9^\ell + \mathcal{O}_{10}^\ell)/2, \\ \mathcal{O}_{RL}^\ell &\equiv (\mathcal{O}'_9{}^\ell - \mathcal{O}'_{10}{}^\ell)/2, & \mathcal{O}_{RR}^\ell &\equiv (\mathcal{O}'_9{}^\ell + \mathcal{O}'_{10}{}^\ell)/2.\end{aligned}$$

R_K sensitive to left-handed leptons:

$$C_{LL}^\ell = C_9^\ell - C_{10}^\ell, \quad C_{RL}^\ell = C'_9{}^\ell - C'_{10}{}^\ell.$$

right-handed leptons: $C_{LR}^\ell = C_9^\ell + C_{10}^\ell$, $C_{RR}^\ell = C'_9{}^\ell + C'_{10}{}^\ell$

This suggests to use in global fits invariant-constraints such as

$$C_9^{\text{NP}\ell} = -C_{10}^{\text{NP}\ell}, \quad C_9^{\text{NP}'\ell} = -C_{10}^{\text{NP}'\ell}.$$

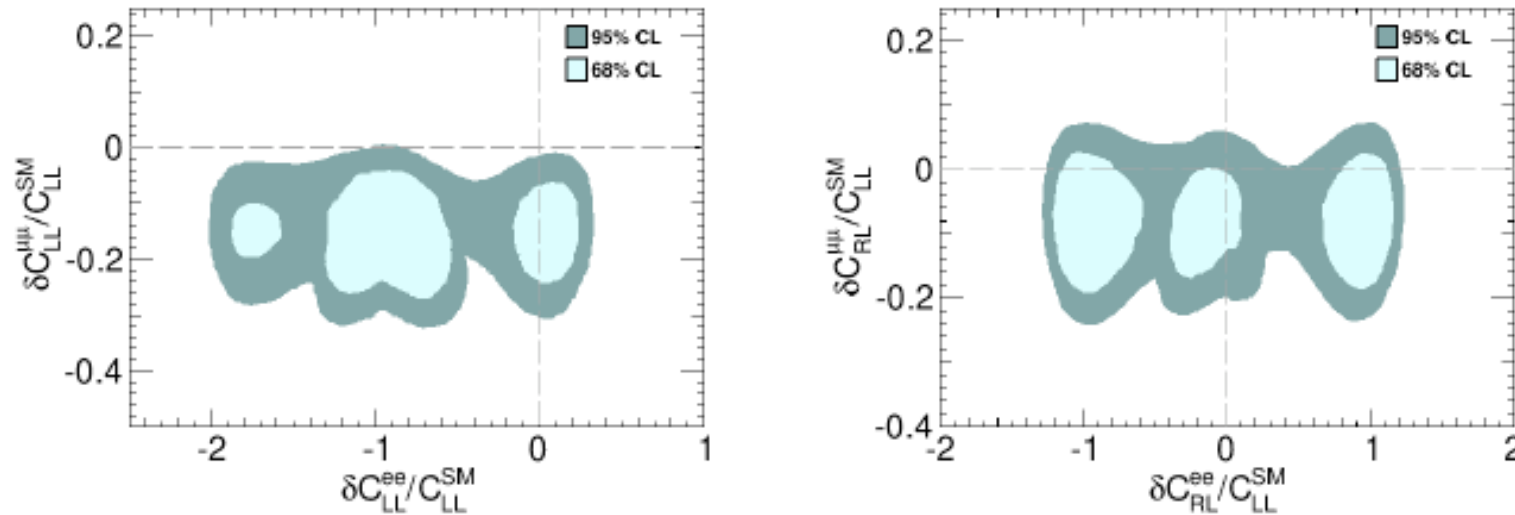


Fig from 1410.4545 – global fit including R_K

- Bounds stronger for $\mu\mu$ (y -axis) than for ee (x -axis).
- Both left-handed quarks C_{LL} (left-handed plot) and right-handed quarks C_{RL} (right-handed plot) can be sizable.

If we assume new physics in muons alone employ $\mathcal{B}(\bar{B}_s \rightarrow \mu\mu)$

$$\frac{\mathcal{B}(\bar{B}_s \rightarrow \mu\mu)^{\text{exp}}}{\mathcal{B}(\bar{B}_s \rightarrow \mu\mu)^{\text{SM}}} = 0.79 \pm 0.20 \quad \text{is suppressed currently .}$$

$$0.0 \lesssim \text{Re}[C_{LR}^\mu + C_{RL}^\mu - C_{LL}^\mu - C_{RR}^\mu] \lesssim 1.9, \quad (\mathcal{B}(B_s \rightarrow \mu\mu))$$

$$0.7 \lesssim -\text{Re}[C_{LL}^\mu + C_{RL}^\mu] \lesssim 1.5. \quad (R_K)$$

This isolates C_{LL}^μ as the only single operator (particle) interpretation of R_K . Note: this is V-A. Iff $\mathcal{B}(\bar{B}_s \rightarrow \mu\mu)$ would be enhanced this would isolate $C_{RL}^\mu \simeq -1$, V+A! $b \rightarrow \text{see}$ way less constrained.

V,A muons and V,A electrons can be realized with leptoquark models

GH, Schmaltz arXiv:1408.1627, Phys. Rev. D 90, 054014 (2014)

A model with C_{RL}^e (includes R-parity violating MSSM):

$\mathcal{L} = -\lambda_{d\ell} \varphi (\bar{d}P_L\ell)$ with leptoquark $\varphi(3, 2)_{1/6}$ with mass M .

$$\mathcal{H}_{\text{eff}} = -\frac{|\lambda_{d\ell}|^2}{M^2} (\bar{d}P_L\ell) (\bar{\ell}P_Rd) = \frac{|\lambda_{d\ell}|^2}{2M^2} [\bar{d}\gamma^\mu P_Rd] [\bar{\ell}\gamma_\mu P_L\ell]$$

from tree level φ exchange and fierzing.

In terms of the usual Wilson coefficients:

$$C_{10}^{\prime e} = -C_9^{\prime e} = \frac{\lambda_{se}\lambda_{be}^*}{V_{tb}V_{ts}^*} \frac{\pi}{\alpha_e} \frac{\sqrt{2}}{4M^2G_F} = -\frac{\lambda_{se}\lambda_{be}^*}{2M^2} (24\text{TeV})^2$$

R_K -benchmark: $C_9^{\prime e} = -C_{10}^{\prime e} \simeq 1/2$ follows $M^2/\lambda_{se}\lambda_{be}^* \simeq (24\text{TeV})^2$

Viable parameters of the (scalar) leptoquarks read

$$1 \text{ TeV} \lesssim M \lesssim 48 \text{ TeV}$$

$$2 \cdot 10^{-3} \lesssim |\lambda_{se} \lambda_{be}^*| \lesssim 4$$

$$4 \cdot 10^{-4} \lesssim |\lambda_{qe}| \lesssim 5$$

- $SU(2)$ implies corresponding effects in $b \rightarrow s\nu\nu$ (only electron-neutrinos affected, signal diluted over 3 species).
 $\mathcal{B}(B \rightarrow K\nu\nu)$ reduced by 5 %, $\mathcal{B}(B \rightarrow K^*\nu\nu)$ enhanced by 5 %, F_L enhanced by 2 % w.r.t SM.
- Further correlation with B_s mixing, $b \rightarrow s\gamma$, and direct searches.
- Decay modes of φ -doublet: $\varphi^{2/3} \rightarrow b e^+$, $\varphi^{-1/3} \rightarrow b \nu$

see talks by Ilja Dorsner and Sacha Davidson for LHC pheno

A LL muon leptoquark model

see talk by Marco Nardeccia

$$\mathcal{L} = -\lambda_{b\mu} \varphi^* q_3 \ell_2 - \lambda_{s\mu} \varphi^* q_2 \ell_2, \quad \varphi(3, 3)_{-1/3}$$

$$\mathcal{H}_{\text{eff}} = -\frac{\lambda_{s\mu}^* \lambda_{b\mu}}{M^2} \left(\frac{1}{4} [\bar{q}_2 \tau^a \gamma^\mu P_L q_3] [\bar{\ell}_2 \tau^a \gamma_\mu P_L \ell_2] + \frac{3}{4} [\bar{q}_2 \gamma^\mu P_L q_3] [\bar{\ell}_2 \gamma_\mu P_L \ell_2] \right)$$

gives $C_9^{\text{NP}\mu} = -C_{10}^{\text{NP}\mu} = \frac{\pi}{\alpha_e} \frac{\lambda_{s\mu}^* \lambda_{b\mu}}{V_{tb} V_{ts}^*} \frac{\sqrt{2}}{2M^2 G_F} \simeq -0.5$ and similar mass range as other model.

Decay modes of φ -triplet:

$$\begin{aligned} \varphi^{2/3} &\rightarrow t \nu \\ \varphi^{-1/3} &\rightarrow b \nu, t \mu^- \\ \varphi^{-4/3} &\rightarrow b \mu^- \end{aligned}$$

The $U(1)_{\tau-\mu}$ -extension of SM [1403.1269 Altmannshofer et al](#) also violates lepton-universality. (V,A-muons-type i) model, no BSM in ee .)

see talks by Andreas Crivellin, and connecting to dark sector, Avelino Vicente

C (LH-quark currents) versus C' (RH quark currents)?

Long story in interpreting $B \rightarrow K^{(*)} \mu\mu$ data/global fits as hadronic uncertainties (power corrections, resonances) could shadow BSM.

e.g. Camalich, Jäger '12, Lyon, Zwicky'14, .. in global fits 1307.5683, 1308.1501, 1310.2478, ...

$$0.7 \lesssim -\text{Re}[C_{LL}^{\mu} + C_{RL}^{\mu} - (C_{LL}^e + C_{RL}^e)] \lesssim 1.5 . \quad (R_K)$$

Diagnosing lepton-nonuniversality

By parity and lorentz invariance, C, C' enter decay amplitudes
 $B \rightarrow K \ell \ell$ etc as [GH, Schmaltz 1411.4773](#)

$$C + C' : K, K_{\perp}^*, \dots$$

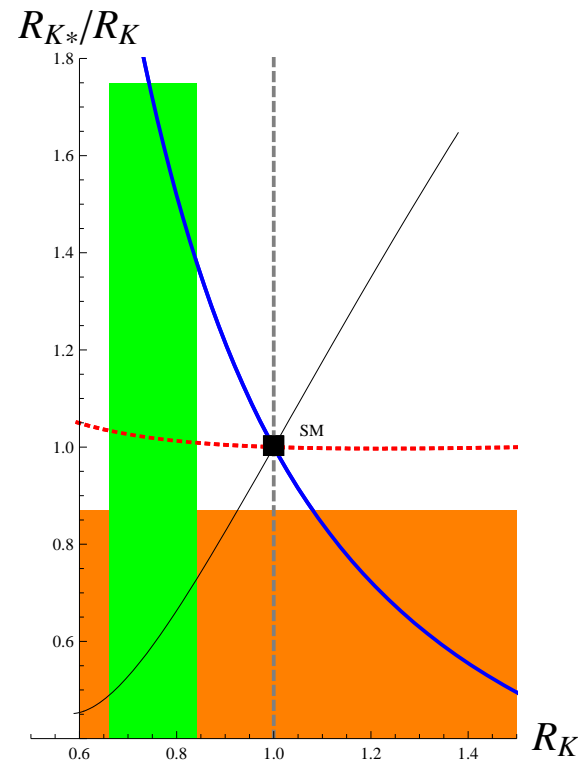
$$C - C' : K_0(1430), K_{0,\parallel}^*, \dots$$

so different ratios R_K, R_{K^*} etc are complementary. It follows that double ratios R_{K^*}/R_K are cleanly probing right-handed currents! In addition, since K^* is dominated by '0' and '||' polarization, the complementarity between R_K and R_{K^*} (similarly R_{φ}) is maximal.

predictions: $R_K = R_{\eta}$, $R_{K^*} = R_{\varphi}$, and correlations between R_H .
Measure two R_H (with $C \pm C'$) and predict all of them !

see talk by Wolfgang Altmannshofer

Diagnosing lepton-nonuniversality



Green band: R_K 1 sigma LHCb. Curves: different BSM scenarios. red dashed: pure C_{LL} . Black solid: $C_{LL} = -2C_{RL}$. Blue: C_{RL} . Orange band is prediction for R_{K^*} (not significantly measured) based on R_K and $B \rightarrow X_s \ell \ell$: $R_{X_s}^{\text{Belle}'09} = 0.42 \pm 0.25$, $R_{X_s}^{\text{BaBar}'13} = 0.58 \pm 0.19$.

Diagnosing quark and lepton flavor

Given the breakdown of lepton-universality, chances are that generically there is lepton flavor violation, too arXiv:1411.0565.

Explaining R_K with muons and electrons requires theory of flavor. That's an opportunity— given a signal— to access origin of flavor arXiv:1503.01084

Leptoquark coupling matrix: $\lambda \equiv \begin{pmatrix} \lambda_{de} & \lambda_{d\mu} & \lambda_{d\tau} \\ \lambda_{se} & \lambda_{s\mu} & \lambda_{s\tau} \\ \lambda_{be} & \lambda_{b\mu} & \lambda_{b\tau} \end{pmatrix}$

Well-motivated ansatz: use $U(1)$ -flavor-symmetry for quarks and non-abelian one e.g. A_4 for leptons and assume Higgs to be uncharged. Predicts generically hierarchies for quarks and "zeros"

Diagnosing quark and lepton flavor

and "ones" for leptons. Explicit realizations include

$$\text{Single lepton flavor } \lambda^{[e]} \equiv \begin{pmatrix} \lambda_{de} & 0 & 0 \\ \lambda_{se} & 0 & 0 \\ \lambda_{be} & 0 & 0 \end{pmatrix}, \quad \lambda^{[\mu]} \equiv \begin{pmatrix} 0 & \lambda_{d\mu} & 0 \\ 0 & \lambda_{s\mu} & 0 \\ 0 & \lambda_{b\mu} & 0 \end{pmatrix}$$

$$\text{hierarchy: } \lambda^{[\rho\kappa]} \sim \lambda_0 \begin{pmatrix} \rho_d \kappa & \rho_d & \rho_d \\ \rho \kappa & \rho & \rho \\ \kappa & 1 & 1 \end{pmatrix}$$

constraints: $\rho_d \lesssim 0.02$, $\kappa \lesssim 0.5$, $10^{-4} \lesssim \rho \lesssim 1$, $\kappa/\rho \lesssim 0.5$, $\rho_d/\rho \lesssim 1.6$

predictions:

$$\mathcal{B}(B \rightarrow K \mu^\pm e^\mp) \simeq 3 \cdot 10^{-8} \kappa^2 \left(\frac{1 - R_K}{0.23} \right)^2, \quad (1)$$

$$\mathcal{B}(B \rightarrow K e^\pm \tau^\mp) \simeq 2 \cdot 10^{-8} \kappa^2 \left(\frac{1 - R_K}{0.23} \right)^2, \quad (2)$$

$$\mathcal{B}(B \rightarrow K \mu^\pm \tau^\mp) \simeq 2 \cdot 10^{-8} \left(\frac{1 - R_K}{0.23} \right)^2, \quad (3)$$

and

$$\mathcal{B}(\mu \rightarrow e\gamma) \simeq 2 \cdot 10^{-12} \frac{\kappa^2}{\rho^2} \left(\frac{1 - R_K}{0.23} \right)^2, \quad (4)$$

$$\mathcal{B}(\tau \rightarrow e\gamma) \simeq 4 \cdot 10^{-14} \frac{\kappa^2}{\rho^2} \left(\frac{1 - R_K}{0.23} \right)^2, \quad (5)$$

$$\mathcal{B}(\tau \rightarrow \mu\gamma) \simeq 3 \cdot 10^{-14} \frac{1}{\rho^2} \left(\frac{1 - R_K}{0.23} \right)^2, \quad (6)$$

$$\mathcal{B}(\tau \rightarrow \mu\eta) \simeq 4 \cdot 10^{-11} \rho^2 \left(\frac{1 - R_K}{0.23} \right)^2. \quad (7)$$

asymmetric branching ratios:

$$\frac{\mathcal{B}(B_s \rightarrow \ell^+ \ell'^-)}{\mathcal{B}(B_s \rightarrow \ell^- \ell'^+)} \simeq \frac{m_\ell^2}{m_{\ell'}^2}. \quad \text{Left-handed leptons only} \quad (8)$$

$$\frac{\mathcal{B}(B_s \rightarrow \mu^+ e^-)}{\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}}} \simeq 0.01 \kappa^2 \cdot \left(\frac{1 - R_K}{0.23} \right)^2, \quad (9)$$

$$\frac{\mathcal{B}(B_s \rightarrow \tau^+ e^-)}{\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}}} \simeq 4 \kappa^2 \cdot \left(\frac{1 - R_K}{0.23} \right)^2, \quad (10)$$

$$\frac{\mathcal{B}(B_s \rightarrow \tau^+ \mu^-)}{\mathcal{B}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}}} \simeq 4 \cdot \left(\frac{1 - R_K}{0.23} \right)^2, \quad (11)$$

- If LHCb's measurement of R_K substantiates it implies that there is more difference between a muon and an electron than their mass. Lepton-universality, a feature of the $SU(3)_C \times SU(2)_L \times U(1)_Y$ SM appears to be violated in $b \rightarrow s$ FCNC transitions.
- Current data allow for model-independent explanations, as well as model frameworks such as leptoquarks, with $M \lesssim 50$ TeV. There is no conflict with other measurements nor with model-building.
- Explanations imply correlations with other FCNC processes including LFV as well as predictions for direct searches, that can be tested in the future.