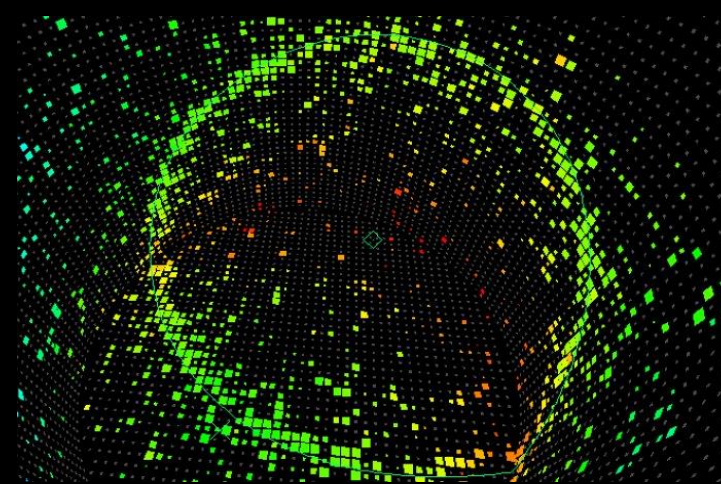
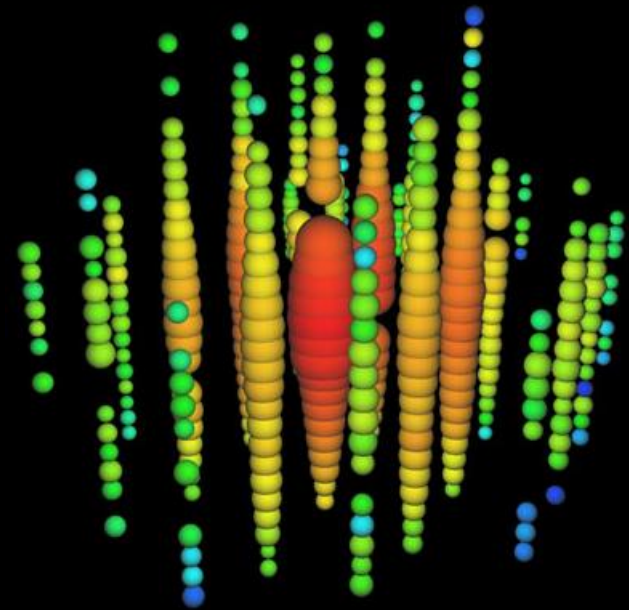


Neutrino properties

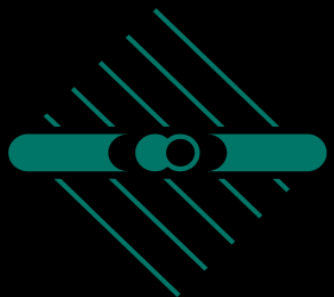
Mass hierarchy and

CP-violation



A. Yu. Smirnov

*Max-Planck Institute for Nuclear Physics,
Heidelberg, Germany
& ICTP*



Outline

1. Neutrino properties
2. Mass hierarchy
3. CP-violation
4. Summary

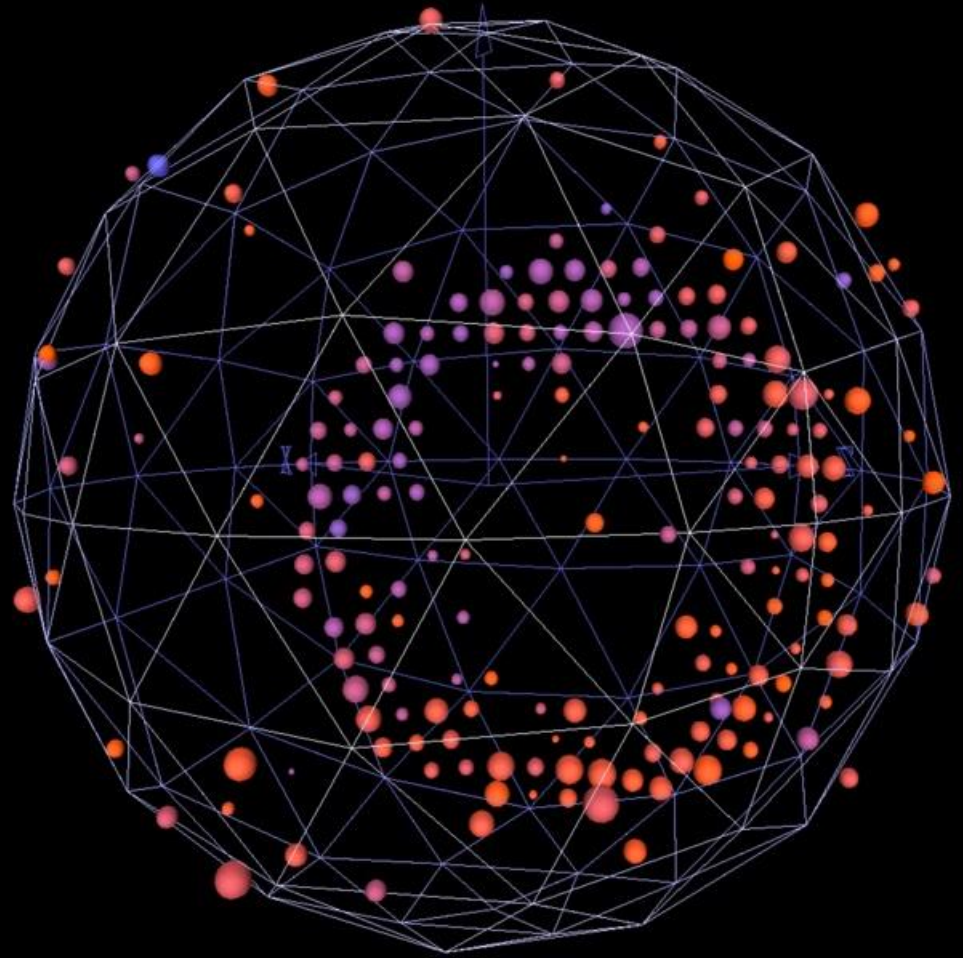
Brief summary of what we know

Next big in neutrino physics?

Ultimate goal; connected to mass hierarchy determination

with emphasis on astrophysical/astroparticle methods

Neutrino properties

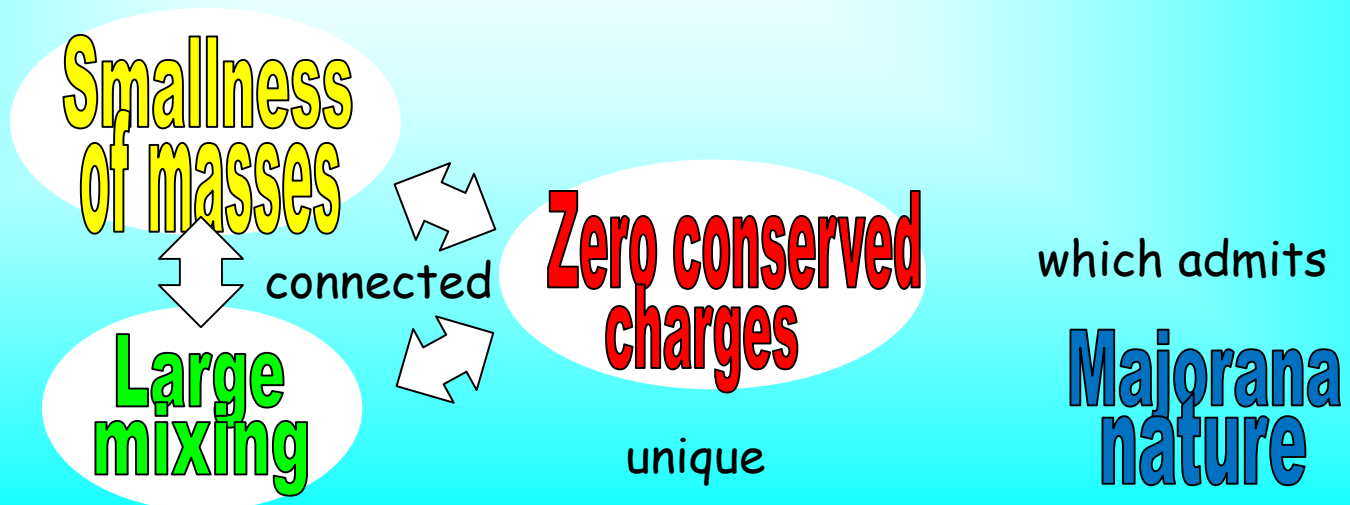


3ν paradigm:

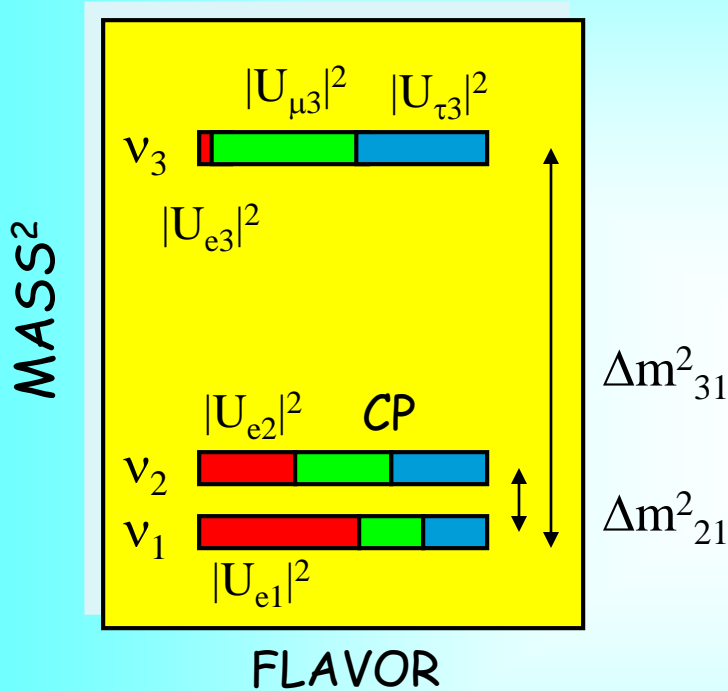
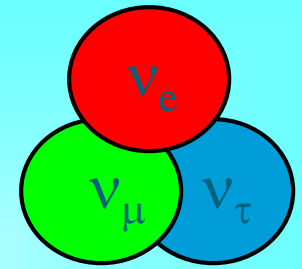
All well established/confirmed results fit well a framework with

- three neutrinos
- interactions described by the standard model
 - with masses and mixing

It is widely believed that peculiar properties



Lepton Mixing



Normal mass hierarchy

$$\Delta m_{ij}^2 = m_i^2 - m_j^2$$

$$\Delta m_{32}^2 = 2.5 \times 10^{-3} \text{ eV}^2$$

$$\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2$$

Mixing parameters

$$\tan^2 \theta_{12} = |U_{e2}|^2 / |U_{e1}|^2 \quad \sim 1/2$$

$$\sin^2 \theta_{13} = |U_{e3}|^2 \quad = 0.022$$

$$\tan^2 \theta_{23} = |U_{\mu 3}|^2 / |U_{\tau 3}|^2 \quad \sim 1.0$$

Mixing matrix:

$$\nu_f = U_{\text{PMNS}} \nu_{\text{mass}}$$

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U_{\text{PMNS}} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Standard parametrization

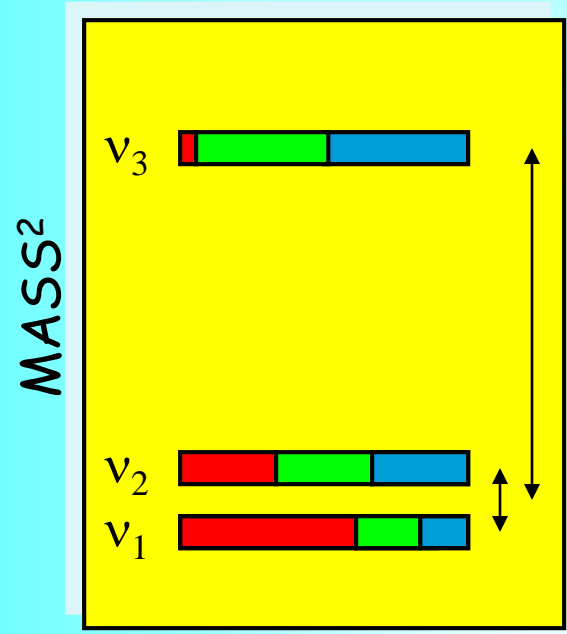
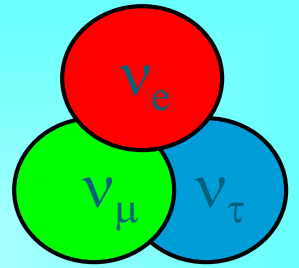
$$U_{\text{PMNS}} = U_{23} I_\delta U_{13} I_{-\delta} U_{12}$$

$$I_\delta = \text{diag}(1, 1, e^{i\delta})$$

TBM,
Symmetry?

CP-phase

Neutrino mass ordering

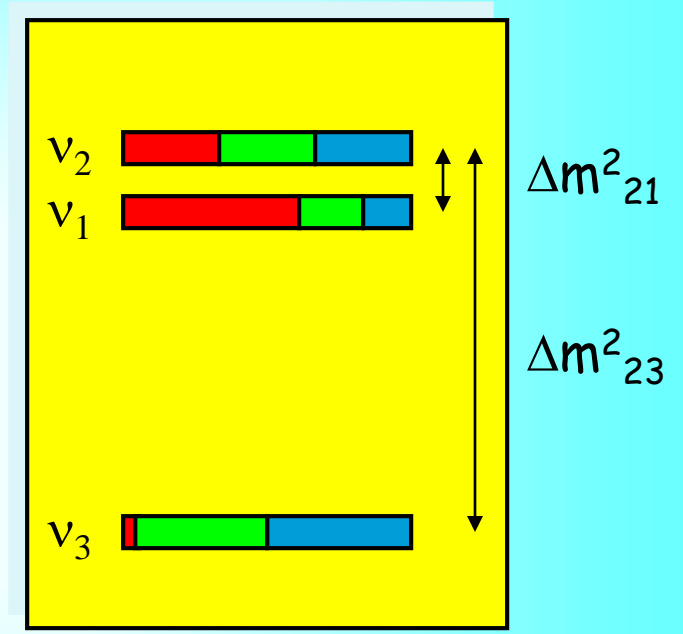


Fixed by solar neutrinos

Normal mass hierarchy

$$\Sigma m > m_h$$

$$|\Delta m^2_{31}| = |\Delta m^2_{32}| + |\Delta m^2_{21}|$$



Inverted mass hierarchy

$$\Sigma m > 2 m_h$$

$$|\Delta m^2_{31}| = |\Delta m^2_{32}| - |\Delta m^2_{21}|$$

$$|\Delta m^2_{ij}| \leftrightarrow D_{ij} = 4|U_{ei}|^2|U_{ej}|^2$$

mass splittings

oscillation depth

TBM Mixing pattern

P. F. Harrison, D. H. Perkins, W. G. Scott

L. Wolfenstein

$$U_{\text{tbm}} = \begin{pmatrix} \sqrt{2/3} & \sqrt{1/3} & 0 \\ -\sqrt{1/6} & \sqrt{1/3} & -\sqrt{1/2} \\ -\sqrt{1/6} & \sqrt{1/3} & \sqrt{1/2} \end{pmatrix}$$

0.15
0.62
0.78

$$U_{\text{tbm}} = U_{23}(\pi/4) U_{12}$$

$$\sin^2 \theta_{12} = 1/3$$

0.30-0.31

Accidental, numerology,
useful for bookkeeping

Accidental symmetry
(still useful)

There is no relation of mixing
with masses (mass ratios)

Not accidental

Lowest order approximation
which corresponds to weakly
broken (flavor) symmetry
of the Lagrangian

with some other physics
and structures associated

Parameters look like C-G coefficients

Global oscillation fit

Solar
neutrinos

KamLAND

Atmospheric
neutrinos

Double Chooz

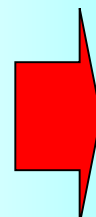
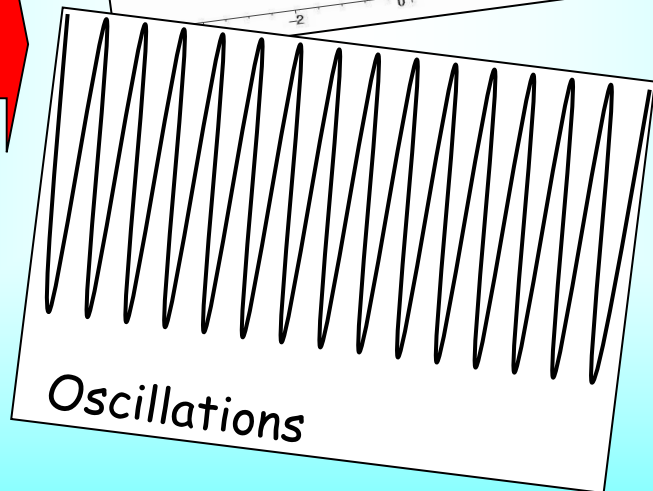
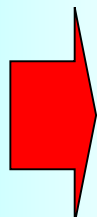
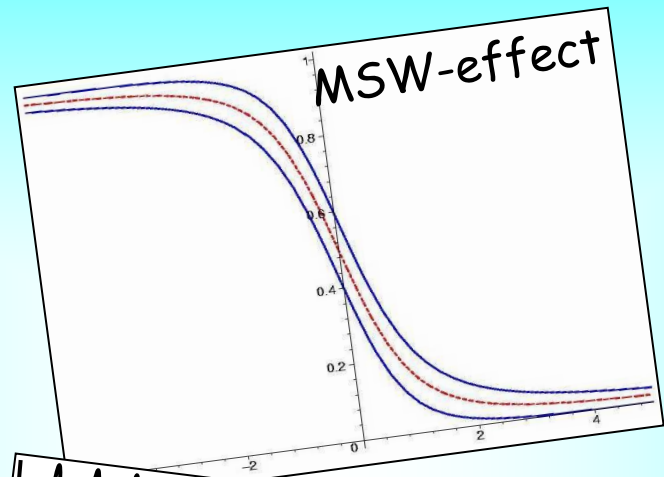
Daya Bay

MINOS

K2K RENO

T2K Antares

DeepCore



$$\Delta m^2$$
$$\theta$$

Can be resonantly
enhanced in matter

Global 3ν - fit

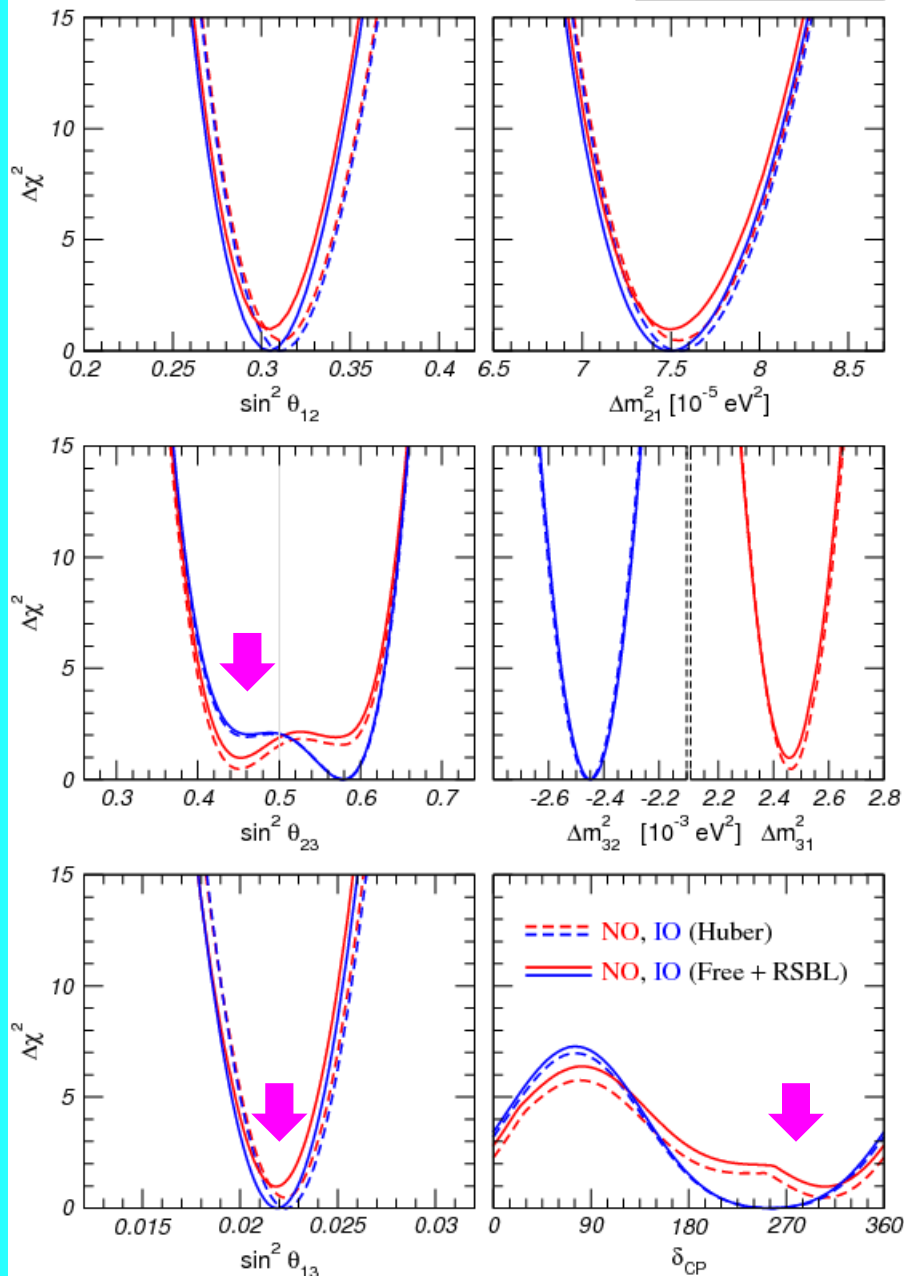
M.C. Gonzalez-Garcia, M. Maltoni,
T. Schwetz, JHEP 1411 (2014)
052,1409.5439 [hep-ph]

2-3 mixing:

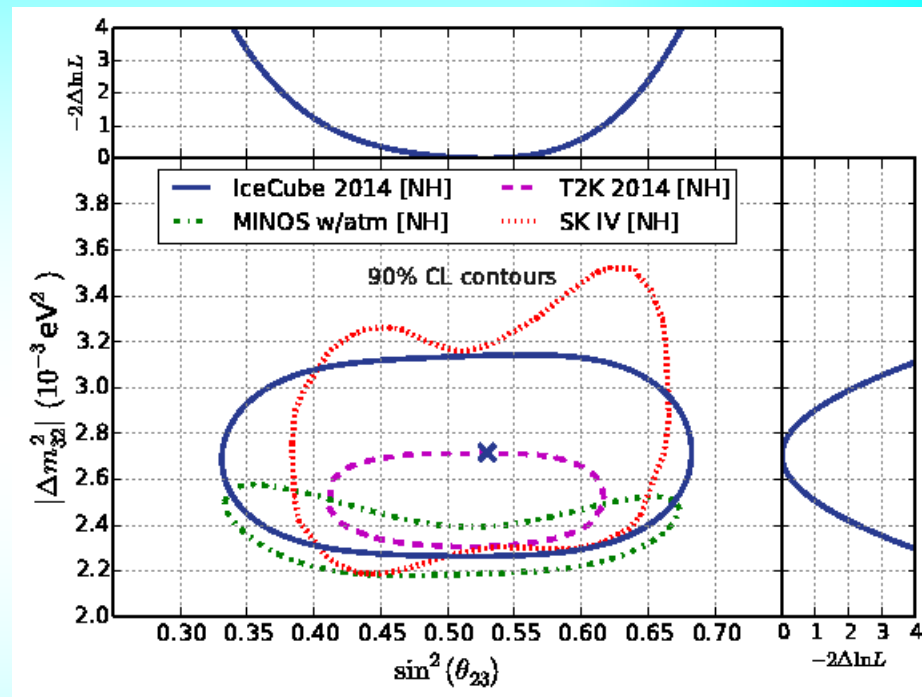
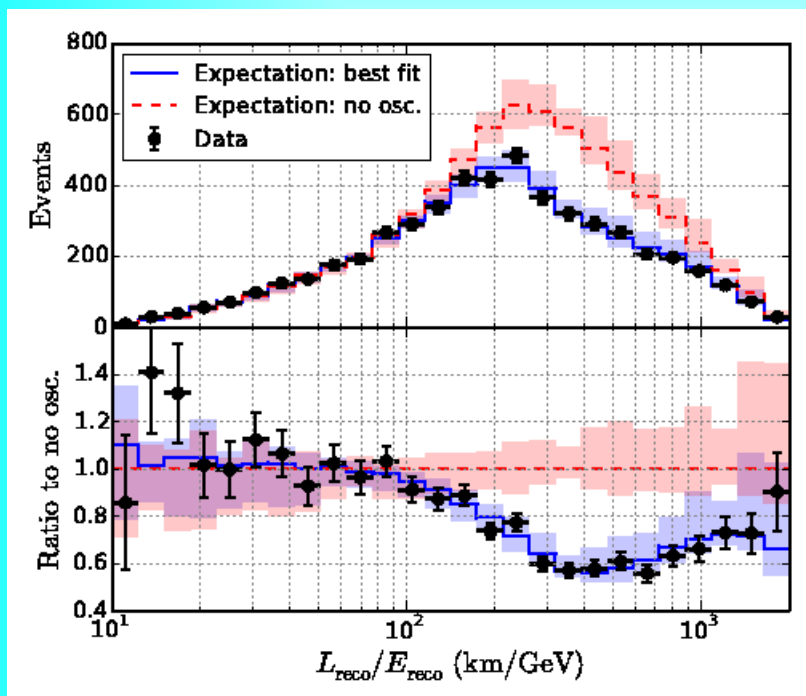
asymmetric for NO and IO
 $\sin^2\theta_{23} = 0.45$ (NO), $= 0.58$ (IO)

Small preference IO and
2nd quadrant

NuFIT 2.0 (2014)



DeepCore oscillation result



atmospheric ν_μ disappearance,
3 years of data

IceCube Collaboration
(M.G. Aartsen *et al.*)
arXiv:1410.7227 [hep-ex] |

$$\Delta m_{32}^2 = (2.72 +0.19/-0.20) 10^{-3} \text{ eV}^2$$
$$\sin^2 \theta_{23} = 0.53 +0.09/-0.12 \quad (\text{NO})$$

compatible and comparable in precision
with accelerator experiments

Neutrino mass scale

Oscillations:

The heaviest neutrino

$$m_h \gtrsim \sqrt{\Delta m_{31}^2} > 0.045 \text{ eV}$$

$$\frac{m_2}{m_3} \gtrsim \sqrt{\frac{\Delta m_{21}^2}{\Delta m_{32}^2}} = 0.18$$

the weakest mass hierarchy, related to large mixing

Cosmology:

$$\Sigma m < 0.136 \text{ eV (95 \% CL) Planck 2015 + BAO+ HST}$$

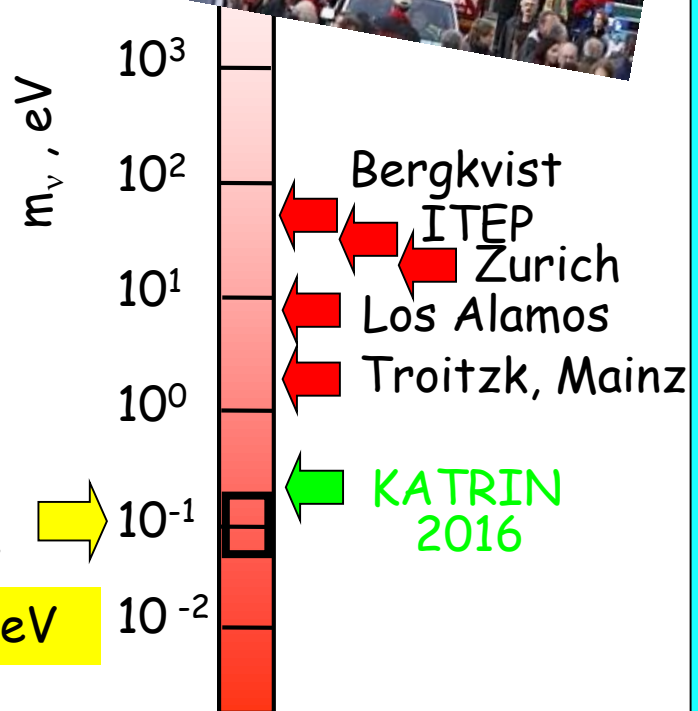
E. Di Valentino, et al
1507.08665 [astro-ph.CO]

$$\Sigma m < (0.3 - 0.4) \text{ eV (95 \% CL)}$$

conservative

Oscillations, & cosmology

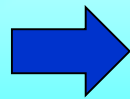
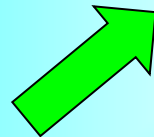
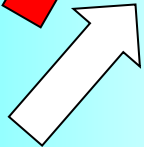
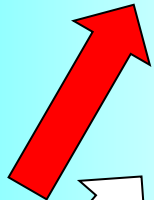
$$m_h \sim (0.045 - 0.10) \text{ eV}$$



Scales of new physics

m_ν

Spurious scale?



GUT - Planck
mass

28 orders of magnitude

$$\frac{V_{EW}^2}{m_\nu}$$

PeV

Electroweak -
LHC

eV-
sub-eV

Neutrino mass itself is the fundamental scale of new physics

High scale seesaw
Quark- lepton
symmetry /analogy
GUT

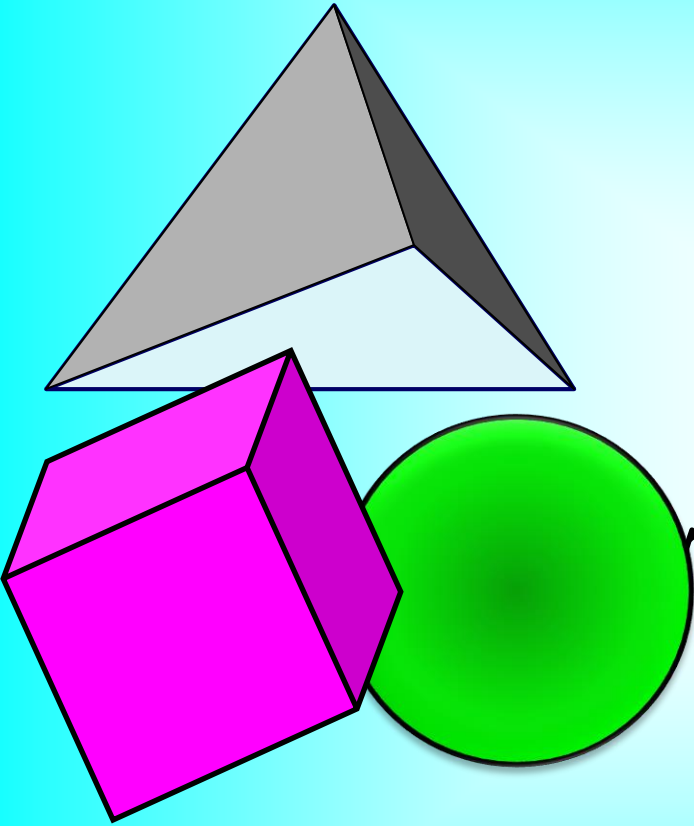
Low scale seesaw,
radiative
mechanisms, RPV,
high dimensional
operators

Scale of neutrino
masses themselves
Relation to dark
energy, MAVAN?

Mixing

- Not much to add
- String landscape
- Multiverse?

from symmetry
to anarchy and
randomness



Complicated constructions,
especially if quarks are
included



PMNS & CKM

Quark
mixing

my prejudice

C. Giunti, M. Tanimoto

H. Minakata, A Y S

Z - Z. Xing

J Harada

S Antusch, S. F. King

Y Farzan, A Y S

M Picariello, ...

$$U_{\text{PMNS}} = U_{\text{CKM}} + U_X$$

where $U_{\text{CKM}} \sim V_{\text{CKM}}$

has similar hierarchical structure
determined by powers of

$$\lambda = \sin \theta_c$$

From the Dirac matrices of
charged leptons and neutrinos

Prediction for
the 1-3 mixing

$$\sin^2 \theta_{13} = \sin^2 \theta_{23} \sin^2 \theta_c (1 + O(\lambda^2))$$

$$\sin^2 \theta_{13} \sim \frac{1}{2} \sin^2 \theta_c$$

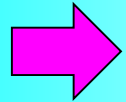
in a good
agreement with
measurements

 U_X has some special form
determined by symmetry
related to mechanism
that explains smallness of
neutrino mass

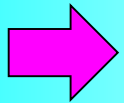
$$U_X \sim U_{23}(\pi/4) U_{12}$$

What does this mean?

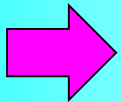
if not
accidental



Quarks and leptons know about each other,
Q L unification, GUT or/and
Common flavor symmetries



Some additional physics is involved in the lepton sector
which explains smallness of neutrino mass and difference
of the quark and lepton mixing patterns



Two types of new physics

CKM

Neutrino new
physics

Indicates $SO(10)$: no CKM mixing
in the first approximation

Challenges and Anomalies

Determination of unknowns within 3ν paradigm

Mass hierarchy/ordering

Absolute values of masses, type of spectrum

CP-violation phase(s)

Nature of neutrino mass: (Majorana-Dirac, hard - soft (effective))

Checks of Anomalies and their explanations

Reactor, Gallium source

Deficit of signal

LSND, MiniBooNE

Excess of signal

1 eV sterile neutrino: not a small perturbation of the 3ν picture

IceCube

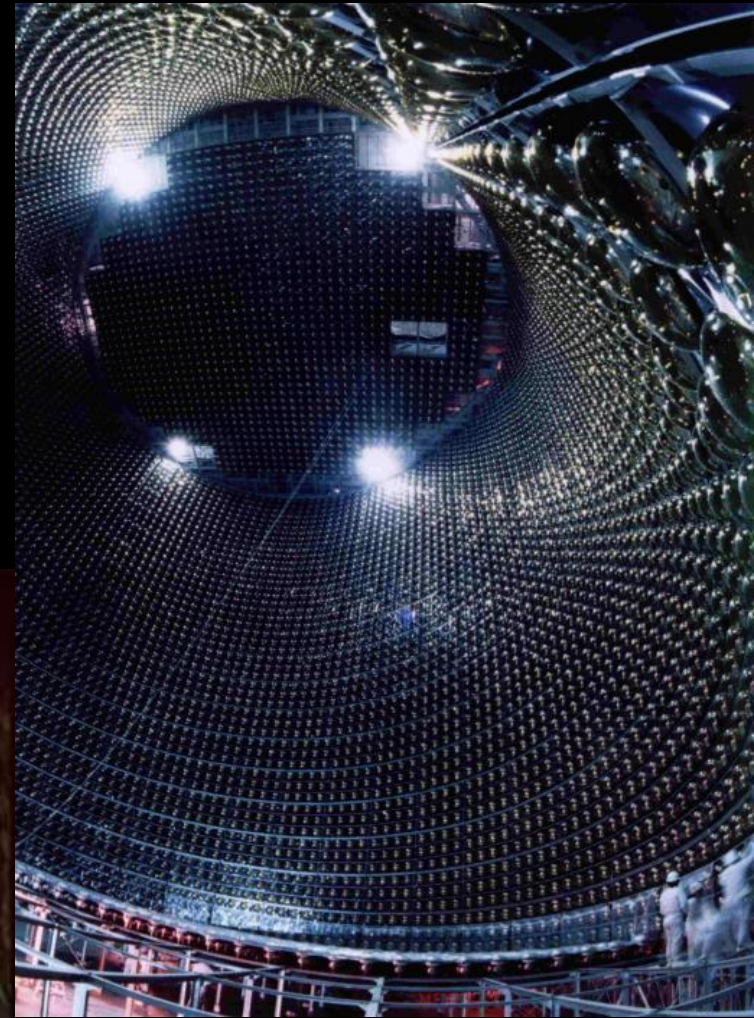
High sensitivity to steriles

Solar neutrino anomaly?

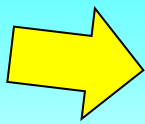
Absence of spectral upturn, large DN asymmetry

steriles? NSI?

Mass hierarchy



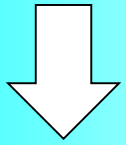
Mass hierarchy



Further advance

Step to discover CP

important by itself



Theoretical implications



Phenomenology

Supernova neutrinos

Atmospheric neutrinos

$b\bar{b}0n$ decay

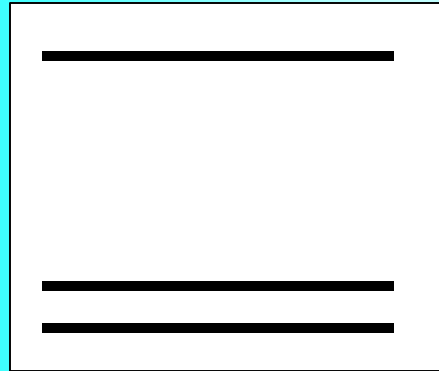
LBL

Solar neutrinos

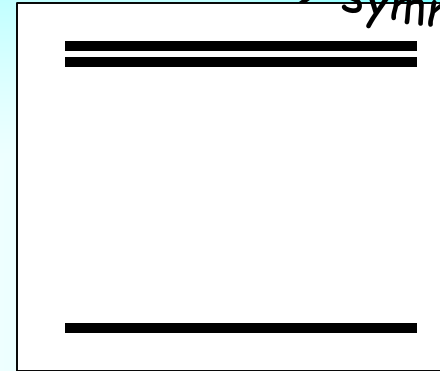
Cosmology

Theoretical implications

generically



Normal vs. special



Quasi-degenerate
→ symmetry

$$\frac{m_2}{m_3} \sim \sqrt{\frac{\Delta m_{21}^2}{\Delta m_{32}^2}} = 0.18$$

$$\theta \sim \sqrt{\frac{m_2}{m_3}}$$

the weakest hierarchy

Similar to quark spectrum

rescaling

See-saw

Quark-lepton symmetry

Unification

$$\frac{\Delta m}{m} \sim \frac{\Delta m_{21}^2}{2 \Delta m_{32}^2} = 1.6 \cdot 10^{-2}$$

but 1-2 mixing strongly deviates from maximal

Pseudo-Dirac + 1 Majorana

Flavor symmetries

Broken $L_e - L_\mu - L_\tau$ symmetry

Race for mass hierarchy

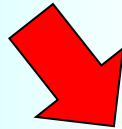
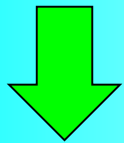
Matter effect
on 1-3 mixing
Oscillations, conversion

Precise measurements
of Δm^2
at reactors

Cosmology

JUNO,
RENO-50

Σm
Double beta decay
 m_{ee}



Atmospheric neutrinos

LBL experiments

Supernova neutrinos

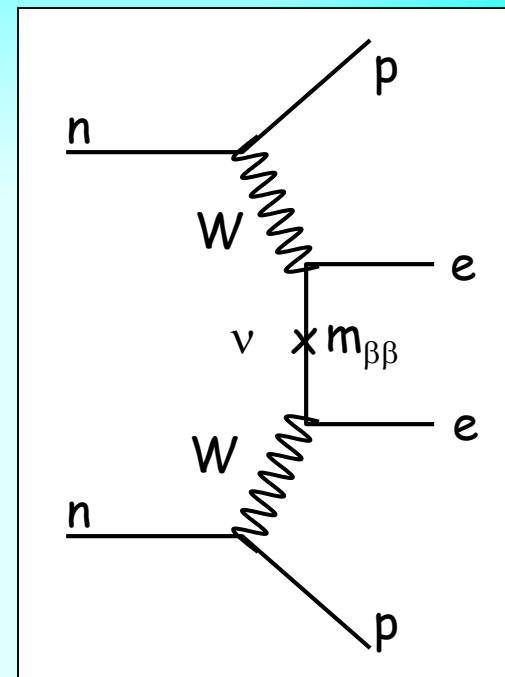
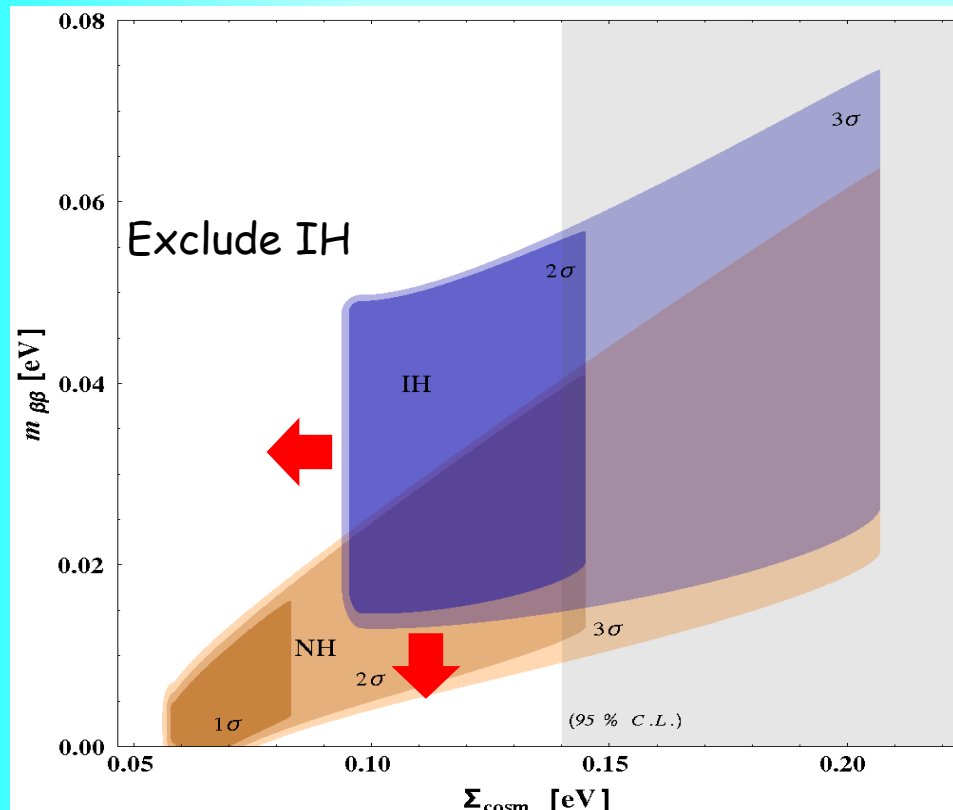
Earth matter effects,
energy spectra

PINGU
ORCA
INO

NOvA
LBNF - DUNE
JPARC-HK

Double beta decay

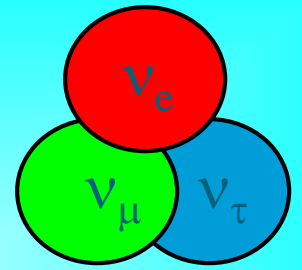
$$m_{\beta\beta} = U_{e1}^2 m_1 + U_{e2}^2 m_2 e^{i\alpha} + U_{e3}^2 m_3 e^{i\phi}$$



*S. Dell'Oro, et al,
1505.02722 [hep-ph]*

Constraints from cosmological surveys and from oscillations.
 The 1 σ region for the IH case is not present at this confidence level.
 The grey band is the 95% C.L. excluded region coming from Cosmology

Flavor in matter



Density increase \rightarrow

Normal mass hierarchy, neutrinos

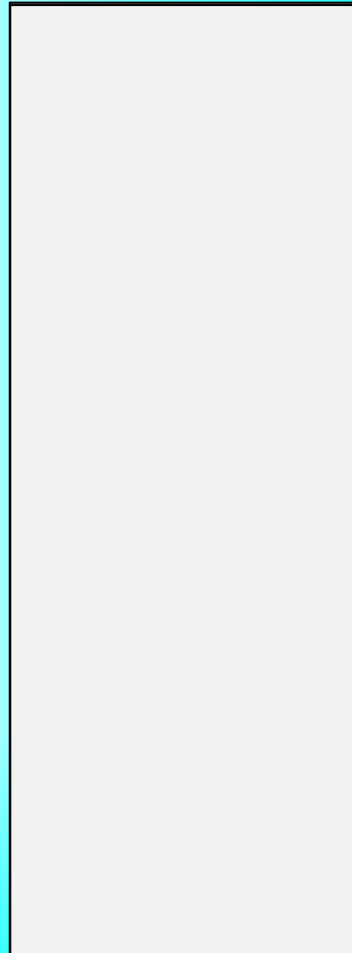
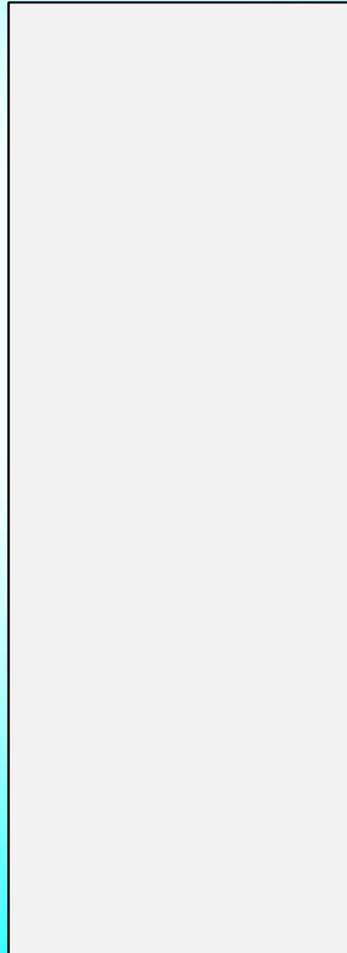
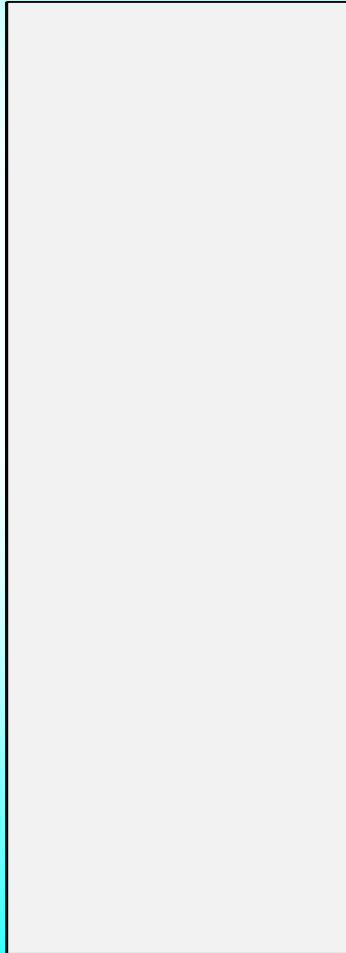
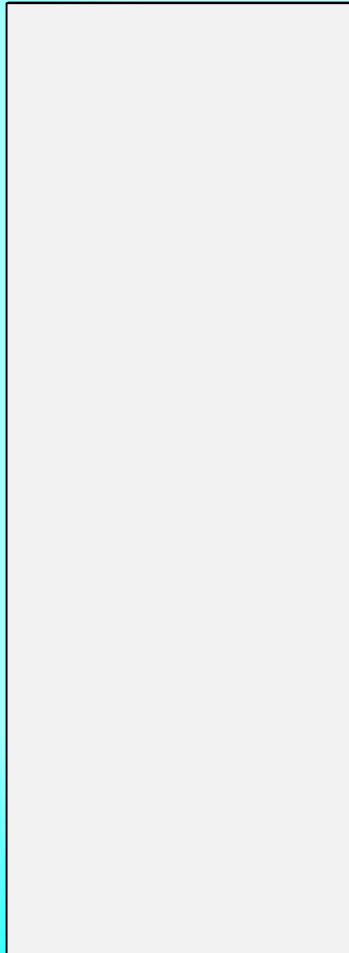
ν_{3m}



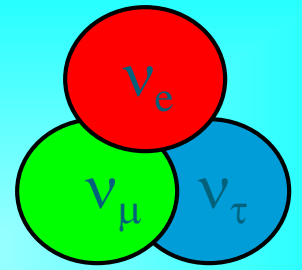
ν_{2m}



ν_{1m}

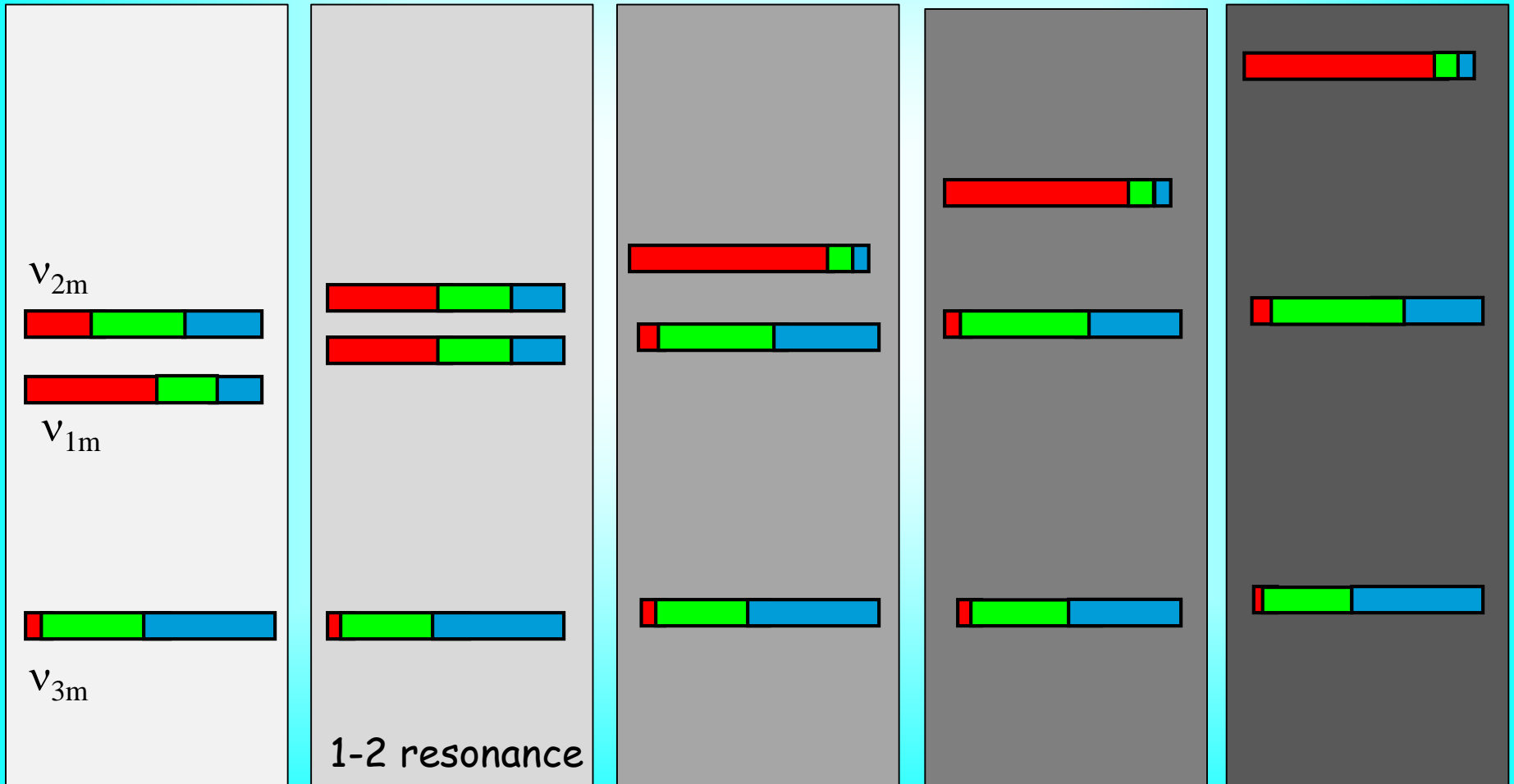


Flavor in matter

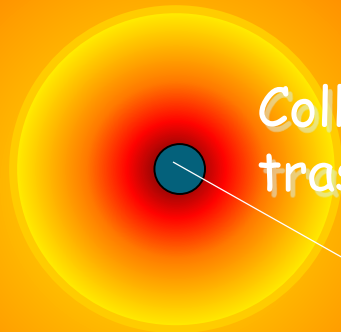


Density increase →

Inverted mass hierarchy, neutrinos



Supernova neutrinos



Collective flavor transformation

Shock wave effect on conversion

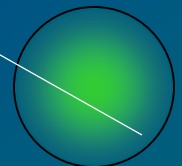
MSW flavor conversion inside the star

Propagation in vacuum

Oscillations inside the Earth

With known 1-3 mixing all MSW transitions are adiabatic

All these effects depend on the type of mass hierarchy



Hierarchy affects

Time rise of the anti- ν_e burst
initial phase: fast \rightarrow IH *P. Serpico et al*

Strong suppression of
the ν_e peak \rightarrow NH

$$\nu_e \rightarrow \nu_3$$

Permutation of the electron and
non-electron neutrino spectra

Earth matter effects

*A. Dighe, A. S.
C. Lunardini*

Shock wave
effect

in neutrino
channels \rightarrow NH
in antineutrino
 \rightarrow IH

*G. Fuller, et al
R. Tomas et al*

Neutrino
collective
effects

Different for IH
and NH cases;
spectral splits
at high energies
 \rightarrow IH

*G. Fuller, et al
B. Dasgupta, et al*

in the antineutrino
channel only \rightarrow NH

in the neutrino
channel only \rightarrow IH

If the earth matter effect is
observed for antineutrinos
NH is established!

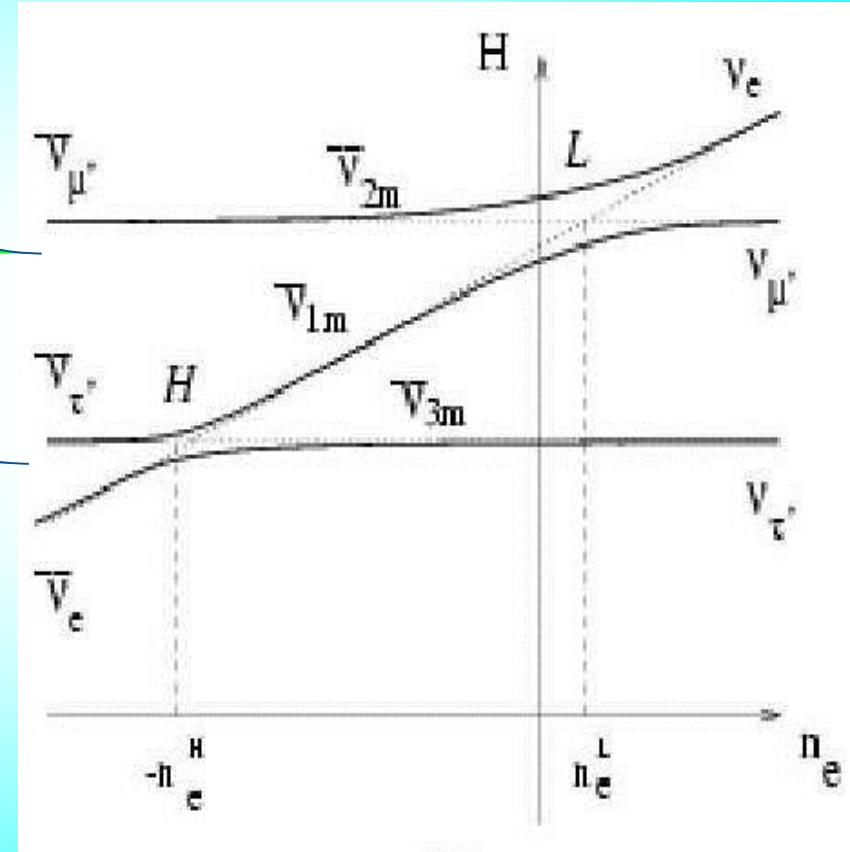
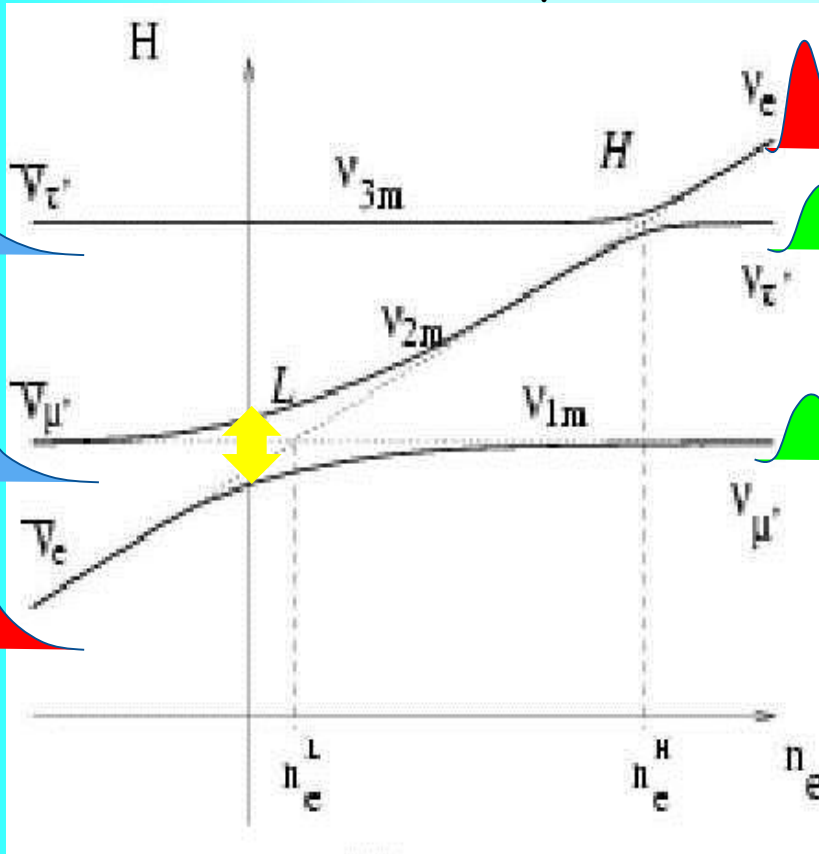
Earth matter effect and hierarchy

Adiabatic evolution

Level crossings

Normal hierarchy

Inverted hierarchy



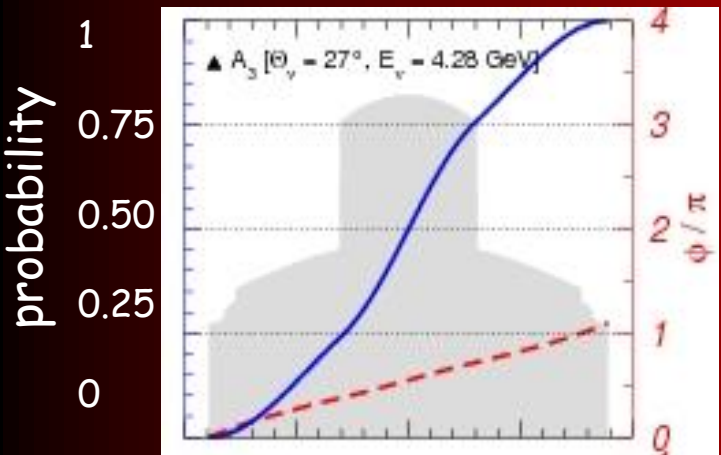
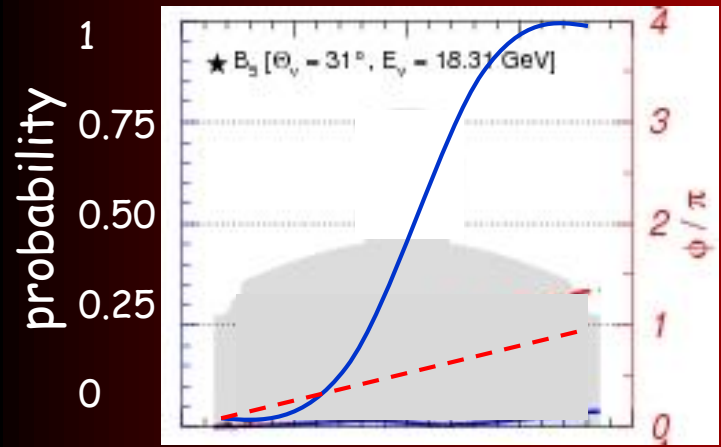
No Earth matter effect provided that initial fluxes of $\nu_{\mu'}$ and $\nu_{\tau'}$ are identical

Collective effects and shock waves may change this.

Atmospheric neutrinos

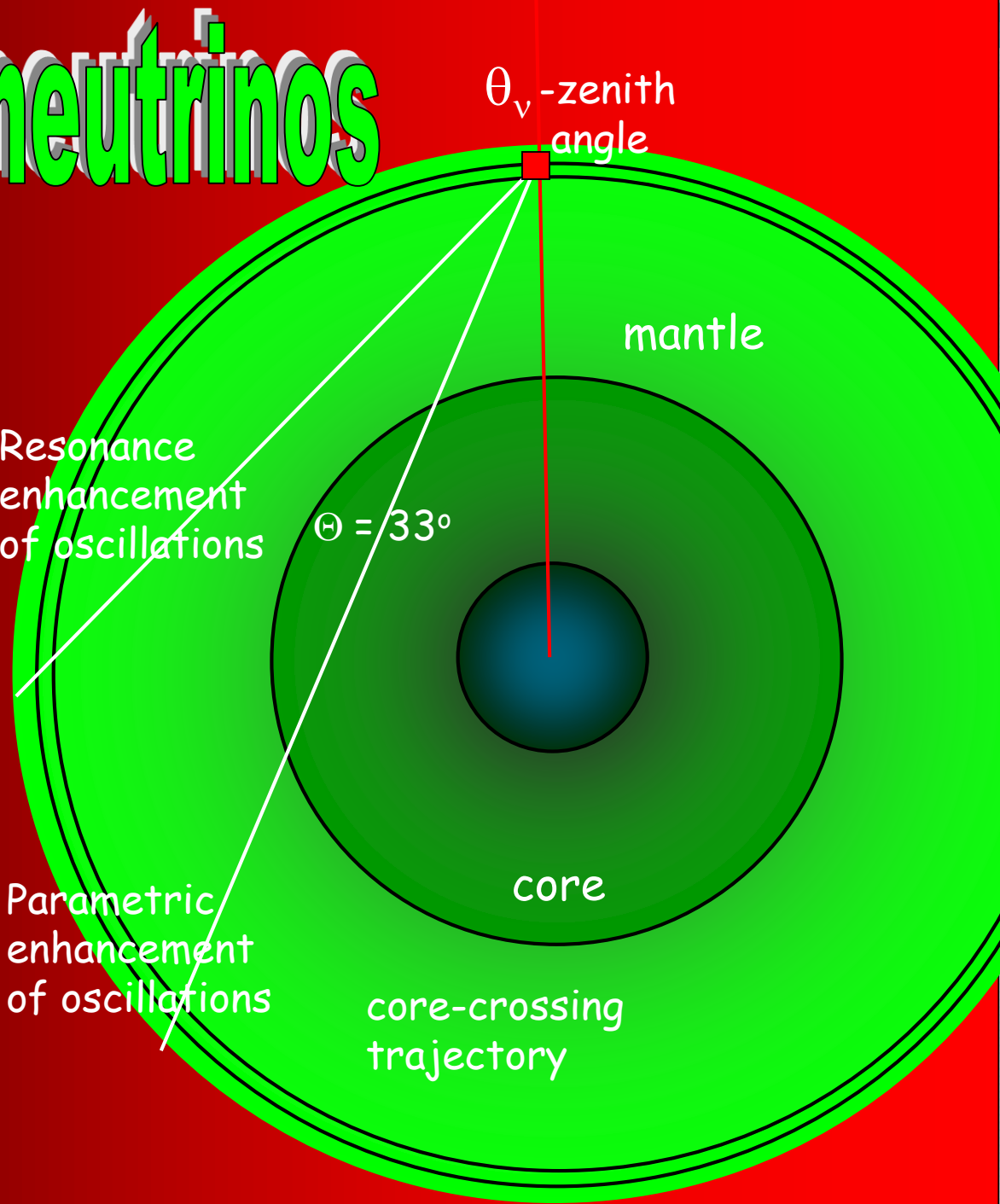
Oscillations in the Earth

$$\nu_e \rightarrow \nu_\mu, \nu_\tau$$



Resonance enhancement of oscillations

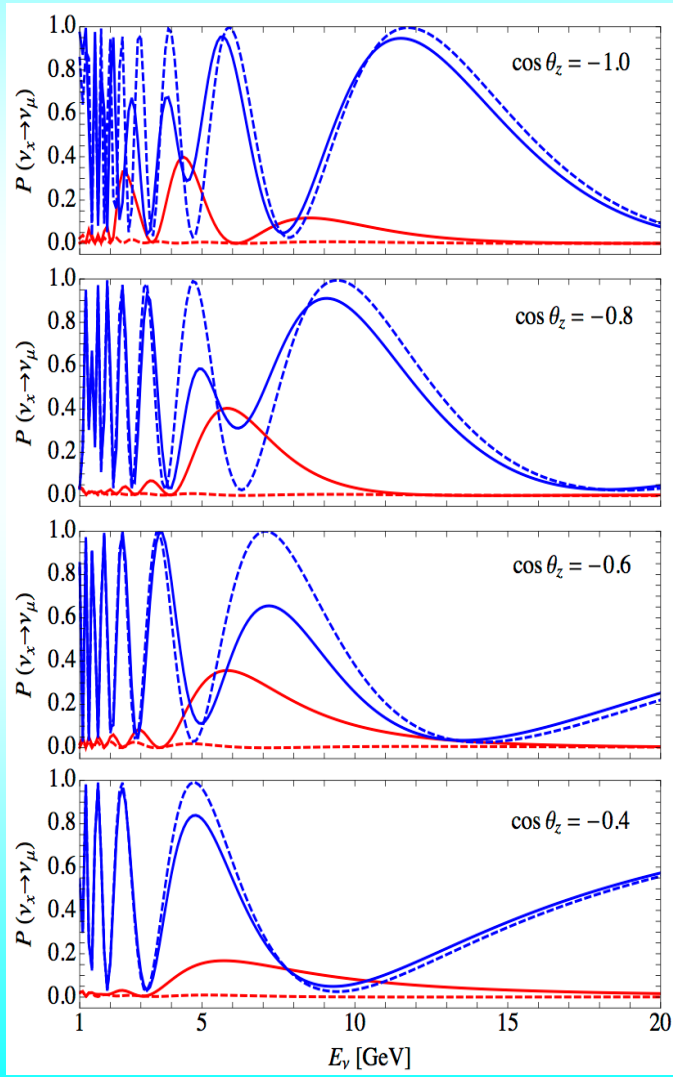
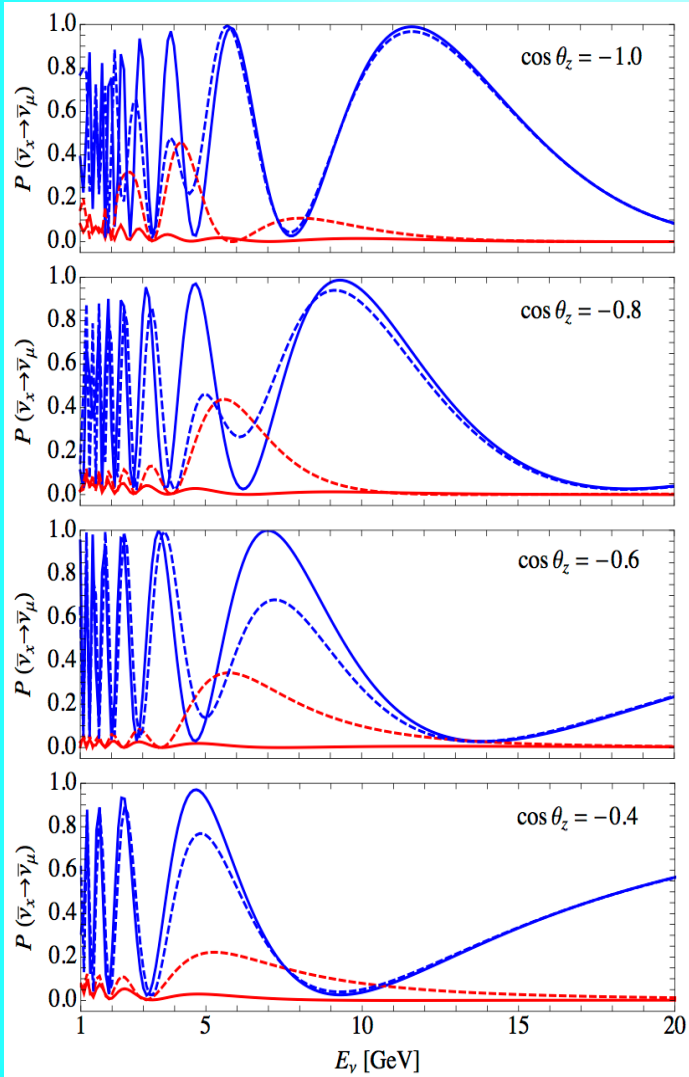
Parametric enhancement of oscillations



Probabilities

neutrinos

antineutrinos



NH - solid
IH - dashed
 $x = \mu$ - blue
 $x = e$ - red

Method

Measurement of $E - \theta$ distributions of different type of events.
Compare events for the normal and inverted orderings

"tracks"

$$\nu_\mu + N \rightarrow \mu + h$$

muon track

+ cascade

$$\nu_\tau + N \rightarrow \tau + h$$

$$\rightarrow \mu + \nu + \nu$$

Measurements

$$E_\mu \quad \theta_\mu \quad E_h$$

inelasticity

$$E_\nu = E_\mu + E_h$$

reconstruction

$$E_h \quad E_\mu \quad \theta_\mu \rightarrow \theta_\nu$$

"cascades"

$$\nu_e + N \rightarrow e + h$$

$$\nu_\alpha + N \rightarrow \nu_\alpha + h$$

cascades

$$\nu_\tau + N \rightarrow \tau + h$$

$$\rightarrow h + \nu$$

$$\rightarrow e + \nu + \nu$$

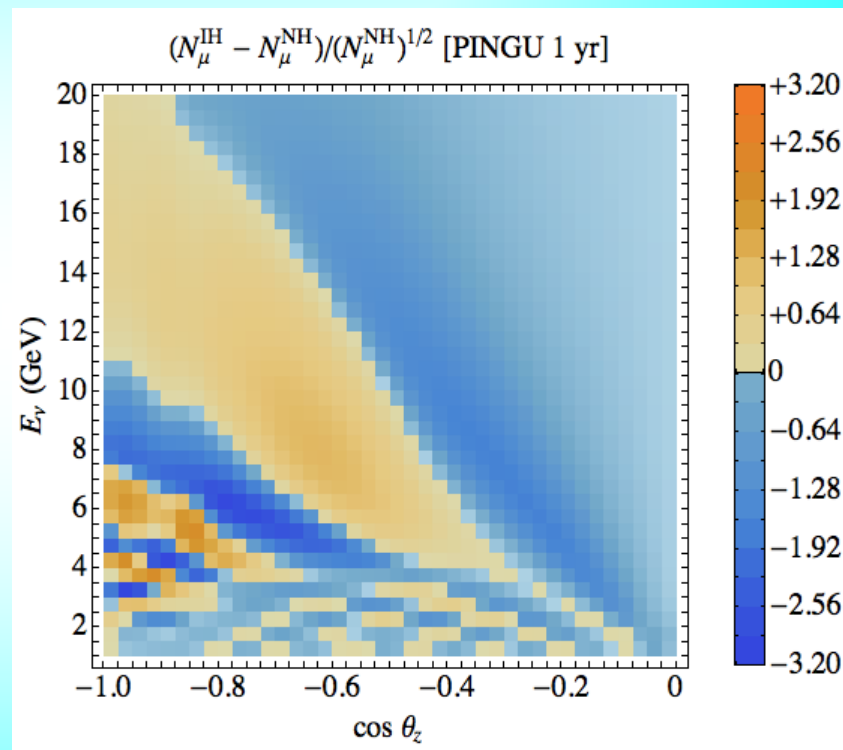
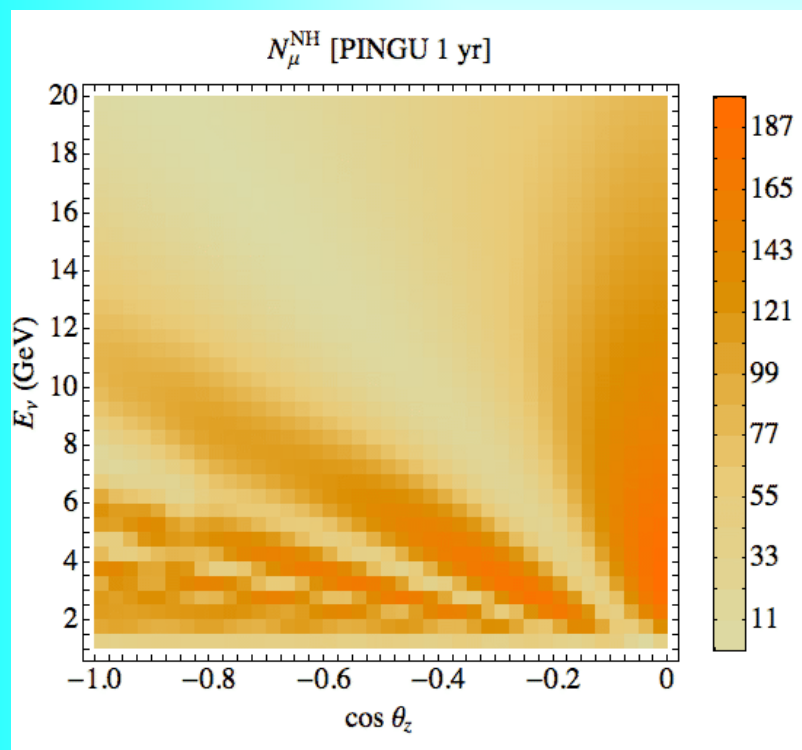
$$E_\nu \quad \theta_\nu$$

reconstruction

Track events

$\sim 10^5$ events/year

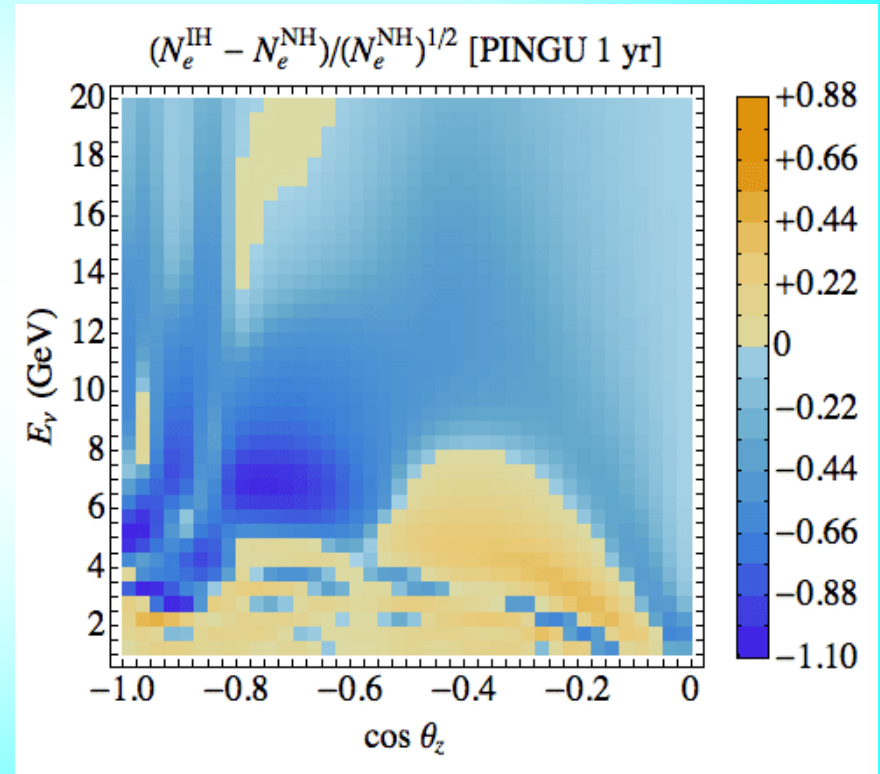
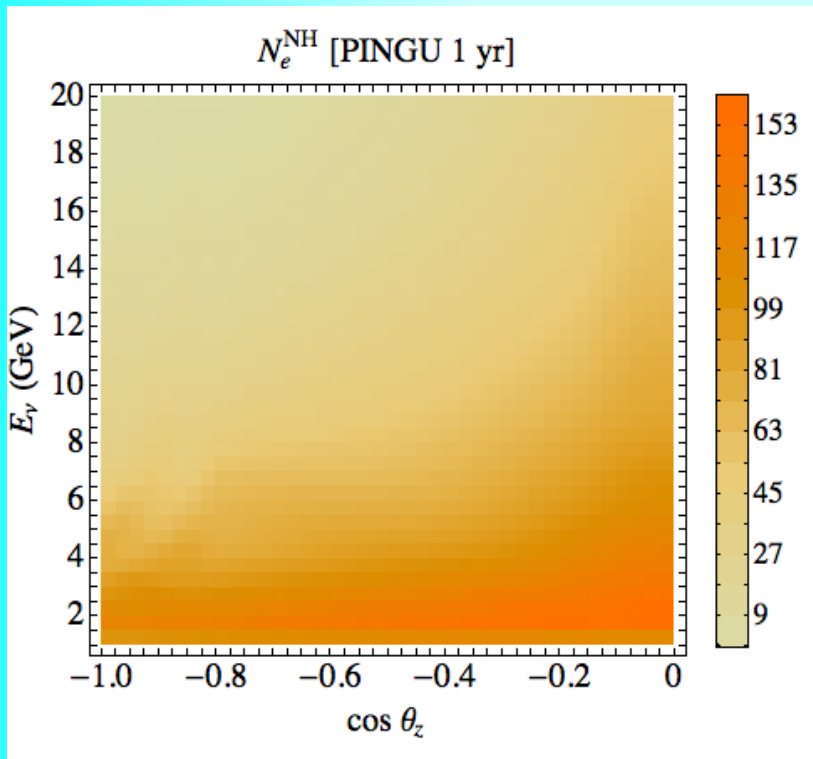
“Distinguishability”



Estimator of sensitivity
S - asymmetry
|S| - significance

Cascade events

“Distinguishability”



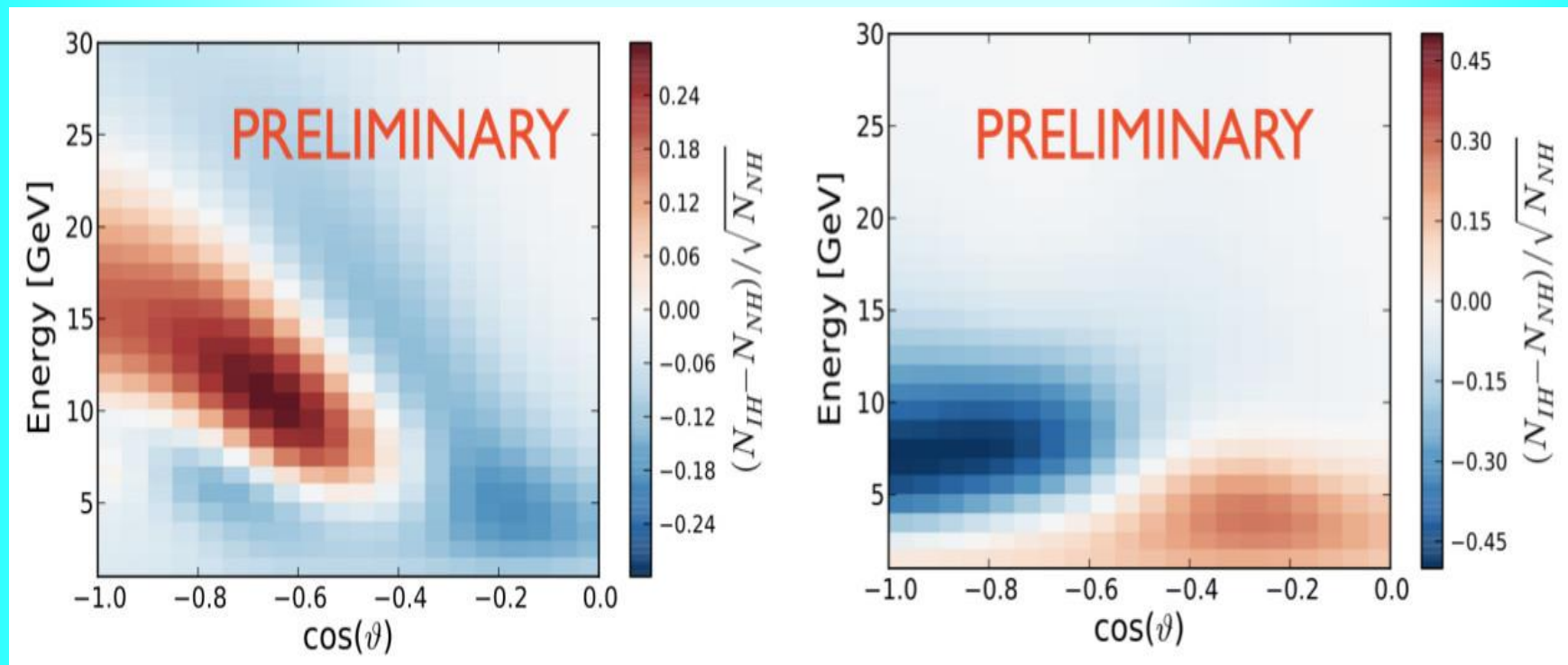
Statistical significance

Smearred distributions

Ken Clark

Over energy and angle
resolution functions

PINGU



tracks

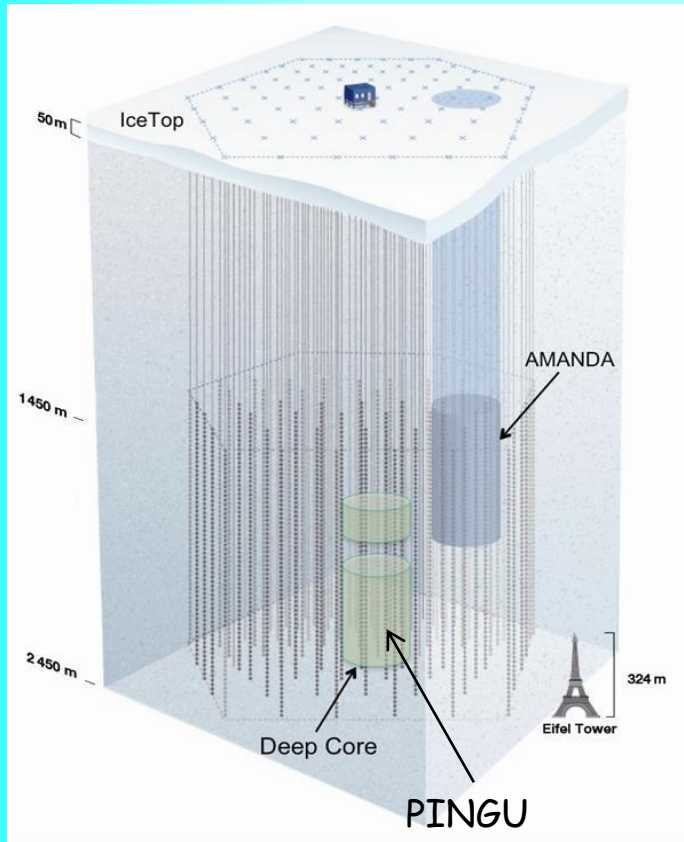
cascades

distinguishability

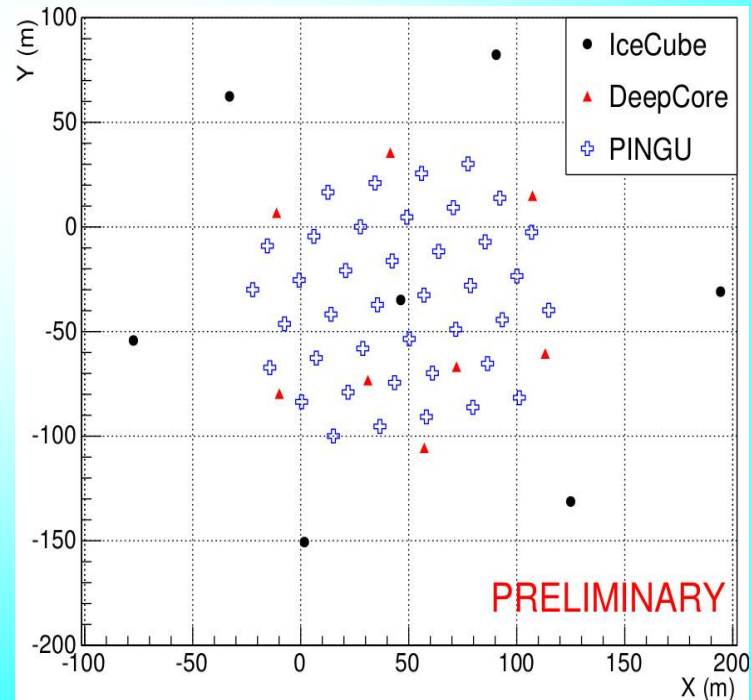
PINGU

Precision IceCube Next Generation Upgrade

K. Clark



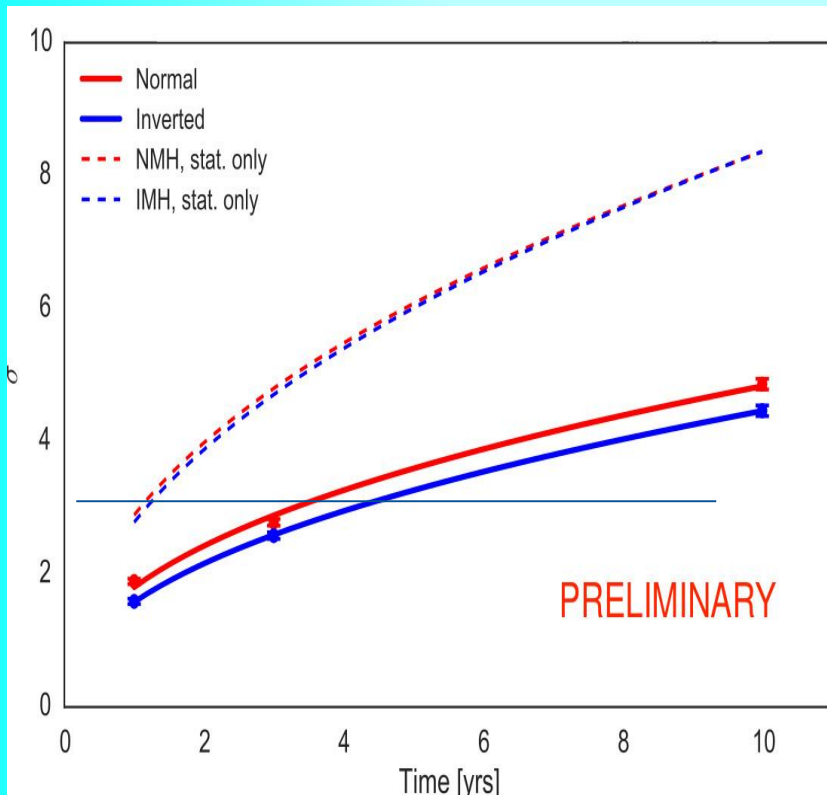
40 strings
96 DOM's per string



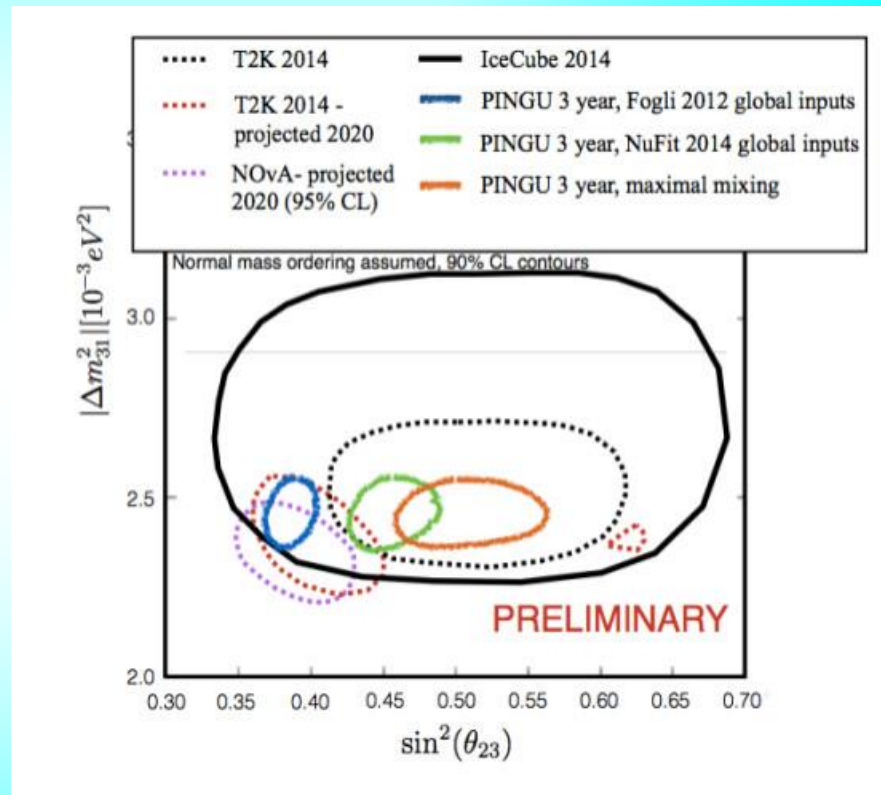
Sensitivity

K. Clark

Mass hierarchy



Parameters of the 2-3 sector



Deviation from maximal:
symmetry or no symmetry, Quadrant
Sensitivity to MH depends on

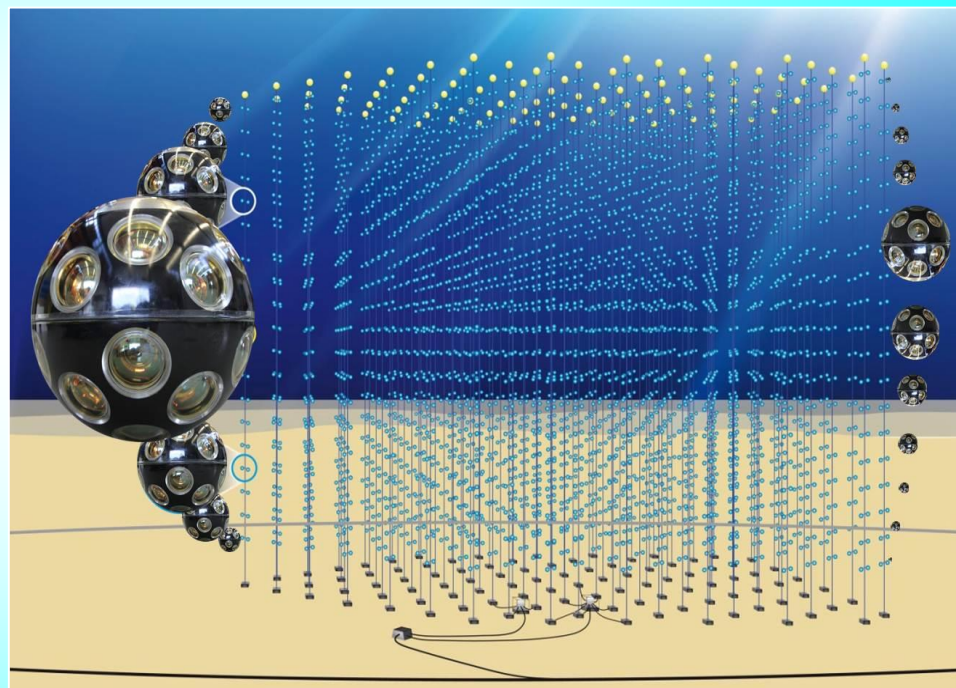
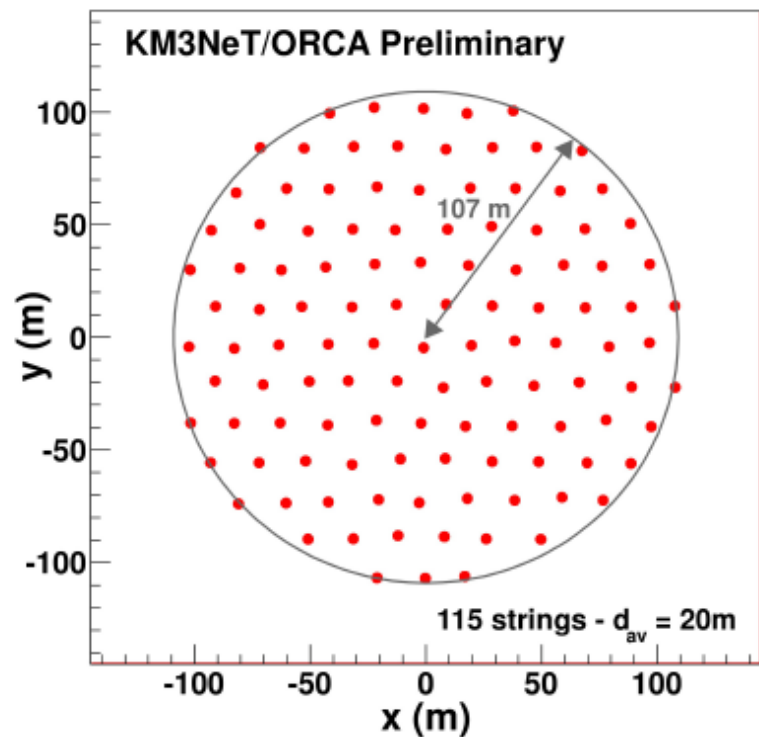
ORCA

Oscillation Research with
Cosmics in the Abyss



115 lines, 20m spaced,
18 DOMs/line, 6m spaced
Instrumented volume ~ 3.8 Mt,
2070 OM

J. Brunner
Highlight talk: C. James

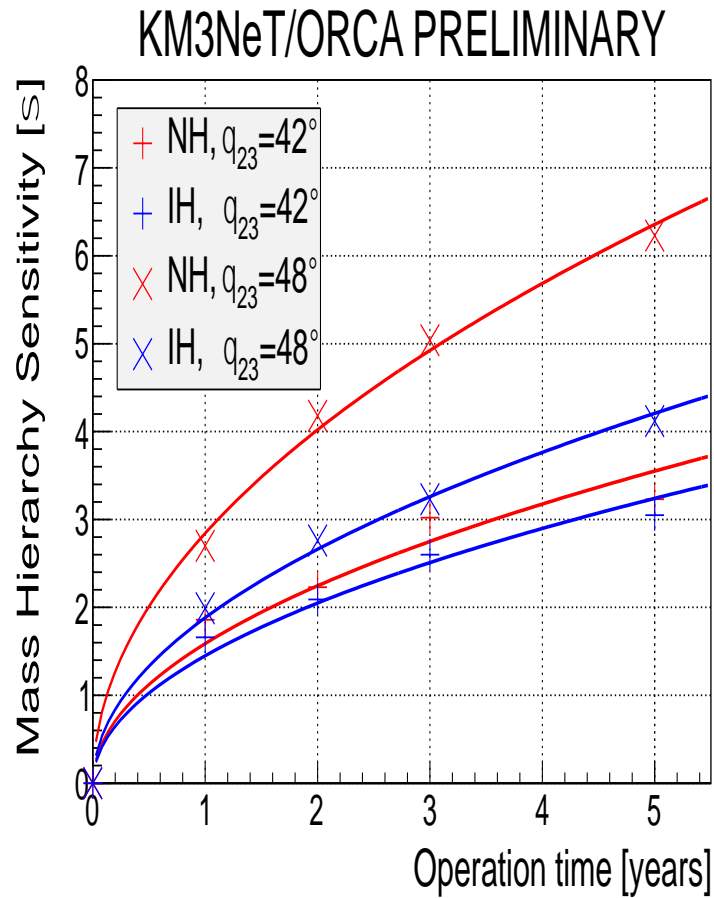


- 31 3" PMTs
- Digital photon counting
- Directional information
- Wide angle view

Poster : Ronald Bruijn

Sensitivity to MH

J. Brunner



Dependence of sensitivity on time
for fixed θ_{23} values and
 δ_{CP} fixed to zero

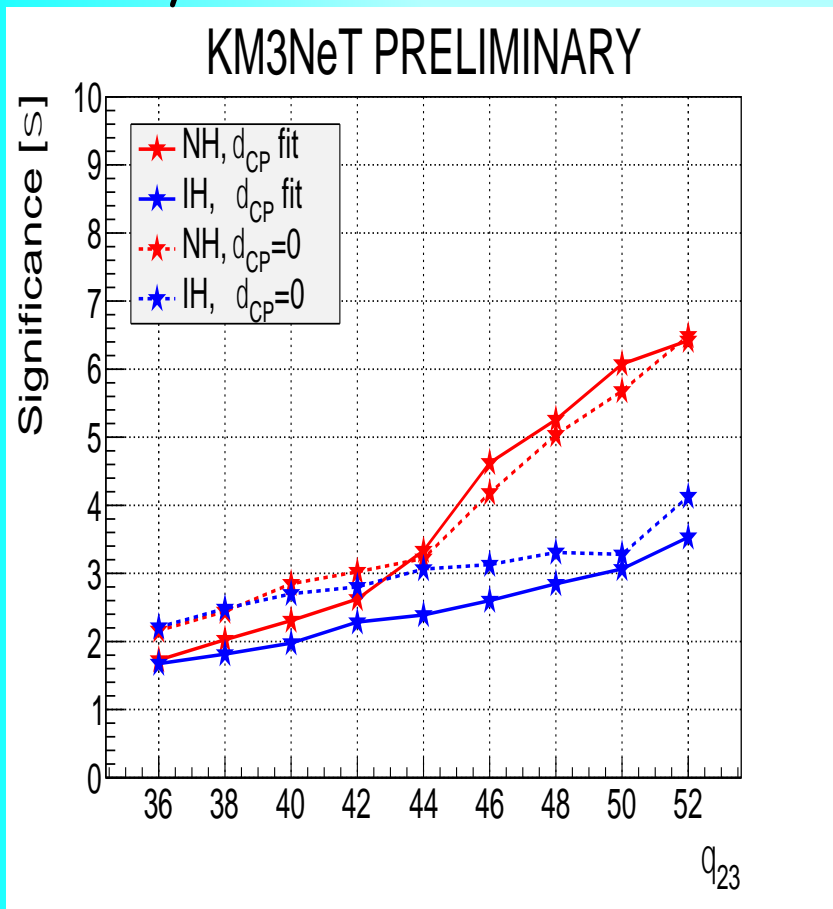
- Track vs shower event classification
- Full MC detector response matrices including misidentified and NC events
- Atmospheric muon contamination
- Neutral current event contamination
- Various Systematic uncertainties

Poster : Martijn Jongen

Sensitivity to mass hierarchy

3 years

J. Brunner



Dependence of sensitivity on θ_{23} .
Higher for NH than IH.

Second octant easier than first octant.

When fixing δ_{CP} to zero sensitivity increases by $\sim 0.5\sigma$

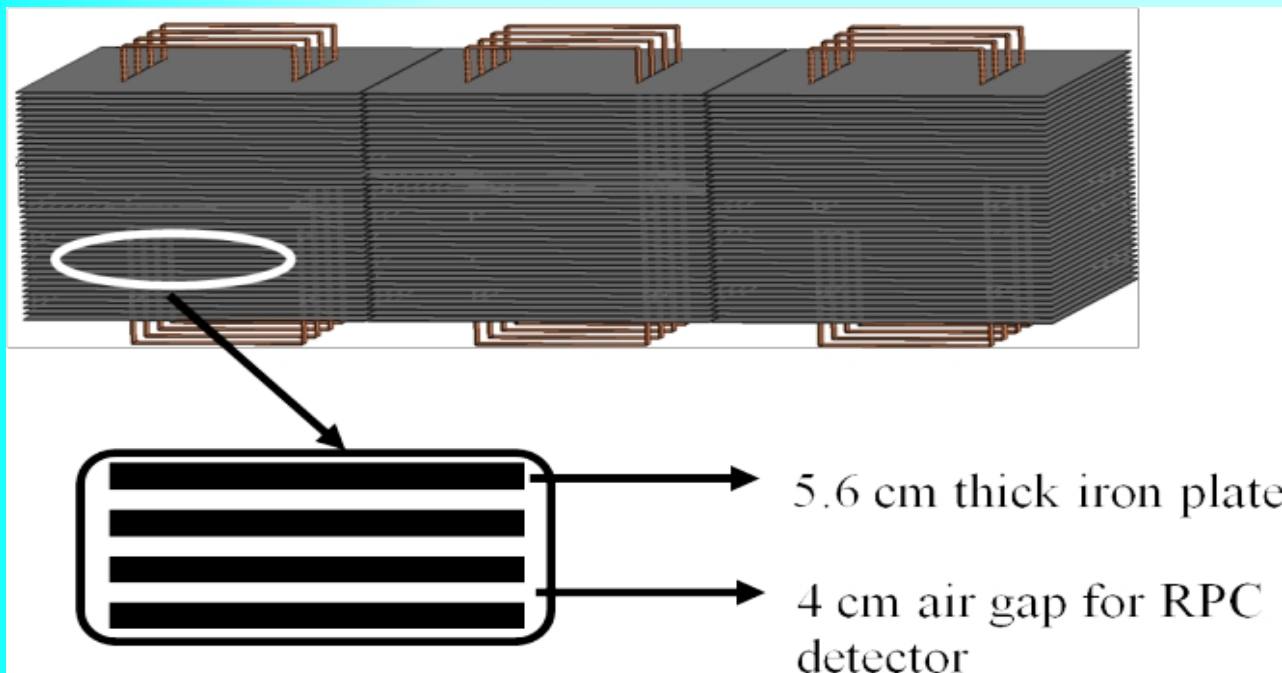


Martijn JONGEN
Poster 935

INO-ICAL

*ICAL Collaboration (Ahmed Shakeel et al.)
arXiv:1505.07380 [physics.ins-det]*

The 50 kt magnetized iron calorimeter (ICAL) detector at the India-based Neutrino Observatory (INO)

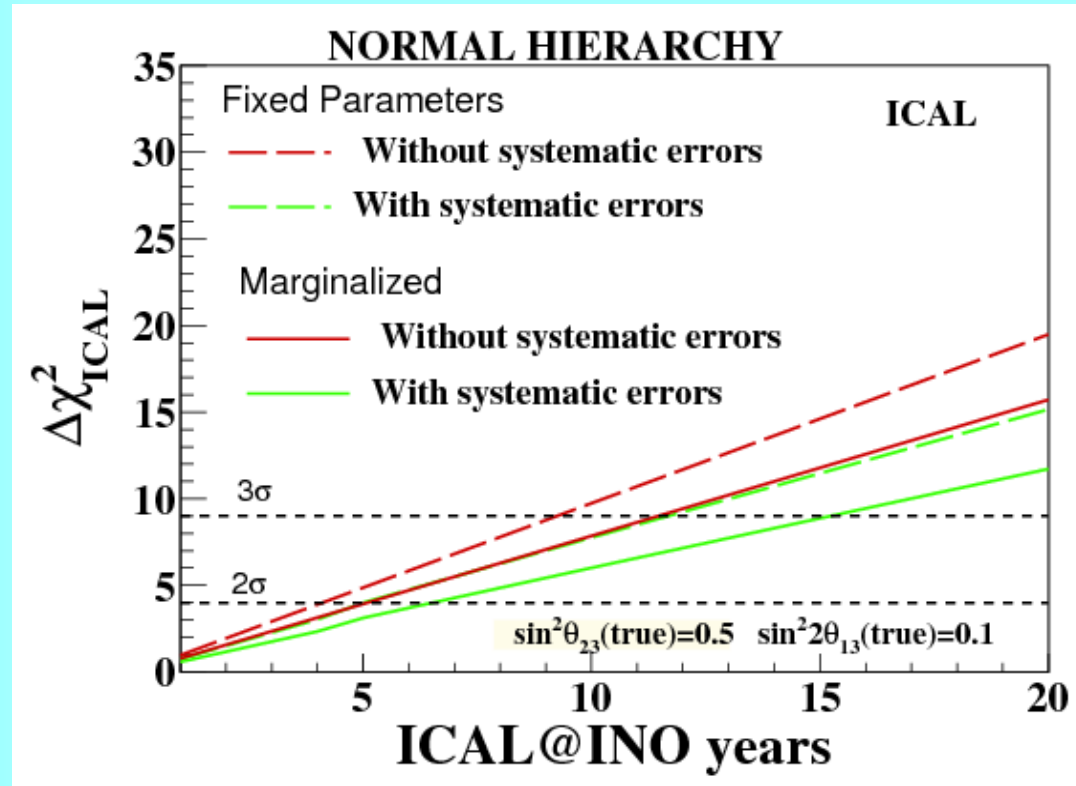


Energy and direction of the muons; energy of multi-GeV hadrons;
charge of muon

The energy and zenith angle dependence of the atmospheric neutrinos
in the multi-GeV range.

Sensitivity to hierarchy

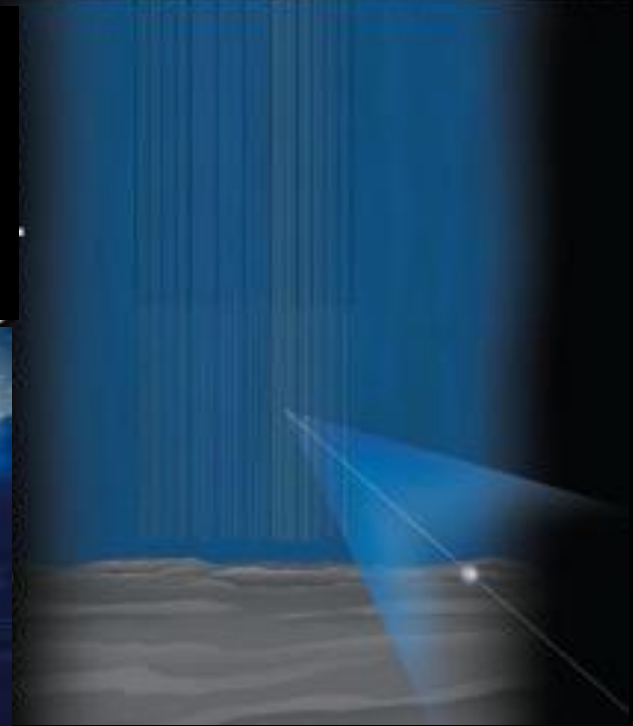
ICAL Collaboration
(Ahmed Shakeel et al.)
arXiv:1505.07380 [physics.ins-det]



10 -15 years

The impact of systematic uncertainties on mass hierarchy sensitivity.
The red (green) lines - without (with) systematic uncertainties
Long-dashed lines are for fixed values of parameters (1-3 mixing, 2-3 mixing, mass splitting), solid -marginalized

CP-violation



Measuring CP-phase

Global fit

Dedicated experiments

T2K + NOvA + reactors

J. PARC- SK

750 kw upgrade

at 2- 3 σ

$3\pi/2$ from 0

J. PARC- HK

DUNE LBNF

ESS

European spallation source Lund

$\sim 5 - 7 \sigma$

result in 2030 - 2035

~ 2 bln US\$

Long term and expensive commitment

Alternative?

All possible alternatives must be explored and scenarios of developments in the next 20 years should be considered

Ice Cube Deep Core

100 GeV

10 - 15 GeV

PINGU ORCA

Mass hierarchy

3 GeV

Super-PINGU ORCA

3 times denser
array than PINGU

0.5 - 1 GeV

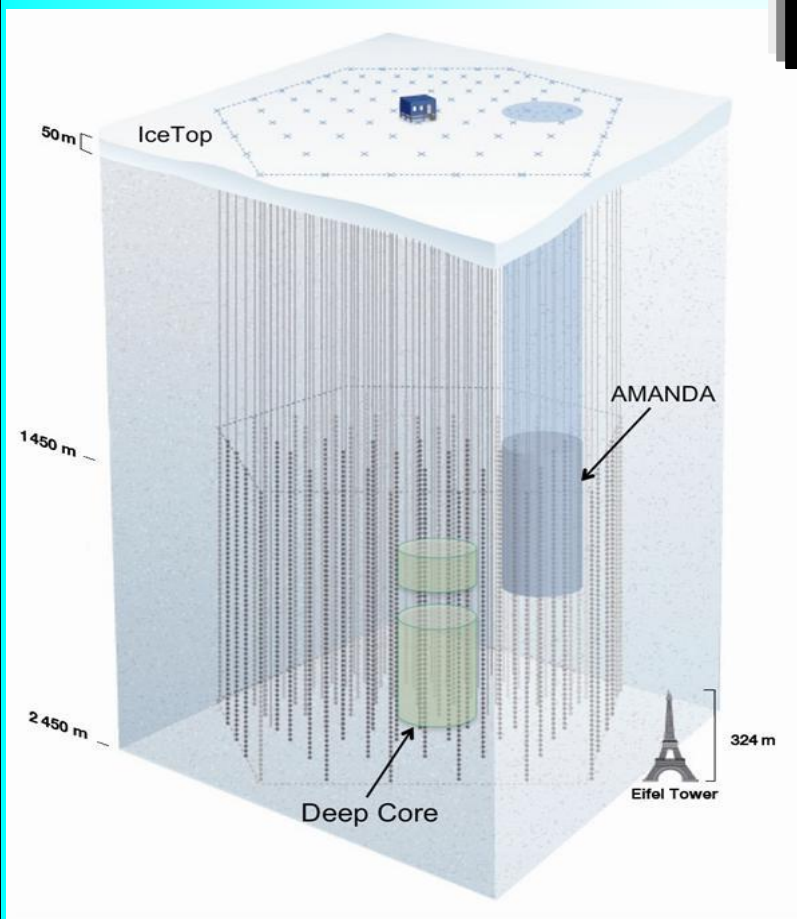
Few Mtons in
sub-GeV range

*S. Razzaque, A.Y.S.
1406.1407 hep-ph*

Megaton-scale
Ice
Cherenkov
Array

MICA

0.01 GeV

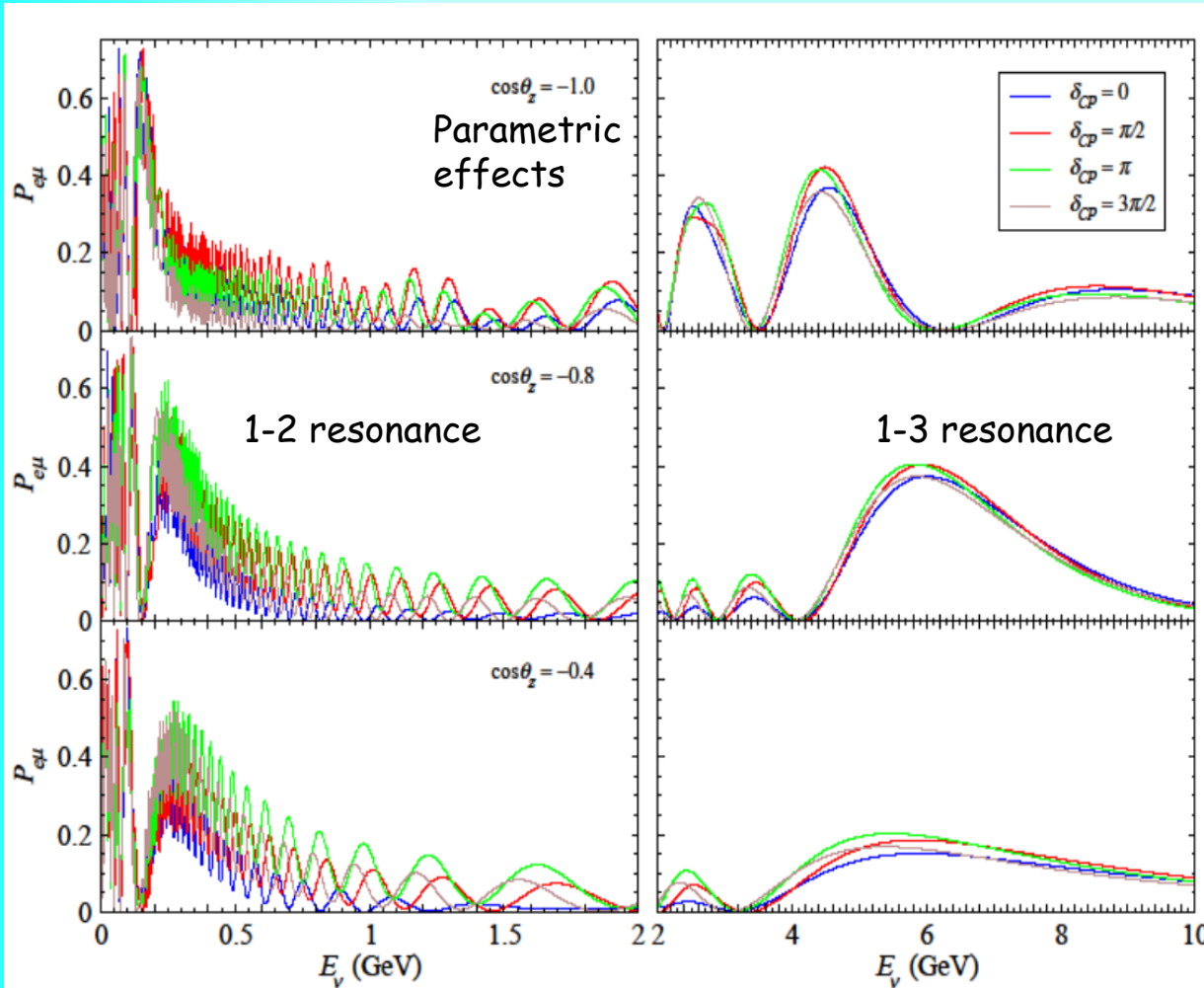


Probabilities

S. Razzaque, A.Y.S.
arXiv: 1406.1407 hep-ph

$$\nu_e \rightarrow \nu_\mu$$

NH



Large (10%) effect
at $E \sim (0.5 - 1.5) \text{ GeV}$

The key: with
change of the phase
systematic shift
of curves,
the same for all zenith
angles in mantle

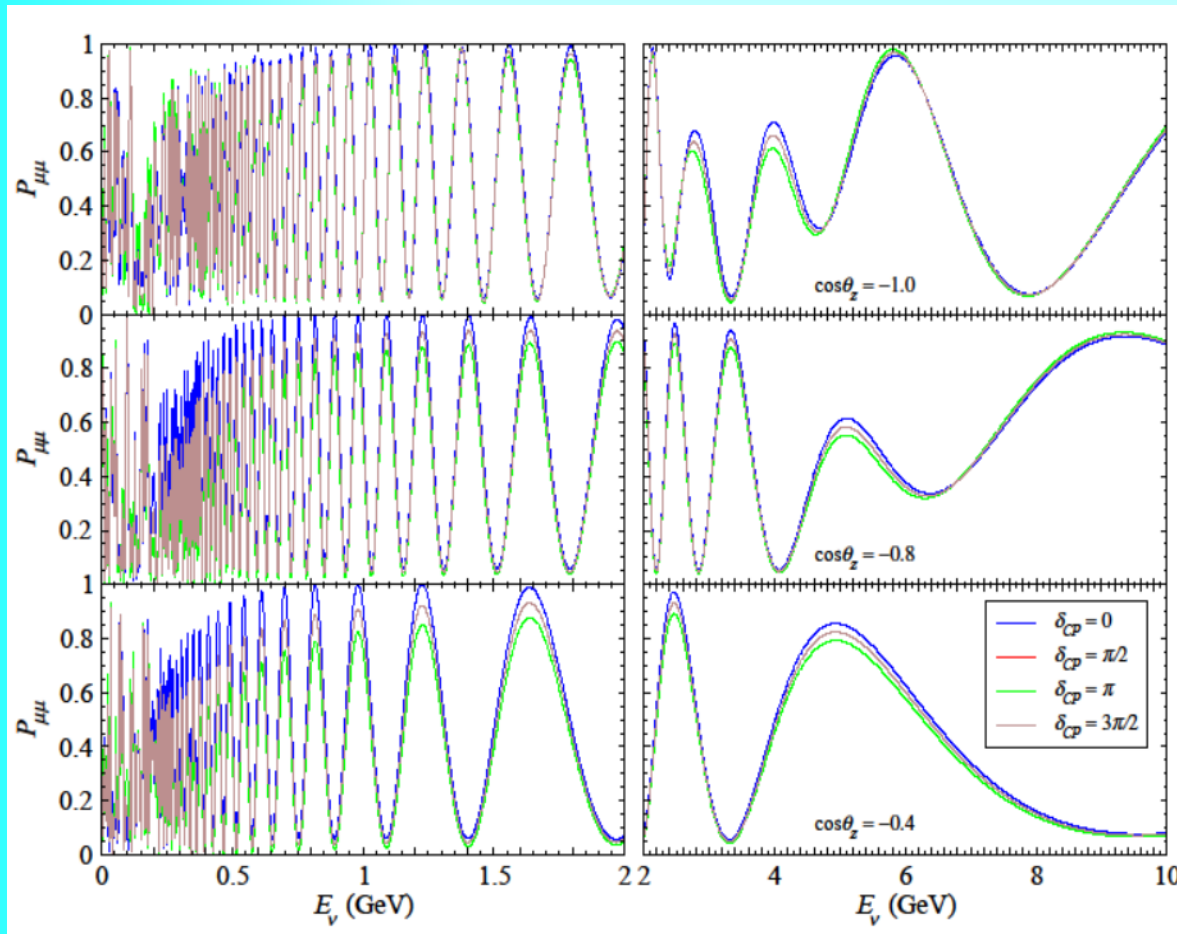


Averaging over
fast oscillations
and integration over
zenith angle does
not wash out CP
phase effect

Probabilities

S. Razzaque A Y S

$$\nu_\mu \rightarrow \nu_\mu$$



No phase shift

Effect is opposite
to $\nu_e \rightarrow \nu_\mu$
with change of δ



Flavor suppression
of effects for
 ν_μ events

Flavor identification
is crucial

Distinguishability for CP

Quick estimator (metric) of discovery potential

For each energy-zenith
angle bin ij
relative CP-difference

$$S_{ij} = \frac{N_{ij}^{\delta} - N_{ij}^{\delta=0}}{\sqrt{N_{ij}^{\delta=0}}}$$

no fluctuations

If is true value $\rightarrow N_{ij}^{\delta}$ corresponds to ``true'' value of events
 $\rightarrow N_{ij}^{\delta=0}$ ``measured'' number of events

$|S_{ij}|$

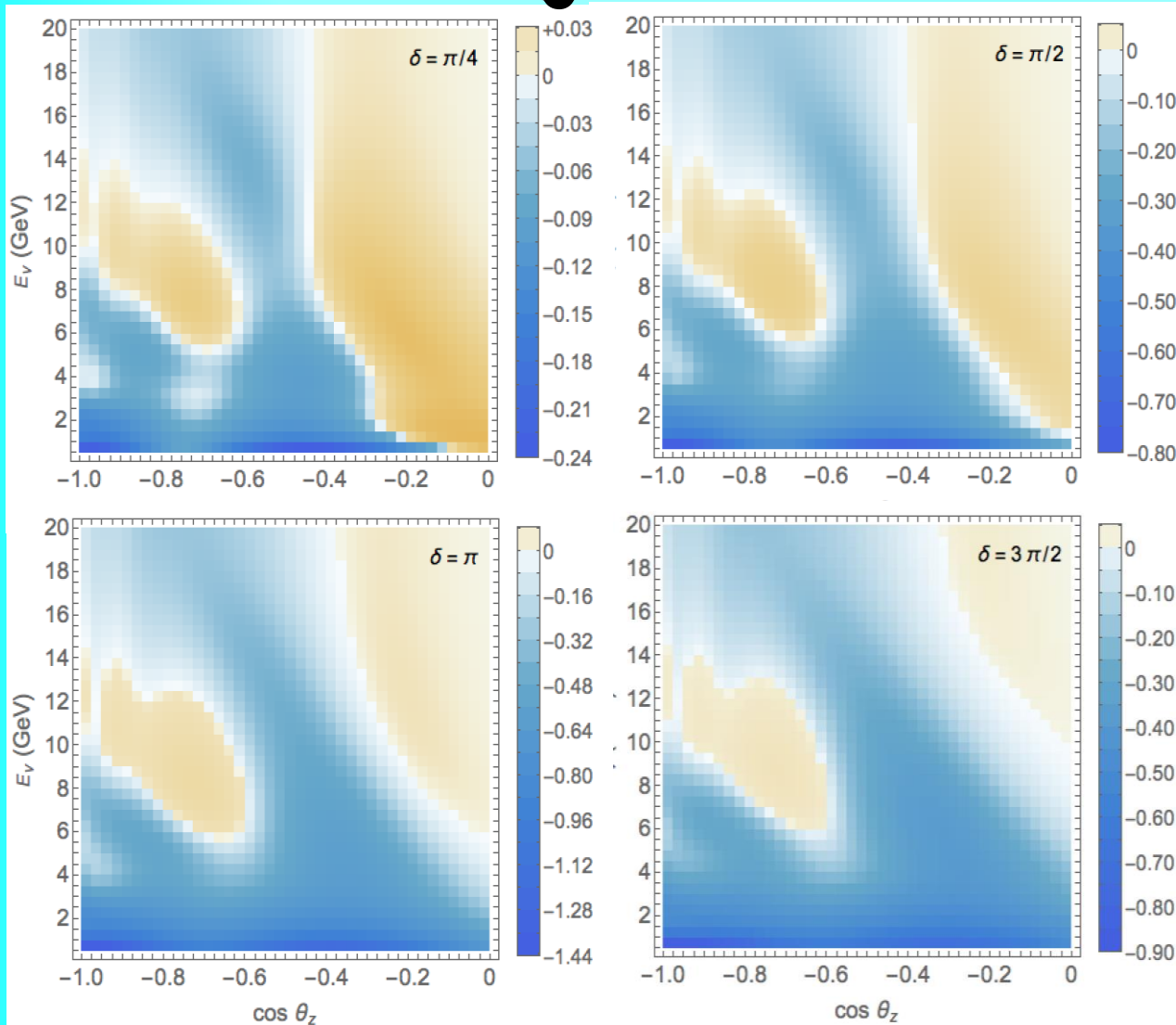
- distinguishability of different values of CP-phase

Total distinguishability

$$S^{\text{tot}} = [\sum_{ij} S_{ij}^2]^{1/2}$$

Neutrino images of the Earth

For different values of CP phase



ν_μ - CC events
(track + cascade)

S-distributions
for different
values of δ

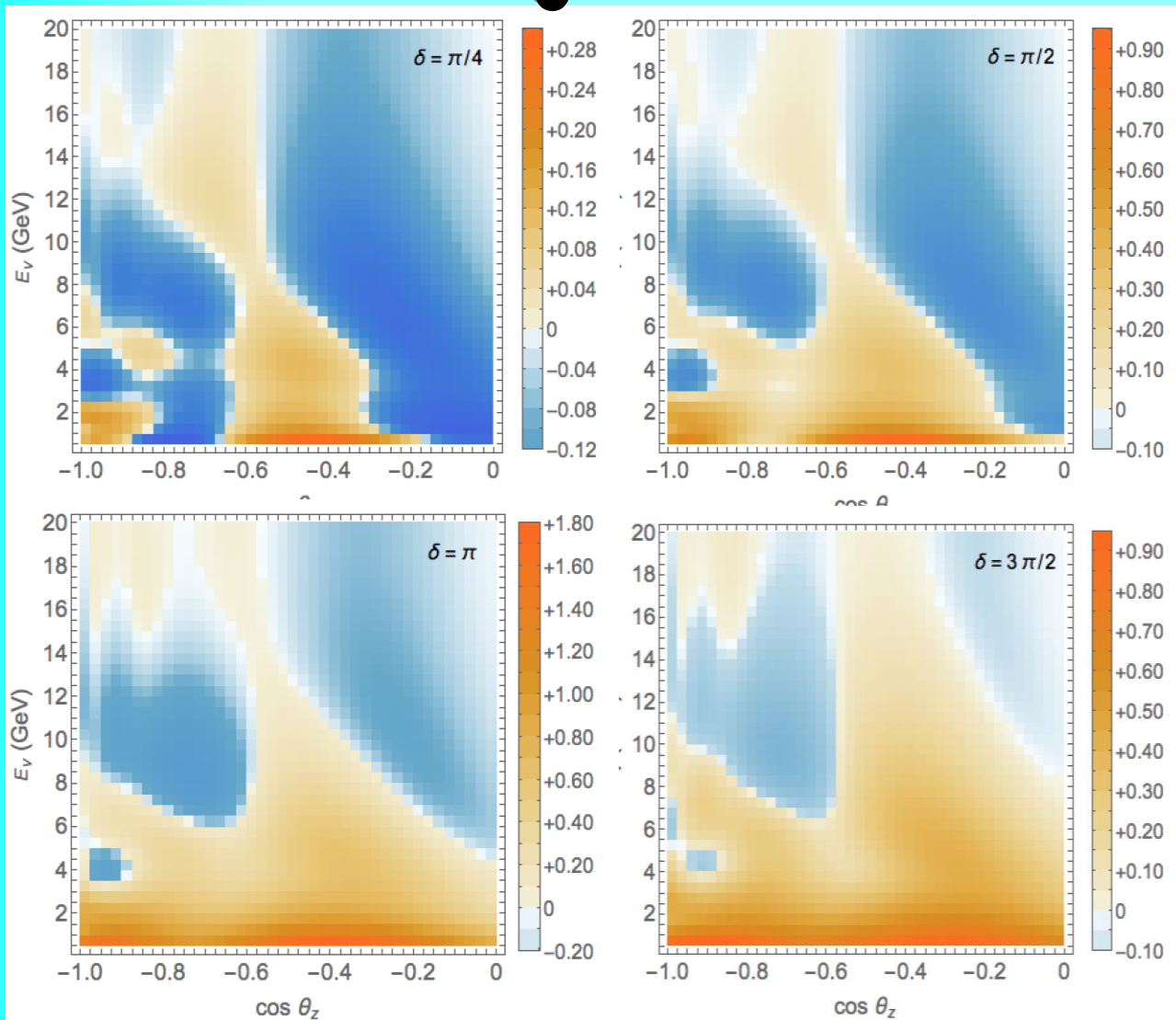
Super PINGU
1 year

After smearing over
neutrino energy and
direction

S distributions

*S. Razzaque, A.Y.S.
arXiv: 1406.1407 v2
hep-ph*

Neutrino images of the Earth



ν_e - CC events
(cascades)

S-distributions
for different
values of δ

Super PINGU
1 year

After smearing over
neutrino energy and
direction

*S. Razzaque, A.Y.S.
arXiv: 1406.1407 v2
hep-ph*

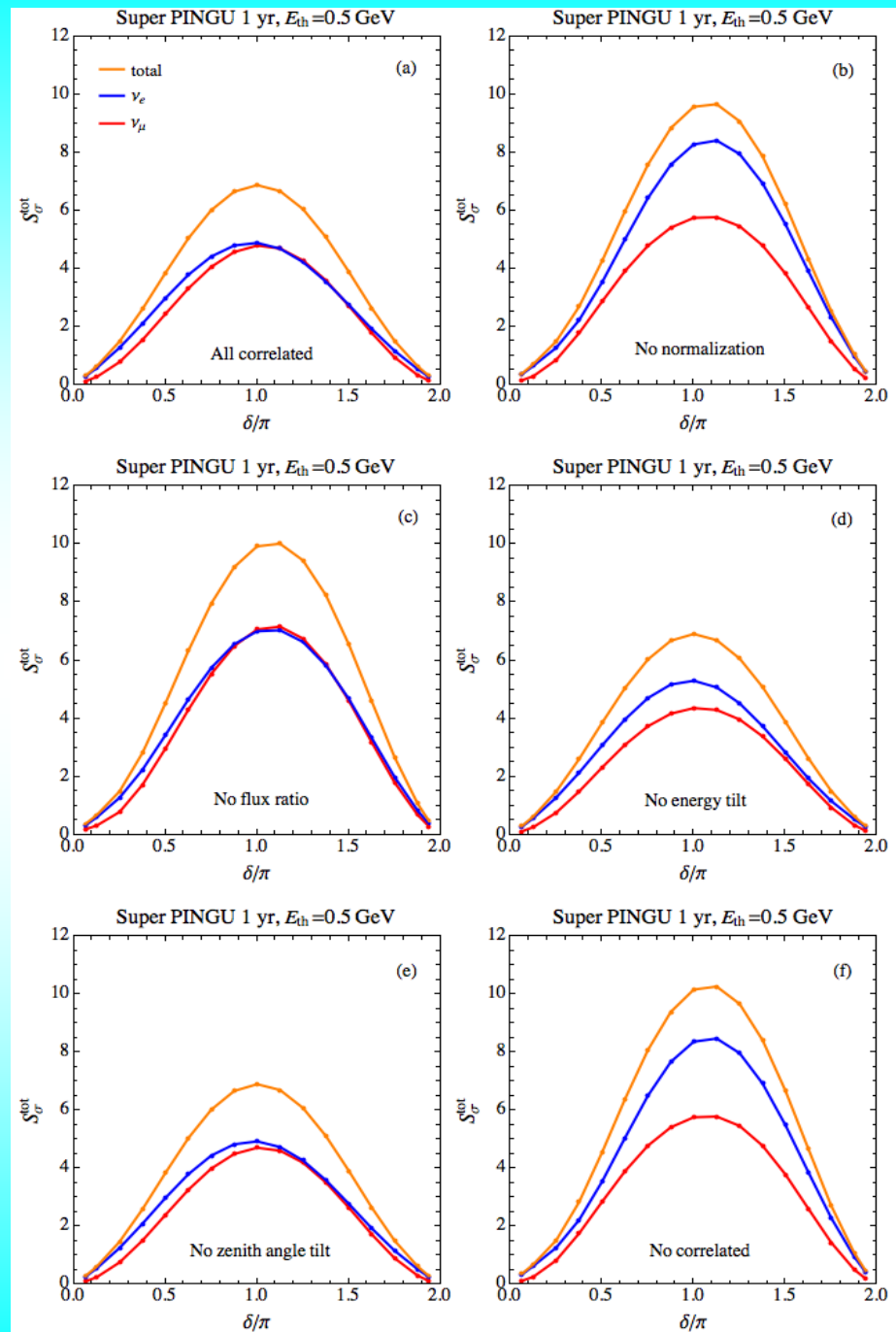
Can we measure this?

Sensitivity of SuperPINGU

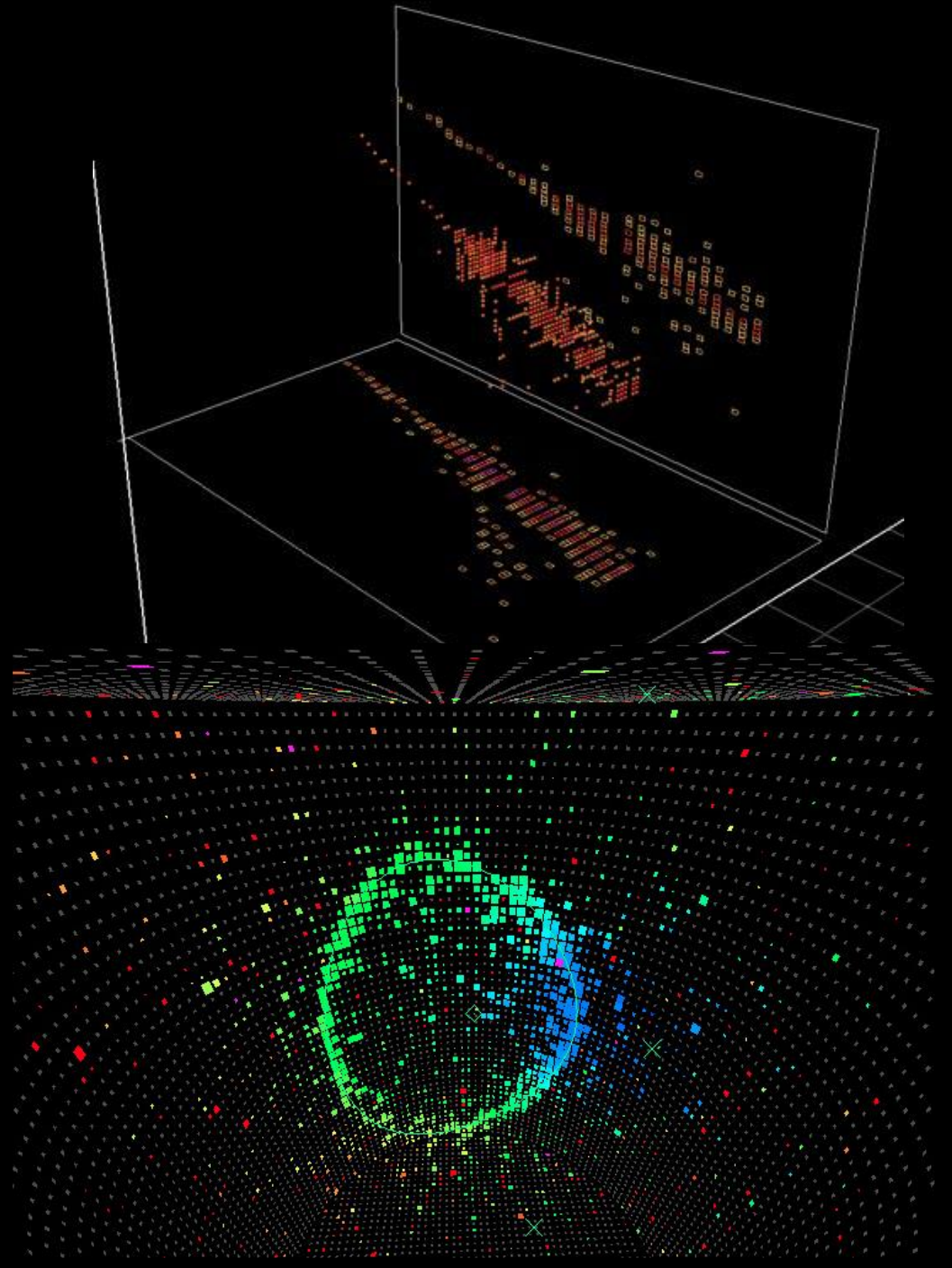
Effect of correlated systematic errors

Flavor misidentification can further reduce distinguishability by factor 1.5 - 2

Still $S_{\sigma} \sim 3-4$ for $\delta = \pi$ after 4 years of exposure



Summary



Enormous progress all mixing angles and mass splittings in 3ν framework are measured

Still physics behind neutrino mass and mixing is not yet identified

Few challenges imply existence of new neutrino states - sterile neutrinos

Measurements of missing parameters of the 3ν paradigm

- mass hierarchy,
- CP phase, as well as
- searches physics beyond 3ν paradigm may lead to breakthrough in the field.

Identification of the neutrino mass ordering - next big in neutrino physics

Large atmospheric neutrino detectors with low (few GeV) energy threshold PINGU, ORCA may be first in this race.

Measurements of the Dirac CP-phase ultimate in oscillation neutrino experiments

A possibility to use further upgrade of PINGU, ORCA detectors to measure the CP phase should be explored

Race for mass hierarchy:

PINGU, ORCA

JUNO, RENO 50

T2K, NOvA

Supernova neutrino bursts

Cosmology

2022 - 2026 ?

Tomorrow? But require
better understanding
collective effects

Fast developments of techniques of detection of low energy (atmospheric) neutrinos in multi Megaton detectors

Can address crucial issues in particle, neutrino physics:

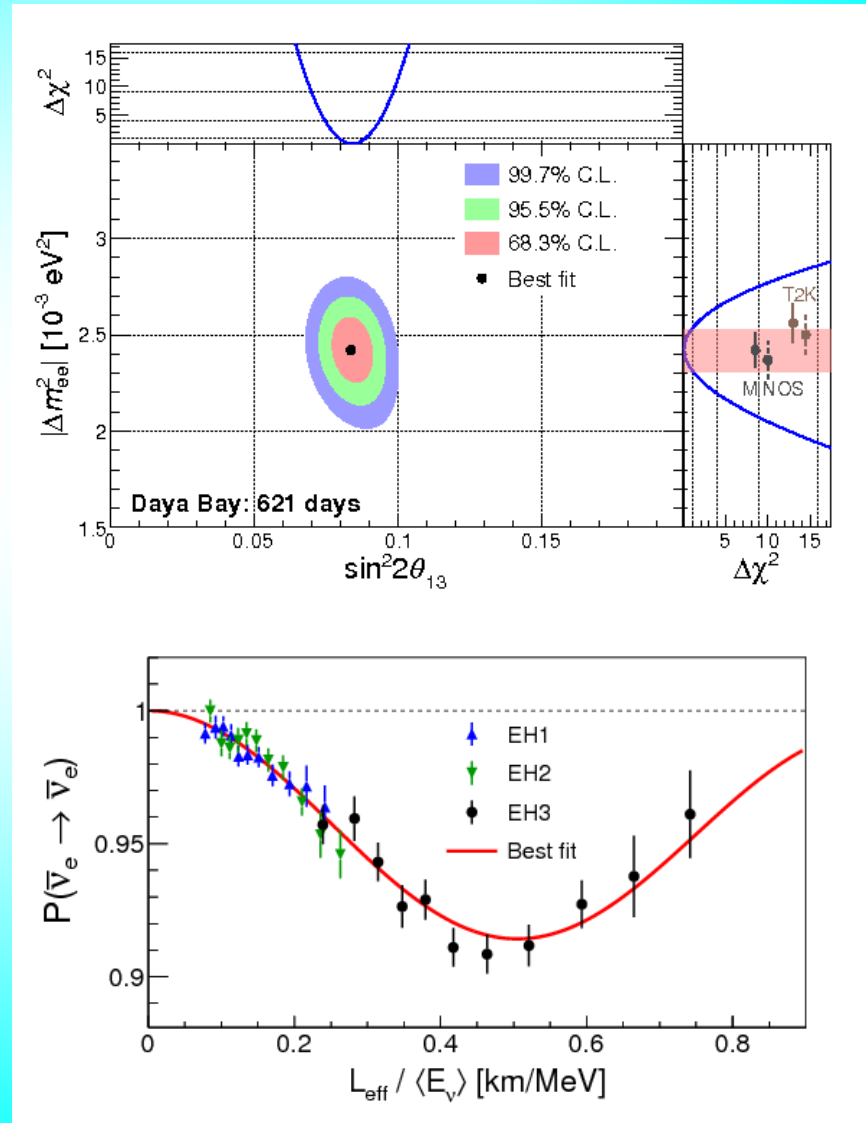
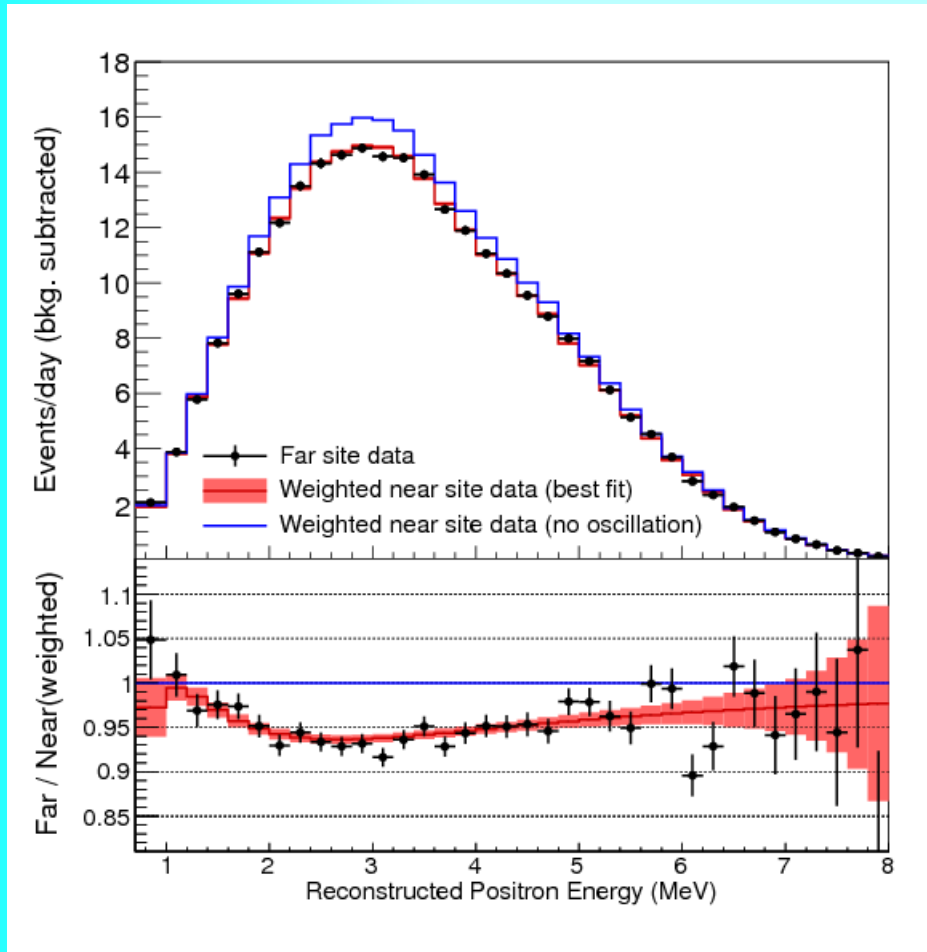
- establishing neutrino mass ordering
- determination of the CP-phase
- searches for sterile neutrinos, and tests of existing hints
- searches for non-standard neutrino interactions, etc.

This may lead to major developments in the field

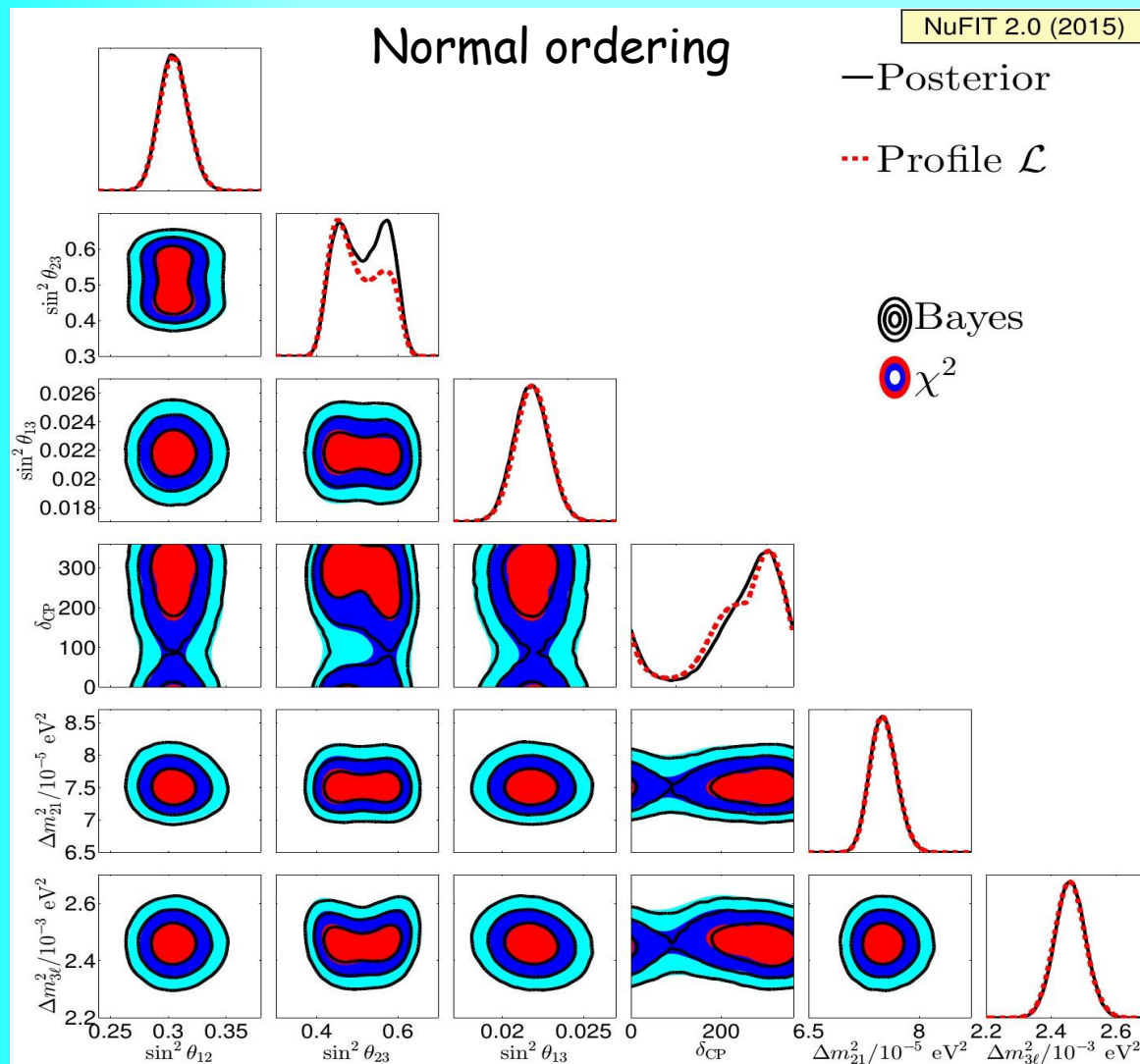
Backup slides

Daya Bay result

Daya Bay Collaboration
(An, F.P. et al.)
arXiv:1505.03456 [hep-ex]

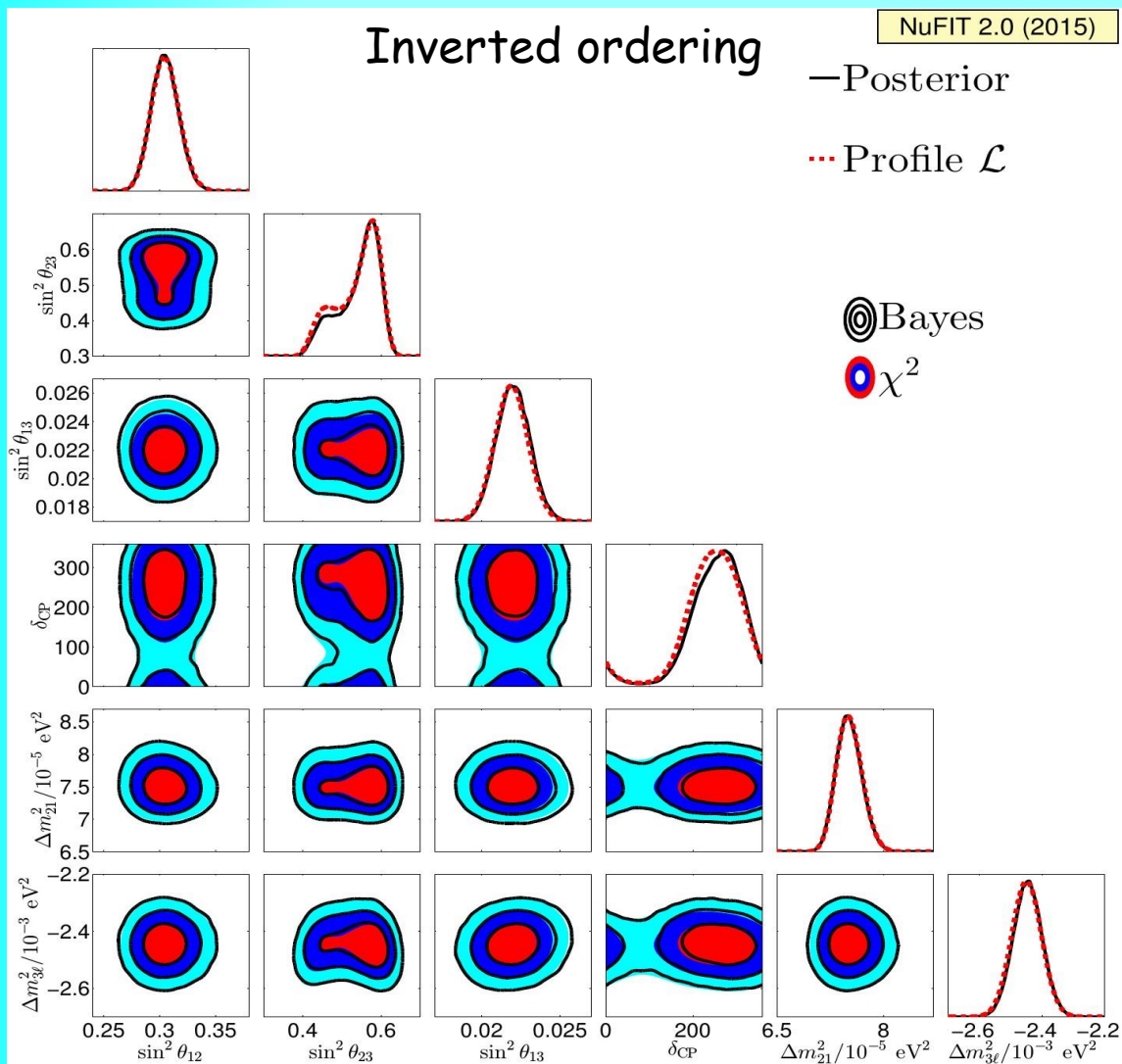


Global fit results



*J. Bergstrom, et al,
1507.0436 [hep-ph]*

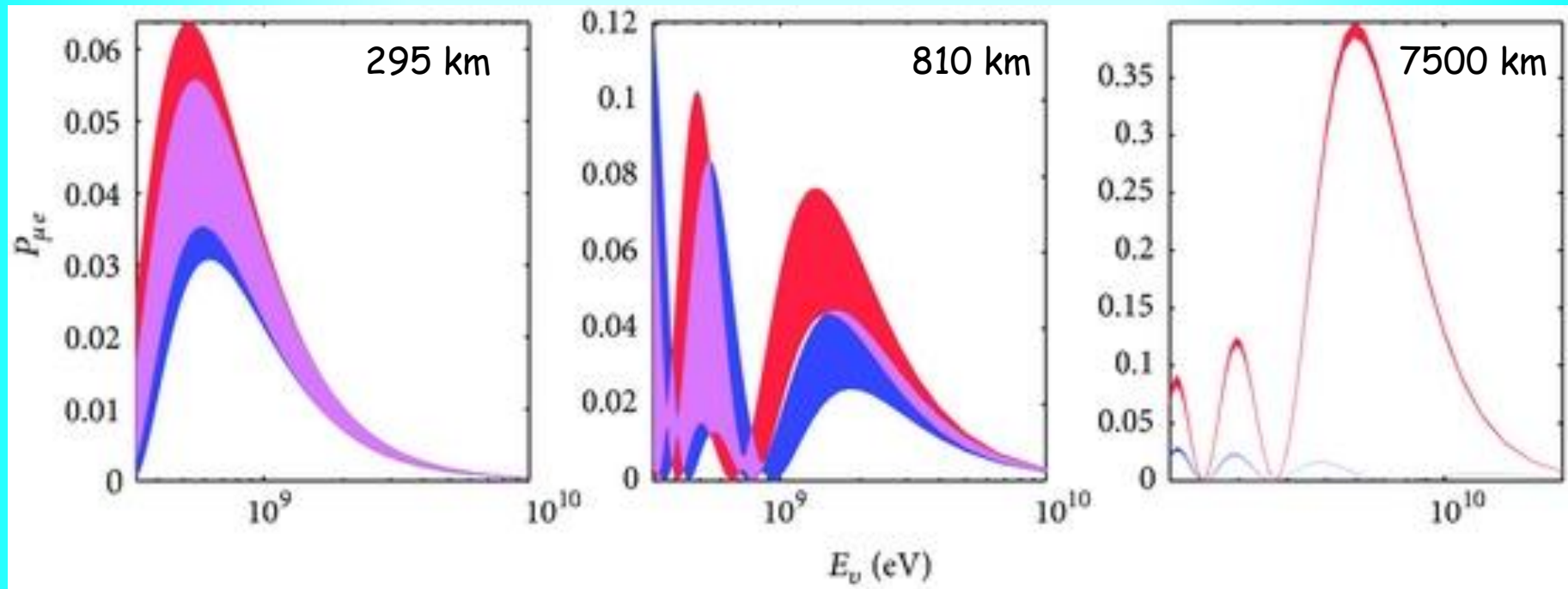
Global fit results



Hierarchy and CP

degeneracy

M. Blennow and A Y S, Advances in High Energy Physics , v. 2013 (2013), ID 972485



The neutrino oscillation probability at baselines of 295 (left), 810 (middle), and 7500 km (right) as a function of the neutrino energy. The red (blue) band corresponds to the normal (inverted) mass hierarchy and the band width is obtained by varying the value of delta. The probabilities for antineutrinos look similar with the hierarchies interchanged. Note the different scales of the axes.

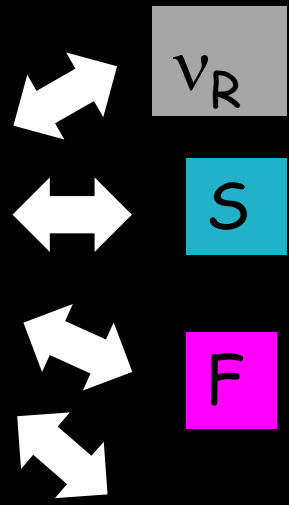
Neutrino Portal



Singlet of SM
 symmetry group
 $SU(3) \times SU(2) \times U(1)$



$$\begin{pmatrix} \nu \\ e \end{pmatrix} \begin{pmatrix} H^+ \\ H^0 \end{pmatrix}$$



F is composite
 fermionic operator
 singlet of symmetry
 group of hidden sector

Non-local interactions
 which violate fundamental
 symmetries eg CPT

H-asymmetry and significance

Quick estimator (metric) of discovery potential

*E. Kh. Akhmedov,
S. Razaque, A. Y. S.
arXiv: 1205.7071*

For each ij- bin
Hierarchy asymmetry
H-asymmetry

$$S_{ij} = \frac{[N_{ij}^{IH} - N_{ij}^{NH}]}{\sqrt{N_{ij}^{NH}}}$$

``Distinguishability''

If NH is true hierarchy $\rightarrow N_{ij}^{NH}$ ``experimental'' number of events
 $\rightarrow N_{ij}^{IH}$ ``fit'' number of events

$|S_{ij}|$ statistical significance of establishing true hierarchy

Uncorrelated
systematic error

$$N_{ij}^{NH} \rightarrow \sigma_{ij}^2 = N_{ij}^{NH} + (f N_{ij}^{NH})^2$$

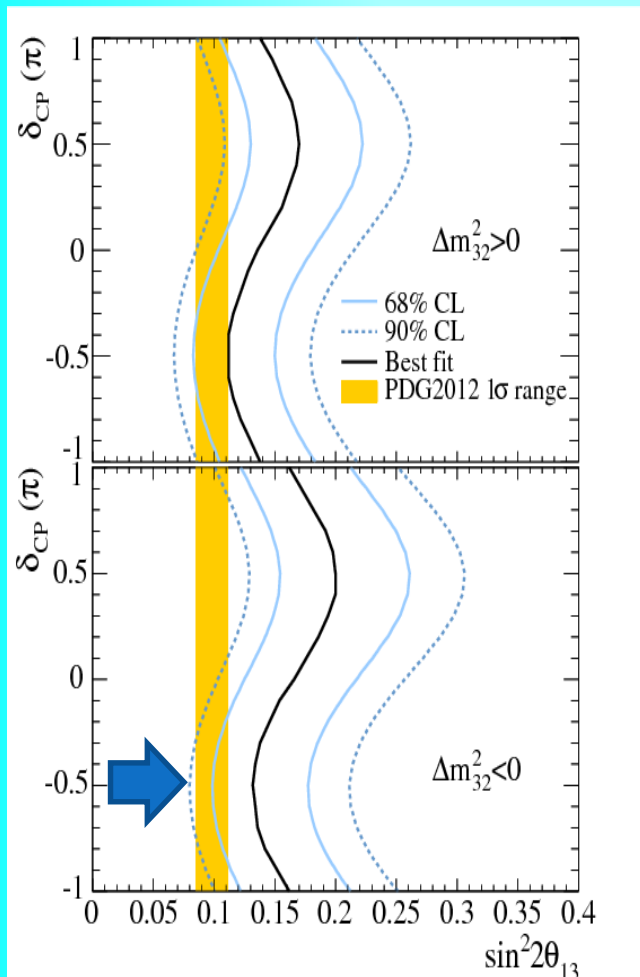
in denominator

Total
distinguishability

$$S^{\text{tot}} = [\sum_{ij} S_{ij}^2]^{1/2}$$

Status and hint

Marginalized over 2-3 mixing



PDG (reactors)

↓ **PARC (beam upgrade) Super Kamiokande**

p.o.t. $6 \cdot 10^{20} \rightarrow 7.8 \cdot 10^{21}$ by 2018

i.e. 13 times higher statistics

sensitivity to the phase δ_{CP} at 90% C.L. or better over

$-115^\circ < \delta_{CP} < -60^\circ$ for NH

$+50^\circ < \delta_{CP} < +130^\circ$ for IH.

if $\theta_{23} = 45^\circ$

T2K Collaboration (K. Abe, et al.)

arXiv:1409.7469 [hep-ex]

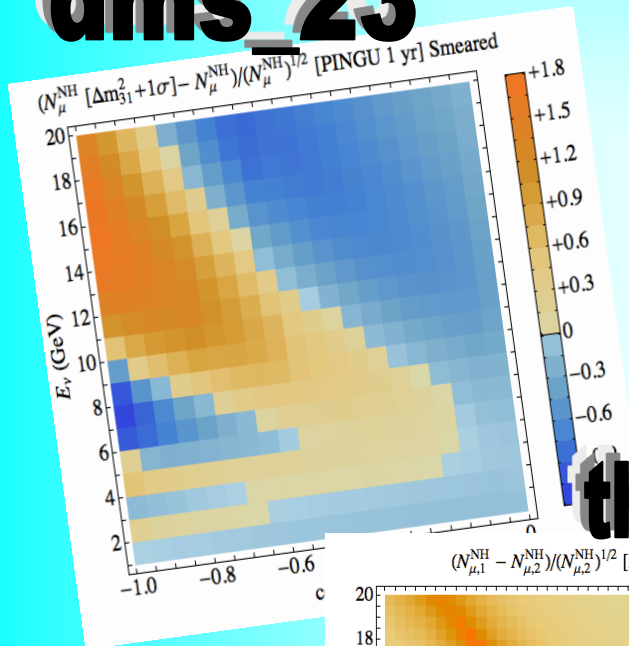
NOVA

further substantial improvements

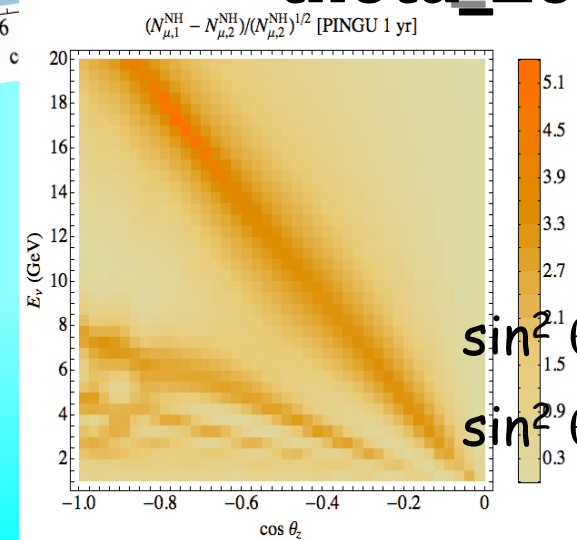
Distinguishing $-\pi/2$ from 0 at $> 3\sigma$ level?

Other physics

dms_23

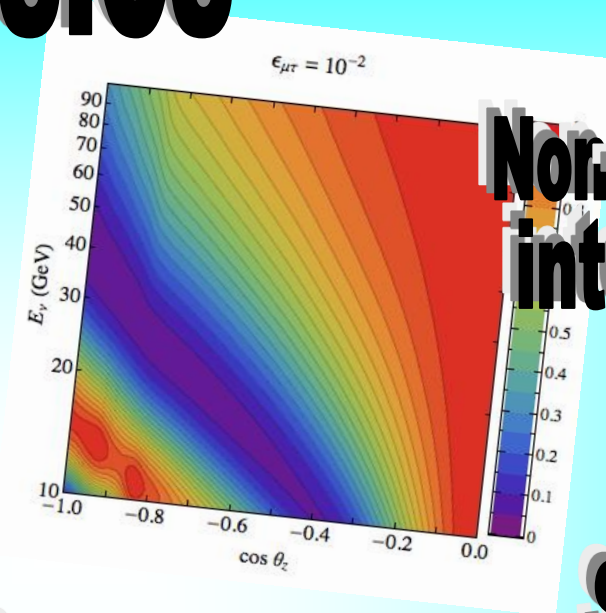


theta_23



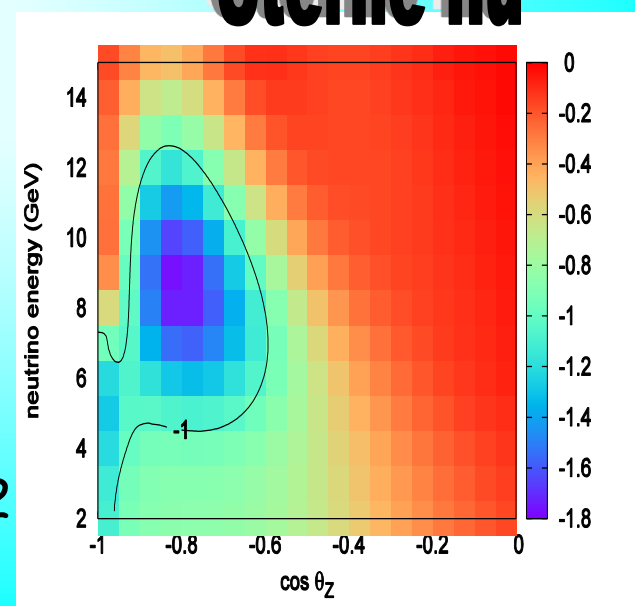
$$\sin^2 \theta_{32, \text{fit}} = 0.50$$

$$\sin^2 \theta_{32, \text{true}} = 0.42$$

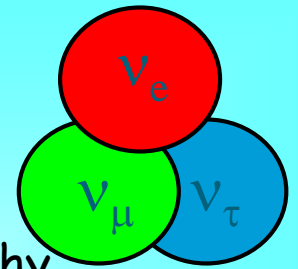


Non-standard interactions

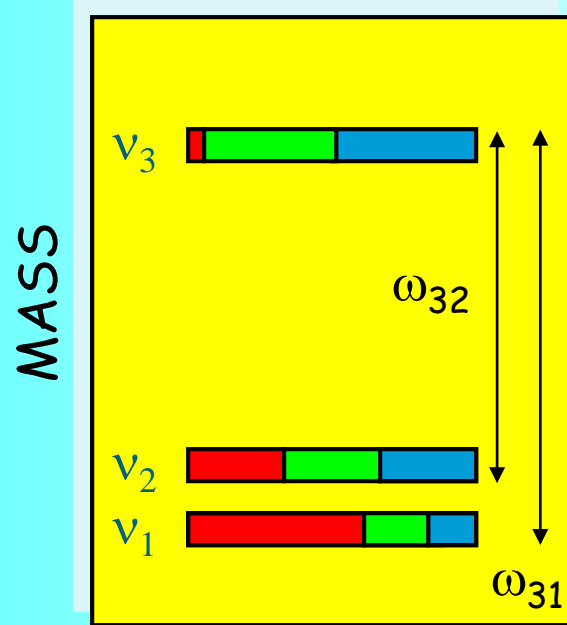
Sterile nu



Mass ordering with reactors



Normal hierarchy



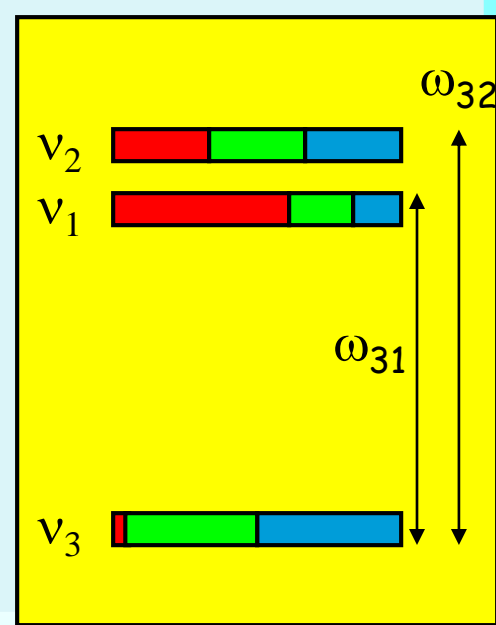
Oscillation frequency
 $\omega_{ij} = \Delta m^2_{ij} / 2E$

Oscillation depth:

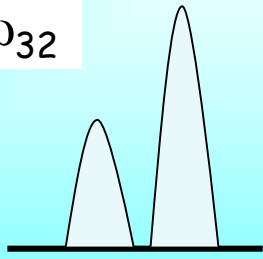
$$D_{31} = 4|U_{e1}|^2|U_{e3}|^2$$

$$D_{31} \sim 2D_{32}$$

Inverted hierarchy



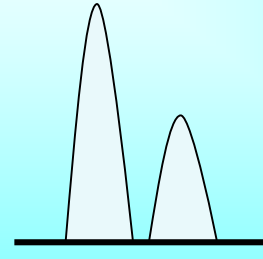
$$\omega_{31} > \omega_{32}$$



ω

Fourier analysis

$$\omega_{31} < \omega_{32}$$



ω

Higher frequency - larger depth

Higher frequency - smaller depth

$$D_{32} = 4|U_{e2}|^2|U_{e3}|^2$$

S. Petcov
M. Piai

JUNO

Jiangmen Underground
Neutrino Observatory

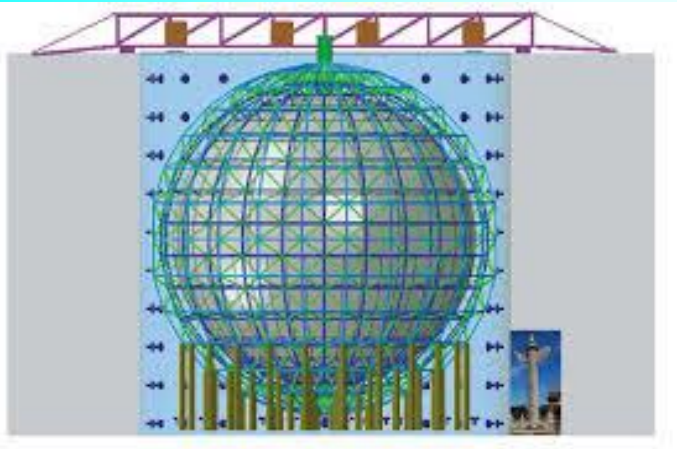
$d = 700 \text{ m}$, $L = 53 \text{ km}$, $P = 36 \text{ GW}$

20 kt LAB scintillator

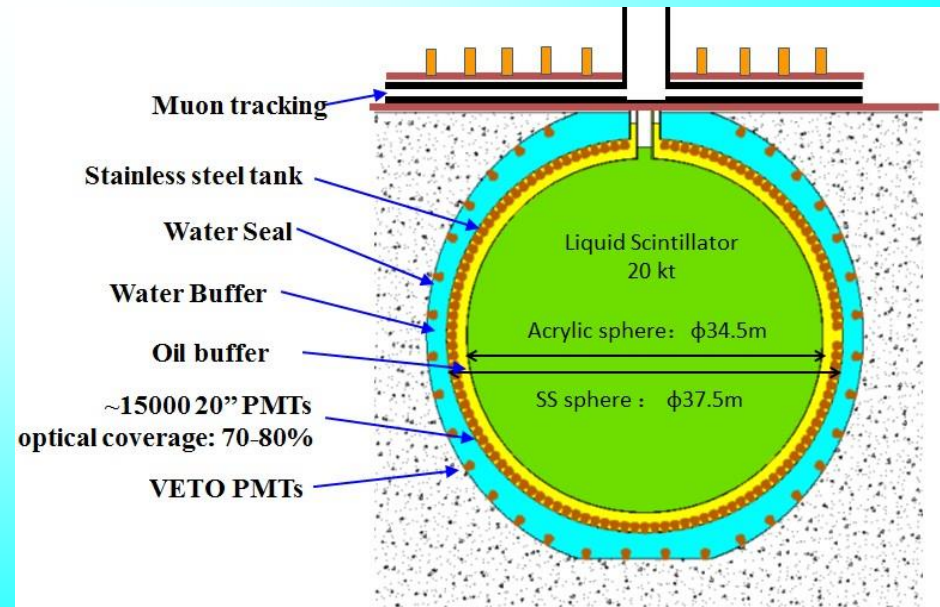
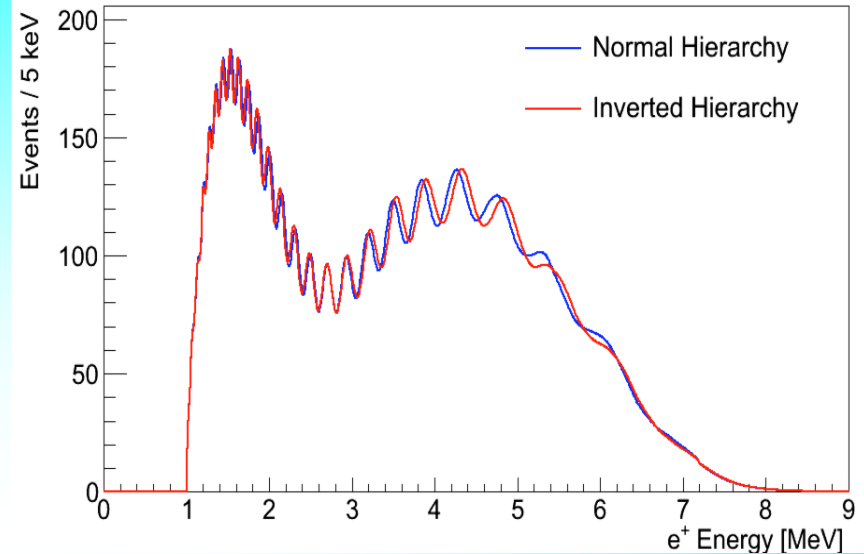
$n + p \rightarrow d + \gamma$

Key requirement:
energy resolution 3% at 1 MeV

Operation in 2020
(3 - 4) σ in 6 years



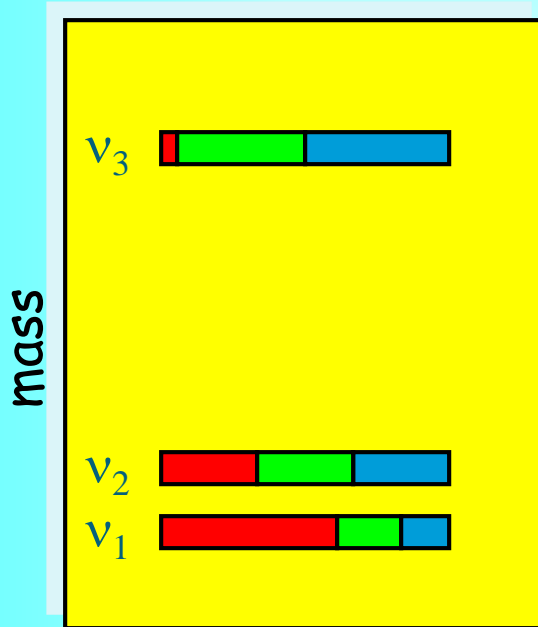
Also RENO-50



Leptons versus quarks

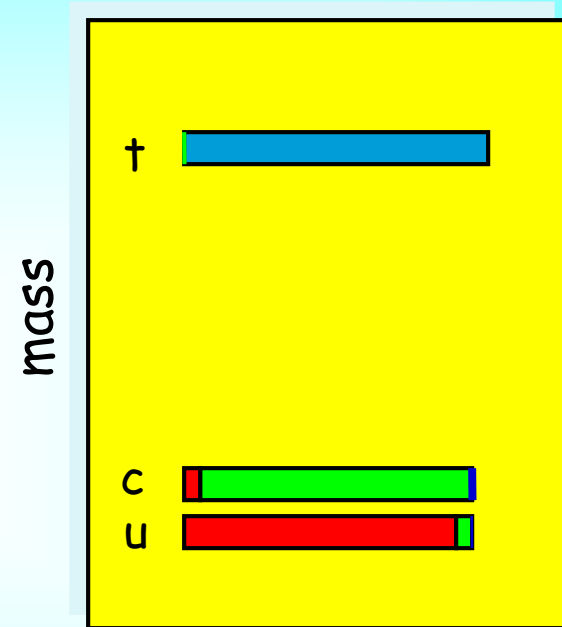
special

normal



Leptons

$$\nu_f = U_{\text{PMNS}} \nu_{\text{mass}}$$



Quarks

$$U_d = V_{\text{CKM}}^+ U$$

$$U = (u, c, t)$$

combination of down-quarks
produced with a given up quark

Solar neutrinos: 1-2 normal ordering

Determined with matter effects on the solar neutrinos

suppression at high energies is smaller than at low energies

$$P_{ee} = \begin{cases} |U_{e2}|^2 \sim \sin^2\theta_{12} \sim 0.3 & \text{for NH} \\ |U_{e1}|^2 \sim \cos^2\theta_{12} \sim 0.7 & \text{for IH} \end{cases}$$

The problem is to determine the 1-3 or 2-3 ordering

Solar neutrinos are not sensitive to 1-3 ordering due to very small matter effect on 1-3 mixing:

$$\sin\theta_{13}^m = \sin\theta_{13} \left(1 \pm \frac{2EV \cos 2\theta_{13}}{\Delta m_{31}^2} \right)$$

NH / IH

few 10^{-2}

Suppression of effects

Original
fluxes



different flavors:
 ν_e and ν_μ

Screening
factors $(1 - r s_{23}^2)$



neutrinos and
antineutrinos

$(1 - \kappa_e)$

$(1 - \kappa_\mu)$

Reduces CP-
asymmetry

Integration
averaging

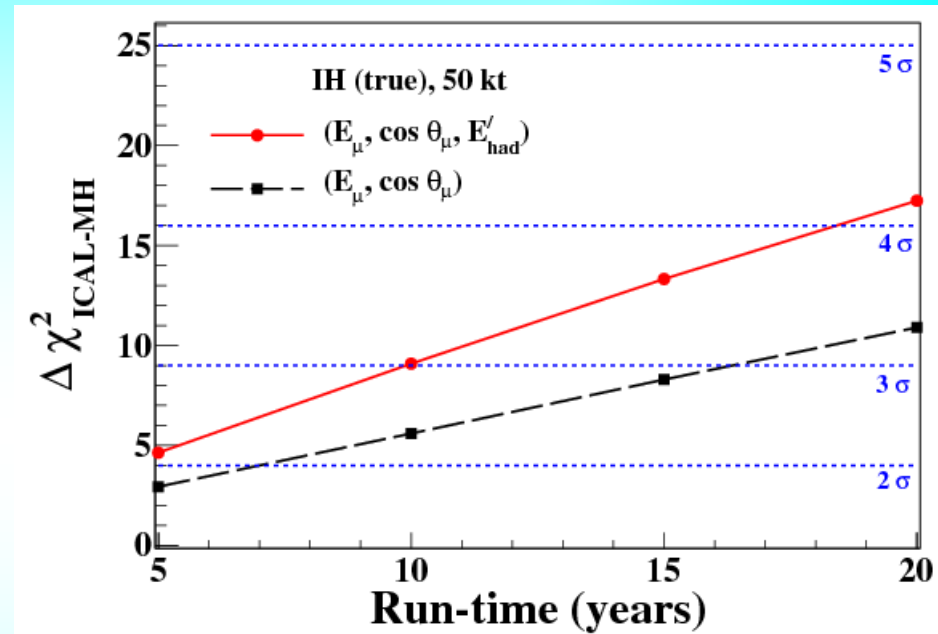
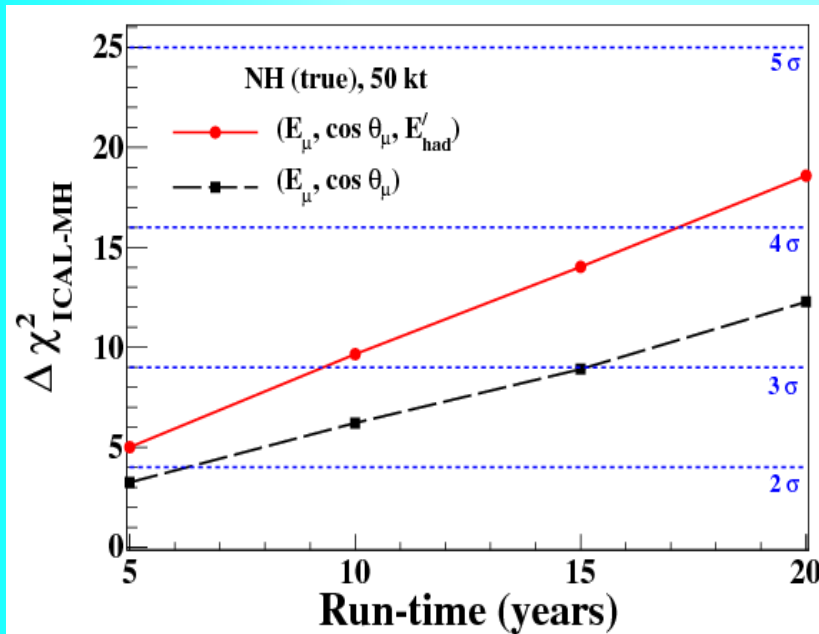
averaging and smoothing effects
reconstruction of neutrino energy
and direction

Detection

identification of flavor

INO-ICAL

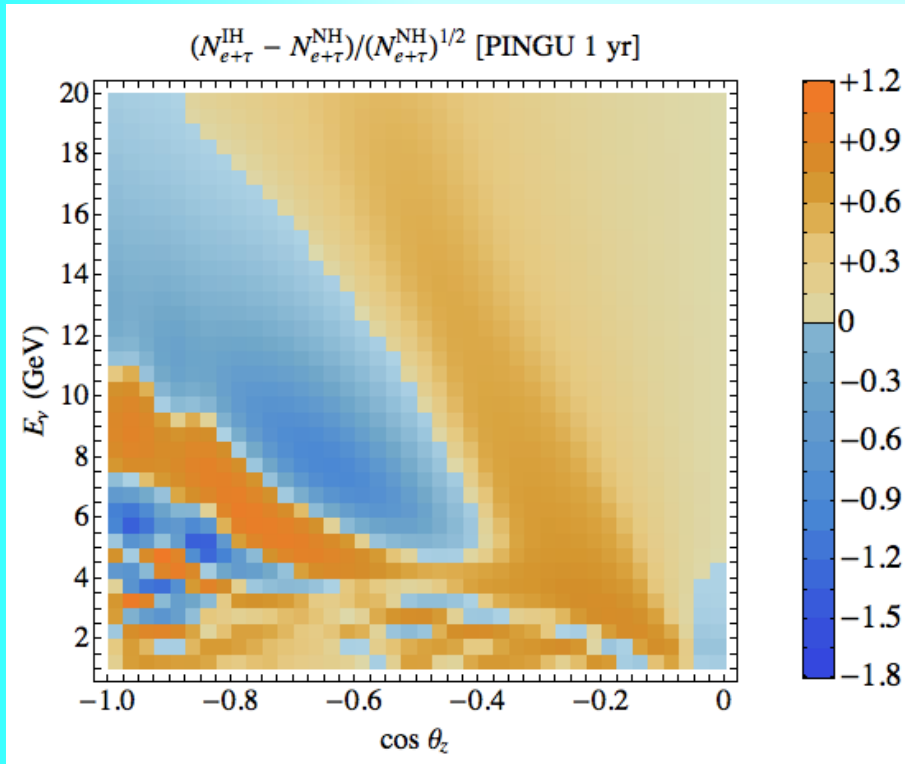
ICAL Collaboration (Ahmed Shakeel et al.)
arXiv:1505.07380 [physics.ins-det]



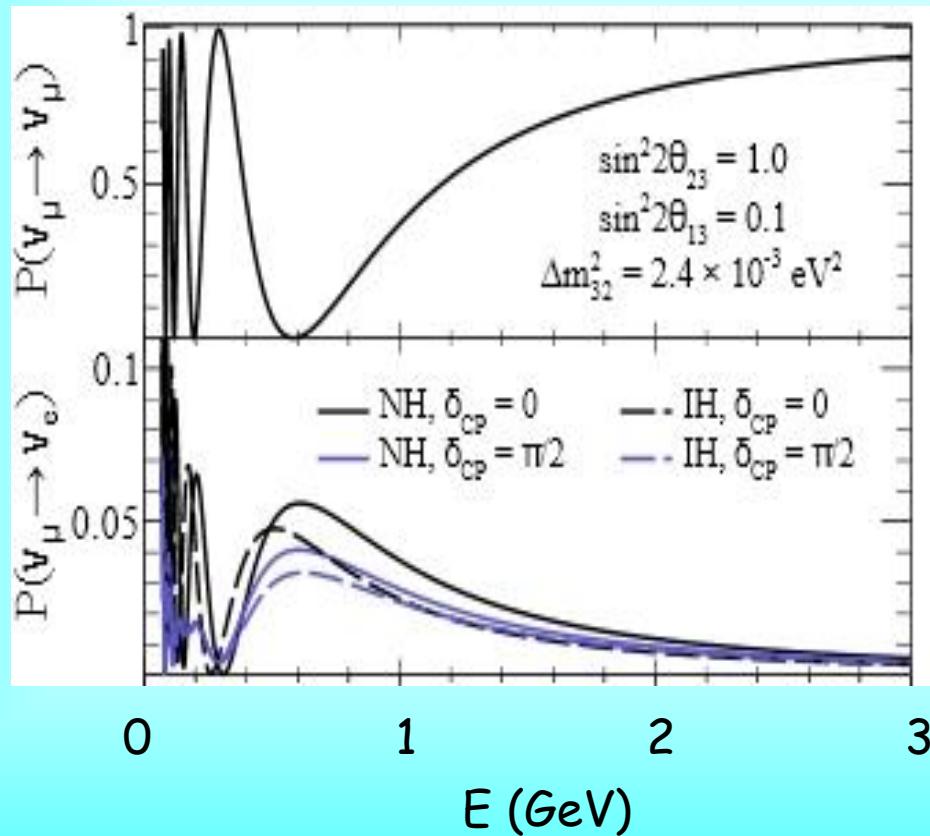
The hierarchy sensitivity of ICAL with input normal hierarchy including correlated hadron energy information, with $|\Delta m^2_{\text{eff}}|$, $\sin^2 \theta_{23}$ and $\sin^2 \theta_{13}$ marginalised over their 3σ ranges. Improvement with the inclusion of hadron energy is significant. $\Delta \chi^2_{\text{ICAL-MH}}$ as a function of the exposure assuming NH (left panel) and IH (right panel) as true hierarchy.

Cascade events $e + \text{neutrino}$

S. Razzque and A.Y.S.,

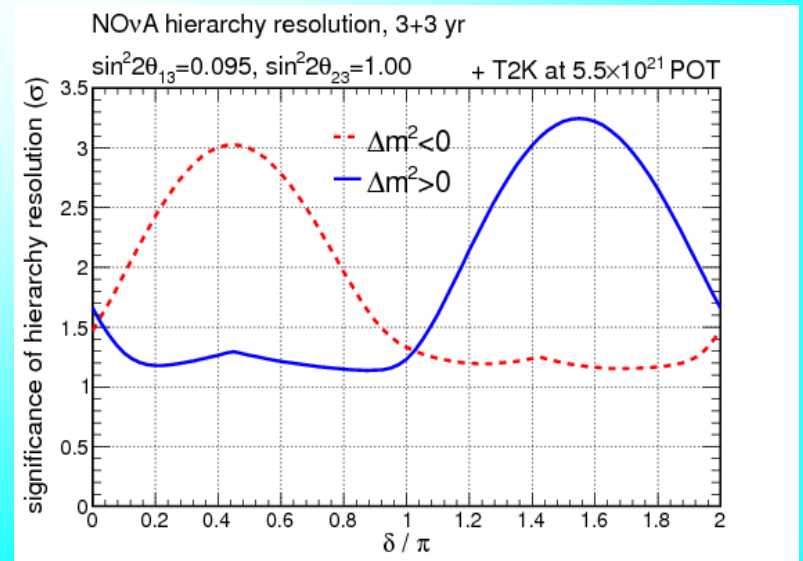
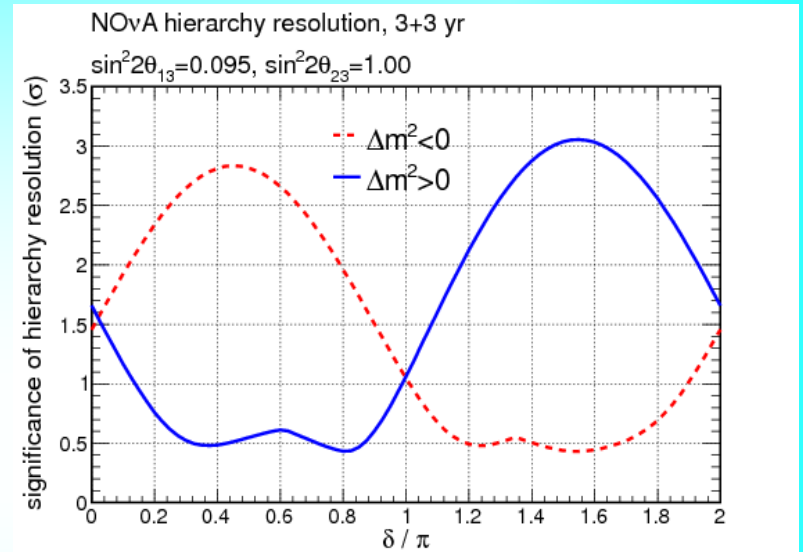
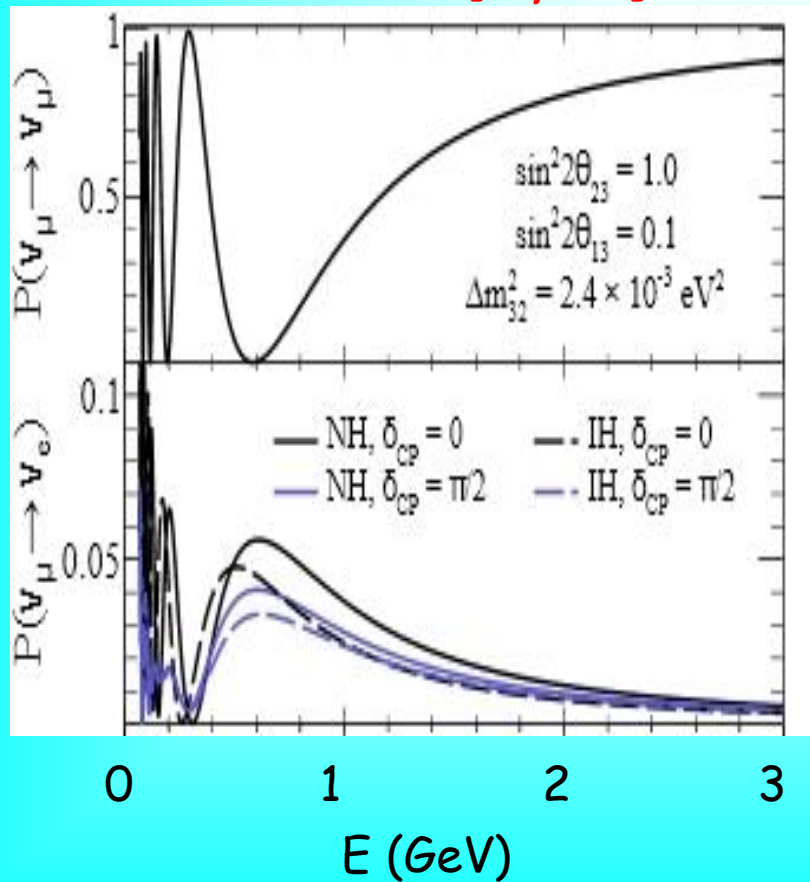


Oscillation probabilities



NOvA and T2K sensitivity

T2K Collaboration (K. Abe et al.)
 Phys.Rev. D91 (2015) 7, 072010
 arXiv:1502.01550 [hep-ex]

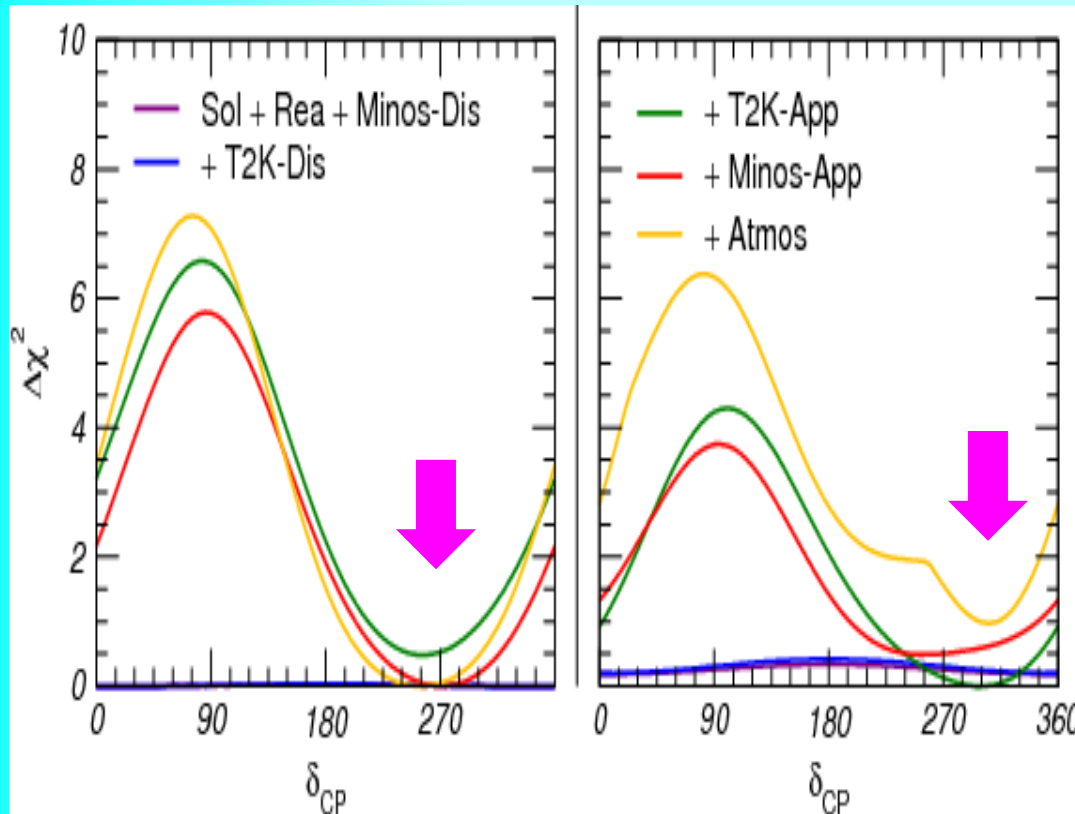


CP-phase from global fit

*M.C. Gonzalez-Garcia, M. Maltoni,
T. Schwetz, JHEP 1411 (2014)
052, 1409.5439 [hep-ph]*

Inverted

Normal



Contribution of different sets of experimental results to the determination of the mass ordering, the octant of θ_{23} and of the CP violating phase.

Genesis of determination

Solar
Reactors
MINOS dis

+ T2K - Dis

+ T2K-App

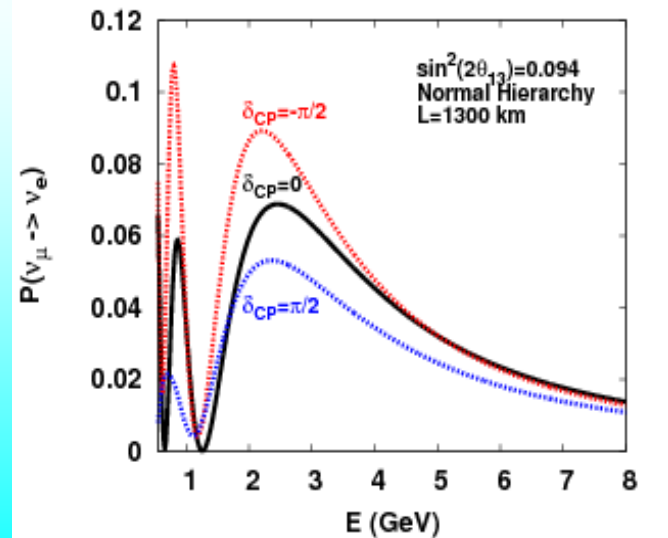
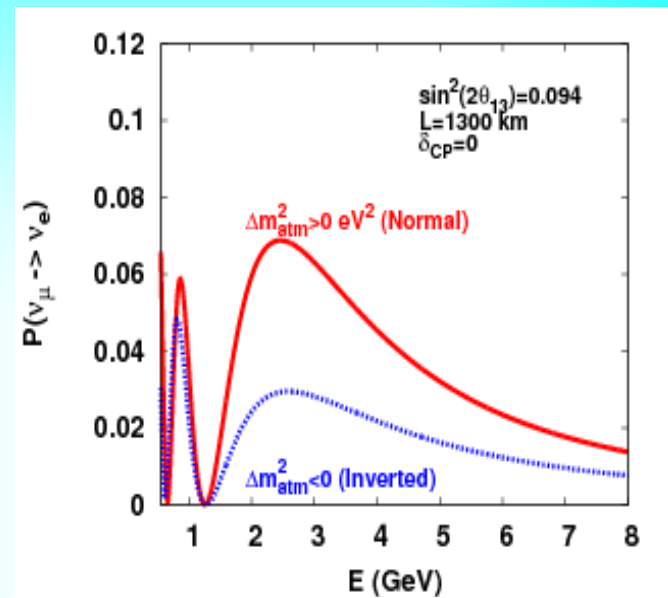
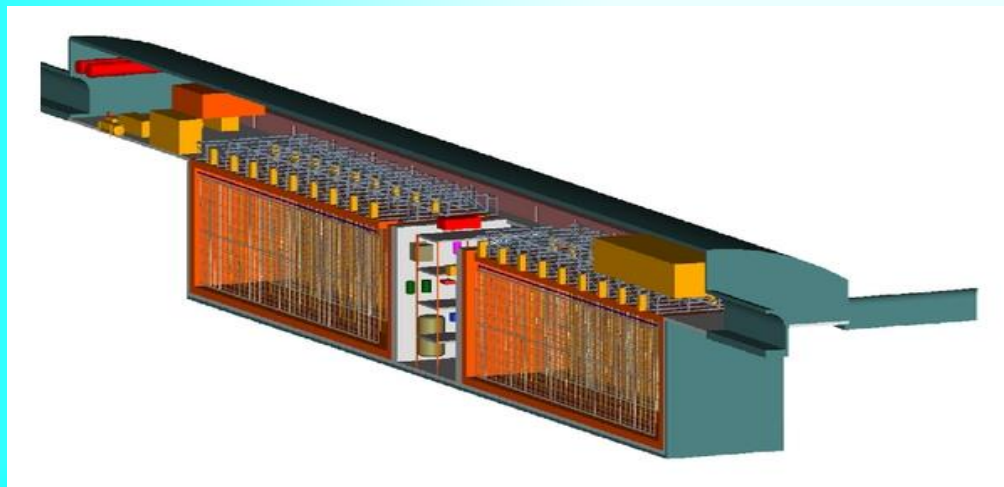
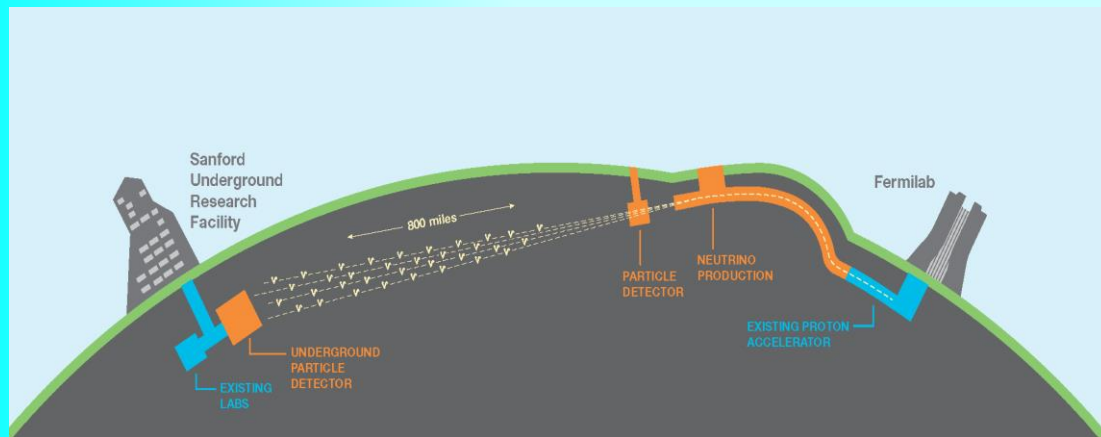
+ MINOS-App

+ Atmospheric

Atm nu contribution: excess
of sub GeV nue events

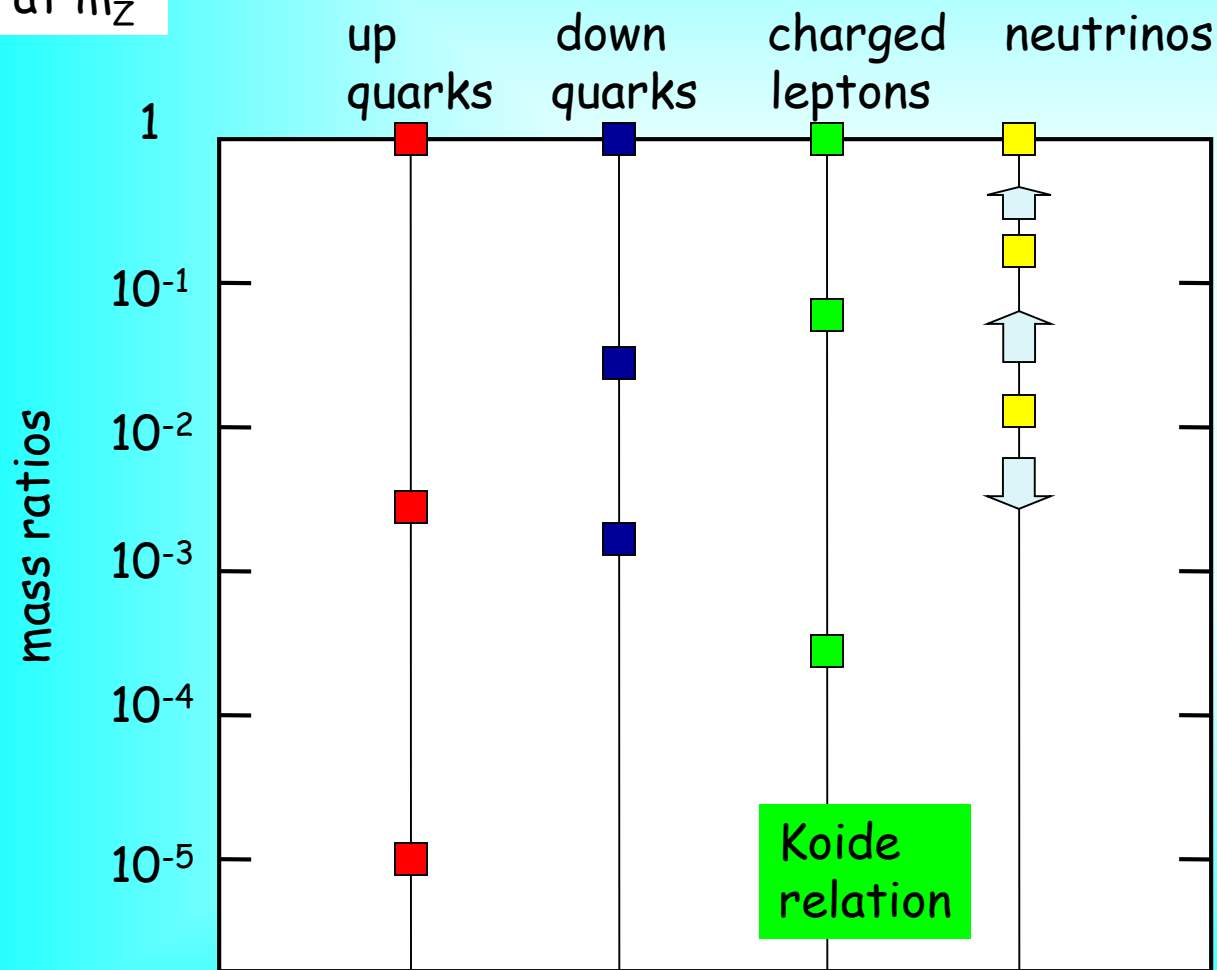
LBNF-DUNE

$L = 1300\text{km}$, LAr TPC 35 kt



Mass hierarchies

at m_Z



$$\frac{m_2}{m_3} \geq \sqrt{\frac{\Delta m_{21}^2}{\Delta m_{32}^2}}$$

~ 0.18

Neutrinos have the weakest mass hierarchy (if any) among fermions

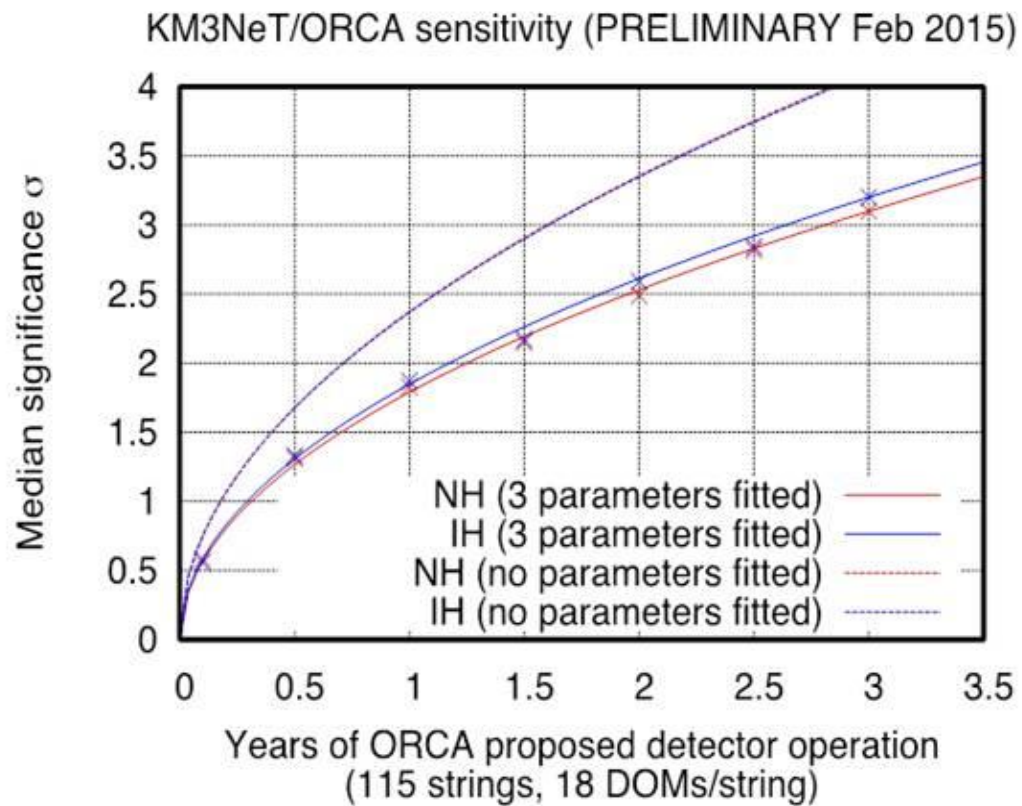
Related to large lepton mixing?

$$m_u m_t = m_c^2$$

$$\sin \theta_C \sim \sqrt{m_d/m_s}$$

Gatto-Sartori-Tonin relation

Sensitivity to MH



CP-violation and CP-phase

Dirac CP-phase in the standard parametrization of the PMNS matrix

$$\nu_f = U_{\text{PMNS}} \nu_{\text{mass}}$$

$$U_{\text{PMNS}} = U_{23} I_\delta U_{13} I_{-\delta} U_{12}$$

$$I_\delta = \text{diag}(1, 1, e^{i\delta})$$

CP-transformations:

$$\nu \rightarrow \nu^c$$

$$\nu^c = i \gamma_0 \gamma_2 \nu^\dagger$$

upto Majorana phase

Under CP-transformations:

Matter potential

$$U_{\text{PMNS}} \rightarrow U_{\text{PMNS}}^*$$



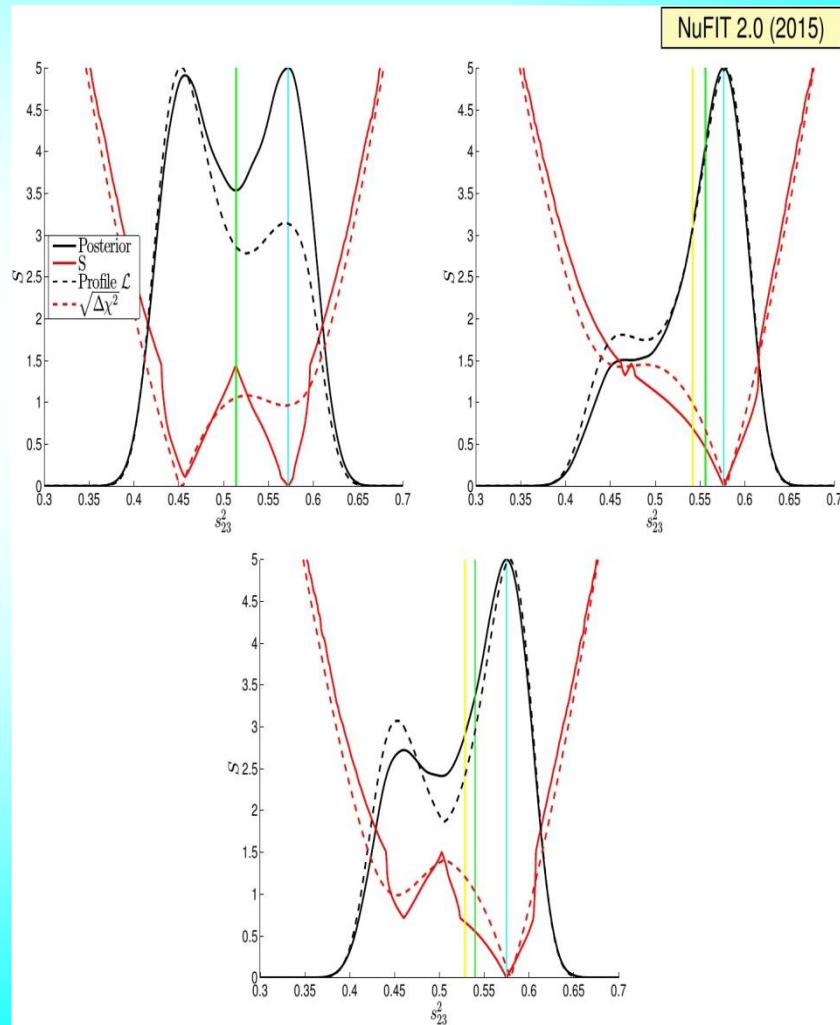
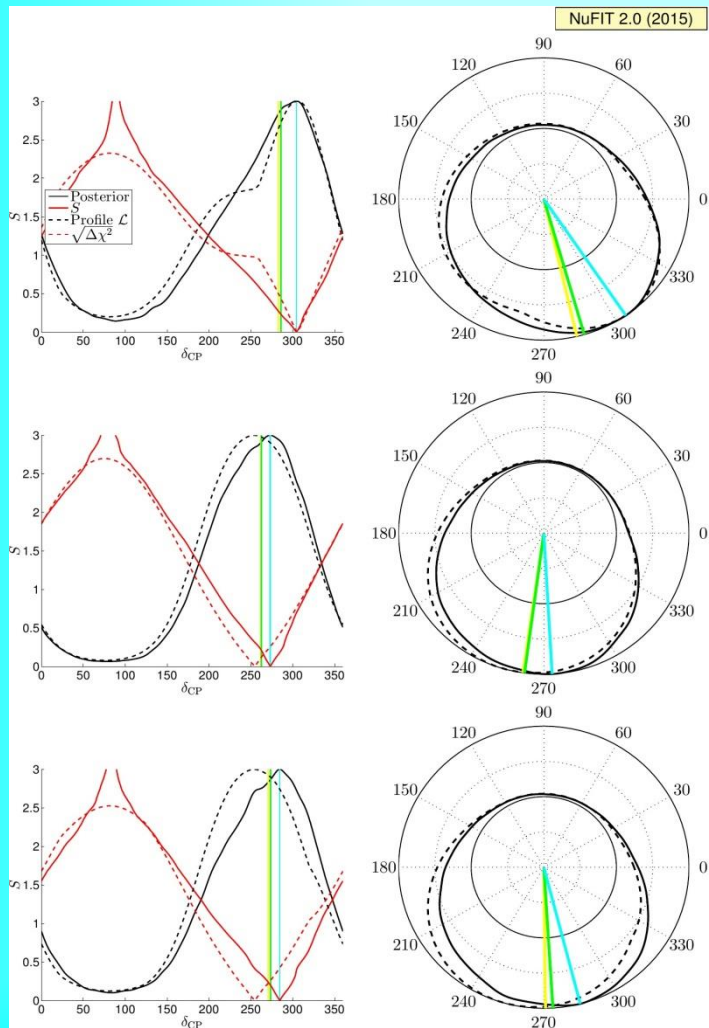
$$\delta \rightarrow -\delta$$

$$V \rightarrow -V$$

usual medium is C-asymmetric which leads to CP asymmetry of interactions

Degeneracy of effects:
Matter can imitate CP-violation

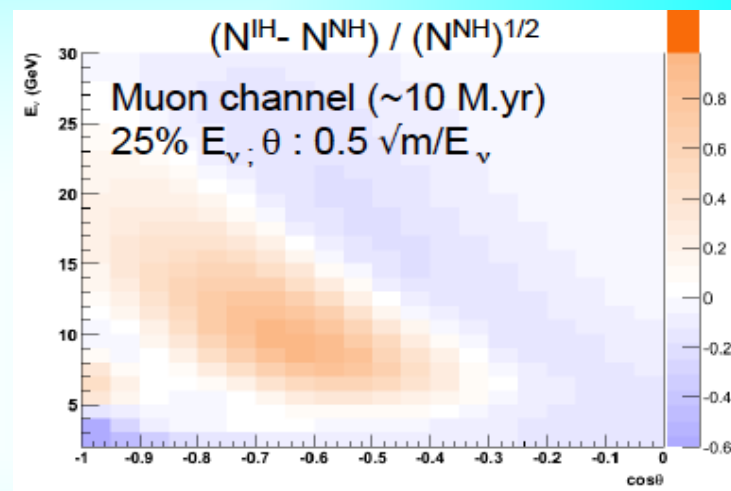
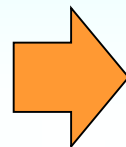
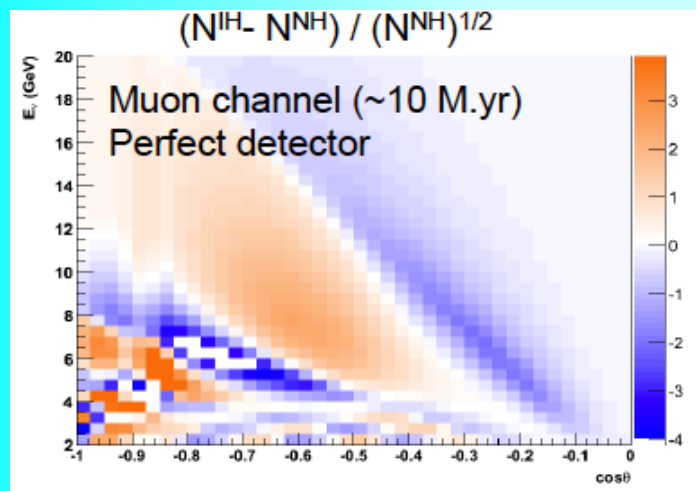
Global Fit



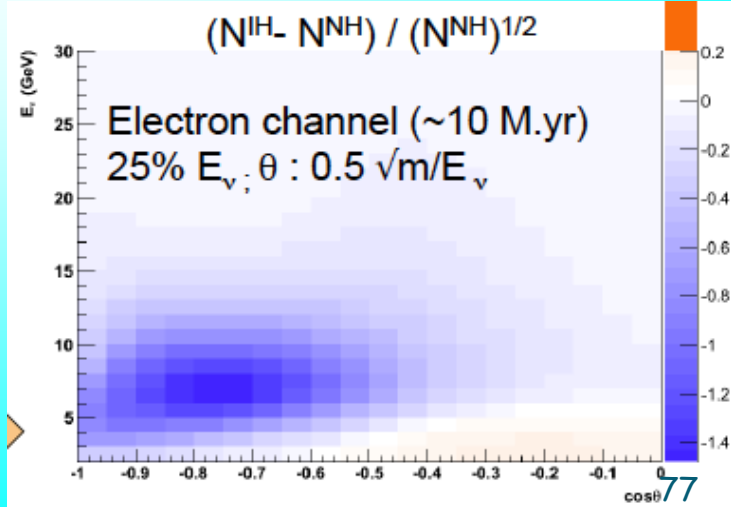
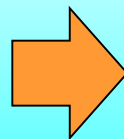
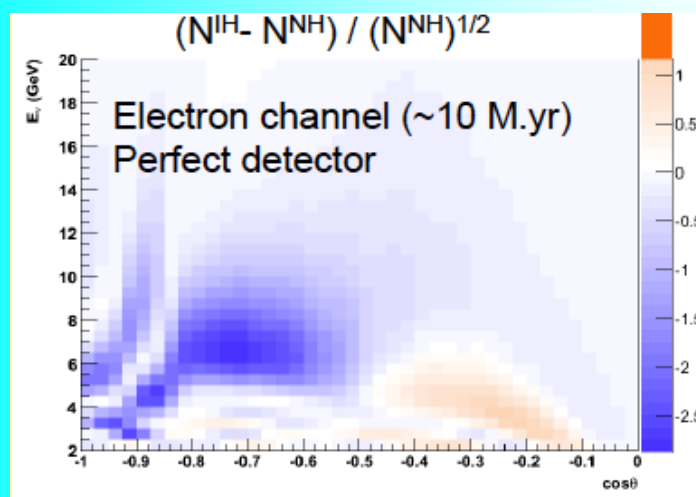
Smearred distributions

J. Brunner [532]

Muon- and electron-channels contribute to net hierarchy asymmetry.
Electron channel more robust against detector resolution effects:

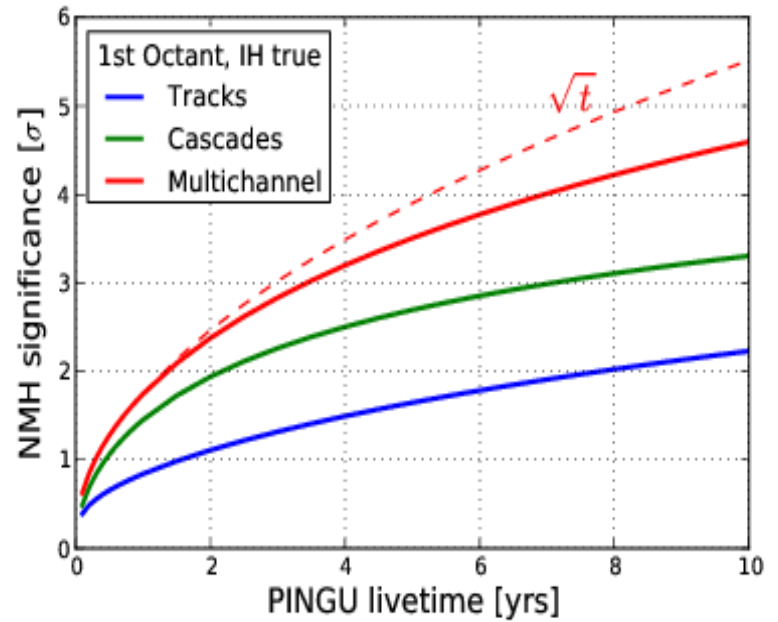
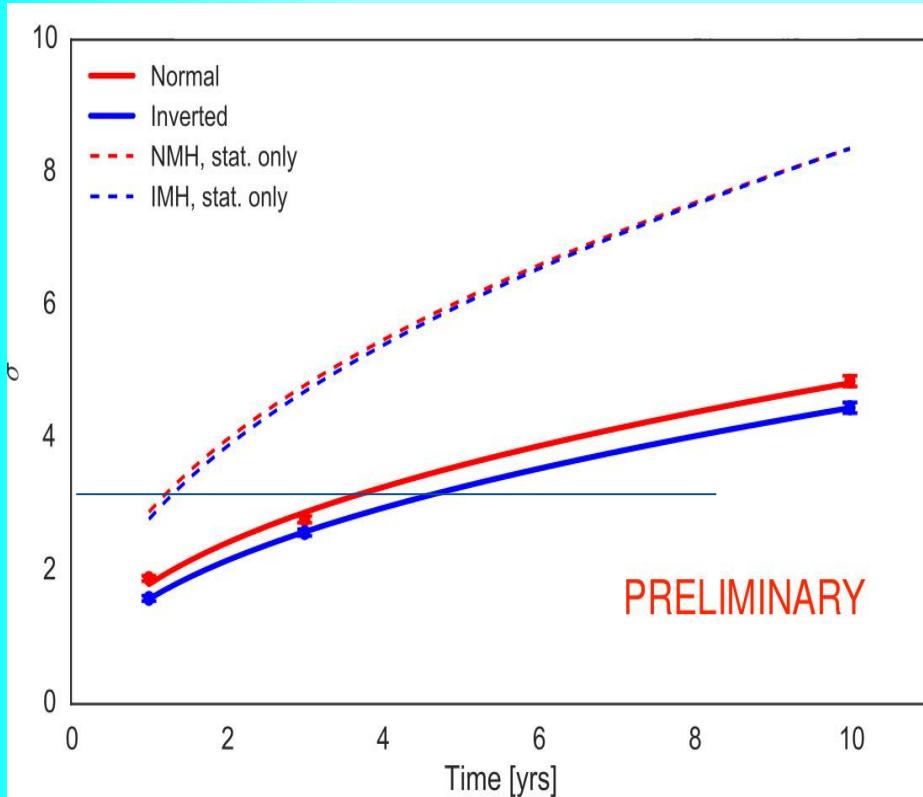


E, θ smearing
(kinematics
+ detector
resolution)



Sensitivity

K. Clark



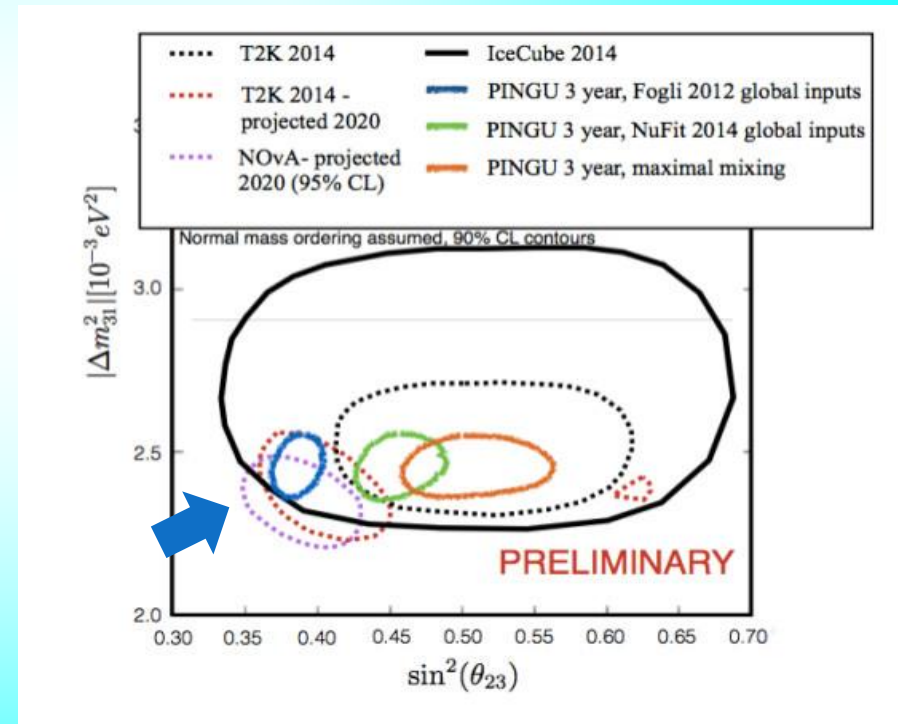
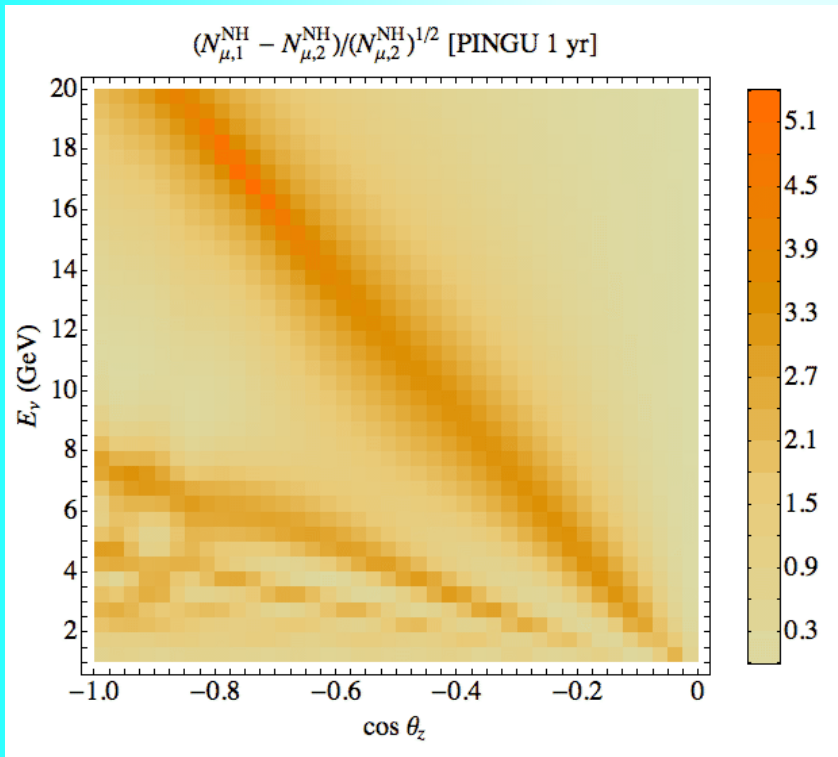
Sensitivity to 2-3 mixing

Deviation from maximal symmetry or no symmetry

K. Clark, [1379]

Quadrant

Sensitivity to MH depends on

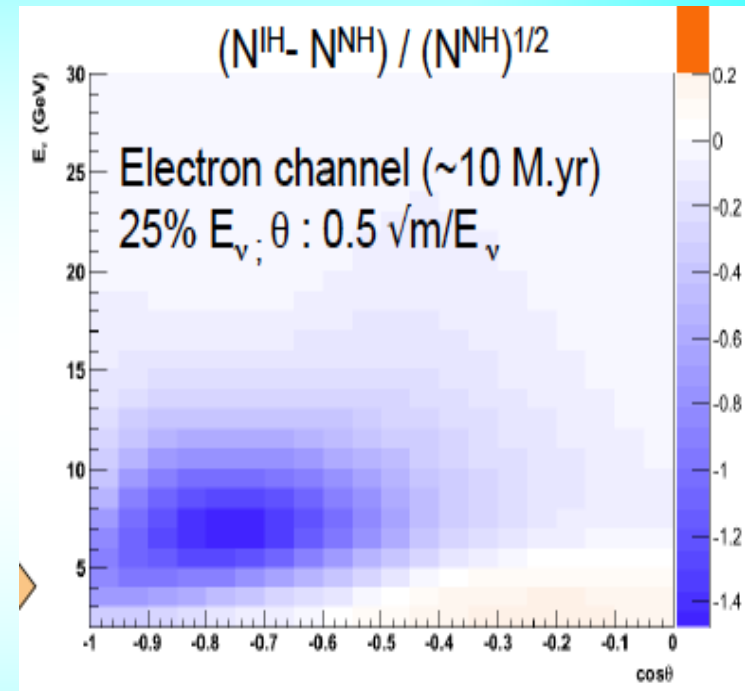
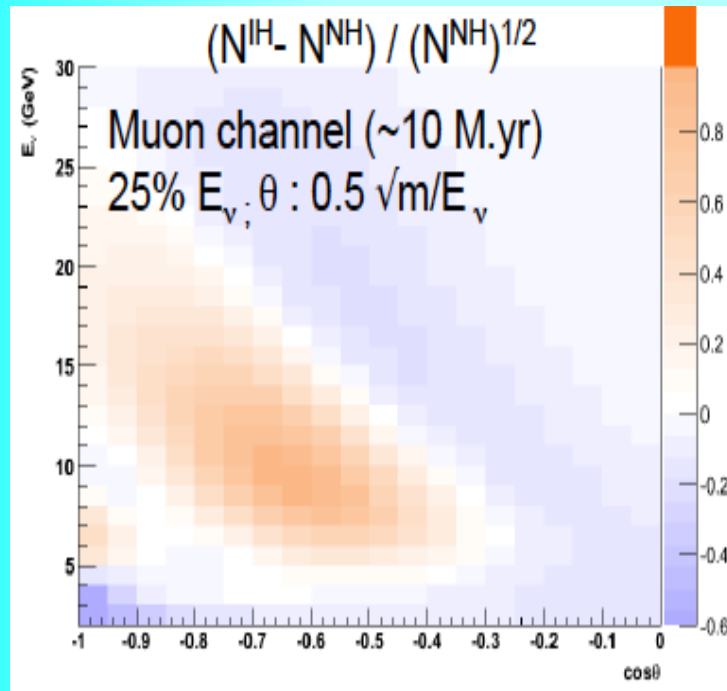


$$\sin^2 \theta_{32, \text{fit}} = 0.50$$

$$\sin^2 \theta_{32, \text{true}} = 0.42$$

Smearred distributions

J. Brunner



Muon- and electron-channels contribute to net hierarchy asymmetry.
Electron channel more robust against detector resolution effects:

Symmetries of Hidden sector