

HEFT BASIS OVERVIEW

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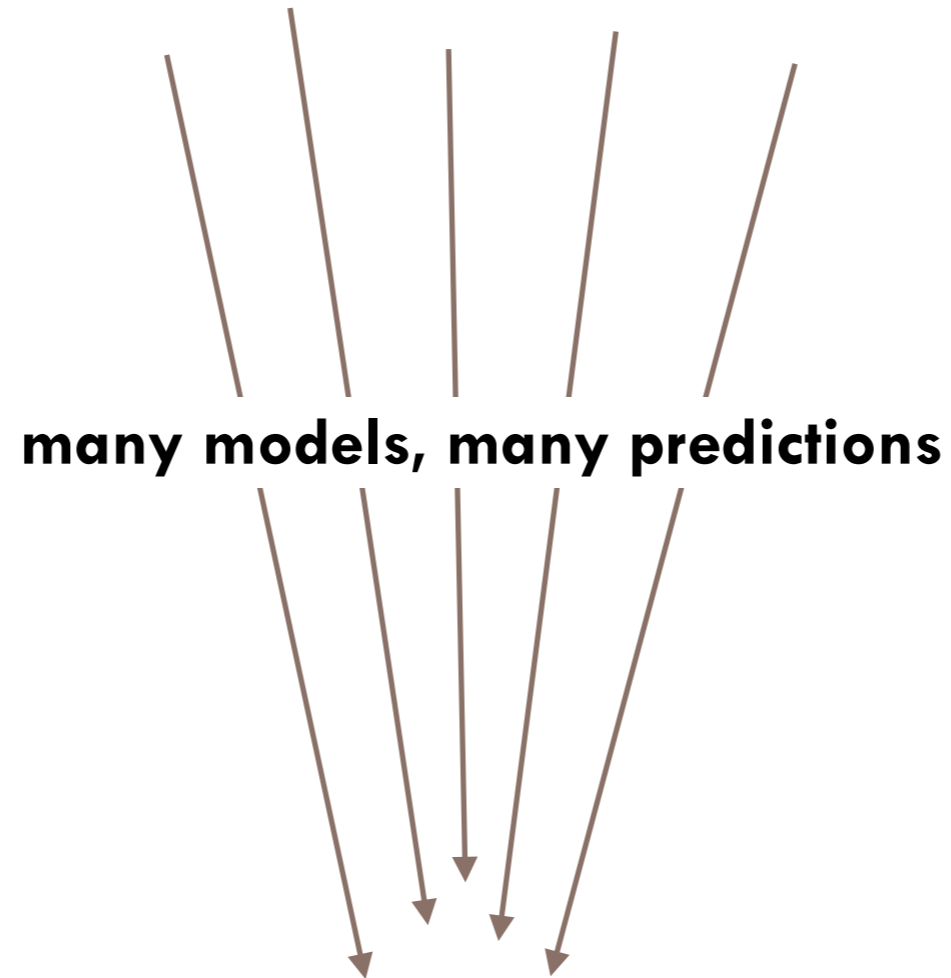
Higgs (N)NLO MC and Tools Workshop for LHC RUN-2, December 17-19, 2014

UV dynamics (BSM models)

Experiments

(performed at “low” energies)

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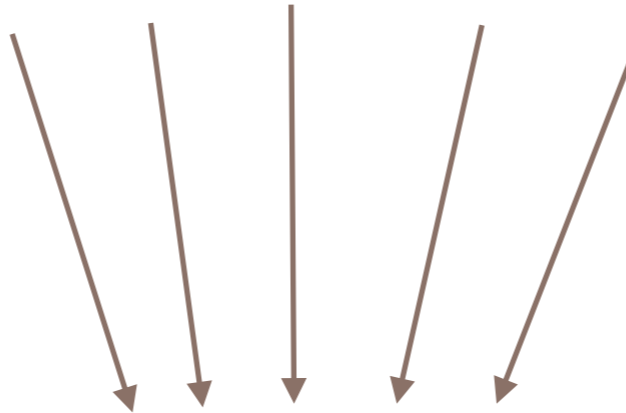


many models, many predictions

Experiments

(performed at "low" energies)

UV dynamics (BSM models)



Effective field theory description



Experiments

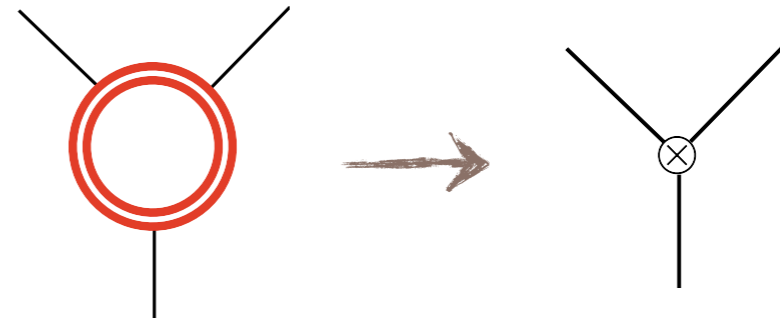
(performed at “low” energies)

- At energies $E \ll m_*$, NP effects are well approximated by local operators

$$\mathcal{L} = \sum_i \bar{c}_i O_i(x)$$

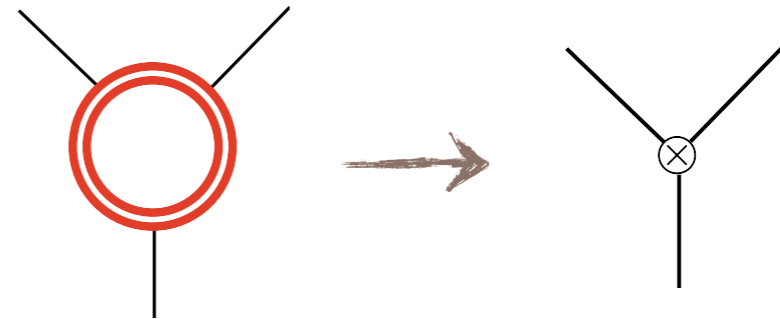
Operators “generated” at m_* with coefficients

$$\bar{c}_i(m_*) \sim \left(\frac{1}{m_*} \right)^{d[O]-4}$$



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Assumptions:

1. There is a gap between the NP scale m_* and m_h
2. The new boson is part of an $SU(2)_L$ doublet

$$H = e^{i\pi/v} \begin{pmatrix} 0 \\ v + h \end{pmatrix}$$

Effective Lagrangian for a Higgs doublet

(1 fermion generation)

- Operators can be classified according to their dimension

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \bar{c}_i O_i \equiv \mathcal{L}_{SM} + \Delta\mathcal{L}^{(6)} + \Delta\mathcal{L}^{(8)} + \dots$$

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Leading effects from dim-6 operators

59 independent operators for 1 SM family

Buchmuller and Wyler NPB 268 (1986) 621

⋮

Grzadkowski et al. JHEP 1010 (2010) 085

For a review see:

RC, Ghezzi, Grojean, Muhlleitner, Spira JHEP 1307 (2013) 035

Effective Lagrangian for a Higgs doublet

(1 fermion generation)

$$\Delta\mathcal{L}^{(6)} = \Delta\mathcal{L}_{SILH} + \Delta\mathcal{L}_{cc} + \Delta\mathcal{L}_{dipole} + \Delta\mathcal{L}_V + +\Delta\mathcal{L}_{4\psi}$$

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16 operators
(12 CP even, 4 CP odd)

SILH operators

Giudice, Grojean, Pomarol, Rattazzi JHEP 0706 (2007) 045

$$\begin{aligned} \Delta\mathcal{L}_{SILH} = & \frac{\bar{c}_H}{2v^2} \partial^\mu (H^\dagger H) \partial_\mu (H^\dagger H) + \frac{\bar{c}_T}{2v^2} \left(H^\dagger \overleftrightarrow{D}^\mu H \right) \left(H^\dagger \overleftrightarrow{D}_\mu H \right) - \frac{\bar{c}_6 \lambda}{v^2} (H^\dagger H)^3 \\ & + \left(\frac{\bar{c}_u}{v^2} y_u H^\dagger H \bar{q}_L H^c u_R + \frac{\bar{c}_d}{v^2} y_d H^\dagger H \bar{q}_L H d_R + \frac{\bar{c}_l}{v^2} y_l H^\dagger H \bar{L}_L H l_R + h.c. \right) \\ & + \frac{i\bar{c}_W g}{2m_W^2} \left(H^\dagger \sigma^i \overleftrightarrow{D}^\mu H \right) (D^\nu W_{\mu\nu})^i + \frac{i\bar{c}_B g'}{2m_W^2} \left(H^\dagger \overleftrightarrow{D}^\mu H \right) (\partial^\nu B_{\mu\nu}) \\ & + \frac{i\bar{c}_{HW} g}{m_W^2} (D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i + \frac{i\bar{c}_{HB} g'}{m_W^2} (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu} \\ & + \frac{\bar{c}_\gamma g'^2}{m_W^2} H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{\bar{c}_g g_S^2}{m_W^2} H^\dagger H G_{\mu\nu}^a G^{a\mu\nu} \\ & + \frac{i\tilde{c}_{HW} g}{m_W^2} (D^\mu H)^\dagger \sigma^i (D^\nu H) \tilde{W}_{\mu\nu}^i + \frac{i\tilde{c}_{HB} g'}{m_W^2} (D^\mu H)^\dagger (D^\nu H) \tilde{B}_{\mu\nu} \\ & + \frac{\tilde{c}_\gamma g'^2}{m_W^2} H^\dagger H B_{\mu\nu} \tilde{B}^{\mu\nu} + \frac{\tilde{c}_g g_S^2}{m_W^2} H^\dagger H G_{\mu\nu}^a \tilde{G}^{a\mu\nu} \end{aligned}$$

Effective Lagrangian for a Higgs doublet

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$$\Delta\mathcal{L}^{(6)} = \Delta\mathcal{L}_{SILH} + \Delta\mathcal{L}_{cc} + \Delta\mathcal{L}_{dipole} + \Delta\mathcal{L}_V + \Delta\mathcal{L}_{4\psi}$$

6 current-current operators

$$\begin{aligned} \Delta\mathcal{L}_{cc} = & \frac{i\bar{c}_{Hq}}{v^2} (\bar{q}_L \gamma^\mu q_L) (H^\dagger \overleftrightarrow{D}_\mu H) + \frac{i\bar{c}'_{Hq}}{v^2} (\bar{q}_L \gamma^\mu \sigma^i q_L) (H^\dagger \sigma^i \overleftrightarrow{D}_\mu H) \\ & + \frac{i\bar{c}_{Hu}}{v^2} (\bar{u}_R \gamma^\mu u_R) (H^\dagger \overleftrightarrow{D}_\mu H) + \frac{i\bar{c}_{Hd}}{v^2} (\bar{d}_R \gamma^\mu d_R) (H^\dagger \overleftrightarrow{D}_\mu H) \\ & + \left(\frac{i\bar{c}_{Hud}}{v^2} (\bar{u}_R \gamma^\mu d_R) (H^{c\dagger} \overleftrightarrow{D}_\mu H) + h.c. \right) \\ & + \frac{i\bar{c}_{HL}}{v^2} (\bar{L}_L \gamma^\mu L_L) (H^\dagger \overleftrightarrow{D}_\mu H) \end{aligned}$$

Notice: two additional operators, O'_{HL} and O_{Hl} , are not independent w.r.t. those in $\Delta\mathcal{L}_{SILH}$

$$O'_{HL} = (\bar{L}_L \gamma^\mu \sigma^i L_L) (H^\dagger \sigma^i \overleftrightarrow{D}_\mu H)$$

$$O_{Hl} = (\bar{l}_R \gamma^\mu l_R) (H^\dagger \overleftrightarrow{D}_\mu H)$$

Effective Lagrangian for a Higgs doublet

(1 fermion generation)

$$\Delta\mathcal{L}^{(6)} = \Delta\mathcal{L}_{SILH} + \Delta\mathcal{L}_{cc} + \Delta\mathcal{L}_{dipole} + \Delta\mathcal{L}_V + \Delta\mathcal{L}_{4\psi}$$

8 dipole operators

$$\begin{aligned}\Delta\mathcal{L}_{dipole} = & \frac{\bar{c}_{uB} g'}{m_W^2} y_u \bar{q}_L H^c \sigma^{\mu\nu} u_R B_{\mu\nu} + \frac{\bar{c}_{uW} g}{m_W^2} y_u \bar{q}_L \sigma^i H^c \sigma^{\mu\nu} u_R W_{\mu\nu}^i + \frac{\bar{c}_{uG} g_S}{m_W^2} y_u \bar{q}_L H^c \sigma^{\mu\nu} \lambda^a u_R G_{\mu\nu}^a \\ & + \frac{\bar{c}_{dB} g'}{m_W^2} y_d \bar{q}_L H \sigma^{\mu\nu} d_R B_{\mu\nu} + \frac{\bar{c}_{dW} g}{m_W^2} y_d \bar{q}_L \sigma^i H \sigma^{\mu\nu} d_R W_{\mu\nu}^i + \frac{\bar{c}_{dG} g_S}{m_W^2} y_d \bar{q}_L H \sigma^{\mu\nu} \lambda^a d_R G_{\mu\nu}^a \\ & + \frac{\bar{c}_{lB} g'}{m_W^2} y_l \bar{L}_L H \sigma^{\mu\nu} l_R B_{\mu\nu} + \frac{\bar{c}_{lW} g}{m_W^2} y_l \bar{L}_L \sigma^i H \sigma^{\mu\nu} l_R W_{\mu\nu}^i + h.c.\end{aligned}$$

Effective Lagrangian for a Higgs doublet

(1 fermion generation)

$$\Delta\mathcal{L}^{(6)} = \Delta\mathcal{L}_{SILH} + \Delta\mathcal{L}_{cc} + \Delta\mathcal{L}_{dipole} + \boxed{\Delta\mathcal{L}_V} + \Delta\mathcal{L}_{4\psi}$$

7 operators built with gauge fields only
(5 CP even, 2 CP odd)

$$\begin{aligned} \Delta\mathcal{L}_V = & \frac{\bar{c}_{2W}}{m_W^2} (D^\mu W_{\mu\nu})^i (D_\rho W^{\rho\nu})^i + \frac{\bar{c}_{2B}}{m_W^2} (\partial^\mu B_{\mu\nu}) (\partial_\rho B^{\rho\nu}) + \frac{\bar{c}_{2G}}{m_W^2} (D^\mu G_{\mu\nu})^a (D_\rho G^{\rho\nu})^a \\ & + \frac{\bar{c}_{3W} g^3}{m_W^2} \epsilon^{ijk} W_\mu^{i\nu} W_\nu^{j\rho} W_\rho^{k\mu} + \frac{\bar{c}_{3G} g_S^3}{m_W^2} f^{abc} G_\mu^{a\nu} G_\nu^{b\rho} G_\rho^{c\mu} \\ & + \frac{\tilde{c}_{3W} g^3}{m_W^2} \epsilon^{ijk} W_\mu^{i\nu} W_\nu^{j\rho} \tilde{W}_\rho^{k\mu} + \frac{\tilde{c}_{3G} g_S^3}{m_W^2} f^{abc} G_\mu^{a\nu} G_\nu^{b\rho} \tilde{G}_\rho^{c\mu} \end{aligned}$$

Effective Lagrangian for a Higgs doublet

(1 fermion generation)

$$\Delta\mathcal{L}^{(6)} = \Delta\mathcal{L}_{SILH} + \Delta\mathcal{L}_{cc} + \Delta\mathcal{L}_{dipole} + \boxed{\Delta\mathcal{L}_V} + \boxed{\Delta\mathcal{L}_{4\psi}}$$

22 four-fermion operators

7 operators built with gauge fields only
(5 CP even, 2 CP odd)

$$\begin{aligned} \Delta\mathcal{L}_V = & \frac{\bar{c}_{2W}}{m_W^2} (D^\mu W_{\mu\nu})^i (D_\rho W^{\rho\nu})^i + \frac{\bar{c}_{2B}}{m_W^2} (\partial^\mu B_{\mu\nu}) (\partial_\rho B^{\rho\nu}) + \frac{\bar{c}_{2G}}{m_W^2} (D^\mu G_{\mu\nu})^a (D_\rho G^{\rho\nu})^a \\ & + \frac{\bar{c}_{3W} g^3}{m_W^2} \epsilon^{ijk} W_\mu^{i\nu} W_\nu^{j\rho} W_\rho^{k\mu} + \frac{\bar{c}_{3G} g_S^3}{m_W^2} f^{abc} G_\mu^{a\nu} G_\nu^{b\rho} G_\rho^{c\mu} \\ & + \frac{\tilde{c}_{3W} g^3}{m_W^2} \epsilon^{ijk} W_\mu^{i\nu} W_\nu^{j\rho} \tilde{W}_\rho^{k\mu} + \frac{\tilde{c}_{3G} g_S^3}{m_W^2} f^{abc} G_\mu^{a\nu} G_\nu^{b\rho} \tilde{G}_\rho^{c\mu} \end{aligned}$$

SILH basis vs Warsaw basis

SILH basis

JHEP 0706 (2007) 045

$$\left\{ O_W, O_B, O_{HW}, O_{HB} \right\}$$



basis of Grzadkowski et al.

JHEP 1010 (2010) 085

$$\left\{ O_{WW}, O_{WB}, O'_{HL}, O_{Hl} \right\}$$

$$O_W + O_B = 2 \tan^2 \theta_W (-O_T + O_{H\Psi}^Y) + O'_{Hq} + O'_{HL} + [\dots]$$

$$O_W - O_B = 2 \tan^2 \theta_W (-O_T + O_{H\Psi}^Y) - O'_{Hq} - O'_{HL} - [\dots]$$

$$O_{HW} = O'_{HL} + O'_{Hq} - O_{WB} - O_{WW} + [\dots]$$

$$O_{HB} = 2 \tan^2 \theta_W (-O_T + O_{H\Psi}^Y) - O_{WB} - \frac{1}{4} O_\gamma$$

$$O_{WW} = \frac{g^2}{4m_W^2} H^\dagger H W_{\mu\nu}^i W^{i\mu\nu}$$

$$O_{WB} = \frac{gg'}{4m_W^2} H^\dagger \sigma^i H W_{\mu\nu}^i B^{\mu\nu}$$

$$O_{H\Psi}^Y \equiv \frac{1}{6} O_{Hq} + \frac{2}{3} O_{Hu} - \frac{1}{3} O_{Hd} + \frac{1}{2} O_{HL} - O_{Hl}$$

$$[\dots] = 2 (O_u + O_d + O_l + h.c.) - 6 O_H - 8 O_6$$

does not contribute to 0-Higgs processes

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 O_W + O_B &= 2 \tan^2 \theta_W (-O_T + O_{H\Psi}^Y) + O'_{Hq} + O'_{HL} + [\dots] \\
 O_W - O_B &= 2 \tan^2 \theta_W (-O_T + O_{H\Psi}^Y) - O'_{Hq} - O'_{HL} + [\dots] \\
 O_{HW} &= O'_{HL} + O'_{Hq} - O_{WB} - O_{WW} + [\dots] \\
 O_{HB} &= 2 \tan^2 \theta_W (-O_T + O_{H\Psi}^Y) - O_{WB} - \frac{1}{4} O_\gamma
 \end{aligned}$$

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JHEP 1010 (2010) 085

$$\left\{ O_{WW}, O_{WB}, O'_{HL}, O_{Hl} \right\}$$

constrained by LEP at 10^{-3} level
(parameter ϵ_3)



$$O_W + O_B = 2 \tan^2 \theta_W (-O_T + O_{H\Psi}^Y) + O'_{Hq} + O'_{HL} + [\dots]$$

two combinations constrained by
TGC at 10^{-2} level, third one
bounded only by $h \rightarrow Z\gamma$



$$O_W - O_B = 2 \tan^2 \theta_W (-O_T + O_{H\Psi}^Y) - O'_{Hq} - O'_{HL} - [\dots]$$

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- in order to simplify and retain fewer operators one must estimate which ones are more important: this requires making *assumptions* on the UV dynamics
- assumptions on the UV dynamics are necessarily subjective and driven by our theoretical prejudice
- the most convenient basis is the one which more easily encodes the largest UV effects and matches with the experimental observables

Estimating the coefficients at m_* : the SILH power counting

Giudice et al. JHEP 0706 (2007) 045

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- each extra power of $H(x)$ costs a factor $\frac{g_*}{m_*} \equiv \frac{1}{f}$

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For a strongly-interacting light Higgs (SILH):

$$g_* \gg 1 \quad \rightarrow \quad \frac{1}{f} \gg \frac{1}{m_*}$$

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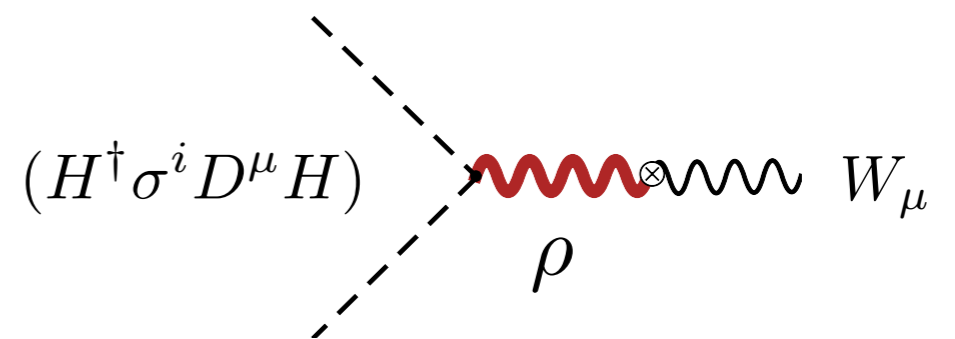
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Example:

$$O_W = \frac{ig}{2m_W^2} (H^\dagger \sigma^i D^\mu H) (D^\nu W_{\mu\nu})^i$$

$$\bar{c}_W \sim \left(\frac{m_W^2}{m_*^2} \right)$$




Secondary Assumptions:

1. The UV physics is minimally coupled

True for some of the popular models (e.g. weakly-coupled SUSY, holographic Higgs), but not necessarily so in more general contexts

see for example: Jenkins, Manohar, Trott JHEP 1309 (2013) 063


 operators generated at loop level suppressed by $(g_*^2/16\pi^2)$
ex: dipole operators

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ex: dipole operators

2. (light) SM fermions are weakly coupled to the UV dynamics

Equivalent to assuming “universality” of NP effects, easier to comply with LEP

 current-current operators subdominant

$$\sim \frac{1}{f^2}$$

$$\partial_\mu (H^\dagger H) \partial^\mu (H^\dagger H)$$

$$\bar{\psi} H \psi (H^\dagger H)$$

$$(H^\dagger H)^3$$

$$\sim \frac{1}{f^2}$$

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$$(H^\dagger H)^3$$

$$\sim \frac{1}{m_*^2}$$

$$\left(H^\dagger \sigma^i \overleftrightarrow{D}^{\mu} H \right) (D^\nu W_{\mu\nu})^i, \quad \left(H^\dagger \overleftrightarrow{D}^{\mu} H \right) (\partial^\nu B_{\mu\nu})$$

$$\sim \frac{1}{f^2} \quad \partial_\mu (H^\dagger H) \partial^\mu (H^\dagger H)$$

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$$\sim \frac{1}{m_*^2} \quad \left(H^\dagger \sigma^i \overleftrightarrow{D}^{\mu} H \right) (D^\nu W_{\mu\nu})^i, \quad \left(H^\dagger \overleftrightarrow{D}^{\mu} H \right) (\partial^\nu B_{\mu\nu})$$

$$\sim \frac{1}{m_*^2} \times \left(\frac{g_*^2}{16\pi^2} \right)$$

$$B_{\mu\nu} B^{\mu\nu} H^\dagger H, \quad G_{\mu\nu} G^{\mu\nu} H^\dagger H$$

$$(D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i, \quad (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}$$

$$F_{\mu\nu} \bar{\psi} \sigma^{\mu\nu} H \psi$$

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$$\sim \frac{1}{m_*^2} \times \left(\frac{\lambda^2}{g_*^2} \right)$$

$$(H^\dagger D_\mu H) (\bar{\psi} \gamma^\mu \psi)$$

$$\sim \frac{1}{f^2}$$

$$\partial_\mu (H^\dagger H) \partial^\mu (H^\dagger H)$$

$$\bar{\psi} H \psi (H^\dagger H)$$

$$(H^\dagger H)^3$$

Leading effects

$$\sim \frac{1}{m_*^2}$$

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**Strongly
constrained
by LEP**

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$$F_{\mu\nu} \bar{\psi} \sigma^{\mu\nu} H \psi$$

$$\sim \frac{1}{m_*^2} \times \left(\frac{\lambda^2}{g_*^2} \right)$$

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$$\sim \frac{1}{m_*^2} \times \left(\frac{g_*^2}{16\pi^2} \right)$$

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Leading effects

$$(D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i, \quad (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}$$

(compete with
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- Add flavor indices to all operators

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- Some constraints much weaker on third generation operators

Ex: dipole operators

Operators that affect Higgs physics only

Elias-Miro, Espinosa, Masso, Pomarol JHEP 1311 (2013) 066

Pomarol, Riva JHEP 01 (2014) 151

$$O_H = (\partial_\mu |H|^2)^2$$

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+ other 3 CP odd

notice: $\frac{g^2}{4m_W^2} H^\dagger H W_{\mu\nu}^i W^{i\mu\nu} \equiv O_{WW} = O_W - O_B + O_{HB} - O_{HW} + \frac{1}{4} O_\gamma$

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shifts all Higgs couplings

$$h \rightarrow \gamma\gamma$$

affect $h \rightarrow Z\gamma$

$$gg \rightarrow h$$

shift $h\psi\psi$

modify inclusive rates and differential distributions (constrained by fit to Higgs couplings)

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Higgs Physics Only	
$\mathcal{O}_H = [\partial_\mu(H^\dagger H)]^2$	1
$\mathcal{O}_{BB} = \frac{g'^2}{4} H ^2 B_{\mu\nu} B^{\mu\nu}$	2
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$\mathcal{O}_{y_u} = y_u H ^2 \bar{Q}_L \tilde{H} u_R$	1
$\mathcal{O}_{y_d} = y_d H ^2 \bar{Q}_L H d_R$	1
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$\mathcal{O}_6 = \lambda H ^6$	1

EW and Higgs Physics	
$\mathcal{O}_W = \frac{ig}{2} \left(H^\dagger \sigma^a \overleftrightarrow{D}^\mu H \right) D^\nu W_{\mu\nu}^a$	2
$\mathcal{O}_B = \frac{ig'}{2} \left(H^\dagger \overleftrightarrow{D}^\mu H \right) \partial^\nu B_{\mu\nu}$	2
$\mathcal{O}_{HB} = ig' (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu}$	2
$\mathcal{O}_T = \frac{1}{2} \left(H^\dagger \overleftrightarrow{D}_\mu H \right)^2$	1
$\mathcal{O}_{Hu} = (iH^\dagger \overleftrightarrow{D}_\mu H) (\bar{u}_R \gamma^\mu u_R)$	1
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$\mathcal{O}_{He} = (iH^\dagger \overleftrightarrow{D}_\mu H) (\bar{e}_R \gamma^\mu e_R)$	1
$\mathcal{O}_{HQ} = (iH^\dagger \overleftrightarrow{D}_\mu H) (\bar{Q}_L \gamma^\mu Q_L)$	1
$\mathcal{O}'_{HQ} = (iH^\dagger \sigma^a \overleftrightarrow{D}_\mu H) (\bar{Q}_L \sigma^a \gamma^\mu Q_L)$	1

Compared to SILH basis: $\mathcal{O}_{HW} \longrightarrow \mathcal{O}_{WW}$

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$\mathcal{O}_W + \mathcal{O}_B$

Constrained by LEP

Compared to SILH basis: $\mathcal{O}_{HW} \longrightarrow \mathcal{O}_{WW}$

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$\mathcal{O}_W + \mathcal{O}_B$

$\mathcal{O}_W - \mathcal{O}_B$ TGC

TGC, $h \rightarrow Z\gamma$

Constrained by LEP

Compared to SILH basis: $\mathcal{O}_{HW} \longrightarrow \mathcal{O}_{WW}$

Higgs Lagrangian in the unitary basis

- In the unitary gauge operators are written in terms of physical fields and physical vertices

$$\begin{aligned}
 \mathcal{L} = & \frac{1}{2} \partial_\mu h \partial^\mu h - \frac{1}{2} m_h^2 h^2 - c_3 \frac{1}{6} \left(\frac{3m_h^2}{v} \right) h^3 - \sum_{\psi=u,d,l} m_{\psi^{(i)}} \bar{\psi}^{(i)} \psi^{(i)} \left(1 + c_\psi \frac{h}{v} + \dots \right) \\
 & + m_W^2 W_\mu^+ W^{-\mu} \left(1 + 2c_W \frac{h}{v} + \dots \right) + \frac{1}{2} m_Z^2 Z_\mu Z^\mu \left(1 + 2c_Z \frac{h}{v} + \dots \right) + \dots \\
 & + \left(c_{WW} W_{\mu\nu}^+ W^{-\mu\nu} + \frac{c_{ZZ}}{2} Z_{\mu\nu} Z^{\mu\nu} + c_{Z\gamma} Z_{\mu\nu} \gamma^{\mu\nu} + \frac{c_{\gamma\gamma}}{2} \gamma_{\mu\nu} \gamma^{\mu\nu} + \frac{c_{gg}}{2} G_{\mu\nu}^a G^{a\mu\nu} \right) \frac{h}{v} \\
 & + \left(c_{W\partial W} (W_\nu^- D_\mu W^{+\mu\nu} + h.c.) + c_{Z\partial Z} Z_\nu \partial_\mu Z^{\mu\nu} + c_{Z\partial\gamma} Z_\nu \partial_\mu \gamma^{\mu\nu} \right) \frac{h}{v} + \dots
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- In fact, the same Lagrangian holds for a generic scalar h non necessarily part of an $SU(2)_L$ doublet (non-linear Lagrangian)

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- Equivalent to BSM Primaries of arXiv:1405.0181 (Gupta, Pomarol, Riva)

Higgs couplings	$\Delta\mathcal{L}_{SILH}$
c_W	$1 - \bar{c}_H/2$
c_Z	$1 - \bar{c}_H/2 - \bar{c}_T$
c_ψ ($\psi = u, d, l$)	$1 - (\bar{c}_H/2 + \bar{c}_\psi)$
c_3	$1 + \bar{c}_6 - 3\bar{c}_H/2$
c_{gg}	$8(\alpha_s/\alpha_2)\bar{c}_g$
$c_{\gamma\gamma}$	$8\sin^2\theta_W\bar{c}_\gamma$
$c_{Z\gamma}$	$(\bar{c}_{HB} - \bar{c}_{HW} - 8\bar{c}_\gamma\sin^2\theta_W)\tan\theta_W$
c_{WW}	$-2\bar{c}_{HW}$
c_{ZZ}	$-2(\bar{c}_{HW} + \bar{c}_{HB}\tan^2\theta_W - 4\bar{c}_\gamma\tan^2\theta_W\sin^2\theta_W)$
$c_{W\partial W}$	$-2(\bar{c}_W + \bar{c}_{HW})$
$c_{Z\partial Z}$	$-2(\bar{c}_W + \bar{c}_{HW}) - 2(\bar{c}_B + \bar{c}_{HB})\tan^2\theta_W$
$c_{Z\partial\gamma}$	$2(\bar{c}_B + \bar{c}_{HB} - \bar{c}_W - \bar{c}_{HW})\tan\theta_W$

from: RC, Ghezzi, Grojean, Muhlleitner, Spira JHEP 1307 (2013) 035

Implementing the Effective Lagrangian into software tools

- MC event generators

At least two FEYNRULES models implementing the Higgs Effective Lagrangian:

“Higgs Effective Lagrangian”

Alloul, Fuks, Sanz JHEP 1404 (2014) 110

<http://feynrules.irmp.ucl.ac.be/wiki/HEL>

“Higgs Characterization Model”

P. Artoisenet et al. JHEP 1311 (2013) 043

<http://feynrules.irmp.ucl.ac.be>

- Higgs decay rates and BRs

eHDECAY [based on HDECAY v5.10]

RC, Ghezzi, Grojean, Muhlleitner, Spira arXiv:1403.3381

<http://www-itp.particle.uni-karlsruhe.de/~maggie/eHDECAY>

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→ uses SILH basis as defined in arXiv:1303.3876

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eHDECAY [based on HDECAY v5.10]

RC, Ghezzi, Grojean, Muhlleitner, Spira arXiv:1403.3381

<http://www-itp.particle.uni-karlsruhe.de/~maggie/eHDECAY>

Implementing the Effective Lagrangian into software tools

■ MC event generators

At least two FEYNRULES models implementing the Higgs Effective Lagrangian:

“Higgs Effective Lagrangian”



uses SILH basis as defined in arXiv:1303.3876

Alloul, Fuks, Sanz JHEP 1404 (2014) 110

<http://feynrules.irmp.ucl.ac.be/wiki/HEL>

“Higgs Characterization Model”



uses a non-linear Lagrangian (basis equivalent to that of arXiv:1303.3876)

P. Artoisenet et al. JHEP 1311 (2013) 043

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■ Higgs decay rates and BRs

eHDECAY [based on HDECAY v5.10]



implements the non-linear Lagrangian, the SILH basis and two Composite Higgs models

RC, Ghezzi, Grojean, Muhlleitner, Spira arXiv:1403.3381

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Conclusions

- Choice of basis becomes relevant when one needs to retain only fewer operators
- Which operators give the leading contribution depends on our assumptions on the UV dynamics
- Advantages of the SILH basis:
 - straightforward matching to popular UV models
 - easily matches to LEP observables
- Perhaps Lagrangian in the unitary basis (non-linear Lagrangian/BSM primaries) is the most convenient and general one. Easier connection to observables, does not assume Higgs in a doublet; not suitable for loop calculations though; correlations among processes must be input



Extra slides

SILH basis

$$O_{HW} + O_{HB}$$

TGC:

$$(O_W - O_B) + (O_{HW} - O_{HB})$$

$$O_{3W}$$

$h \rightarrow Z\gamma$

$$O_{HW} - O_{HB}$$

$$O_\gamma$$

Modified SILH basis

$$O_{HB} - \frac{1}{2}O_{WW}$$

$$(O_W - O_B) - \frac{1}{2}O_{WW}$$

$$O_{3W}$$

$$O_{WW}$$

$$O_\gamma$$

Radiative corrections

- QCD radiative corrections usually important, can be often derived (and re-summed) from SM calculations

Example: $h \rightarrow gg$ rate

[RC, Ghezzi, Grojean, Muhlleitner, Spira arXiv:1403.3381]

$$\Gamma(gg)|_{SILH} = \frac{G_F \alpha_s^2 m_h^3}{4\sqrt{2}\pi^3} \left[\frac{1}{9} \sum_{q,q'=t,b,c} (1 - \bar{c}_H - \bar{c}_q - \bar{c}_{q'}) A_{1/2}^*(\tau_{q'}) A_{1/2}(\tau_q) c_{eff}^2 \kappa_{soft} \right. \\ \left. + 2 \operatorname{Re} \left(\sum_{q=t,b,c} \frac{1}{3} A_{1/2}^*(\tau_q) \frac{16\pi \bar{c}_g}{\alpha_2} \right) c_{eff} \kappa_{soft} \right. \\ \left. + \left| \sum_{q=t,b,c} \frac{1}{3} A_{1/2}(\tau_q) \right|^2 c_{eff}^2 \kappa_{ew} \kappa_{soft} \right. \\ \left. + \frac{1}{9} \sum_{q,q'=t,b} (1 - \bar{c}_H - \bar{c}_q - \bar{c}_{q'}) A_{1/2}^*(\tau_q) A_{1/2}(\tau_{q'}) \kappa^{NLO}(\tau_q, \tau_{q'}) \right].$$

$$\frac{\Gamma(h \rightarrow gg)}{\Gamma(h \rightarrow gg)_{SM}} \simeq 1 - \bar{c}_H - 2.12 \bar{c}_t + 0.024 \bar{c}_c + 0.1 \bar{c}_b + 22.2 \bar{c}_g \frac{4\pi}{\alpha_2}.$$

- Inclusion of EW radiative corrections requires ad-hoc calculations. They are usually very small because α_W is small and $\log(\Lambda_{EW}/\Lambda_{UV})$ is also small (interesting case is one with big gap of scales, since NP effects scale like $1/\Lambda_{UV}^2$)

A closer look to eHDECAY

RC, Ghezzi, Grojean, Muhlleitner, Spira arXiv:1403.3381

$$\frac{\Gamma(\bar{\psi}\psi)}{\Gamma(\bar{\psi}\psi)_{SM}} \simeq 1 - \bar{c}_H - 2\bar{c}_\psi,$$

$$\frac{\Gamma(h \rightarrow W^{(*)}W^*)}{\Gamma(h \rightarrow W^{(*)}W^*)_{SM}} \simeq 1 - \bar{c}_H + 2.2\bar{c}_W + 3.7\bar{c}_{HW},$$

$$\begin{aligned} \frac{\Gamma(h \rightarrow Z^{(*)}Z^*)}{\Gamma(h \rightarrow Z^{(*)}Z^*)_{SM}} &\simeq 1 - \bar{c}_H + 2.0 (\bar{c}_W + \tan^2\theta_W \bar{c}_B) \\ &+ 3.0 (\bar{c}_{HW} + \tan^2\theta_W \bar{c}_{HB}) - 0.26\bar{c}_\gamma, \end{aligned}$$

$$\begin{aligned} \frac{\Gamma(h \rightarrow Z\gamma)}{\Gamma(h \rightarrow Z\gamma)_{SM}} &\simeq 1 - \bar{c}_H + 0.12\bar{c}_t - 5 \cdot 10^{-4}\bar{c}_c - 0.003\bar{c}_b - 9 \cdot 10^{-5}\bar{c}_\tau \\ &+ 4.2\bar{c}_W + 0.19 (\bar{c}_{HW} - \bar{c}_{HB} + 8\bar{c}_\gamma \sin^2\theta_W) \frac{4\pi}{\sqrt{\alpha_2\alpha_{em}}}, \end{aligned}$$

$$\begin{aligned} \frac{\Gamma(h \rightarrow \gamma\gamma)}{\Gamma(h \rightarrow \gamma\gamma)_{SM}} &\simeq 1 - \bar{c}_H + 0.54\bar{c}_t - 0.003\bar{c}_c - 0.007\bar{c}_b - 0.007\bar{c}_\tau \\ &+ 5.04\bar{c}_W - 0.54\bar{c}_\gamma \frac{4\pi}{\alpha_{em}}, \end{aligned}$$

$$\frac{\Gamma(h \rightarrow gg)}{\Gamma(h \rightarrow gg)_{SM}} \simeq 1 - \bar{c}_H - 2.12\bar{c}_t + 0.024\bar{c}_c + 0.1\bar{c}_b + 22.2\bar{c}_g \frac{4\pi}{\alpha_2}.$$

$$\alpha_2 \equiv \frac{\sqrt{2}G_F m_W^2}{\pi}$$

$$\alpha_{em} \equiv \alpha_{em}(q^2 = 0)$$

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RC, Ghezzi, Grojean, Muhlleitner, Spira arXiv:1403.3381

- Decay rates computed by making a multiple perturbative expansion in (E/Λ) , (v/f) , $(\alpha_{SM}/4\pi)$
- QCD (long-distance) corrections factorize and can be easily included
- EW corrections do not factorize and can be included at $O(\alpha_2/4\pi)$, i.e. neglecting $O[(\alpha_2/4\pi)(v^2/f^2)]$

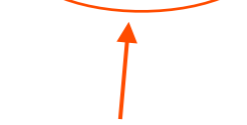
$$\Gamma(\bar{\psi}\psi)|_{SILH} = \Gamma_0^{SM}(\bar{\psi}\psi) \left[1 - \bar{c}_H - 2\bar{c}_\psi + \frac{2}{|A_0^{SM}|^2} \text{Re} (A_0^{*SM} A_{1,ew}^{SM}) \right] [1 + \delta_\psi \kappa^{QCD}]$$

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 $O(v^2/f^2)$
corrections

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QCD corrections

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$O(v^2/f^2)$ corrections
EW corrections $O(\alpha_2/4\pi)$
QCD corrections