

# top and bottom-mass effects in HNNLOPS

*Giulia Zanderighi (CERN & Oxford)*

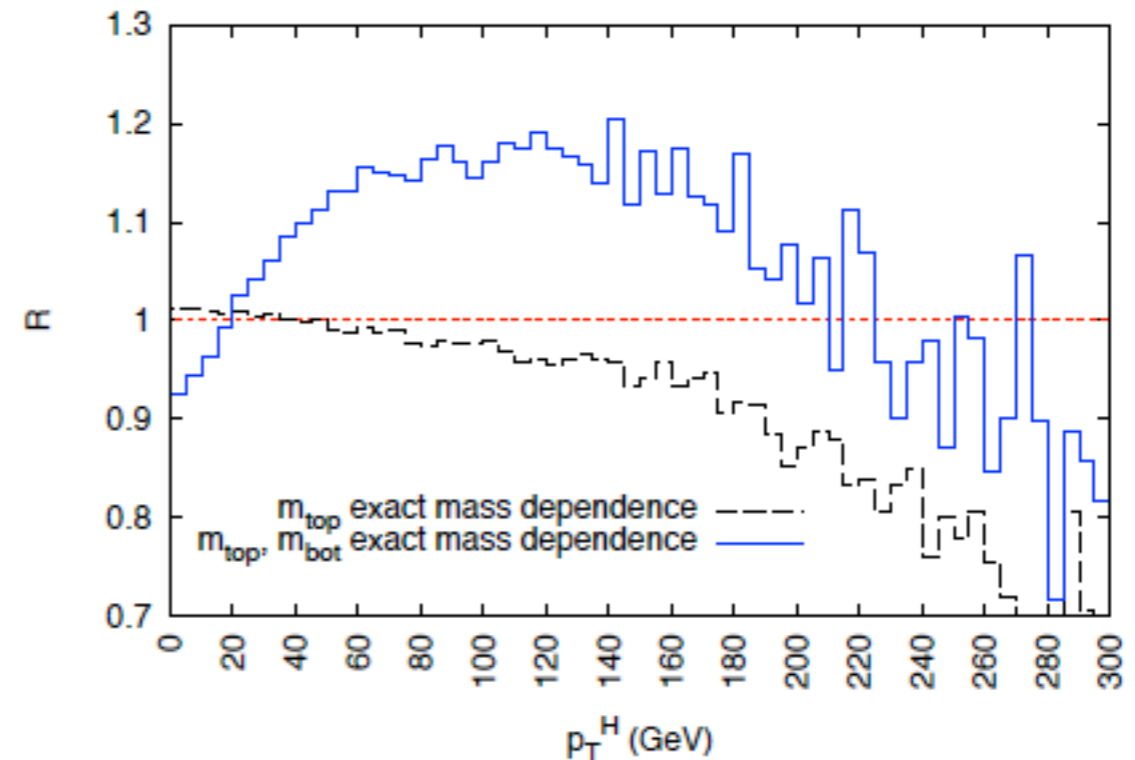
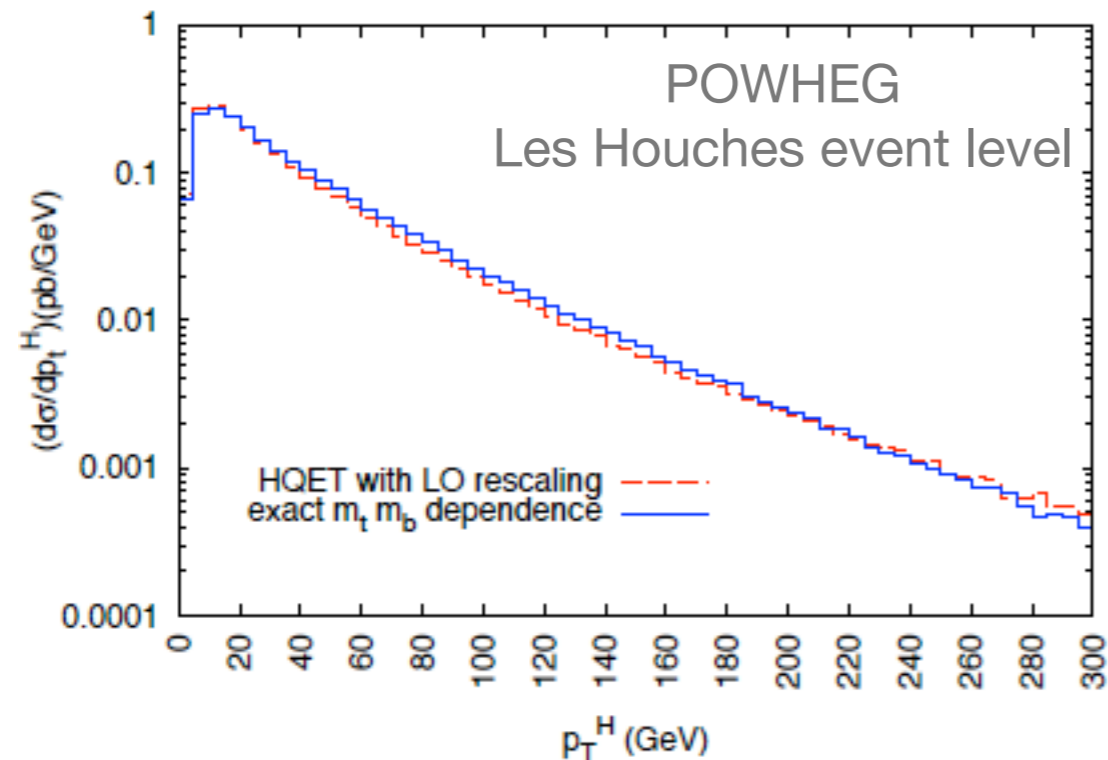
*in collaboration with Keith Hamilton and Paolo Nason*

# Outline

- Higgs production most studied in the [heavy-top effective theory](#), since this approximation was shown to work in practice remarkably well (even if  $m_H \approx m_t$ ) as long as  $p_{t,H} < m_t$
- recently more attention paid to [finite-quark mass effects](#)
- discussions triggered by paper of [Bagnaschi et al 1111.2854](#), which shows very large effects in the  $p_{t,H}$  distribution even at high  $p_{t,H}$  in POWHEG when finite-mass effects are included. In the following:
  - start from Bagnaschi et al results
  - discussion of the problem see talks by Hayk Sargsyan and Pier Monni
  - sketch of [Grazzini & Sargsyan 1306.4581](#) and of [Banfi, Monni and GZ 1308.4634](#) approaches
  - **new: b-mass effects in HNNLOPS and associated uncertainty**

# Higgs production with t,b

Bagnaschi et al 1111.2854



- large effects, even at high  $p_{t,H}$
- sizable difference wrt to MC@NLO or resummed calculations
- reason..?

# Higgs production with t,b

POWHEG Sudakov form factor is computed using b-mass effects

$$\exp \left[ - \int_{p'_T > p_T} \frac{R(\Phi_B, \Phi'_{\text{rad}})}{B(\Phi_B)} d\Phi'_{\text{rad}} \right]$$

Standard resummed calculations assume that when gluons are soft ( $p_t \ll m_H$ ) the real emission is **Altarelli-Parisi  $\times$  Born**

But soft gluons ( $m_b \approx p_t \ll m_H$ ) resolve **bottom loops and violate this structure**

Two approaches:

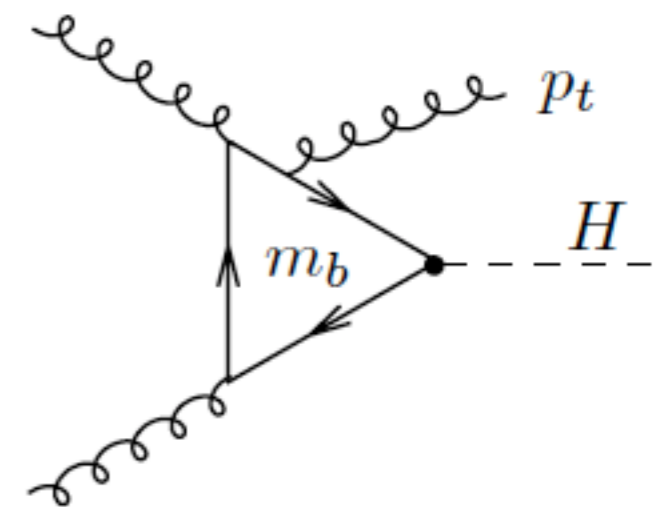
- use a resummation scale of the order of  $m_b$  (i.e. use only fixed order above  $m_b$ )  
Grazzini and Sargsyan 1306.4581
- show that soft  $m_b$  double logs cancel and that the impact of  $m_b$  can be treated as any finite remainder

Banfi, Monni, Zanderighi 1308.4634

# Mass effects in JetVHeto

Banfi, Monni, Zanderighi 1308.4634

- bottom-mass effects suppressed by Yukawa and  $m_b$  from loop, i.e. start at  $O(m_b^2)$  in the amplitude
- but enhanced by large **logs**  $\log^2(p_t/m_b)$  (exp. region of interest if  $p_t \sim 25\text{-}30$  GeV)
- dominant contribution from interference  $O((m_b m_t/m_H^2)^2 \log^2(p_t/m_b) \log^2(p_t/m_t))$  in the region  $m_b \ll p_t \ll m_H$
- soft terms shown to cancel at this order



For  $p_t \ll m_b$  standard factorization holds, hence these terms are finite for  $p_t \rightarrow 0$  and it is legitimate to treat them as a finite remainder, i.e. **they are computed at fixed-order** and matched to the resummed result

# Mass effects in JetVHeto

Banfi, Monni, Zanderighi 1308.4634

Top/bottom mass effects included in JetVHeto in the following way:

Large logs  $\log(m_H/p_t)$  (singular) treated in the large  $m_t$  limit

$$\Sigma(p_t) \sim C(\alpha_s, m_H, m_t, m_b, \dots) e^{-R(p_t)} \mathcal{F}(R') + \text{remainder}$$

Coefficient functions in heavy top limit and one-loop virtual with top/bottom in the loop, contains  $\log(m_H/m_b)$  (non-singular)

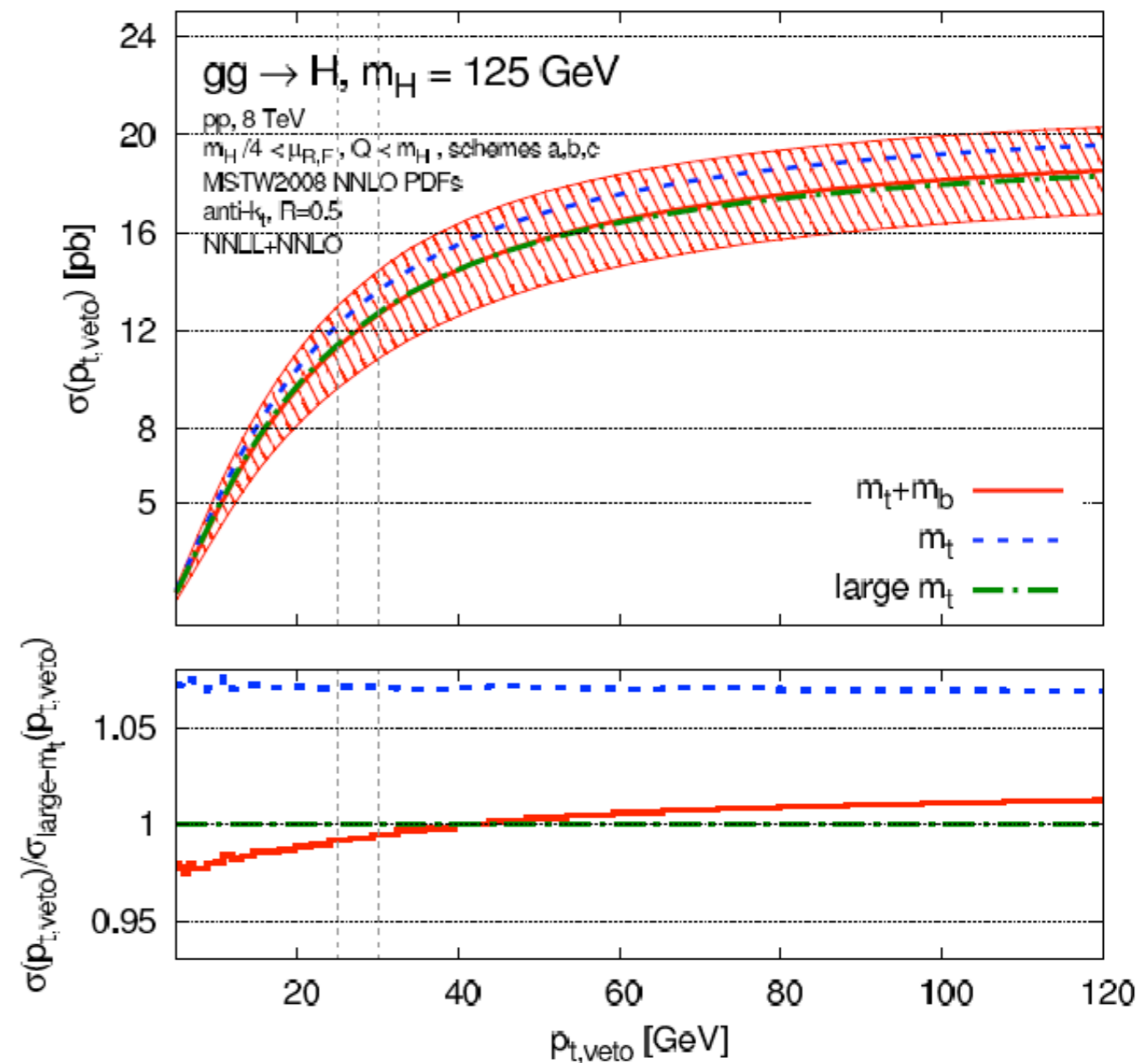
Power-suppressed terms and non-factorizing logs  $\log(m_b/p_t)$  (non-singular)

# Mass effects in JetVHeto

Banfi, Monni, Zanderighi 1308.4634

Impact of bottom-mass effects in the jet-veto cross-section:

- $m_b$  cancels positive  $m_t$  effect, but gives also a shape distortion
- overall smaller effect (about 3%)

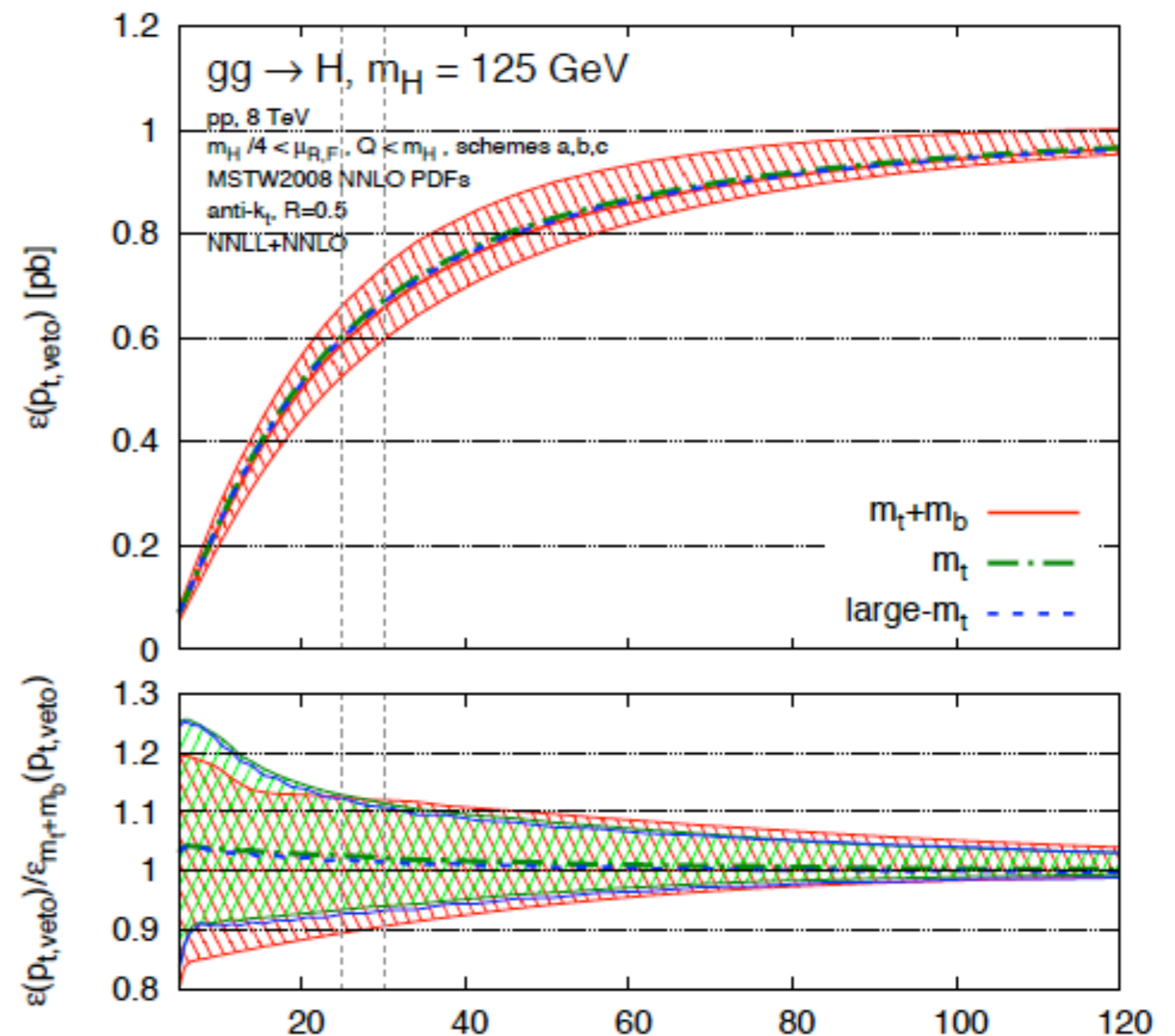


# Mass effects in JetVHeto

Banfi, Monni, Zanderighi 1308.4634

Impact of bottom-mass effects in the jet-veto efficiency:

- within the uncertainty of the large  $m_t$  approximation (estimated with JVE method)
- uncertainty slightly larger at 25 GeV when mass effects are included



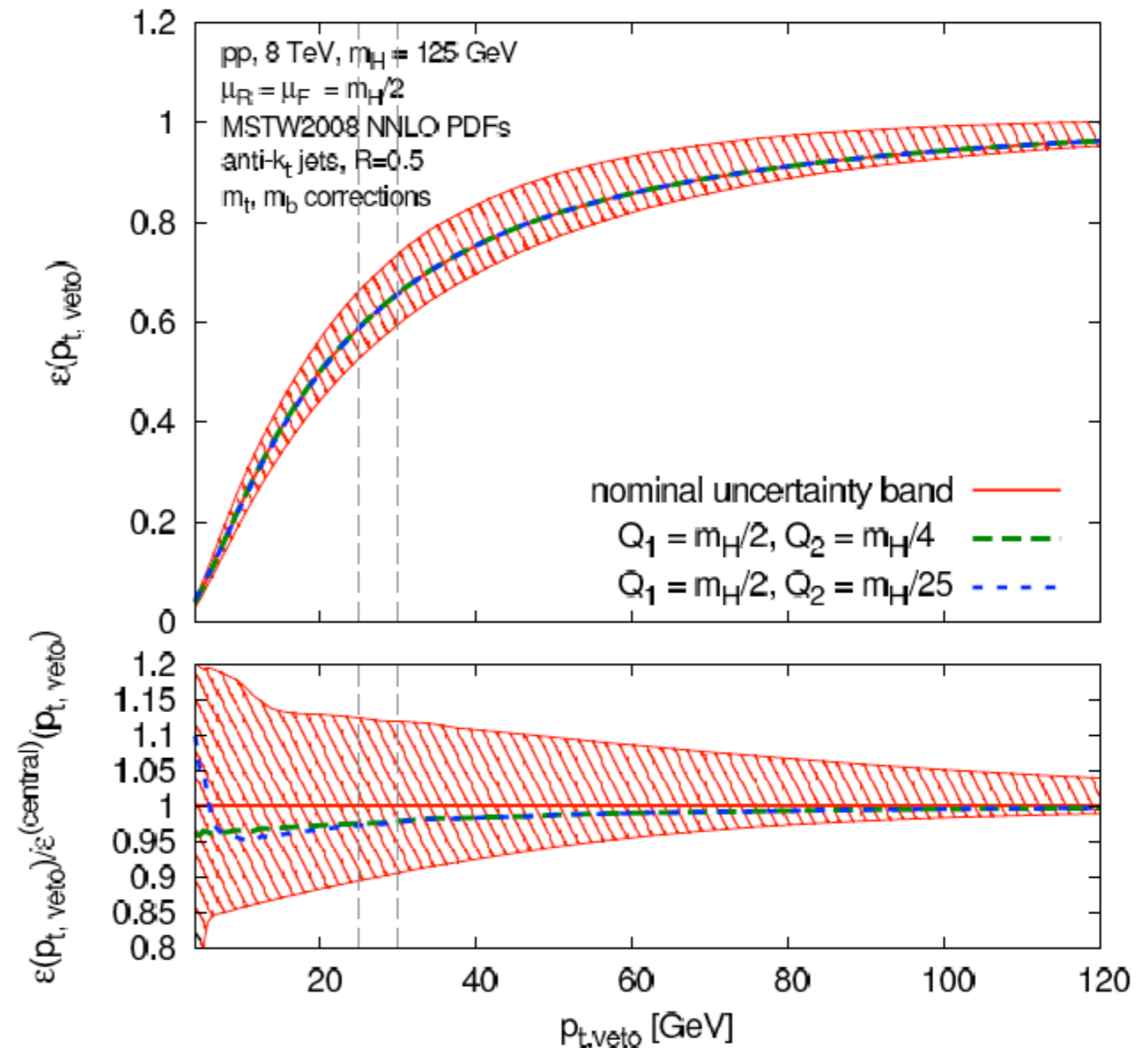


# Mass effects in JetVHeto

Banfi, Monni, Zanderighi 1308.4634

Impact of resummation scale:

- theory arguments suggest that resummation scale for bottom induced ( $Q_2$ ) should be smaller
- variation of  $Q_2$  very modest impact
- similar effect of  $p_{t,H}$



# MiNLO-NNLOPS method

Reminder: within the MiNLO approach, a NNLOPS generator is constructed using the following ingredients

see talk by Paolo Nason

1. plain **HJ NLO** generator
2. MiNLO procedure on HJ  $\Rightarrow$  **HJ-MiNLO** (finite and NLO accurate even for inclusive Higgs production)
3. **NNLO** results (e.g. from HNNLO or HPro) differential in the Higgs rapidity distribution (in general in the Born phase phase)
4. **re-weighting** of Les Houches events from HJ-MiNLO with ratio of HNNLO/HJ-MiNLO Higgs rapidity distribution

In the following, I will discuss how quark-mass effects can be implemented in 1. - 4., and how the uncertainty associated to missing higher orders related to b-mass effects can be estimated

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# 1. t,b-mass in HJ

Mass-effects known exactly for HJ at LO only, i.e. no  $O(\alpha_s^4)$  for Higgs + jet with mass effects available at the moment

At NLO re-weight Born, real, virtual and subtraction terms computed in the effective theory, *point-by-point in phase space* with

$$\frac{|M_{\text{Born}}^{\text{HJ},t+b}|^2(p_{\text{B}}, \dots)}{|M_{\text{Born}}^{\text{HJ},\infty}|^2(p_{\text{B}}, \dots)}$$

- ➔ Born matrix elements include mass effects exactly
- ➔ collinear and soft singular real and virtual terms proportional to the Born are also correct
- ➔ no effect on POWHEG Sudakov, as R/B unchanged

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## 2. t,b-mass in MiNLO

Two options:

1. assume that there are no large ( $m_b$ ) logs to all orders, so keep the original MiNLO Sudakov (correct only matrix elements)
2. assume that bottom-mass effects exponentiate to all orders, so multiply the MiNLO Sudakov by

$$\Delta_{m_b}(p_{t,H}, y_H) = \exp \left[ - \int_{p'_{t,H} > p_{t,H}} \left( \frac{R_{tb}}{B_{tb}} - \frac{R_{m_t=\infty}}{B_{m_t=\infty}} \right) \right]$$

Notice: this is the factor that turns the inclusive H POWHEG Sudakov in the effective theory into the one that includes mass effects  $\Rightarrow$  expect results similar to those of Bagnaschi et al.

# MiNLO-NNLOPS method

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# 3. t,b-mass in NNLO

Use HNNLO2.0 with t,b-mass effects, i.e.

- t, b mass implemented exactly at NLO  $O(\alpha_s^3)$
- currently NNLO  $O(\alpha_s^4)$  mass effects not included
- could be implemented approximatively as a rescaling of NNLO results by Born top-mass correction factor  $|F_0(\tau_t)|^2, \dots$

$$|\mathcal{M}_B|^2 = |\mathcal{M}_B^\infty|^2 \left| \sum_q F_0(\tau_q) \right|^2$$



# MiNLO-NNLOPS method

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In the following, I will discuss how quark-mass effects can be implemented in 1-4, and how the uncertainty associated due to missing higher orders related to b-mass effects can be estimated

# 4. t,b mass in re-weighting

The re-weighting procedure obviously unchanged, only the ingredients are modified, as discussed before

# Validation and results

## Settings and input parameters

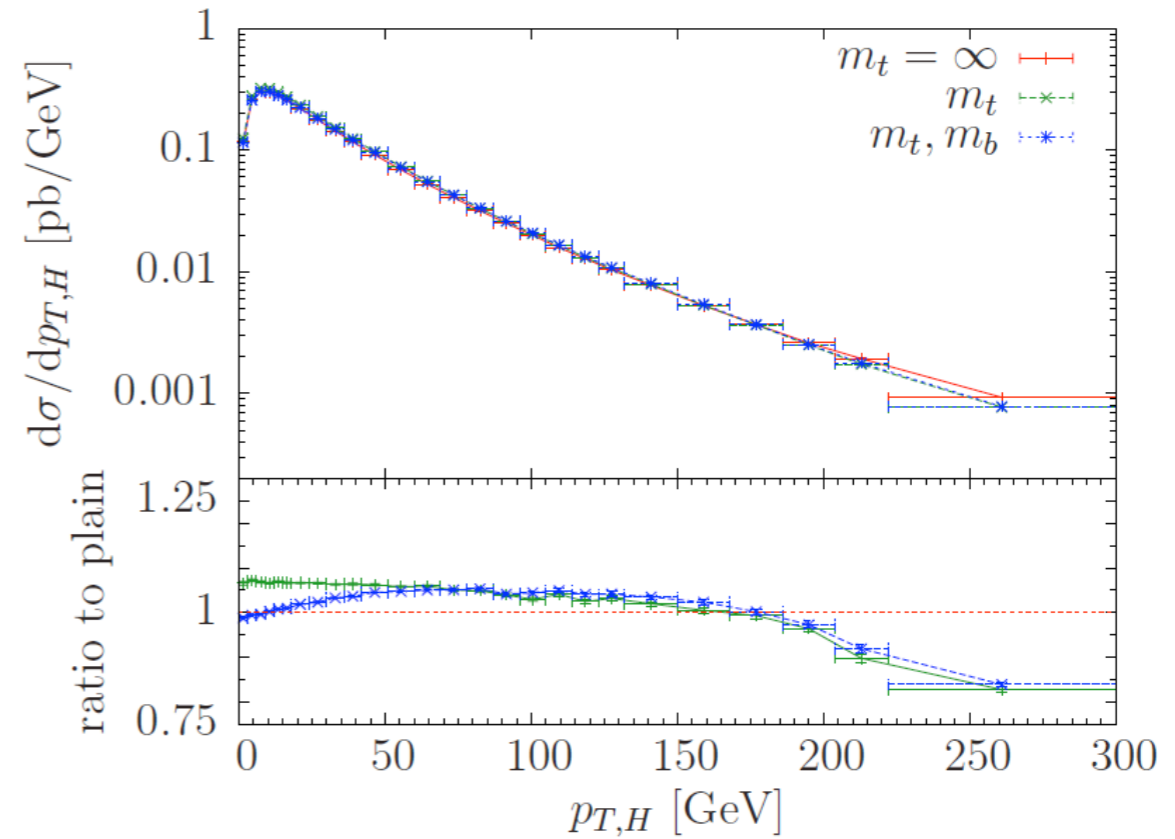
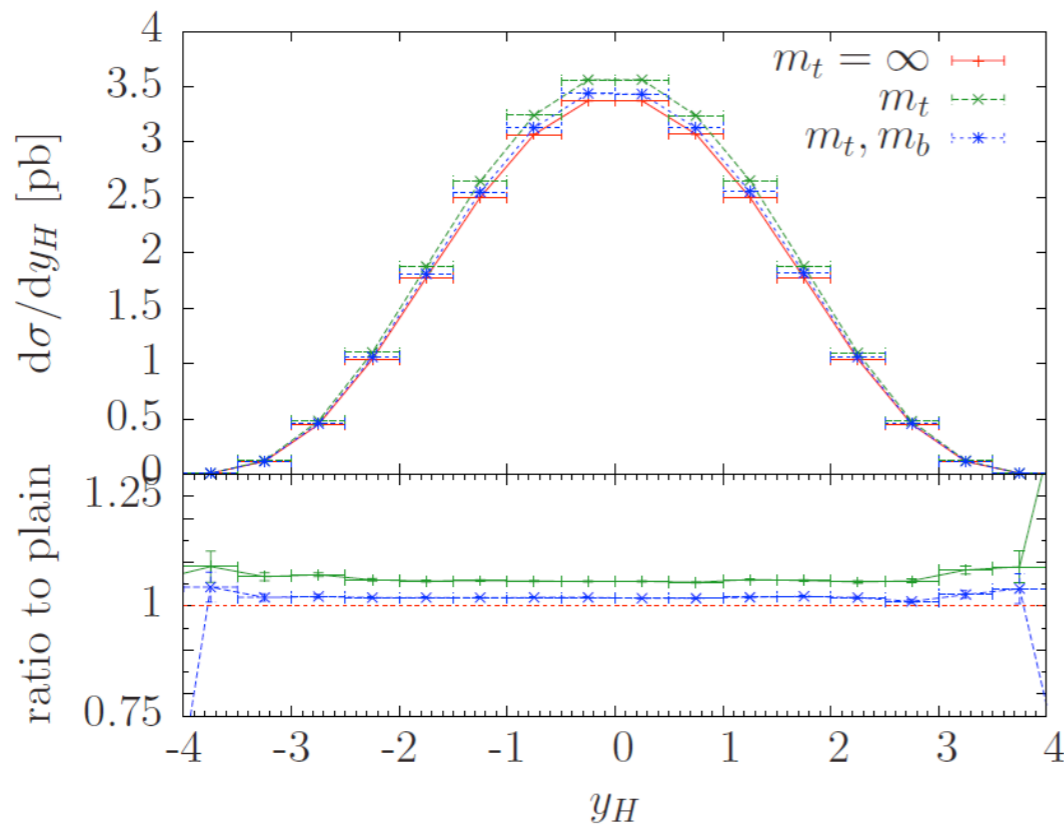
- 8 TeV LHC collisions, MSTW2008NNLO pdfs
- $m_H = 125.5$  GeV,  $m_t = 172.5$  GeV,  $m_b = 4.75$  GeV (pole mass)

Scheme for b-mass: no NLO scheme compensation. Use as default **MSbar-scheme** (i.e. corresponds to setting  $m_b = 3.38$  GeV) since

- sensible to use a running mass at the Higgs hardness scale (bottom in loop, not on-shell production)
- impact of mass effects more similar at LO and NLO

	on-shell scheme	$\overline{\text{MS}}$ scheme
$\sigma_{tb}^{\text{LO}} / \sigma_t^{\text{LO}}$	0.89	0.93
$\sigma_{tb}^{\text{NLO}} / \sigma_t^{\text{NLO}}$	0.93	0.94

# t,b in matrix elements only



Pattern very similar to what observed for inclusive Higgs production at NLO, i.e.

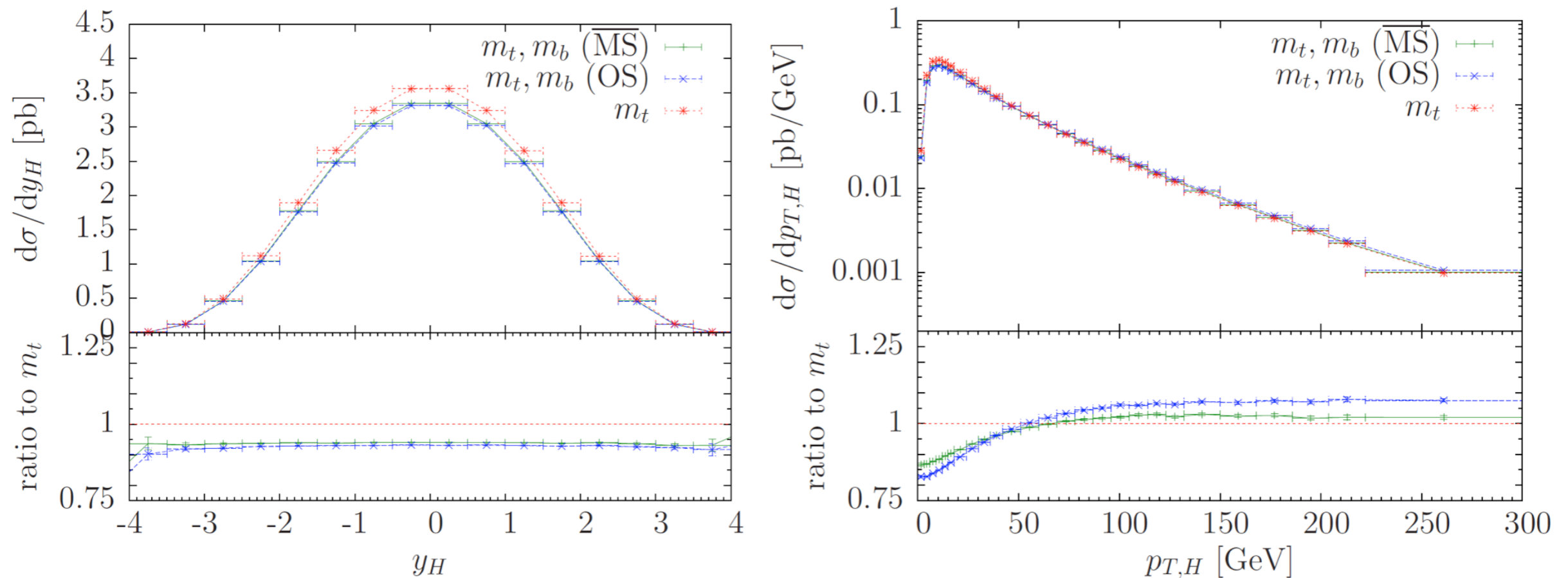
$$\sqrt{m_t} \Rightarrow +(6-7)\%$$

$$\sqrt{m_t+m_b} \Rightarrow \pm 1\%$$

This is non-trivial and due to MiNLO

# Resummed t,b-effects

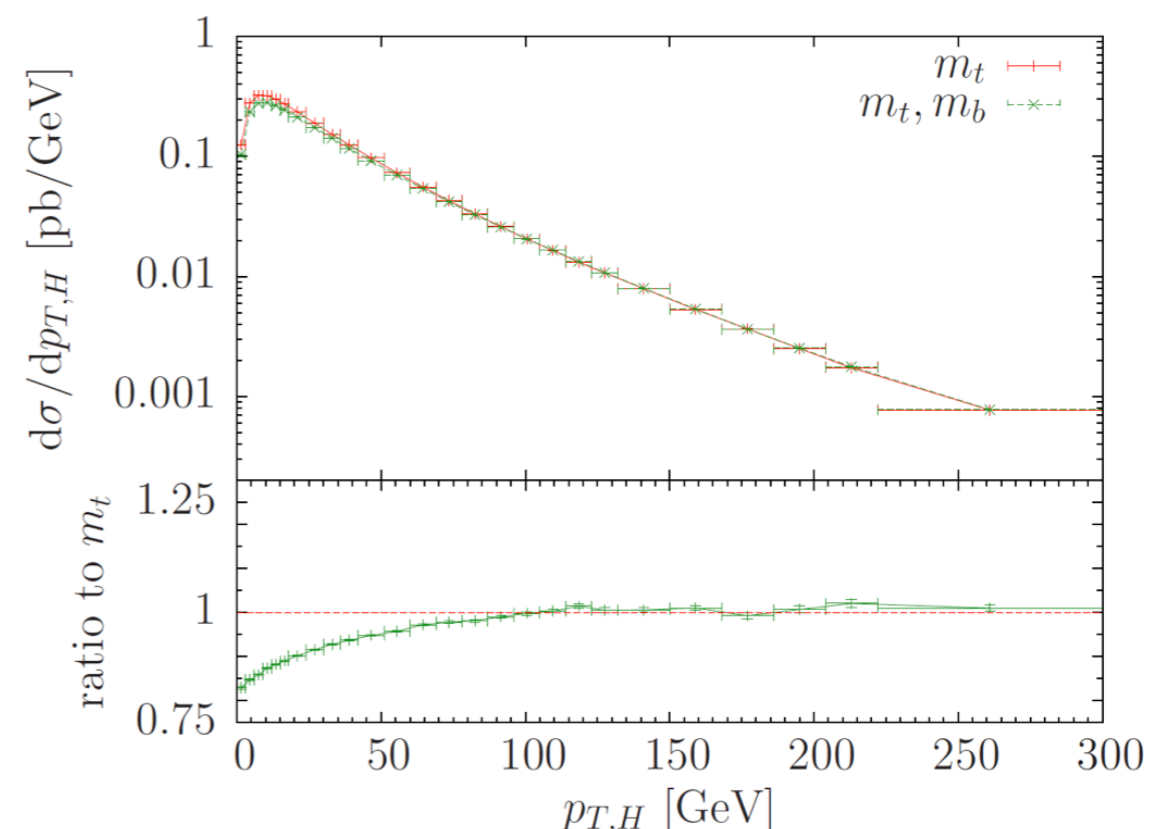
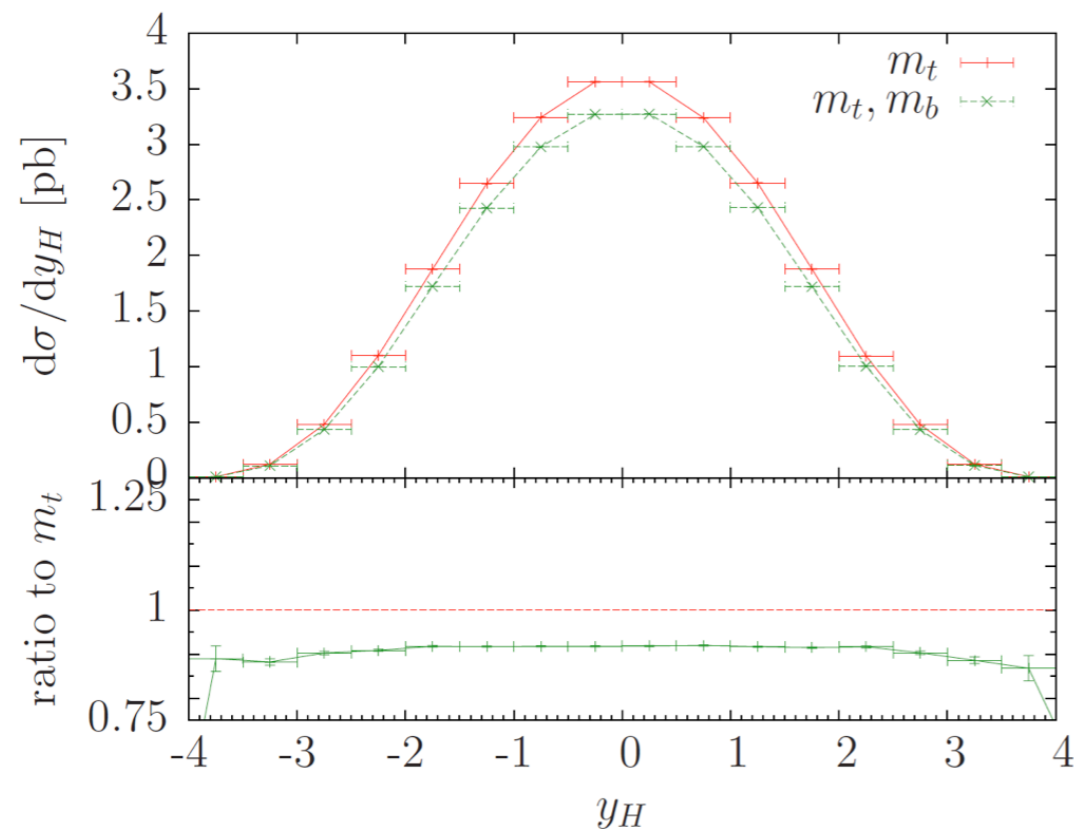
Expected size of effect from [Bagnaschi et al \(ggH\\_quark-mass-effects\)](#):



- in  $\overline{\text{MS}}$  scheme: about 15-20% at low  $p_{t,H}$ , 5-10% intermediate  $p_{t,H}$ , vanishes asymptotically (larger effects in OS)
- mass effects more modest in  $\overline{\text{MS}}$  scheme (expected)

# Resummed t,b-effects

HJ-MiNLO with masses (no HNNLOPS yet...)



- sizable  $m_b$  effect at low  $p_{t,H}$ , affects normalization of rapidity dist.
- must estimate the uncertainty associated with unknown higher order structure of b-mass corrections
- two options in HJ-MiNLO: fully exponentiate the effect in MiNLO Sudakov, or not. Difference between two approaches provides a **robust assessment of theory uncertainty**

# Conclusion

- presented work in progress on implementation of t,b-mass effects in HJ-MiNLO
- effects can be resummed in MiNLO Sudakov, or not  $\Rightarrow$  robust uncertainty estimate
- phenomenology for full HNNLOPS with mass effects in progress
- code will be released soon (January?)