

# Higgs production in association with bottom quarks

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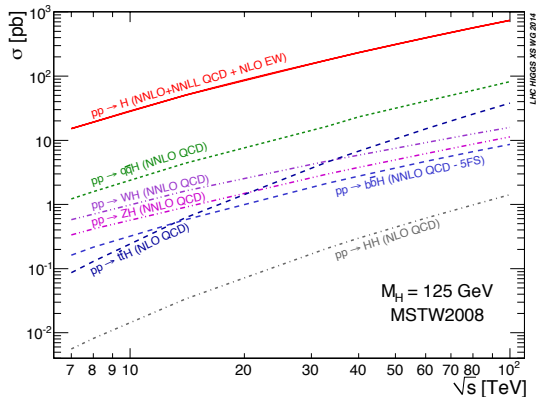
University of Zürich

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# Outline

1. Motivation
2. Schemes
3. Cross Section
4. Tools and results

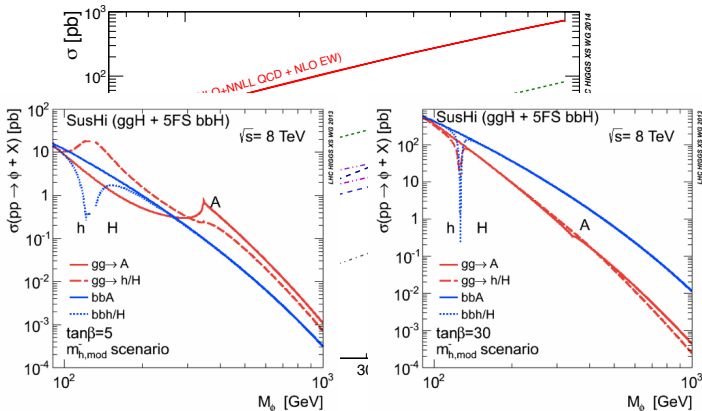
# SM vs. MSSM Higgs production



## ► SM:

- gluon fusion by far dominant
- $b\bar{b}H$  sizeable only with  $b$ -tagging

# SM vs. MSSM Higgs production



## ► SM:

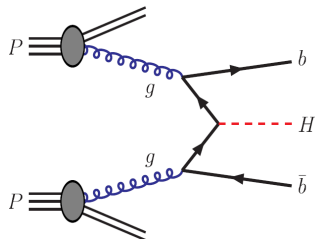
- gluon fusion by far dominant
- $b\bar{b}H$  sizeable only with  $b$ -tagging

## ► MSSM/2HDM:

- 3 neutral Higgs:  $h$ ,  $H$  and  $A$
- $y_b/y_t$  enhanced by  $\tan\beta$
- $h$ : constrained to be SM-like
- $b\bar{b}H/A$  dominant for large  $\tan\beta$

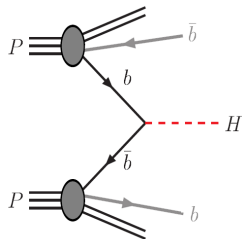
# Associated $H(b\bar{b})$ production

## 4-flavour scheme



- ▶ massive  $b$ 's
- ▶ potentially large logs  $\ln(m_b/Q)$
- ▶ power terms  $(m_b/Q)^n$
- ▶ involved  $2 \rightarrow 3$  at LO
- ▶ 2 exclusive  $b$ 's at LO
- ▶  $b(-\text{tag})$  well defined

## 5-flavour scheme



- ▶ massless  $b$ 's
- ▶ resummation into  $b$ -PDFs
- ▶ —
- ▶ simple  $2 \rightarrow 1$  at LO
- ▶ exclusive  $b$ 's at higher orders
- ▶  $b$  part of light jets

## 4-flavour scheme

- ▶ inclusive (exclusive)  
up to NLO

[Dittmaier, Krämer, Spira '04]

[Dawson, Jackson, Reina, Wackerth '04]

- ▶ exclusive NLO+PS

[MW, Frederix, Frixione, Hirschi,

Maltoni, Torrielli '14]

## 5-flavour scheme

- ▶ inclusive up to NNLO

[Harlander, Kilgore '03]

- ▶ towards N<sup>3</sup>L0

[Ahmed, Rana, Ravindran '14], [Ahmed, Mandal,

Rana, Ravindran '14], [Gehrmann, Kara '14]

- ▶ exclusive H+b at NLO

[Campbell, Ellis, Maltoni, Willenbrock '03]

- ▶ exclusive H+n-jet ( $n = 0/1/2$ )

[Harlander, Ozeren, MW '10],[Harlander, MW '11]

- ▶ exclusive up to NNLO

[Buehler, Herzog, Lazopoulos, Mueller '12]

- ▶  $p_T$  resummation

NLO+NLL [Belyaev, Nadolsky, Yuan '06]

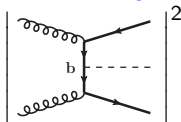
NNLO+NNLL [Harlander, Tripathi, MW '14]

- ▶ exclusive NLO+PS

[MW, Frederix, Frixione, Hirschi, Maltoni, Torrielli '14]

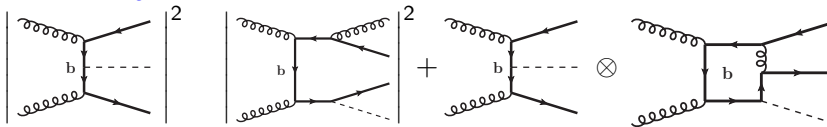
# The $b\bar{b}H$ cross section

$$\sigma_{b\bar{b}H}^{4FS} = \underbrace{\alpha_s^2 y_b^2 \Delta_{y_b^2}^{(0)}}_{LO}$$



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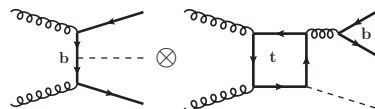
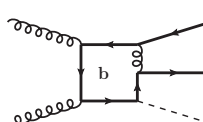
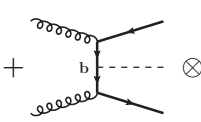
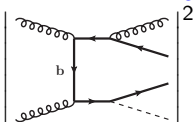
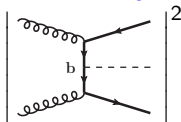
$$\sigma_{b\bar{b}H}^{4FS} = \underbrace{\alpha_s^2 y_b^2 \Delta_{y_b^2}^{(0)}}_{LO} + \alpha_s^3 \left( y_b^2 \Delta_{y_b^2}^{(1)} + \right.$$





# The $b\bar{b}H$ cross section

$$\sigma_{b\bar{b}H}^{4FS} = \underbrace{\alpha_s^2 y_b^2 \Delta_{y_b^2}^{(0)}}_{LO} + \underbrace{\alpha_s^3 \left( y_b^2 \Delta_{y_b^2}^{(1)} + y_b y_t \Delta_{y_b y_t}^{(1)} \right)}_{NLO}$$



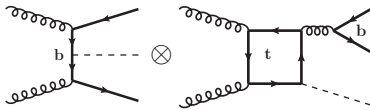
# The $b\bar{b}H$ cross section

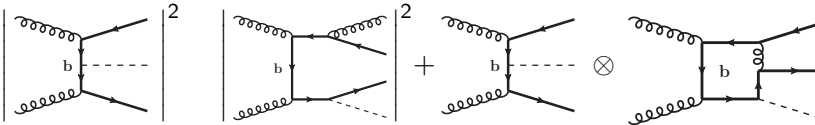
$$\begin{aligned}
 \sigma_{b\bar{b}H}^{4FS} &= \underbrace{\alpha_s^2 y_b^2 \Delta_{y_b^2}^{(0)}}_{LO} + \underbrace{\alpha_s^3 \left( y_b^2 \Delta_{y_b^2}^{(1)} + y_b y_t \Delta_{y_b y_t}^{(1)} \right)}_{NLO} \\
 &+ \underbrace{\alpha_s^4 \left( y_b^2 \Delta_{y_b^2}^{(2)} + y_b y_t \Delta_{y_b y_t}^{(2)} + y_t^2 \Delta_{y_t^2}^{(2)} \right)}_{NNLO} + \mathcal{O}(\alpha_s^5)
 \end{aligned}$$

The diagrammatic expansion is shown below the equation:

- LO:** A tree-level diagram with a top quark loop and a bottom quark exchange.
- NLO:** Includes a tree-level diagram with a top quark loop and a bottom quark exchange (squared), and a tree-level diagram with a top quark loop and a bottom quark exchange (crossed).
- NNLO:** Includes a tree-level diagram with a top quark loop and a bottom quark exchange (squared).

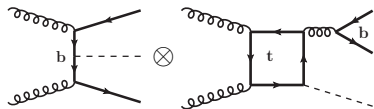
# The $b\bar{b}H$ cross section

$$\sigma_{b\bar{b}H}^{4FS} = \underbrace{\alpha_s^2 y_b^2 \Delta_{y_b^2}^{(0)}}_{LO} + \underbrace{\alpha_s^3 \left( y_b^2 \Delta_{y_b^2}^{(1)} + y_b y_t \Delta_{y_b y_t}^{(1)} \right)}_{NLO}$$


$$+ \underbrace{\alpha_s^4 \left( y_b^2 \Delta_{y_b^2}^{(2)} + y_b y_t \Delta_{y_b y_t}^{(2)} + y_t^2 \Delta_{y_t^2}^{(2)} \right)}_{NNLO} + \mathcal{O}(\alpha_s^5)$$


$$\sigma_{b\bar{b}H}^{5FS} = y_b^2 \Delta_{y_b^2}^{(0)} + \alpha_s y_b^2 \Delta_{y_b^2}^{(1)} + \alpha_s^2 \left( y_b^2 \Delta_{y_b^2}^{(2)} + y_t^2 \Delta_{y_t^2}^{(2)} \right) + \mathcal{O}(\alpha_s^3)$$

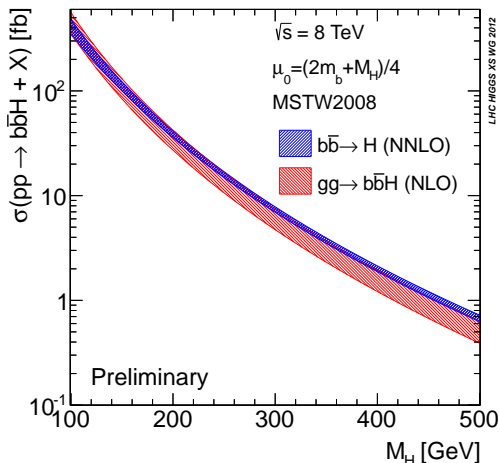
# The $b\bar{b}H$ cross section



$$\begin{aligned}
 \sigma_{b\bar{b}H}^{4FS} &= \underbrace{\alpha_s^2 y_b^2 \Delta_{y_b^2}^{(0)}}_{y_b^2\text{-term at NLO}} + \alpha_s^3 \left( y_b^2 \Delta_{y_b^2}^{(1)} + \underbrace{y_b y_t \Delta_{y_b y_t}^{(1)}}_{y_b y_t\text{-term at NLO}} \right) \\
 &+ \alpha_s^4 \left( y_b^2 \Delta_{y_b^2}^{(2)} + y_b y_t \Delta_{y_b y_t}^{(2)} + \underbrace{y_t^2 \Delta_{y_t^2}^{(2)}}_{y_t^2\text{-term at NNLO}} \right) + \mathcal{O}(\alpha_s^5) \\
 \sigma_{b\bar{b}H}^{5FS} &= y_b^2 \Delta_{y_b^2}^{(0)} + \alpha_s y_b^2 \Delta_{y_b^2}^{(1)} + \alpha_s^2 \left( y_b^2 \Delta_{y_b^2}^{(2)} + y_t^2 \Delta_{y_t^2}^{(2)} \right) + \mathcal{O}(\alpha_s^3)
 \end{aligned}$$

- ▶  $y_b y_t$ -term enters at NLO:
  - interference with (contamination from) gluon fusion
  - no double counting with gluon fusion cross section!
- ▶  $y_t^2$ -term enters at NNLO:
  - part of gluon fusion cross section
  - sizable in SM  $\sim 40\%$  (LO – large uncertainties)
  - e.g., with MG5@LO in 4FS HEFT; agreement with full theory

# 4FS vs. 5FS: Inclusive cross section



## 4FS NLO:

[Dittmaier, Krämer, Spira '04]

[Dawson, Jackson, Reina, Wackerroth '04]

grids  $m_\phi = 80 - 1000 \text{ GeV}$  for  $y_b^2$   
and  $y_b y_t$  produced by M. Spira

## 5FS NNLO:

[Harlander, Kilgore '03]

grids  $m_\phi = 80 - 1000 \text{ GeV}$  for  $y_b^2$   
and produced with SusHi

[Harlander, Liebler, Mantler '13]

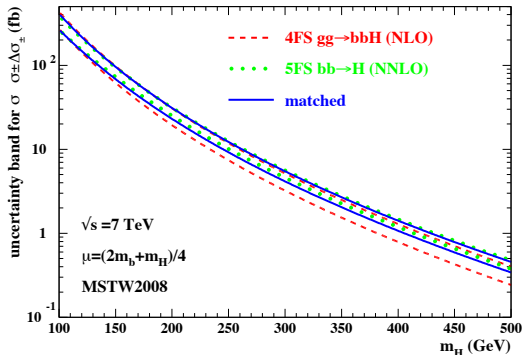
**MSSM:**  $\frac{1}{1-\Delta_b}$  ( $\tan\beta$ -resummation)  $y_b$ -reweighting approach  
(captures dominant effects) [Dawson, Jackson, Reina, Wackerroth '05],

[Dittmaier, Häfliger, Krämer, Spira, Walser '14]

## 4FS vs. 5FS: Santander matching

$$\sigma = \frac{\sigma^{4FS} + w \sigma^{5FS}}{1 + w}, \quad w = \ln(m_\phi / m_b) - 2$$

[Harlander, Krämer, Schumacher '11]



combined grids available on:

<http://twiki.cern.ch/twiki/bin/view/LHCPhysics/CERNYellowReportPageAt8TeV>

- **now:**  $y_b y_t$  included (crucial for large- $y_t$  scenarios)
- e.g, SM:  $y_b y_t \sim -10\%$
- $y_t^2$  simply from gluon fusion

Alternative matching scheme: [Bonvini, Papanastasiou, Tackmann]  
work in progress...

# Tools for exclusive $b\bar{b}H$ cross section and distributions

- ▶ Higgs distributions (inclusive over  $b$ 's)
    - 5FS  $y^H$  at NNLO: private code  
[Bühler, Herzog, Lazopoulos, Müller '12]
    - 5FS  $p_T(H)$  at NNLO+NNLL: private code by M. Wiesemann  
[Harlander, Tripathi, MW '14]
    - 4FS at NLO: private code by M. Spira  
[Dittmaier, Krämer, Spira '04]
    - 4FS at NLO+PS: MG5\_aMC with  $y_b^{\overline{MS}}$   
[MW, Frederix, Frixione, Hirschi, Maltoni, Torielli '14]
  - ▶ exclusive cross section with  $b$ -tagging
    - 4FS at NLO+PS: MG5\_aMC with  $y_b^{\overline{MS}}$  (both  $y_b^2$  and  $y_b y_t$ )  
[MW, Frederix, Frixione, Hirschi, Maltoni, Torielli '14]
- process folder publicly available on:

<https://cp3.irmp.ucl.ac.be/projects/madgraph/wiki/bbH>

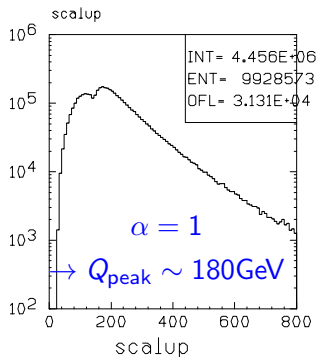
# shower scale in MG5\_aMC

- ▶ shower scale  $Q$  event-wise chosen from distribution
- ▶ interval of distribution determined from inputs  $(\alpha, f_1, f_2)$ :

$$\alpha f_1 \sqrt{s_0} \leq Q \leq \alpha f_2 \sqrt{s_0}, \quad s_0 : \text{LO center of mass energy}$$

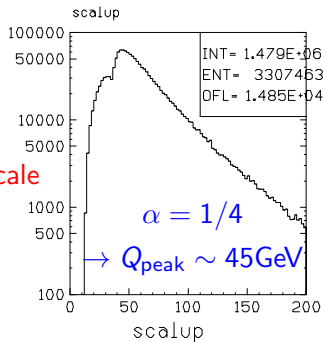
default values:  $\alpha = 1, f_1 = 0.1, f_2 = 1$

- ▶ peaked at  $Q_{\text{peak}} \sim \alpha(f_1 + f_2)\sqrt{\langle s_0 \rangle}/2$
- ▶ for  $b\bar{b}H$  in 4FS follows:



NOTE: related scale

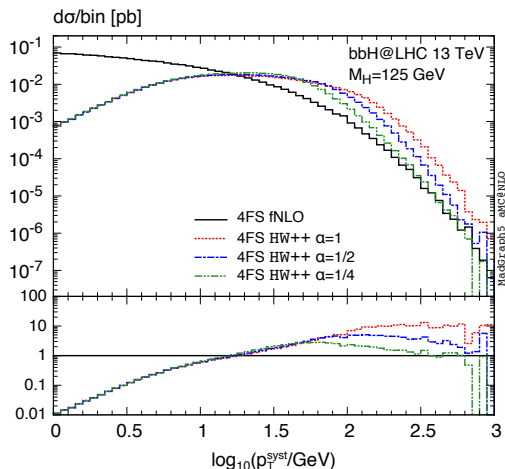
$$\mu_F \sim \frac{m_\phi + 2m_b}{4} \\ \sim 34\text{GeV}$$





# 4FS: choosing the shower scale

[MW, Frederix, Frixione, Hirschi, Maltoni, Torielli '14]



$$\alpha = 1 \quad \hat{=} \quad Q_{\text{peak}} \sim 180 \text{ GeV}$$

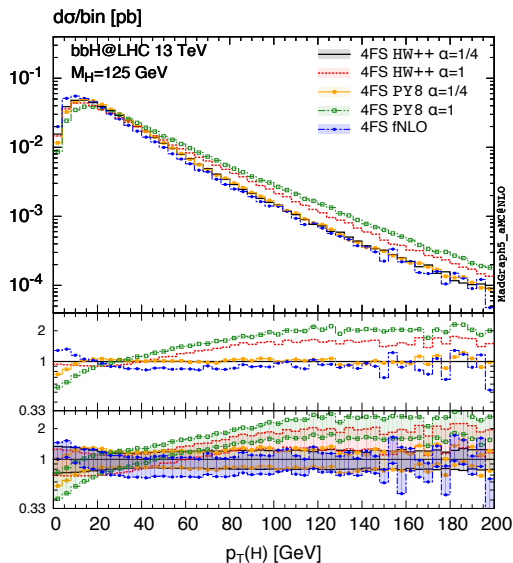
$$\alpha = 1/2 \quad \hat{=} \quad Q_{\text{peak}} \sim 90 \text{ GeV}$$

$$\alpha = 1/4 \quad \hat{=} \quad Q_{\text{peak}} \sim 45 \text{ GeV}$$

$Q$  event-wise from a distribution peaked at  $Q_{\text{peak}} \sim \alpha(f_1 + f_2)\sqrt{\langle s_0 \rangle}/2$   
in an interval:  $\alpha f_1 \sqrt{s_0} \leq Q \leq \alpha f_2 \sqrt{s_0}$ ,  $f_1 = 0.1$ ,  $f_2 = 1$ ,  $s_0$ : LO c.m.e.

# 4FS: choosing the shower scale

[MW, Frederix, Frixione, Hirschi, Maltoni, Torielli '14]



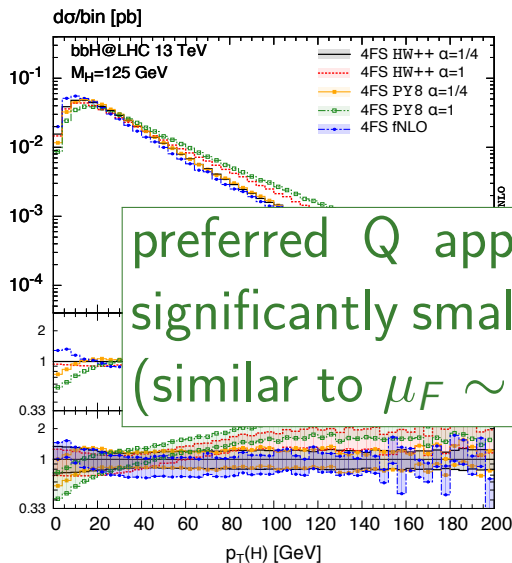
$$\alpha = 1 \quad \hat{=} \quad Q_{\text{peak}} \sim 180\text{GeV}$$

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# 4FS: choosing the shower scale

[MW, Frederix, Frixione, Hirschi, Maltoni, Torielli '14]



$$\alpha = 1 \quad \hat{=} \quad Q_{\text{peak}} \sim 180\text{GeV}$$

$$\alpha = 1/2 \quad \hat{=} \quad Q_{\text{peak}} \sim 90\text{GeV}$$

$$\alpha = 1/4 \quad \hat{=} \quad Q_{\text{peak}} \sim 45\text{GeV}$$

preferred  $Q$  appears to be significantly smaller than  $m_\phi$  (similar to  $\mu_F \sim m_\phi/4$ )

## Exclusive $b\bar{b}H$ cross section

SM NLO+PS with Pythia 8;  $\mu_F = \mu_R = H_T/4$ ;

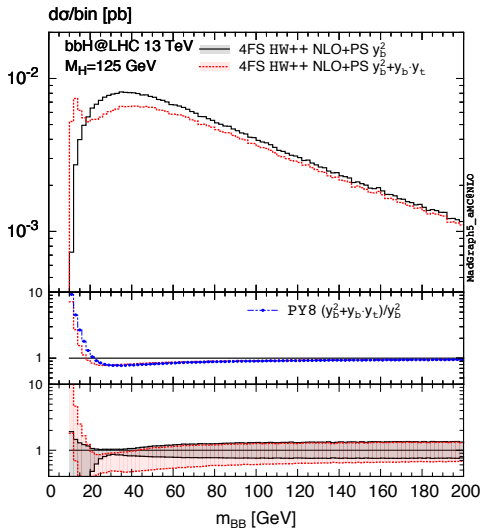
shower scale according to [MW, Frederix, Frixione, Hirschi, Maltoni, Torielli '14]

- ▶ significantly reduced residual uncertainty at NLO
- ▶  $y_b y_t$  always  $\sim -10\%$  with large uncertainty (effectively LO)
- ▶  $b$ -tag reduces cross section by factor of 3 – 4
- ▶ second  $b$ -tag by additional factor of 10

$\sigma[\text{pb}]$	NLO			LO
	$y_b^2$	$y_b y_t$	$y_b^2 + y_b y_t$	$y_b^2$
inclusive	$0.448^{+19.8\%}_{-20.8\%}$	$-0.0365^{+35.5\%}_{-62.8\%}$	$0.411^{+24.6\%}_{-28.4\%}$	$0.478^{+59.0\%}_{-34.6\%}$
$\geq 1j_b$	$0.133^{+16.7\%}_{-17.3\%}$	$-0.0148^{+35.0\%}_{-60.1\%}$	$0.118^{+23.5\%}_{-26.8\%}$	$0.150^{+55.9\%}_{-32.8\%}$
$\geq 2j_b$	$0.0133^{+13.7\%}_{-16.0\%}$	$-0.00147^{+34.3\%}_{-58.8\%}$	$0.0118^{+20.0\%}_{-25.1\%}$	$0.0168^{+54.4\%}_{-32.7\%}$

# $m_{BB}$ : $y_b^2$ vs. $y_b y_t$ (4FS)

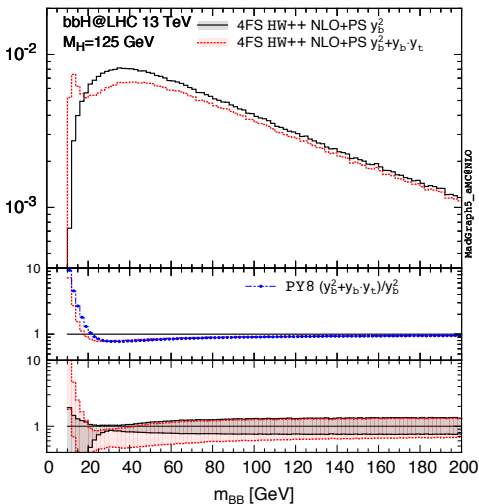
[MW, Frederix, Frixione, Hirschi, Maltoni, Torielli '14]



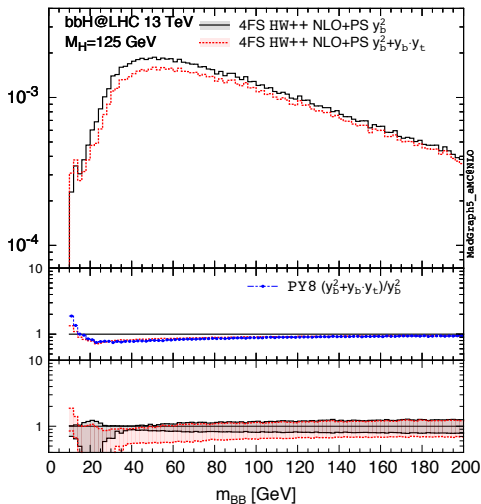
# $m_{BB}$ : $y_b^2$ vs. $y_b y_t$ (4FS)

[MW, Frederix, Frixione, Hirschi, Maltoni, Torielli '14]

$d\sigma/\text{bin}$  [pb]



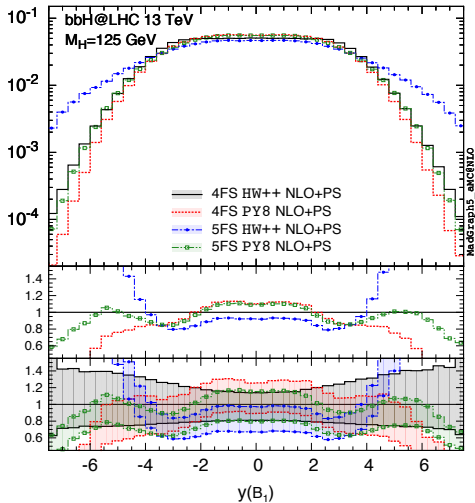
$d\sigma/\text{bin}$  [pb]  $\geq 1b\text{-jet}$



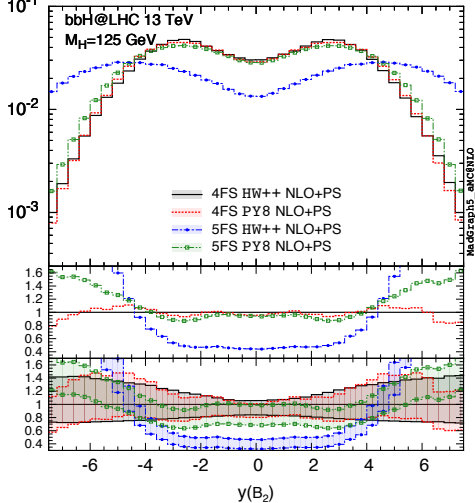
# $y_B$ : 4FS vs. 5FS

[MW, Frederix, Frixione, Hirschi, Maltoni, Torielli '14]

$d\sigma/\text{bin}$  [pb]

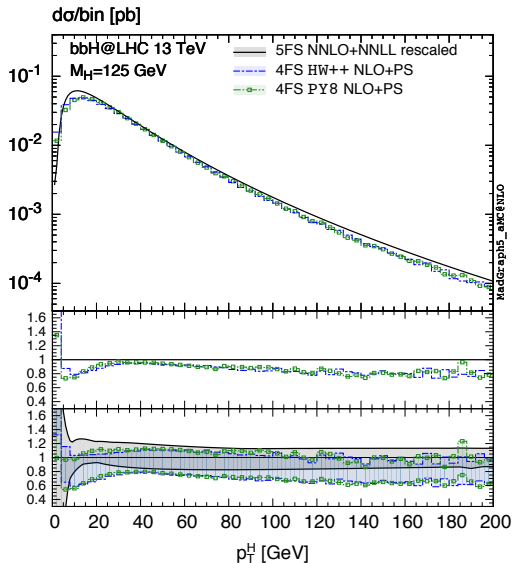


$d\sigma/\text{bin}$  [pb]



# $p_T^H$ : 4FS vs. 5FS NNLO+NNLL

[MW, Frederix, Frixione, Hirschi, Maltoni, Torielli '14], [Harlander, Tripathi, MW '14]



analytic resummation:

$$\mu_F = \mu_R = m_T/4$$

NLO+PS:

$$\mu_F = \mu_R = H_T/4$$



# Conclusions and Outlook

- ▶ NLO+PS 4FS: shower scale smaller than  $m_\phi$
- ▶ NLO+PS 4FS: improved residual uncertainties
- ▶ NLO+PS 4FS:  $b$ -tagging strongly reduces cross section
- ▶  $y_b y_t$ :  $\sim -10\%$ , generally flat, except handful observables, e.g., prominent peak structure in  $m_{BB}$
- ▶ 4FS vs. 5FS: fairly good agreement, except  $y$  of  $B$ -hadrons
- ▶ 4FS vs. 5FS: remarkable similar shapes in  $p_T(H)$

## more things to do...

- contribution from  $ggF$  to exclusive  $b\bar{b}H$  ( $y_t^2$  terms)
- combination with  $ggF$  for inclusive Higgs observables
- relative importance of  $ggF$  and  $b\bar{b}H$  in various 2HDM/MSSM scenarios (done for inclusive cross section)

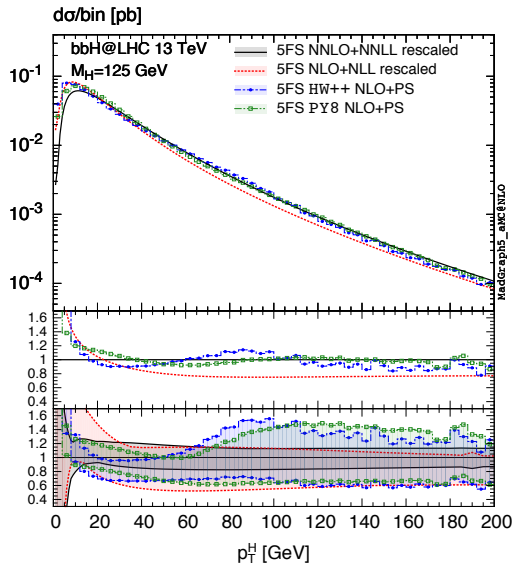
[Bagnaschi, Harlander, Liebler, Mantler, Slavich, Vicini '14]

- extend comparison of 4FS and 5FS to higher Higgs masses

# BackUp

# $p_T^H$ in 5FS: NLO+PS vs. analytic resummation

[MW, Frederix, Frixione, Hirschi, Maltoni, Torielli '14]



analytic resummation:

$$\mu_F = \mu_R = m_T/4$$

NLO+PS:

$$\mu_F = \mu_R = H_T/4$$