

Implications of an additional scale on Leptogenesis

Diego Aristizabal

INFN-Laboratori Nazionali di Frascati, Italy

Based on

Phys. Lett. B **659**, 328 (2008)

In collaboration with E. Nardi and M. Losada

Purely Flavored Leptogenesis—[arXiv:0901.????](#)

Work in progress in collaboration with E. Nardi and A. Muñoz

Outline

● Outline

Theoretical facts

The model

Scenarios for Leptogenesis

Conclusions

■ Motivation:

Two experimental facts:

(i) Massive neutrinos: the seesaw mechanism, as a natural possibility, can account for this fact \Rightarrow lepton number violation $M_N \Rightarrow$ leptogenesis.

(ii) Hierarchy among the different SM Yukawa couplings: this fact can be understood by the presence of an abelian flavor symmetry broken at a high scale σ .

■ Description of the model

■ Different possibilities for leptogenesis **SCENARIOS**

◆ **Scenario I:** The abelian flavor symmetry breaking scale (σ) as well as M_F are larger than the lepton number breaking scale (M_N).

◆ The abelian flavor symmetry breaking scale (σ) is below M_N .

■ **Scenario II:** $M_F > M_{N_1}$.

■ **Scenario III:** $M_{N_1} > M_F$.

■ Final remarks

● Outline

Theoretical facts

● Motivation

The model

Scenarios for Leptogenesis

Conclusions

Theoretical facts

Motivation

★ Seesaw Mechanism

The smallness of the light neutrino masses can be explained by the presence of heavy right-handed neutrinos (SM singlets). In addition:

- Lepton number violation
- New sources of CP violation
- Departure from thermal equilibrium

LEPTON ASYMMETRY

Leptogenesis as an explanation of B asymmetry of the Universe is a quantitative question

★ Froggatt-Nielsen mechanism and the fermion mass hierarchies

The presence of heavy fields (F) and the non-trivial transformation of the SM fields under $U(1)_X \Rightarrow$ Fermion mass operators arise as effective operators

$$f \sim \left(\frac{\langle S \rangle}{M_F}\right)^n$$

Can the presence of $\langle S \rangle = \sigma$ have an impact on leptogenesis?

● Outline

Theoretical facts

● Motivation

The model

Scenarios for Leptogenesis

Conclusions

● Outline

Theoretical facts

The model

- A simple realization
- Light neutrinos mass matrix

Scenarios for Leptogenesis

Conclusions

The model

A simple realization

At a large scale close to the leptogenesis scale a horizontal $U(1)_X$ symmetry forbids direct couplings between the leptons and the heavy Majorana neutrinos.

$$-\mathcal{L} = \frac{1}{2} N_\alpha M_{N_\alpha} N_\alpha + \bar{F}_a M_{F_a} F_a + h_{ia} \bar{l}_i P_R F_a \Phi + \lambda_{\alpha a} \bar{N}_\alpha F_a S + \lambda_{\alpha a}^{(5)} \bar{N}_\alpha \gamma_5 F_a S$$

F are heavy Dirac fields $F = (F_R, F_L)^T$
 N heavy R-H Majorana fields $N = (N_R, N_R^c)^T$

$U(1)_X$ is broken by $\langle S \rangle = \sigma$
and $\sigma \lesssim M_F$ is assumed

A simple charge assignment that forbids $\bar{l} P_R N \Phi$ is

$$X(l_{L_i}, F_{L_a}, F_{R_a}) = +1, X(S) = -1 \text{ and } X(N_\alpha, \Phi) = 0$$

$U(1)$ global accidental symmetry
 $L(l_L, F_L, F_R, N_R) = +1$ and $L(S, \Phi) = 0$

As in the standard seesaw this symmetry
is broken only by the Majorana mass term

● Outline

Theoretical facts

The model

● A simple realization

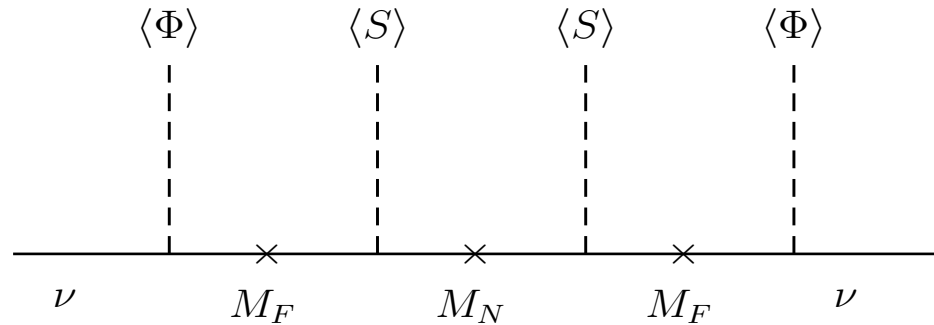
● Light neutrinos mass matrix

Scenarios for Leptogenesis

Conclusions

Light neutrinos mass matrix

After EW and $U(1)_X$ symmetry breaking light neutrinos become massive



$$-(\mathcal{M}_\nu)_{ij} = \left[h^* \frac{\sigma}{M_F} \lambda^T \frac{v^2}{M_N} \lambda \frac{\sigma}{M_F} h^\dagger \right]_{ij} = \left[\tilde{\lambda}^T \frac{v^2}{M_N} \tilde{\lambda} \right]_{ij}$$

Seesaw coupling

$$\tilde{\lambda}_{\alpha i} = \left(\lambda \frac{\sigma}{M_F} h^\dagger \right)_{\alpha i}$$

- ❶ In contrast to the seesaw there is an additional suppression factor σ/M_F .
- ❷ The minimal model defined by 2 N and 2 F :

$$(N, F) \Rightarrow \mathcal{M}_\nu \propto \begin{pmatrix} \tilde{\lambda}_1^2 & \tilde{\lambda}_1 \tilde{\lambda}_2 & \tilde{\lambda}_1 \tilde{\lambda}_3 \\ \cdot & \tilde{\lambda}_2^2 & \tilde{\lambda}_2 \tilde{\lambda}_3 \\ \cdot & \cdot & \tilde{\lambda}_3^2 \end{pmatrix}$$

\mathcal{M} is projective $\Rightarrow m_{\nu_{1,2}} = 0$
Non consistent with data

● Outline

Theoretical facts

The model

● A simple realization

● Light neutrinos mass matrix

Scenarios for Leptogenesis

Conclusions

- Outline

Theoretical facts

The model

Scenarios for Leptogenesis

- Relevant scales
- Scenario I
- Scenario I: N_1 lower bound
- Scenario II
- Constraints on M_{N_1}
- BE: for N_1 and $\Delta\ell_i$
- OEQ condition and Flavor dynamics

Conclusions

Scenarios for Leptogenesis

Relevant scales

Relevant scales of the model apart from the EW scale are:

- 1 The mass of the heavy fields, M_F
- 2 The lepton number violating scale, M_N
- 3 The flavor breaking scale [$U(1)_X$ symmetry breaking], σ

Depending on the hierarchy among these scales there are different possibilities for leptogenesis

- 1 The flavor breaking scale is above the L violating scale:
 - ➡ **Scenario I:** Standard Leptogenesis case, $M_F > M_N$.
- 2 The flavor violating scale is below the L breaking scale ($M_{N_3} > M_{N_2} > M_{N_1}$):
 - ➡ **Scenario II:** $M_F > M_{N_1}$
 - ➡ **Scenario III:** $M_F < M_{N_1}$

● Outline

Theoretical facts

The model

Scenarios for Leptogenesis

● **Relevant scales**

● Scenario I

● Scenario I: N_1 lower bound

● Scenario II

● Constraints on M_{N_1}

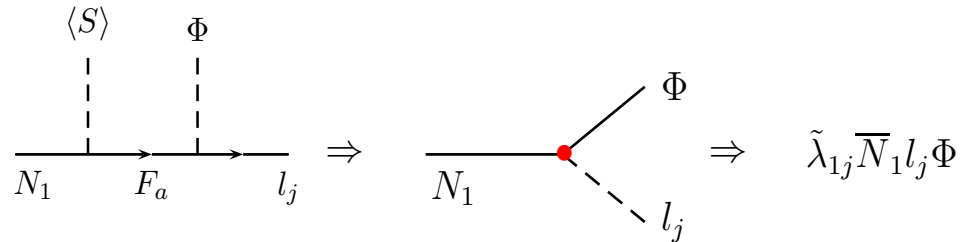
● BE: for N_1 and $\Delta\ell_i$

● OEQ condition and Flavor dynamics

Conclusions

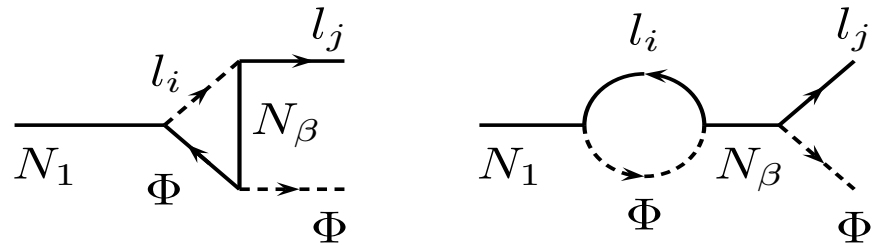
Scenario I

After integrating out the heavy F_a fields the standard seesaw Lagrangian is obtained



N_1 decay width and CP-asymmetries are the same as in the standard case

$$\Gamma_{N_1} = \frac{M_{N_1}}{16\pi} (\tilde{\lambda}\tilde{\lambda}^\dagger)_{11}$$



$$\epsilon_{N_1 \rightarrow l_j} = \frac{1}{8\pi(\tilde{\lambda}\tilde{\lambda}^\dagger)_{11}} \sum_{\beta \neq 1} \text{Im} \left\{ \tilde{\lambda}_{\beta j} \tilde{\lambda}_{1j}^* \left[(\tilde{\lambda}\tilde{\lambda}^\dagger)_{\beta 1} \tilde{F}_1(z_\beta) + (\tilde{\lambda}\tilde{\lambda}^\dagger)_{1\beta} \tilde{F}_2(z_\beta) \right] \right\}$$

$$z_\beta = M_{N_\beta}^2 / M_{N_1}^2$$

$$\epsilon_{N_1} = \frac{3}{16\pi(\tilde{\lambda}\tilde{\lambda}^\dagger)_{11}} \sum_{\beta} \text{Im} \left[\frac{1}{\sqrt{z_\beta}} (\tilde{\lambda}\tilde{\lambda}^\dagger)_{\beta 1}^2 \right]$$

$$M_\nu \propto \tilde{\lambda}^2, \Gamma \propto \tilde{\lambda}^2, \epsilon_{N_1} \propto \tilde{\lambda}^2$$

● Outline

Theoretical facts

The model

Scenarios for Leptogenesis

● Relevant scales

● Scenario I

● Scenario I: N_1 lower bound

● Scenario II

● Constraints on M_{N_1}

● BE: for N_1 and $\Delta\ell_i$

● OEQ condition and Flavor dynamics

Conclusions

Scenario I: N_1 lower bound

In the hierarchical case [$M_{N_1} \ll M_{N_2}, M_{N_3}$] the asymmetry is bounded by the Davidson-Ibarra limit

$$|\epsilon_{N_1}| \leq \frac{3}{16\pi} \frac{M_{N_1}}{v^2} (m_{\nu_3} - m_{\nu_1}) \lesssim \frac{3}{16\pi} \frac{M_{N_1}}{v^2} \frac{\Delta m_{\text{atm}}^2}{2m_{\nu_3}}$$

This bound in turn implies a lower limit on M_{N_1} :

▶ B asymmetry from N_1 dynamics:

$$\frac{n_B}{s} = -\kappa_s \epsilon_{N_1} \eta$$

Dilution factor: $\kappa \sim 1.3 \times 10^{-3}$

Efficiency factor: $\eta = [0, 1] (10^{-2} - 10^{-1})$

▶ WMAP data

$$\frac{n_B}{s} \sim (8.7 \pm 0.4) \times 10^{-11}$$

$$M_{N_1} \gtrsim 10^9 \frac{m_{\nu_3}}{\eta \sqrt{\Delta m_{\text{atm}}^2}}$$

M_{N_1} should be above the electroweak scale

● Outline

Theoretical facts

The model

Scenarios for Leptogenesis

● Relevant scales

● Scenario I

● Scenario I: N_1 lower bound

● Scenario II

● Constraints on M_{N_1}

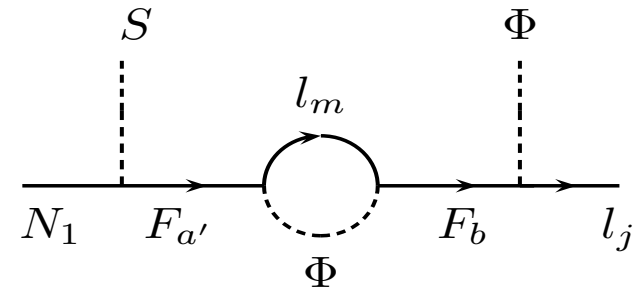
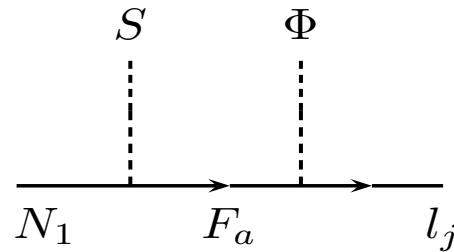
● BE: for N_1 and $\Delta \ell_i$

● OEQ condition and Flavor dynamics

Conclusions

Scenario II

In this case R-H neutrinos decay to three-body channels: $N_1 \rightarrow S l \Phi$



Decay width

At leading order in $r_a = M_{N_1}^2 / M_{F_a}^2$

$$\Gamma_{N_1} = \frac{M_{N_1}}{192\pi^3} \left(\frac{M_{N_1}}{\sigma} \right)^2 (\tilde{\lambda}\tilde{\lambda}^\dagger)_{11}$$

CP-asymmetry

$$\epsilon_{N_1} = \frac{3}{128\pi} \frac{\sum_{a,a',b} \text{Im} \left[\overbrace{(h^\dagger h)_{a'b} (h^\dagger h)_{ba} \lambda_{1a'} \lambda_{1a}^*}^A \right] r_{a'} r_a r_b^2}{\sum_{a,a'} (h^\dagger h)_{a'a} (\lambda_{1a'} \lambda_{1a}^*) r_a r_{a'}}$$

$A : a \leftrightarrow a' \Rightarrow A \rightarrow A^*$
 The CP asymmetry vanishes
 There is no L violation

$$\epsilon_{N_1 \rightarrow l_j} = \frac{3}{128\pi} \frac{\sum_i \text{Im} \left[(hr^2 h^\dagger)_{ij} \tilde{\lambda}_{1i} \tilde{\lambda}_{1j}^* \right]}{(\tilde{\lambda}\tilde{\lambda}^\dagger)_{11}} \neq 0$$

Flavor effects are responsible
 for Leptogenesis

● Outline

Theoretical facts

The model

Scenarios for Leptogenesis

● Relevant scales

● Scenario I

● Scenario I: N_1 lower bound

● Scenario II

● Constraints on M_{N_1}

● BE: for N_1 and $\Delta \ell_i$

● OEQ condition and Flavor dynamics

Conclusions

Constraints on M_{N_1}

⇒ The CP asymmetry is not constrained by neither low energy neutrino data nor the out-of-equilibrium decay condition: $\mathcal{M}_\nu \propto \tilde{\lambda}^2$, $\Gamma \propto \tilde{\lambda}^2$, $\epsilon_{N_1} \propto |h r^2 h^\dagger|$

⇒ Out of equilibrium condition \Rightarrow upper bound on $\tilde{\lambda}$

$$\Gamma_{N_1} \lesssim \xi \cdot H(M_{N_1})$$

$$\xi \sim 0.1 - 10$$

$$H(M_{N_1}) \simeq 1.66 \sqrt{g_*} \frac{M_{N_1}^2}{M_{\text{Pl}}}$$

$$(\tilde{\lambda}\tilde{\lambda}^\dagger)_{11} \lesssim 10^5 \xi \left(\frac{\sigma}{M_{N_1}} \right)^2 \frac{M_{N_1}}{M_{\text{Pl}}}$$

⇒ Low energy neutrino experimental data

$$\sum_i m_{\nu_i} \approx \frac{v^2}{M_{N_1}} (\tilde{\lambda}\tilde{\lambda}^T)_{11} \approx 0.3 \underbrace{\xi \left(\frac{\sigma}{M_{N_1}} \right)^2}_{\sim 10^{-1}} \overbrace{\text{eV}}^{\Delta m_{\text{atm}} \sim 0.05 \text{ eV}}$$

The out-of-equilibrium condition can be satisfied for the correct scale of m_ν

$$(\tilde{\lambda}\tilde{\lambda}^\dagger)_{11} \lesssim 10^{-12} (M_{N_1}/1 \text{ TeV})$$

M_{N_1} can be at the TeV scale

● Outline

Theoretical facts

The model

Scenarios for Leptogenesis

- Relevant scales
- Scenario I
- Scenario I: N_1 lower bound
- Scenario II

● Constraints on M_{N_1}

- BE: for N_1 and $\Delta\ell_i$
- OEQ condition and Flavor dynamics

Conclusions

Preliminary Results

D.A.S, E. Nardi and Luis A. Muñoz
arXiv:0901.????

Relevant processes [Order($h\lambda$)²]: Decays [$N_1 \leftrightarrow Sl_i\Phi$] + Scatterings
 $[\bar{S}N_1 \leftrightarrow l_i\Phi]$, $[\bar{\Phi}N_1 \leftrightarrow l_iS]$ and $[\bar{l}_iN_1 \leftrightarrow \Phi S]$
 $\underbrace{\hspace{10em}}_{s\text{-channel}} \quad \underbrace{\hspace{10em}}_{t\text{-channel}} \quad \underbrace{\hspace{10em}}_{t\text{-channel}}$

Boltzmann equations

Suitable subtraction of on-shell N_1 require [3↔3] and [2↔4] processes

$$\dot{Y}_{N_1} = -(y_{N_1} - 1) \gamma_{tot}$$

$$\dot{Y}_{\Delta\ell_i} = (y_{N_1} - 1) \epsilon_i \gamma_i - \Delta y_i \left(\gamma_i + (y_{N_1} - 1) \gamma_{S\Phi}^{N_1\bar{l}_i} \right)$$

$$Y_a = n_a/s, \quad \dot{Y}_a = zHs \frac{dY_a}{dz}, \quad y_a \equiv Y_a/Y_a^{eq}$$

$$\gamma_i = \gamma_{S\Phi l_i}^{N_1} + \gamma_{\Phi l_i}^{N_1\bar{S}} + \gamma_{Sl_i}^{N_1\bar{\Phi}} + \gamma_{S\Phi}^{N_1\bar{l}_i}$$

$$\gamma_{tot} = \sum_{i=e,\mu,\tau} \gamma_i$$

● Outline

Theoretical facts

The model

Scenarios for Leptogenesis

● Relevant scales

● Scenario I

● Scenario I: N_1 lower bound

● Scenario II

● Constraints on M_{N_1}

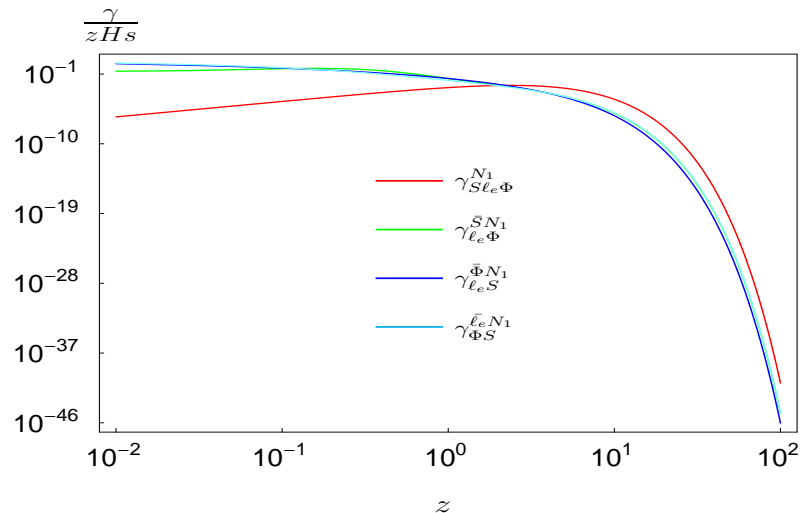
● BE: for N_1 and $\Delta\ell_i$

● OEQ condition and Flavor dynamics

Conclusions

OEQ condition and Flavor dynamics

$\mathcal{O}(S) = \mathcal{O}(D)$. Since $N_1 \rightarrow 3\text{body} \Rightarrow \Gamma_{N_1}|_{z=1} \sim H$ does not guarantee the out-of-equilibrium condition.

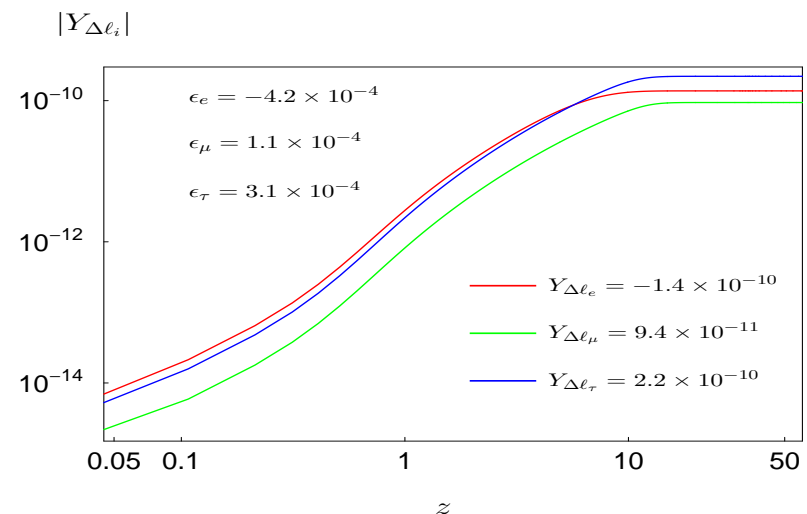


$$\gamma_{tot}/(zHs) |_{z \sim 1} > 1$$

Different washout regimens for the different flavors

Non vanishing final Lepton Asymmetry

$$\mathcal{O}(M_1) \sim \text{TeV}$$



Outline

Theoretical facts

The model

Scenarios for Leptogenesis

- Relevant scales
- Scenario I
- Scenario I: N_1 lower bound
- Scenario II
- Constraints on M_{N_1}
- BE: for N_1 and $\Delta\ell_i$

● OEQ condition and Flavor dynamics

Conclusions

- Outline

Theoretical facts

The model

Scenarios for Leptogenesis

Conclusions

- Final remarks

Conclusions

Final remarks

● Outline

Theoretical facts

The model

Scenarios for Leptogenesis

Conclusions

● Final remarks

- The presence of new scales different from that of lepton number breaking might change the standard Leptogenesis picture.
- We have investigated the possible *impact* due to a scale related to the breaking of an abelian flavor symmetry
- Most interesting cases arise when the new scale is below the L breaking scale
 - Successful Leptogenesis possible only to flavor dynamics.
 - Leptogenesis scale lowered down to the TeV scale
- More “sophisticated” models can be considered in which, in addition to successful Leptogenesis, the fermion mass hierarchy problem can be addressed too.