

# The nature of the electroweak Higgs sector

Discrete 2008, December 11-16 Valencia (Spain)

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December 13, 2008

The outline of this talk is

## Outline

- ▶ The Standard Model
- ▶ Supersymmetry
- ▶ Little Higgs
- ▶ Gauge-Higgs unification
- ▶ Unhiggs
- ▶ Conclusion

## Outline

Standard Model

MSSM

Little Higgs

Gauge-Higgs  
unification

Conformal Higgs

Conclusion

- ▶ In the Standard Model the electroweak symmetry is spontaneously broken by the Higgs mechanism where an  $SU(2)_L$  doublet Higgs boson is needed

## Higgs mechanism

$$H = \begin{pmatrix} H^+ \\ H^0 \end{pmatrix}, \mathcal{L}_{Higgs} = |D_\mu H|^2 - \frac{\lambda}{2} \left[ |H|^2 - \frac{v^2}{2} \right]^2 + \mathcal{L}_Y$$

- ▶ The term  $|D_\mu H|^2$  gives a mass to gauge bosons  $W$  and  $Z$  which absorb the Goldstone bosons  $H^+$  and  $ImH^0$
- ▶ The term  $\mathcal{L}_Y$  gives a mass to SM fermions
- ▶ The Higgs can “regularize” the bad UV behaviour of gauge bosons with longitudinal polarization

$$\epsilon_L^\mu \simeq \frac{p^\mu}{M_V}$$

# Unitarity bound

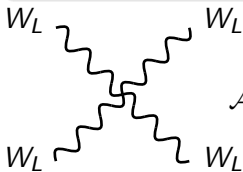
The Higgs unitarizes the scattering of longitudinal gauge bosons

## Partial wave decomposition

$$\mathcal{A} = 16\pi \sum_{\ell} (2\ell + 1) P_{\ell}(\cos \theta) a_{\ell}, \quad \sigma = \frac{16}{\pi} \sum_{\ell} (2\ell + 1) |a_{\ell}|^2$$

## Optical theorem

$$\sigma = \frac{1}{s} \text{Im} \mathcal{A}(\cos \theta = 1) \Rightarrow \text{Im}(a_{\ell}) = |a_{\ell}|^2 \Rightarrow \text{Re}(a_{\ell}) \leq \frac{1}{2}$$



$$\mathcal{A} \propto g^2 \frac{s^2}{M_W^4} \Rightarrow s \leq M_W^2$$

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Standard Model Drawbacks

Little Hierarchy Problem

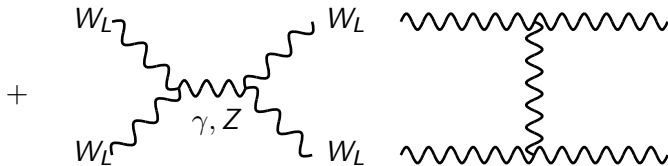
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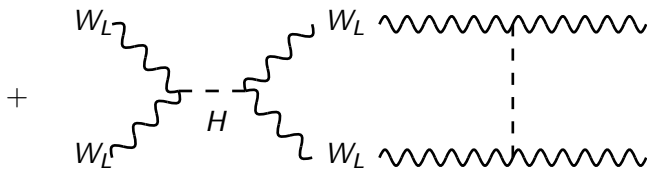
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$$a_0 = \frac{g^2 s}{16\pi M_W^2} \Rightarrow \sqrt{s} \leq 1.7 \text{ TeV}$$



$$a_0 = \frac{g^2 m_H^2}{64\pi M_W^2} \Rightarrow m_H \leq 1.2 \text{ TeV}$$

Including the ZZ scattering one gets

$$m_H \leq 780 \text{ GeV}$$

# THEORETICAL CONSTRAINTS

- ▶ The Higgs mass

$m_H^2 = 2\lambda v^2$  is an independent parameter in the SM.

- ▶ Loop corrections to the  $\lambda$  parameter

## RGE

$$8\pi^2 \frac{d\lambda}{d \log \Lambda} = 3(4\lambda^2 + 2h_t^2\lambda - h_t^2) + \dots$$

produce two bounds on  $m_H$  for a given scale  $\Lambda$

- ▶ For large values of  $\lambda$  (large Higgs masses) there is a **Landau pole** for some value of  $\Lambda$ : **triviality bound**
- ▶ For small values of  $\lambda$  (small Higgs masses) the quartic coupling becomes **negative** for some value of  $\Lambda$ : **stability bound**

## Triviality bounds

- ▶ For large Higgs masses RGE are dominated by

$$8\pi^2 \frac{d\lambda}{d \log \Lambda} \simeq 12\lambda^2$$

and  $\lambda$  increases with  $\Lambda$

$$\lambda(\Lambda) \simeq \frac{m_H^2}{2v^2 - \frac{3m_H^2}{2\pi^2} m_H^2 \log \frac{\Lambda}{v}}$$

- ▶ For fixed  $\Lambda$  there is a lower bound on the Higgs mass

$$m_H^2 \leq \frac{4\pi^2 v^2}{3 \log(\Lambda/v)}$$

- ▶ For fixed  $m_H$  there is an upper bound on  $\Lambda$

$$\Lambda \leq v \exp(4\pi^2 v^2 / 3m_H^2)$$

## Stability bounds

- ▶ For small Higgs masses RGE are dominated by

$$8\pi^2 \frac{d\lambda}{d \log \Lambda} \simeq -3h_t^4$$

and  $\lambda$  decreases with  $\Lambda$

$$\lambda(\Lambda) \simeq \lambda - \frac{3}{8\pi^2} h_t^4 \log \frac{\Lambda}{v}$$

- ▶ When  $\lambda(\Lambda) < 0$  the potential is unbounded from below
- ▶ For fixed  $\Lambda$  there is a lower bound on the Higgs mass

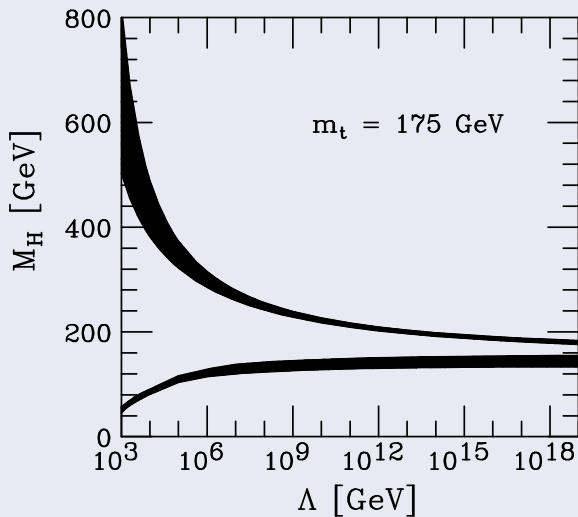
$$m_H^2 \geq \frac{3h_t^2 m_t^2}{2\pi^2} \log \frac{\Lambda}{v}$$

- ▶ For fixed  $m_H$  there is an upper bound on  $\Lambda$

$$\Lambda \leq v \exp(2\pi^2 m_H^2 / 3h_t^2 m_t^2)$$



## The Standard Model Window



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# EXPERIMENTAL CONSTRAINTS

- ▶ Non-observation of the Higgs at LEP-2 in the process  $e^+e^- \rightarrow ZH$  imposes the direct lower bound

## Direct search limit

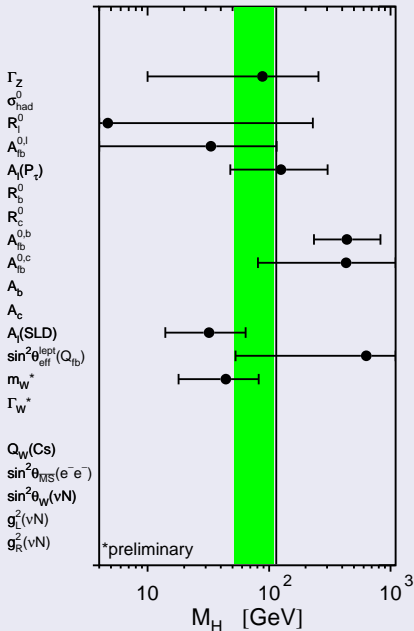
$$m_H > 114.4 \text{ GeV}$$

- ▶ The Higgs mass enters the quantum corrections of electroweak observables, in particular through the  $\rho = 1 + \Delta\rho = 1 + T$  and  $S$  parameters

$$T = \frac{\Pi_{33}(0) - \Pi_{+-}(0)}{M_W^2} \simeq \frac{3G_F}{8\pi^2\sqrt{2}} \left[ m_t^2 - (M_Z^2 - M_W^2) \log \frac{m_H^2}{M_Z^2} \right]$$

$$S \propto \Pi'_{3B}(0) \simeq \frac{1}{6\pi} \log \frac{m_H}{M_Z}$$

# Electroweak observables



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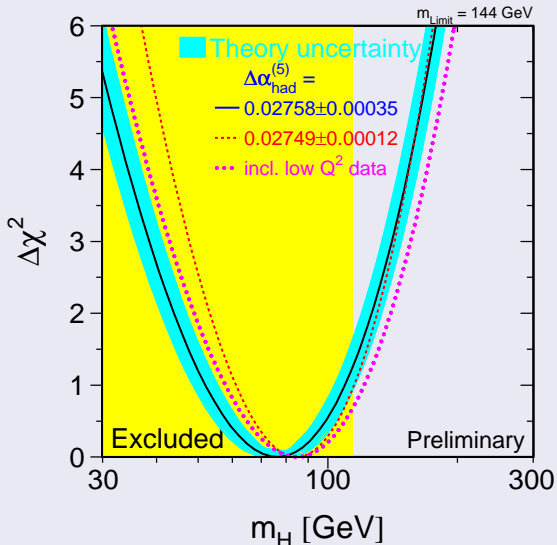
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# Indirect search limit

$$m_H < 144 \text{ GeV } 95\% \text{ C.L.}$$



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## Standard Model Drawbacks

- ▶ Big Hierarchy problem: The Higgs mass is **sensitive to UV** physics. Quantum corrections are quadratically sensitive to the cutoff  $\Lambda$

$$\Delta m_H^2(F, B) = \mp \frac{n_{F, B} g_{F, B}^2}{16\pi^2} \Lambda^2$$

They are not protected by any symmetry which is enhanced when  $m_H = 0$

- ▶ On the contrary fermions masses

$$\Delta m_F \propto \frac{m_F}{16\pi^2} \log \Lambda$$

are protected by chiral symmetry for  $m_F = 0$

- ▶ Electroweak symmetry breaking requires a **tachyonic mass** for the Higgs
- ▶ **Dark Matter**: there is no candidate
- ▶ There is no gauge coupling **unification**
- ▶ Strong CP-problem: **axion** required

# The Little Hierarchy Problem/LEP paradox

- ▶ The leading quantum correction to the Higgs mass parameter is expected to come from the top sector as

$$\Delta m_H^2 = -\frac{3h_t^2}{8\pi^2}\Lambda^2$$

- ▶ In the absence of tuning this implies a lower bound on the cutoff scale as

$$\Lambda < 600 \text{ GeV} \left( \frac{m_H}{200 \text{ GeV}} \right)$$

- ▶ Why did LEP not detect any deviation from the SM predictions? (LEP paradox)
- ▶ In particular one can parametrize the new effects as non-renormalizable operators ( $d = 6$ )

$$\mathcal{L}_{\text{eff}} = \frac{c_1}{\Lambda^2} (\bar{e}\gamma^\mu e)^2 + \dots$$

- ▶ If  $c_i = \mathcal{O}(1) \Rightarrow \Lambda > 10 \text{ TeV} \Rightarrow$  tension

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## Higgs sector

- ▶ An **extended Higgs** sector

$$H_1 = \begin{pmatrix} H_1^0 \\ H_1^- \end{pmatrix}_{-1/2}, \quad H_2 = \begin{pmatrix} H_2^+ \\ H_2^0 \end{pmatrix}_{1/2}$$

- ▶ After the Higgs mechanism  $\langle H_1^0 \rangle = v_1$ ,  $\langle H_2^0 \rangle = v_2$ ,  $\tan \beta = v_2/v_1$  there are **five Higgses** left: two scalar ( $h, H$ ), one pseudoscalar ( $A$ ) and two charged ( $H^\pm$ )
- ▶ Supersymmetry has to be broken, e.g. by embedding the MSSM into a local supersymmetry
- ▶ The Higgs spectrum is determined by two free parameters:  $m_A$  and  $\tan \beta$

$$m_{H^\pm} = m_A^2 + M_W^2, \quad m_{h,H} =$$

$$\frac{1}{2} \left[ m_A^2 + M_Z^2 \mp \sqrt{(m_A^2 + M_Z^2)^2 - 4m_A^2 M_Z^2 \cos^2 2\beta} \right]$$

## Big Hierarchy problem

- ▶ Because quantum corrections to the Higgs mass from bosonic loops have *opposite* signs there is a **cancellation between supersymmetric partners**. Supersymmetry protects the Higgs mass
- ▶ When supersymmetry is broken by *soft* terms the supersymmetric cancellation holds up to supersymmetry breaking terms
- ▶ Quadratic divergences are still absent
- ▶ Hierarchy problem is *technically* solved by the ***non-renormalization theorems*** of supersymmetry

## Dark Matter

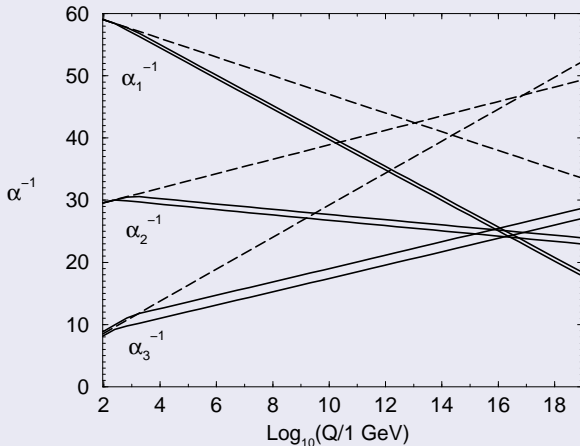
There is a natural candidate for Cold Dark Matter in the MSSM: the **lightest neutralino**, provided that *R*-parity is unbroken



# Gauge coupling unification

Consistently with LEP measurements and if superparticles are at  $\sim$  TeV scale gauge couplings unify at a scale

$$M_{GUT} \sim 2 \times 10^{16} \text{ GeV}$$



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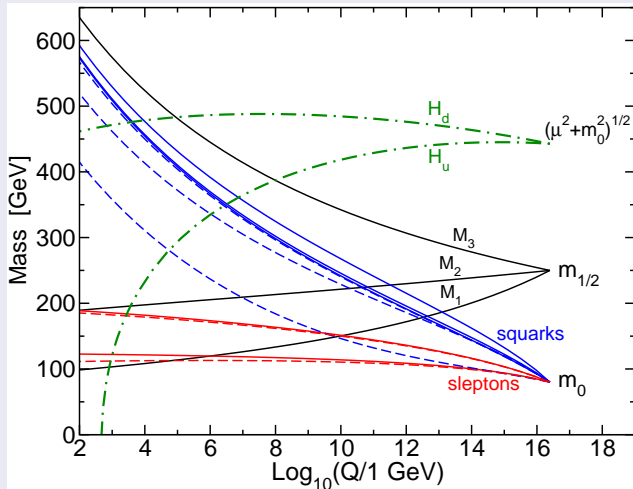
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# Electroweak breaking

If soft breaking parameters are generated at  $M_{GUT}$  a **tachyonic mass** can be **triggered by RGE** at the weak scale



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## Stability/triviality problems

- ▶ The stability ( $\lambda < 0$ ) and triviality/Landau pole ( $\lambda \rightarrow \infty$ ) problems are solved because of the supersymmetric relation

$$\lambda = \frac{1}{8}(g^2 + g'^2)$$

- ▶ Because the gauge couplings remain perturbative (and positive) up to  $M_{GUT}$  there is no stability and/or triviality problem in the MSSM
- ▶ As a consequence: the Higgs mass (unlike in the SM) is **NOT** a free parameter. For the SM-like Higgs

$$m_h^2 \simeq M_Z^2 \cos^2 2\beta + \frac{3G_F m_t^4}{\sqrt{2}\pi^2} \left[ \log \frac{m_t^2}{m_t^2} + \frac{A_t^2}{M_S^2} \left( 1 - \frac{A_t^2}{12M_S^2} \right) \right]$$

- ▶ The Higgs mass is a **prediction** in a supersymmetric theory  $\Rightarrow$  theoretical constraints

# THEORETICAL CONSTRAINTS

- ▶ The Higgs mass is a **prediction** in the MSSM
  - ▶ At the **tree level** there is the absolute bound

## Tree-level

$$m_h^2 \leq M_Z^2$$

- ▶ At **one-loop** there is an important contribution controlled by the top/stop sector

## One-loop

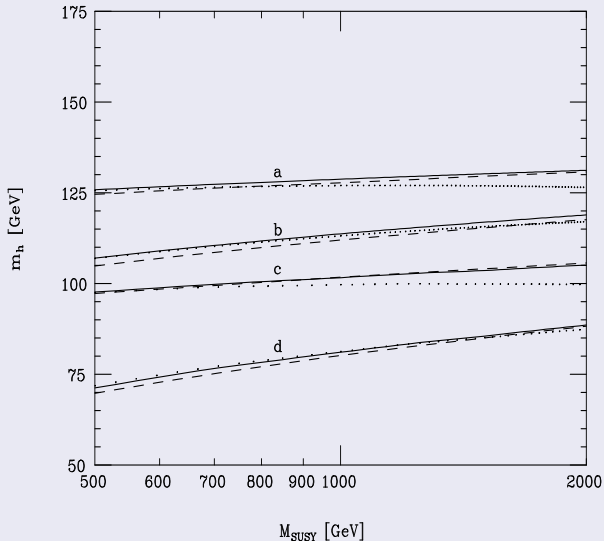
$$\Delta m_h^2 = \frac{3G_F m_t^4}{\sqrt{2}\pi^2} \left[ \log \frac{m_t^2}{m_h^2} + \frac{A_t^2}{M_S^2} \left( 1 - \frac{A_t^2}{12M_S^2} \right) \right]$$

- ▶ Even if the one-loop contribution can be larger than the tree-level **perturbation theory holds**

## Little fine-tuning problem

To satisfy the experimental bounds a **stop around the TeV scale** is needed which produces a  $\sim 1\%$  fine-tuning in the determination of the Z-mass

$m_h$  Vs.  $M_{SUSY}$  [ $m_A \sim 1$  TeV, (a,b)  $\tan \beta = 15$   
 $A_t/M_{SUSY} = (\sqrt{6}, 0)$ ; (c,d)  $\tan \beta = 2$ ]



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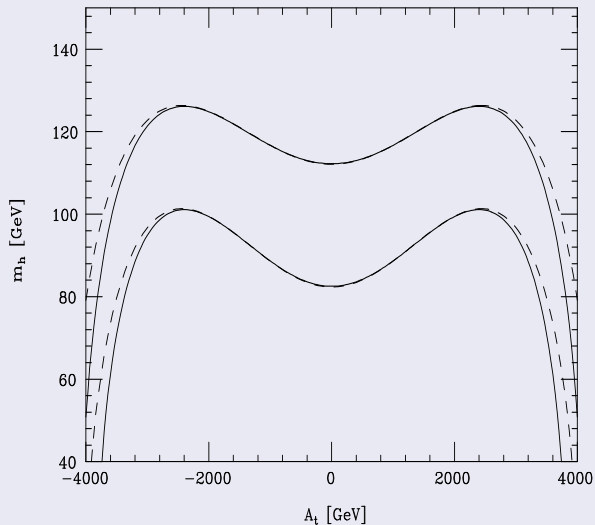
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# $m_h$ Vs. $A_t$ [ $M_{SUSY}, m_A \sim 1$ TeV, $\tan \beta = 15, 2$ ]



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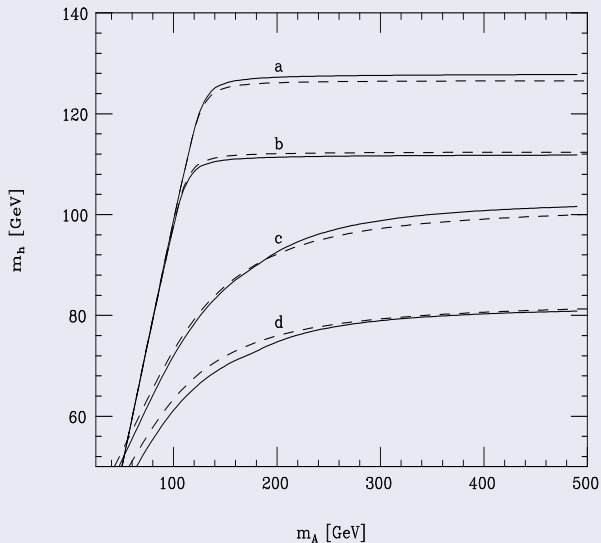
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# $m_h$ Vs. $m_A$ [ $M_{SUSY} \sim 1$ TeV]



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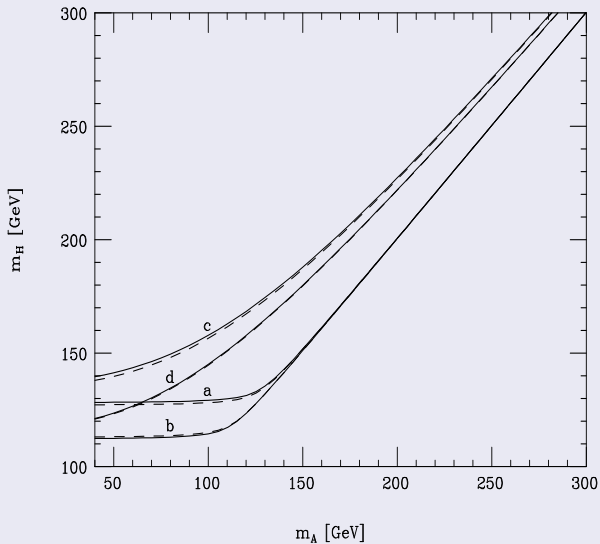
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# $m_H$ Vs. $m_A$ [ $M_{SUSY} \sim 1$ TeV]



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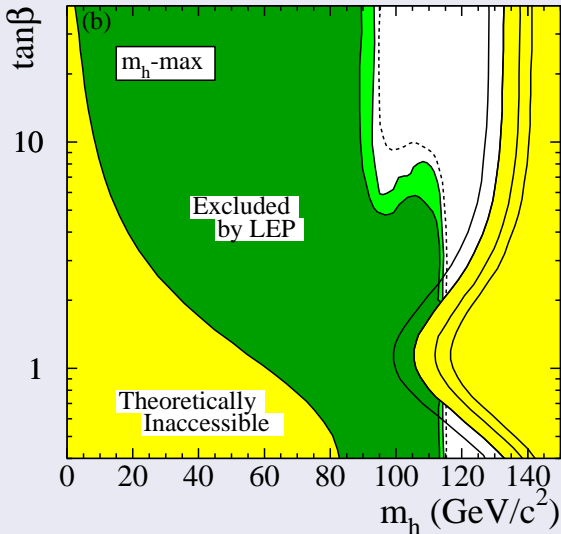
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# Experimental constraints from LEP-2



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# Drawbacks of the MSSM

- ▶ Little fine tuning:  $\sim 1\%$  **fine-tuning**
- ▶ **Large number** ( $\sim 10^2$ ) of free parameters
- ▶ Uncertainty in the mechanism of **supersymmetry breaking**:
  - ▶ **Gravity mediation**:
    - ▶ Universal mechanism solving the  $\mu/B\mu$  problem
    - ▶ Its minimal version reduces the number of free parameters to a few
    - ▶ So-called **Supergravity** models
  - ▶ **Gauge mediation**
    - ▶ It is **flavor blind**
    - ▶ It has  $\mu/B\mu$  problems
    - ▶ **Gravitino is the LSP**
  - ▶ **Anomaly mediation**
    - ▶ **Tachyonic** sleptons
- ▶ **Supersymmetric flavor problem**: supersymmetric partners can create FCNC and CP violating operators
- ▶ Gravity mediation has to be **subdominant** ( $\sim 0.1\%$  of gauge mediation)

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# LITTLE HIGGS

- ▶ Little Higgs models aim to solve the **Little Hierarchy** problem
- ▶ The symmetry that protects the (little) hierarchy is a **global symmetry** of which the **Higgs** is an approximate **(pseudo) Goldstone boson**
- ▶ It is inspired from low energy hadronic physics: there  $\pi^{\pm 0}$  are Goldstone bosons associated to the spontaneous breaking  $SU(2)_L \times SU(2)_R \rightarrow SU(2)_I$
- ▶ Similarly the Higgs is the Goldstone boson of a global symmetry  $G_0 \rightarrow H_0$ . It is in the coset space  $H \in G_0/H_0$
- ▶ The symmetry  $H \rightarrow H + c$  is broken (in particular) by Yukawa interactions

$$\Rightarrow m_H^2 \sim \frac{\alpha_t}{4\pi} \Lambda^2 \Rightarrow \text{LEP paradox}$$

- ▶ LH is a clever construction to avoid the appearance of the lowest order contribution to  $m_H^2$

## Collective breaking

- ▶ The mass of a Higgs pseudo-Goldstone boson from the different couplings  $\alpha_j$  that break the Goldstone symmetry is

$$m_H^2 = \left( c_i \frac{\alpha_i}{4\pi} + c_{ij} \frac{\alpha_i \alpha_j}{(4\pi)^2} \right) \Lambda^2$$

where the coefficients are controlled by selection rules

- ▶ If the Goldstone symmetry is **restored when any single coupling  $\alpha_j = 0$**

$\Rightarrow$  To totally destroy the Goldstone symmetry one requires the combined effect [**collective breaking**] of **at least two non-zero couplings**

$$\Rightarrow m_H^2 \sim \left( \frac{\alpha}{4\pi} \right)^2 \Lambda^2 \Rightarrow \Lambda \sim 10 \text{ TeV}$$

- ▶ This is a solution to the LEP paradox/Little Hierarchy problem

## General structure

- ▶ There is a global group  $G_g$  which spontaneously breaks to a subgroup  $H_g$  at a scale  $f \sim 1 \text{ TeV}$  and the theory becomes strong at the scale  $\Lambda \sim 4\pi f \sim 10 \text{ TeV}$  [Scales are similar to  $\Lambda_{QCD}$  and  $f_\pi$  in QCD]
- ▶ The subgroup  $G_I \subset G_g$  is gauged:  $G_I \supset SU(2) \times U(1)$
- ▶ The combination of spontaneous and collective breaking makes:  $G_I \rightarrow SU(2) \times U(1)$  leaving heavy vector bosons and fermions with masses

$$M_{\text{Heavy}} \sim g f \sim 1 \text{ TeV}$$

- ▶ Higgs is part of the Goldstone multiplet which parametrizes the coset space  $G_g/H_g$

Model	$G_g$	$H_g$
<i>Littlest</i>	$SU(5)$	$SO(5)$
<i>Simplest</i>	$SU(3)^2$	$SU(2)^2$

## General structure

- ▶ The generators of  $G_I$  do not commute with the generators of the Higgs and thus **gauge and Yukawa couplings collectively break the Goldstone symmetry and induce a Higgs mass**
- ▶ The global invariance of the SM must be **extended** according to the different models (Littlest, Simplest,...)
- ▶ There are **same spin partners** for every SM field.
- ▶ When computing corrections to the Higgs mass these partners enforce the selection rule  $c_i = 0$  by cancelling the one-loop quadratic divergent contributions of the Higgs field
- ▶ For instance if  $SU(3) \subset G_g$ 
  - ▶ The quarks appear in triplets or singlets

$$\begin{pmatrix} t \\ b \\ T \end{pmatrix}_L, t_R, b_R, T_R$$

- ▶ The Higgs boson arises as a pseudo-Goldstone boson from the spontaneous breaking  $SU(3) \rightarrow SU(2) \times U(1)$

## General structure

- ▶ The gauge structure is also enlarged

Model	$G_g$	$H_g$	$G_l$
<i>Littlest</i>	$SU(5)$	$SO(5)$	$[SU(2) \times U(1)]^2$
<i>Simplest</i>	$SU(3)^2$	$SU(2)^2$	$SU(3) \times U(1)$

- ▶ **Littlest:**

- $SU(5) \rightarrow SO(5)$ :  $24-10=14$  Goldstone bosons
- 4 absorbed by the broken gauge group
- 10 Goldstone bosons = 4 (Higgs doublet) + 6 (Higgs triplet)

- ▶ The one-loop **quadratic divergence** from the **top** quark

$$\Delta M_H^2 \sim -\frac{\alpha_t}{4\pi} \Lambda^2$$

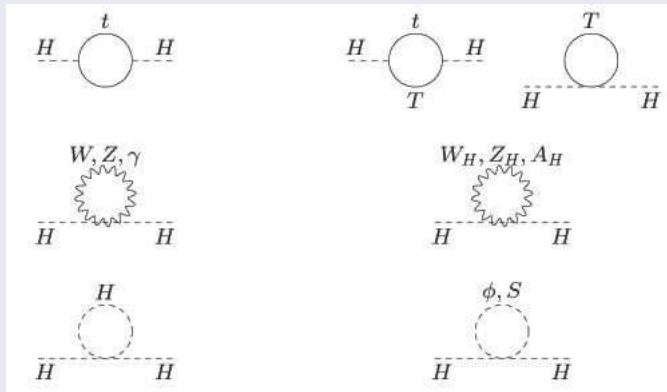
is cancelled by that from the  $T$  quark

- ▶ The one-loop **quadratic divergence** from the  $W$  gauge boson

$$\Delta M_H^2 \sim \frac{\alpha_W}{4\pi} \Lambda^2$$

is cancelled by that from the  $W_H$  gauge boson

## Cancellation of quadratic divergences



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**General structure**

General features

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## Electroweak breaking

It is triggered by the  $t - T$  sector analogously to the MSSM

$$\Delta m_H^2 = -\frac{3}{8\pi^2} h_t^2 m_T^2 \log \frac{\Lambda}{m_T}$$

Since  $\Delta m_H^2 \sim m_T^2$  electroweak breaking requires some **tuning** of at least 5% as in the MSSM

## Dark Matter

In the **Littlest** LH models one can introduce a  $T$ -parity such that **SM particles** (extra particles) are **T-even** (**T-odd**). In this case the lightest T-odd gauge boson is a candidate to DM

## Electroweak precision tests

T-parity forbids the mixing between T-odd and T-even gauge bosons leading naturally to  $S = 0$

# GAUGE HIGGS UNIFICATION

- ▶ We have explored two symmetries protecting the Higgs from quadratic divergences: **supersymmetry and a global symmetry**
- ▶ In higher dimensional theories there is another symmetry which could do the job: **a gauge symmetry**
- ▶ The gauge bosons of a higher dimensional gauge symmetry decompose as

## Lorentz Decomposition

$$A_M^A = A_\mu^A, A_i^A \quad [\mu = 0, \dots, 3, i = 1, \dots, d]$$

- ▶  $A_\mu^A$  are gauge bosons in four dimensions
- ▶  $A_i^A$  are scalar in the **adjoint** representation

## Orbifold constructions

We need to compactify extra dimensions in an orbifold:

e.g. for  $d = 1$  ( $A_\mu, A_5$ )

$$S^1/\mathbb{Z}_2$$

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How to get a doublet  
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Radiative symmetry  
breaking

Difficulties with GHU  
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- ▶ The orbifold group has to act non trivially on the group generators such that:

## Orbifold Decomposition

$$A_{\mu}^A = A_{\mu}^a(\text{even}), A_{\mu}^{\hat{a}}(\text{odd})$$

$$A_5^A = A_5^a(\text{odd}), A_5^{\hat{a}}(\text{even})$$

- ▶ Only even fields have zero modes  $\phi_{\text{even}}^{(n)}, n = 0, 1, 2, \dots$  while odd field have only non zero modes  $\phi_{\text{odd}}^{(n)}, n = 1, 2, \dots$
- ▶ The Higgs mechanism acts for all modes as

## Higgs mechanism

$$(A_{\mu}^{\hat{a}} \text{ massless} + A_5^{\hat{a}})^{(n \neq 0)} = A_{\mu}^{\hat{a}(n \neq 0)} \text{ massive}$$

$$(A_{\mu}^a \text{ massless} + A_5^a)^{(n \neq 0)} = A_{\mu}^{a(n \neq 0)} \text{ massive}$$

- ▶ The massless states are the zero modes

## Massless states

$$A_{\mu}^{a(n=0)}, A_5^{\hat{a}(n=0)}$$

- ▶ To get a doublet out of an adjoint one has to make a careful orbifold breaking
- ▶ One has to **enlarge** the gauge group since the

SM Higgs is **NOT** in the adjoint representation of  $SU(2) \times U(1)$

- ▶ For instance

$$SU(3) \rightarrow SU(2) \times U(1)$$

Achieved by the orbifold action

$$A_\mu(-y) = UA_\mu(y)U^\dagger, \quad A_5(-y) = -UA_5(y)U^\dagger \text{ with}$$

$$\text{diag}(-1, -1, +1)$$

which breaks  $SU(3)$  into  $SU(2) \times U(1)$

- ▶ The Higgs mass is protected from **quadratic divergences** in the bulk of the extra dimension by the **five-dimensional gauge symmetry**





There is a number of difficulties with this (otherwise very nice) scenario

## Drawbacks

- ▶ In more than five dimensions a (quadratically divergent) **tadpole** localized at the fixed points  $F_{ij}$  is generated by radiative corrections while the **quartic** Higgs coupling is sizeable and generated by the term  $F_{ij}^2$  in the bulk
- ▶ In **five** dimensions there is no localized tadpole but there is neither a tree-level quartic coupling which means difficulties with *too small a Higgs mass*
- ▶ It is difficult to have a theory with the correct prediction for the **weak** angle [extra  $U(1)$ 's are usually required]
- ▶ **Fermion masses** are difficult to accommodate since they come from gauge couplings: in particular the top quark used to be too light
- ▶ The compactification scale is usually too small in conflict with EWPT
- ▶ The theory has a very **low cutoff** after which it becomes non-perturbative

Some of these difficulties can be alleviated by embedding GHU in a **warped** (Randall-Sundrum) five-dimensional space time

## Wayouts

- ▶ Warped models are valid up to scales of order  $M_{GUT}$  or  $M_{Planck}$  and they can unify
- ▶ The Higgs is **holographic**, i.e. it is localized towards the IR brane [at higher scales it is composite]
- ▶ **Fermion masses** can be implemented by means of their **localization**, i.e. five-dimensional masses
- ▶ The top quark (to get a big mass) is **localized** as the Higgs. So it is also **holographic**
- ▶ EWPT as well as corrections to the  $Zb\bar{b}$  vertex lead to KK-masses in the 2.5 – 4 TeV, which imply  $\sim 1\%$  fine-tuning for the Higgs mass (similar to the MSSM)
- ▶ These models are the modern version of technicolor theories: they make use of the **AdS/CFT** correspondence for **calculability**



## Unparticles

- ▶ Recently Georgi <sup>a</sup> has introduced a new way of studying **conformal sectors**, with a fixed point at the scale  $\Lambda$ , that couple to the Standard Model.
- ▶ Fields in a conformal theory can acquire **large anomalous dimensions**  $\gamma$  and modify the scaling dimension  $d$  of the field
- ▶ If the conformal symmetry is broken at a scale  $m_g$ , which provides a continuum of states above the mass gap the propagator for a scalar particle can be described as

$$\Delta(p) \propto \frac{1}{(-p^2 + m_g^2 - i\epsilon)^{1-\gamma}}$$

- ▶ The particle propagator is reached for the case  $\gamma = 0$

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<sup>a</sup>H. Georgi, hep-ph/0703260

- ▶ Making a step forward along the previous direction one can speculate with the idea that the **Higgs** is an object of a conformal theory (unparticle) with a fixed point at a scale  $\Lambda$  and a scaling dimension  $d = 1 + \gamma$ , where  $\gamma$  is the anomalous dimensions: an un-Higgs<sup>a</sup>
- ▶ The un-Higgs is coupled to the SM fields by Yukawa interactions

$$\mathcal{L} = h_t \frac{1}{\Lambda^\gamma} H^\dagger \bar{q}_L t_R + h.c.$$

- ▶ For  $\gamma > 0$  the operator is **irrelevant** and does not take the conformal theory out of the fixed point
- ▶ The **conformal symmetry** should be **broken at a scale  $m_g$**  which is related to the VEV of the un-Higgs,  $v^d$ : it can be triggered by SM top-loop effects

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<sup>a</sup>D. Stancato and J. Terning, 0807.3961 [hep-ph]

## The fine-tuning/hierarchy problem

- ▶ The Higgs mass term is given by

$$m_H^{2(1-\gamma)} |H|^2$$

- ▶ The radiative corrections induced by the top Yukawa coupling are

$$\delta m_H^{2(1-\gamma)} = \frac{3h_t^2}{8\pi^2} \Lambda^{2(1-\gamma)}$$

- ▶ The **sensitivity** of the Higgs mass to radiative corrections is

$$1 + \frac{3h_t^2}{8\pi^2} \left( \frac{\Lambda^2}{m_H^2} \right)^{1-\gamma}$$

- ▶ For  $\gamma = 0$  it is the usual sensitivity appearing from quadratic divergences
- ▶ For  $\gamma \rightarrow 1$  the sensitivity is tiny for any value of  $\Lambda$
- ▶ For instance for  $\gamma = 0.7$  one can push  $\Lambda = 10$  TeV without much tuning

## Conclusions

- ▶ The last word will be from **LHC**
- ▶ One possibility is that the theory below  $M_{Planck}$  is **just the Standard Model**: in that case we should try to find other solutions to the hierarchy problem, as e.g. an anthropic solution/landscape
- ▶ If the Higgs is **light** ( $< 135$  GeV) then an excellent candidate is the MSSM although supersymmetric particles should show up at LHC
- ▶ If the Higgs is **heavy** then other particles should appear to restore agreement with present electroweak precision tests
- ▶ If there is **no Higgs** at all other resonances should appear to restore unitarity in  $WW$  scattering
- ▶ **Even if the Higgs is found we will (probably) need a linear collider for Higgs precision physics**