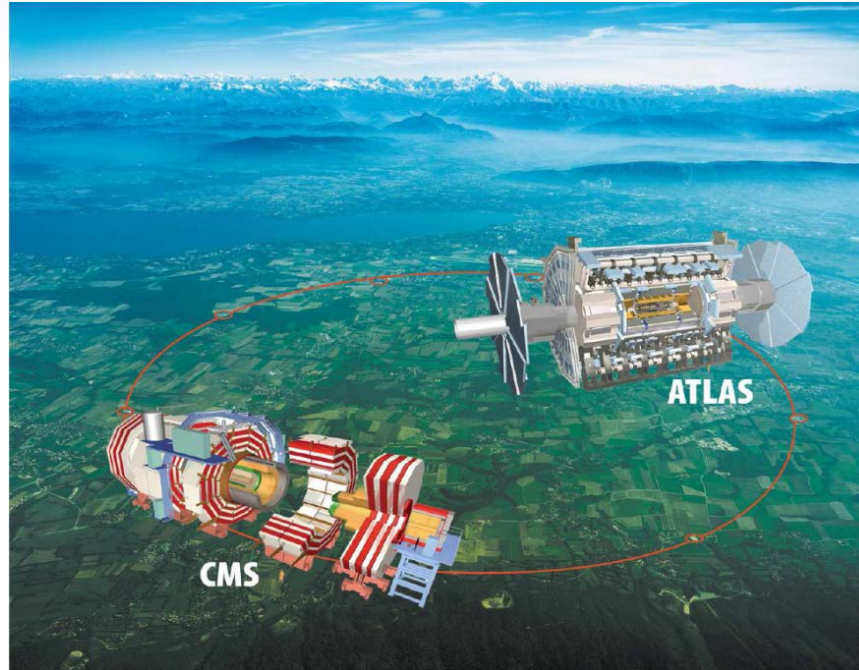


Measurements of the 7 and 8 TeV cross sections for $Z \rightarrow 4l$ in pp collisions with ATLAS and CMS



Bing Zhou

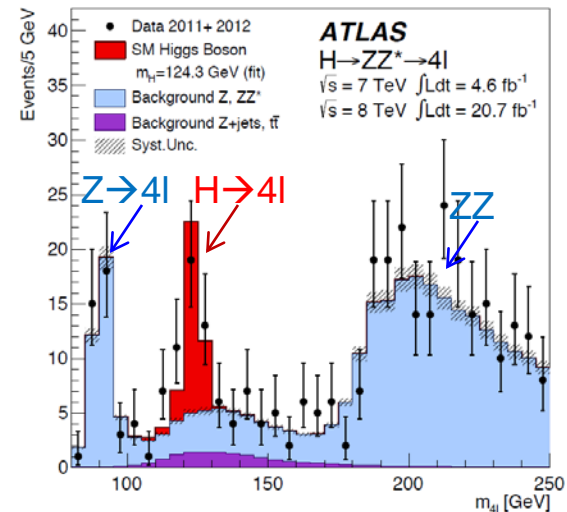
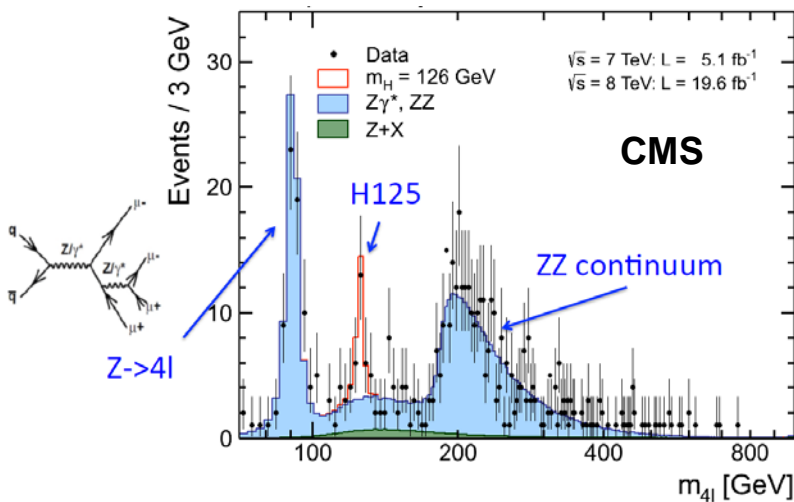
The University of Michigan

XXII International Workshop on Deep-Inelastic Scattering and Related Subjects

4/28-5/2 2014, Warsaw, Poland

Introduction

- ❖ The $Z \rightarrow 4\ell$ production was first observed at the LHC by both ATLAS and CMS experiments along with the Higgs boson discovery in the 4ℓ decay channel
- ❖ Cross section measurement of the $Z \rightarrow 4\ell$ production provides
 - A SM test for a rare decay process (measurements of $\sigma(4\ell)$ and $BR(Z \rightarrow 4\ell)$)
 - A complementary test of the detector response for $H \rightarrow 4\ell$ detection



References:

- **ATLAS:** [arXiv:1403.5657 \[hep-ex\]](https://arxiv.org/abs/1403.5657); ATLAS-CONF-2013-055
- **CMS:** JHEP 12 (2012) 034, [arXiv:1210.3844 \[hep-ex\]](https://arxiv.org/abs/1210.3844); CMS PAS SMP-12-009

4 ℓ Production at Z Resonance

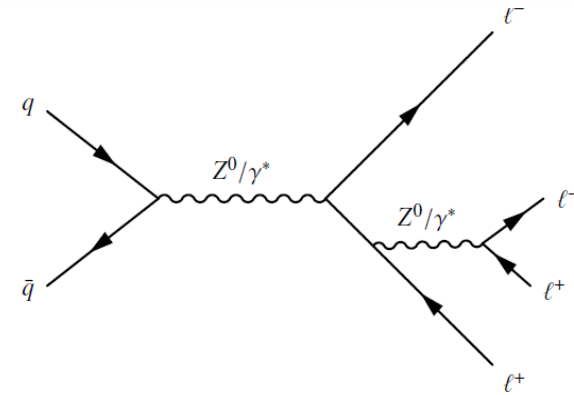
❖ Four lepton final states: 4e, 4 μ and 2e2 μ

❖ **Resonant 4 ℓ production** via an s-channel

-- $Z \rightarrow \ell^+ \ell^-$ include an additional $\ell^+ \ell^-$ from internal conversion of Z^*/γ^*

-- s-channel is dominant

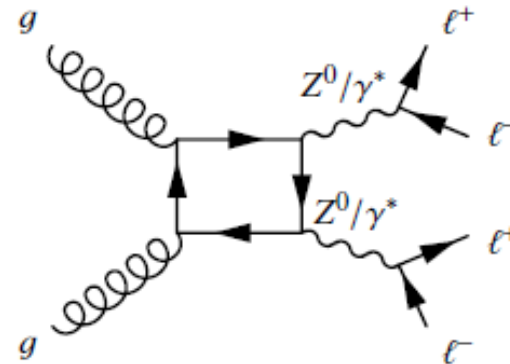
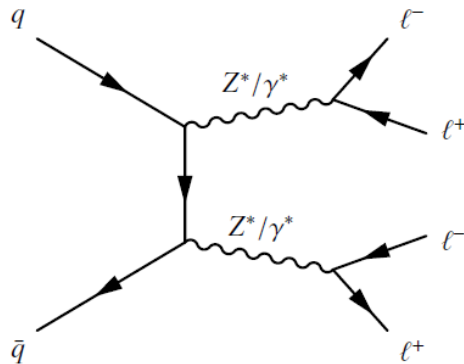
(>96% for $80 < m_{4\ell} < 100$ GeV, $m_{2\ell} > 5$ GeV)



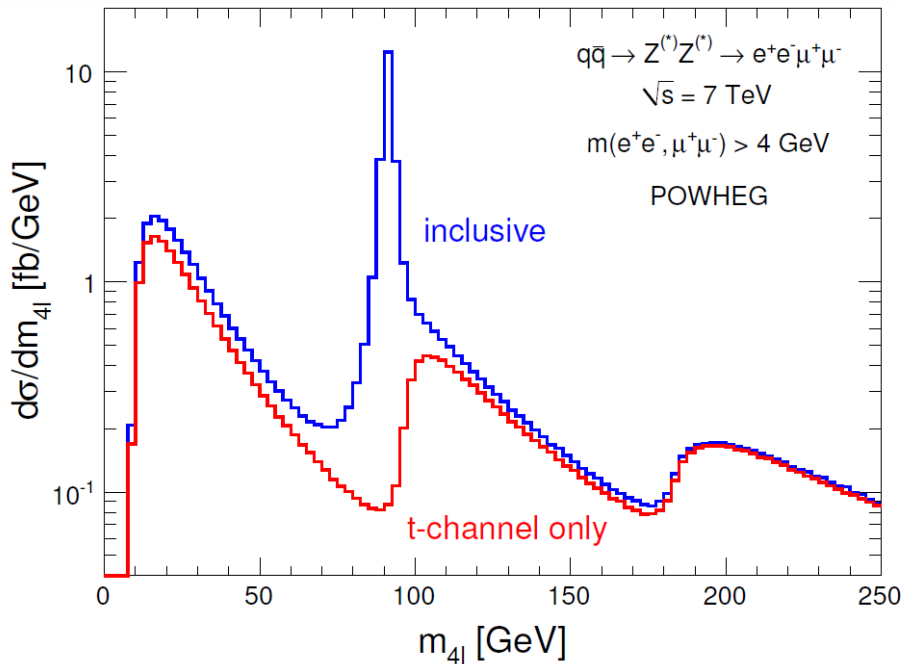
❖ **Non-resonant 4 ℓ production**

- via t-channel: $q\bar{q} \rightarrow Z^*/\gamma^* + Z^*/\gamma^* \rightarrow 4\ell$ including the Z production with ISR internal conversion (< 4% 4 ℓ event rate at the Z resonance)

- via $gg \rightarrow ZZ \rightarrow 4\ell$ (~0.1% 4 ℓ event rate at the Z resonance)



4 ℓ Production Modeling



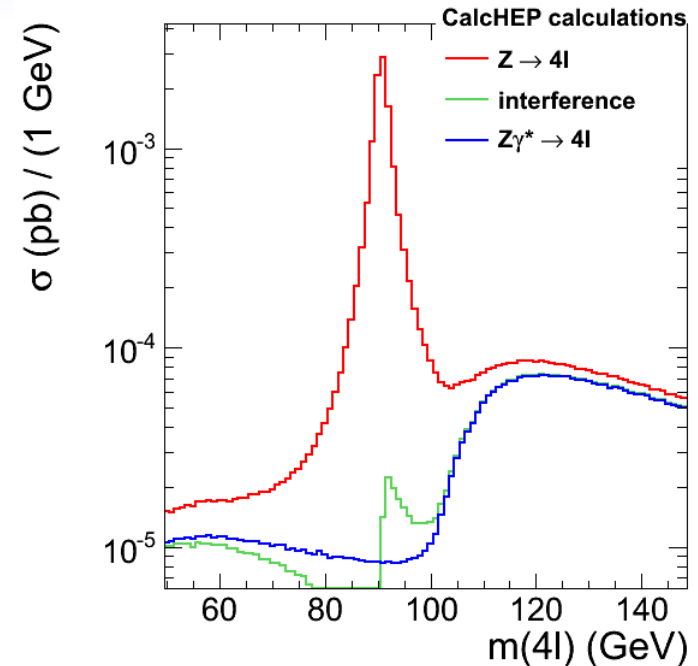
$q\bar{q} \rightarrow Z/Z^*Z^* \rightarrow 4\ell$ modeled by Powheg MC for

- Cross section calculations (NLO QCD)
- Event generations (interfaced to PYTHIA)

$g\bar{g} \rightarrow ZZ \rightarrow 4\ell$ modeled by GG2ZZ MC for

- Cross section calculations (LO QCD)
- Event generations (interfaced to Herwig/Jimmy)

MCFM MC used to cross check cross sections



CalcHEP MC (LO QCD) used to calculate the magnitude of interference between the s-channel and the t-channel 4ℓ production processes

- $\sim 0.2\%$ in the 4ℓ phase space

$80 < m_{4\ell} < 100$ GeV, $m_{2\ell} > 5$ GeV

- treat it as systematic uncertainty when determine the $Z \rightarrow 4\ell$ branching fraction

Z → 4l Is A Rare Decay

- **No measurement before the LHC**
- NLO Calculation by Powheg MC (PDF: CT10, Scales: $m_{4\ell}$) in a phase space: $80 < m_{4\ell} < 100$ GeV and $m_{\ell+\ell-} > 5$ GeV

Expected quantity	7 TeV	8 TeV
Total inclusive cross-section of $pp \rightarrow Z$	26.0 ± 0.6 nb	30.3 ± 0.8 nb
Total cross-section of $pp \rightarrow Z/ZZ^* \rightarrow 4\ell(e, \mu)$	89.97 ± 2.06 fb	104.84 ± 2.50 fb
Cross-section of $pp \rightarrow Z/ZZ^* \rightarrow 4e, 4\mu$	45.78 ± 1.10 fb	53.35 ± 1.24 fb
Cross-section of $pp \rightarrow Z/ZZ^* \rightarrow 2e2\mu$	44.19 ± 1.04 fb	51.49 ± 1.26 fb
Total t -ch. cross-section of $pp \rightarrow ZZ^* \rightarrow 4\ell(e, \mu)$	3.28 ± 0.08 fb	3.80 ± 0.09 fb
t -ch. cross-section of $pp \rightarrow ZZ^* \rightarrow 4e, 4\mu$	1.55 ± 0.04 fb	1.79 ± 0.04 fb
t -ch. cross-section of $pp \rightarrow ZZ^* \rightarrow 2e2\mu$	1.73 ± 0.04 fb	2.01 ± 0.05 fb
Branching ratio of $Z \rightarrow 4\ell(e, \mu)$	$(3.33 \pm 0.01) \times 10^{-6}$	

- For a larger phase space $80 < m_{4\ell} < 100$ GeV, $m_{\ell+\ell-} > 4$ GeV, the inclusive 4ℓ cross section is 35% higher

Measurement Approaches

- **ATLAS (with data collected at 7 and 8 TeV)**

- Measure **inclusive** 4ℓ production cross-section at the Z resonance, i.e. the non-resonance 4ℓ events are treated as *signal* \rightarrow cross section measurement will be less depending on theory interpretation; measured both **fiducial** and **final phase space** cross sections.
- In determination of $Z \rightarrow 4\ell$ decay branching fraction, the non-resonance 4ℓ contribution is subtracted and the resonance 4ℓ event yield is normalized by the $Z \rightarrow \mu\mu$ with the same dataset

- **CMS (with data collected at 7 TeV)**

- Measure the resonance $Z \rightarrow 4\ell$ production cross section, and treat the t-channel 4ℓ events as background
- Using the $Z \rightarrow \mu\mu$ events to normalize the $Z \rightarrow 4\ell$ events to determine the $BR(Z \rightarrow 4\ell)$

- **Phase space for measurements**

- **ATLAS:** $80 < m_{4\ell} < 100$ GeV and $m_{\ell^+\ell^-} > 5$ GeV;
also measured BR in a larger phase space: $m_{\ell^+\ell^-} > 4$ GeV
- **CMS:** $80 < m_{4\ell} < 100$ GeV, $m_{\ell\ell} > 4$ GeV (for any pairs of leptons)

Data Sets for $Z \rightarrow 4l$ Analysis

- **ATLAS**

- 4.6 fb⁻¹ at 7 TeV (collected in 2011);
- 20.3fb⁻¹ at 8 TeV (collected in 2012)
- In detection fiducial volume, trigger efficiencies for 4 l event detection: 95 - 99% (2011); 94 – 98% (2012)

- **CMS**

- 5.0 fb⁻¹ at 7 TeV (collected in 2010 and 2011)
- In detection fiducial volume, trigger efficiencies: 96 – 99%

Experimental Challenge to Detect $Z \rightarrow 4\ell$

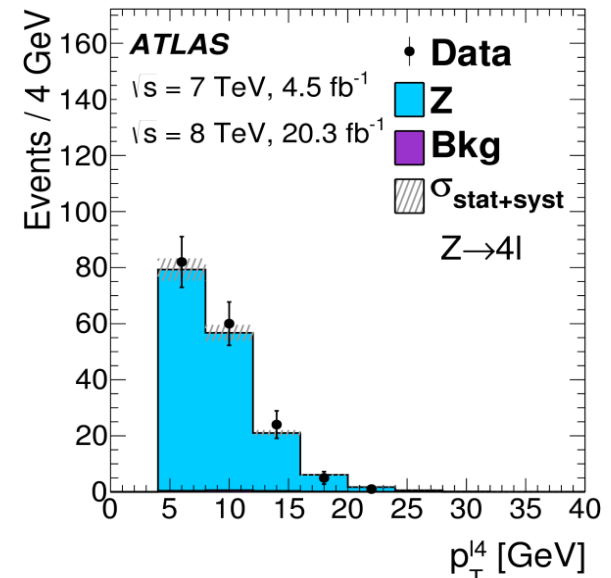
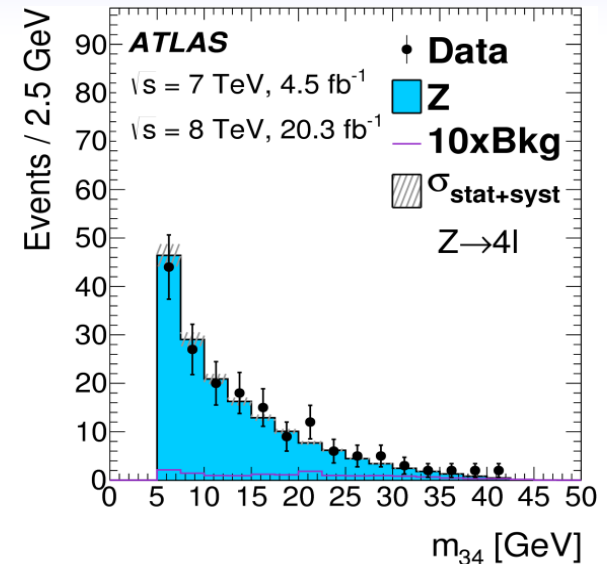
- The $Z \rightarrow 4\ell$ process is dominant by low mass m_{34} and low p_T leptons (the p_T -ordered 4th leptons)
- **Need to detect low p_T leptons**

ATLAS $Z \rightarrow 4\ell$ selection:

$e : p_T > 20, 15, 10, 7 \text{ GeV}, |\eta| < 2.5$
 $\mu : p_T > 20, 15, 8, 4 \text{ GeV}, |\eta| < 2.7$
 $m_{12} (\ell^+\ell^-) > 20 \text{ GeV}, m_{34} (\ell^+\ell^-) > 5 \text{ GeV}$
 $80 \text{ GeV} < m_{4\ell} < 100 \text{ GeV}$

CMS $Z \rightarrow 4\ell$ selection:

$e : p_T > 20, 10, 7, 7 \text{ GeV}, |\eta| < 2.5$
 $\mu : p_T > 20, 10, 5, 5 \text{ GeV}, |\eta| < 2.4$
 $m_{\ell\ell} > 4 \text{ GeV}$
 $80 \text{ GeV} < m_{4\ell} < 100 \text{ GeV}$



Event Display of $Z \rightarrow 4\mu$



CMS

Run: 180076

Event : 456795917

pT_1 : 43.76 GeV

pT_2 : 24.20 GeV

pT_3 : 10.51 GeV

pT_4 : 7.39 GeV

M_{Z1} : 62.58 GeV

M_{Z2} : 17.27 GeV

M_{4L} : (91.30 ± 0.61) GeV

Min(mass2l) : 12.22 GeV

Max(mass2l) : 62.58 GeV

CMS Experiment at LHC, CERN
Data recorded: Thu Oct 27 17:10:24 2011 EDT
Run/Event: 180076 / 456795917

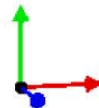


Figure 5: Event display of a typical event from the peak at the Z boson mass.

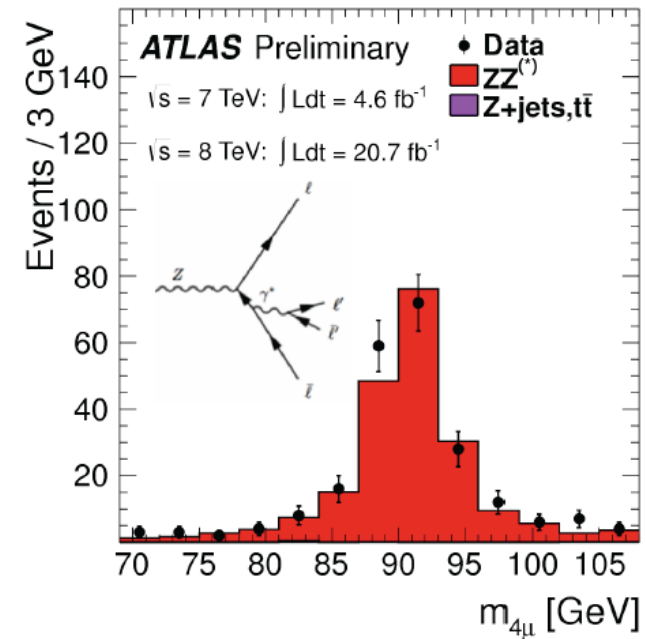
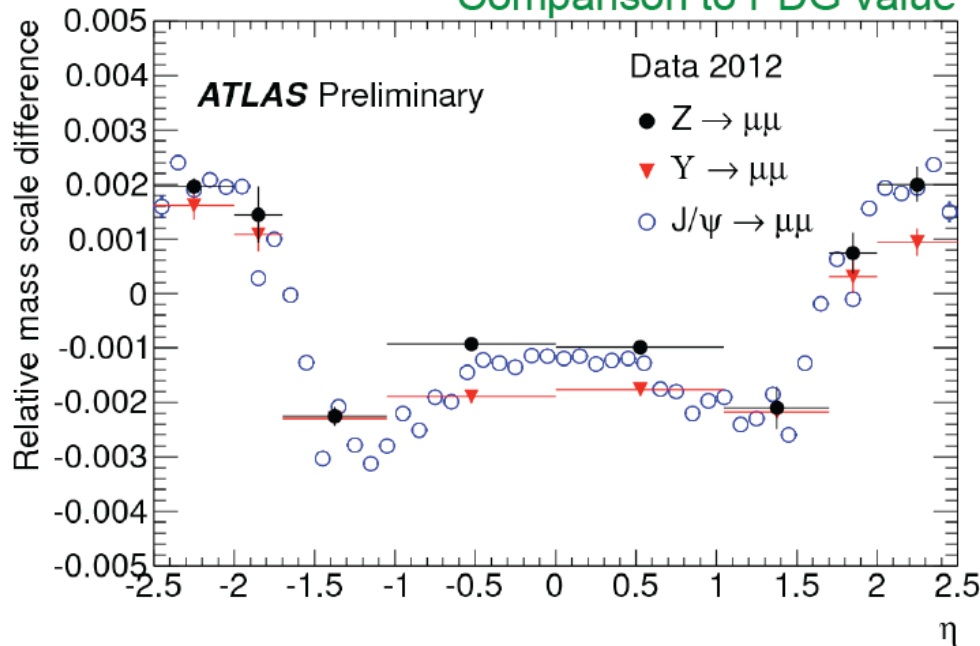
Muon Momentum Scale and Resolution

ATLAS

Muon energy scale and resolution corrections and systematic uncertainties determined from large Z, J/ψ and Y samples

- Resolution correction (0.2-1.3%), scale correction ($< 0.1\%$)
- Independent measurements from Muon Spectrometer and inner tracker
- Probe global and local scale biases, overall uncertainty on 4μ scale 0.2%
- Calibration using $Z \rightarrow 4\mu$ mass peak (with $m_{21} > 1$ GeV)

Comparison to PDG value

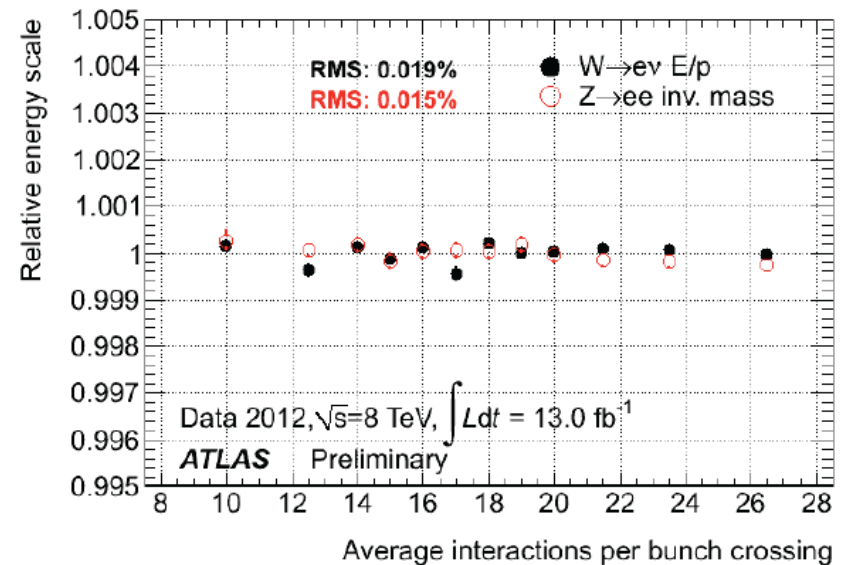
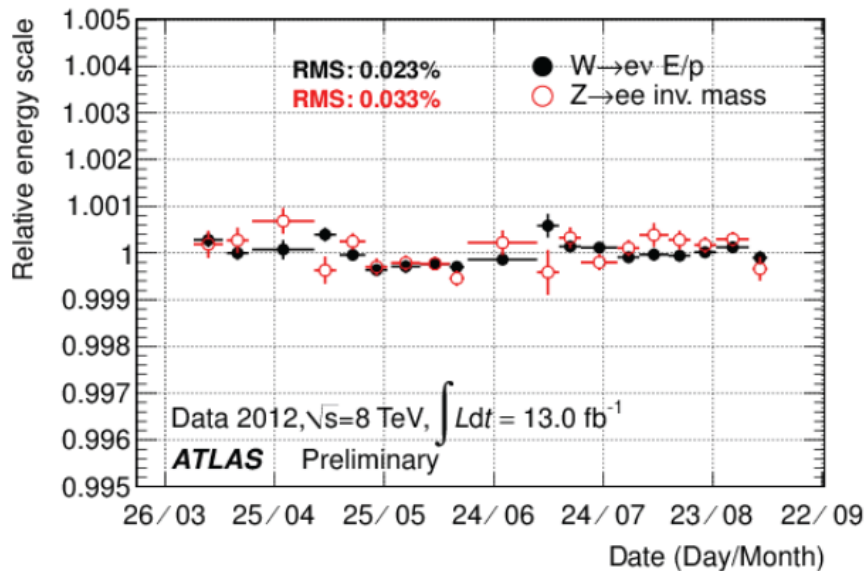


EM Calorimeter Calibration

ATLAS

- In-situ energy calibration results and their stability checked with different methods (E/P with $W \rightarrow e\nu$, $Z \rightarrow ee$, and $J/\psi \rightarrow ee$)
- Uncertainty on the diphoton mass scale 0.6%, largely contributions
 - Material effects (separately for volumes for $|\eta| < 1.8$, and $|\eta| > 1.8$)
 - Uncertainty on the in-situ calibration method

Stability of EM calorimeter response vs time/pile-up better than 0.1%



Acceptance $A_{4\ell}$, Correction Factor $C_{4\ell}$, σ^{fid} and σ^{total}

Fiducial volume definition

ATLAS

$$p_T^{\ell 1} > 20 \text{ GeV}; p_T^{\ell 2} > 15 \text{ GeV};$$

$$p_T^{\ell 3} > 10 \text{ GeV (if electron), } > 8 \text{ GeV (if muon);}$$

$$p_T^{\ell 4} > 7 \text{ GeV (if electron), } > 4 \text{ GeV (if muon);}$$

$$|\eta^\mu| < 2.7 \text{ for all muons; } |\eta^e| < 2.5 \text{ for all electrons;}$$

$$\Delta R(\ell, \ell') > 0.1 \text{ for all same flavor pairings and } > 0.2 \text{ for different flavor pairings;}$$

$$M_{\ell^+ \ell^-} > 20 \text{ GeV for at least one SFOS lepton pair;}$$

$$M_{\ell^+ \ell^-} > 5 \text{ GeV for all SFOS lepton pair;}$$

$$80 < M_{4\ell} < 100 \text{ GeV.}$$

Acceptance factors:

$$C_{4\ell} = N_{4\ell} (\text{pass full selection}) / N_{4\ell} (\text{in F. V.})$$

$$A_{4\ell} = N_{4\ell} (\text{in F.V.}) / N_{4\ell} (\text{in P.S.})$$

σ^{fiducial} and σ^{total} :

$$\sigma_{Z \rightarrow 4\ell}^{\text{fiducial}} = \frac{N_{\text{obs}} - N_{\text{bkg}}}{\mathcal{L} \mathcal{C}_{Z \rightarrow 4\ell}}$$

$$\sigma_{Z \rightarrow 4\ell}^{\text{total}} = \frac{\sigma_{Z \rightarrow 4\ell}^{\text{fiducial}}}{A_{Z \rightarrow 4\ell}}$$

Signal Acceptance A_{4l} and C_{4l}

ATLAS

The acceptance and correction factors are determined by using Powheg MC signal samples

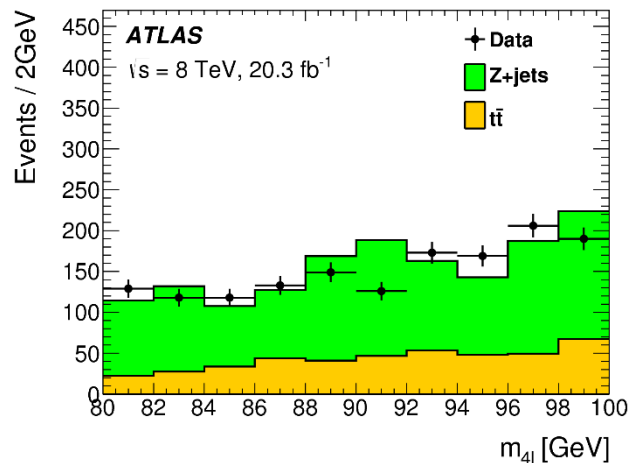
7 TeV	eeee	ee $\mu\mu$	$\mu\mu ee$	$\mu\mu\mu\mu$
A_{4l}	7.47%	15.83%	8.79%	18.26%
C_{4l}	21.5%	49.0%	36.3%	59.2%
8 TeV				
A_{4l}	7.30%	14.8%	7.91%	17.79%
C_{4l}	36.06%	55.54%	46.24%	71.13%

- The uncertainties on A_{4l} are theoretical due to scales and PDF (1.3 - 1.7%)
- The uncertainties on C_{4l} are mainly experimental: lepton reconstruction and identification efficiencies and energy/momentum scales and resolution;
 $\Delta C_{4l}/C_{4l}$: 2.7%, 3.7%, 6.2% and 9.4% for 4m, ee $\mu\mu$, $\mu\mu ee$ and 4e channel, respectively (at 8 TeV).
- Larger C_{4l} values at 8 TeV due to lepton recon. And ID improvements
- **Currently statistical uncertainties are larger than the systematic uncertainties**

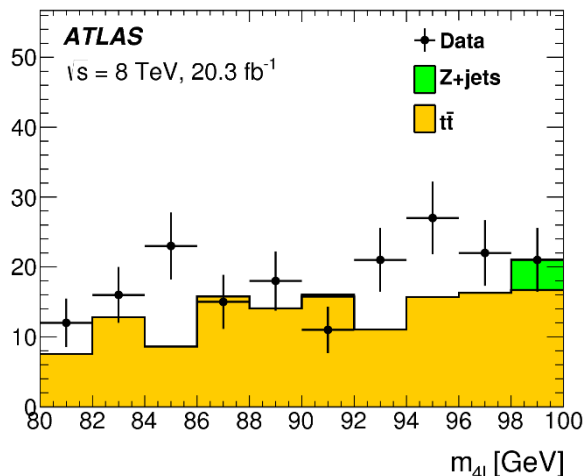
Data Driven Top and Z+jet Background Estimation

ATLAS

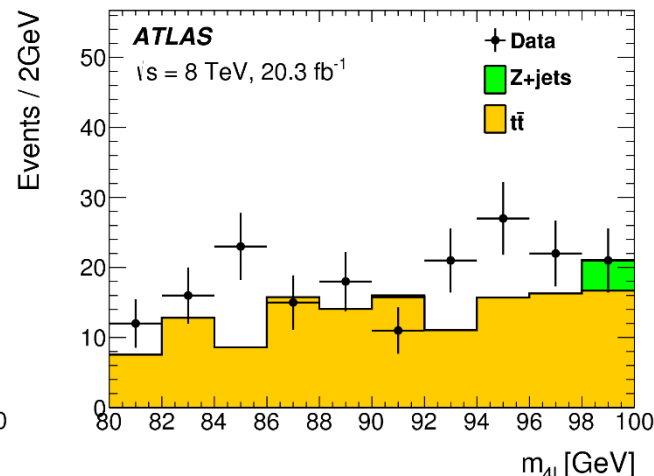
- Select the $\ell\ell+jj_{\ell\ell}$ background control samples, where $jj_{\ell\ell}$ are two lepton-like jets (selected with invert lepton selection cuts)



Two electron-like jets



One electron-like jet
One muon-like jet



Two muon-like jets

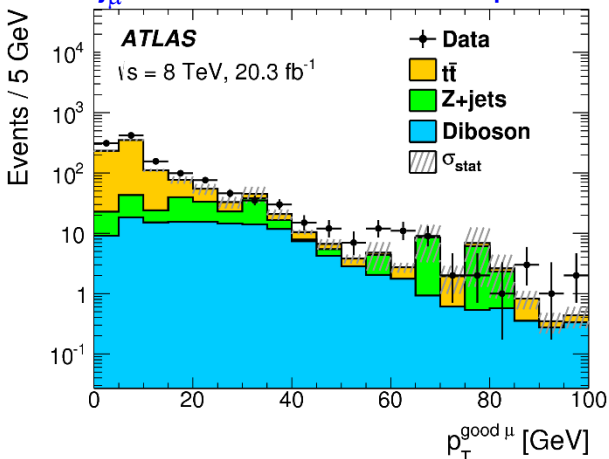
- MC background control samples indicate the jet compositions
- Each event in the control samples is scaled by a fake-factor product $f_1 \times f_2$ to estimate the background in the signal region
- f is determined using jet enriched $t\bar{t}$ and Z+jet samples

Determination of Fake-Factor f

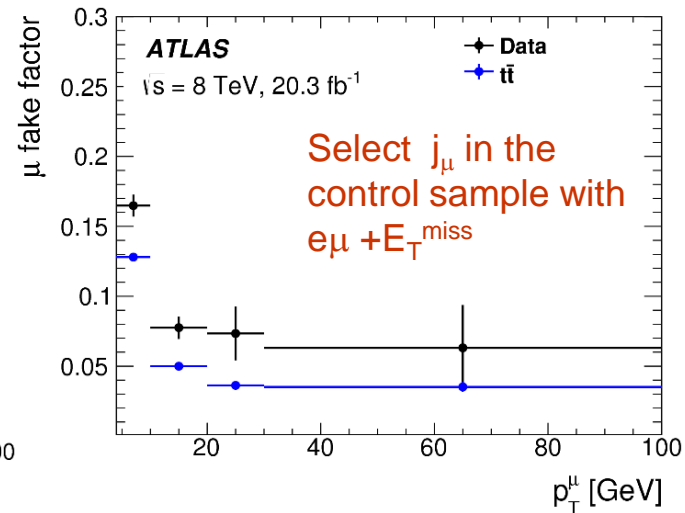
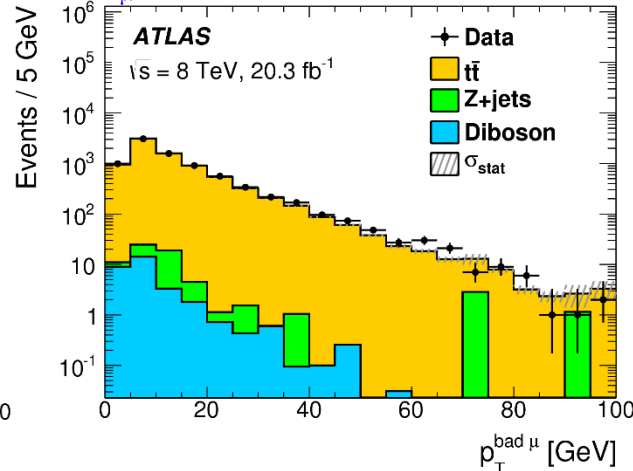
ATLAS

$$f = N_j (\text{pass full lepton selection}) / N_j (\text{fail full lepton selection})$$

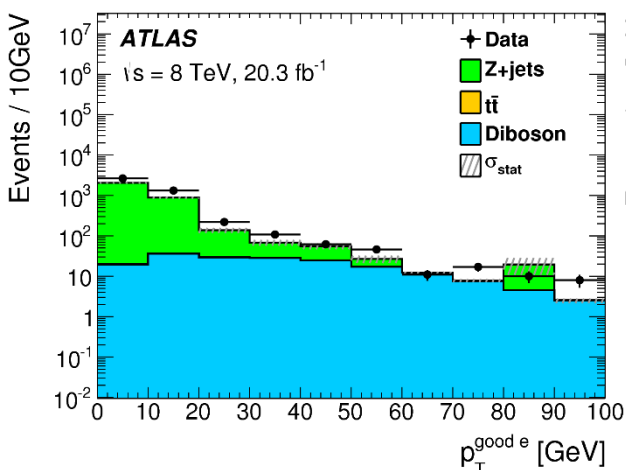
j_μ from $t\bar{t}$ control sample



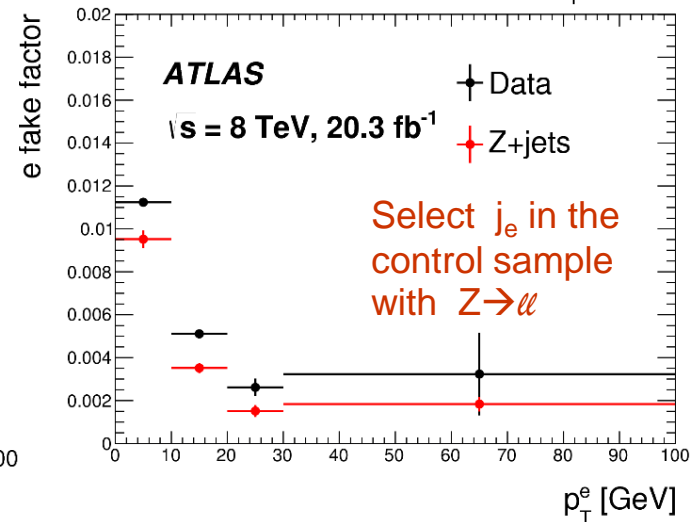
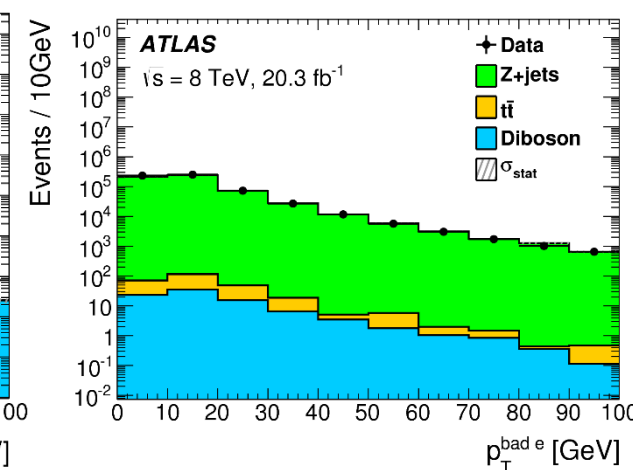
j_μ from $t\bar{t}$ control sample



j_e from Z+jet control sample



j_e from Z+jet control sample



Summary of Estimated Background

ATLAS

Dibosons (including τ final states and gg production) estimated with MC, $t\bar{t}$ and $Z + X$ estimated with data and fake factor as before.

Year	Channel	diboson from MC	Z+jet and $t\bar{t}$ from data-driven	total
2011	$4e$	0.010 ± 0.002	0.11 ± 0.05	0.12 ± 0.04
	$2e2\mu$	0.024 ± 0.002	0.16 ± 0.09	0.18 ± 0.09
	$2\mu2e$	0.015 ± 0.002	0.06 ± 0.03	0.08 ± 0.04
	4μ	0.038 ± 0.003	0.05 ± 0.04	0.09 ± 0.04
2012	$4e$	0.064 ± 0.009	0.10 ± 0.01	0.16 ± 0.03
	$2e2\mu$	0.156 ± 0.019	0.20 ± 0.05	0.36 ± 0.05
	$2\mu2e$	0.132 ± 0.017	0.08 ± 0.02	0.21 ± 0.04
	4μ	0.301 ± 0.026	0.11 ± 0.05	0.41 ± 0.05

Remark:

- Overall background contribution to selected 4l sample is $< 1\%$
- Likelihood e-ID significantly reduce the fake electron rate in 2012 data analysis

Selected Candidates Observation vs Predictions

ATLAS

	Channel	Data	Total expected	MC signal ($Z/ZZ \rightarrow 4\ell$)	Backgrounds
7 TeV	$eeee$	1	1.8 ± 0.3	1.7 ± 0.3	0.12 ± 0.04
	$e\mu\mu$	7	8.0 ± 0.4	7.7 ± 0.4	0.18 ± 0.09
	$\mu\mu e$	5	3.3 ± 0.3	3.2 ± 0.3	0.08 ± 0.04
	$\mu\mu\mu$	8	11.3 ± 0.5	11.2 ± 0.3	0.09 ± 0.04
	Combined	21	24.4 ± 1.2	23.8 ± 1.2	0.47 ± 0.11
8 TeV	$eeee$	16	14.4 ± 1.2	14.3 ± 1.2	0.16 ± 0.03
	$e\mu\mu$	48	43.2 ± 2.3	42.9 ± 2.2	0.36 ± 0.05
	$\mu\mu e$	16	19.3 ± 1.2	19.1 ± 1.2	0.21 ± 0.04
	$\mu\mu\mu$	71	68.8 ± 3.0	68.4 ± 2.9	0.41 ± 0.05
	Combined	151	145.7 ± 7.7	145 ± 7	1.14 ± 0.13

CMS (7 TeV)

Final state channels	4e	4 μ	2e2 μ	4 ℓ
Irreducible background ($pp \rightarrow Z\gamma^* \rightarrow 4\ell$)	0.07	0.25	0.14	0.46 ± 0.05
Other (reducible) backgrounds	0.01	0.01	0.05	0.07 ± 0.1
Expected signal ($pp \rightarrow Z \rightarrow 4\ell$)	3.8	13.6	12.0	29.4 ± 2.6
Total expected (simulation)	3.9	13.9	12.2	30.0 ± 2.6
Observed events	2	14	12	28
Yield from fit to the observed mass distribution	-	13.6 ± 3.8	11.5 ± 3.1	27.3 ± 5.4

CMS 4l Spectrum at 7 TeV

arXiv:1210.3844

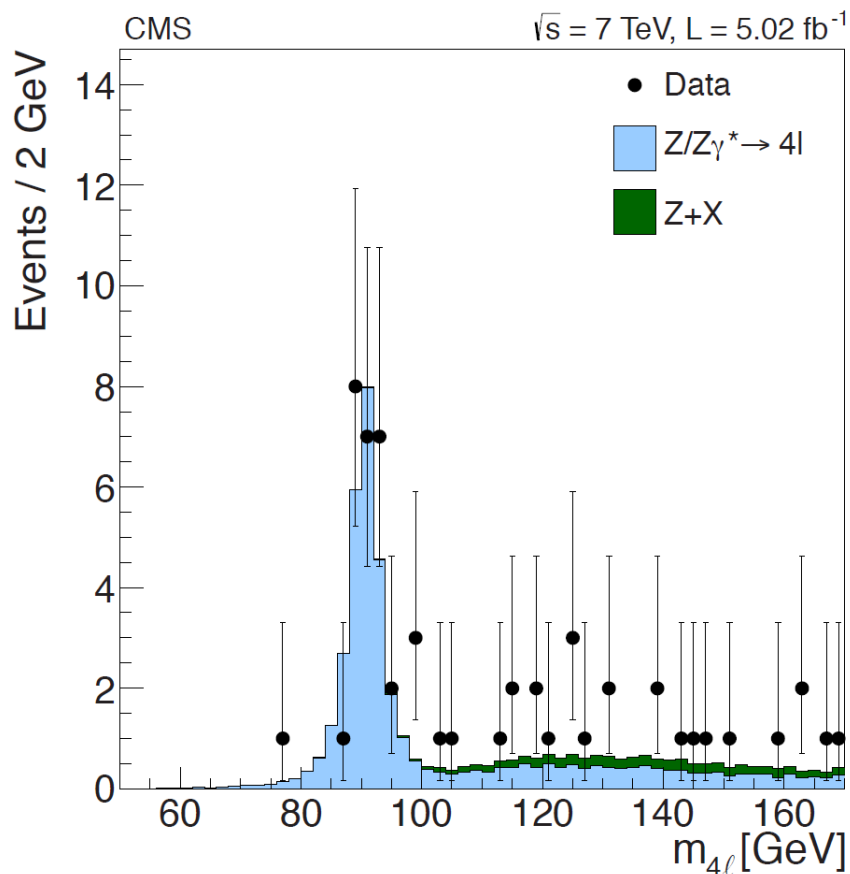


Figure 2: Four-lepton invariant mass distribution for events passing all selection requirements except that on $m_{4\ell}$. The data are shown by points. The filled histograms represent standard model expectations for $pp \rightarrow Z/Z\gamma^* \rightarrow 4\ell$ and for reducible backgrounds. The three final states, $4e$, 4μ , and $2e2\mu$, are combined.

ATLAS 4l Mass Distributions

arXiv:1403.5657

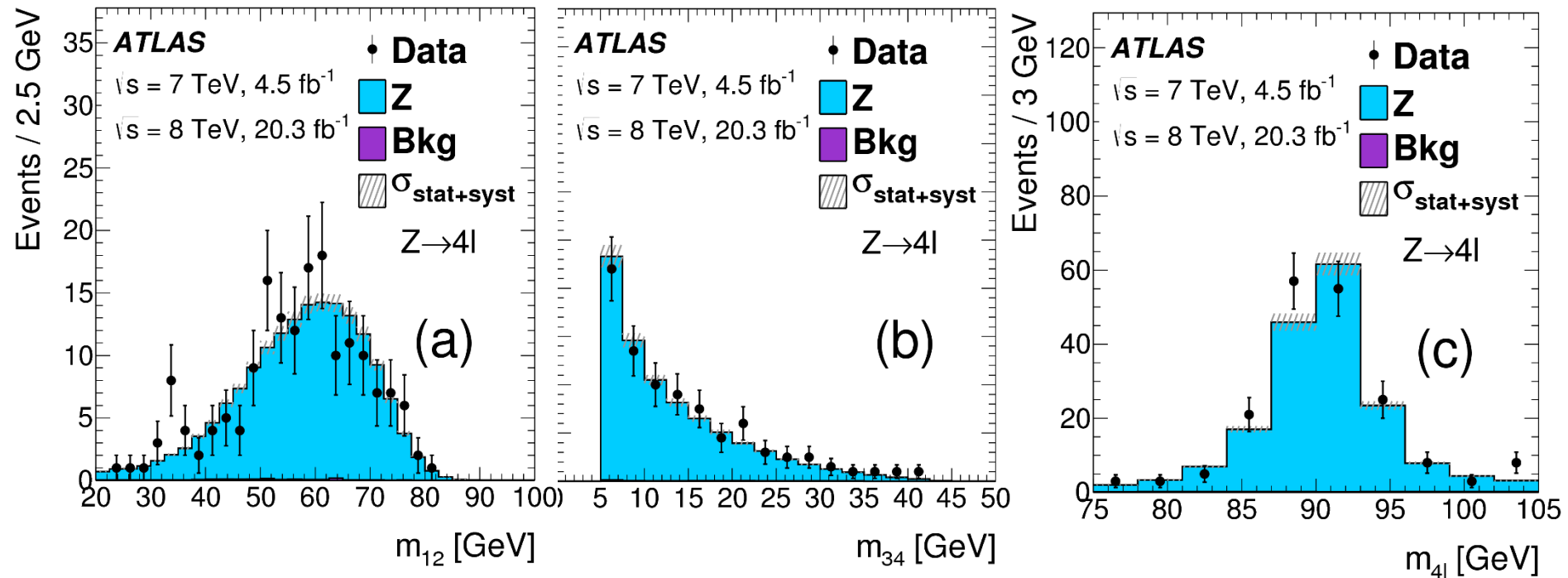
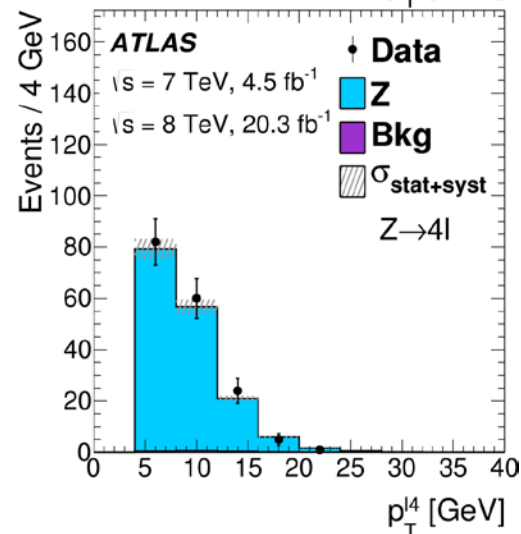
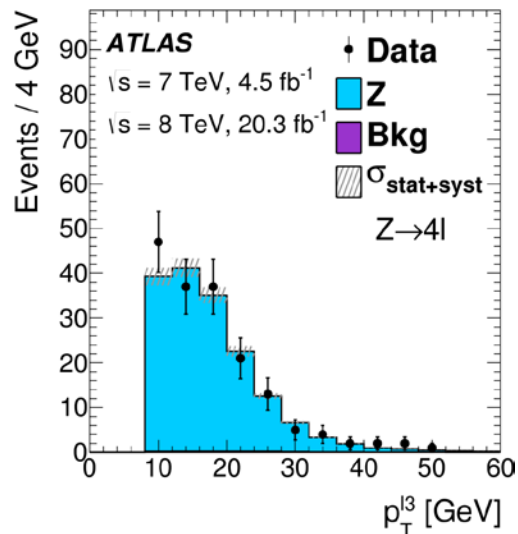
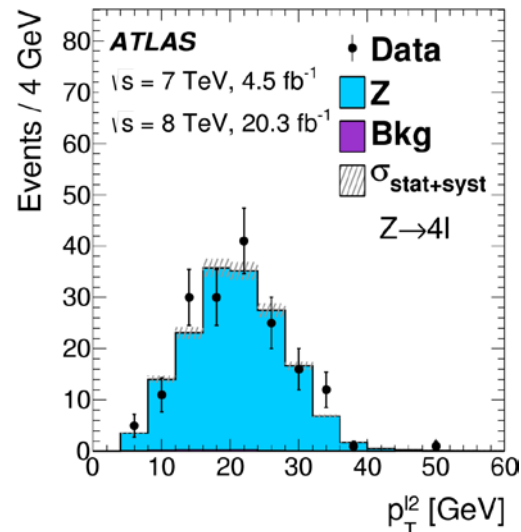
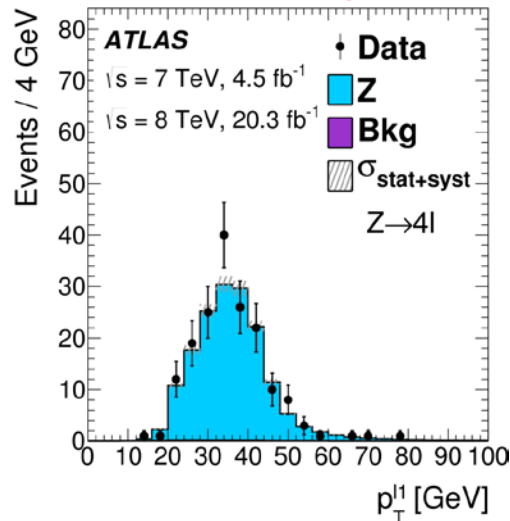


FIG. 2. Invariant mass distributions of (a) the leading lepton pair, m_{12} , (b) the subleading lepton pair, m_{34} , and (c) the four-lepton system, $m_{4\ell}$. The MC simulation expectation for a combination of all channels is compared to $\sqrt{s} = 7$ and 8 TeV data. All selections are applied except in (c) there is no $m_{4\ell}$ requirement. The background contributes $< 1\%$ of the total expected signal (invisible in the plots).

pT of Leptons

arXiv:1403.5657

Good data and MC agreement in lepton kinematic distributions



Measured Fiducial Cross Sections

$$\sigma_{Z \rightarrow 4\ell}^{fiducial} = \frac{N_{obs} - N_{bkg}}{\mathcal{L}C_{Z \rightarrow 4\ell}}$$

ATLAS

\sqrt{s}	Final state	$C_{4\ell}$	Measured σ^{Fid} fb
7 TeV	$eeee$	21.5%	$0.910^{+1.39}_{-0.72}$ (stat) ± 0.14 (syst) ± 0.02 (lumi) fb
	$\mu\mu\mu\mu$	59.2%	$2.970^{+1.18}_{-0.94}$ (stat) ± 0.07 (syst) ± 0.05 (lumi) fb
	$ee\mu\mu$	49.0%	$3.091^{+1.35}_{-1.05}$ (stat) ± 0.16 (syst) ± 0.05 (lumi) fb
	$\mu\mu ee$	36.3%	$3.015^{+1.57}_{-1.17}$ (stat) ± 0.30 (syst) ± 0.06 (lumi) fb
8 TeV	$eeee$	36.06%	$2.16^{+0.59}_{-0.50}$ (stat) ± 0.16 (syst) ± 0.06 (lumi) fb
	$\mu\mu\mu\mu$	71.13%	$4.89^{+0.66}_{-0.56}$ (stat) ± 0.13 (syst) ± 0.14 (lumi) fb
	$ee\mu\mu$	55.54%	$4.23^{+0.65}_{-0.59}$ (stat) ± 0.15 (syst) ± 0.12 (lumi) fb
	$\mu\mu ee$	46.24%	$1.68^{+0.46}_{-0.39}$ (stat) ± 0.07 (syst) ± 0.04 (lumi) fb

σ_{4l} measurement in final phase-space

ATLAS measurement in final phase space
 $80 < m_{4l} < 100$ GeV and $m_{\ell^+\ell^-} > 5$ GeV

$$\sigma_{Z \rightarrow 4\ell}^{total} = \frac{\sigma_{Z \rightarrow 4\ell}^{fiducial}}{A_{Z \rightarrow 4\ell}}$$

- ❖ The 4e and 4 μ channels, and The 2e2 μ and 2 μ 2e channels are combined with 2x2 covariance error matrices for σ measurement
- ❖ The 4l $\sigma^{total} = \sigma(4e+4\mu) + \sigma(2e2\mu)$, uncertainties are determined by 4x4 error matrices

\sqrt{s}	4 ℓ state	$N_{4\ell}^{obs}$	$N_{4\ell}^{exp}$	$N_{4\ell}^{bkg}$	$C_{4\ell}$	$\sigma_{Z4\ell}^{fid}$ [fb]	$A_{4\ell}$	$\sigma_{Z4\ell}$ [fb]	
7 TeV	$ee + ee$	1	1.8 ± 0.3	0.12 ± 0.04	21.5%	$0.9_{-0.7}^{+1.4} \pm 0.14 \pm 0.02$	7.5%	} 4e, 4 μ	$32 \pm 11 \pm 1.0 \pm 0.6$
	$\mu\mu + \mu\mu$	8	11.3 ± 0.5	0.08 ± 0.04	59.2%	$3.0_{-0.9}^{+1.2} \pm 0.07 \pm 0.05$	18.3%		
	$ee + \mu\mu$	7	7.9 ± 0.4	0.18 ± 0.09	49.0%	$3.1_{-1.1}^{+1.4} \pm 0.16 \pm 0.05$	15.8%	} 2e2 μ	$44 \pm 14 \pm 3.3 \pm 0.9$
	$\mu\mu + ee$	5	3.3 ± 0.3	0.07 ± 0.04	36.3%	$3.0_{-1.2}^{+1.6} \pm 0.30 \pm 0.06$	8.8%		
	combined	21	24.2 ± 1.2	0.44 ± 0.14					$76 \pm 18 \pm 4 \pm 1.4$
8 TeV	$ee + ee$	16	14.4 ± 1.4	0.14 ± 0.03	36.1%	$2.2_{-0.5}^{+0.6} \pm 0.20 \pm 0.06$	7.3%	} 4e, 4 μ	$56 \pm 6 \pm 1.8 \pm 1.6$
	$\mu\mu + \mu\mu$	71	68.8 ± 2.7	0.34 ± 0.05	71.1%	$4.9_{-0.6}^{+0.7} \pm 0.13 \pm 0.14$	17.8%		
	$ee + \mu\mu$	48	43.2 ± 2.1	0.32 ± 0.05	55.5%	$4.2_{-0.6}^{+0.7} \pm 0.16 \pm 0.12$	14.8%	} 2e2 μ	$52 \pm 7 \pm 2.4 \pm 1.5$
	$\mu\mu + ee$	16	19.3 ± 1.3	0.18 ± 0.04	46.2%	$1.7_{-0.4}^{+0.5} \pm 0.10 \pm 0.04$	7.9%		
	combined	151	146 ± 7	1.0 ± 0.11					$107 \pm 9 \pm 4 \pm 3.0$

Measured σ^{total} vs Predicted σ^{total}

ATLAS	Phase-space cross section ($m_{2l} > 5 \text{ GeV}$, $80 < m_{4l} < 100 \text{ GeV}$)
7 TeV measured	$76 \pm 18 \text{ (stat.)} \pm 4 \text{ (syst.)} \pm 1.4 \text{ (lumi.) fb}$
7 TeV NLO SM prediction	$90.0 \pm 2.1 \text{ fb}$
8 TeV measured	$107 \pm 9 \text{ (stat.)} \pm 4 \text{ (syst.)} \pm 3.0 \text{ (lumi.) fb}$
8 TeV NLO SM prediction	$104.8 \pm 2.5 \text{ fb}$

CMS	Phase-space cross section ($m_{2l} > 4 \text{ GeV}$, $80 < m_{4l} < 100 \text{ GeV}$)
7 TeV measured	$112^{+23}_{-20} \text{ (stat.)} ^{+7}_{-5} \text{ (syst.)} ^{+3}_{-2} \text{ (lumi.) fb}$
7 TeV NLO SM prediction	$120 \pm 2.1 \text{ fb}$

Determination of BR(Z→4l)

ATLAS

- ❑ Measure the $Z \rightarrow 2\mu$ cross section and take the known $\text{Br}(Z \rightarrow 2\mu)$ to get inclusive cross section of Z from pp collisions
- ❑ Cancels luminosity uncertainty and theoretical uncertainty of $\sigma(\text{pp} \rightarrow Z)$
- ❑ Derive the BR ($Z \rightarrow 4l$) as below

$$\text{BR}(Z \rightarrow 4\ell) = \text{BR}(Z \rightarrow 2\mu)(1 - f_t) \frac{(N_{\text{obs.}} - N_{\text{bkg.}})^{4\ell} (C \times A)^{2\mu}}{(N_{\text{obs.}} - N_{\text{bkg.}})^{2\mu} (C \times A)^{4\ell}}$$

Uncertainty on $\text{BR}(Z \rightarrow 2\mu)$ is small. f_t = fraction of t -channel in phase-space.

$$f_t = (3.35 \pm 0.02)\% \text{ for } 4e, 4\mu; \quad f_t = (3.90 \pm 0.02)\% \text{ for } 2e2\mu$$

- **Cancel luminosity uncertainty: 2.8% (8 TeV)**
- **Cancel NLO $\sigma(Z)$ calculation uncertainties (Scales, PDF, NNLO correction): 4%**

Branching Fraction of $Z \rightarrow 4\ell$

Branching fraction results uses an error weighted combination of 7 and 8 TeV results. For phase space $m_{2\ell} > 5 \text{ GeV}$, $80 < m_{4\ell} < 100 \text{ GeV}$

Quantity	\sqrt{s}	Value	ATLAS
Measured	7 TeV	$(2.67 \pm 0.62 \text{ (stat)} \pm 0.14 \text{ (syst)}) \times 10^{-6}$	
	8 TeV	$(3.33 \pm 0.27 \text{ (stat)} \pm 0.11 \text{ (syst)}) \times 10^{-6}$	
	Combined	$(3.20 \pm 0.25 \text{ (stat)} \pm 0.12 \text{ (syst)}) \times 10^{-6}$	
Expected		$(3.33 \pm 0.01) \times 10^{-6}$	

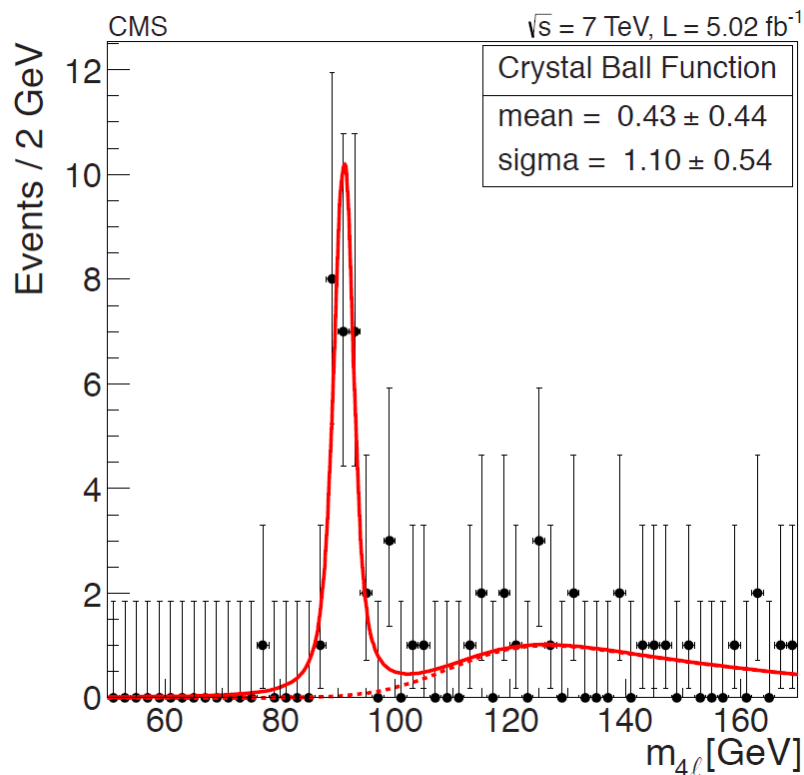
For phase space $m_{2\ell} > 4 \text{ GeV}$, $80 < m_{4\ell} < 100 \text{ GeV}$

	BR (measured)	BR (predicted)
ATLAS	$(4.31 \pm 0.34 \pm 0.17) \times 10^{-6}$	$(4.50 \pm 0.01) \times 10^{-6}$
CMS	$(4.2^{+0.9}_{-0.8} \pm 0.2) \times 10^{-6}$	4.45×10^{-6}

Cross Check the Mass Scale for $H \rightarrow 4l$ Mass Measurement

CMS PAS SMP-12-009

CMS
 $4l$ mass scale

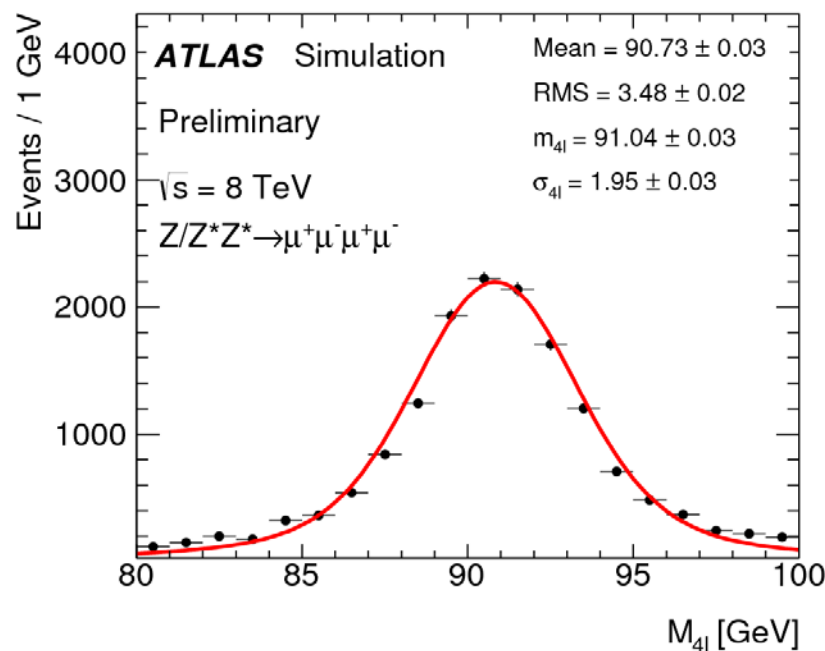
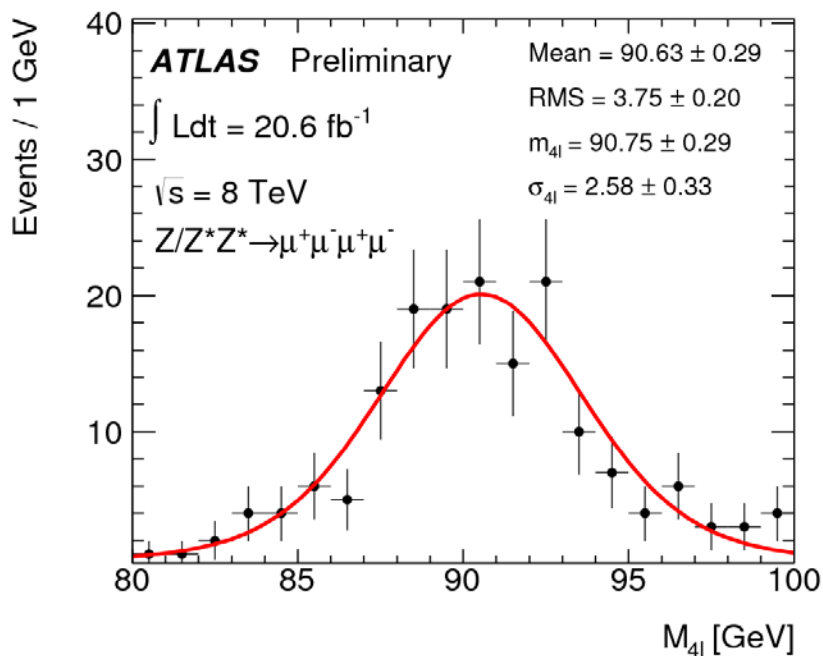


From the fit results, as shown in Fig. above, one can see that the offset of the peak is 0.4 ± 0.4 GeV (to the right) (the “mean” value of the Crystal Ball function represents an offset with respect to the fixed Breit–Wigner function peak position), or, in relative units, $0.4 \pm 0.4\%$. These numbers can be used to constrain the possible systematic uncertainty of the four-lepton mass scale. With the current data there is no evidence for a statistically significant bias.

ATLAS 4ℓ Mass Scale

ATLAS-CONF-2013-055

4ℓ mass fitted with the convolution of a Breit-Wigner and a Gaussian distribution for four 4ℓ channels shown good consistence with MC predictions. Example of 4μ mass fit for data and MC



Invariant mass distributions of 4μ , fitted with the convolution of a Breit-Wigner and a Gaussian distribution, for the reconstructed events within the Z-mass window of 80 to 100 GeV using (a) 4μ data, (b) simulated $Z \rightarrow 4\mu$. All for 8 TeV datasets using relaxed dilepton mass requirement in event selection, $m_{2\ell} > 1 \text{ GeV}$. The parameter $m_{4\ell}$ is the fit mean and $\sigma_{4\ell}$ is the standard deviation of the Gaussian component of the fit.

Summary

- The 4ℓ production at the Z resonance has been observed at the LHC by both ATLAS and CMS experiments
- The 4ℓ production cross sections are measured by ATLAS (at 7 and 8 TeV) and by CMS (at 7 TeV). Results are consistent with the SM predictions calculated to NLO (QCD) (Powheg/MCFM)
- The rare decay branching fraction of $Z \rightarrow 4\ell$ is determined from the cross section measurements by normalizing the 4ℓ events to the $Z \rightarrow \mu\mu$ events. Results are consistent within uncertainties from both experiments

	Phase Space	BR (measured)	BR (predicted)
ATLAS	$80 < m_{4\ell} < 100 \text{ GeV}$ and $m_{\ell\ell} > 5 \text{ GeV}$	$(3.20 \pm 0.25 \pm 0.13) \times 10^{-6}$	$(3.33 \pm 0.01) \times 10^{-6}$
	$80 < m_{4\ell} < 100 \text{ GeV}$ and $m_{\ell\ell} > 4 \text{ GeV}$	$(4.31 \pm 0.34 \pm 0.17) \times 10^{-6}$	$(4.50 \pm 0.01) \times 10^{-6}$
CMS	$80 < m_{4\ell} < 100 \text{ GeV}$ and $m_{\mu\mu} > 4 \text{ GeV}$	$(4.2^{+0.9}_{-0.8} \pm 0.2) \times 10^{-6}$	4.45×10^{-6}

- The 4ℓ mass scales and resolutions between data and MC simulations are consistent for both ATLAS and CMS, which provide a good cross-check on the Higgs $\rightarrow 4\ell$ mass measurement.

Backup slides

ATLAS 4l Event Selection

Red indicates differences from $H \rightarrow ZZ^* \rightarrow 4\ell$

Electrons	GSF electrons selected with Loose++ from the H4 2011 menu (2011) or Loose from the Likelihood menu (2012) with $E_T > 7$ GeV and $ \eta < 2.47$
Muons	Combined, segment-tagged, calo-tagged ($p_T > 15$ GeV), and stand-alone Staco muons with $p_T > 4$ GeV and $ \eta < 2.7$

Event Selection	
Quadruplet selection	Two pairs of same-flavour opposite-charge leptons. The three leading leptons in the quadruplet have $p_T > 20, 15,$ and 10 GeV. If the third lepton is a muon it may have $p_T > 8$ GeV Pick the pair that has M_{Z1} nearest the Z-mass, and then a second pair with M_{Z2} greatest.
Kinematic selection	Leading di-lepton pair must have inv. mass $M_{Z1} > 20$ GeV Sub-leading di-lepton pair must have inv. mass $M_{Z2} > 5$ GeV No same-flavor opposite-charge di-lepton giving $M_{\ell+\ell-} < 5$ GeV (J/ψ veto) $\Delta R(\ell, \ell') > 0.1$ (0.2) for all same-flavor (opposite-flavor) leptons in the quadruplet.
Isolation	Lepton track isolation ($\Delta R = 0.20$): $\sum p_T / p_T < 0.15$ Lepton calorimeter isolation ($\Delta R = 0.20$): $\sum E_T / E_T < 0.30$ except < 0.15 for stand-alone muons and in 2012 < 0.20 for electrons,
Impact parameter significance	Apply impact parameter significance cut to all leptons of the quadruplet. For electrons : $d_0 / \sigma_{d_0} < 6.5$ For muons : $d_0 / \sigma_{d_0} < 3.5$
Four-body mass	$80 < m_{4\ell} < 100$ GeV
