

***Enhanced Gene Expression Programming
for Signal-Background Discrimination
in Particle Physics***

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Outline

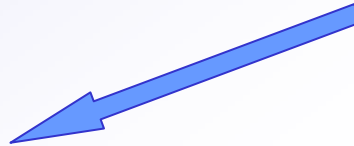
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- ❖ ***Gene Expression Programming***
- ❖ ***New developments on Gene Expression Programming***
 - ✓ *alternative solution representation*
 - ✓ *controlled evolution*
 - ✓ *dynamic classification threshold*
- ❖ ***Comparative studies***
 - ✓ *experiments*
 - ✓ *results*
- ❖ ***Conclusions***

GEP - Evolutionary Algorithm

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Gene Expression Programming (GEP) – a new Evolutionary Algorithm (EA)



Multi-purpose algorithms inspired by natural evolution theories

String based

- ❖ **Genetic Algorithms (GA)** (J. H. Holland, 1975)
- ❖ **Evolutionary Strategies (ES)** (I. Rechenberg, H-P. Schwefel, 1975)

Tree based

- ❖ **Genetic Programming (GP)** (J. R. Koza, 1992)

Hybrid representation

- ❖ **Gene Expression Programming (GEP)** (C. Ferreira, 2001)

Terminology

❖ *Individual* – candidate solution to a problem

decoding ↑ ↓ *encoding*

❖ *Chromosome* – representation of the candidate solution

❖ *Gene* – constituent entity of the chromosome

❖ *Population* – set of individuals/chromosomes

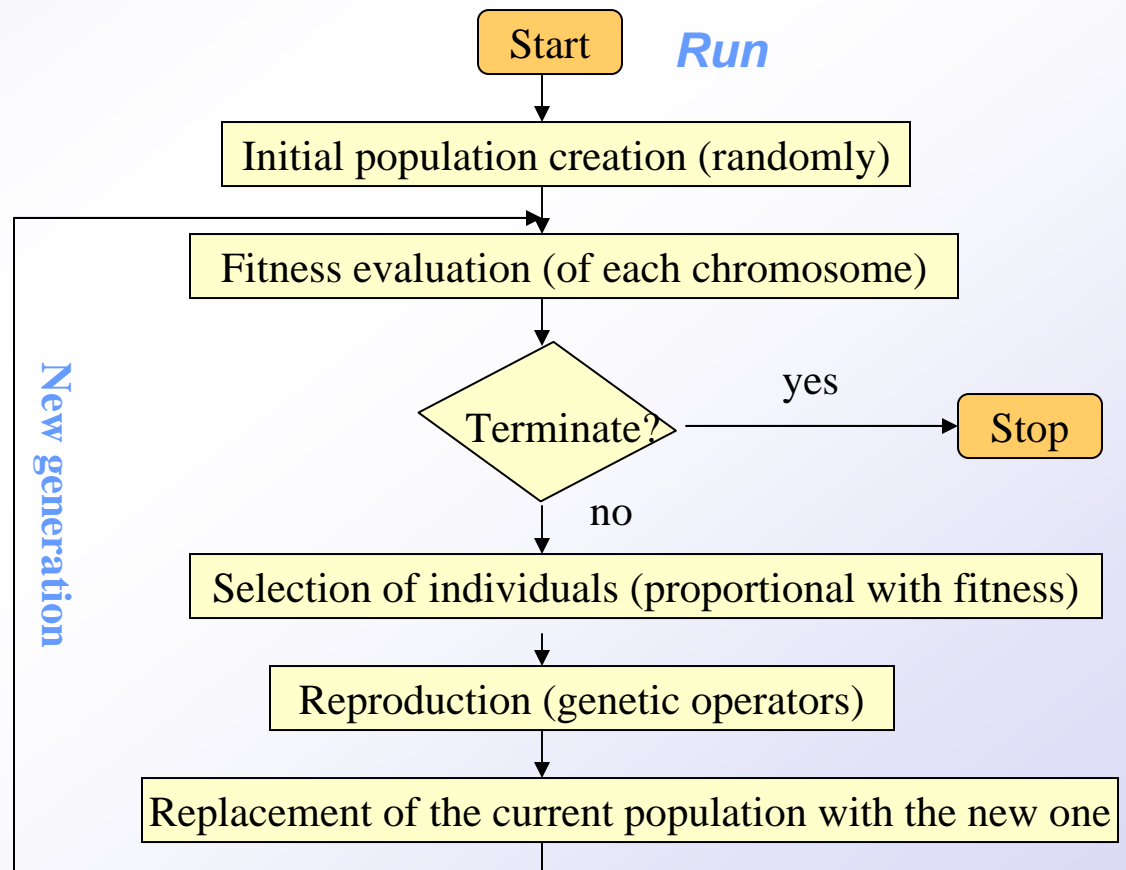
❖ *Fitness function* – representation of how good a candidate solution is

❖ *Genetic operators* – operators applied on chromosomes in order to create **genetic variation** (other chromosomes)

Evolutionary Algorithms

EA - iteratively improve the quality of the solution until an optimal/feasible solution is found

- ❖ *Problem definition*
- ❖ *Solution representation (encoding the candidate solution)*
- ❖ *Fitness definition*
- ❖ *Run*
- ❖ *Decoding the best fitted chromosome = **solution***



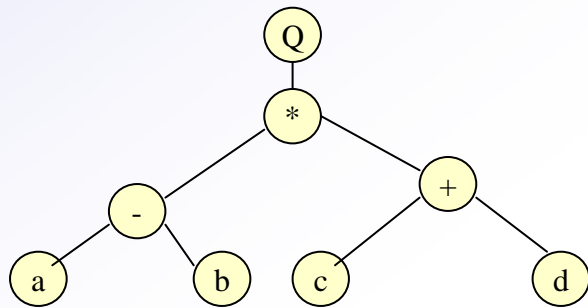
Gene Expression Programming

Chromosome - sequence of symbols (functions and terminals)

Head (h) Tail (t) $t=h(n-1)+1$
 Q^*+abcd *aaabbb* $n - \text{highest arity}$

↓ mapping

Expression tree (ET)



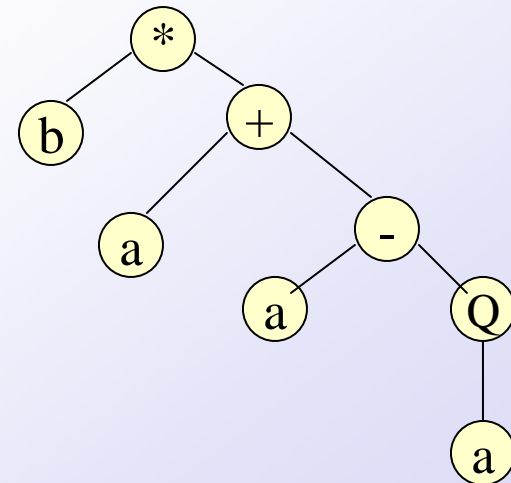
↓ Translation
(as in GP)

Mathematical expression

$$\sqrt{(a - b) \cdot (c + d)}$$

**ET ends before
the end of the gene!**

**b+a-aQab+//+b+babbabbbababbaaa*



GEP (cont.)

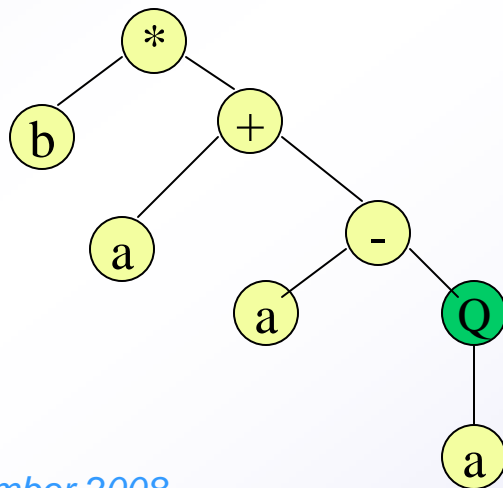
Reproduction

Genetic operators applied on chromosomes not on ET =>
always produce syntactically correct structures!

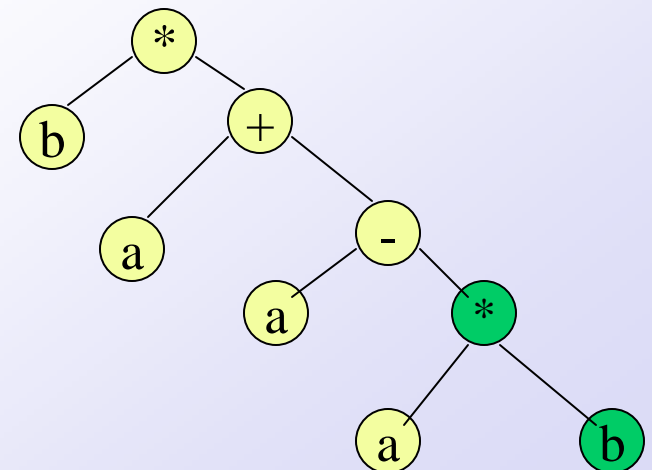
- ❖ Cross-over – exchanges parts of two chromosomes
- ❖ Mutation – changes the value of a node
- ❖ Transposition – moves a part of a chromosome to another location in the same chromosome

e.g. Mutation: Q replaced with *

*b+a-aQab+//+b+babbabbababbaaa



*b+a-a*ab+//+b+babbabbababbaaa



GEP in PP - event selection

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L. Teodorescu, *IEEE Trans. Nucl. Phys.*, vol. 53, no.4, p. 2221 (2006)

L. Teodorescu, D. Sherwood, *Comp Phys. Comm.* 178, p 409 (2008)

also talks at IEEE NSS 06, CHEP06 and ACAT 2007

CERN Yellow Report CERN-2008-02

cuts/selection criteria finding for signal/background classification
(statistical learning approach)

❖ **fitness function** - number of **events correctly classified** as signal or background (maximise classification accuracy)

❖ **input functions**

- logical functions => cut type rules

- all common mathematical functions => continuous function

❖ **input data** - Monte-Carlo simulation from BaBar experiment for K_S production in e^+e^- (~10 GeV), $K_S \rightarrow \pi^+ \pi^-$

8 variables (used in cut-based analysis)

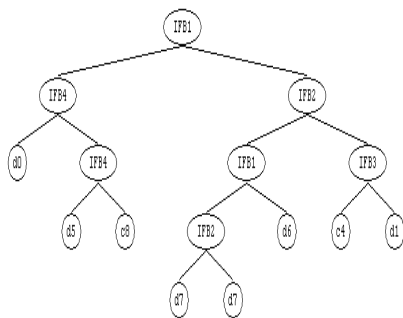
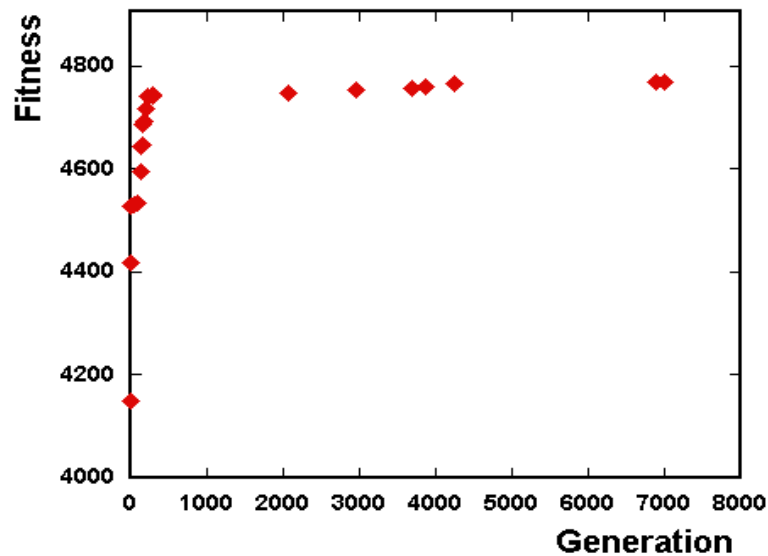
- d_{oca} (distance of closest approach)
- $|\cos(\theta_{hel})|$ (K_S helicity angle)
- F_{sig} (Flight Significance)
- Mass (K_S reconstructed mass)
- $RXY, |RZ|$ (region around interaction point)
- SFL (Signed Flight Length)
- P_{chi} (χ^2 probability of the vertex)

20 variables – previous and

- cartesian coordinates of K_S vertex
- polar coordinate K_S momentum
- polar coordinates of π daughter particles

Previous results

GEP analysis *optimises classification*



$F_{sig} \geq 4.1$
 $R_{xy} < 0.2cm$
 $SFL > 0.2cm$
 $P_{chi} > 0$

Cut-based analysis *optimises signal significance*

$F_{sig} \geq 4.0$
 $R_{xy} \leq 0.2cm$
 $SFL \geq 0cm$
 $P_{chi} > 0.001$

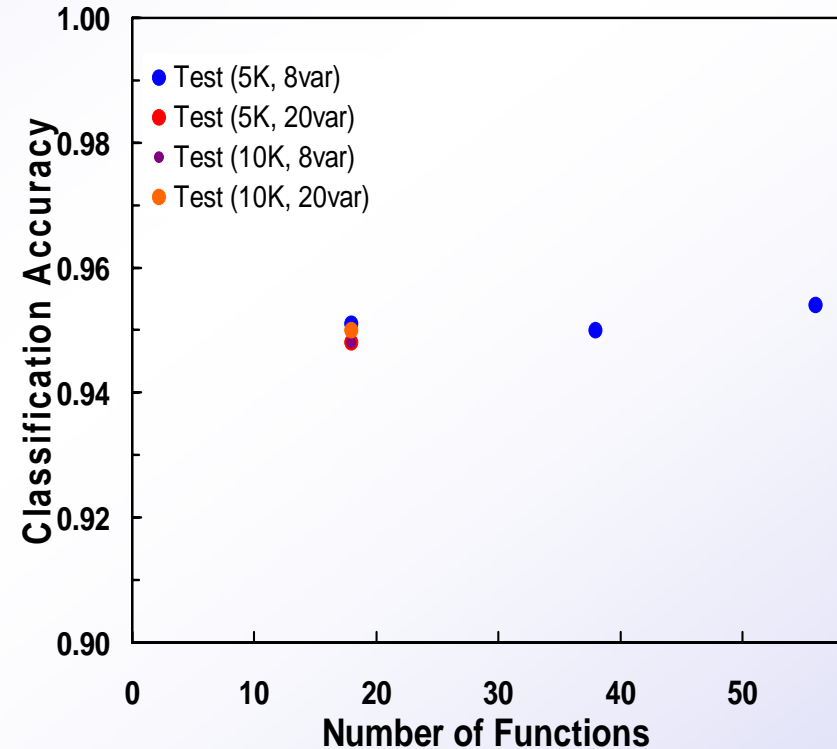
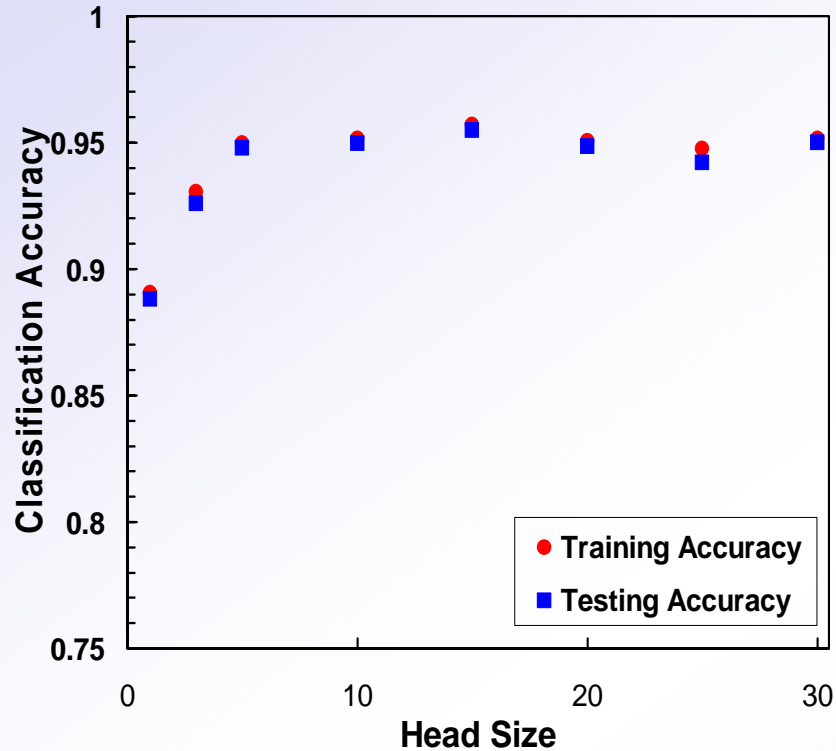
Reduction
S: 15%
B: 98%

$doca \leq 0.4cm$
 $|Rz| \leq 2.8cm$

Reduction
S: 16%
B: 98.3%

Previous results (cont.)

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- ❖ **Solutions with good generalisation power**
- ❖ **No overtraining observed**

No dependence on

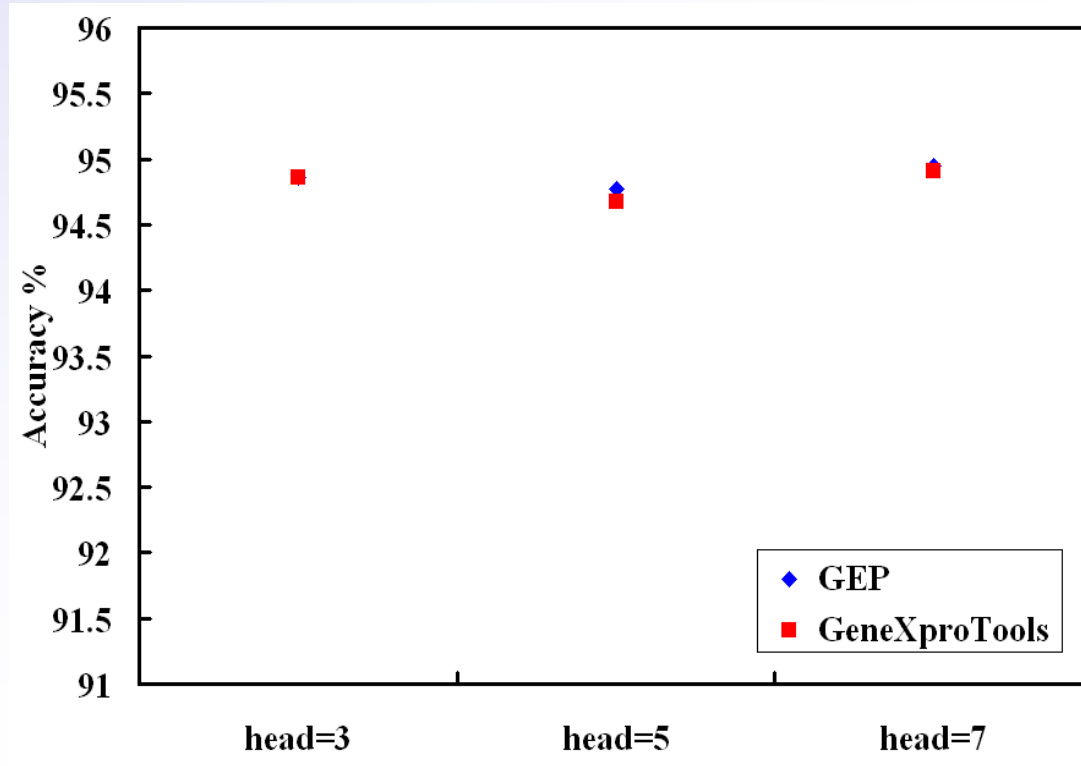
- ❖ *event variables (automatic selection of relevant variables)*
- ❖ *number of input functions,*
- ❖ *number of training events*

New developments

Software implementation

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- ❖ *Previous studies with GeneXproTools (commercial software package developed by the GEP developer)*
- ❖ *Current studies with a private implementation*



Head=3 (5000 generations)

Head=5 (7000 generations)

Head=7 (15000 generations)

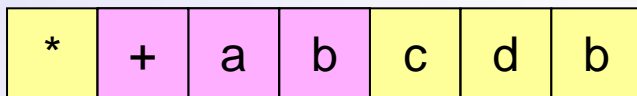
(less than 0.1% difference)

Chromosom - ET mapping

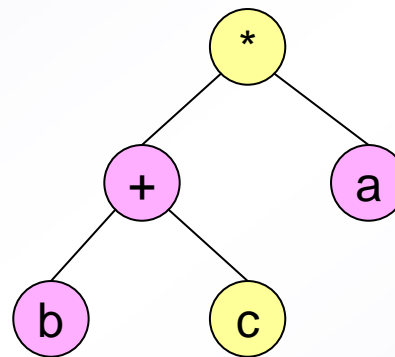
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Postfix order - original GEP (Ferreira, 2001)

Chromosome



ET

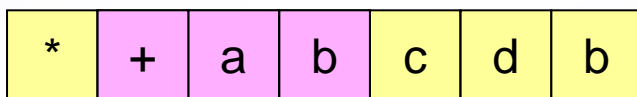


Mathematical expression

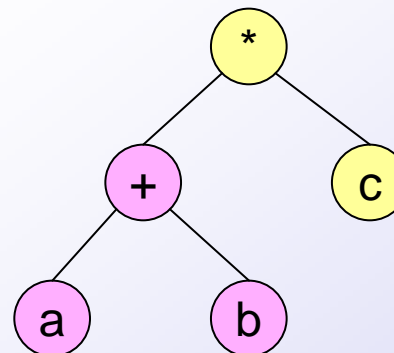
$$(b + c) * a$$

Prefix order - pGEP (X. Li et.al. , GECCO2005)

Chromosome



ET



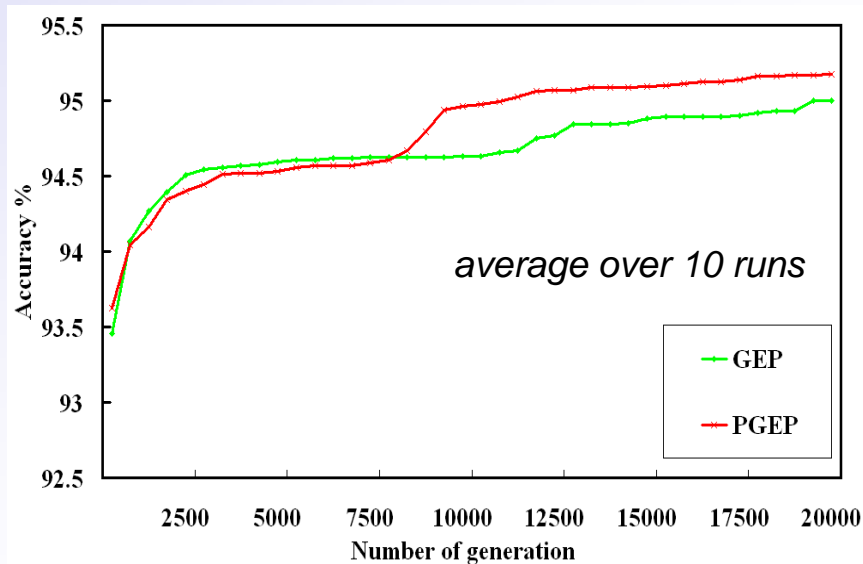
Mathematical expression

$$(a + b) * c$$

GEP vs. pGEP

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pGEP keeps the proximity of the genetic material during the translation process → expected lower destructive effect of the genetic operators



*pGEP- earlier convergence
- slightly higher accuracy
student t-test significance = 35%*

Proximity of the related genetic material - not controlled during the evolution process

Further developments - enforce keeping the related genetic material together might help the evolution

Controlled evolution

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- ❖ *Eliminate the weak individuals (individuals with fitness lower than a threshold) from the evolution process*

- ❖ *Setting the value of **Fitness Threshold (FT)***

Population Diversity vs. Convergence

- ✓ ***Static FT** - fixed value for all individuals/generations*

- ✓ ***Online FT** – guided by the average fitness per generation*

*FT = average fitness per generation * scaling factor*

Scaling factor should be optimised (typical values between 0.5 to 1.5)

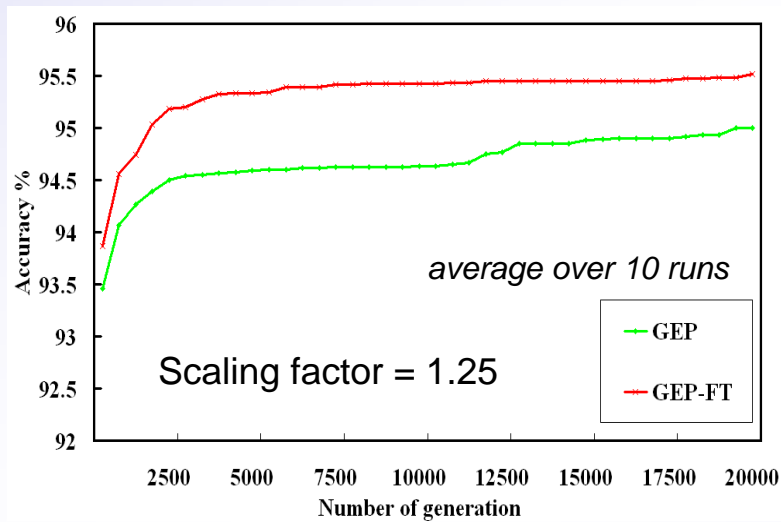
*Versions developed: **GEP-FT, pGEP-FT***

GEP vs. GEP-FT & pGEP-FT

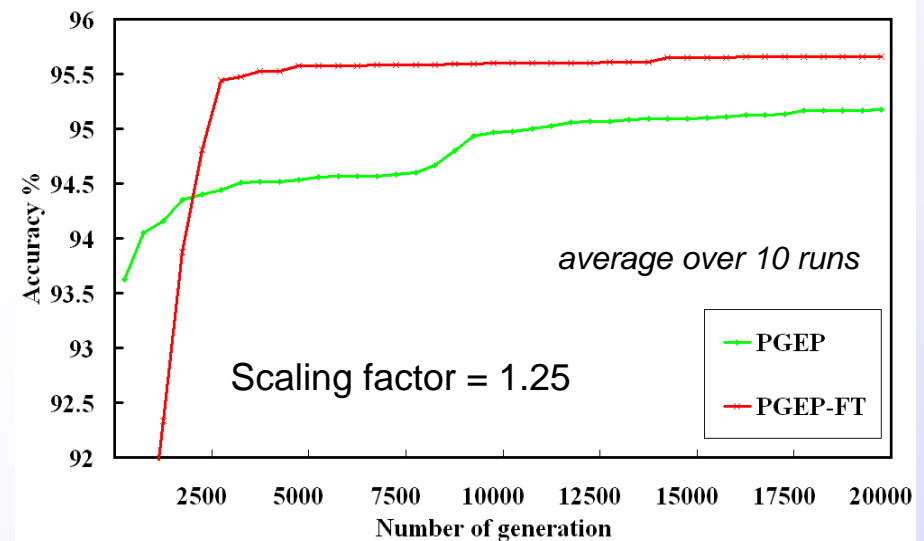
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Static FT – creates uniformity in the population => convergence problems

Online FT – better pressure on the evolution if FT properly chosen (FT too high => convergence problems)



student t-test significance = 0.6%



student t-test significance = 0.4%

GEP-FT and pGEP-FT - earlier convergence
- slightly higher accuracy

Dynamic classification threshold

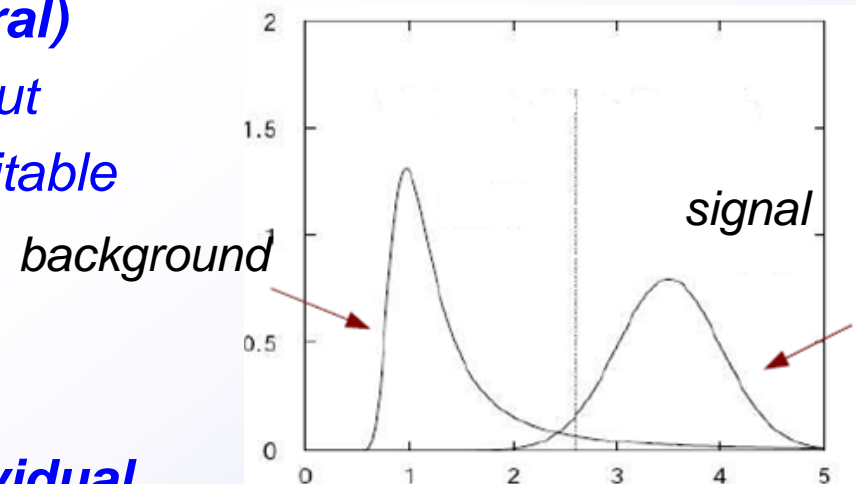
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Fixed classification threshold

- ❖ *for other methods - chosen at the end of the process (on the final output)*
- ❖ *not suitable for GEP (and EA, in general)*
 - ✓ *each individual provides its own output*
 - ✓ *threshold for one individual is not suitable for another*

Dynamic classification threshold

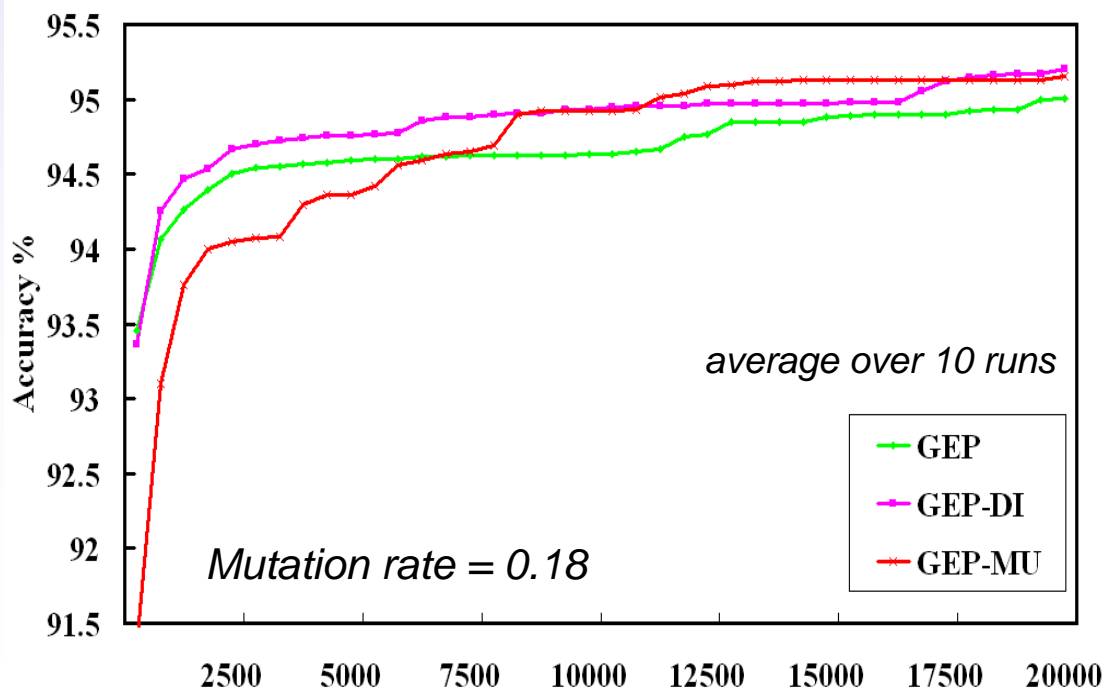
- ❖ *threshold value adapted to each individual*
- ❖ *two implementations (GEP-DI and GEP-MU)*



GEP vs. GEP-DI & GEP-MU

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- ❖ For each individual the optimal threshold is determined by scanning the full range of the output function (GEP-DI)
- ❖ Each chromosome has an additional element which contains the potential threshold value which is evolved with a mutation operator (GEP-MU)



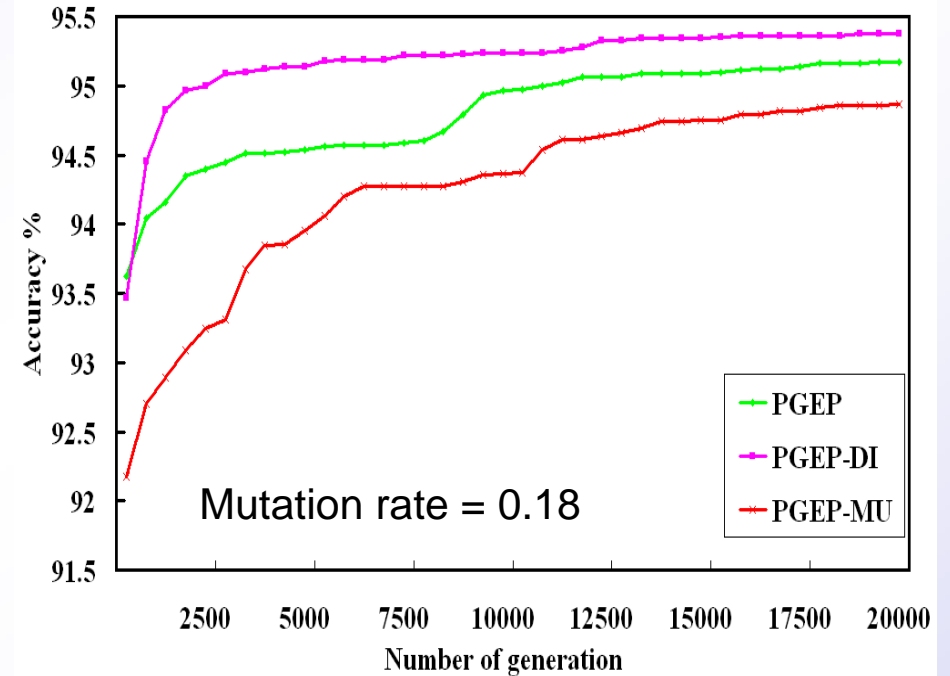
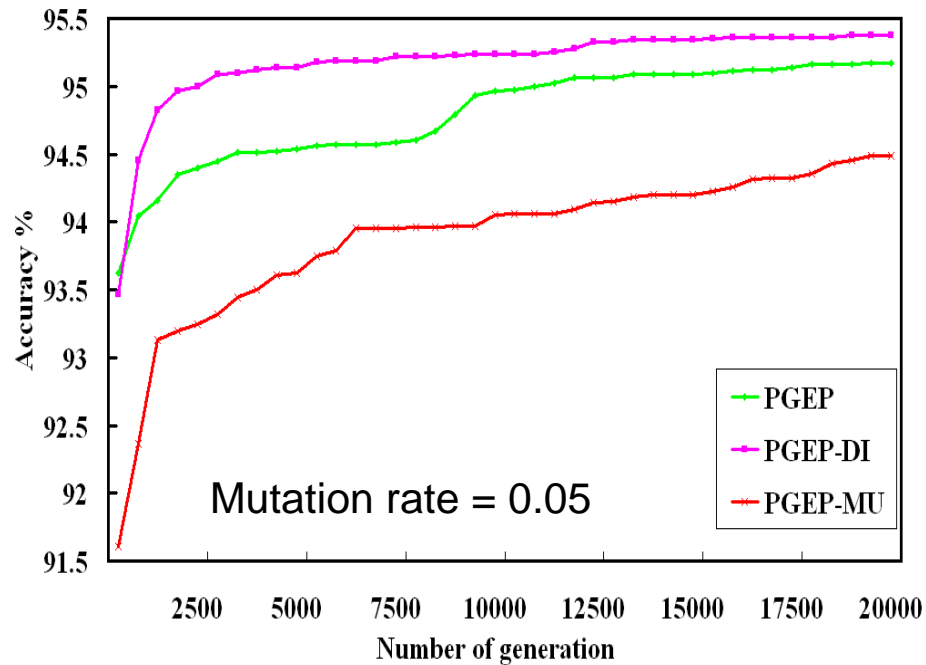
GEP-DI & GEP-MU - similar accuracy, slightly higher than GEP

GEP-MU – slower early evolution but earlier convergence than GEP-DI

student t-test sig. = 20%

pGEP vs. pGEP-DI & pGEP-MU

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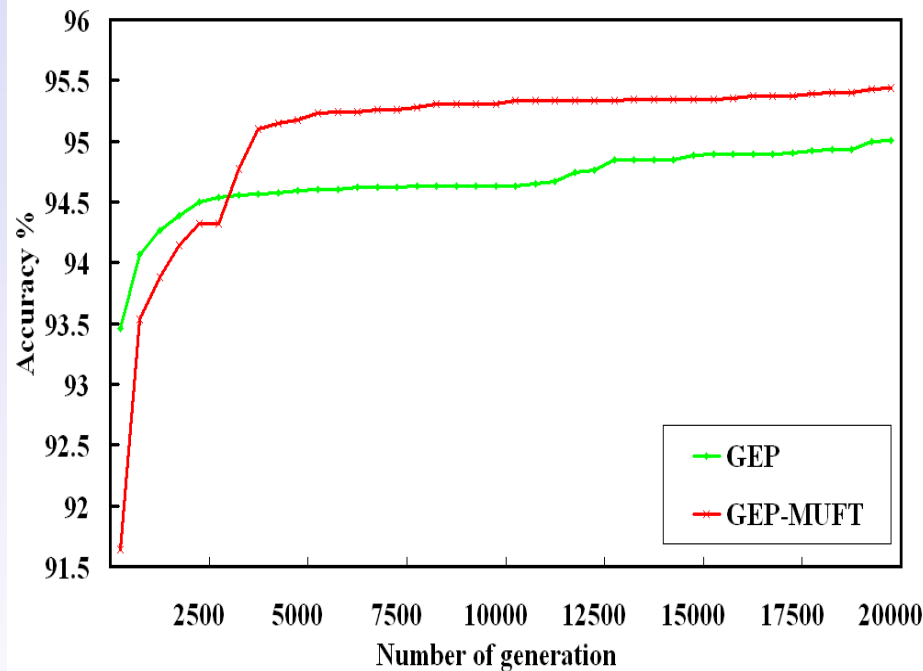


student t-test sig. (pGEP vs. pGEP-DI) = 23%

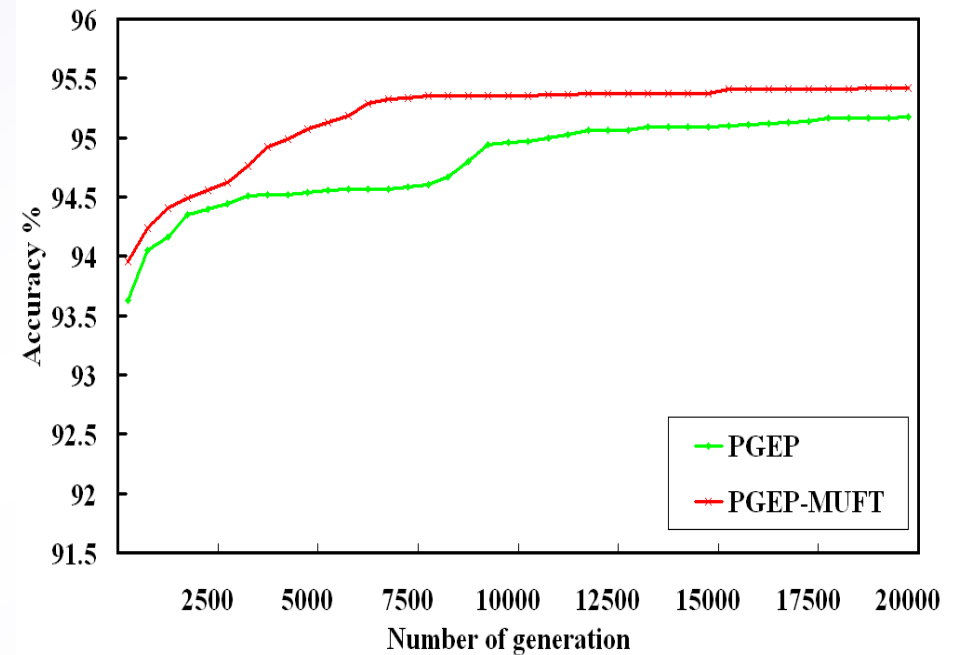
Mutation rate – not optimised

Combined developments

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Student t-test sig. = 2%



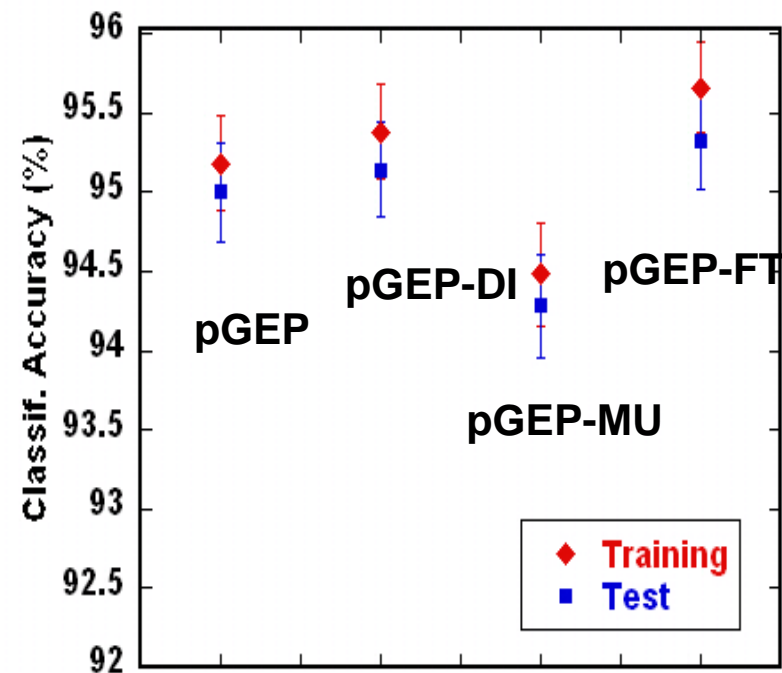
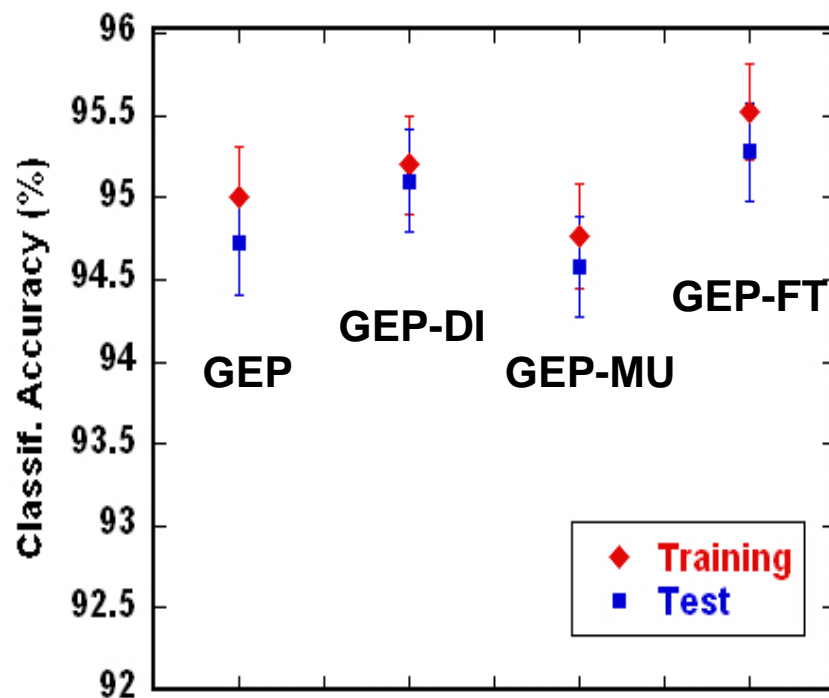
Student t-test sig. = 15%

Mutation rate – not fully optimised in this case

*Improvements - earlier convergence
- slightly higher accuracy*

Training - test comparison

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All models – good generalisation power

Conclusions

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Current developments of GEP

- ❖ *software development – allowed us flexibility*
 - ❖ *algorithmic research*
 - ✓ *prefix order mapping*
 - ✓ *controlled evolution – online fitness threshold*
 - ✓ *dynamic classification threshold*
(mutation based & range scanning)
- New developments – earlier convergence and higher accuracy at various levels (slightly higher accuracy – for this problem)*

Further developments

- ❖ *algorithms research – further control of the evolution*
- ❖ *software development – extensions to more fitness functions, multi-objective optimisation*
- ❖ *other applications*