

# Production of particles at large momentum transfer

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New Trends in High Energy Physics and QCD



# Outline:

**1** Introduction

**2** Formalism

**3** Results

**4** Conclusions



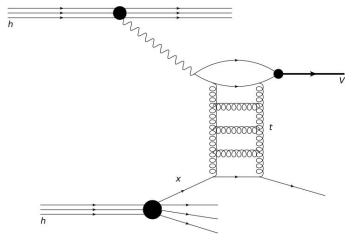
# Motivations

- Exchange of the BFKL Pomeron in high momentum transfer in coherent interactions to study the QCD dynamics at LHC



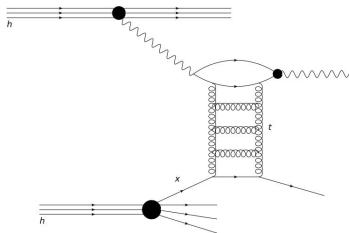
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- Exclusive processes of production of mesons ( $\rho$ ,  $J/\psi$  and  $\Upsilon$ )
- Photo-production of photons.



# Cross sections

The differential and total cross sections:

$$\frac{d\sigma_{\gamma h \rightarrow YX}}{dt} = \int_{x_{\min}}^1 dx_j \frac{d\sigma}{dt dx_j}, \quad \sigma_{\text{tot}} = \int_{t_{\min}}^{t_{\max}} dt \frac{d\sigma_{\gamma h \rightarrow YX}}{dt}$$

$$\frac{d\sigma}{dt dx_j} = \left[ \frac{81}{16} G(x_j, |t|) + \sum_j (q_j(x_j, |t|) + \bar{q}_j(x_j, |t|)) \right] \frac{d\hat{\sigma}}{dt}.$$

We use CTEQ6L (for vectors) and MSTW2008LO (for photons) parton parametrization in proton-proton collisions and EKS for the ion-ion case.



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Partonic cross section for photon production:

$$\frac{d\hat{\sigma}}{dt}(\gamma^* q \rightarrow \gamma q) = \frac{1}{16\pi} \{ |\mathcal{A}_{(+,+)}(s, t)|^2 + |\mathcal{A}_{(+,-)}(s, t)|^2 \},$$

where  $(+, \pm)$  are related to helicities states.





# Amplitudes

Meson production:

$$\mathcal{A}_V(s, t) = \frac{2}{9\pi^2} \int d\nu \frac{\nu^2}{(\nu^2 + 1/4)^2} \left(\frac{s}{\Lambda^2}\right)^{\omega(\nu)} I_\nu^{\gamma V}(Q_\perp) I_\nu^{qq}(Q_\perp)^*,$$

The quantities  $I$ 's are related with the impact factors of  $\gamma \rightarrow V$  and  $q \rightarrow q$ ,

$$I_\nu^{\gamma V_i}(Q_\perp) = -C_i \alpha_s \frac{16\pi}{Q_\perp^3} \frac{\Gamma(1/2 - i\nu)}{\Gamma(1/2 + i\nu)} \left(\frac{Q_\perp^2}{4}\right)^{i\nu} \int_{1/2 - i\infty}^{1/2 + i\infty} \frac{du}{2\pi i} \left(\frac{Q_\perp^2}{4M_{V_i}^2}\right)^{1/2 + u} \\ \times \frac{\Gamma^2(1/2 + u) \Gamma(1/2 - u/2 - i\nu/2) \Gamma(1/2 - u/2 + i\nu/2)}{\Gamma(1/2 + u/2 - i\nu/2) \Gamma(1/2 + u/2 + i\nu/2)}.$$

$$I_\nu^{qq}(Q_\perp) = -\frac{4\pi\alpha_s}{Q_\perp} \left(\frac{Q_\perp^2}{4}\right)^{i\nu} \frac{\Gamma(\frac{1}{2} - i\nu)}{\Gamma(\frac{1}{2} + i\nu)}.$$



# Amplitudes

Photon production:

$$\mathcal{A}_{(+,+)} = i\alpha\alpha_s^2 \sum_q e_q^2 \frac{4\pi}{3} \frac{1}{|t|} \int d\nu \frac{\nu^2}{(1/4 + \nu^2)^2} \frac{\tanh(\pi\nu)}{\pi\nu} \frac{11/4 + 3\nu^2}{1 + \nu^2} \left[ \frac{s}{s_0} \right]^{\omega(\nu)}$$

$$\mathcal{A}_{(+,-)} = i\alpha\alpha_s^2 \sum_q e_q^2 \frac{4\pi}{3} \frac{1}{|t|} \int d\nu \frac{\nu^2}{(1/4 + \nu^2)^2} \frac{\tanh(\pi\nu)}{\pi\nu} \frac{1/4 + \nu^2}{1 + \nu^2} \left[ \frac{s}{s_0} \right]^{\omega(\nu)}$$



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**BFKL characteristic function:**

$$\omega(\nu) = \bar{\alpha}_s \chi(\gamma), \quad \bar{\alpha}_s = (N_c \alpha_s) / \pi, \quad \gamma = 1/2 + i\nu$$



# BFKL (LO)

At leading order:

$$\chi^{\text{LO}}(\gamma) = 2\psi(1) - \psi(\gamma) - \psi(1 - \gamma)$$

where  $\psi(z)$  is the digamma function.

## Several problems:

- 1 the energy scale  $\Lambda$  is arbitrary;
- 2  $\alpha_s$  is fixed;
- 3 the power growth with energy violates  $s$ -channel unitarity at large rapidities.



# BFKL (NLO)

Original NLO BFKL kernel obtained by Fadin, Ciafaloni:

$$\chi(\gamma) = \chi^{\text{LO}}(\gamma) + \bar{\alpha}_s \chi^{\text{NLO}}(\gamma), \quad \bar{\alpha}_s = N_c \alpha_s / \pi,$$

with the  $\chi^{\text{NLO}}$  function being given by

$$\begin{aligned} \chi^{\text{NLO}}(\gamma) = & \mathcal{C} \chi^{\text{LO}}(\gamma) + \frac{1}{4} [\psi''(\gamma) + \psi''(1-\gamma)] - \frac{1}{4} [\phi(\gamma) + \phi(1-\gamma)] \\ & - \frac{\pi^2 \cos(\pi\gamma)}{4 \sin^2(\pi\gamma)(1-2\gamma)} \left\{ 3 + \left( 1 + \frac{N_f}{N_c^3} \right) \frac{(2+3\gamma(1-\gamma))}{(3-2\gamma)(1+2\gamma)} \right\} \\ & + \frac{3}{2} \zeta(3) - \frac{\beta_0}{8N_c} (\chi^{\text{LO}}(\gamma))^2, \end{aligned}$$

with  $\mathcal{C} = (4 - \pi^2 + 5\beta_0/N_c) / 12$ ,  $\beta_0 = (11N_c - 2N_f)/3$ ,  $N_f$  is the number of flavours,  $\psi^{(n)}(z)$  is the polygamma function,  $\zeta(n)$  is the Riemann zeta-function and

$$\phi(\gamma) + \phi(1-\gamma) = \sum_{m=0}^{\infty} \left[ \frac{1}{\gamma+m} + \frac{1}{1-\gamma+m} \right] \left[ \psi' \left( \frac{2+m}{2} \right) - \psi' \left( \frac{1+m}{2} \right) \right]$$



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## Several problems:

- 1 the choice of energy scale;
- 2 large correction;



# BFKL (all-poles)

## An alternative:

Sabio-Vera (2005): collinearly improved BFKL kernel characteristic function:  $\Rightarrow$  resum collinear effects

$$\begin{aligned} \omega_{\text{All-poles}} = & \bar{\alpha}_s \chi^{\text{LO}}(\gamma) + \bar{\alpha}_s^2 \chi^{\text{NLO}}(\gamma) + \\ & + \sum_{m=0}^{\infty} \left[ \left( \sum_{n=0}^{\infty} \frac{(-1)^n (2n)!}{2^n n! (n+1)!} \frac{(\bar{\alpha}_s + a \bar{\alpha}_s^2)^{n+1}}{(\gamma + m - b \bar{\alpha}_s)^{2n+1}} \right) - \frac{\bar{\alpha}_s}{\gamma + m} - \right. \\ & \left. - \bar{\alpha}_s^2 \left( \frac{a}{\gamma + m} + \frac{b}{(\gamma + m)^2} - \frac{1}{2(\gamma + m)^3} \right) \right] + \{\gamma \rightarrow 1 - \gamma\} \quad (1) \end{aligned}$$

where

$$a = \frac{5\beta_0}{12N_c} - \frac{13N_f}{36N_c^3} - \frac{55}{36}, \quad b = -\frac{\beta_0}{8N_c} - \frac{N_f}{6N_c^3} - \frac{11}{12}.$$



# BFKL BLM-MOM

Another alternative by Brodsky, Fadin, Kim, Lipatov, Pivovarov

BLM optimal scale + MOM renormalization scheme

$$\omega_{\text{BLM}}^{\text{MOM}} = \chi^{\text{LO}}(\gamma) \frac{\alpha_{\text{MOM}}(\hat{Q}^2) N_c}{\pi} \left[ 1 + \hat{r}(\nu) \frac{\alpha_{\text{MOM}}(\hat{Q}^2)}{\pi} \right], \quad (3)$$

$$\alpha_{\text{MOM}} = \alpha_s \left[ 1 + \frac{\alpha_s}{\pi} T_{\text{MOM}} \right]$$

$$\hat{Q}^2(\nu) = Q^2 \exp \left[ \frac{1}{2} \chi^{\text{LO}}(\gamma) - \frac{5}{3} + 2 \left( 1 + \frac{2}{3} \varrho \right) \right],$$

$$\begin{aligned} \hat{r}(\nu) = & -\frac{\beta_0}{4} \left[ \frac{\chi^{\text{LO}}(\nu)}{2} - \frac{5}{3} \right] - \frac{N_c}{4\chi^{\text{LO}}(\nu)} \left\{ \frac{\pi^2 \sinh(\pi\nu)}{2\nu \cosh^2(\pi\nu)} \right. \\ & \times \left[ 3 + \left( 1 + \frac{N_f}{N_c^3} \right) \frac{11 + 12\nu^2}{16(1 + \nu^2)} \right] - \chi''^{\text{LO}}(\nu) + \frac{\pi^2 - 4}{3} \chi^{\text{LO}}(\nu) \\ & \left. - \frac{\pi^3}{\cosh(\pi\nu)} - 6\zeta(3) + 4\tilde{\phi}(\nu) \right\} + 7.471 - 1.281\beta_0, \end{aligned}$$





# Vector mesons:<sup>1</sup>

## Strongly depend on

- coupling constant:  $\alpha_s = 0.21$
- energy scale with free parameters  $\Lambda \equiv s_0 = \beta M_V^2 + \gamma|t|$

## Calculation:

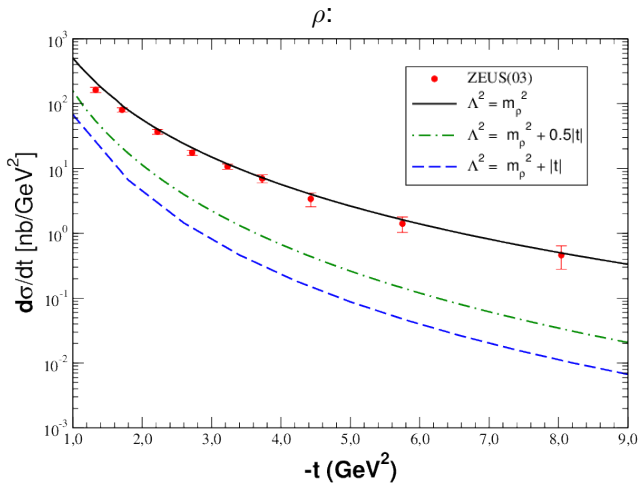
Impact factors and BFKL kernel at LO



<sup>1</sup>Gonçalves, Sauter, Phys.Rev. D81 (2010) 074028, Eur.Phys.J. A47 (2011) 117

# Vector mesons:<sup>1</sup>

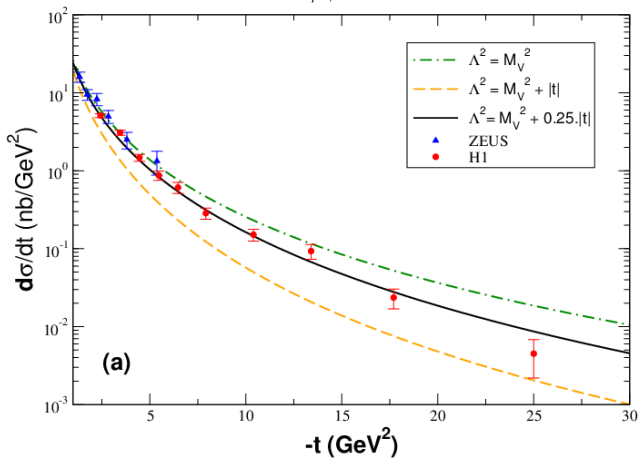
$d\sigma/dt$  using to fixing the parameters:



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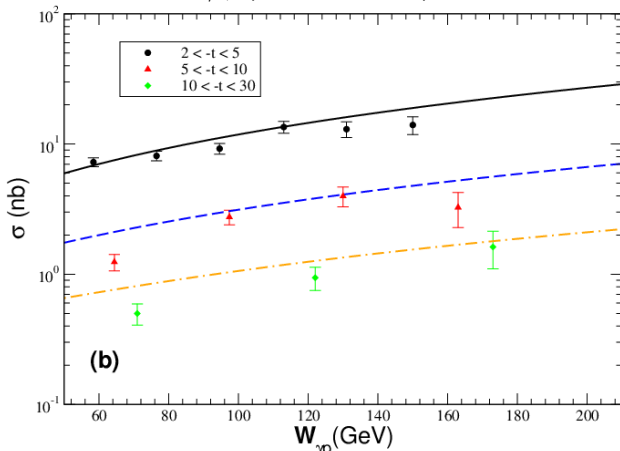
$J/\psi$ :



# Vector mesons:<sup>1</sup>

$\sigma_{tot}$  with the parameters fixed:

$J/\psi$  (H1 & ZEUS03):



# Photon:<sup>2</sup>

## Depends on:

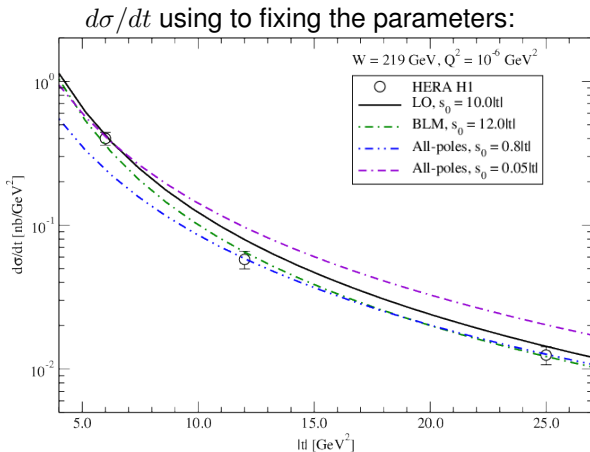
- Energy scale:  $\Lambda^2 = \gamma'|t|$
- $\alpha_s$  &  $\alpha_{\text{elm}}$

## Mixed calculation:

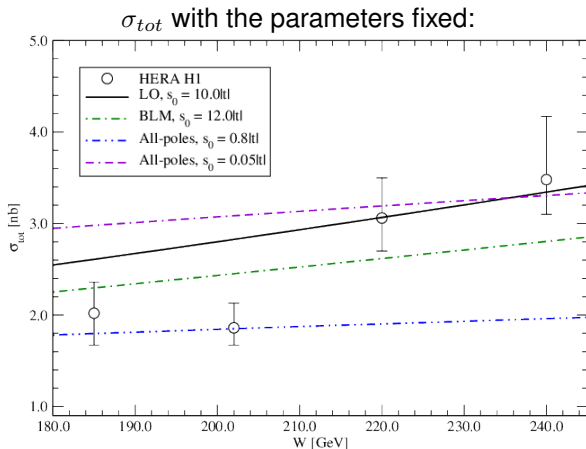
- Impact factors of the transition  $\gamma^* \rightarrow \gamma$  at LO
- Distinct analytical forms for the NLO BFKL kernel as well as the LO one



# Photon:<sup>2</sup>



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# Coherent hadronic collisions

- Cross section:

$$\frac{d\sigma [h_1 + h_2 \rightarrow h_1 \otimes Y \otimes X]}{dy} = \int_{t_{\min}}^{t_{\max}} dt \omega \frac{dN_\gamma(\omega)}{d\omega} \frac{d\sigma_{\gamma h \rightarrow YX}}{dt}(\omega)$$

- Proton photon flux (*Dress et al.*):

$$\frac{dN_\gamma^{PP}(\omega)}{d\omega} = \frac{\alpha_{em}}{2\pi\omega} \left[ 1 + \left( 1 - \frac{2\omega}{\sqrt{S_{NN}}} \right)^2 \right] \left( \ln \Omega - \frac{11}{6} + \frac{3}{\Omega} - \frac{3}{2\Omega^2} + \frac{1}{3\Omega^3} \right)$$

- Nucleus photon flux (*Weissäcker/Williams*):

$$\frac{dN_\gamma^{AA}(\omega)}{d\omega} = \frac{2Z^2\alpha_{em}}{\pi\omega} \left[ \bar{\eta} K_0(\bar{\eta}) K_1(\bar{\eta}) - \frac{\bar{\eta}^2}{2} (K_1^2(\bar{\eta}) - K_0^2(\bar{\eta})) \right]$$

where  $\bar{\eta} = \omega (R_{h_1} + R_{h_2}) / \gamma_L$

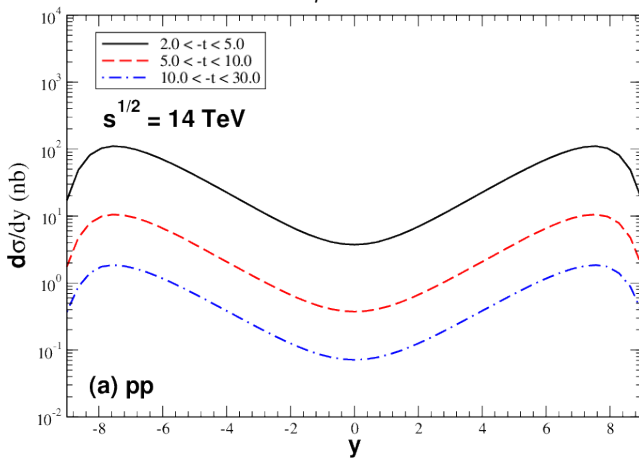




# Coherent hadronic collisions

Using the previous parameters.

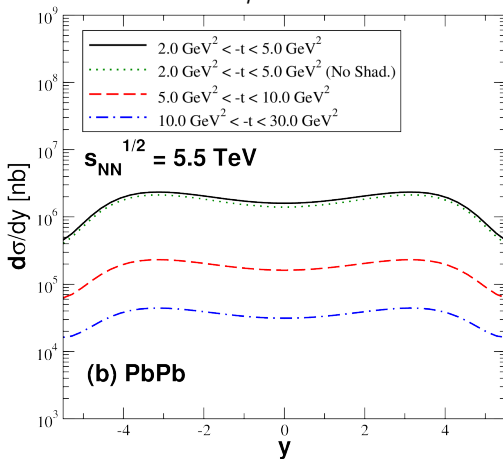
$\rho$ :



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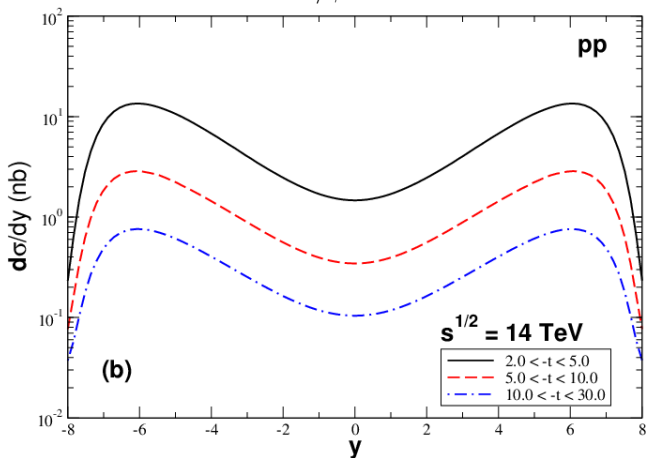
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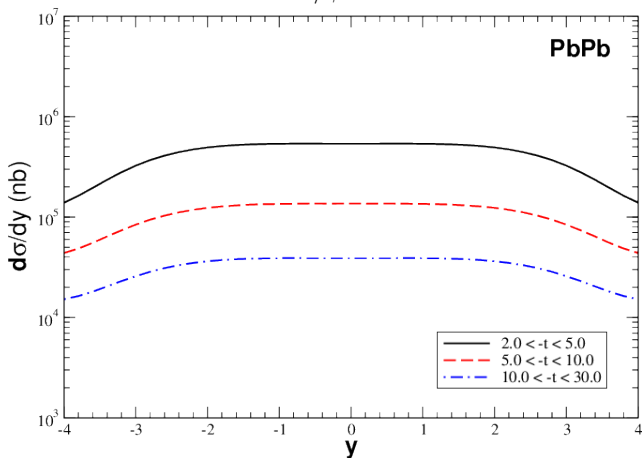
$J/\psi$ :



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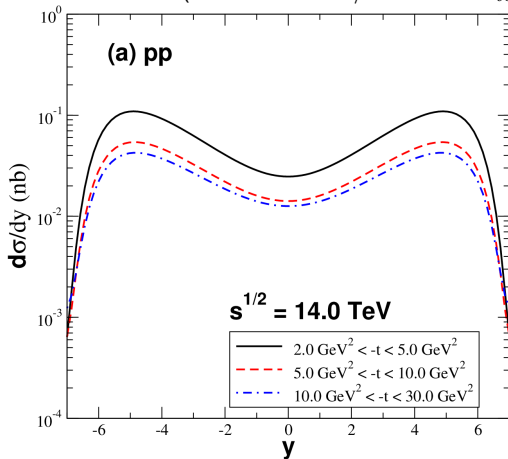
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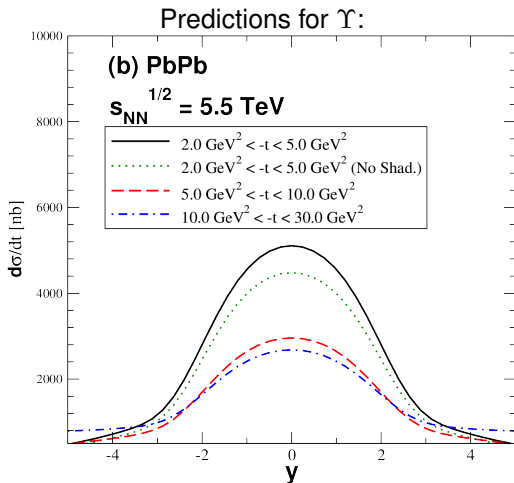


# Coherent hadronic collisions

Predictions for  $\Upsilon$  (no data for  $d\sigma/dt$  and/or  $\sigma_{tot}$ ):



# Coherent hadronic collisions



# Event rates

LHC energies ( $pp$  and  $PbPb$  collisions):

Meson	$t$ range	$pp$ ( $\sqrt{s} = 14$ TeV)	$PbPb$
$\rho$	$2.0 <  t  < 5.0$	751.0 nb (7510.0)	20.0 mb (8.4)
	$5.0 <  t  < 10.0$	71.0 nb (710.0)	2.2 mb (0.9)
	$10.0 <  t  < 30.0$	12.0 nb (120.0)	0.4 mb (0.17)
$J/\psi$	$2.0 <  t  < 5.0$	97.0 nb (970.0)	3.0 mb (13.0)
	$5.0 <  t  < 10.0$	21.0 nb (210.0)	0.9 mb (0.38)
	$10.0 <  t  < 30.0$	6.0 nb (60.0)	0.3 mb (0.12)
$\Upsilon$	$2.0 <  t  < 5.0$	0.8 nb (8.0)	0.26 mb (0.1)
	$5.0 <  t  < 10.0$	0.4 nb (4.0)	0.17 mb (0.07)
	$10.0 <  t  < 30.0$	0.3 nb (3.0)	0.16 mb (0.06)



# Conclusions

## Summary:

- description of the high energy limit of QCD
- to improve the analysis of the exclusive vector meson and photon production at large- $t$
- probe the QCD dynamics

## Our results:

- 1 BFKL formalism is able to describe the current experimental data of  $ep$  collisions at HERA with suitable choice of parameters
- 2 coherent  $pp$  interactions at LHC  $\Rightarrow$  able to constrain the QCD dynamics
- 3 complementary to the recent theoretical and phenomenological studies that use NLO BFKL Pomeron as  $\gamma^*\gamma^*$ , Mueller-Navelet jets.

