

CP violation in charged Higgs decays in MSSM

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$H^\pm \Rightarrow$ **Physics beyond SM**

- 2HDM
- Higgs triplet model
- MSSM
- ...

If H^\pm will be found at the Tevatron or LHC:

- ⇒ more work is needed to find which New Physics it is
- ⇒ couplings must be measured

We consider: CP violation in H^\pm in MSSM

MSSM: 5 Higgs bosons h^0, H^0, A^0, H^\pm

- 2 parms. only: $\tan\beta, m_A \Leftrightarrow 50$ (if FV 124) in MSSM
- TH *and* Exp. bounds:
 - 1) TH: $m_{H^+}^2 = m_W^2 + m_{A^0}^2 \geq m_{W^+}^2$
 - 2) Exp: LEP: $m_{H^+} \geq 78.6$ GeV, Tevatron: $m_{H^+} \geq 200$ GeV
- CP inv. at tree level
- CPV in Higgs sector → loop effects

We consider

H^\pm -decays into ordinary particles:

$$H^\pm \rightarrow tb$$

$$H^\pm \rightarrow \tau^\pm \nu$$

$$H^\pm \rightarrow W^\pm h^0$$

- decay rate asymmetries:

$$\delta^{CP} = \frac{\Gamma(H^+ \rightarrow \dots) - \Gamma(H^- \rightarrow \dots)}{\Gamma(H^+ \rightarrow \dots) + \Gamma(H^- \rightarrow \dots)}$$

$$\delta_{tb}, \quad \delta_{\nu\tau}, \quad \delta_{Wh^0}$$

We consider

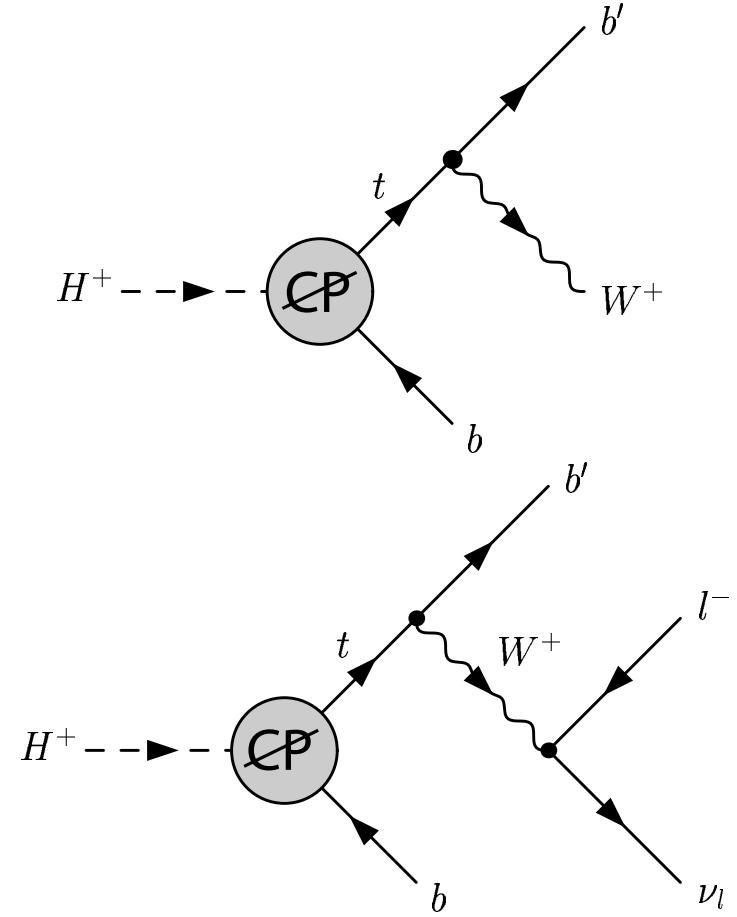
t decays keeping its momentum and polarization!

We study the decay products of t :

$$H^\pm \rightarrow tb \rightarrow b\mathbf{b}'W^\pm$$

$$H^\pm \rightarrow tb \rightarrow bb'W^\pm \rightarrow bb'\mathbf{l}^\pm\nu$$

- angular asymmetries: $\mathbf{b}', \mathbf{l}^\pm \Rightarrow \Delta A^{CP} = A_+^{FB} - A_-^{FB}$
- energy asymmetries: $\mathbf{b}' \Rightarrow \Delta R^{CP} = R_+ - R_-$



we measure CPV induced by loop corrections in $H^\pm \rightarrow bt$

in general: vertex & self energy loop corrections



$$CPV : \delta\Gamma^{CP} \approx \frac{(ig^{CP})}{CPV \text{ coupling}} \times i \underbrace{\cancel{Sm} (MSSM \text{ loops})}_{\text{a SUSY channel open}}$$

for **CPV** we need both:

- ig^{CP}
- at least 1 SUSY channel open for H^\pm -decay

$$m_{H^+} > \tilde{m}_1 + \tilde{m}_2 > 200 \text{ GeV}$$

MSSM

- The particles in the loops:

\tilde{g} , $\tilde{\chi}^\pm$, \tilde{t} , \tilde{b} and $\tilde{\chi}^0$ in the loops

Recall: gluino $\tilde{g} \leftrightarrow g$,

charginos $\tilde{\chi}^\pm \leftrightarrow (\tilde{W}^\pm, \tilde{H}^\pm)$,

neutralinos $\tilde{\chi}^0 \leftrightarrow (\tilde{\gamma}, \tilde{Z}, \tilde{H}_1^0, \tilde{H}_2^0)$

scalar quarks $\tilde{q} \leftrightarrow q$

scalar leptons $\tilde{l} \leftrightarrow l$

- The CP phases:

1) the Higgs mass parameter $\mu = |\mu| e^{i\phi_\mu}$,

- exp: $d_e, d_n \Rightarrow \phi_\mu < 10^{-2}$, $\tilde{m}_{SUSY} \sim$ few 100 GeV

2) the gaugino masses: M_1, M_2

GUT: $M_1 = (5/3) \tan^2 \theta_W M_2 \Rightarrow \phi_1 = 0$

$$|M_1| = (5/3) \tan^2 \theta_W |M_2| \Rightarrow \phi_1 \neq 0$$

3) the trilinear coupls. of sfermions and Higgs:

$A_t = |A_t| e^{i\phi_t}$, $A_b = |A_b| e^{i\phi_b}$, $A_\tau = |A_\tau| e^{i\phi_\tau}$,

$$\textcolor{red}{\underline{\mathbf{H}^\pm \rightarrow tb}}$$

*H. Eberl, S. Kraml,
W. Majerotto, E. Ch.*

*N.P. **B***

$$\mathcal{M}_{H^\pm} = \frac{i g}{\sqrt{2} m_W} \bar{u}(p_t) \left[\textcolor{blue}{Y_t^\pm} P_L + \textcolor{blue}{Y_b^\pm} P_R \right] u(-p_{\bar{b}})$$

$$\textcolor{blue}{Y_i^\pm} = y_i + \delta Y_i^{inv} \pm \textcolor{red}{\delta Y_i^{CP}}$$

$$y_t = m_t \cot \beta, \quad y_b = m_b \tan \beta$$

$$\textcolor{red}{\delta Y_i^{CP}} = \Re e \textcolor{red}{\delta Y_i^{CP}} + i \Im m \delta Y_i^{CP}$$

2 CPV formfactors: $\Re e \delta Y_t^{CP}$ & $\Re e \delta Y_b^{CP}$

- we have: 2 CPV form factors $\Re e \delta Y_t^{CP}$ and $\Re e \delta Y_b^{CP}$
- we need: 2 measurable quantities:

1) the decay rate: $\Gamma^\pm = \Gamma^{inv} \pm \Gamma^{CP}$

2) the t polarization: $\mathcal{P}^\pm = \pm \mathcal{P}^{inv} + \mathcal{P}^{CP}$

$$\Gamma^{CP} = [y_t \Re e \delta Y_t^{CP} + y_b \Re e \delta Y_b^{CP}] (p_t p_b) -$$

$$- m_t m_b [y_b \Re e \delta Y_t^{CP} + y_t \Re e \delta Y_b^{CP}]$$

$$\mathcal{P}^{CP} = \frac{y_t \Re e \delta Y_t^{CP} - y_b \Re e \delta Y_b^{CP}}{(y_t^2 + y_b^2)(p_t p_b) - 2 m_t m_b y_t y_b}$$

Our CPV asymmetries:

*H. Eberl, E. Ginina,
W. Majerotto, E. Ch.*

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- decay rate asymmetries: $\delta^{CP} \simeq \Gamma^{CP}$
- CPV forward-backward asymmetries: $\Delta A_f^{CP} \simeq \mathcal{P}^{CP}$
- CPV energy asymmetry $\Delta R^{CP} \simeq \mathcal{P}^{CP}$

$$\Delta A_f^{CP} = A_+^{FB} - A_-^{FB} = \alpha_f m_t^2 m_H^2 \frac{m_H^2 - m_t^2}{(m_H^2 + m_t^2)^2} \mathcal{P}^{CP}$$

$$A_+^{FB} = \frac{N_+^F - N_+^B}{N_+^F + N_+^B}, \quad A_-^{FB} = \frac{N_-^F - N_-^B}{N_-^F + N_-^B}$$

sensitivity to t polar : $\alpha_b = \frac{m_t^2 - 2m_W^2}{m_t^2 + 2m_W^2} \simeq 0.4$, $\alpha_l = 1$

$$\Delta R^{CP} = R_+ - R_- = \alpha_b (m_H^2 - m_t^2) \mathcal{P}^{CP}, \quad R_+ = \frac{N_+(E > E_0) - N_+(E < E_0)}{N_+(E > E_0) + N_+(E < E_0)}$$

$H^+ \rightarrow \nu\tau$

H. Eberl, S. Kraml,
W. Majerotto, E. Ch.

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$m_\nu = 0 \Rightarrow$ one formfactor δY_τ^{CP} :

$$Y_\tau^\pm = y_\tau + \delta Y_\tau^{inv} \pm \delta Y_\tau^{CP}, \quad \delta_{\nu\tau} = \frac{Re \delta Y_\tau^{CP}}{y_\tau}$$

$H^\pm \rightarrow W^\pm h^0$

The difference: $h^0 = \text{not observed (yet!)}$

E.Ginina, M. Stoilov,
E. Ch. JHEP

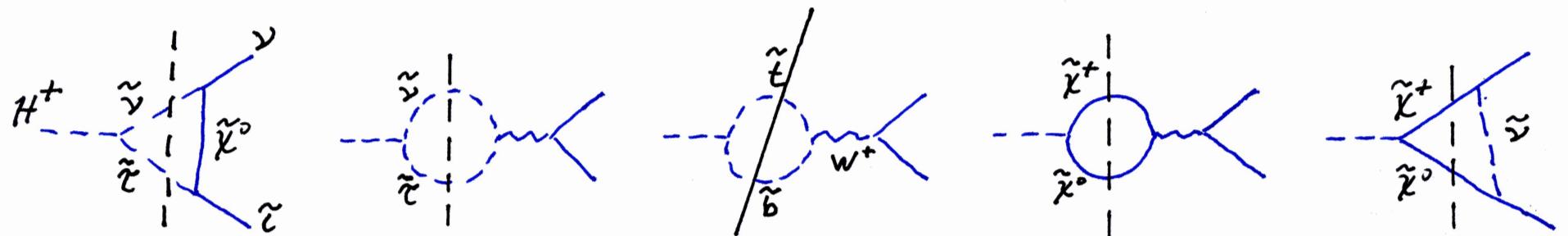
TH: $m_{h^0} = m_{h^0}(m_{H^+}, \tan \beta), \quad g_{WH^+h^0} = g_{WH^+h^0}(m_{H^+}, \tan \beta)$

$$\begin{aligned}\mathcal{M}_{H^\pm} &= ig \varepsilon_\alpha^\lambda(p_W) p_h^\alpha Y^\pm, \\ Y^\pm &= y + \delta Y^{inv} \pm \delta Y^{CP}, \quad y = \cos(\alpha - \beta)\end{aligned}$$

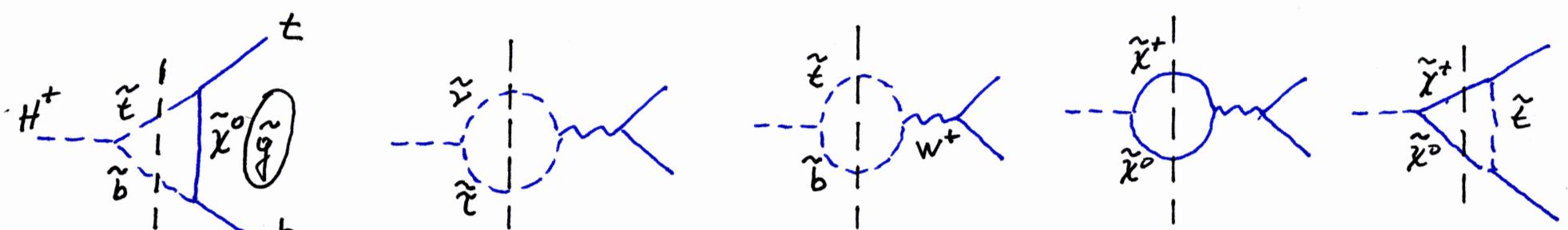
$$\delta_{Wh} \simeq \frac{\Re e \delta Y^{CP}}{y}$$

$BR(H^\pm \rightarrow W^\pm h^0) \sim 10\% \text{ for low } m_{H^+} \& \text{ low } \tan \beta, \text{ quickly drops with } \tan \beta$

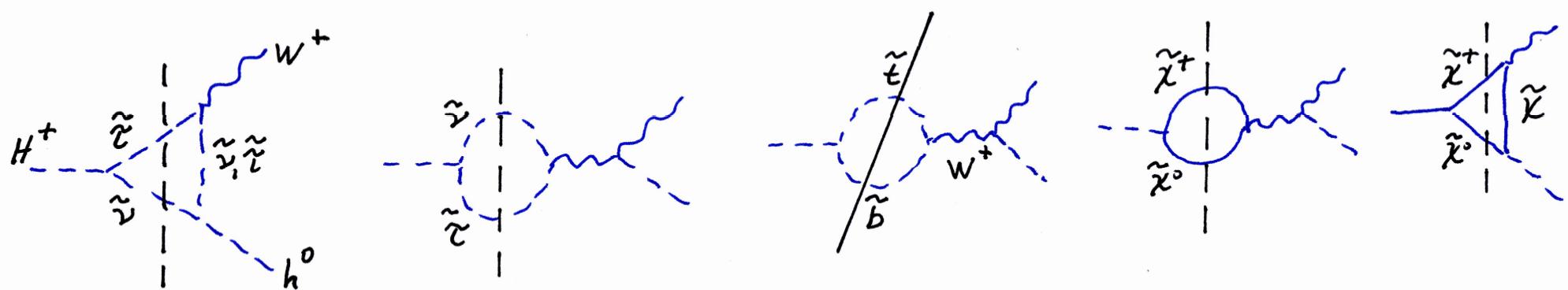
$H^\pm \rightarrow \nu\tau : m_H \simeq 200 - 300 \text{ GeV}, \tan\beta > 10$



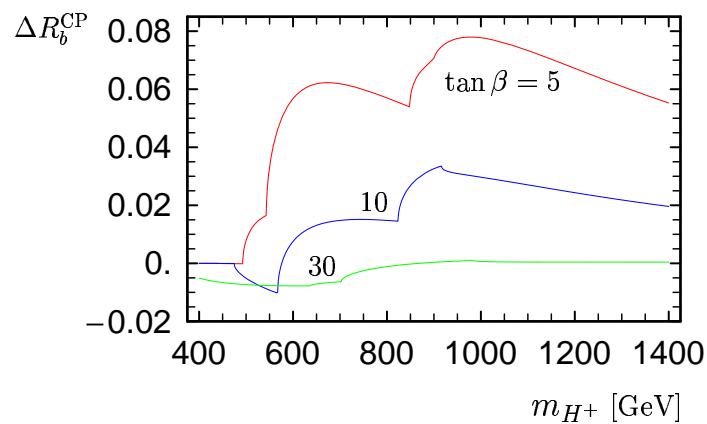
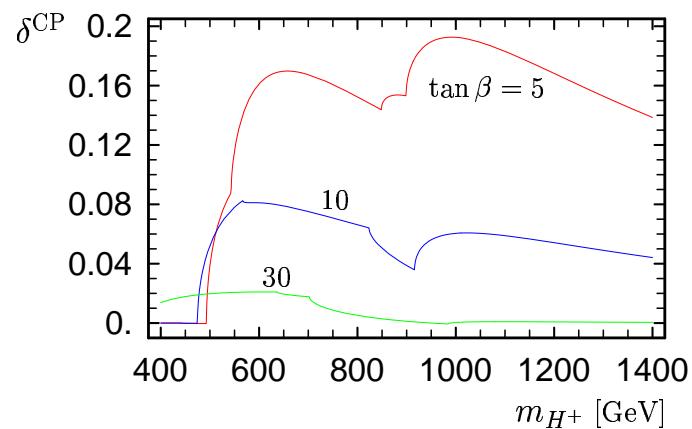
$H^\pm \rightarrow tb : m_H > m_t + m_b > 200 \text{ GeV}$



$H^\pm \rightarrow W^\pm h^0 : m_H \simeq 200 - 250 \text{ GeV}, \tan\beta \simeq 3 - 5$

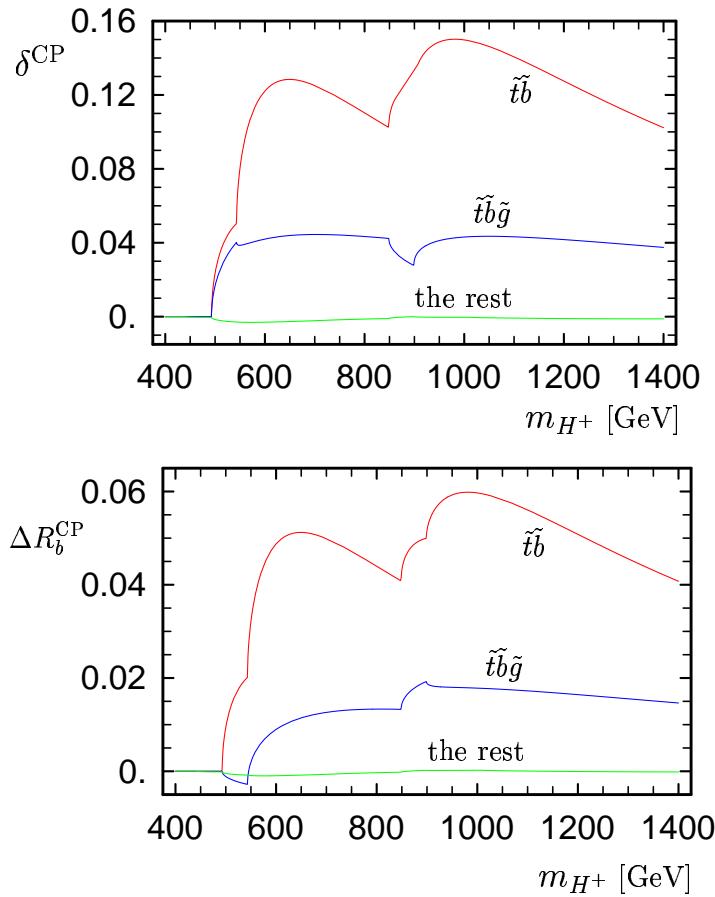


The CPV asymmetries in $H^\pm \rightarrow tb$



$\phi_{A_t} = \pi/2$, no sensitivity to ϕ_{A_b}

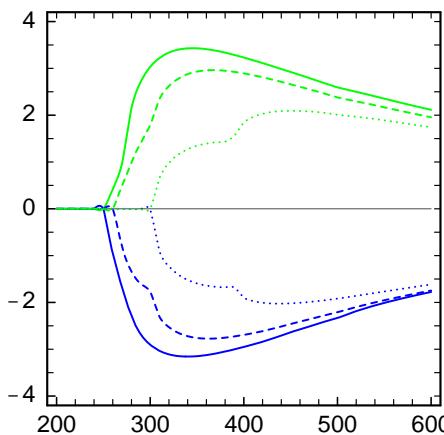
The different contributions to $H^\pm \rightarrow tb$



δ_{tb} significant when $H^+ \rightarrow \tilde{t}\tilde{b}$ open (sensitive to $\phi_{\tilde{t}}$), otherwise – negligible,

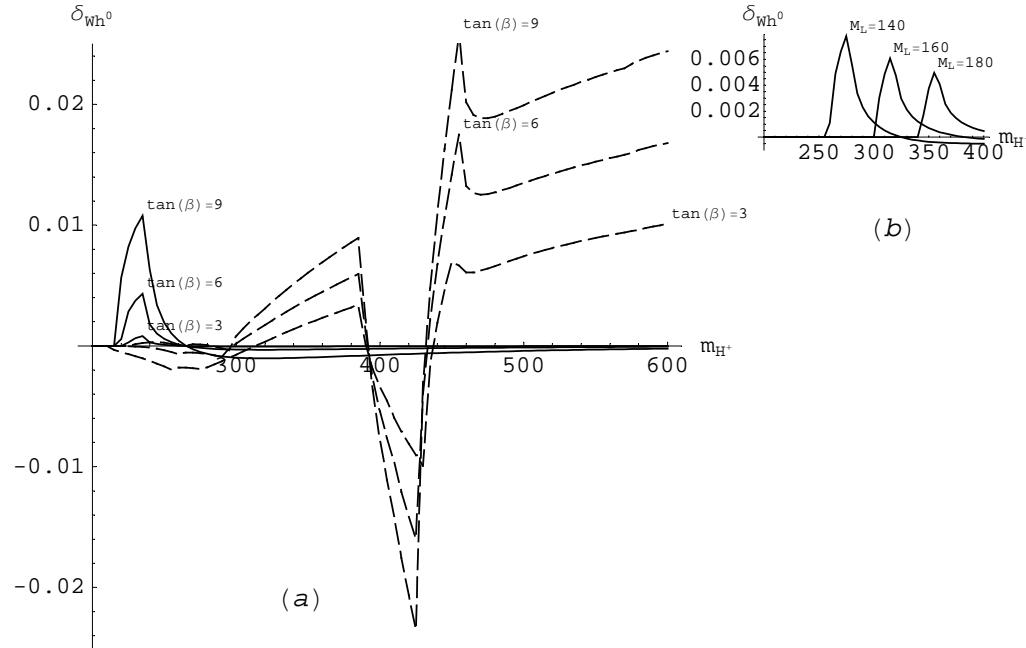
$\tan \beta = 5$, $\phi_{A_t} = \pi/2$, $\phi_{A_b} = \phi_\mu = 0$.

The CPV asymmetry in $H^+ \rightarrow \nu\tau$



- $\delta_{\nu\tau}[10^{-3}]$ as function of m_{H^+} , sensitive to ϕ_τ and ϕ_1 ; $m_{H^+} > m_{\tilde{\nu}} + m_{\tilde{\tau}}$
 $\delta(\phi_\tau = \pi/2) \simeq -\delta(\phi_1 = \pi/2), \quad \delta(\phi_\tau = \phi_1 = \pi/2) \simeq 0,$
- BR important for low m_{H^+} and $\tan\beta > 10$

The CPV asymmetry in $H^+ \rightarrow W^\pm h^0$



δ_{Wh^0} as a function of m_{H^+} a) , $M_L = 120$ GeV; solid lines are for $\phi_\tau = -\pi/2, \phi_1 = 0$; dashed lines are for $\phi_\tau = 0, \phi_1 = -\pi/2$. b) for different values of M_L , at $\tan \beta = 9, \phi_\tau = -\pi/2, \phi_1 = 0$.

BR important for low m_{H^+} and low $\tan \beta \simeq 3 - 5$

The BR of H^\pm

For example, for $m_{H^+} = 250$ GeV, we have

$$\begin{aligned}\tan \beta &= 5 \\ BR(H^+ \rightarrow t\bar{b}) &= 0.90 \\ BR(H^+ \rightarrow \nu\tau) &= 0.062 \\ BR(H^+ \rightarrow W^+ h^0) &= 0.04\end{aligned}$$

$$\begin{aligned}\tan \beta &= 30 \\ BR(H^+ \rightarrow t\bar{b}) &= 0.64 \\ BR(H^+ \rightarrow \nu\tau) &= 0.36 \\ BR(H^+ \rightarrow W^+ h^0) &= 0.0006\end{aligned}$$

Conclusions

CPV in MSSM: $H^\pm \rightarrow tb, H^\pm \rightarrow \nu\tau, H^\pm \rightarrow W^\pm h^0$:

$\Rightarrow \tan \beta$ & m_{H^+} are unknown

\Rightarrow depending on $\tan \beta$ & m_{H^+} different decay modes will play role

\Rightarrow different phases will be measured

$$\delta^{CP} = \frac{\Gamma(H^+ \rightarrow \dots) - \Gamma(H^- \rightarrow \dots)}{\Gamma(H^+ \rightarrow \dots) + \Gamma(H^- \rightarrow \dots)}$$

- simple measurement – only the decay rates
- always decay modes $H^+ \rightarrow$ SUSY partls. needed for $\delta^{CP} \neq 0$
 - \Rightarrow this decreases $BR(H^+ \rightarrow$ ordinary partls.)
 - a simult. consider. of δ^{CP} & BR needed

- $H^\pm \rightarrow tb$, $\delta^{CP}(\tilde{t}\tilde{b}) \sim 16\% - 20\%$, $\Rightarrow \phi_t \& \phi_b$, $m_{H^+} > 500$ GeV
- $H^\pm \rightarrow \nu\tau^\pm$, $\delta^{CP}(\tilde{\nu}\tilde{\tau}) \leq 0, 5 \cdot 10^{-3}$ $\Rightarrow \phi_\tau \& \phi_1$,
 $\tan\beta > 10$, $m_{H^+} \simeq 200 - 300$ GeV
- $H^\pm \rightarrow W^\pm h^0$, $\delta^{CP}(\tilde{\nu}\tilde{\tau}) \leq 10^{-2}$ $\Rightarrow \phi_\tau \& \phi_1$,
 $\tan\beta \simeq 3 - 5$, $m_{H^+} \simeq 200 - 300$ GeV
- $H^\pm \rightarrow tb_1 \rightarrow b_1 \textcolor{blue}{b}_2 W \rightarrow b_1 b_2 \textcolor{blue}{l} \nu$
 $\Rightarrow \Delta A_{FB}^{CP} \& \Delta R_b^{CP} \sim 10\%$

- **Measurability**

δ^{CP} depends on H^\pm -production:

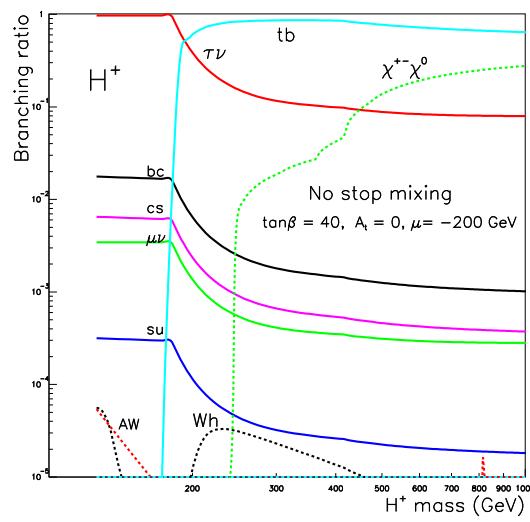
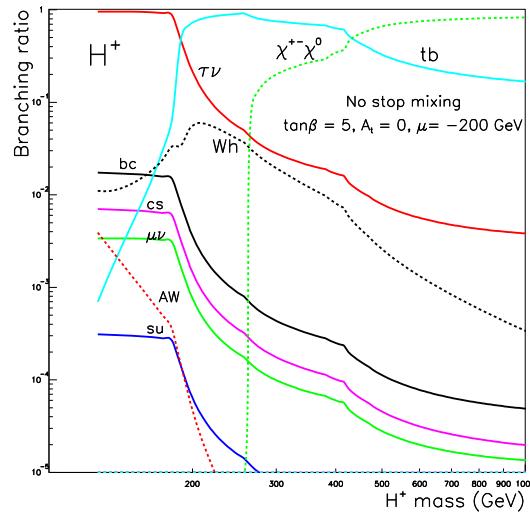
$$\delta^{CP} = \delta_P^{CP} + \delta_D^{CP}$$

\Rightarrow at the Tevatron: $m_{H^+} < 200$ GeV

\Rightarrow at LHC: $m_{H^+} < 1000$ GeV

\Rightarrow at LC: $m_{H^+} < \sqrt{s}/2$ GeV

LHC: $pp \rightarrow H^\pm t$ **see the next talk!**



The BR of H^+ for $\tan\beta = 5, 40$ (A.Djouadi, J.Kalinowski, M.Spira)

Measurability – depends on the H^\pm -production

- $H^\pm \rightarrow tb$

LHC: $gb \rightarrow H^\pm t$ with large background

SLHC needed! $L=1000-3000$ fb

- $H^\pm \rightarrow \nu\tau$, $H^\pm \rightarrow W^\pm h^0$

LHC: BR too low

interesting for e^+e^- -colliders: $e^+e^- \rightarrow H^+H^-$: m_H^\pm - the only param.

- the number of H^\pm needed to measure $\delta_{...}^{CP}$ in $H \rightarrow ...$ with N_σ standard deviations is

$$N \geq \frac{N_\sigma^2}{\delta^2 BR(H \rightarrow \dots)}$$

- the number of $H^\pm \rightarrow \dots$ seen at LHC at the given mode is

$$N = \sigma_P BR \times \text{acceptance} \times \text{luminosity}$$

The loops in $H^\pm \rightarrow tb$

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