

Physics at Hadron Colliders

Lecture II

Beate Heinemann

*University of California, Berkeley and
Lawrence Berkeley National Laboratory*

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Outline

- Lecture I: Introduction
 - Outstanding problems in particle physics
 - and the role of hadron colliders
 - Current and near future colliders: Tevatron and LHC
 - Hadron-hadron collisions
- Lecture II: Standard Model Measurements
 - Standard Model Cross Section Measurements as Tests of QCD
 - Precision measurements in electroweak sector
- Lecture III: Searches for the Higgs Boson
 - Standard Model Higgs Boson
 - Higgs Bosons beyond the Standard Model
- Lecture IV: Searches for New Physics
 - Supersymmetry
 - High Mass Resonances (Extra Dimensions etc.)

Standard Model Cross Section Measurements as test of QCD

- **Jets**
- **W and Z bosons**
- **Top Quark Production**

What is a Cross Section?

- Differential cross section: $d\sigma/d\Omega$:
 - Probability of a scattered particle in a given quantum state per solid angle $d\Omega$
 - E.g. Rutherford scattering experiment
- Other differential cross sections: $d\sigma/dE_T(\text{jet})$
 - Probability of a jet with given E_T
- Integrated cross section
 - Integral: $\sigma = \int d\sigma/d\Omega d\Omega$

Measurement:

$$\sigma = (N_{\text{obs}} - N_{\text{bg}}) / (\epsilon L)$$

Luminosity

Luminosity Measurement

$$R_{pp} = \mu_{pp} \cdot f_{BC} = \sigma_{LM} \cdot \sigma_{inel} \cdot \epsilon_{pp} \cdot \delta(L) \cdot L$$

L - luminosity

f_{bc} - Bunch Crossing rate

μ_a - # of pp / BC

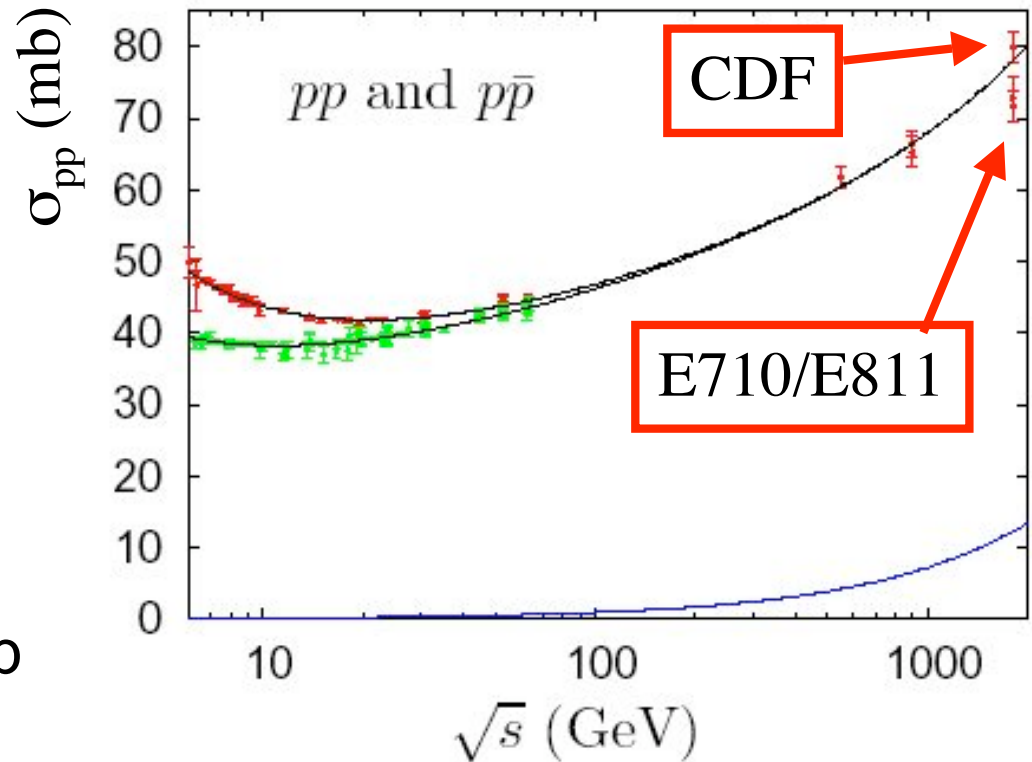
σ_{LM}

σ_{inel} - inelastic x-section

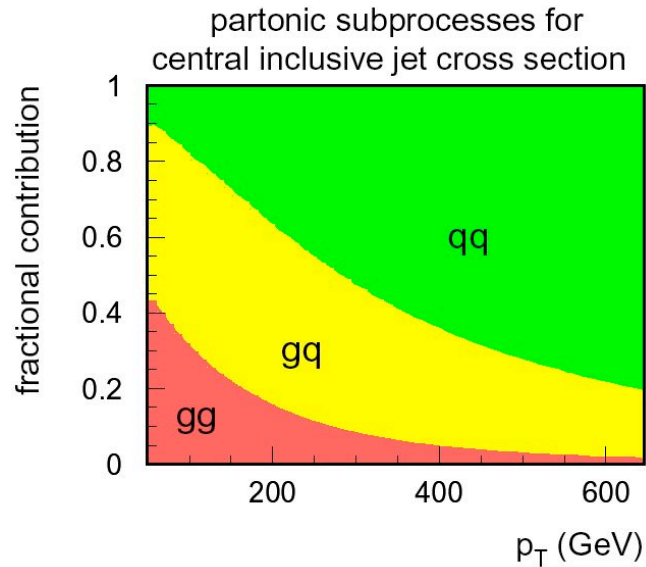
ϵ_{pp} - acceptance for a single pp

$\delta(L)$ - detector non-linearity

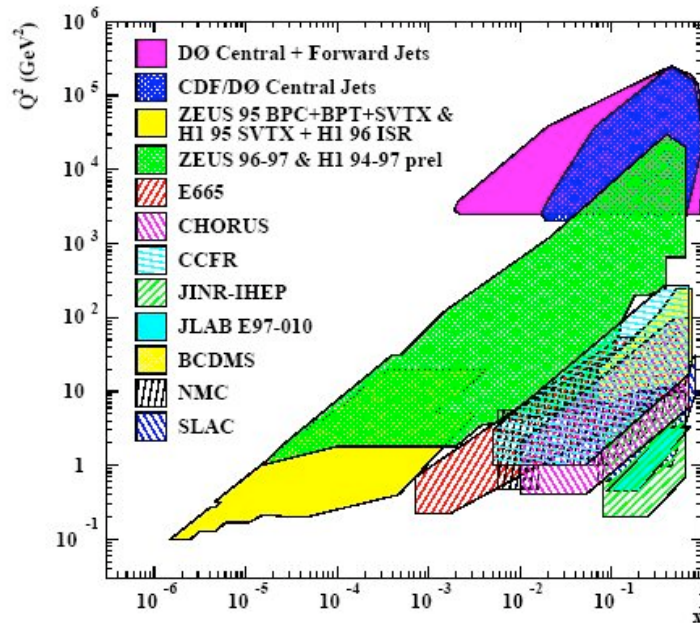
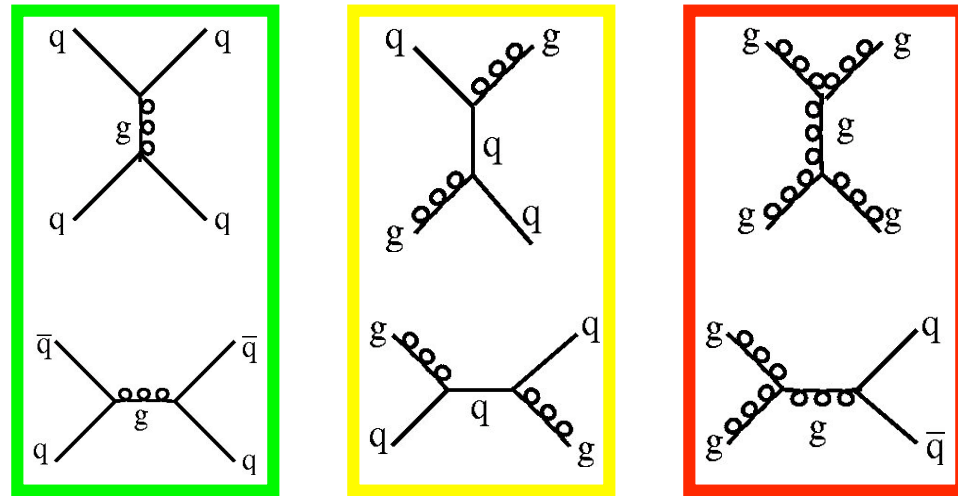
- Measure events with 0 interactions
 - Related to R_{pp}
- Normalize to measured inelastic pp cross section
 - Tevatron: 60.7+/-2.4 mb
- LHC: 70-120 mb



Jet Cross Sections

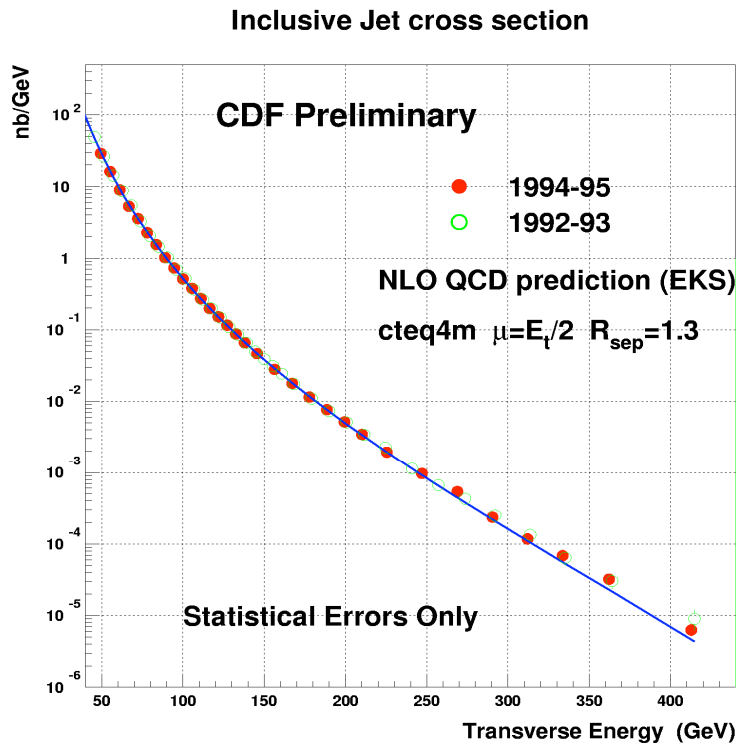


- Inclusive jets: processes qq, qg, gg

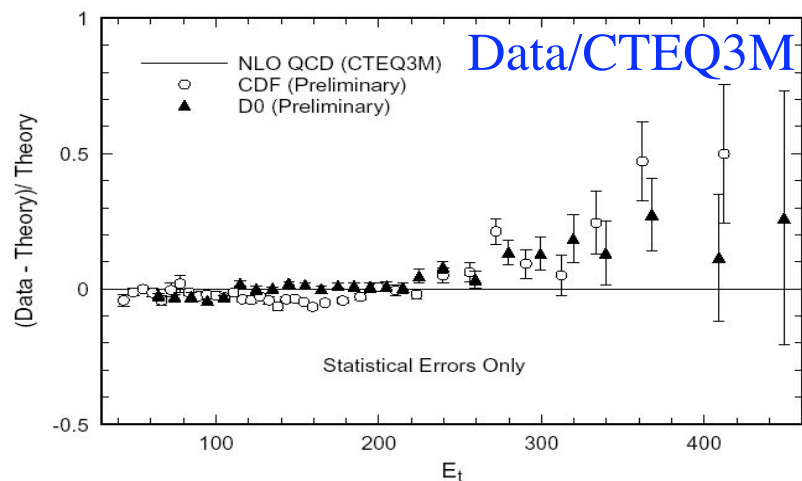


- Highest E_T probes shortest distances
 - Tevatron: $r_q < 10^{-18}$ m
 - LHC: $r_q < 10^{-19}$ m (?)
 - Could e.g. reveal substructure of quarks
- Tests perturbative QCD at highest energies

Jet Cross Section History

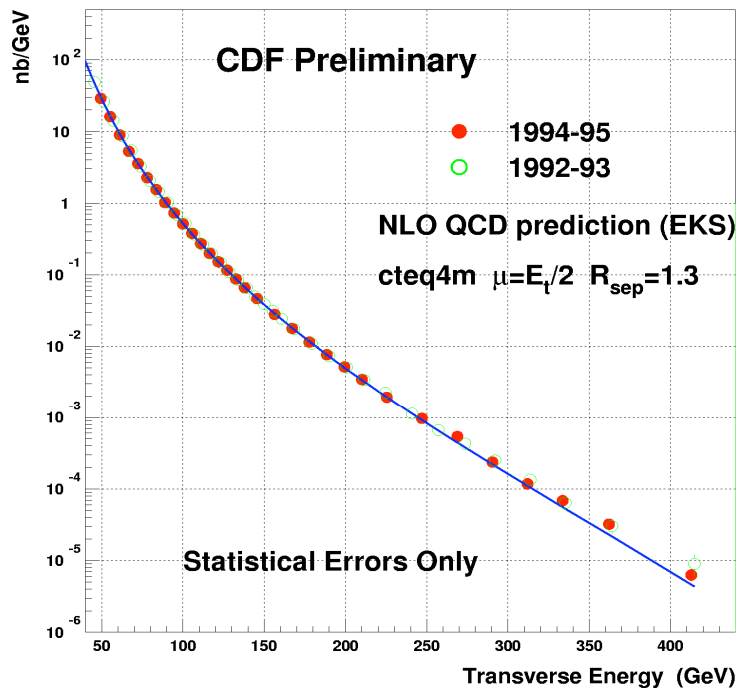


- Run I (1996):
 - Excess at high E_T
 - Could be signal for quark substructure?!?



Jet Cross Section History

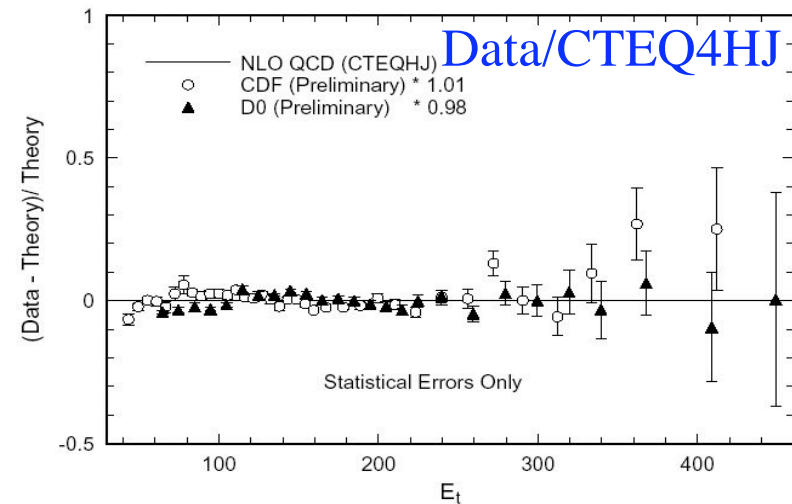
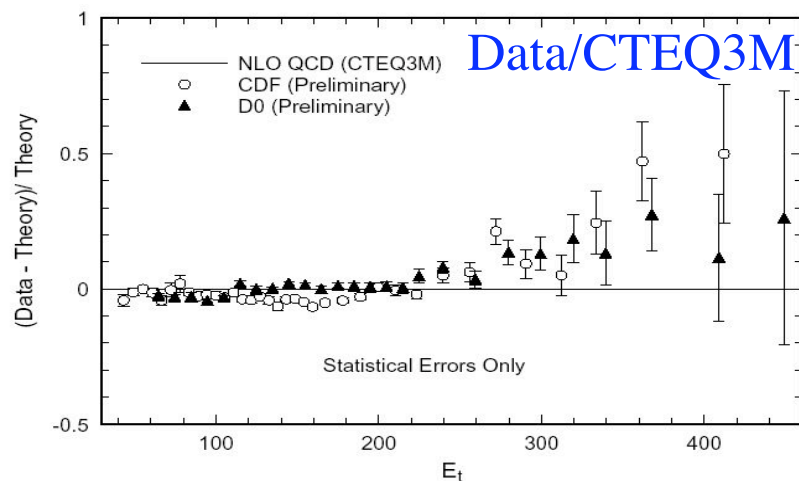
Inclusive Jet cross section



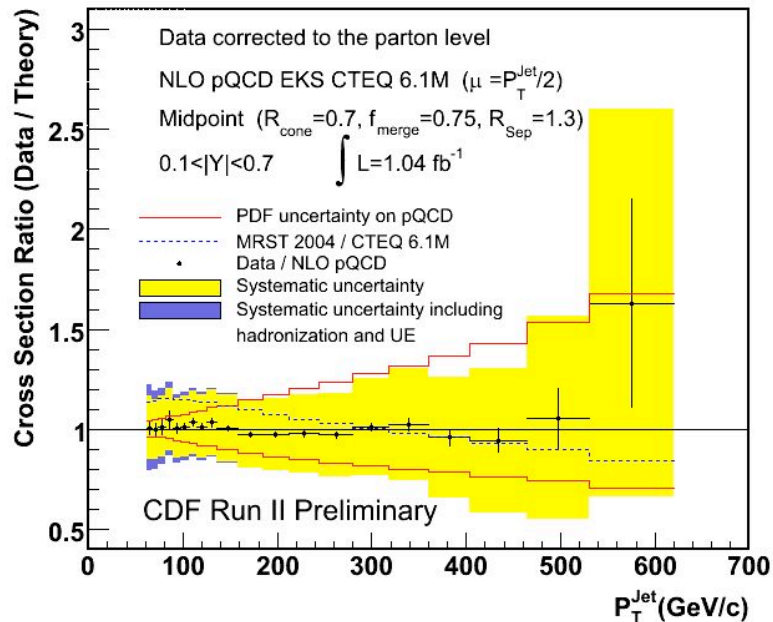
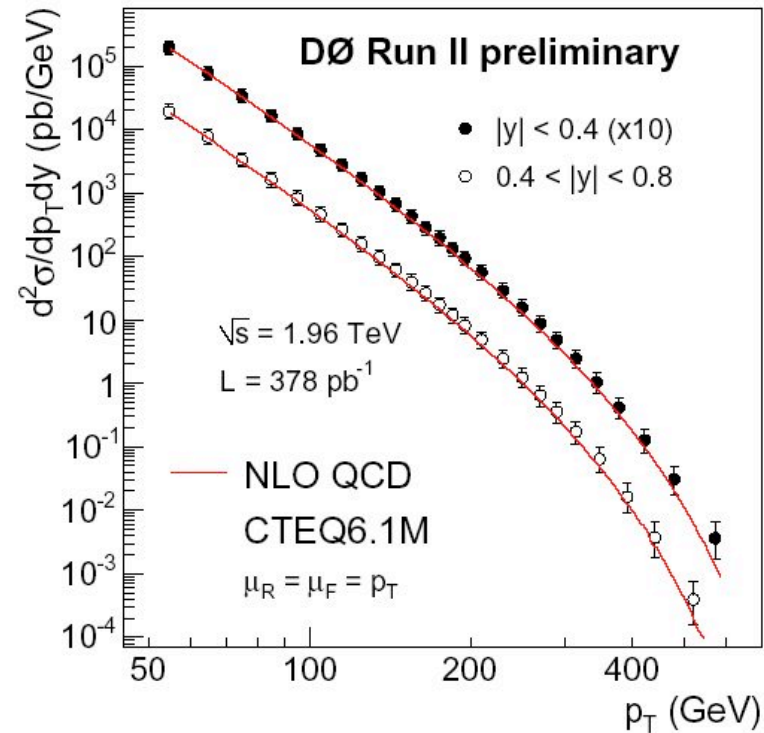
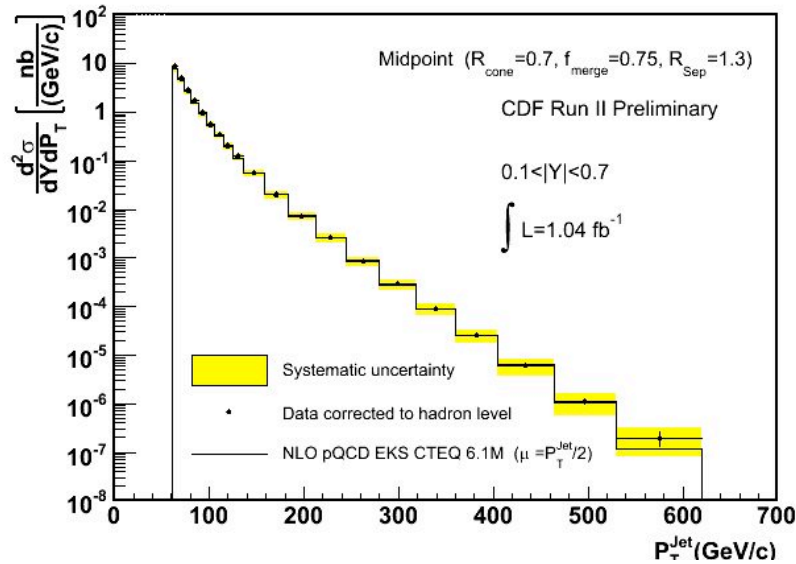
- Since Run I:

- Revision of parton density functions

- Gluon is uncertain at high x
- Including these data describes data well

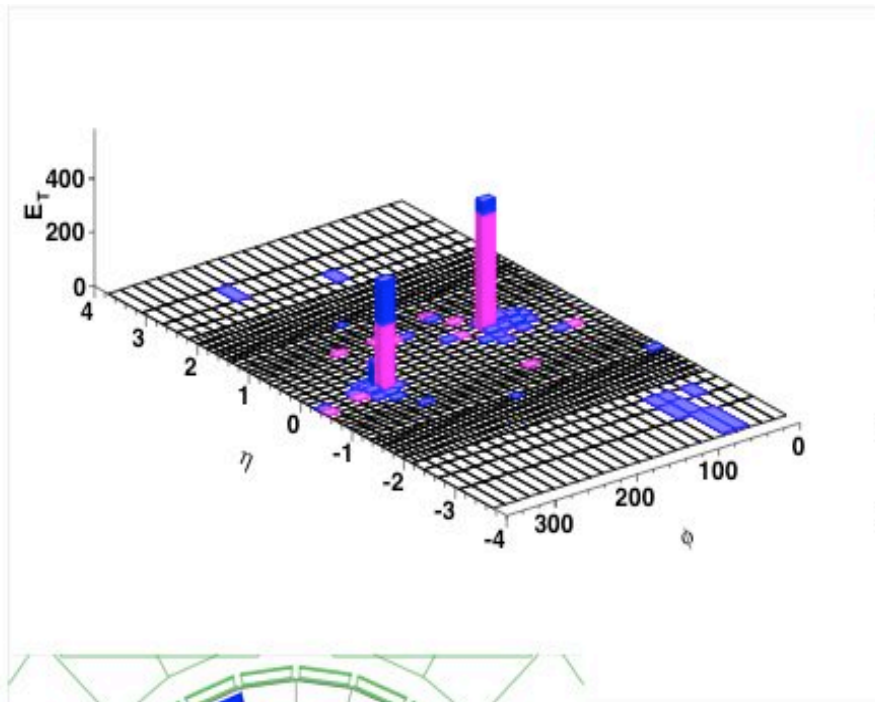


Jet Cross Sections in Run II



- Excellent agreement with QCD calculation over 8 orders of magnitude!
- No excess any more at high E_T
 - Large pdf uncertainties will be constrained by these data

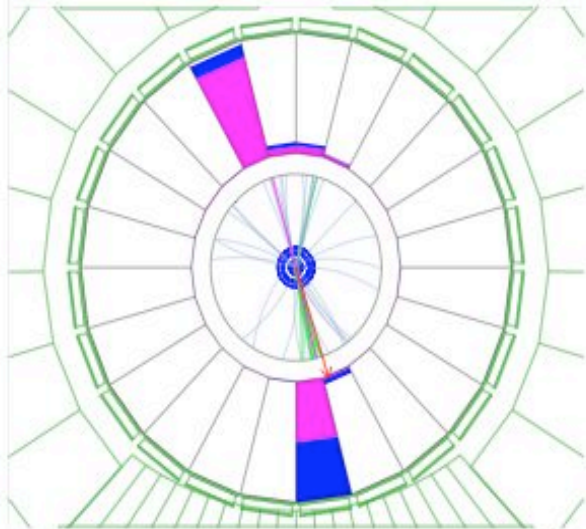
High Mass Dijet Event: $M=1.4$ TeV



CDF Run II Preliminary

Jet E_{T1} = 666 GeV (corr)
583 GeV (raw)
 η_{1} = 0.31 (detector)
0.43 (corr z)

Jet E_{T2} = 633 GeV (corr)
546 GeV (raw)
 η_{2} = -0.30 (detector)
-0.19 (corr z)



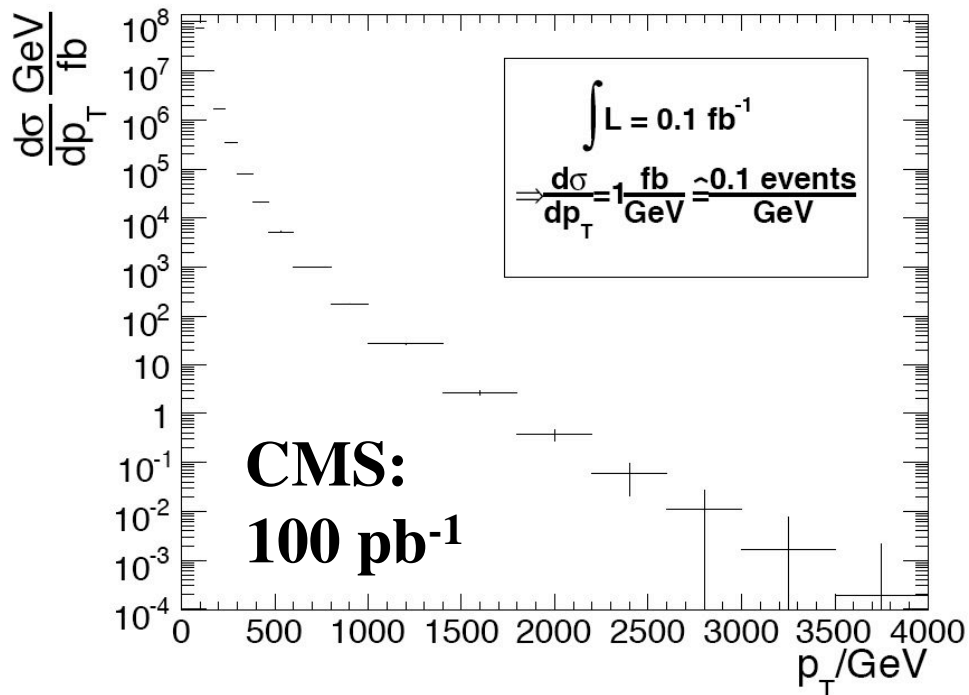
Run 152507
Event 1222318

DiJet Mass = 1364 GeV (corr)

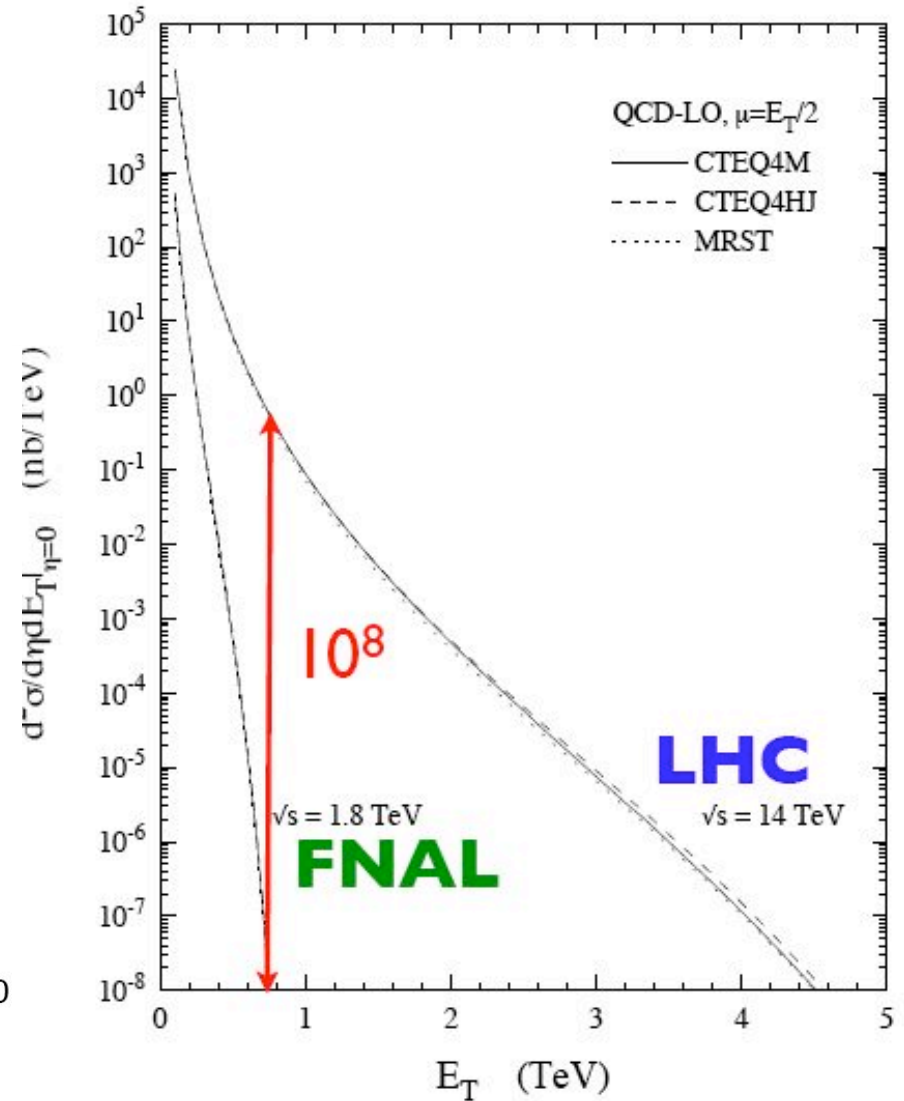
z vertex = -25 cm

Jets at the LHC

- Much higher rates than at the Tevatron
 - Reach ~3 TeV already with 100 pb⁻¹ of LHC data

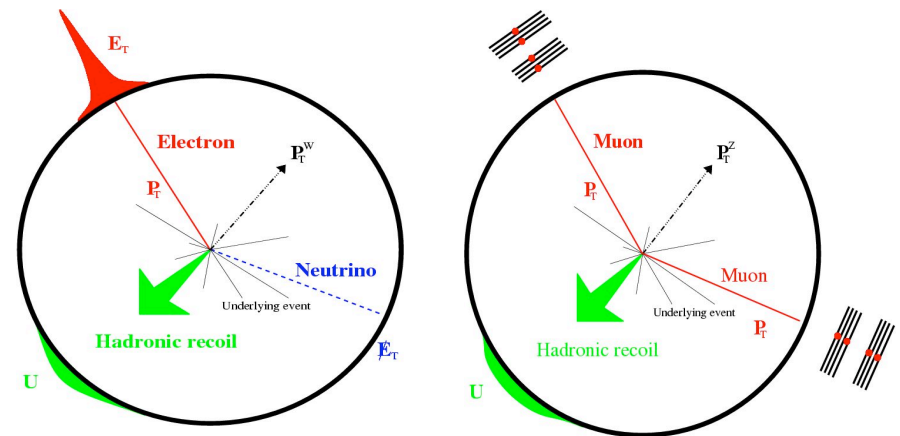
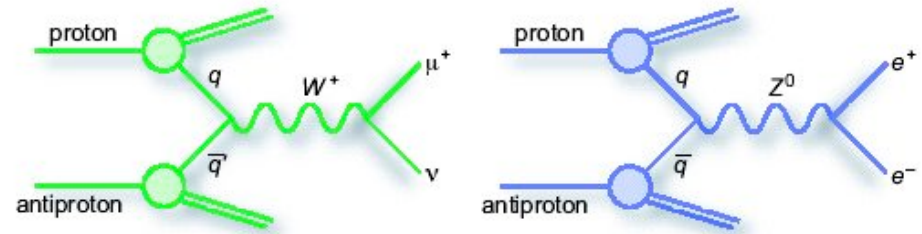


Jet Cross Section



W and Z Bosons

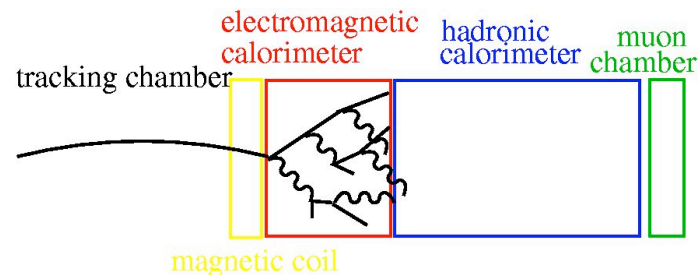
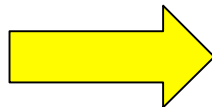
- Focus on leptonic decays:
 - Hadronic decays ~impossible due to enormous QCD dijet background
- Selection:
 - Z:
 - Two leptons $p_T > 20$ GeV
 - Electron, muon, tau
 - W:
 - One lepton $p_T > 20$ GeV
 - Large imbalance in transverse momentum
 - Missing $E_T > 20$ GeV
 - Signature of undetected particle (neutrino)
- Excellent calibration signal for many purposes:
 - Electron energy scale
 - Track momentum scale
 - Lepton ID and trigger efficiencies
 - Missing E_T resolution
 - Luminosity ...



Lepton Identification

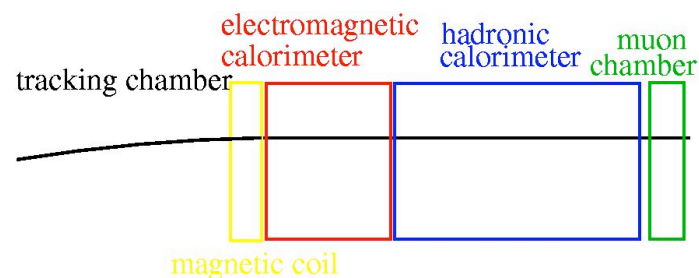
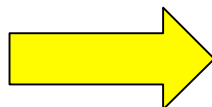
■ Electrons:

- compact electromagnetic cluster in calorimeter
- Matched to track



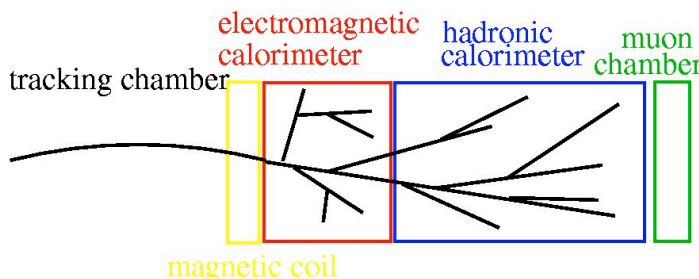
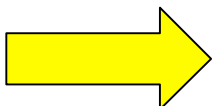
■ Muons:

- Track in the muon chambers
- Matched to track



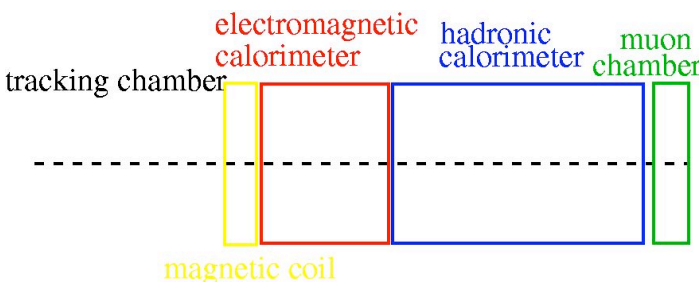
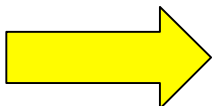
■ Taus:

- Narrow jet
- Matched to one or three tracks



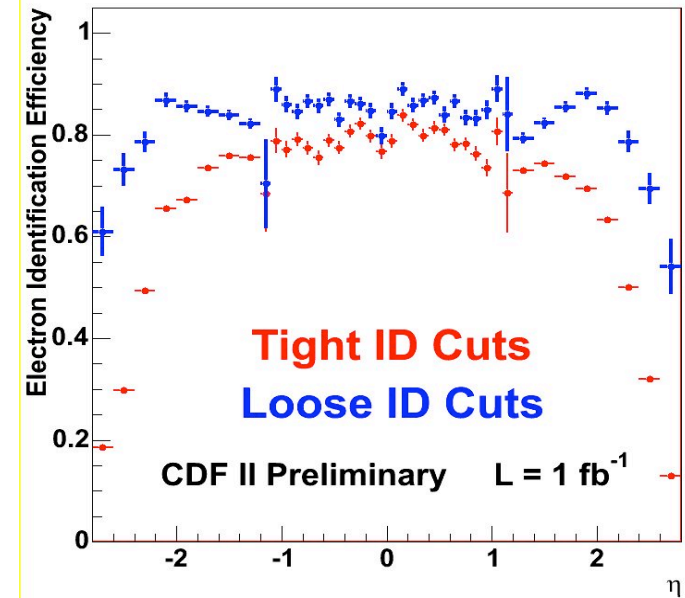
■ Neutrinos:

- Imbalance in transverse momentum
- Inferred from total transverse energy measured in detector
- More on this in Lecture 4

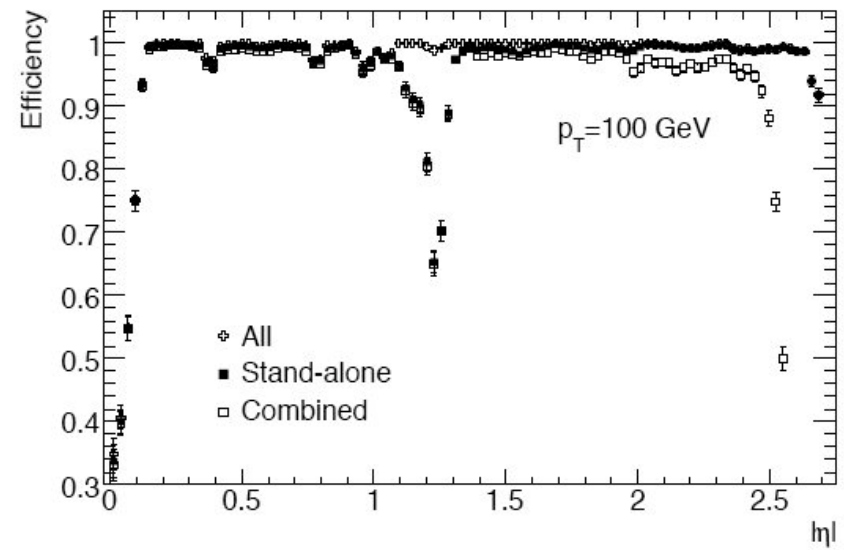


Electron and Muon Identification

- Desire:
 - High efficiency for isolated electrons
 - Low misidentification of jets



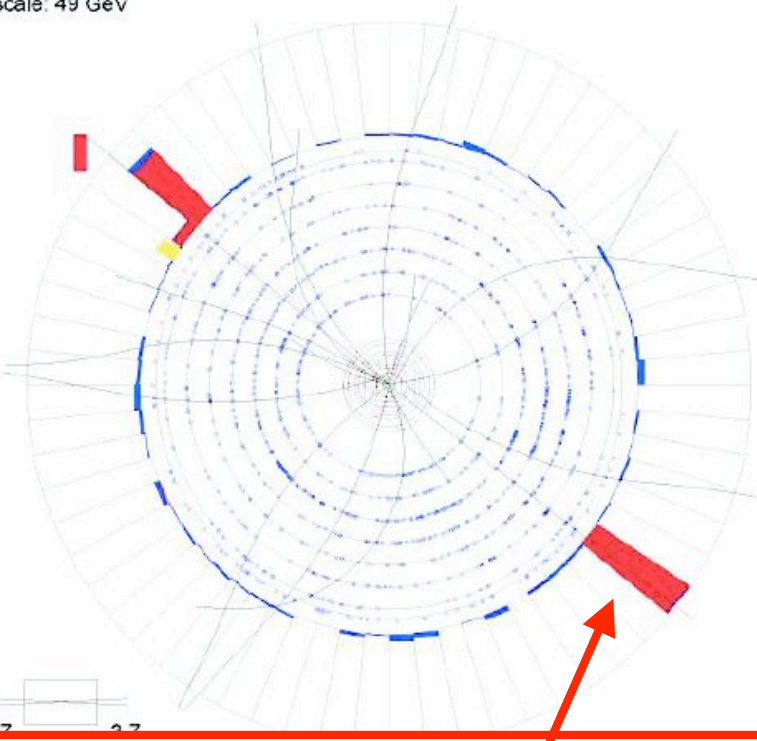
- Performance:
 - Efficiency:
 - 60-100% depending on $|\eta|$
 - Measured using Z's



Electrons and Jets

Run 166892 Evt 2775140 Sun Oct 27 03:15:49 2002

ET scale: 49 GeV

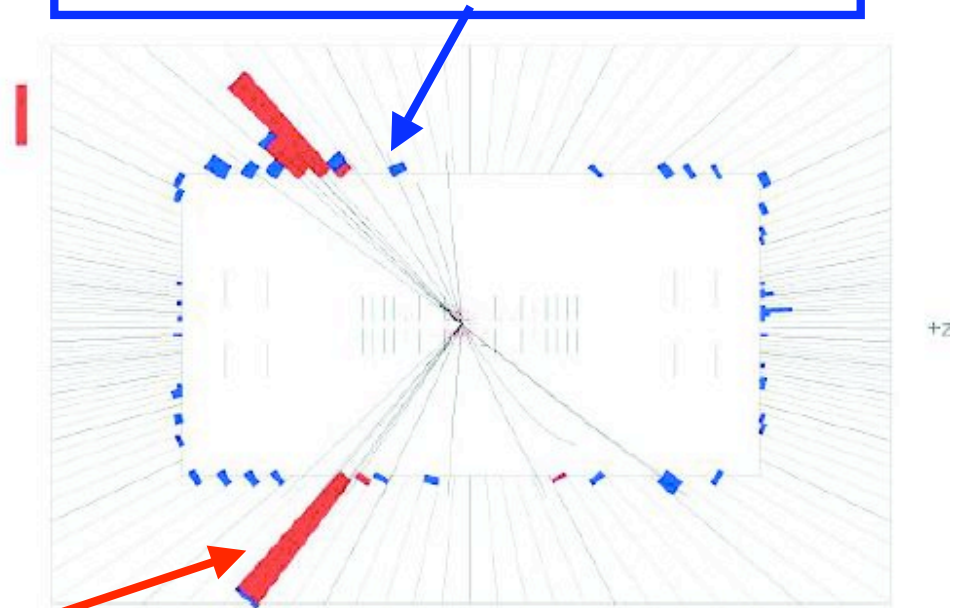


Electromagnetic Calorimeter Energy

Run 166892 Evt 3223863 Sun Oct 27 03:43:08 2002

E scale: 20 GeV

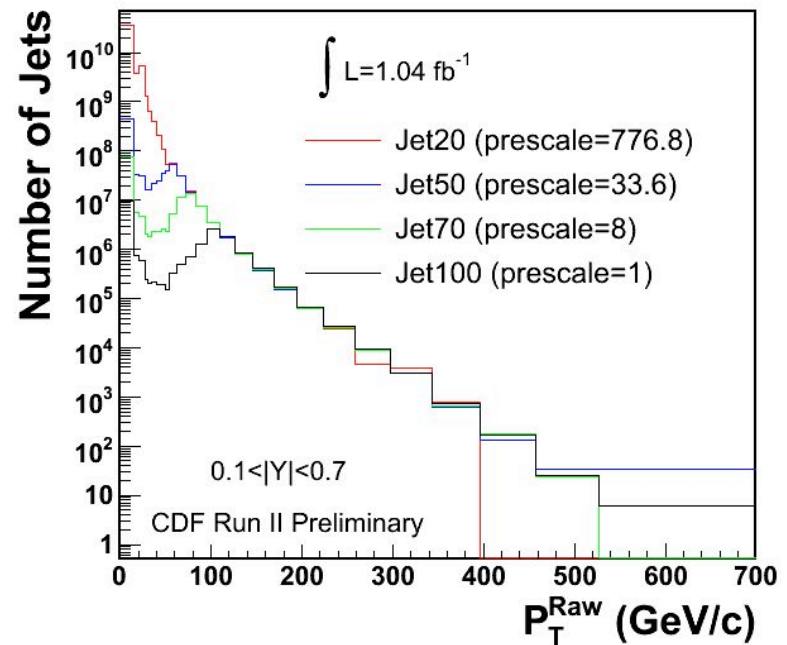
Hadronic Calorimeter Energy



- Jets can look like electrons, e.g.:
 - photon conversions from π^0 's: ~13% of photons convert (in CDF)
 - early showering charged pions
- And there are lots of jets!!!

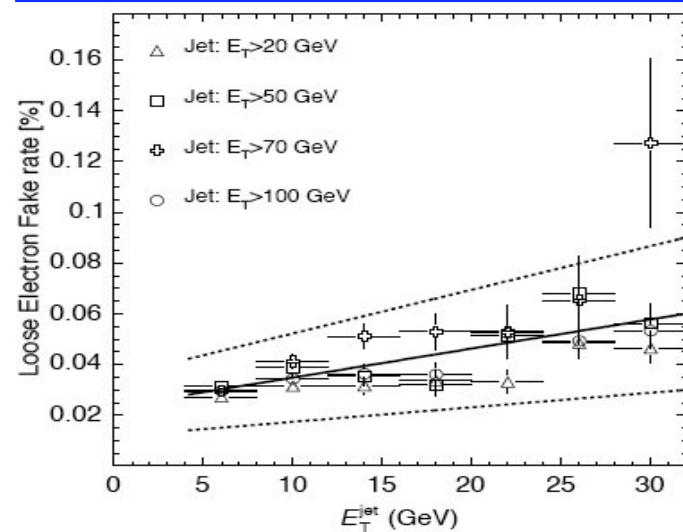
Jets faking Electrons

- Jets can pass electron ID cuts,
 - Mostly due to
 - early showering charged pions
 - Conversions: $\pi^0 \rightarrow \gamma\gamma \rightarrow ee + X$
 - ♣ Semileptonic b-decays
 - ♣ Difficult to model in MC
 - Hard fragmentation
 - Detailed simulation of calorimeter and tracking volume
- Measured in inclusive jet data at various E_T thresholds
 - Prompt electron content negligible:
 - $N_{\text{jet}} \sim 10$ billion at 50 GeV!
 - Fake rate per jet:
 - CDF, tight cuts: 1/10000
 - ATLAS, tight cuts: 1/80000
 - Typical uncertainties 50%



Jets faking “loose” electrons

Fake Rate (%)



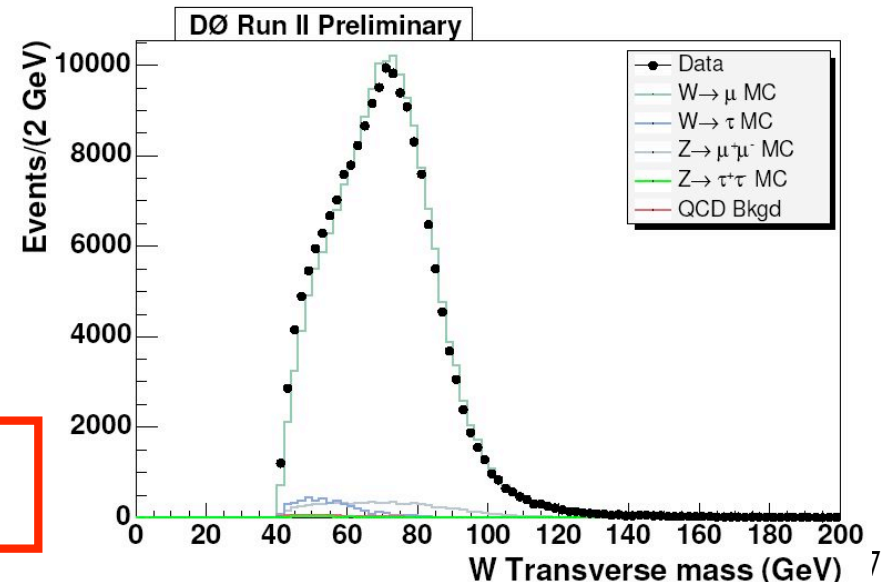
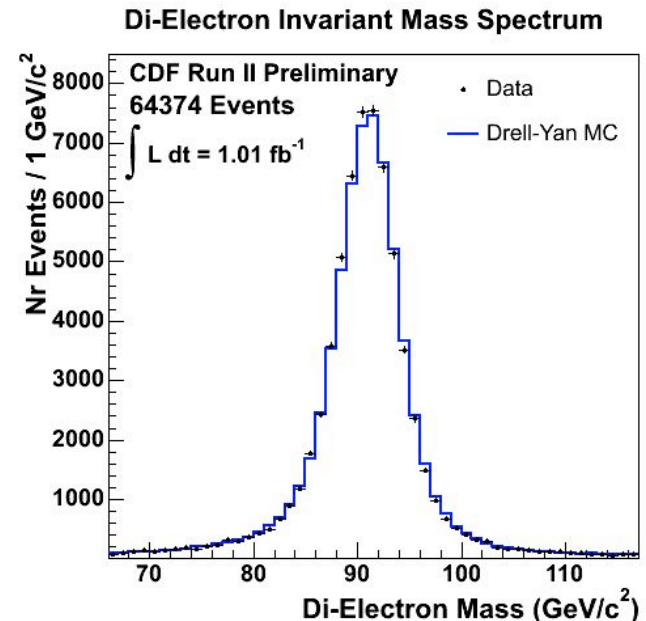
W's and Z's

- **Z** mass reconstruction
 - Invariant mass of two leptons

$$m = \sqrt{(E_1 + E_2)^2 - (\vec{p}_1 + \vec{p}_2)^2}$$

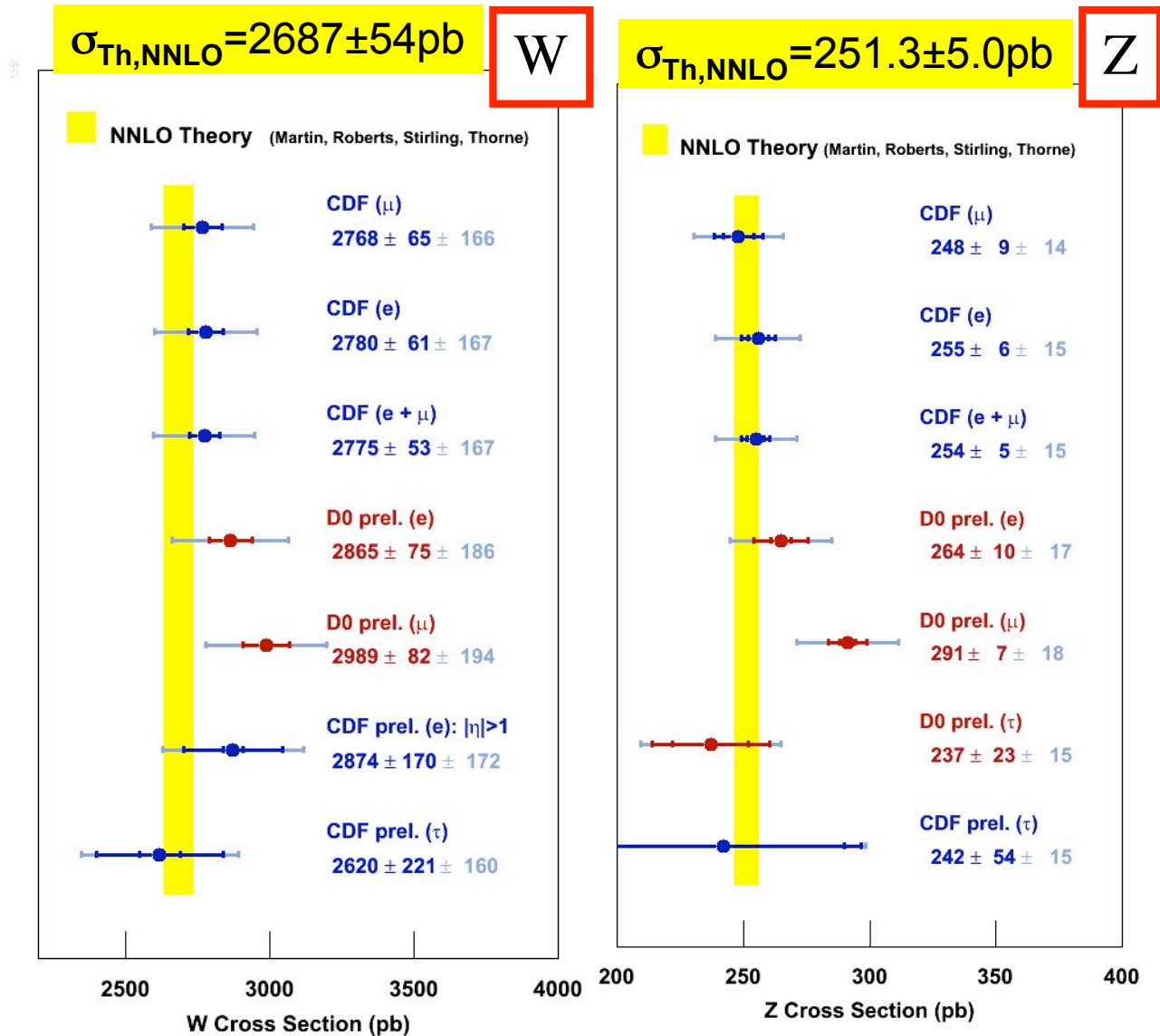
- Sets electron energy scale by comparison to LEP measured value
-
- **W** mass reconstruction
 - Do not know neutrino p_z
 - No full mass reconstruction possible
 - **Transverse mass**:

$$m_T = \sqrt{|p_T^\ell|^2 + |p_T^\nu|^2 - (\vec{p}_T^\ell + \vec{p}_T^\nu)^2}$$

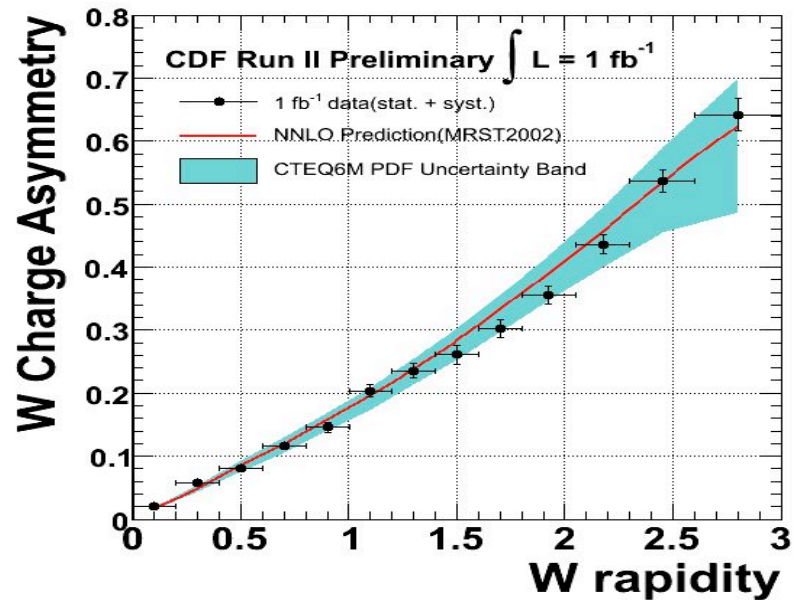
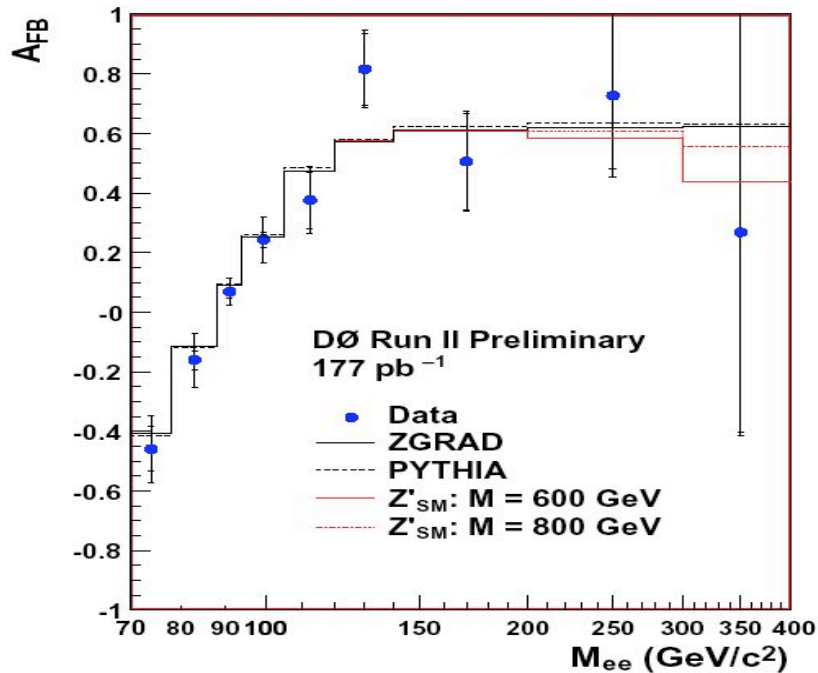
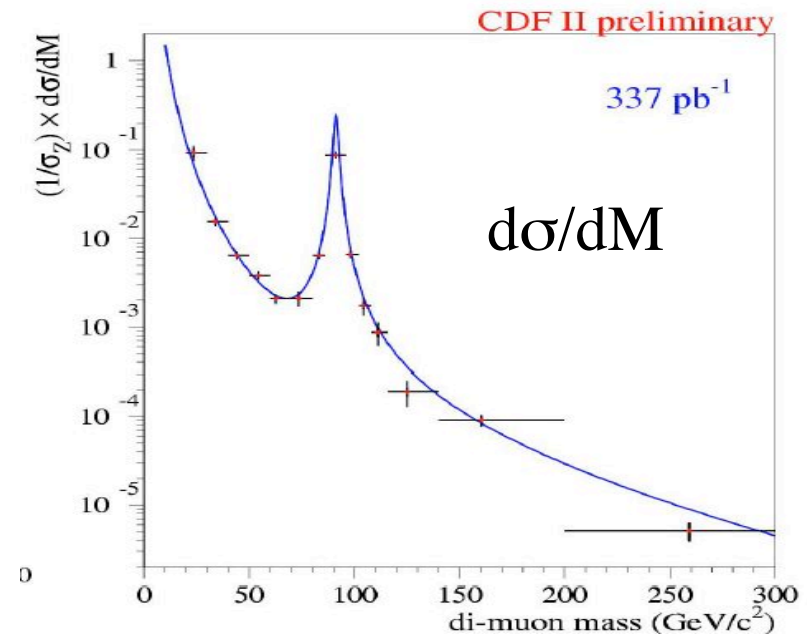
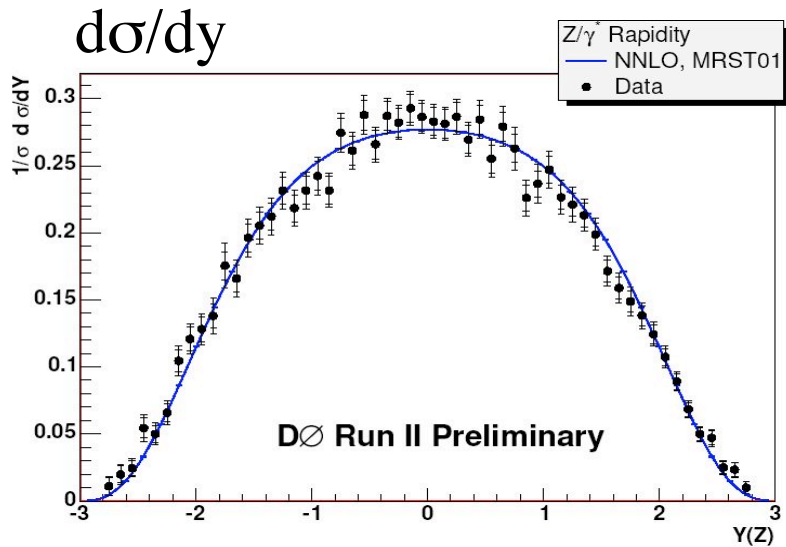


Tevatron W and Z Cross Section Results

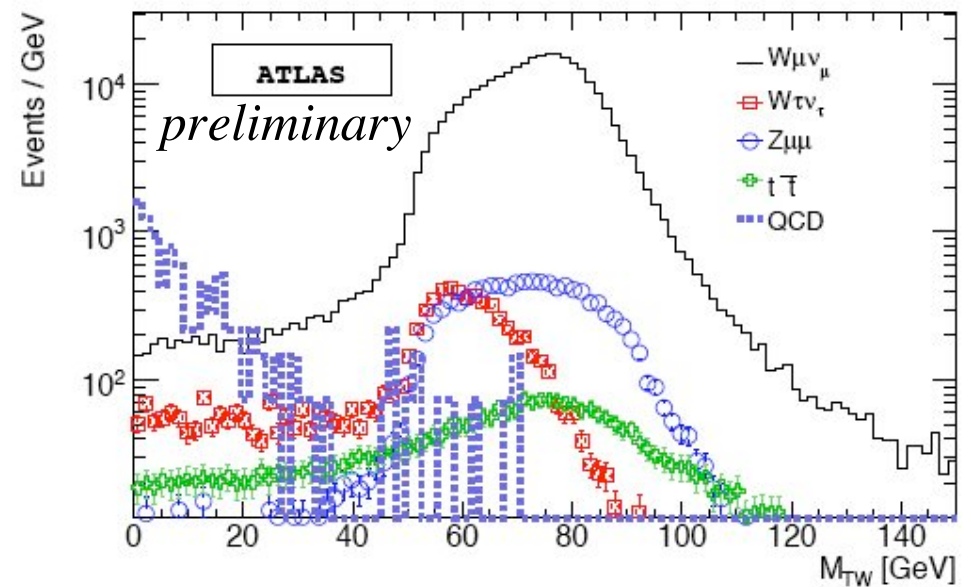
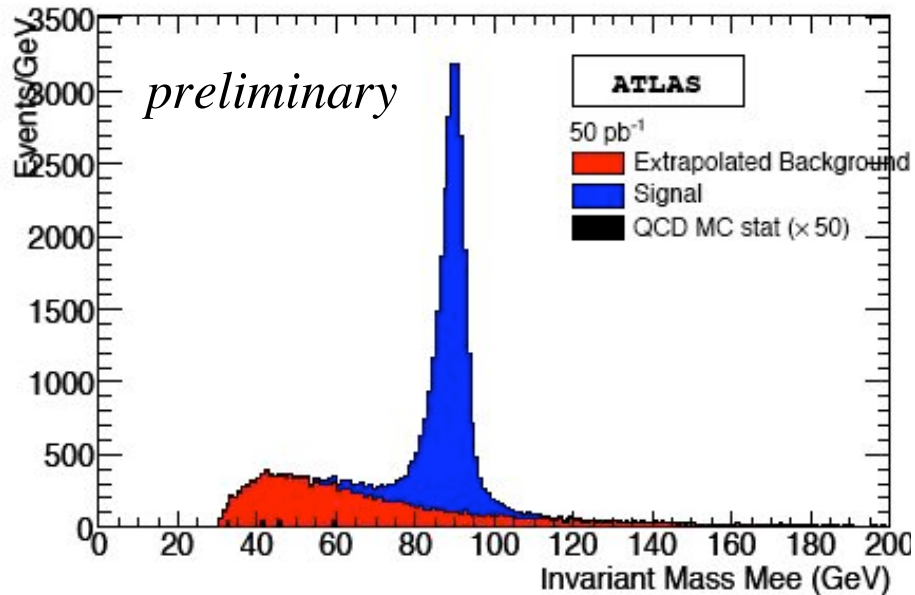
- Uncertainties:
 - Experimental: 2%
 - Theoretical: 2%
 - Luminosity: 6%
- Can we use these processes to normalize luminosity?
 - Is theory reliable enough?



More Differential W/Z Measurements



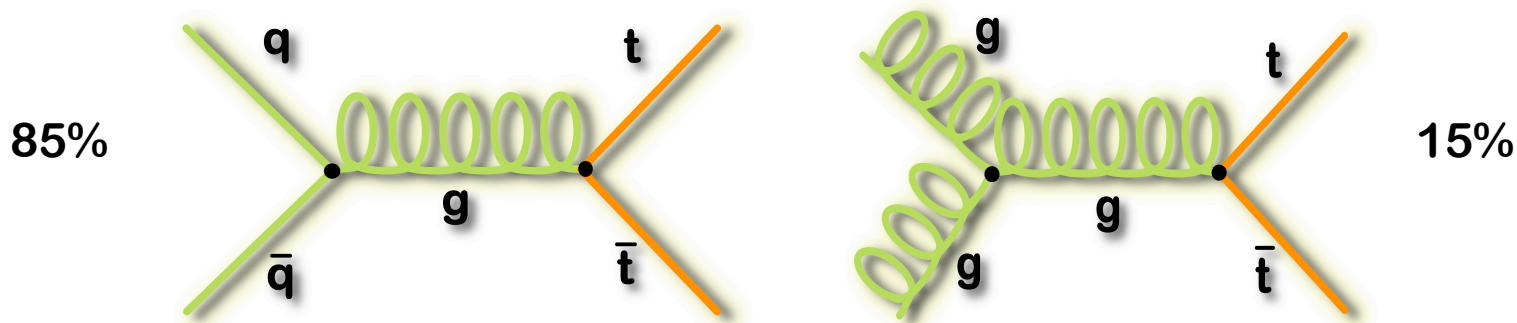
LHC signals of W's and Z's with 50 pb⁻¹



- 50 pb⁻¹ yield clean signals of W's and Z's
- Experimental precision
 - ~5% for 50 pb⁻¹ ⊕ ~10% (luminosity)
 - ~2.5% for 1 fb⁻¹ ⊕ ~10% (luminosity)

Top Quark Production and Decay

- At Tevatron, mainly produced in pairs via the strong interaction

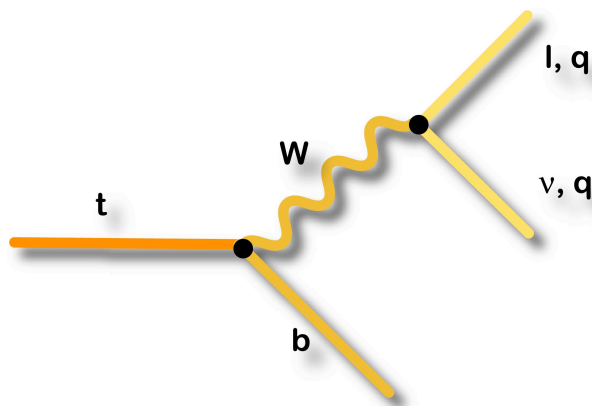


- Decay via the electroweak interactions $Br(t \rightarrow Wb) \sim 100\%$
Final state is characterized by the decay of the W boson

Dilepton

Lepton+Jets

All-Jets



Different sensitivity and challenges in each channel

How to identify the top quark

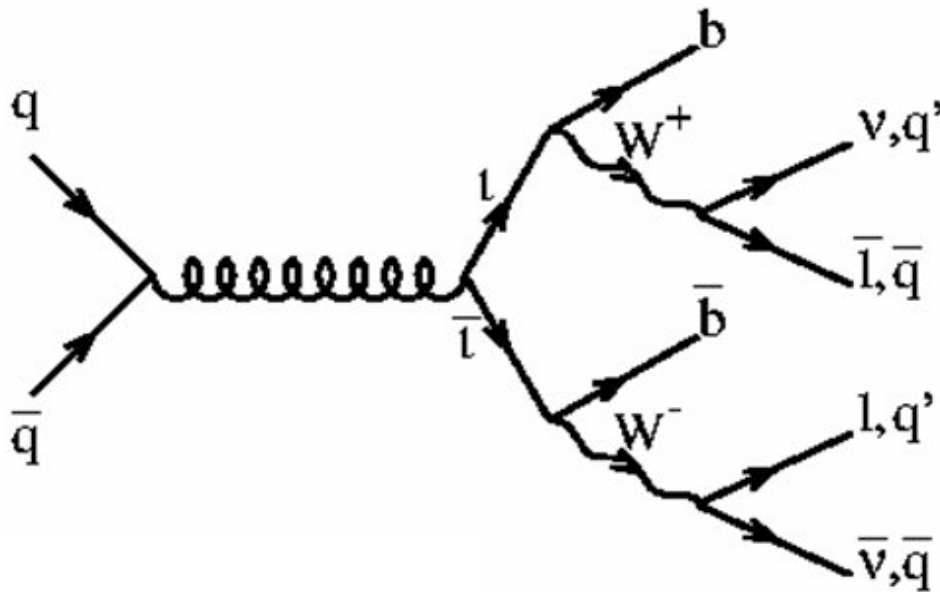
SM: $t\bar{t}$ pair production, $\text{Br}(t \rightarrow bW) = 100\%$, $\text{Br}(W \rightarrow l\nu) = 1/9 = 11\%$

dilepton (4/81) 2 leptons + 2 jets + missing E_T

l+jets (24/81) 1 lepton + 4 jets + missing E_T

fully hadronic (36/81) 6 jets

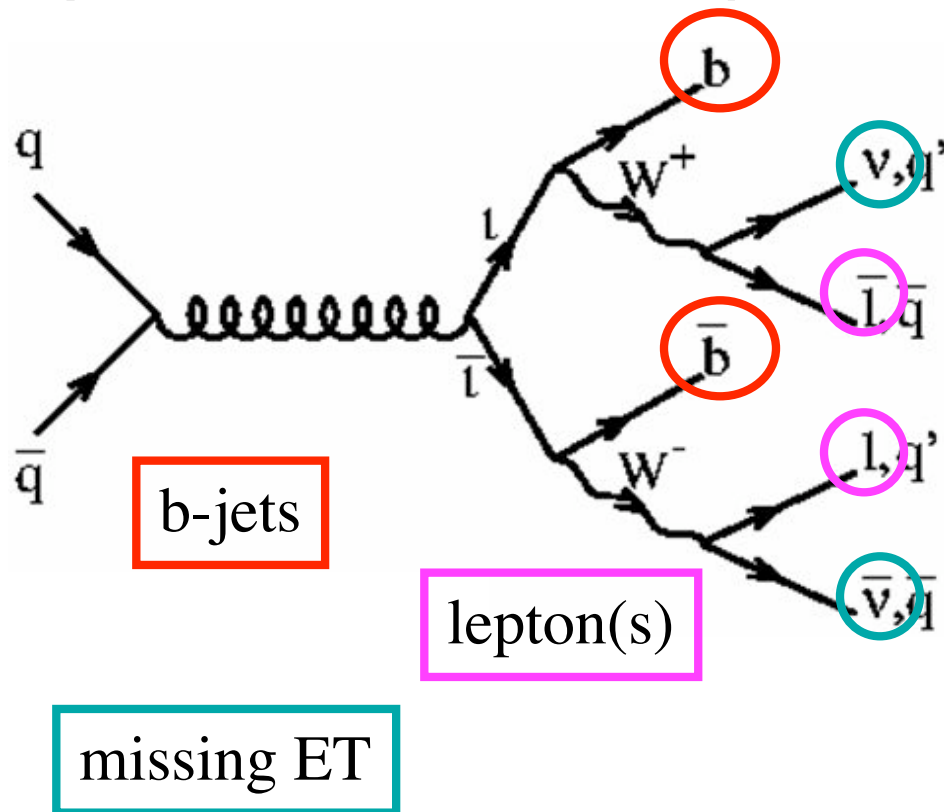
(here: $l = e, \mu$)



How to identify the top quark

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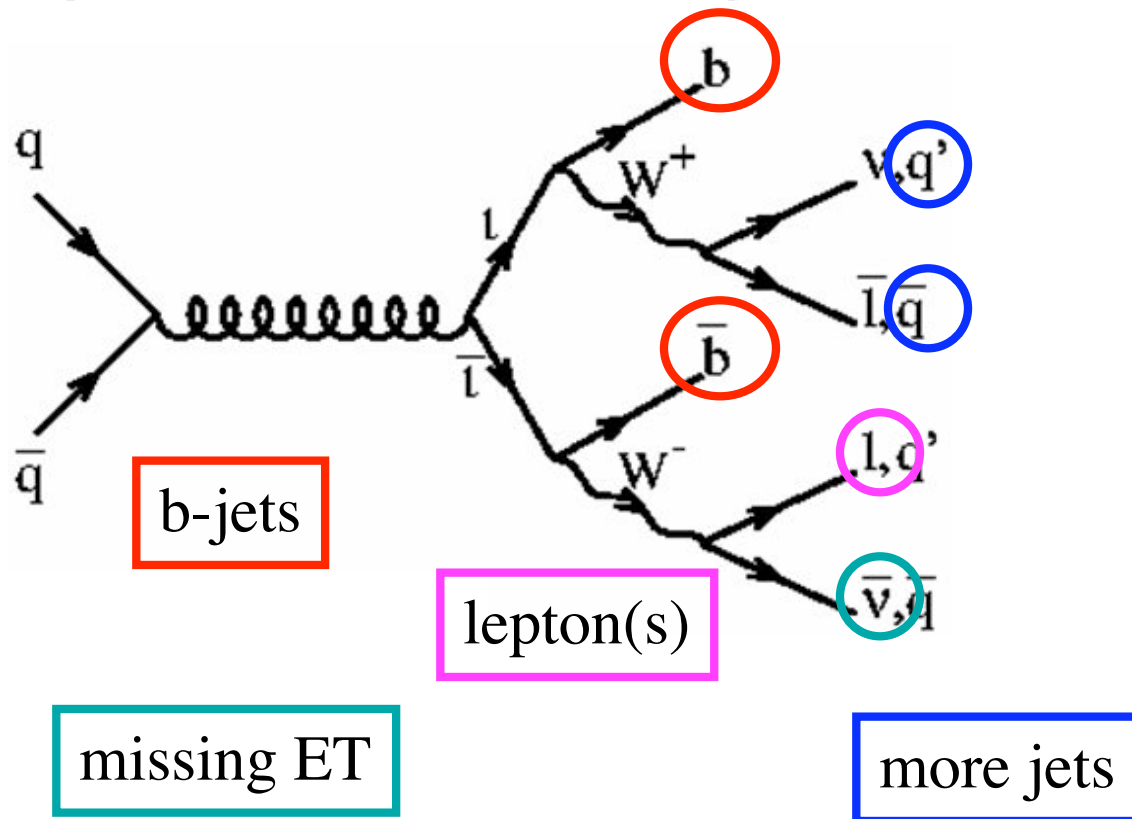
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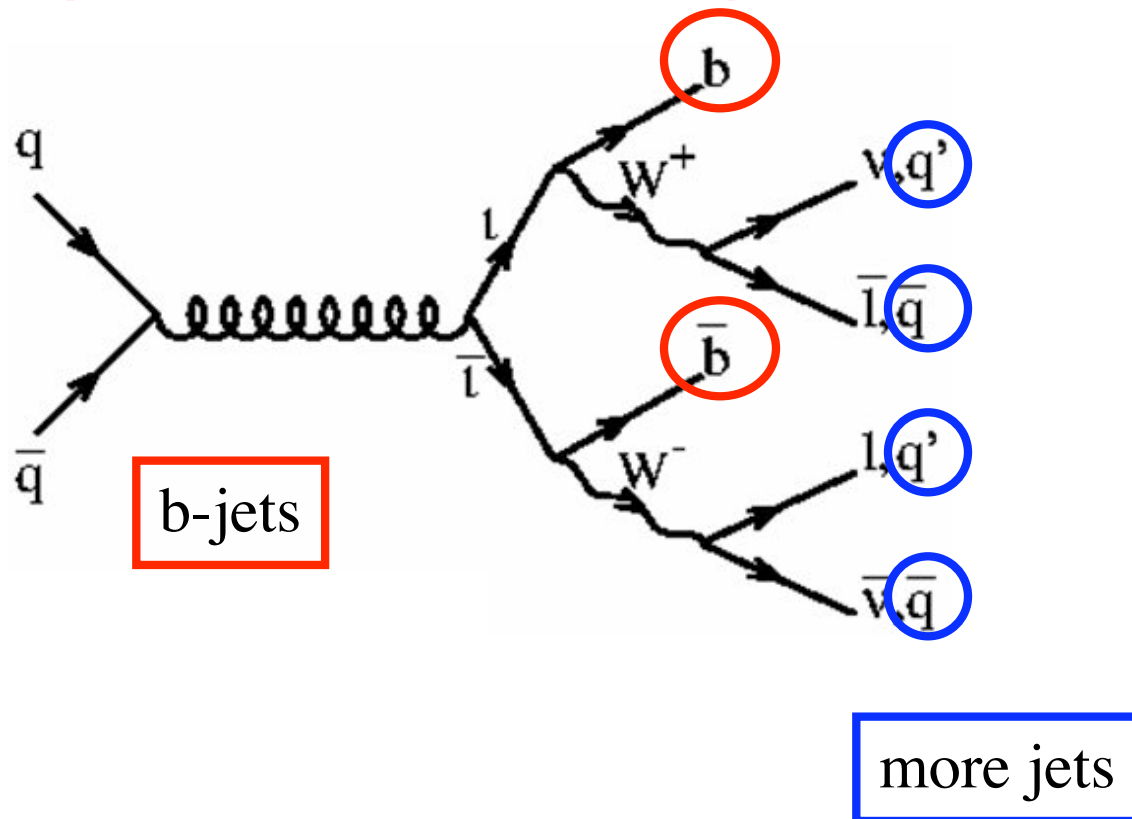
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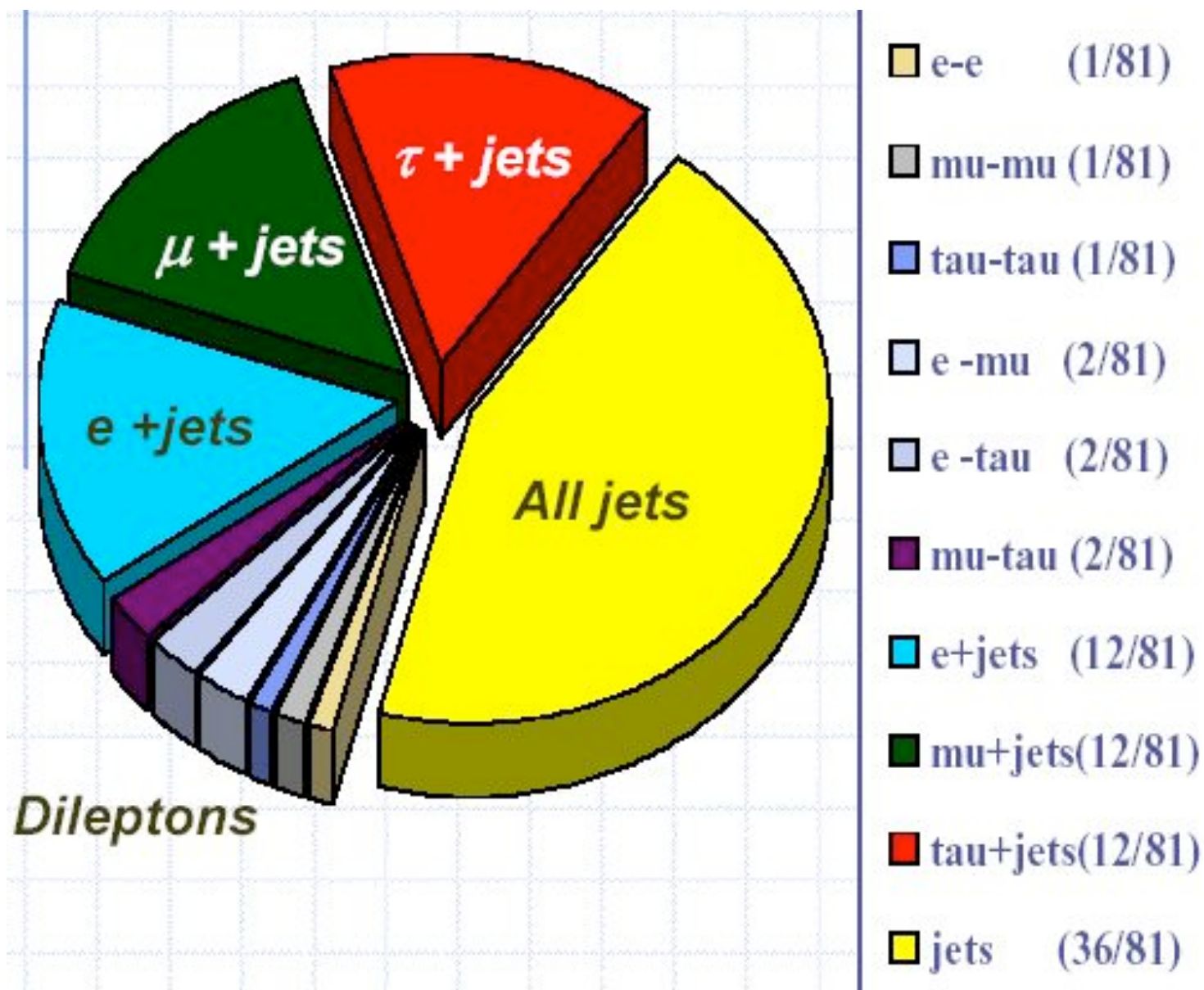
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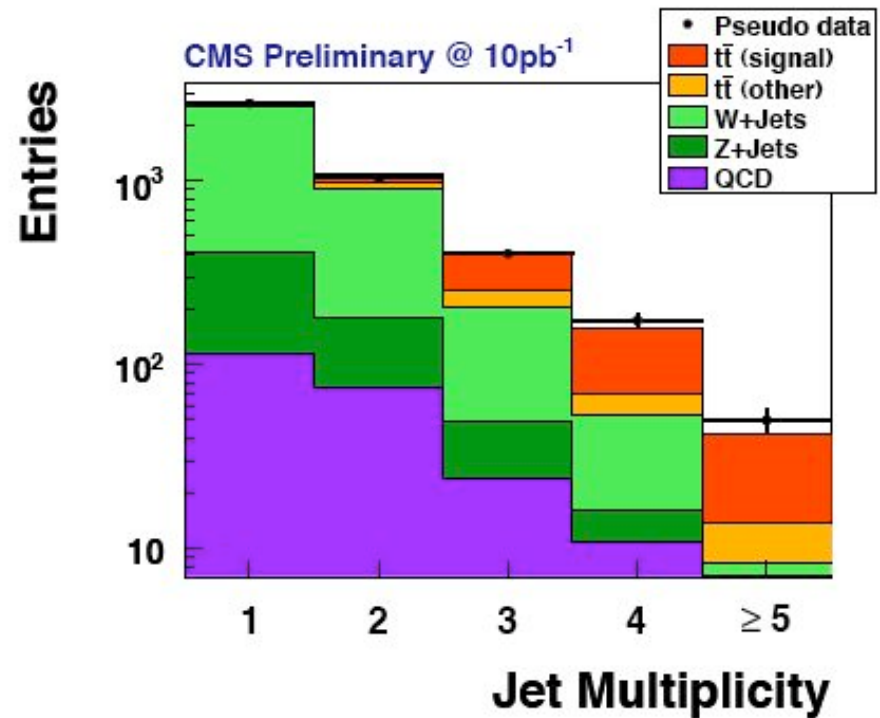
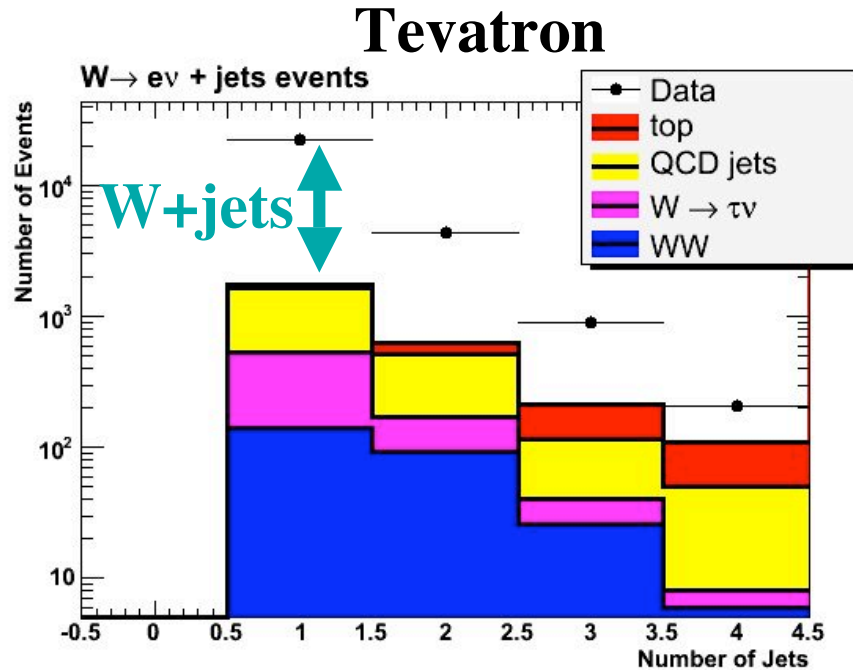
fully hadronic (36/81) 6 jets



Top Event Categories

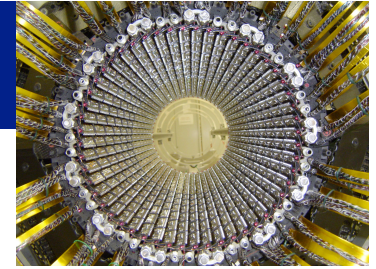


Finding the Top at Tevatron and LHC without b-quark identification

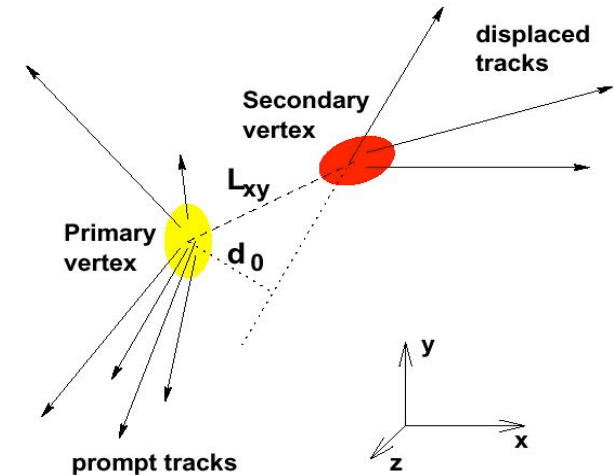


- Tevatron:
 - Top is overwhelmed by backgrounds:
 - Even for 4 jets the top fraction is only 30%
 - Use b-jets to purify sample
- LHC
 - Signal clear even without b-tagging: $S/B > 1.5$

Finding the b-jets

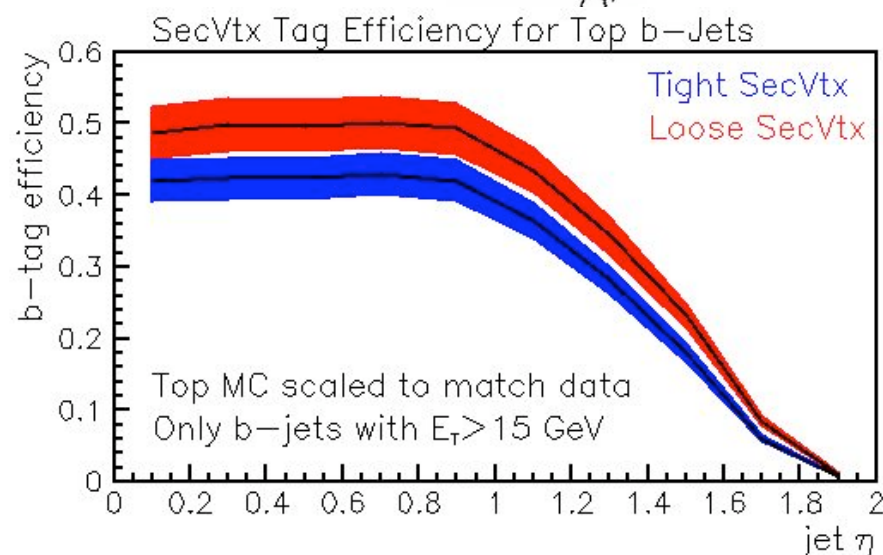
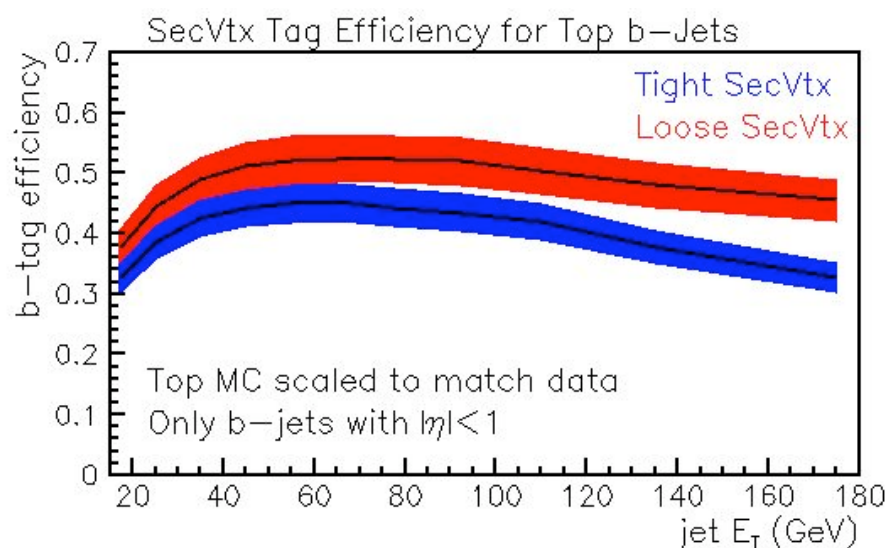
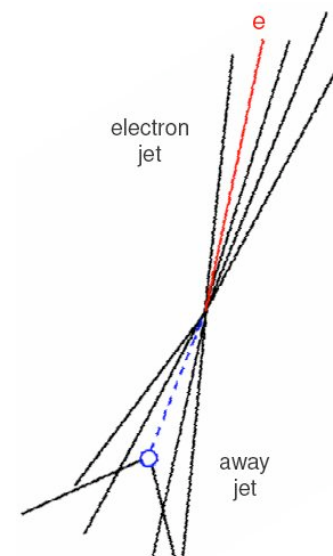


- Exploit large lifetime of the b-hadron
 - B-hadron flies before it decays: $d=c\tau$
 - Lifetime $\tau = 1.5 \text{ ps}^{-1}$
 - $d=c\tau = 460 \text{ }\mu\text{m}$
 - Can be resolved with silicon detector resolution
- Procedure “Secondary Vertex”:
 - reconstruct primary vertex:
 - resolution $\sim 30 \text{ }\mu\text{m}$
 - Search tracks inconsistent with primary vertex (large d_0):
 - Candidates for secondary vertex
 - See whether three or two of those intersect at one point
 - Require displacement of secondary from primary vertex
 - Form L_{xy} : transverse decay distance projected onto jet axis:
 - $L_{xy} > 0$: b-tag along the jet direction \Rightarrow real b-tag or mistag
 - $L_{xy} < 0$: b-tag opposite to jet direction \Rightarrow mistag!
 - Significance: e.g. $\delta L_{xy} / L_{xy} > 7$ (i.e. 7σ significant displacement)
- More sophisticated techniques exist



Characterise the B-tagger: Efficiency

- Efficiency of tagging a true b-jet
 - Use Data sample enriched in b-jets
 - Select jets with electron or muons
 - From semi-leptonic b-decay
 - Measure efficiency in data and MC



Achieve efficiency of about 40-50% at Tevatron
(can use top events directly to measure efficiency at LHC)

Characterise the B-tagger: Mistag rate

- Mistag Rate measurement:

- Probability of light quarks to be misidentified
- Use “negative” tags: $L_{xy} < 0$
 - Can only arise due to misreconstruction

- Mistag rate for $E_T = 50$ GeV:

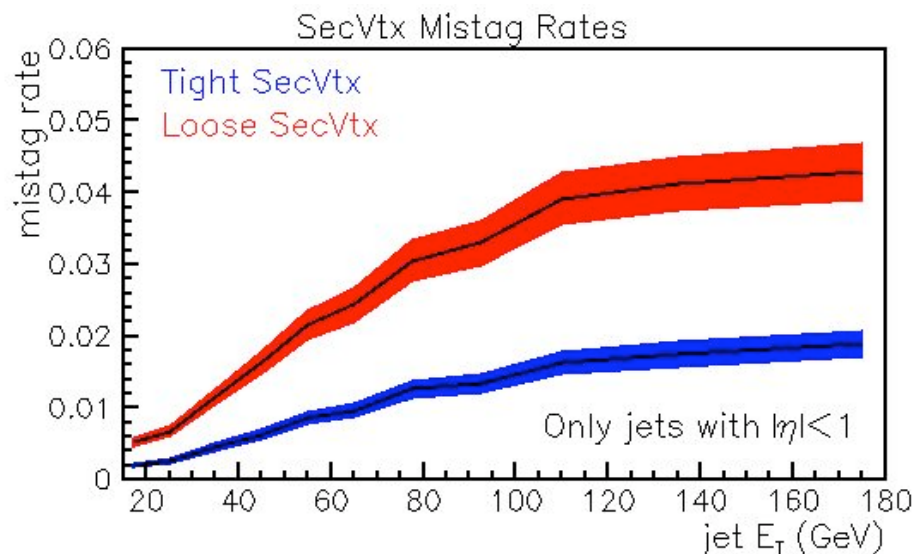
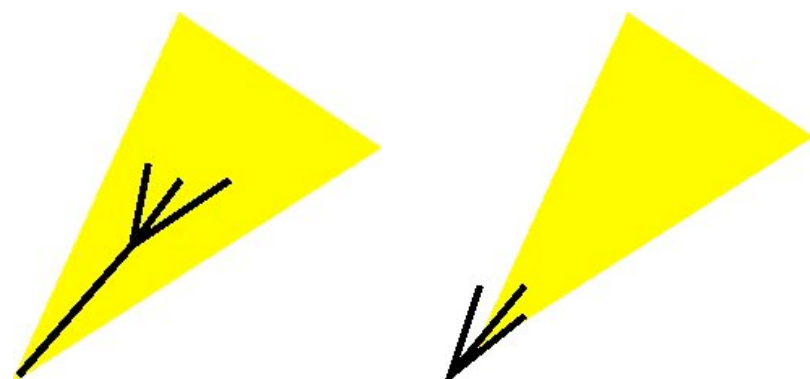
- Tight: 0.5% ($\epsilon = 43\%$)
- Loose: 2% ($\epsilon = 50\%$)

- Depending on physics analyses:

- Choose “tight” or “loose” tagging algorithm

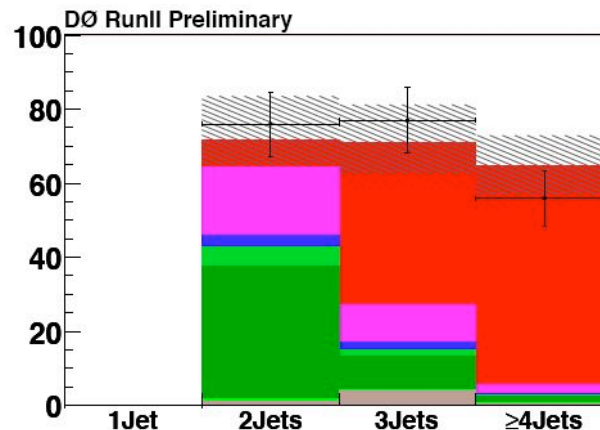
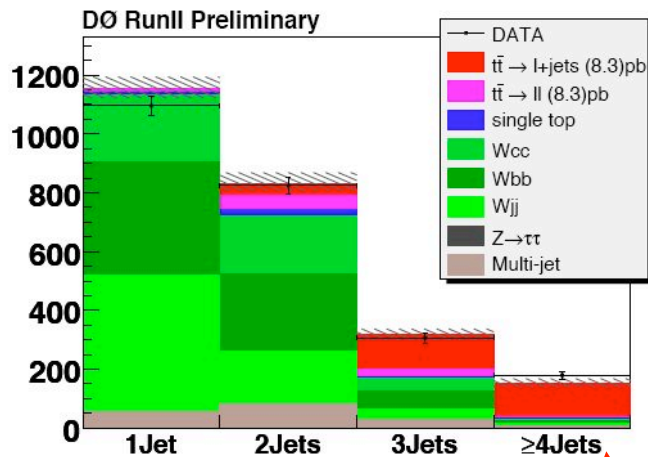
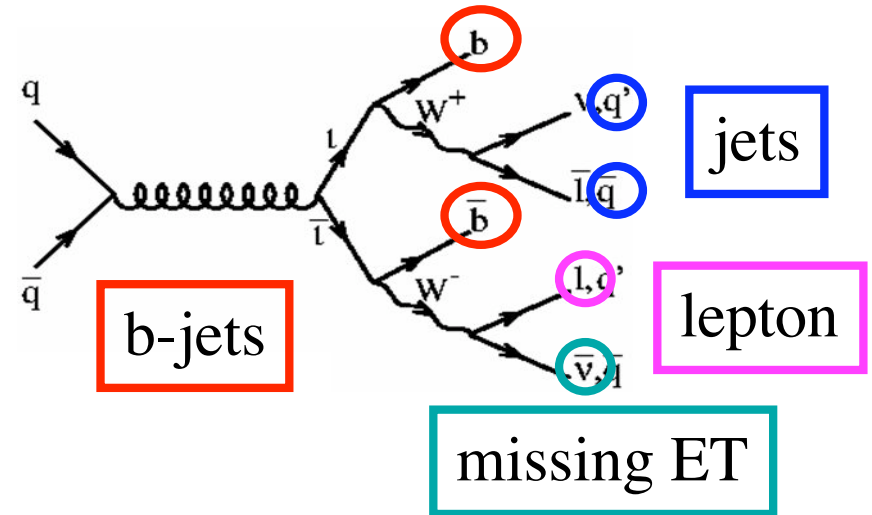
“positive” tag

“negative” tag



The Top Signal: Lepton + Jets

- Select:
 - 1 electron or muon
 - Large missing E_T
 - 1 or 2 b-tagged jets



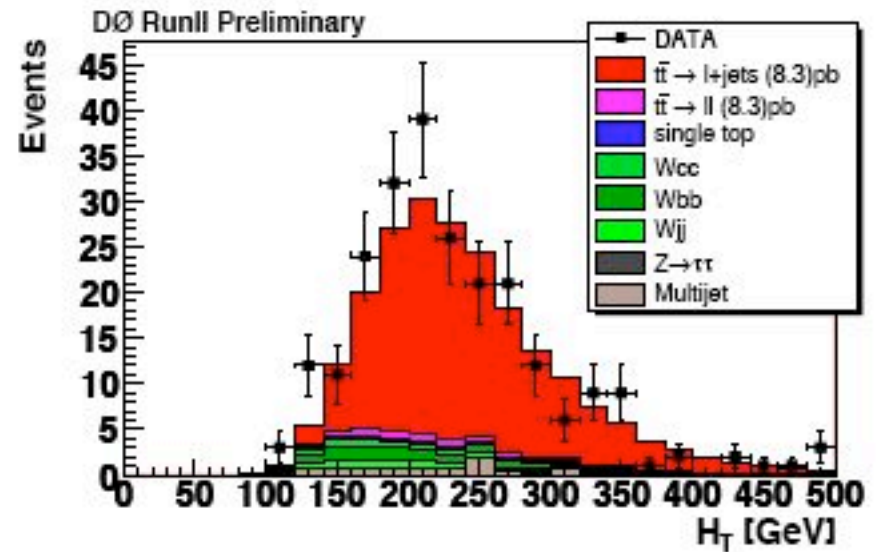
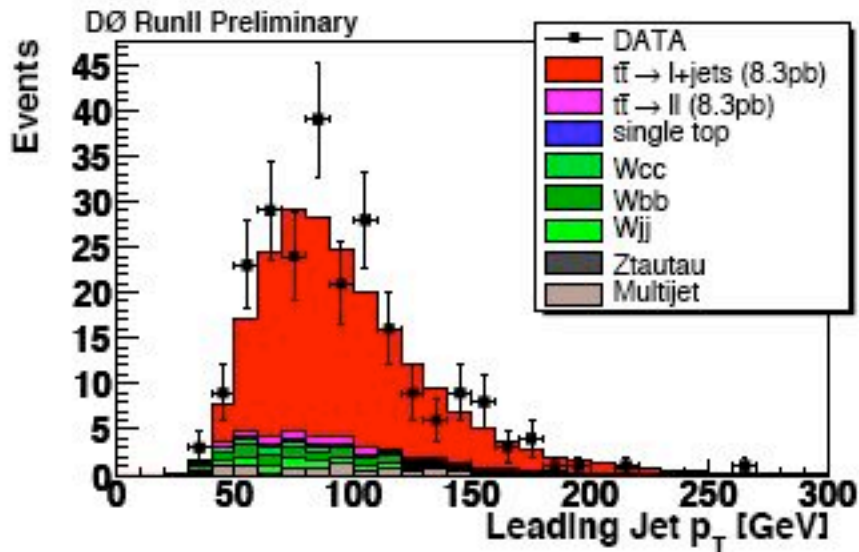
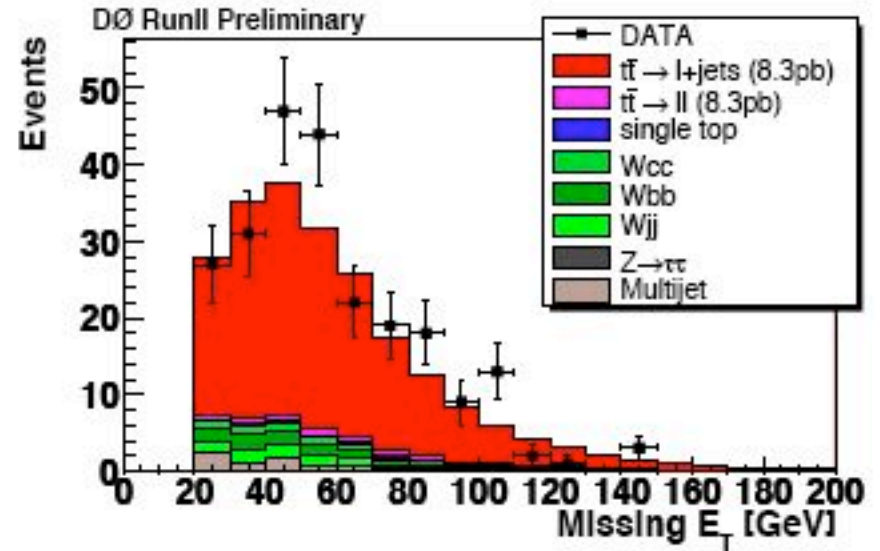
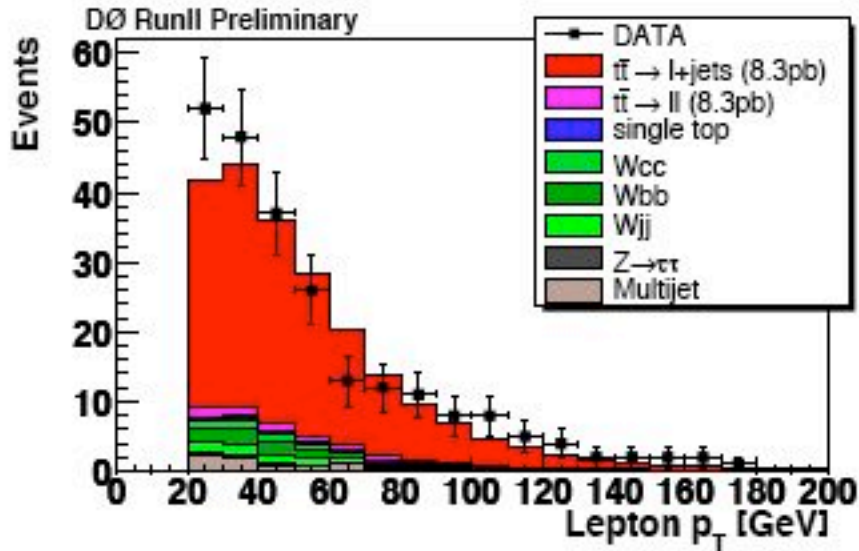
double-tagged events, nearly no background

Check backgrounds

Top Signal

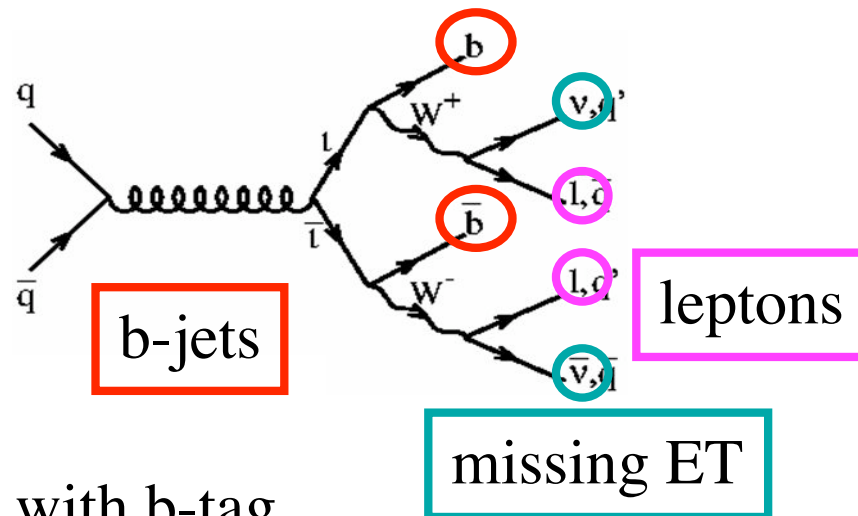
$$\sigma(t\bar{t}) = 8.3^{+0.6}_{-0.5}(\text{stat}) \pm 1.1(\text{syst}) \text{ pb}$$

Data and Monte Carlo Comparison

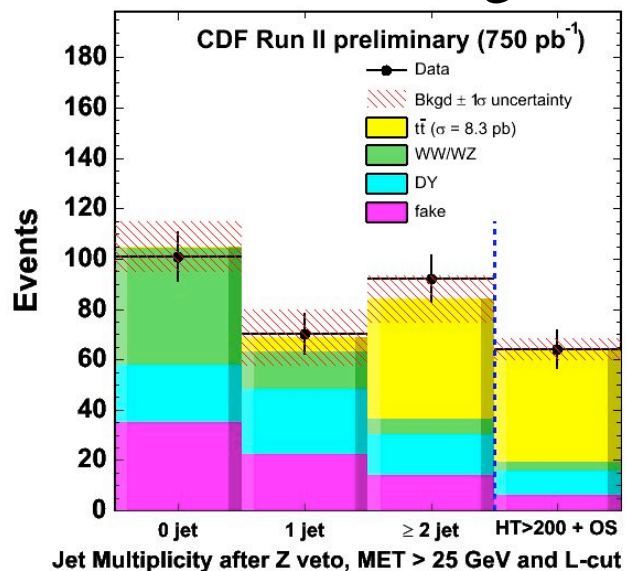


The Top Signal: Dilepton

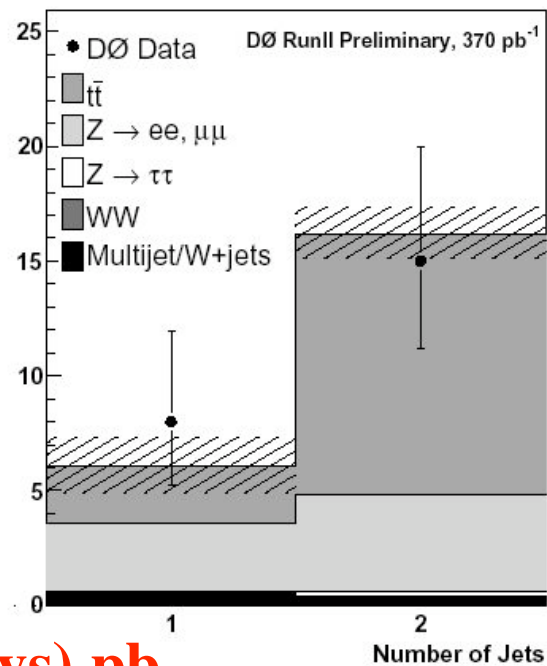
- Select:
 - 2 leptons: $ee, e\mu, \mu\mu$
 - Large missing E_T
 - 2 jets (with or w/o b-tag)



w/o b-tag

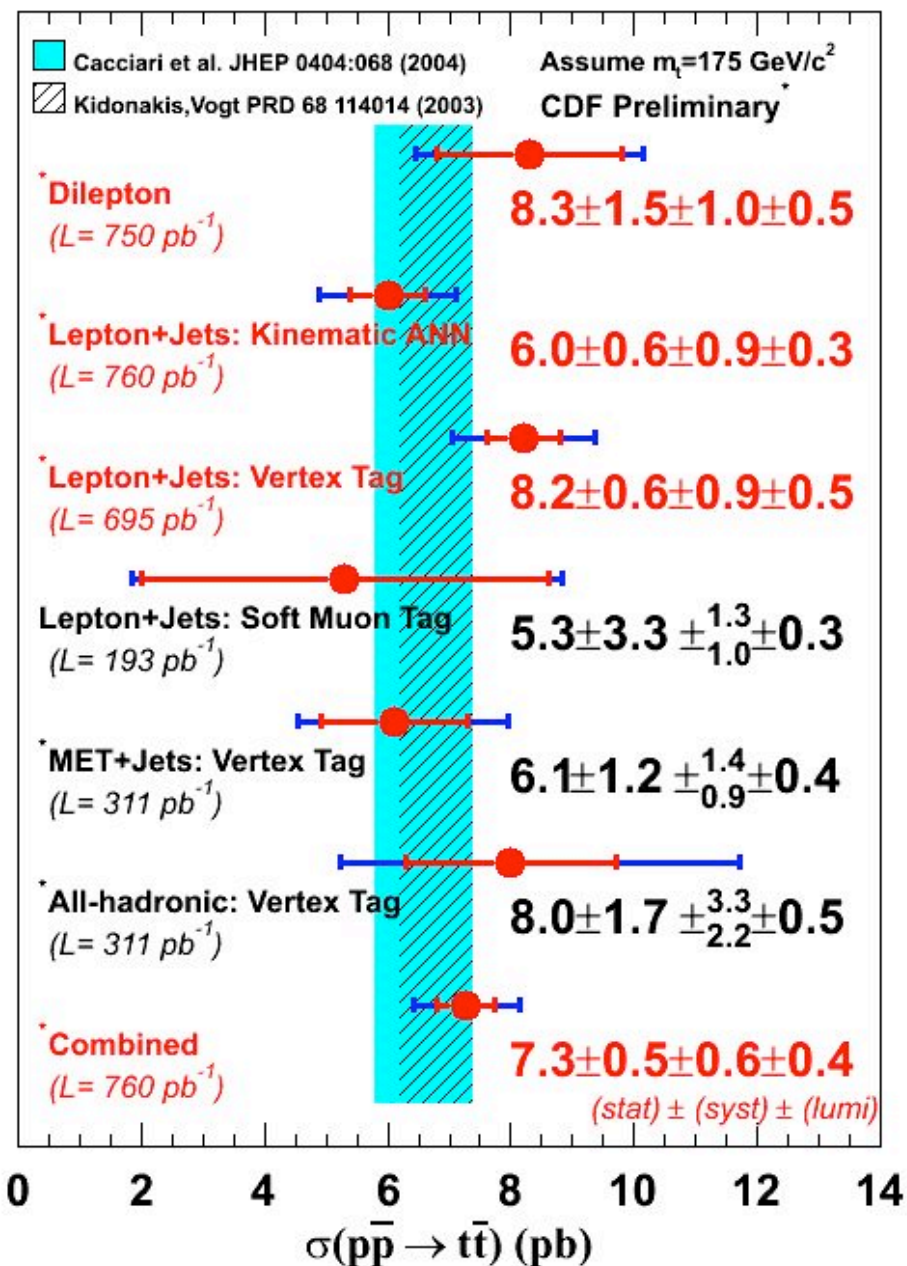


with b-tag



$$\sigma = 6.2 \pm 0.9 \text{ (stat)} \pm 0.9 \text{ (sys) pb}$$

The Top Cross Section



■ Tevatron

- Measured using many different techniques
- Good agreement
 - between all measurements
 - between data and theory
- Precision: $\sim 13\%$

■ LHC:

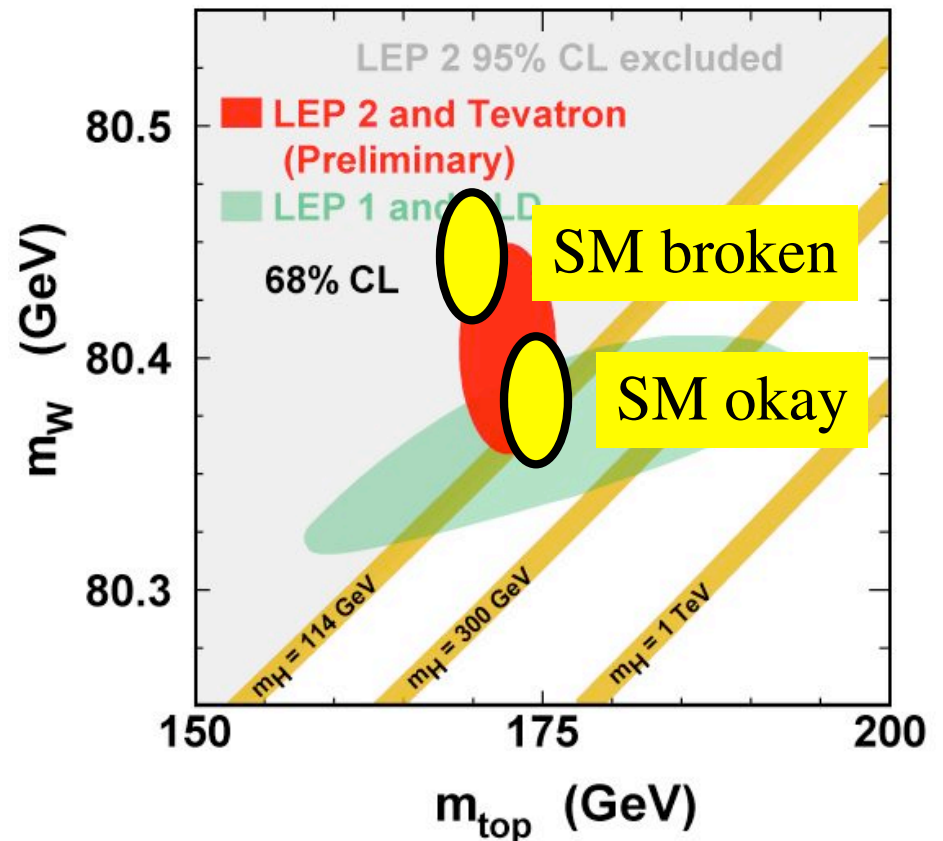
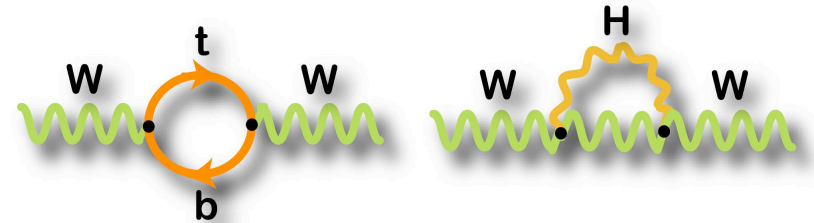
- Cross section ~ 100 times larger
- Measurement will be one of the first milestones (already with 10 pb^{-1})
 - Test prediction
 - demonstrate good understanding of detector
- Expected precision
 - $\sim 4\%$ with 100 pb^{-1}

Precision Measurement of Electroweak Sector of the Standard Model

- **W boson mass**
- **Top quark mass**
- **Implications for the Higgs boson**

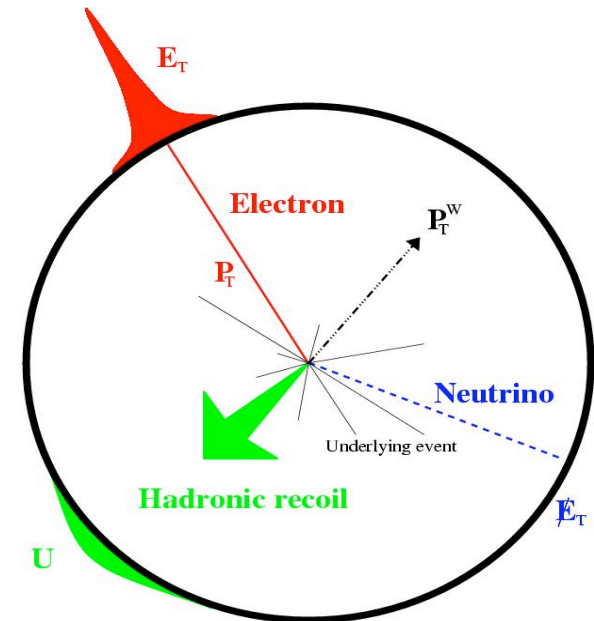
The W boson, the top quark and the Higgs boson

- Top quark is the heaviest known fundamental particle
 - Today: $m_{\text{top}} = 172.6 \pm 1.4$ GeV
 - Run 1: $m_{\text{top}} = 178 \pm 4.3$ GeV/c²
 - Is this large mass telling us something about electroweak symmetry breaking?
 - Top yukawa coupling:
 - $\langle H \rangle / (\sqrt{2} m_{\text{top}}) = 1.008 \pm 0.008$
- Masses related through radiative corrections:
 - $m_W \sim M_{\text{top}}^2$
 - $m_W \sim \ln(m_H)$
- If there are new particles the relation might change:
 - Precision measurement of top quark and W boson mass can reveal new physics



W Boson mass

- Real **precision** measurement:
 - LEP: $M_W = 80.367 \pm 0.033 \text{ GeV}/c^2$
 - Precision: 0.04%
 - => Very challenging!
- Main measurement ingredients:
 - **Lepton** p_T
 - **Hadronic recoil** parallel to lepton: $u_{||}$
- $Z \rightarrow ll$ superb calibration sample:
 - ♣ but statistically limited:
 - About a factor 10 less Z's than W's
 - Most systematic uncertainties are related to size of Z sample
 - Will scale with $1/\sqrt{N_Z}$ ($=1/\sqrt{L}$)

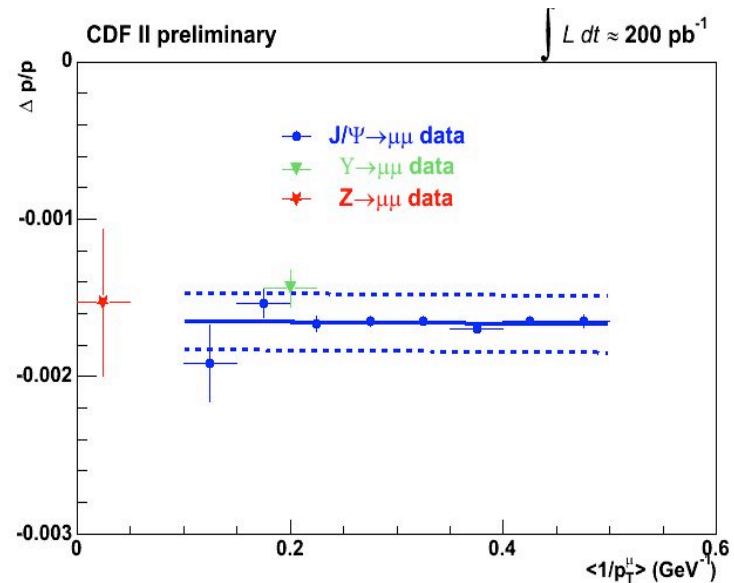
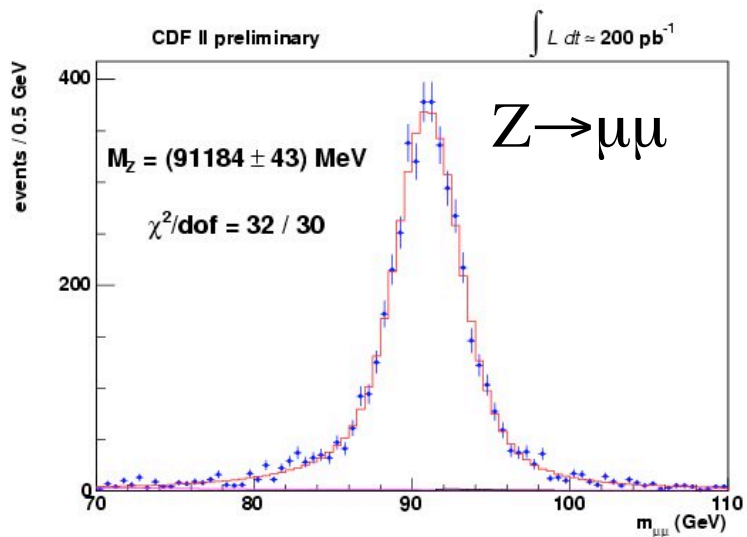
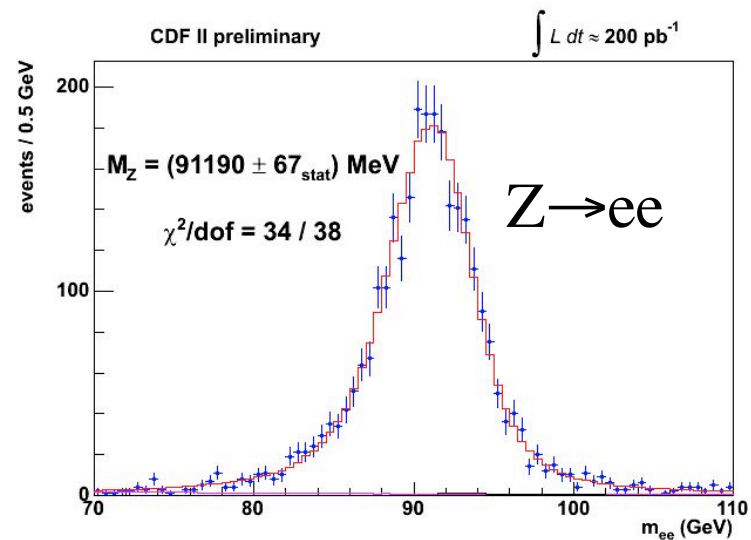
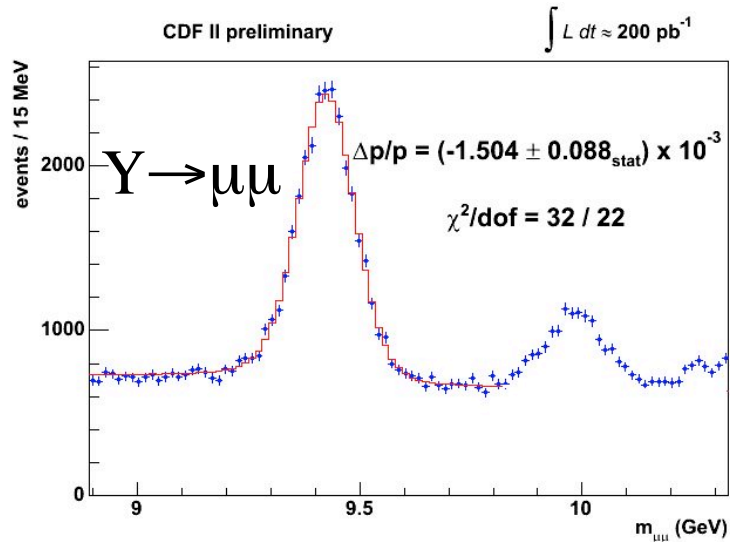


$$m_T = \sqrt{2p_T^l \cancel{p}_T (1 - \cos \Delta\phi)},$$

$$\cancel{p}_T \approx |p_T + u_{||}|$$

$$m_T \approx 2p_T \sqrt{1 + u_{||}/p_T} \approx 2p_T + u_{||}$$

Lepton Momentum Scale and Resolution



- Systematic uncertainty on momentum scale: 0.04%

Systematic Uncertainties

m_T Fit Uncertainties			
Source	$W \rightarrow \mu\nu$	$W \rightarrow e\nu$	Correlation
Tracker Momentum Scale	17	17	100%
Calorimeter Energy Scale	0	25	0%
Lepton Resolution	3	9	0%
Lepton Efficiency	1	3	0%
Lepton Tower Removal	5	8	100%
Recoil Scale	9	9	100%
Recoil Resolution	7	7	100%
Backgrounds	9	8	0%
PDFs	11	11	100%
W Boson p_T	3	3	100%
Photon Radiation	12	11	100%
Statistical	54	48	0%
Total	60	62	-

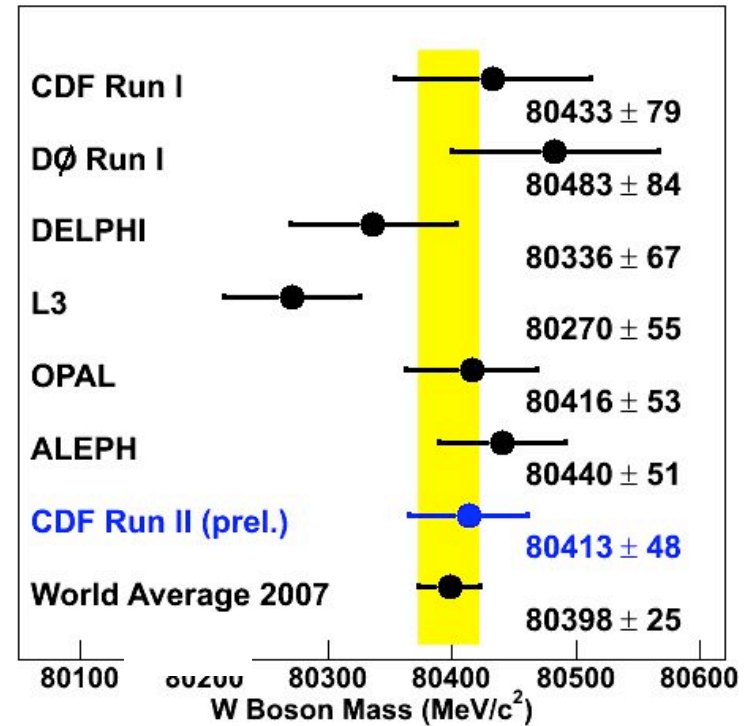
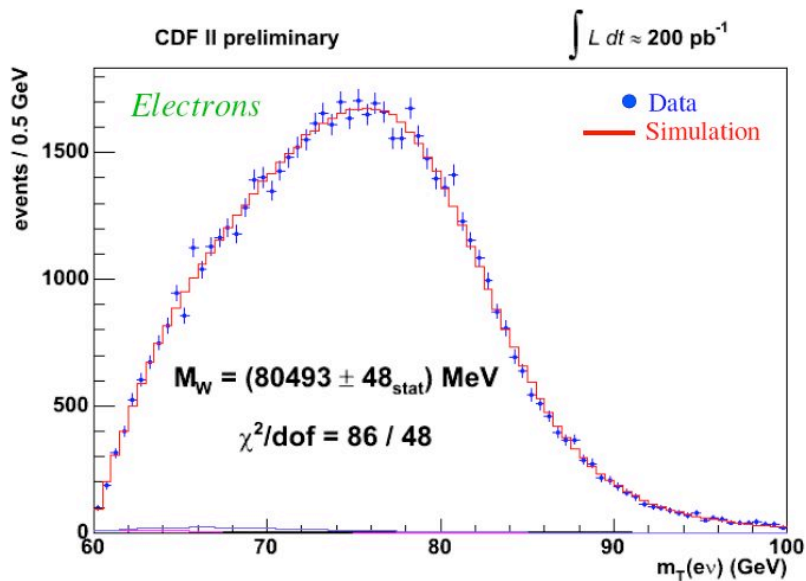
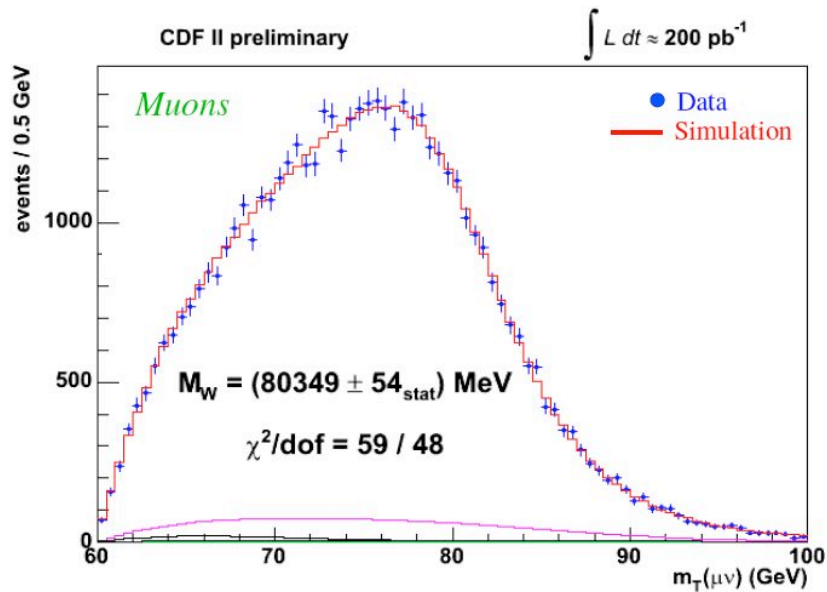
Limited by data statistics

Limited by data and theoretical understanding

TABLE IX: Uncertainties in units of MeV on the transverse mass fit for m_W in the $W \rightarrow \mu\nu$ and $W \rightarrow e\nu$ samples.

- Overall uncertainty 60 MeV for both analyses
 - Careful treatment of correlations between them
- Dominated by stat. error (50 MeV) vs syst. (33 MeV)

W Boson Mass



New world average:

$$M_W = 80398 \pm 25 \text{ MeV}$$

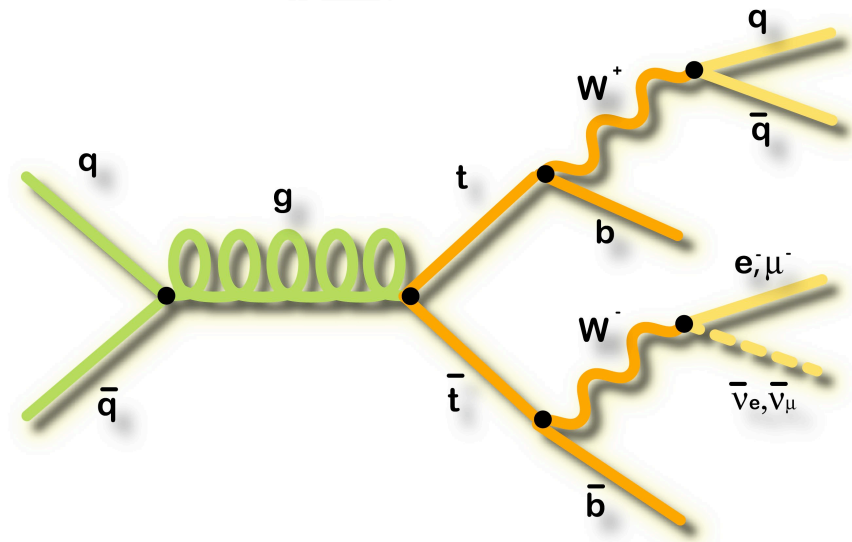
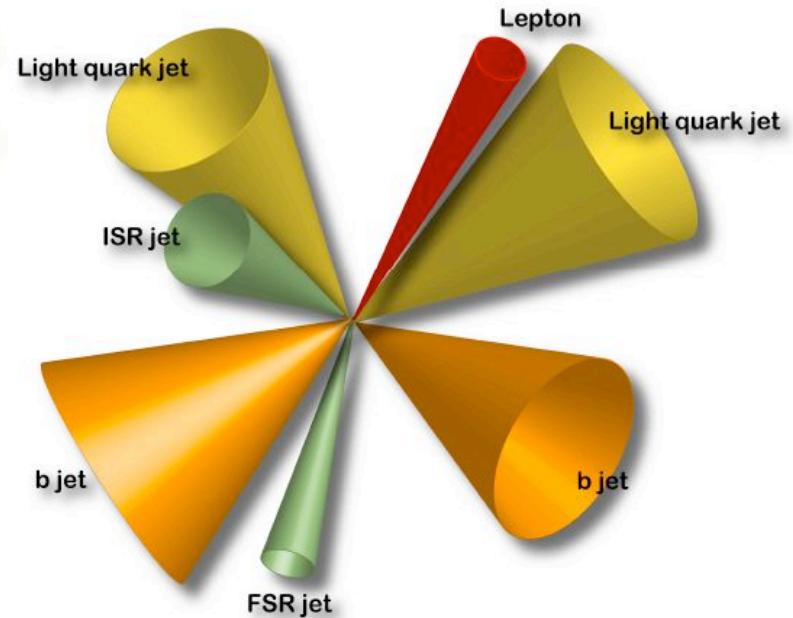
Ultimate precision:

Tevatron: 15 MeV

LHC: unclear (5 MeV?)

Top Mass Measurement: $tt \rightarrow (bl\nu)(bqq)$

- 4 jets, 1 lepton and missing E_T
 - Which jet belongs to what?
 - Combinatorics!
- B-tagging helps:
 - 2 b-tags => 2 combinations
 - 1 b-tag => 6 combinations
 - 0 b-tags => 12 combinations
- Two Strategies:
 - Template method:
 - Uses “best” combination
 - Chi2 fit requires $m(t)=m(\bar{t})$
 - Matrix Element method:
 - Uses all combinations
 - Assign probability depending on kinematic consistency with top



Top Mass Determination

- Inputs:

- Jet 4-vectors
- Lepton 4-vector
- Remaining transverse energy

$p_{T,UE}$:

- $p_{T,v} = -(p_{T,l} + p_{T,UE} + \sum p_{T,jet})$

- Constraints:

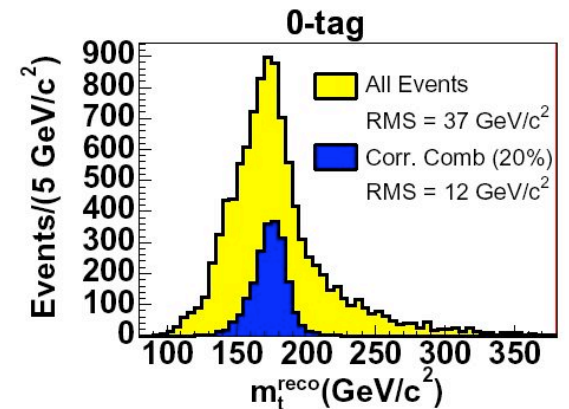
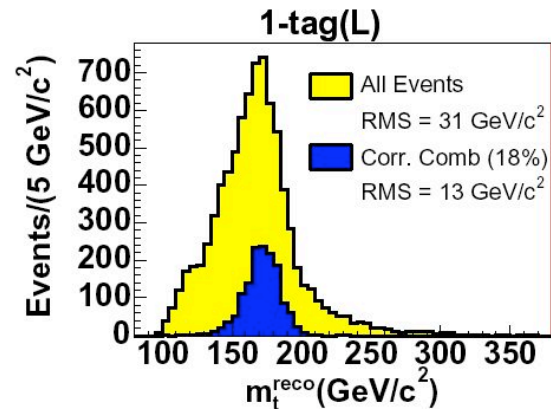
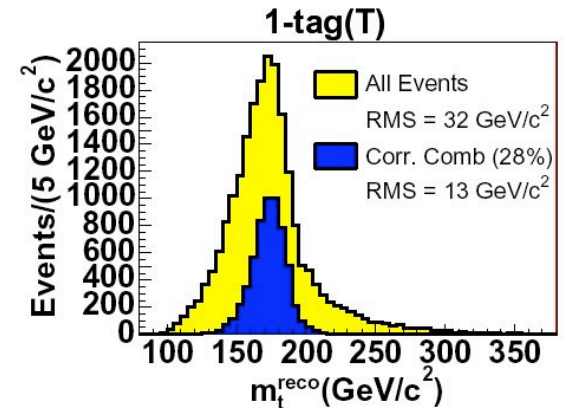
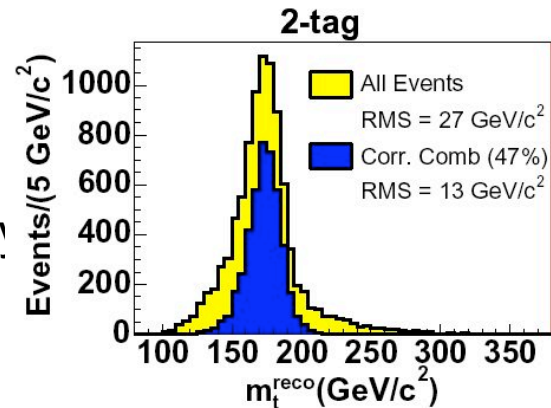
- $M(l\nu) = M_W$
- $M(q\bar{q}) = M_{\underline{W}}$
- $M(t) = M(t)$

- Unknown:

- Neutrino p_z

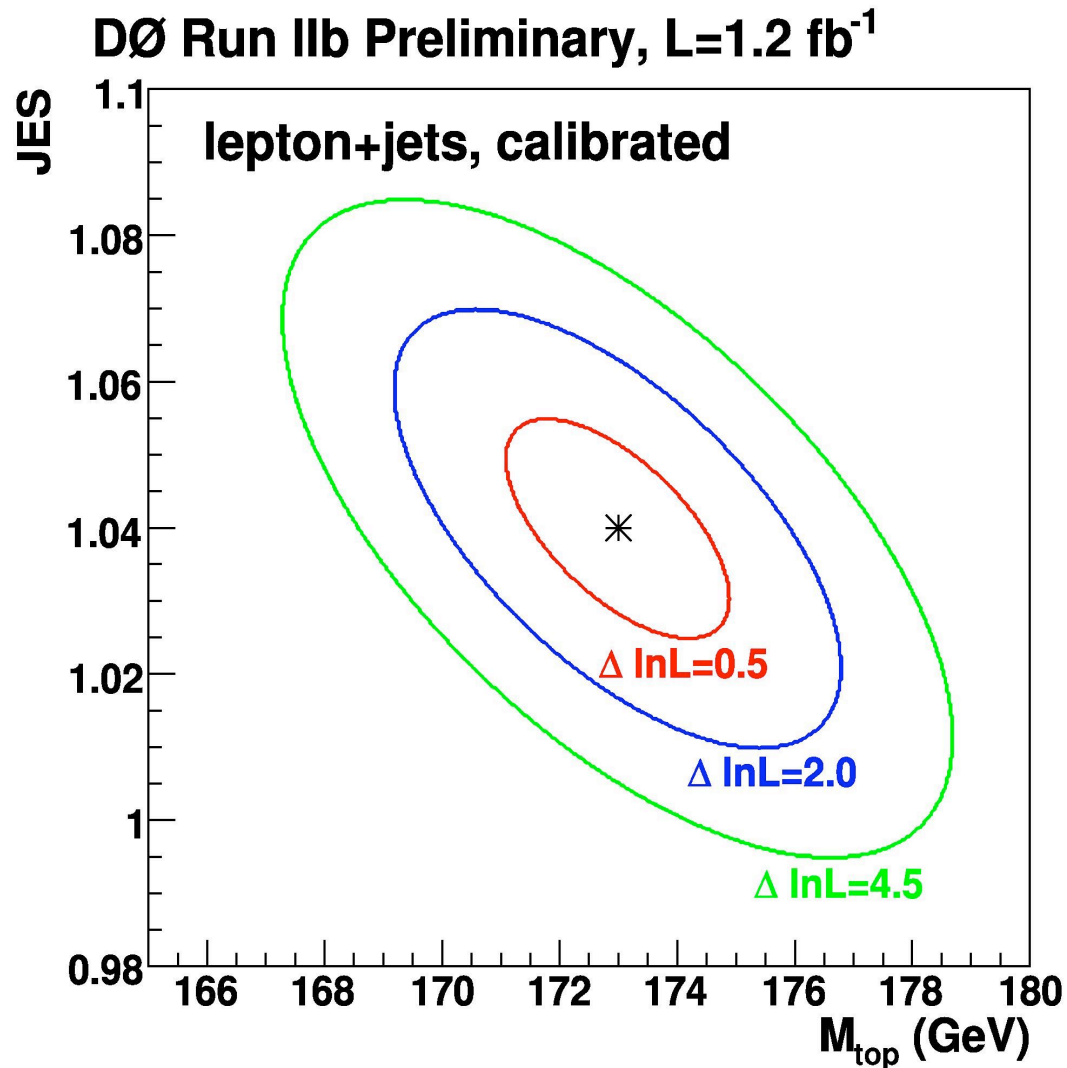
- 1 unknown, 3 constraints:

- Overconstrained
- Can measure $M(t)$ for each event: m_t^{reco}
- Leave jet energy scale (“JES”) as free parameter



Selecting correct combination
20-50% of the time

Example Results on m_{top}

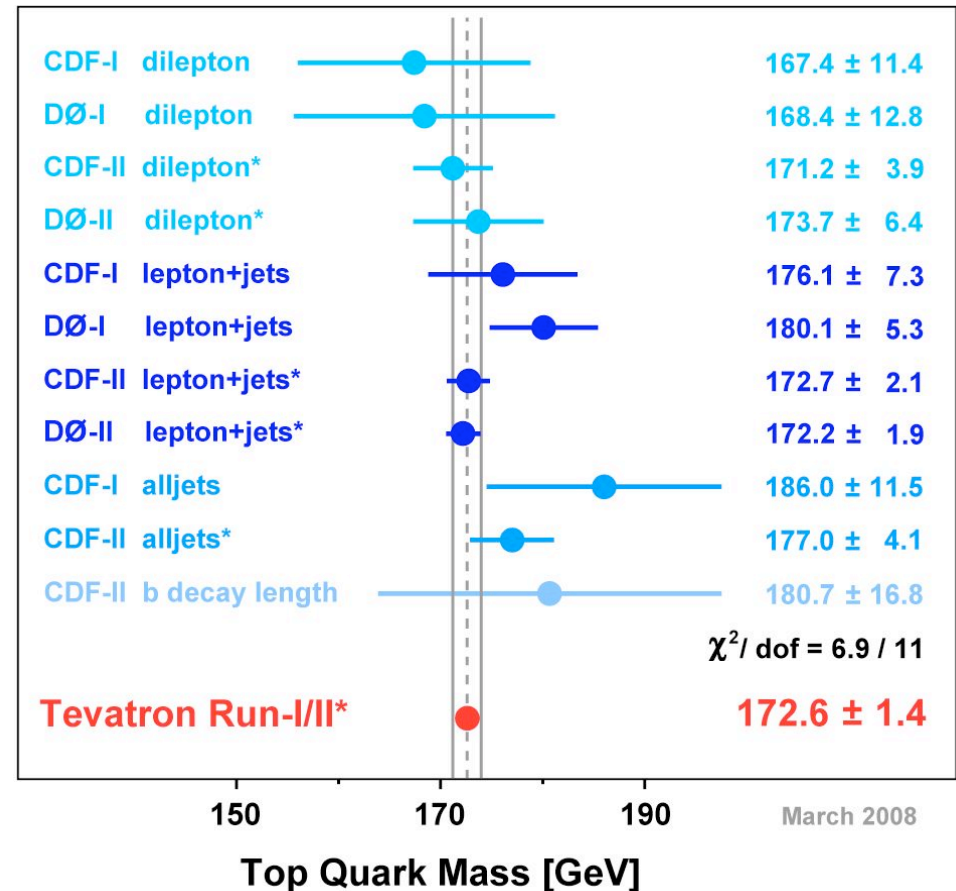


$172.2 \pm 1.9 \text{ GeV}/c^2$

Combining M_{top} Results

- Excellent results in each channel
 - Dilepton
 - Lepton+jets
 - All-hadronic
- Combine them to improve precision
 - Include Run-I results
 - Account for correlations
- **Uncertainty: 1.4 GeV**
 - Dominated by syst. uncertainties
- Precision so high that theorists wonder about what it's exact definition is!

Best Independent Measurements
of the Mass of the Top Quark (*=Preliminary)

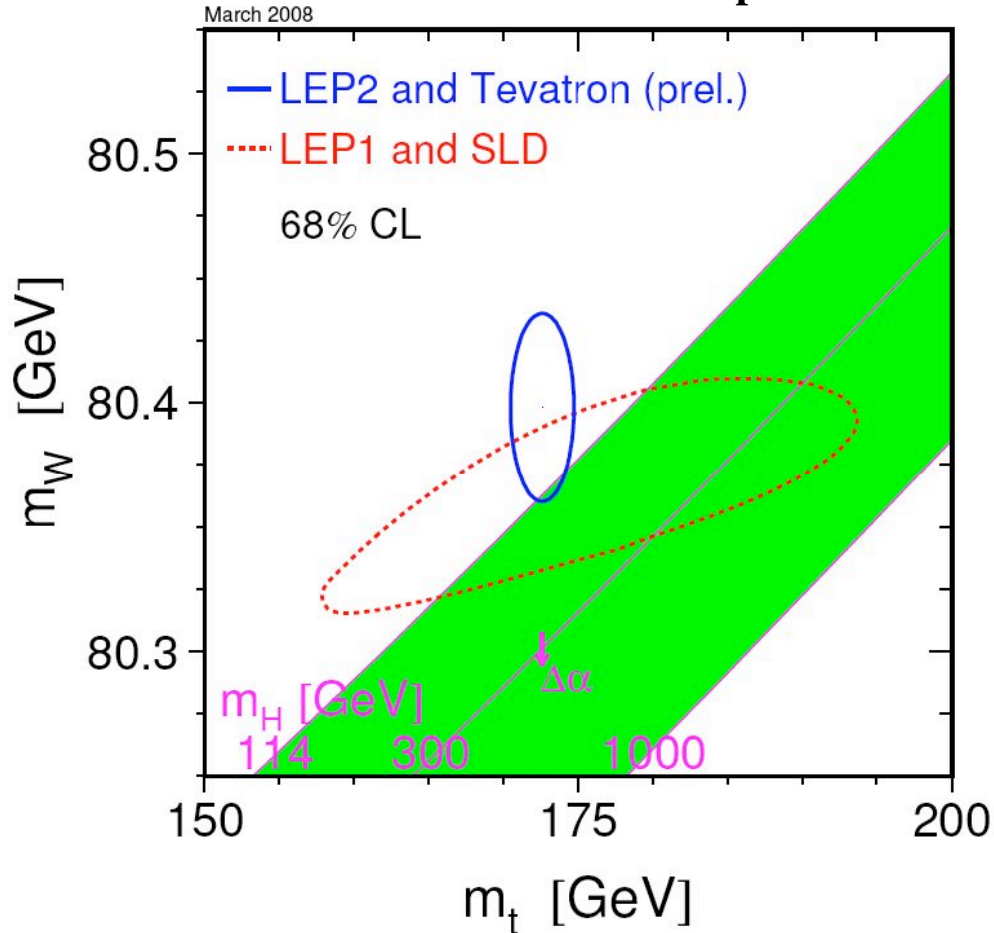


Tevatron/LHC expect to improve precision to ~ 1 GeV

Implications for the Higgs Boson

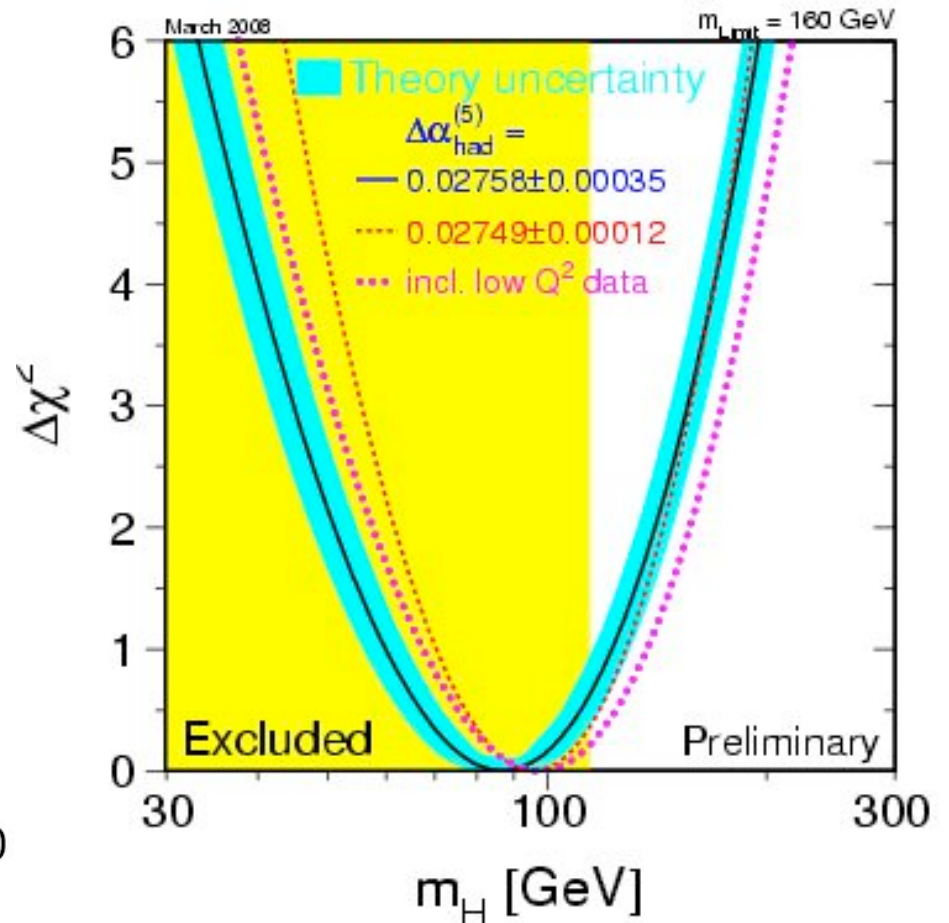
LEPEWWG 03/08

Relation: M_W vs m_{top} vs M_H



Standard Model still works!

$$m_H = 86^{+36}_{-27} \text{ GeV}$$



Indirect constraints:

$m_H < 160 \text{ GeV @95\%CL}$

Conclusions

- Perturbative QCD describes hadron collider data successfully:
 - Jet cross sections: $\Delta\sigma/\sigma \approx 20\text{-}100\%$
 - W/Z cross section: $\Delta\sigma/\sigma \approx 6\%$
 - Top cross section: $\Delta\sigma/\sigma \approx 15\%$
- High Precision measurements
 - W boson mass: $\Delta M_W/M_W = 0.031\%$
 - top quark mass: $\Delta m_{\text{top}}/m_{\text{top}} = 0.8\%$
- Standard Model still works!
 - Higgs boson constrained
 - $114 < m_H < 160 \text{ GeV}/c^2$ at 95% C.L.
 - Let's look for it in the next lecture!