

# Spectroscopy of particle-phonon coupled states in $^{133}\text{Sb}$ by the cluster transfer reaction $^{132}\text{Sn}$ on $^7\text{Li}$ : an advanced test of nuclear interactions

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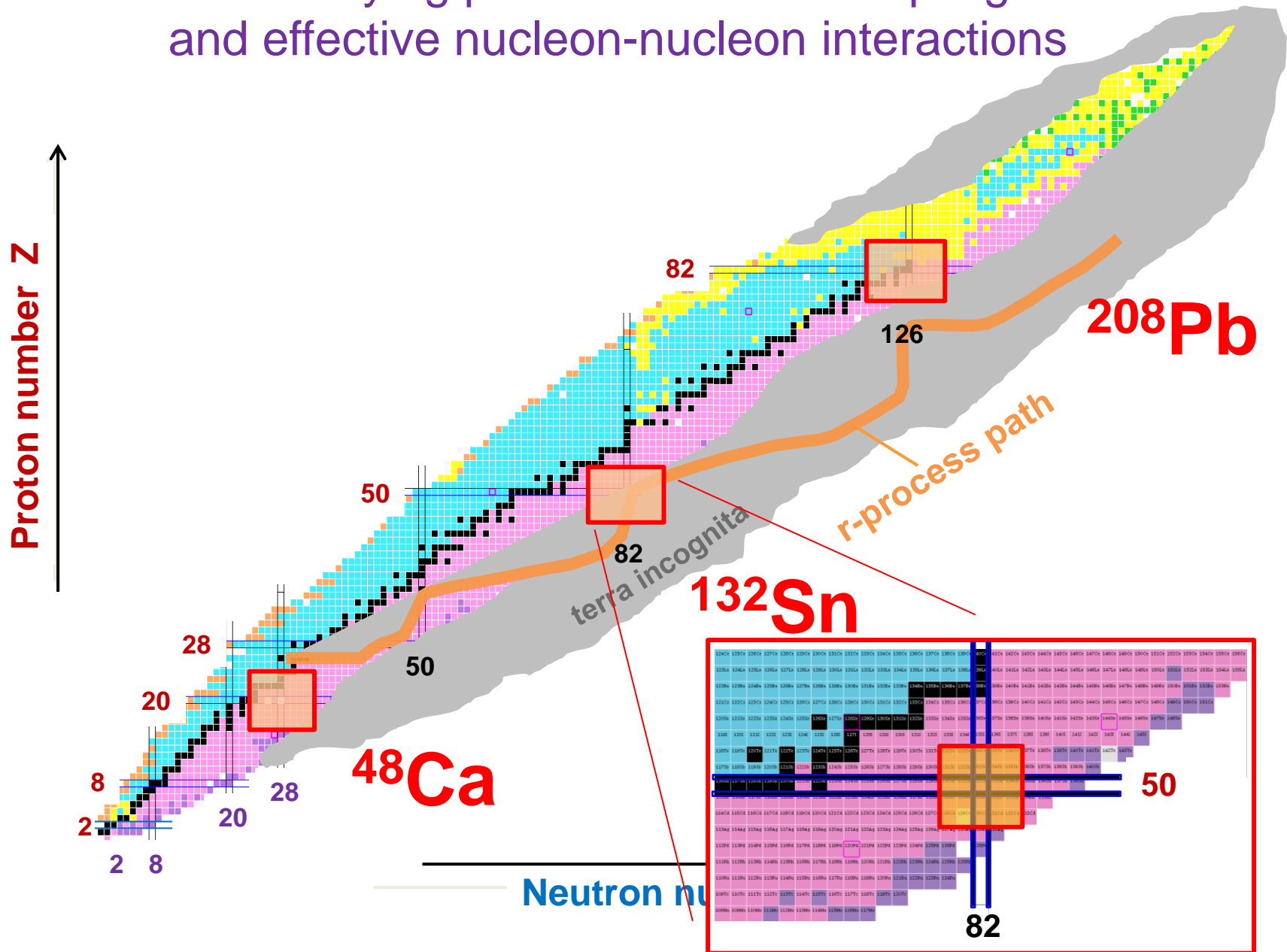
<sup>12</sup> *TU München, Germany*

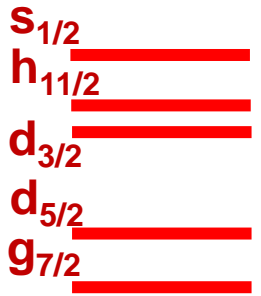
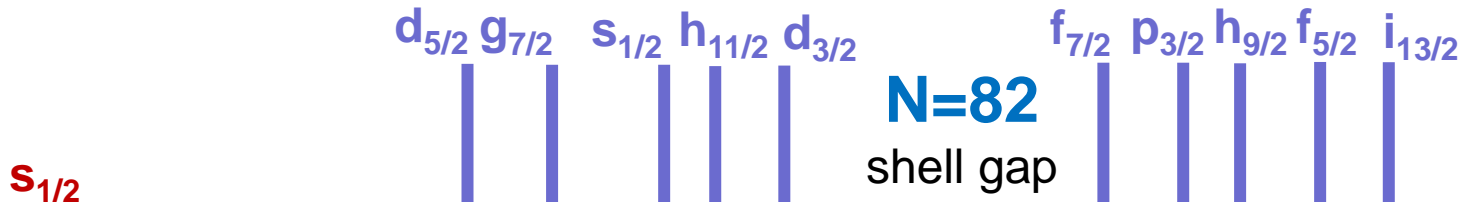
<sup>13</sup> *Argonne National Laboratory, USA*

<sup>14</sup> *ISOLDE, CERN, Switzerland*

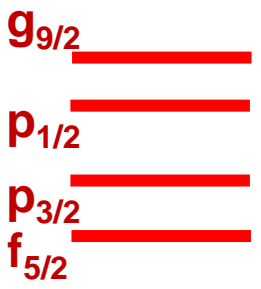


# Neighborhoods of doubly-magic nuclei as a laboratory for studying particle-vibration couplings and effective nucleon-nucleon interactions



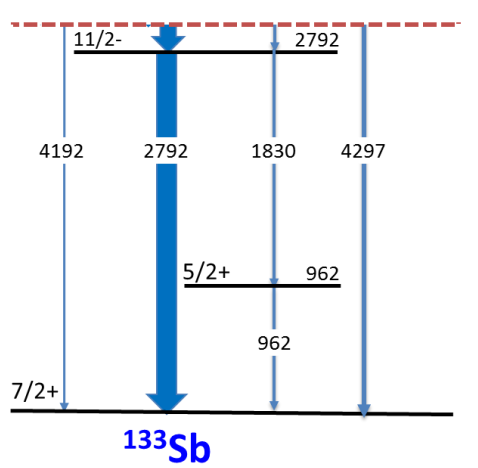
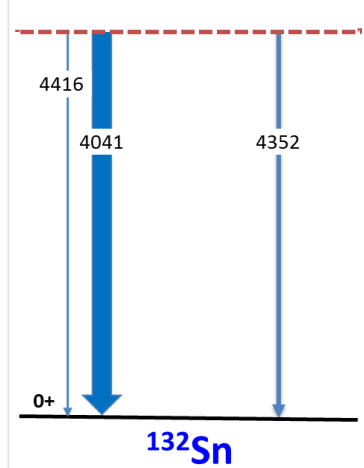
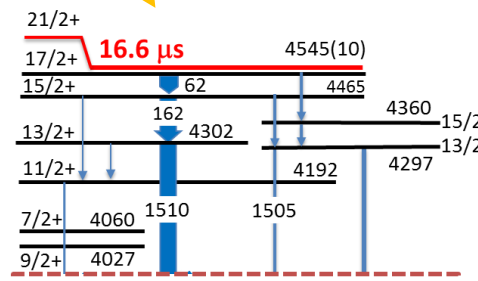
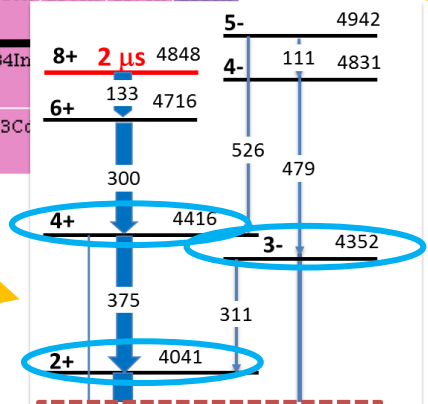


shell gap  
**Z=50**



Xe	128Xe	129Xe	130Xe	131Xe	132Xe	133Xe	134Xe	135Xe	136Xe	137Xe	138Xe	139Xe	140Xe	141Xe	142Xe	143Xe	144Xe
I	127I	128I	129I	130I	131I	132I	133I	134I	135I	136I	137I	138I	139I	140I	141I	142I	143I
Te	126Te	127Te	128Te	129Te	130Te	131Te	132Te	133Te	134Te	135Te	136Te	137Te	138Te	139Te	140Te	141Te	142Te
Sb	125Sb	126Sb	127Sb	128Sb	129Sb	130Sb	131Sb	132Sb	133Sb	134Sb	135Sb	136Sb	137Sb	138Sb	139Sb	140Sb	
Sn	124Sn	125Sn	126Sn	127Sn	128Sn	129Sn	130Sn	131Sn	132Sn	133Sn	134Sn	135Sn	136Sn	137Sn	138Sn		
In	123In	124In	125In	126In	127In	128In	129In	130In	131In	132In	133In	134In					
Cd	122Cd	123Cd	124Cd	125Cd	126Cd	127Cd	128Cd	129Cd	130Cd	131Cd	132Cd	133Cd					
Ag	121Ag	122Ag	123Ag	124Ag	125Ag	126Ag	127Ag	128Ag	129Ag	130Ag							
Pd	120Pd	121Pd	122Pd	123Pd	124Pd	125Pd	126Pd										
	74	76	78	80					82								

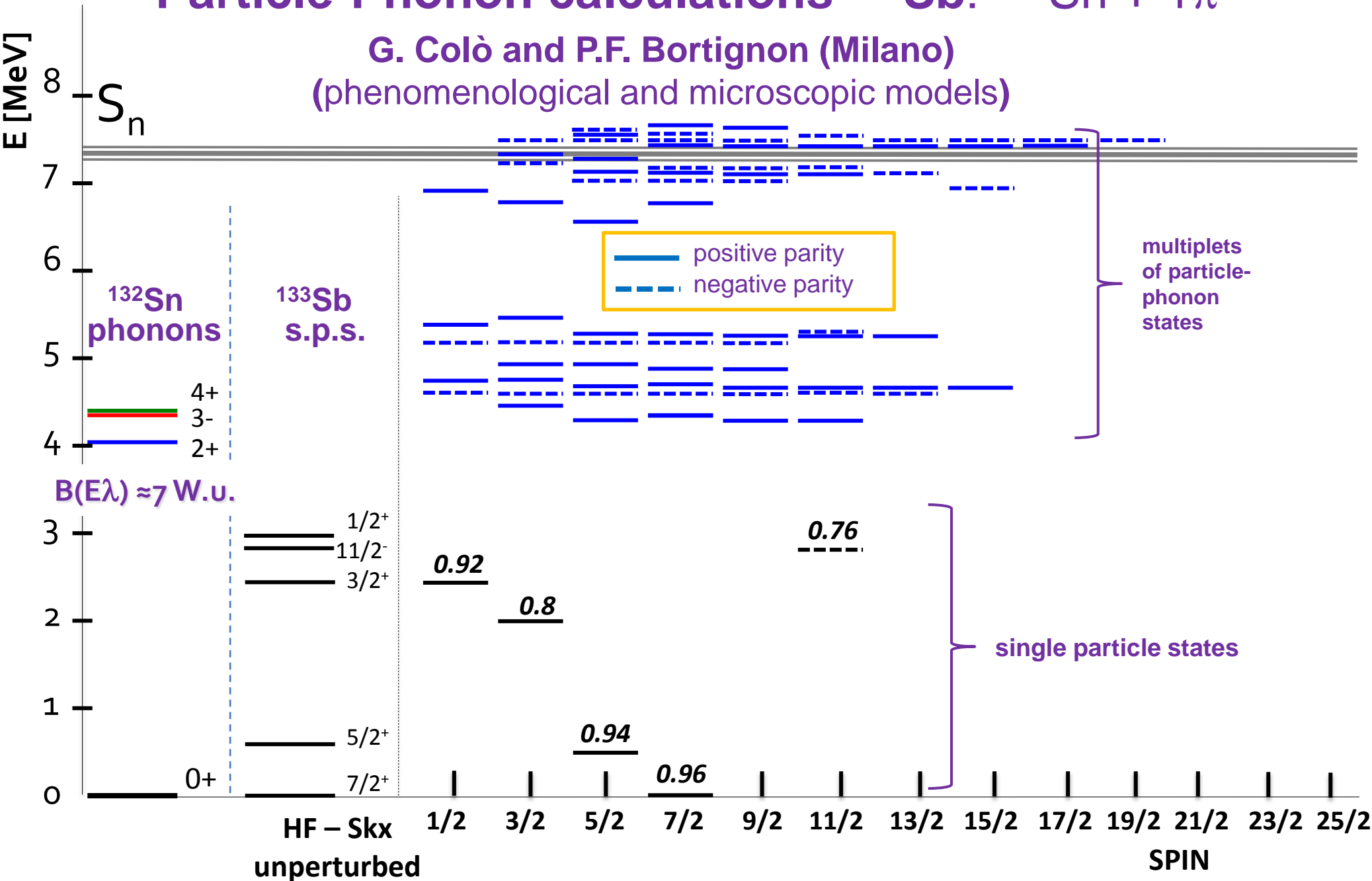
**133**  
**132Sn**





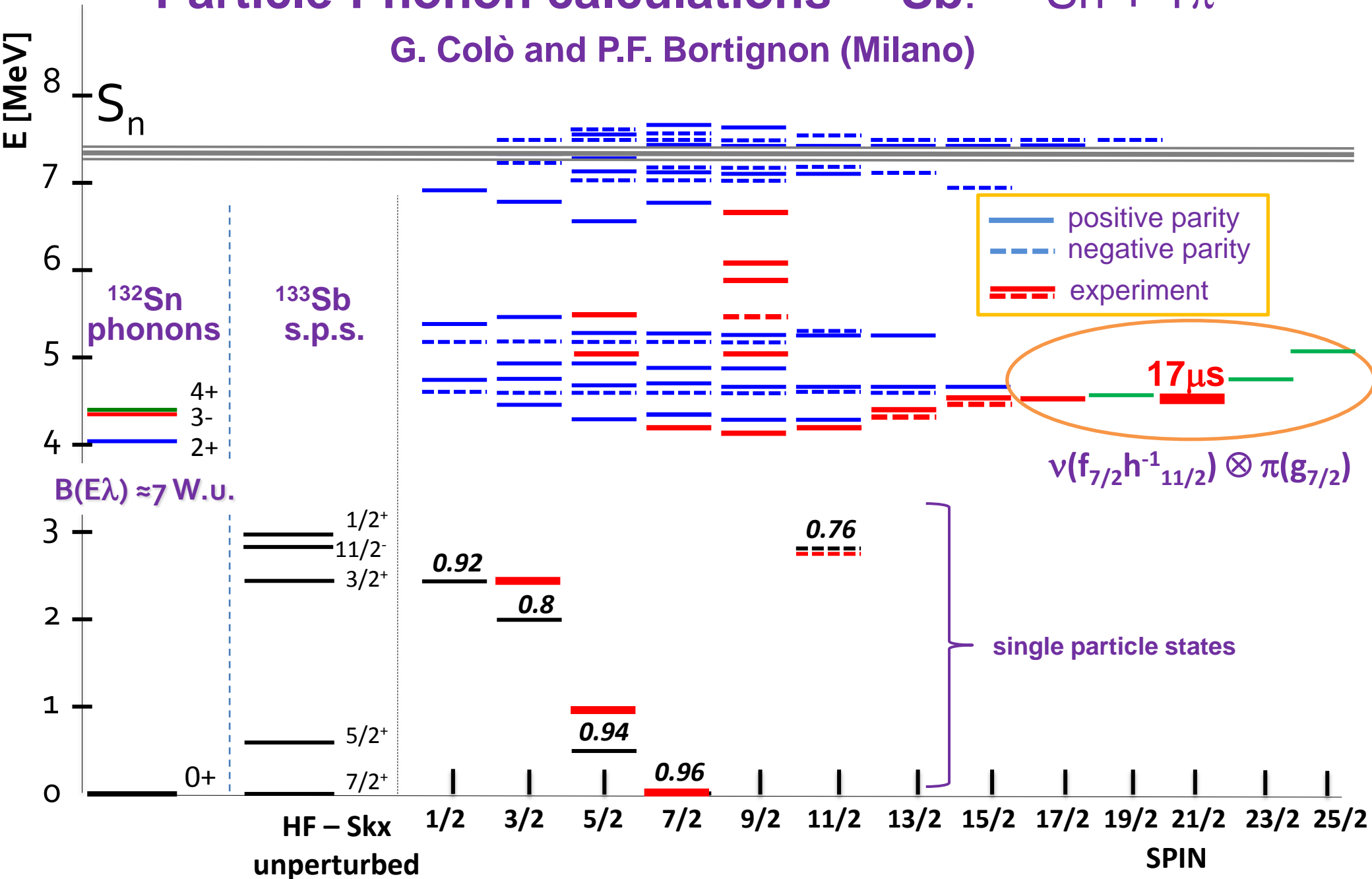
# Particle-Phonon calculations $^{133}\text{Sb}: ^{132}\text{Sn} + 1\pi$

G. Colò and P.F. Bortignon (Milano)  
 (phenomenological and microscopic models)



# Particle-Phonon calculations $^{133}\text{Sb}: ^{132}\text{Sn} + 1\pi$

G. Colò and P.F. Bortignon (Milano)



EXPERIMENTAL TOOLS for gamma-ray spectroscopy of excited states  
in neutron-rich nuclei

**$\beta$ -decay**

low-lying selected states

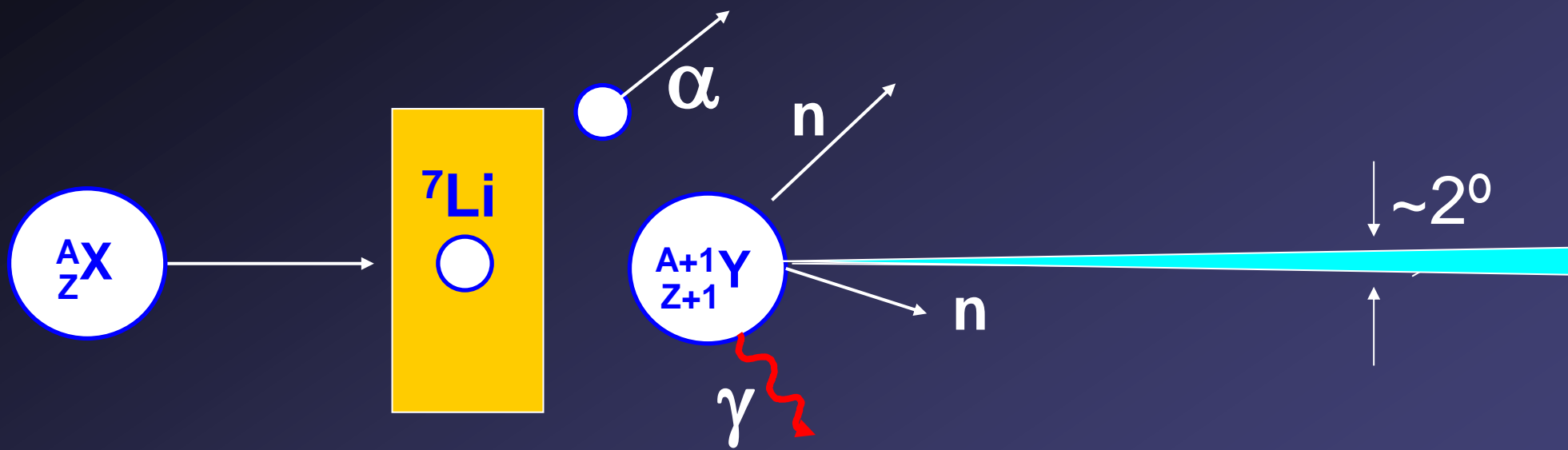
**Fission, Deep-Inelastic**

YRAST Spectroscopy

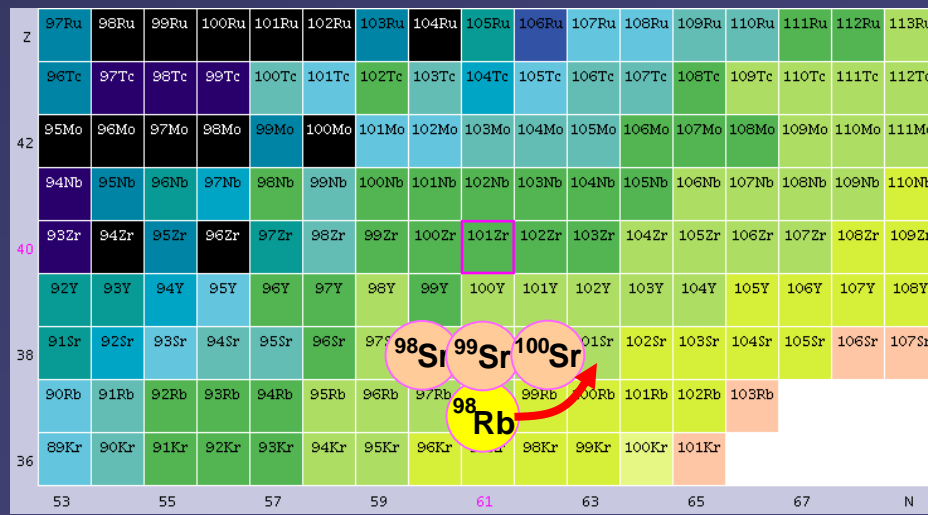
**Fragmentation**

ISOMER spectroscopy

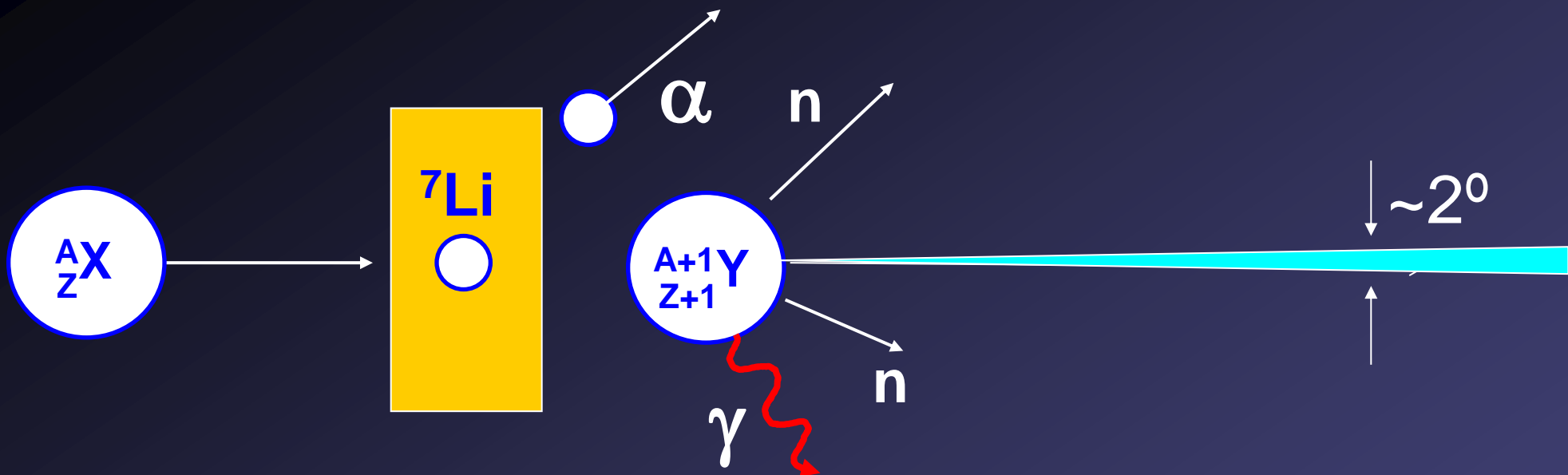
To perform gamma-ray spectroscopic studies of yrast and non-yrast structures in neutron-rich nuclei, we proposed to use the triton transfer process induced by radioactive beams on a  ${}^7\text{Li}$  target



EXAMPLE:







### Advantages of the proposed method:

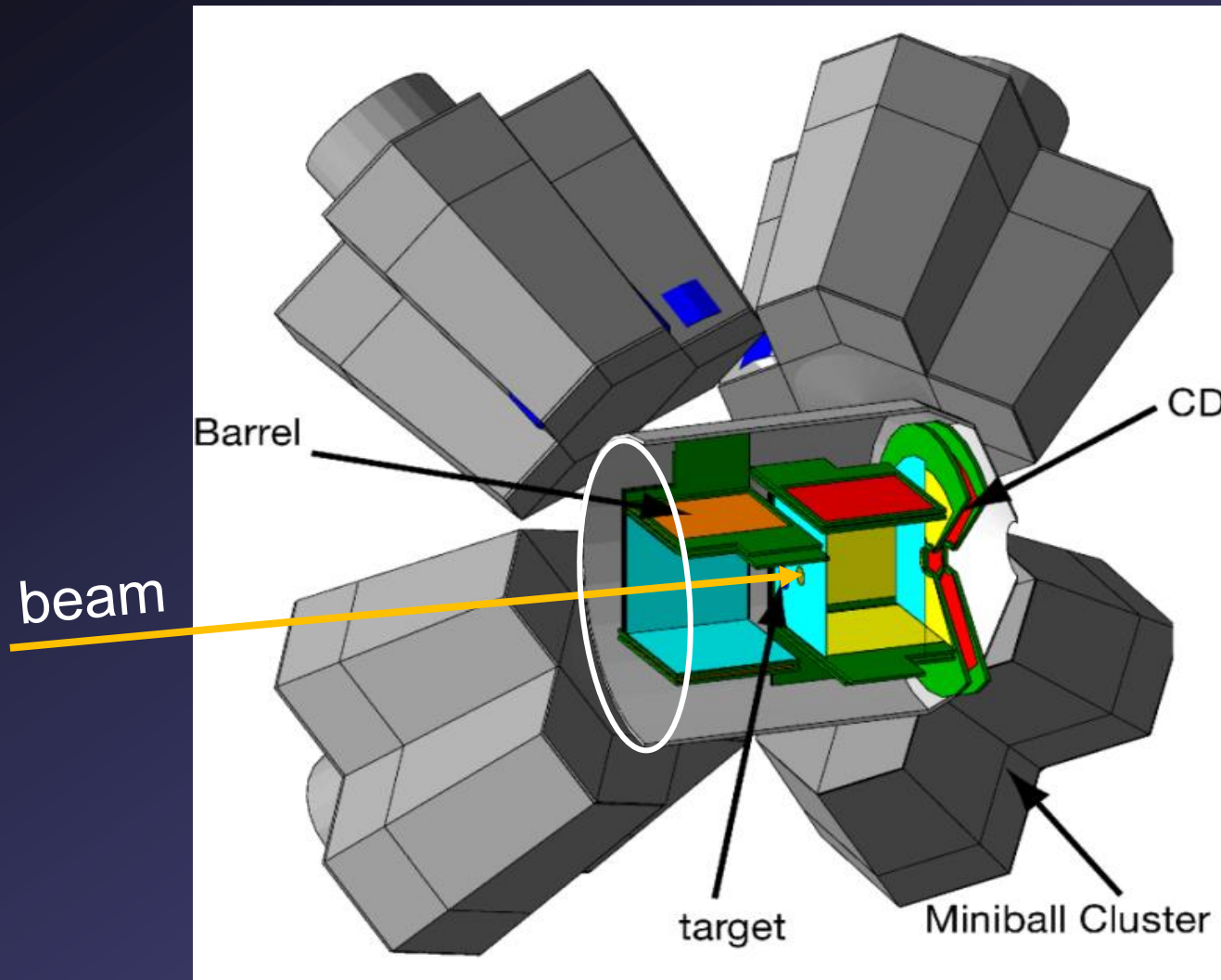
The very inverse kinematics guarantees that the product nuclei travel downstream in a very small recoil cone, **thus Doppler correction does not require recoil detection.**

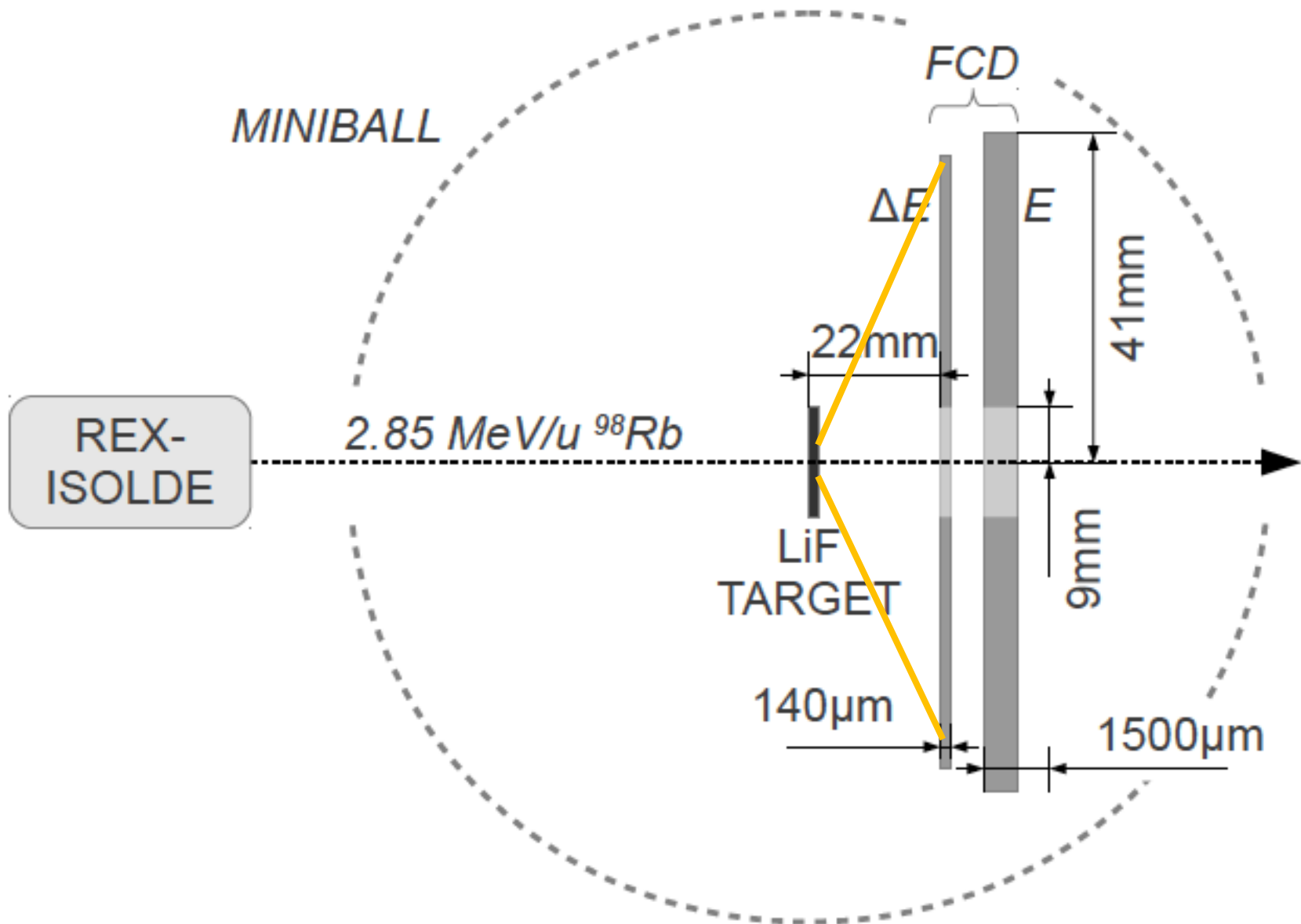
Reaction channel of interest will be **uniquely associated with the emission of an  $\alpha$  particle**: emitted alpha particles may be used as event tags.



# REX-ISOLDE + MINIBALL + T-REX

$^{98}\text{Rb}$ (60%) +  $^{98}\text{Sr}$ (40%) (2.84 MeV/u) +  $^7\text{LiF}$  (1.5 mg/cm<sup>2</sup>)



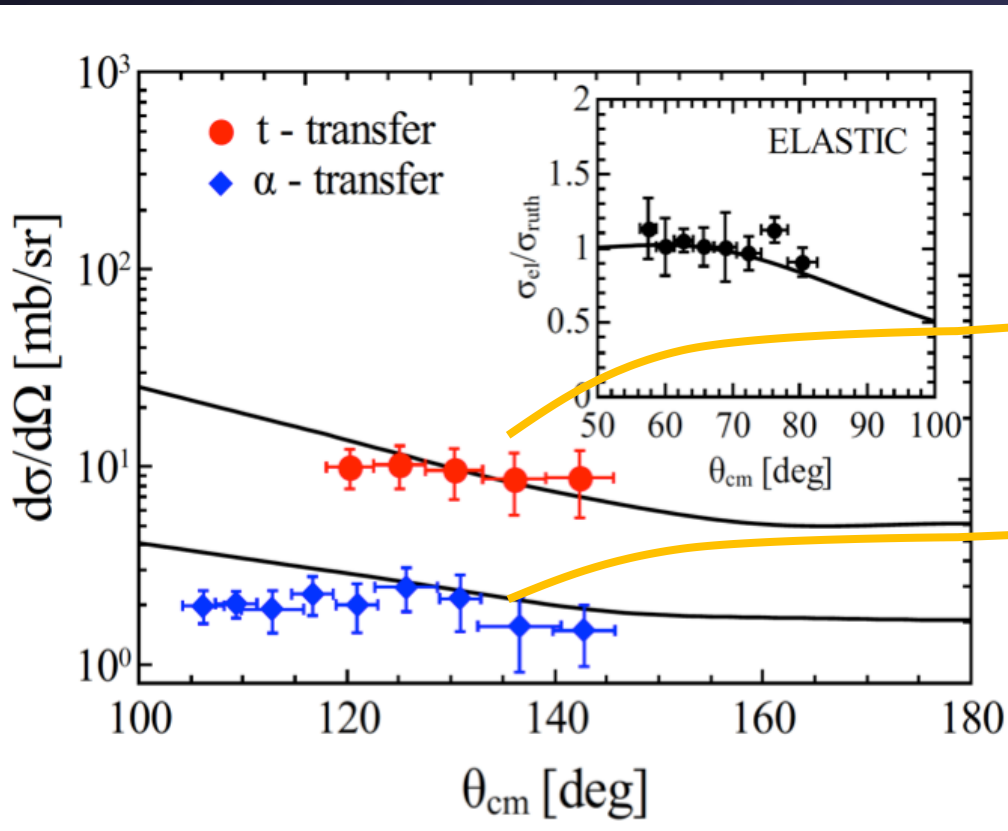


# REX-ISOLDE + MINIBALL + T-REX

$^{98}\text{Rb}(60\%)+^{98}\text{Sr}(40\%)$  (2.84 MeV/u) +  $^7\text{LiF}$  (1.5 mg/cm<sup>2</sup>)

Data were analyzed by Simone Bottoni,  
Ph.D. Thesis Univ. of Milano and KU Leuven

Experimental data on cross-section  
for t- and  $\alpha$ -transfer



Process

MEASURED  
cross section  
[mb]

ESTIMATED  
TOTAL  
cross section  
[mb]

triton  
transfer

**27**

**~90**

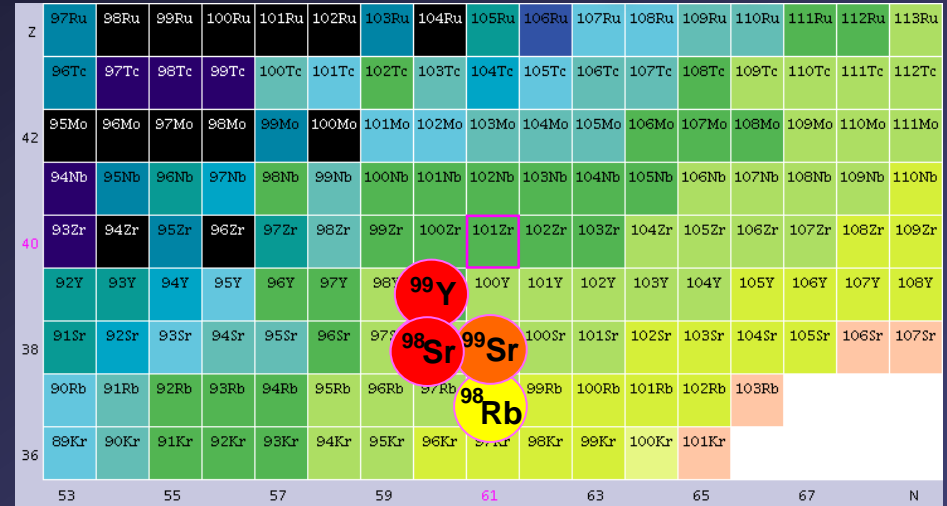
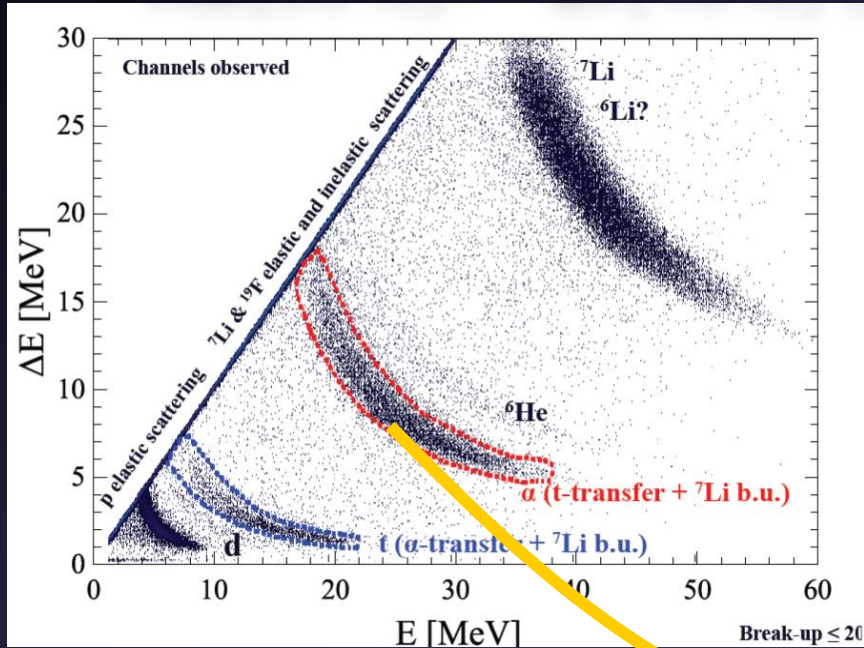
alpha  
transfer

**5**

**~15**

# REX-ISOLDE + MINIBALL + T-REX

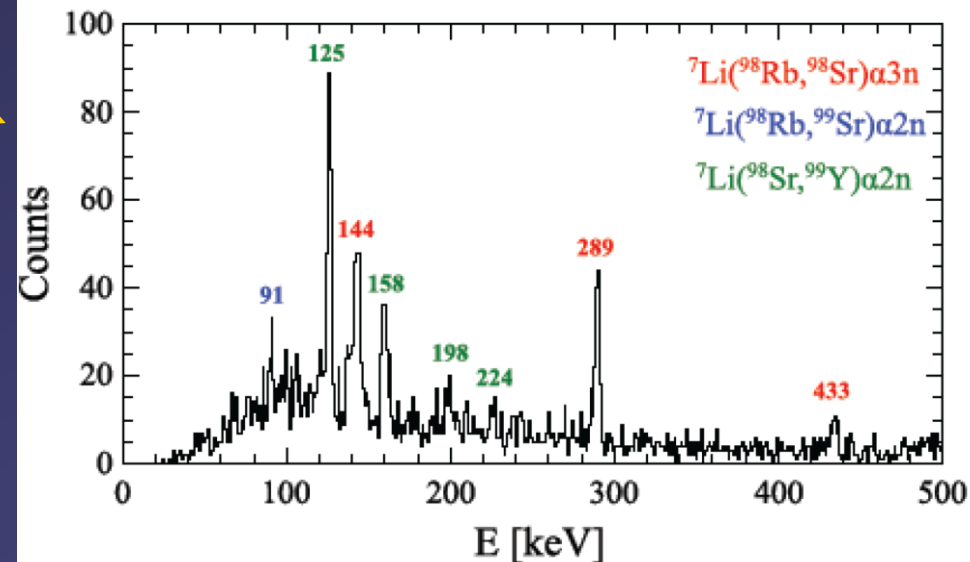
$^{98}\text{Rb}(60\%) + ^{98}\text{Sr}(40\%)$  (2.84 MeV/u) +  $^7\text{LiF}$  (1.5 mg/cm<sup>2</sup>)



$I_{\text{BEAM}} (^{98}\text{Ru}/^{98}\text{Sr}) \approx 2.5 \times 10^4$  pps

Counting rate:  
 ~0.03 ev/s for  $\alpha$ - $\gamma$   
 (10 k in 4 days)

## t - transfer



Data were analyzed by Simone Bottoni,  
 Ph.D. Thesis Univ. of Milano and KU Leuven

## REX-ISOLDE + MINIBALL + T-REX

$^{98}\text{Rb}(60\%) + ^{98}\text{Sr}(40\%)$  (2.84 MeV/u) +  $^7\text{LiF}$  (1.5 mg/cm<sup>2</sup>)

### Results:

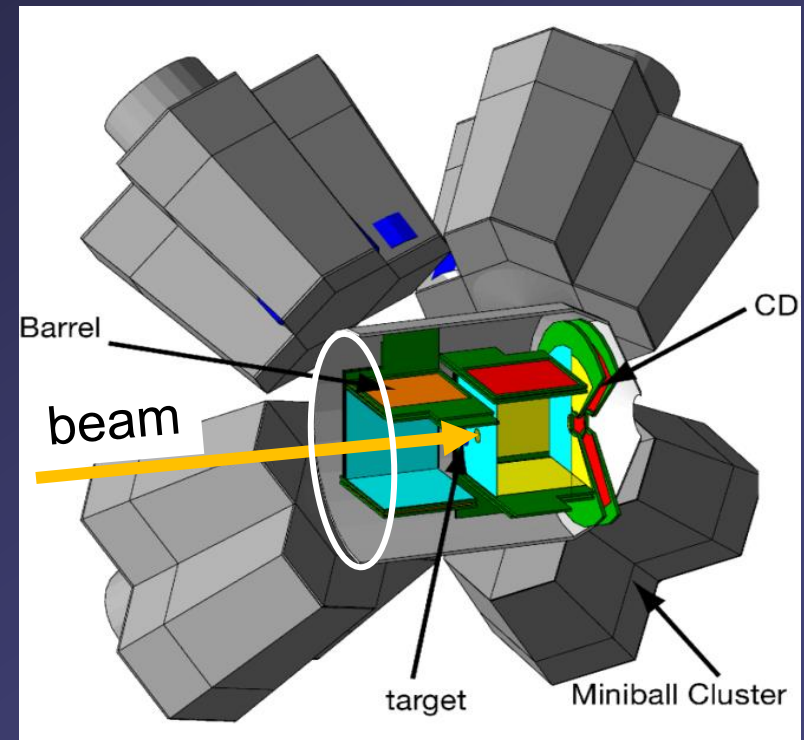
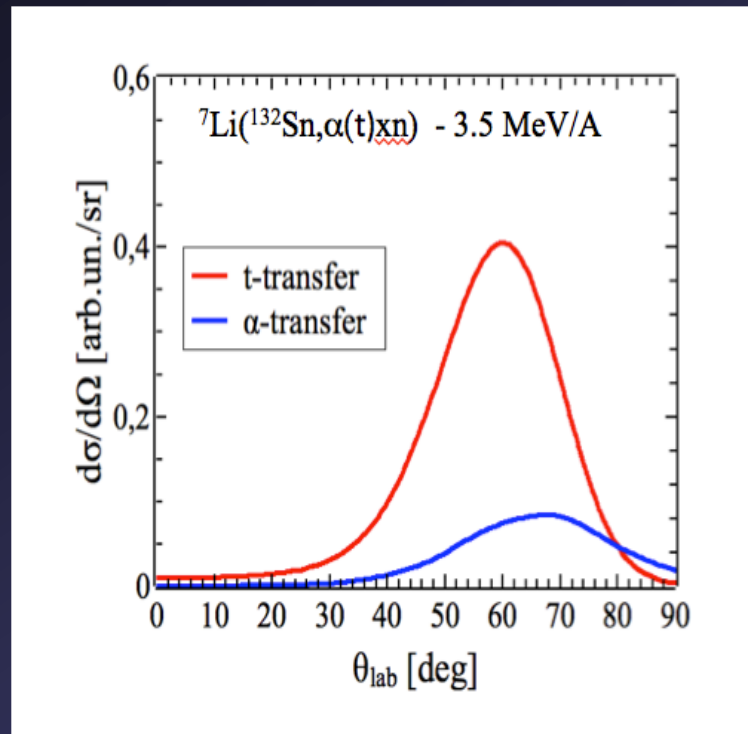
- Transfer of tritons into  $^{98}\text{Rb}$ , with emission of alpha particles, has a sizeable cross-section as predicted by DWBA calculations.
- By tagging on  $\alpha$  particles one obtains clean  $\gamma$ -ray spectra from triton transfer products.
- Yrast, near-yrast and non-yrast states are populated.

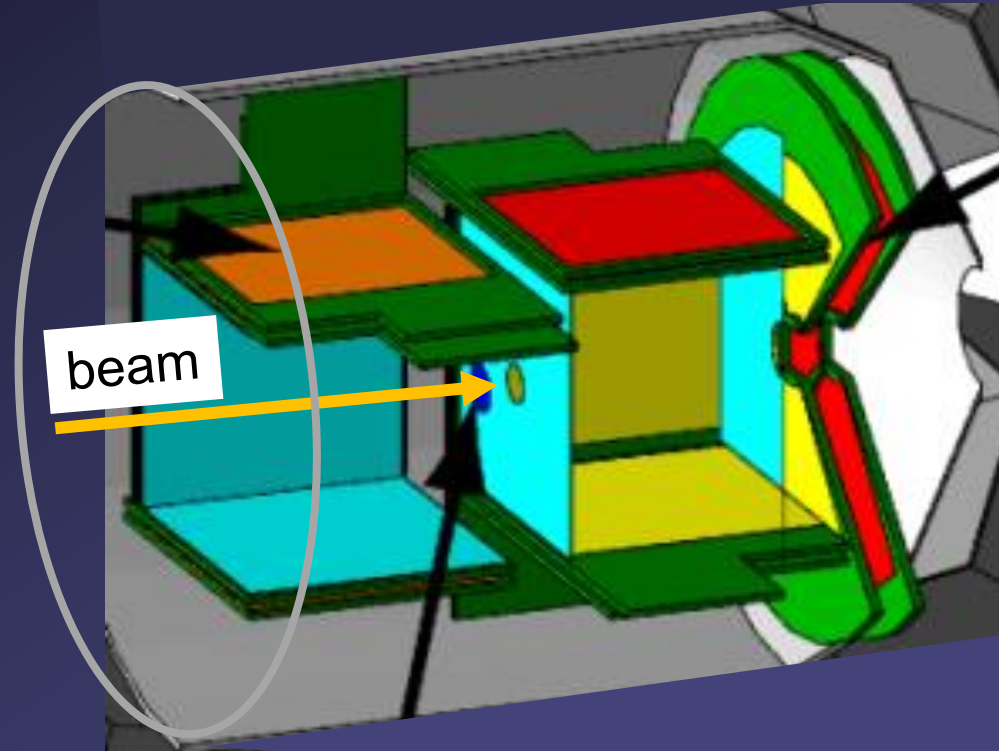
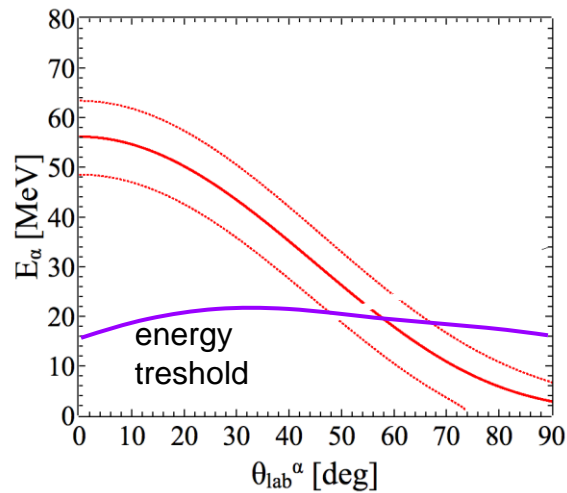
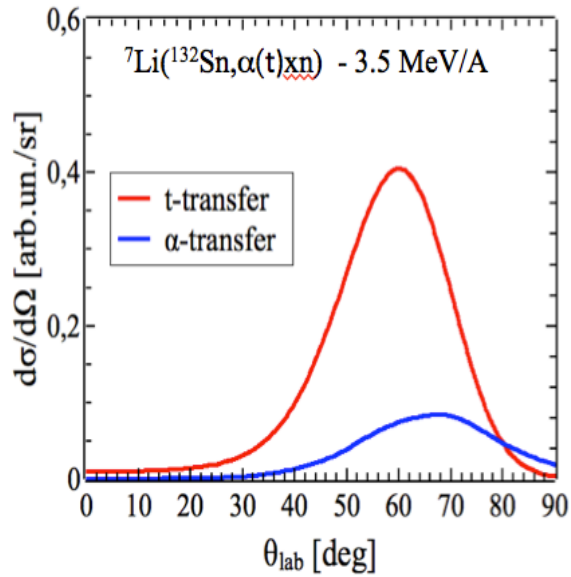


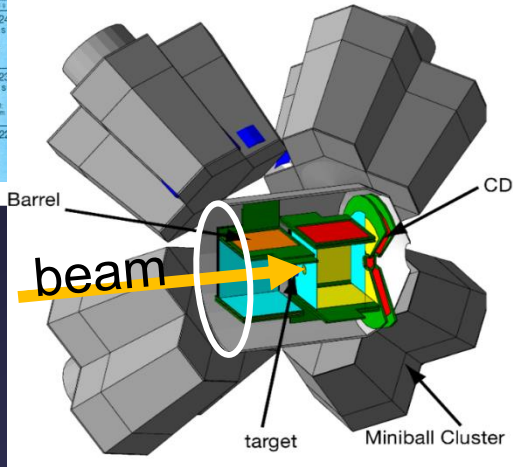




## DWBA calculations of alpha particles emitted following t-transfer reaction





## Reaction data and counting rates:

**Beam:**  $^{132}\text{Sn}$ ,  $E_{\text{beam}} = 510 \text{ MeV}$  (3.9 MeV/A)  
 $8 \cdot 10^5$  pps (on target)

**Target:**  $^7\text{LiF}$ ,  $1.5 \text{ mg/cm}^2$

**Cross section:**  $100 \text{ mb}$  for  $t$ -transfer  
 ( $^{135}\text{Sb}$  production)

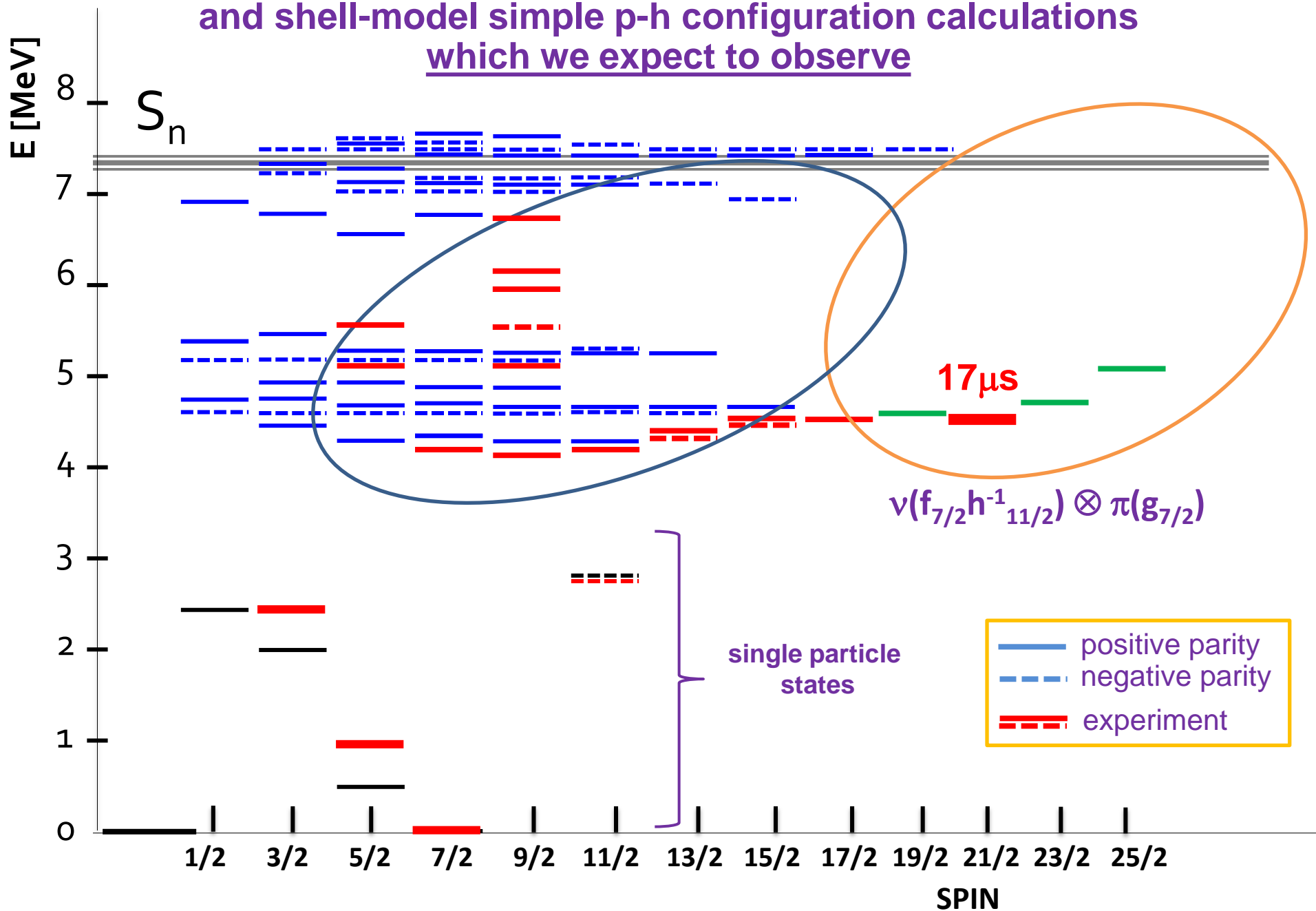
**Final products:** 80% 2n-evap.  $^{133}\text{Sb}$   
 20% 1n-evap.  $^{134}\text{Sb}$

**Counting rates:**  $\approx 1$   $\alpha$ -particle/s in T-REX

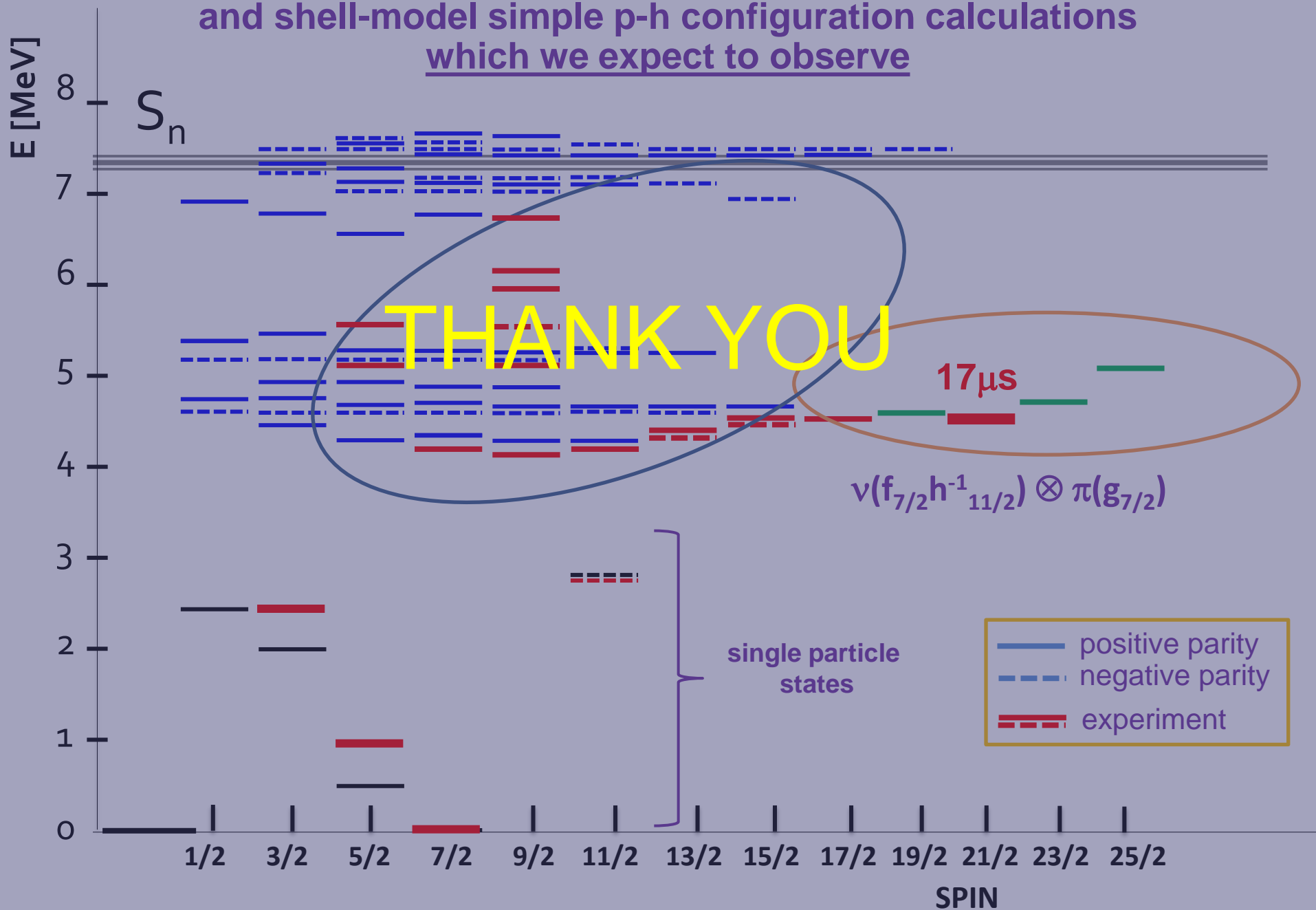
for a  $\gamma$  line with 1% intensity: 300 counts in 7 days

**We ask for 21 shifts**

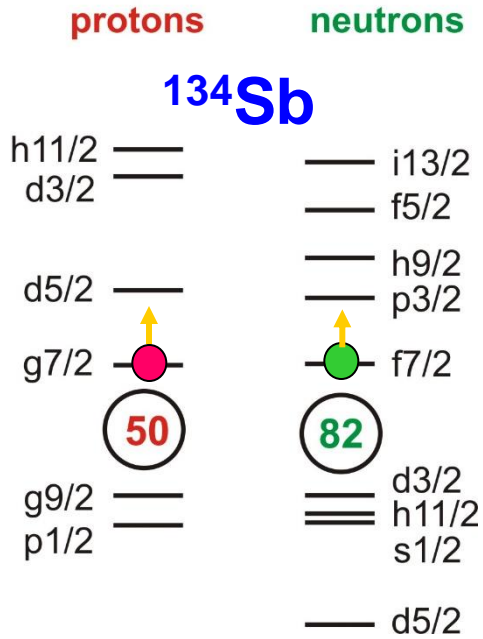
States in  $^{133}\text{Sn}$  predicted by the particle-phonon  
and shell-model simple p-h configuration calculations  
which we expect to observe



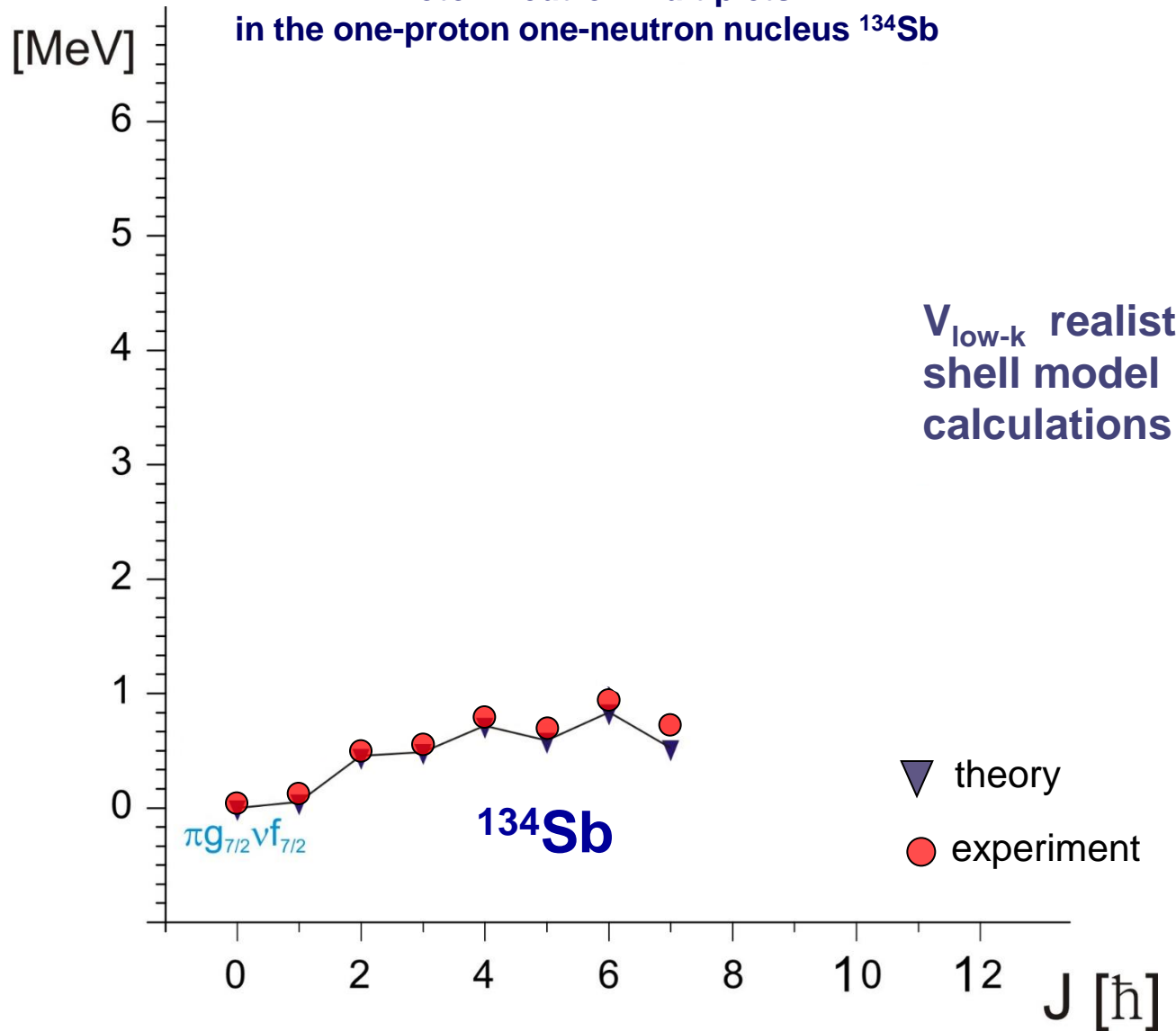
States in  $^{133}\text{Sn}$  predicted by the particle-phonon  
and shell-model simple p-h configuration calculations  
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# Single particle orbitals

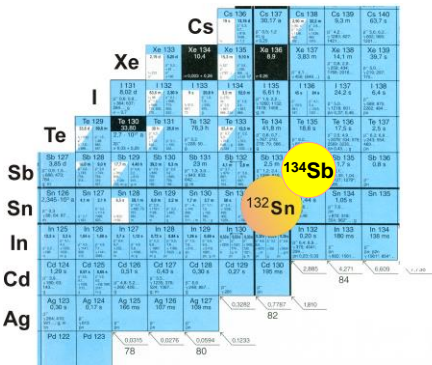


# Proton-neutron multiplets in the one-proton one-neutron nucleus $^{134}\text{Sb}$



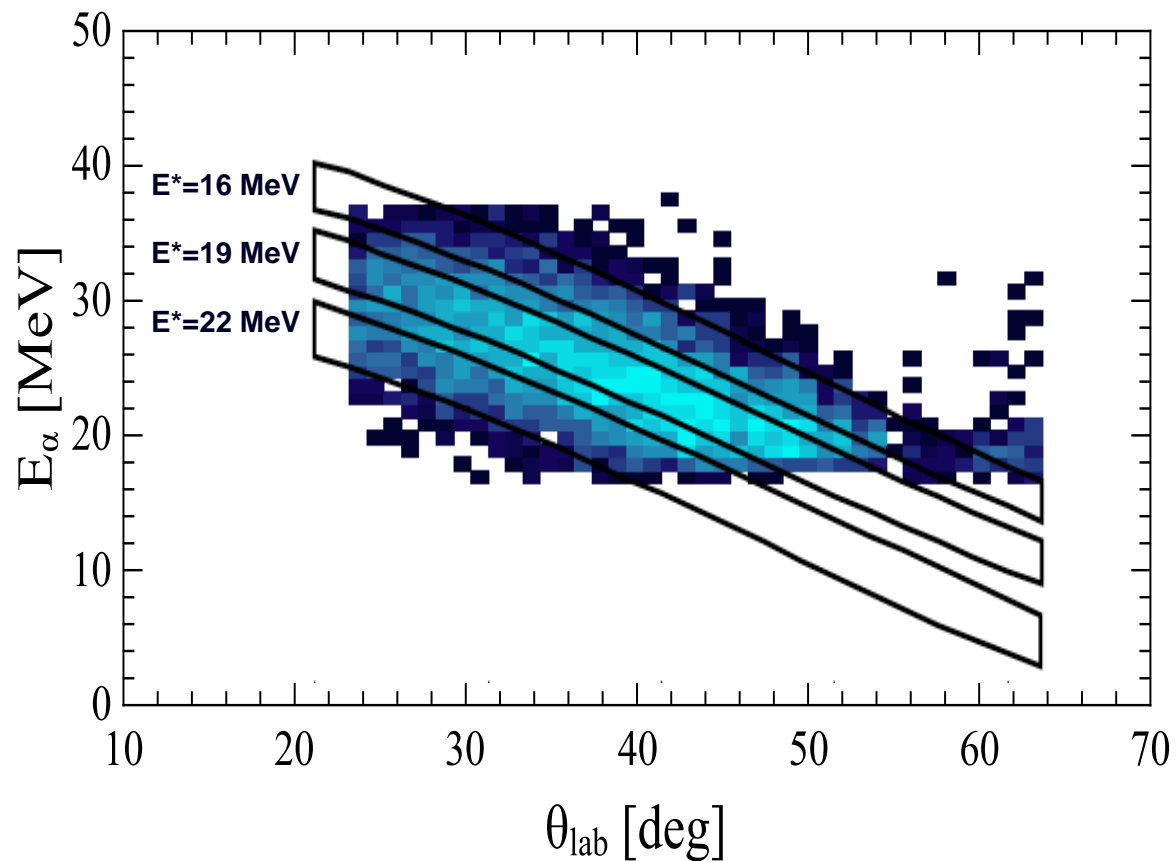
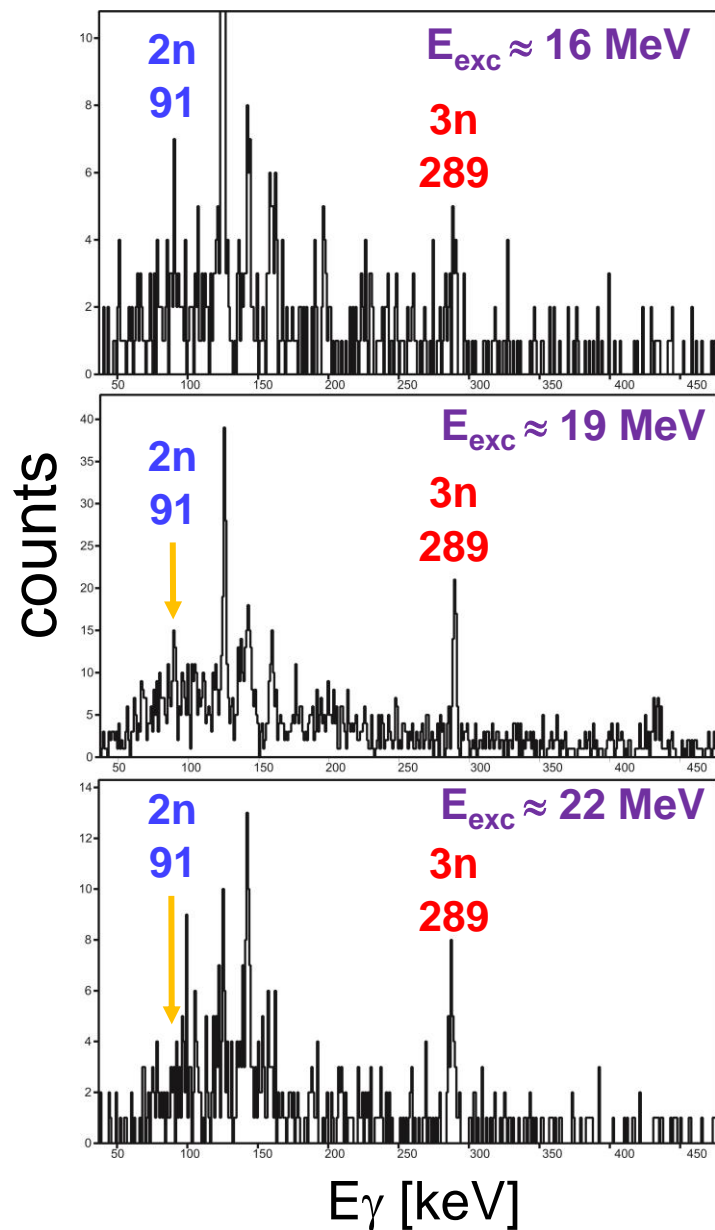
$V_{\text{low-k}}$  realistic shell model calculations

▼ theory  
● experiment



What little is known comes mainly from beta-decay studies or spectroscopic investigations of fission products.

# Identification method



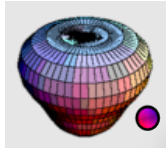
# Theoretical Description

## PHENOMENOLOGICAL

Particle-phonon  
WEAK coupling calculations  
(Bohr & Mottelson)

$^{49}\text{Ca}$

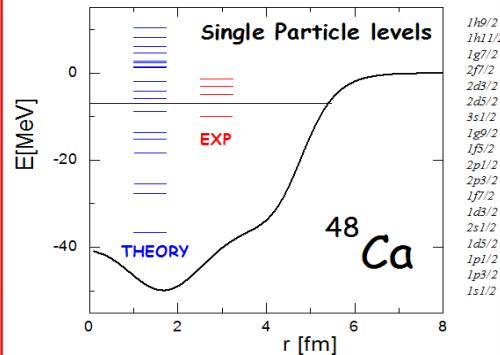
$3^- \otimes p_{3/2}$   
 $[\lambda \otimes j_1]_1$



Multiplet of States  $9/2^+, 7/2^+, 5/2^+, 3/2^+$

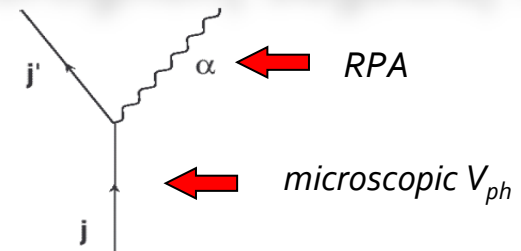
Energy Shift 
$$\delta E(I)_{a,b,c,d} = \pm \sum_{j_2} \frac{\hbar^2(j_2, j_1, \lambda)}{\varepsilon(j_1) - \varepsilon(j_2) \pm \hbar\omega_\lambda} \times C_{recoupling}$$

- $\hbar\omega_\lambda, B(E\lambda)$   
→ Exp. Values/Theory
- s.p. Energies  
 $\varepsilon(j_1), \varepsilon(j_2)$   
→ HF - SkX
- matrix element  
 $h(j_2, j_1, \lambda)$   
→ Bohr & Mott.



## MICROSCOPIC

Calculations based on  
SELF-CONSISTENT Scheme  
(Colò, Bortignon, Sagawa, ...)



- Hartree-Fock with  $V_{\text{eff}}$   
→ short-range correlations included
- Particle-Vibration coupling on top  
→ same Hamiltonian or EDF
- NO approximation in the vertex

**EXACT treatment of COUPLING**  
**use of WHOLE phonon wave function**

Need for More Experimental Input