

2⁺ Anomaly and Configurational Isospin Polarization of ¹³⁶Te



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DARMSTADT

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(CSIC Madrid)

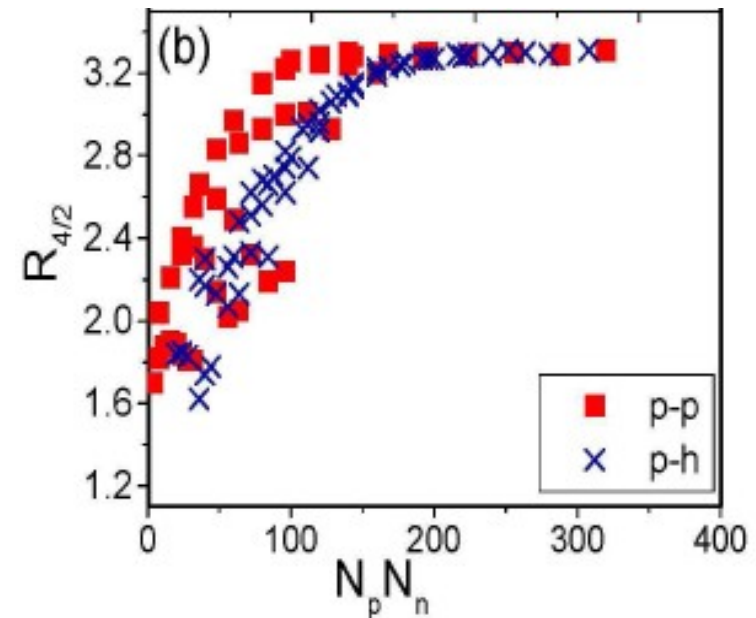
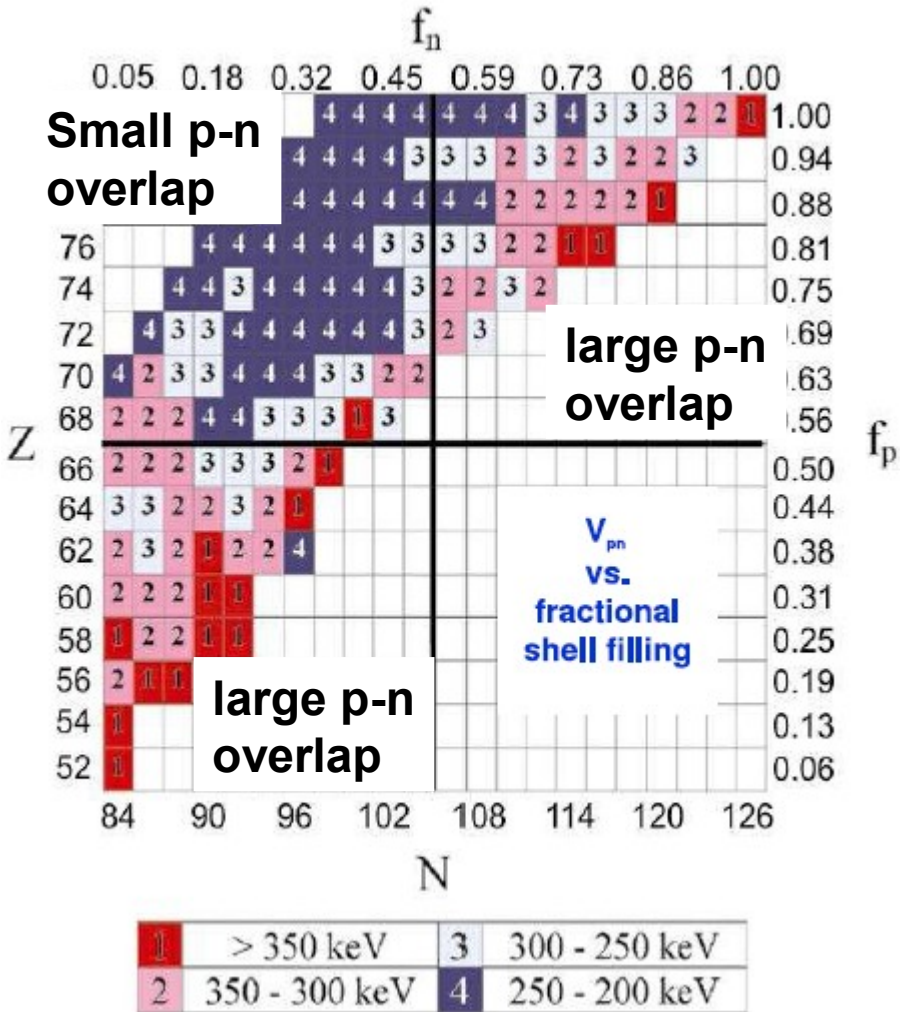
T. Stora

(CERN)

Contact: E. Rapisarda

Observables sensitive to V_{pn}

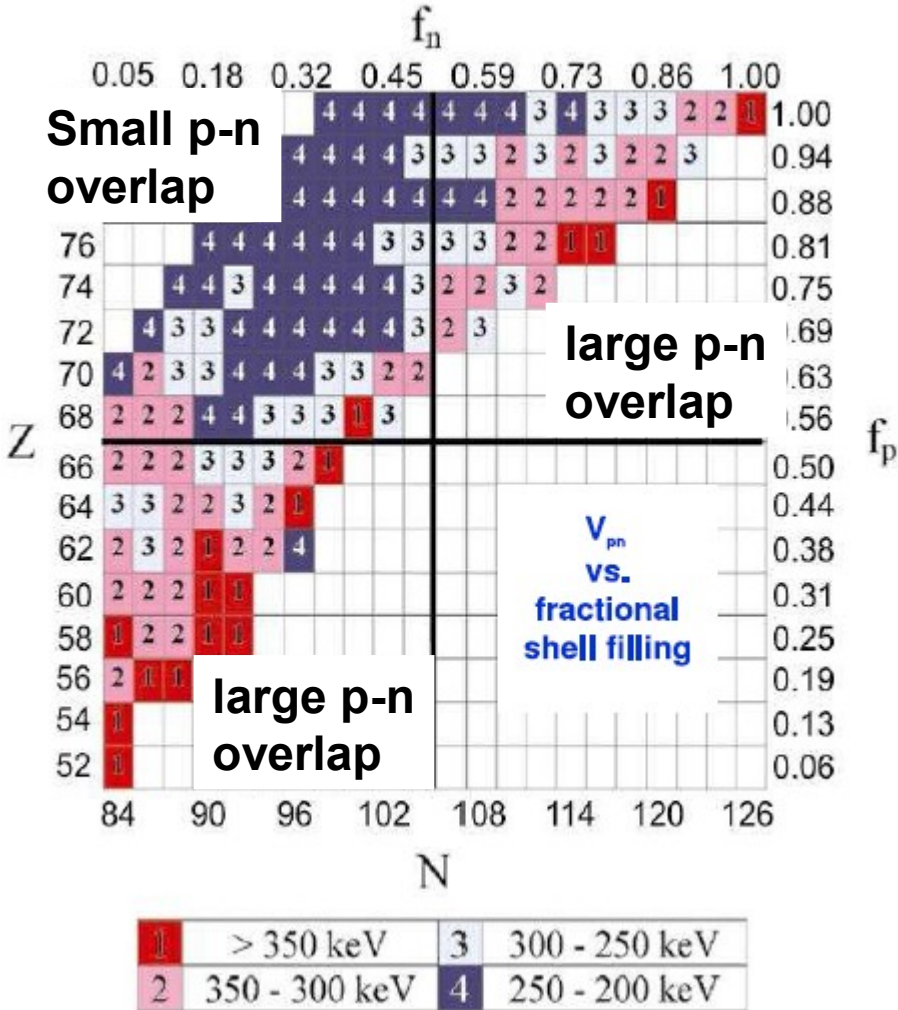
R.B. Cakirli and R.F. Casten, PRL 96, 132501 (2006)



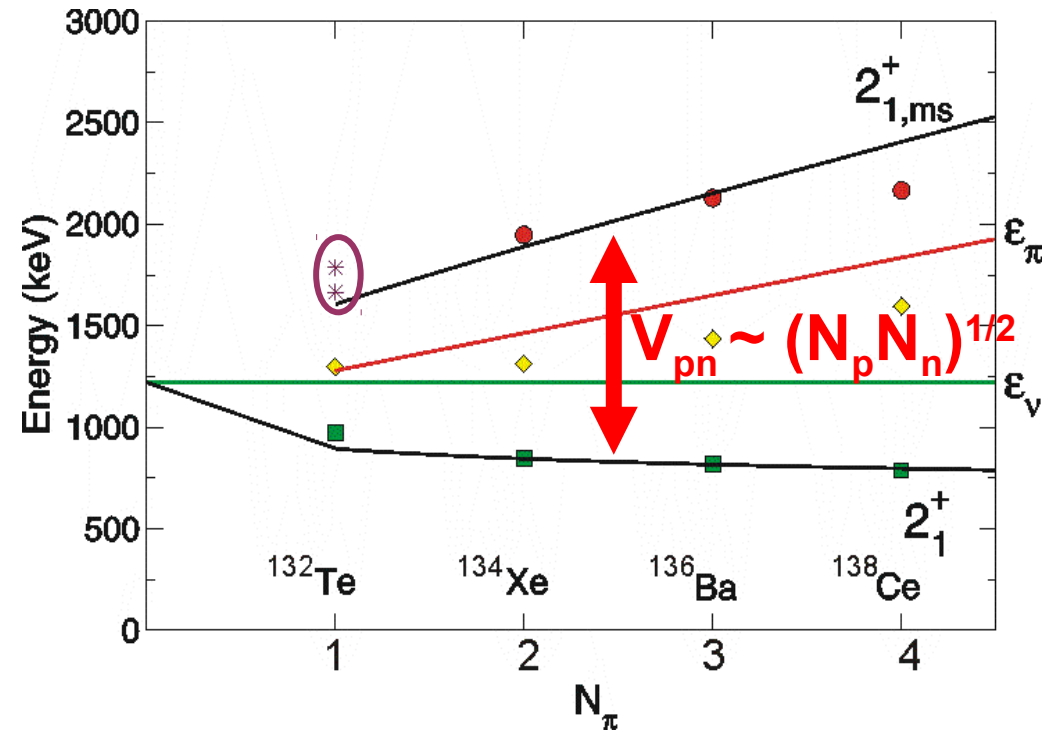
$$\delta V_{pn}(Z, N) = -\frac{1}{4}(\{ME(Z, N) - ME(Z, N - 2)\} - \{ME(Z - 2, N) - ME(Z - 2, N - 2)\})$$

Observables sensitive to V_{pn}

R.B. Cakirli and R.F. Casten, PRL 96, 132501 (2006)



Proton-Neutron degree of freedom in excited-state wave functions



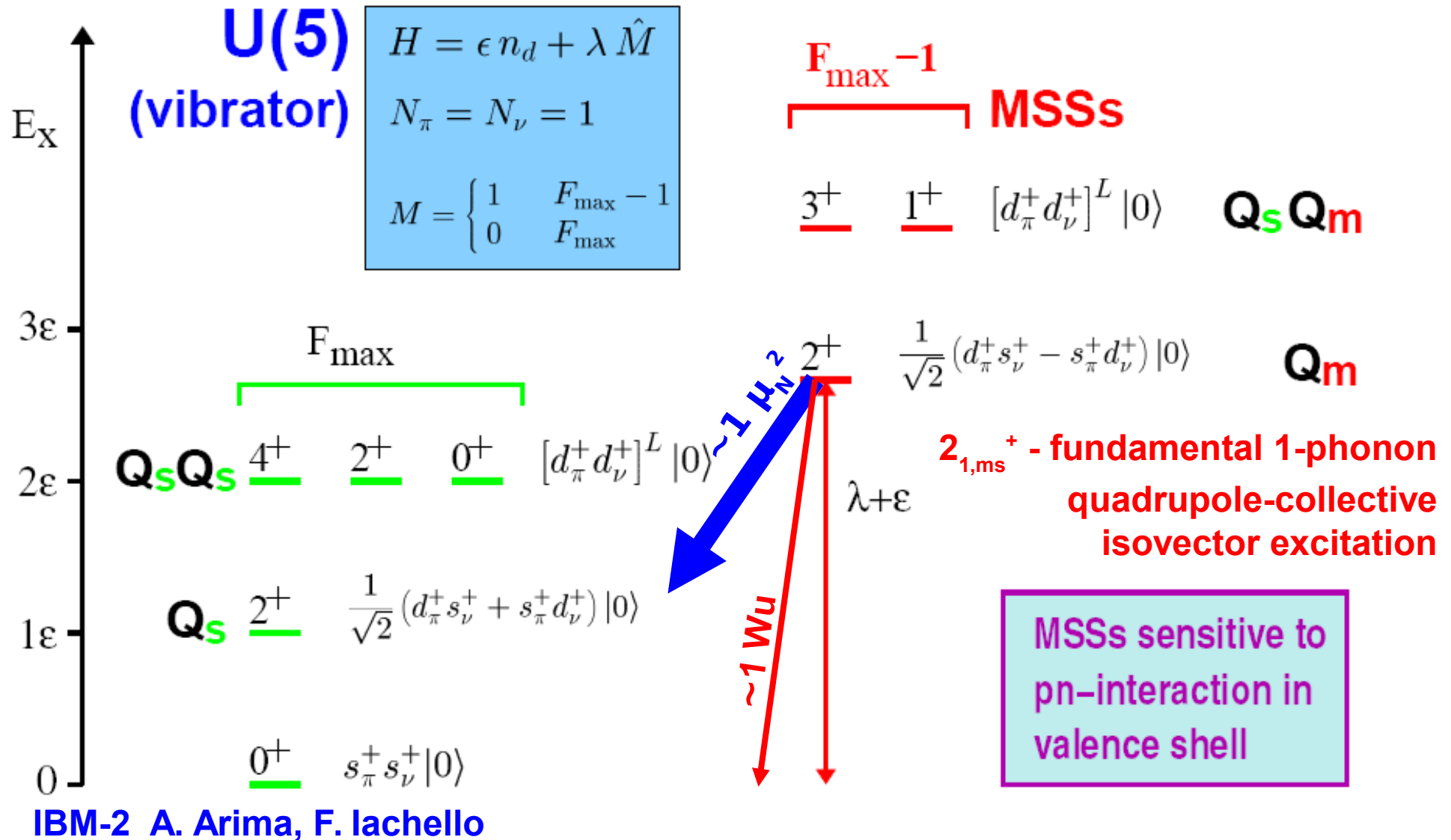
$$\delta V_{pn}(Z, N) = -\frac{1}{4}(\{ME(Z, N) - ME(Z, N - 2)\} - \{ME(Z - 2, N) - ME(Z - 2, N - 2)\})$$

T. Ahn, L. Coquard, N. Pietralla et al., Phys. Lett. B 679, 19 (2010)

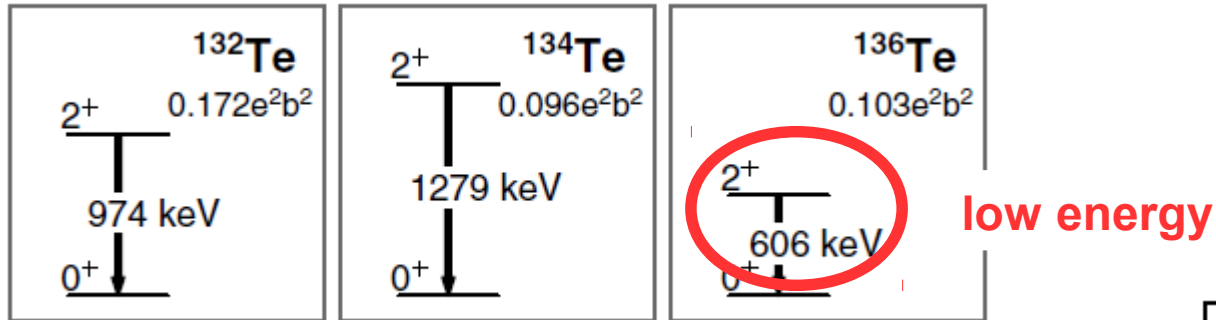
What are Mixed-Symmetry States



Simple Example: Harmonic Oscillator, N=2



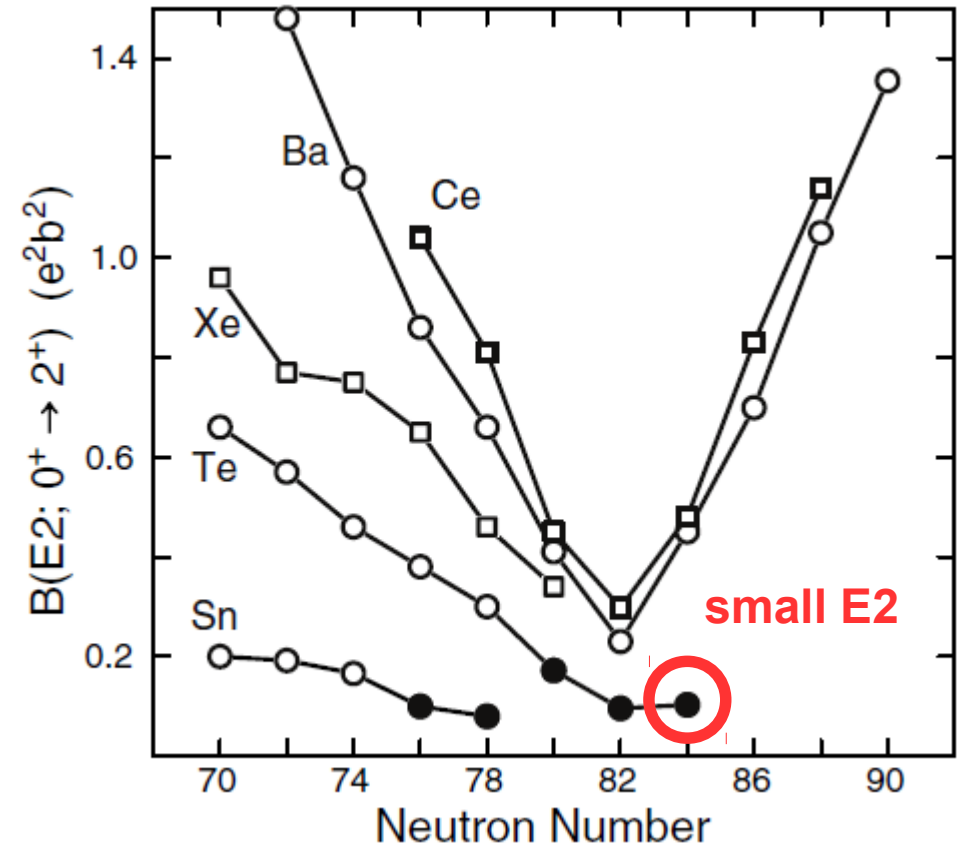
B(E2) "anomaly" in ^{136}Te



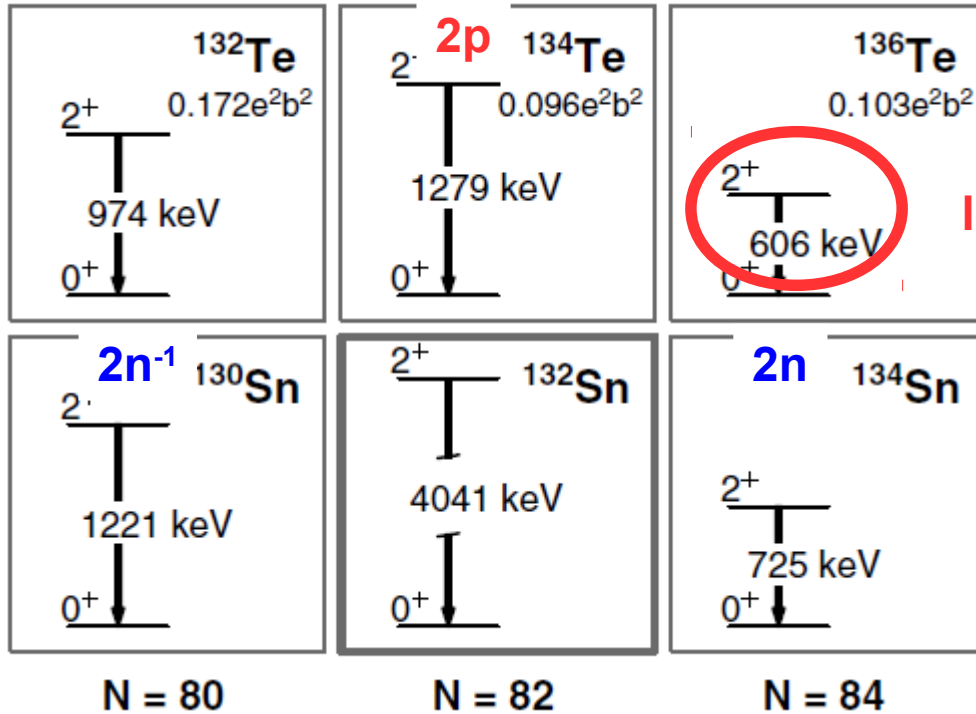
N = 80

N = 82

N = 84



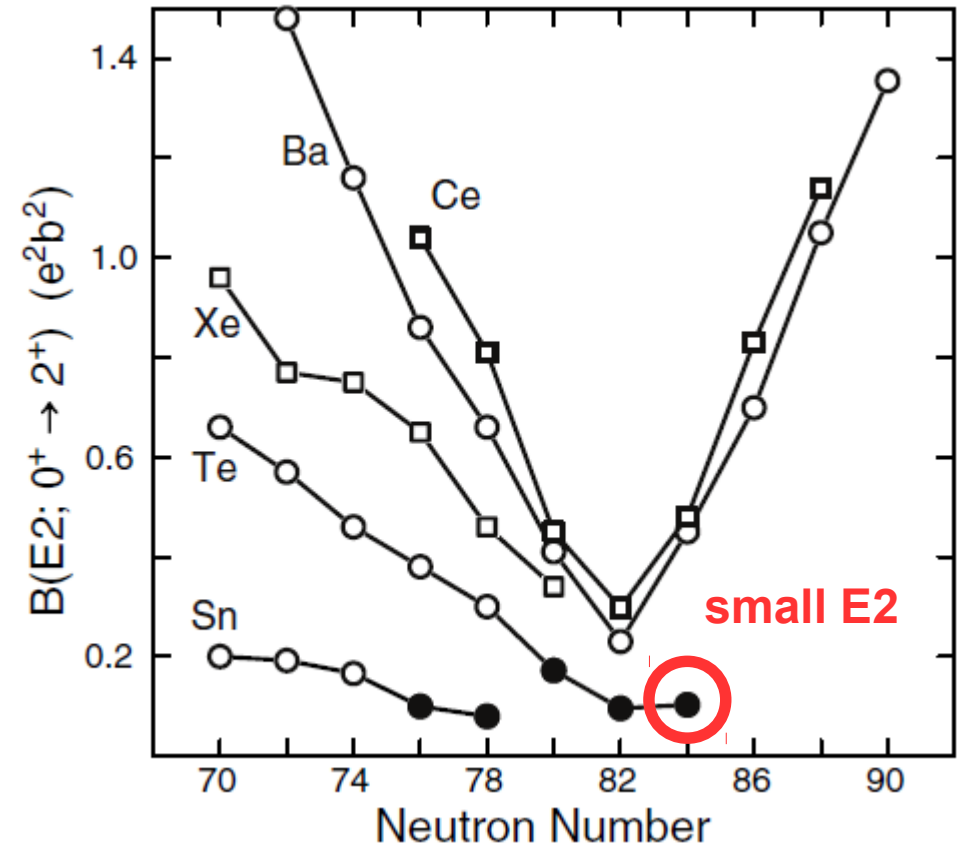
B(E2) "anomaly" in ^{136}Te



low energy

Origin of the anomaly:

Neutron dominance in the 2₁⁺ wave function



small E2

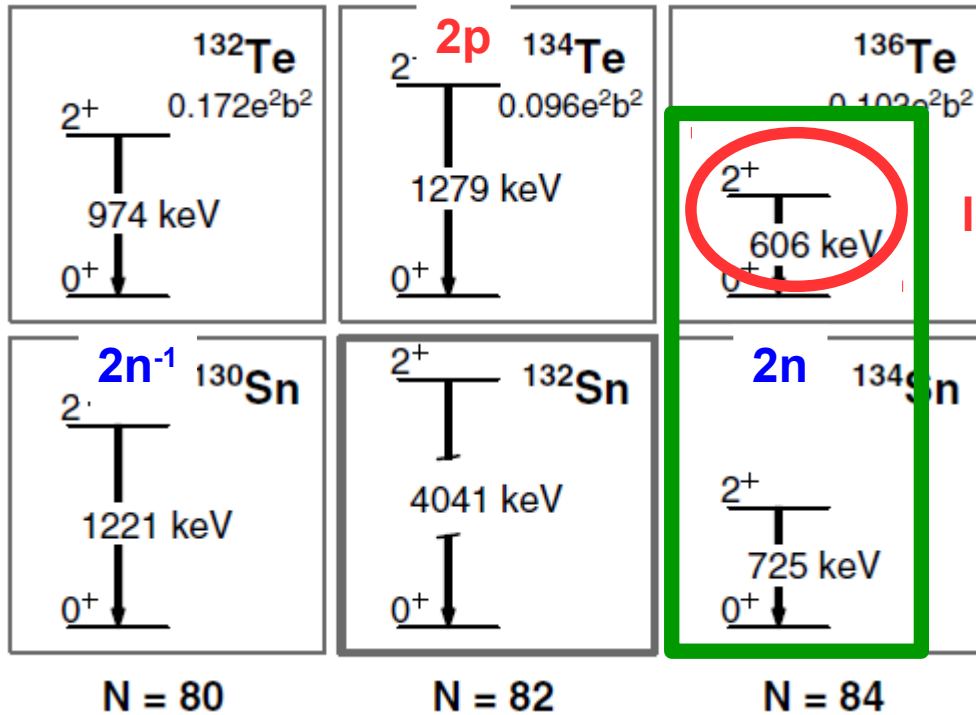
Shell Model:

N. Shimizu, T. Otsuka, T. Mizusaki, M. Honma,
PRC 70, 054313 (2004)

QRPA:

J. Terasaki et al., PRC 66, 054313 (2002)

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low energy

Origin of the anomaly:

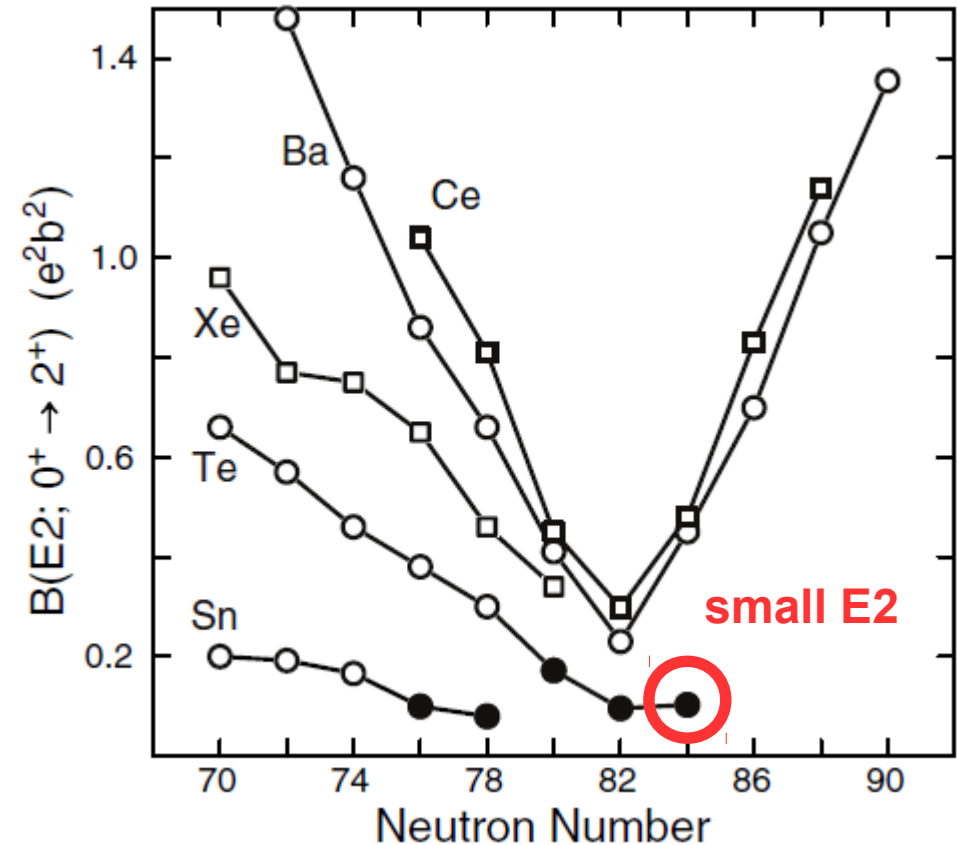
Neutron dominance in the 2_1^+ wave function

Shell Model:

N. Shimizu, T. Otsuka, T. Mizusaki, M. Honma,
PRC 70, 054313 (2004)

QRPA:

J. Terasaki et al., PRC 66, 054313 (2002)

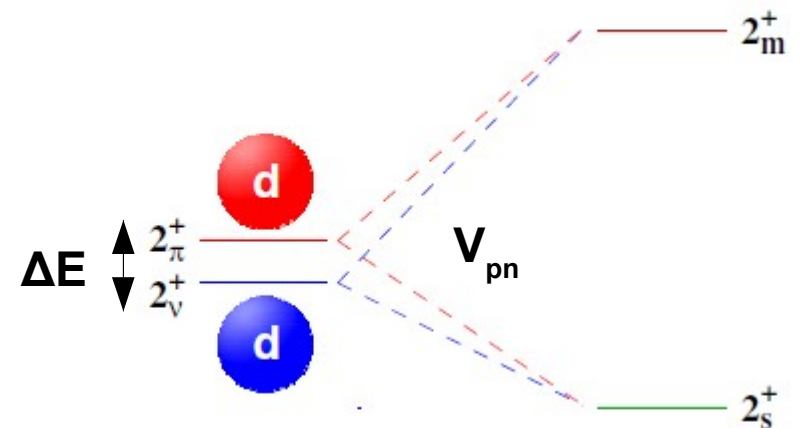
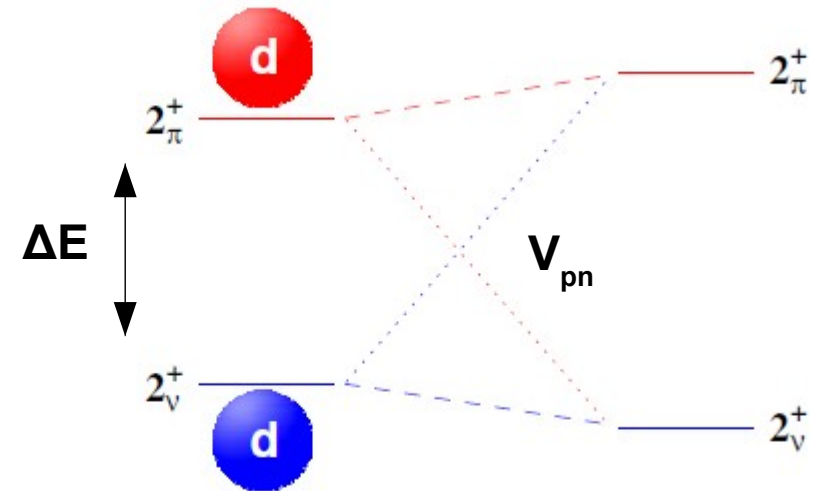


small E2

Configurational Isospin Polarization

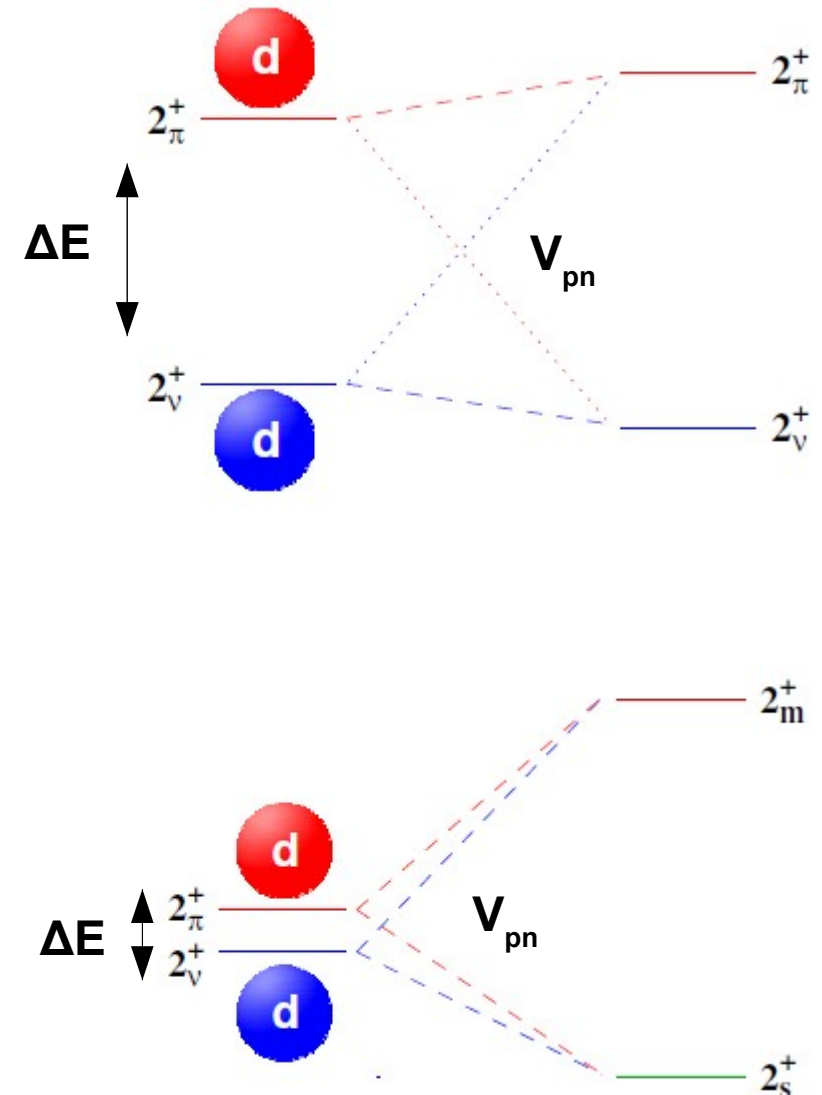
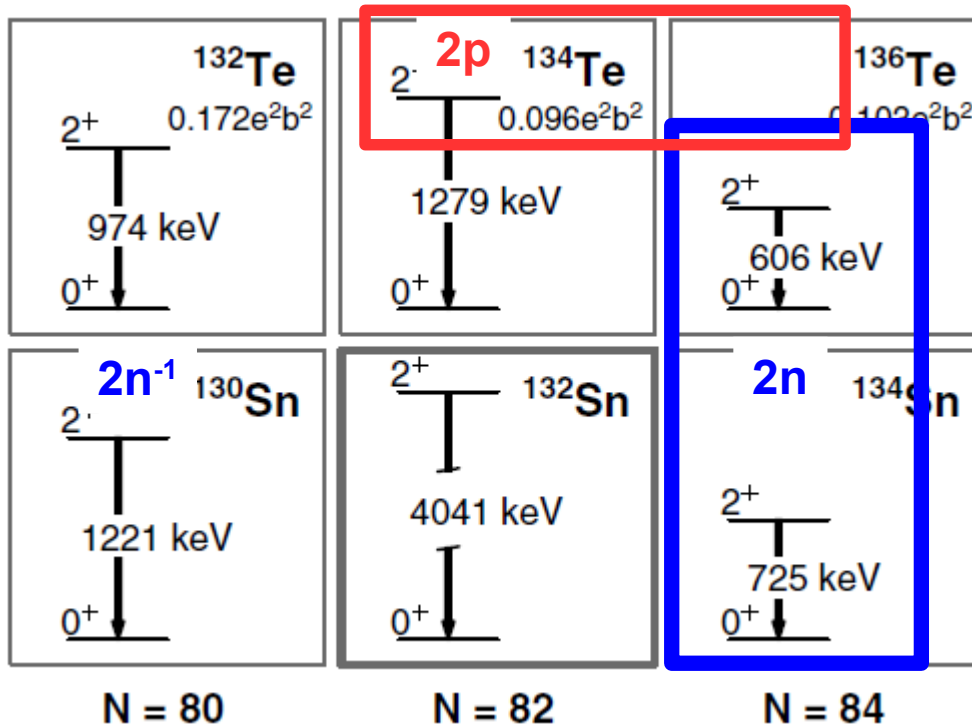


- Structure of FS / MS States sensitive to the interplay of ΔE and V_{pn}

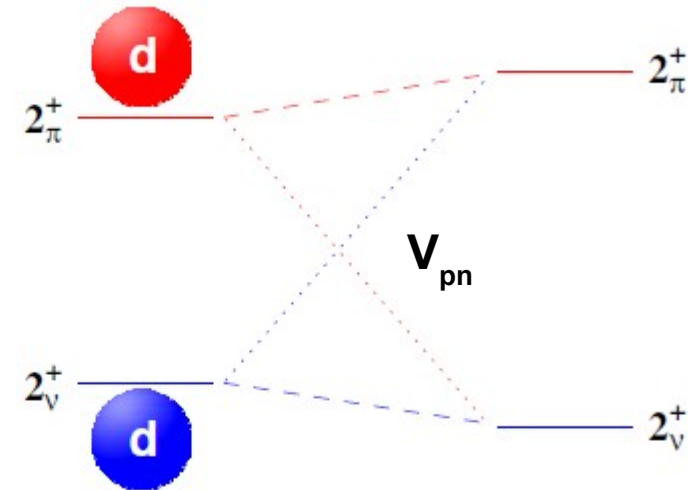
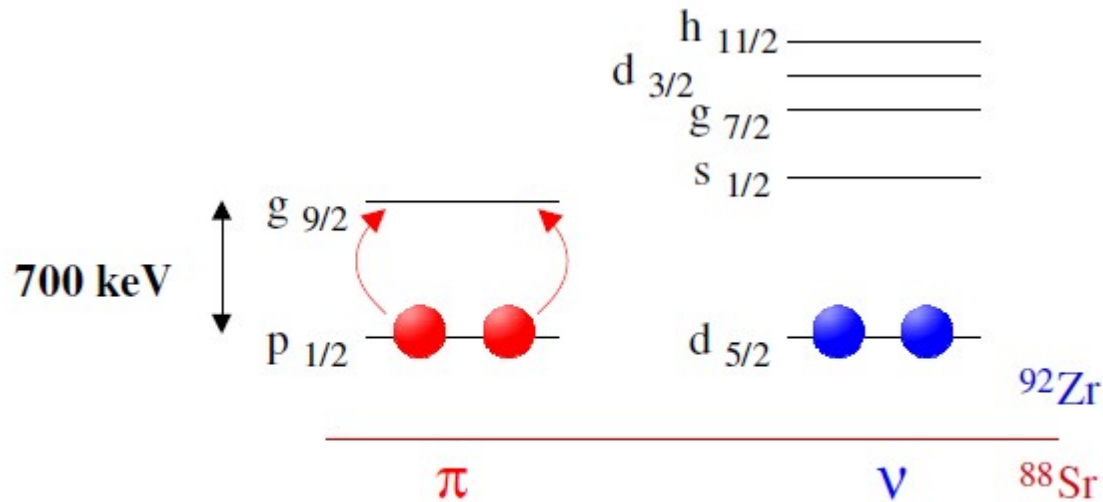


Configurational Isospin Polarization

- Structure of FS / MS States sensitive to the interplay of ΔE and V_{pn}



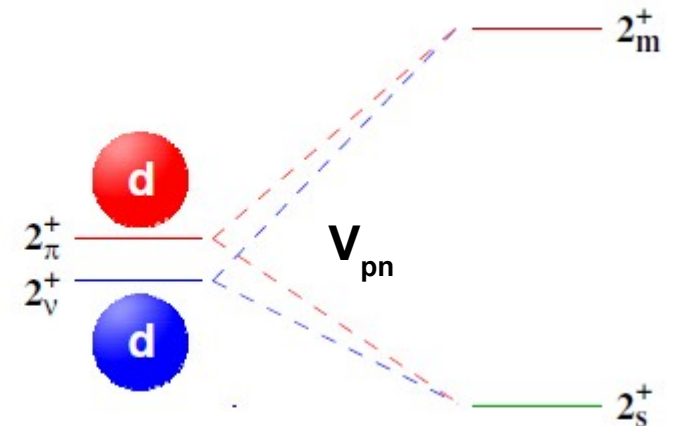
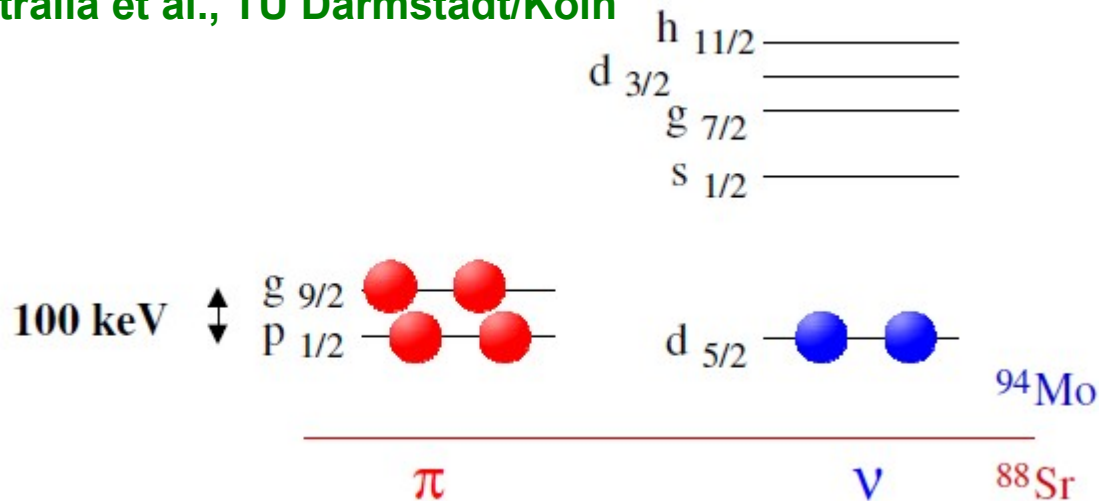
First CIP found at N=52 Zr



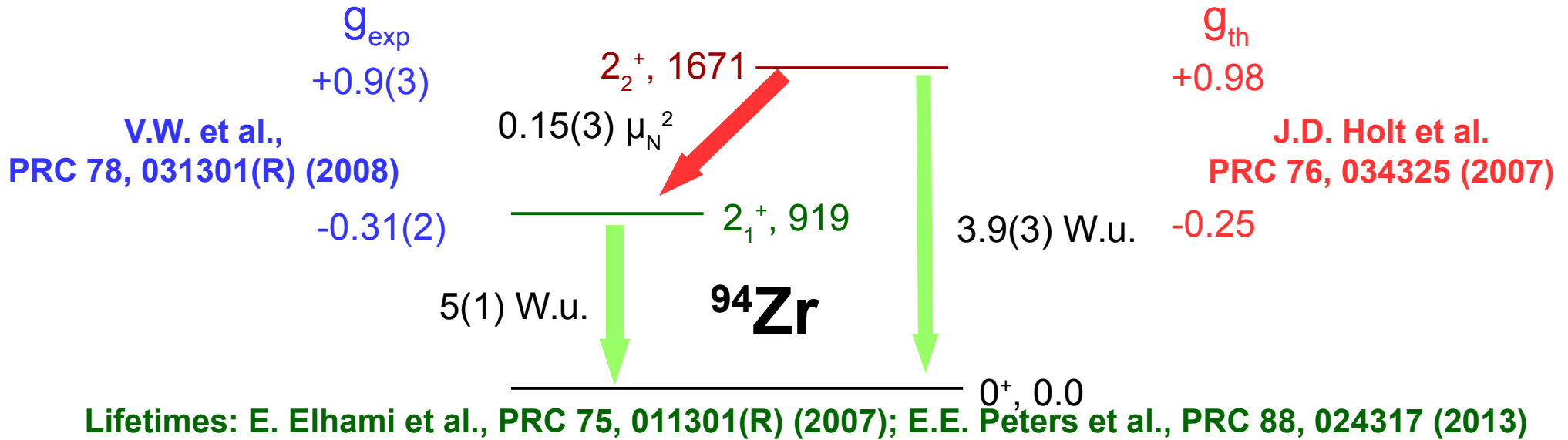
VW et al., Yale/Stuttgart

Yates et al., Lexington

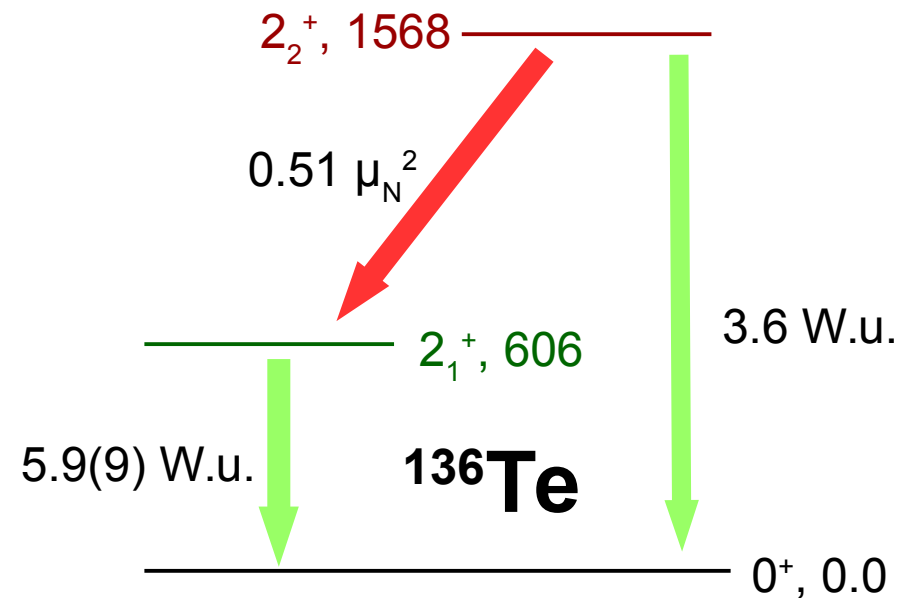
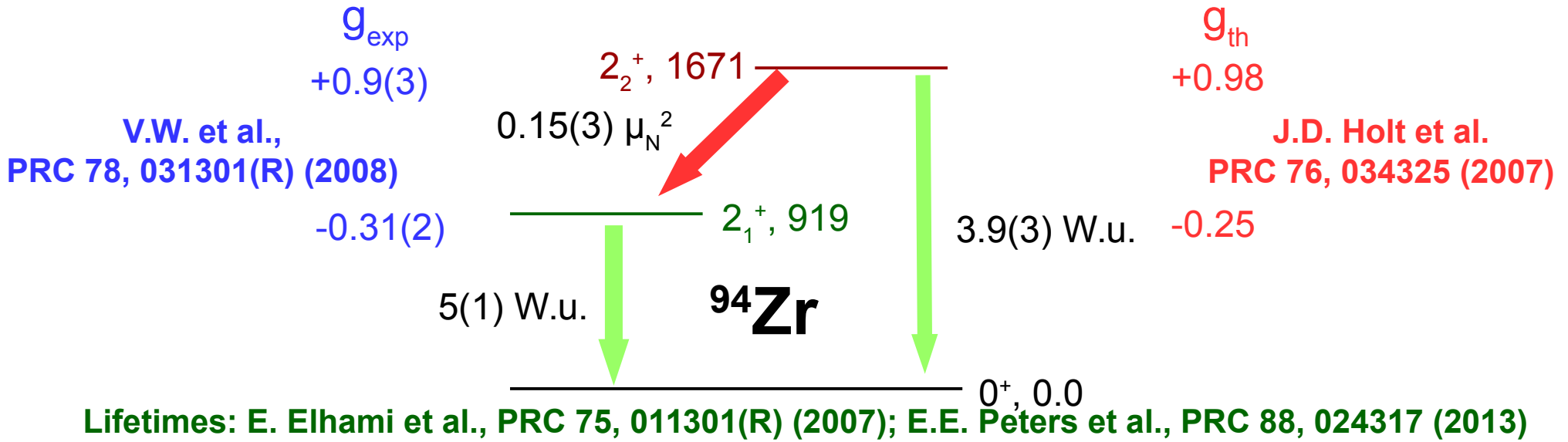
Pietralla et al., TU Darmstadt/Köln



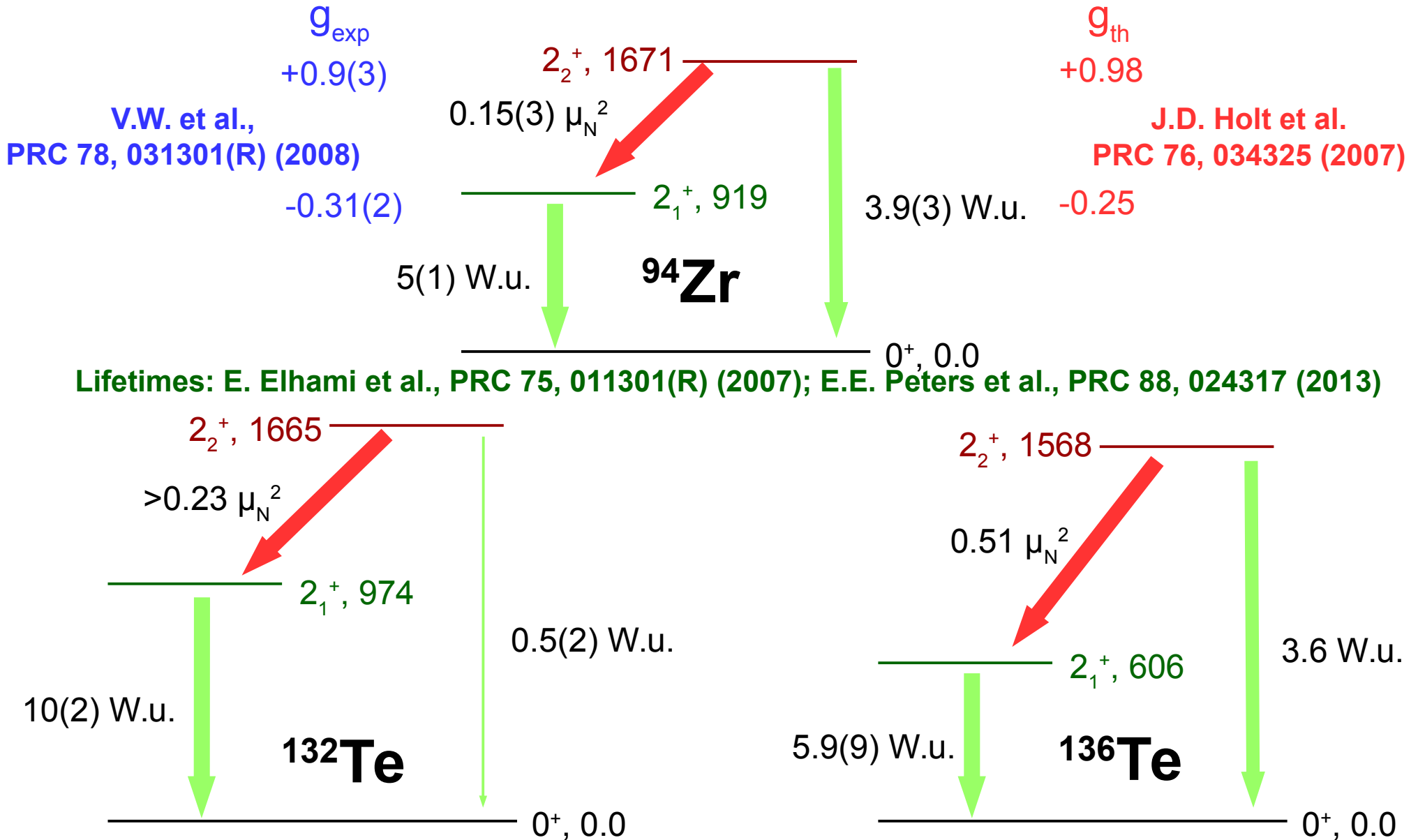
CIP in ^{94}Zr vs. $^{132,136}\text{Te}$



CIP in ^{94}Zr vs. $^{132,136}\text{Te}$

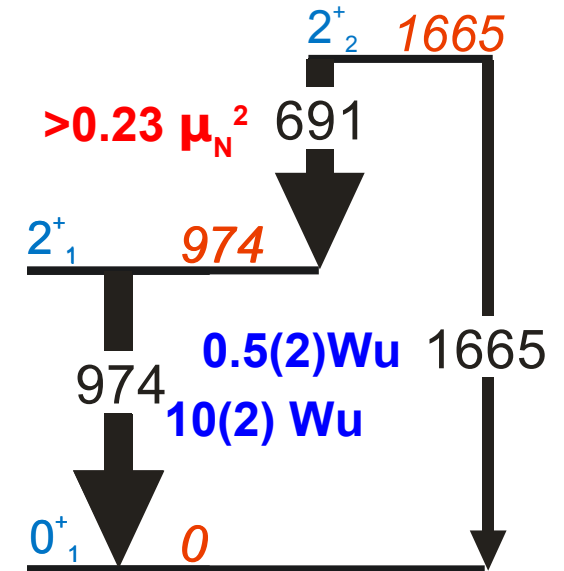
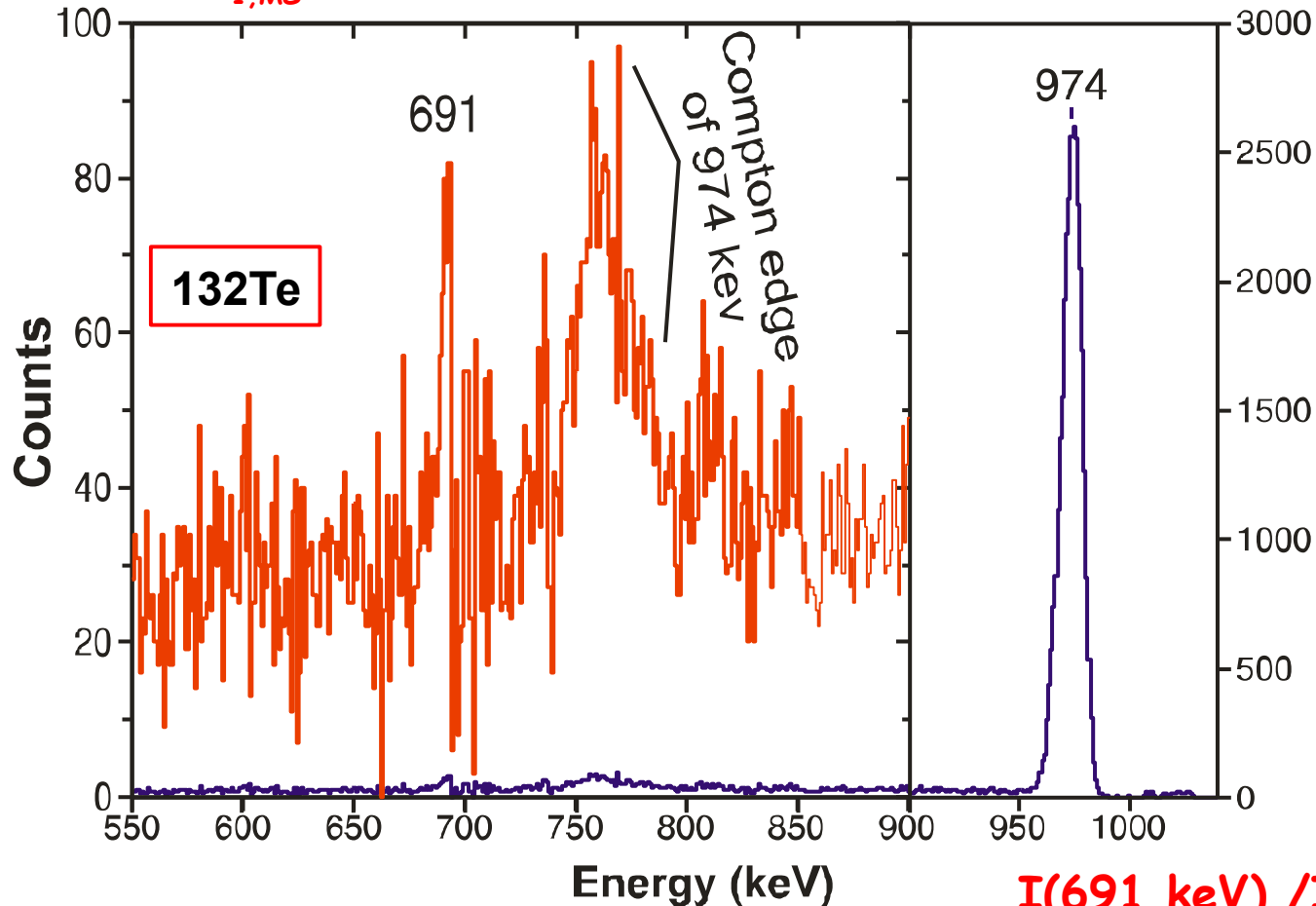


CIP in ^{94}Zr vs. $^{132,136}\text{Te}$



First MS observation with RIB

$2_{1,MS}^+$ observed in coincidence with ^{12}C recoils detected in HyBall.



M. Danchev, G. Rainovski,
N. Pietralla *et al.*,
PRC84 ('11) 061306(R)

$$I(691 \text{ keV}) / I(1665 \text{ keV}) = 100 (52)$$

$$^{132}\text{Te}: \frac{I_\gamma(691 \text{ keV})}{I_\gamma(974 \text{ keV})} = 1.01(28)\%$$

$$\frac{Y(2_2^+)}{Y(2_1^+)} = \frac{\sigma(0_1^+ \rightarrow 2_2^+)}{\sigma(0_1^+ \rightarrow 2_1^+)} \mu \frac{B(E2; 0_1^+ \rightarrow 2_2^+)}{B(E2; 0_1^+ \rightarrow 2_1^+)}$$

New CIP case predicted: ^{136}Te



2+1 and 2+2 have significant E2 -> 1-phonon states
Strong M1 between them -> 2+2 = 2+1, MS

	$\lambda_i^{\pi} = 2_i^+$	Energy (MeV)		Structure	$B(E2; 0_{gs}^+ \rightarrow 2_i^+)$ ($e^2\text{fm}^4$)		$B(E2; 2_i^+ \rightarrow 2_1^+)$ ($e^2\text{fm}^4$)		$B(M1; 2_i^+ \rightarrow 2_1^+)$ (μ_N^2)	
		Expt.	Theory		Expt.	Theory	Expt.	Theory	Expt.	Theory
^{136}Te	2_1^+	0.606	0.92	97% $[2_1^+]_{\text{QRPA}}$	1220 ± 180	1120				
	2_2^+	1.568	2.01	94% $[2_2^+]_{\text{QRPA}}$	740		20		0.51	

$[2_1^+]_{\text{QRPA}} = \sim 86\%$ Neutron, $[2_2^+]_{\text{QRPA}} \sim 68\%$ Proton (opposite phase)

QPM: A.P. Severyukhin, N.N. Arsenyev, N. Pietralla, and V.W., PRC 90, 011306(R) (2014)

Other theory:

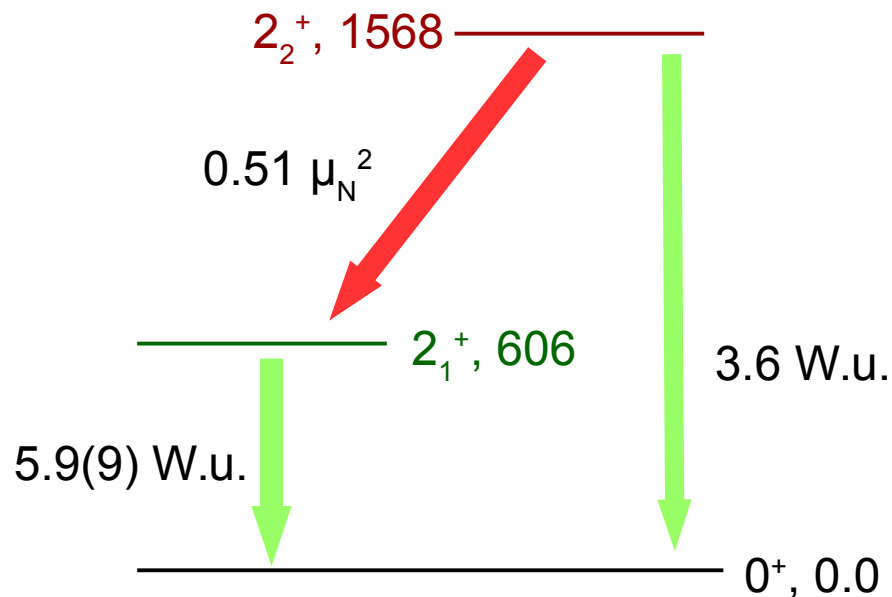
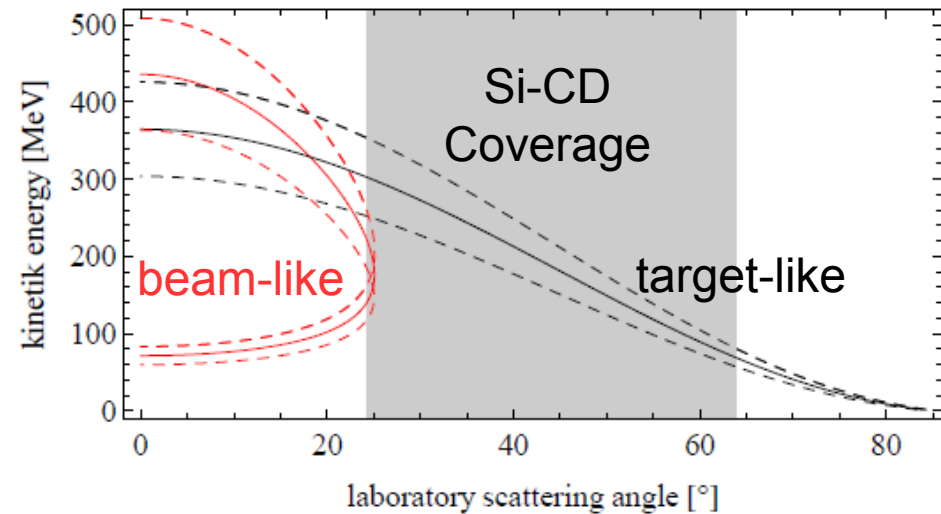
Shell Model: N. Shimizu, T. Otsuka, T. Mizusaki, M. Honma, PRC 70, 054313 (2004)

2_1^+ neutron dominated; 2_2^+ is MS state

CIP in ^{136}Te : Proposed Experiment



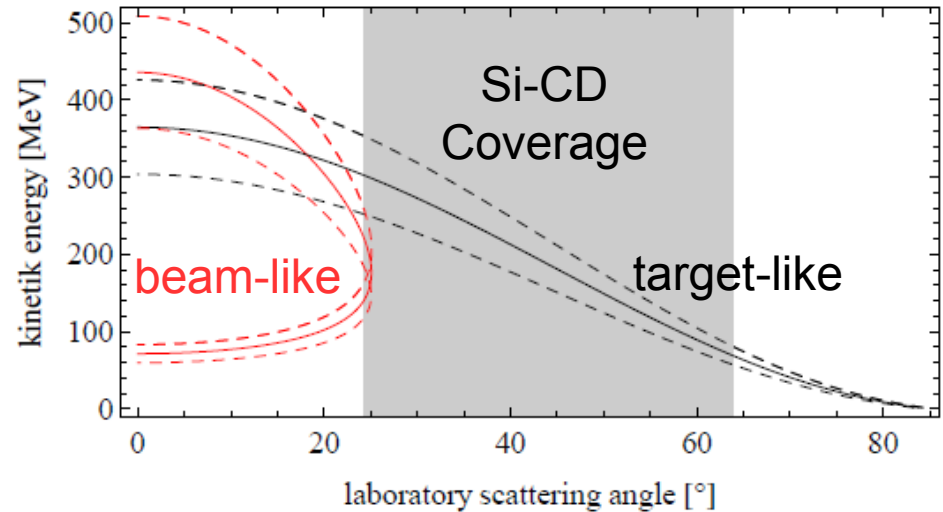
Measure E/M matrix elements
from Coulex yields using
MINIBALL + Si-CD



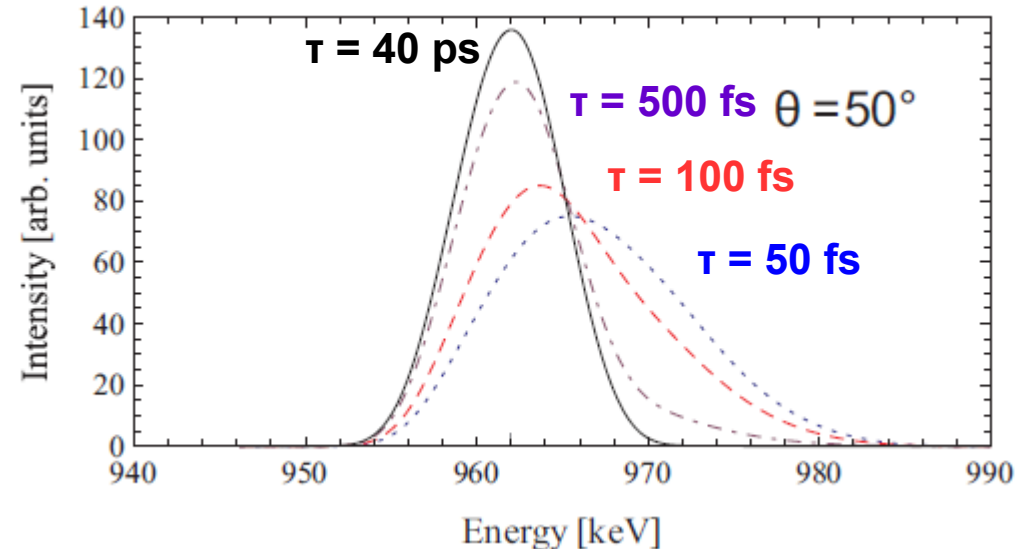
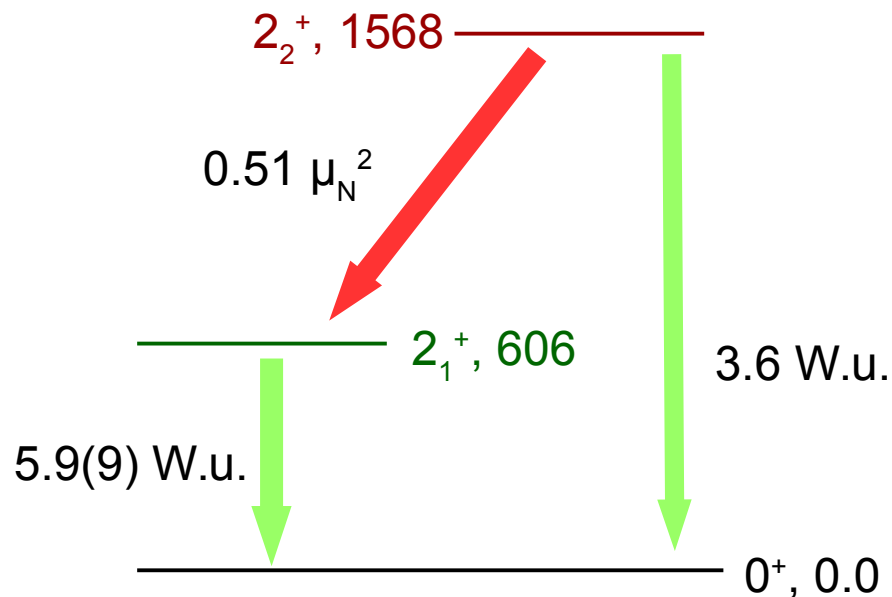
CIP in ^{136}Te : Proposed Experiment



Measure E/M matrix elements
from Coulex yields using
MINIBALL + DSSD



In addition, measure ~ 100 fs 2_2^+ lifetime
through differential DSAM



^{136}Te beam:

- Contaminants (TAC mentions ^{136}Cs , maybe ^{136}Xe) to be reduced to ~50% of total rate, in order to reduce target excitation from contaminants (->laser ionization would be desirable, needs to be quantified at ISOLDE)
- Te beam needs development / knowledge on contaminants
- INTC already recommended development of beam (P-342, Kröll) (^{136}Te focus 2_1^+ B(E2))
- Synergy with proposal INTC-P-296 (Grahm) ($^{116,118}\text{Te}$)

Request



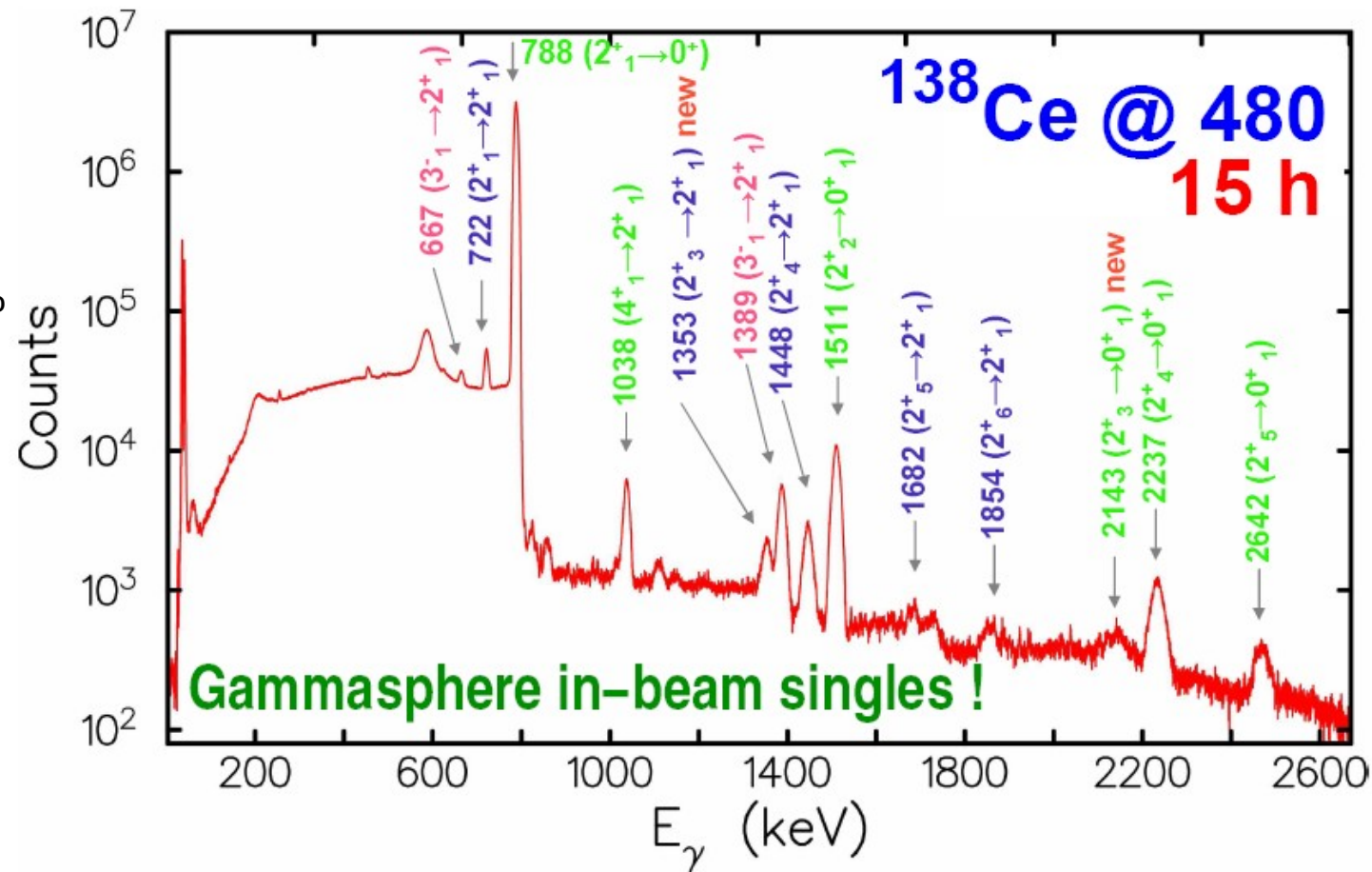
- ^{136}Te beam $\sim 10^5$ pps on target, 510 MeV = 3.75 A MeV
- ^{58}Ni target, 3 mg/cm² for relative Coulex yields and diff. DSAM
- MINIBALL + Si-CD detector
- 3 shifts (one day): test beam production / impurity analysis
- 6 shifts (two days): data run
- -> est. Yield 2^+_{ms} : ~ 1000 counts

Example of Data (e.g. ^{138}Ce @ 480 MeV [1])



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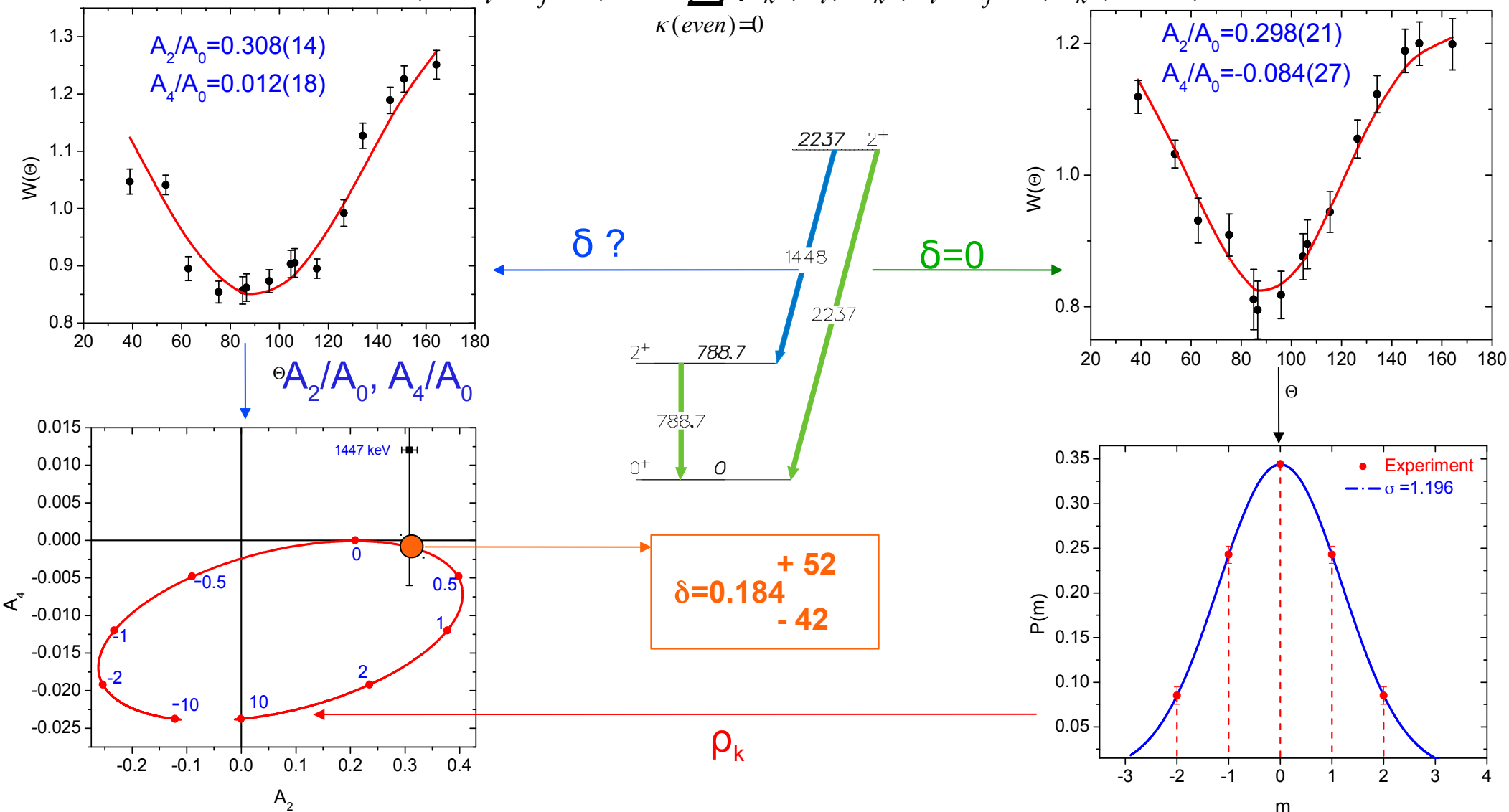
- Background subtraction
- Doppler shift corrections
- Lorentz boost corrections ($v \sim 6\%$ c)
- Angular distributions (Gammasphere=17 rings, 17θ)
- Coulex analysis: Coulex codes (CLX, Gosia)



[1] G.Rainovski, N. Pietralla et al., *Phys. Rev. Lett.* **96** 122501 (2006).

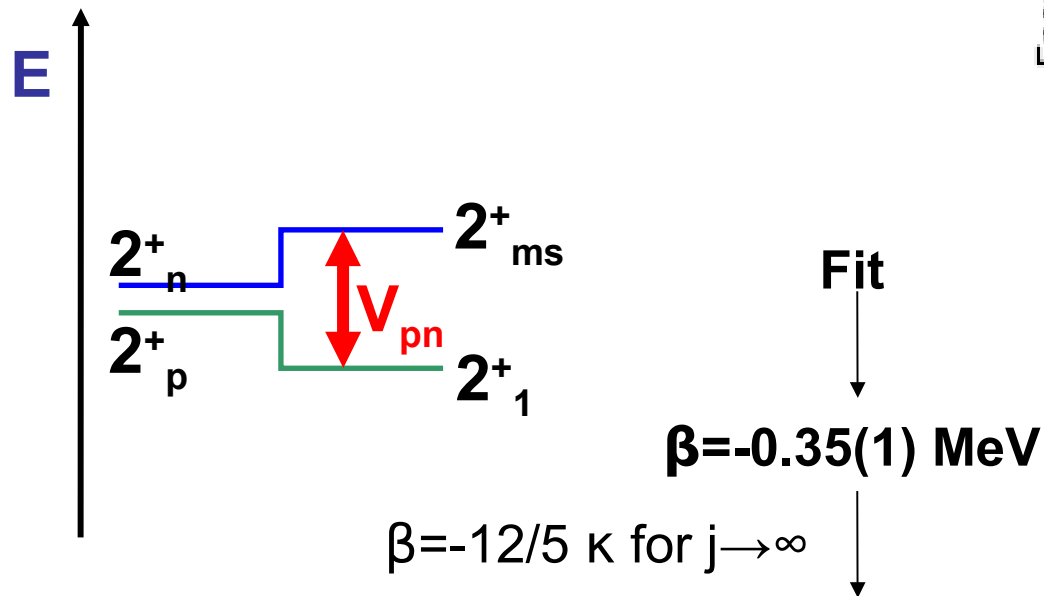
Multipolarities from angular distribution (^{138}Ce)

$$W(\theta, J_i, J_f, \delta) = \sum_{\kappa(\text{even})=0}^2 \rho_{\kappa}(J_i) A_{\kappa}(J_i, J_f, \delta) P_{\kappa}(\cos \theta)$$



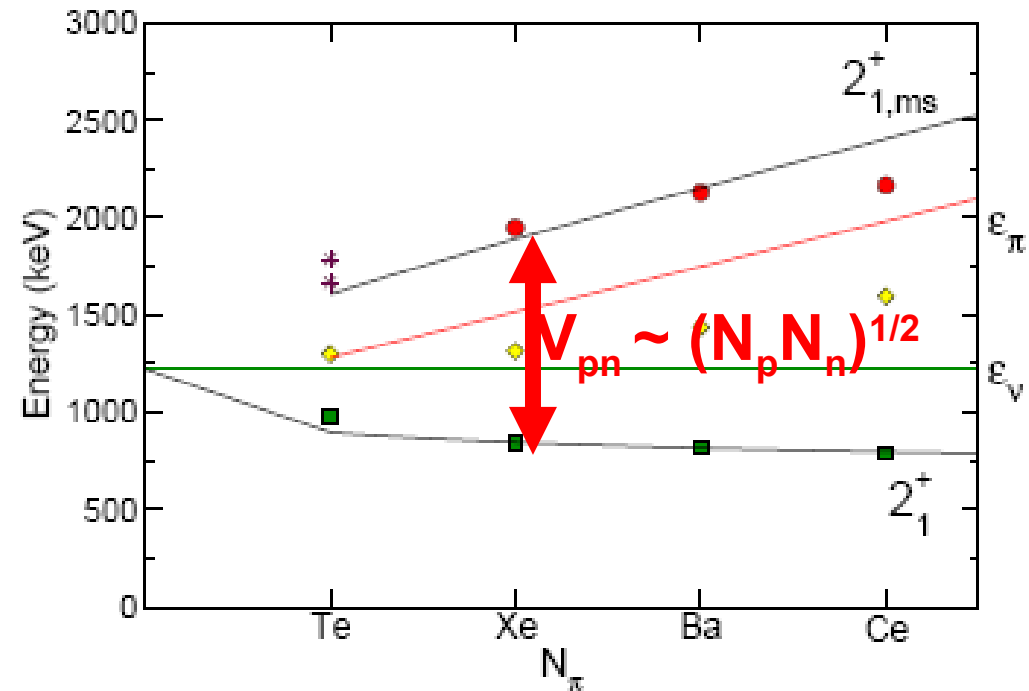
Evolution of the $2^+_{1,ms}$ in $N=80$

$$H = \begin{pmatrix} \epsilon_\pi & V_{\pi\nu} \\ V_{\pi\nu} & \epsilon_\nu \end{pmatrix} \quad \text{with } V_{\pi\nu} = \beta (N_\pi N_\nu)^{1/2}$$



$\kappa = -0.15(1) \text{ MeV}$

agrees with Sau & Heyde 1981



$$\epsilon_\pi = a + b * (N_\pi - 1) \text{ with } a = E(2^+_1) \text{ of } ^{134}\text{Te}$$

$$\epsilon_\nu = cst = E(2^+_1) \text{ of } ^{130}\text{Sn}$$

$$E_{AV} = \frac{\epsilon_\pi + \epsilon_\nu}{2}$$

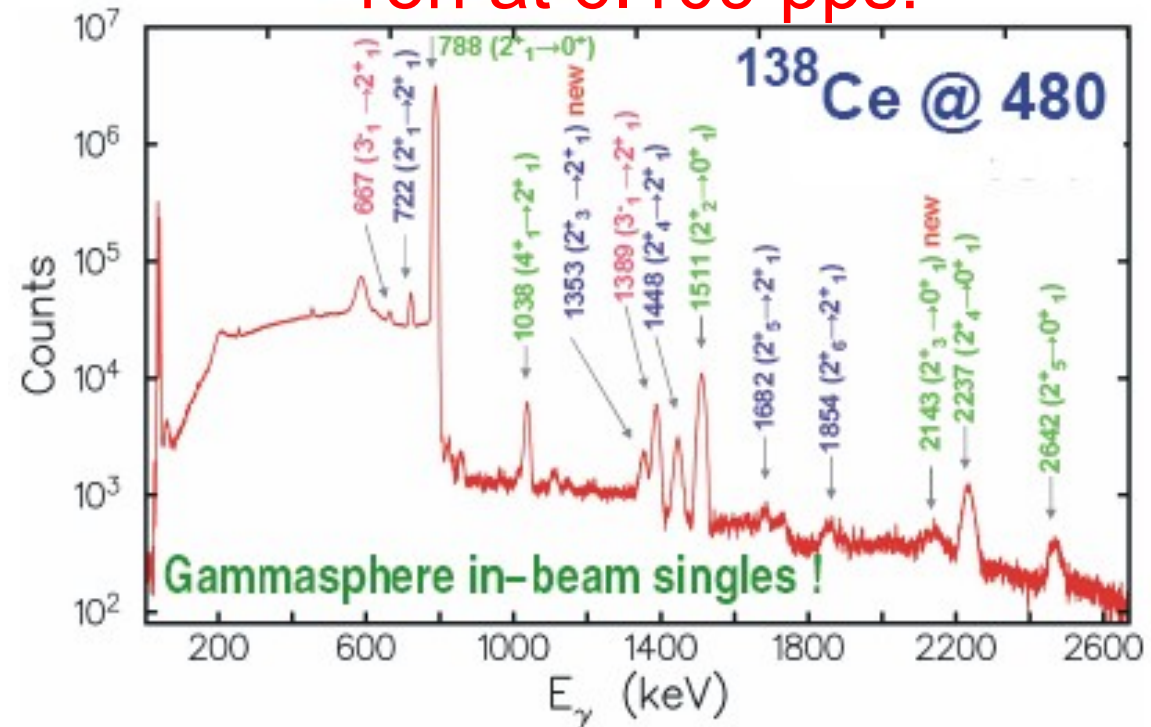
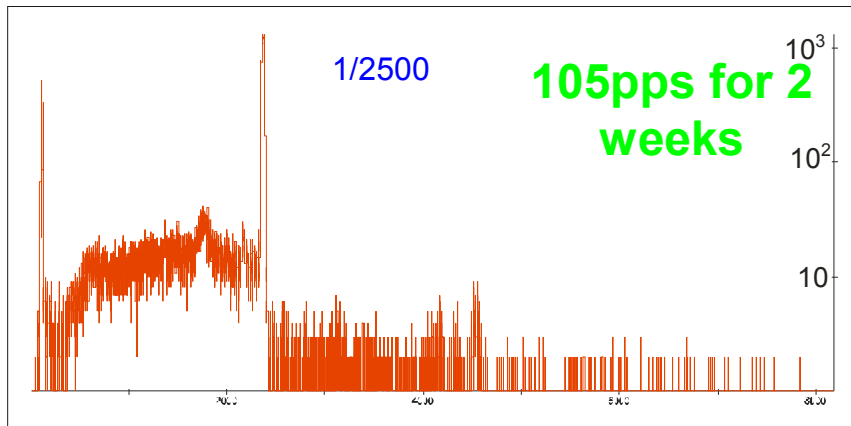
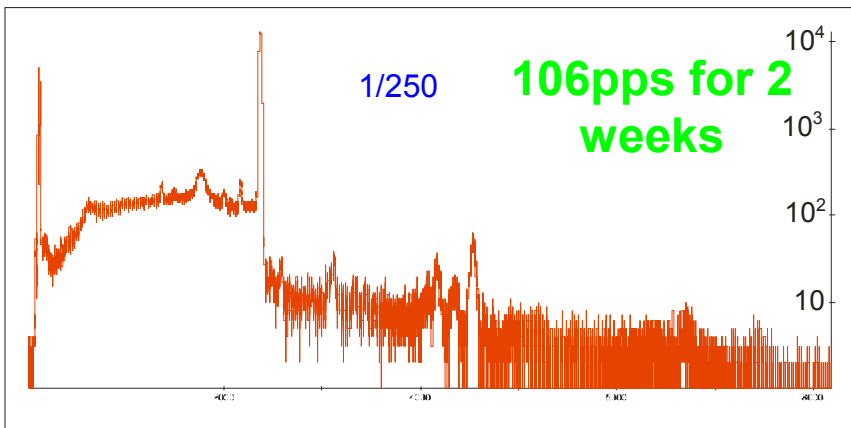
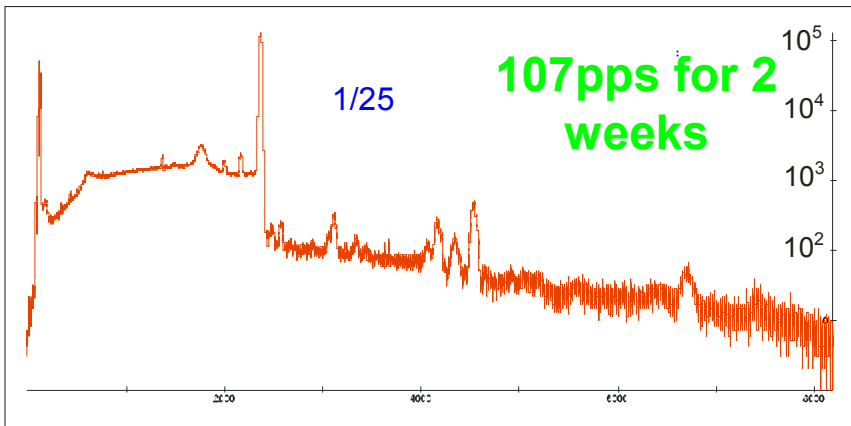
$$E(2^+_{1,ms}) = E_{AV} + \sqrt{\frac{1}{4} * (\epsilon_\pi - \epsilon_\nu)^2 + \beta^2 * N_\pi}$$

$$E(2^+_1) = E_{AV} - \sqrt{\frac{1}{4} * (\epsilon_\pi - \epsilon_\nu)^2 + \beta^2 * N_\pi}$$

Experimental approach

Coulomb excitations in inverse kinematics on C target
predominantly **one-step processes** and **clean γ -spectrum** (no target excitations)

15h at 6.109 pps!



To identify excited 2⁺ states (beyond the 2₁⁺) in vibrational nucleus (B(E2)~1Wu) with a 10% array for 2 weeks beam time we need **105pps**. For complete spectroscopy **106-107 pps** will be needed!

Feasible, but requires beam energy **~85% CB** (3.5-4 MeV/n)

well within the capability of H-I

New CIP case predicted: ^{136}Te

2+1 and 2+2 have significant E2 -> 1-phonon states
Strong M1 between them -> 2+2 = 2+1, MS

	$\lambda_i^\pi = 2_i^+$	Energy (MeV)		Structure	$B(E2; 0_{gs}^+ \rightarrow 2_i^+)$ ($e^2\text{fm}^4$)		$B(E2; 2_i^+ \rightarrow 2_1^+)$ ($e^2\text{fm}^4$)		$B(M1; 2_i^+ \rightarrow 2_1^+)$ (μ_N^2)	
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QPM: A.P. Severyukhin, N.N. Arsenyev, N. Pietralla, and V.W., PRC 90, 011306(R) (2014)

New CIP case predicted: ^{136}Te

2+1 and 2+2 have significant E2 \rightarrow 1-phonon states

Strong M1 between them \rightarrow 2+2 = 2+1, MS

2+1 neutron dominated, 2+2 large proton amplitudes

\rightarrow CouEx

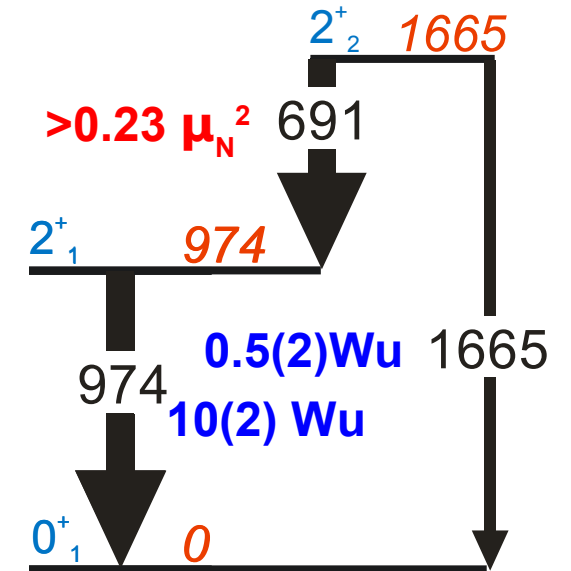
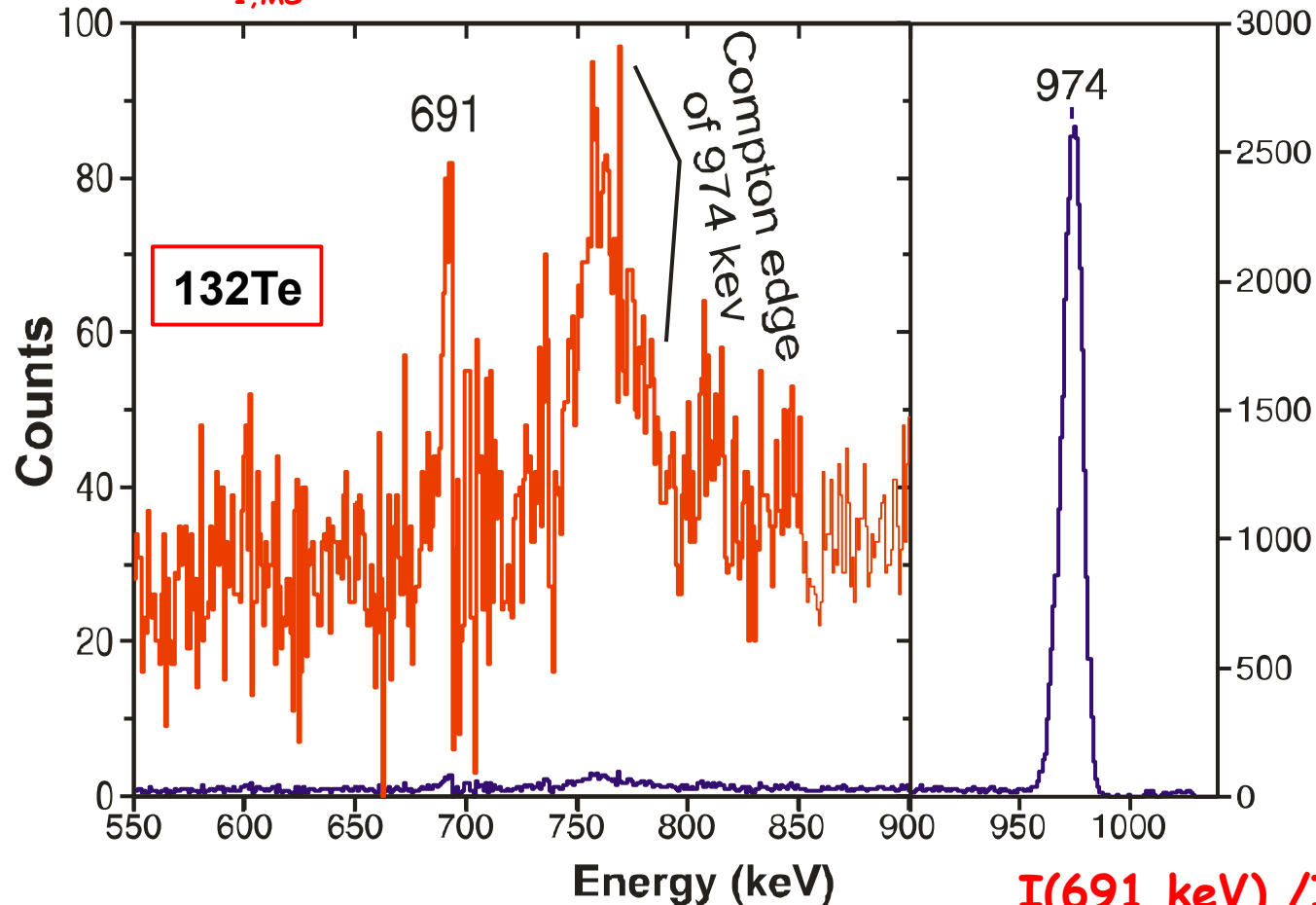
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	State	Energy (MeV)	$B(M1; 2_i^+ \rightarrow 2_1^+)$ (μ_N^2)	$B(E2; 0_{gs}^+ \rightarrow 2_i^+)$ ($e^2\text{fm}^4$)	$\{n_1 l_1 j_1, n_2 l_2 j_2\}_\tau$	X	Y	%
^{136}Te	$[2_1^+]_{\text{QRPA}}$	1.05		1010	$\{2f_{7/2}, 2f_{7/2}\}_\nu$	1.32	0.14	86
					$\{2d_{5/2}, 2d_{5/2}\}_\pi$	0.32	0.13	4
					$\{1g_{7/2}, 1g_{7/2}\}_\pi$	0.30	0.12	4
	$[2_2^+]_{\text{QRPA}}$	2.20	0.44	920	$\{2f_{7/2}, 2f_{7/2}\}_\nu$	-0.52	0.13	13
					$\{2d_{5/2}, 2d_{5/2}\}_\pi$	0.82	0.04	34
					$\{1g_{7/2}, 1g_{7/2}\}_\pi$	0.83	0.04	34

QPM: A.P. Severyukhin, N.N. Arsenyev, N. Pietralla, and V.W., PRC 90, 011306(R) (2014)

First MS observation with RIB

$2_{1,MS}^+$ observed in coincidence with ^{12}C recoils detected in HyBall.



M. Danchev *et al.*, PRC84 ('11) 061306(R)

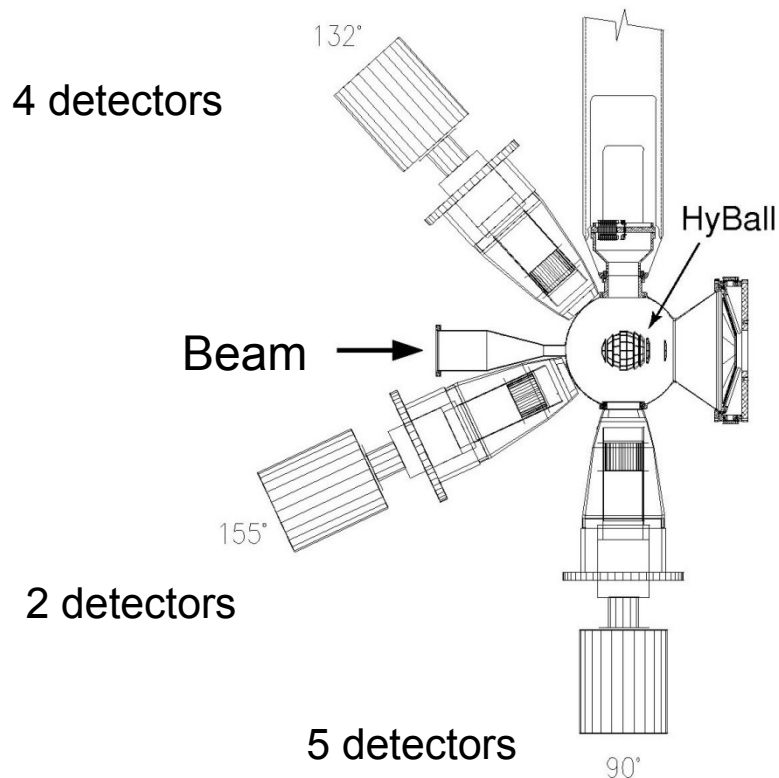
Note: in ^{136}Te $E(2_1^+ \rightarrow 0_1^+) = 606 \text{ keV}$; $E(2_2^+ \rightarrow 2_1^+) = 962 \text{ keV} \Rightarrow$ no Compton, cleaner !!

ORNL – 2_1^+ g factor Experiment

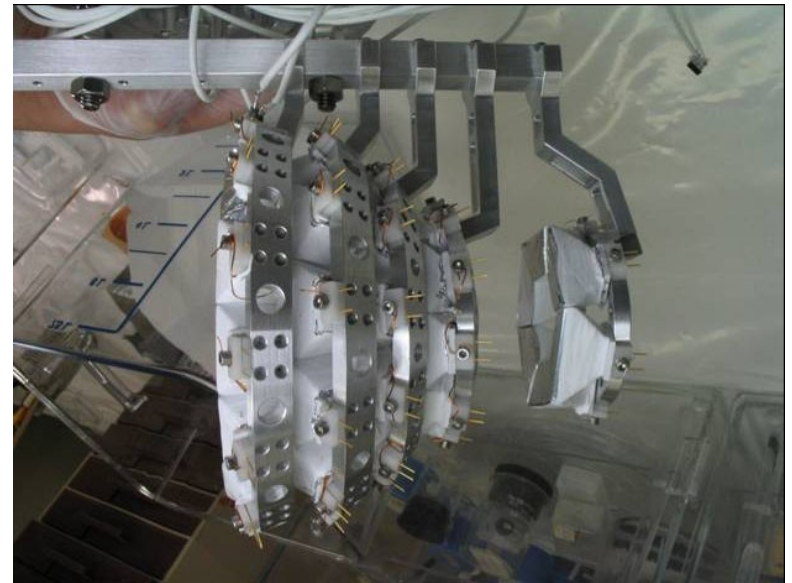
Experimental details:

- inverse kinematic reaction ^{132}Te on a C target (0.83 mg/cm²);
- beam energy 3 MeV/u (80% CB);
- beam intensity 3×10^7 pps, run time 64 hours;

Clarion array – 11 clovers



HyBall array

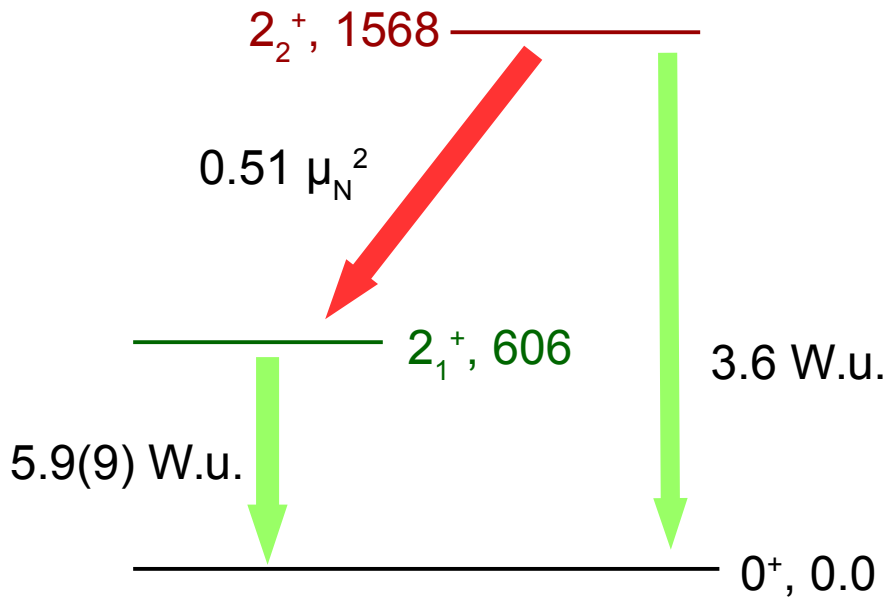


CsI charged particle detectors:

- Ring 1 – 6 detectors 7° - 14°
- Ring 2 – 10 detectors 14° - 28°
- Ring 3 - 12 detectors 28° - 44°

CIP in ^{136}Te

Enhanced Proton Content in second 2^+ yields exceptionally large $B(E2)$



Other theory:

Shell Model:

N. Shimizu, T. Otsuka, T. Mizusaki, M. Honma,
PRC 70, 054313 (2004)

2_1^+ neutron dominated;

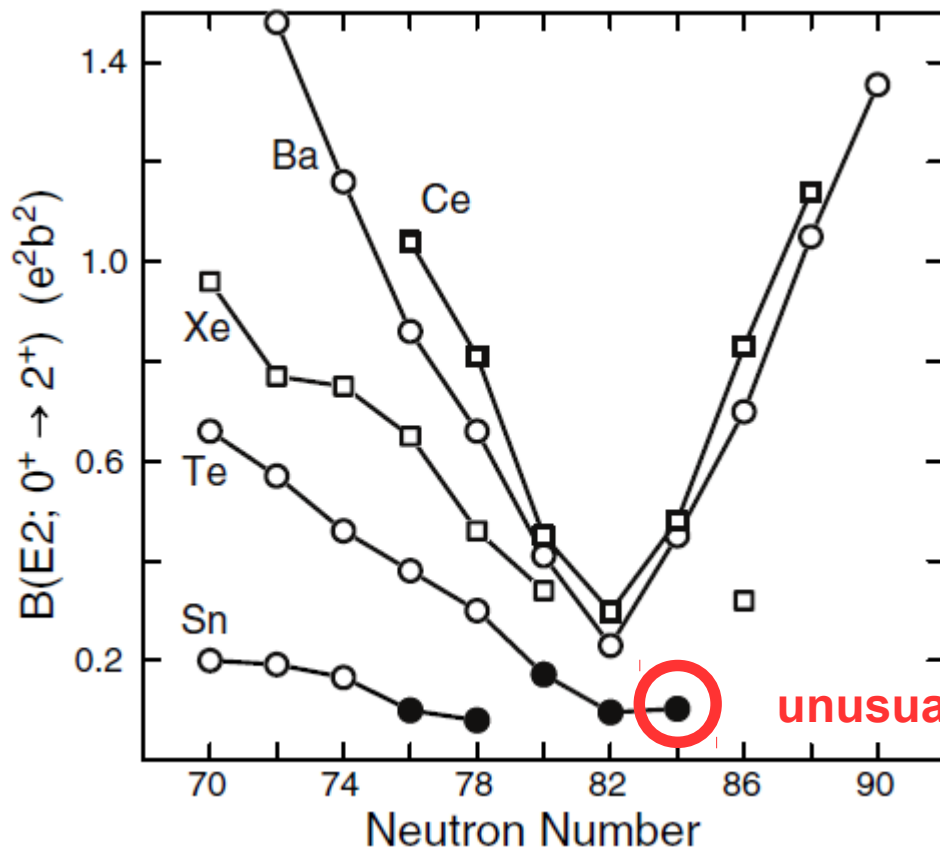
2_2^+ is MS state, M1: $0.24 \mu_N^2$, E2 $300 e^2\text{fm}^4$

QRPA:

J. Terasaki et al., PRC 66, 054313 (2002)

M. Danchev, G. Rainovski,
N. Pietralla et al.,
PRC 84, 061306(R) (2011)
 $B(E2)_{\text{up}} = 1220(180) e^2\text{fm}^4$

B(E2) "anomaly" in ^{136}Te



Origin of the anomaly:

Neutron dominance in the 2_1^+ wave function

Shell Model:

N. Shimizu, T. Otsuka, T. Mizusaki, M. Honma,
PRC 70, 054313 (2004)

2_1^+ neutron dominated; 2_2^+ is MS state

QRPA:

J. Terasaki et al., PRC 66, 054313 (2002)

D.C. Radford et al., PRL 88, 222501 (2002)

Configurational Isospin Polarization (CIP)



$$2_{sym}^+ = a_1 \cdot 2_n^+ + b_1 2_p^+$$

$$2_{ms}^+ = a_2 \cdot 2_n^+ - b_2 2_p^+$$

protons and neutrons contribute about equally: large mixing

$$|a_i| \approx |b_i|$$

imbalance in proton and neutron contributions: small mixing

$$|a_i| \neq |b_i|$$

**observables which are sensitive to p/n content:
B(E2)'s and M1**

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	$\lambda_i^\pi = 2_i^+$	Energy (MeV)		Structure	$B(E2; 0_{gs}^+ \rightarrow 2_i^+)$ ($e^2\text{fm}^4$)		$B(E2; 2_i^+ \rightarrow 2_1^+)$ ($e^2\text{fm}^4$)		$B(M1; 2_i^+ \rightarrow 2_1^+)$ (μ_N^2)	
		Expt.	Theory		Expt.	Theory	Expt.	Theory	Expt.	Theory
^{136}Te	2_1^+	0.606	0.92	97% $[2_1^+]_{\text{QRPA}}$	1220 ± 180	1120				
	2_2^+	1.568	2.01	94% $[2_2^+]_{\text{QRPA}}$	740		20		0.51	

$[2_1^+]_{\text{QRPA}} = \sim 86\% \text{ Neutron}$, $[2_2^+]_{\text{QRPA}} \sim 68\% \text{ Proton}$

QPM: A.P. Severyukhin, N.N. Arsenyev, N. Pietralla, and V.W., PRC 90, 011306(R) (2014)

Other theory:

Shell Model: N. Shimizu, T. Otsuka, T. Mizusaki, M. Honma, PRC 70, 054313 (2004)

2_1^+ neutron dominated; 2_2^+ is MS state, M1: $0.24 \mu_N^2$, E2 $300 e^2\text{fm}^4$