

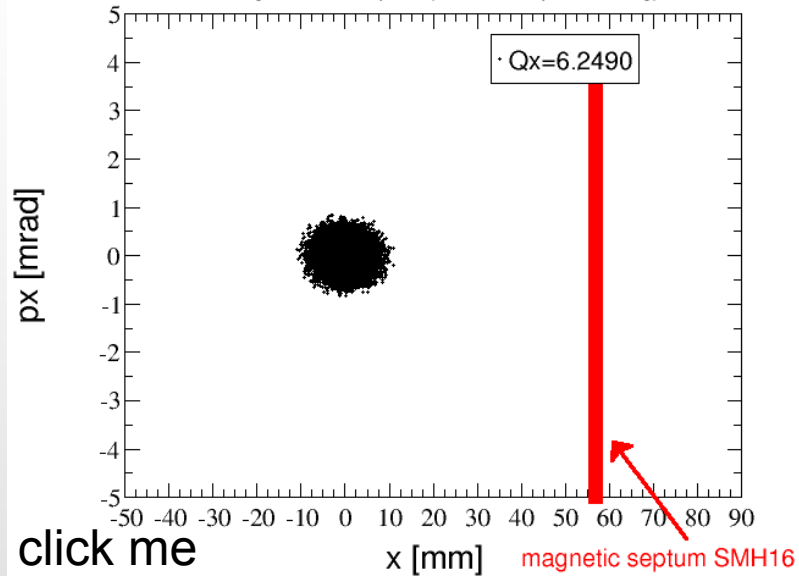
# Can we inject or extract a beam without magnetic septa?

Andrea Franchi (ESRF)  
Massimo Giovannozzi (CERN)

AOC workshop, CERN, 5-6 January 2015

resonance crossing [.0249,.255] in 20,000 turns 40,000 particles  $\Delta=0$

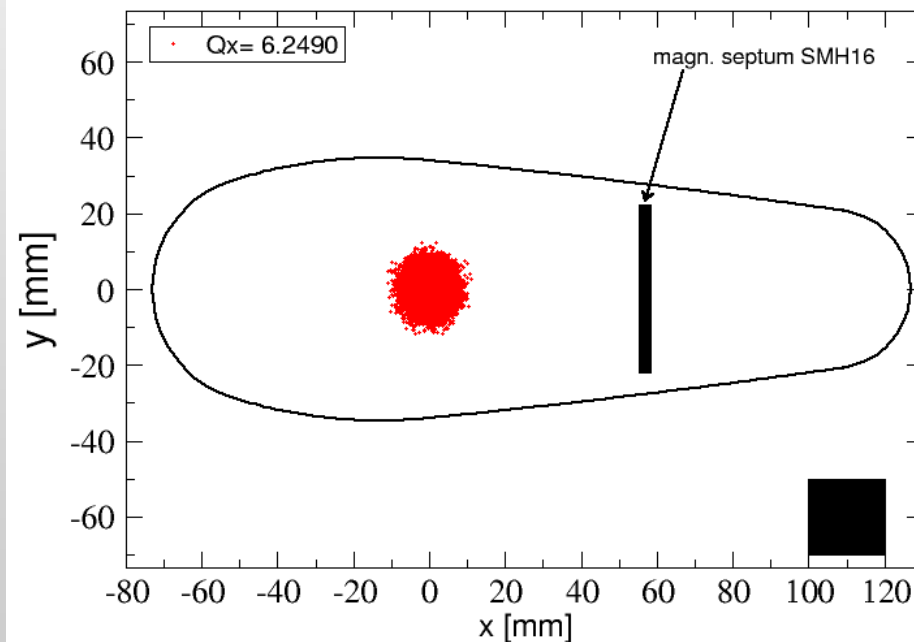
HORIZONTAL PHASE SPACE @ SMH16  
during the island capture (MAD8 multi-part. tracking)



## Multi-Turn Extraction @ CERN PS

- $\frac{1}{4}$  horizontal resonance crossed
- beam split into 4 islands + core
- extraction via slow bump + 1<sup>st</sup> fast bump (4 turns for islands) + 2<sup>nd</sup> fast bump (1 turn for the core)

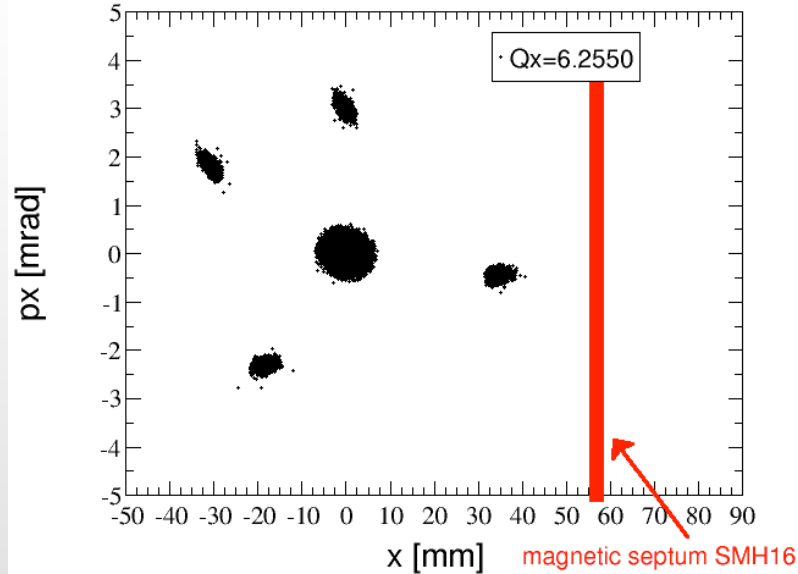
click me Island capture (end of MU15)  
high-intensity beam  $E_x=9.4$ ,  $E_y=6.4$  mm mrad



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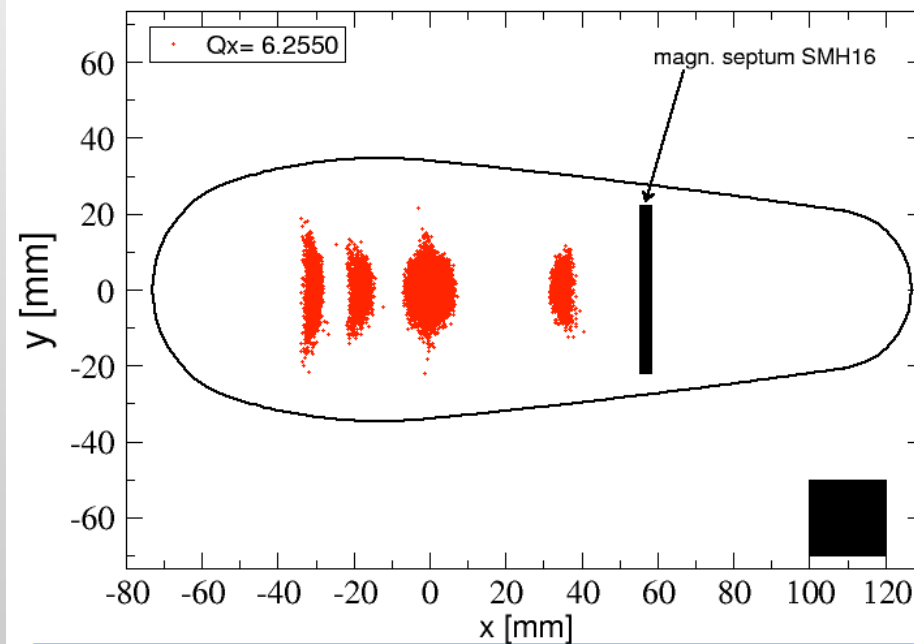


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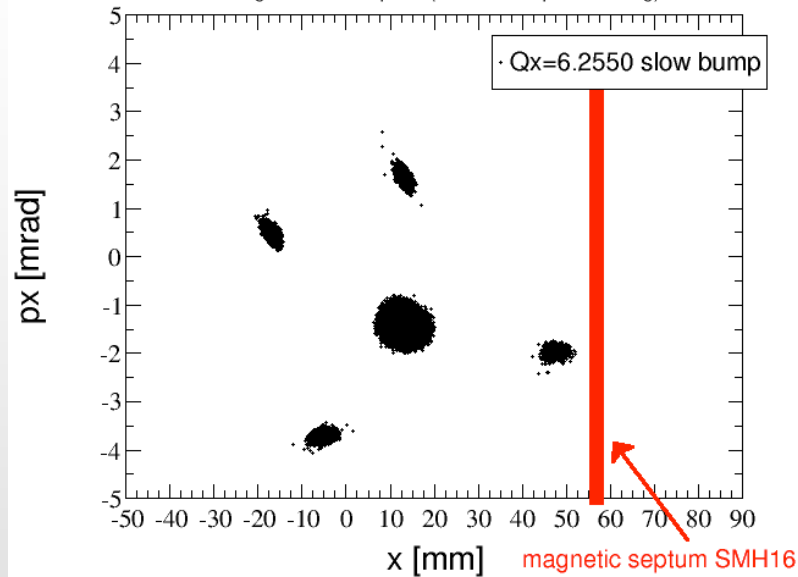
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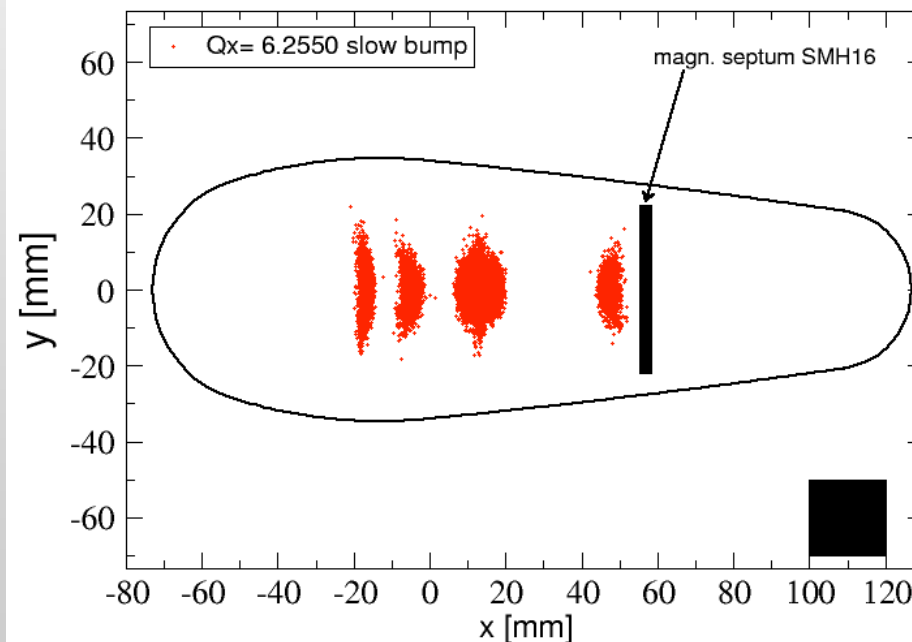
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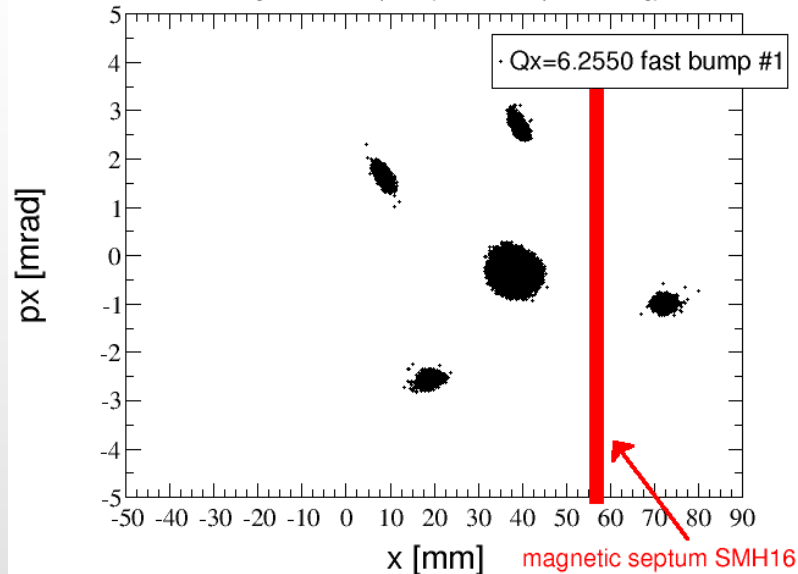
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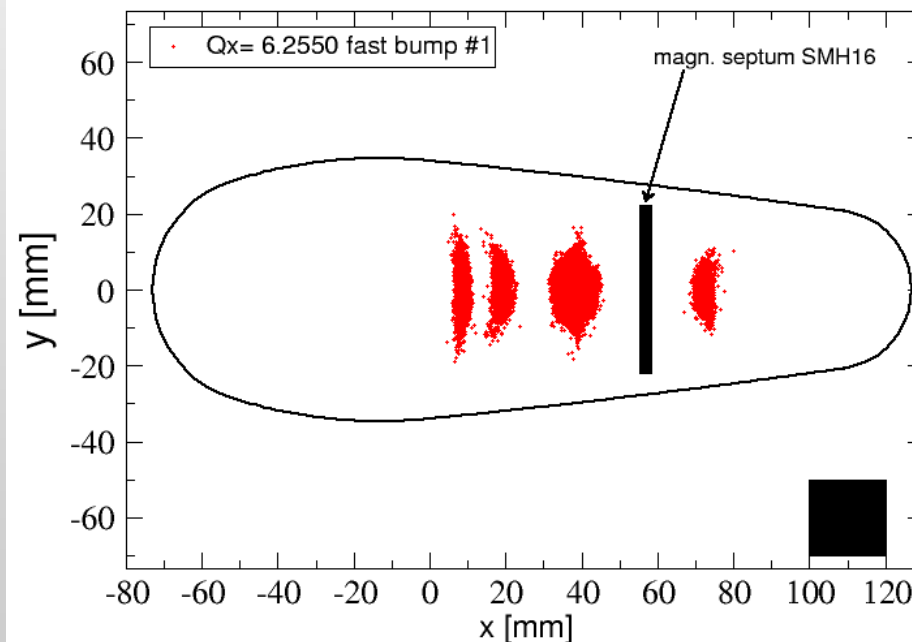
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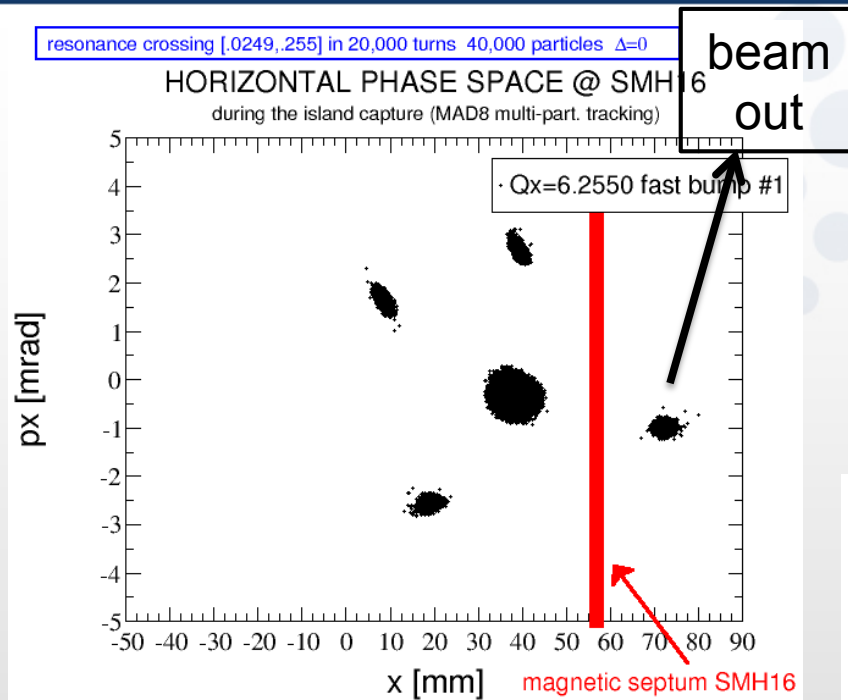
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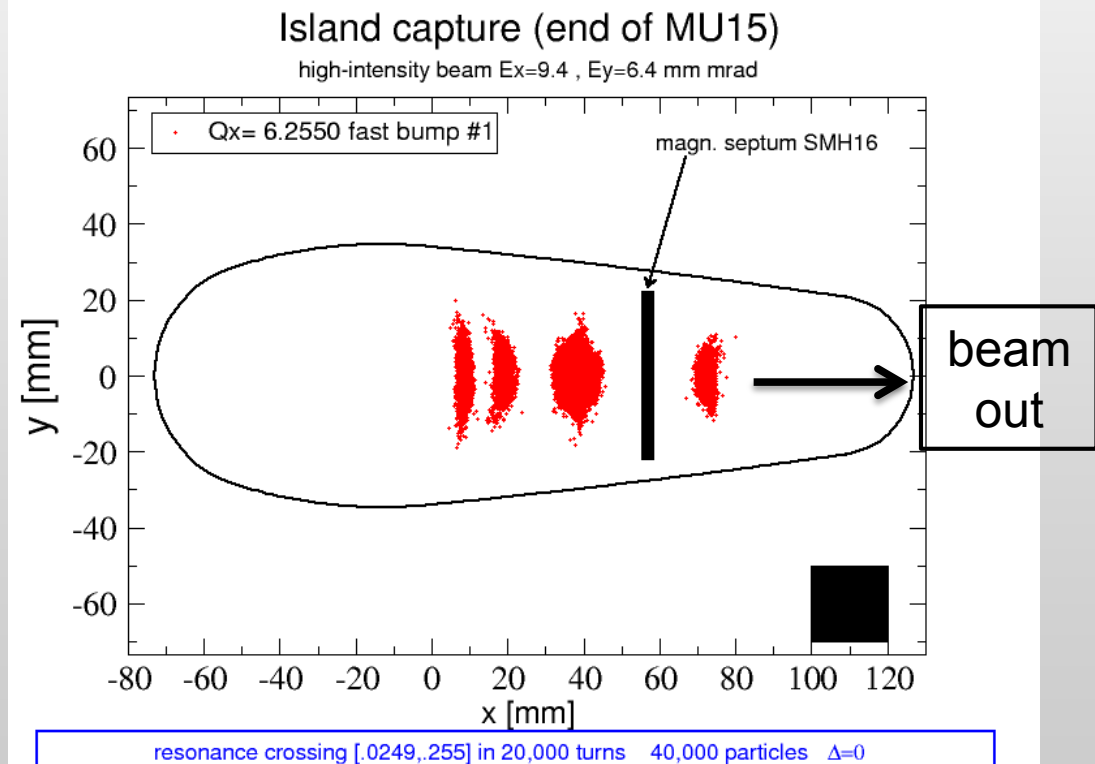
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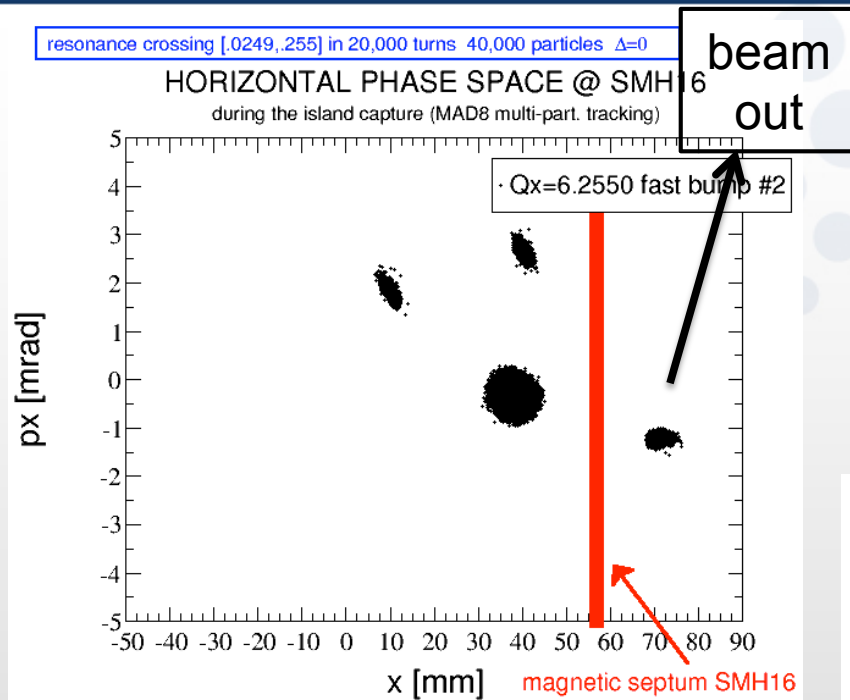
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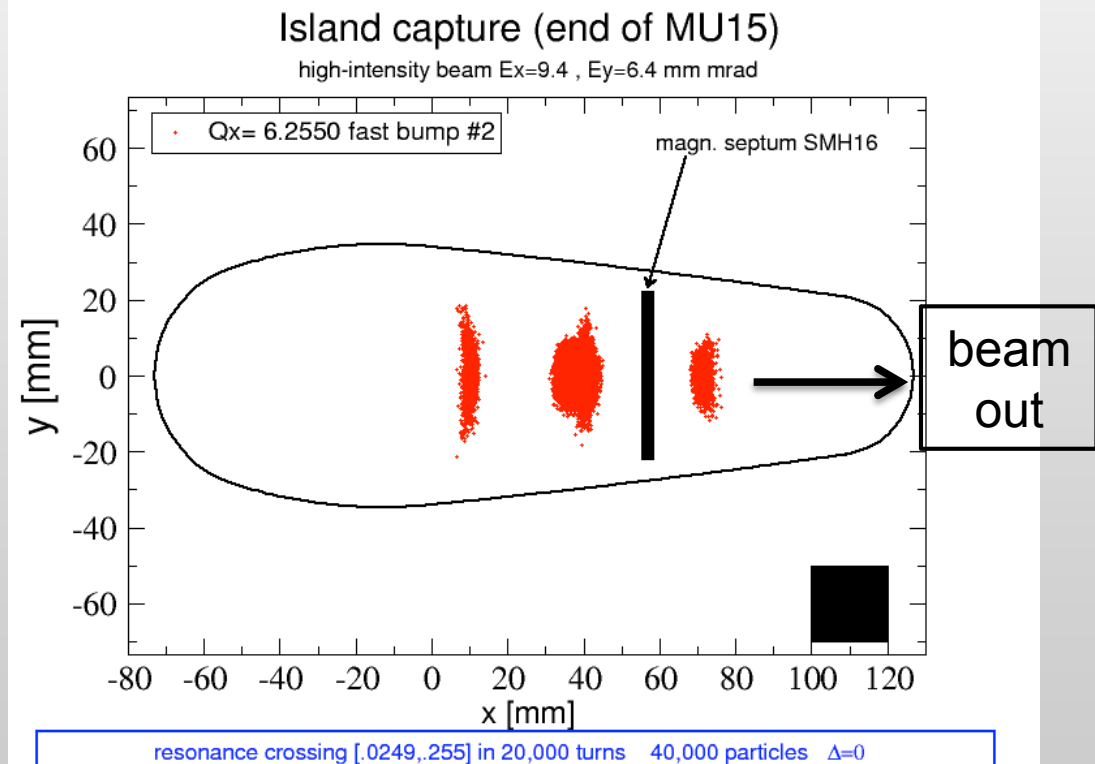
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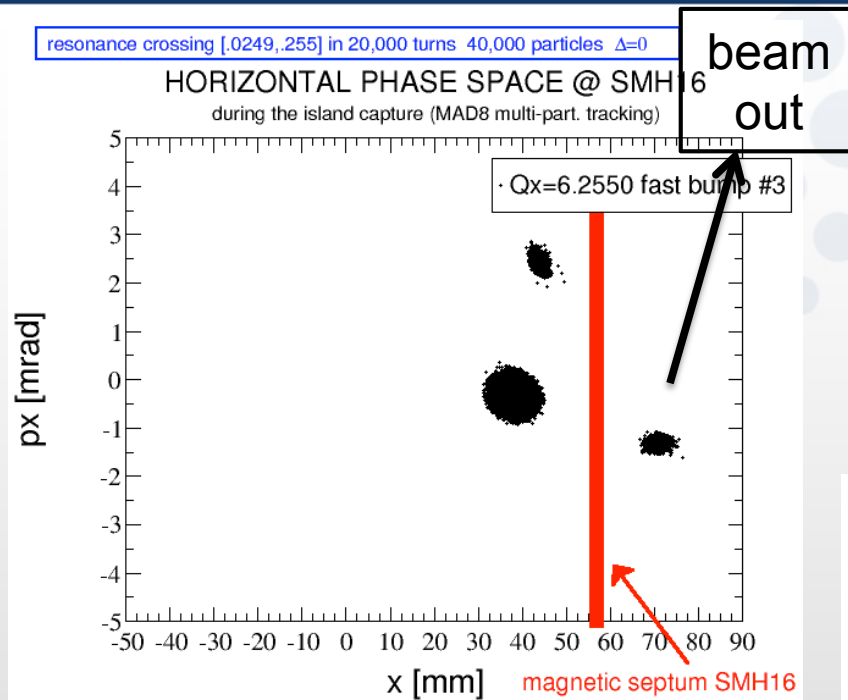
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( $\delta x \approx 0$  mm,  $\delta p_x \approx 10$  mrad)





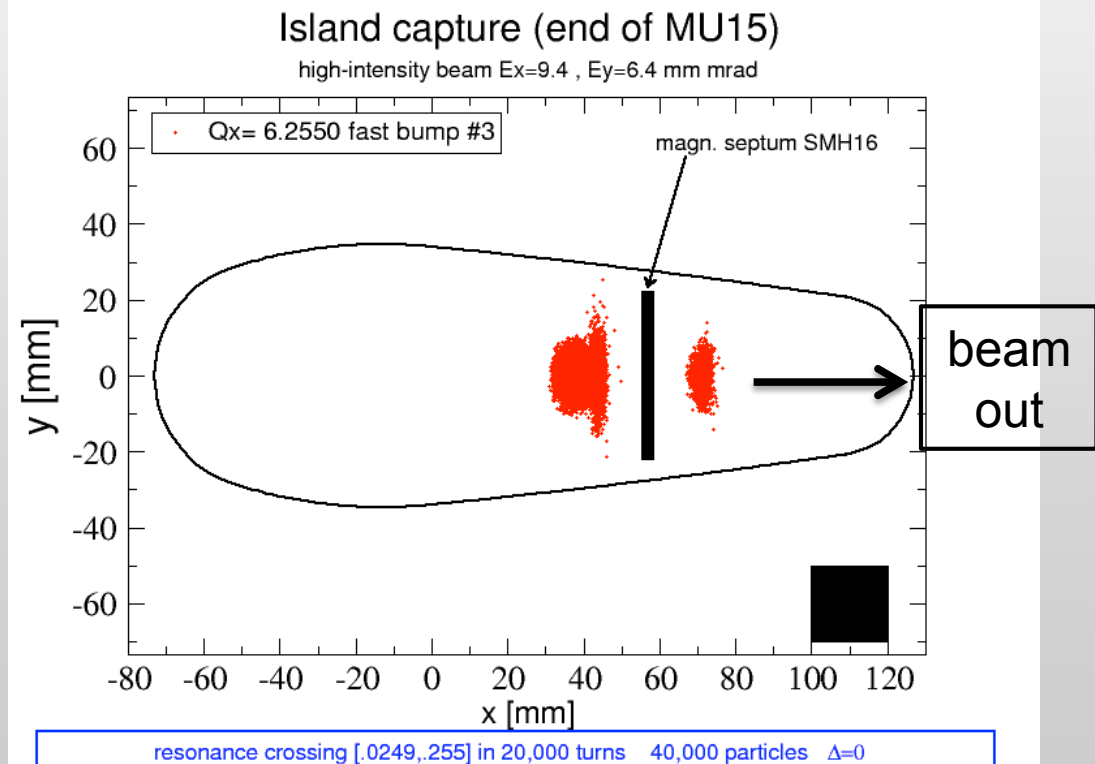
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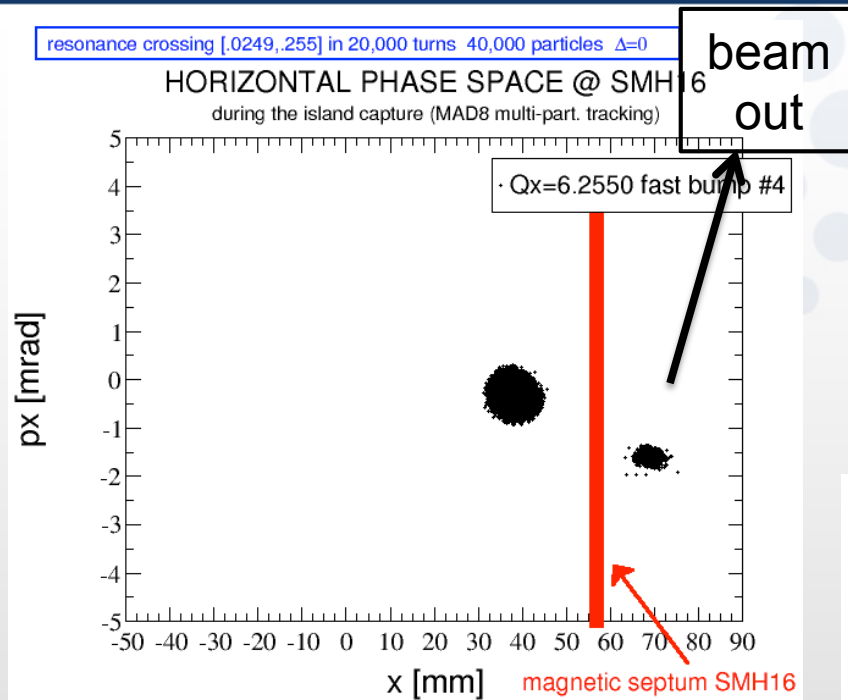
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**Extraction:** magnetic septum  
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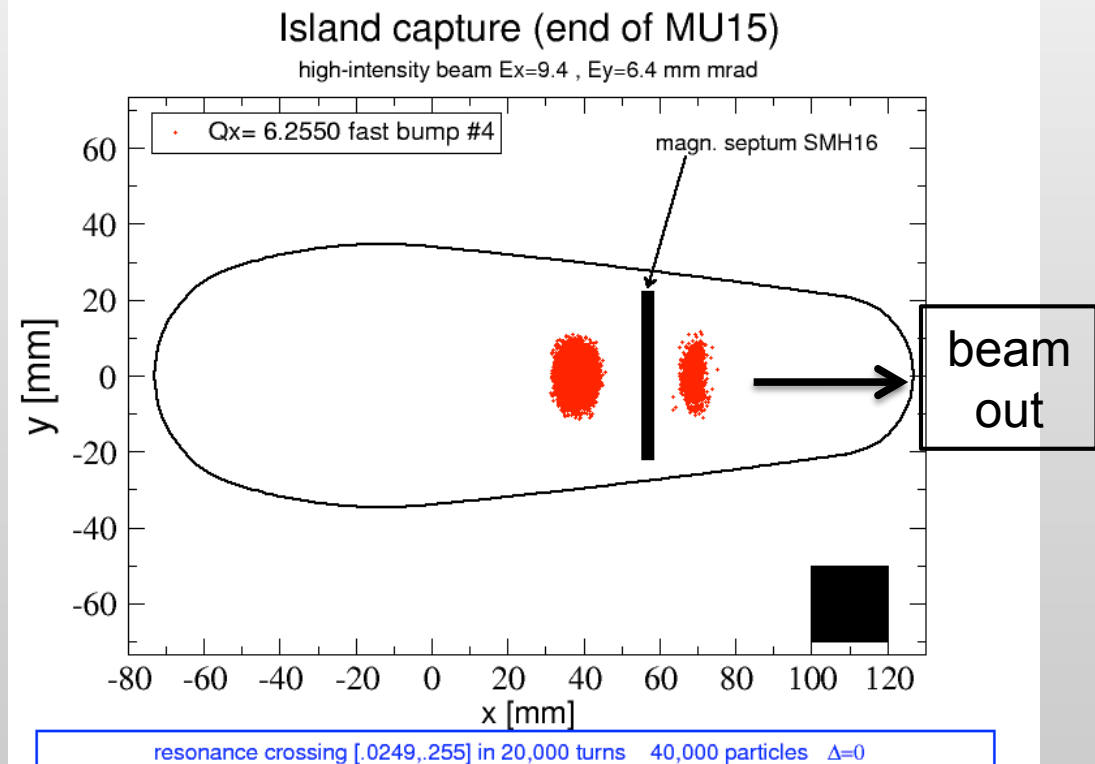
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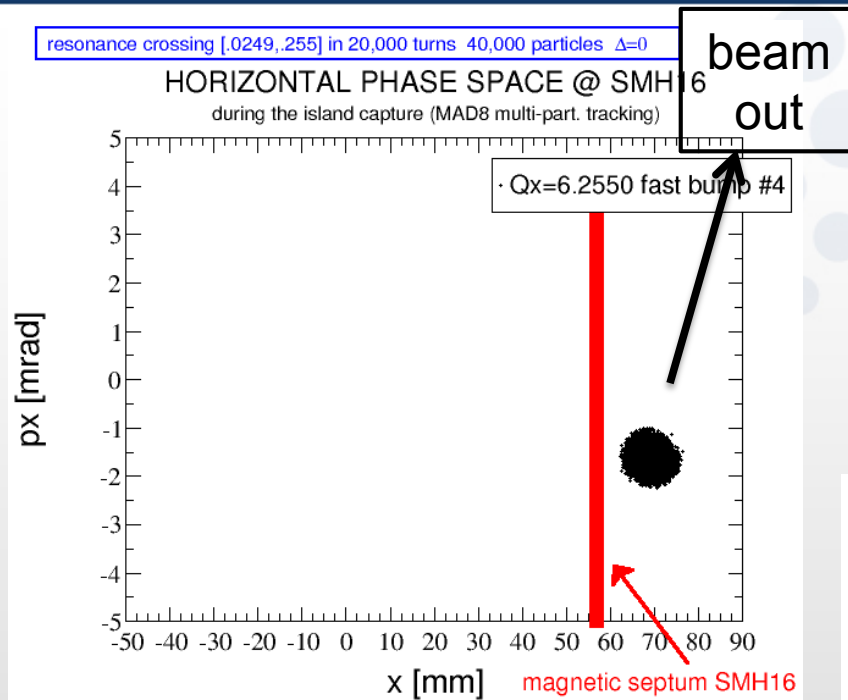
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**Extraction:** magnetic septum  
( $\delta x \approx 0$  mm,  $\delta p_x \approx 10$  mrad)





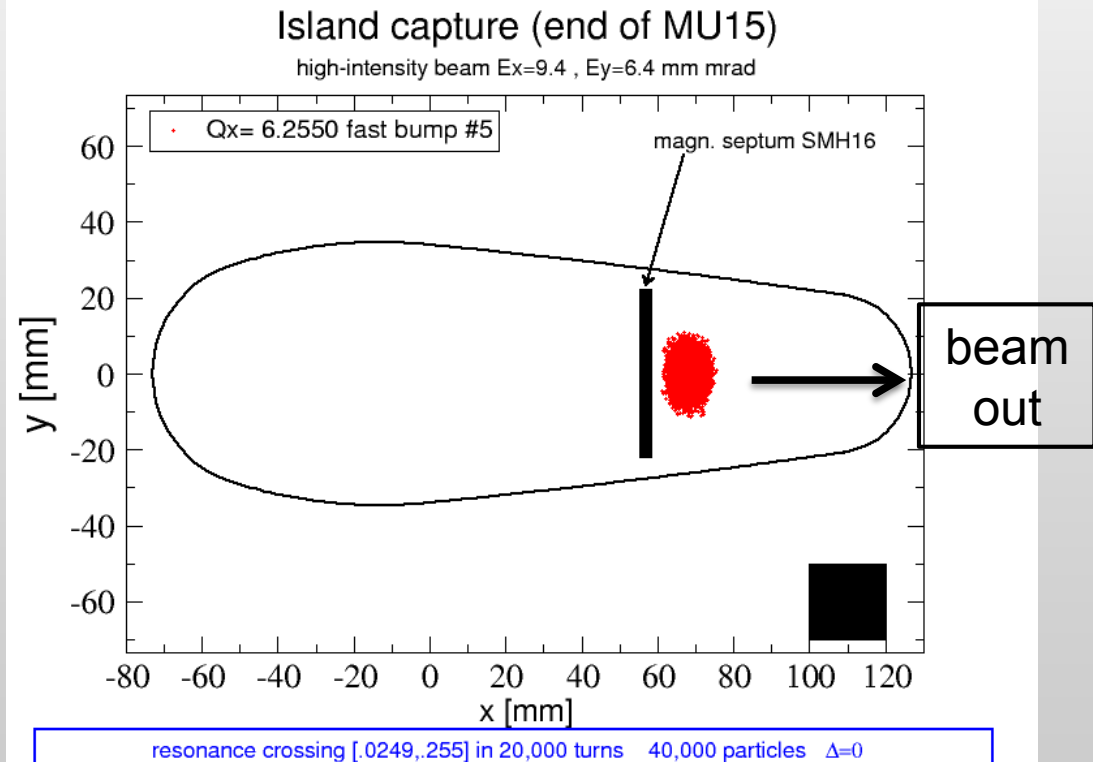
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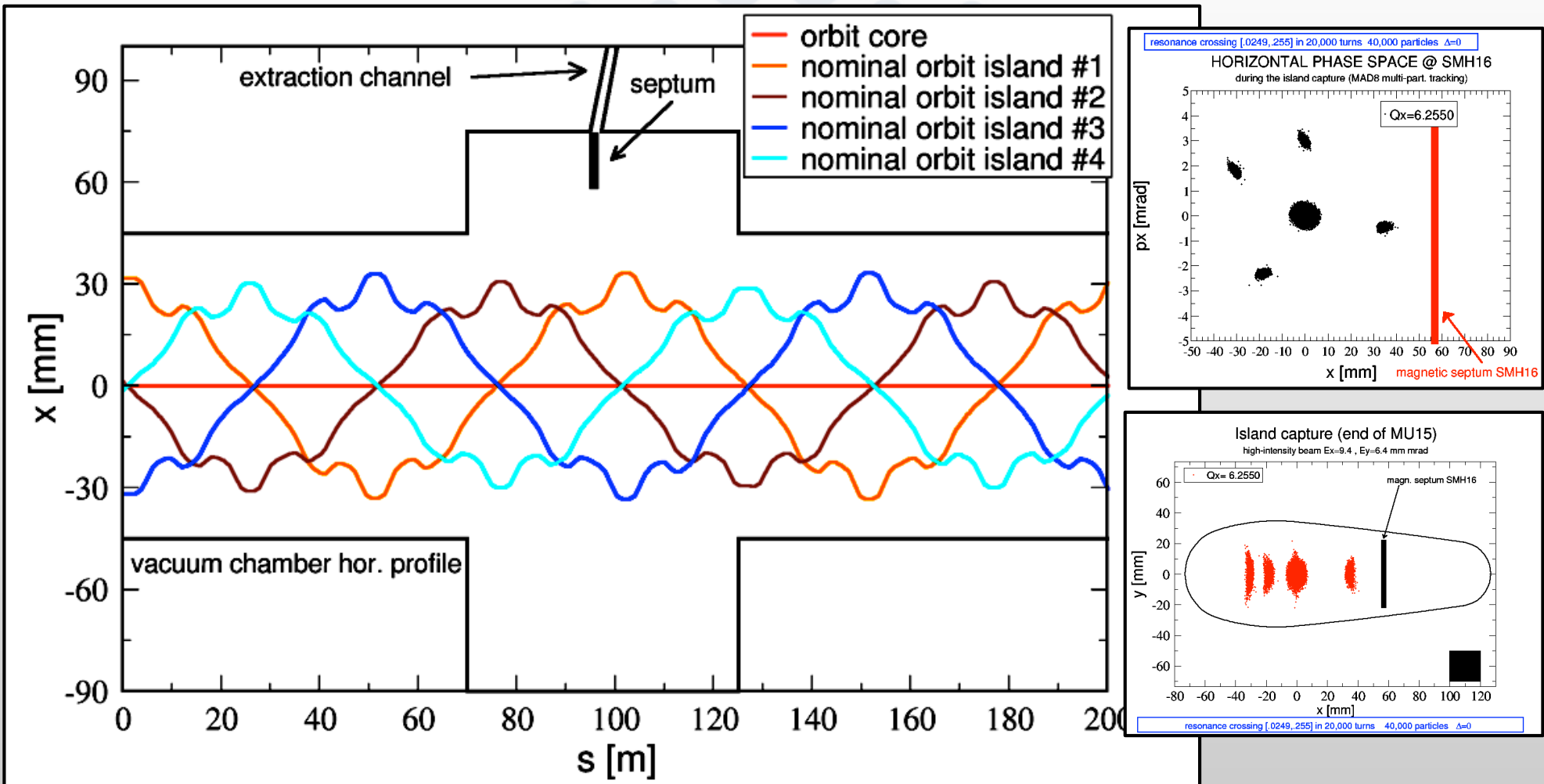
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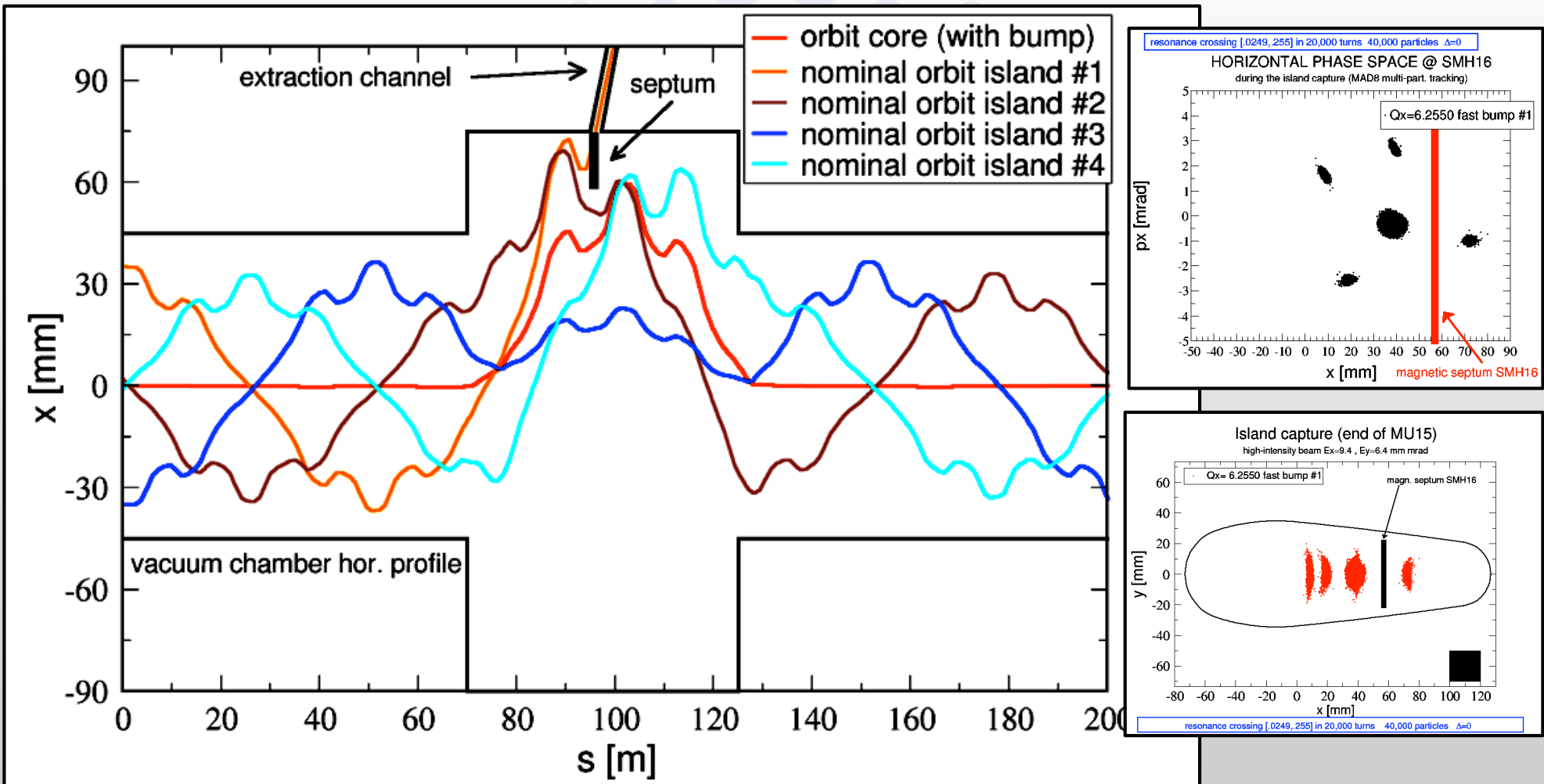
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## Multi-Turn Extraction @ CERN PS : split beam prior orbit bump



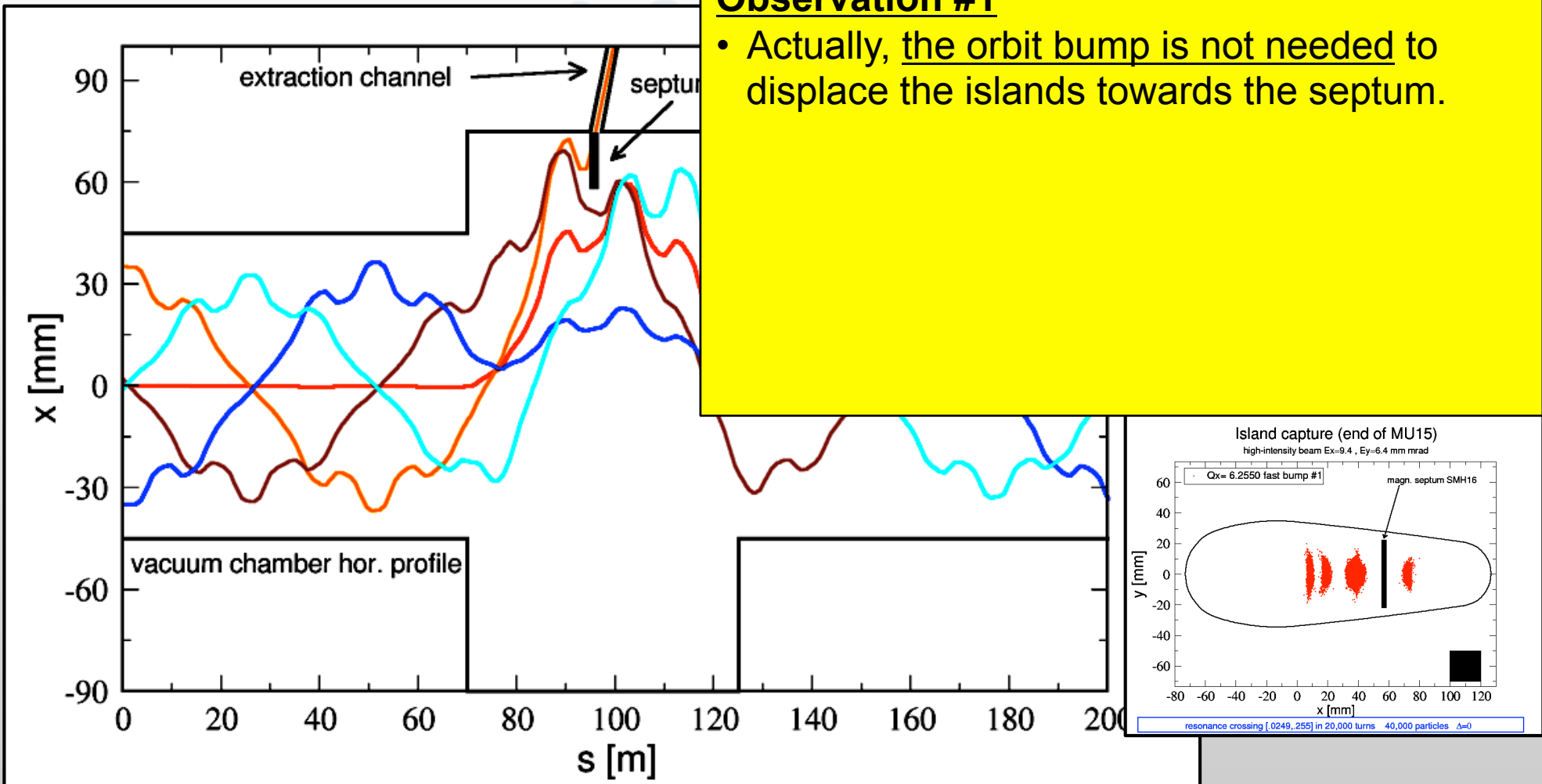
## Multi-Turn Extraction @ CERN PS : split beam with orbit bump



## MTE : some observations

### Observation #1

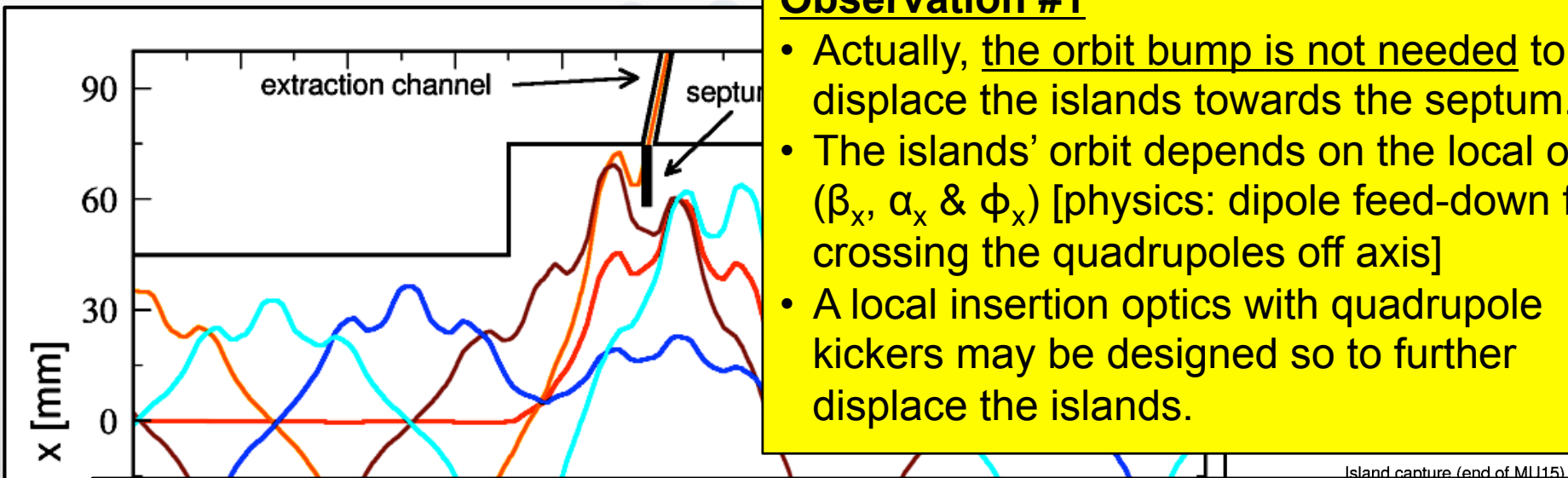
- Actually, the orbit bump is not needed to displace the islands towards the septum.



## MTE : some observations

### Observation #1

- Actually, the orbit bump is not needed to displace the islands towards the septum.
- The islands' orbit depends on the local optics ( $\beta_x$ ,  $\alpha_x$  &  $\phi_x$ ) [physics: dipole feed-down from crossing the quadrupoles off axis]
- A local insertion optics with quadrupole kickers may be designed so to further displace the islands.



$$x^*(\Delta, \Omega_2, s) \simeq \sqrt{\beta_x(s) \rho^*(\Delta, \Omega_2)} \cos \Phi(s)$$

$$p^*(\Delta, \Omega_2, s) \simeq -\sqrt{\frac{\rho^*(\Delta, \Omega_2)}{\beta_x(s)}} \left[ \alpha_x(s) \cos \Phi(s) + \sin \Phi(s) \right]$$

$$\Phi(s) \simeq \phi_x(s) + \frac{2n\pi}{4}, \quad 1 \leq n \leq 4, \quad \rho^*(\Delta, \Omega_2) \simeq -\frac{2\pi\Delta}{\Omega_2} \begin{cases} \Delta = Q_x - \bar{Q}_x \\ \Omega_2 = \text{detuning coefficient} \end{cases}$$

## MTE : some observations

### Observation #2

- The insertion optics may be designed so to have  $x^* \approx 70$  mm and  $p_x^* \approx 10$  mrad (via  $\beta_x$ ,  $\alpha_x$  &  $\phi_x$ ) at the the extraction channel
- Need no magnetic septum, just of a physical septum at larger distance (i.e. larger beam stay clear)

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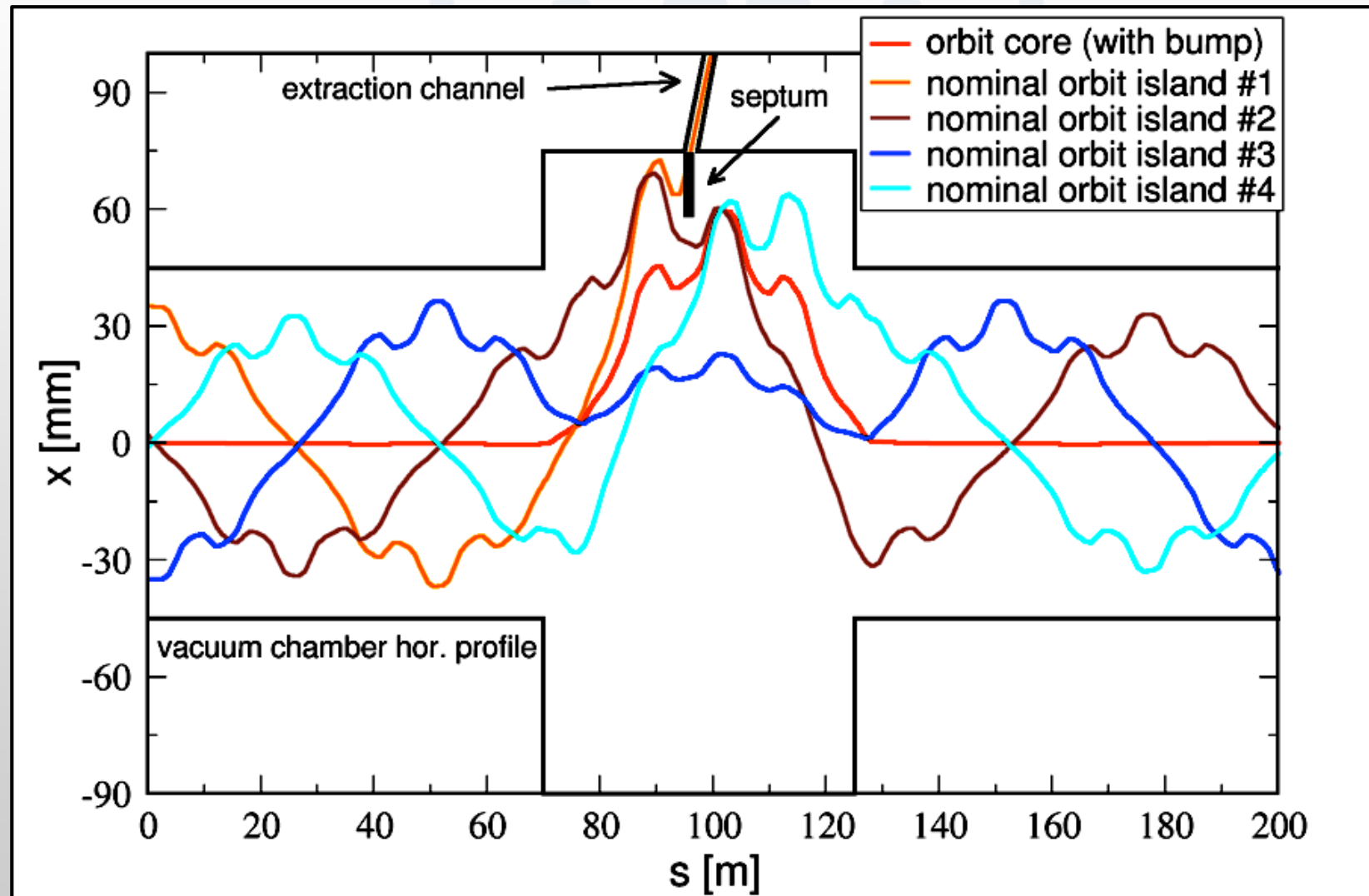
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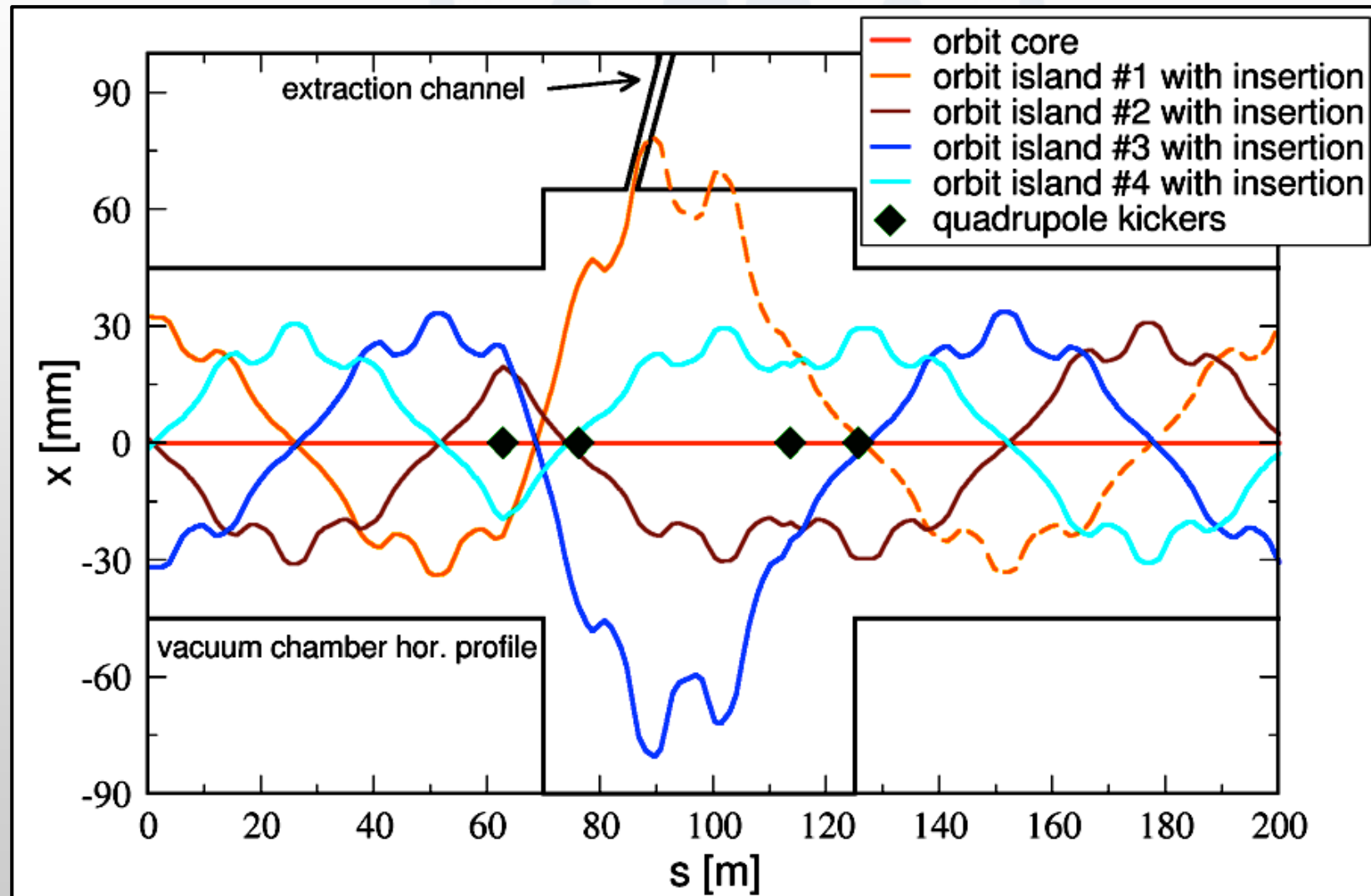
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## MTE: islands' extraction **with** orbit bump & septum magnets

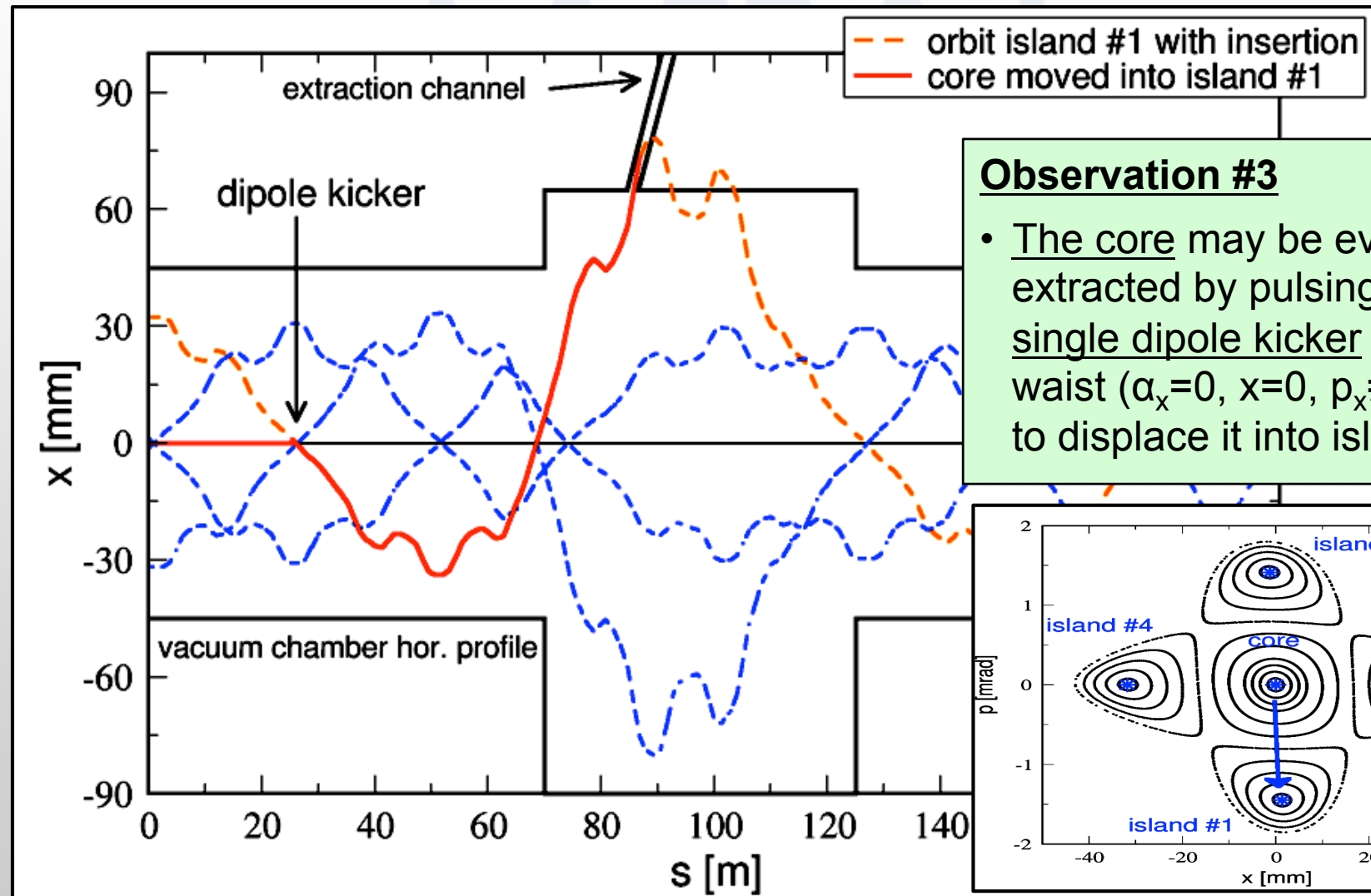




**MTE: islands' extraction with neither orbit bump nor septum magnets**

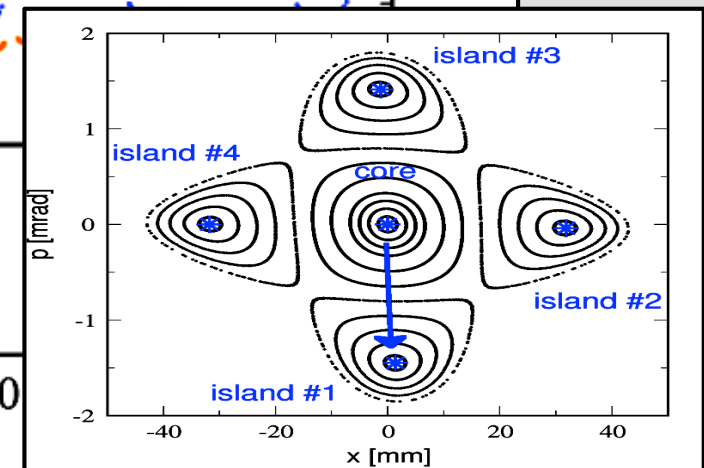


## MTE : core extraction with a single dipole kicker



### Observation #3

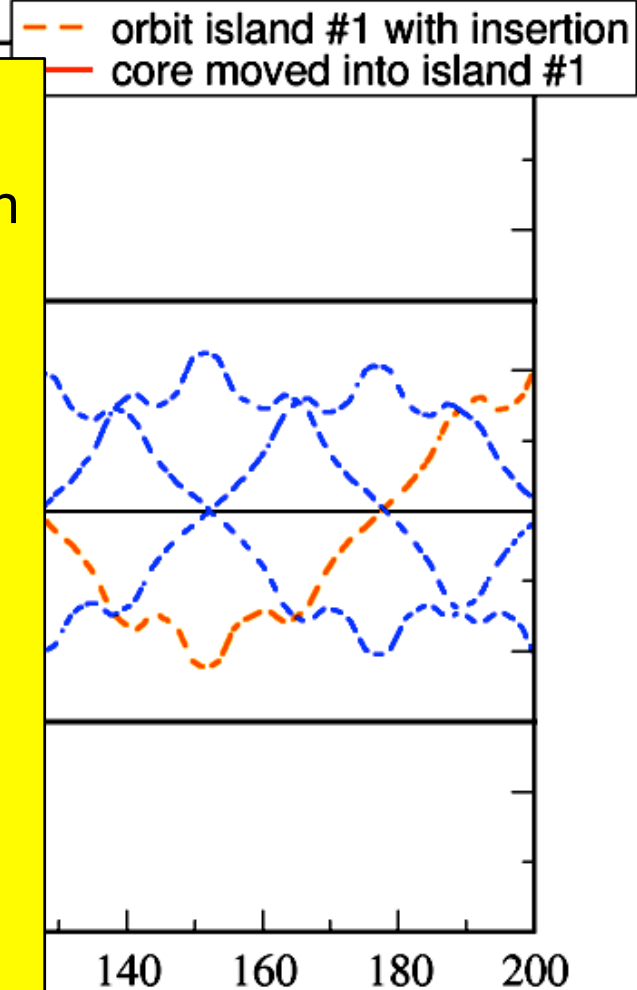
- The core may be eventually extracted by pulsing a single dipole kicker at a waist ( $\alpha_x=0, x=0, p_x \neq 0$ ) so to displace it into island #1



## MTE : core extraction with a single dipole kicker

### septum-less Multi-Turn Extraction

- closed fast orbit bump replaced by an insertion optics
- dipole kickers replaced by quadrupole kickers (for the islands)
- only one dipole kicker needed to extract the core



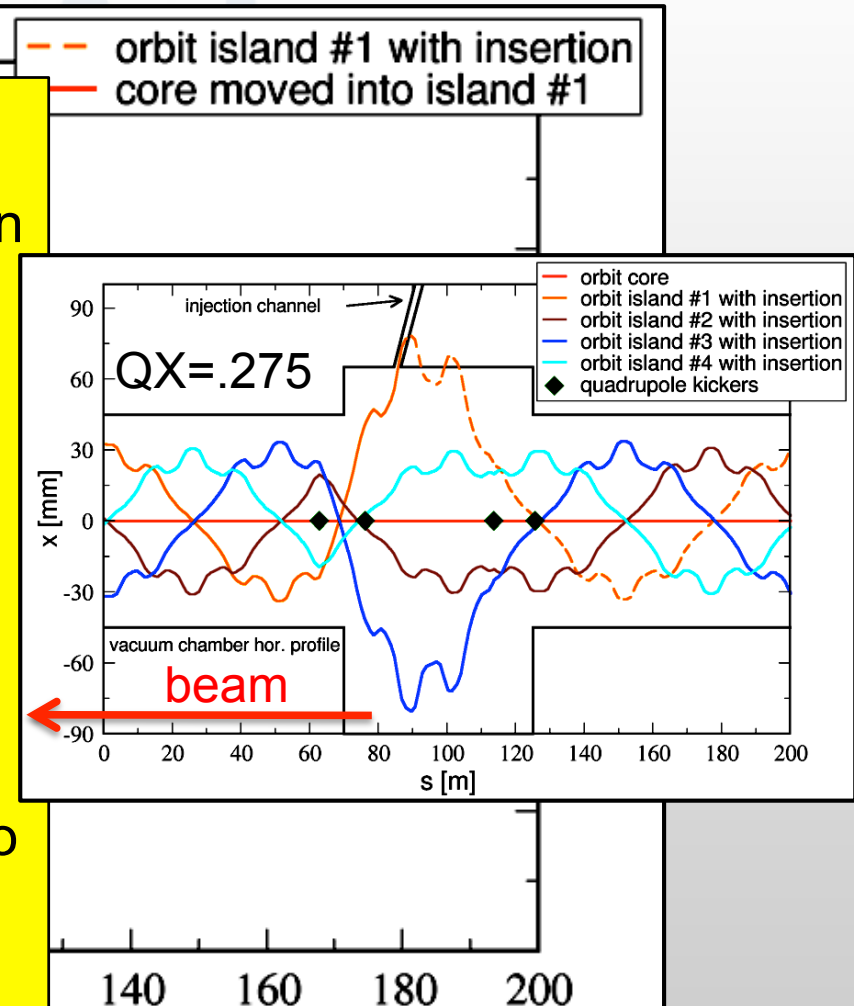
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as above, look at the plots from right to left + no need to inject the core => no need of dipole kicker



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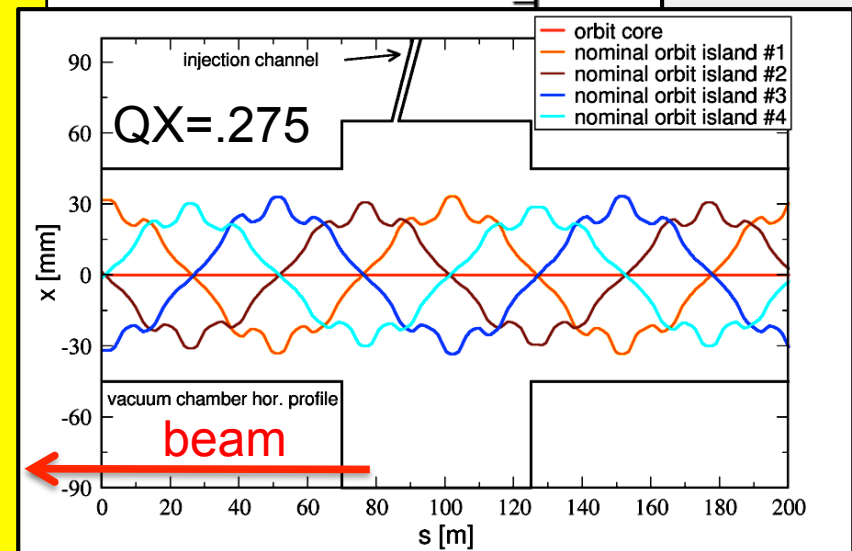
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-- orbit island #1 with insertion  
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140 160 180 200

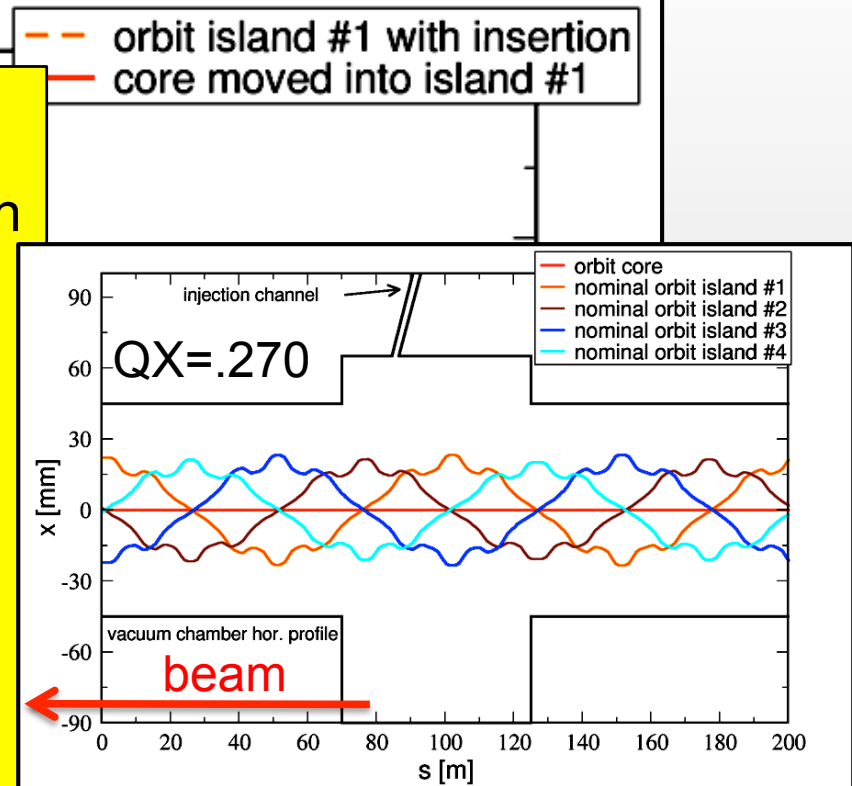
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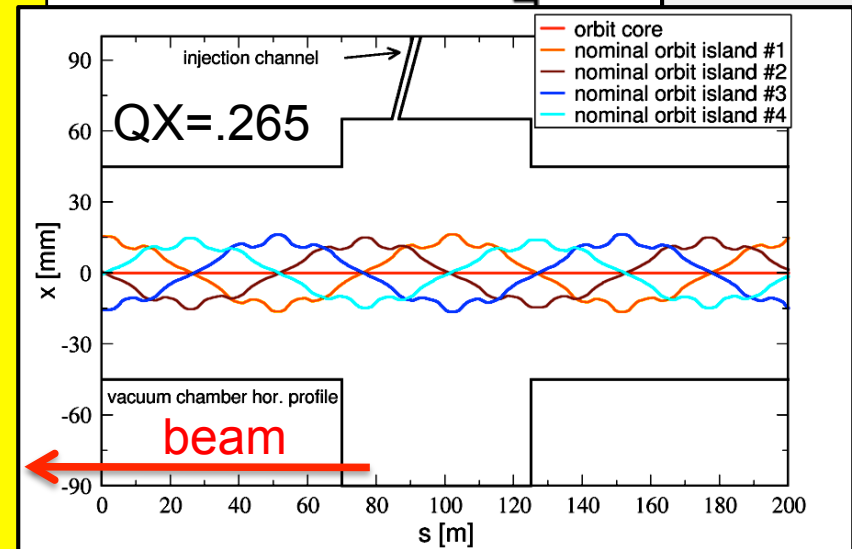
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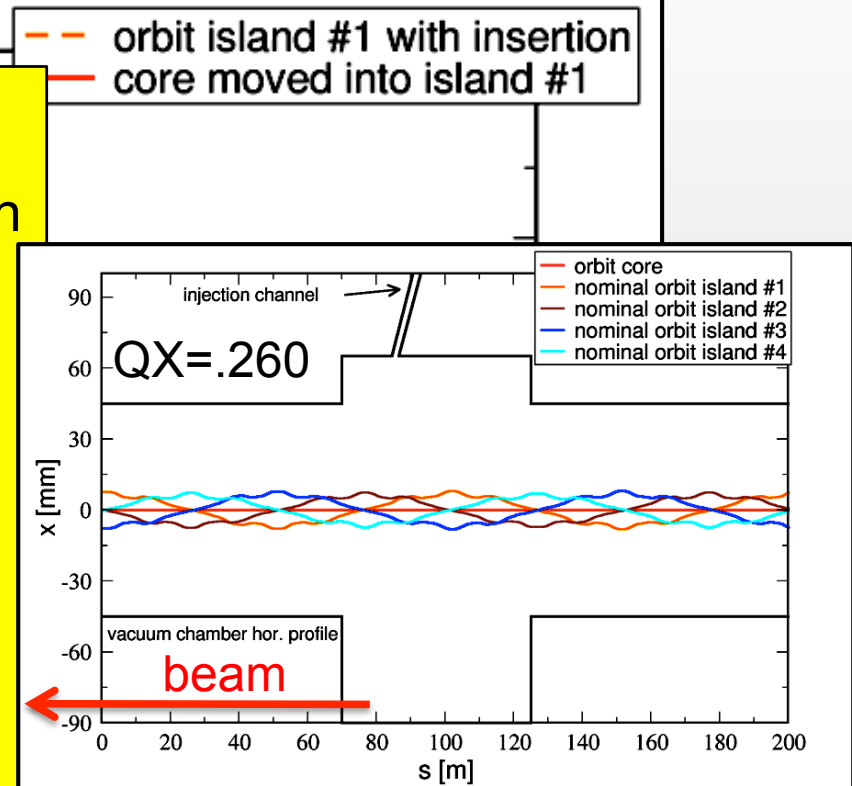
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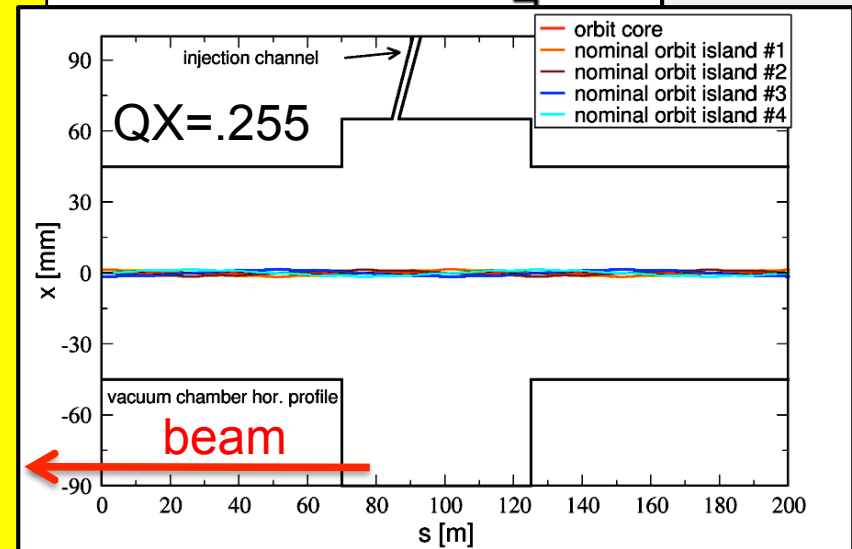
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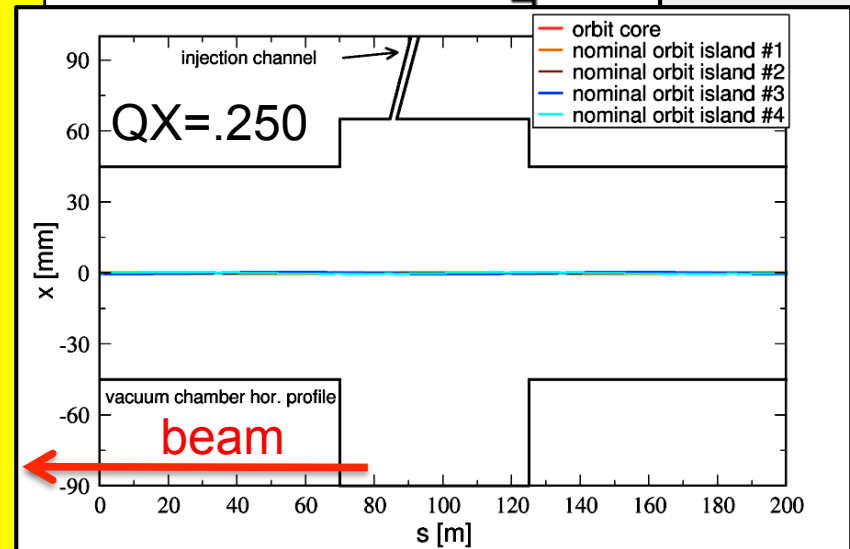
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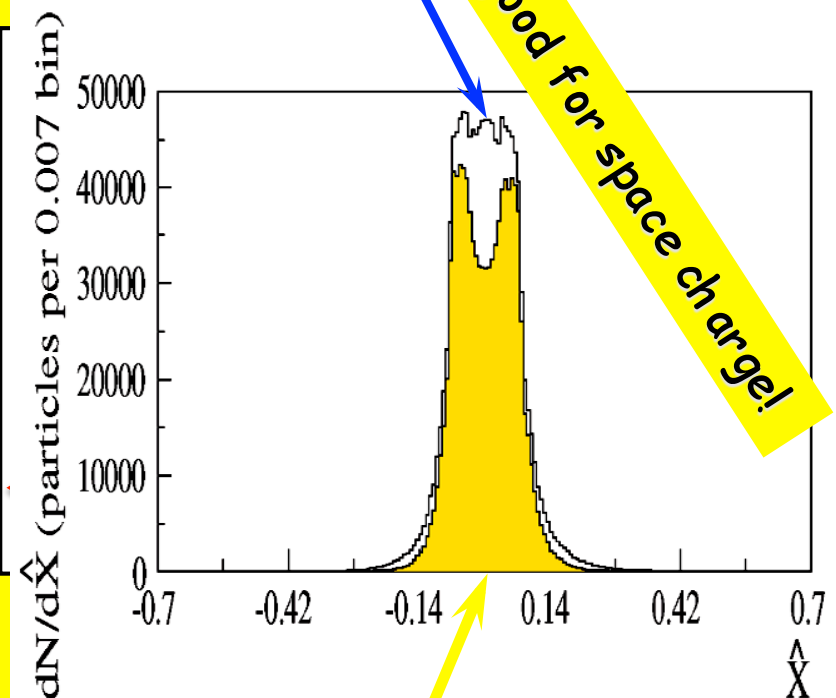
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Flat beam distribution obtained by injecting a fifth turn in the centre.



Hollow beam distribution

## MTE : core extraction with a single dipole kicker

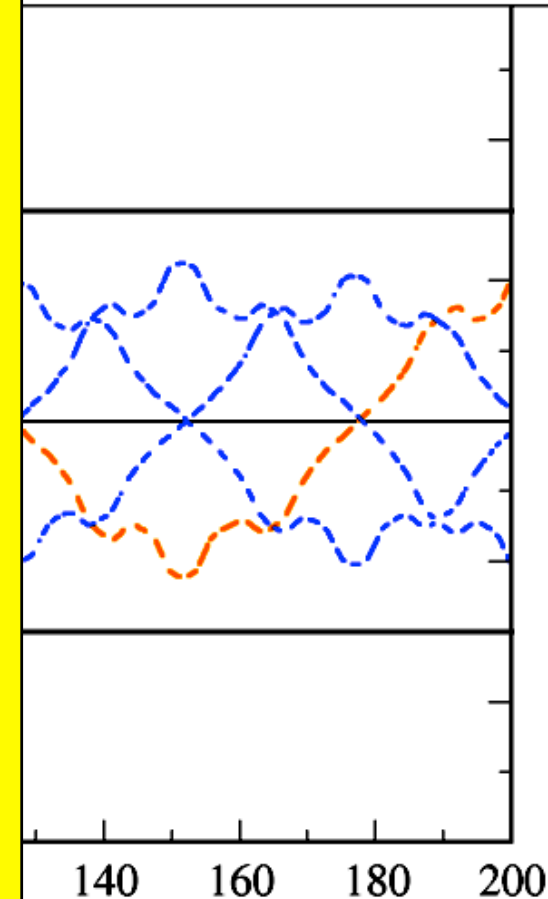
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- only one dipole kicker needed to extract the core

⇒ larger beam clearance, but not necessarily less “ferrite” in the ring.

But ...

--- orbit island #1 with insertion  
 --- core moved into island #1



## MTE : core extraction with a single dipole kicker

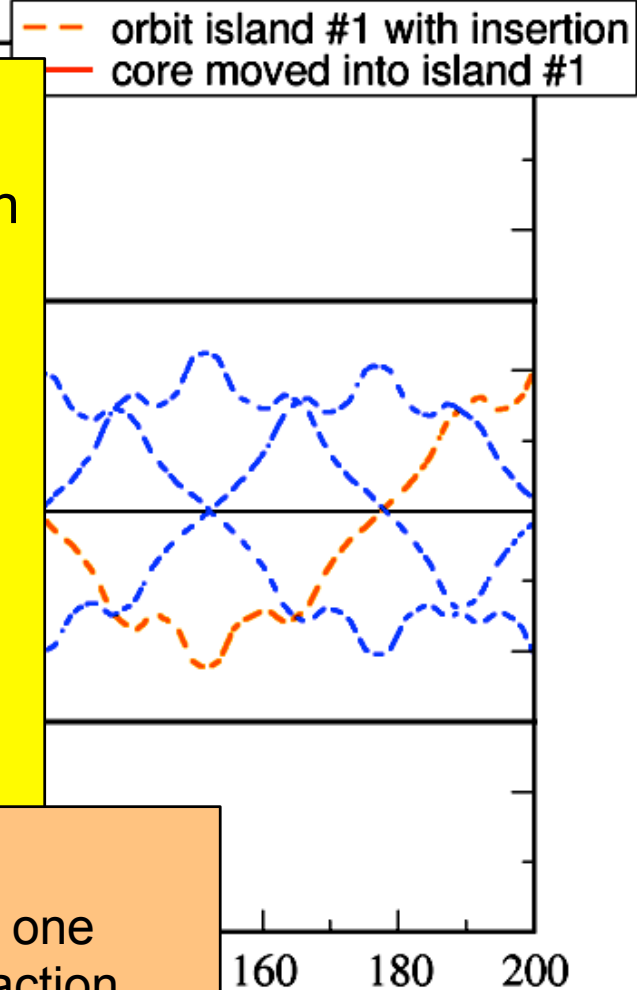
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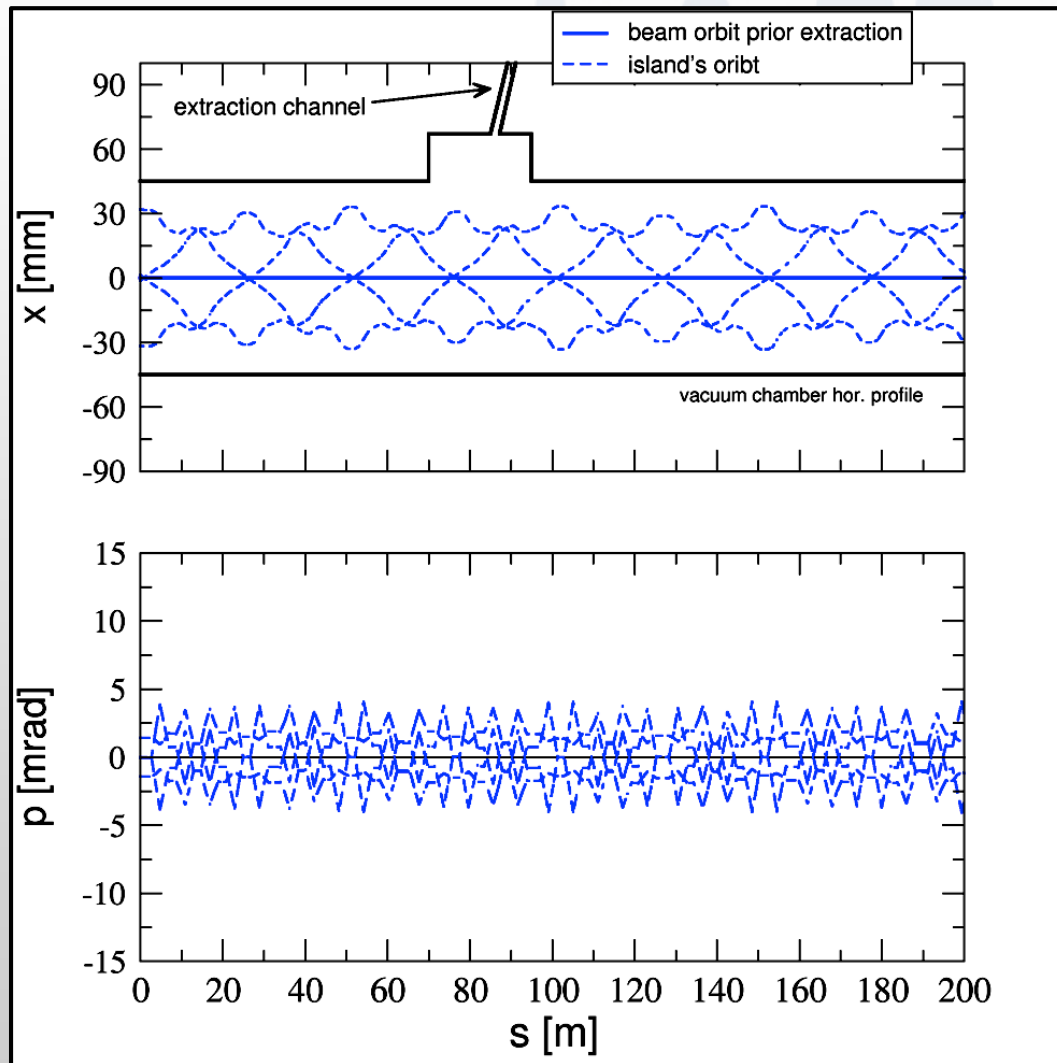
But ...

#### Observation #4

- The extraction of the core (over one turn) is equivalent to a fast extraction

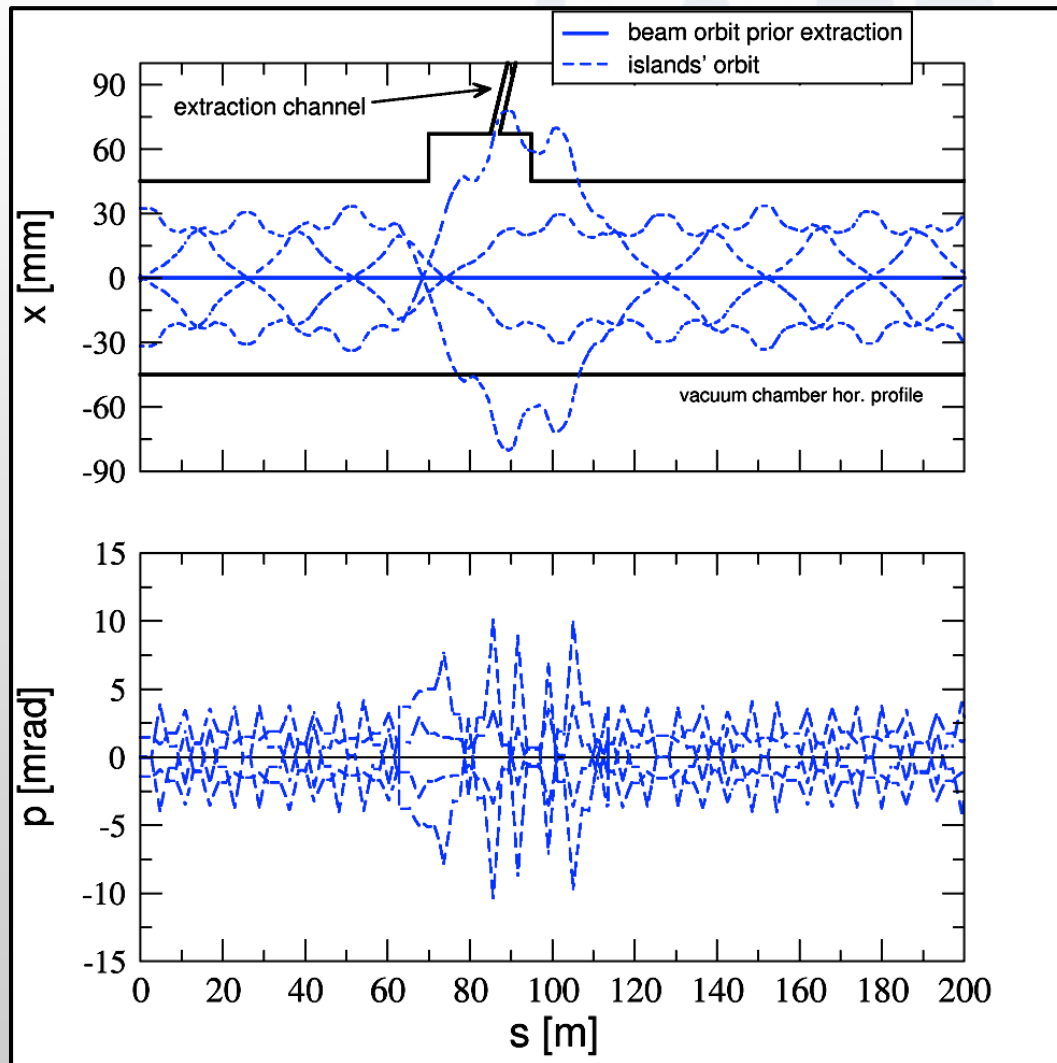


## Fast Extraction with 4<sup>th</sup> order resonance



**step 1:** generate (though do not populate) four islands. the beam remain on axis

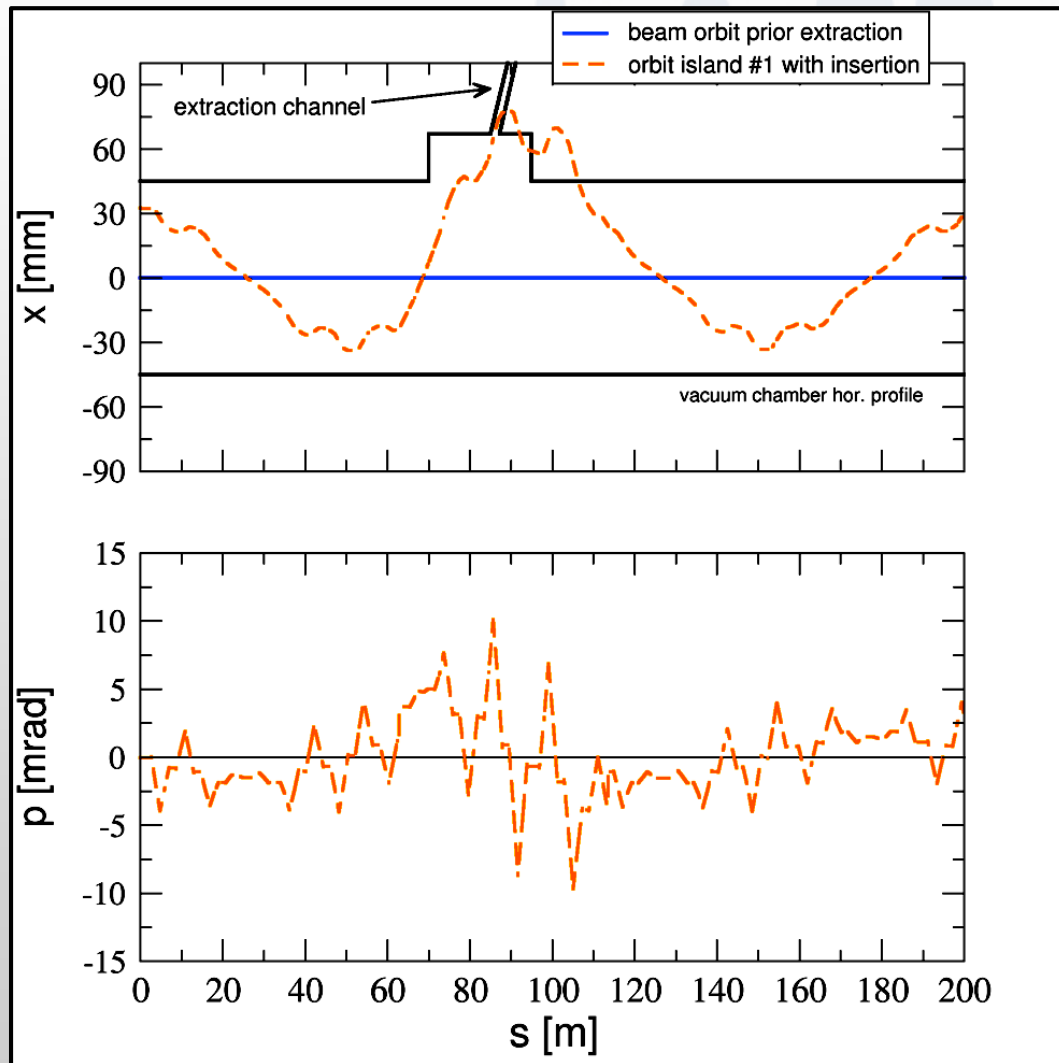
## Fast Extraction with 4<sup>th</sup> order resonance



**step 1:** generate (though do not populate) four islands. the beam remain on axis

**step 2:** introduce the insertion optics via quadrupole bumpers, not kickers (actually not needed)

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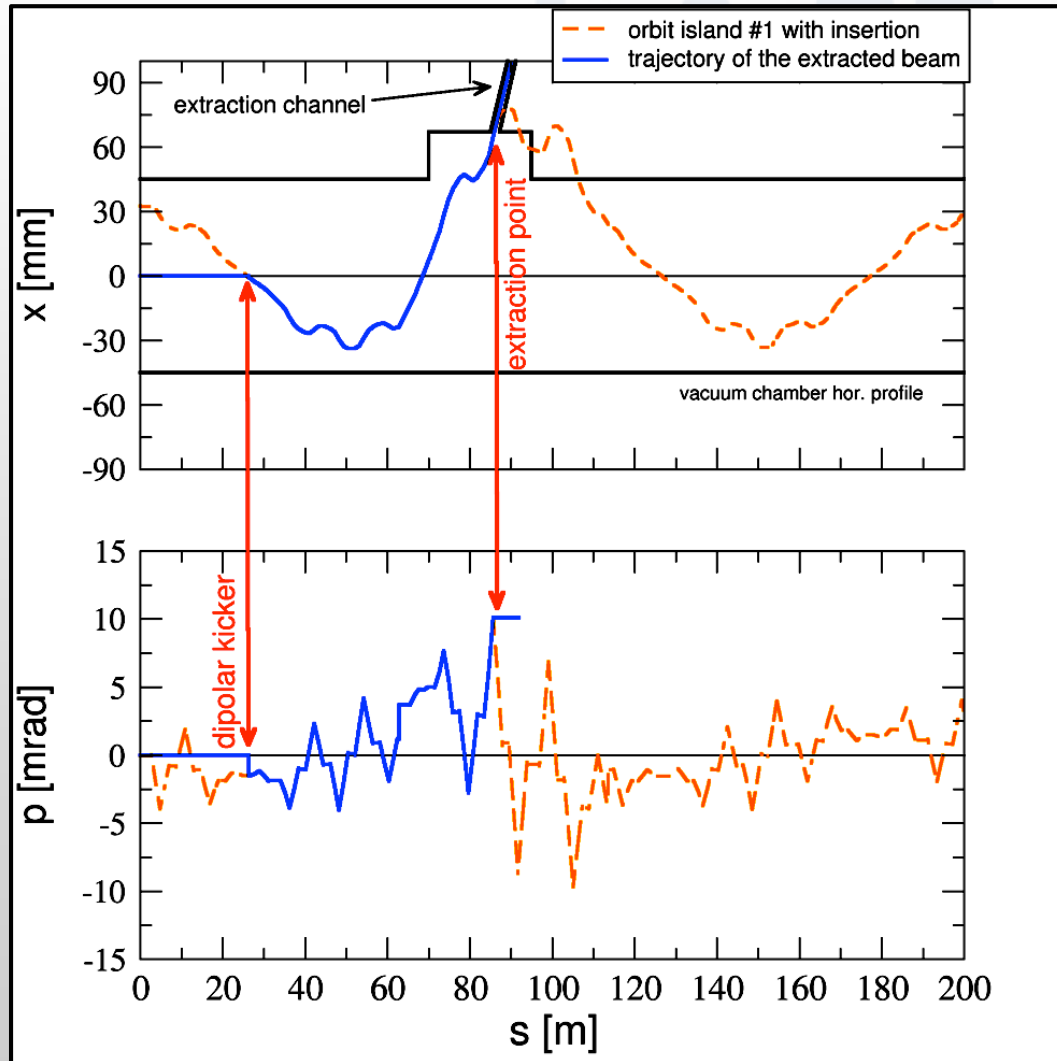


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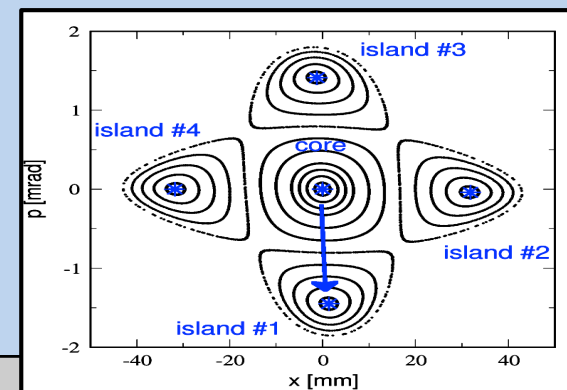
## Fast Extraction with 4<sup>th</sup> order resonance



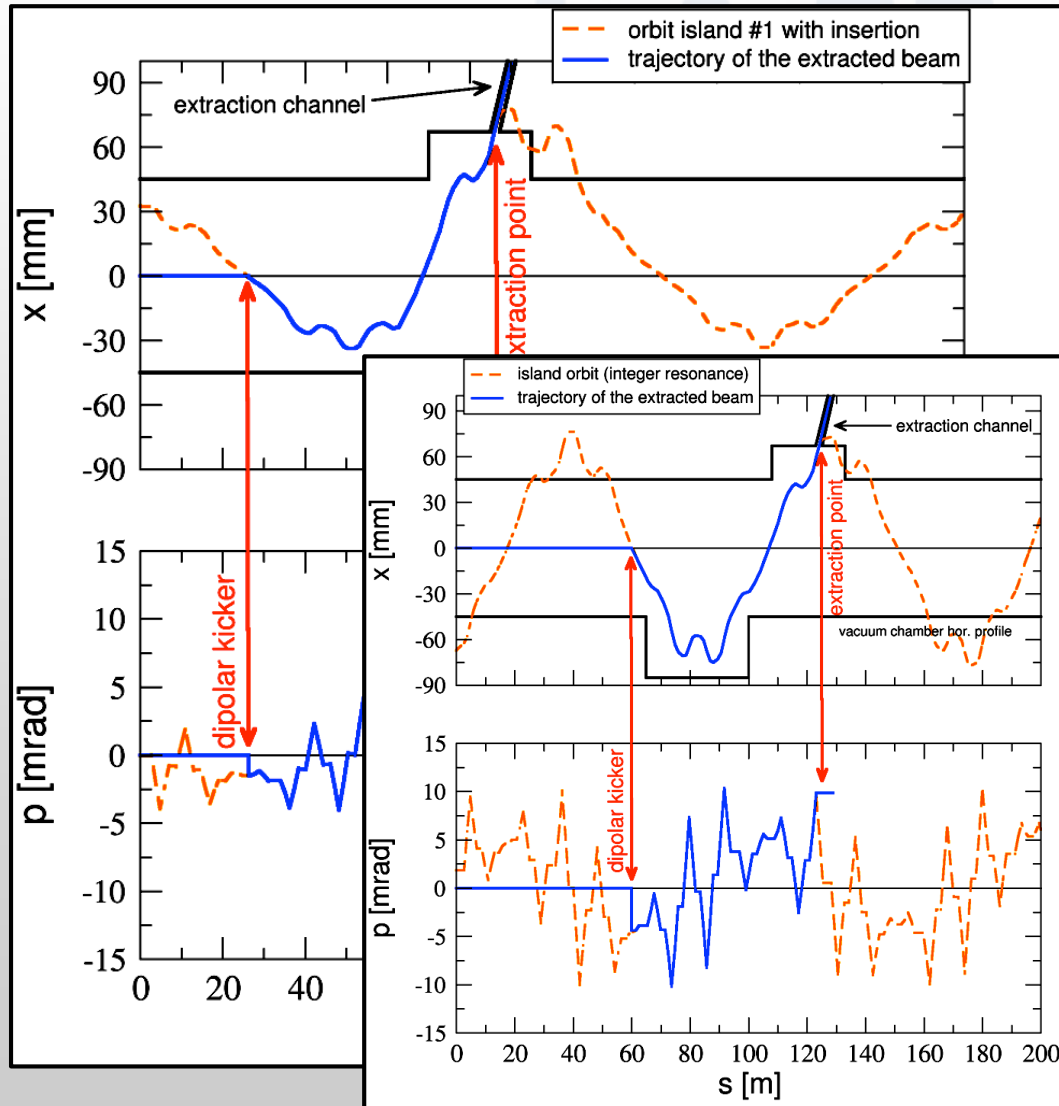
**step 1:** generate (though do not populate) four islands. the beam remain on axis

**step 2:** introduce the insertion optics via quadrupole bumpers, not kickers (actually not needed)

**step 3:** install and pulse a dipole kicker at a waist to move the beam from the axis to the island



## Fast Extraction with 4<sup>th</sup> order resonance



to avoid insertion optics (unpopulated) islands may be displaced by moving  $Q_x$  only

**step 2:** introduce the **insertion optics** via quadrupole bumpers, not kickers (**actually not needed**)

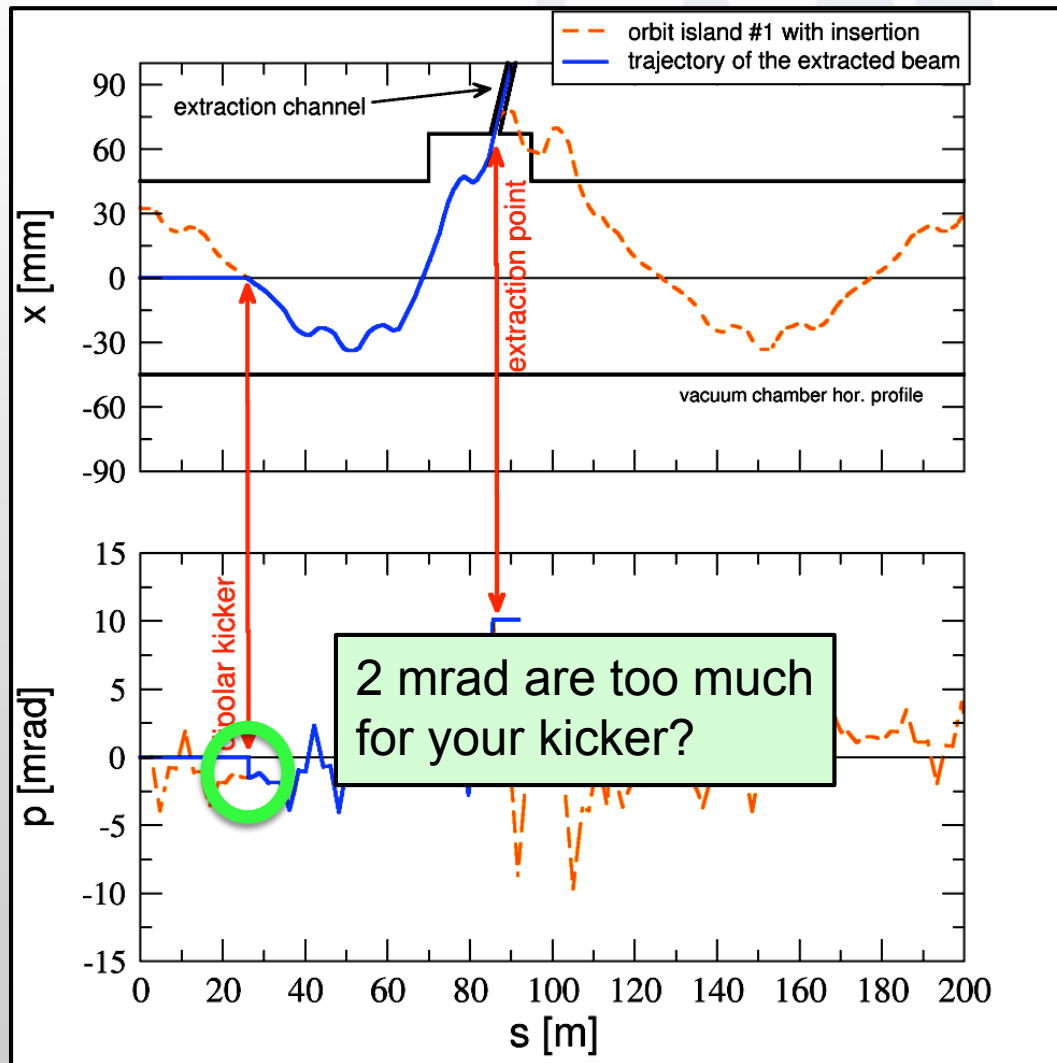
**step 3:** install and pulse a dipole kicker at a waist to move the beam from the axis

$$x^*(\Delta, \Omega_2, s) \propto \sqrt{\beta_x(s)} \rho^*(\Delta, \Omega_2)$$

$$\rho^*(\Delta, \Omega_2, s) \propto -\sqrt{\frac{\rho^*(\Delta, \Omega_2)}{\beta_x(s)}}$$

$$\rho^*(\Delta, \Omega_2) \simeq -\frac{2\pi\Delta}{\Omega_2} \begin{cases} \Delta = Q_x - \bar{Q}_x \\ \Omega_2 = \text{detuning coefficient} \end{cases}$$

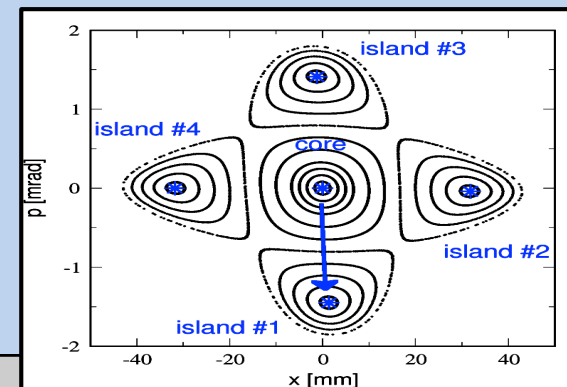
## Fast Extraction with 4<sup>th</sup> order resonance



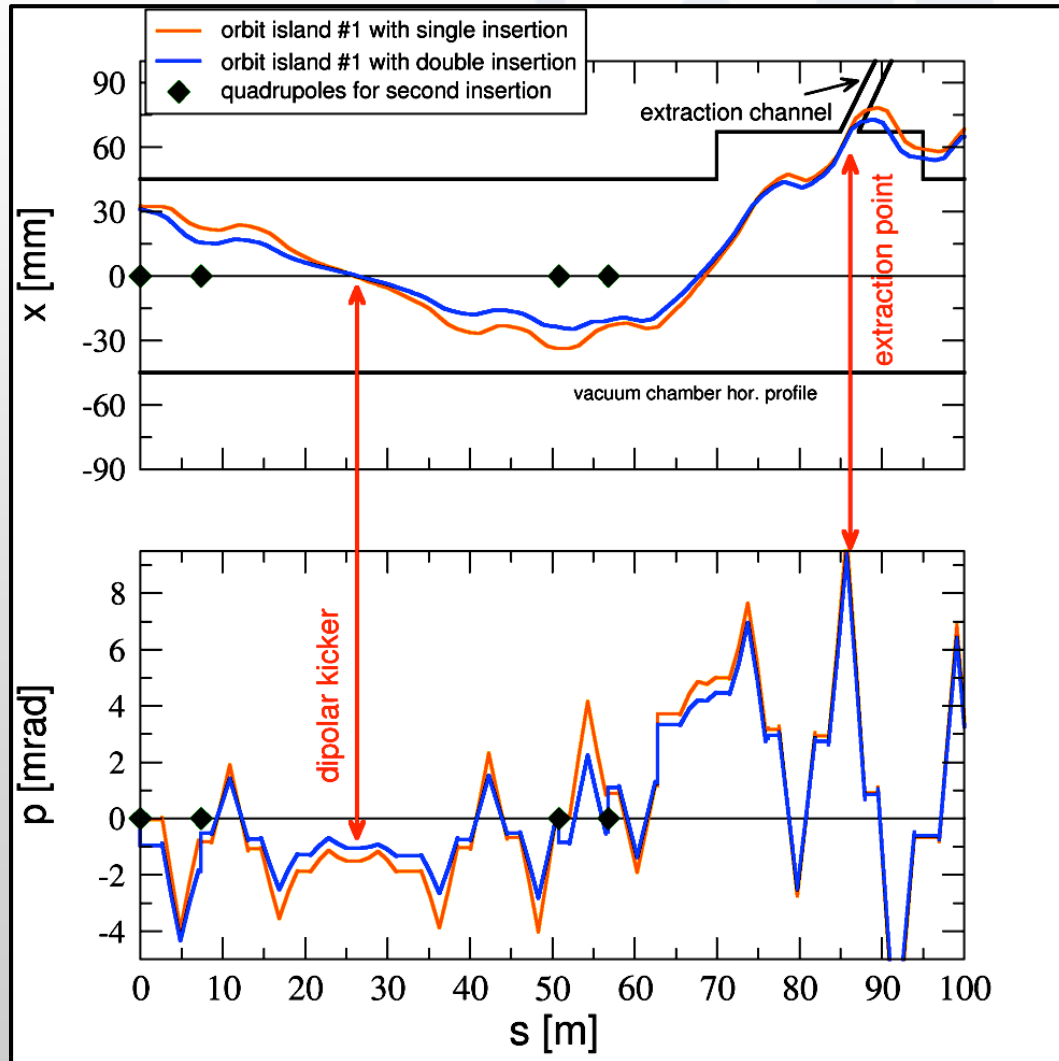
**step 1:** generate (though do not populate) four islands. the beam remain on axis

**step 2:** introduce the insertion optics via quadrupole bumpers, not kickers (actually not needed)

**step 3:** install and pulse a dipole kicker at a waist to move the beam from the axis to the island



## Fast Extraction with 4<sup>th</sup> order resonance



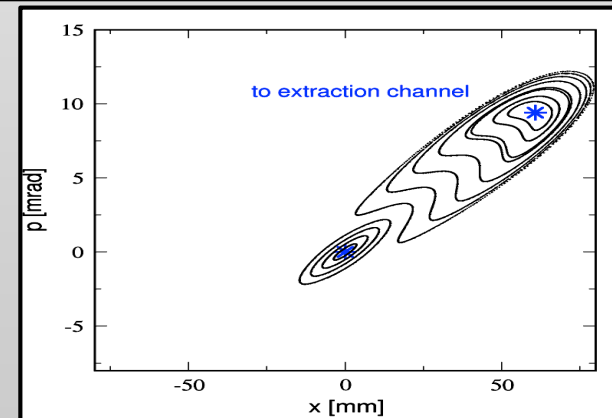
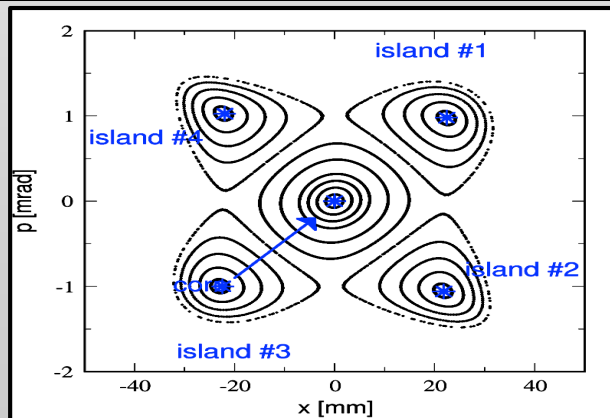
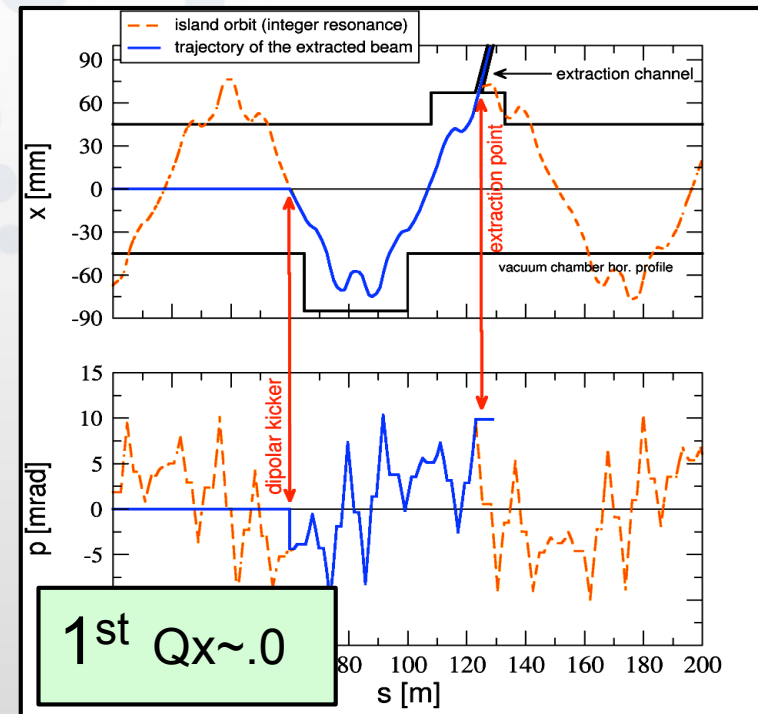
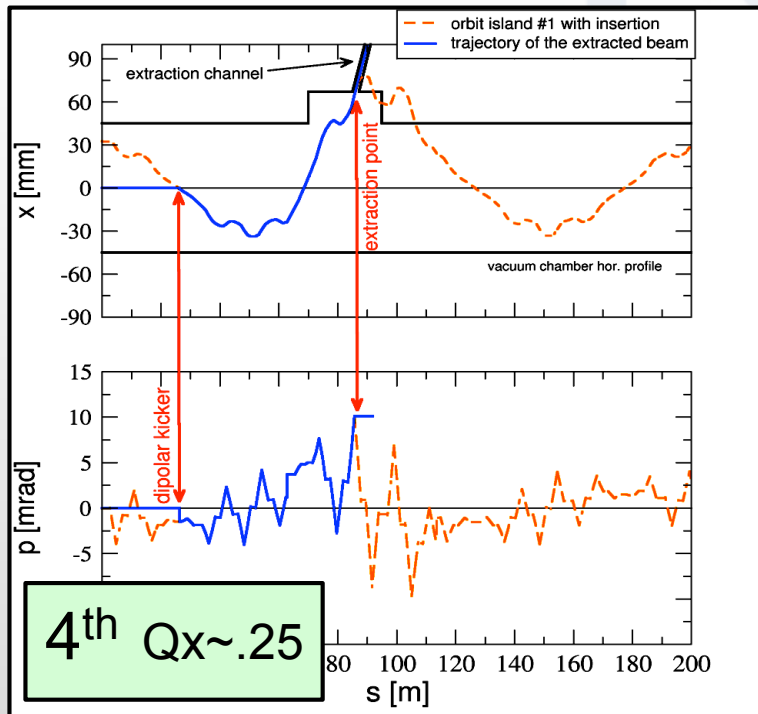
**step 1:** generate (though do not populate) four islands. the beam remain on axis

**step 2:** introduce the insertion optics via quadrupole bumpers, not kickers (actually not needed)

**step 3:** install and pulse a dipole kicker at a waist to move the beam from the axis to the island

**step 4:** introduce an insertion optics around the waist (i.e. the kicker) to increase  $\beta_x$  and hence to reduce  $p_x$  & kicker strength

## Fast Extraction with $N^{\text{th}}$ order resonance



## Septum-less fast extraction (injection)

- nonlinear optics designed to generate N unpopulated stable islands with one orbit suitable to enter the extraction channel (with quadrupole bumpers only, though not needed)
- only one dipole kicker is needed, whose strength may be minimized with high- $\beta$  insertion optics

### septum-less fast injection:

- as above, look at the plots from right to left.