

# EW Corrections in Top-Quark Physics

*part II*



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# OUTLINE

## Charge asymmetry at the Tevatron and the LHC

## NLO QCD and EW corrections to $t\bar{t}V$ , ( $V = H, W, Z$ )

- Completely automated results at 8, 13, 100 TeV and in a boosted regime

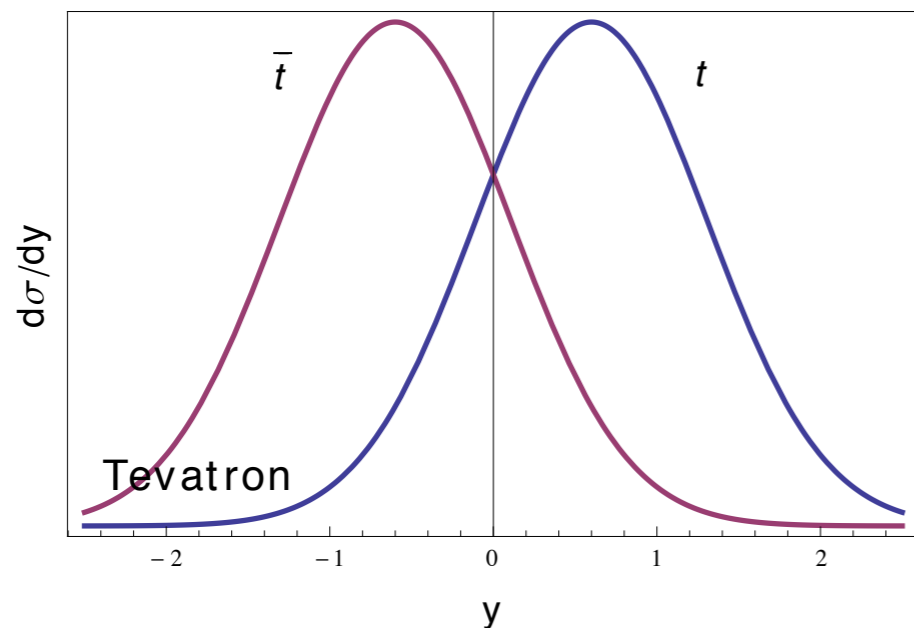
## $t\bar{t}V$ and $t\bar{t}VV$ at NLO QCD (V radiation is EW!)

- Completely automated results and total cross section energy dependence
- Asymmetries in  $t\bar{t}V$  at NLO in QCD

## Single top and its pathologies

## Conclusions

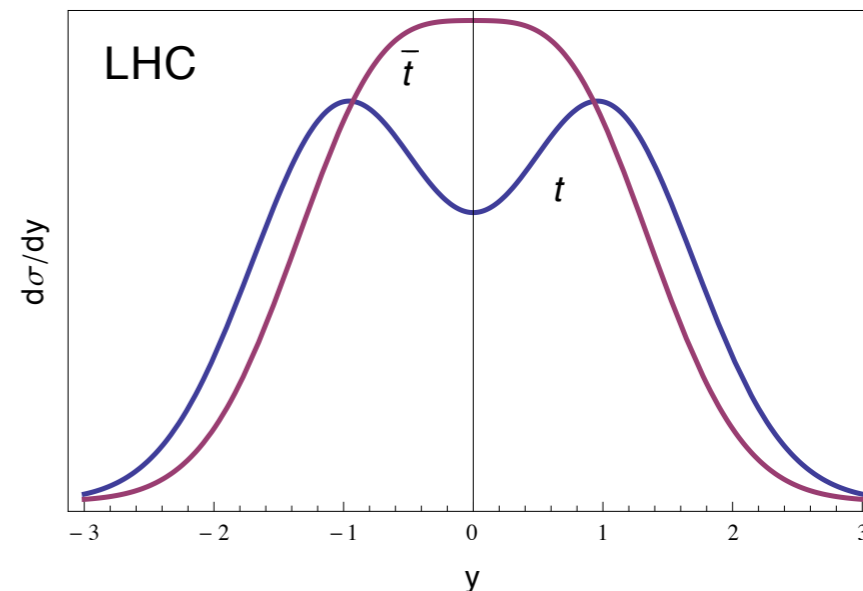
# Charge asymmetry



forward-backward

$$A_{t\bar{t}} = \frac{N(y_t > y_{\bar{t}}) - N(y_{\bar{t}} > y_t)}{N(y_t > y_{\bar{t}}) + N(y_{\bar{t}} > y_t)}$$

$$A_{\text{lab}} = \frac{N(y_t > 0) - N(y_t < 0)}{N(y_t > 0) + N(y_t < 0)}$$

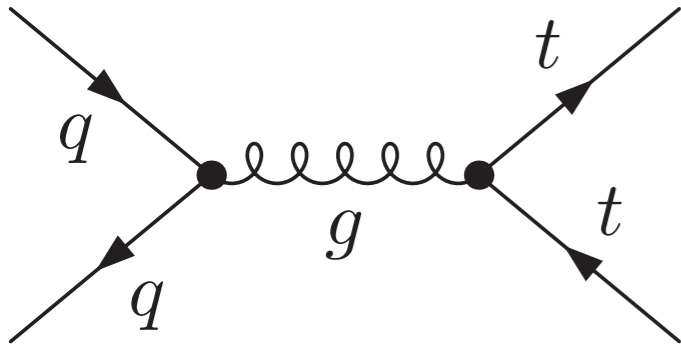


central

$$A_C^\eta = \frac{N(\Delta_\eta > 0) - N(\Delta_\eta < 0)}{N(\Delta_\eta > 0) + N(\Delta_\eta < 0)}$$

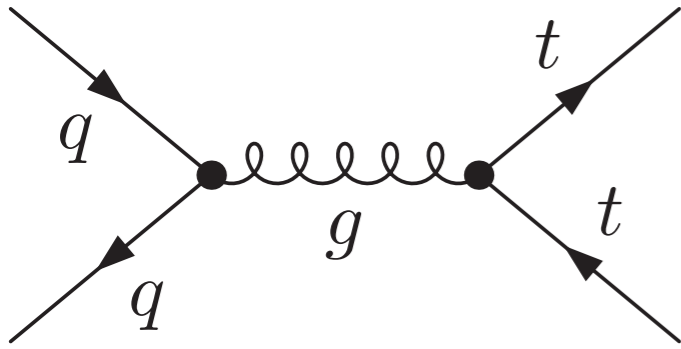
$$A_C^y = \frac{N(\Delta_y > 0) - N(\Delta_y < 0)}{N(\Delta_y > 0) + N(\Delta_y < 0)}$$

Same mechanisms at the matrix level for Tevatron and the LHC



At LO partonic processes are not asymmetric.  
 QCD produces the asymmetry only at NLO!  
NLO in the cross-section, LO in  $A_{FB}$

$$A_{FB} = \frac{N}{D} = \frac{\alpha^2 \tilde{N}_0 + \alpha_s^3 N_1 + \alpha_s^2 \alpha \tilde{N}_1 + \alpha_s^4 N_2 + \dots}{\alpha^2 \tilde{D}_0 + \alpha_s^2 D_0 + \alpha_s^3 \tilde{D}_1 + \alpha_s^2 \alpha \tilde{D}_1 + \dots} = \alpha_s \frac{N_1}{D_0} + \alpha \frac{\tilde{N}_1}{D_0} + \frac{\alpha^2}{\alpha_s^2} \frac{\tilde{N}_0}{D_0}$$



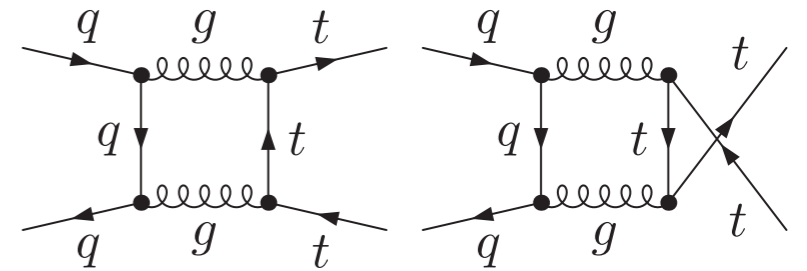
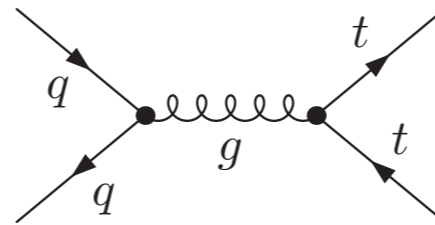
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gg initial state does not contribute to Tevatron and LHC asymmetry numerator!  
 q-qbar QCD contribution only from interactions between initial and final state!

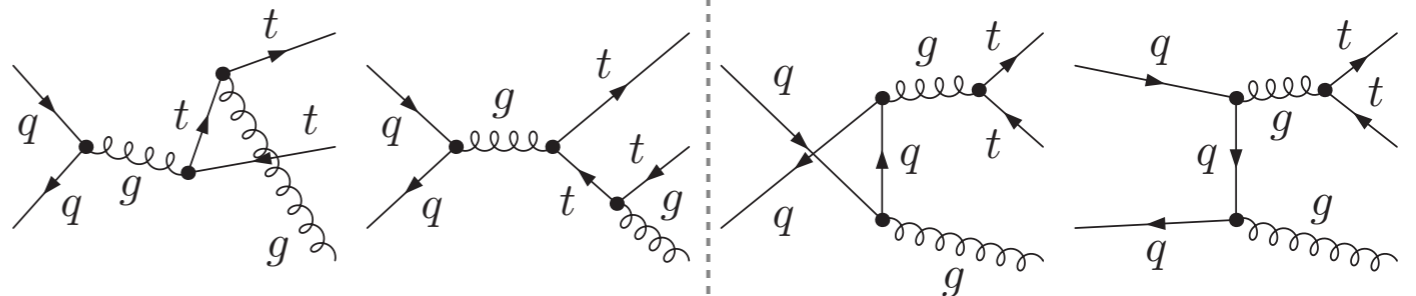
$$\alpha_s \frac{N_1}{D_0}$$

VIRTUAL (Only Boxes)  
 NO UV, NO Coll. Div.  
 Only IR



REAL

Only the interference of initial- and final-state gluon emissions is asymmetric.



Final

Initial

*Kuhn, Rodrigo '99*

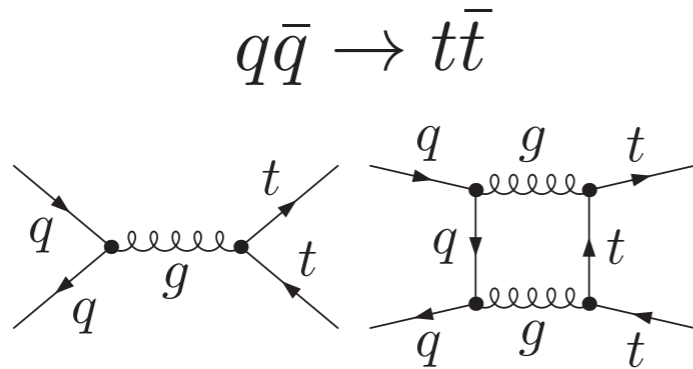
$$\alpha \frac{\tilde{N}_1}{D_0}$$

It is useful to divide the electroweak contribution into a QED (photon) and a weak (Z) part.

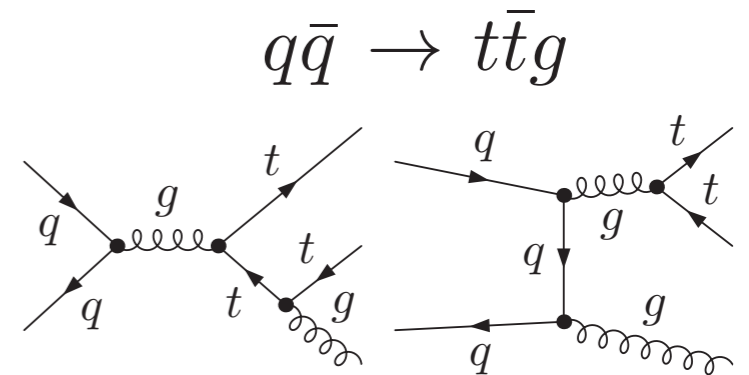
**QED**

The QED contribution can be easily obtained from the QCD calculation and the substitution of one gluon into one photon in the squared amplitudes.

$$|\overline{\mathcal{M}^{t\bar{t}}}|^2_{\mathcal{O}(\alpha_s^3)}$$



$$|\overline{\mathcal{M}^{t\bar{t}g}}|^2_{\mathcal{O}(\alpha_s^3)}$$



$$\alpha \frac{\tilde{N}_1}{D_0}$$

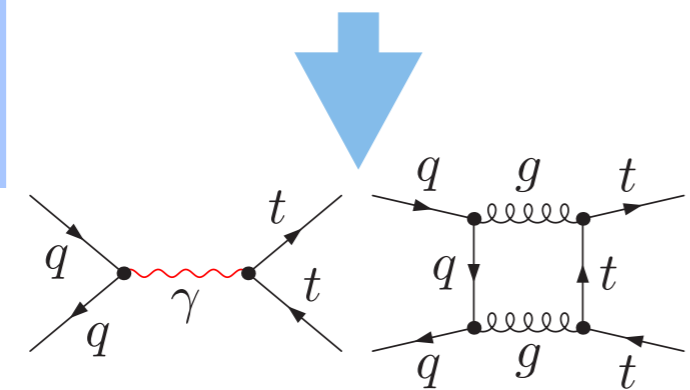
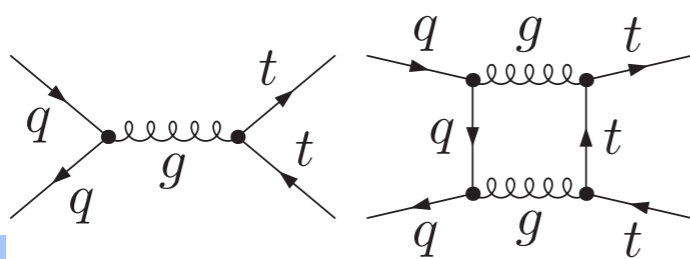
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# QED

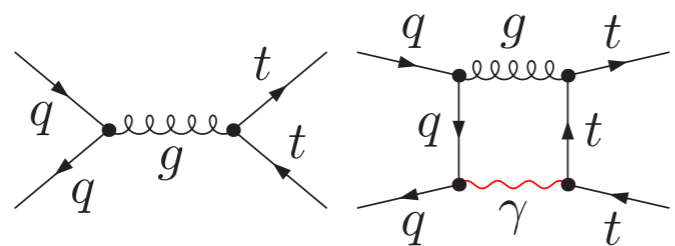
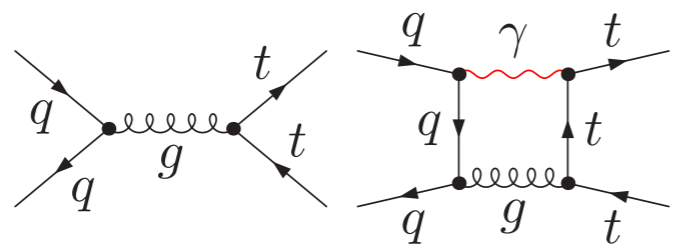
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#(QED diagrams)  
= 3 #(QCD diagrams)

$$q\bar{q} \rightarrow t\bar{t}$$

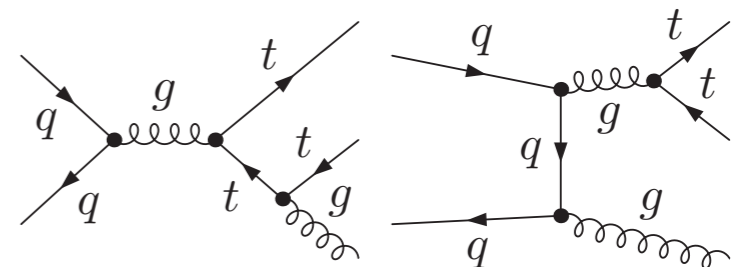


$$|\mathcal{M}^{t\bar{t}}|^2_{\mathcal{O}(\alpha_s^2\alpha)}$$

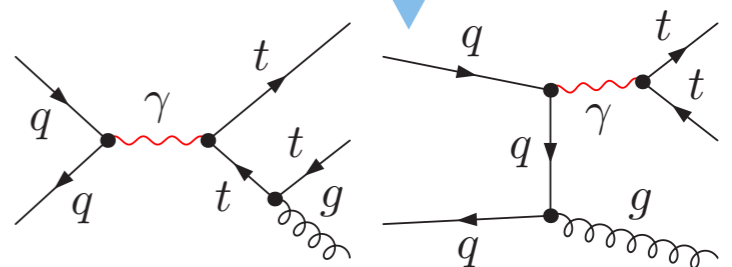


$$q\bar{q} \rightarrow t\bar{t}g$$

$$|\mathcal{M}^{t\bar{t}g}|^2_{\mathcal{O}(\alpha_s^3)}$$

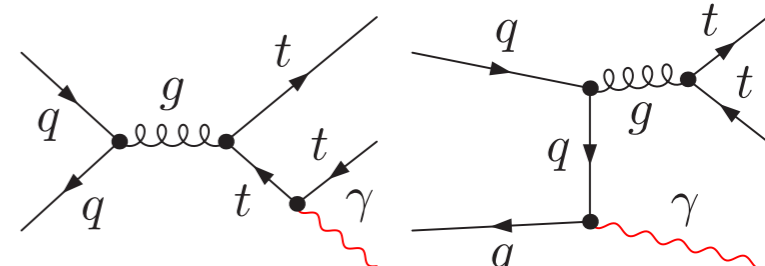


$$|\mathcal{M}^{t\bar{t}g}|^2_{\mathcal{O}(\alpha_s^2\alpha)}$$



$$q\bar{q} \rightarrow t\bar{t}\gamma$$

$$|\mathcal{M}^{t\bar{t}\gamma}|^2_{\mathcal{O}(\alpha_s^2\alpha)}$$



**DIFFERENCES:**  
Only couplings and color factors!

$$A_{FB} = \frac{N}{D} = \frac{\alpha^2 \tilde{N}_0 + \alpha_s^3 N_1 + \alpha_s^2 \alpha \tilde{N}_1 + \alpha_s^4 N_2 + \dots}{\alpha^2 \tilde{D}_0 + \alpha_s^2 D_0 + \alpha_s^3 D_1 + \alpha_s^2 \alpha \tilde{D}_1 + \dots} = \alpha_s \frac{N_1}{D_0} + \alpha \frac{\tilde{N}_1}{D_0} + \frac{\alpha^2}{\alpha_s^2} \frac{\tilde{N}_0}{D_0}$$

*Hollik, D.P. '11*

$$R_{QED}(Q_q) = \frac{\alpha \tilde{N}_1^{QED}}{\alpha_s N_1} = Q_q Q_t \frac{36}{5} \frac{\alpha}{\alpha_s}$$

QED corrections can be obtained from  $QCD \times R_{QED}$



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QED corrections can be obtained from  $\text{QCD} \times R_{\text{QED}}$

**Weak**

The same diagrams as in the QED part, but  $\gamma \rightarrow Z$ .

Z is not massless  $\rightarrow$  If we write  $\text{Weak} = \text{QCD} \times R_{\text{Weak}}$ :

$R_{\text{Weak}}$  does not depend only on couplings and color factors.

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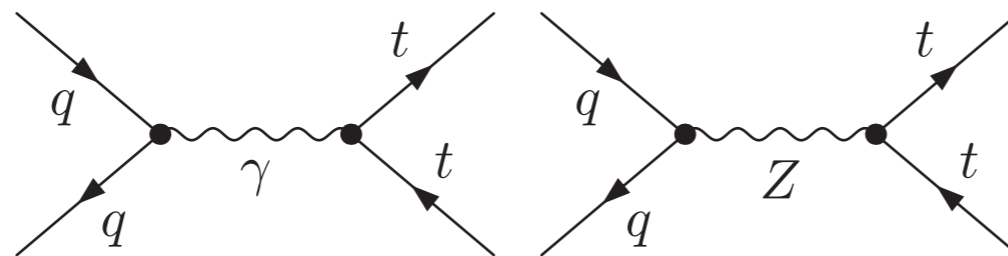
QED corrections can be obtained from  $QCD \times R_{QED}$

**Weak**

The same diagrams as in the QED part, but  $\gamma \rightarrow Z$ .

Z is not massless  $\rightarrow$  If we write Weak =  $QCD \times R_{Weak}$ :  
 $R_{Weak}$  does not depend only on couplings and color factors.

$$\frac{\alpha^2 \tilde{N}_0}{\alpha_s^2 D_0}$$



Different couplings for different chiralities produce asymmetric terms in the cross section

$$\frac{d\sigma_{asym}}{d\cos\theta} = 2\pi\alpha^2 \cos\theta \left(1 - \frac{4m_t^2}{s}\right) \left[ \kappa \frac{Q_q Q_t A_q A_t}{(s - M_Z^2)} + 2\kappa^2 \frac{A_q A_t V_q V_t}{(s - M_Z^2)^2} \frac{s}{(s - M_Z^2)^2} \right]$$

# Forward-backward asymmetry

(a)  $A_{FB}^{t\bar{t}}$

$A_{FB}^{t\bar{t}}$		$\mu = m_t/2$	$\mu = m_t$	$\mu = 2m_t$
$\mathcal{O}(\alpha_s^3)$	$u\bar{u}$	7.01%	6.29%	5.71%
$\mathcal{O}(\alpha_s^3)$	$d\bar{d}$	1.16%	1.03%	0.92%
$\mathcal{O}(\alpha_s^2\alpha)_{QED}$	$u\bar{u}$	1.35%	1.35%	1.35%
$\mathcal{O}(\alpha_s^2\alpha)_{QED}$	$d\bar{d}$	-0.11%	-0.11%	-0.11%
$\mathcal{O}(\alpha_s^2\alpha)_{weak}$	$u\bar{u}$	0.16%	0.16%	0.16%
$\mathcal{O}(\alpha_s^2\alpha)_{weak}$	$d\bar{d}$	-0.04%	-0.04%	-0.04%
$\mathcal{O}(\alpha^2)$	$u\bar{u}$	0.18%	0.23%	0.28%
$\mathcal{O}(\alpha^2)$	$d\bar{d}$	0.02%	0.03%	0.03%
tot	$p\bar{p}$	9.72%	8.93%	8.31%

EW CORRECTIONS

$$R_{QED}^{u\bar{u}} = (0.192, 0.214, 0.237)$$

$$R_{QED}^{d\bar{d}} = (-0.096, -0.107, -0.119)$$

- $R_{QED}$  depend only on the renormalization scale, not on  $A_{FB}$  definitions and cuts.  
(with fixed scales)

*Hollik, DP '11*

$\mathcal{O}(\alpha_s^2\alpha)$  QED is the dominant contribution of the electroweak corrections. It is stable under factorization and renormalization scale variation.

u and d have different charges: contributions of opposite sign for  $\mathcal{O}(\alpha_s^2\alpha)$

# Forward-backward asymmetry

$$R_{EW}^{t\bar{t}} = \frac{N_{\mathcal{O}(\alpha_s^2\alpha)+\mathcal{O}(\alpha^2)}^{t\bar{t}}}{N_{\mathcal{O}(\alpha_s^3)}^{t\bar{t}}} = (0.190, 0.220, 0.254)$$

$$R_{EW}^{t\bar{t}}(M_{t\bar{t}} > 450 \text{ GeV}) = (0.200, 0.232, 0.266)$$

$$R_{EW}^{p\bar{p}} = \frac{N_{\mathcal{O}(\alpha_s^2\alpha)+\mathcal{O}(\alpha^2)}^{p\bar{p}}}{N_{\mathcal{O}(\alpha_s^3)}^{p\bar{p}}} = (0.186, 0.218, 0.243)$$

$$R_{EW}^{t\bar{t}}(|\Delta y| > 1) = (0.191, 0.216, 0.246)$$

The complete ratios  $R_{EW}$  depend on fac/ren scales, and very slightly on  $A_{FB}$  definitions and cuts.

*Hollik, DP '11*

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*Hollik, DP '11*

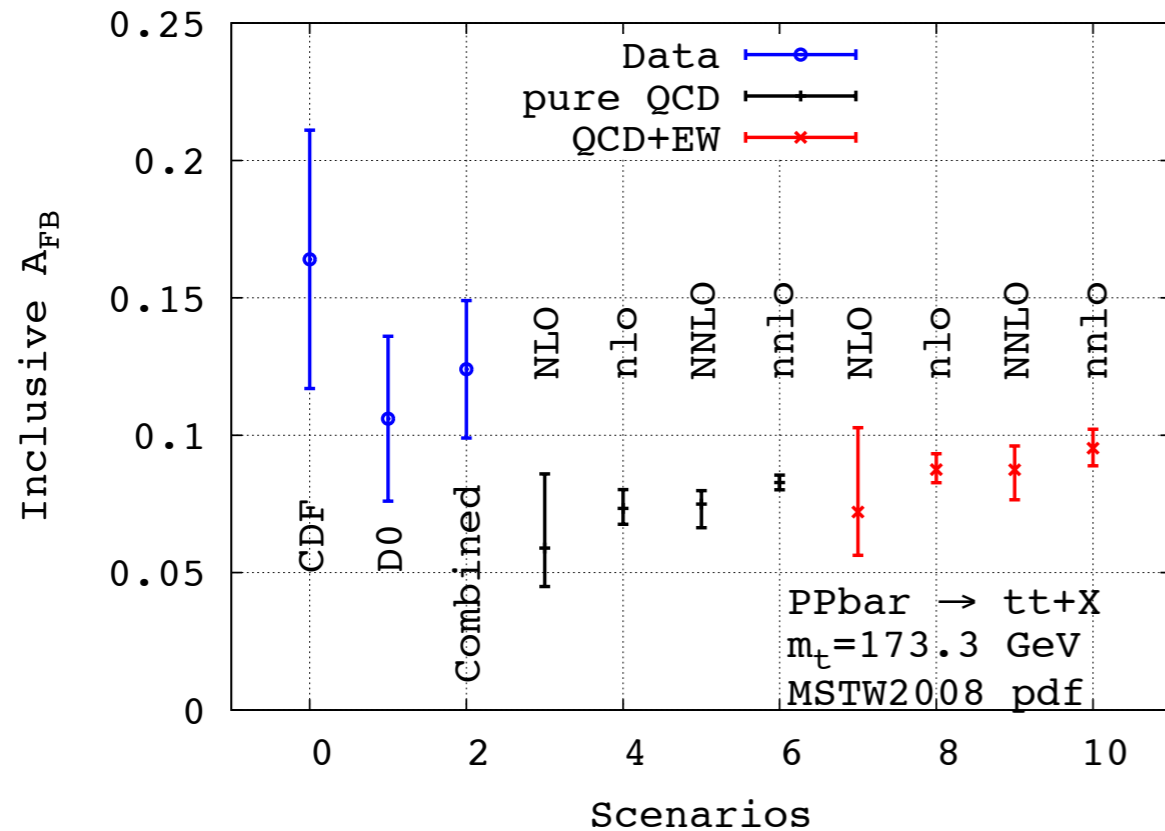
EW corrections to AFB are not induced by Sudakov logs. However, they are “more important” than EW corrections to cross sections. 2 Reasons:

- LO cross section is  $\mathcal{O}(\alpha_s^2)$ , LO numerator of  $A_{FB}$  is  $\mathcal{O}(\alpha_s^3)$

- The dominant EW contribution ( $\mathcal{O}(\alpha_s^2\alpha)$  QED) to the  $A_{FB}$  originates only from boxes: 3 times the number of diagrams of the QCD case.

The QED contribution to the total cross section originates “from vertex corrections”: same number of diagrams of QCD case.

# Forward-backward asymmetry



Capital: unexpanded  
 Small: expanded  
 Red: QCD+EW  
 Black: QCD

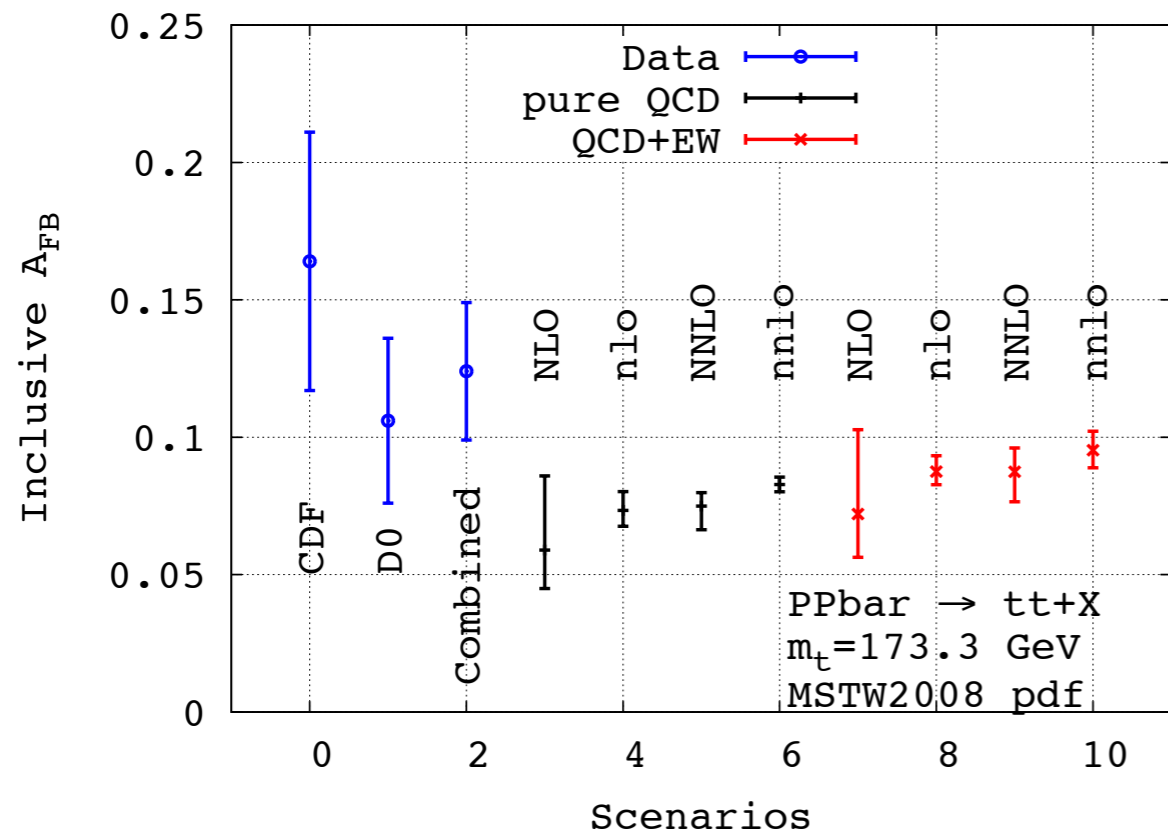
No EW corrections in the denominator of:

$$A_{t\bar{t}} = \frac{N(y_t > y_{\bar{t}}) - N(y_{\bar{t}} > y_t)}{N(y_t > y_{\bar{t}}) + N(y_{\bar{t}} > y_t)}$$

- EW contribution is relevant.
- $NLO \neq NNLO$ ,  $nlo \sim nnlo$ .

Czakov, Fiedler, Mitov '14

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- EW contribution is relevant.
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*Czakon, Fiedler, Mitov '14*

Sudakov logs suppress the total cross section in the denominator (especially for high invariant mass) and increase the asymmetric numerator.

Resummed logs increase  $A_{FB}$  by a factor 1.05. (0.5% overlap with NLO EW)

Bin [GeV]	$A_{FB}^{t\bar{t}}(\%)$			$\mathcal{R}_{FB}(t)$	$\mathcal{R}_{FB}^{\alpha_s^2}(t)$	$\mathcal{R}_t$
$[2 m_{t\bar{t}}, 1960]$	7.7	7.5	1.6	1.02	1.03	0.98
$[2 m_{t\bar{t}}, 450]$	5.6	5.4	—	1.02	1.03	0.98
$[450, 900]$	11	12	2.3	1.02	1.04	0.97

*Manohar, Trott '12*

# Charge asymmetry

At the LHC same partonic processes, but different partonic luminosities.

The gluon-gluon luminosity is larger, so the asymmetry is smaller.  
Gluon-quark initial states start to be “interesting” (per mill).

The ratio of integrated luminosities  $u\bar{u}/d\bar{d}$  at the Tevatron(LHC) is 4(2).  
The cancellation between QED contributions is bigger. The EW contribution at the LHC is in general smaller ( $\sim 15\%$ ,  $20\%$  of QCD contribution).

$$R_{QED}(Q_q) = \frac{\alpha \tilde{N}_1^{QED}}{\alpha_s N_1} = Q_q Q_t \frac{36}{5} \frac{\alpha}{\alpha_s}$$

$\sqrt{s}$		$M_c = 2m_t$	0.5 TeV	0.7 TeV	1 TeV
7 TeV	QCD: $A_C^{\Delta y }$ (%)	1.07 (4)	1.27 (4)	1.68 (4)	2.06 (5)
	QCD + EW: $A_C^{\Delta y }$ (%)	1.23 (5)	1.48 (4)	1.95 (4)	2.40 (6)
8 TeV	QCD: $A_C^{\Delta y }$ (%)	0.96 (4)	1.14 (4)	1.48 (4)	1.85 (4)
	QCD + EW: $A_C^{\Delta y }$ (%)	1.11 (4)	1.33 (5)	1.73 (5)	2.20 (5)
		$M_c = 2m_t$	0.5 TeV	1 TeV	2 TeV
14 TeV	QCD: $A_C^{\Delta y }$ (%)	0.58 (3)	0.74 (3)	1.11 (5)	1.72 (10)
	QCD + EW: $A_C^{\Delta y }$ (%)	0.67 (4)	0.86 (5)	1.32 (8)	2.12 (10)

*Bernreuther, Si '12*



# Top-quark pair in association with a heavy boson

$$t\bar{t}V \quad V = H, W, Z$$

**Weak** corrections to **Higgs** hadroproduction in association with a top-quark pair

*Frixione, Hirschi, DP, Shao, Zaro* arXiv:1407.0823

$$t\bar{t}H$$

QCD NLO and **EW** NLO corrections to **ttH** production with top quark decays  
at hadron collider

*Yu, Wen-Gan, Ren-You, Chong, Lei* arXiv:1407.1110

$$t\bar{t}H$$

**Electroweak** and QCD corrections to top-pair hadroproduction in association  
with **heavy bosons**

*Frixione, Hirschi, DP, Shao, Zaro* arXiv:1504.03446

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QCD corrections included in a consistent framework, with scale uncertainties.  
PDF errors for NLO QCD+EW.

Automated results via MadGraph5\_aMC@NLO.

# $t\bar{t}V$ production: numerical results

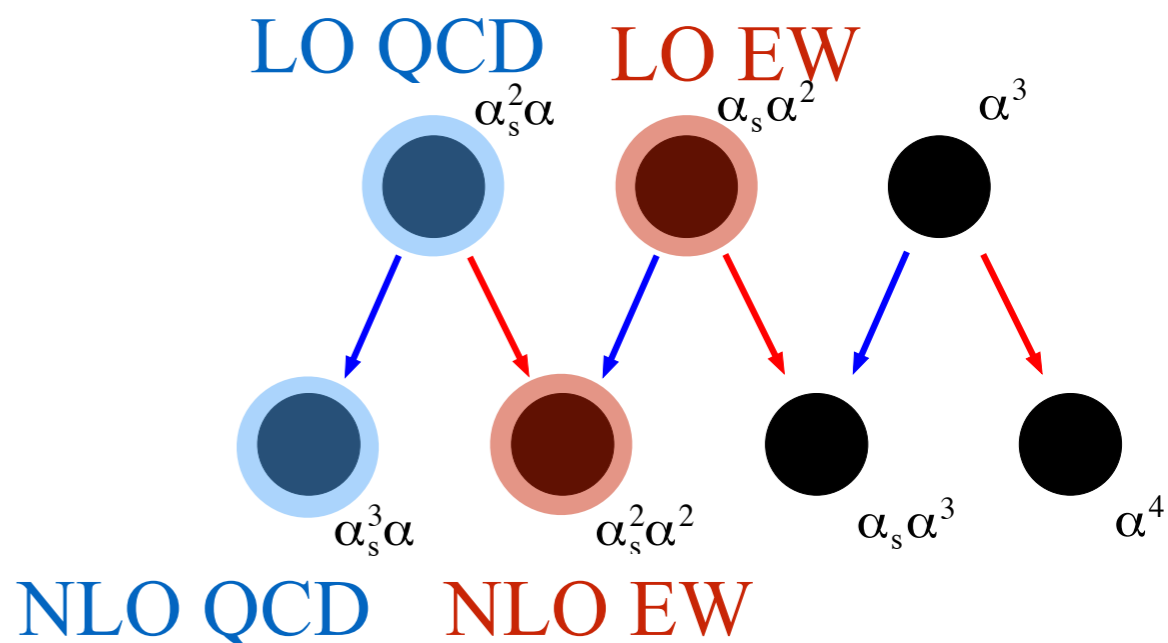
Alpha(mZ)-scheme, NNPDF2.3\_QED,

$$\mu = \frac{H_T}{2}, \quad \frac{1}{2}\mu \leq \mu_R, \mu_F \leq 2\mu$$

## Contributions

Heavy Boson radiation HBR ( $pp \rightarrow t\bar{t}V + V'$ )  
is of the same order of NLO EW.  
(Does it cancel Sudakov logs?)

The Photon PDF (with large uncertainties)  
enters in LO EW and NLO EW.



# $t\bar{t}V$ production: numerical results

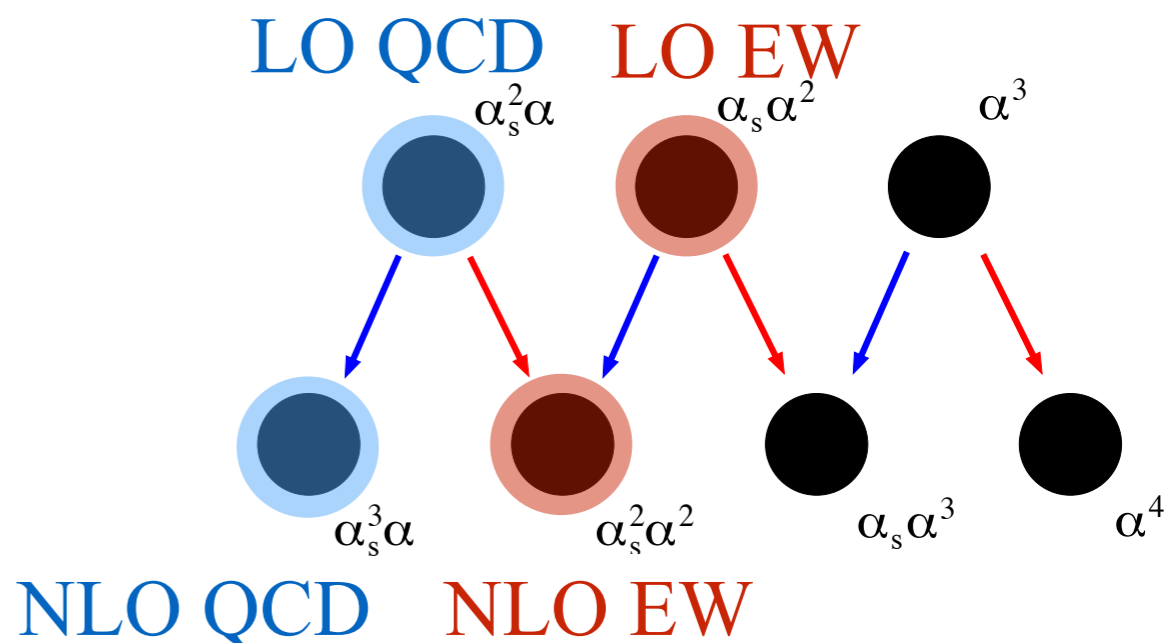
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## Contributions

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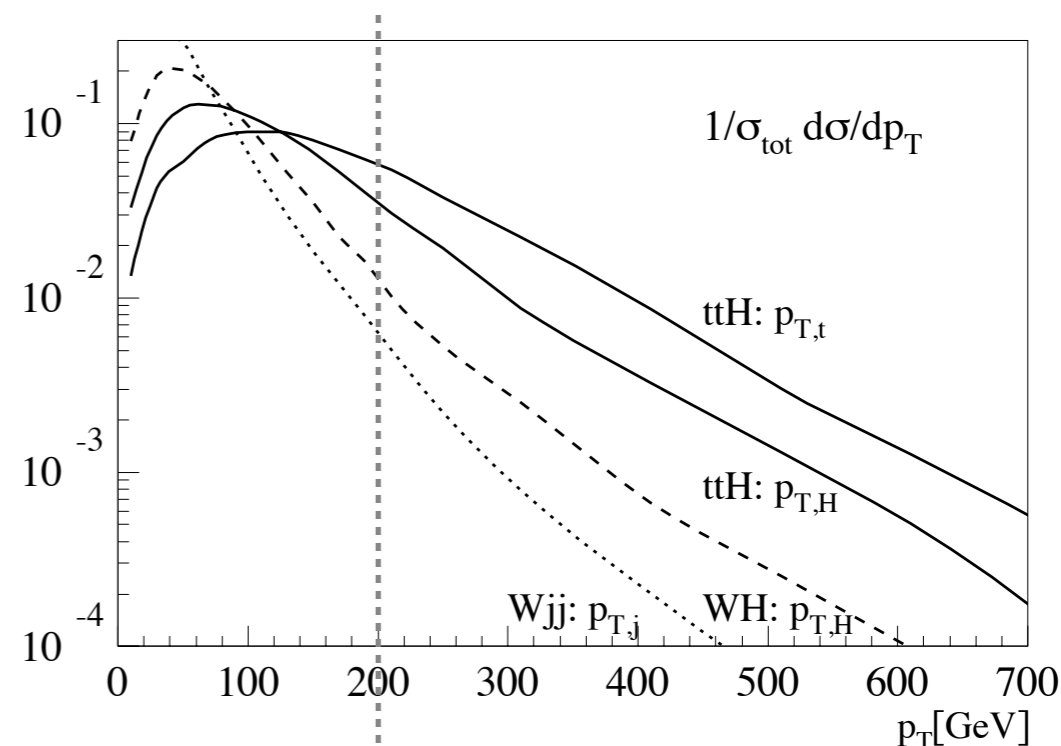
## Boosted regime

$$p_T(t) \geq 200 \text{ GeV}, \quad p_T(\bar{t}) \geq 200 \text{ GeV}, \quad p_T(H) \geq 200 \text{ GeV}$$

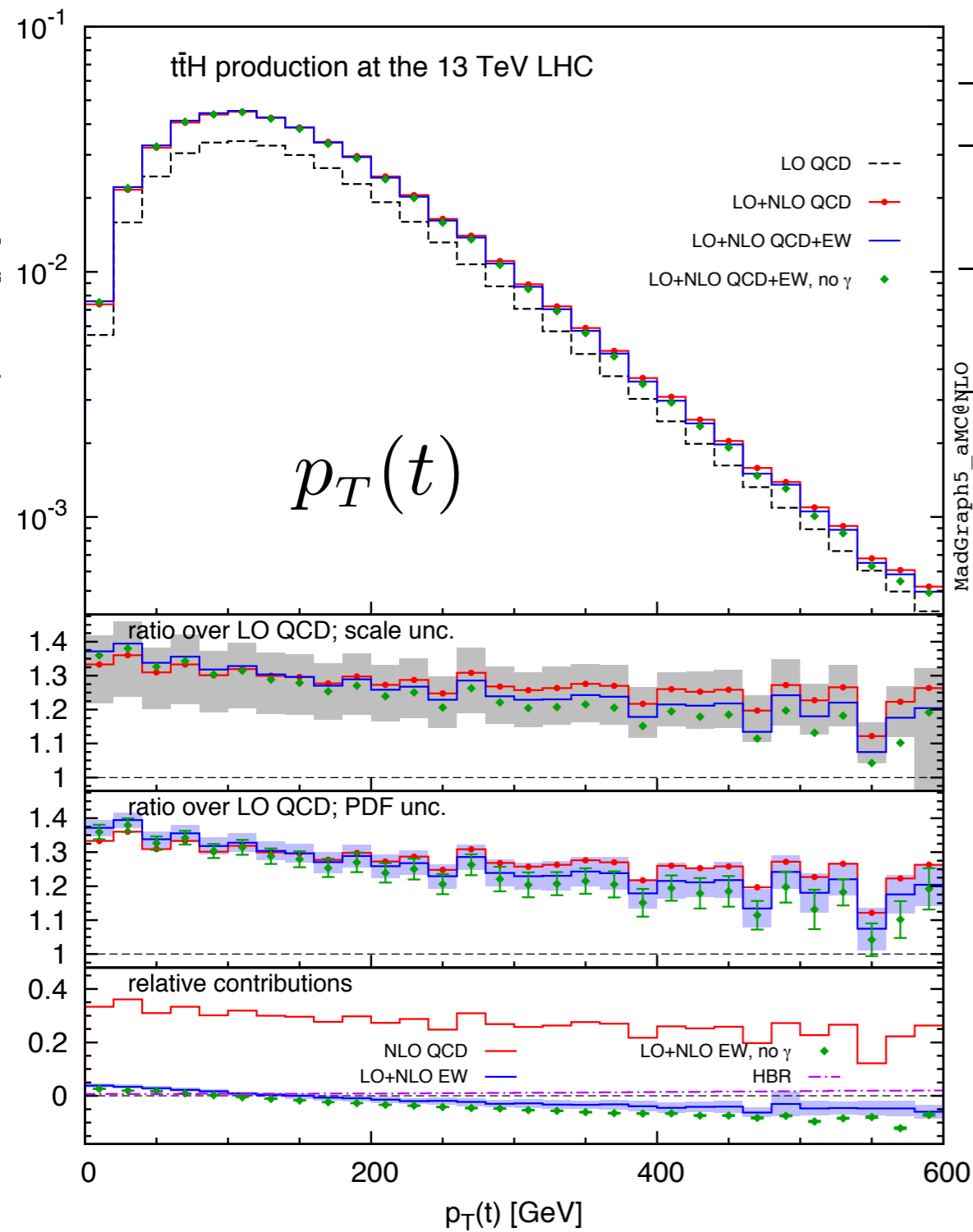
S/B increases for boosted tops and Higgs.

*Plehn, Salam, Spannowsky '10*

Sudakov logs are relevant in these regions!



# Numerical results



$t\bar{t}H : \delta(\%)$	8 TeV	13 TeV	100 TeV
NLO QCD	$25.9^{+5.4}_{-11.1}$	$29.7^{+6.8}_{-11.1}$ (24.2 <sup>+4.8</sup> <sub>-10.6</sub> )	$40.8^{+9.3}_{-9.1}$
LO EW	$1.8 \pm 1.3$	$1.2 \pm 0.9$ (2.8 $\pm$ 2.0)	$0.0 \pm 0.2$
LO EW no $\gamma$	$-0.3 \pm 0.0$	$-0.4 \pm 0.0$ (-0.2 $\pm$ 0.0)	$-0.6 \pm 0.0$
NLO EW	$-0.6 \pm 0.1$	$-1.2 \pm 0.1$ (-8.2 $\pm$ 0.3)	$-2.7 \pm 0.0$
NLO EW no $\gamma$	$-0.7 \pm 0.0$	$-1.4 \pm 0.0$ (-8.5 $\pm$ 0.2)	$-2.7 \pm 0.0$
HBR	0.88	0.89 (1.87)	0.91

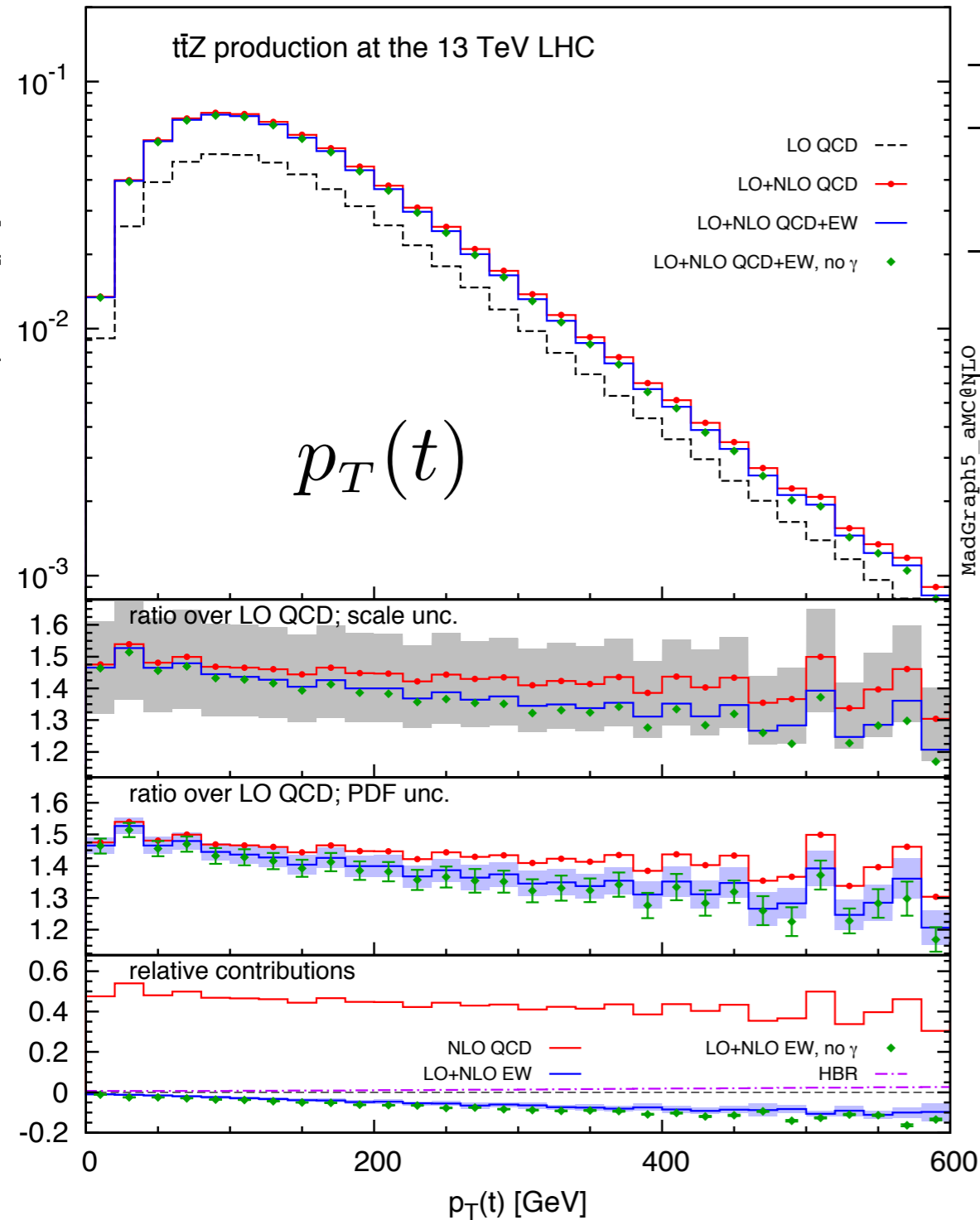
(Boosted regime in brackets)

Scale variation

(NLO QCD+EW) PDF var.

$t\bar{t}H$

# Numerical results



$t\bar{t}Z : \delta(\%)$	8 TeV	13 TeV	100 TeV
NLO QCD	$43.2^{+12.8}_{-15.9}$	$45.9^{+13.2}_{-15.5}$ (40.2 <sup>+11.1</sup> <sub>-15.0</sub> )	$50.4^{+11.4}_{-10.9}$
LO EW	$0.5 \pm 0.9$	$0.0 \pm 0.7$ (2.1 $\pm$ 1.6)	$-1.1 \pm 0.2$
LO EW no $\gamma$	$-0.8 \pm 0.1$	$-1.1 \pm 0.0$ (-0.3 $\pm$ 0.0)	$-1.6 \pm 0.0$
NLO EW	$-3.3 \pm 0.3$	$-3.8 \pm 0.2$ (-11.1 $\pm$ 0.5)	$-5.2 \pm 0.1$
NLO EW no $\gamma$	$-3.7 \pm 0.1$	$-4.1 \pm 0.1$ (-11.5 $\pm$ 0.3)	$-5.4 \pm 0.0$
HBR	0.95	0.96 (2.13)	0.85

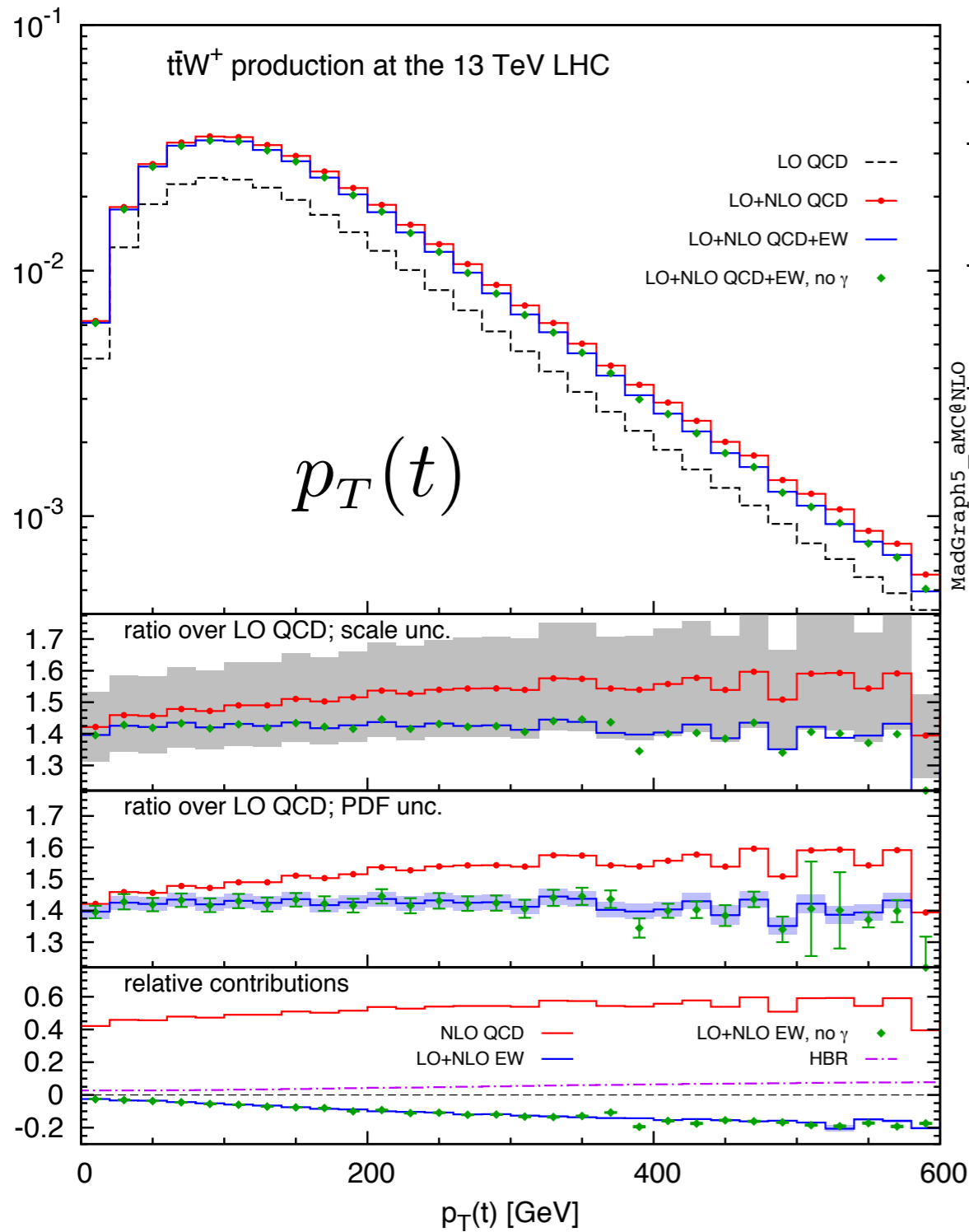
(Boosted regime in brackets)

Scale variation

(NLO QCD+EW) PDF var.

$t\bar{t}Z$

# Numerical results



$t\bar{t}W^+ : \delta(\%)$	8 TeV	13 TeV	100 TeV
NLO QCD	$40.8^{+11.2}_{-12.3}$	$50.1^{+14.2}_{-13.5}$ (59.7 <sup>+18.9</sup> <sub>-17.7</sub> )	$156.4^{+38.3}_{-35.0}$
LO EW	0	0	0
LO EW no $\gamma$	0	0	0
NLO EW	$-6.9 \pm 0.2$	$-7.7 \pm 0.2$ ( $-19.2 \pm 0.7$ )	$-9.3 \pm 0.2$
NLO EW no $\gamma$	$-7.1 \pm 0.2$	$-8.0 \pm 0.2$ ( $-20.0 \pm 0.5$ )	$-9.6 \pm 0.1$
HBR	2.41	3.88 (7.41)	21.52

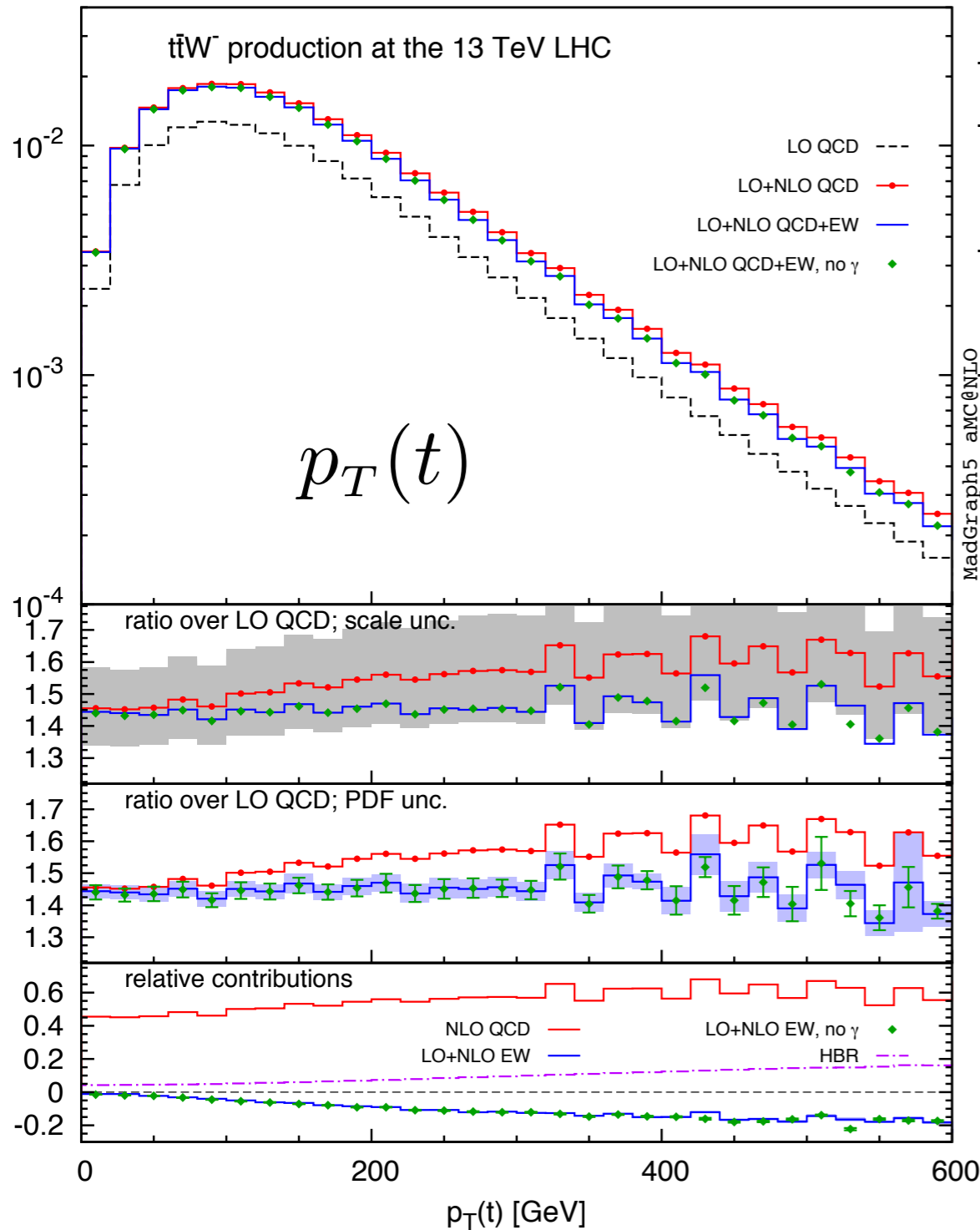
(Boosted regime in brackets)

Scale variation

(NLO QCD+EW) PDF var.

$t\bar{t}W^+$

# Numerical results



$t\bar{t}W^- : \delta(\%)$	8 TeV	13 TeV	100 TeV
NLO QCD	$42.2^{+11.9}_{-12.7}$	$51.5^{+14.8}_{-13.8}$ (66.3 <sup>+21.7</sup> <sub>-19.6</sub> )	$153.6^{+37.7}_{-34.9}$
LO EW	0	0	0
LO EW no $\gamma$	0	0	0
NLO EW	$-6.0 \pm 0.3$	$-6.7 \pm 0.2$ ( $-18.3 \pm 0.8$ )	$-8.5 \pm 0.2$
NLO EW no $\gamma$	$-6.2 \pm 0.2$	$-7.0 \pm 0.2$ ( $-19.1 \pm 0.6$ )	$-8.8 \pm 0.1$
HBR	4.35	6.50 (15.01)	28.91

(Boosted regime in brackets)

Scale variation

(NLO QCD+EW) PDF var.

$t\bar{t}W^-$



# Top-quark pair in association with one or two vector bosons at NLO QCD

$$\begin{array}{l} t\bar{t}W^\pm, \quad t\bar{t}Z, \quad t\bar{t}\gamma, \quad t\bar{t}H \qquad t\bar{t}V \\ \hline t\bar{t}W^+W^-, \quad t\bar{t}ZZ, \quad t\bar{t}\gamma\gamma, \quad t\bar{t}W^\pm\gamma, \quad t\bar{t}W^\pm Z, \quad t\bar{t}Z\gamma \qquad t\bar{t}VV \\ \hline \end{array}$$

$t\bar{t}t\bar{t}$

... that is  $t\bar{t}H$  and its possible irr. backgrounds in leptonic and diphoton signatures

*Maltoni, DP, Tsinikos '15*

Automated results via MadGraph5\_aMC@NLO.

- “Only” NLO QCD corrections.
- Consistent framework for all the processes.
- Study of PDFs and scale uncertainties.
- NLO results for top-quark charge asymmetry

# Top-quark pair in association with one or two vector bosons at NLO QCD

$$\begin{array}{l} t\bar{t}W^\pm, \quad t\bar{t}Z, \quad t\bar{t}\gamma, \quad t\bar{t}H \qquad t\bar{t}V \\ \hline t\bar{t}W^+W^-, \quad t\bar{t}ZZ, \quad t\bar{t}\gamma\gamma, \quad t\bar{t}W^\pm\gamma, \quad t\bar{t}W^\pm Z, \quad t\bar{t}Z\gamma \qquad t\bar{t}VV \\ \hline \end{array}$$

$t\bar{t}t\bar{t}$

... that is  $t\bar{t}H$  and its possible irr. backgrounds in leptonic and diphoton signatures

*Maltoni, DP, Tsinikos '15*

See also:

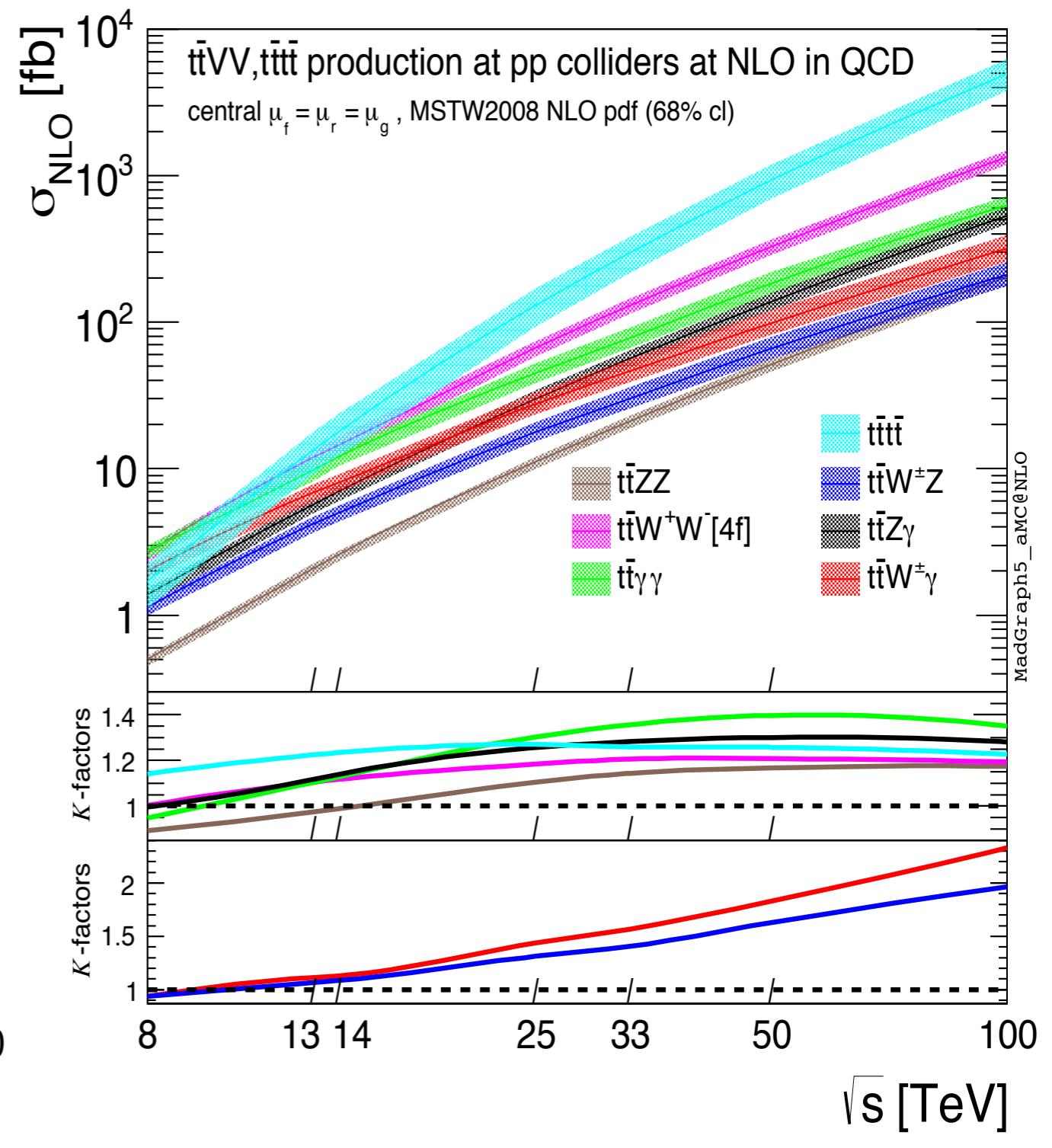
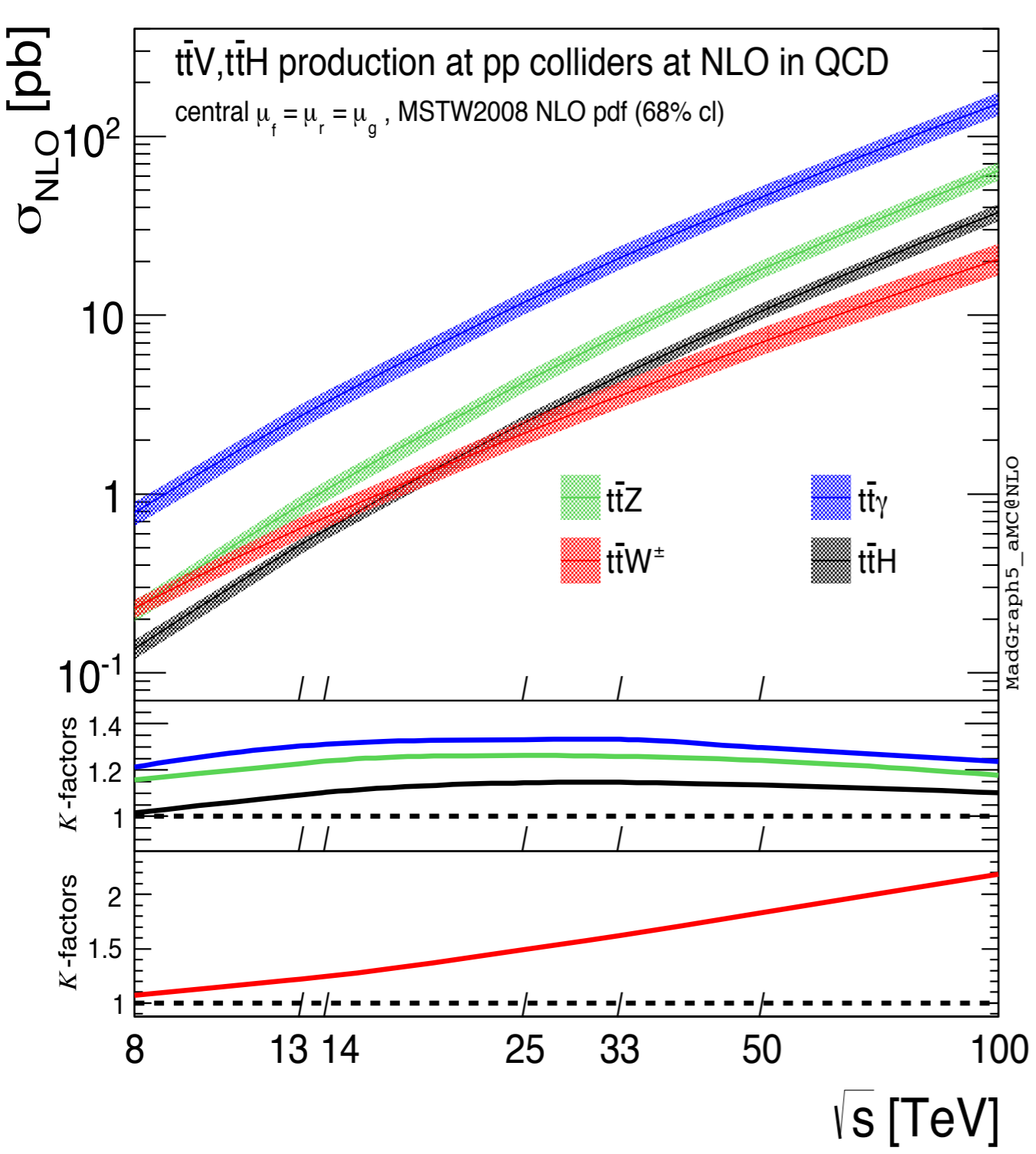
$t\bar{t}W^\pm$  *Garzelli et al '12, Campbell Ellis '12, Maltoni et al '14*

$t\bar{t}Z$  *Lazopoulos et al '08, Garzelli et al '11, Kardos et al '11*

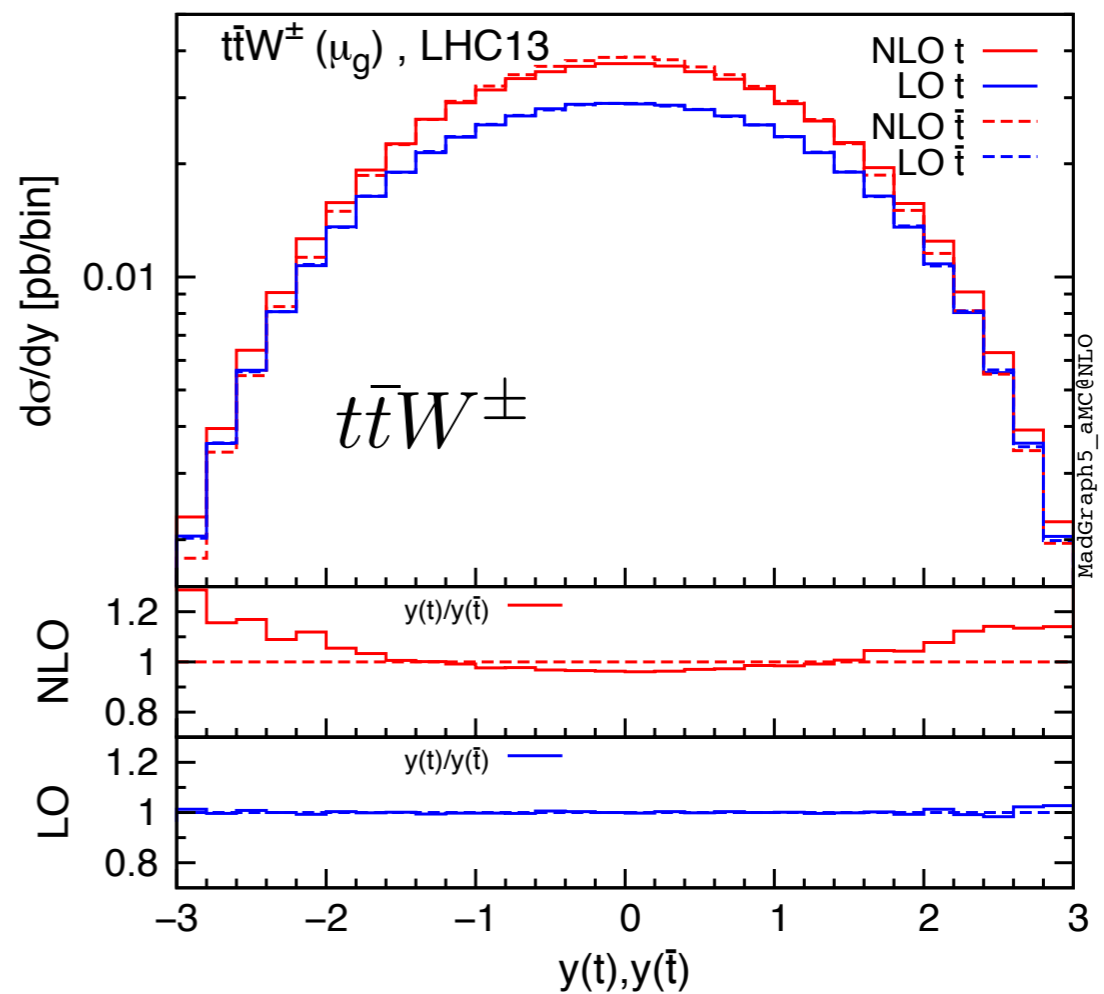
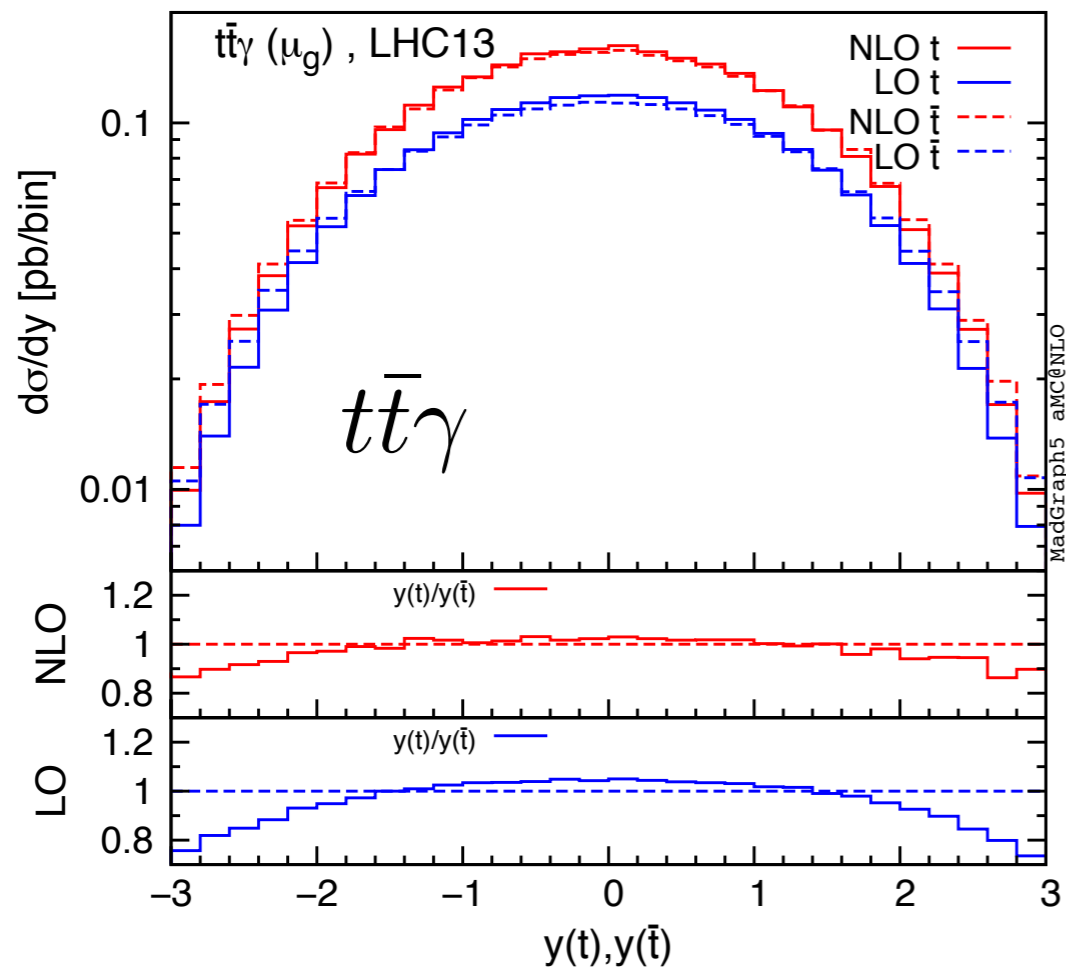
$t\bar{t}H$  *Beenakker et al '02, Dawson et al '03, Frederix et al '11, Garzelli et al '11*

$t\bar{t}\gamma\gamma$  *Kardos Trocsanyi '14, van Deurzen et al '15*

# Energy dependence



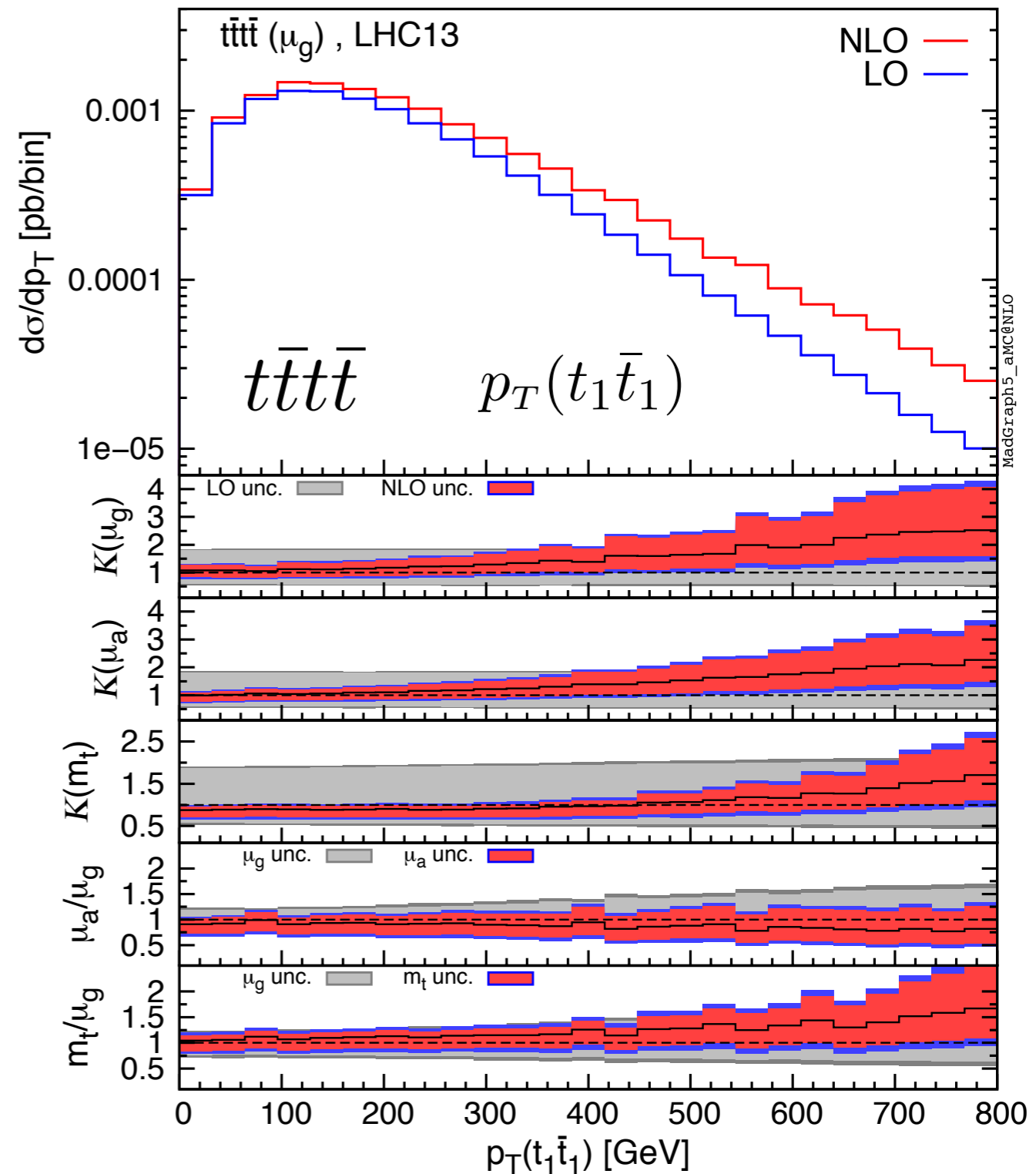
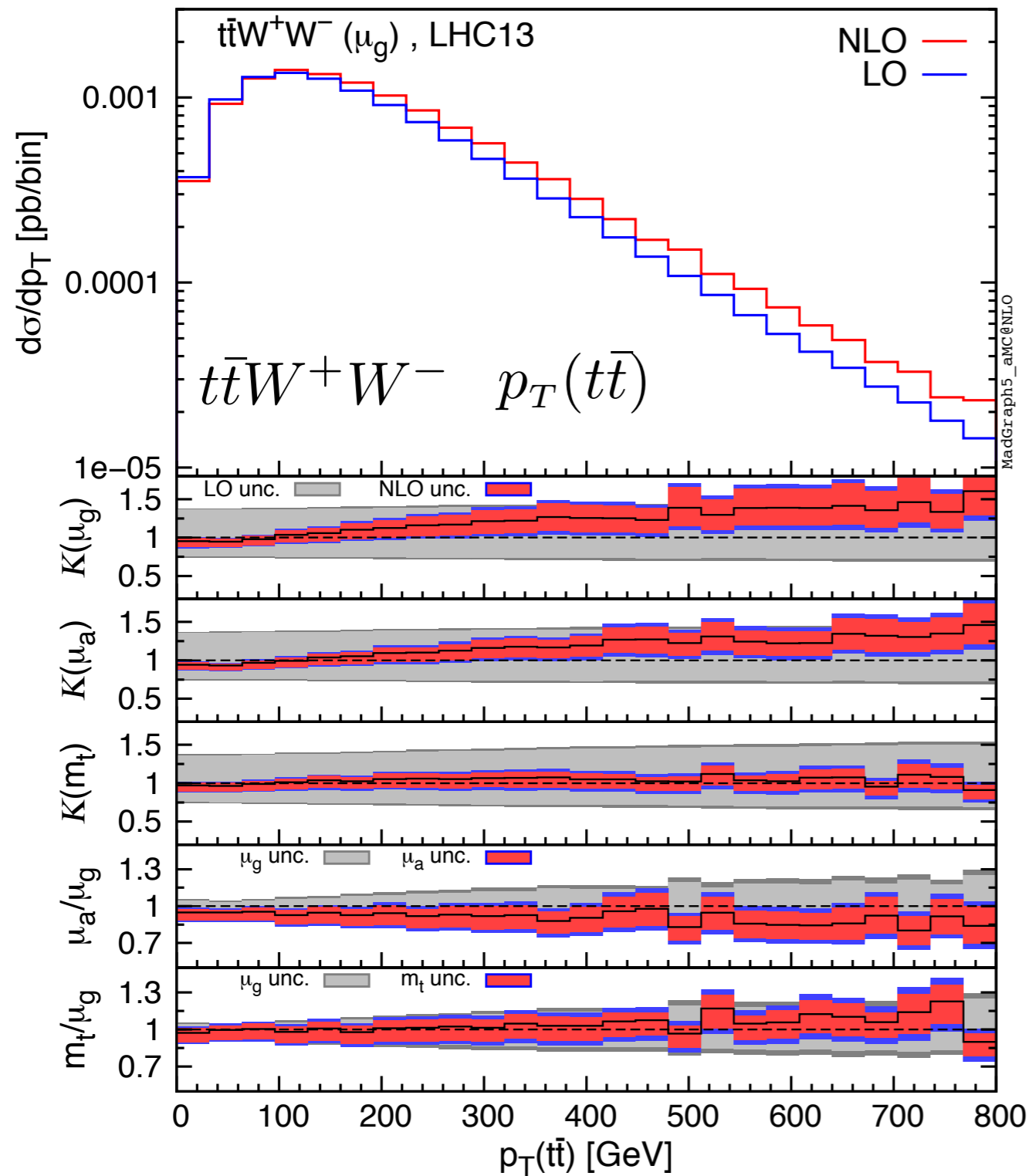
# Distributions: representative results at fixed order



## Central Asymmetries

13 TeV $A_c$ [%]	$t\bar{t}H$	$t\bar{t}Z$	$t\bar{t}W^\pm$	$t\bar{t}\gamma$
LO	-	$-0.12^{+0.01}_{-0.01} \quad +0.01 \quad -0.02 \pm 0.03$	-	$-3.93^{+0.26}_{-0.23} \quad +0.14 \quad -0.11 \pm 0.03$
NLO	$1.00^{+0.30}_{-0.20} \quad +0.06 \quad -0.04 \pm 0.02$	$0.85^{+0.25}_{-0.17} \quad +0.06 \quad -0.05 \pm 0.03$	$2.90^{+0.67}_{-0.47} \quad +0.06 \quad -0.07 \pm 0.07$	$-1.79^{+0.50}_{-0.39} \quad +0.06 \quad -0.09 \pm 0.06$

# Distributions: representative results at fixed order



# Single-top and its pathologies

**Associated  $tW$**  production at LHC: a complete calculation of **electroweak supersymmetric** effects at one loop

*Beccaria, Macorini, Renard, Verzegnassi*



arXiv:hep-ph/0601175

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**A complete one-loop** description of **associated  $tW$**  production at LHC and a search for possible genuine **supersymmetric** effects at hadron collider

*Beccaria, Carloni Calame, Macorini, Montagna, Piccinini, Renard, Verzegnassi* arXiv:0705.3101

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Single top production in the  **$t$ -channel** at LHC: a realistic **test of electroweak models**

*Beccaria, Macorini, Renard, Verzegnassi*



arXiv:hep-ph/0605108

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**Electroweak Corrections to  $t$ -channel** single top production at the LHC

*Mirabella*



arXiv:0811.2051

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Electroweak Radiative Corrections to Single-top Production ( **$s$ - and  $t$ -channel**)

*Bardin, Bondarenko, Kalinovskaya, Kolesnikov, von Schlippe*



arXiv:1008.1859

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NLO EW and QCD proton-proton cross section calculations with **mcsanc-v1.01** ( **$s$ - and  $t$ -channel**)

*Bondarenko, Saprnov*



arXiv:1301.3687

---



*Real QED only soft*



*Within MSSM*



*IR regularized with  $\Gamma_t$*



*Only partonic results*

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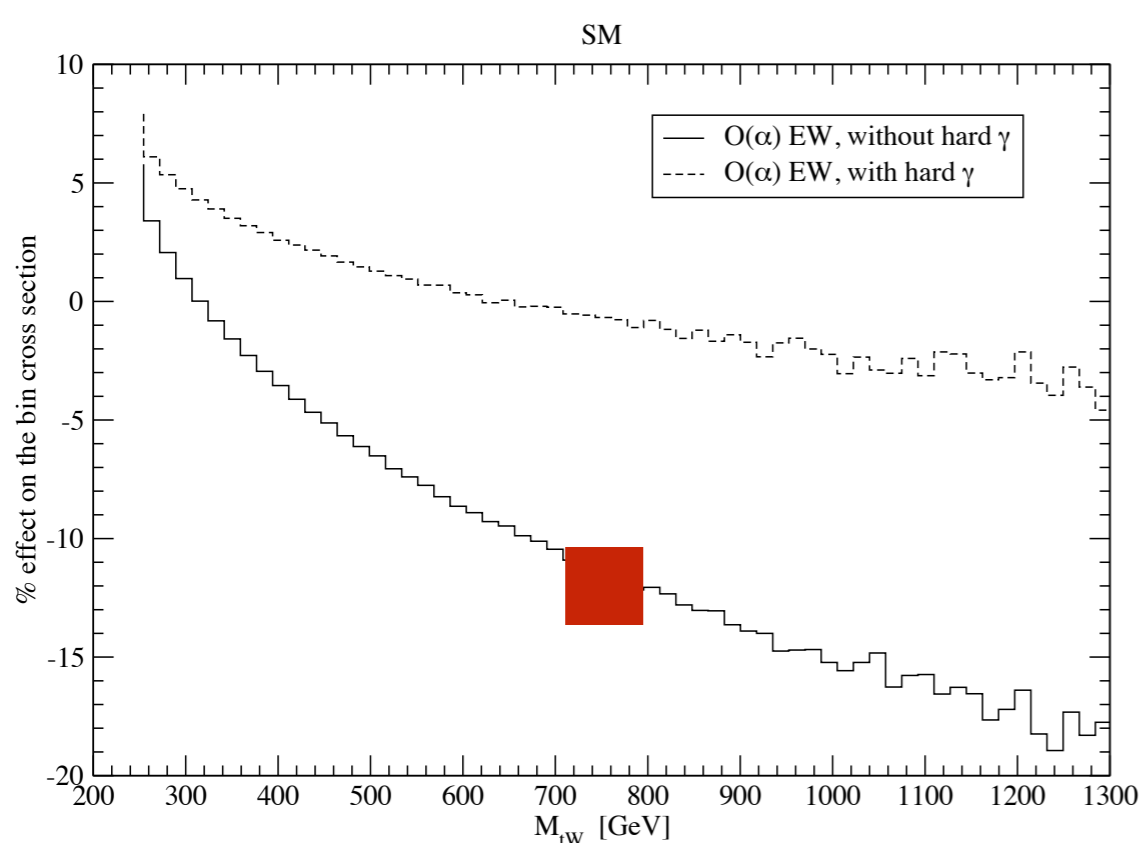


*IR regularized with  $\Gamma_t$*



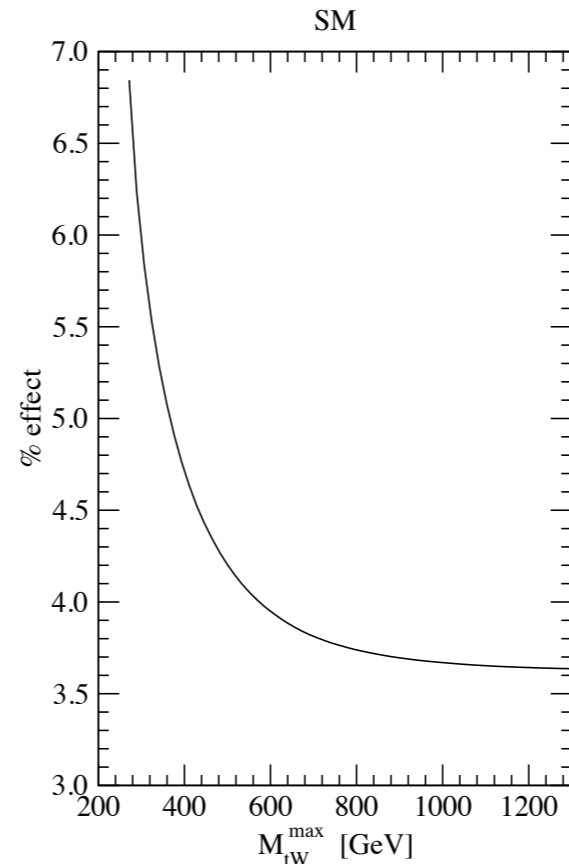
*Only partonic results*

# numerical results at the LHC 14 TeV



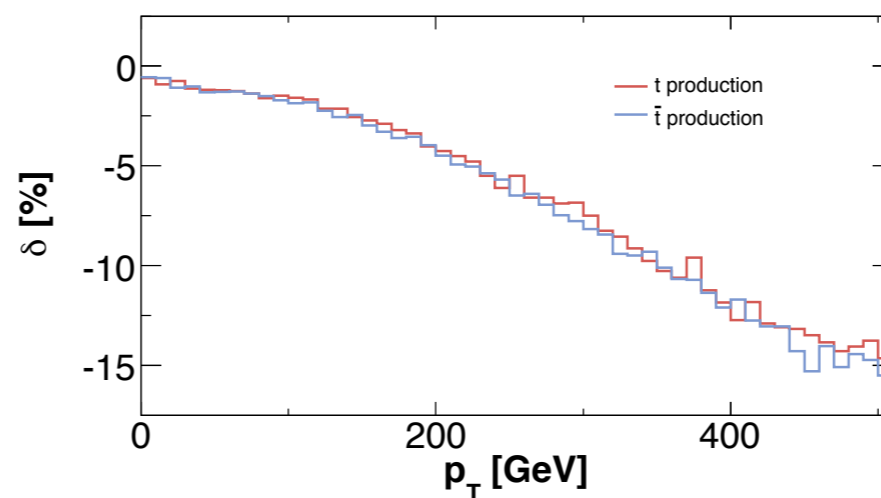
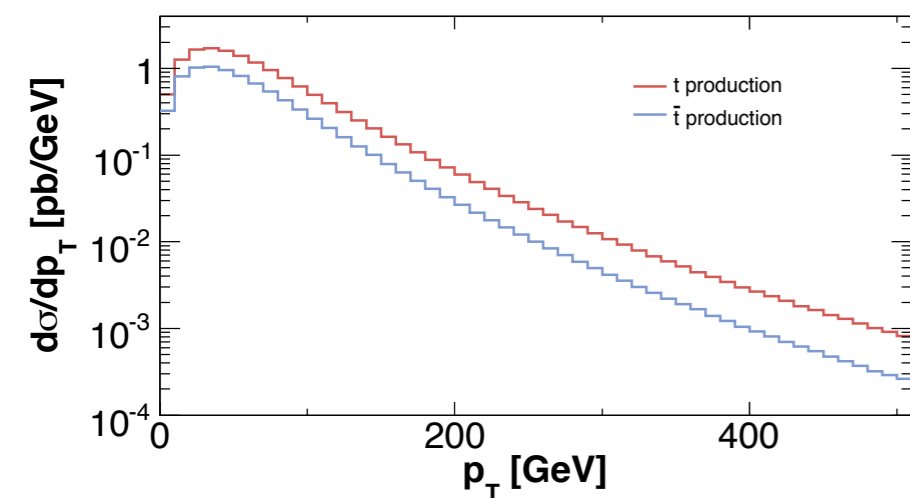
Associated  $tW$

arXiv:0705.3101



t-channel

arXiv:0811.2051



s- and t-channel

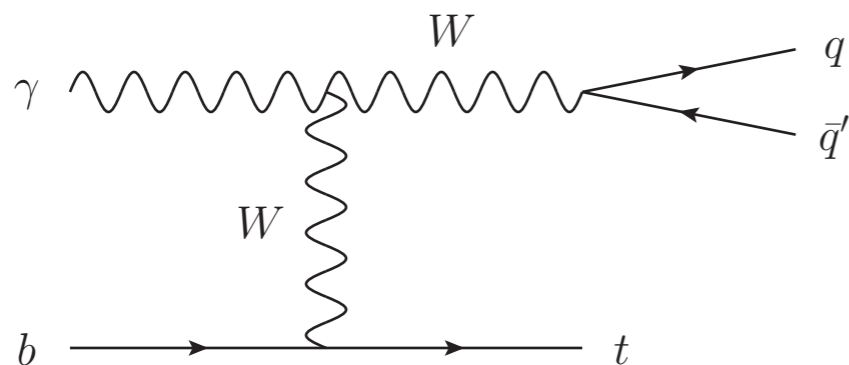
arXiv:1301.3687

$pp \rightarrow$	$t + b$ (s-channel)	$\bar{t} + b$ (s-channel)
LO	5.134(1)	3.205(1)
LO MCFM	5.133(1)	3.203(1)
NLO QCD	6.921(2)	4.313(2)
NLO MCFM	6.923(2)	4.309(1)
NLO EW	5.022(1)	3.140(1)
$\delta_{QCD}, \%$	34.79(5)	34.56(8)
$\delta_{EW}, \%$	-2.18(1)	-2.02(2)
$pp \rightarrow$	$t + q$ (t-channel)	$\bar{t} + q$ (t-channel)
LO	158.73(2)	95.18(2)
LO MCFM	158.69(7)	95.27(4)
NLO QCD	152.13(9)	90.44(7)
NLO MCFM	152.07(14)	90.50(8)
NLO EW	164.44(5)	98.65(4)
$\delta_{QCD}, \%$	-4.17(6)	-4.08(8)
$\delta_{EW}, \%$	3.59(3)	3.66(5)

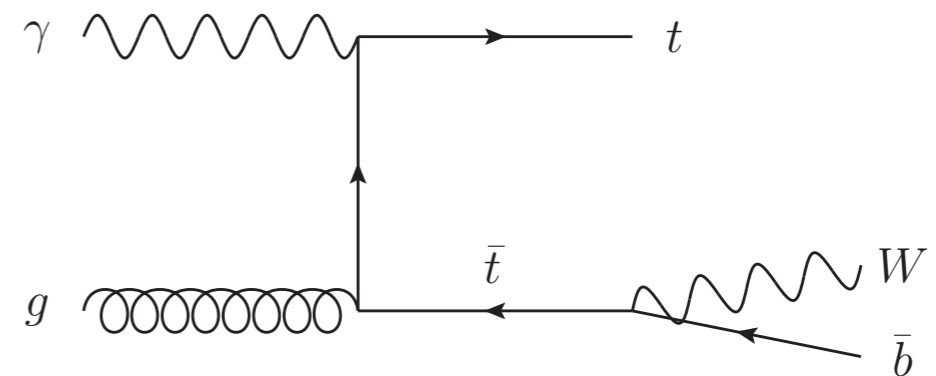


# Pathologies

All the previous calculations included **only** real photon radiation.  
Real quark radiation and initial-state photons have **NOT** been taken into account.  
What if we include them?



NLO EW quark radiation to  $tj$  or  $tW$  with  $W$  decay?



NLO EW quark radiation to  $tW$  or  $t\bar{t}$  with  $t$  decay?

NLO QCD pathologies are present also at the NLO EW.  
With 4FS (and HBR) pathologies become even worse.

Is it necessary to move to stable final-state particles?

# CONCLUSION

EW corrections to the asymmetries are huge and necessary for a realistic description. They are not Sudakov enhanced.

The  $t\bar{t}V$  ( $V = H, W, Z$ ) processes show non-negligible corrections for large  $p_t$ , due to Sudakov logs. They are particularly large for  $t\bar{t}W^+$

$t\bar{t}V$  and  $t\bar{t}VV$  have been studied at NLO QCD accuracy, K-factors for charged final states strongly depend on energy of pp collision. Top-quark asymmetries are present also for  $t\bar{t}V$  and NLO QCD corrections reduce the value for  $t\bar{t}\gamma$ .

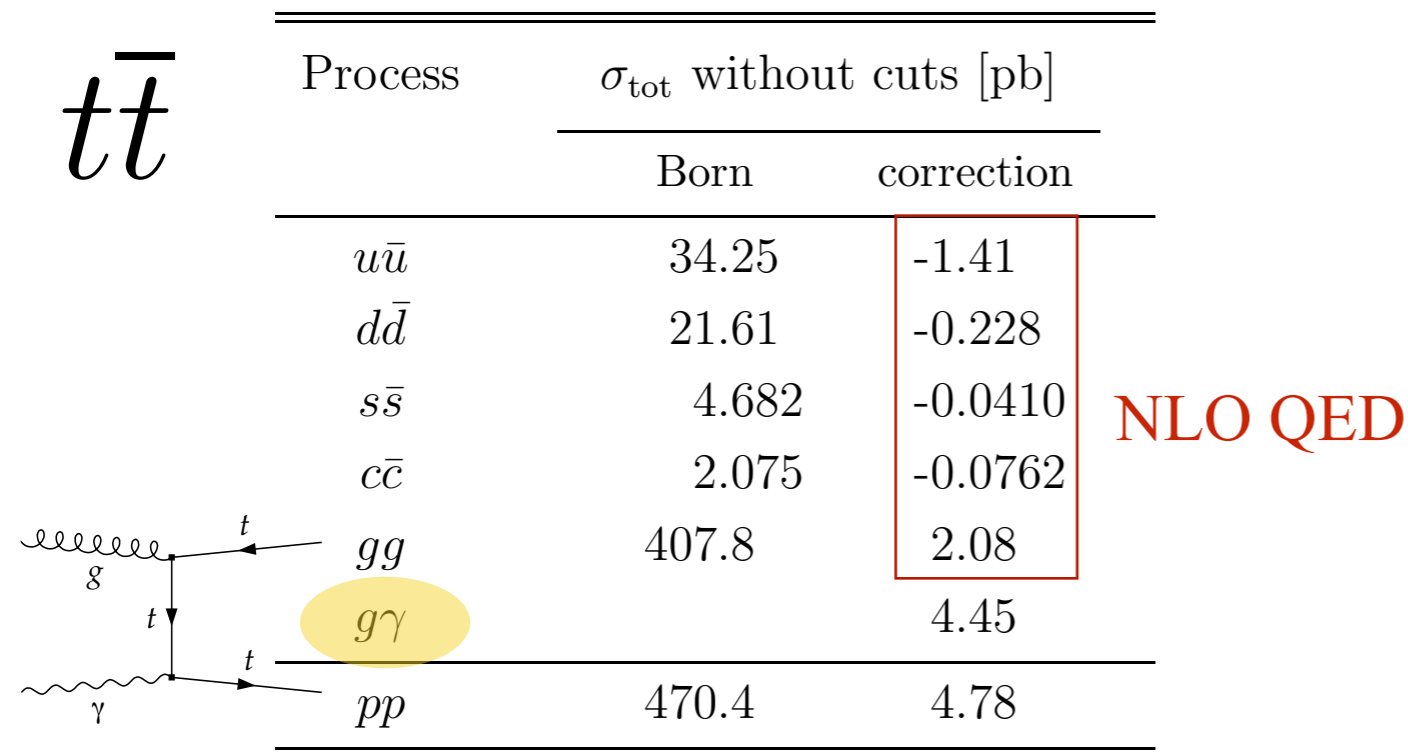
Single top: EW corrections are large for  $tW$  production. For t-channel, they are of the same size of NLO QCD corrections, with opposite sign.

Updated results involving quark radiation and photons in the initial states are desirable, but technically not straightforward.

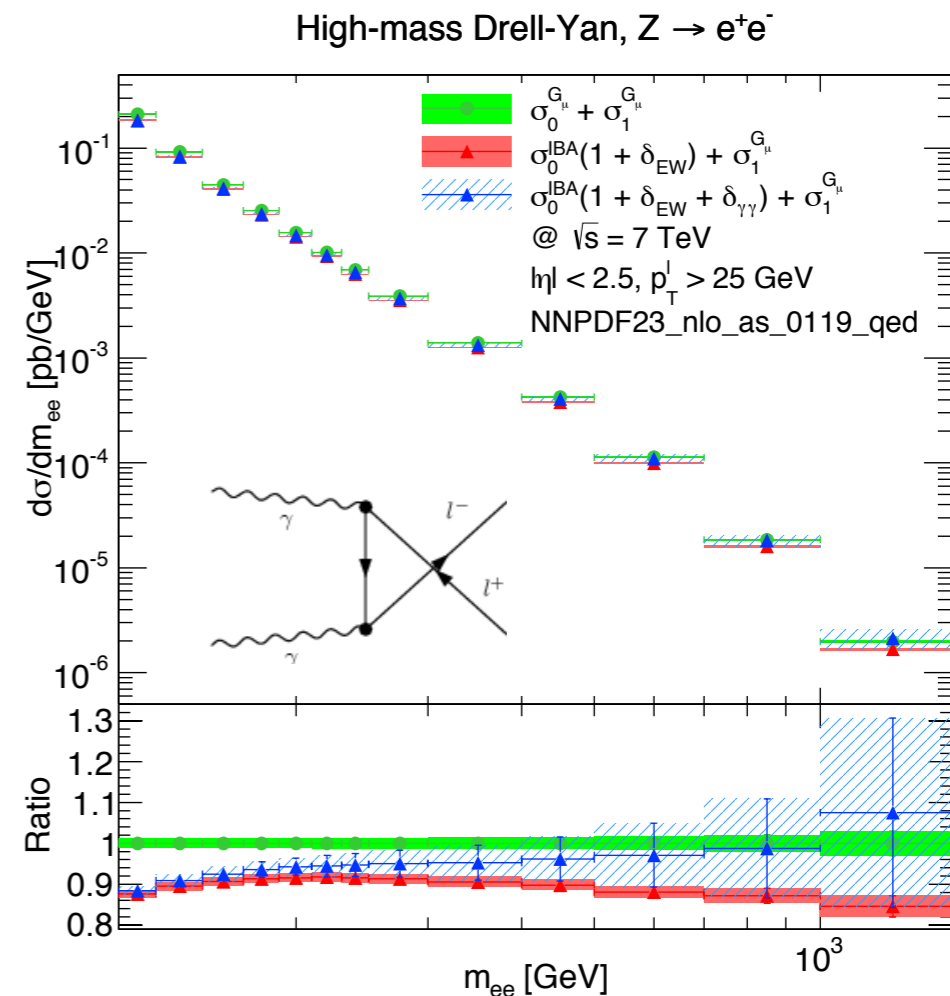
EXTRA SLIDES

# Why do we care about photons in the proton?

## 2 representative examples:

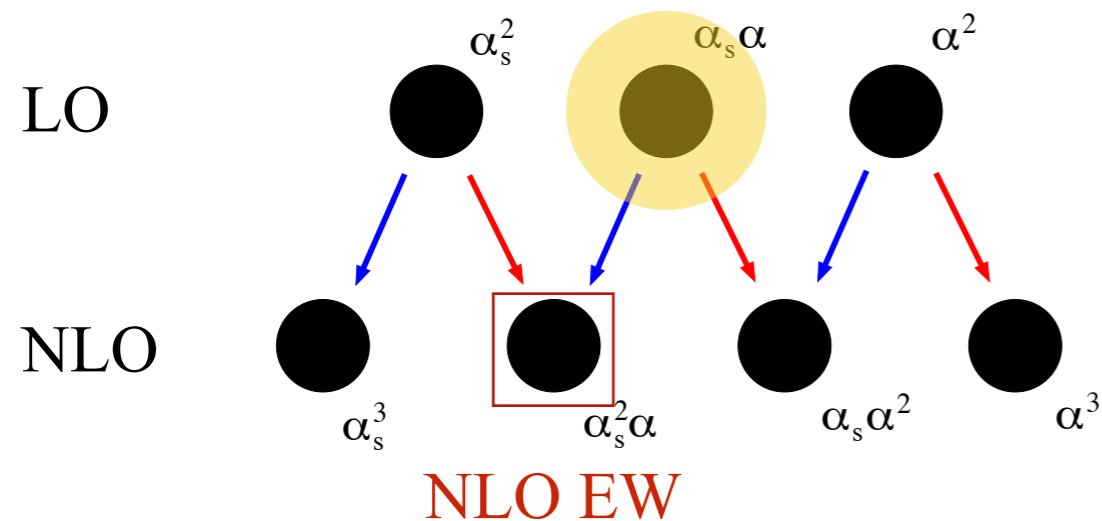


Integrated hadronic cross section for  $t\bar{t}$  production at the LHC, at NLO QED



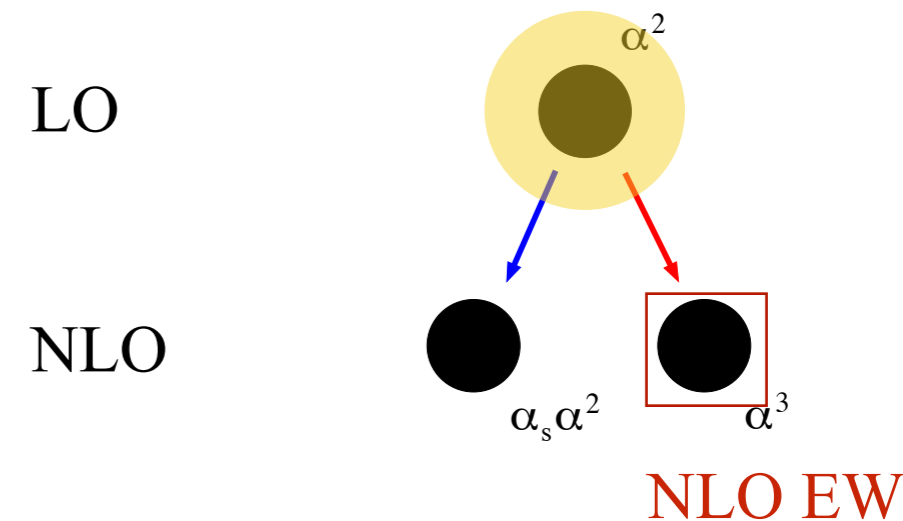
Hollik, Kollar '07

MRST2004QED

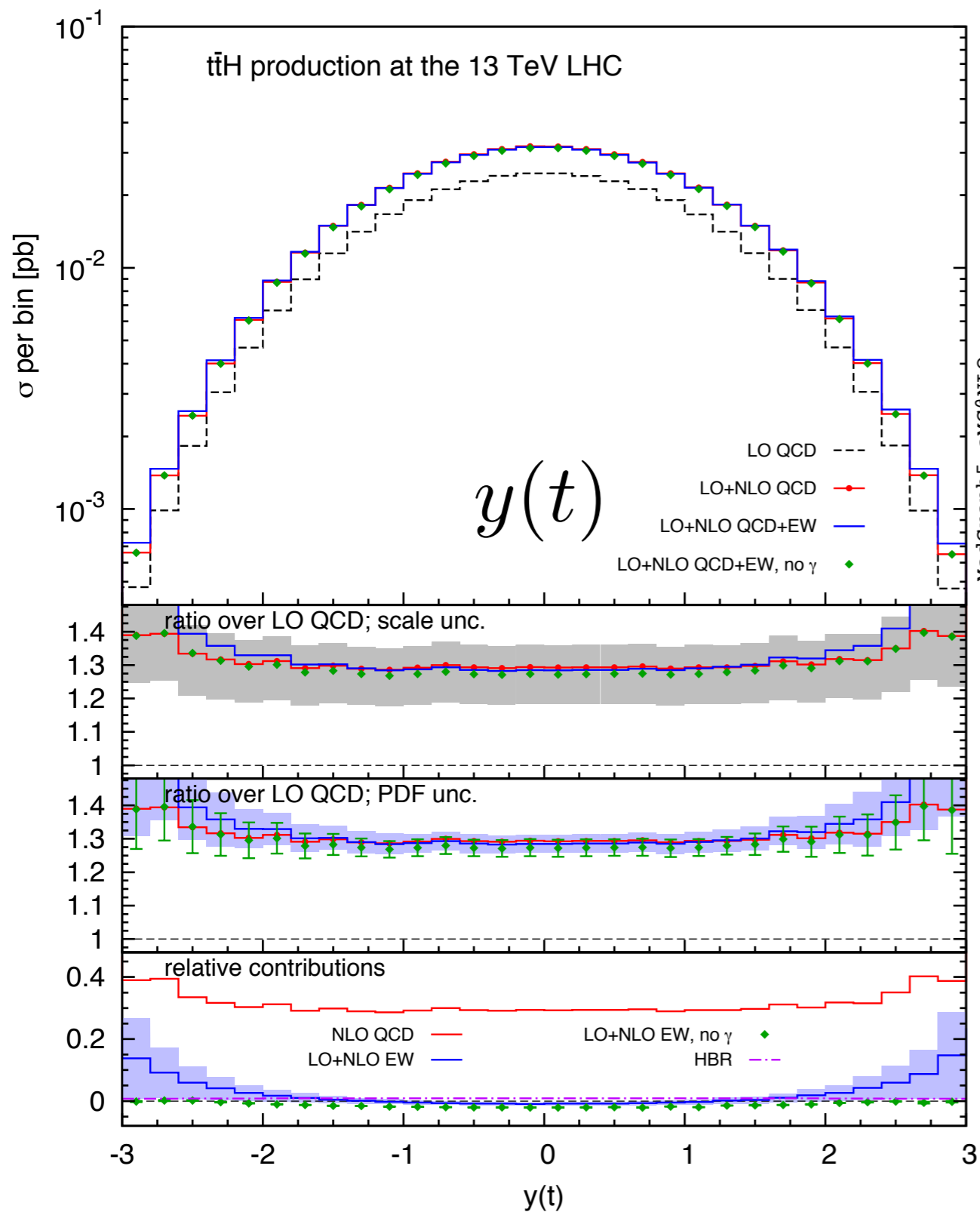


Carrazza '14

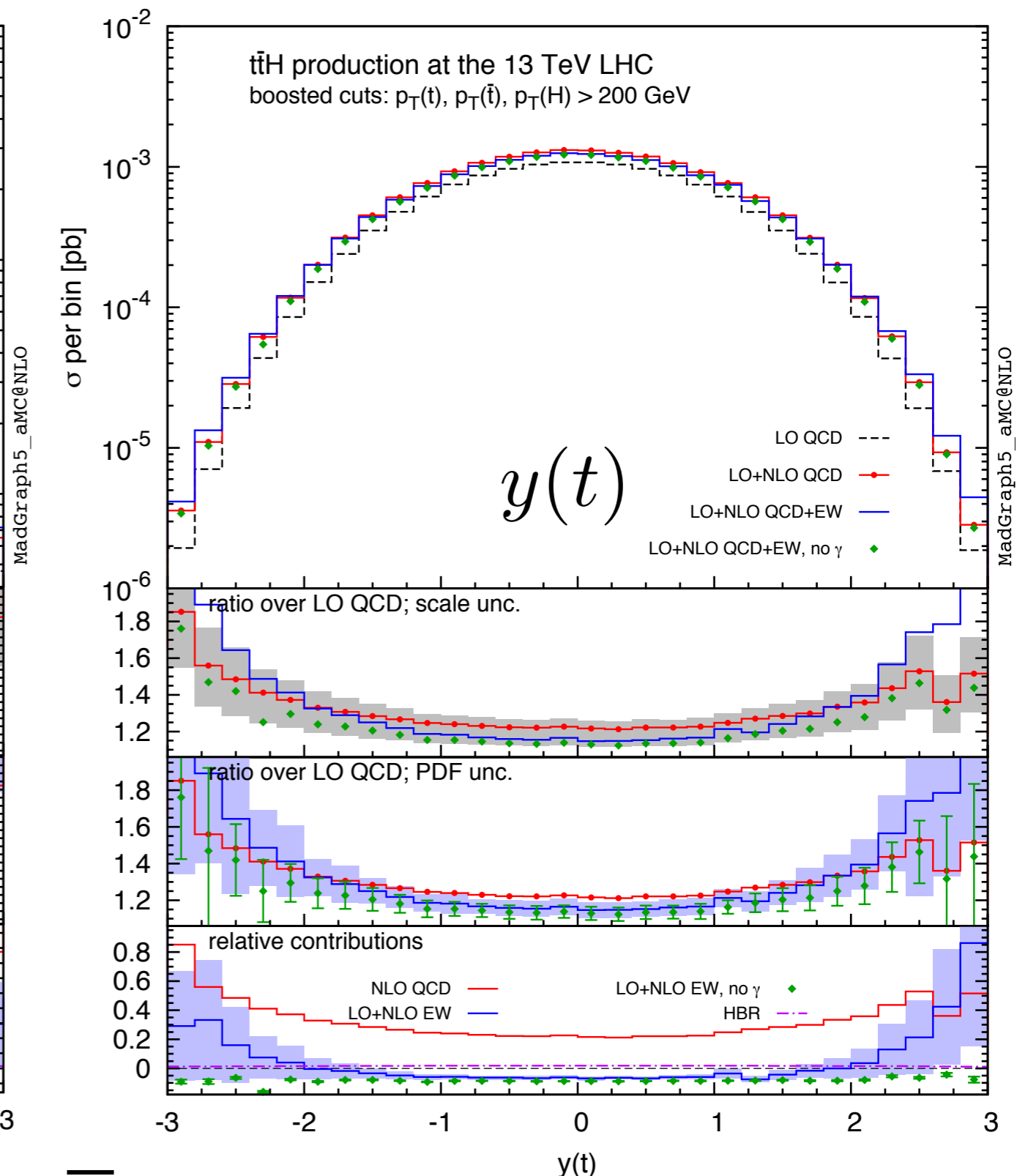
NNPDF2.3QED



# Rapidity distributions: unboosted vs. boosted



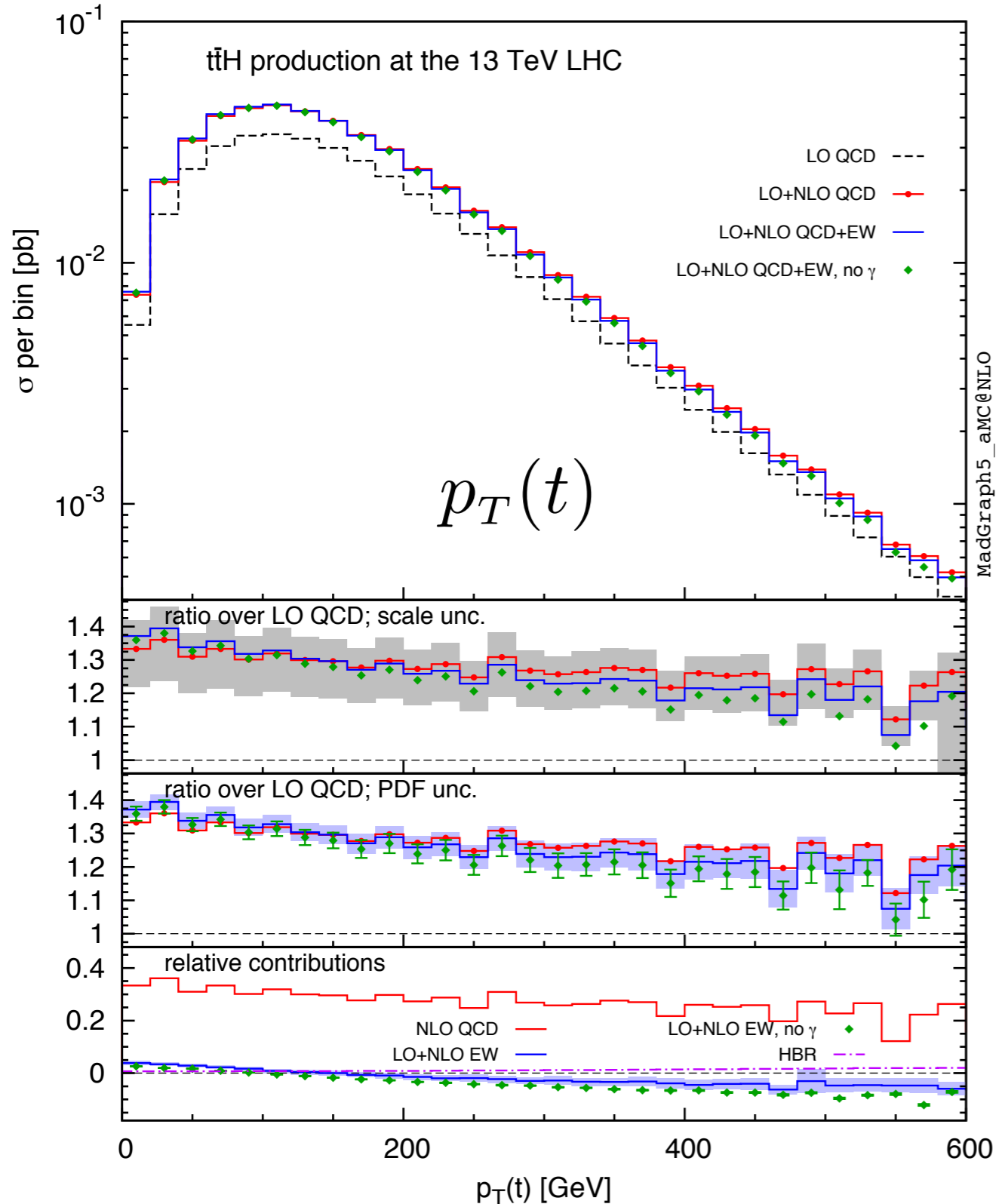
13 TeV



$t\bar{t}H$

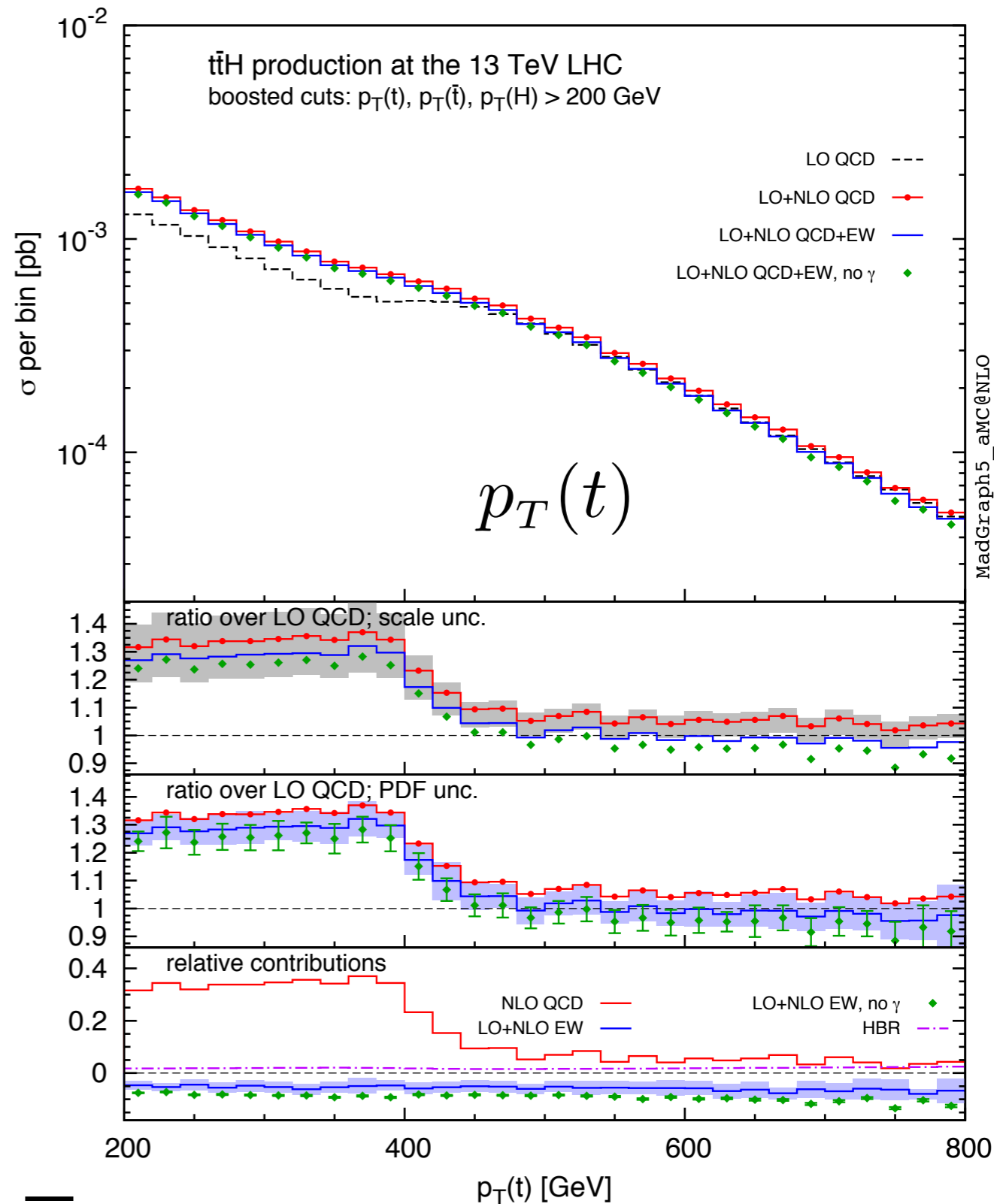
13 TeV

# Transverse momentum distributions: unboosted vs. boosted



13 TeV

$t\bar{t}H$



13 TeV

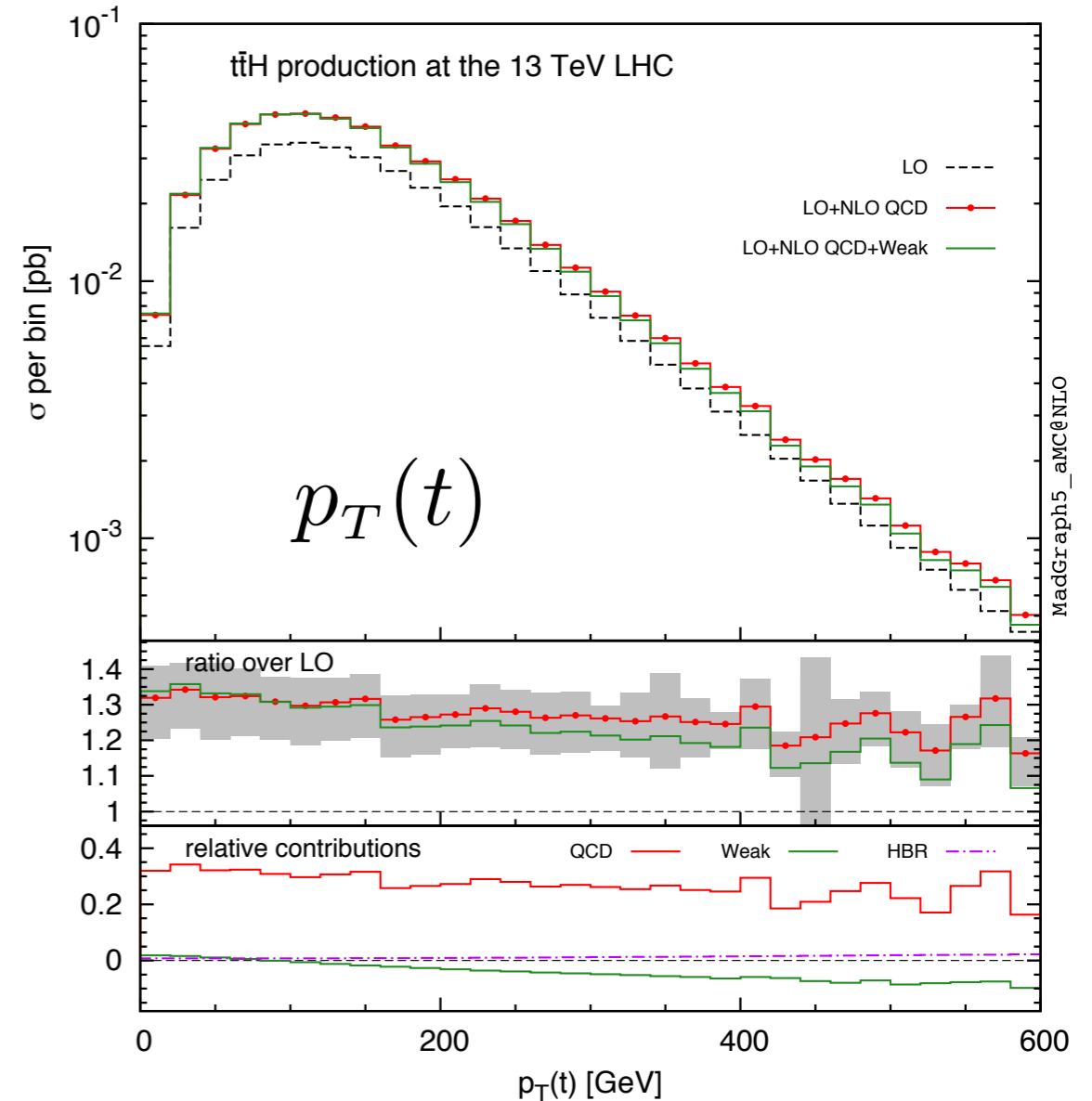
# Pheno studies

NLO purely Weak and QCD corrections to  $t\bar{t}H$  production have been produced “assembling by hand” the FKS counterterms.

Frixione, Hirschi, DP, Shao, Zaro '14

Now, for the complete NLO QCD and EW corrections, with photons in the initial state, we need to type:

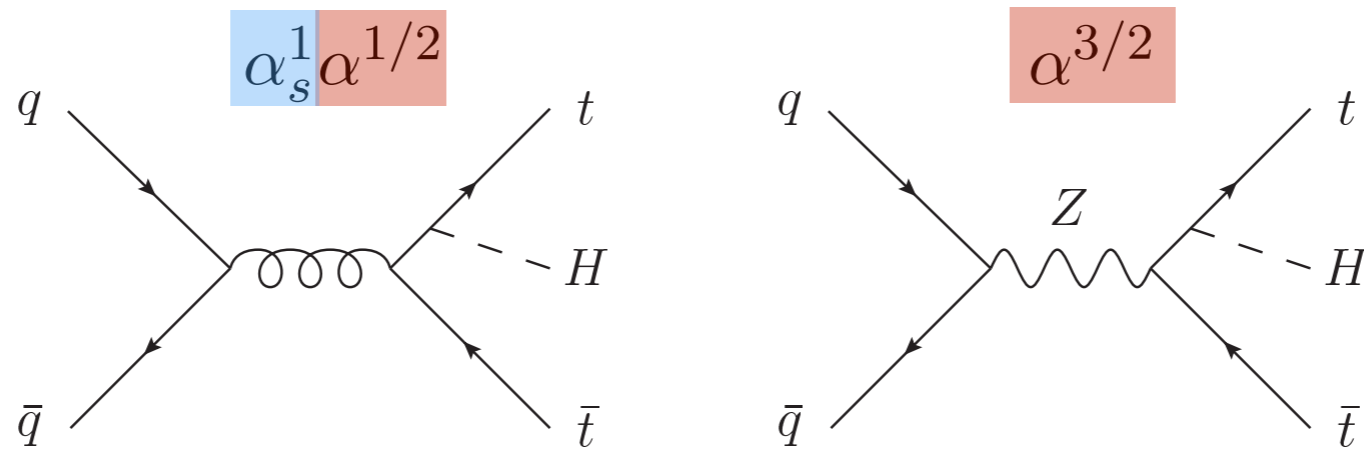
```
define p = p b b~ a
generate p p > t t~ h [QCD QED]
output ttbarh_QCD_QED
```



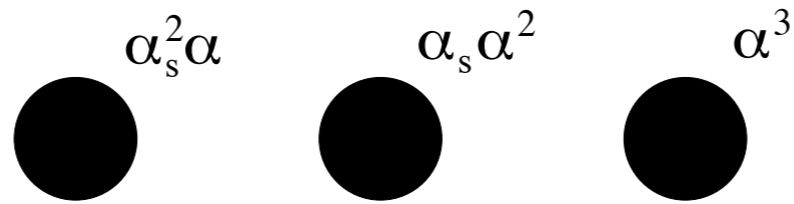
In this talk I will present results for NLO QCD and EW corrections to  $t\bar{t}V$ ,  $V = H, W, Z$

Frixione, Hirschi, DP, Shao, Zaro '15

# Structure of NLO EW-QCD corrections

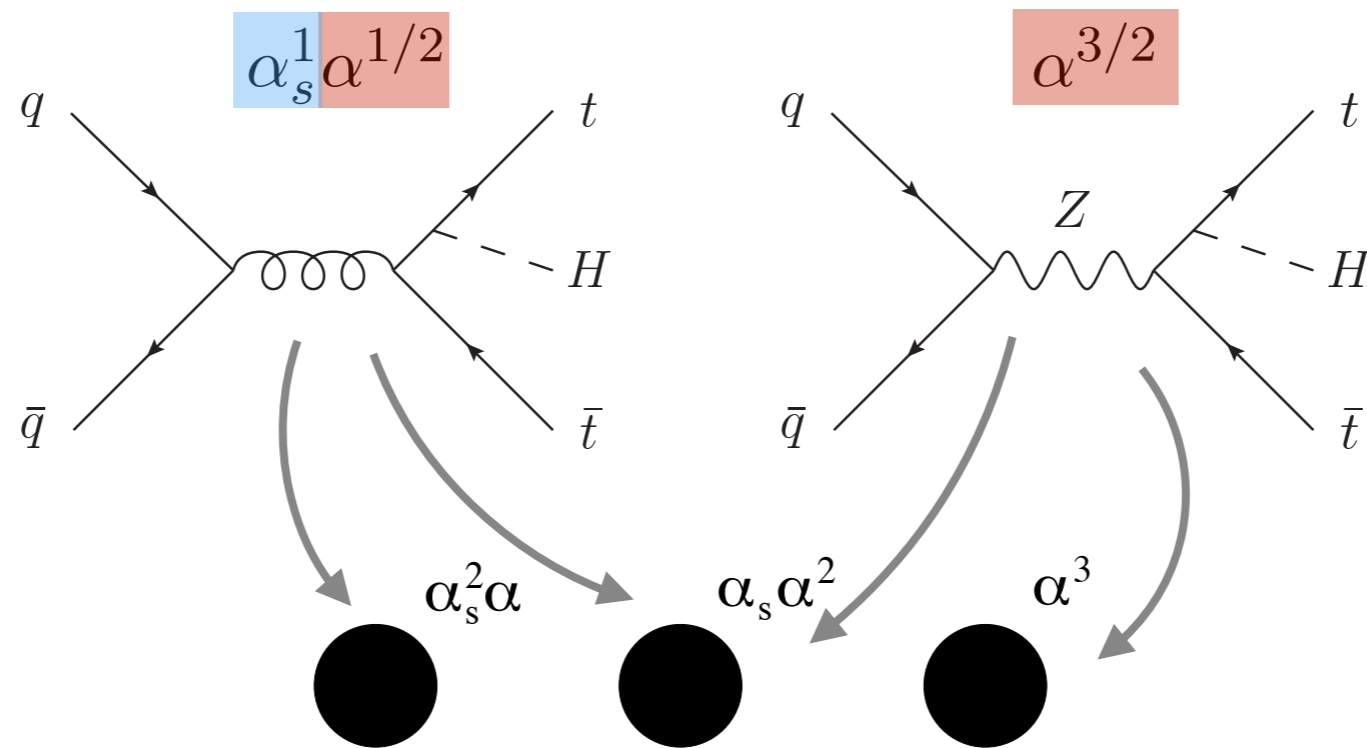


LO



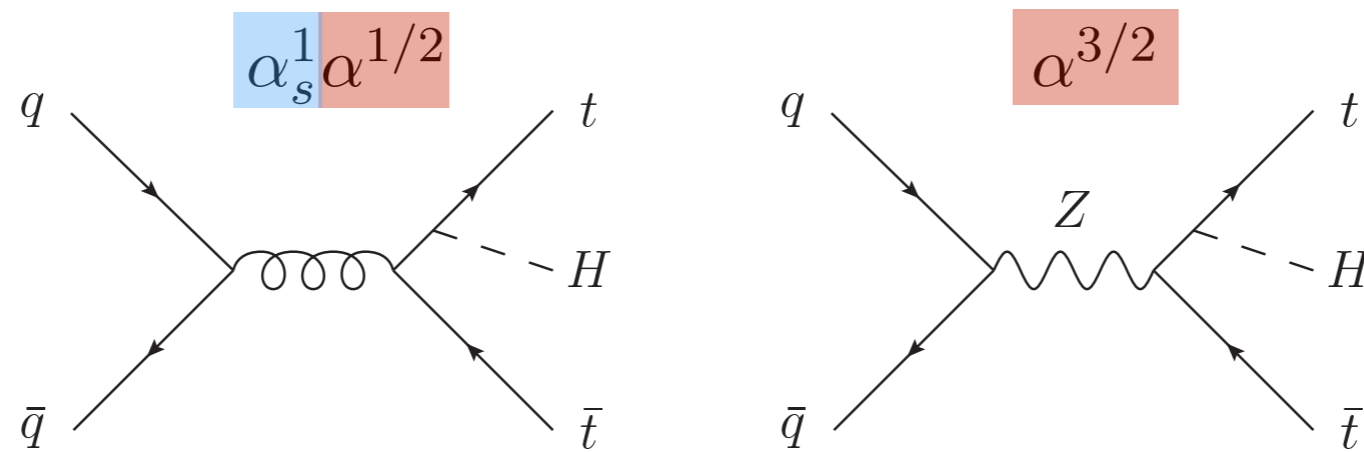


# Structure of NLO EW-QCD corrections

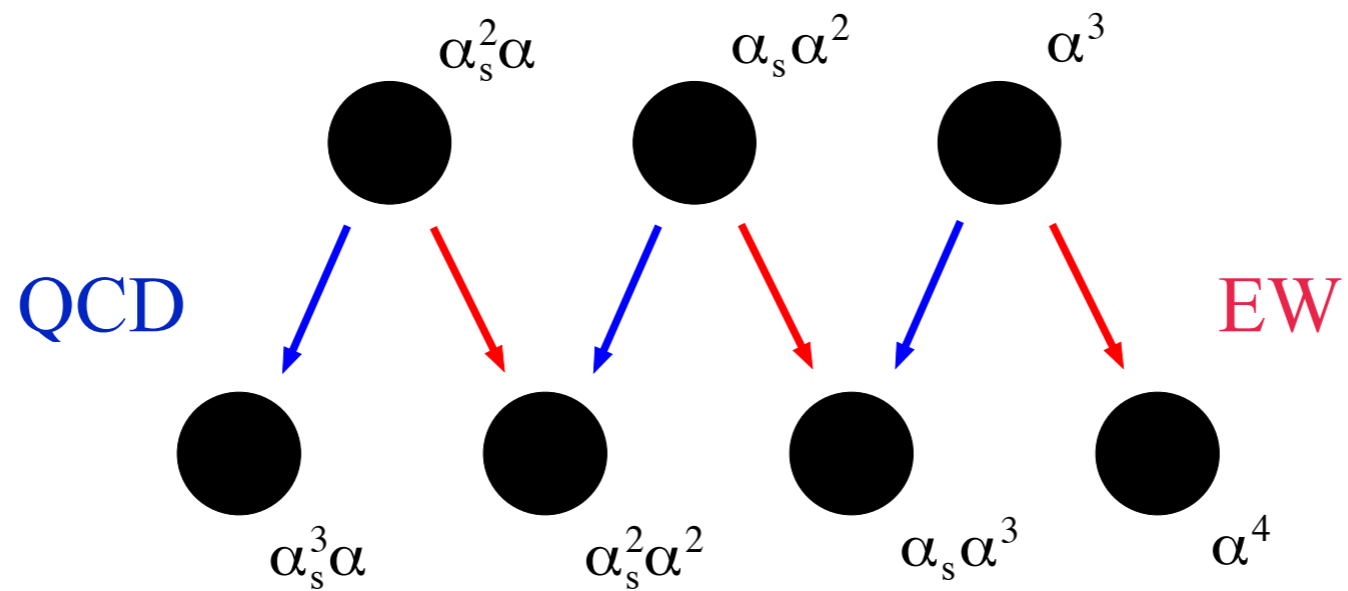


LO

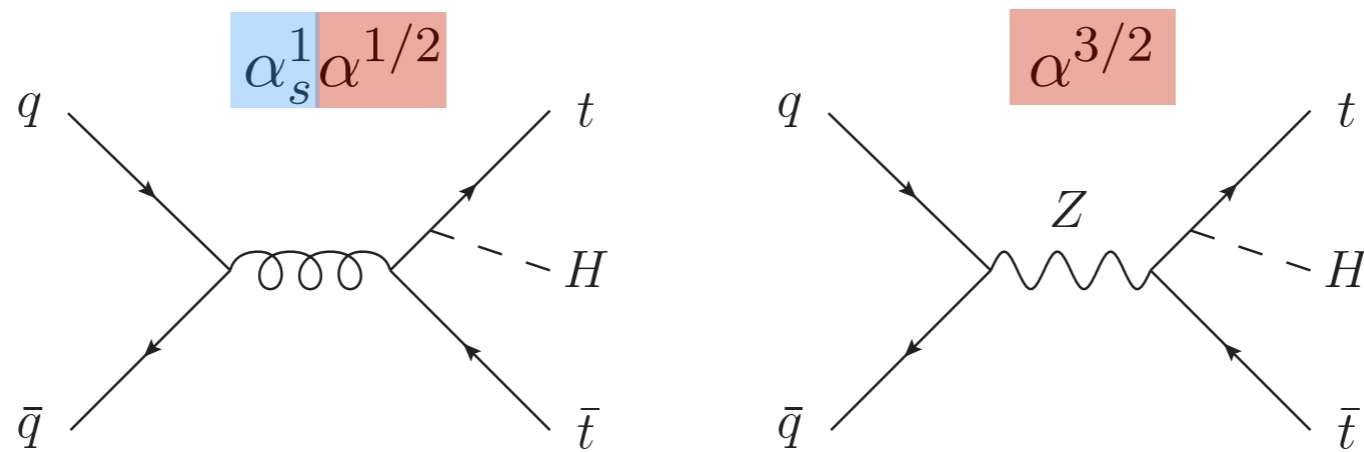
# Structure of NLO EW-QCD corrections



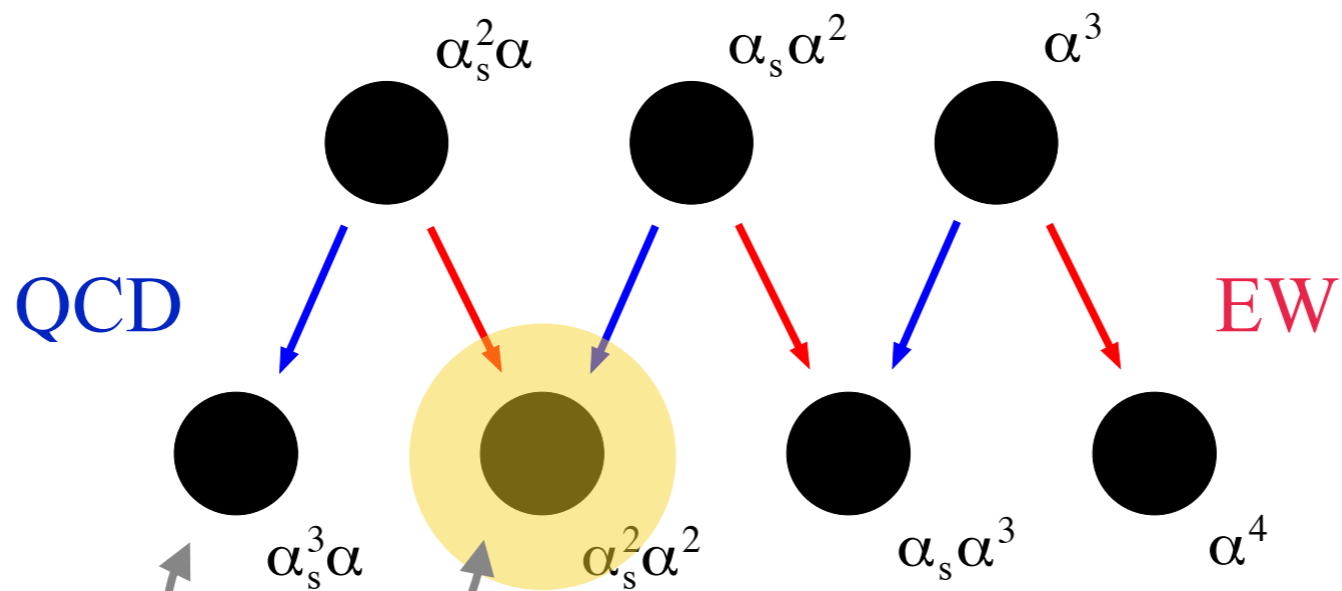
LO



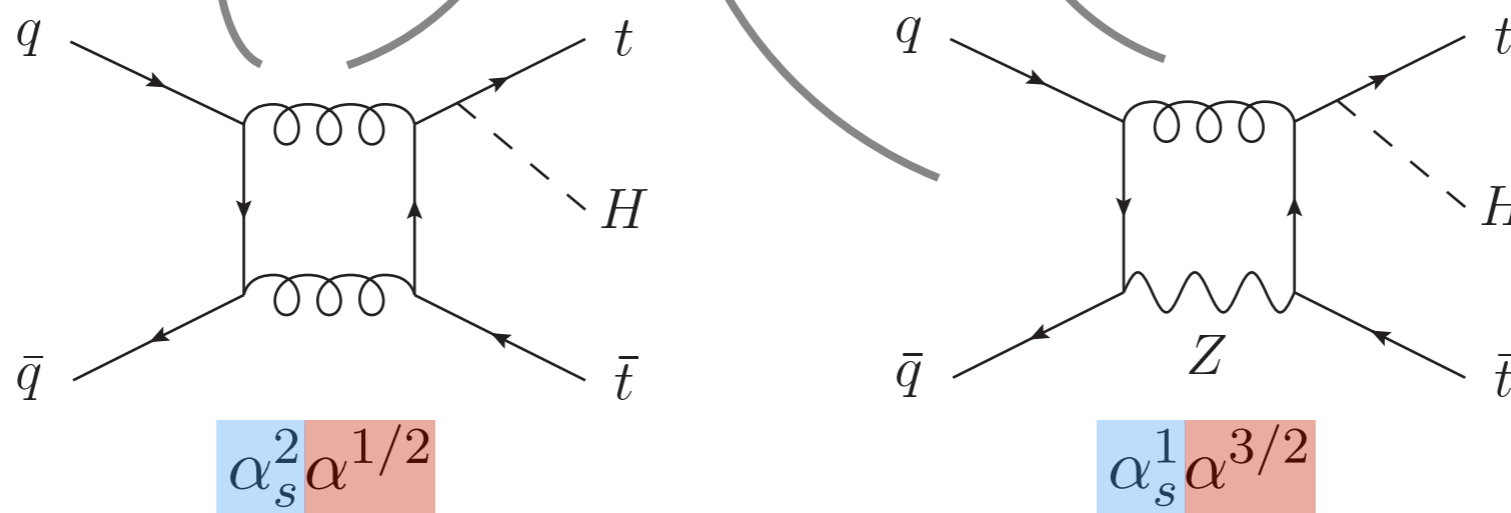
# Structure of NLO EW-QCD corrections



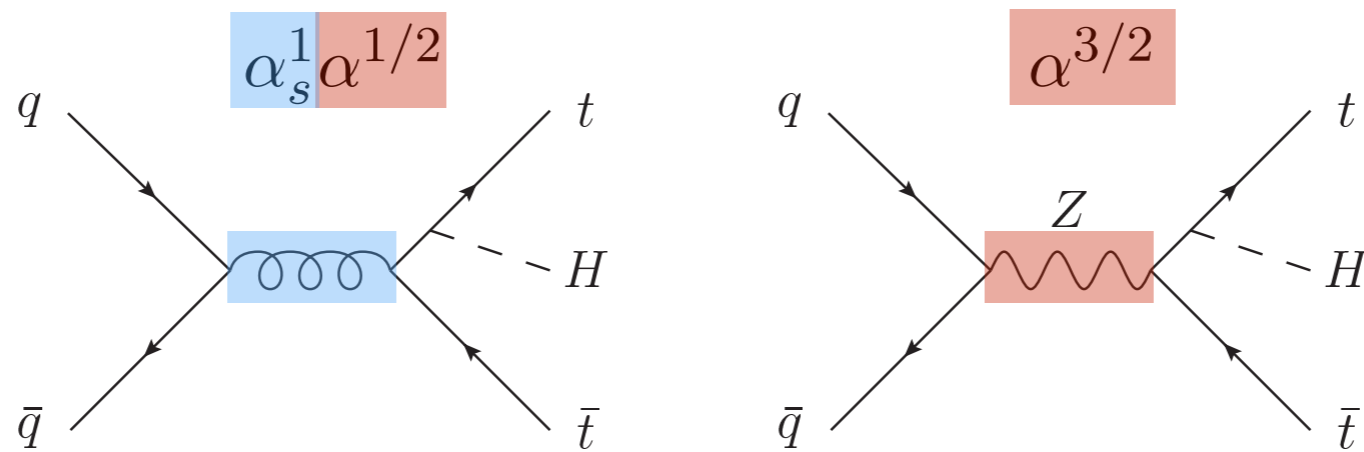
LO



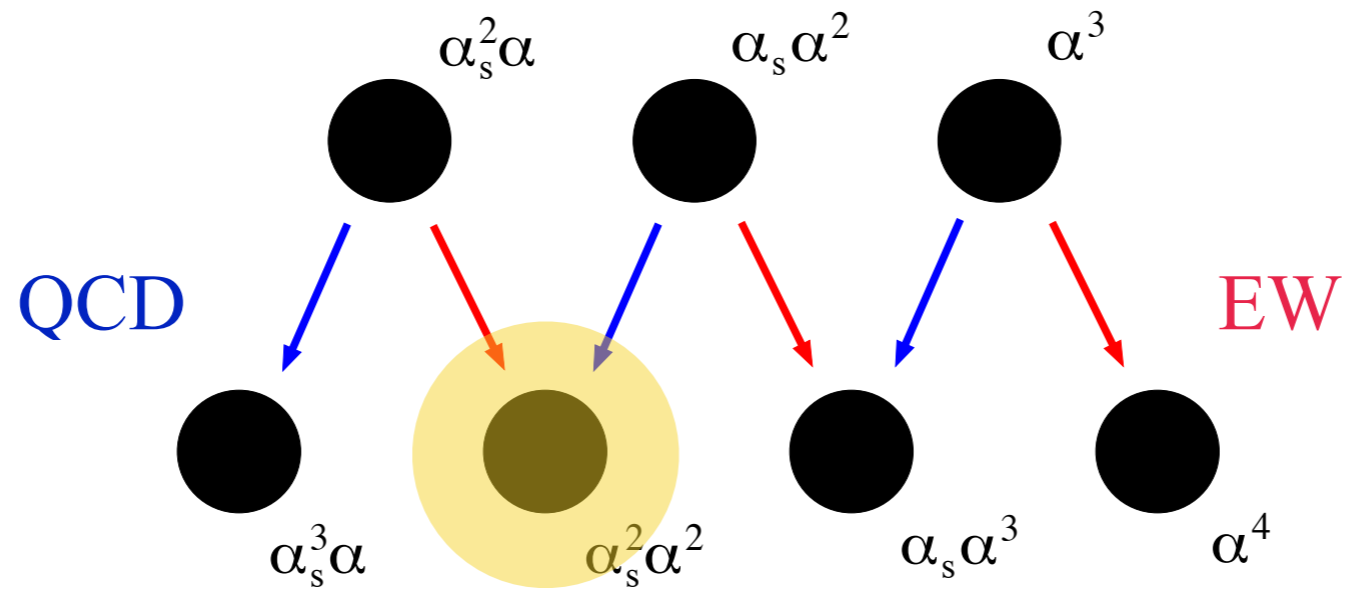
NLO



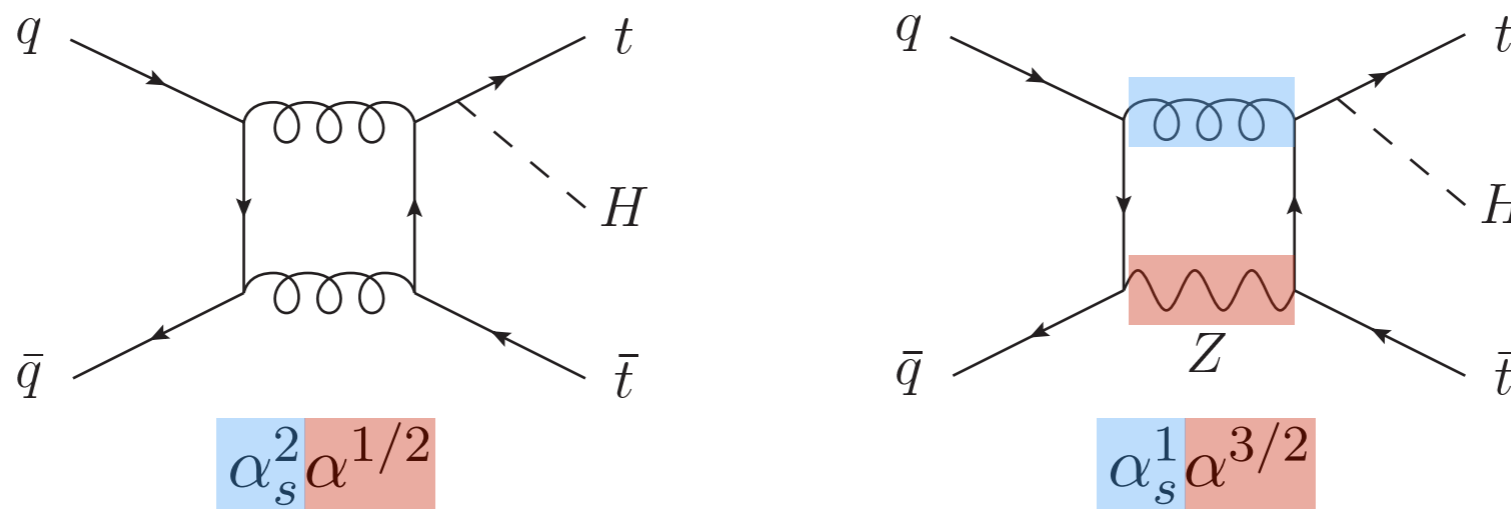
# Structure of NLO EW-QCD corrections



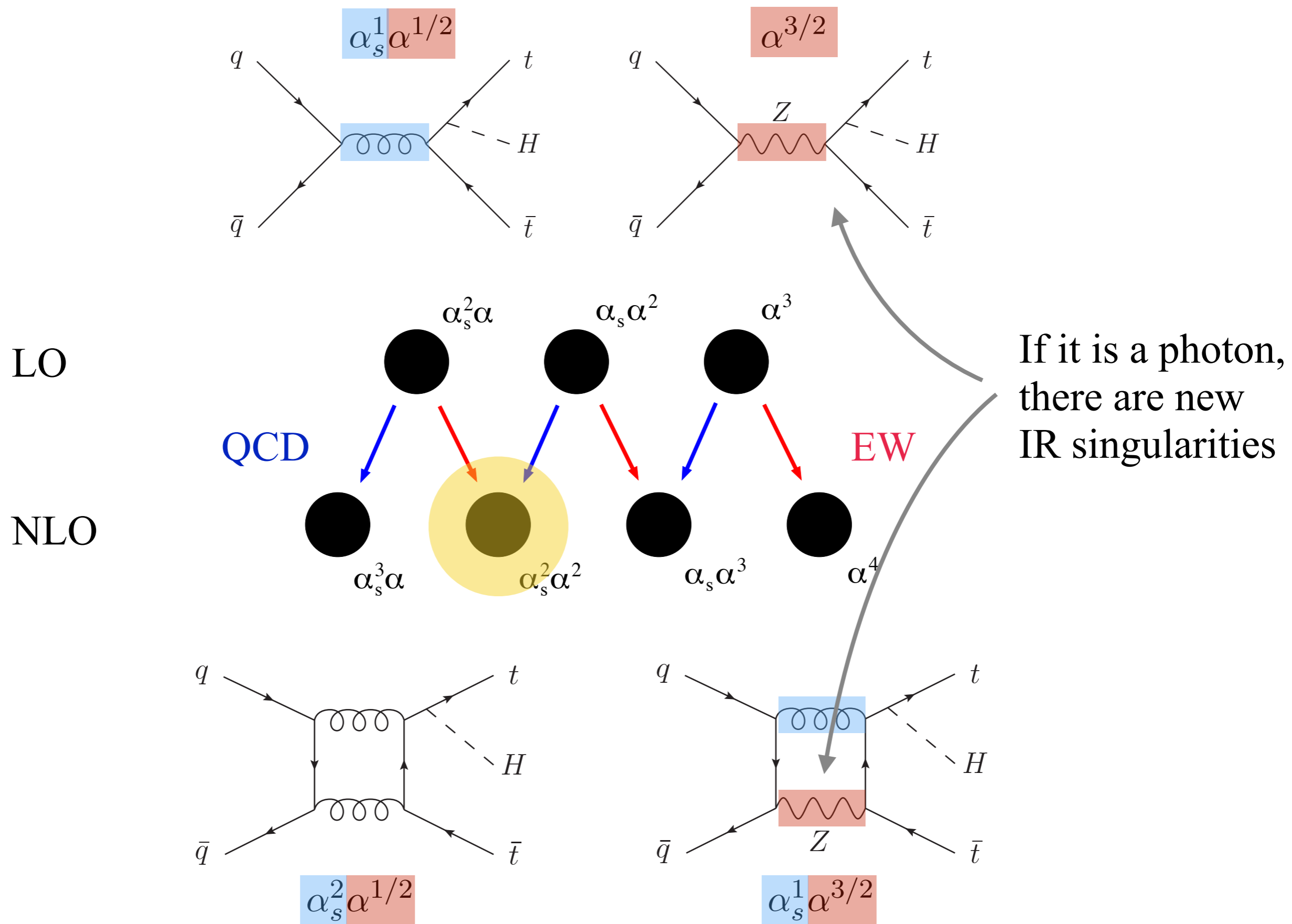
LO



NLO



# Structure of NLO EW-QCD corrections



# Comparison between different schemes

$$m_W = 80.385 \text{ GeV}, \quad m_Z = 91.188 \text{ GeV}$$

$$\begin{aligned} \alpha(m_Z) \text{ scheme} & \longrightarrow \frac{1}{\alpha(m_Z)} = 128.93 \\ G_\mu \text{ scheme} & \longrightarrow G_\mu = 1.16639 \cdot 10^{-5} \longrightarrow \frac{1}{\alpha} = 132.23 \end{aligned}$$

	$t\bar{t}H$	$t\bar{t}Z$	$t\bar{t}W^+$	$t\bar{t}W^-$
$\sigma_{\text{LO QCD}}(\text{pb})$	$3.617 \cdot 10^{-1}$	$5.282 \cdot 10^{-1}$	$2.496 \cdot 10^{-1}$	$1.265 \cdot 10^{-1}$
$\sigma_{\text{LO QCD}}^{G_\mu}(\text{pb})$	$3.527 \cdot 10^{-1}$	$5.152 \cdot 10^{-1}$	$2.433 \cdot 10^{-1}$	$1.234 \cdot 10^{-1}$
$\Delta_{\text{LO QCD}}^{G_\mu}(\%)$	2.5	2.5	2.5	2.5
$\delta_{\text{LO EW}}(\%)$	1.2	0.0	0	0
$\delta_{\text{LO EW}}^{G_\mu}(\%)$	1.2	0.0	0	0
$\Delta_{\text{LO EW}}^{G_\mu}(\%)$	2.5	2.5	2.5	2.5
$\delta_{\text{NLO EW}}(\%)$	-1.2	-3.8	-7.7	-6.7
$\delta_{\text{NLO EW}}^{G_\mu}(\%)$	1.8	-0.7	-4.5	-3.5
$\Delta_{\text{NLO EW}}^{G_\mu}(\%)$	-0.5	-0.7	-0.9	-0.9

$$\Delta_{\text{LO QCD}}^{G_\mu} = \frac{\sigma_{\text{LO QCD}} - \sigma_{\text{LO QCD}}^{G_\mu}}{\sigma_{\text{LO QCD}}}$$

$$\delta_X = \frac{\sigma_X}{\sigma_{\text{LO QCD}}}$$

Table 11: Comparison between results in the  $\alpha(m_Z)$  and  $G_\mu$  scheme, at 13 TeV.

# Why Weak corrections to $t\bar{t}H$ production?

We calculated NLO corrections of mixed QCD-Weak origin, ignoring QED effects. We compared them to NLO QCD corrections.

## Phenomenology motivations

Electroweak corrections are in general small. However, the Sudakov logarithms  $\alpha_W \ln^2 s/M_W^2$  can enhance their size. They originate only from Weak corrections

The cross section of  $t\bar{t}H$  depends directly on  $\lambda_{t\bar{t}H}^2$ . At NLO, only Weak corrections introduce a dependence on other Higgs couplings.

## Automation of NLO corrections

Without QED (photons), the structure of IR singularities is simpler  
 $t\bar{t}H$  was the first pheno study of EW corrections in the **MG5\_aMC@NLO** framework.

# Numerical results weak corrections

## Inclusive rates

(Boosted regime in brackets)

### NLO corrections

$\delta_{\text{NLO}}(\%)$	8 TeV	13 TeV	100 TeV
QCD	$+25.6^{+6.2}_{-11.8}$ (+19.6 <sup>+3.7</sup> <sub>-11.0</sub> )	$+29.3^{+7.4}_{-11.6}$ (+23.9 <sup>+5.4</sup> <sub>-11.2</sub> )	$+40.4^{+9.9}_{-11.6}$ (+39.1 <sup>+9.7</sup> <sub>-10.4</sub> )
weak	-1.2 (-8.3)	-1.8 (-8.2)	-3.0 (-7.8)

### Heavy Boson Radiation

$\delta_{\text{HBR}}(\%)$	8 TeV	13 TeV	100 TeV
$W$	+0.42(+0.74)	+0.37(+0.70)	+0.14(+0.22)
$Z$	+0.29(+0.56)	+0.34(+0.68)	+0.51(+0.95)
$H$	+0.17(+0.43)	+0.19(+0.48)	+0.25(+0.53)
sum	+0.88(+1.73)	+0.90(+1.86)	+0.90(+1.70)

Partial compensation of Sudakov logs

### NLO weak subchannels

$\delta_{\text{NLO}}(\%)$	8 TeV	13 TeV	100 TeV
$gg$	-0.67 (-2.9)	-1.12 (-4.0)	-2.64 (-6.8)
$u\bar{u}$	-0.01 (-3.2)	-0.15 (-2.3)	-0.10 (-0.5)
$d\bar{d}$	-0.55 (-2.2)	-0.52 (-1.9)	-0.23 (-0.5)



# Processes

$$t\bar{t}W^\pm, \quad t\bar{t}Z, \quad t\bar{t}\gamma, \quad \boxed{t\bar{t}H}$$

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$$t\bar{t}W^+W^-, \quad t\bar{t}ZZ, \quad t\bar{t}\gamma\gamma, \quad t\bar{t}W^\pm\gamma, \quad t\bar{t}W^\pm Z, \quad t\bar{t}Z\gamma \quad t\bar{t}VV$$

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$$t\bar{t}t\bar{t}$$

... that is  $t\bar{t}H$  and its possible irr. backgrounds

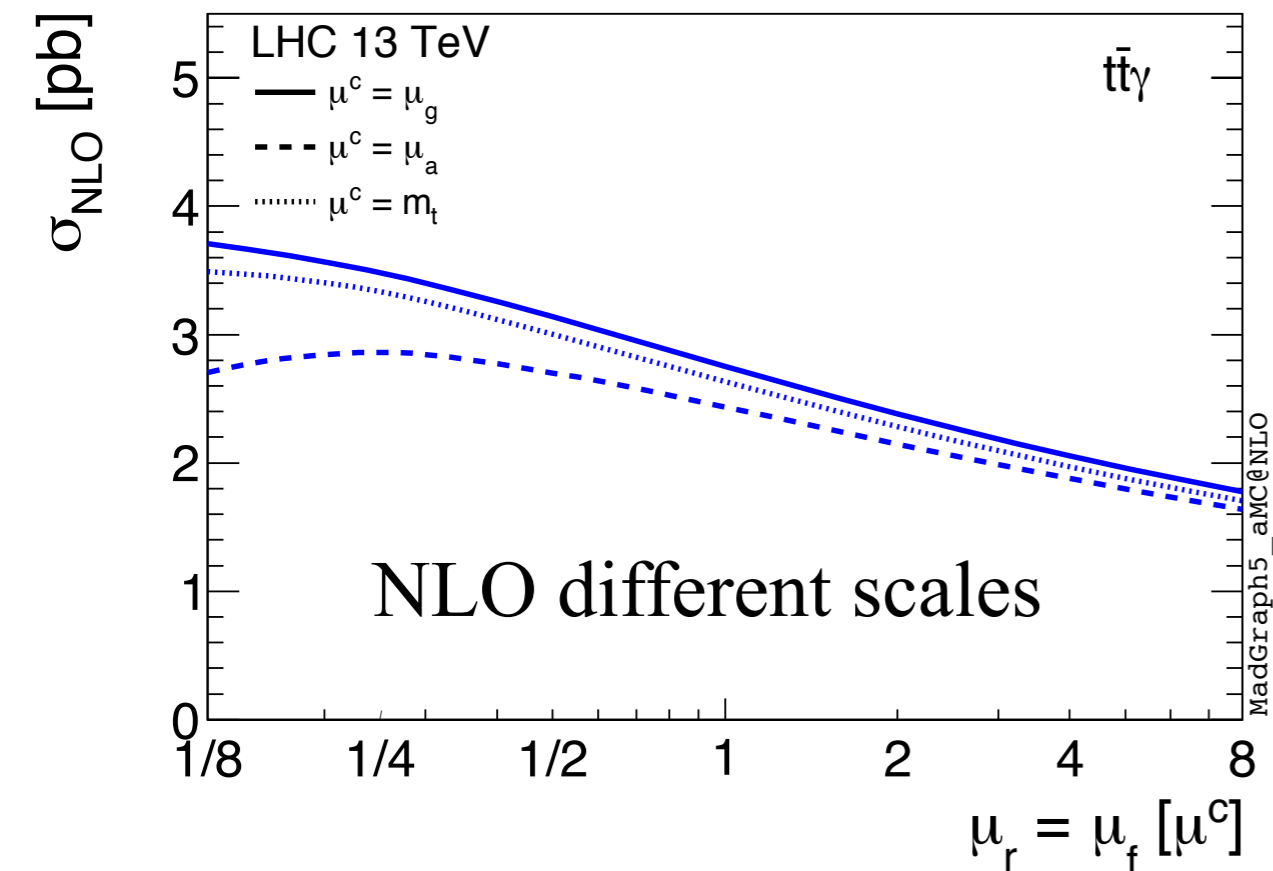
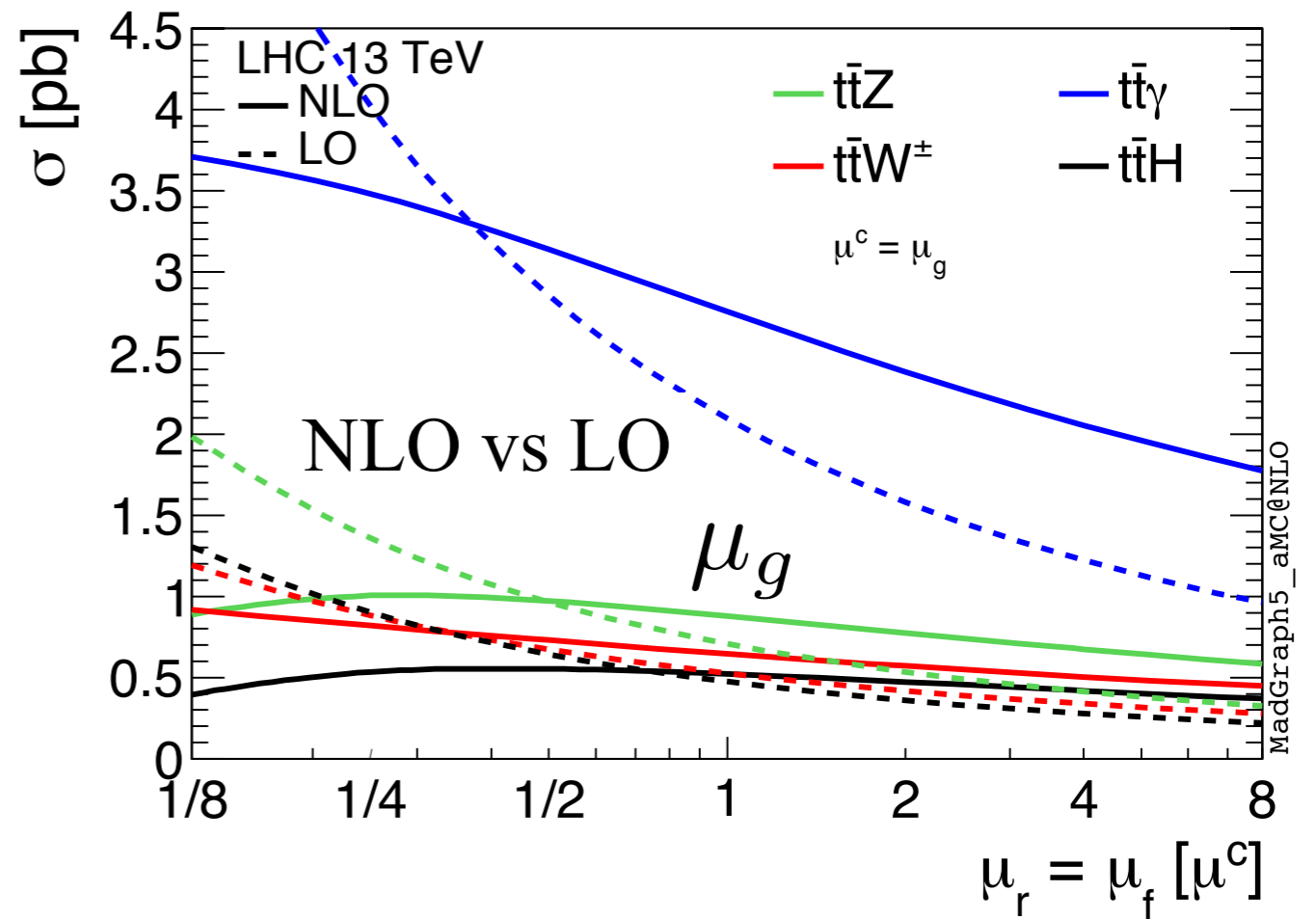
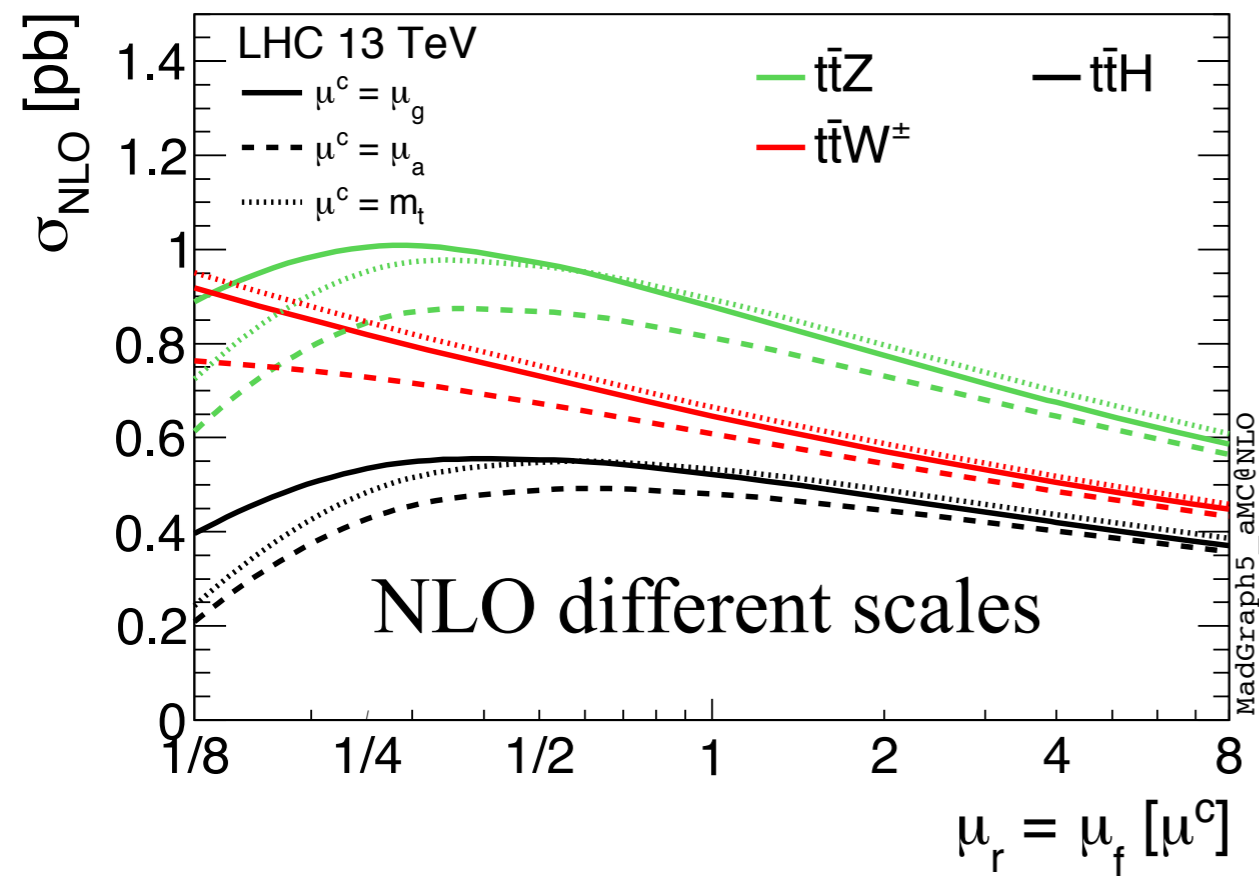
## Scale definitions

We compare the scale dependencies for the fixed scale and for two (common) definitions of dynamical scales: the arithmetic and geometric mean of final-state transverse masses.

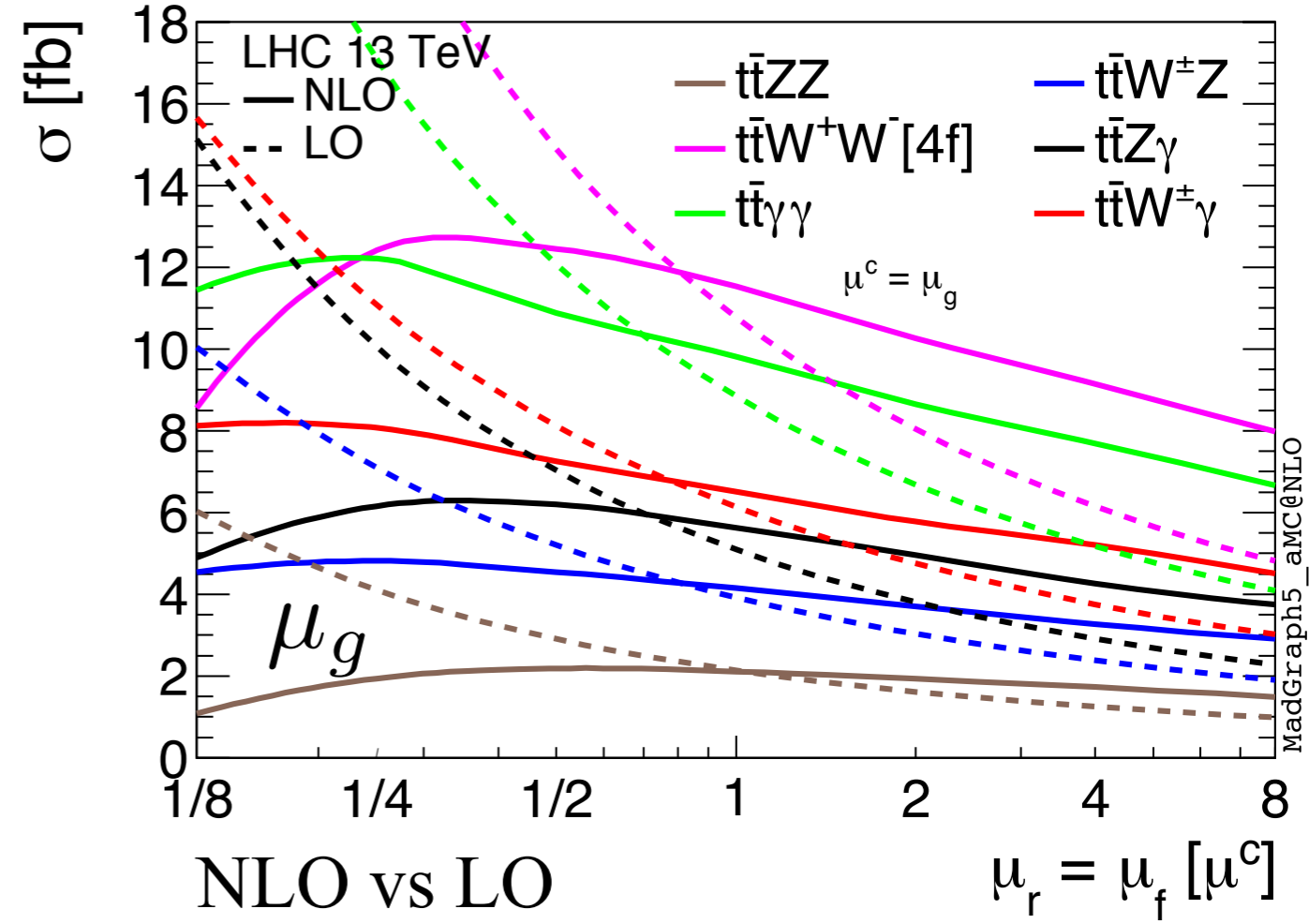
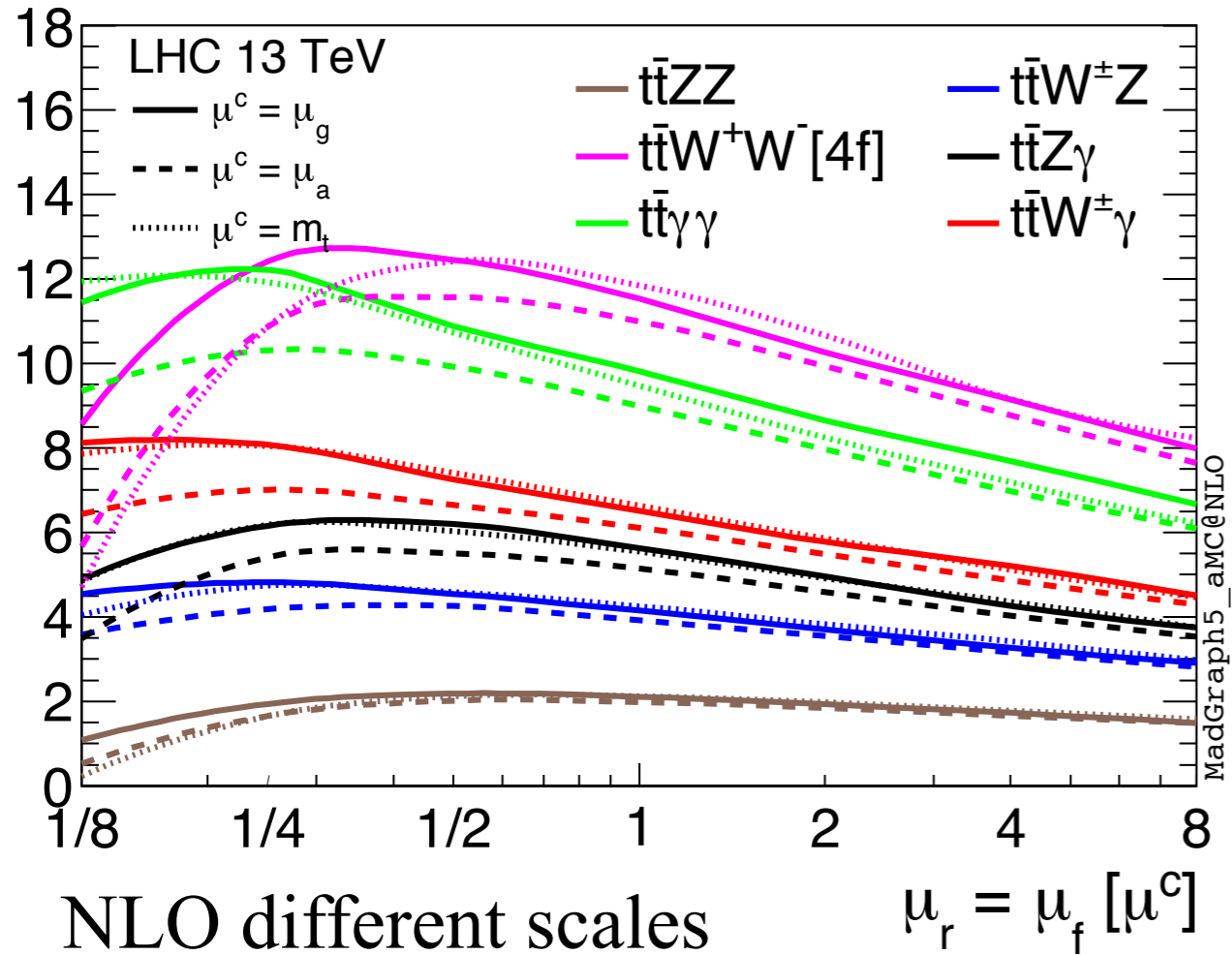
**WE DO NOT SEARCH FOR THE BEST SCALE!**

$$\mu_a = \frac{H_T}{N} := \frac{1}{N} \sum_{i=1, N(+1)} m_{T,i}$$
$$\mu_g := \left( \prod_{i=1, N} m_{T,i} \right)^{1/N}$$

# Scale dependence: $t\bar{t}V$ processes



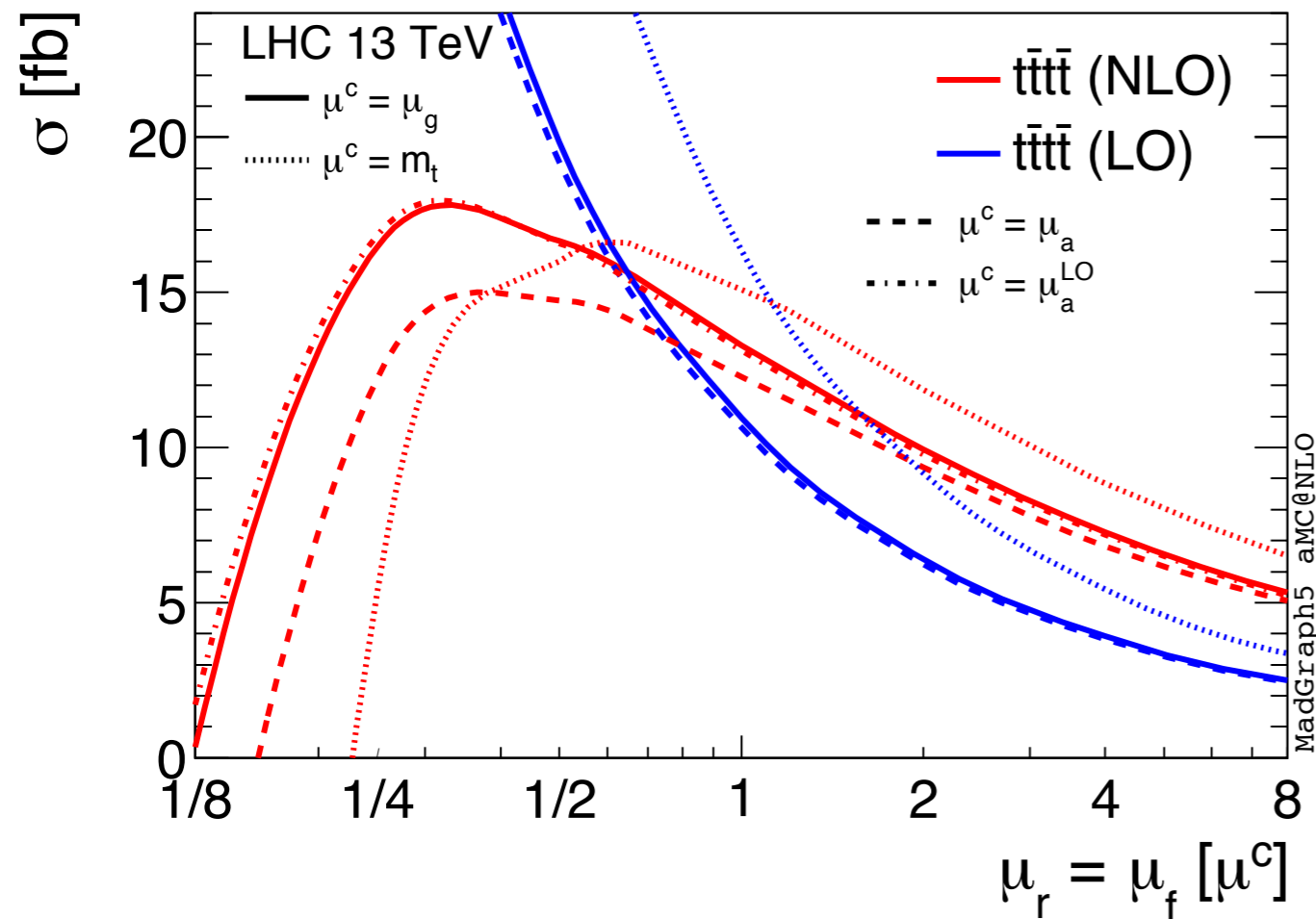
# Scale dependence: $t\bar{t}VV$ processes



13 TeV $\sigma$ [fb]	$t\bar{t}ZZ$	$t\bar{t}W^+W^- [4f]$	$t\bar{t}\gamma\gamma$
NLO	$2.117^{+3.8\% +1.9\%}_{-8.6\% -1.8\%}$	$11.84^{+8.3\% +2.3\%}_{-11.2\% -2.4\%}$	$10.26^{+13.9\% +1.3\%}_{-13.3\% -1.3\%}$
LO	$2.137^{+36.1\% +1.9\%}_{-24.4\% -1.9\%}$	$10.78^{+38.3\% +2.2\%}_{-25.4\% -2.2\%}$	$8.838^{+36.5\% +1.5\%}_{-24.5\% -1.6\%}$
$K$ -factor	0.99	1.10	1.16

13 TeV $\sigma$ [fb]	$t\bar{t}W^\pm Z$	$t\bar{t}Z\gamma$	$t\bar{t}W^\pm\gamma$
NLO	$4.157^{+9.8\% +2.2\%}_{-10.7\% -1.6\%}$	$5.771^{+10.5\% +1.8\%}_{-12.1\% -1.9\%}$	$6.734^{+12.0\% +1.8\%}_{-11.6\% -1.4\%}$
LO	$3.921^{+32.6\% +2.3\%}_{-22.8\% -2.2\%}$	$5.080^{+38.0\% +1.9\%}_{-25.3\% -1.9\%}$	$6.145^{+32.4\% +2.1\%}_{-22.6\% -2.0\%}$
$K$ -factor	1.06	1.14	1.10

# Scale dependence: $t\bar{t}t\bar{t}$



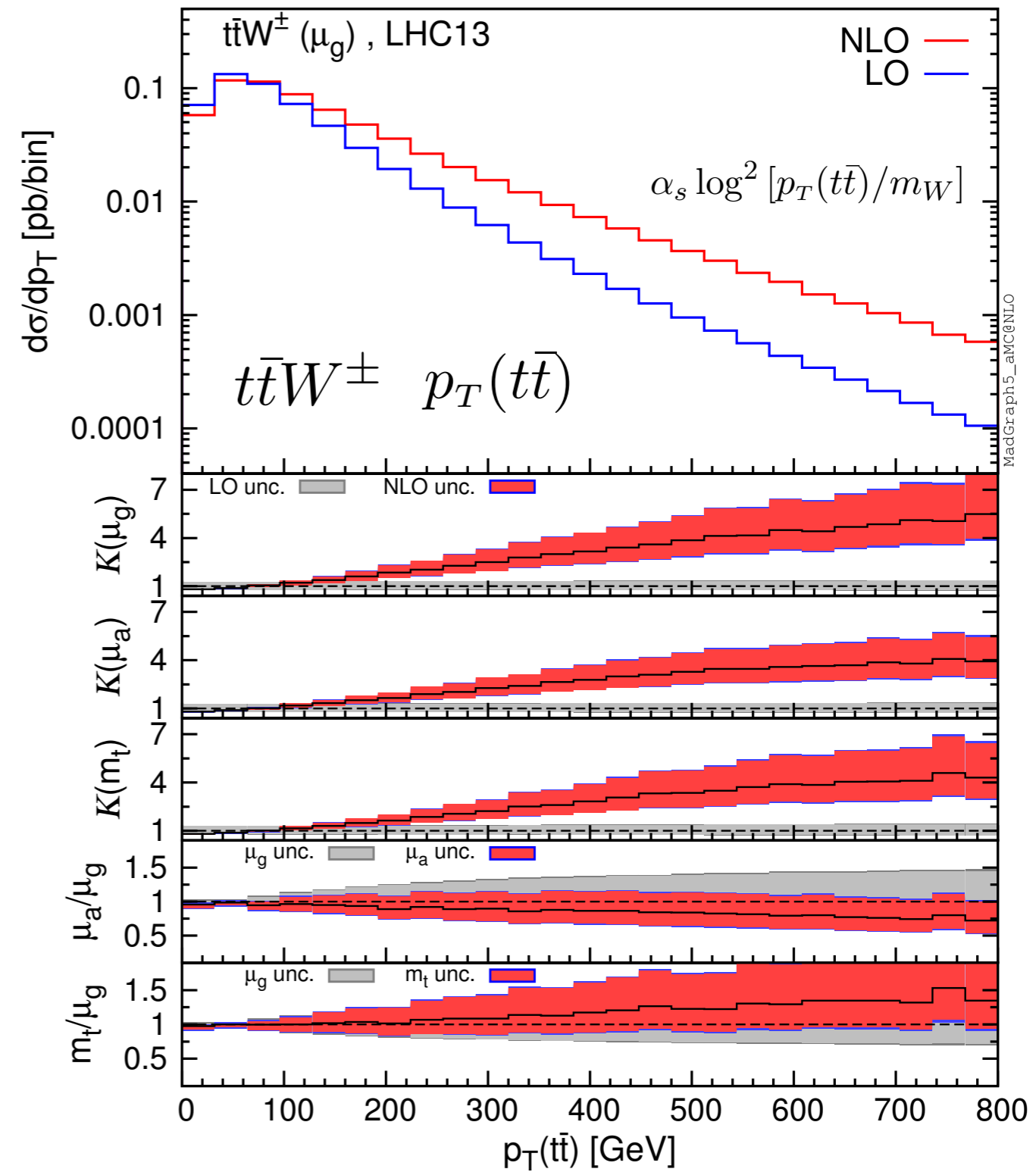
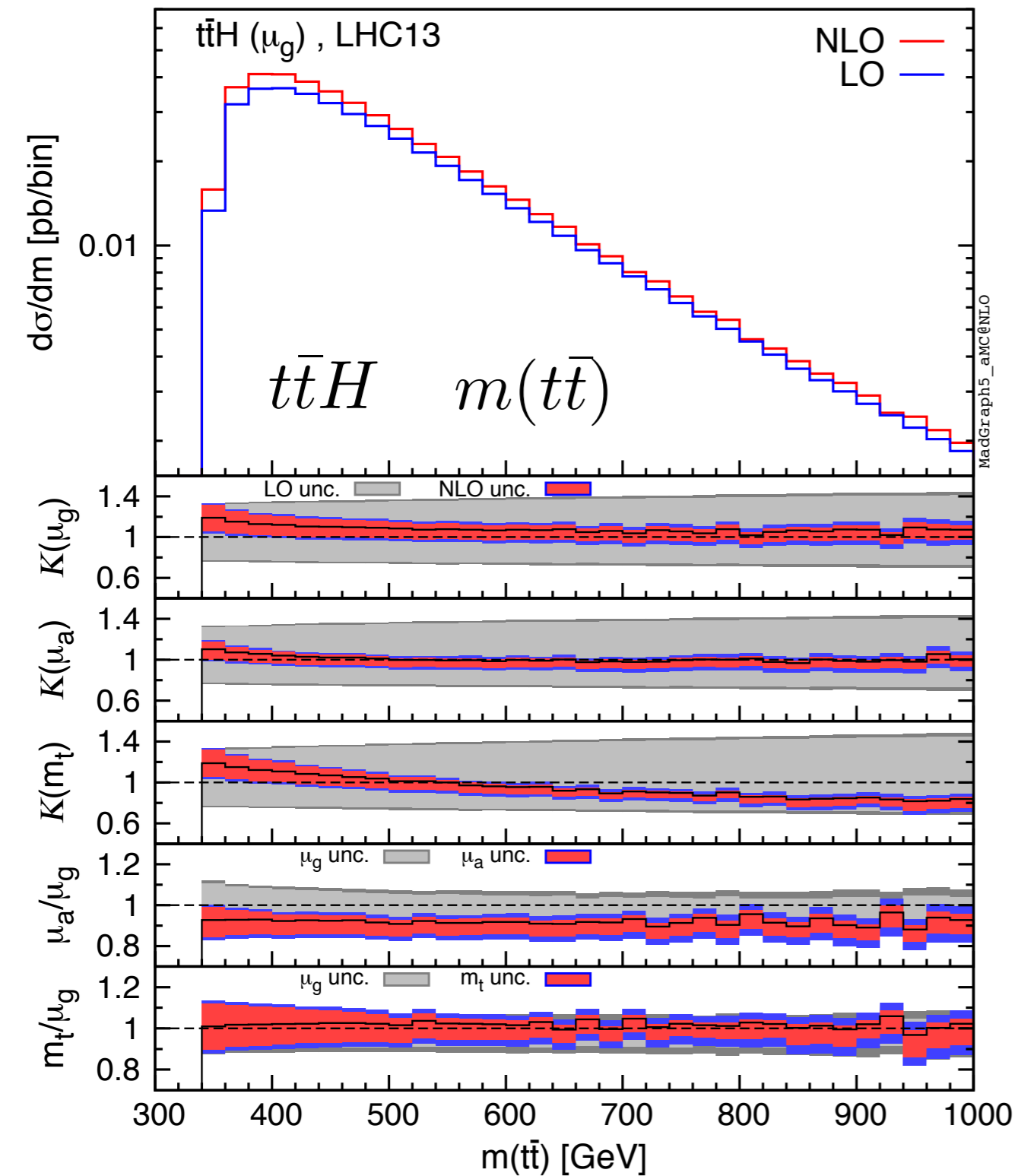
NLO vs LO, different scales.  
 Studies performed also in  
 Bevilacqua and Worek '12

$$\sigma_{\text{NLO}} = 13.31^{+25.8\%}_{-25.3\%} \text{ } ^{+5.8\%}_{-6.6\%} \text{ fb}$$

$$\sigma_{\text{LO}} = 10.94^{+81.1\%}_{-41.6\%} \text{ } ^{+4.8\%}_{-4.7\%} \text{ fb}$$

$$K\text{-factor} = 1.22$$

# Distributions: representative results at fixed order



# Distributions: representative results at fixed order

