



InVisibles Workshop 2015, Madrid

22-26 June 2015

*eV sterile ν problem and
cosmological bounds for
secret interactions*

Ninetta Saviano
IPPP, Durham University

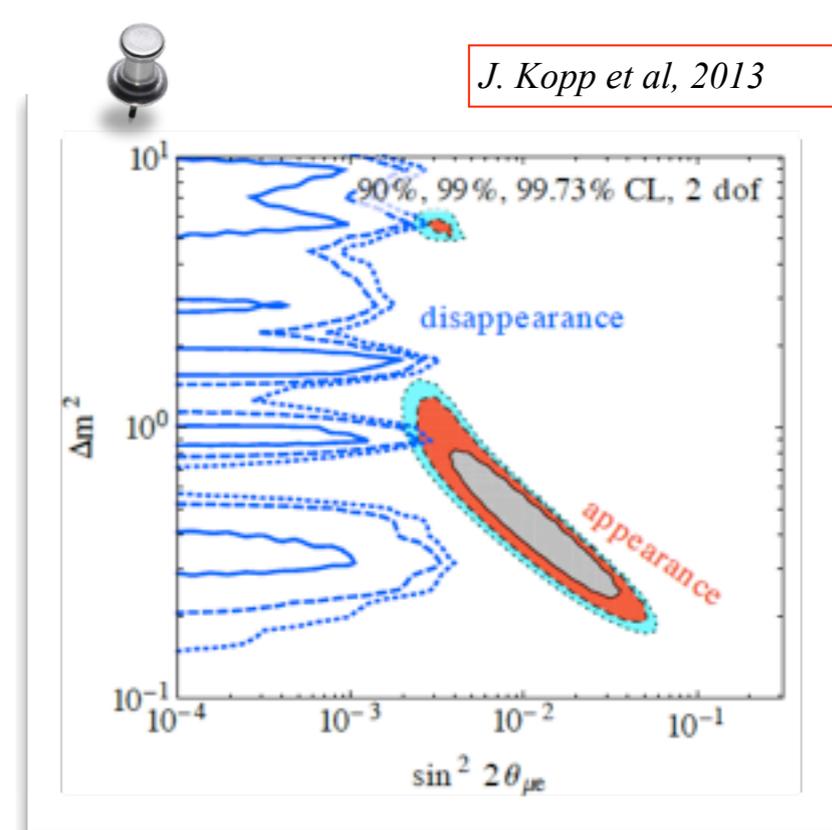
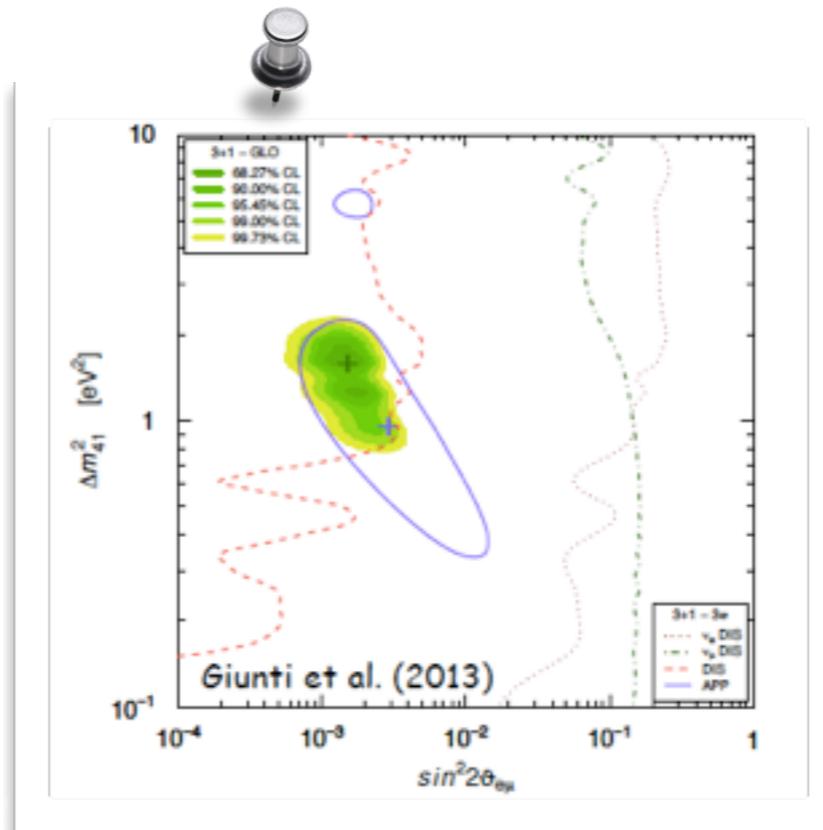


eV Sterile Neutrino

The investigation on Light Sterile Neutrinos has been stimulated by the presence of anomalous results from neutrino oscillation experiments

-  **LNSD**
-  **MiniBooNE**
-  **Gallium**
-  **Reactor**

see
White paper, Abazajian et al., 2012



...sometimes in tension among themselves...
appearance VS disappearance

...waiting new data (IceCube...)

Interpretation: **1** (or more) *sterile neutrino* with $\Delta m^2 \sim O(eV^2)$ and $\theta_s \sim O(\theta_{13})$

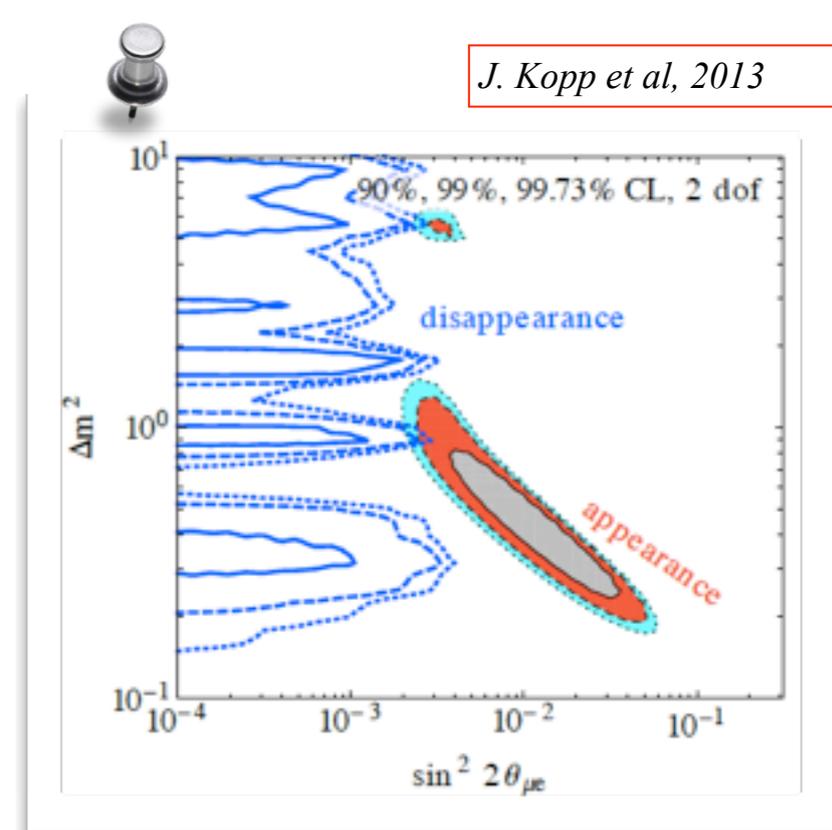
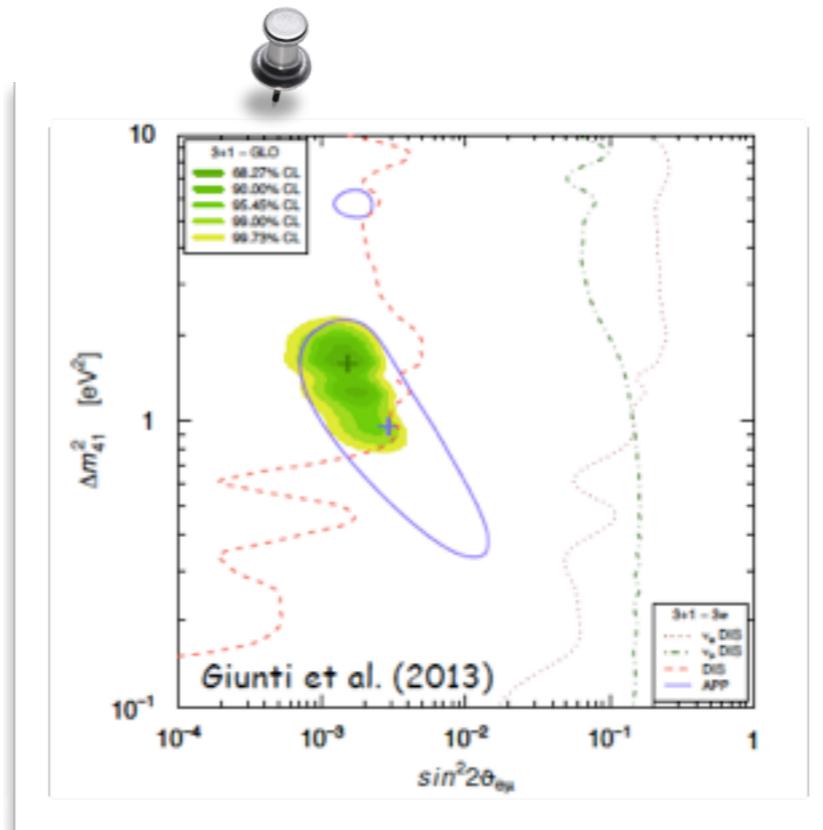
eV

eV Sterile Neutrino

The investigation on Light Sterile Neutrinos has been stimulated by the presence of anomalous results from neutrino oscillation experiments

-  LNSD
-  MiniBooNE
-  Gallium
-  Reactor

see
White paper, Abazajian et al., 2012



...sometimes in tension among themselves...
appearance VS disappearance

3+1, 3+2 schemes

...waiting new data (IceCube...)

Interpretation: *1* (or more) *sterile neutrino* with $\Delta m^2 \sim O(eV^2)$ and $\theta_s \sim O(\theta_{13})$

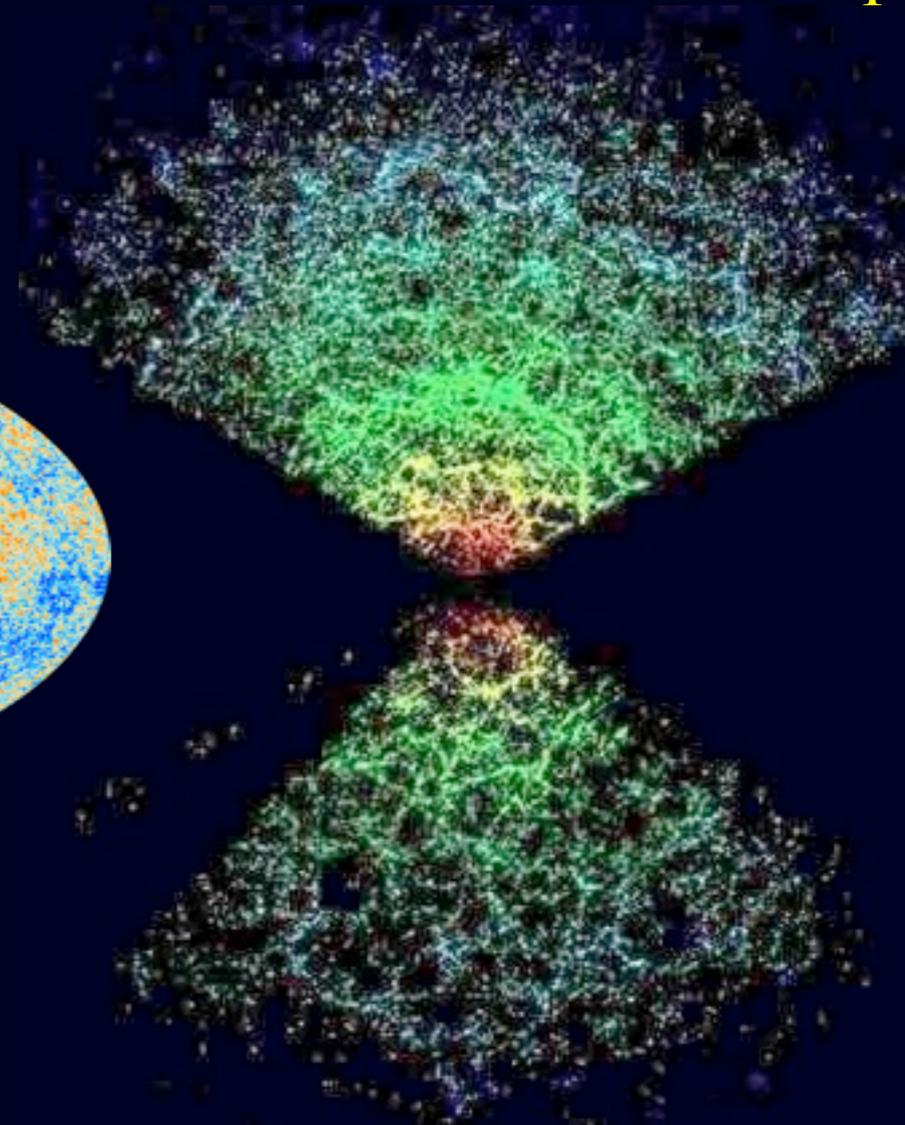
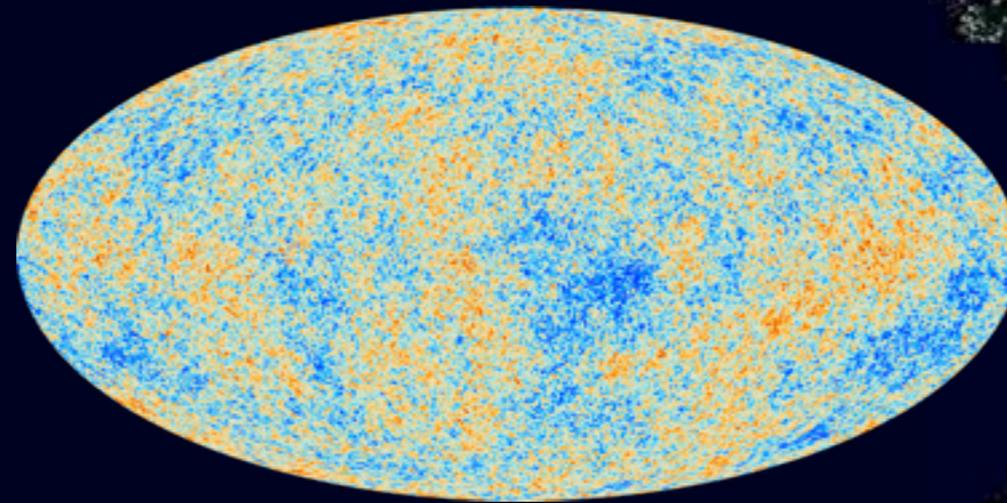
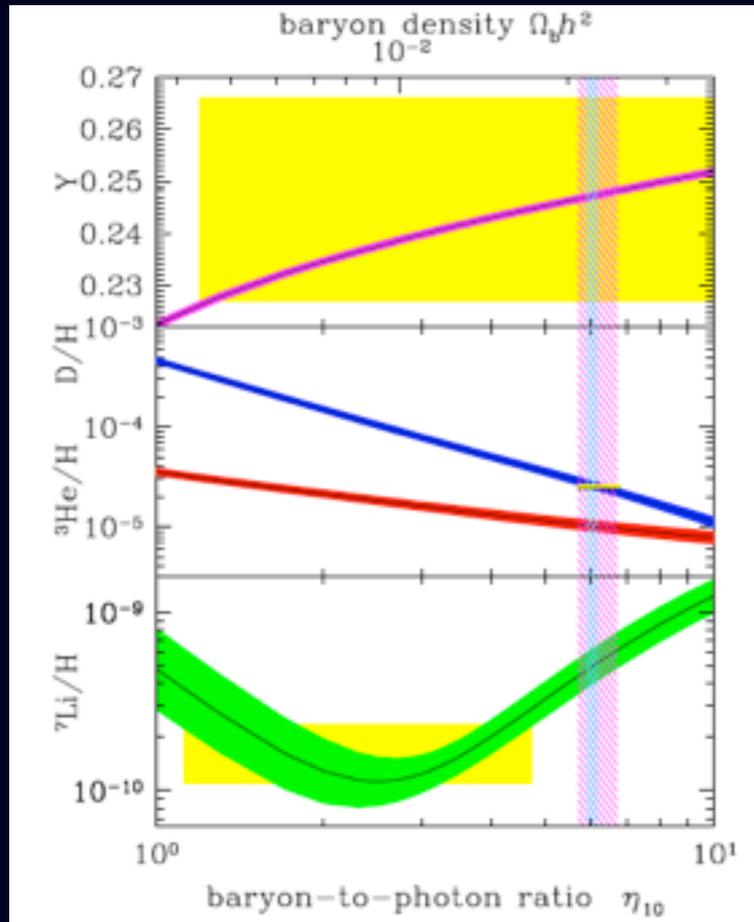
Are eV ν_s compatible with cosmology?

Cosmological observations

1 MeV

1 eV

T



Sensitivity to N_{eff} and ν flavour

Sensitivity to N_{eff} and ν masses



Radiation Content in the Universe

At $T < m_e$, the radiation content of the Universe is

$$\varepsilon_R = \varepsilon_\gamma + \varepsilon_\nu + \varepsilon_x$$

The **non-e.m.** energy density is parameterized by the effective numbers of neutrino species N_{eff}

$$\varepsilon_\nu + \varepsilon_x = \frac{7}{8} \frac{\pi^2}{15} T_\nu^4 N_{\text{eff}} = \frac{7}{8} \frac{\pi^2}{15} T_\nu^4 (N_{\text{eff}}^{\text{SM}} + \Delta N)$$

$$N_{\text{eff}}^{\text{SM}} = 3.046 \quad \text{due to non-instantaneous neutrino decoupling}$$

(+ oscillations)

Mangano et al. 2005

ΔN = Extra Radiation: axions and axion-like particles, **sterile neutrinos (totally or partially thermalized)**, neutrinos in very low-energy reheating scenarios, relativistic decay products of heavy particles...

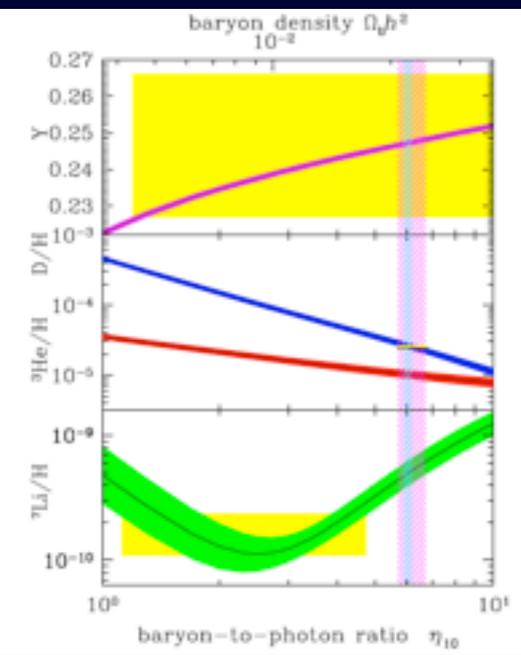
Di Bari et al. 2013, Boehm et al. 2012, Conlon and Marsh, 2013, Gelmini, Palomarez-Ruiz, Pascoli, 2004

Impact on Big Bang Nucleosynthesis

At $T \sim 1 - 0.01$ MeV production of the primordial abundances of light elements, in particular ^2H , ^4He

When $\Gamma_{n \leftrightarrow p} < H \rightarrow$ *neutron-to-proton ratio freezes out*

$$\frac{n_n}{n_p} = \frac{n}{p} = e^{-\Delta m/T} \rightarrow 1/7$$

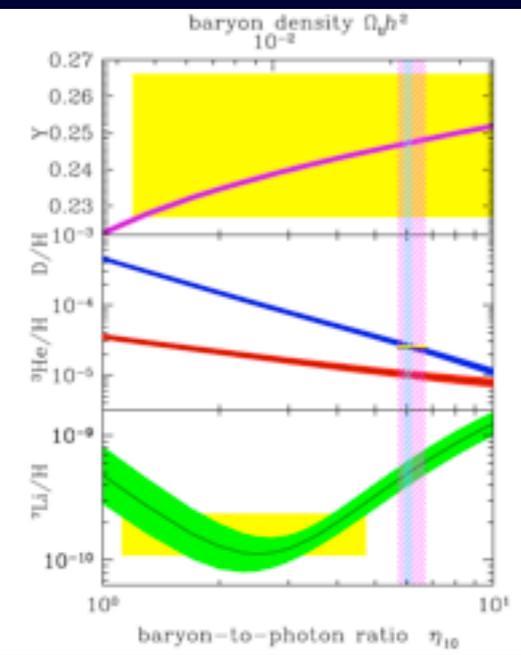


Impact on Big Bang Nucleosynthesis

At $T \sim 1 - 0.01$ MeV production of the primordial abundances of light elements, in particular ^2H , ^4He

When $\Gamma_{n \leftrightarrow p} < H \rightarrow$ *neutron-to-proton ratio freezes out*

$$\frac{n_n}{n_p} = \frac{n}{p} = e^{-\Delta m/T} \rightarrow 1/7$$



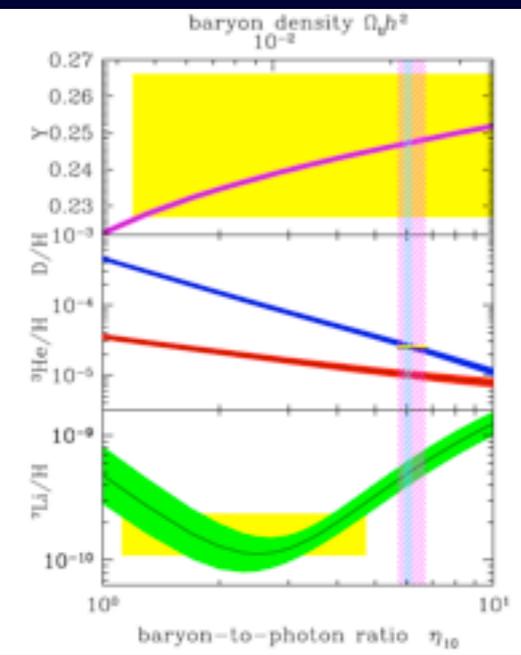
Sterile ν influence on BBN :

Impact on Big Bang Nucleosynthesis

At $T \sim 1 - 0.01$ MeV production of the primordial abundances of light elements, in particular ^2H , ^4He

When $\Gamma_{n \leftrightarrow p} < H \rightarrow$ *neutron-to-proton ratio freezes out*

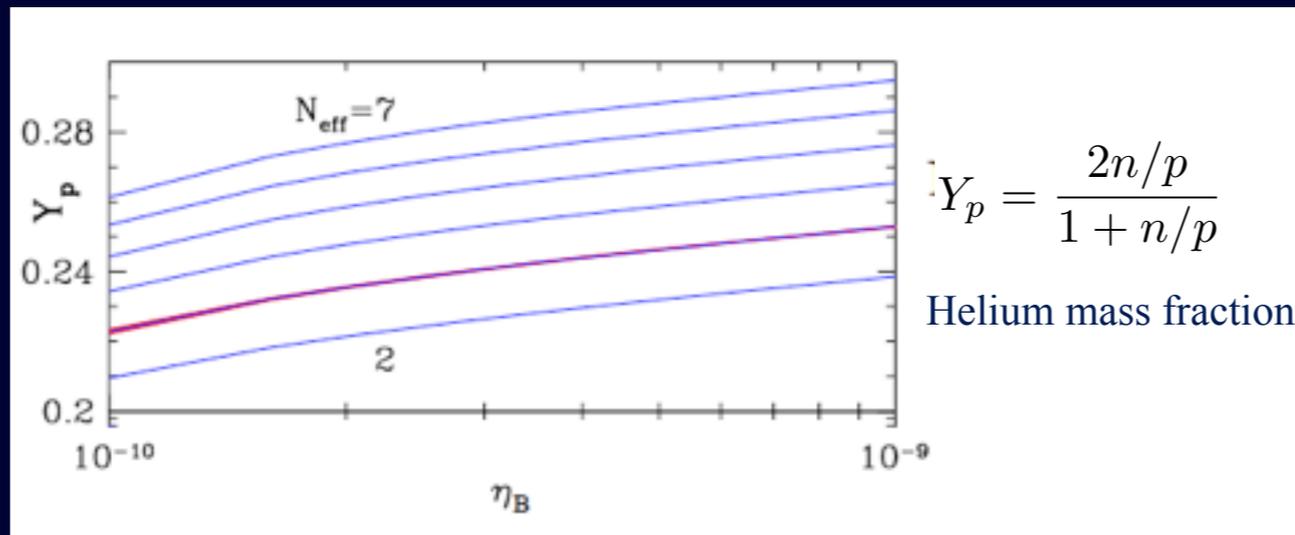
$$\frac{n_n}{n_p} = \frac{n}{p} = e^{-\Delta m/T} \rightarrow 1/7$$



Sterile ν influence on BBN :

📍 contribution to the radiation energy density governing H before and during BBN

$N_{\text{eff}} \uparrow \rightarrow H \uparrow \rightarrow$ early freeze out $\rightarrow n/p \uparrow \rightarrow ^4\text{He} \uparrow$



$$Y_p = \frac{2n/p}{1 + n/p}$$

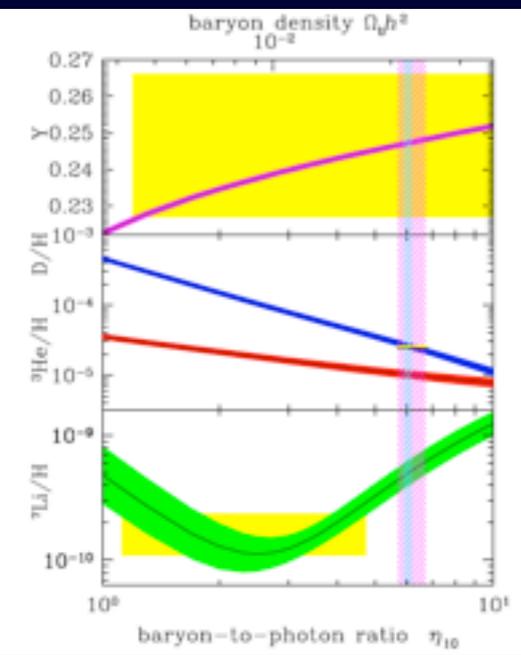
Helium mass fraction

Impact on Big Bang Nucleosynthesis

At $T \sim 1 - 0.01$ MeV production of the primordial abundances of light elements, in particular ^2H , ^4He

When $\Gamma_{n \leftrightarrow p} < H \rightarrow$ *neutron-to-proton ratio freezes out*

$$\frac{n_n}{n_p} = \frac{n}{p} = e^{-\Delta m/T} \rightarrow 1/7$$

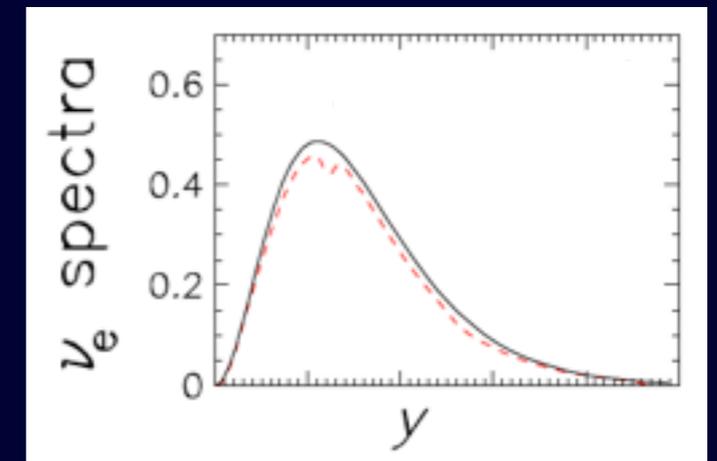


Sterile ν influence on BBN :

- contribution to the radiation energy density governing H before and during BBN

$$N_{\text{eff}} \uparrow \rightarrow H \uparrow \rightarrow \text{early freeze out} \rightarrow n/p \uparrow \rightarrow ^4\text{He} \uparrow$$

- oscillating with the active neutrinos, can distort the active spectra which are the basic input for BBN

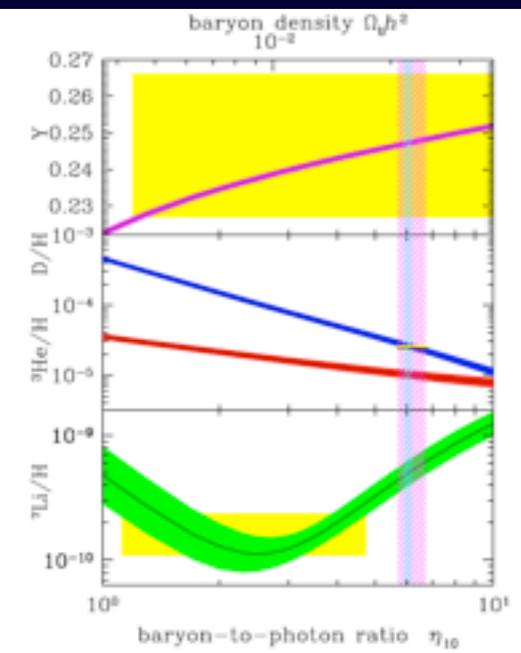


Impact on Big Bang Nucleosynthesis

At $T \sim 1 - 0.01$ MeV production of the primordial abundances of light elements, in particular ^2H , ^4He

When $\Gamma_{n \leftrightarrow p} < H \rightarrow$ *neutron-to-proton ratio freezes out*

$$\frac{n_n}{n_p} = \frac{n}{p} = e^{-\Delta m/T} \rightarrow 1/7$$



Sterile ν influence on BBN :

- contribution to the radiation energy density governing H before and during BBN

$$N_{\text{eff}} \uparrow \rightarrow H \uparrow \rightarrow \text{early freeze out} \rightarrow n/p \uparrow \rightarrow ^4\text{He} \uparrow$$

- oscillating with the active neutrinos, can distort the active spectra which are the basic input for BBN

BBN constraint on ΔN_{eff} : NO strong preference

$$\Delta N_{\text{eff}} \leq 1 \quad (95\% \text{ C.L.})$$

Hamann et al, 2011, Mangano and Serpico. 2012

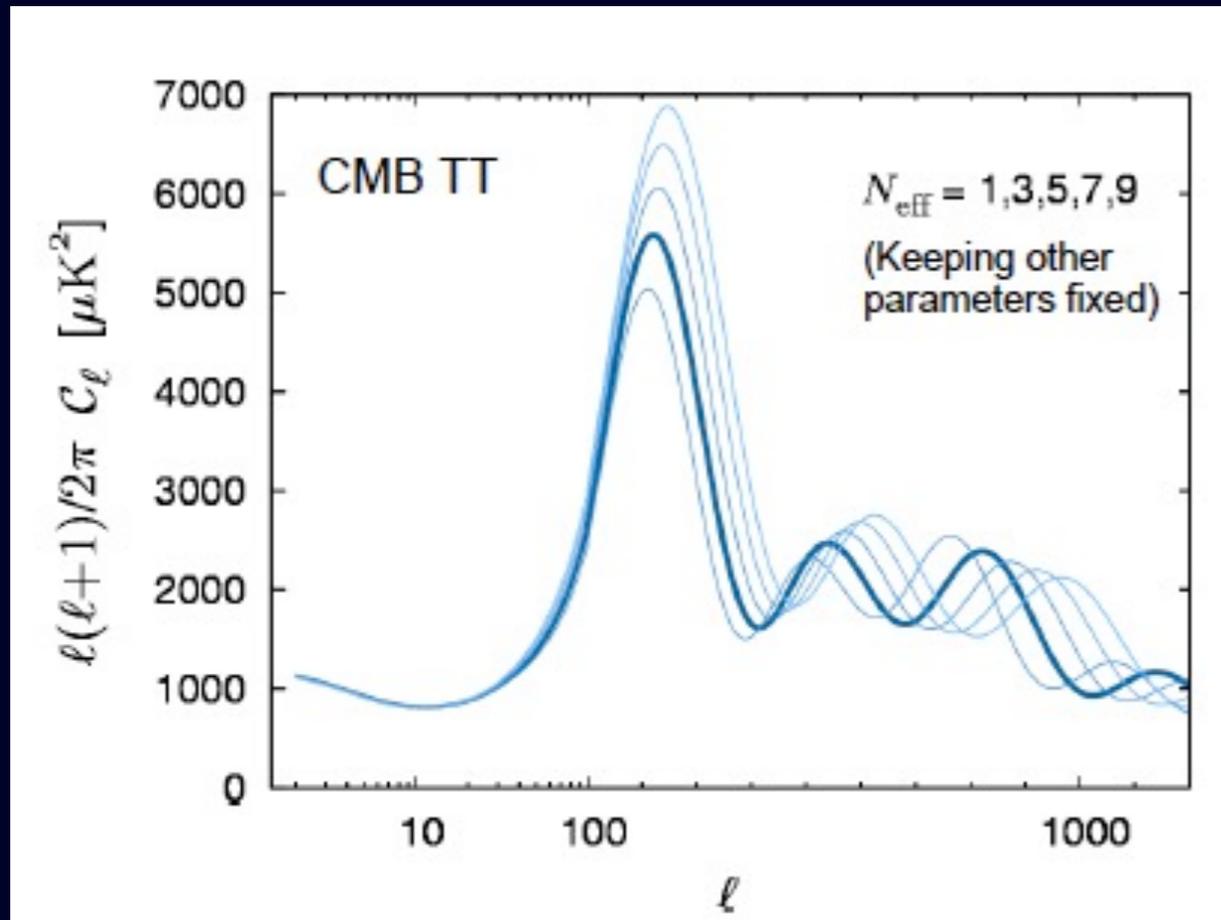
From new precise measure of D in damped Lyman- α system

$$N_{\text{eff}} = 3.28 \pm 0.28, 1 \text{ extra d.o.f. ruled out at } 99.3 \text{ C.L.}$$

Cooke, Pettini et al., 2013

Impact on CMB and LSS

If sterile neutrinos are still relativistic at the CMB epoch, they impact the CMB spectrum

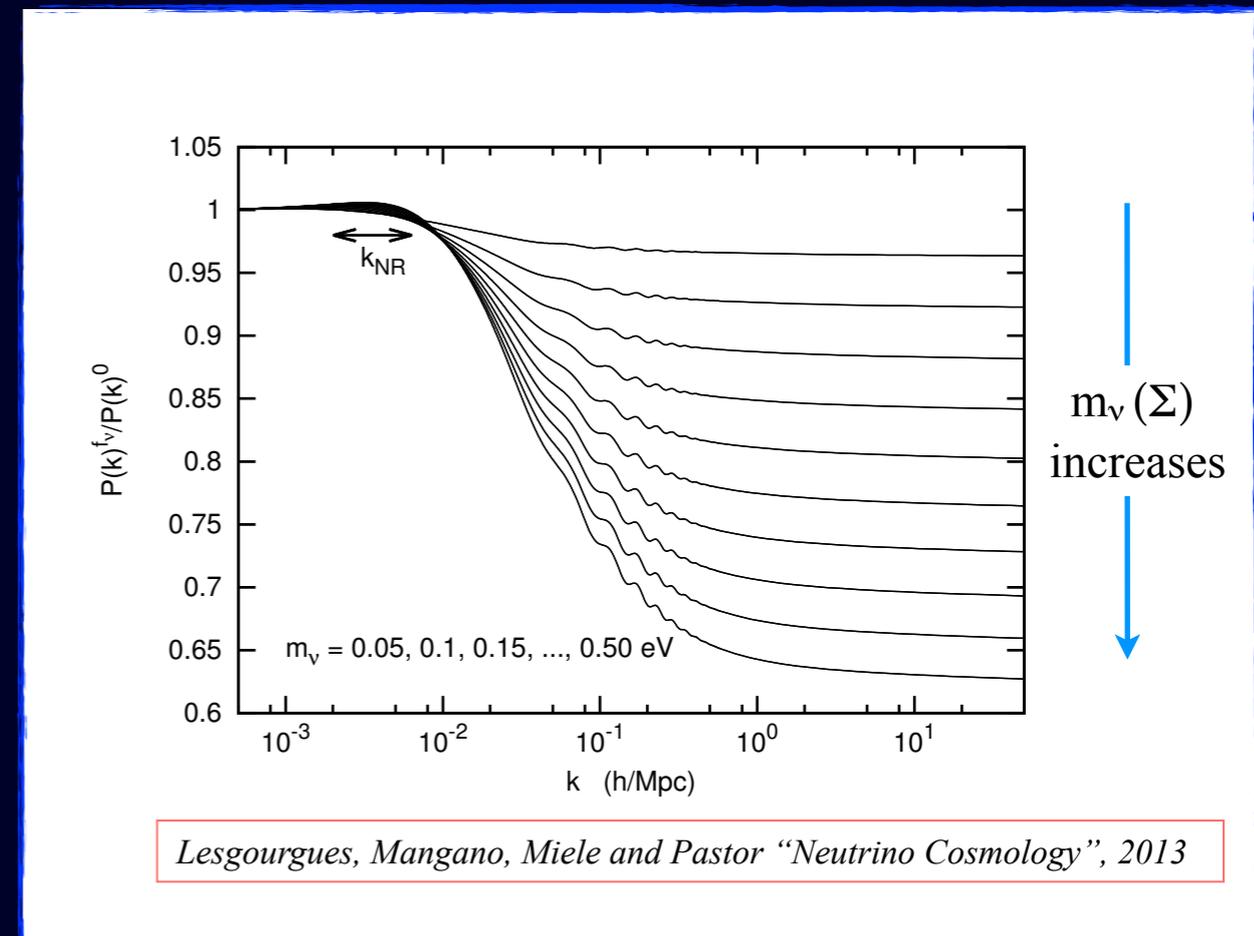


degeneracy among the parameters \rightarrow necessary to combine with other cosmological probes

See Archidiacono's and Wong talks

The small-scale matter power spectrum $P(k > k_{\text{nr}})$ is reduced in presence of massive ν :

- ✓ free-streaming neutrinos do not cluster
- ✓ slower growth rate of CDM (baryon) perturbations



Lesgourgues, Mangano, Miele and Pastor "Neutrino Cosmology", 2013

Joint constraints on N_{eff} and $m_{\nu_s}^{\text{eff}}$

| model | Planck TT + | mass bound (eV) (95% C.L.) |
|--|------------------|---|
| Joint analysis N_{eff} & 1 mass ν_s (prior $m_{\nu_s}^{\text{ph}} < 10$ eV) | lowP+lensing+BAO | $N_{\text{eff}} < 3.7$ $m_{\nu_s}^{\text{eff}} < 0.52$ |
| Joint analysis N_{eff} & 1 mass ν_s (prior $m_{\nu_s}^{\text{ph}} < 2$ eV) | lowP+lensing+BAO | $N_{\text{eff}} < 3.7$ $m_{\nu_s}^{\text{eff}} < 0.38$ |

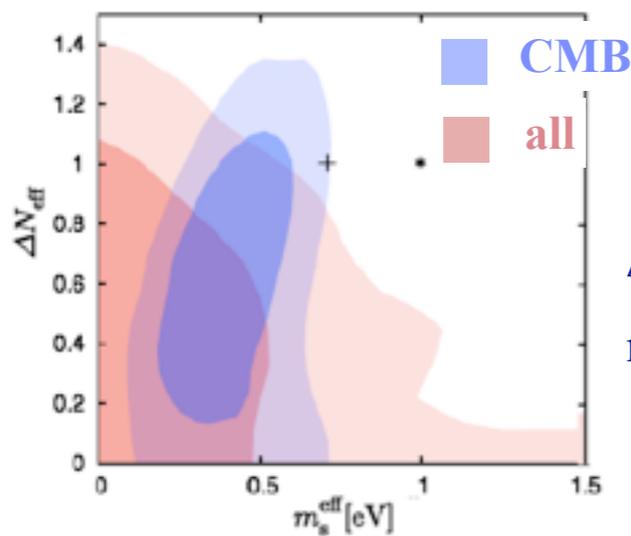
See Galli's talk

$$m_{\nu_s}^{\text{eff}} \equiv (94, 1 \Omega_\nu h^2) \text{eV}$$

$$m_{\nu_s}^{\text{eff}} = \rho_{ss} m_{\nu_s}^{\text{ph}}$$

Planck XIII, 2015

Hamann and Hasenkamp, 2013



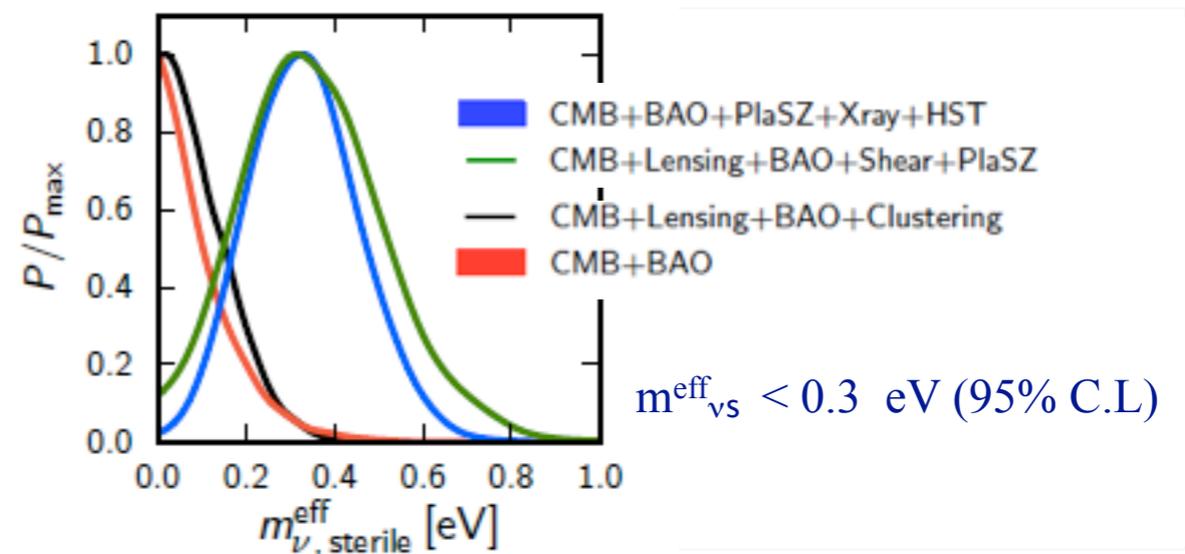
$$\Delta N_{\text{eff}} = 0.61 \pm 0.30$$

$$m_{\nu_s}^{\text{eff}} = 0.41 \pm 0.13 \text{ eV}$$

(68% C.L.)

all= CMB+H0+ C+ CFHTLens

L. Verde et al, 2014



$$m_{\nu_s}^{\text{eff}} < 0.3 \text{ eV (95% C.L.)}$$

Less stringent mass bound from combined analysis $\rightarrow m_{\nu_s}^{\text{eff}} < 0.7 \text{ eV}$

Active-sterile flavour evolution

Sterile ν are produced in the Early Universe by the mixing with the active species in presence of collisions

(3+1) Scenario

Evolution equation:

$$i \frac{d\rho}{dt} = [\Omega, \rho] + C[\rho]$$

$$\rho_{\mathbf{p}} = \begin{pmatrix} \rho_{ee} & \rho_{e\mu} & \rho_{e\tau} & \rho_{es} \\ \rho_{\mu e} & \rho_{\mu\mu} & \rho_{\mu\tau} & \rho_{\mu s} \\ \rho_{\tau e} & \rho_{\tau\mu} & \rho_{\tau\tau} & \rho_{\tau s} \\ \rho_{se} & \rho_{s\mu} & \rho_{s\tau} & \rho_{ss} \end{pmatrix}$$

ν ensemble

$$\Omega = \Omega_{\text{vac}} + \Omega_{\text{mat}} + \Omega_{\nu-\nu} + \dots$$

Vacuum term

MSW effect with background medium
(refractive effect)

refractive ν - ν
self-interactions term

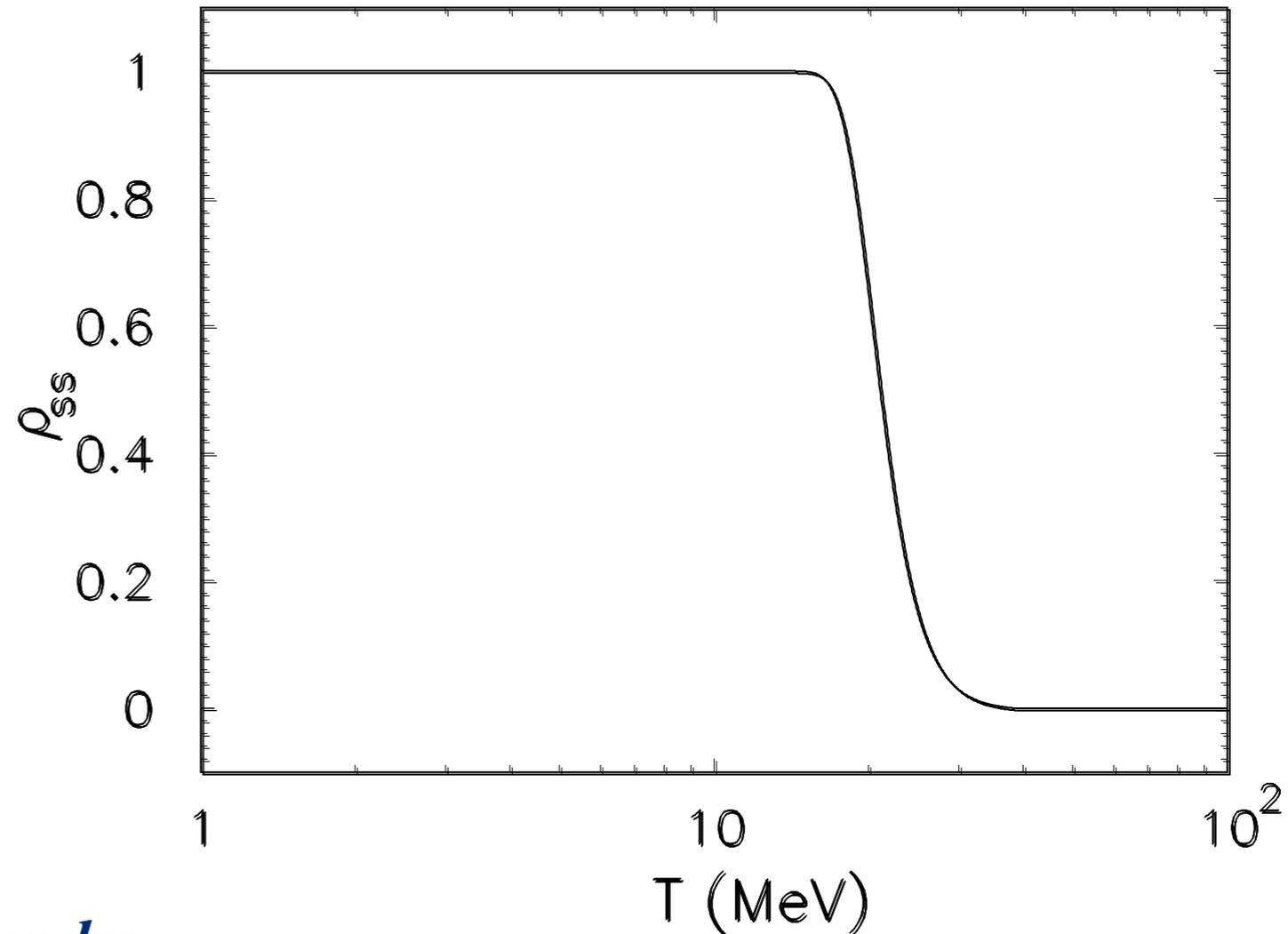
$C[\rho]$

Collisional term

creation, annihilation and all the momentum exchanging processes

Stodolsky, Raffelt and Sigl, 1992;
Sigl and Raffelt 1993;

For the mass and mixing parameters preferred by laboratory sterile ν are copiously produced, reaching 1 extra d.o.f



Comparing with the cosmological bounds:

Thermalized sterile ν with $m \sim O(1 \text{ eV})$ strongly disfavored by cosmological constraints

- 3+1: Too *heavy* for LSS/CMB
- 3+2: Too *heavy* for LSS/CMB and too *many* for BBN/CMB

Possible solutions...?

- *Different mechanisms to suppress the ν_s abundance:*

1. **large $\nu-\bar{\nu}$ asymmetries**

In the presence of large $\nu-\bar{\nu}$ asymmetries ($L \sim 10^{-2}$) sterile production strongly suppressed. Mass bound can be evaded

*Mirizzi, N.S., Miele, Serpico 2012
Saviano et al., 2013
Hannestad, Tamborra and Tram 2012
Chu & Cirelli, 2006
Di Bari et al, 2001*

2. **“secret” interactions for sterile neutrinos**

3. **low reheating scenario**

sterile abundance depends on reheating temperature

*Hannestad et al., 2013,
Dasgupta and Kopp 2013,
Bringmann et al., 2013
Archidiacono et al., 2014
Saviano et al., 2014
Mirizzi, Mangano, Pisanti, N.S.*

*Gelmini, Palomarez-Ruiz, Pascoli, 2004
Yaguna 2007*

- *Modification of cosmological models*

Inflationary Freedom

Shape of primordial power spectrum of scalar perturbations different from the usual power-law

Gariazzo, Giunti Laveder, 2015

Possible solutions...?

- *Different mechanisms to suppress the ν_s abundance:*

1. **large $\nu-\bar{\nu}$ asymmetries**

In the presence of large $\nu-\bar{\nu}$ asymmetries ($L \sim 10^{-2}$) sterile production strongly suppressed. Mass bound can be evaded

2. **“secret” interactions for sterile neutrinos**

3. **low reheating scenario**

sterile abundance depends on reheating temperature

- *Modification of cosmological models*

Inflationary Freedom

Shape of primordial power spectrum of scalar perturbations different from the usual power-law

Secret interactions for sterile ν_s

Hannestad, Hansen & Tram, 2013

4-fermion point-like interaction:
new secret self-interactions among
sterile ν mediated by a massive
gauge boson X : $M_X \ll M_W$



*Suppress the thermalization of
sterile neutrinos
(Effective ν_a - ν_s mixing reduced by a large
matter term)*

$$\nu_s - \nu_s \text{ interaction strength } G_X = \frac{\sqrt{2}}{8} \frac{g_X^2}{M_X^2} \quad \text{for } T \ll M_X$$

Secret interactions for sterile ν_s

Hannestad, Hansen & Tram, 2013

4-fermion point-like interaction:
new secret self-interactions among
sterile ν mediated by a massive
gauge boson X : $M_X \ll M_W$



*Suppress the thermalization of
sterile neutrinos*
(Effective ν_a - ν_s mixing reduced by a large
matter term)

$$\nu_s - \nu_s \text{ interaction strength } G_X = \frac{\sqrt{2}}{8} \frac{g_X^2}{M_X^2} \quad \text{for } T \ll M_X$$

 Only for sterile sector... \longrightarrow *secret interactions apparently unconstrained...*

Caveat: can also generate **MSW-like resonant flavor conversions and collisional induced conversions** among active and sterile neutrinos, enhancing their production



consequences on cosmological bounds at low temperature

Secret interactions for sterile ν_s

Hannestad, Hansen & Tram, 2013

4-fermion point-like interaction:
new secret self-interactions among
sterile ν mediated by a massive
gauge boson X : $M_X \ll M_W$



*Suppress the thermalization of
sterile neutrinos*
(Effective ν_a - ν_s mixing reduced by a large
matter term)

$$\nu_s - \nu_s \text{ interaction strength } G_X = \frac{\sqrt{2}}{8} \frac{g_X^2}{M_X^2} \quad \text{for } T \ll M_X$$

 Only for sterile sector... \longrightarrow *secret interactions apparently unconstrained...*

Caveat: can also generate **MSW-like resonant flavor conversions and collisional induced conversions** among active and sterile neutrinos, enhancing their production



consequences on cosmological bounds at low temperature

 If the new mediator interaction X also couples to Dark Matter \longrightarrow
 \longrightarrow possible attenuation of some of the small scale structure problems
(“missing satellites” problem...)

see Archidiacono's talk

Secret interactions for sterile ν_s

Hannestad, Hansen & Tram, 2013

4-fermion point-like interaction:
new secret self-interactions among
sterile ν mediated by a massive
gauge boson X : $M_X \ll M_W$



*Suppress the thermalization of
sterile neutrinos*
(Effective ν_a - ν_s mixing reduced by a large
matter term)

$$\nu_s - \nu_s \text{ interaction strength } G_X = \frac{\sqrt{2}}{8} \frac{g_X^2}{M_X^2} \quad \text{for } T \ll M_X$$

for pseudo-scalar model see Archidiacono's talk

Evolution equation:

$$i \frac{d\rho}{dt} = [\Omega, \rho] + C[\rho]$$

$$\Omega = \Omega_{\text{vac}} + \Omega_{\text{mat}} + \Omega_{\nu-\nu} + \Omega_{\nu_s-\nu_s}^{\text{secr}}$$

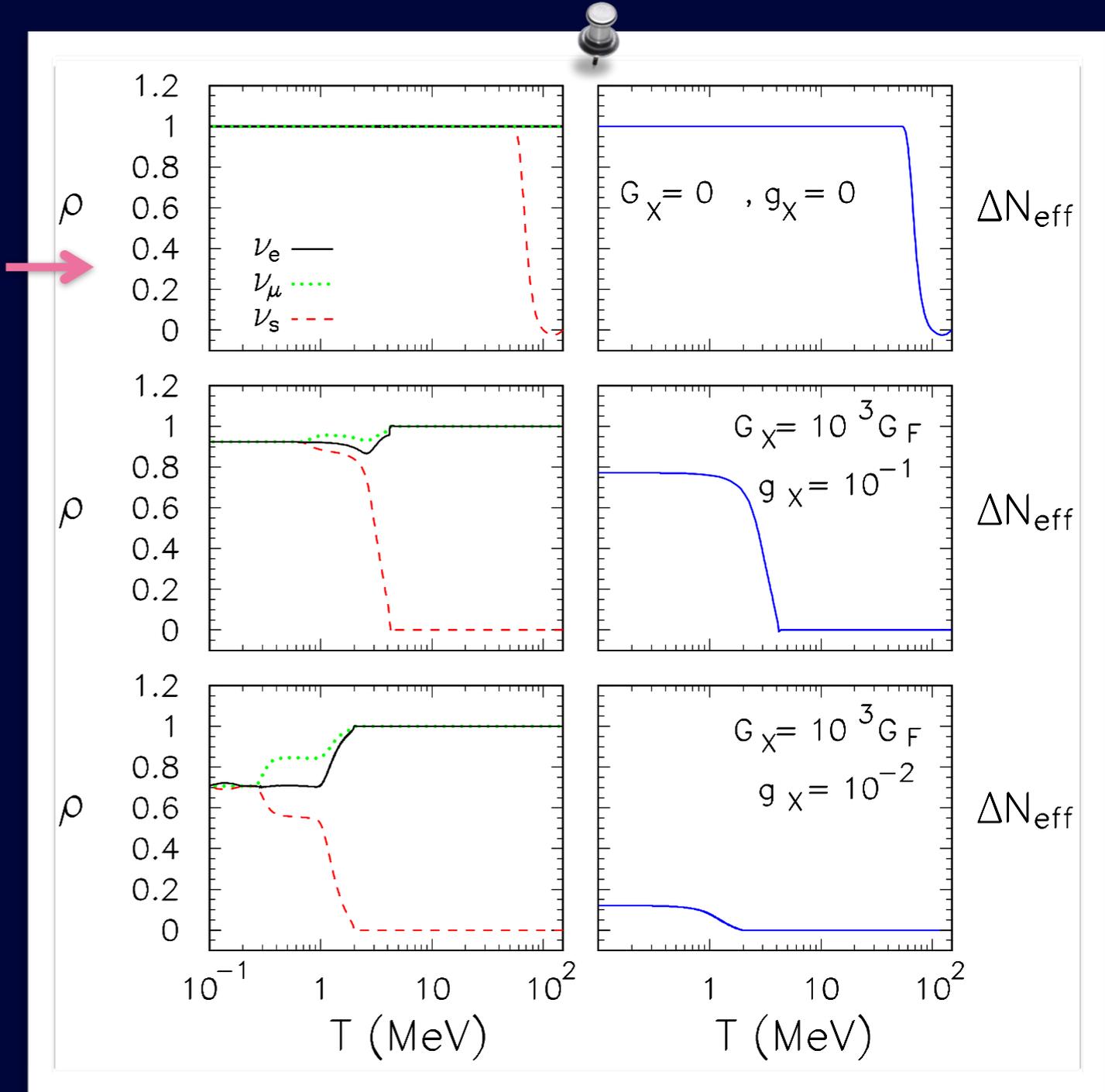
$\swarrow \propto G_F$ $\swarrow \propto G_X$

$$C = C_{\text{SM}} + C_{\text{secr}}$$

$\downarrow \propto G_F^2$ $\swarrow \propto G_X^2$

Sterile production by secret interactions

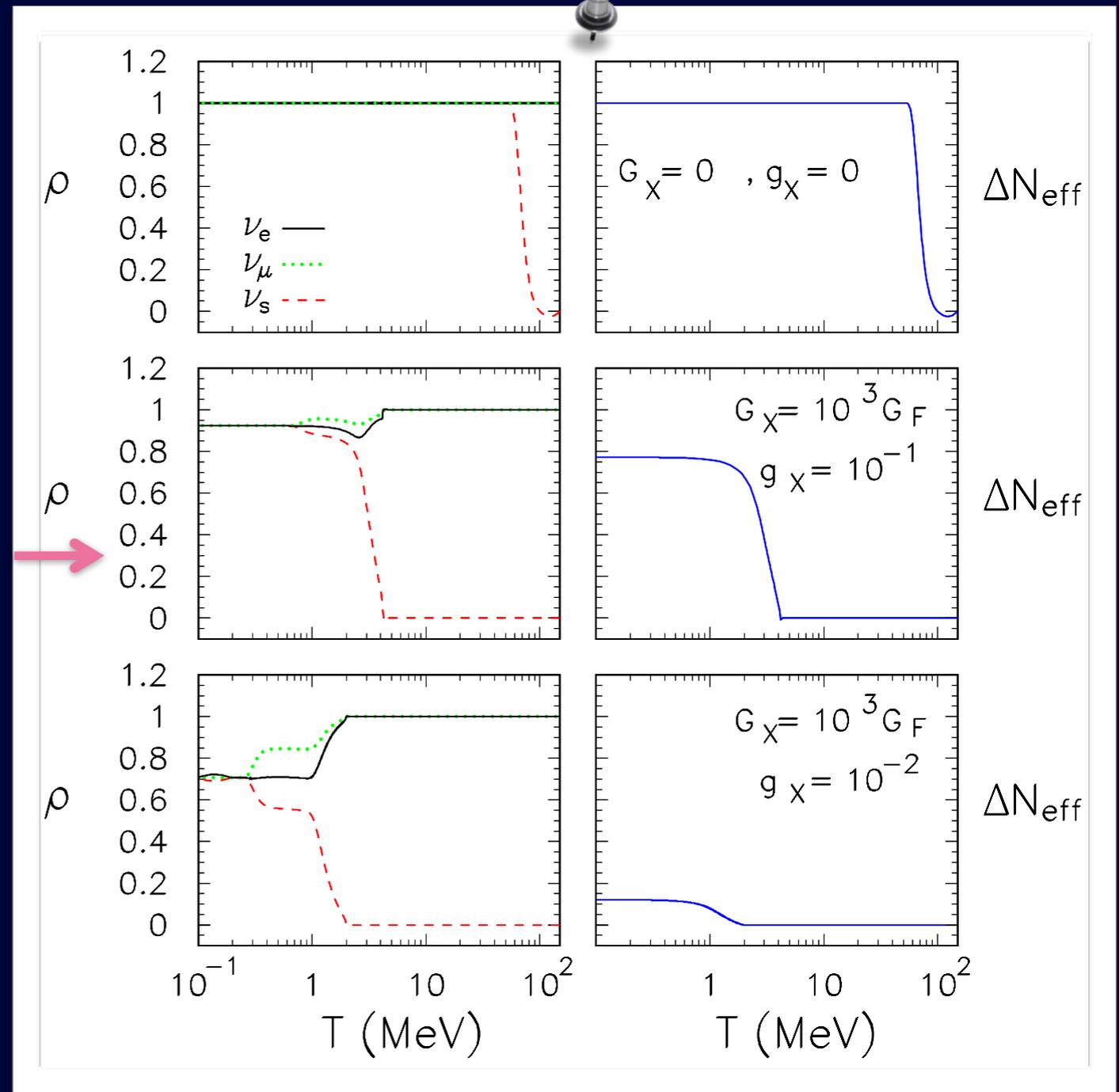
Standard case: as expected the sterile are copiously produced and thermalize



Saviano, Pisanti, Mangano, Mirizzi 2014, ArXiv: 1409.1680

Sterile production by secret interactions

Secret interactions: shift of the conversions at lower T. Flavor equilibrium induced by the collisional term



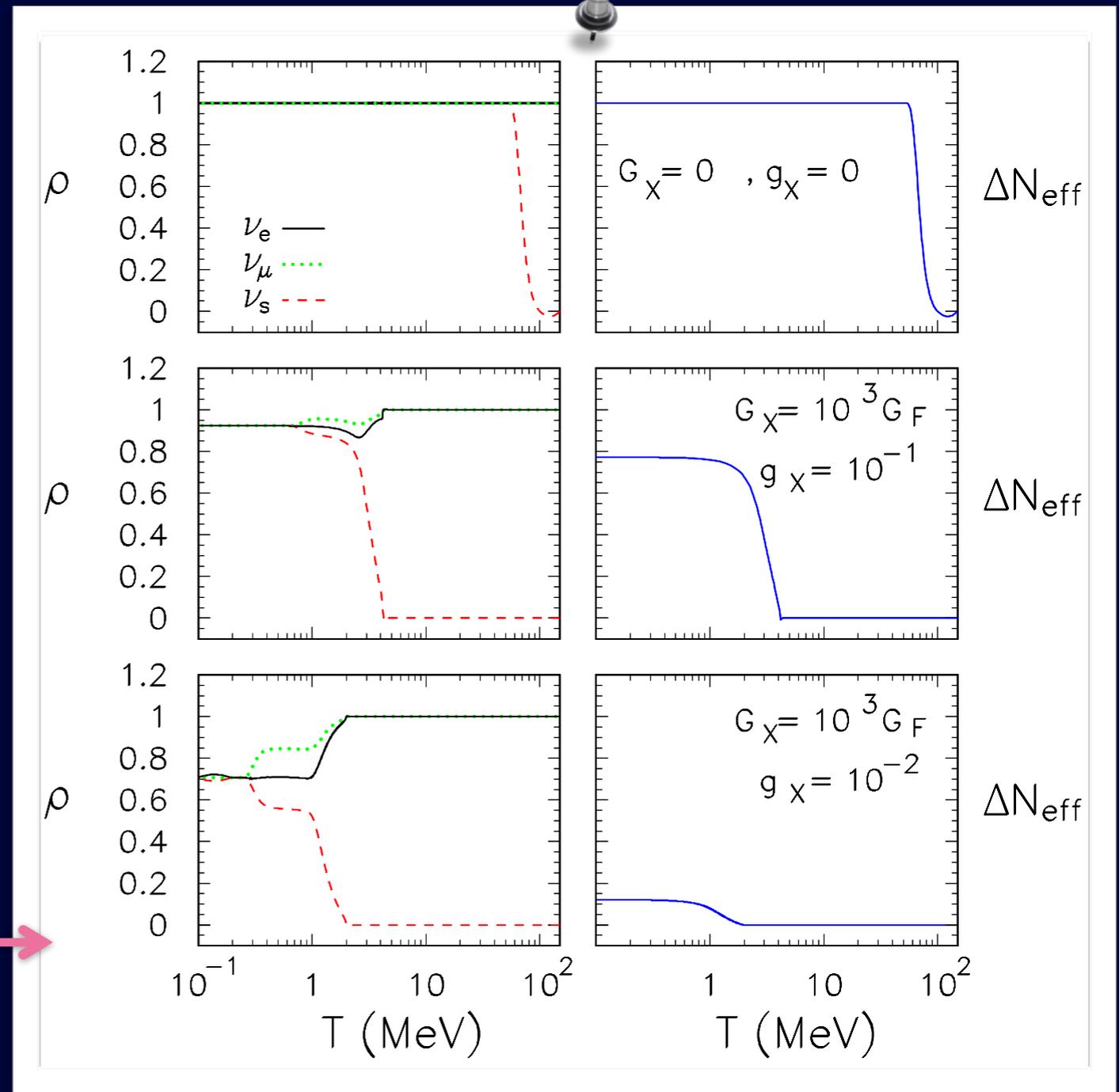
Saviano, Pisanti, Mangano, Mirizzi 2014, ArXiv: 1409.1680

Sterile production by secret interactions

Secret interactions: conversions around 1 MeV, sterile ν partially suppressed, flavor equilibrium.

Note that also ν_e and ν_μ are depleted: crucial for N_{eff} (strongly reduced) but also for BBN

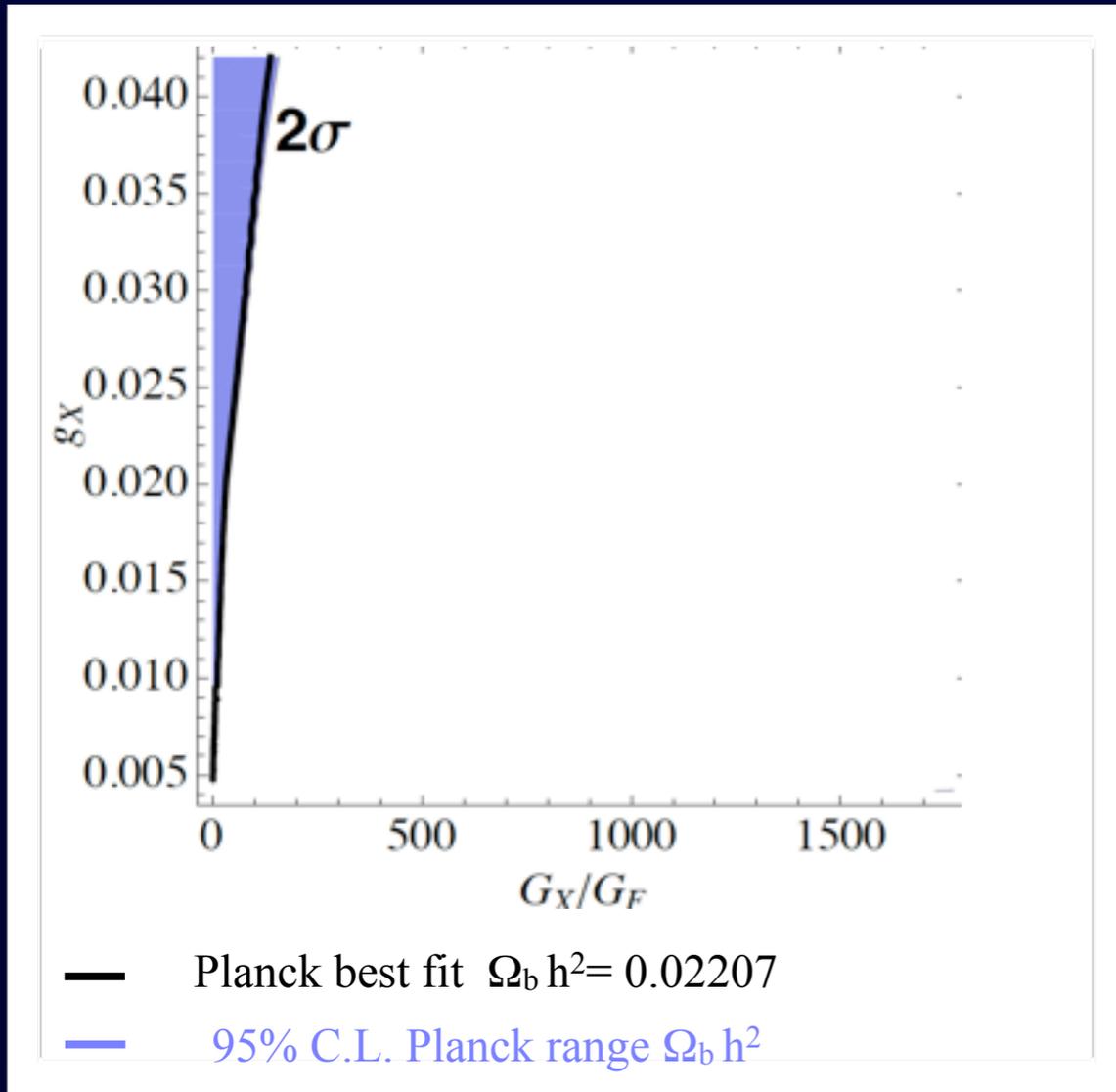
$$\rho_{ee} = 0.7, \quad \Delta N_{\text{eff}} = 0.18$$



Saviano, Pisanti, Mangano, Mirizzi 2014, ArXiv: 1409.1680

BBN constraints

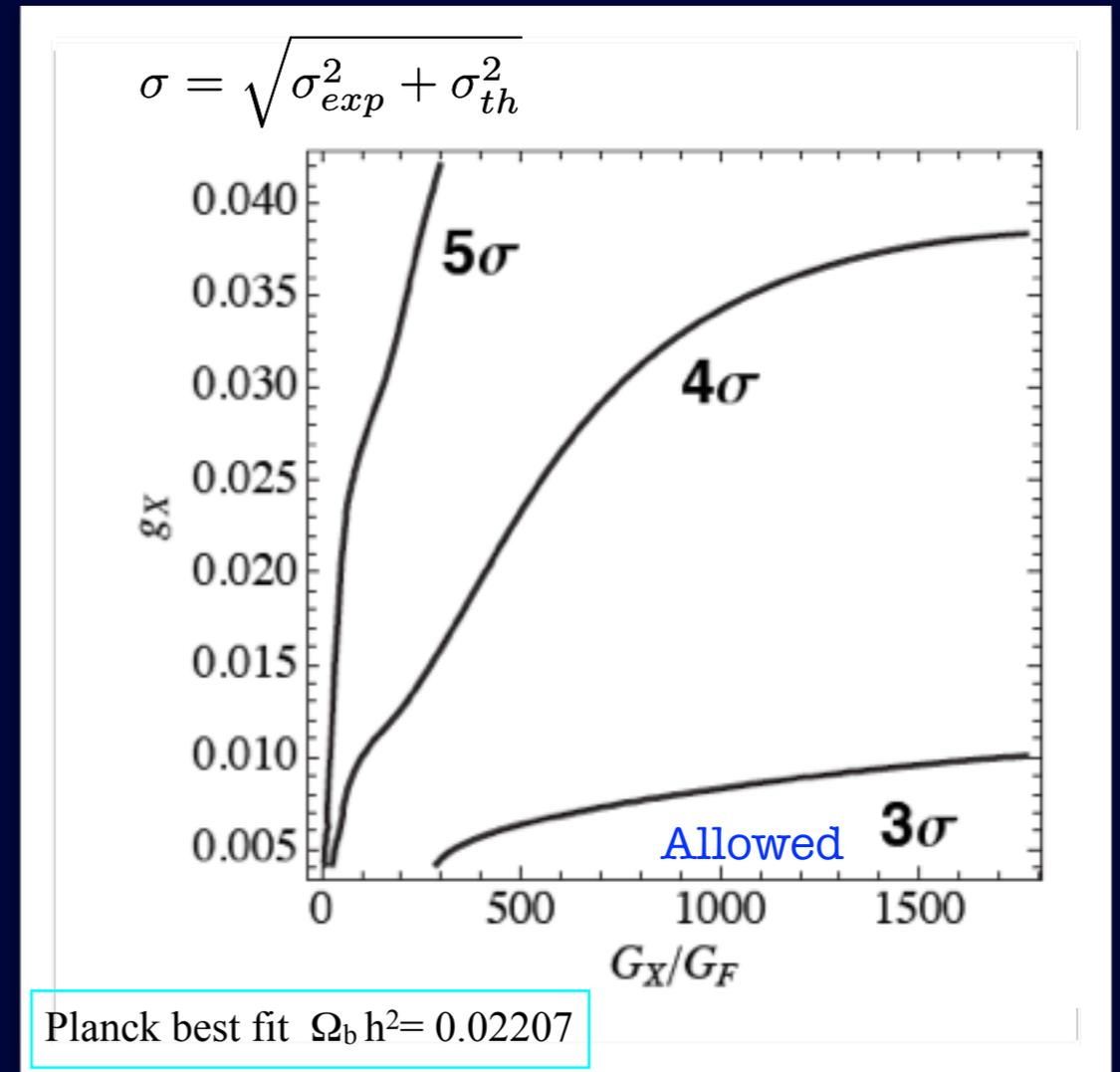
^4He yield



D yield

Experimental reference value: $^2\text{H}/\text{H} = (2.53 \pm 0.04) \times 10^{-5}$
 $\underbrace{\hspace{10em}}_{\sigma_{\text{exp}}}$

Uncertainty on the reaction $d(p, \gamma)^3\text{He} \rightarrow \sigma_{\text{th}} = 0.062 \times 10^{-5}$



Experimental reference value: $Y_p = 0.2551 \pm 0.0022$

Saviano, Pisanti, Mangano, Mirizzi 2014, ArXiv: 1409.1680

PARthENoPE code
 Pisanti et al, 2012

Most of the parameter space excluded at 3σ $M_X \geq 40 \text{ MeV}$

Mass constrains

lower $M_X \leftrightarrow$ very large $G_X (> 10^5 G_F)$ \rightarrow very strong secret collisional term leading to a quick flavor equilibrium

$$\text{Scatterig rate: } \Gamma_X \simeq G_X^2 T_\nu^5 \frac{p}{\langle p \rangle} \frac{n_s}{n_a}$$

The flavour evolution (scattering-induced decoherent production) leads to a large population of sterile states Stodolsky, 1987

$$\begin{aligned} (\rho_{ee}, \rho_{\mu\mu}, \rho_{\tau\tau}, \rho_{ss})_{\text{initial}} &\rightarrow (\rho_{ee}, \rho_{\mu\mu}, \rho_{\tau\tau}, \rho_{ss})_{\text{final}} \\ (1, 1, 1, 0) &\quad (3/4, 3/4, 3/4, 3/4) \end{aligned}$$

Mirizzi, Mangano, Pisanti Saviano, 2014, ArXiv:1410.1385

Impact on the mass bound:

$$m_{\text{st}}^{\text{eff}} = \rho_{ss} \sqrt{\Delta m_{\text{st}}^2} = \frac{3}{4} \sqrt{\Delta m_{\text{st}}^2} \rightarrow \text{the laboratory lower value in the } 2\sigma \text{ range gives } m_{\text{st}}^{\text{eff}} \sim 0.8 \text{ eV}$$

$$m_{\text{st}}^{\text{eff}} \sim 0.8$$

BUT... the less stringent cosmological bounds on sterile mass give 0.7 eV

Secret interaction scenario: disfavored $M_X \geq 0.1 \text{ MeV}$

Conclusions

- eV sterile ν *incompatible* with cosmological bounds:
too heavy for structure formation
- possible but not guaranteed reconciliation via suppression of sterile abundance:

Conclusions

- eV sterile ν *incompatible* with cosmological bounds:
too heavy for structure formation
- possible but not guaranteed reconciliation via suppression of sterile abundance:
 - *Secret interactions among ν_s :*
 - Very large $M_X \rightarrow$ thermalization of $\nu_s \leftrightarrow$ secret interactions do not have effect
 - $400 \text{ MeV} > M_X > 0.1 \text{ MeV} \rightarrow$ mechanism strongly disfavoured by BBN bounds and by sterile mass bounds

Conclusions

- eV sterile ν *incompatible* with cosmological bounds:
too heavy for structure formation
- possible but not guaranteed reconciliation via suppression of sterile abundance:
 - *Secret interactions among ν_s :*
 - Very large $M_X \rightarrow$ thermalization of $\nu_s \leftrightarrow$ secret interactions do not have effect
 - $400 \text{ MeV} > M_X > 0.1 \text{ MeV} \rightarrow$ mechanism strongly disfavoured by BBN bounds and by sterile mass bounds
 - $M_X < 0.1 \text{ MeV} \rightarrow$ unconstrained at the moment: ν_s still coupled at CMB and LSS epochs \rightarrow no free-streaming

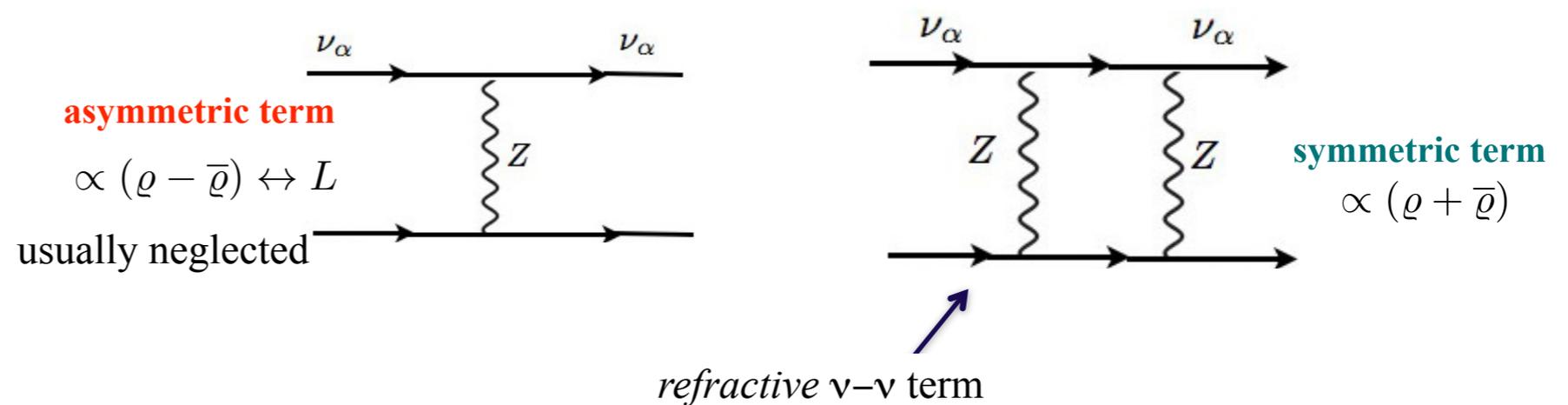
Present cosmological mass bound obtained considering free-streaming ν
 \rightarrow an appropriated analysis should be performed for 4-fermion model

Conclusions

- eV sterile ν *incompatible* with cosmological bounds:
too heavy for structure formation
 - possible but not guaranteed reconciliation via suppression of sterile abundance:
 - **Secret interactions among ν_s :**
 - Very large $M_X \rightarrow$ thermalization of $\nu_s \leftrightarrow$ secret interactions do not have effect
 - $400 \text{ MeV} > M_X > 0.1 \text{ MeV} \rightarrow$ mechanism strongly disfavoured by BBN bounds and by sterile mass bounds
 - $M_X < 0.1 \text{ MeV} \rightarrow$ unconstrained at the moment: ν_s still coupled at CMB and LSS epochs \rightarrow no free-streaming
- Present cosmological mass bound obtained considering free-streaming ν
 \rightarrow an appropriated analysis should be performed for 4-fermion model
- relevant also for small scale DM problems: the game is still open**

Thank you!

Equations of motion



self-interactions of ν with the ν background:
 off-diagonal potentials \Rightarrow **non-linear EoM**

Vacuum term
 with M neutrino mass matrix
 $U M^2 U^\dagger$

$$\Omega = \frac{M^2}{2p} + \sqrt{2} G_F \left[-\frac{8p}{3} \left(\frac{E_\ell}{M_W^2} + \frac{E_\nu}{M_Z^2} \right) \right] + \sqrt{2} G_X \left[-\frac{8p E_s}{3M_X^2} \right]$$

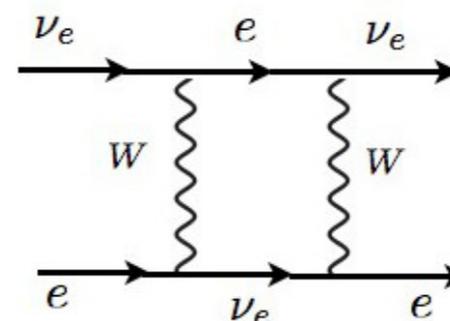
MSW effect with background medium (*refractive effect*)

charged lepton asymmetry subleading ($O(10^{-9})$) \rightarrow

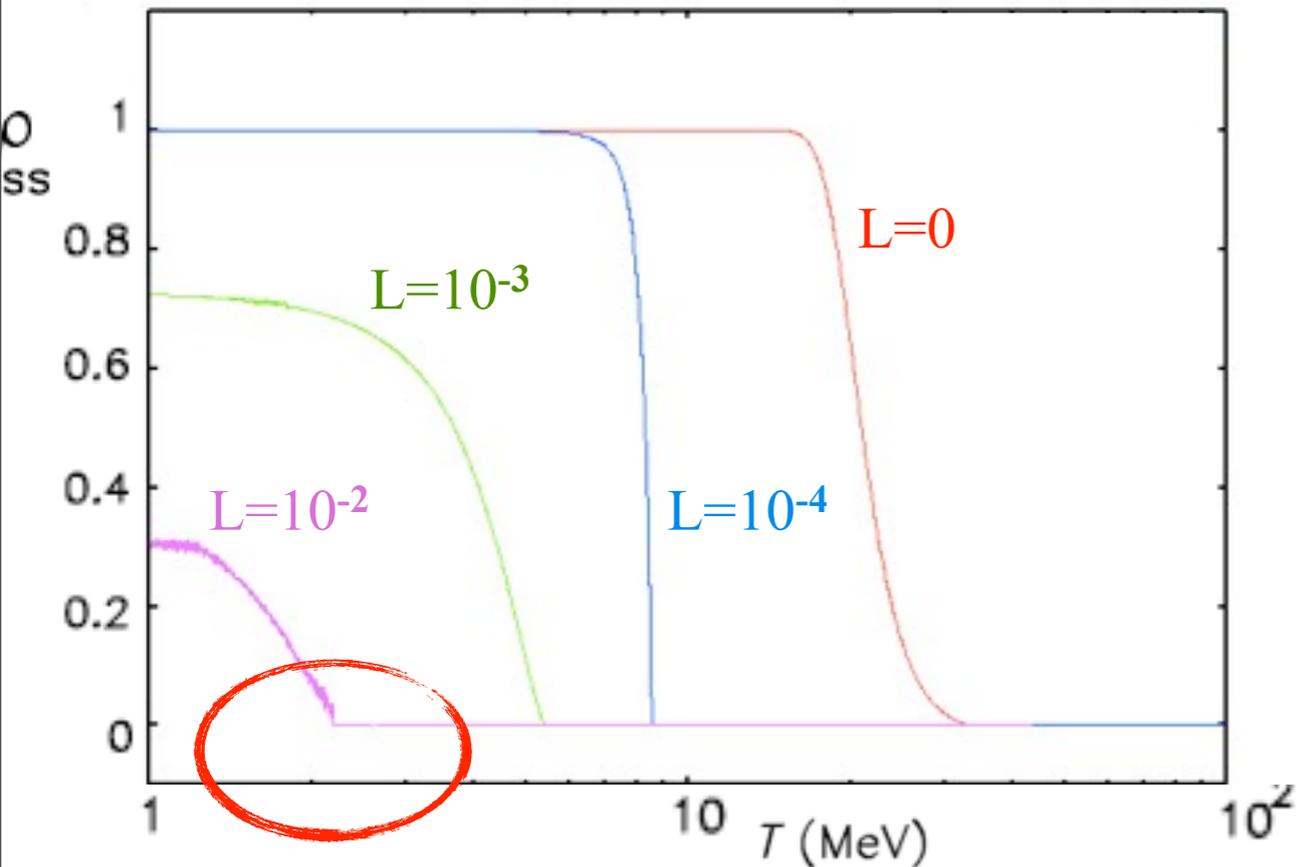
\rightarrow 2th order term: “symmetric” matter effect

sum of $e^- - e^+$ energy densities ϵ

$$E_\ell \equiv \text{diag}(\epsilon_e, 0, 0, 0)$$

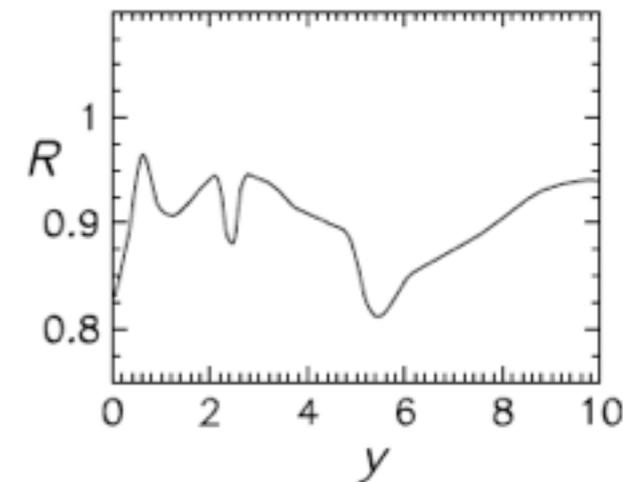
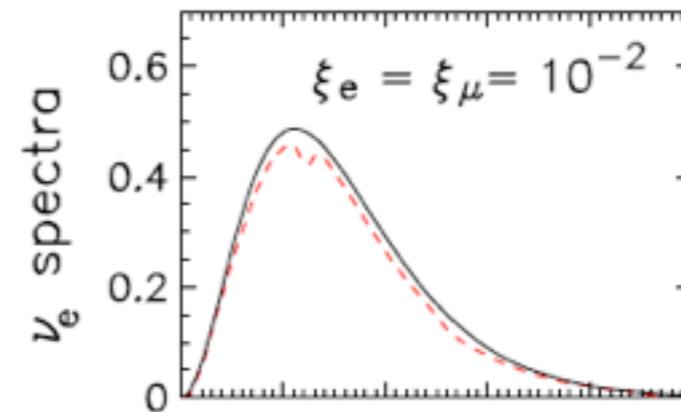


Sterile production by neutrino asymmetry



Very large asymmetries are necessary to suppress the sterile neutrino abundances leading to *non trivial consequences on BBN*

conversions occur at $T \sim T_\nu$ decoupling
 \Rightarrow active not repopulated anymore by collisions ($\rho_{ee} < 1$)

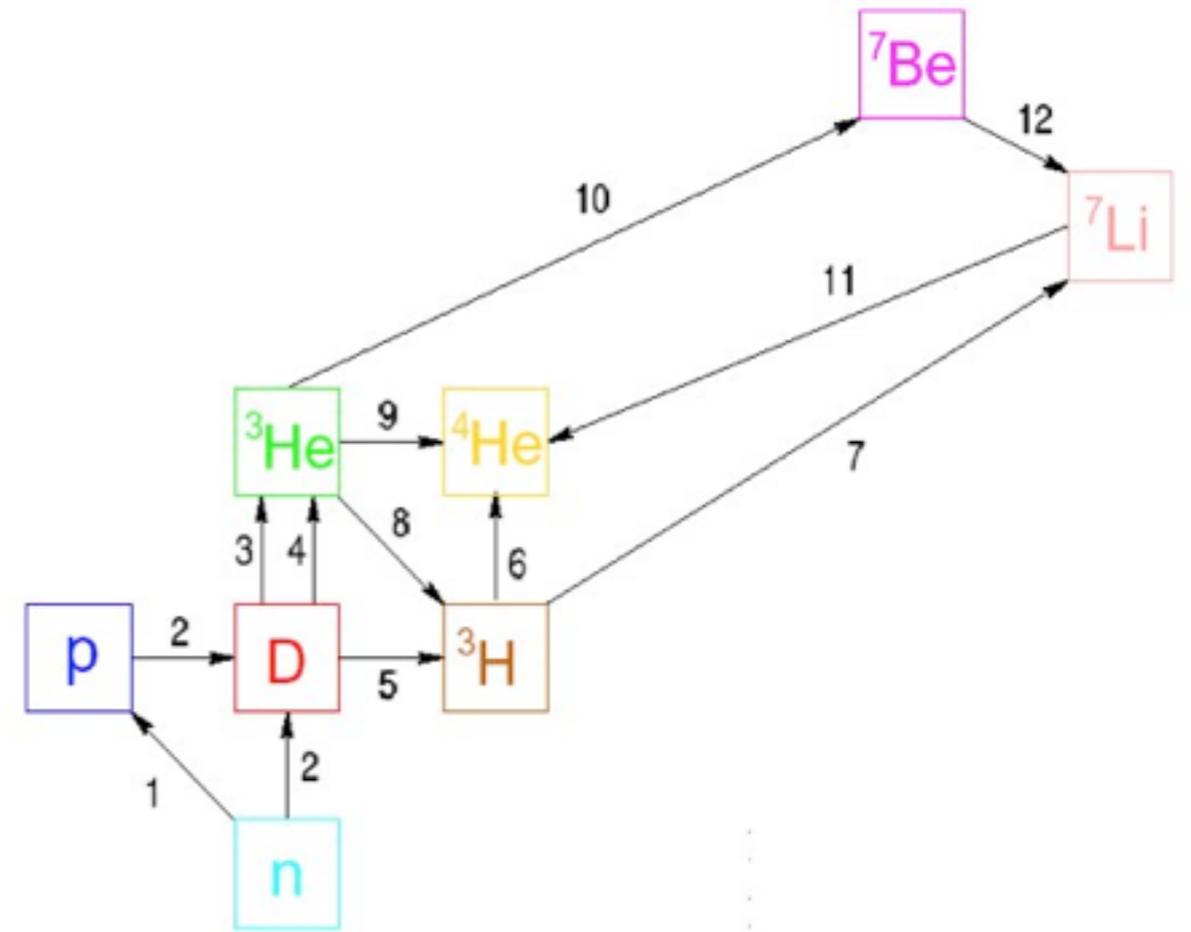
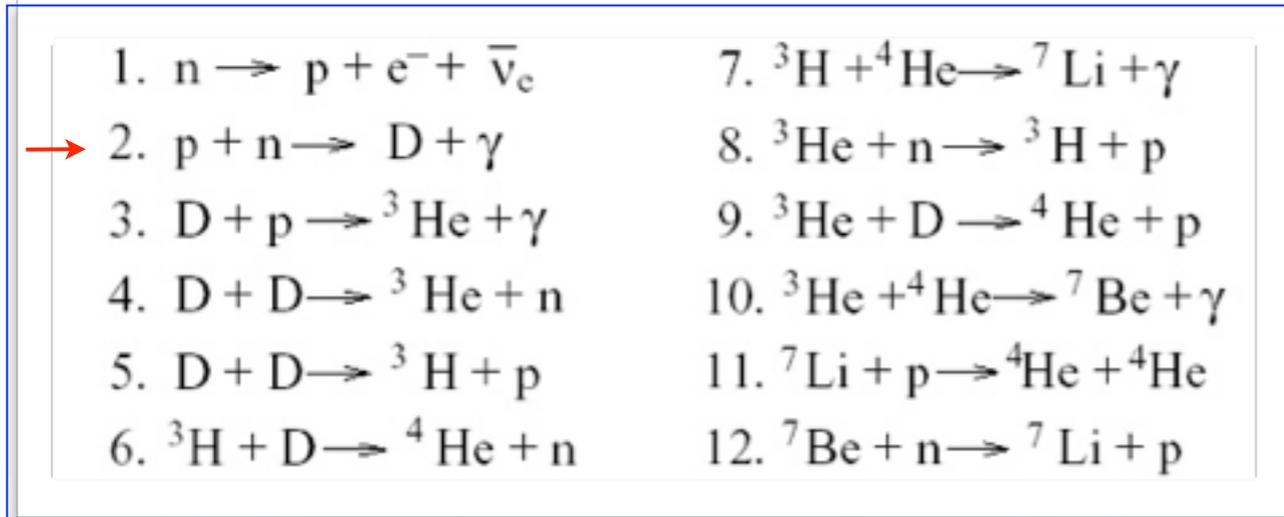


$$L_\alpha \simeq 0.68 \xi_\alpha \left(\frac{T_\nu}{T_\gamma} \right)^3$$

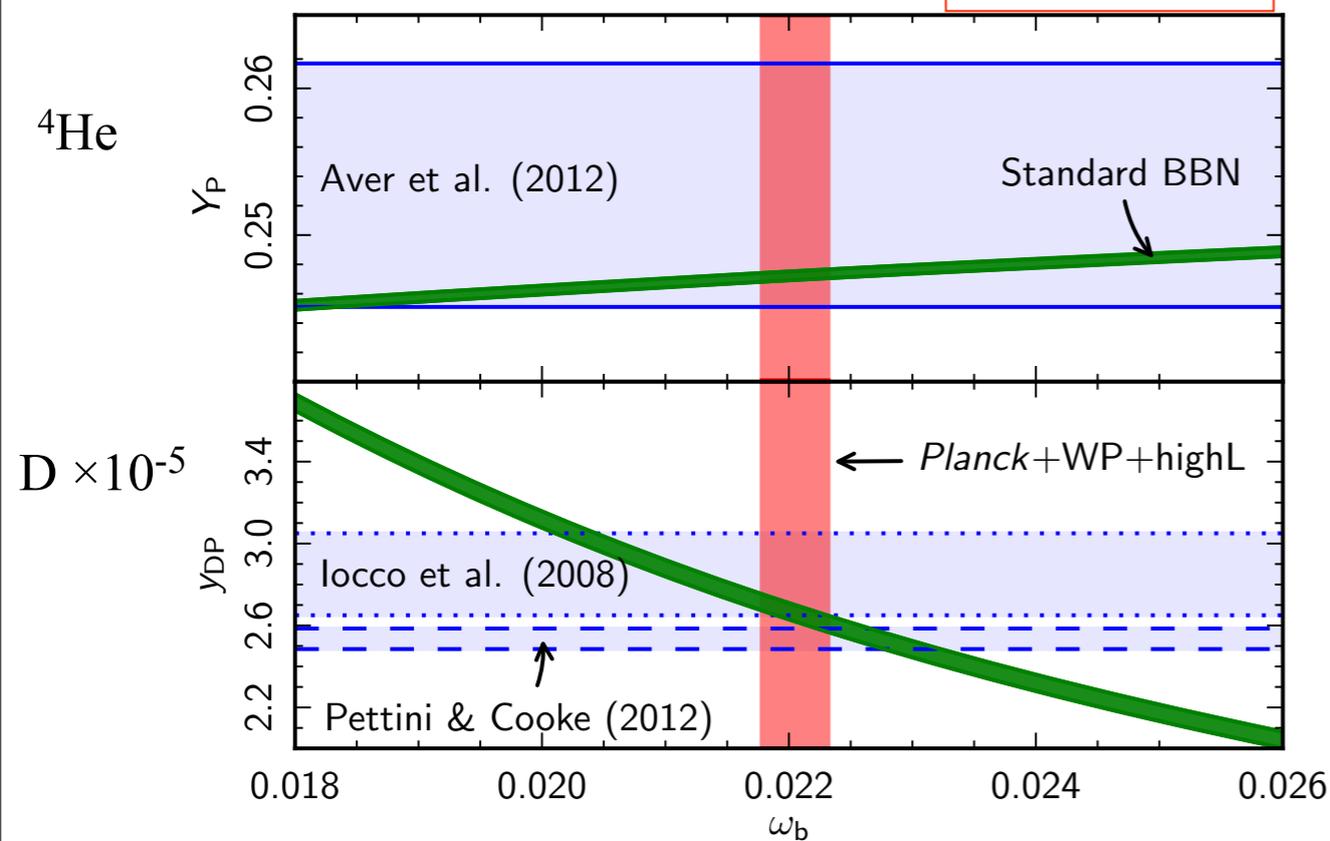
Big Bang Nucleosynthesis

* 0.1-0.01 MeV

Formation of light nuclei starting from D



Planck XVI, 2013



Prediction for ${}^4\text{He}$ and D in a **standard** BBN obtained by Planck collaboration using **PARthENoPE**

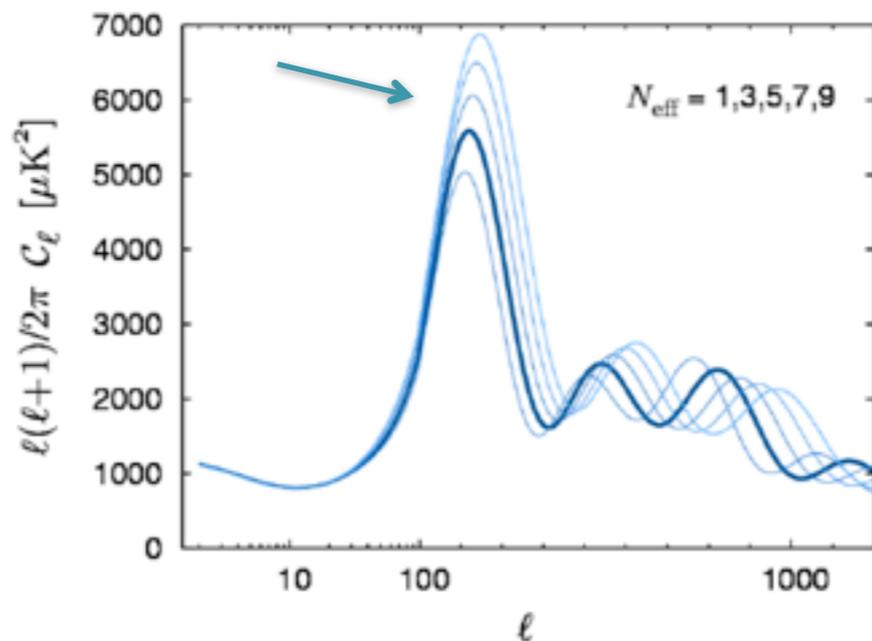
Blue regions: primordial yields from measurements performed in different astrophysical environments

$$\omega_b = 0.02207 \pm 0.00027$$

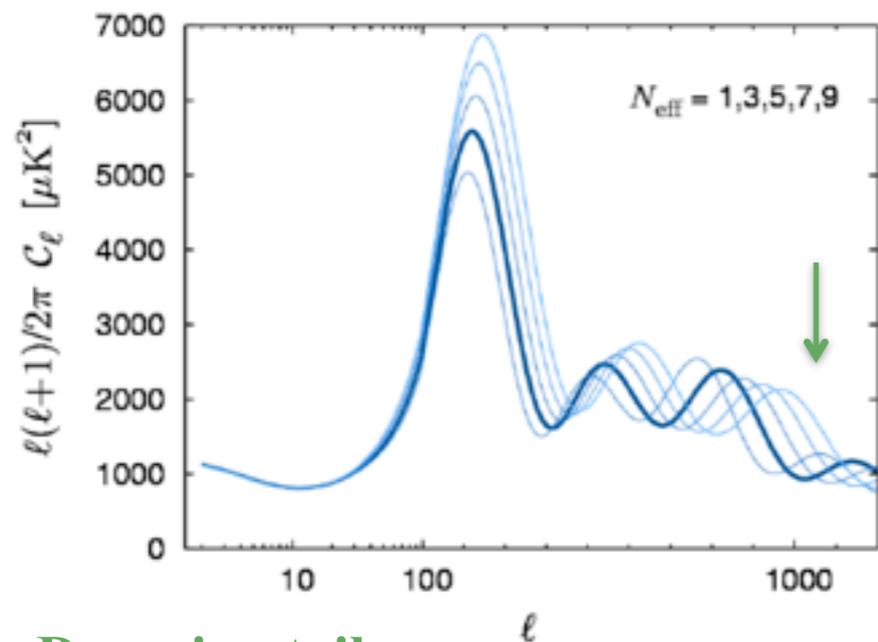
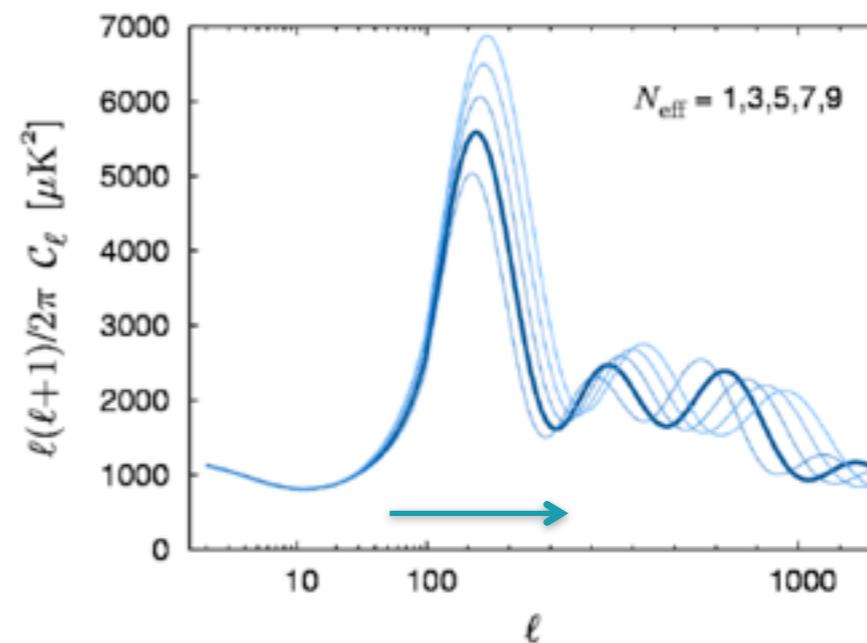
Impact on CMB

Matter-radiation equality

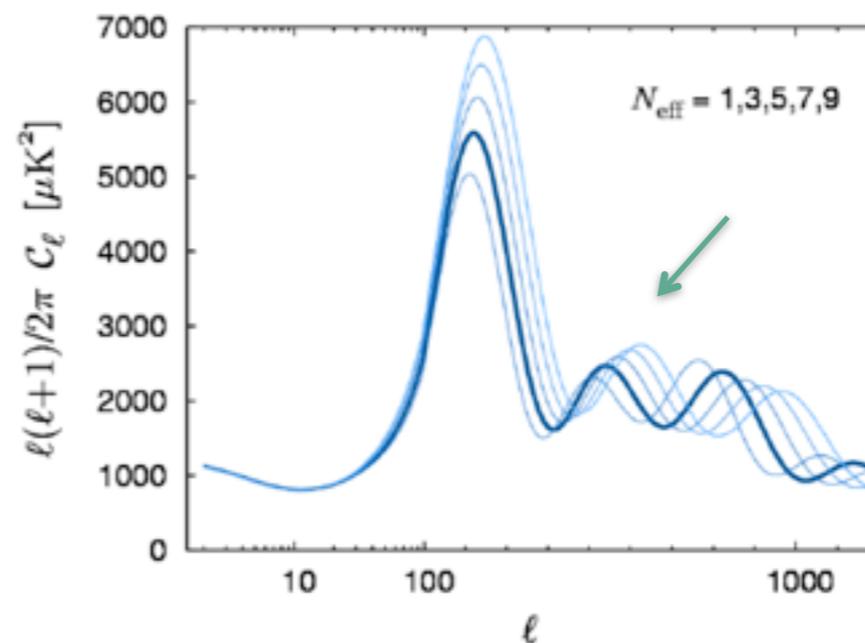
degenerate with Ω_m



Sound horizon/angular positions of the peaks degenerate with H_0 and Ω_m



Damping tail degenerate with Y_p

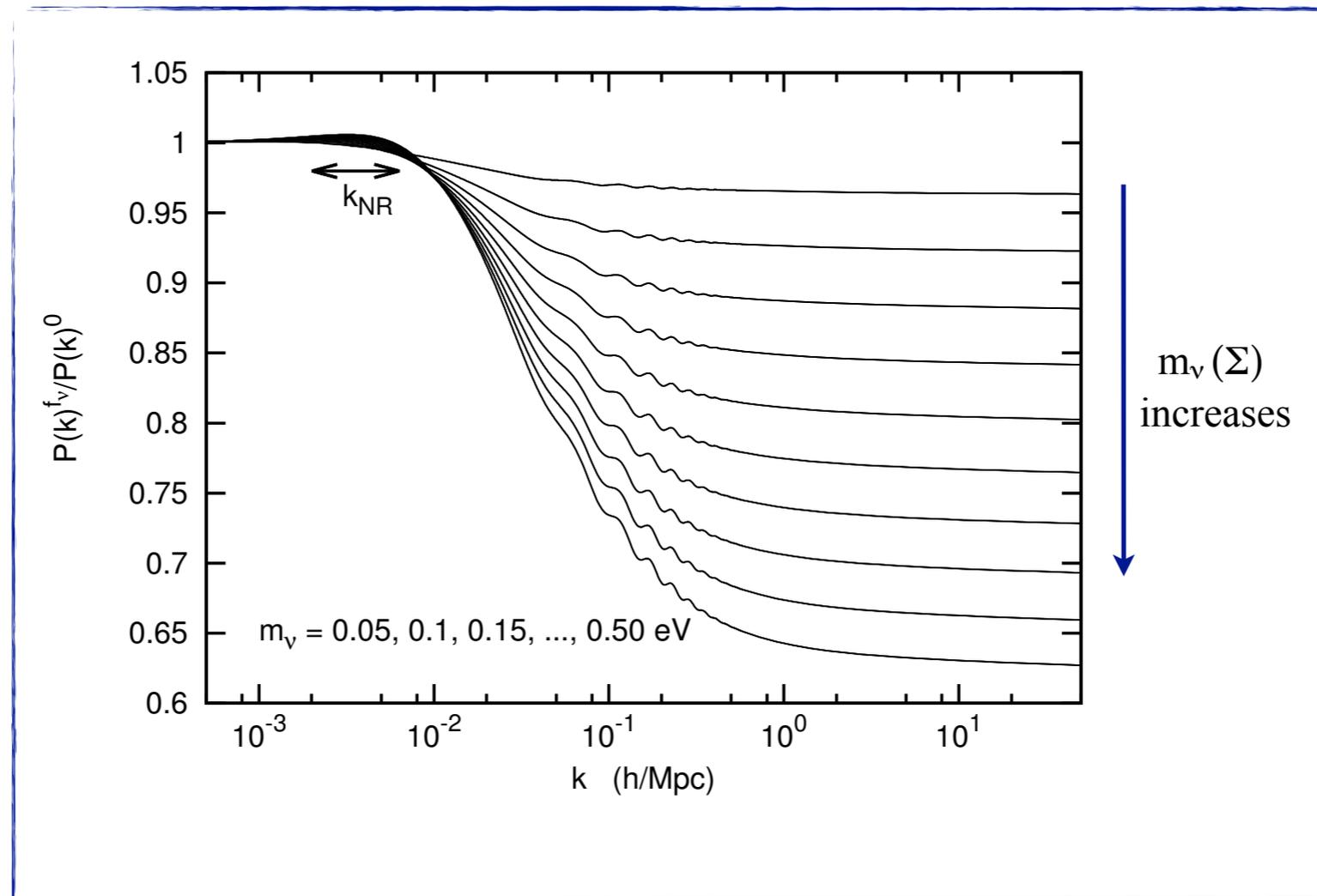


Anisotropic stress (partially) degenerate with A_s and n_s

Impact on the LSS

The small-scale matter power spectrum $P(k > k_{\text{NR}})$ is reduced in presence of massive ν :

- ✓ free-streaming neutrinos do not cluster
- ✓ slower growth rate of CDM (baryon) perturbations

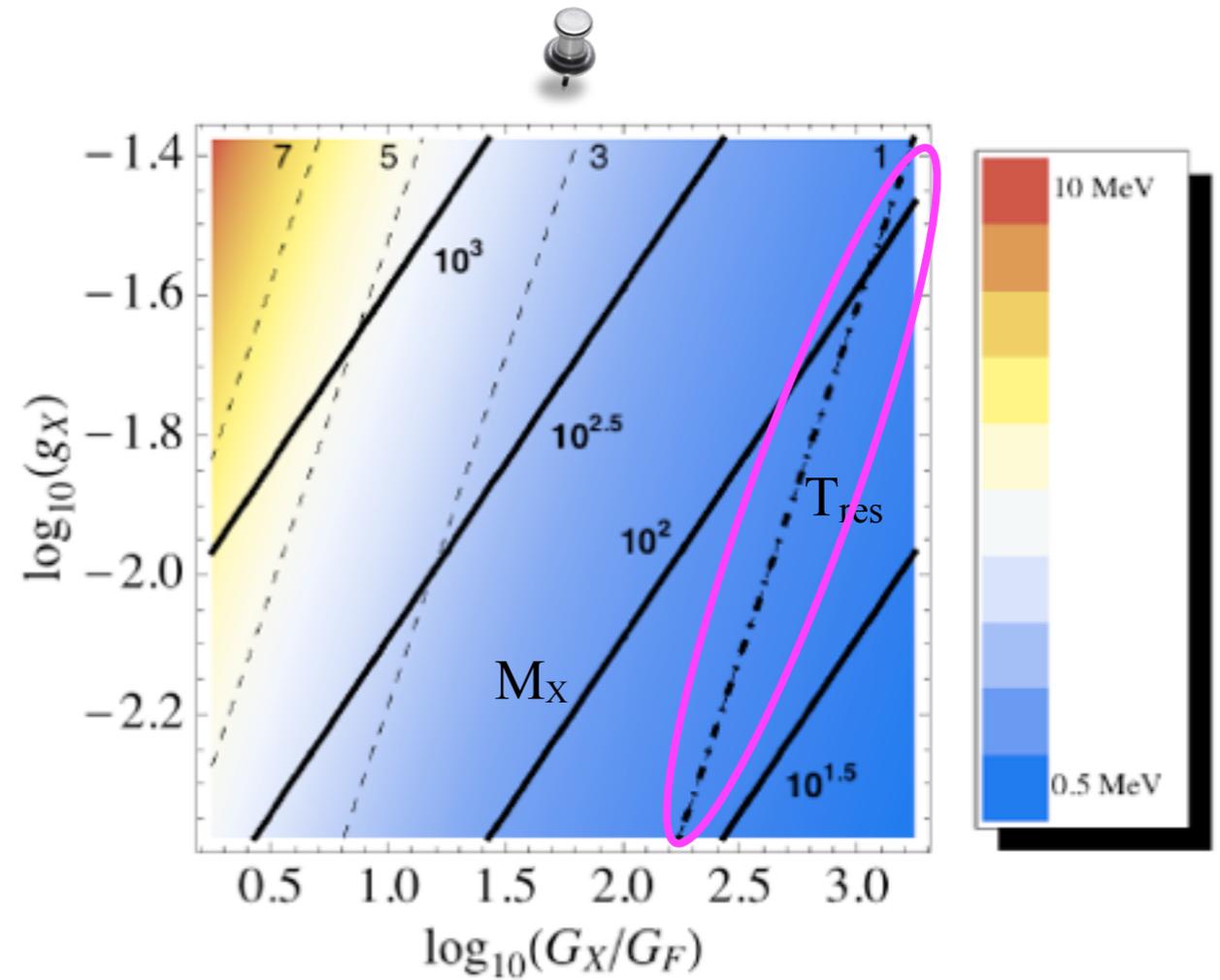
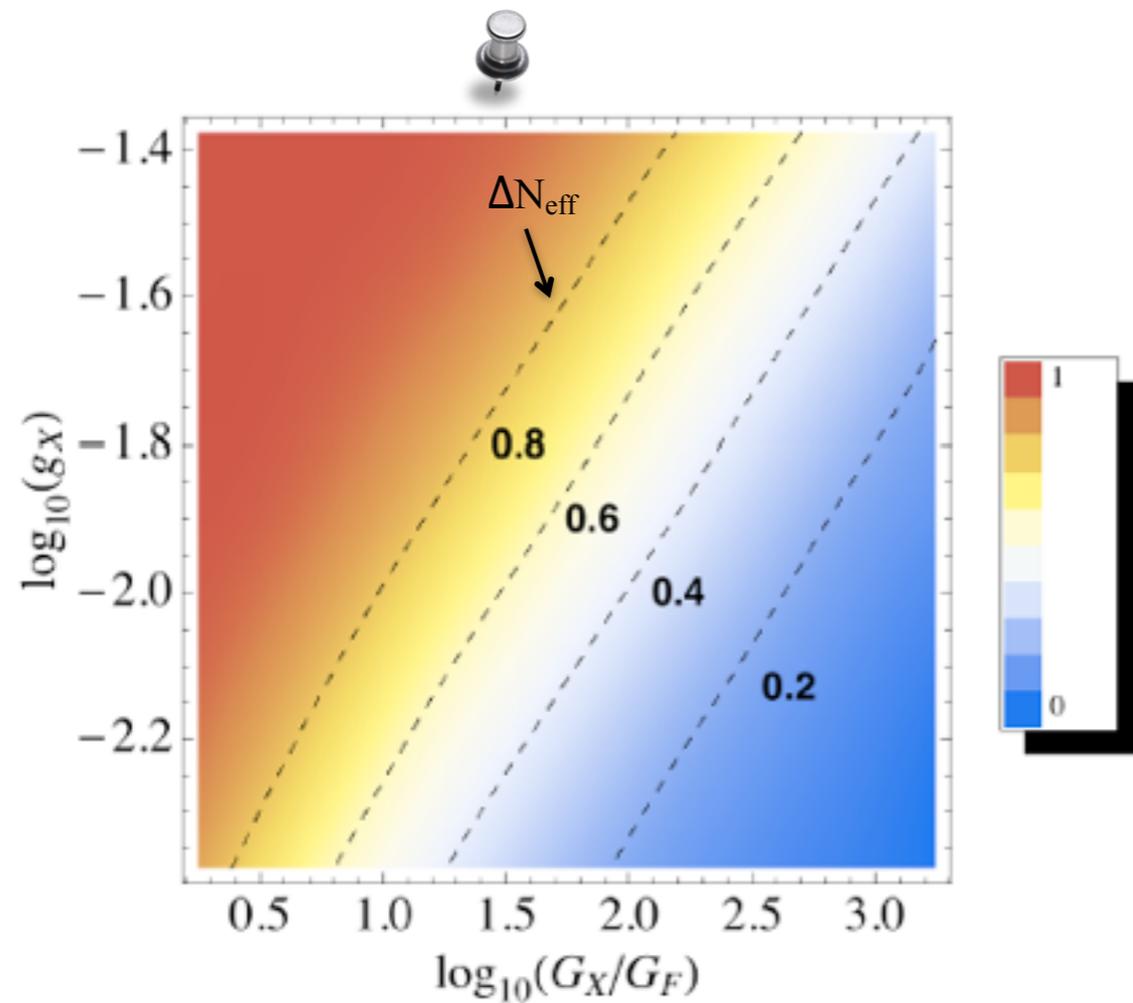


$$f_\nu \equiv \frac{\rho_\nu}{(\rho_{\text{cdm}} + \rho_{\text{b}} + \rho_\nu)} = \frac{\Omega_\nu}{\Omega_{\text{m}}}$$

$$\Delta P(k)/P(k) \simeq -8f_\nu$$

Secret interactions and BBN

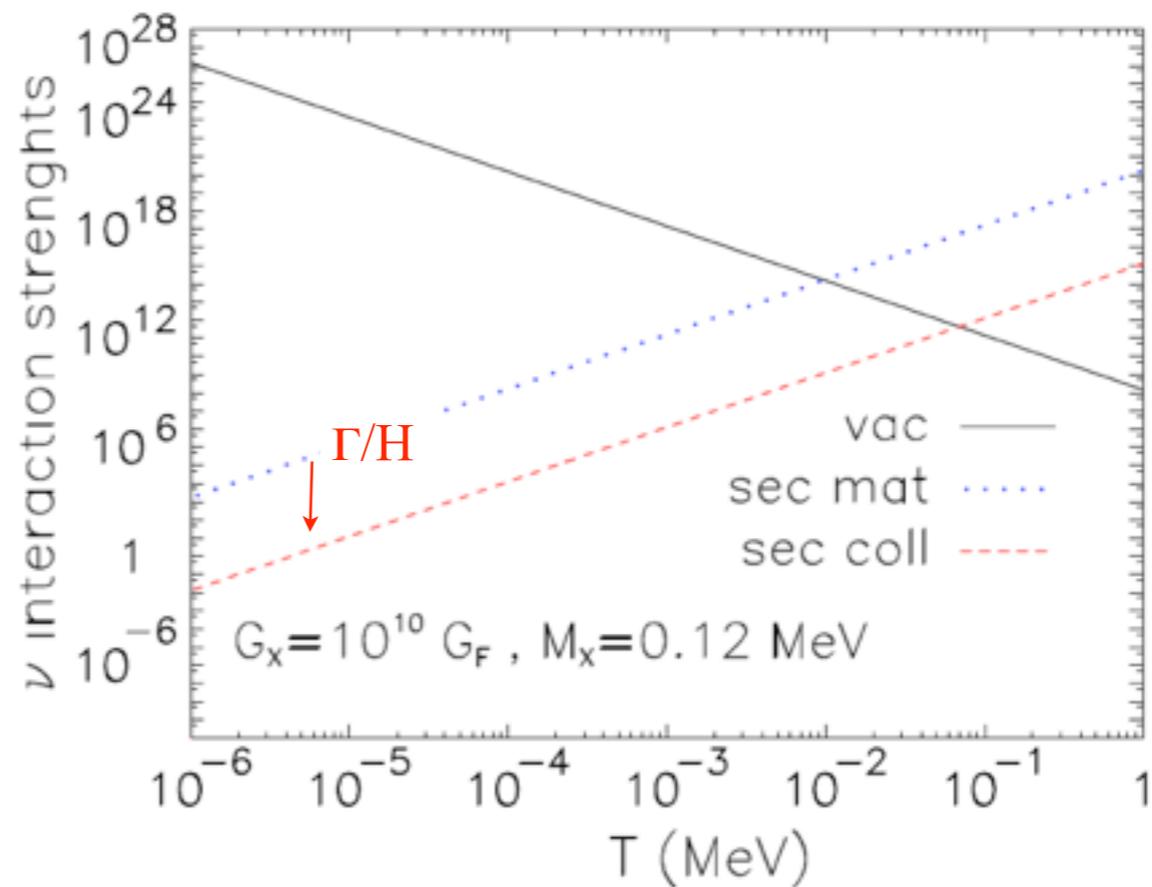
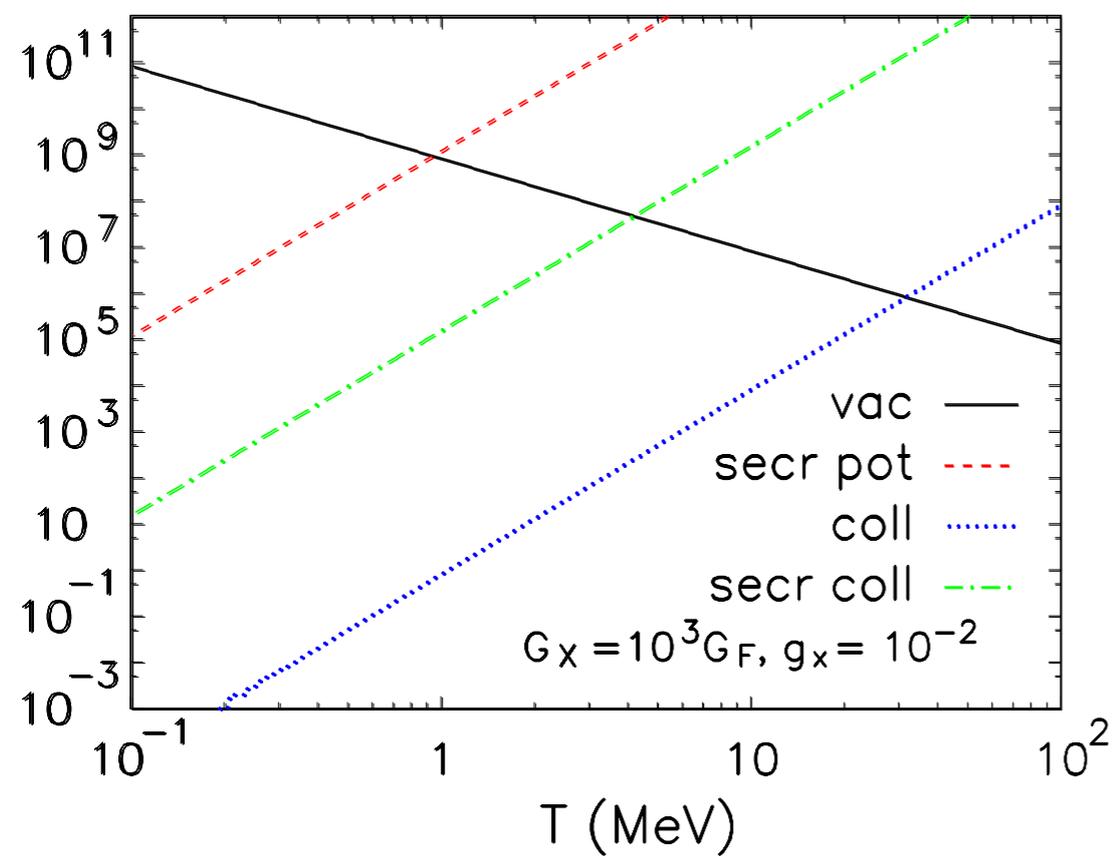
Asymptotic values of ΔN_{eff} versus G_X and g_X



Resonance temperature in the plane (G_X, g_X)

Dashed curves: constant T_{res} contours

Solid curves: constant M_X contours



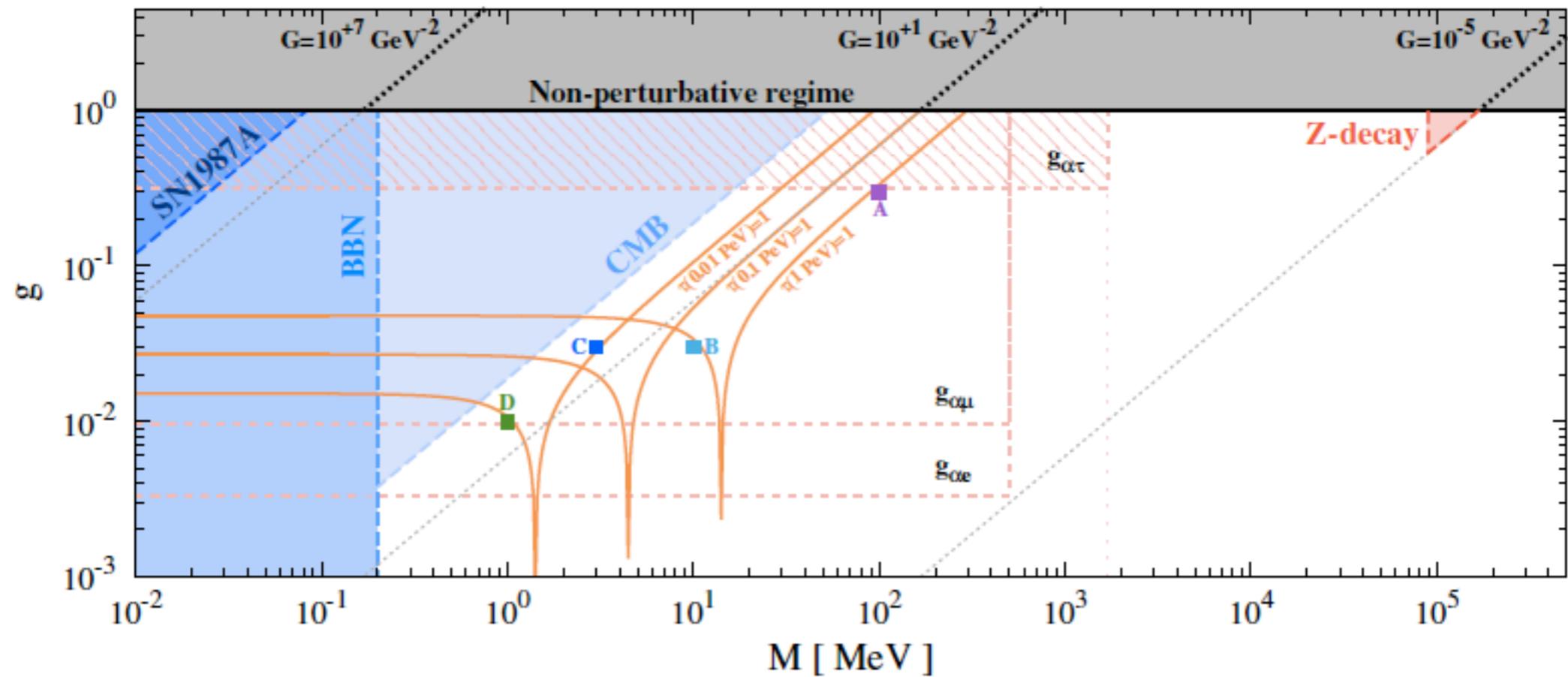


FIG. 1. Present constraints and future sensitivity to ν SI in terms of neutrino coupling, g , and mediator mass, M , with diagonal dotted contours shown for values of the dimensionful coupling G . The blue shaded regions are excluded by astrophysical and cosmological considerations based on SN 1987A [6], BBN [34], and the CMB [35, 36]. The pink dashed lines indicate flavor-dependent limits based on laboratory measurements of meson and lepton decays [37]; we consider only the weakest limit, for ν_τ , to be robustly excluded for all flavors, and it is shaded. The red shaded region is excluded based on measurement of Z-boson decay [9]. The gray shaded region indicates the non-perturbative regime. The orange lines are contours of unit optical depth for different initial neutrino energies (Eq. 10), indicating the approximate boundary of the parameter space above which IceCube is sensitive to ν SI. The squares represent the example parameters (given in Table I) used in our calculations.