



# Double Parton Scattering @ LHC

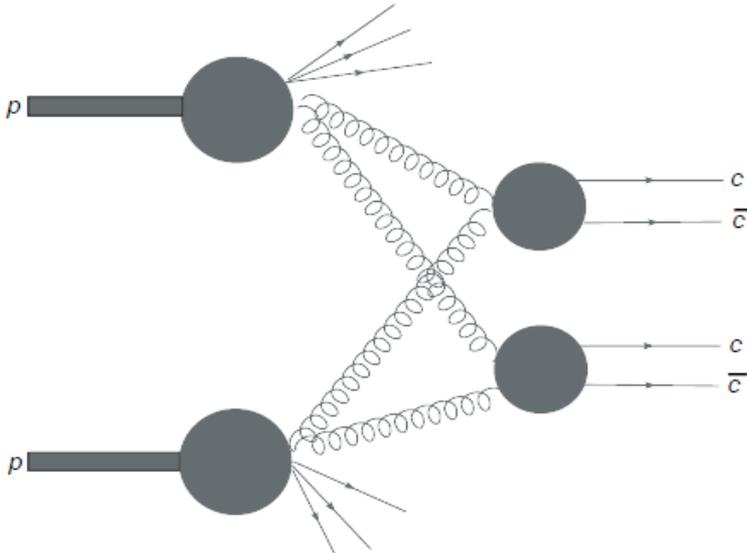
*(ATLAS, CMS & LHCb)*

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# DPS: simple paradigm



Two independent hard scattering processes  
 Relations through (unknown) *double* PDF

$$\Gamma_{ij}(x_1, x_2; b_1, b_2; Q_1^2, Q_2^2) = D_h^{ij}(x_1, x_2; Q_1^2, Q_2^2) f(b_1) f(b_2),$$

Assume factorization of *double* PDFs

$$D_h^{ij}(x_1, x_2; Q_1^2, Q_2^2) = D_h^i(x_1; Q_1^2) D_h^j(x_2; Q_2^2).$$

(Can't be true for all  $x, Q^2$ )

Easy to make predictions!  
 And the predictions are easy to test

Pocket formula

$$\sigma_{DPS}^{AB} = \frac{m}{2} \frac{\sigma_{SPS}^A \sigma_{SPS}^B}{\sigma_{eff}} \quad m=1,2$$

Universal (energy and process independent) factor)

$$1/\sigma_{eff} = \int d^2b F^2(b)$$

$$\sigma_{eff}^{DPS} = 14.5 \pm 1.7_{-2.3}^{+1.7} \text{ mb}$$

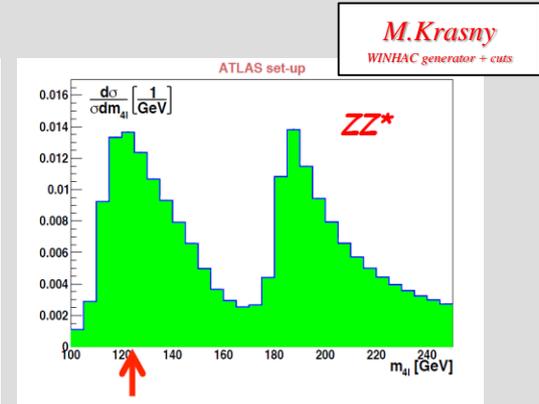
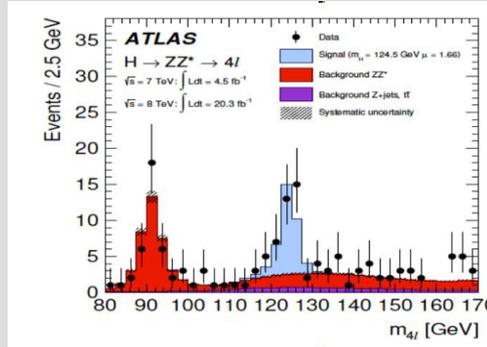
CDF, F.Abe *et al.*, PDR 56 3811 (1997)



# DPS importance



- Can easily mimic crucial signals



- DPS importance grows with energy/gluon density (smaller x)
- Interparton correlations
- First observed long time ago:
  - 4-jets AFS@ISR
  - 3-jets+ $\gamma$  CDF, D0, ...
- @ LHC
  - ATLAS, CMS: 4-jets, W+jets, 2 $\times$ J/ $\psi$ , W+J/ $\psi$ , Z+J/ $\psi$ , ...
  - LHCb: 2 $\times$ J/ $\psi$ , Z+D, double charm, ...

$\sigma_{\text{eff}}$  is important QCD parameter:

Energy independent (?)

Process independent (?)

**TEST IT!**





# How to access DPS: 3 approaches



- ATLAS & CMS: separation via correlations
- DPS: *no correlations* vs SPS: *strong correlations*



- Study correlations, e.g. fit  $\Delta\phi$ 
  - Separate small (DPS) component
- Tune DPS fraction in corresponding generator
  - Model dependence of SPS shapes
  - E.g. initial gluon  $p_T$



# CMS: 4-jets

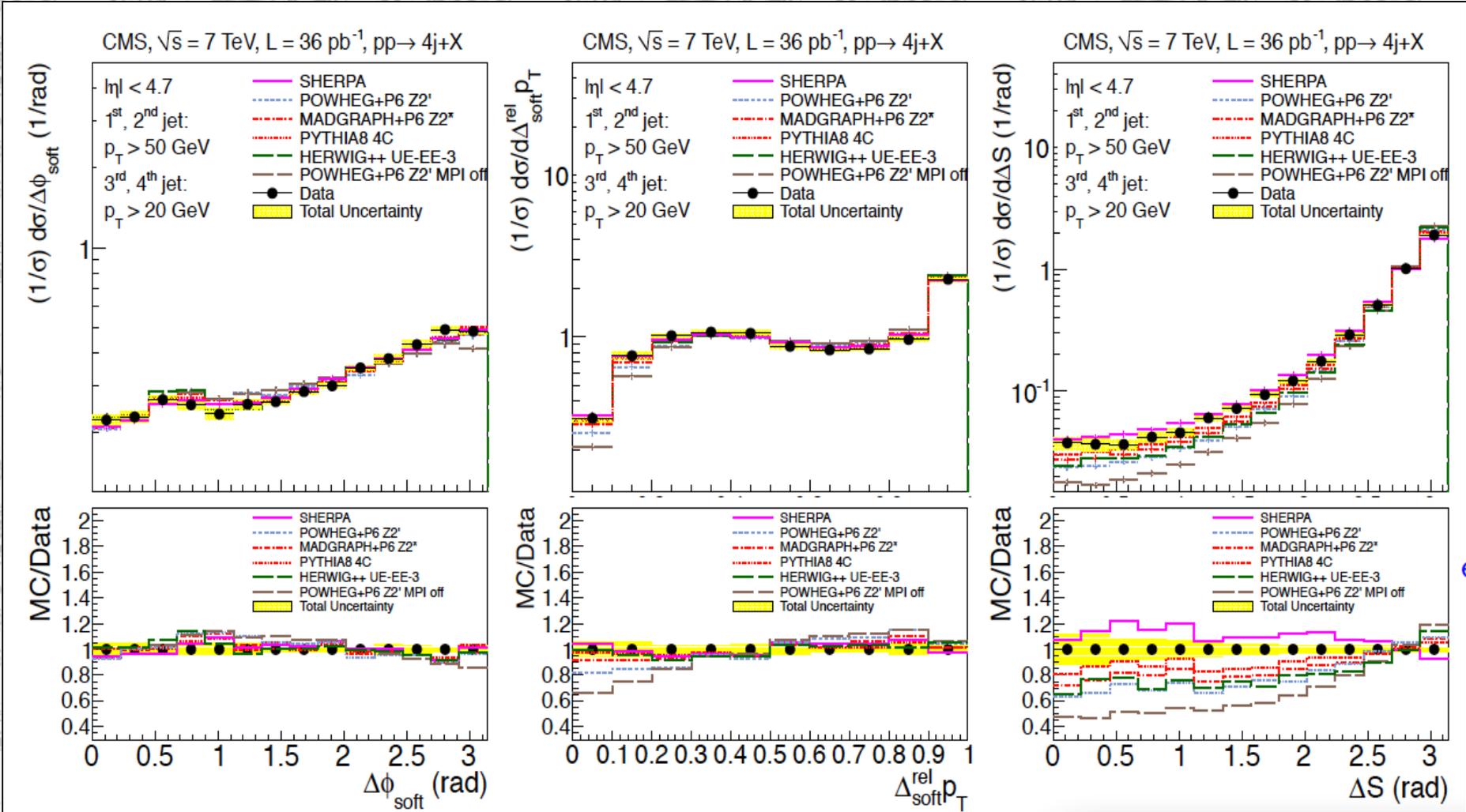
CMS, PRD 89 (2014) 092010



$$\Delta\phi(j_i, j_k) = \phi_i - \phi_k$$

$$\Delta_{\text{soft}}^{\text{rel}} p_T = \frac{|\vec{p}_T(j_i, j_k)|}{|\vec{p}_T(j_i)| + |\vec{p}_T(j_k)|}$$

$$\Delta S = \arccos\left(\frac{\vec{p}_T(j^i, j^k) \cdot \vec{p}_T(j^l, j^m)}{|\vec{p}_T(j^i, j^k)| \cdot |\vec{p}_T(j^l, j^m)|}\right)$$





# CMS: $\sigma_{\text{eff}}$ from 4-jets



- Extracted  $\sigma_{\text{eff}}$  is tune-dependent: 19-30mb

<b>CDPSTP8S1</b>	$21.3^{+1.2}_{-1.6}$
<b>CDPSTP8S1</b>	$19.0^{+4.7}_{-3.0}$
<b>CUETP8S1-CTEQ6L1</b>	$27.8^{+1.2}_{-1.3}$
<b>CUETP8S1-HERAPDF</b>	$29.1^{+2.3}_{-2.0}$

Pythia-8 tunes  
Choice of PDF

- Depends on interplay between soft and hard MPI
- DPS contribution is rather small  $O(\%)$ 
  - DPS templates from data

Other processes?



# W+2jets



ATLAS, NJP 15(2013) 033038

$$\frac{\hat{\sigma}_Y(s) \cdot \hat{\sigma}_Z(s)}{f_{DP}^{(D)} \cdot \hat{\sigma}_{Y+Z}^{(tot)}(s)} \cdot \sigma_{\text{eff}} = \frac{1}{f_{DP}^{(D)}} \cdot \frac{N_{W_{0j}} N_{2j}}{N_{W+2j}} \cdot \frac{\mathcal{L}_{W_{0j}+2j\text{DPI}}}{\mathcal{L}_{W_{0j}} \mathcal{L}_{2j}} \cdot \frac{A_{W_{0j}+2j\text{DPI}}}{A_{W_{0j}} A_{2j}} \cdot \frac{C_{W_{0j}+2j\text{DPI}}}{C_{W_{0j}} C_{2j}} \cdot \frac{\varepsilon_{W_{0j}+2j\text{DPI}}}{\varepsilon_{W_{0j}} \varepsilon_{2j}}$$

$$\sigma_{\text{eff}} = \frac{1}{f_{DP}^{(D)}} \cdot \frac{N_{W_{0j}}}{N_{W+2j}} \cdot \frac{N_{2j}}{\mathcal{L}_{2j}}$$

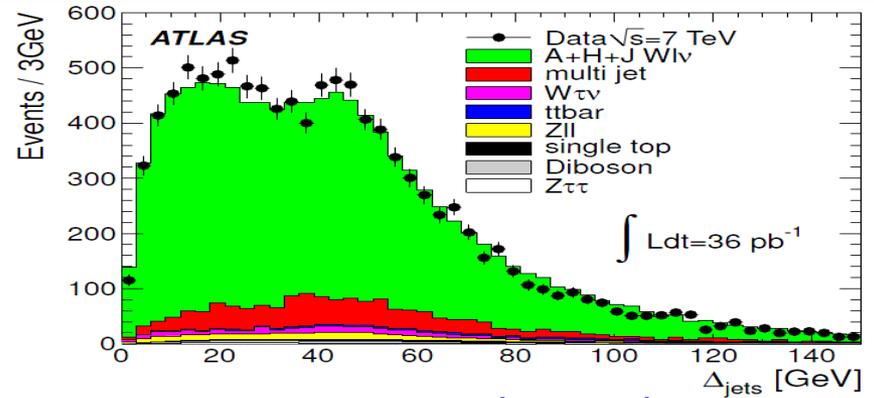
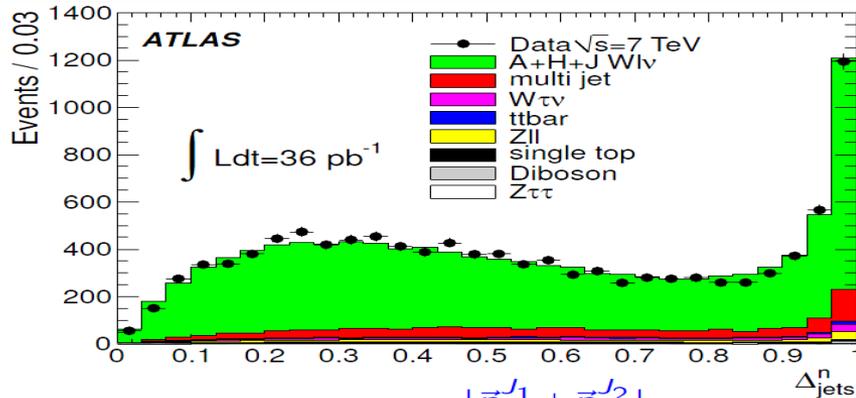
- 3 selections: W+0j, W+2j - selected in similar way
  - $\text{anti-}k_T, p_T(j) > 20 \text{ GeV}$
  - $p_T(l) > 20 \text{ GeV}$  - trigger
  - $E_{T\text{miss}} > 25 \text{ GeV}$
  - $M_T > 40 \text{ GeV}$
- *dijets*- use minimum bias trigger (fully efficient)



# Fraction of DPS

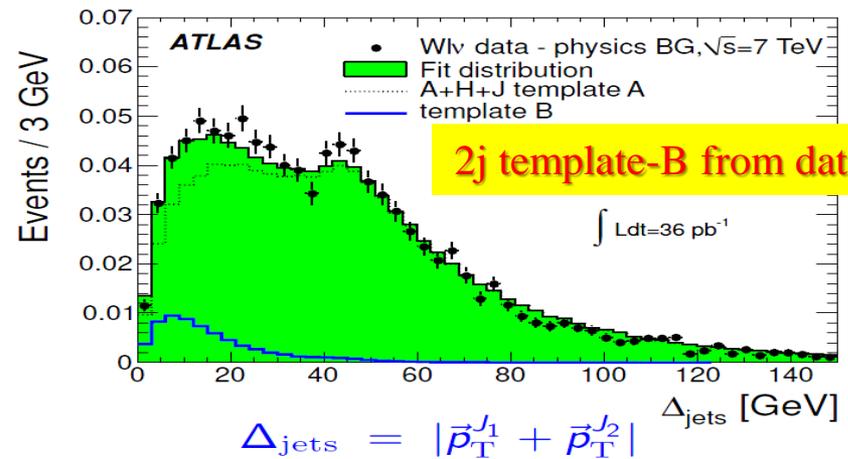
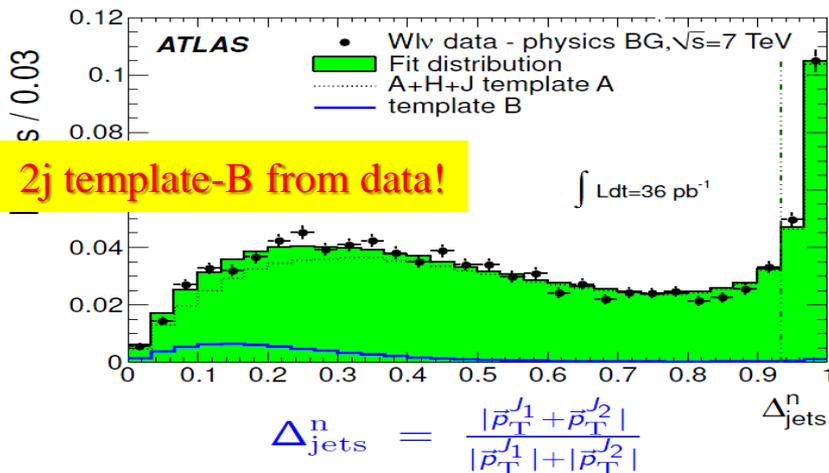


ATLAS, NJP 15(2013) 033038



back-to-back ←  $\Delta_{\text{jets}}^n = \frac{|\vec{p}_T^{J1} + \vec{p}_T^{J2}|}{|\vec{p}_T^{J1}| + |\vec{p}_T^{J2}|}$  → collinear

$\Delta_{\text{jets}} = |\vec{p}_T^{J1} + \vec{p}_T^{J2}|$





# $\sigma_{\text{eff}}$ from $W+2j$



**ATLAS, NJP 15(2013) 033038**

$f_{\text{DP}}$

Systematic source	Unc [%]
Theory	10
Pile-up	13
Jet energy scale	12
Jet energy resolution	8
Background & lepton	11
Total systematic	24
Total statistical	17

$\sigma_{\text{eff}}$

Systematic source	Unc. [%]
$f_{\text{DP}}^{(D)}$	24
Background & lepton response	3
Luminosity	3
Total systematic	+33 -20
Total statistical	17

$$f_{\text{DP}} = 0.08 \pm 0.01(\text{stat}) \pm 0.02(\text{syst})$$

$$\sigma_{\text{eff}} = 15 \pm 3(\text{stat}) + 5/-3(\text{syst}) \text{ mb}$$



$\sigma_{\text{eff}} = 20.7 \pm 0.8(\text{stat}) \pm 6.6(\text{syst}) \text{ mb}$

**CMS, JHEP03(2014) 032**

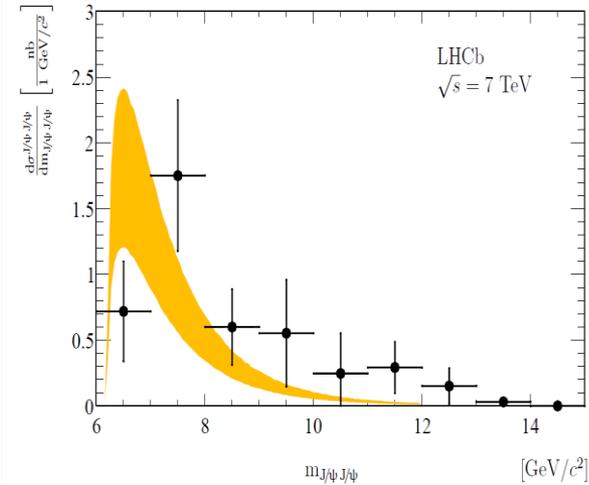
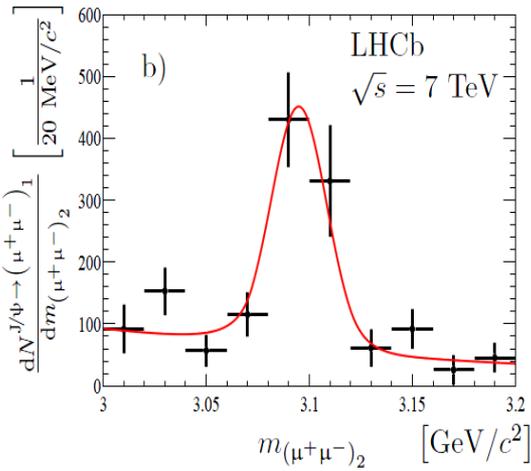
**DPS purity is still small..**



# Other processes? $2 \times J/\psi$



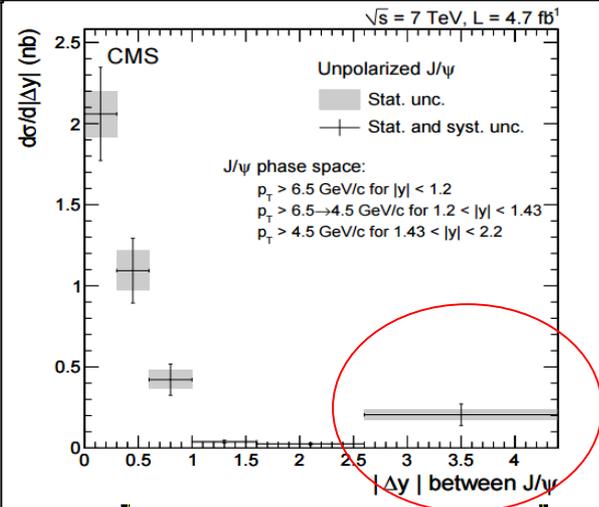
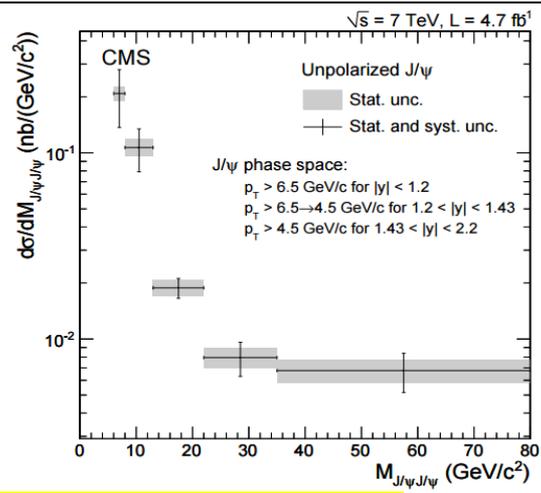
LHCb, PLB707(2012)52



$$\sigma^{J/\psi J/\psi} = 5.1 \pm 1.0 \pm 1.1 \text{ nb,}$$

$$\sigma^{J/\psi J/\psi} / \sigma^{J/\psi} = (5.1 \pm 1.0 \pm 0.6^{+1.2}_{-1.0}) \times 10^{-4},$$

**SPS CS 4nb (~30%)**  
**DPS 2.3nb**  
*Not too conclusive (116 events)*



**CMS: 446±32 events**  
**Study differential distributions**  
**Positive signal in region where SPS is suppressed:**  
***very strong argument for DPS***

$$\sigma(pp \rightarrow J/\psi J/\psi + X) = 1.49 \pm 0.07 \pm 0.13 \text{ nb,}$$

CMS, JHEP1409(2014)094



# Other processes? $J/\psi+c\bar{c}$



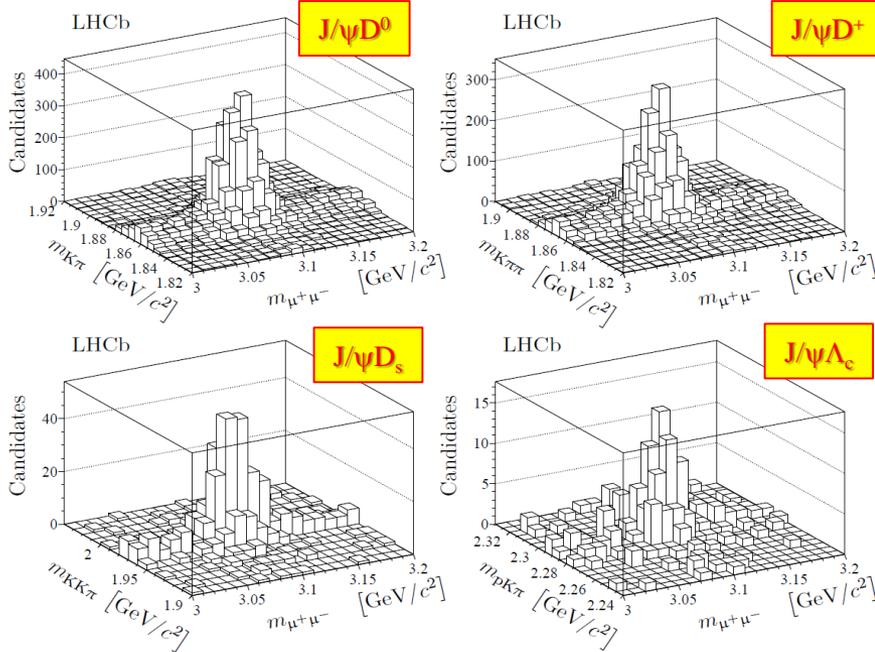
LHCb, [JHEP1206\(2012\)141](#), [JHEP 1403\(2014\)108](#)

## Something + $c\bar{c}$ at LHCb

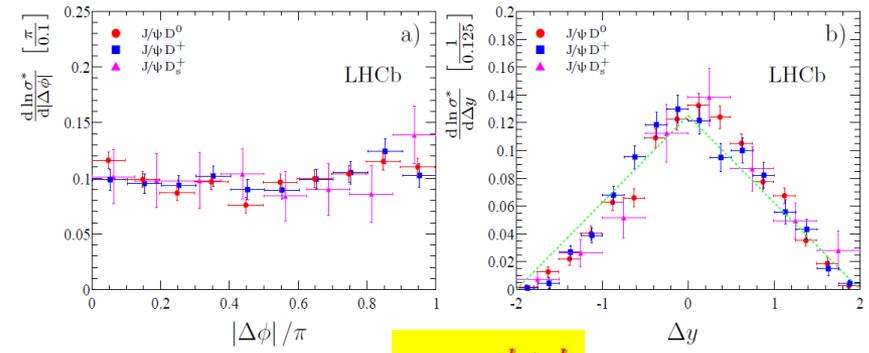
$$\sigma(c\bar{c})_{p_T < 8 \text{ GeV}/c, 2.0 < y < 4.5} = 1419 \pm 12 \text{ (stat)} \pm 116 \text{ (syst)} \pm 65 \text{ (frag)} \mu\text{b},$$

$$\sigma(X+c\bar{c})_{\text{DPS}} = \sigma(X) \times \sigma(c\bar{c}) / \sigma_{\text{eff}} \approx 10\% \sigma(X)$$

• 10% of "hard" events has additional charm!



Mode	$\sigma_{J/\psi C} / \sigma_{J/\psi} [10^{-3}]$	$\sigma_{J/\psi C} / \sigma_C [10^{-4}]$	$\sigma_{J/\psi} \sigma_C / \sigma_{J/\psi C} [\text{nb}]$
J/psi D <sup>0</sup>	$16.2 \pm 0.4 \pm 1.3^{+3.4}_{-2.5}$	$6.7 \pm 0.2 \pm 0.5$	$14.9 \pm 0.4 \pm 1.1^{+2.3}_{-3.1}$
J/psi D <sup>+</sup>	$5.7 \pm 0.2 \pm 0.6^{+1.2}_{-0.9}$	$5.7 \pm 0.2 \pm 0.4$	$17.6 \pm 0.6 \pm 1.3^{+2.8}_{-3.7}$
J/psi D <sub>s</sub> <sup>+</sup>	$3.1 \pm 0.3 \pm 0.4^{+0.6}_{-0.5}$	$7.8 \pm 0.8 \pm 0.6$	$12.8 \pm 1.3 \pm 1.1^{+2.0}_{-2.7}$
J/psi Lambda <sub>c</sub> <sup>+</sup>	$4.3 \pm 0.7 \pm 1.2^{+0.9}_{-0.7}$	$5.5 \pm 1.0 \pm 0.6$	$18.0 \pm 3.3 \pm 2.1^{+2.8}_{-3.8}$



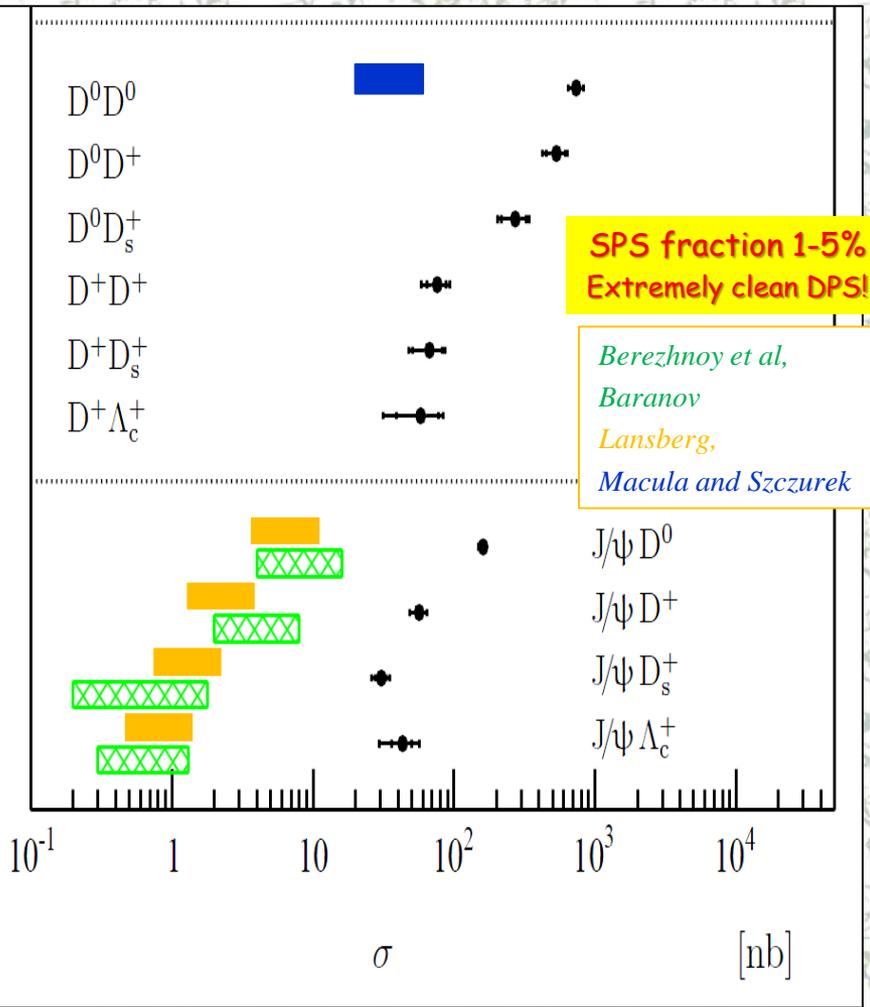
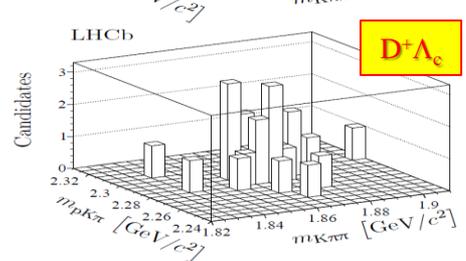
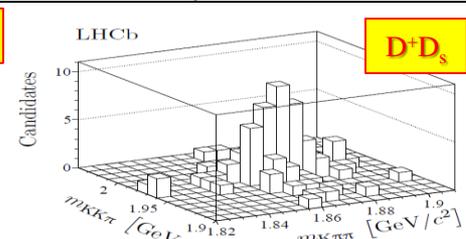
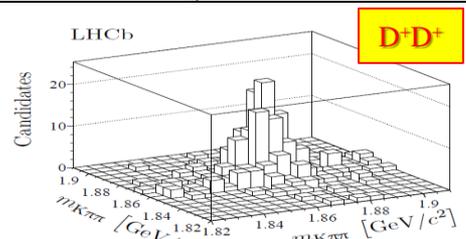
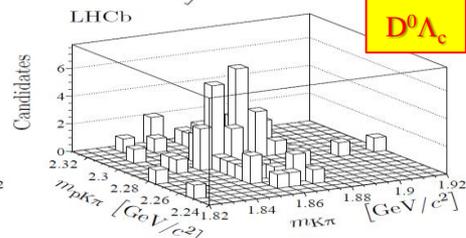
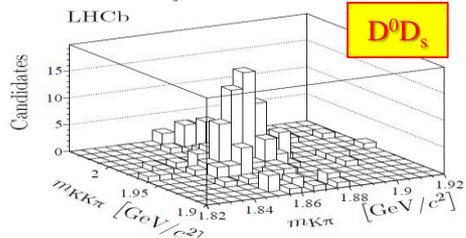
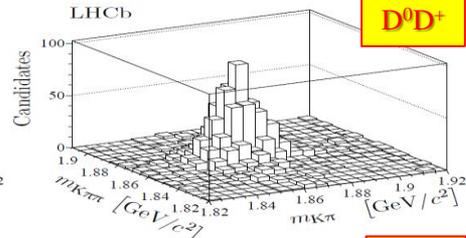
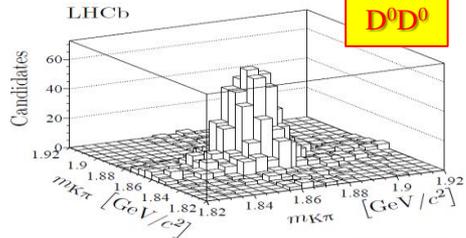
uncorrelated



# Other processes? $2 \times (c\bar{c})$



LHCb, [JHEP1206\(2012\)141](#), [JHEP 1403\(2014\)108](#)



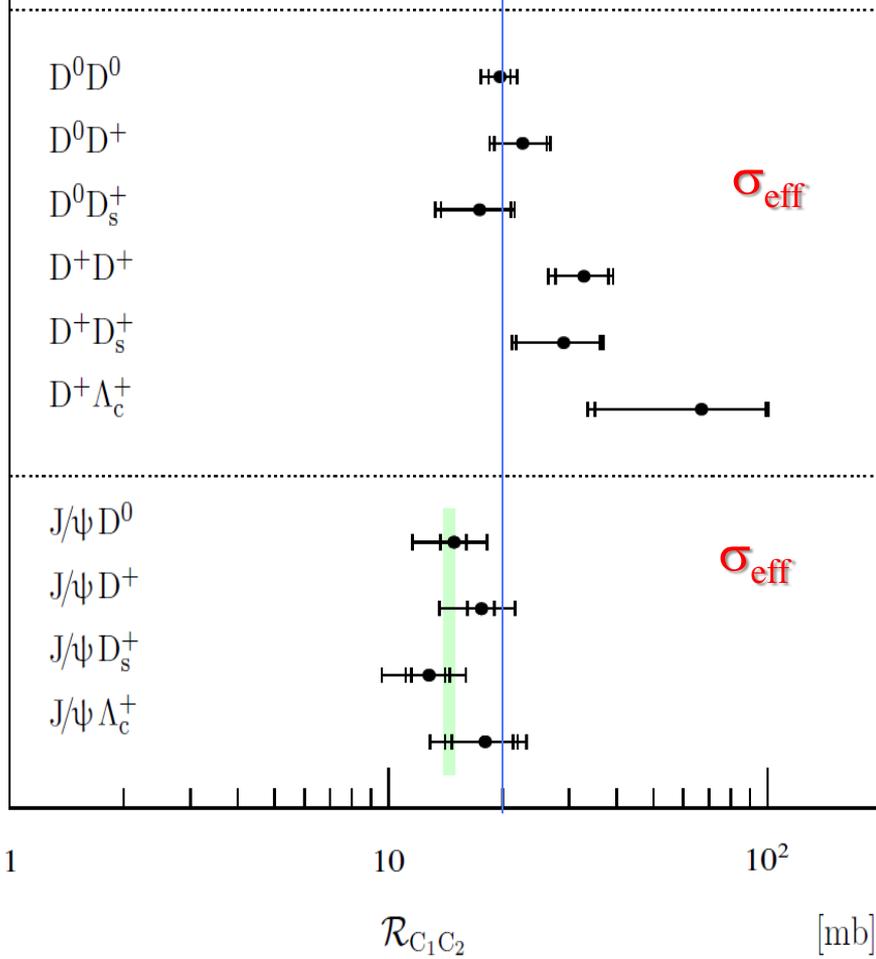


# $\sigma_{\text{eff}}$ from $J/\psi+c\bar{c}$ and $2\times(c\bar{c})$



LHCb, JHEP1206(2012)141, JHEP 1403(2014)108

- DPS with charm is not rare
- DPS dominates over SPS
- Extra clean environment and large signals
  - "DPS factory"
  - e.g. look for factorisation violation



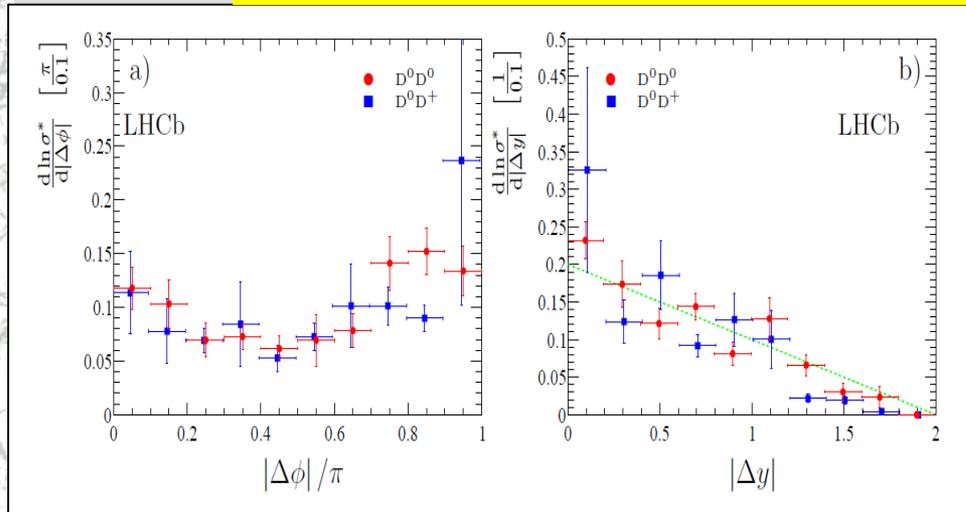
Mode	$\sigma$ [nb]	$\sigma_{c\bar{c}}/\sigma_{c\bar{c}}$ [%]	$\sigma_{C_1}\sigma_{C_2}/\sigma_{C_1C_2}$ [mb]
$D^0\bar{D}^0$	$690 \pm 40 \pm 70$	$10.9 \pm 0.8$	$2 \times (42 \pm 3 \pm 4)$
$D^0\bar{D}^+$	$6230 \pm 120 \pm 630$		$2 \times (4.7 \pm 0.1 \pm 0.4)$
$D^0\bar{D}^+$	$520 \pm 80 \pm 70$	$12.8 \pm 2.1$	$47 \pm 7 \pm 4$
$D^0\bar{D}^-$	$3990 \pm 90 \pm 500$		$6.0 \pm 0.2 \pm 0.5$
$D^0\bar{D}_s^+$	$270 \pm 50 \pm 40$	$15.7 \pm 3.4$	$36 \pm 8 \pm 4$
$D^0\bar{D}_s^-$	$1680 \pm 110 \pm 240$		$5.6 \pm 0.5 \pm 0.6$
$D^0\bar{\Lambda}_c^-$	$2010 \pm 280 \pm 600$	—	$9 \pm 2 \pm 1$
$D^+\bar{D}^+$	$80 \pm 10 \pm 10$	$9.6 \pm 1.6$	$2 \times (66 \pm 11 \pm 7)$
$D^+\bar{D}^-$	$780 \pm 40 \pm 130$		$2 \times (6.4 \pm 0.4 \pm 0.7)$
$D^+\bar{D}_s^+$	$70 \pm 15 \pm 10$	$12.1 \pm 3.3$	$59 \pm 15 \pm 6$
$D^+\bar{D}_s^-$	$550 \pm 60 \pm 90$		$7 \pm 1 \pm 1$
$D^+\bar{\Lambda}_c^+$	$60 \pm 30 \pm 20$	$10.7 \pm 5.9$	$140 \pm 70 \pm 20$
$D^+\bar{\Lambda}_c^-$	$530 \pm 130 \pm 170$		$15 \pm 4 \pm 2$



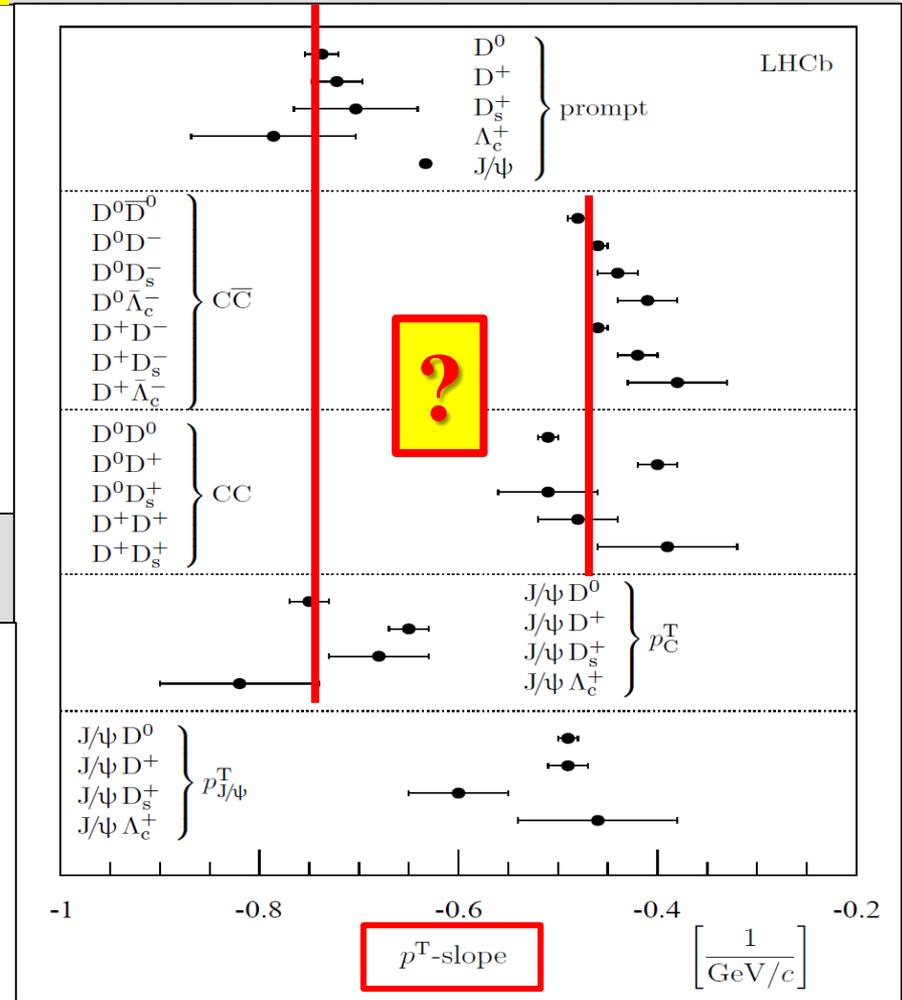
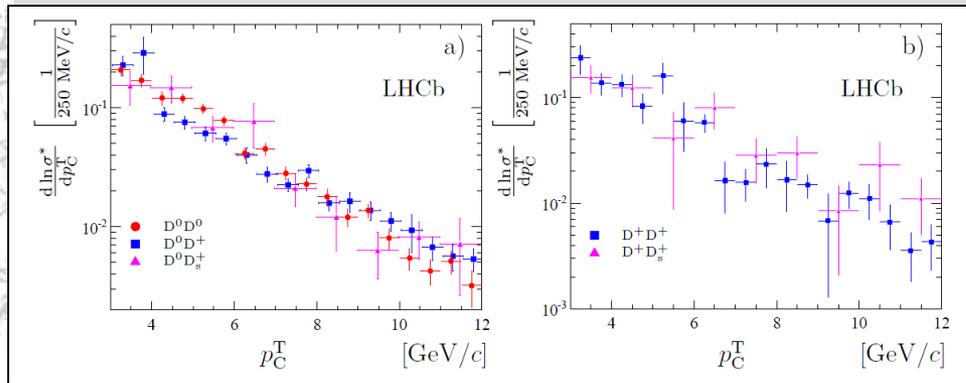
# DPS: is everything fine?



LHCb, JHEP1206(2012)141, JHEP 1403(2014)108



Compare  $p_T$ -spectra and fit with *exp*



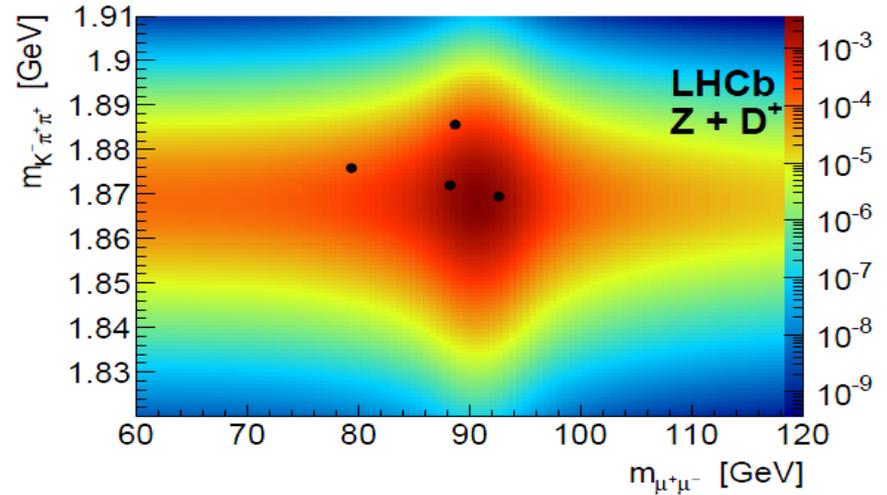
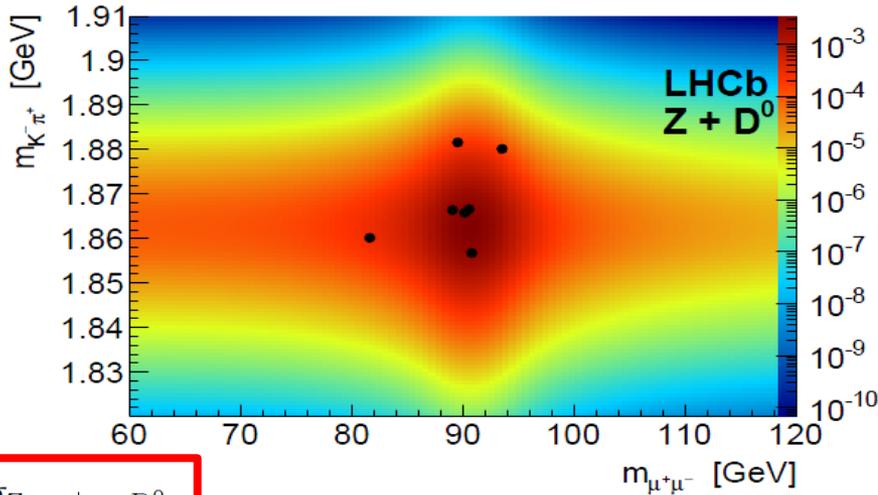


# Try harder scale: $Z+c\bar{c}$



7+4 background free  $ZD^0$  and  $ZD^+$  events

LHCb, JHEP 1404(2014) 091



$\sigma_{Z \rightarrow \mu^+ \mu^-, D^0}$

$\sigma_{Z \rightarrow \mu^+ \mu^-, D^+}$

measured

MCFM massless

MCFM massive

DPS

$Z + D^0$   $2.50 \pm 1.12 \pm 0.22$

$0.85^{+0.12}_{-0.07} \quad ^{+0.11}_{-0.17} \pm 0.05$

$0.64^{+0.01}_{-0.01} \quad ^{+0.08}_{-0.13} \pm 0.04$

$3.28^{+0.68}_{-0.58}$

$Z + D^+$   $0.44 \pm 0.23 \pm 0.03$

$0.37^{+0.05}_{-0.03} \quad ^{+0.05}_{-0.07} \pm 0.03$

$0.28^{+0.01}_{-0.01} \quad ^{+0.04}_{-0.06} \pm 0.02$

$1.29^{+0.27}_{-0.23}$

More data is needed.

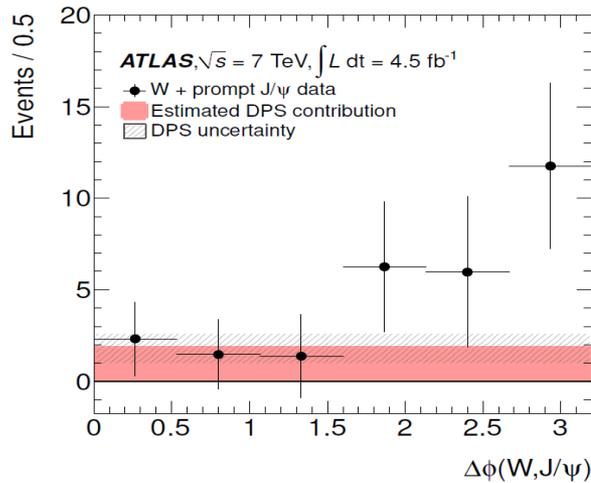
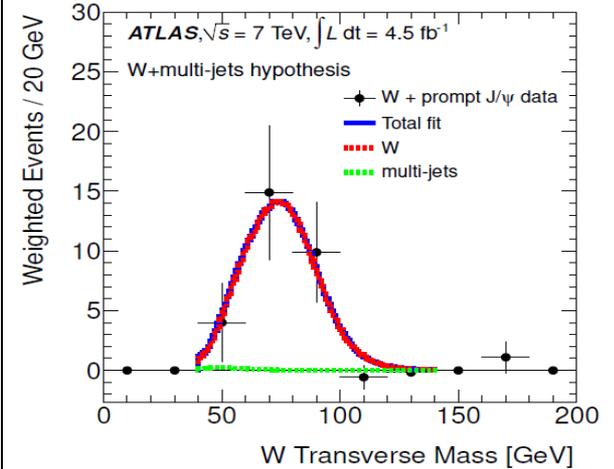
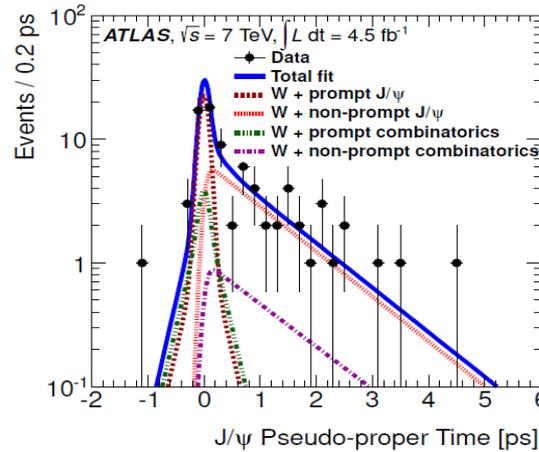
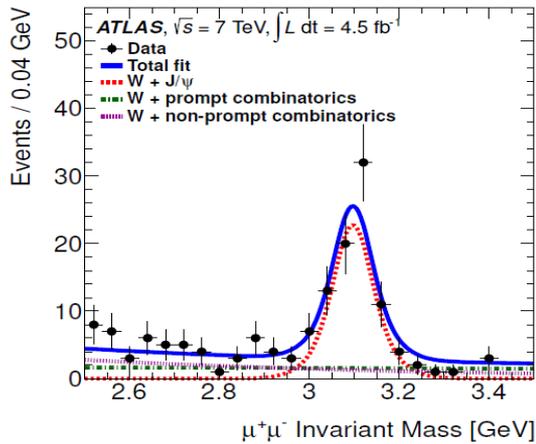
Very interesting region: 30-90% violation of factorization formula is expected



# One more process: W+J/ψ



JHEP04(2014)172



Small statistics ~30 events

Very interesting region for DPS. DPS is large but not dominant

$$R_{J/\psi}^{\text{incl}} = \frac{\text{BR}(J/\psi \rightarrow \mu^+ \mu^-)}{\sigma_{\text{fid}}(pp \rightarrow W^\pm)} \cdot \frac{d\sigma(pp \rightarrow W^\pm + J/\psi)}{dy}$$

$$R_{J/\psi}^{\text{incl}} = (126 \pm 32 \pm 9_{-25}^{+41}) \times 10^{-8}$$

$$R_{J/\psi}^{\text{DPS sub}} = (78 \pm 32 \pm 22_{-25}^{+41}) \times 10^{-8},$$



# Summary



- **DPS is actively explored at LHC by ATLAS, CMS and LHCb**
  - **Great degree of complementarity:**
    - large variety of processes
    - different kinematics range
    - different DPS purity
- **Qualitative and quantitative testing the basic principles of DPS paradigm**
  - ... and search for factorization violation
- **DPS processes have different energy dependence from SPS**
  - data at  $\sqrt{s}=13\text{TeV}$  will be very useful for better DPS understanding
  - for  $\sqrt{s}=13\text{TeV}$  for some processes, e.g.  $c\bar{c}$ , one probably can speculate also about *Triple Parton Scattering*



# Energy/process independent?

