

# Precise electroweak predictions for $V+$ multijet production

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# Outline

- 1 General aspects of EW corrections
- 2  $V$ +jets
- 3  $pp \rightarrow Z(\ell^+\ell^-) + 2$  jets at NLO EW
- 4  $pp \rightarrow W + 1, 2, 3$  jets at NLO QCD+EW

# NLO EW automation

## NLO EW corrections at the LHC

- exceed NLO QCD uncertainties at  $Q^2 \gg M_W^2$
- known for most  $2 \rightarrow 2$  processes
- missing for numerous  $2 \rightarrow 3, 4$  processes (with decays and NLOPS matching!)
- more involved than NLO QCD: virtual corrections involve various massive particles ( $\gamma, Z, W, H, b, t$ ) and tend to dominate over bremsstrahlung

Process	State of the Art	Desired
V	$d\sigma(\text{lept. V decay}) @ \text{NNLO QCD}$ $d\sigma(\text{lept. V decay}) @ \text{NLO EW}$	$d\sigma(\text{lept. V decay}) @ \text{NNLO QCD}$ and $\text{NNLO QCD+EW}$ NNLO+PS
V + j(j)	$d\sigma(\text{lept. V decay}) @ \text{NLO QCD}$ $d\sigma(\text{lept. V decay}) @ \text{NLO EW}$	$d\sigma(\text{lept. V decay})$ $@ \text{NNLO QCD} + \text{NLO EW}$
VV'	$d\sigma(\text{V decays}) @ \text{NLO QCD}$ $d\sigma(\text{on-shell V decays}) @ \text{NLO EW}$	$d\sigma(\text{decaying off-shell V})$ $@ \text{NNLO QCD} + \text{NLO EW}$
gg $\rightarrow$ VV	$d\sigma(\text{V decays}) @ \text{LO QCD}$	$d\sigma(\text{V decays}) @ \text{NLO QCD}$
V $\gamma$	$d\sigma(\text{V decay}) @ \text{NLO QCD}$ $d\sigma(\text{PA, V decay}) @ \text{NLO EW}$	$d\sigma(\text{V decay})$ $@ \text{NNLO QCD} + \text{NLO EW}$
Vbb	$d\sigma(\text{lept. V decay}) @ \text{NLO QCD}$ massive b	$d\sigma(\text{lept. V decay}) @ \text{NNLO QCD}$ $+ \text{NLO EW, massless b}$
VV' $\gamma$	$d\sigma(\text{V decays}) @ \text{NLO QCD}$	$d\sigma(\text{V decays})$ $@ \text{NLO QCD} + \text{NLO EW}$
VV'VV'	$d\sigma(\text{V decays}) @ \text{NLO QCD}$	$d\sigma(\text{V decays})$ $@ \text{NLO QCD} + \text{NLO EW}$
VV' + j	$d\sigma(\text{V decays}) @ \text{NLO QCD}$	$d\sigma(\text{V decays})$ $@ \text{NLO QCD} + \text{NLO EW}$
VV' + jj	$d\sigma(\text{V decays}) @ \text{NLO QCD}$	$d\sigma(\text{V decays})$ $@ \text{NLO QCD} + \text{NLO EW}$
$\gamma\gamma$	$d\sigma @ \text{NNLO QCD} + \text{NLO EW}$	$q\bar{q}$ resummation at NNLL matched to NNLO

Table 3: Wishlist part 3 - Electroweak Gauge Bosons (V = W, Z)

## NLO EW automation and first results

- RECOLA+COLLIER:  $pp \rightarrow \ell^+ \ell^- jj$  [arXiv:1411.0916]
- OPENLOOPS+ MUNICH and SHERPA:  $pp \rightarrow W + 1, 2, 3 \text{ jets}$  [arXiv:1412.5156]
- MADGRAPH5\_AMC@NLO:  $pp \rightarrow t\bar{t} + V$  [arXiv:1504.03446]

$\Rightarrow$  focus on general features of NLO EW calculations . . .

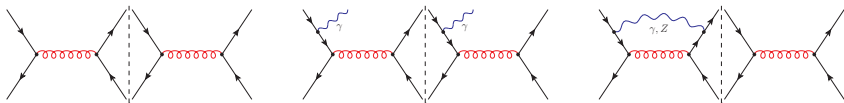
# Nontrivial QCD-EW interplay

$q\bar{q} \rightarrow q\bar{q} + \dots$  cross sections receive various Born contributions

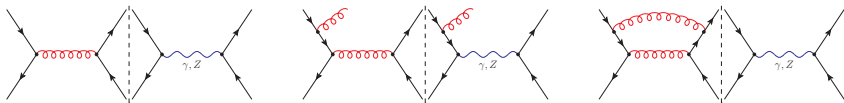
$$\underbrace{\mathcal{O}(\alpha_S^n \alpha^m)}_{\text{"QCD"}} + \underbrace{\mathcal{O}(\alpha_S^{n-1} \alpha^{m+1})}_{\text{"EW-QCD interf."}} + \dots + \underbrace{\mathcal{O}(\alpha_S^{n-k} \alpha^{m+k})}_{\text{"EW"}}$$

$\mathcal{O}(\alpha_S^n \alpha^{m+1})$  NLO EW corrections to leading QCD Born, e.g. in  $q\bar{q} \rightarrow q\bar{q}$

- EW corrections  $\times$  QCD Born



- QCD corrections  $\times$  EW-QCD interference

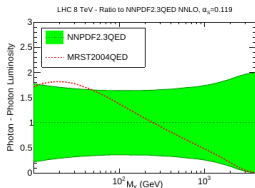
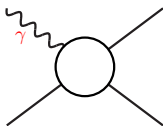
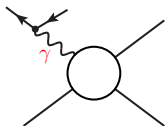


In practice above naive splitting inconsistent

- only complete  $\mathcal{O}(\alpha_S^{n-k} \alpha^{m+k+1})$  IR finite  $\Rightarrow$  nontrivial bookkeeping (automated)
- note that  $\mathcal{O}(\alpha)$  corrections can involve emissions of photons and QCD-partons

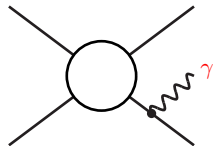
## Cancellation of IS Photon singularities

- requires QED factorisation and PDF evolution [MRST2004, NNPDF2.3]
- $\gamma$ -induced processes  $\Rightarrow$  possible TeV-scale enhancements but large PDF uncertainty



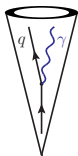
## Cancellation of FS photon singularities

- requires IR subtraction method [Catani,Dittmaier,Seymour, Trocsanyi; Frixione, Kunszt, Signer]
- photon emission off quarks renders **IR safe jet definition nontrivial at NLO EW**

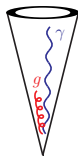


# Treatment of photons inside jets at NLO EW

## Option A: Democratic jet-algorithm approach (jets $\equiv$ photons)



collinear  $q \rightarrow q\gamma$  singularities  
cancelled clustering  $q, g, \gamma$  on  
same footing

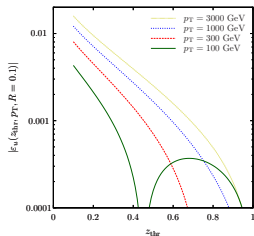


soft gluon singularities  $\leftrightarrow$  hard  
photons inside jets: cancelled in  
jet-production (NLO EW) +  
 $\gamma$ -production (NLO QCD)

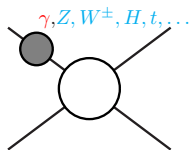
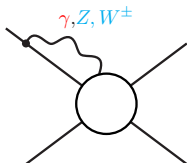
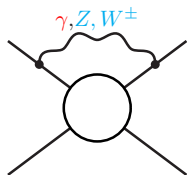
## Option B: Separation of jets from photons through $E_\gamma/E_{\text{jet}} < z_{\text{thr}}$ inside jets

- **rigorous approach:** absorb  $q \rightarrow q\gamma$  singularity into fragmentation function [1411.0916]
- **approximation:** cancel singularity via  $q\gamma$  recombination in small cone  $\Delta R_{q\gamma} < 0.1$  [1412.5156]

$\Rightarrow$  difference  $\ll 1\%$  for typical  $z_{\text{thr}}$  choices



# EW Sudakov logarithms I



**Virtual EW bosons coupling to on-shell legs at  $Q^2 \gg M_W^2$**

$\Rightarrow$  large soft/collinear  $\alpha \ln^2(Q^2/M_W^2)$  corrections

**Universality and factorisation** [Denner,S.P. '01] similarly as in QCD

$$\delta \mathcal{M}_{\text{LL+NLL}}^{1\text{-loop}} = \frac{\alpha}{4\pi} \sum_{k=1}^n \left\{ \frac{1}{2} \sum_{l \neq k} \sum_{a=\gamma, Z, W^\pm} I^a(k) I^{\bar{a}}(l) \ln^2 \frac{\hat{s}_{kl}}{M^2} + \gamma^{\text{ew}}(k) \ln \frac{\hat{s}}{M^2} \right\} \mathcal{M}_0$$

- depend on external EW charges (anomalous dimensions) and kinematic details
- **large negative corrections to any process** at high  $p_T, E_{T,\text{miss}}, H_T, M_{\text{inv}}, \dots$

**Typical size of corrections at 1 TeV:**  $> 10\%$  at **1-loop** and  $> 1\%$  at **2-loops**

$$\begin{aligned} \left(\frac{\delta\sigma_1}{\sigma_0}\right)_{\text{LL}} &\simeq -\frac{4\alpha}{\pi s_w^2} \ln^2\left(\frac{1\text{ TeV}}{M_W}\right) \simeq -26.4\% & \left(\frac{\delta\sigma_2}{\sigma_0}\right)_{\text{LL}} &\simeq +\frac{8\alpha^2}{\pi^2 s_w^4} \ln^4\left(\frac{1\text{ TeV}}{M_W}\right) \simeq 3.5\% \\ \left(\frac{\delta\sigma_1}{\sigma_0}\right)_{\text{NLL}} &\simeq +\frac{6\alpha}{\pi s_w^2} \ln\left(\frac{1\text{ TeV}}{M_W}\right) \simeq +15.6\% & \left(\frac{\delta\sigma_2}{\sigma_0}\right)_{\text{NLL}} &\simeq -\frac{24\alpha^2}{\pi^2 s_w^4} \ln^3\left(\frac{1\text{ TeV}}{M_W}\right) \simeq -4.1\% \end{aligned}$$

- various 2-loop results and resummations available [Bauer, Becher, Ciafaloni, Comelli, Denner, Fadin, Jantzen, Kühn, Lipatov, Manohar Martin, Melles, Penin, Pozzorini, Smirnov, ...]

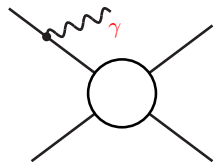
$\Rightarrow$  EW corrections crucial for SM tests and BSM searches at TeV scale



# Electroweak bremsstrahlung

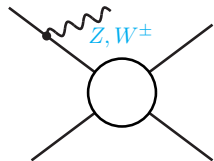
## Real photon emission

- mandatory since soft/collinear  $\gamma$  unresolved
- complete cancellation of QED singularities



## Real $Z, W$ emission [Ciafaloni, Comelli, ...]

- **inclusive emission**: only **partial  $\ln(\hat{s}/M_W)$  cancellation**
- $\leftrightarrow$  free SU(2) charges, collinear IS logs, kinematic  $M_{Z,W}$  effects
- **typical experimental cuts**: **modest  $\ln(\hat{s}/M_W)$  cancellation** (strongly dependent on process and analysis)



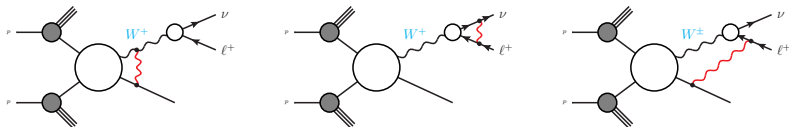
## Bookkeeping of $pp \rightarrow X$ and $pp \rightarrow X + V$ processes

- important to **add both contributions** to physical observables while **keeping them as separate processes** ( $XV$  production  $\ni$   $X$  production)
- **otherwise double counting**, e.g. overlap of  $ZW$ ,  $Z(+V)$  and  $W(+V)$  production
- separation **trivial** since  $Z/W$  emission is tree level and IR finite

# Decays of Z/W bosons

## Leptonic Z and W decays are nontrivial at NLO EW (in contrast to NLO QCD)

- NLO EW corrections to **production**  $\times$  **resonance**  $\times$  **decay** + non-factor corrections



## Option A: complex mass scheme [Denner, Dittmaier]

- exact NLO description (always desirable)
- **high complexity** corresponding to total number of particles *after* decays

## Option B: narrow-width approximation (production $\times$ decay)

- **simpler but applicability to V+multijets limited** to certain  $\mathcal{O}(\alpha_S^n \alpha^{m+1})$  (see later)
- captures **all large  $\ln(\hat{s}/M_W^2)$  effects** (present only in production sub-process)
- typical **uncertainty**  $\lesssim 1\text{--}3\%$  (apart from  $\gamma^*/Z^* \rightarrow \ell^+\ell^-$  at small  $m_{\ell\ell}$ )

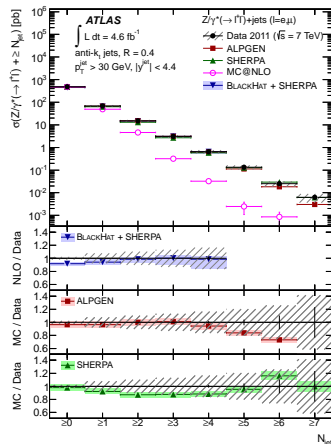
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# High precision in perturbative QCD

## $V + 1, 2, 3, 4, (5)$ jets at NLO

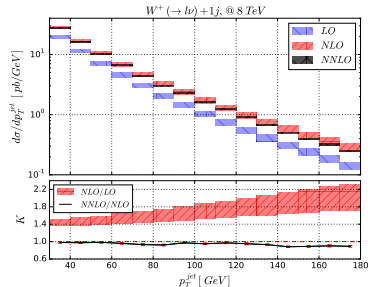
[BLACKHAT+SHERPA '09-'13]



$\Rightarrow \mathcal{O}(10\%)$  scale uncertainties

## $W + 1$ jet at NNLO

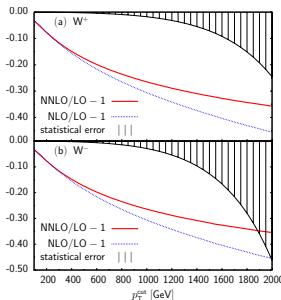
[Boughezal,Focke,Liu,Petriello '15]



$\Rightarrow \mathcal{O}(1\%)$  scale uncertainty

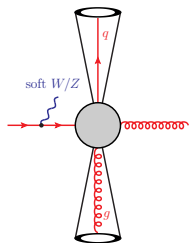
## Very large EW corrections to $pp \rightarrow Z/W + 1 \text{ jet}$

- NLO (electro)weak [Maina, Ross, Moretti '04; Kühn, Kulesza, S.P., Schulze '04-'07]
- EW Sudakov logs beyond NLO [Kühn, Kulesza, S.P., Schulze '04-'07; Becher, Garcia i Tormo '13]
- NLO QCD+EW with off-shell  $Z/W$  decays [Denner, Dittmaier, Kasprzik, Muck '09-'11]



## Strong motivations for $V + \text{multijets}$ at NLO EW

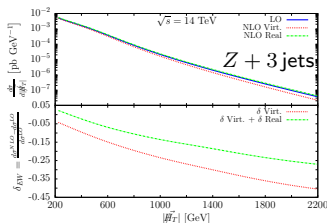
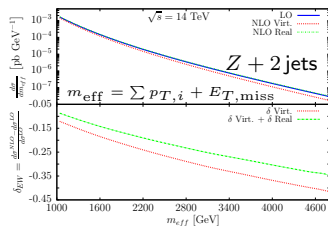
- multi-jet case: EW Sudakov poorly explored and crucial for BSM searches
- huge di-jet contributions at high jet  $p_T \Rightarrow V + 1 \text{ jet NLO EW insufficient!!}$
- overlap with EW processes (VBF,  $VV'$ ,  $tj$ ,  $tW$ ,  $t\bar{t}$ ) and interference with QCD



# EW Sudakov logarithms in $pp \rightarrow Z(\nu\bar{\nu}) + 2, 3 \text{ jets}$ [Chiesa,

Montagna, Barzé, Moretti, Nicosini, Piccinini, Tramontano '13]

## $Z(\nu\bar{\nu}) + \text{multijet background to MET} + 2/3j + 0\ell$ searches in ATLAS/CMS



## Virtual Sudakov LL+NLL effects [Denner, S.P. '01]

- process-independent implementation in ALPGEN
- ⇒ 15–40% negative corrections in (multi)TeV range

## Real emission effects from $pp \rightarrow ZZ/WW/WZ + n\text{-jets}$

- with  $Z/W \rightarrow jj, \ell^+\ell^-, \ell\nu, \nu\bar{\nu}$  decays and  $n = 0, \dots, 2/3$  (not fixed!)
- ⇒ modest positive correction 5–10%

**Strong motivation for  $pp \rightarrow V + \text{multijets}$  at NLO EW!**

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## Automated Tools

- Loops amplitudes: **RECOLA** [Actis, Denner, Hofer, Scharf, Uccirati '13] and **COLLIER** [Denner, Dittmaier, Hofer '14]
- Monte Carlo: in-house program

⇒ **Full NLO QCD+EW automation for any  $2 \rightarrow 2, 3, 4$  SM process**

## Application to $Z + 2\text{jet}$ production (complex mass scheme)

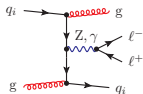
- ⇒ **nontrivial  $2 \rightarrow 4$  calculation** for full  $pp \rightarrow \ell^+\ell^-jj$  processes
- ⇒ exact treatment of  $\gamma^*/Z^*$  and **non-resonant effects!**

## Off-shell effects vs $q\bar{q} \rightarrow Z^* \rightarrow \ell^+\ell^-$ pole approximation

- **1.5% (11%)** with (without)  $|M_{\ell\ell} - M_Z| < 15$  GeV cut

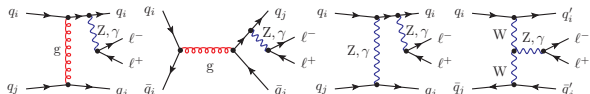


# LO contributions to $\sigma_{\text{int}}$



## Two-quark channels

$$\Rightarrow \mathcal{O}(\alpha_S^2 \alpha^2)$$



## Four-quark channels

$$\Rightarrow \mathcal{O}(\alpha_S^2 \alpha^2) + \underbrace{\mathcal{O}(\alpha_S \alpha^3)}_{\text{for } q_i=q_j} + \underbrace{\mathcal{O}(\alpha^4)}_{\text{VBF, ZV}(jj)}$$

## Integrated $\sigma_{\text{LO}}$ at 13 TeV with "standard" and VBF cuts

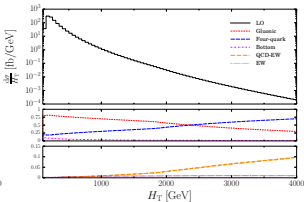
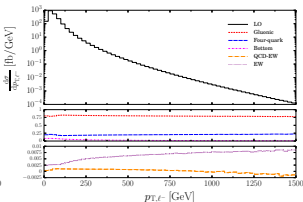
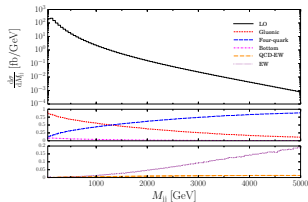
- $\sigma_{4q}/\sigma_{2q}$  from 20% (standard cuts) to 40% (VBF cuts)
- **QCD dominant** also with VBF cuts (but no jet veto...)
- **tiny EW-QCD interference** (accidental)

cuts	channels			order		
	2q	4q	$\gamma$ -ind.	$\alpha_S^2 \alpha^2$	$\alpha_S \alpha^3$	$\alpha^4$
standard	80%	20%	< 0.05%	99%	< 0.1%	1%
VBF	60%	40%	-	93%	0.01	7%

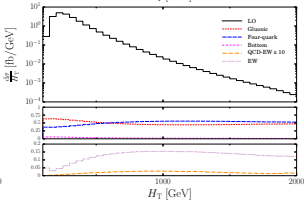
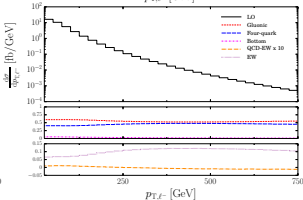
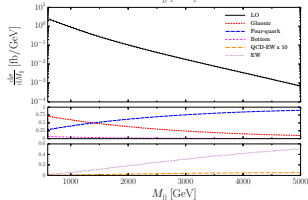
$\gamma p$  and  $\gamma\gamma$  induced processes of  $\mathcal{O}(\alpha_S \alpha^3) + \mathcal{O}(\alpha^4) \Rightarrow 10^{-3} \times \sigma_{\text{tot}}$  (neglected)

# LO contributions to $d\sigma_{\text{LO}}/dX$

standard cuts



VBF cuts



## Strong kinematic dependence of 2q/4q and QCD/EW contributions

- $\sigma_{4q}/\sigma_{2q}$  grows from 20% to 50(75)% at  $H_T, M_{jj}=2(4)$  TeV
- EW contribution enhanced from 1 to 10–20% by VBF cuts and at large  $M_{jj}$
- EW–QCD interference  $\sim 10\%$  at very large  $H_T$  and  $p_{T,j}$  but suppressed otherwise

# NLO EW corrections to $pp \rightarrow Z(\ell^+\ell^-) + 2\text{jets}$

## NLO EW vs full NLO SM corrections

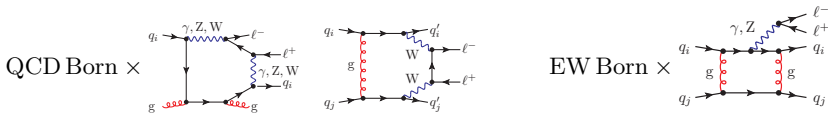
$$\underbrace{\mathcal{O}(\alpha_S^3\alpha^2)}_{\text{"NLO QCD"}}$$

$$\underbrace{\mathcal{O}(\alpha_S^2\alpha^3)}_{\text{"NLO EW"}}$$

$$\mathcal{O}(\alpha_S^1\alpha^4)$$

$$\mathcal{O}(\alpha_S^0\alpha^5)$$

## Virtual EW corrections (examples of EW/QCD loops in 2q/4q channels)



$\Rightarrow \mathcal{O}(1000)$  1-loop diagrams with  $\mathcal{O}(100)$  hexagons+pentagons per channel

## Real EW corrections (examples of photon/gluon emission in 2q/4q channels)

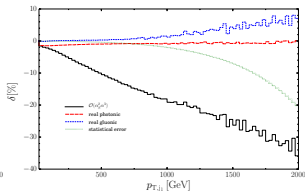
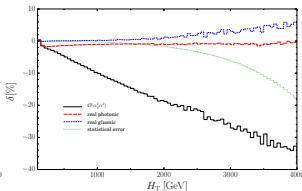
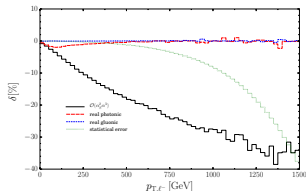


## Integrated cross section (with standard or VBF cuts)

- only 2–3% negative corrections wrt LO

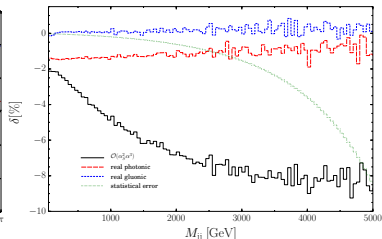
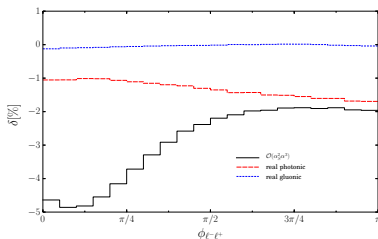
## Distributions in $p_T$ and $H_T$ (similar results with standard and VBF cuts)

- large negative corrections of **-20% to -35% in the (multi)TeV region**
- dominated by virtual corrections** (typical Sudakov EW behaviour)
  - photon bremsstrahlung\*  $\lesssim 1-2\%$  \* ( $\overline{\text{MS}}$  subtraction of IR sing.)
  - gluon bremsstrahlung\*  $\lesssim 1-2\%$  apart from  $p_{T,j}$  and  $H_T$  tails (+6–8%)
- NLO EW **statistically relevant up to  $H_T = 5 \text{ TeV}$**  at  $L = 300 \text{ fb}^{-1}$



## Angular and $M_{jj}$ distributions (similar results with standard and VBF cuts)

- only **mild corrections**:  $\lesssim 5\%$  in general and  $\lesssim 10\%$  in  $M_{jj}$  tail
- slight shape deformation of  $\phi_{\ell+\ell^-}$
- no strong Sudakov enhancement at  $M_{jj} = 5$  TeV** (dominated by scale  $t \ll M_{jj}$ )



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- 4  $pp \rightarrow W + 1, 2, 3$  jets at NLO QCD+EW

# $pp \rightarrow W + 1, 2, 3 \text{ jets}$ at NLO QCD+EW

[Kallweit, Lindert, Maierhöfer, S.P., Schönherr '14]

## Automated Tools

- Loop amplitudes: **OPENLOOPS** [Casoli, Lindert, Maierhöfer, S.P. '13] and **COLLIER** [Denner, Dittmaier, Hofer '14]
- Monte Carlo: **MUNICH** [Kallweit] or **SHERPA** [Hoeche, Hoeth, Krauss, Schoenherr, Schumann, Siegert, Zapp]

⇒ **Full NLO QCD+EW automation for any  $2 \rightarrow 2, 3, 4$  SM process**

## Application to $W$ +multijet production

- ⇒ investigate technical performance of tools for **multi-jet case**
- ⇒ go up to  $N_{\text{jets}} = 3$  **keeping on-shell  $W$**  (stable or NWA decay)
- ⇒ investigate  $N_{\text{jets}}$ -**dependence of NLO EW**

# Generic partonic channels for $pp \rightarrow W^+ + n \text{ jets } (n \leq 3)$

	$pp \rightarrow W + n \text{ jets @LO}$					$pp \rightarrow W + n \text{ jets @NLO}$				
	$\alpha_S^n \alpha$	$\alpha_S^{n-1} \alpha^2$	$\alpha_S^{n-2} \alpha^3$	$\alpha_S^{n-3} \alpha^4$	$\alpha_S^{n+1} \alpha$	$\alpha_S^n \alpha^2$	$\alpha_S^{n-1} \alpha^3$	$\alpha_S^{n-2} \alpha^4$	$\alpha_S^{n-3} \alpha^5$	
$u_i \bar{d}_i \rightarrow W + n g$	×	-	-	-	×	×	-	-	-	
$u_i \bar{d}_i \rightarrow W + q\bar{q} + (n-2)g$	×	×	×	-	×	×	×	×	-	
$\gamma u_i \rightarrow d_i W + (n-1)g$	-	×	-	-	-	-	-	-	-	
$\gamma u_i \rightarrow d_i W + q\bar{q} + (n-3)g$	-	×	×	×	-	-	-	-	-	
$\gamma\gamma \rightarrow \bar{u}_i d_i W + (n-2)g$	-	-	×	-	-	-	-	-	-	
$u_i \bar{d}_i \rightarrow W + (n+1)g$	-	-	-	-	×	-	-	-	-	
$u_i \bar{d}_i \rightarrow W + q\bar{q} + (n-1)g$	-	-	-	-	×	×	×	-	-	
$u_i \bar{d}_i \rightarrow W + q\bar{q}q'q' + (n-3)g$	-	-	-	-	×	×	×	×	×	
$u_i \bar{d}_i \rightarrow W + n g + \gamma$	-	-	-	-	-	×	-	-	-	
$u_i \bar{d}_i \rightarrow W + q\bar{q} + (n-2)g + \gamma$	-	-	-	-	-	×	×	×	×	

× (×) = (not) included in 1412.5156

## Automated bookkeeping crucial

- many crossings and flavour combinations ( $u_i, d_i, q, q' \in \{u, d, c, s, b\}$ )

## LO contributions from $2q, 4q, \gamma$ - and $\gamma\gamma$ -induced channels

- $2q$ : QCD
- $4q$ : QCD, EW  $\supset$  VBF,  $WV(jj)$ ,  $t(Wb)j$ ,  $Wt(jjj)$  and QCD-EW interf.

## NLO contributions of order $\alpha_S^{n+1}\alpha$ and $\alpha_S^n\alpha^2$

- $\mathcal{O}(\alpha_S)$  corrections to LO QCD
- $\mathcal{O}(\alpha)$  corrections to LO QCD  $\equiv \mathcal{O}(\alpha_S)$  corrections to LO EW-QCD interf.



# Technical aspects

**Number of diagrams in  $pp \rightarrow W + 1, 2, 3 \text{ jets}$**  (in parenthesis:  $q = u_i, d_i$  case)

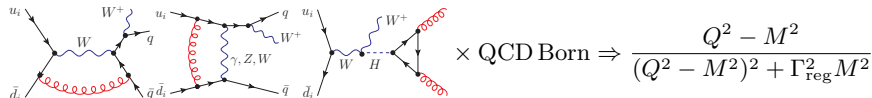
Channel	QCD trees	EW trees	QCD 1-loop	EW 1-loop
$u_i \bar{d}_i \rightarrow W^+ g$	2	-	11	32
$u_i \bar{d}_i \rightarrow W^+ q \bar{q}$	2 (4)	7 (14)	33 (66)	105 (210)
$u_i \bar{d}_i \rightarrow W^+ gg$	8	-	150	266
$u_i \bar{d}_i \rightarrow W^+ q \bar{q} g$	12 (24)	33 (66)	352 (704)	1042 (2084)
$u_i \bar{d}_i \rightarrow W^+ g g g$	54	-	2043	2616

- moderate growth of complexity wrt NLO QCD (up to  $3 \times$  more loop diagrams)
- 1-loop QCD and EW similarly fast  $\Rightarrow$  0.1% stat precision for  $W + 1, 2, 3 \text{ jets}$  at NLO QCD+EW costs 13,210,6300 CPU h (dominated by NLO QCD!)

## On-shell external $W$ and “pseudo resonances”

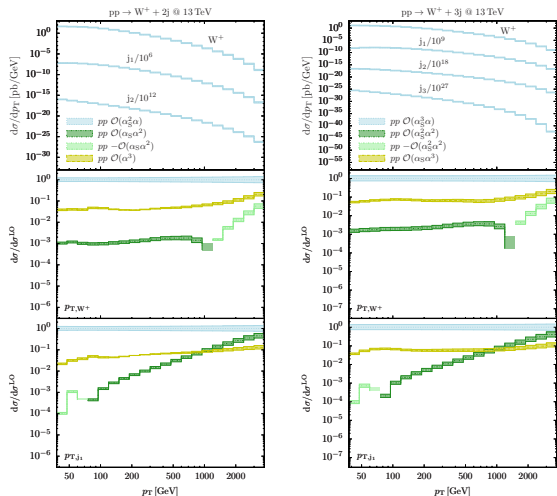
- external  $W$  stable ( $\Gamma_W = 0$ ) but small  $\Gamma_{\text{reg}} \rightarrow 0$  for s-channel  $t, W, Z, H$  propagators in QCD  $\times$  EW interf

(IR EW singularities tricky...)



- can be extended to  $W \rightarrow \ell \nu$  decays in NWA but not to full NLO SM

# LO EW–QCD interplay in $pp \rightarrow W^+ + 2, 3 \text{ jets}$ at 13 TeV



## “QCD cuts” throughout

- $p_T > 30 \text{ GeV}, \eta < 4.5$
- ⇒ QCD dominates

## EW contributions (WV, VBF, single-t)

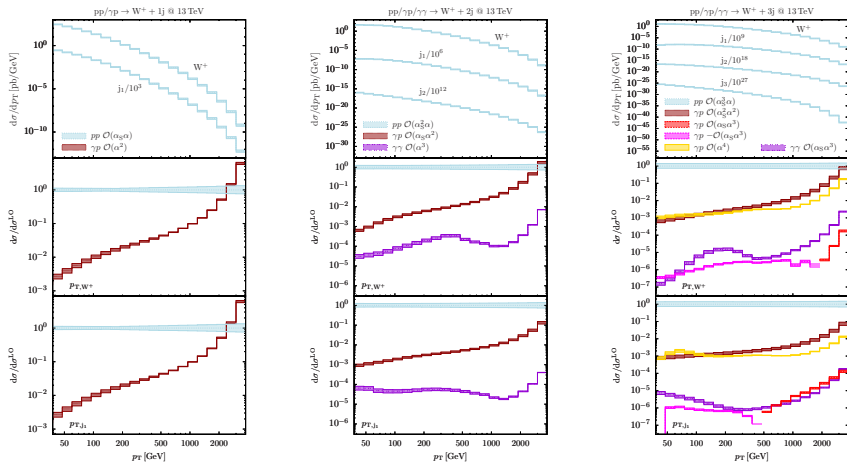
- 3–6% in  $\sigma_{\text{int}}$
- 10–20% at 1–4 TeV

## EW–QCD interference

- $\mathcal{O}(10^{-3})$  in  $\sigma_{\text{int}}$
- 10–50% at 1–4 TeV (dominant!)

⇒ nontrivial QCD–EW interplay at the TeV scale (with  $V$ +jets “QCD cuts”)

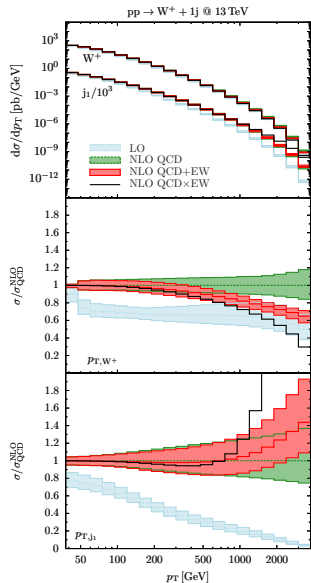
# LO $\gamma$ -induced contributions in $pp \rightarrow W^+ + 1, 2, 3 \text{ jets}$



## Single- $\gamma$ contributions

- from  $\mathcal{O}(10^{-3})$  in  $\sigma_{\text{int}}$  to **5–100%** at  $p_{T,W} = 1\text{--}4 \text{ TeV}$ !
- driven by  $\gamma$ -PDF (NNPDF2.3 QED) at large  $x$  (huge  $\gamma$ -PDF uncertainty...)

# NLO QCD+EW corrections to $pp \rightarrow W^+ + 1 \text{ jet}$



**Inclusive**  $\sigma(pp \rightarrow W + 1, 2, 3 \text{ jets})$  ( $p_{T,j} > 30 \text{ GeV}$ )

- $\lesssim 1\%$  EW correction

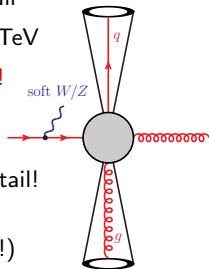
**W-boson  $p_T$  (Sudakov behaviour)**

- +100% QCD correction in the tail
- -20-35% EW correction at 1-4 TeV
- **large extra EW $\times$ QCD correction!**

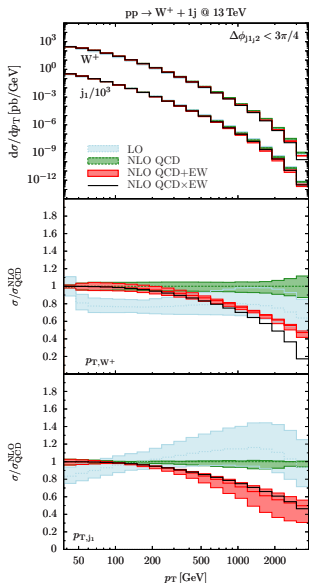
**Jet  $p_T$  (di-jet dominance)**

- **factor-10 QCD correction** in the tail!
- **positive 10-50% EW correction** (QCD-EW quark bremsstrahlung!)

$\Rightarrow$  **pathologic (large uncertainties)!**



Same with “dijet-veto cut”  $\phi_{jj} < \frac{3}{4\pi}$



## QCD corrections

- still sizable in  $p_{T,W}$  tail but moderate at high  $p_{T,\text{jet}}$

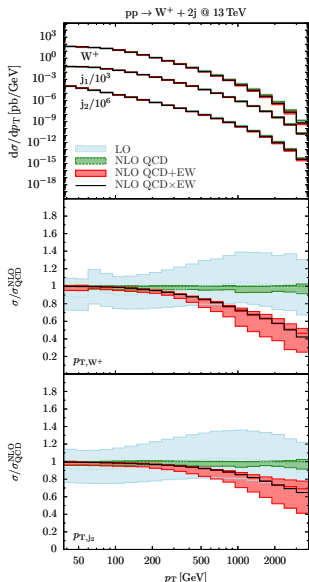
## EW corrections

- Sudakov behaviour in both tails
- -20-50% at 1-4 TeV (more pronounced)

## Bottom line

- W + 1 jet at NLO ok for *exclusive* case
- *inclusive* case requires W + 2 jets at NLO

# NLO QCD+EW corrections to $pp \rightarrow W^+ + 2\text{jets}$



## QCD corrections

- small and almost  $p_T$  independent
- $\lesssim 10\%$  scale dependence at NLO

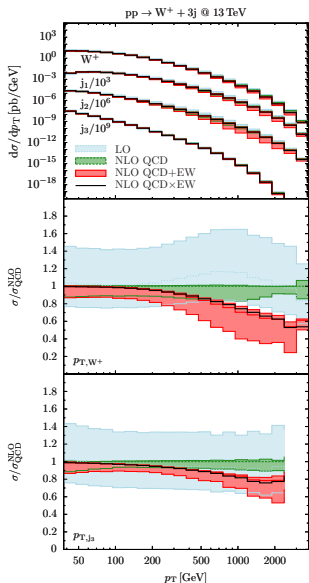
## EW corrections

- Sudakov effects in  $W^-$  and jet- $p_T$  tails
- $\Rightarrow -30-60\%$  at  $p_{T,W} = 1-4$  TeV
- $\Rightarrow -15-25\%$  at  $p_{T,j} = 1-4$  TeV

## Bottom line

- **different behaviour of  $W$  and jets**  
(due to hard-dijet contributions and positive QCD-EW bremsstrahlung)
- **NLO very well behaved**  
(but might need EW Sudakov resummation)

# NLO QCD+EW corrections to $pp \rightarrow W^+ + 3\text{jets}$



## QCD corrections

- mild apart from first two jets (not shown)
- $\lesssim 10\%$  scale dependence

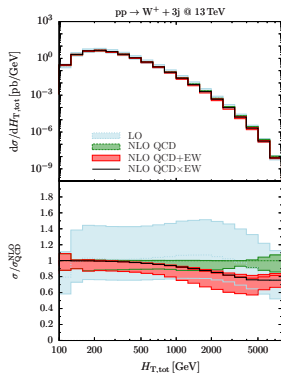
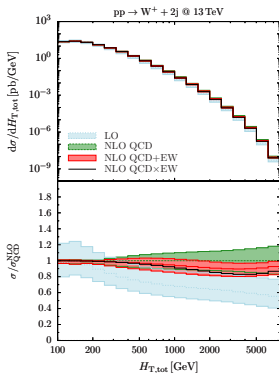
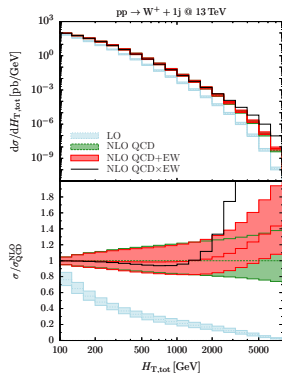
## EW corrections

- Sudakov effects in  $W^-$  and jet- $p_T$  tails
- $\Rightarrow -30-50\%$  at  $p_{T,W} = 1-4$  TeV
- $\Rightarrow -20-30\%$  at  $p_{T,j} = 1-4$  TeV

## Bottom line

- similar picture as for  $W + 2$  jets

# NLO corrections to $H_{T,tot}$ in $pp \rightarrow W^+ + 1, 2, 3 \text{ jets}$



- first exciting results
- NLO QCD in  $H_{T,tot}$  tail well behaved only starting from  $W + 3 \text{ jets}$  (calls for NLO multi-jet merging)
- only  $-20\%$  EW corrections at very high  $H_{T,tot}$  (more if also  $p_{T,W}$  is high!)



# Summary and Outlook

## NLO QCD+EW for $V$ +multijets

- EW corrections crucial at the TeV scale
- large QCD radiation calls for EW+QCD corrections for multi-jet final states

## NLO QCD+EW automation

- applicable to any  $2 \rightarrow 2, 3, 4$  SM process
- various nontrivial physics features (EW-QCD interplay, decays, “overlapping” processes, jet/photon definition, ...)

## Next steps

- full NLO SM predictions
- how to disentangle  $W$ +multijets from VBF and  $WW/WZ$ ,  $tj$ ,  $Wt$ ,  $tt$  production  $\times$  decays?
- NLO QCD+EW matching and multi-jet merging
- ...

Backup slides

# NLO amplitudes with OpenLoops

$$\mathcal{N}_{\alpha}^{\beta}(\mathcal{I}_n; q) = \begin{array}{c} \beta \\ \leftarrow \\ \text{---} \\ \text{---} \\ \alpha \\ \rightarrow \end{array} \text{---} \text{---} \text{---} \text{---} \text{---} \begin{array}{c} i_n \\ \circ \\ \text{---} \\ \text{---} \\ \circ \\ i_1 \end{array} = \begin{array}{c} \beta \\ \leftarrow \\ \text{---} \\ \text{---} \\ \alpha \\ \rightarrow \end{array} \text{---} \text{---} \text{---} \text{---} \begin{array}{c} i_n \\ \circ \\ \text{---} \\ \text{---} \\ \circ \\ i_{n-1} \\ \text{---} \\ \text{---} \\ \circ \\ i_1 \end{array}$$

## OpenLoops approach [Cascioli, Maierhöfer, Pozzorini '12]

- numerical recursion for “loop-momentum dependent trees”

$$\sum_{r=0}^n \mathcal{N}_{\mu_1 \dots \mu_r; \alpha}^{\beta}(\mathcal{I}_n) q^{\mu_1} \dots q^{\mu_r} = \left( Y_{\gamma\delta}^{\beta} + q^{\nu} Z_{\nu; \gamma\delta}^{\beta} \right) \sum_{r=0}^{n-1} \mathcal{N}_{\mu_1 \dots \mu_r; \alpha}^{\beta}(\mathcal{I}_{n-1}) q^{\mu_1} \dots q^{\mu_r}$$

- automated & fast generation of NLO QCD MEs for any  $2 \rightarrow 4(5)$  SM process
  - (1-loop)  $\times$  tree and (1-loop)<sup>2</sup> amplitudes
  - trees including helicity and colour correlations
- High speed at runtime with tensor reduction (COLLIER [Denner, Dittmaier, Hofer]) and/or OPP reduction (CUTTOOLS [Ossola, Papadopolous, Pittau '07])

# OpenLoops Public Release

## OpenLoops 1.0 [Cascioli, Lindert, Maierhöfer, Pozzorini]

- publicly available since Sept '14 at [openloops.hepforge.org](http://openloops.hepforge.org)
- library with **more than 100 hadron-collider processes** at NLO QCD available
- svn download**  

```
$ svn co http://openloops.hepforge.org/  
svn/OpenLoops/branches/public ./OpenLoops
```
- installation of OpenLoops with selected processes**  

```
$ cd ./OpenLoops  
$ ./scons  
$ ./openloops libinstall ppttj,ppzjjj,...
```

**Complete NLO automation** through interfaces with various Monte Carlo Tools

- **SHERPA** [Hoeche, Hoeth, Krauss, Schoenherr, Schumann, Siegert, Zapp]  
⇒ S-MC@NLO matching to SHERPA shower and MEPS@NLO multi-jet merging
- **MUNICH** [multi-purpose parton-level Monte Carlo by S. Kallweit]  
⇒ very fast integration at NLO (Catani–Seymour) and NNLO ( $q_T$  subtraction)
- **BLHA and/or native interfaces** for MATCHBOX (HERWIG), POWHEG and other MC tools

# OpenLoops applications at (N)NLO QCD

## Results for $2 \rightarrow 4$ processes with massive b-quarks and off-shell top quarks

- S-MC@NLO for  $pp \rightarrow t\bar{t}b\bar{b}$  with  $m_b > 0$  [Cascioli, Maierhöfer, Moretti, Pozzorini, Siebert, arXiv:1309.5912]
- NLO for  $pp \rightarrow W^+W^-b\bar{b}$  with  $m_b > 0$  [Cascioli, Kallweit, Maierhöfer, Pozzorini, arXiv:1312.0546]

## NLO merging with OpenLoops+Sherpa and Herwig

- MEPS@NLO for  $l\bar{l}\nu\nu+0,1$  jets, [Cascioli, Höche, Krauss, Maierhöfer, Pozzorini, Siebert, arXiv:1309.0500]
- (1-loop)<sup>2</sup> merging for  $pp \rightarrow HH+0,1$  jets, [Maierhöfer, Papaefstathiou, arXiv:1401.0007]
- MEPS@NLO for  $WWW+0,1$  jets, [Höche, Krauss, Pozzorini, Schönherr, Thompson arXiv:1403.7516]
- MEPS@NLO for  $t\bar{t}+0,1,2$  jets, [Höche, Krauss, Maierhöfer, Pozzorini, Schönherr, Siebert arXiv:1402.6293]

## NNLO calculations for di-bosons and $t\bar{t}$ with OpenLoops+Munich

- $pp \rightarrow \gamma Z$  [Grazzini, Kallweit, Rathlev, Torre, arXiv:1309.7000]
- $q\bar{q} \rightarrow t\bar{t}$  [Abelof, Gehrmann-de Ridder, Maierhöfer, Pozzorini, arXiv:1404.6493]
- $pp \rightarrow ZZ$  [Cascioli, Gehrmann, Grazzini, Kallweit, Maierhöfer, von Manteuffel, Pozzorini, Rathlev, Tancredi, Weihs, arXiv:1405.2219]
- $pp \rightarrow W^+W^-$  [Gehrmann, Grazzini, Kallweit, Maierhöfer, von Manteuffel, Pozzorini, Rathlev, Tancredi arXiv:1408.5243]
- $pp \rightarrow W\gamma$  and  $Z\gamma$  [Grazzini, Kallweit, Rathlev, arXiv:1504.01330]