



LHC probe of Lepto-filic 2HDM for muon $g-2$

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In collaboration with A. Broggio, M. Passera, K.M. Patel, S.K. Vempati, arXiv:1409.3199
Z. Kang, M. Takeuchi, Y.L.S. Tsai, arXiv:1507.08067
(J.S. Kim, work in progress)

"Can a 2HDM explain muon g-2?"

$$\Delta a_\mu \equiv a_\mu^{\text{EXP}} - a_\mu^{\text{SM}} = +262(85) \times 10^{-11}$$

- Only in Lepton-specific (Type X) 2HDM through Barr-Zee two-loop with a light pseudoscalar A and large t_β . arXiv:1409.3199
- The parameter space limited by EWPD, vacuum stability & perturbativity, $h(126)$, and $B_s \rightarrow \mu\mu$.
- Stronger constraints on loop corrections to tau vertices from the lepton universality in $l \rightarrow l'\nu\nu$ & $Z \rightarrow ll$. (arXiv:1605.xxxxx)
- LHC probe of the model: a light A mainly decaying to $\tau\tau$. arXiv:1507.08067
$$pp \rightarrow h \rightarrow AA^{(*)} \rightarrow 4\tau; \quad pp \rightarrow H^{0,\pm} A \rightarrow AA + Z/W \rightarrow 4\tau + Z/W$$

4 types of 2HDM with natural flavor conservation

Impose Z_2 to couple only one Higgs to each down-type Yukawa

$$\Phi_2(+), \Phi_1(-); t_R(+), d_R(\pm), e_R(\pm)$$

Model	u_R^i	d_R^i	e_R^i		y_u^A	y_d^A	y_l^A	y_u^H	y_d^H	y_l^H	y_u^h	y_d^h	y_l^h
Type I	Φ_2	Φ_2	Φ_2	Type I	$\cot \beta$	$-\cot \beta$	$-\cot \beta$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$
Type II	Φ_2	Φ_1	Φ_1	Type II	$\cot \beta$	$\tan \beta$	$\tan \beta$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$-\frac{\sin \alpha}{\cos \beta}$	$-\frac{\sin \alpha}{\cos \beta}$
Lepton-specific	Φ_2	Φ_2	Φ_1	Type X	$\cot \beta$	$-\cot \beta$	$\tan \beta$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$-\frac{\sin \alpha}{\cos \beta}$
Flipped	Φ_2	Φ_1	Φ_2	Type Y	$\cot \beta$	$\tan \beta$	$-\cot \beta$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$-\frac{\sin \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\sin \beta}$

$$\begin{aligned}
 V_{2\text{HDM}} = & m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - \left[m_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.} \right] + \frac{1}{2} \lambda_1 \left(\Phi_1^\dagger \Phi_1 \right)^2 + \frac{1}{2} \lambda_2 \left(\Phi_2^\dagger \Phi_2 \right)^2 \\
 & + \lambda_3 \left(\Phi_1^\dagger \Phi_1 \right) \left(\Phi_2^\dagger \Phi_2 \right) + \lambda_4 \left(\Phi_1^\dagger \Phi_2 \right) \left(\Phi_2^\dagger \Phi_1 \right) + \left\{ \frac{1}{2} \lambda_5 \left(\Phi_1^\dagger \Phi_2 \right)^2 + \left[\lambda_6 \left(\Phi_1^\dagger \Phi_1 \right) \right. \right. \\
 & \left. \left. + \lambda_7 \left(\Phi_2^\dagger \Phi_2 \right) \right] \left(\Phi_1^\dagger \Phi_2 \right) + \text{h.c.} \right\}.
 \end{aligned}$$

Aligned/decoupled limit: $\sin(\beta - \alpha) \rightarrow 1$

$$\mathcal{L}_{gauge} = g_V m_V (s_{\beta-\alpha} h + c_{\beta-\alpha} H) VV + \dots$$

Model	u_R^i	d_R^i	e_R^i	y_u^A	y_d^A	y_l^A	y_u^H	y_d^H	y_l^H	y_u^h	y_d^h	y_l^h
Type I	Φ_2	Φ_2	Φ_2	$\cot \beta$	$-\cot \beta$	$-\cot \beta$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$
Type II	Φ_2	Φ_1	Φ_1	$\cot \beta$	$\tan \beta$	$\tan \beta$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$-\frac{\sin \alpha}{\cos \beta}$	$-\frac{\sin \alpha}{\cos \beta}$
Lepton-specific	Φ_2	Φ_2	Φ_1	$\cot \beta$	$-\cot \beta$	$\tan \beta$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$-\frac{\sin \alpha}{\cos \beta}$
Flipped	Φ_2	Φ_1	Φ_2	$\cot \beta$	$\tan \beta$	$-\cot \beta$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\cos \beta}$	$\frac{\sin \alpha}{\sin \beta}$	$\frac{\cos \alpha}{\sin \beta}$	$-\frac{\sin \alpha}{\cos \beta}$	$\frac{\cos \alpha}{\sin \beta}$

$$-\mathcal{L}_{\text{Yukawa}}^{\text{2HDMs}} = \sum_{f=u,d,l} \frac{m_f}{v} \left((y_f^h) h \bar{f} f + (y_f^H) H \bar{f} f - (y_f^A) A \bar{f} \gamma_5 f \right) + \left[\sqrt{2} V_{ud} H^+ \bar{u} \left(\frac{m_u}{v} (y_u^A) P_L + \frac{m_d}{v} (y_d^A) P_R \right) d + \sqrt{2} \frac{m_l}{v} (y_l^A) H^+ \bar{\nu} P_R l + h.c. \right]$$

$$y_\tau = -\frac{s_\alpha}{c_\beta} = s_{\beta-\alpha} - t_\beta c_{\beta-\alpha} \approx \pm 1 \quad \begin{matrix} \text{RS} \\ \text{WS} \end{matrix}$$

Muon $g-2$ from Barr-Zee 2-loop

- Needs a light A and large $y_{\mu,f}^A \approx t_\beta$:

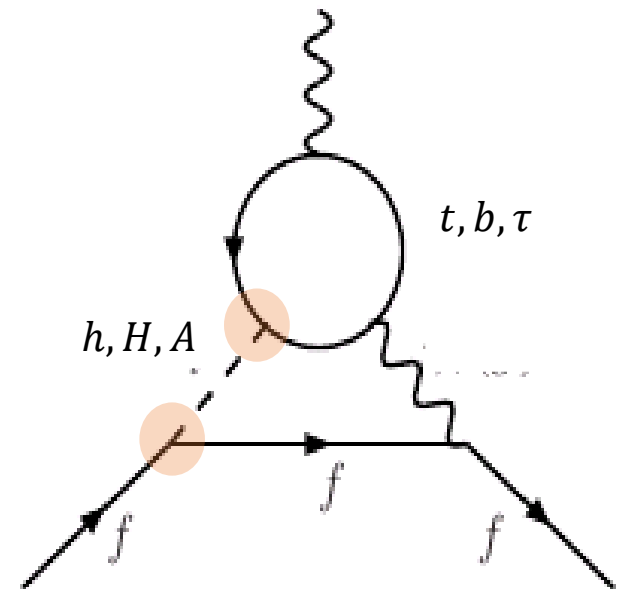
$$\delta a_\mu^{2\text{HDM}}(2\text{loop} - \text{BZ}) = \frac{G_F m_\mu^2}{4\pi^2 \sqrt{2}} \left(\frac{\alpha_{\text{em}}}{\pi} \right) \sum_{f; i=h,H,A} N_f^c Q_f^2 y_\mu^i y_f^i r_f^i g_i(r_f^i)$$

$$g_{h,H}(r) < 0$$

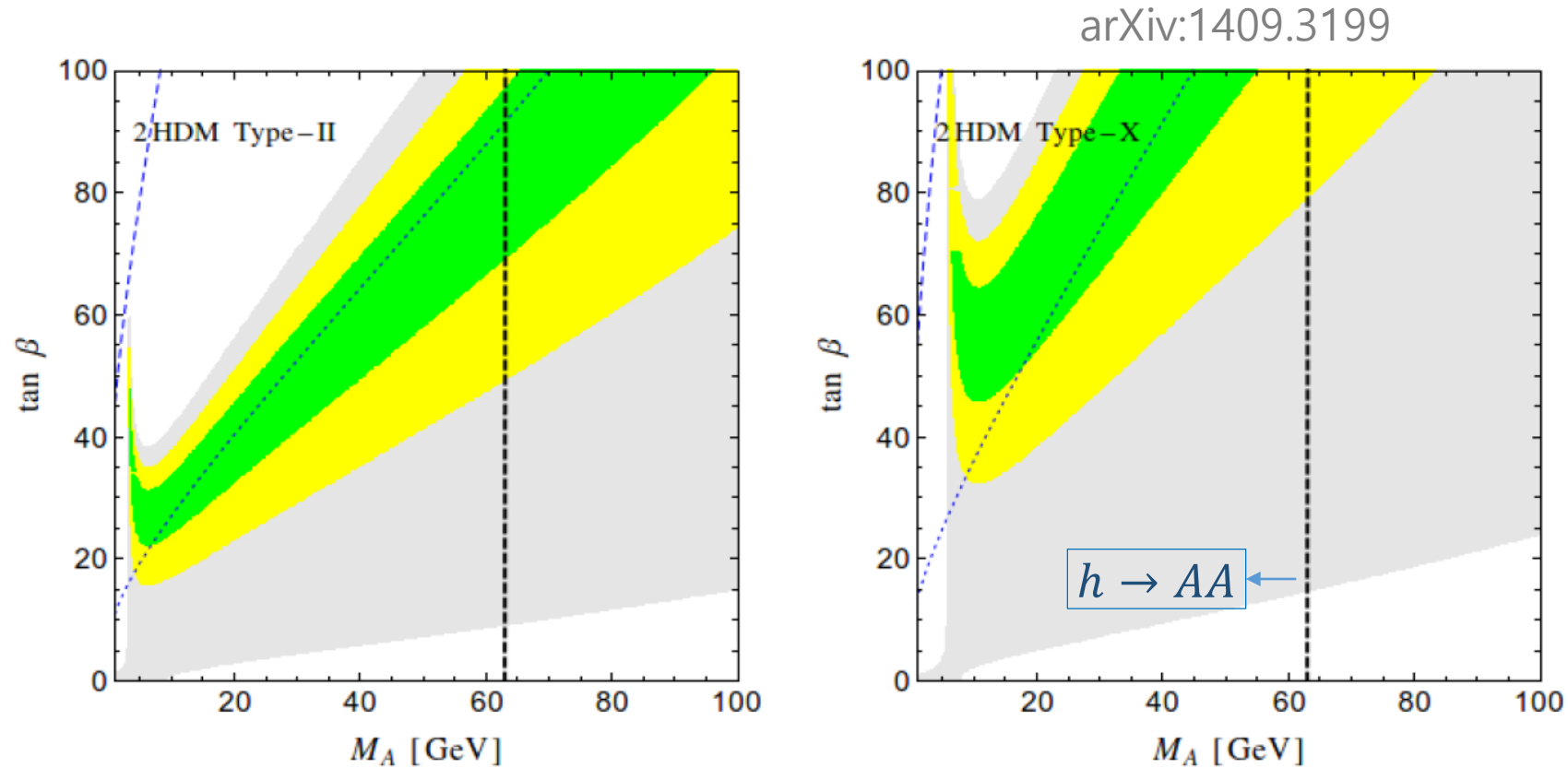
$$g_A(r) > 0$$

$$t_\beta^2 \quad m_f^2/m_{h,H,A}^2$$

	τ	t	b
I	$1/t_\beta^2$	$-1/t_\beta^2$	$1/t_\beta^2$
II	t_β^2	1	t_β^2
X	t_β^2	1	-1
Y	$1/t_\beta^2$	$-1/t_\beta^2$	-1



Muon $g-2$ in Type II & X



$$m_h (m_H) = 125 (200) \text{ GeV}$$

EWPD requires $m_A \ll m_H \approx m_{H^\pm}$

$$M_W^2 = \frac{M_Z^2}{2} \left[1 + \sqrt{1 - \frac{4\pi\alpha}{\sqrt{2}G_F M_Z^2} \frac{1}{1 - \Delta r}} \right]$$

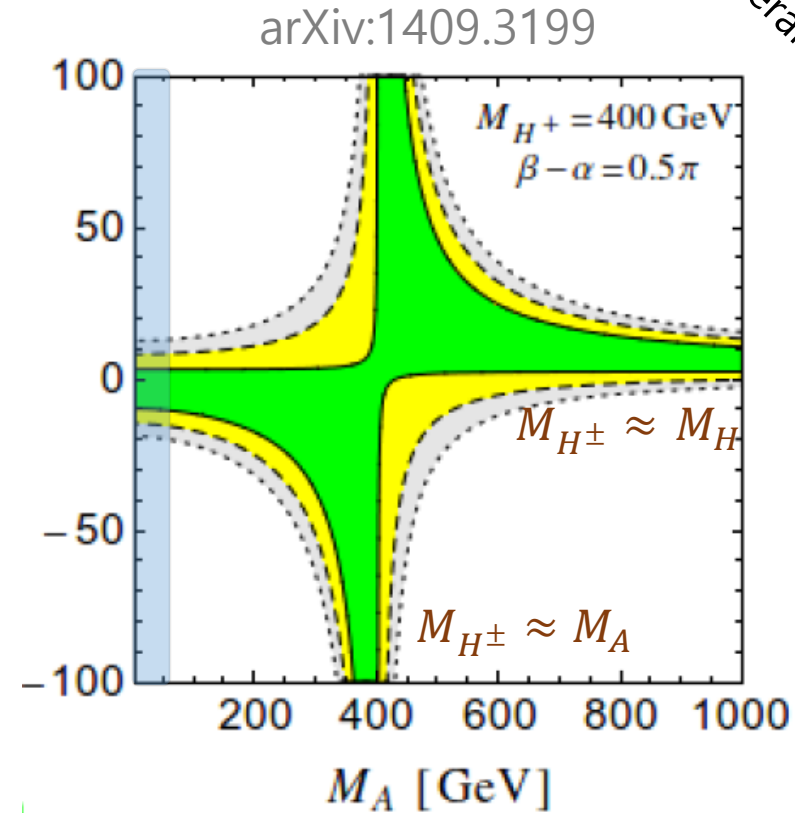
$$\sin^2 \theta_{\text{eff}}^{\text{lept}} = k_l (M_Z^2) \sin^2 \theta_W$$

$$\Delta r^{2\text{HDM}} = \Delta \alpha^{2\text{HDM}} - \frac{\cos^2 \theta_W}{\sin^2 \theta_W} \Delta \rho^{2\text{HDM}} + \dots,$$

$$\Delta k_l^{2\text{HDM}} = + \frac{\cos^2 \theta_W}{\sin^2 \theta_W} \Delta \rho^{2\text{HDM}} + \dots,$$

$$M_W^{\text{exp}} = 80.385 \pm 0.015 \text{ GeV},$$

$$\sin^2 \theta_{\text{eff}}^{\text{lept, exp}} = 0.23153 \pm 0.00016.$$



Generalized custodial symmetry
 Gerard-Herquet, 0703051

Vacuum stability & perturbativity

$$\lambda_{1,2} > 0, \quad \lambda_3 > -\sqrt{\lambda_1\lambda_2}, \quad |\lambda_5| < \lambda_3 + \lambda_4 + \sqrt{\lambda_1\lambda_2}$$

$$m_{12}^2(m_{11}^2 - m_{22}^2\sqrt{\lambda_1/\lambda_2})(\tan\beta - (\lambda_1/\lambda_2)^{1/4}) > 0$$

$$|\lambda_i| < 4\pi$$

In the limit of $\tan\beta \gg 1$ & $\sin(\beta - \alpha) \approx 1$,

$$M_A^2 = \frac{m_{12}^2}{\sin\beta \cos\beta} - \lambda_5 v^2,$$

$$M_{H^\pm}^2 = M_A^2 + \frac{1}{2}v^2(\lambda_5 - \lambda_4).$$

$$\lambda_2 v^2 \approx M_h^2$$

$$\lambda_3 v^2 \approx 2M_{H^\pm}^2 - (1 + s_{\beta-\alpha}y_\tau)M_H^2 + s_{\beta-\alpha}y_\tau M_h^2$$

$$\lambda_4 v^2 \approx -2M_{H^\pm}^2 + M_H^2 + M_A^2$$

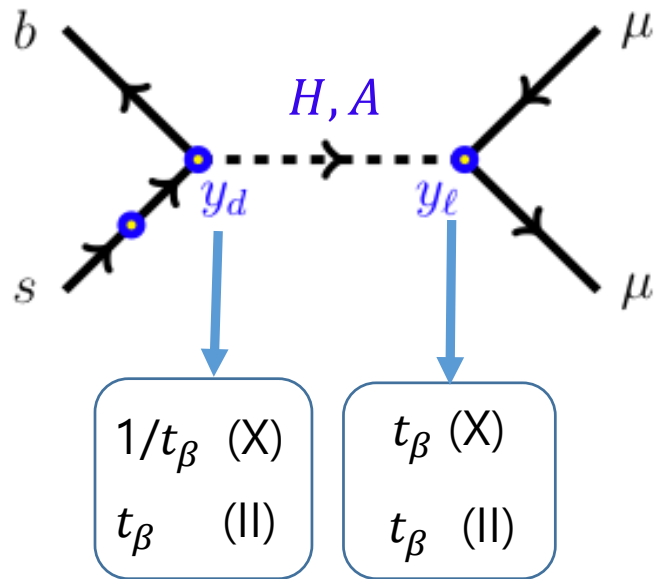
$$\lambda_5 v^2 \approx M_H^2 - M_A^2$$



$$\lambda_{hAA} \propto \lambda_5 - \lambda_3 - \lambda_4 \approx (1 + s_{\beta-\alpha}y_\tau)M_H^2 - 2M_A^2 - s_{\beta-\alpha}y_\tau M_h^2 < \sqrt{\lambda_1}vM_h$$

$$s_{\beta-\alpha}y_\tau = \pm 1 \begin{matrix} \text{RS} \\ \text{WS} \end{matrix}$$

$B_s \rightarrow \mu^+ \mu^-$ requires heavy A and low t_β



$$\propto \frac{t_\beta^2}{m_{H,A}^2} \text{ (II)}$$

$$\propto \frac{1}{m_{H,A}^2} \text{ (X)}$$

Type II excluded

Type X with $m_A \gtrsim 10 \text{ GeV}$

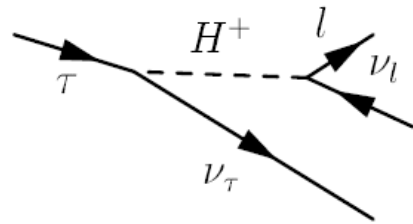
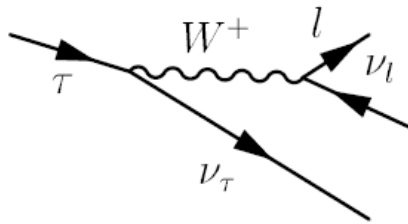
$1/t_\beta$ (X)
 t_β (II)

t_β (X)
 t_β (II)

$$Br(B_s \rightarrow \mu^+ \mu^-) = (2.9 \pm 0.7) \times 10^{-9} \text{ @ LHC}$$

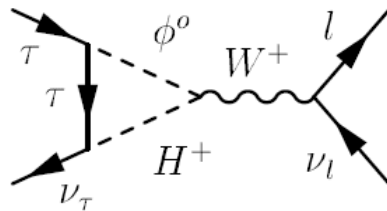
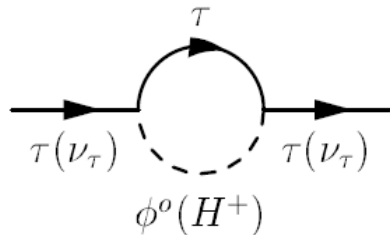
Lepton universality in τ decay

- Tree-level contribution from H^\pm .
- One-loop corrections mediated by A, H, H^\pm .



$$G_{\tau \rightarrow l} = G_F (1 + \delta_{tree} + \delta_{loop})$$

$$\delta_{tree} = \frac{m_\tau^2 m_l^2}{8 m_{H^\pm}^4} t_\beta^4 - \frac{m_l^2}{m_{H^\pm}^2} t_\beta^2 \kappa(m_l^2/m_\tau^2)$$



$$\delta_{loop} = \frac{G_F m_\tau^2 t_\beta^2}{16\sqrt{2} \pi^2} \left(3 + \frac{1}{2} \left[G \left(\frac{m_A}{m_{H^\pm}} \right) + s_{\beta-\alpha}^2 G \left(\frac{m_H}{m_{H^\pm}} \right) + c_{\beta-\alpha}^2 G \left(\frac{m_h}{m_{H^\pm}} \right) \right] \right)$$

Krawczyk, Temes, 0410248
Abe, et.al., 1504.07059

LU constraining the muon $g-2$ region

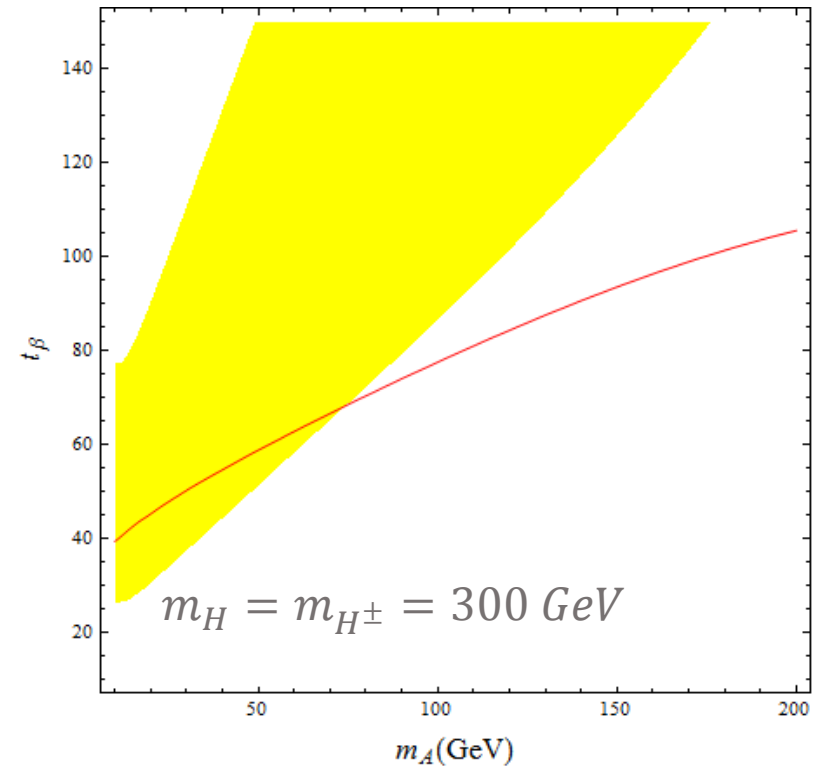
- Two independent data from $l \rightarrow l' \nu \nu$ and the combined data from $\tau \rightarrow \nu \pi / K$ leads to

$$\sqrt{\frac{3}{2}} \delta_{tree} = 0.0022 \pm 0.0017 \quad \text{HFAG, 1412.7515}$$

$$\delta_{loop} = 0.0001 \pm 0.0014$$

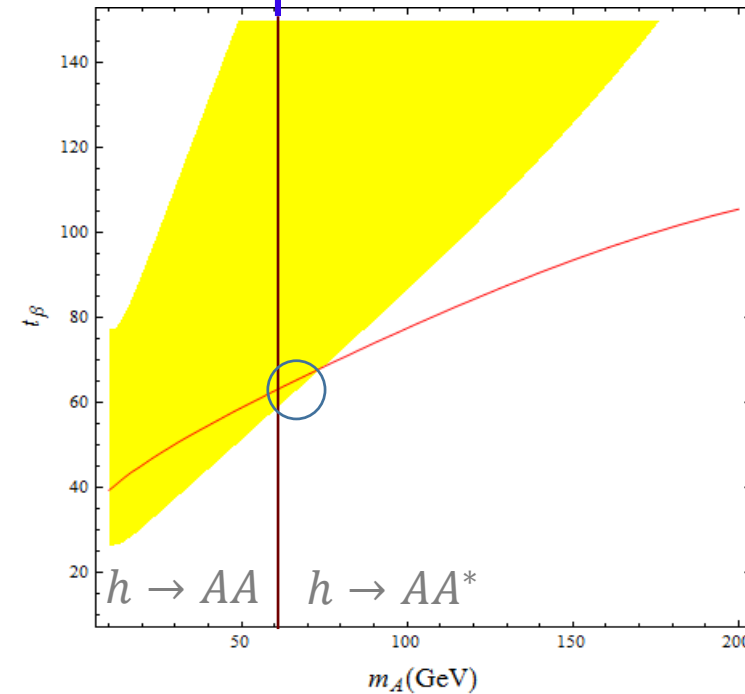
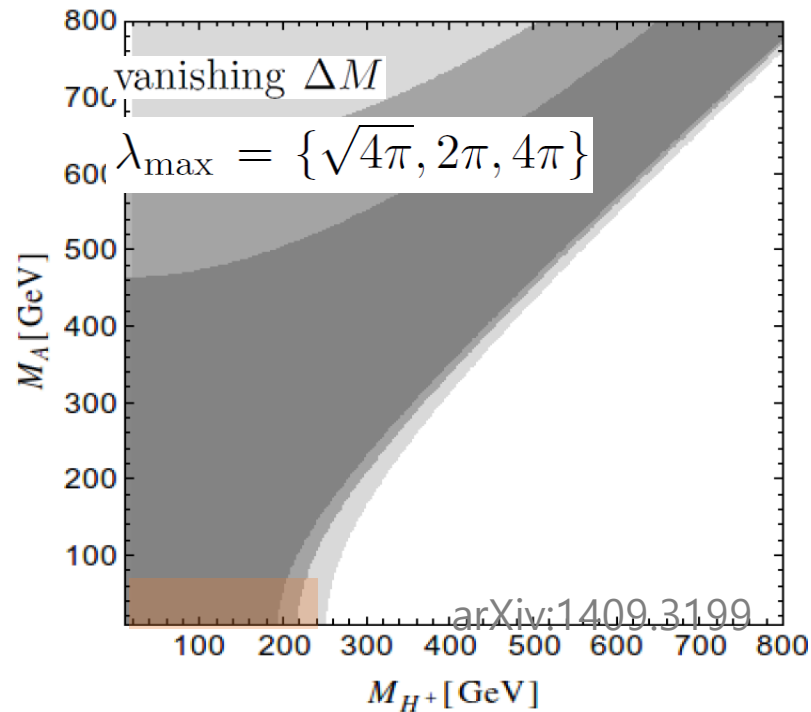
$$\sqrt{\frac{1}{2}} \delta_{tree} + \sqrt{2} \delta_{loop} = 0.0028 \pm 0.0019$$

- The muon $g-2$ favoured region is strongly limited:



L2HDM in the right-sign limit ($y_\tau s_{\beta-\alpha} \approx +1, c_{\beta-\alpha} \approx 0$)

$$\lambda_{hAA} v \approx -(1 + s_{\beta-\alpha} y_\tau) M_H^2 + 2M_A^2 + s_{\beta-\alpha} y_\tau M_h^2 > y_b v^2$$



$$63 \text{ GeV} \lesssim M_A \ll M_H \approx M_{H^\pm} \lesssim 250 \text{ GeV}$$

L2HDM in the wrong-sign limit ($y_\tau s_{\beta-\alpha} \approx -1, c_{\beta-\alpha} \approx \frac{2}{t_\beta}$)

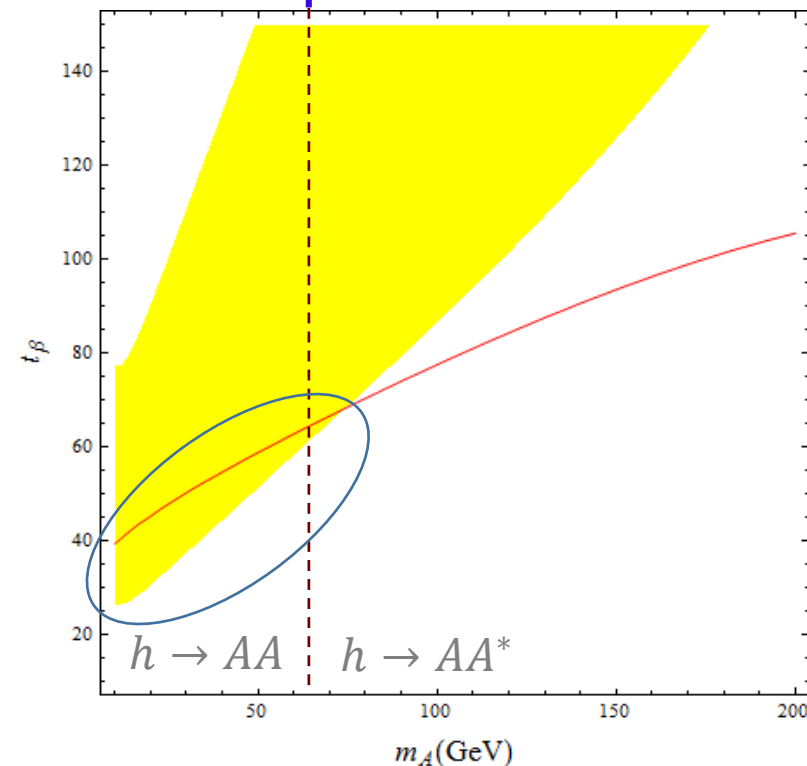
- $h \rightarrow AA$ can be arbitrarily suppressed even for $M_h \ll M_H$ allowed up to the perturbativity limit.

Wang, Han, arXiv:1412.4874

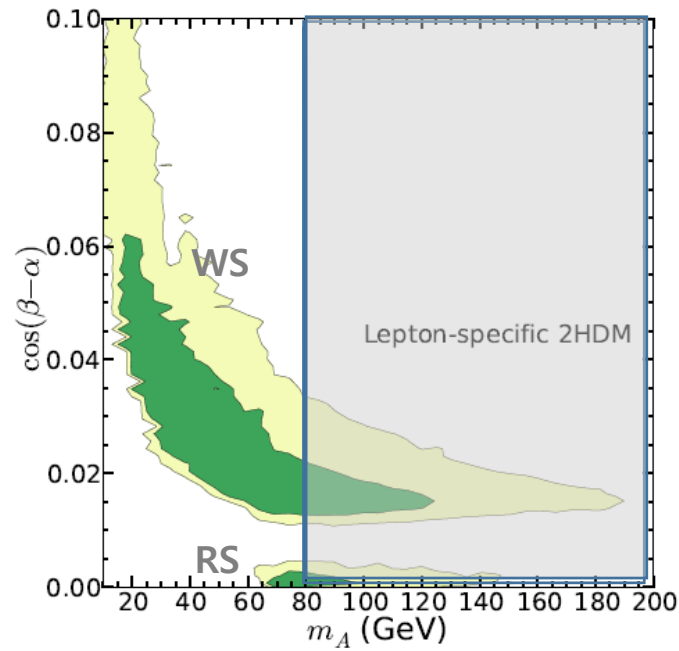
$$10 \text{ GeV} \lesssim m_A \ll m_H \approx m_{H^\pm} \lesssim \sqrt{4\pi}v$$

$$\lambda_{hAA}v \approx -(1 + s_{\beta-\alpha}y_\tau)M_H^2 + 2M_A^2 + s_{\beta-\alpha}y_\tau M_h^2 \rightarrow 0$$

$$y_\tau \approx -\frac{M_H^2 - 2M_A^2 - \lambda_{hAA}v}{M_H^2 - M_h^2}$$

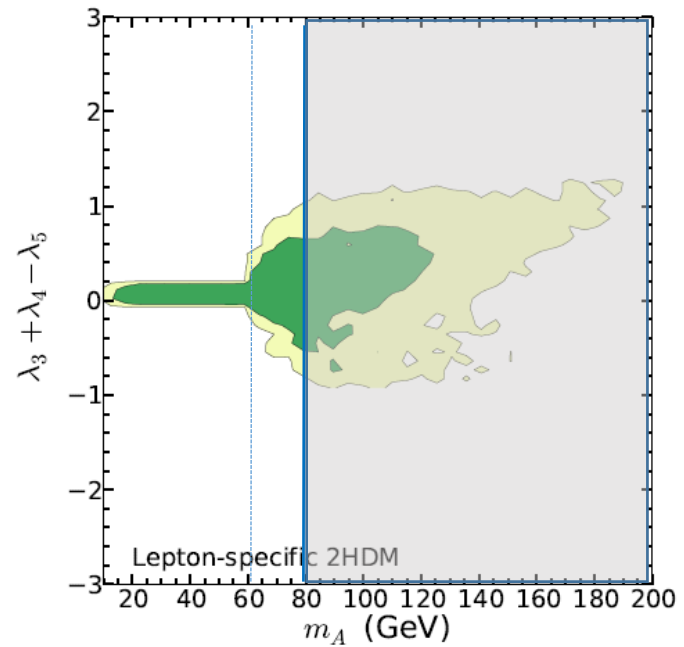


Allowed parameter space



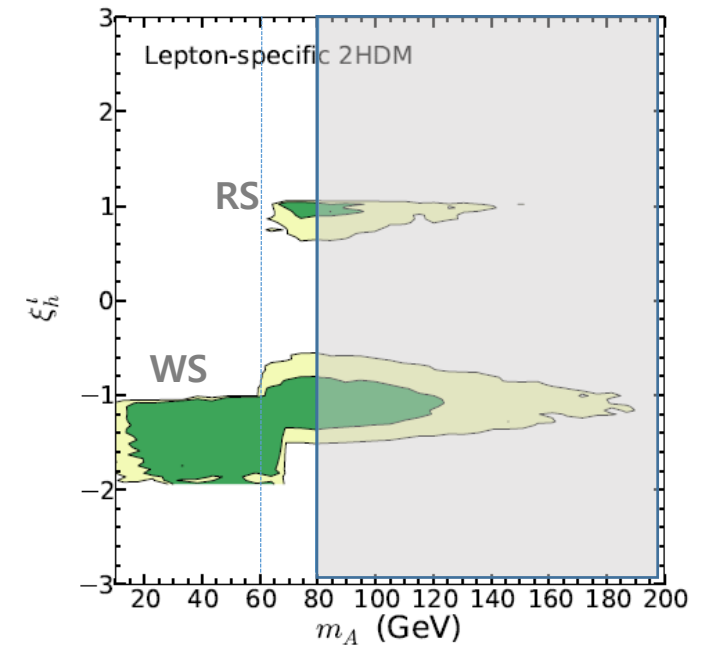
$\cos(\beta - \alpha)$

arXiv:1507.08067



$\lambda_{hAA} \propto \lambda_3 + \lambda_4 - \lambda_5$

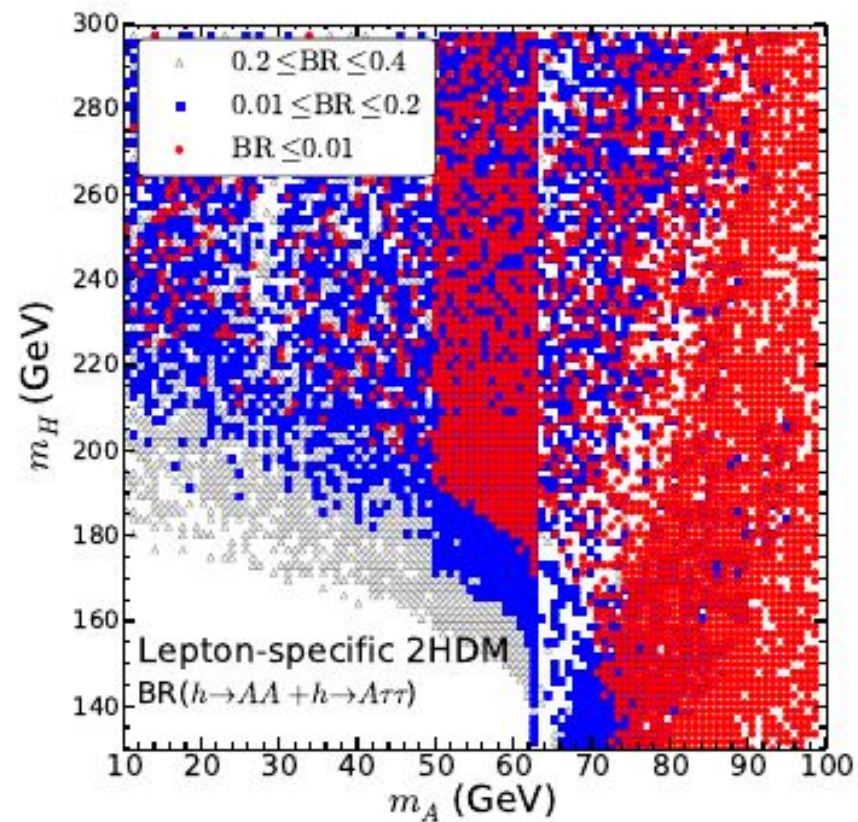
Assuming $BR(h \rightarrow AA) < 40\%$



y_τ

LHC signatures from $h \rightarrow AA^{(*)} \rightarrow 4\tau$?

arXiv:1507.08067



LHC signatures from $pp \rightarrow H^{0,\pm} A \rightarrow 3\tau/4\tau$

- EW production of extra Higgses decaying mainly to taus

$$pp \rightarrow H^\pm A \rightarrow AA + W^\pm \rightarrow 4\tau + W$$

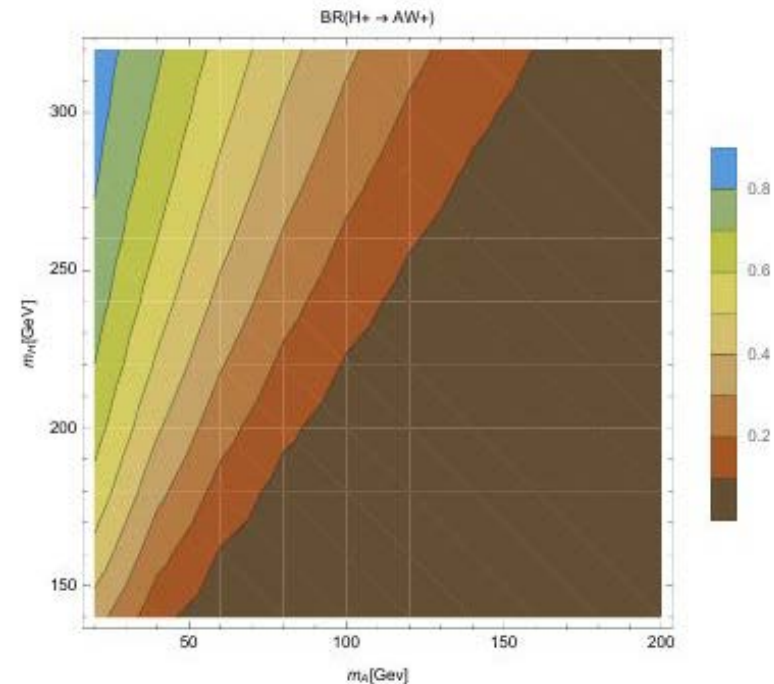
$$pp \rightarrow H^\pm A \rightarrow 3\tau + \nu$$

$$pp \rightarrow H^0 A \rightarrow AA + Z \rightarrow 4\tau + Z$$

$$pp \rightarrow H^0 A \rightarrow 4\tau$$

$$\tan \beta = 1.25 \left(\frac{m_A}{\text{GeV}} \right) + 25.$$

Region A: $m_{H^\pm} = m_H + 15 \text{ GeV}$

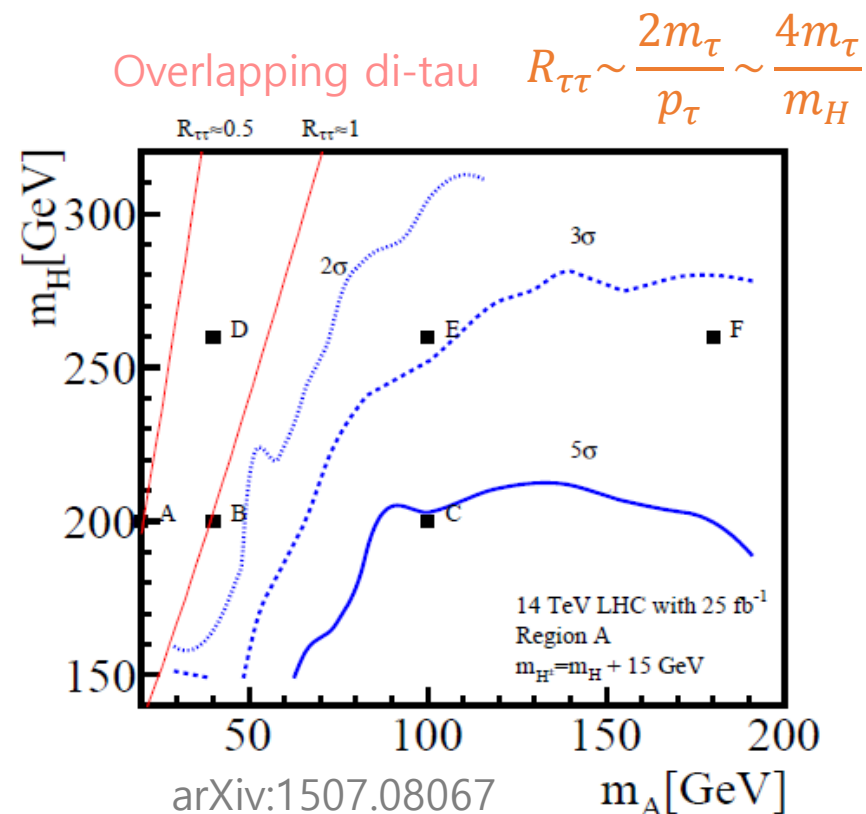


- Signal selection: $3\tau + MET, 0b, 0j$

LHC14 perspective with 25/fb

- Challenges to probe lighter A producing softer $\tau\tau$, and heavy H^\pm/H producing boosted $A(\tau\tau)$.
- Needs HL-LHC.

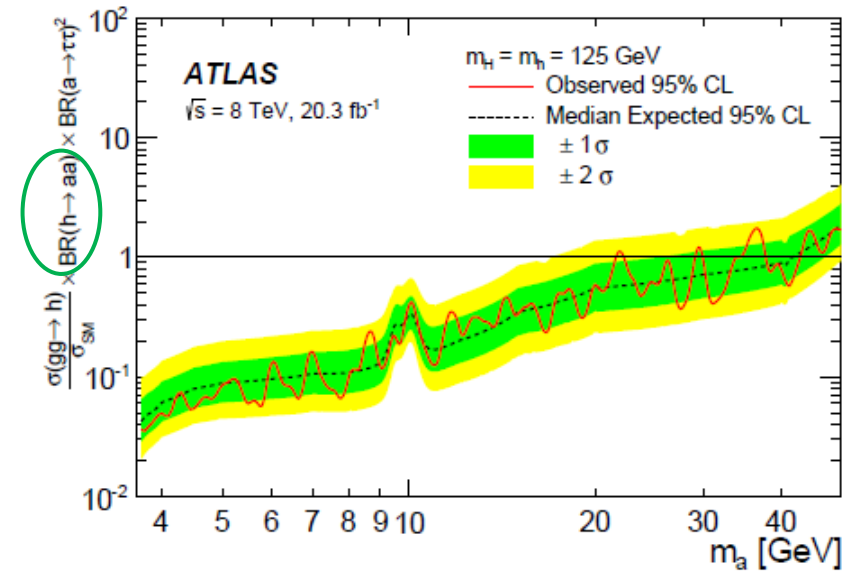
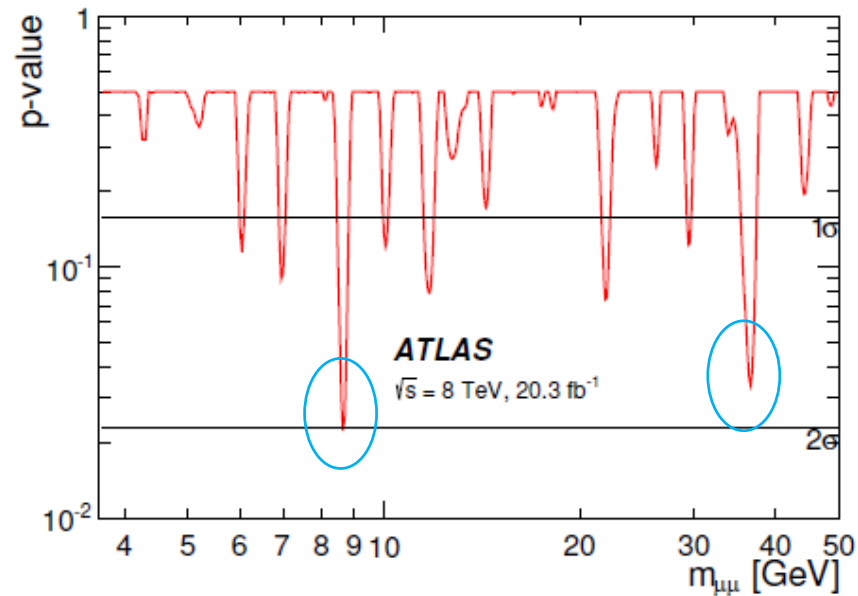
	point A	point B	point C	point D	point E	point F
m_A [GeV]	20	40	100	40	100	180
m_H [GeV]	200	200	200	260	260	260
total σ_{gen} [fb]	270.980	241.830	153.580	100.430	71.271	44.163
$n_\ell \geq 3$	6.606	16.681	21.713	7.110	11.962	8.822
$n_\tau \geq 3$	0.894	2.602	4.386	0.888	2.346	1.971
$E_T > 100$ GeV	0.201	0.547	1.179	0.209	0.765	0.926
$n_b = n_j = 0$	0.098	0.314	0.857	0.121	0.479	0.631
S/B	0.1	0.5	1.2	0.2	0.7	0.9
$S/\sqrt{B}_{25\text{fb}^{-1}}$	0.6	1.9	5.2	0.7	2.9	3.8



LHCski discussion

✓ Search for $h \rightarrow A A \rightarrow \mu\mu \tau\tau$

ATLAS, 1505.01609



✓ Also for $pp \rightarrow H^{0,\pm} A \rightarrow \mu\mu \tau(\tau) + X$?

Conclusion

- 2HDM-X is still a viable option for muon $g-2$.
- The most strong constraint comes from the lepton universality tests strongly limiting the allowed region (at 2σ):

$$m_A \approx 10 - 80 \text{ GeV} \ \& \ t_\beta \approx 25 - 60$$

$$\text{in the RS limit: } 63 \text{ GeV} \lesssim m_A \ll m_H \approx m_{H^\pm} \lesssim 250 \text{ GeV}$$

$$\text{in the WS limit: } 10 \text{ GeV} \lesssim m_A \ll m_H \approx m_{H^\pm} \lesssim \sqrt{4\pi}v$$

- LHC can search for $A \rightarrow \tau\tau$ ($\mu\mu$) through $pp \rightarrow h \rightarrow AA^{(*)} \rightarrow 4\tau$ ($\mu\mu\tau\tau$), or $pp \rightarrow H^{0,\pm}A \rightarrow 4\tau + X$ ($\mu\mu\tau\tau + X$).
- Challenge to probe a light A : more data and/or further studies on boosted di-tau tagging.

Back up

Muon g-2 from 1-loop

- For a light H and large $y_\mu^H \approx t_\beta$ (II, X):

$$\delta a_\mu^{2\text{HDM}}(1\text{loop}) = \frac{G_F m_\mu^2}{4\pi^2 \sqrt{2}} \sum_{j=h,H,A,H^\pm} (y_\mu^j)^2 r_\mu^j f_j(r_\mu^j)$$

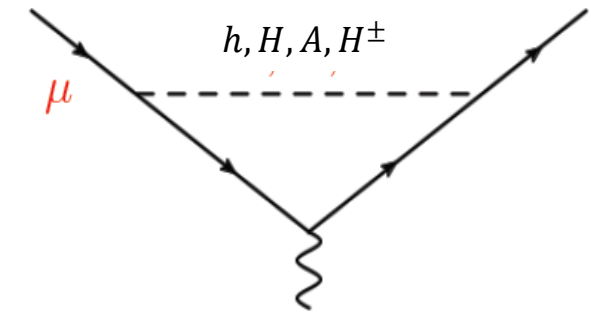
For $r_\mu^j = m_\mu^2/M_j^2 \ll 1$:

$$f_{h,H}(r) \sim -\ln r - 7/6 + O(r) > 0$$

$$f_A(r) \sim +\ln r + 11/6 + O(r) < 0$$

$$f_{H^\pm}(r) \sim -1/6 + O(r) < 0$$

roughly scales with m_μ^4 !



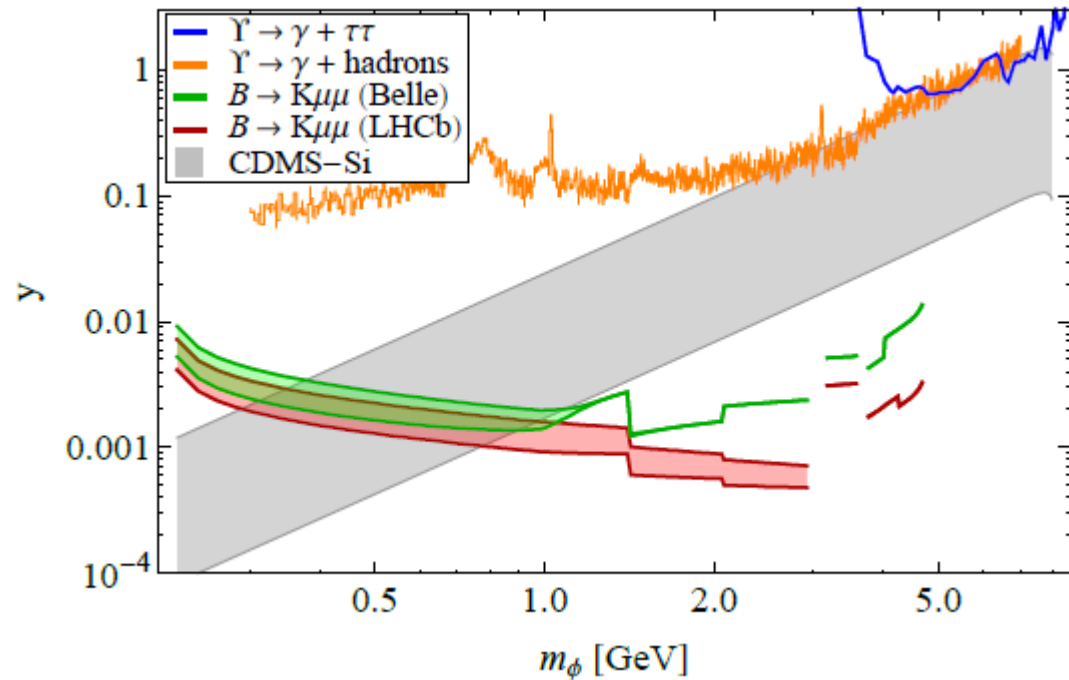
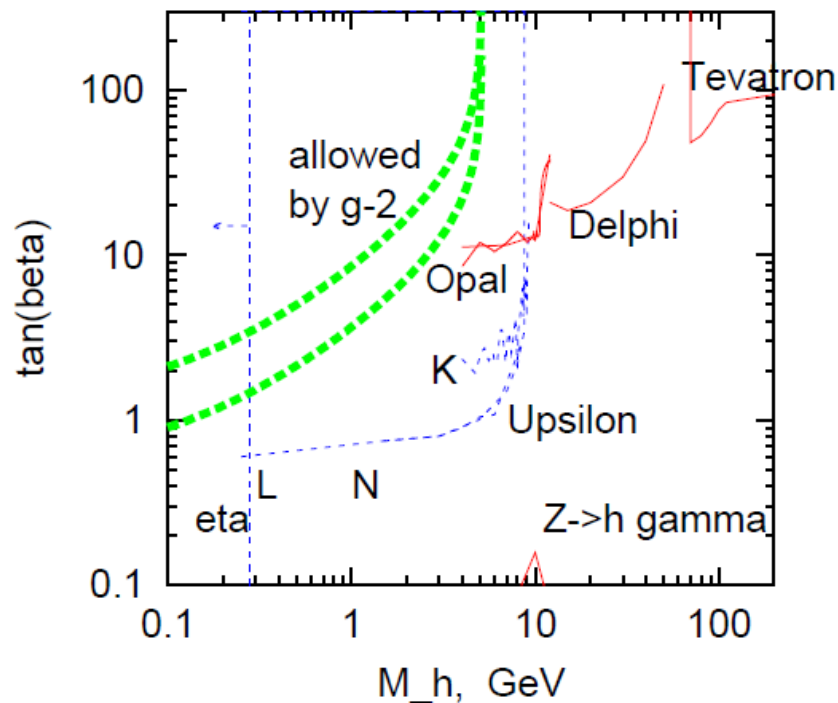
One-loop solution excluded!

- Muon $g-2$ requires H below 5GeV, but in contradiction with $\Upsilon \rightarrow \gamma + X, B \rightarrow K\mu\mu$ (& $B_s \rightarrow \mu\mu$).

Krawczyk, 0208076

Exclusion 95%C.L. for h in 2HDM(II)

Schmidt-Horberg, et.al., 1310.6752



Lepton Universality test by HFAG

HFAG, 1412.7515

- From pure leptonic processes: $l \rightarrow l' \nu \nu$

Note) Only two ratios are independent

$$\left(\frac{g_\tau}{g_\mu}\right) = 1.0011 \pm 0.0015, \quad \left(\frac{g_\tau}{g_e}\right) = 1.0029 \pm 0.0015, \quad \left(\frac{g_\mu}{g_e}\right) = 1.0018 \pm 0.0014$$

- From semi-hadronic processes: $\frac{(\tau \rightarrow \nu \pi / K)}{(\pi / K \rightarrow \mu \nu)}$

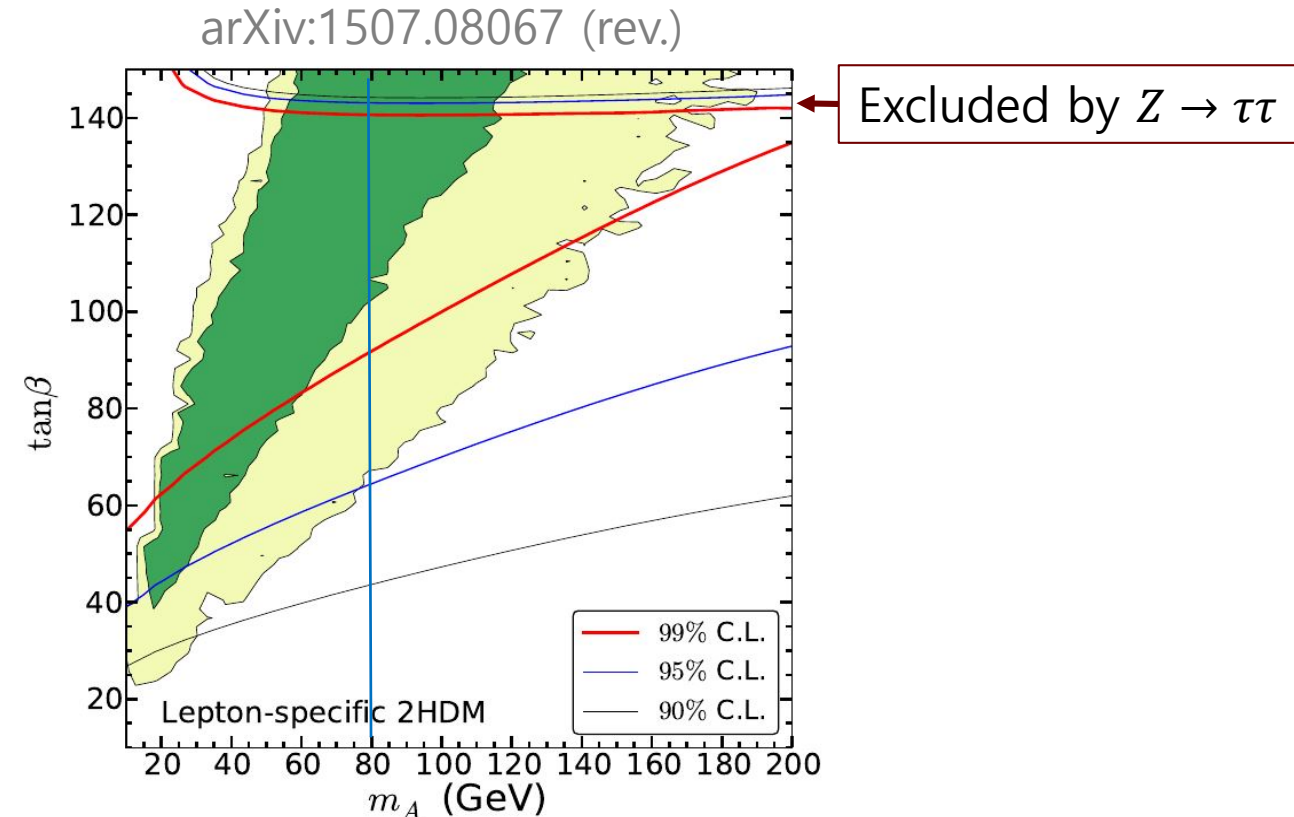
$$\left(\frac{g_\tau}{g_\mu}\right)_\pi = 0.9963 \pm 0.0027, \quad \left(\frac{g_\tau}{g_\mu}\right)_K = 0.9858 \pm 0.0071$$

- Combining the three in (g_τ/g_μ) : $\left(\frac{g_\tau}{g_\mu}\right)_{\tau+\pi+K} = 1.0001 \pm 0.0014$

Profile likelihood analysis

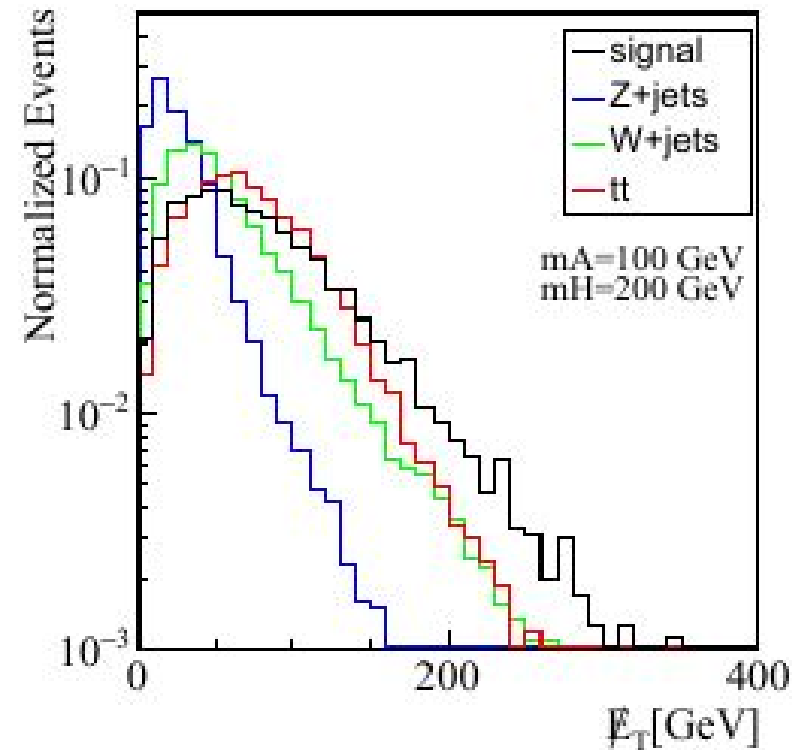
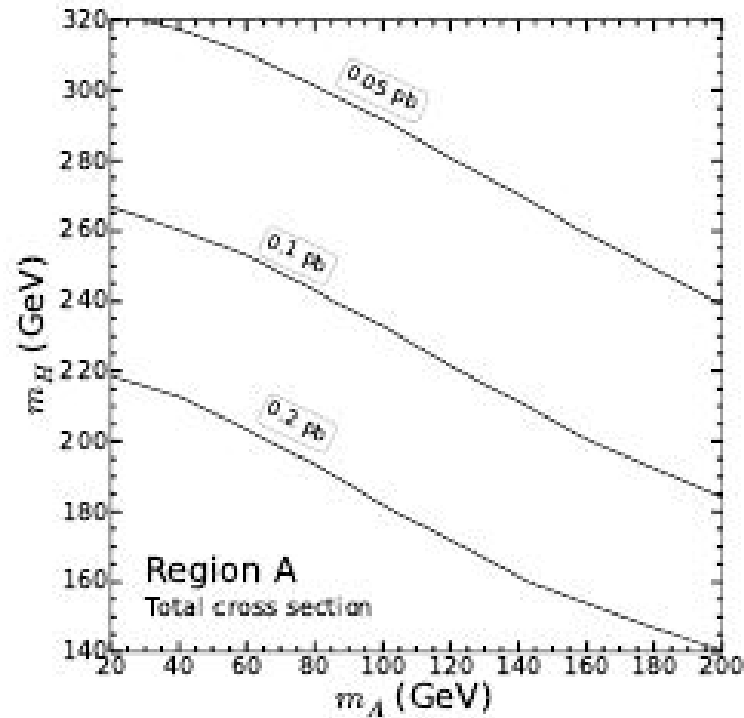
- Scanning through all the parameter space combining the h(125) data, muon g-2, EWPD, theoretical constraints, and the relevant LEP, B decay and LU limits.

2HDM parameter	Range
Scalar Higgs mass (GeV)	$125 < m_H < 400$
Pseudoscalar Higgs mass (GeV)	$10 < m_A < 400$
Charged Higgs mass (GeV)	$94 < m_{H^\pm} < 400$
$c_{\beta-\alpha}$	$0.0 < c_{\beta-\alpha} < 0.1$
$\tan \beta$	$10 < \tan \beta < 150$
λ_1	$0.0 < \lambda_1 < 4\pi$



LHC tau-rich signatures

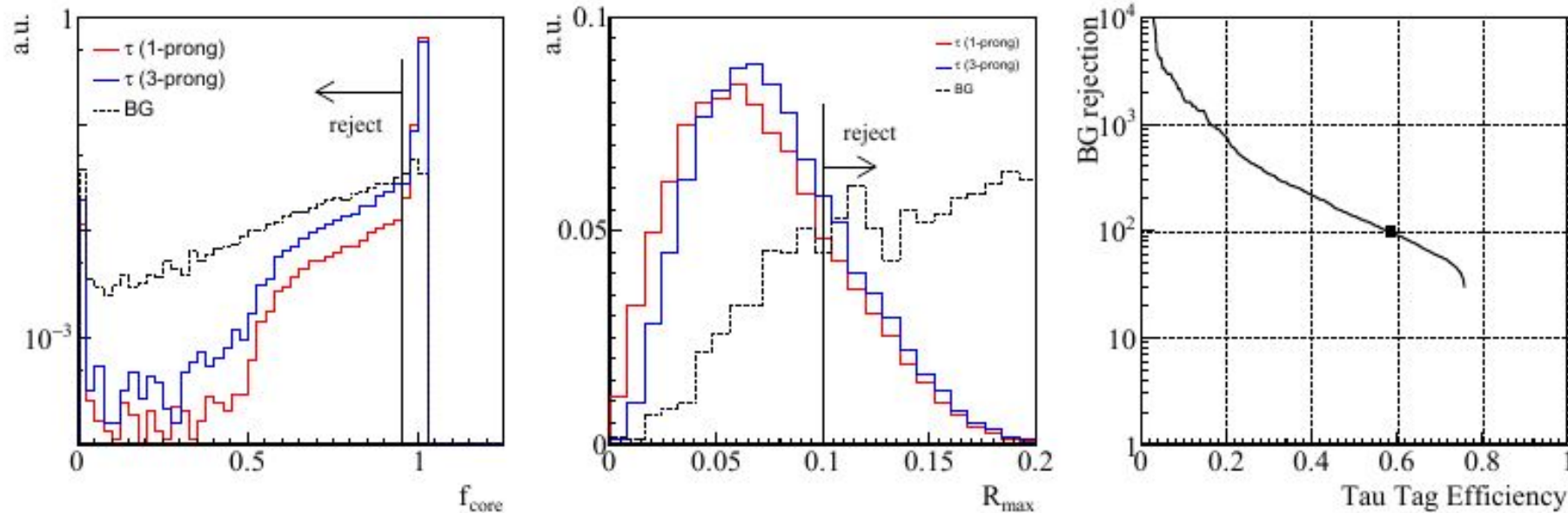
- Production X-section & missing signature:



Tau identification and reconstruction

- Our working point: $R_{max}^{cut} = 0.1, \epsilon_{BG-jets} \approx 1\% \rightarrow \epsilon_{\tau} \approx 60\%$

$$R_{max} = \max_{\text{tracks}} \Delta R(p_j, p_i) \quad \text{and} \quad f_{core} = \frac{\sum_{R < 0.1} E_T^{calo}}{\sum_{R < 0.2} E_T^{calo}}$$



Event selection cuts

ex) $m_A = 100 \text{ GeV}$ & $m_H = 200 \text{ GeV}$

selection cuts	point C	$t\bar{t}$	W +jets	Z +jets	WW	WZ	ZZ	total BG	S/B	$S/\sqrt{B}_{25\text{fb}^{-1}}$
total σ_{gen} [fb]	153.580	$102 \cdot 10^3$	$1365 \cdot 10^3$	$714 \cdot 10^3$	8125	942	112	$2190 \cdot 10^3$	-	-
$n_\ell \geq 3$	21.713	273.27	138.59	3412.84	6.495	88.937	26.965	3947.1	-	1.7
$n_\tau \geq 3$	4.386	5.837	13.776	91.324	0.070	0.343	0.174	111.52	0.04	2.1
$E_T > 100 \text{ GeV}$	1.179	1.482	0.232	1.244	0.000	0.018	0.003	2.980	0.4	3.4
$n_b = n_j = 0$	0.857	0.163	0.000	0.505	0.000	0.017	0.003	0.688	1.2	5.2

LHC8 limits

- mostly from chargino-neutralino searches.

