

Heavy Flavour Physics

Lecture 3 of 3

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Contents

- Part 1
 - Why is flavour physics interesting?
- Part 2
 - What do we know from previous experiments?
- **Part 3**
 - What do we hope to learn from current and future heavy flavour experiments?

Today I'd better cover Part 3

(no really)

CP violation in decay

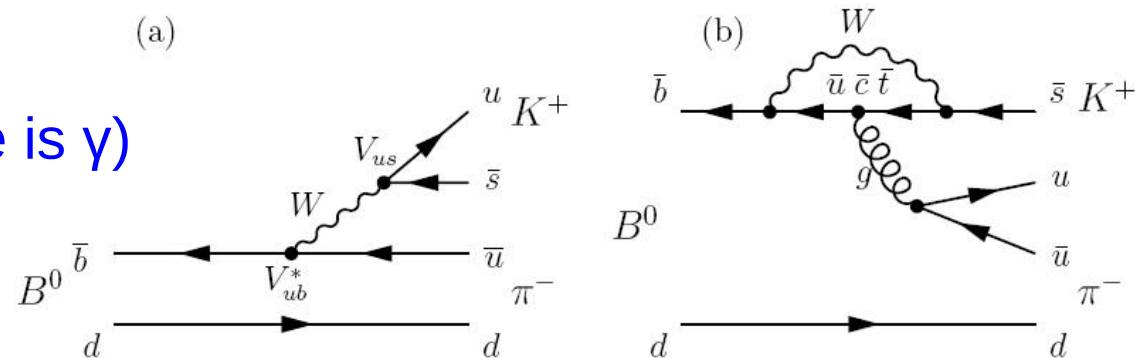
- Condition for CPV in decay: $|\bar{A}/A| \neq 1$
- Need \bar{A} and A to consist of (at least) two parts
 - with different weak (φ) and strong (δ) phases
- Often realised by “tree” and “penguin” diagrams

$$A = |T|e^{i(\delta_T - \phi_T)} + |P|e^{i(\delta_P - \phi_P)} \quad \bar{A} = |T|e^{i(\delta_T + \phi_T)} + |P|e^{i(\delta_P + \phi_P)}$$

$$A_{CP} = \frac{|\bar{A}|^2 - |A|^2}{|\bar{A}|^2 + |A|^2} = \frac{2|T||P|\sin(\delta_T - \delta_P)\sin(\phi_T - \phi_P)}{|T|^2 + |P|^2 + 2|T||P|\cos(\delta_T - \delta_P)\cos(\phi_T - \phi_P)}$$

Example: $B \rightarrow K\pi$

(weak phase difference is γ)



Feynman tree (a) and penguin (b) diagrams for the $B_d^0 \rightarrow K^+ \pi^-$ decay

The famous penguin story

Penguin diagram

From Wikipedia, the free encyclopedia

In quantum field theory, **penguin diagrams** are a class of Feynman diagrams which are important for understanding CP violating processes in the standard model.

They were first isolated and studied by Mikhail Shifman, Arkady Vainshtein, and Valentin Zakharov.^[1] The processes which they describe were first directly observed in 1991 and 1994 by the CLEO collaboration.

Origin of the name

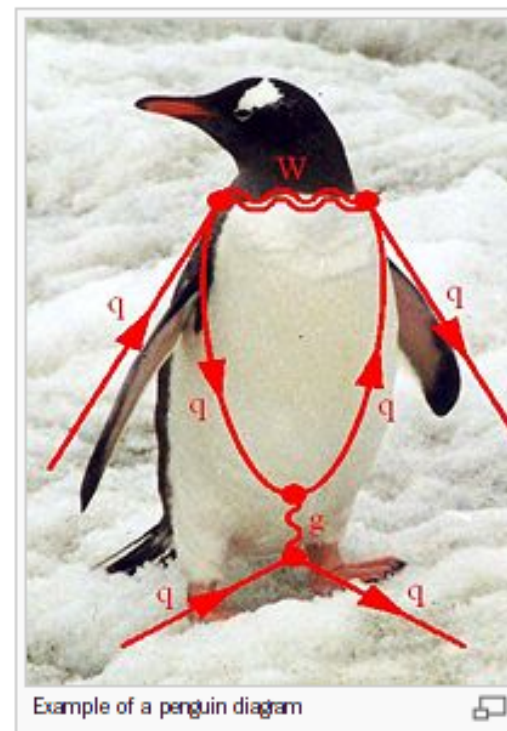
[edit]

John Ellis was the first to refer to a certain class of Feynman diagrams as **penguin diagrams**, due in part to their shape, and in part to a legendary bar-room bet with Melissa Franklin. According to John Ellis:^[2]

“ Mary K. [Gaillard], Dimitri [Nanopoulos] and I first got interested in what are now called penguin diagrams while we were studying CP violation in the Standard Model in 1976... The penguin name came in 1977, as follows.

In the spring of 1977, Mike Chanowitz, Mary K and I wrote a paper on GUTs predicting the b quark mass before it was found. When it was found a few weeks later, Mary K, Dimitri, Serge Rudaz and I immediately started working on its phenomenology. That summer, there was a student at CERN, Melissa Franklin who is now an experimentalist at Harvard. One evening, she, I, and Serge went to a pub, and she and I started a game of darts. We made a bet that if I lost I had to put the word penguin into my next paper. She actually left the darts game before the end, and was replaced by Serge, who beat me. Nevertheless, I felt obligated to carry out the conditions of the bet.

For some time, it was not clear to me how to get the word into this b quark paper that we were writing at the time. Then, one evening, after working at CERN, I stopped on my way back to my apartment to visit some friends living in Meyrin where I smoked some illegal substance. Later, when I got back to my apartment and continued working on our paper, I had a sudden flash that the famous diagrams look like penguins. So we put the name into our paper, and the rest, as they say, is history.



The famous penguin story

Penguin diagram

From Wikipedia, the free encyclopedia

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They were first isolated and studied by Marciano and Susskind in 1975. They were first directly observed in 1991 and 1994 by the CLEO collaboration.

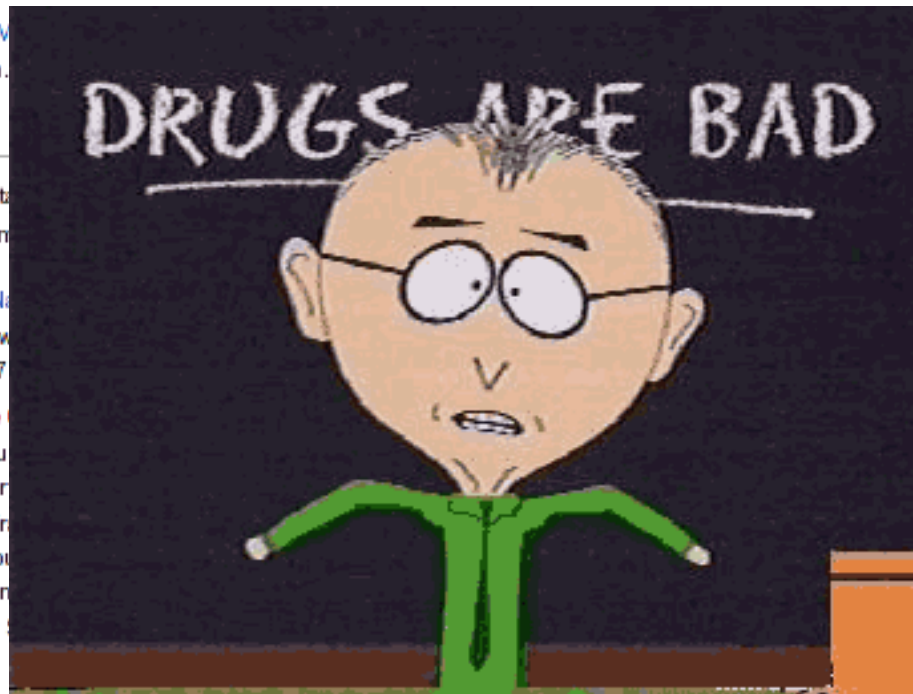
Origin of the name

John Ellis was the first to refer to a certain shape, and in part to a legendary bar-room

“ Mary K. [Gaillard], Dimitri [Nemenman] and I were talking about penguin diagrams while we were in the bar. The penguin name came in 1977.

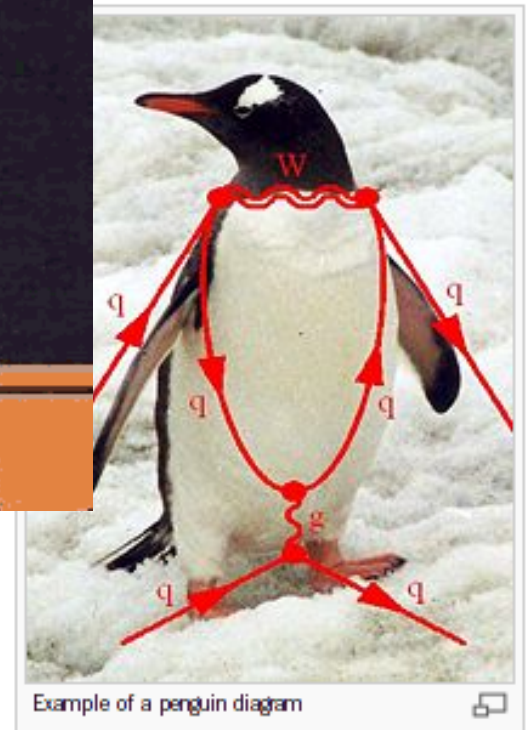
In the spring of 1977, Mike [Mason] and I were calculating the quark mass before it was found. Mike [Mason] and I immediately started working on it. I was a post-graduate student at CERN, Melissa [Frankfurt] was a post-graduate student there, I, and Serge went to a party. I lost I had to put the word penguin at the end, and was replaced by the word quark. The conditions of the bet.

For some time, it was not clear to me how to get the word into this b quark paper that we were writing at the time. Then, one evening, after working at CERN, I stopped on my way back to my apartment to visit some friends living in Meyrin where I smoked some illegal substance. Later, when I got back to my apartment and continued working on our paper, I had a sudden flash that the famous diagrams look like penguins. So we put the name into our paper, and the rest, as they say, is history.



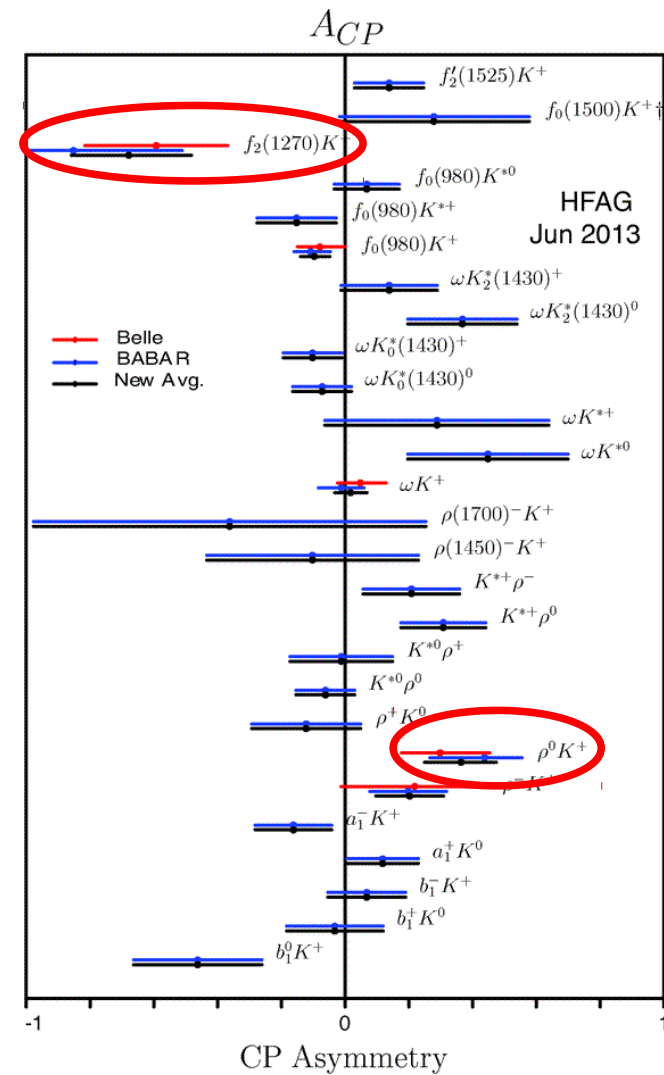
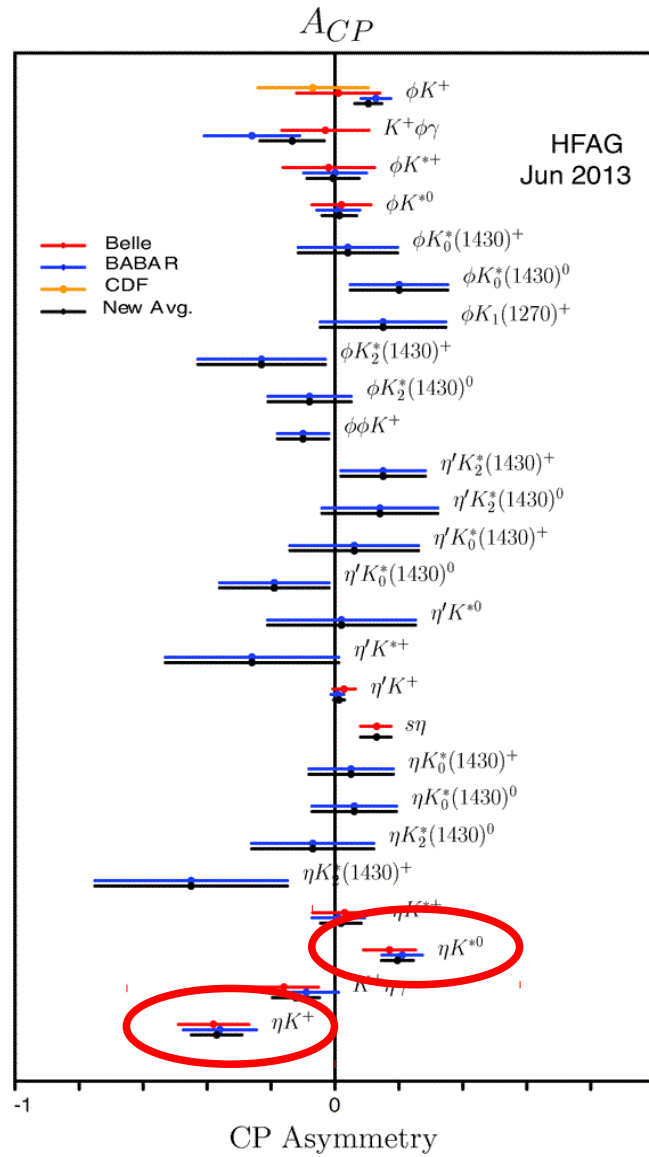
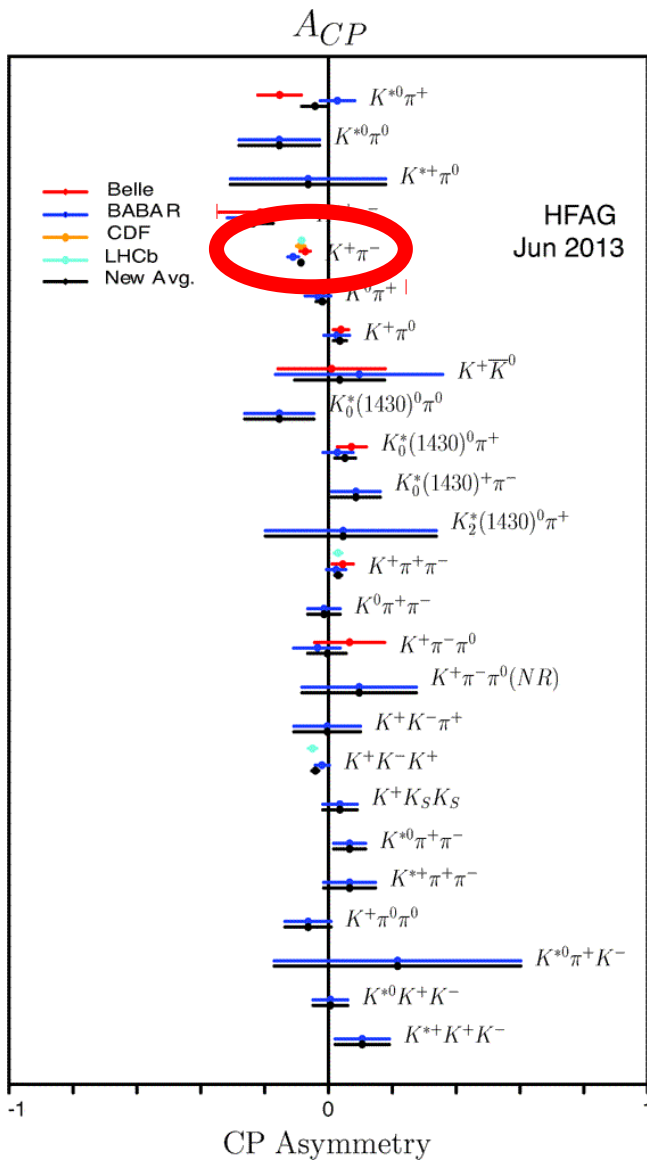
describe were first directly observed in

[edit]



Example of a penguin diagram

Direct CP asymmetries in charmless hadronic B decays



Direct CP violation in $B \rightarrow K\pi$

- Direct CP violation in $B \rightarrow K\pi$ sensitive to γ
too many hadronic parameters \Rightarrow need theory input
- NB. interesting deviation from naïve expectation

“ $K\pi$ puzzle”

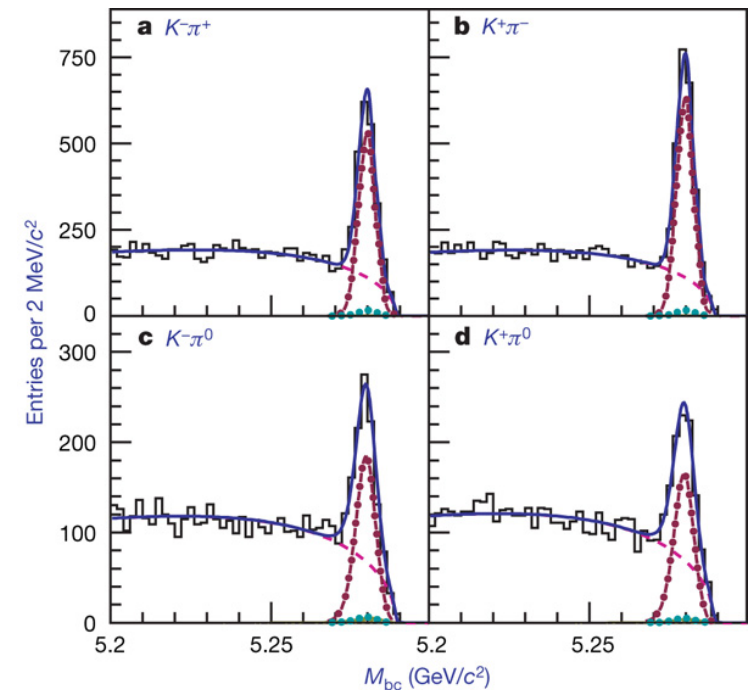
$$A_{\text{CP}}(K^-\pi^+) = -0.087 \pm 0.008$$

$$A_{\text{CP}}(K^-\pi^0) = +0.037 \pm 0.021$$

HFAG averages

Could be a sign of new physics ...
... first need to rule out possibility of
larger than expected QCD corrections

Belle Nature 452 (2008) 332



Clean observables in $B \rightarrow K\pi$ (etc.)

- Measure more $B_{u,d} \rightarrow K\pi$ decays & relate by isospin
- Perform similar analysis on $B \rightarrow K^*\pi$ &/or $B \rightarrow K\rho$
 - Dalitz plot analyses of $K\pi\pi$ final states extract both amplitudes and relative phases \rightarrow more observables
- Measure $B_s \rightarrow KK$ decays & relate by U-spin
 - e.g. relation between time-dependent CP violation observables in $B_s \rightarrow K^+K^-$ and $B^0 \rightarrow \pi^+\pi^-$
- Dalitz plot analyses of $B_{(s)} \rightarrow hhh$

Note: flavour symmetries very useful

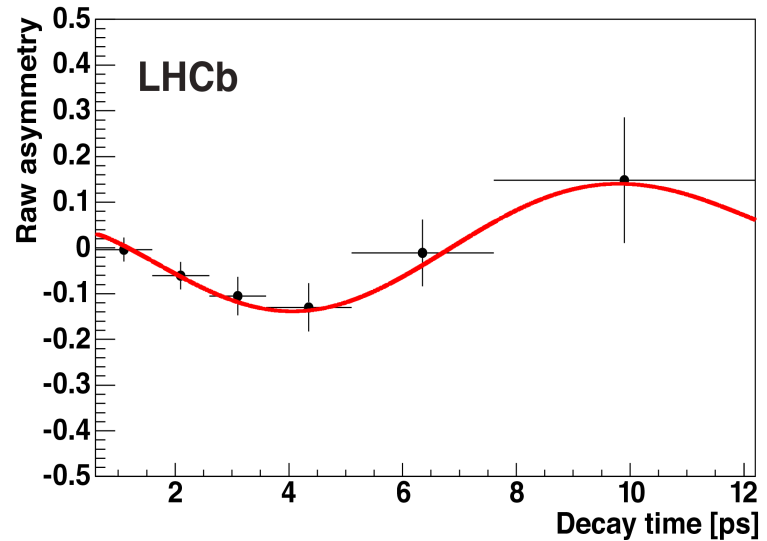
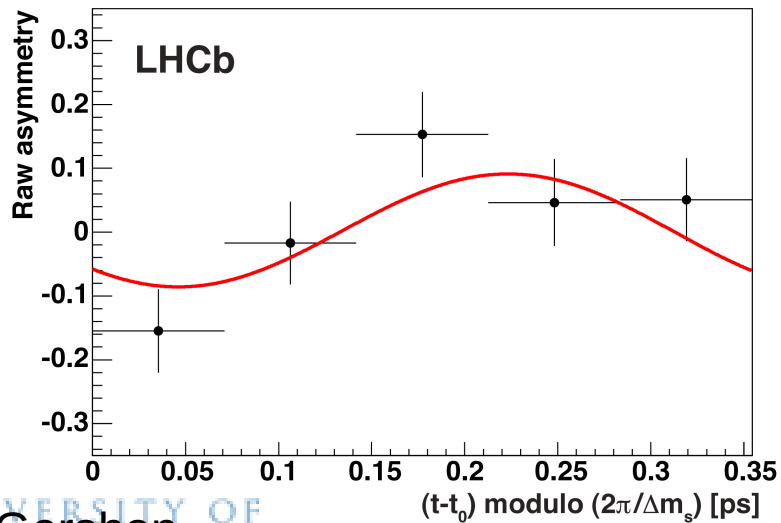
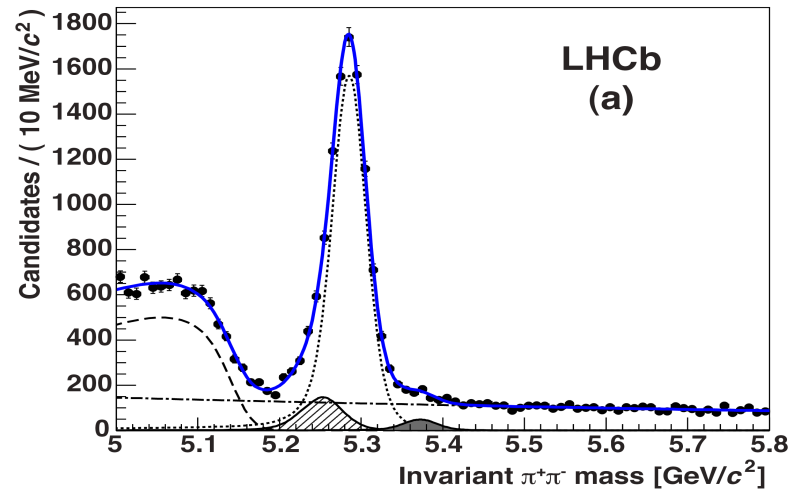
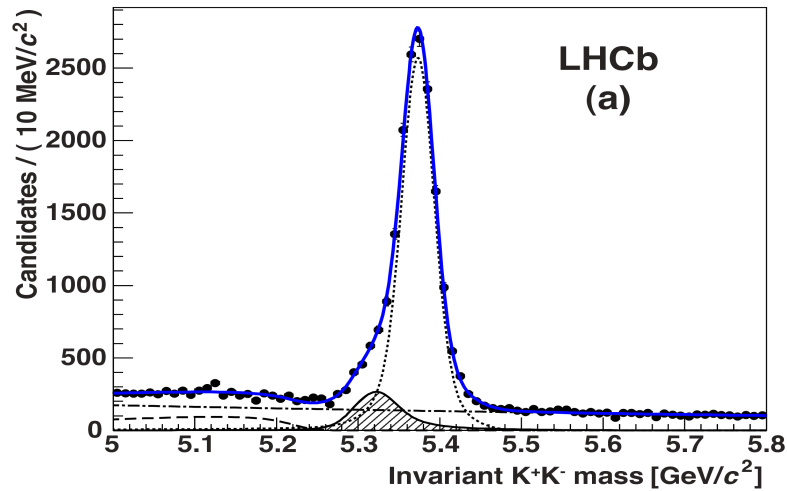
But, still get theory error from symmetry breaking (difficult to evaluate)

... data driven methods will win in the end (unless miracle breakthrough)

$$B^0 \rightarrow \pi^+ \pi^- \text{ \& \ } B_s^0 \rightarrow K^+ K^-$$

First CP violation measurements in these channels
at a hadron collider ($B^0 \rightarrow \pi^+ \pi^-$) / ever ($B_s^0 \rightarrow K^+ K^-$)

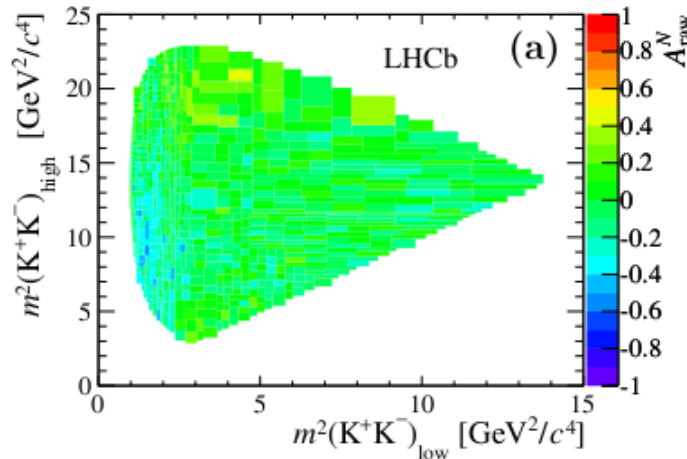
JHEP 10 (2013) 183



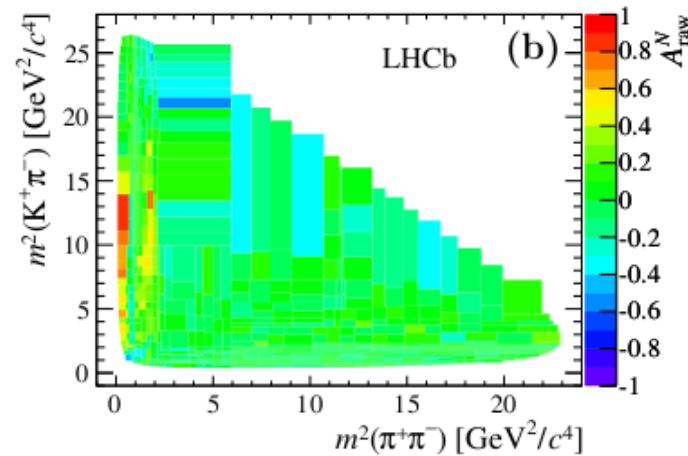
Latest results on multibody charmless B decays

PRD 90 (2014) 112004

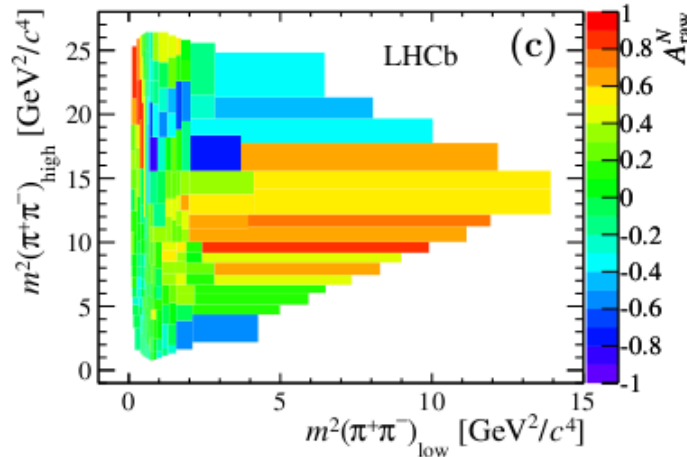
$B \rightarrow KKK$



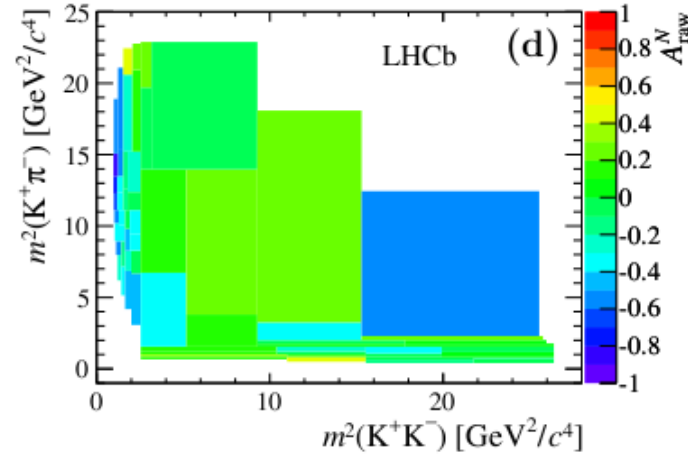
$B \rightarrow K\pi\pi$



$B \rightarrow \pi\pi\pi$



$B \rightarrow KK\pi$



Importance of γ from $B \rightarrow DK$

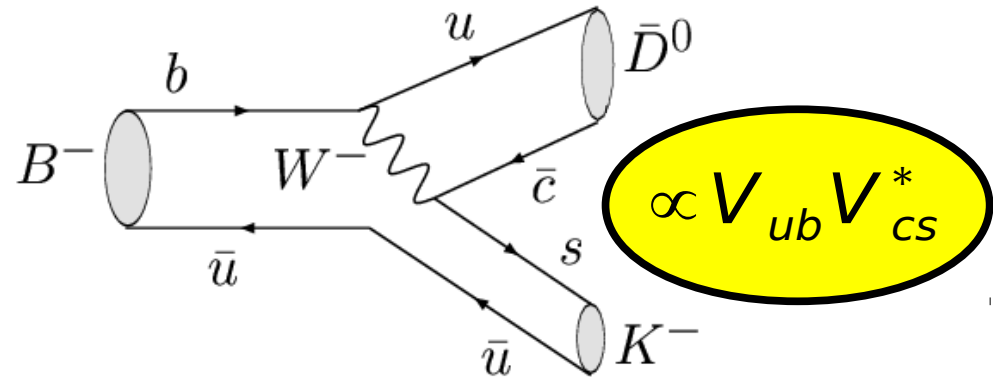
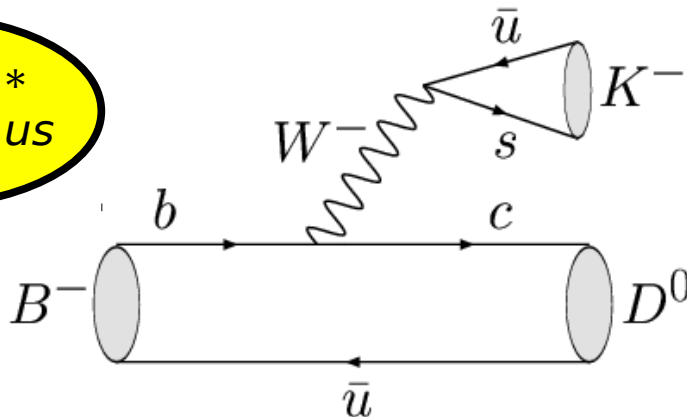
- γ plays a unique role in flavour physics

the only CP violating parameter that can be measured through tree decays (*)

(*) more-or-less

- A benchmark Standard Model reference point
 - doubly important after New Physics is observed

$$\propto V_{cb} V_{us}^*$$



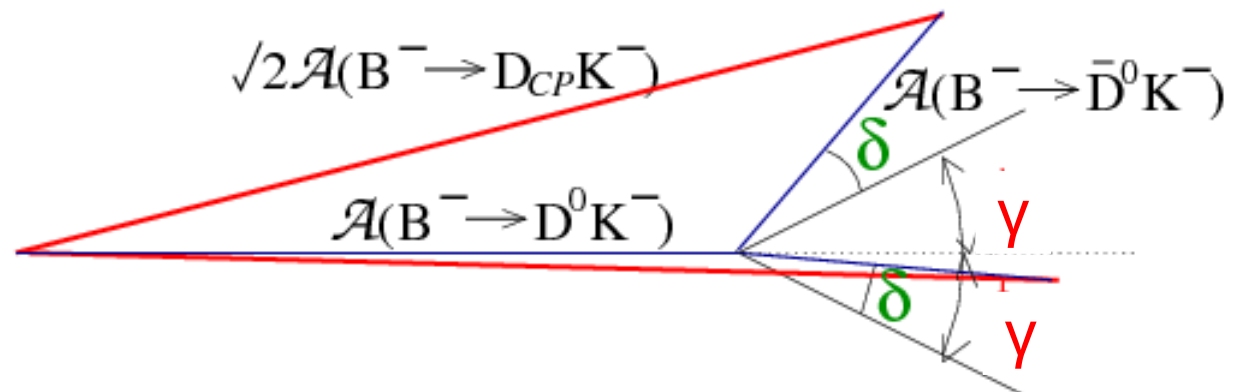
$$\propto V_{ub} V_{cs}^*$$

Variants use different B or D decays

require a final state common to both D^0 and \bar{D}^0

Why is $B \rightarrow DK$ so nice?

- For theorists:
 - theoretically clean: no penguins; factorisation works
 - all parameters can be determined from data
- For experimentalists:
 - many different observables (different final states)
 - all parameters can be determined from data
 - γ & δ_B (weak & strong phase differences), r_B (ratio of amplitudes)



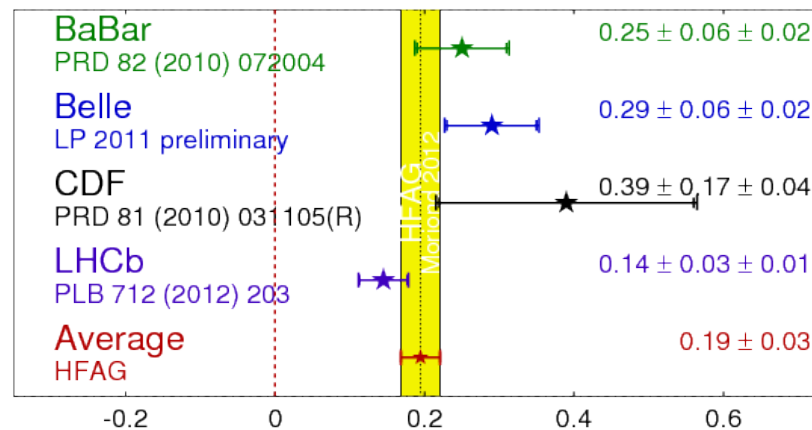
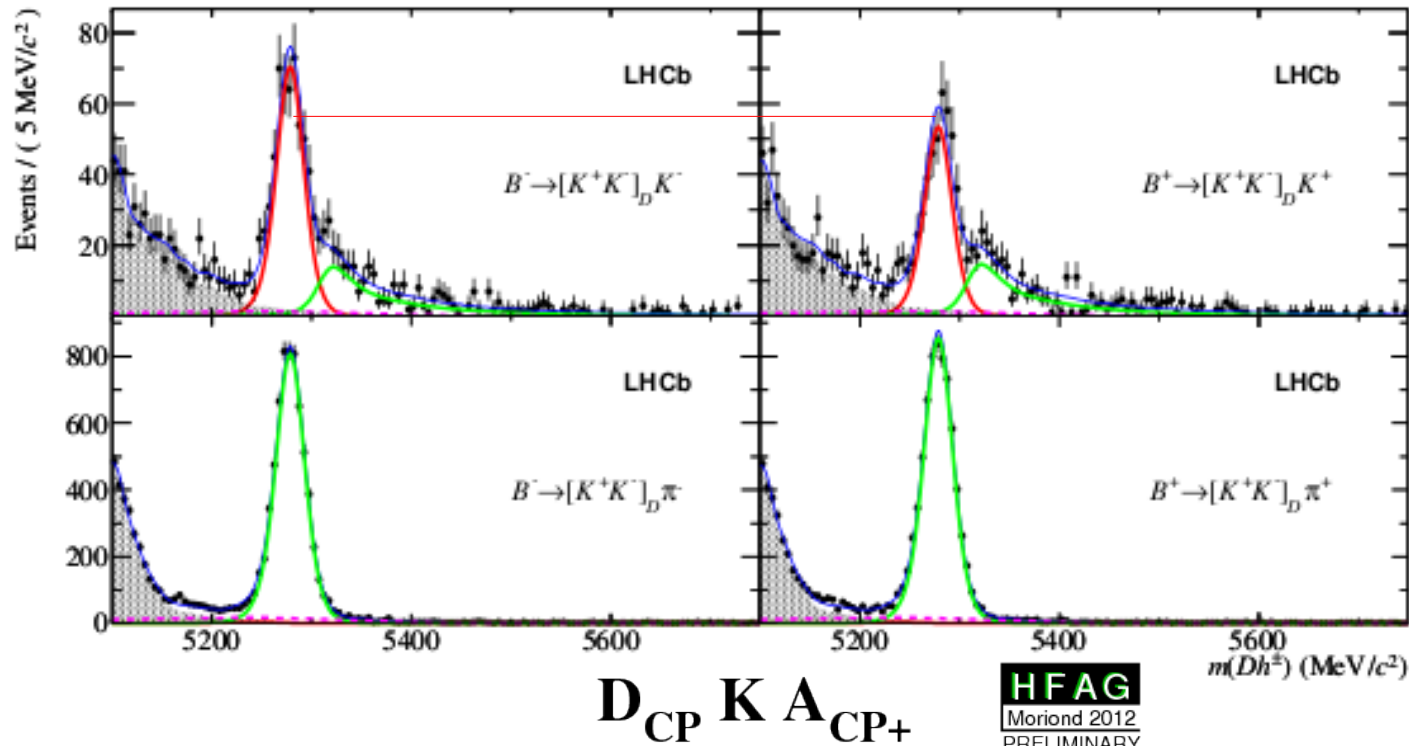
B → DK methods

- Different D decay final states
 - CP eigenstates, e.g. K^+K^- (GLW)
 - doubly-Cabibbo-suppressed decays, e.g. $K^+\pi^-$ (ADS)
 - singly-Cabibbo-suppressed decays, e.g., $K^{*+}K^-$ (GLS)
 - self-conjugate multibody decays, e.g., $K_S \pi^+ \pi^-$ (GGSZ)
- Different B decays
 - $B^- \rightarrow DK^-, D^*K^-, DK^{*-}$ never studied before (or not much)
 - $B^0 \rightarrow DK^{*0}$ (or $B \rightarrow DK\pi$ Dalitz plot analysis)
 - $B^0 \rightarrow DK_S, B_S^0 \rightarrow D\phi$ (with or without time-dependence)
 - $B_S^0 \rightarrow D_S K, B^0 \rightarrow D^{(*)}\pi$ (time-dependent)

Latest results on $B \rightarrow DK$: GLW

PLB 712 (2012) 203

Evidence for CP violation ($\gamma \neq 0$)



Observed CP violation effects

As listed in PDG 2014

- Kaon sector

- $|\epsilon| = (2.228 \pm 0.011) \times 10^{-3}$
- $\text{Re}(\epsilon'/\epsilon) = (1.65 \pm 0.26) \times 10^{-3}$

- B sector

- $S_{\psi K_0} = +0.682 \pm 0.019$

- $S_{\eta' K_0} = +0.63 \pm 0.06$, $S_{\phi K_0} = +0.74^{+0.11}_{-0.13}$, $S_{f_0 K_0} = +0.69^{+0.10}_{-0.12}$, $S_{K+K-K_0} = +0.68^{+0.09}_{-0.10}$

- $S_{\pi+\pi^-} = -0.66 \pm 0.06$, $C_{\pi+\pi^-} = -0.31 \pm 0.05$

- $S_{\psi \pi^0} = -0.93 \pm 0.15$, $S_{D+D^-} = -0.98 \pm 0.17$, $S_{D^{*+} D^{*-}} = -0.71 \pm 0.09$

- $A_{K \mp \pi^\pm} = -0.082 \pm 0.006$, $A_{B_s \rightarrow K \mp \pi^\pm} = -0.082 \pm 0.006$

- $A_{D(CP^+)K^\pm} = +0.19 \pm 0.03$, CP violation in the phase space of $B \rightarrow 3h$ decays

The other Unitarity Triangles

- High statistics available at LHCb will allow sensitivity to smaller CP violating effects
 - CP violating phase in B_s oscillations ($O(\lambda^4)$)
 - B_s oscillations (Δm_s) measured 2006 (CDF)
 - CP violating phase in D^0 oscillations ($O(\lambda^5)$)
 - D^0 oscillations ($x_D = \Delta m_D / \Gamma_D$ & $y_D = \Delta \Gamma_D / 2\Gamma_D$) measured 2007 (Babar, Belle, later CDF)
- Observations of CP violation in both K^0 and B^0 systems won Nobel prizes!

Time-dependent CP Violation Formalism

- Generic (but shown for B_s) decays to CP eigenstates

$$\Gamma(B_s(t) \rightarrow f) = \mathcal{N}_f |A_f|^2 \frac{1 + |\lambda_f|^2}{2} e^{-\Gamma t} \times \left[\cosh \frac{\Delta\Gamma t}{2} + \mathcal{A}_{\text{CP}}^{\text{dir}} \cos(\Delta m t) + \mathcal{A}_{\Delta\Gamma} \sinh \frac{\Delta\Gamma t}{2} + \mathcal{A}_{\text{CP}}^{\text{mix}} \sin(\Delta m t) \right]$$

$$\Gamma(\bar{B}_s(t) \rightarrow f) = \mathcal{N}_f |A_f|^2 \frac{1 + |\lambda_f|^2}{2} (1 + a) e^{-\Gamma t} \times \left[\cosh \frac{\Delta\Gamma t}{2} - \mathcal{A}_{\text{CP}}^{\text{dir}} \cos(\Delta m t) + \mathcal{A}_{\Delta\Gamma} \sinh \frac{\Delta\Gamma t}{2} - \mathcal{A}_{\text{CP}}^{\text{mix}} \sin(\Delta m t) \right].$$

Time-dependent CP Violation Formalism

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$$\Gamma(\bar{B}_s(t) \rightarrow f) = \mathcal{N}_f |A_f|^2 \frac{1 + |\lambda_f|^2}{2} (1 - a) e^{-\Gamma t} \times \left[\cosh \frac{\Delta\Gamma t}{2} - \mathcal{A}_{CP}^{dir} \cos(\Delta m t) + \mathcal{A}_{\Delta\Gamma} \sinh \frac{\Delta\Gamma t}{2} - \mathcal{A}_{CP}^{mix} \sin(\Delta m t) \right].$$

CP violating asymmetries

CP conserving parameter

$$A_{CP}^{dir} = C_{CP} = \frac{1 - |\lambda_{CP}|^2}{1 + |\lambda_{CP}|^2} \quad A_{\Delta\Gamma} = \frac{2 \Re(\lambda_{CP})}{1 + |\lambda_{CP}|^2} \quad A_{CP}^{mix} = S_{CP} = \frac{2 \Im(\lambda_{CP})}{1 + |\lambda_{CP}|^2}$$

$$(A_{CP}^{dir})^2 + (A_{\Delta\Gamma})^2 + (A_{CP}^{mix})^2 = 1$$

Time-dependent CP Violation Formalism

- Generic (but shown for B_s) decays to CP eigenstates

$$\Gamma(B_s(t) \rightarrow f) = \mathcal{N}_f |A_f|^2 \frac{1 + |\lambda_f|^2}{2} e^{-\Gamma t} \times \left[\cosh \frac{\Delta\Gamma t}{2} \quad \text{[red oval]} + \mathcal{A}_{\Delta\Gamma} \sinh \frac{\Delta\Gamma t}{2} \quad \text{[red oval]} \right]$$

$$\Gamma(\bar{B}_s(t) \rightarrow f) = \mathcal{N}_f |A_f|^2 \frac{1 + |\lambda_f|^2}{2} (1 + a) e^{-\Gamma t} \times \left[\cosh \frac{\Delta\Gamma t}{2} \quad \text{[red oval]} + \mathcal{A}_{\Delta\Gamma} \sinh \frac{\Delta\Gamma t}{2} \quad \text{[red oval]} \right].$$

- Untagged analyses still sensitive to some interesting physics

Time-dependent CP Violation Formalism

- Generic (but shown for B_s) decays to CP eigenstates

$$\Gamma(B_s(t) \rightarrow f) = \mathcal{N}_f |A_f|^2 \frac{1 + |\lambda_f|^2}{2} e^{-\Gamma t} \times \left[\cosh \frac{\Delta\Gamma t}{2} + 0 + \mathcal{A}_{\Delta\Gamma} \sinh \frac{\Delta\Gamma t}{2} + \mathcal{A}_{\text{CP}}^{\text{mix}} \sin(\Delta m t) \right]$$

$$\Gamma(\bar{B}_s(t) \rightarrow f) = \mathcal{N}_f |A_f|^2 \frac{1 + |\lambda_f|^2}{2} (1 + 0) e^{-\Gamma t} \times \left[\cosh \frac{\Delta\Gamma t}{2} - 0 + \mathcal{A}_{\Delta\Gamma} \sinh \frac{\Delta\Gamma t}{2} - \mathcal{A}_{\text{CP}}^{\text{mix}} \sin(\Delta m t) \right].$$

- In some channels, expect no CP violation in decay
- and/or no CP violation in mixing

Time-dependent CP Violation Formalism

- Generic (but shown for B_s) decays to CP eigenstates

$$\Gamma(B_s(t) \rightarrow f) = \mathcal{N}_f |A_f|^2 \frac{1 + |\lambda_f|^2}{2} e^{-\Gamma t} \times \left[\mathbf{1} + \mathcal{A}_{\text{CP}}^{\text{dir}} \cos(\Delta m t) + \mathbf{0} + \mathcal{A}_{\text{CP}}^{\text{mix}} \sin(\Delta m t) \right]$$

$$\Gamma(\bar{B}_s(t) \rightarrow f) = \mathcal{N}_f |A_f|^2 \frac{1 + |\lambda_f|^2}{2} (1 + a) e^{-\Gamma t} \times \left[\mathbf{1} - \mathcal{A}_{\text{CP}}^{\text{dir}} \cos(\Delta m t) + \mathbf{0} - \mathcal{A}_{\text{CP}}^{\text{mix}} \sin(\Delta m t) \right].$$

- In some channels, expect no CP violation in decay
- B_d case: $\Delta\Gamma$ negligible

Time-dependent CP Violation Formalism

- Generic (but shown for B_s) decays to CP eigenstates

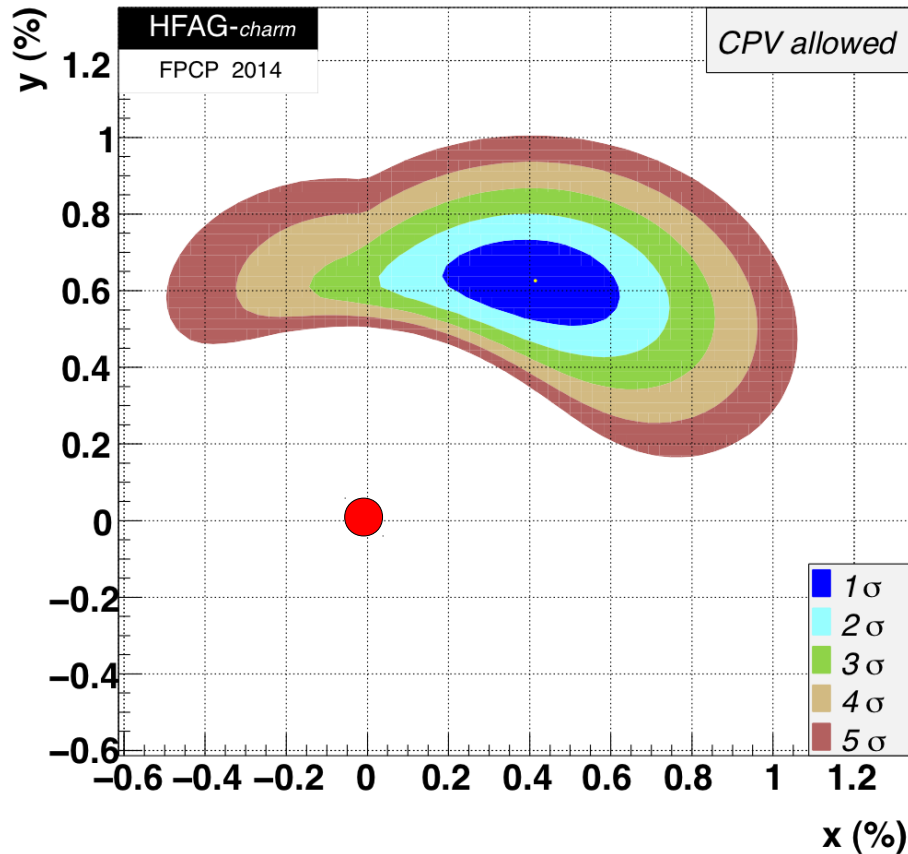
$$\Gamma(B_s(t) \rightarrow f) = \mathcal{N}_f |A_f|^2 \frac{1 + |\lambda_f|^2}{2} e^{-\Gamma t} \times \left[\mathbf{1} + \mathcal{A}_{\text{CP}}^{\text{dir}} \mathbf{1} + \mathcal{A}_{\Delta\Gamma} y\Gamma t + \mathcal{A}_{\text{CP}}^{\text{mix}} x\Gamma t \right]$$

$$\Gamma(\bar{B}_s(t) \rightarrow f) = \mathcal{N}_f |A_f|^2 \frac{1 + |\lambda_f|^2}{2} (1 + a) e^{-\Gamma t} \times \left[\mathbf{1} - \mathcal{A}_{\text{CP}}^{\text{dir}} \mathbf{1} + \mathcal{A}_{\Delta\Gamma} y\Gamma t - \mathcal{A}_{\text{CP}}^{\text{mix}} x\Gamma t \right]$$

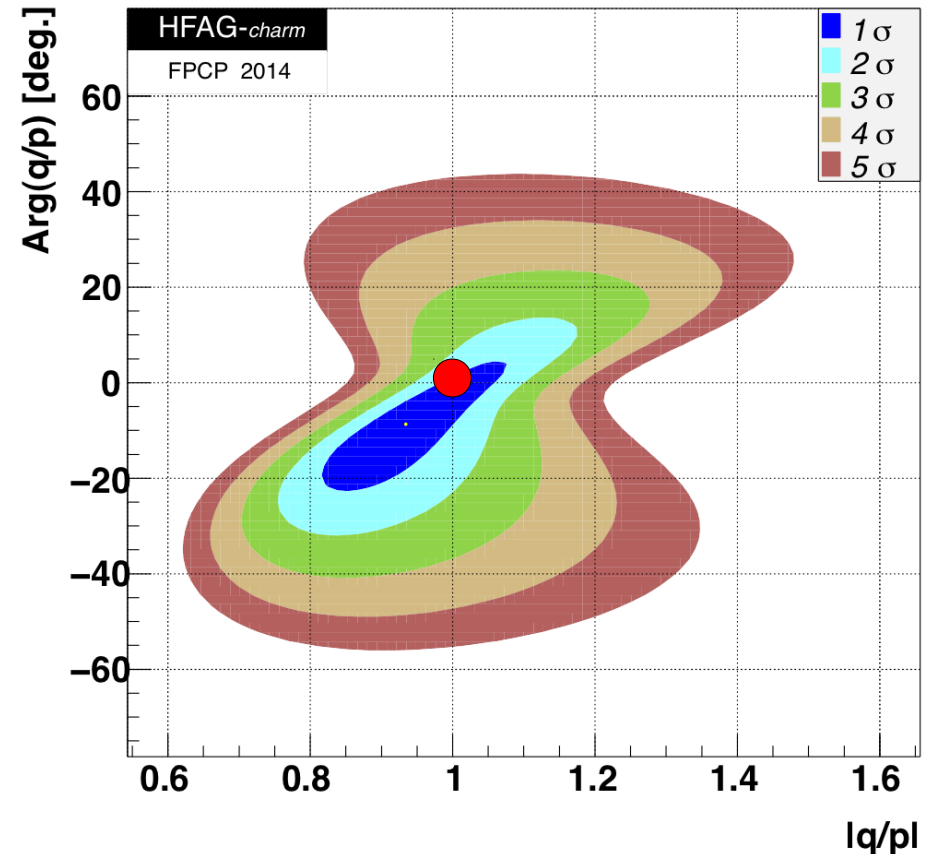
- In some channels, expect no CP violation in decay
- B_d case: $\Delta\Gamma$ negligible
- D^0 case: both $x = \Delta m/\Gamma$ and $y = \Delta\Gamma/2\Gamma$ small

Charm mixing and CP violation

HFAG world average Including results from BABAR, Belle, CDF, CLEO(c), FOCUS, LHCb



Inconsistent with no mixing point (0,0)



Consistent with no CP violation point (1,0)

CP violation in D decay?

e.g. PRL 108 (2012) 111602

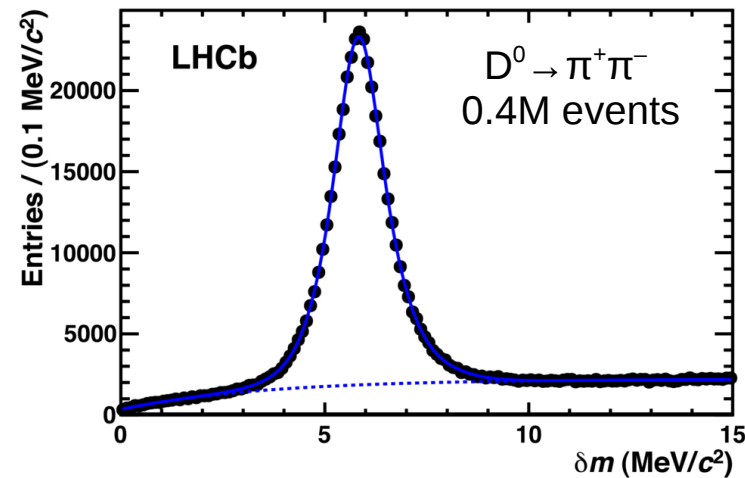
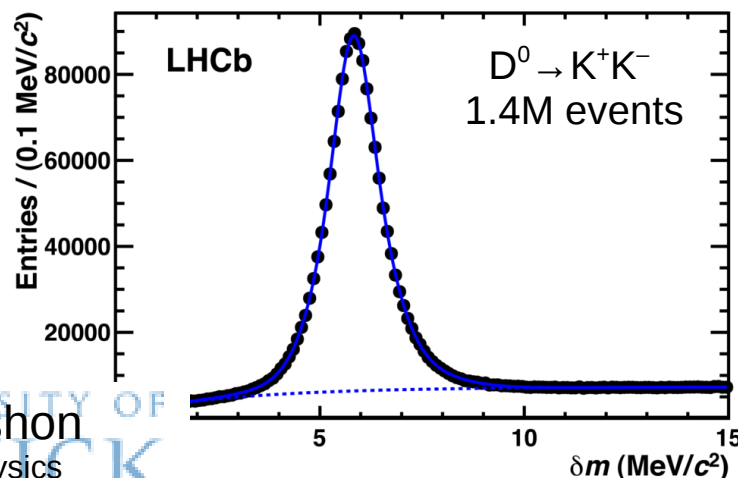
Measurement of CP asymmetry at pp collider requires knowledge of production and detection asymmetries; e.g. for $D^0 \rightarrow f$, where D meson flavour is tagged by $D^{*+} \rightarrow D^0 \pi^+$ decay

$$A_{\text{raw}}(f) = A_{CP}(f) + A_D(f) + A_D(\pi_s^+) + A_P(D^{*+}).$$

final state detection asymmetry vanishes for CP eigenstate

Cancel asymmetries by taking difference of raw asymmetries in two different final states (Since A_D and A_P depend on kinematics, must bin or reweight to ensure cancellation)

$$\Delta A_{CP} = A_{\text{raw}}(K^- K^+) - A_{\text{raw}}(\pi^- \pi^+).$$



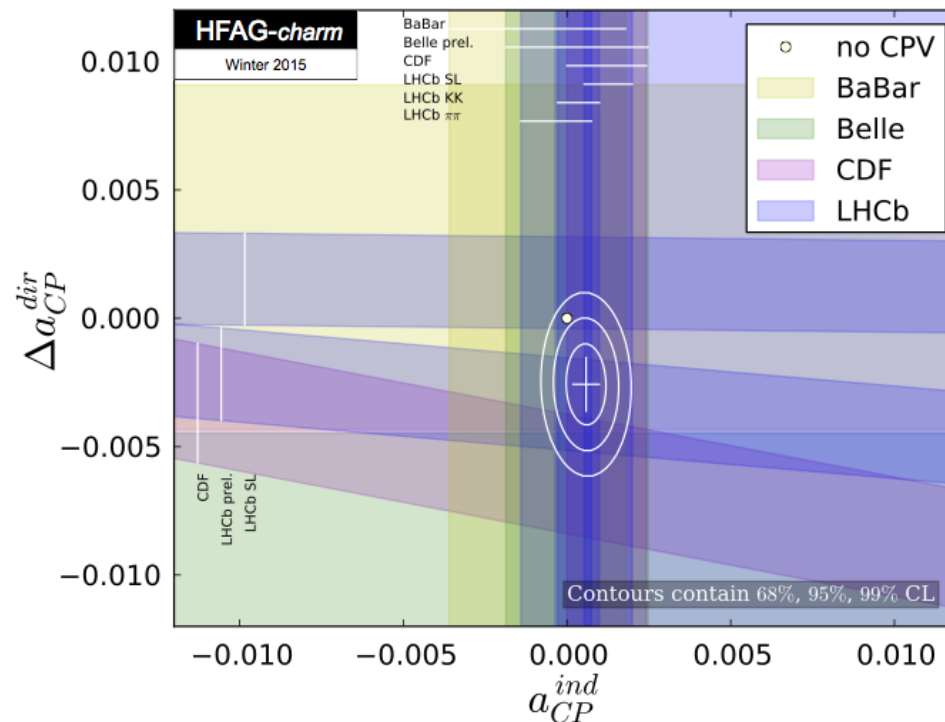
CP violation in D decays

$$\begin{aligned} \Delta A_{CP} &\equiv A_{CP}(K^- K^+) - A_{CP}(\pi^- \pi^+) \\ &= [a_{CP}^{\text{dir}}(K^- K^+) - a_{CP}^{\text{dir}}(\pi^- \pi^+)] + \frac{\Delta\langle t \rangle}{\tau} a_{CP}^{\text{ind}}. \end{aligned}$$

Singly Cabibbo-suppressed decays have tree and penguin contributions

Two body decays give largest yields – best sensitivity

Small contribution from “indirect” CP asymmetry due to non-perfect cancellation of decay time acceptance – also measured with decay-time-dependent methods



$$\Phi_s = -2\beta_s (B_s \rightarrow J/\psi\phi)$$

- VV final state

three helicity amplitudes

→ mixture of CP-even and CP-odd

disentangled using angular & time-dependent distributions

→ additional sensitivity

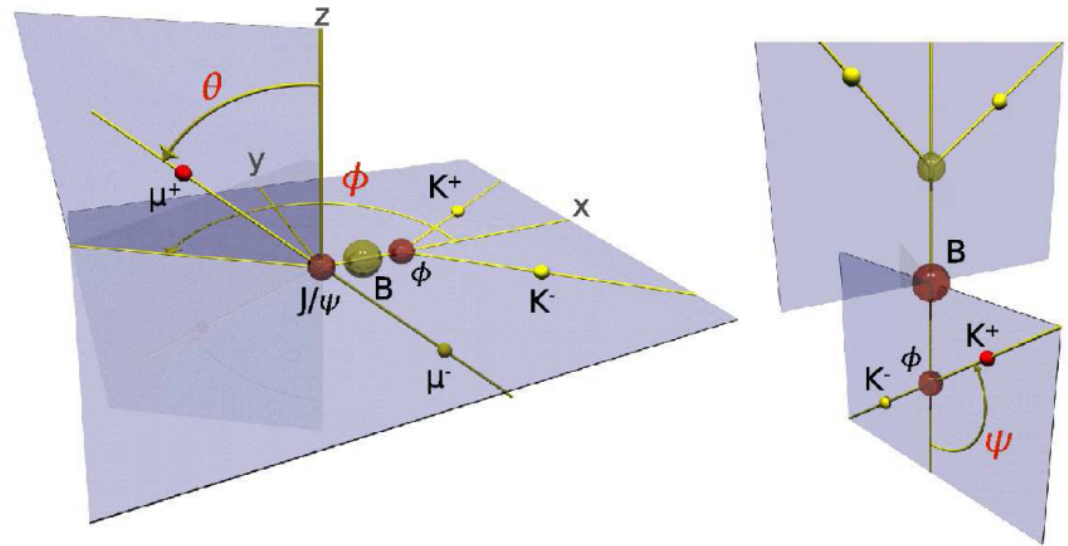
many correlated variables

→ complicated analysis

- LHCb also uses $B_s \rightarrow J/\psi f_0$ ($f_0 \rightarrow \pi^+\pi^-$)

- CP eigenstate; simpler analysis

- fewer events; requires input from $J/\psi\phi$ analysis ($\Gamma_s, \Delta\Gamma_s$)



$B_s \rightarrow J/\psi\phi$ formalism

Differential decay rate:

$$\frac{d^4\Gamma(B_s^0 \rightarrow J/\psi\phi)}{dt d\cos\theta d\varphi d\cos\psi} \equiv \frac{d^4\Gamma}{dt d\Omega} \propto \sum_{k=1}^6 h_k(t) f_k(\Omega)$$

B_s

\bar{B}_s

k	$h_k(t)$	$h_k(t)$	$f_k(\theta, \psi, \varphi)$
1	$ A_0(t) ^2$	$ \bar{A}_0(t) ^2$	$2\cos^2\psi(1 - \sin^2\theta\cos^2\varphi)$
2	$ A_{\parallel}(t) ^2$	$ \bar{A}_{\parallel}(t) ^2$	$\sin^2\psi(1 - \sin^2\theta\sin^2\varphi)$
3	$ A_{\perp}(t) ^2$	$ \bar{A}_{\perp}(t) ^2$	$\sin^2\psi\sin^2\theta$
4	$\Im\{A_{\parallel}^*(t)A_{\perp}(t)\}$	$\Im\{\bar{A}_{\parallel}^*(t)\bar{A}_{\perp}(t)\}$	$-\sin^2\psi\sin 2\theta\sin\varphi$
5	$\Re\{A_0^*(t)A_{\parallel}(t)\}$	$\Re\{\bar{A}_0^*(t)\bar{A}_{\parallel}(t)\}$	$\frac{1}{\sqrt{2}}\sin 2\psi\sin^2\theta\sin 2\varphi$
6	$\Im\{A_0^*(t)A_{\perp}(t)\}$	$\Im\{\bar{A}_0^*(t)\bar{A}_{\perp}(t)\}$	$\frac{1}{\sqrt{2}}\sin 2\psi\sin 2\theta\cos\varphi$

$A_0(0) \rightarrow$ CP even
 $A_{\parallel}(0) \rightarrow$ CP even
 $A_{\perp}(0) \rightarrow$ CP odd

\pm signs differ for B_s and \bar{B}_s

$$|\bar{A}_0(t)|^2 = |\bar{A}_0(0)|^2 e^{-\Gamma_s t} \left[\cosh\left(\frac{\Delta\Gamma_s t}{2}\right) - \cos\Phi \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) - \sin\Phi \sin(\Delta m_s t) \right],$$

$$|\bar{A}_{\parallel}(t)|^2 = |\bar{A}_{\parallel}(0)|^2 e^{-\Gamma_s t} \left[\cosh\left(\frac{\Delta\Gamma_s t}{2}\right) - \cos\Phi \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) - \sin\Phi \sin(\Delta m_s t) \right],$$

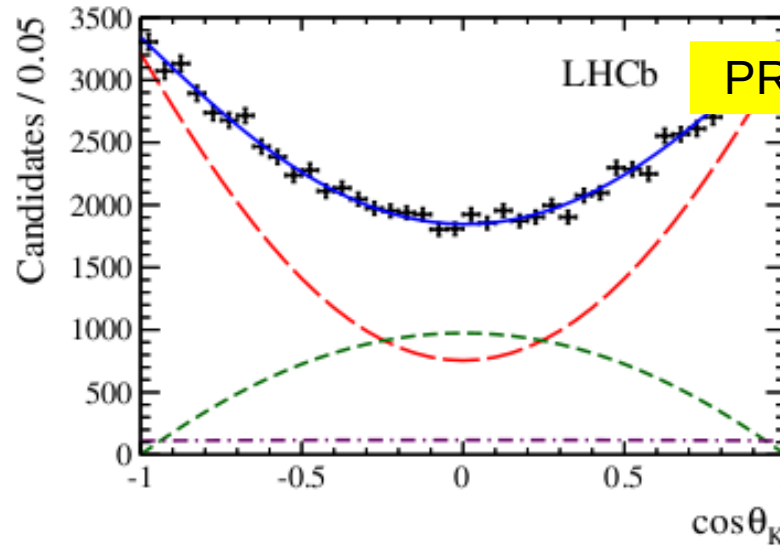
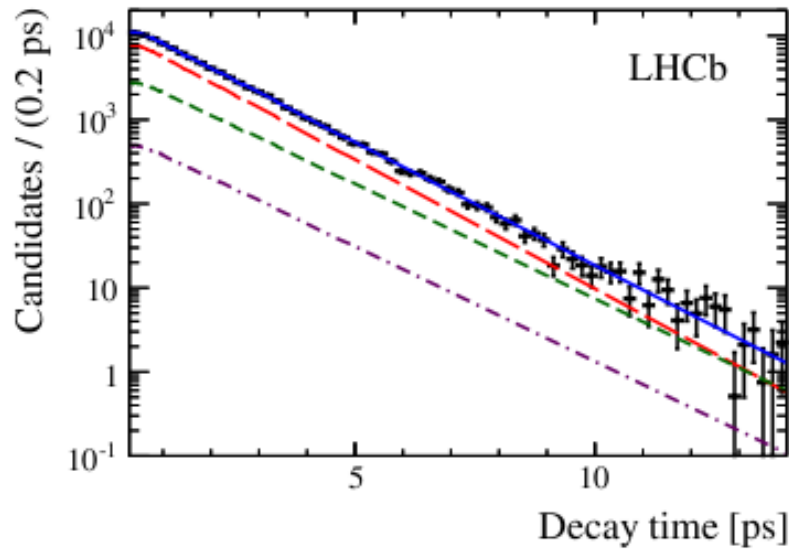
$$|\bar{A}_{\perp}(t)|^2 = |\bar{A}_{\perp}(0)|^2 e^{-\Gamma_s t} \left[\cosh\left(\frac{\Delta\Gamma_s t}{2}\right) + \cos\Phi \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) + \sin\Phi \sin(\Delta m_s t) \right],$$

$$\Im\{\bar{A}_{\parallel}^*(t)\bar{A}_{\perp}(t)\} = |\bar{A}_{\parallel}(0)||\bar{A}_{\perp}(0)| e^{-\Gamma_s t} \left[-\cos(\delta_{\perp} - \delta_{\parallel}) \sin\Phi \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) - \sin(\delta_{\perp} - \delta_{\parallel}) \cos(\Delta m_s t) + \cos(\delta_{\perp} - \delta_{\parallel}) \cos\Phi \sin(\Delta m_s t) \right],$$

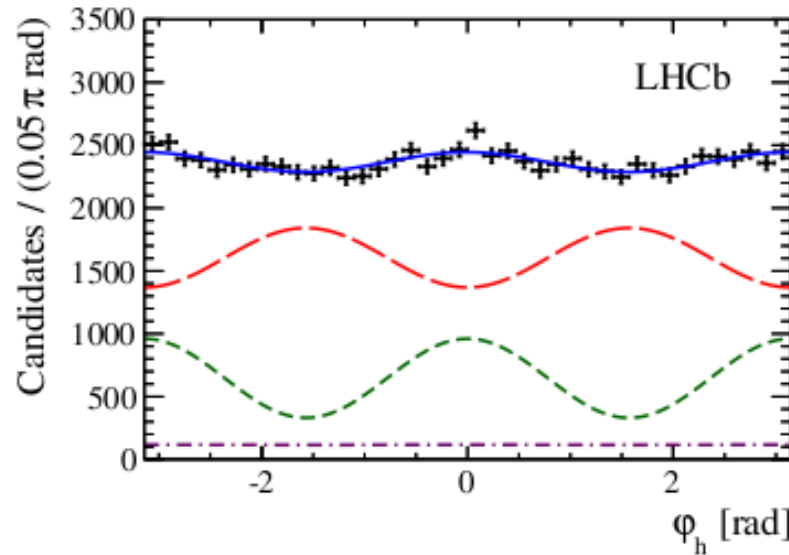
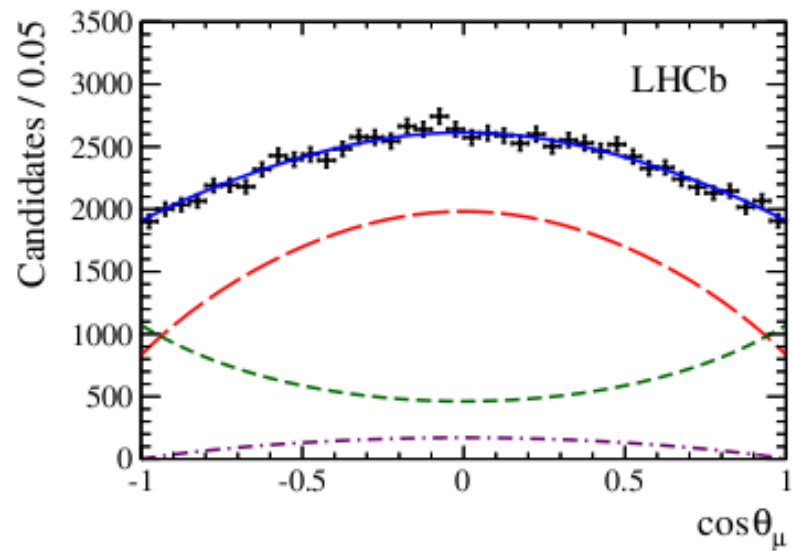
$$\Re\{\bar{A}_0^*(t)\bar{A}_{\parallel}(t)\} = |\bar{A}_0(0)||\bar{A}_{\parallel}(0)| e^{-\Gamma_s t} \cos\delta_{\parallel} \left[\cosh\left(\frac{\Delta\Gamma_s t}{2}\right) - \cos\Phi \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) - \sin\Phi \sin(\Delta m_s t) \right] \text{ and}$$

$$\Im\{\bar{A}_0^*(t)\bar{A}_{\perp}(t)\} = |\bar{A}_0(0)||\bar{A}_{\perp}(0)| e^{-\Gamma_s t} \left[-\cos\delta_{\perp} \sin\Phi \sinh\left(\frac{\Delta\Gamma_s t}{2}\right) - \sin\delta_{\perp} \cos(\Delta m_s t) + \cos\delta_{\perp} \cos\Phi \sin(\Delta m_s t) \right].$$

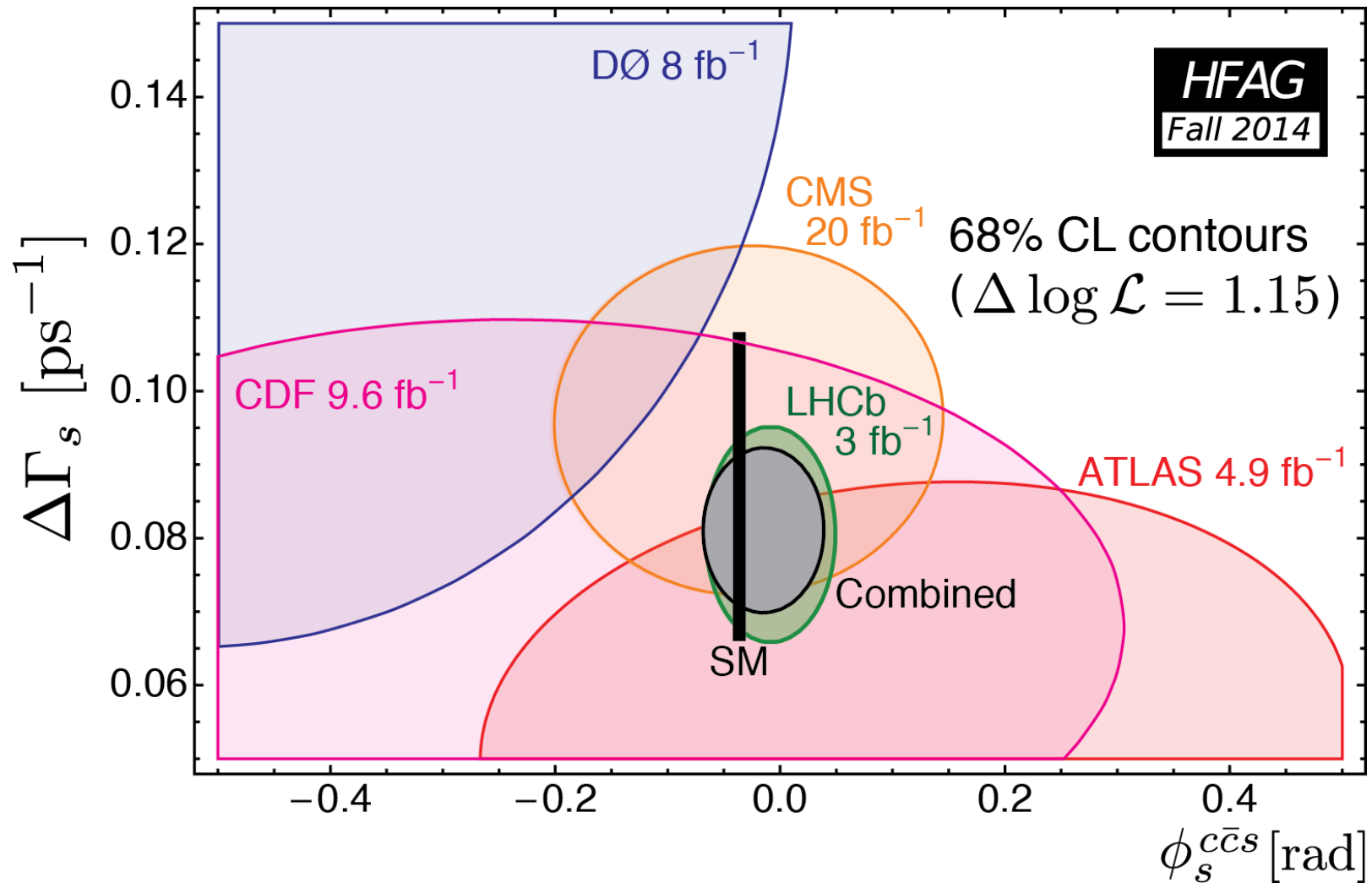
CP violation in $B_c \rightarrow J/\psi\phi$ & $J/\psi\pi\pi$



PRL 114 (2015) 041801



CP violation in interference between B_s mixing and $b \rightarrow c\bar{c}s$ decay (ϕ_s)

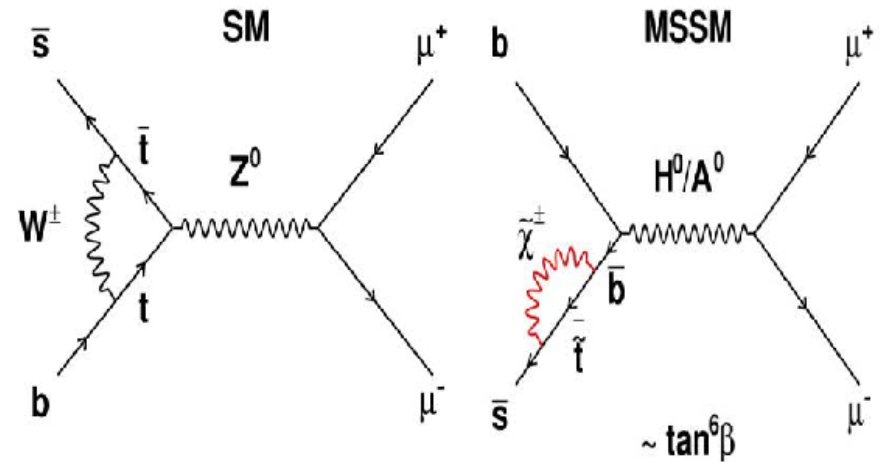


Rare Decays

$$B_{(s)}^0 \rightarrow \mu^+ \mu^-$$

Killer app. for new physics discovery

- Very small in the SM
 - no tree-level FCNC
 - CKM suppression
 - helicity suppression

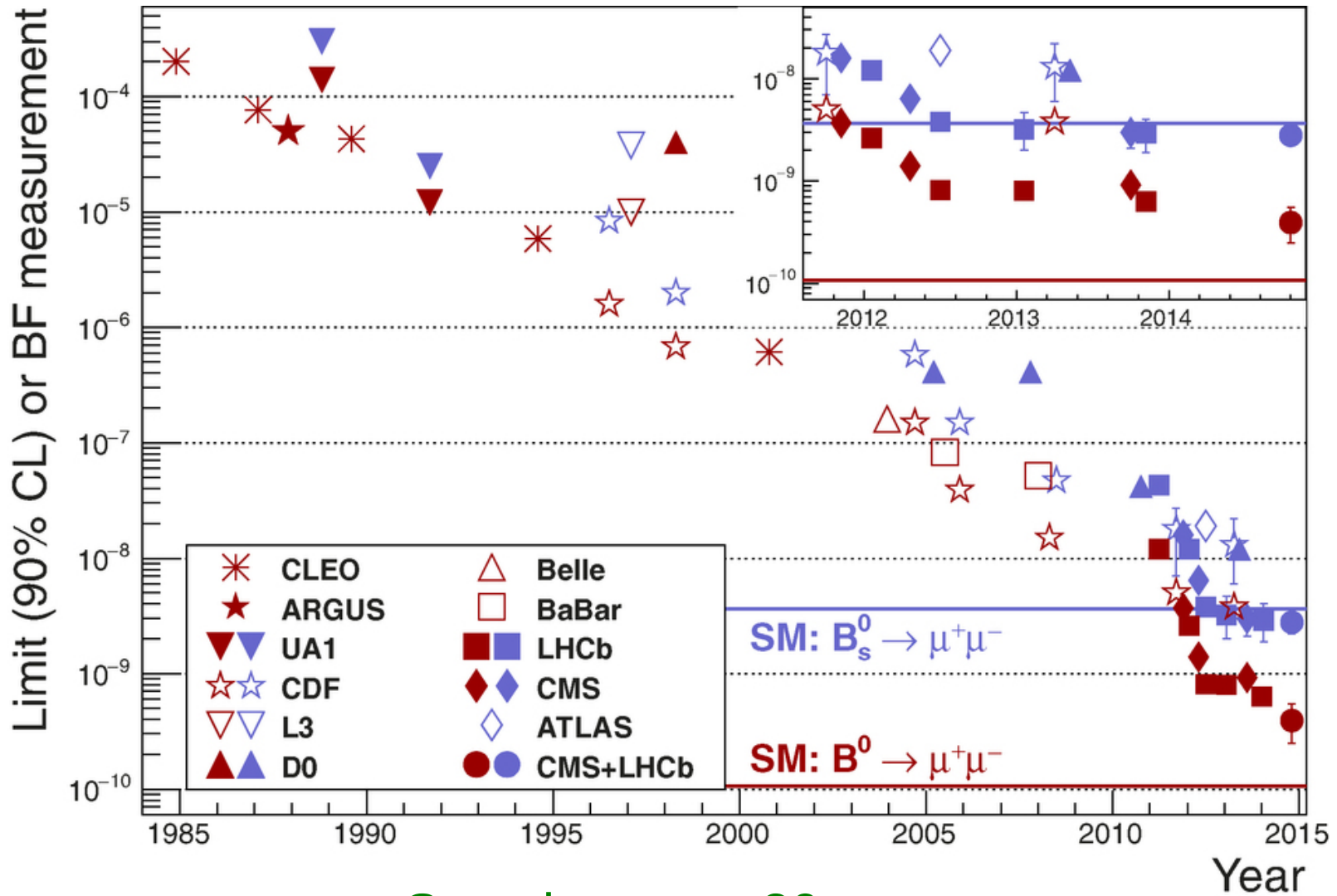


- Huge NP enhancement possible ($\tan \beta =$ ratio of Higgs vevs)

$$BR(B_s \rightarrow \mu^+ \mu^-)^{SM} = (3.3 \pm 0.3) \times 10^{-9} \quad BR(B_s \rightarrow \mu^+ \mu^-)^{MSSM} \propto \tan^6 \beta / M_{A^0}^4$$

- Clean experimental signature

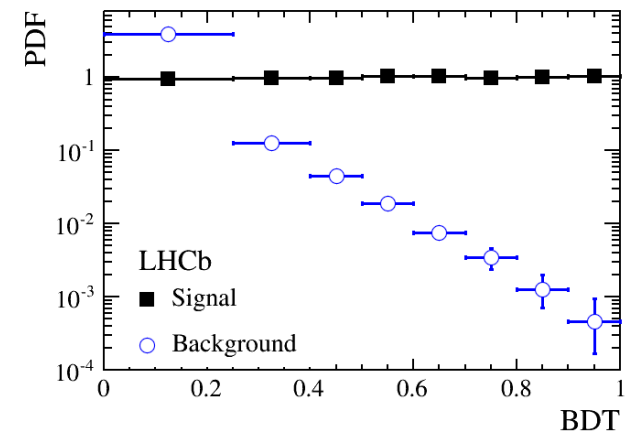
$$B_{(s)}^0 \rightarrow \mu^+ \mu^-$$



Searches over 30 years

$B_{(s)}^0 \rightarrow \mu^+ \mu^-$ – analysis ingredients

- Produce a very large sample of B mesons
- Trigger efficiently on dimuon signatures
- Reject background
 - excellent vertex resolution (identify displaced vertex)
 - excellent mass resolution (identify B peak)
 - also essential to resolve B^0 from B_s^0 decays
 - powerful muon identification (reject background from B decays with misidentified pions)
 - typical to combine various discriminating variables into a multivariate classifier
 - e.g. Boosted Decision Trees algorithm

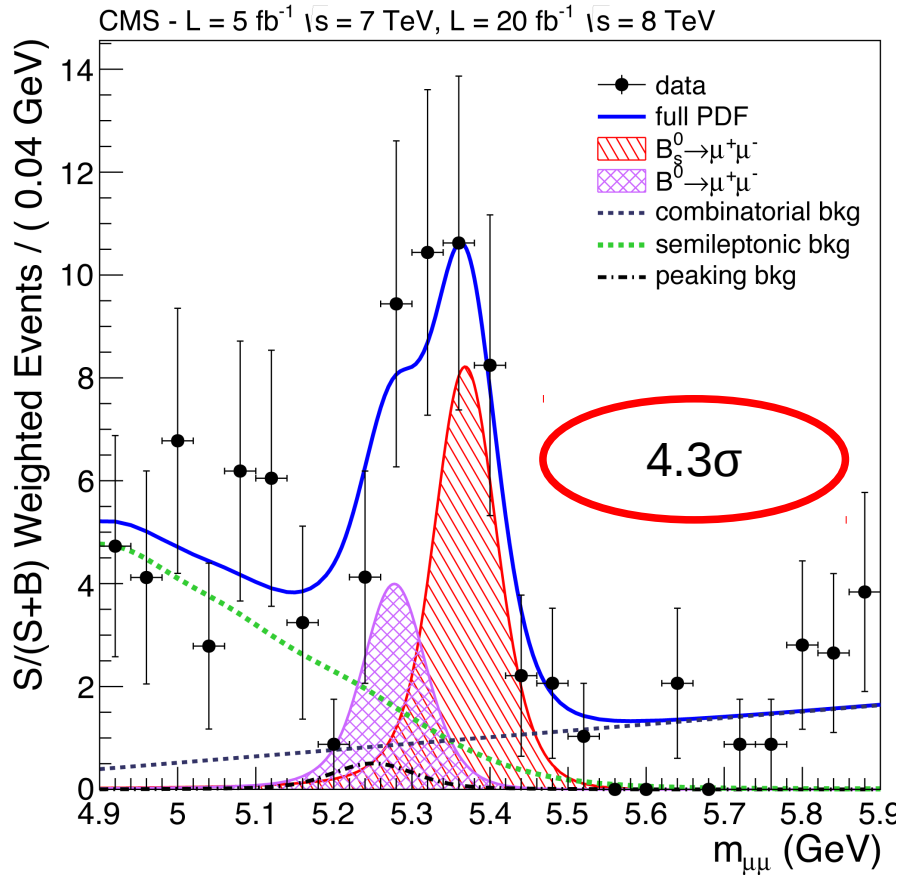


$$B_{(s)}^0 \rightarrow \mu^+ \mu^-$$

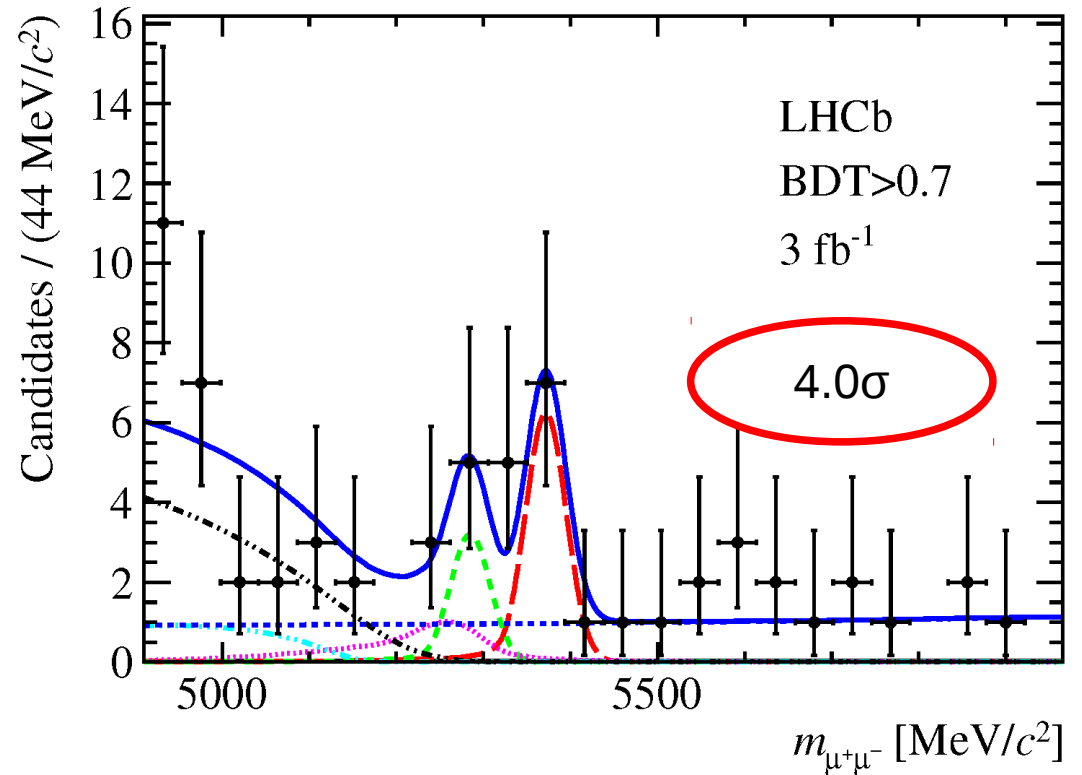
latest results from CMS & LHCb

CMS PRL 111 (2013) 101804

LHCb PRL 111 (2013) 101805

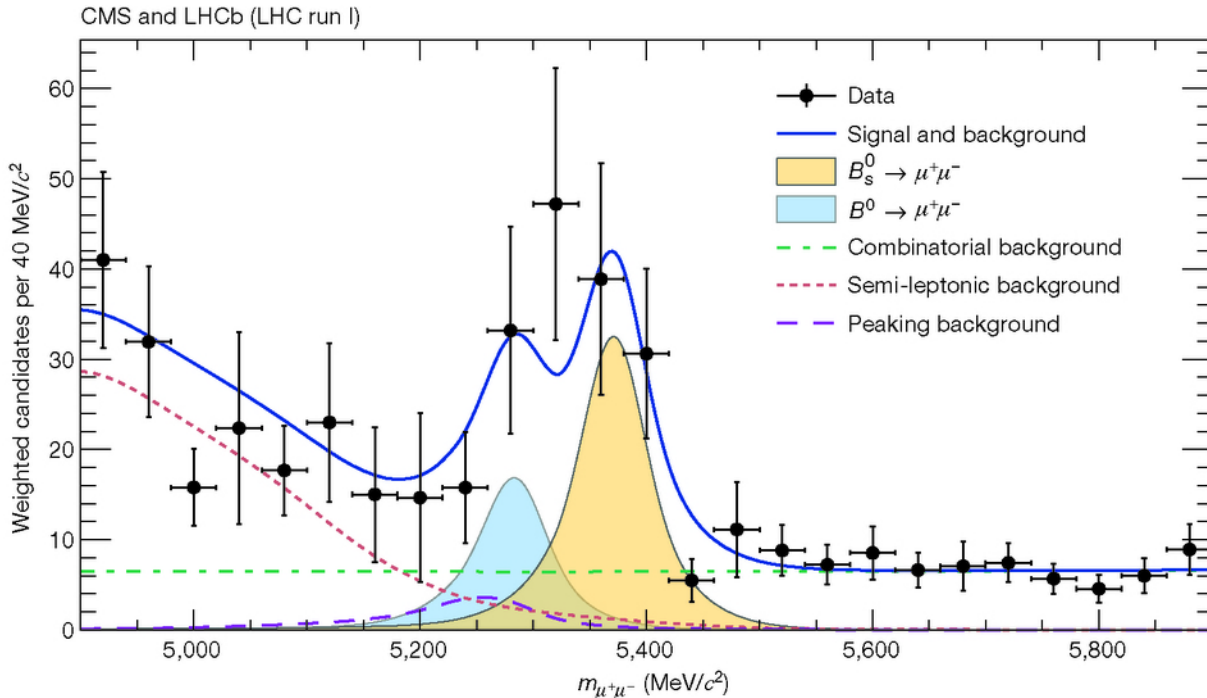


Events weighted by S/(S+B)



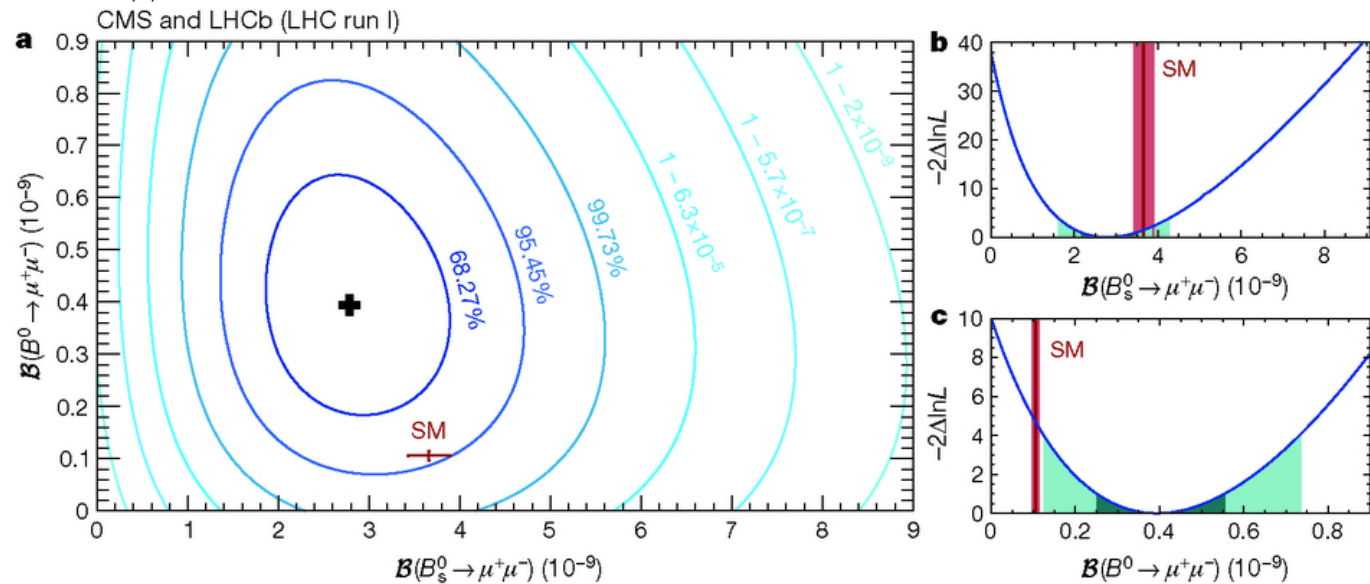
Only events with BDT > 0.7

$$B_s \rightarrow \mu^+ \mu^-$$



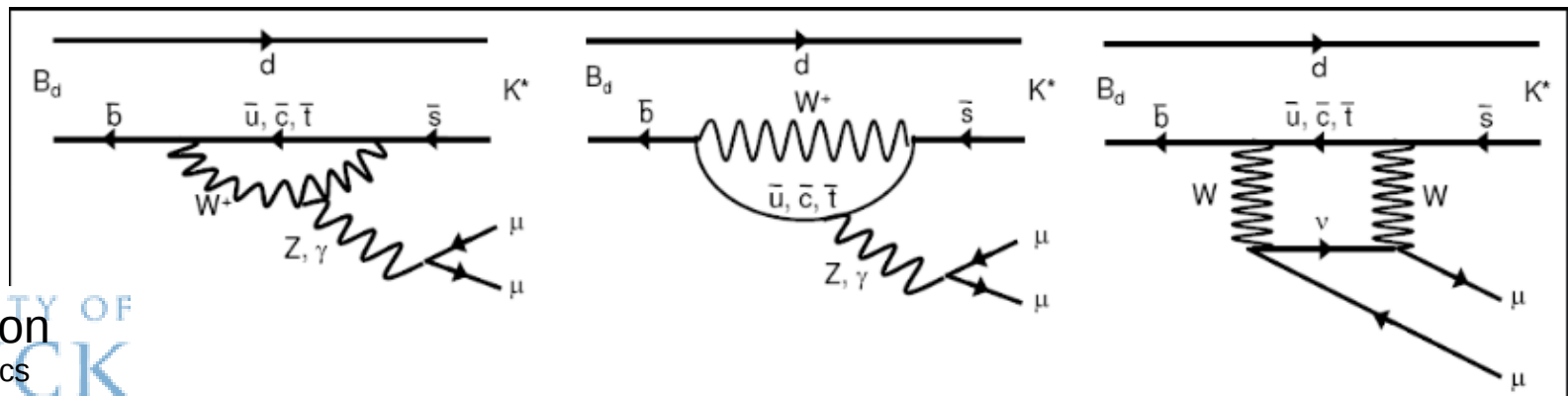
Combination of CMS and LHCb data results in first observation of $B_s \rightarrow \mu^+\mu^-$ and first evidence for $B^0 \rightarrow \mu^+\mu^-$

Results consistent with SM at 2 σ level



$$B \rightarrow K^* \mu^+ \mu^-$$

- $b \rightarrow s l^+ l^-$ processes also governed by FCNCs
 - rates and asymmetries of many exclusive processes sensitive to NP
- Queen among them is $B_d \rightarrow K^{*0} \mu^+ \mu^-$
 - superb laboratory for NP tests
 - **experimentally clean signature**
 - many kinematic variables ...
 - ... **with clean theoretical predictions (at least at low q^2)**



Operator Product Expansion

Build an effective theory for b physics

- take the weak part of the SM
- integrate out the heavy fields (W,Z,t)
- (like a modern version of Fermi theory for weak interactions)

$$\mathcal{L}_{(\text{full EW} \times \text{QCD})} \longrightarrow \mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{QED} \times \text{QCD}} \left(\begin{array}{l} \text{quarks } \neq t \\ \& \text{ leptons} \end{array} \right) + \sum_n C_n(\mu) Q_n$$

Q_n - local interaction terms (operators), C_n - coupling constants (Wilson coefficients)

Wilson coefficients

- encode information on the weak scale
- are calculable and known in the SM (at least to leading order)
- are affected by new physics

For $K^* \mu \mu$ we care about C_7 (also affects $b \rightarrow s \gamma$), C_9 and C_{10}

Effective operators

$$\mathcal{H}_W^{\Delta B=1, \Delta C=0, \Delta S=-1} = 4 \frac{G_F}{\sqrt{2}} \left(\lambda_c^s (C_1(\mu) Q_1^c(\mu) + C_2(\mu) Q_2^c(\mu)) \right. \\ \left. + \lambda_u^s (C_1(\mu) Q_1^u(\mu) + C_2(\mu) Q_2^u(\mu)) - \lambda_t^s \sum_{i=3}^{10} C_i(\mu) Q_i(\mu) \right)$$

where the $\lambda_q^s = V_{qb}^* V_{qs}$ and the operator basis is given by

$$\begin{aligned} Q_1^q &= \bar{b}_L^\alpha \gamma^\mu q_L^\alpha \bar{q}_L^\beta \gamma_\mu s_L^\beta & Q_2^q &= \bar{b}_L^\alpha \gamma^\mu q_L^\beta \bar{q}_L^\beta \gamma_\mu s_L^\alpha \\ Q_3 &= \bar{b}_L^\alpha \gamma^\mu s_L^\alpha \sum_q \bar{q}_L^\beta \gamma_\mu q_L^\beta & Q_4 &= \bar{b}_L^\alpha \gamma^\mu s_L^\beta \sum_q \bar{q}_L^\beta \gamma_\mu q_L^\alpha \\ Q_5 &= \bar{b}_L^\alpha \gamma^\mu s_L^\alpha \sum_q \bar{q}_R^\beta \gamma_\mu q_R^\beta & Q_6 &= \bar{b}_L^\alpha \gamma^\mu s_L^\beta \sum_q \bar{q}_R^\beta \gamma_\mu q_R^\alpha \\ Q_7 &= \frac{3}{2} \bar{b}_L^\alpha \gamma^\mu s_L^\alpha \sum_q e_q \bar{q}_R^\beta \gamma_\mu q_R^\beta & Q_8 &= \frac{3}{2} \bar{b}_L^\alpha \gamma^\mu s_L^\beta \sum_q e_q \bar{q}_R^\beta \gamma_\mu q_R^\alpha \\ Q_9 &= \frac{3}{2} \bar{b}_L^\alpha \gamma^\mu s_L^\alpha \sum_q e_q \bar{q}_L^\beta \gamma_\mu q_L^\beta & Q_{10} &= \frac{3}{2} \bar{b}_L^\alpha \gamma^\mu s_L^\beta \sum_q e_q \bar{q}_L^\beta \gamma_\mu q_L^\alpha \end{aligned}$$

Four-fermion operators (except $Q_{7\gamma}$ & Q_{8g}) – dimension 6

$$Q_{7\gamma} = \frac{e}{16\pi^2} m_b \bar{b}_L^\alpha \sigma^{\mu\nu} F_{\mu\nu} s_L^\alpha$$

$$Q_{8g} = \frac{g_s}{16\pi^2} m_b \bar{b}_L^\alpha \sigma^{\mu\nu} G_{\mu\nu}^A T^A s_L^\alpha$$

$$Q_{9V} = \frac{1}{2} \bar{b}_L^\alpha \gamma^\mu s_L^\alpha \bar{l} \gamma_\mu l$$

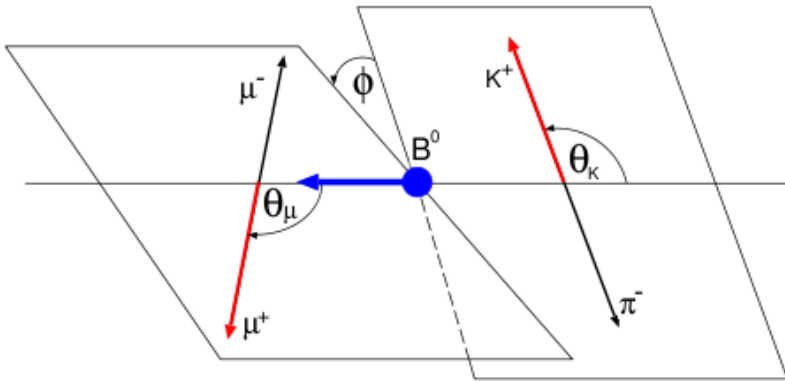
$$Q_{10A} = \frac{1}{2} \bar{b}_L^\alpha \gamma^\mu s_L^\alpha \bar{l} \gamma_\mu \gamma_5 l$$

Angular analysis of $B \rightarrow K^* \mu^+ \mu^-$

LHCb-CONF-2015-002

- Differential decay distribution

$$\begin{aligned} \frac{1}{d(\Gamma + \bar{\Gamma})/dq^2} \frac{d^3(\Gamma + \bar{\Gamma})}{d\vec{\Omega}} \Big|_P &= \frac{9}{32\pi} \left[\frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K \right. \\ &\quad + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_l \\ &\quad - F_L \cos^2 \theta_K \cos 2\theta_l + S_3 \sin^2 \theta_K \sin^2 \theta_l \cos 2\phi \\ &\quad + S_4 \sin 2\theta_K \sin 2\theta_l \cos \phi + S_5 \sin 2\theta_K \sin \theta_l \cos \phi \\ &\quad + \frac{4}{3} A_{FB} \sin^2 \theta_K \cos \theta_l + S_7 \sin 2\theta_K \sin \theta_l \sin \phi \\ &\quad \left. + S_8 \sin 2\theta_K \sin 2\theta_l \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_l \sin 2\phi \right]. \end{aligned}$$

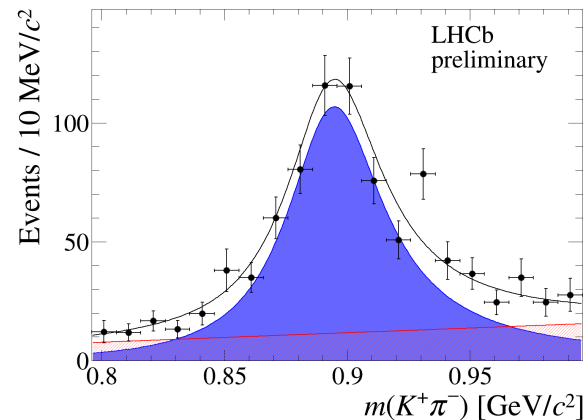
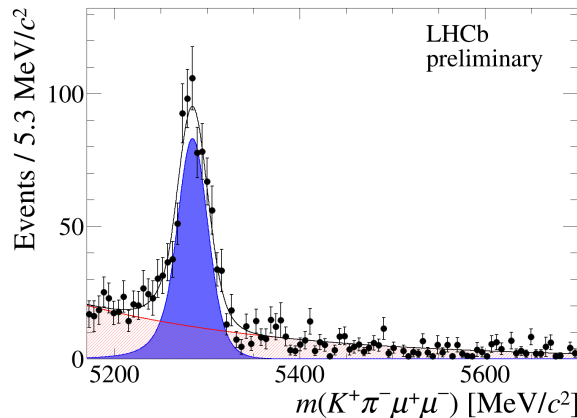


S_i terms related to Wilson coefficients and form factors

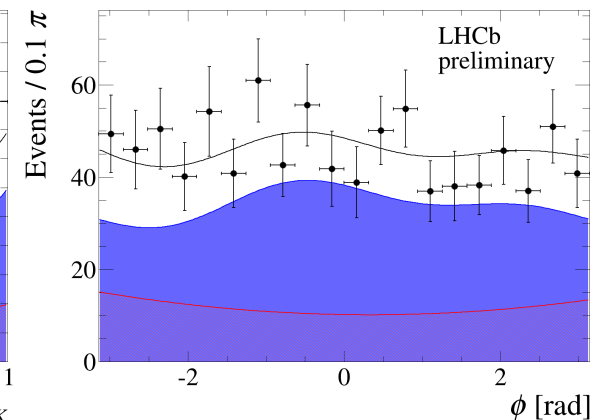
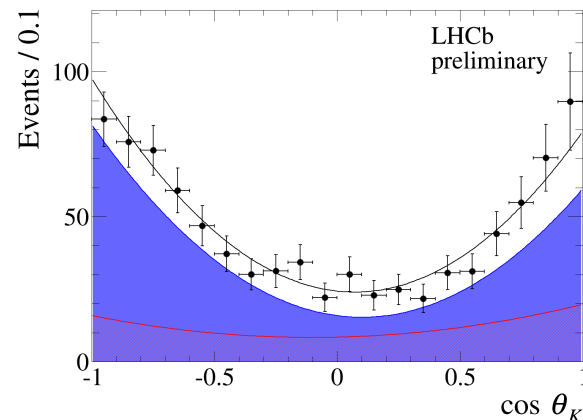
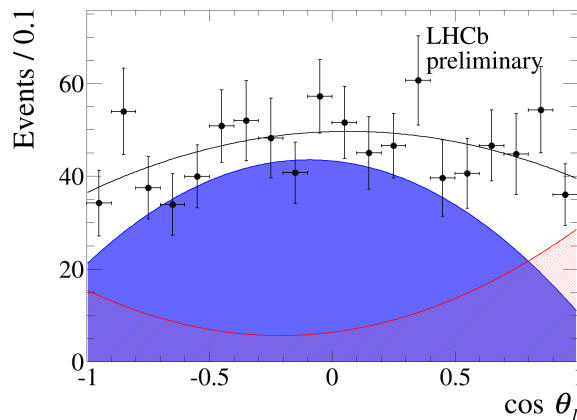
Full angular analysis of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

LHCb-CONF-2015-002

- Example of fits, in $1.1 < q^2 < 6.0 \text{ GeV}^2$ bin

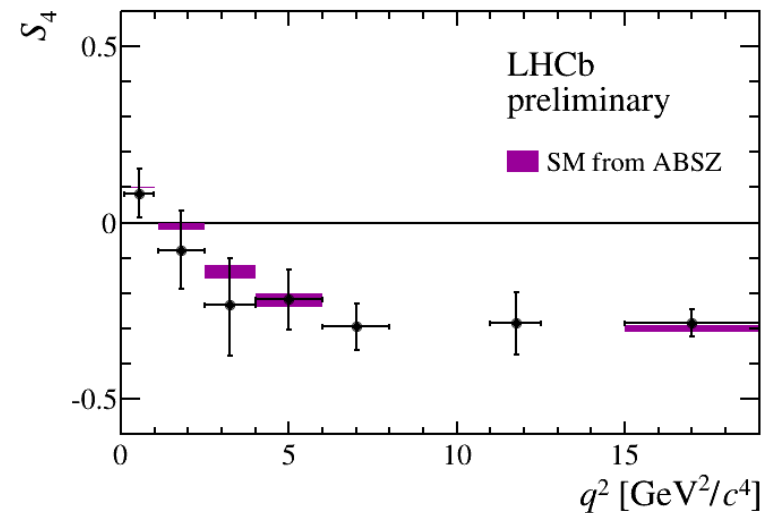
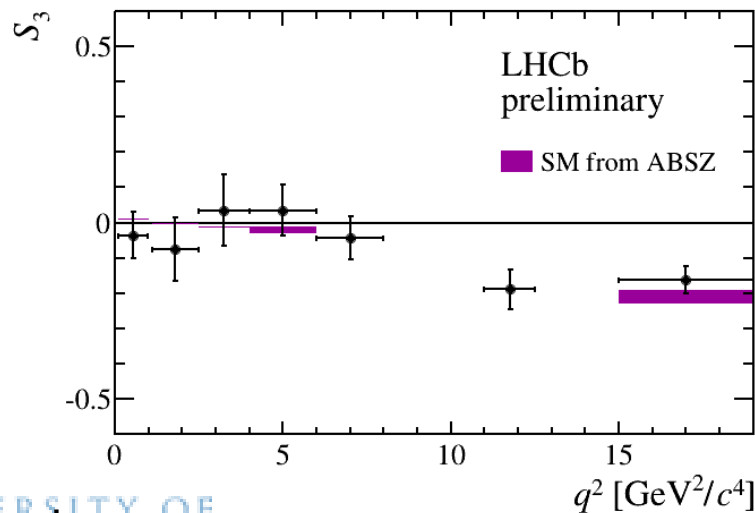
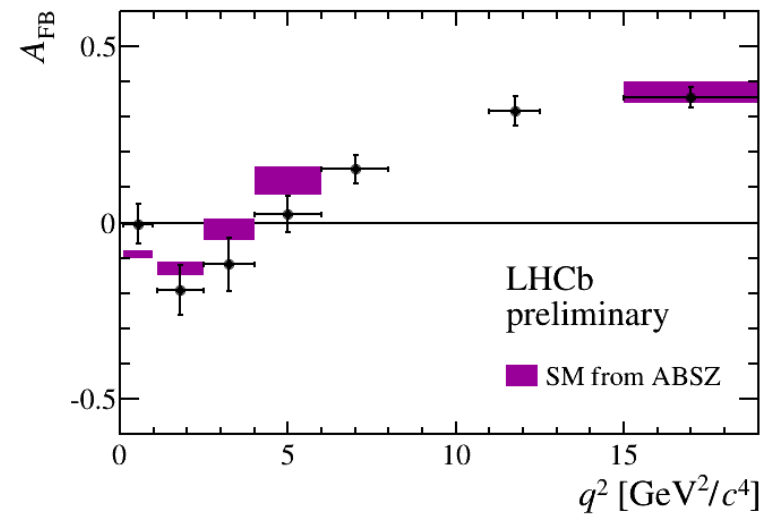
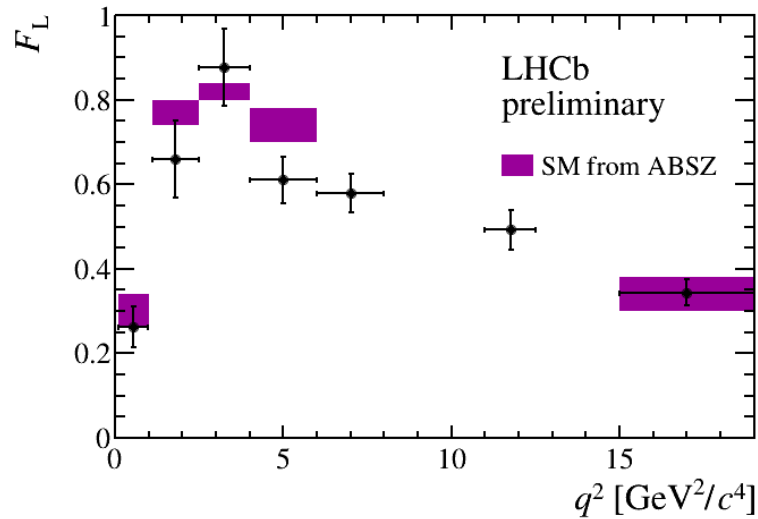


Angle and $m(K\pi)$
projections in $\pm 50 \text{ MeV}$
around B peak



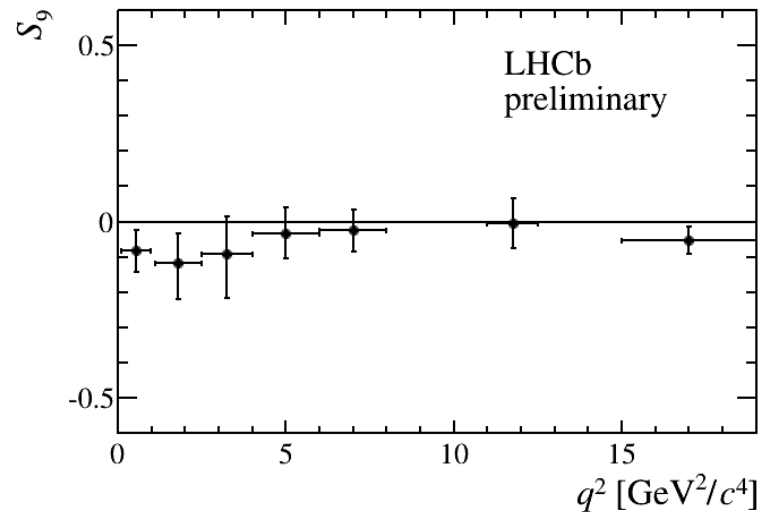
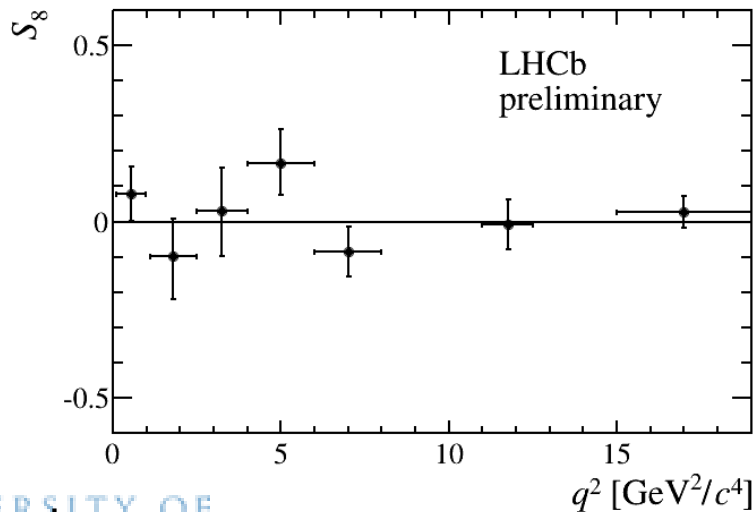
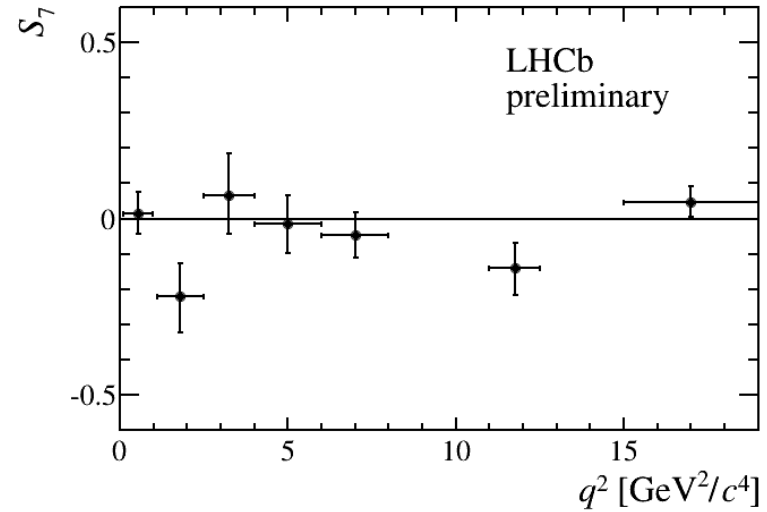
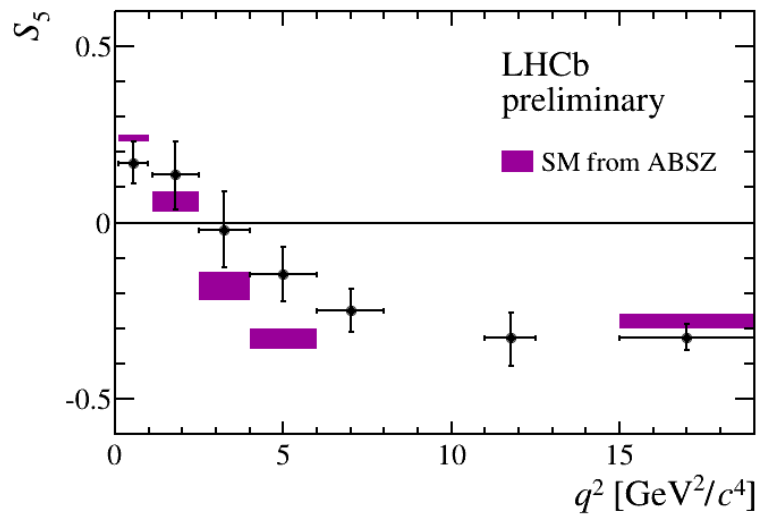
Full angular analysis of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

LHCb-CONF-2015-002



Full angular analysis of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$

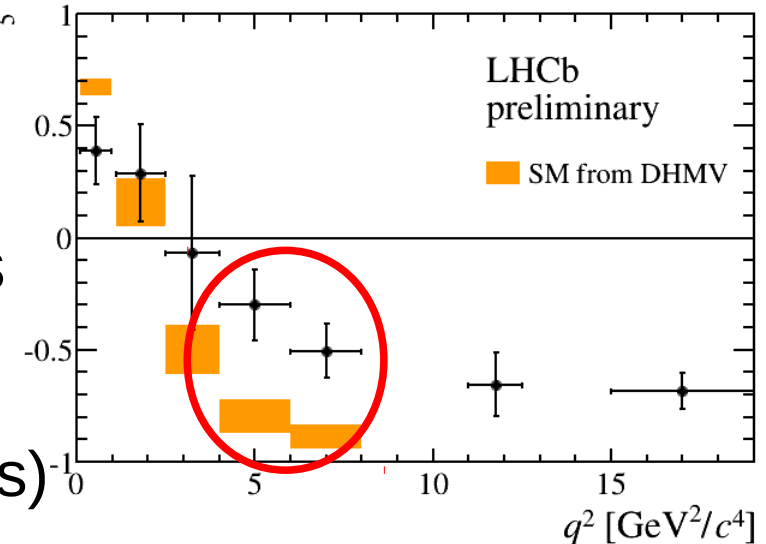
LHCb-CONF-2015-002



Tension in P_5'

LHCb-CONF-2015-002

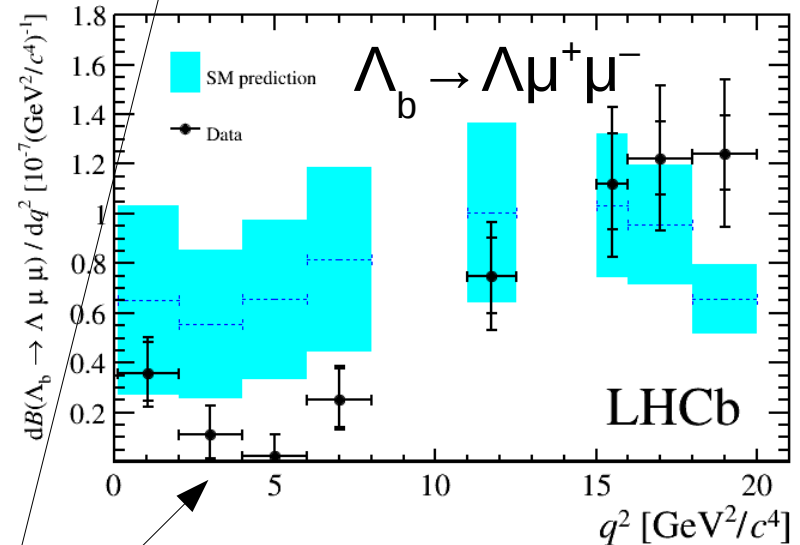
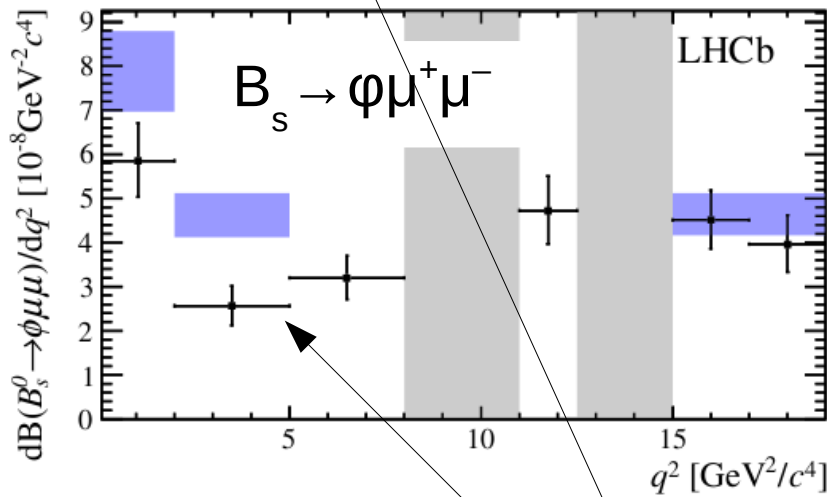
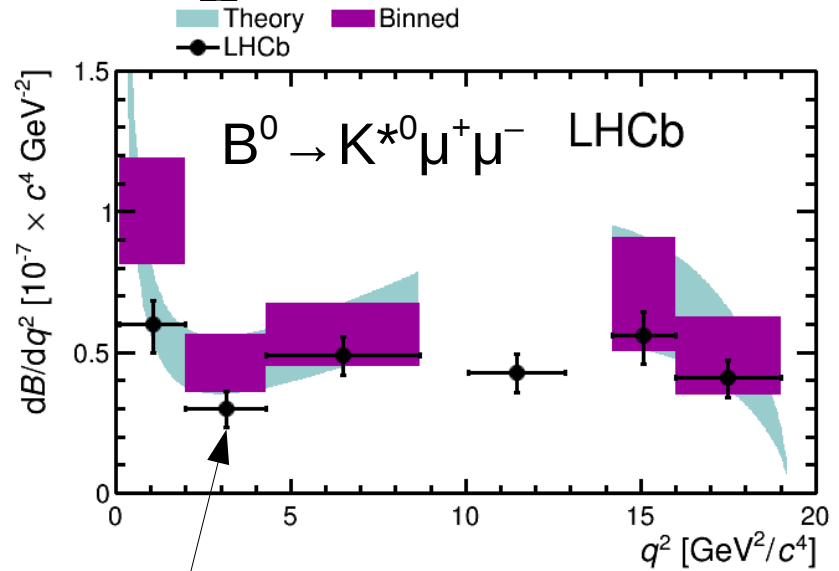
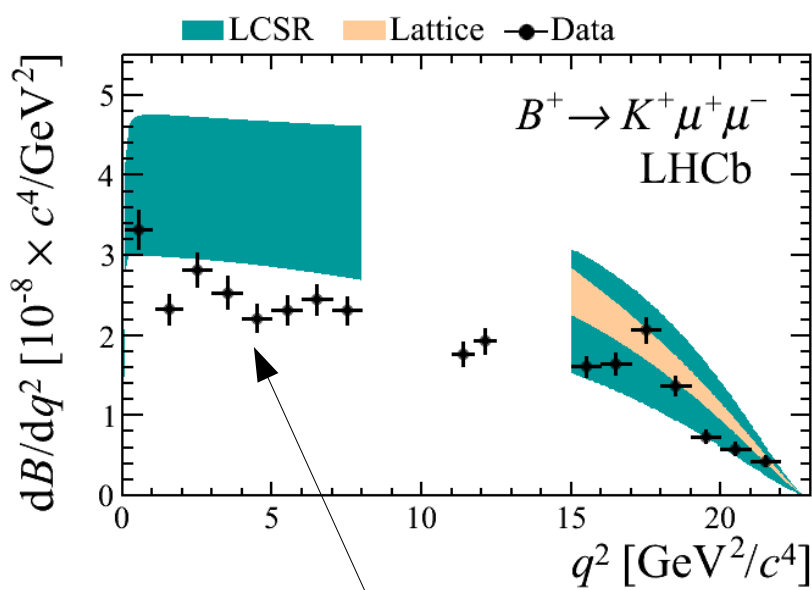
- Dimuon pair is predominantly spin-1 P_5'
 - either vector (V) or axial-vector (A)
- There are 6 non-negligible amplitudes
 - 3 for VV and 3 for VA
 - expressed as $A_{0,\perp,\parallel}^{L,R}$ (transversity basis)
- P_5' related to difference between relative phase of longitudinal (0) and perpendicularly (\perp) polarised amplitudes for VV and VA
 - constructed so as to minimise form-factor uncertainties



$$P_5' = \sqrt{2} \frac{\text{Re}(A_0^L A_\perp^{L*} - A_0^R A_\perp^{R*})}{\sqrt{(|A_0^L|^2 + |A_0^R|^2) (|A_\parallel^L|^2 + |A_\parallel^R|^2 + |A_\perp^L|^2 + |A_\perp^R|^2)}}$$

Sensitive to NP in V or A couplings (Wilson coefficients $C_9^{(i)}$ & $C_{10}^{(i)}$)

$b \rightarrow s \mu^+ \mu^-$ branching fractions

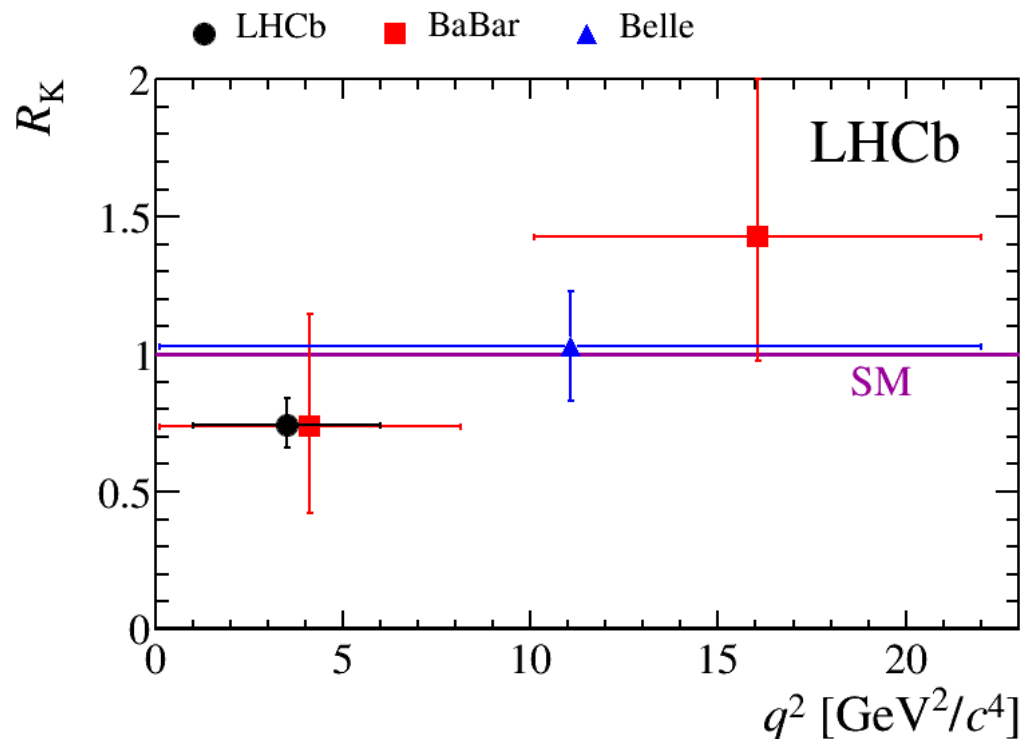


Trend to be below SM prediction at low q^2 ?

Lepton universality – R_K

PRL 113 (2014) 151601

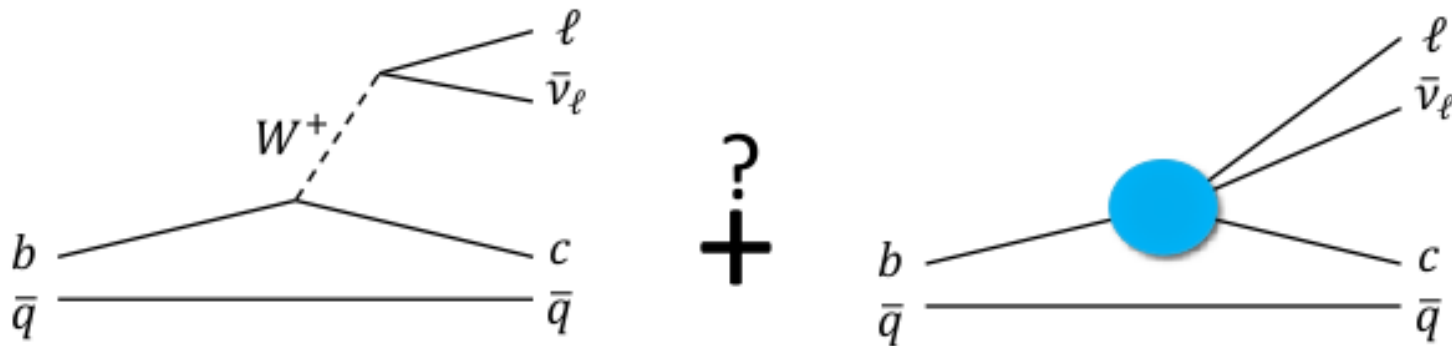
Deficit of $B \rightarrow K\mu^+\mu^-$ compared to expectation
also seen in $K\mu^+\mu^-/Ke^+e^-$ ratio (R_K) – negligible theoretical uncertainty



$$R_K(1 < q^2 < 6 \text{ GeV}^2) = 0.745^{+0.090}_{-0.074} \pm 0.036$$

$$B \rightarrow D^{(*)} \tau \nu$$

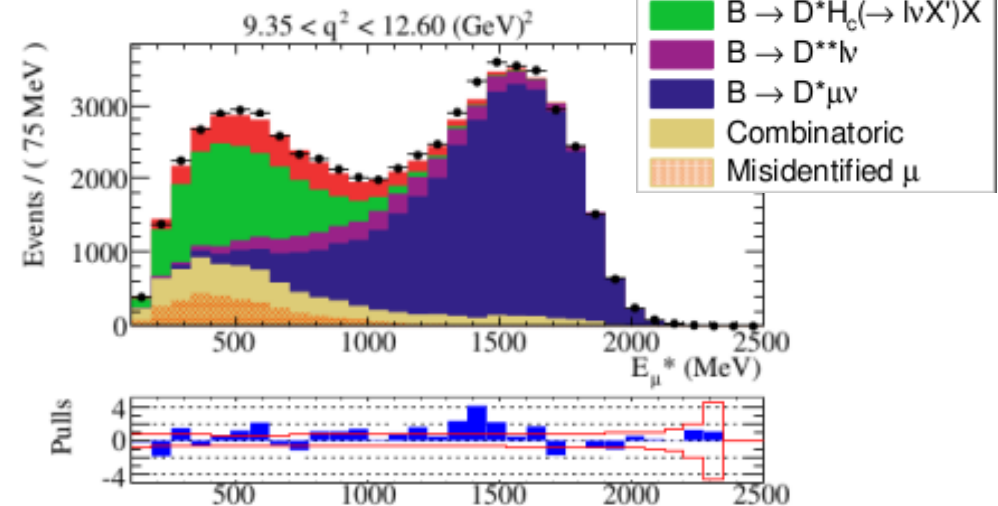
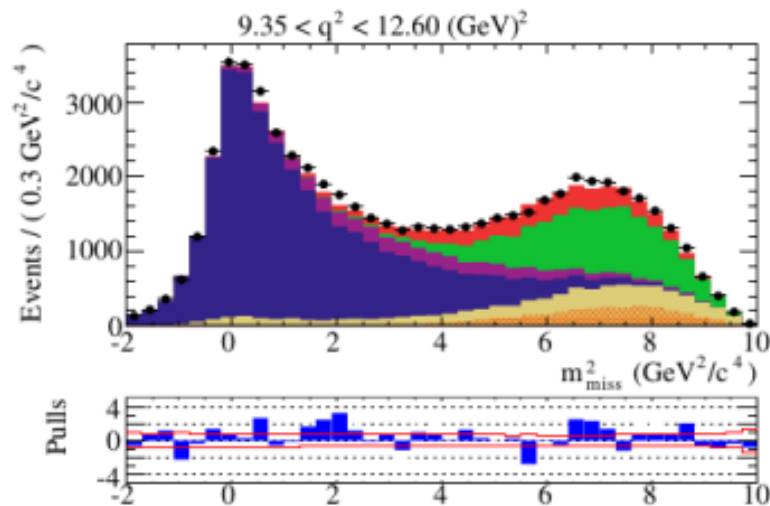
- Powerful channel to test lepton universality
 - ratios $R(D^{(*)}) = B(B \rightarrow D^{(*)} \tau \nu) / B(B \rightarrow D^{(*)} \mu \nu)$ could deviate from SM values, e.g. in models with charged Higgs
- Heightened interest in this area
 - anomalous results from BaBar
 - other hints of lepton universality violation, e.g. R_K , $H \rightarrow \tau \mu$



$B \rightarrow D^* \tau \nu$ at LHCb

LHCb-PAPER-2015-025

- Identify $B \rightarrow D^* \tau \nu$, $D^* \rightarrow D \pi$, $D \rightarrow K \pi$, $\tau \rightarrow \mu \nu \bar{\nu}$
 - Kinematic reconstruction to calculate $M_{\text{miss}}^2 = (p_B - p_{D^*} - p_\mu)^2$
 - Require significant B, D, τ flight distance & use isolation MVA
- Separate signal / background by fitting in M_{miss}^2 , q^2 and E_μ
 - Shown below high q^2 region only (best sensitivity)

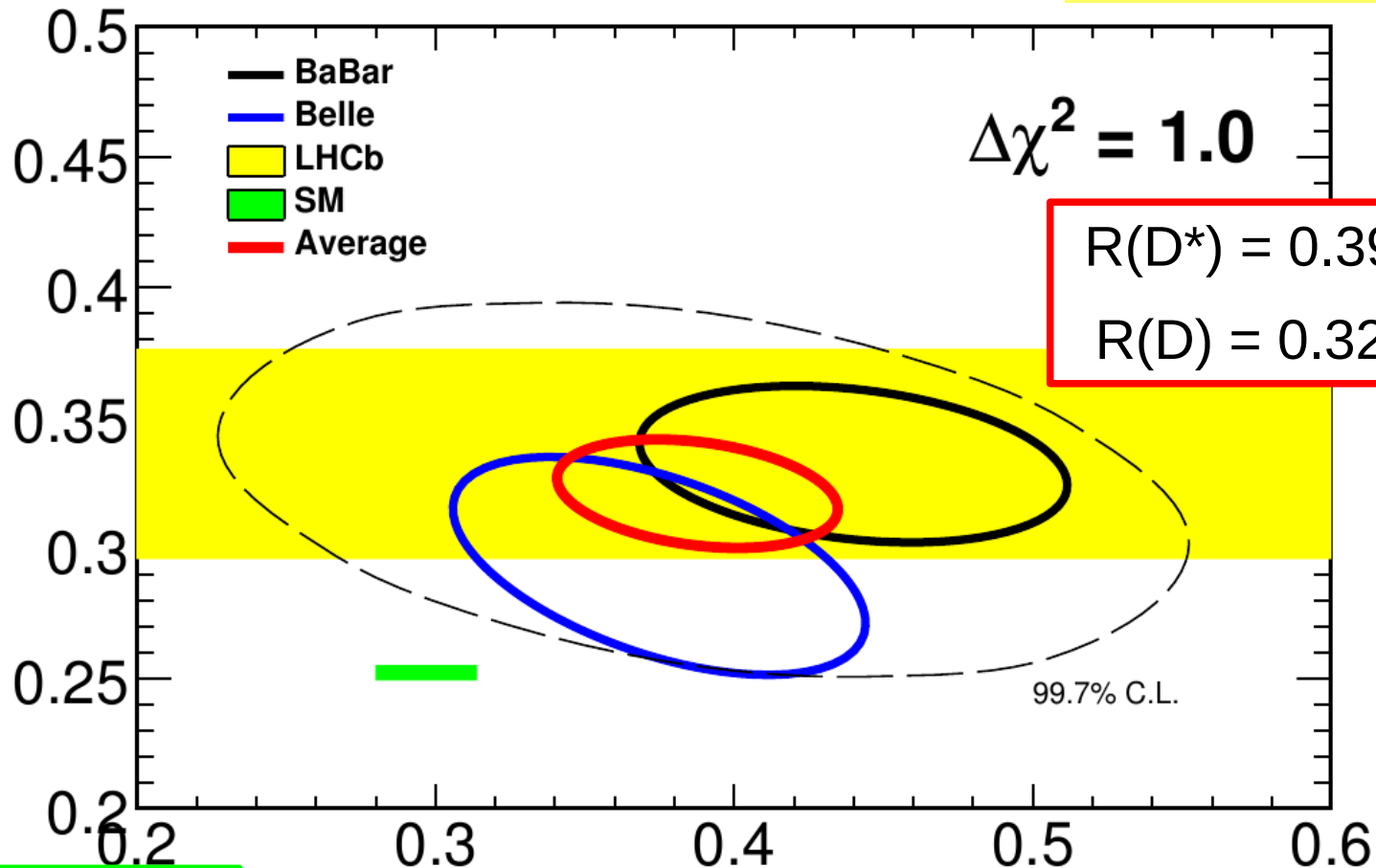


$$R(D^*) = 0.336 \pm 0.027 \pm 0.030$$

$B \rightarrow D^{(*)}TV$

Tension with SM seems to persist

Very preliminary & unofficial average including new LHCb & Belle results



$$R(D^*) = 0.390 \pm 0.047$$

$$R(D) = 0.322 \pm 0.021$$

SM predictions from
PRD 85 (2012) 094025

Careful averaging needed to account for
statistical and systematic correlations

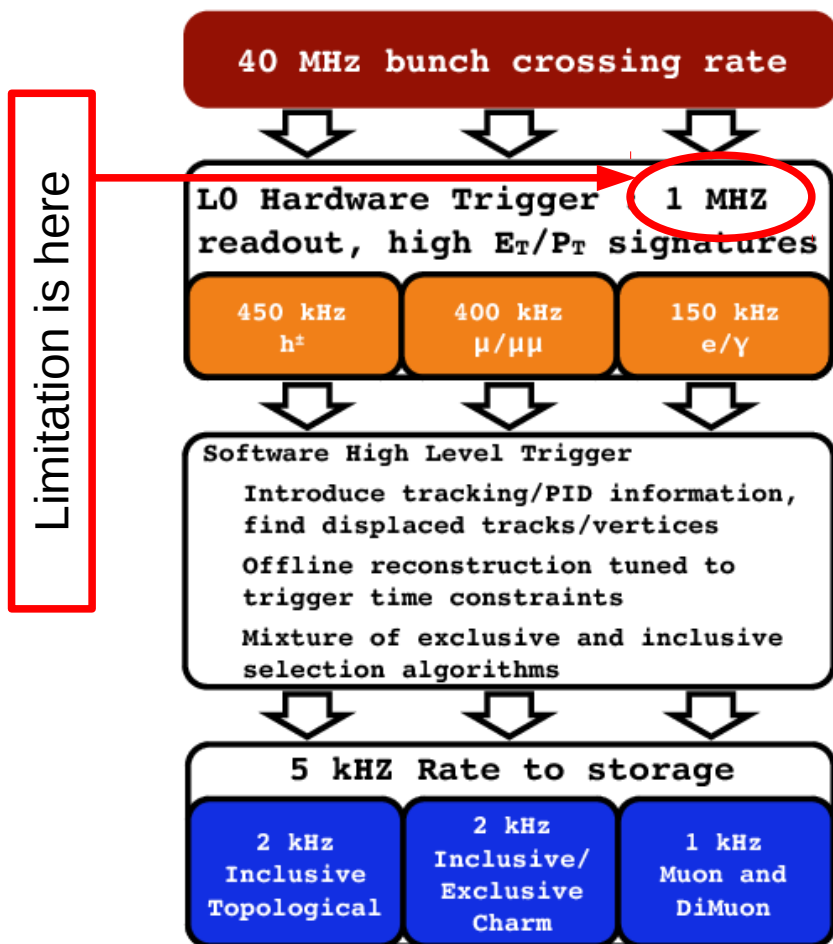
Summary of rare decays

- Accumulating hints of non-SM effects?
 - in particular related to lepton universality
 - observables with negligible theoretical uncertainty
- It is easy to see patterns, yet there may be none
 - no single effect with 5σ significance
 - various models proposed that can explain effects
- Need more data!
 - many results still to come from Run I data
 - from ATLAS and CMS, as well as LHCb
 - ... and Run II is happening

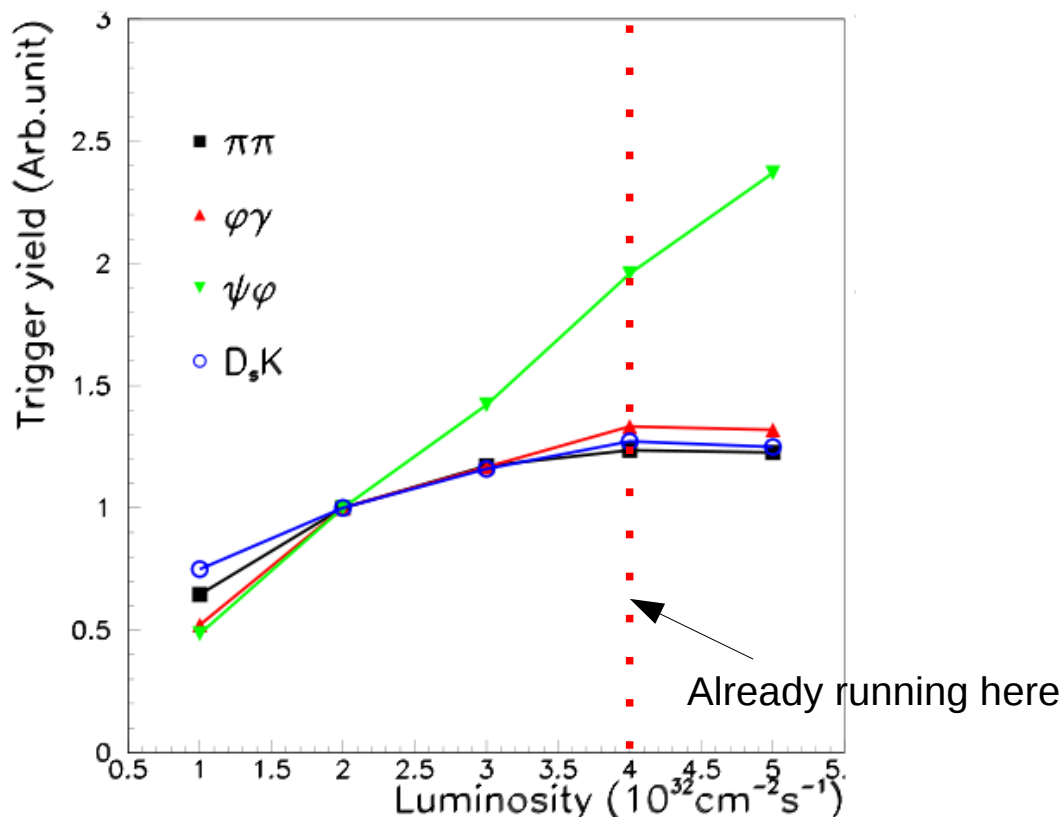
LHCb upgrade

- To fully exploit LHC potential for heavy flavour physics will require an upgrade to LHCb
 - full readout & trigger at 40 MHz to enable high L running
 - “high L” = $10^{33}/\text{cm}^2/\text{s}$ (so independent of machine upgrade)
 - planned for 2018 shutdown
- Physics case:
 - “exploration” of 1st phase will become “precision studies”
 - new opportunities for exploration open up (e.g. testing consistency of CP violation in tree vs. loop processes)

LHC upgrade and the all important trigger

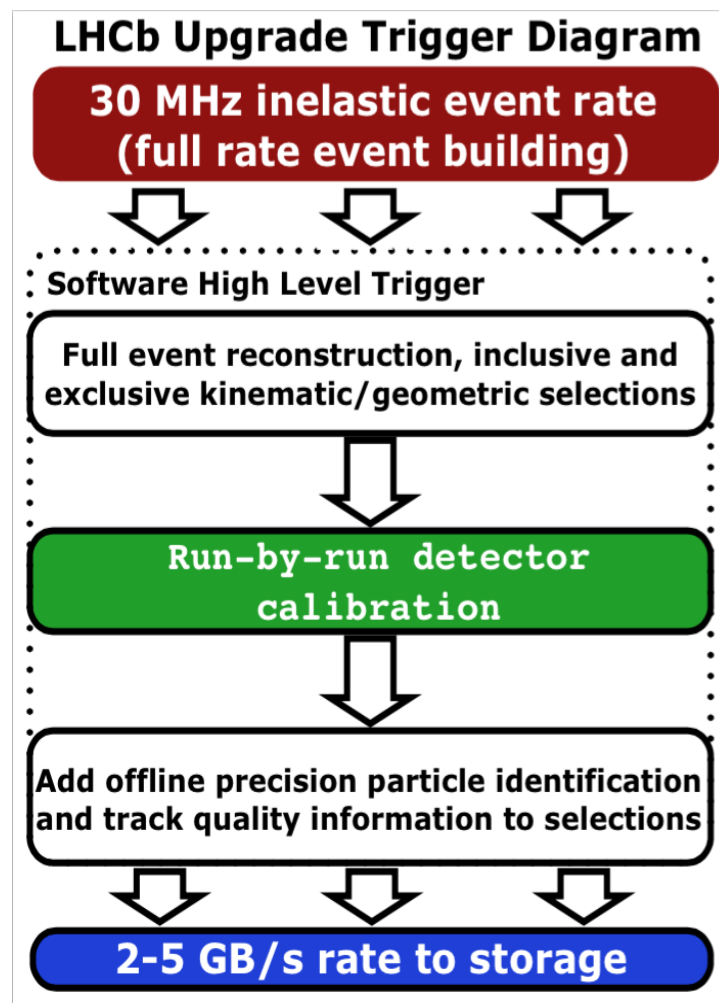
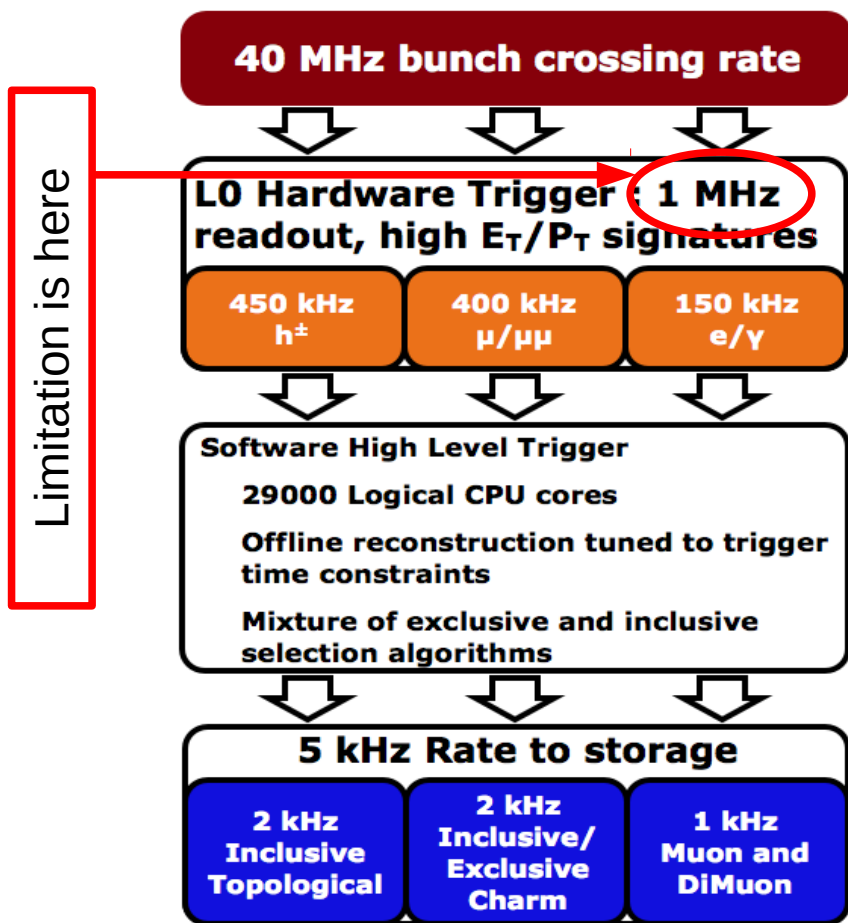


higher luminosity
 → need to cut harder at L0 to keep rate at 1 MHz
 → lower efficiency



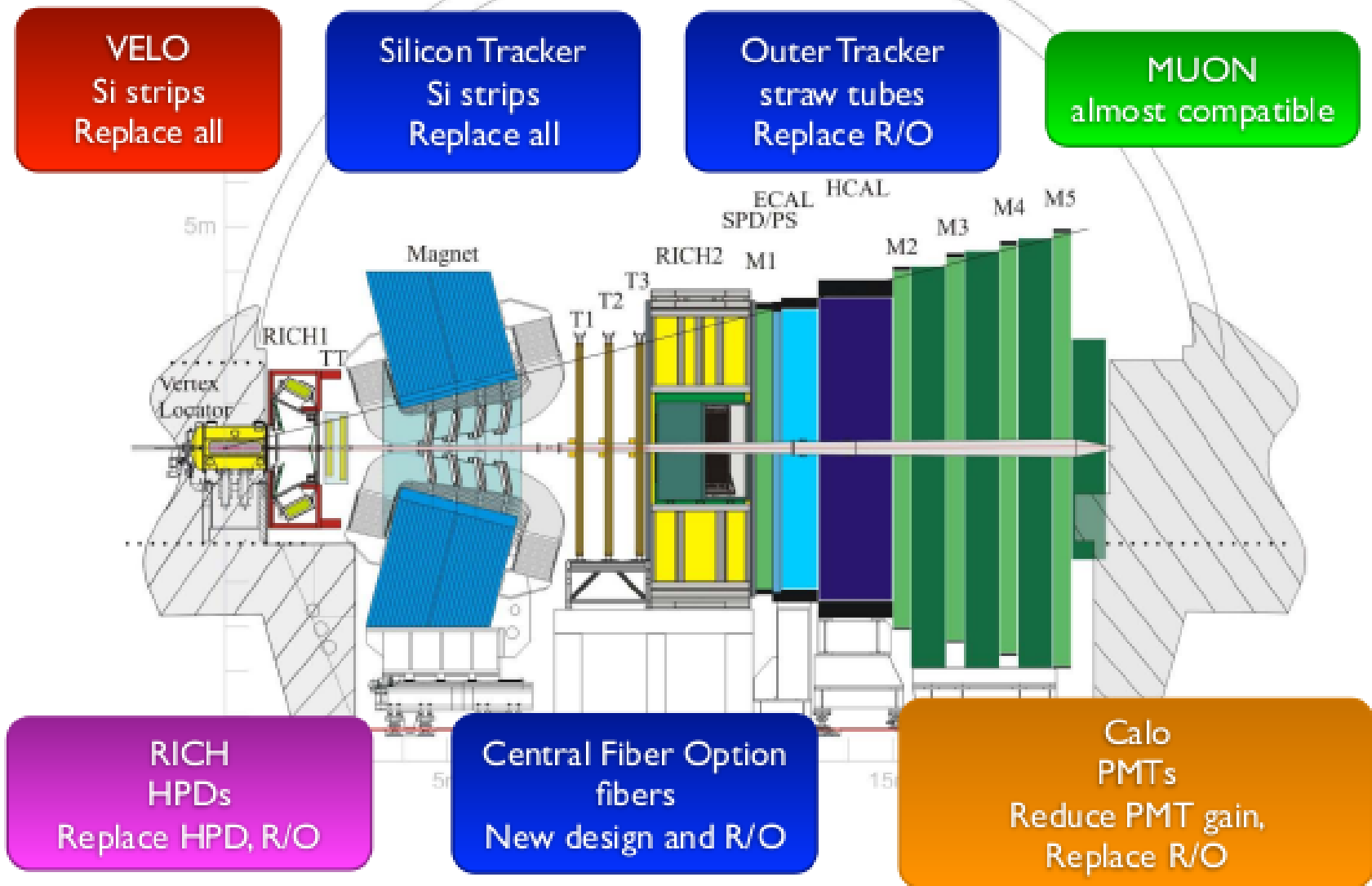
- readout detector at 40 MHz
- implement trigger fully in software → efficiency gains
- run at L_{inst} up to $2 \cdot 10^{33} / \text{cm}^2 / \text{s}$

LHC upgrade and the all important trigger



- readout detector at 40 MHz
- implement trigger fully in software → efficiency gains
- run at L_{inst} up to $2 \cdot 10^{33}/\text{cm}^2/\text{s}$

LHCb detector upgrade



Other future flavour experiments

- SuperKEKB/Belle2 & SuperB
 - $B \rightarrow \tau \nu$, inclusive measurements, τ physics, ...
- Rare kaon decays
 - $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ (NA62, CERN); $K^0 \rightarrow \pi^0 \nu \bar{\nu}$ (KOTO, J-PARC)
- Muon to electron conversion (charged lepton flavour violation)
 - COMET/PRIME (J-PARC); $\mu 2e$ (FNAL)

The holy grail of kaon physics: $K \rightarrow \pi \nu \bar{\nu}$

Highest CKM suppression
of the $s \rightarrow d$ coupling:

$$A \sim (m_t/m_W)^2 |V_{ts}^* V_{td}| \sim \lambda^5$$

SM branching ratios

(Brod, Gorbahn, Stamou; PRD83 (2011) 034030)

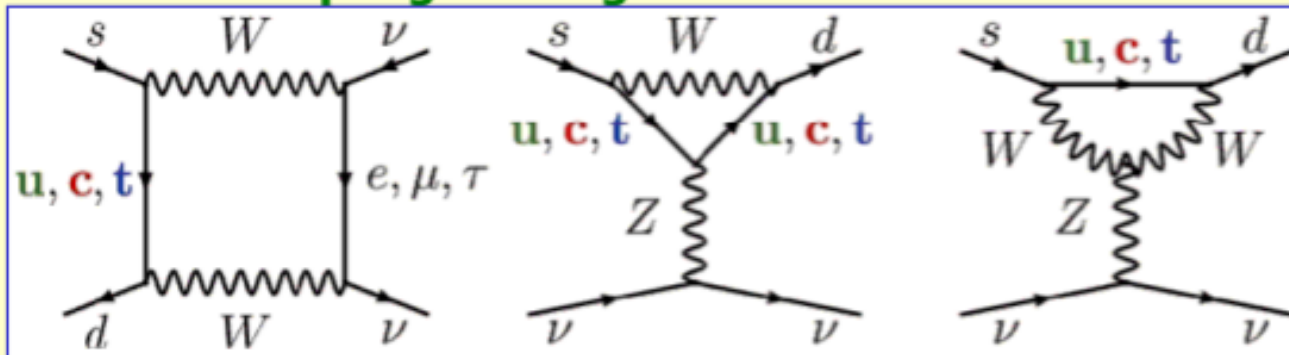
Mode	$BR_{SM} \times 10^{11}$
$K^+ \rightarrow \pi^+ \nu \bar{\nu} (\gamma)$	$7.81 \pm 0.75 \pm 0.29$
$K_L \rightarrow \pi^0 \nu \bar{\nu}$	$2.43 \pm 0.39 \pm 0.06$



CKM parametric
(mainly $|V_{ts}|$)

Intrinsic

SM: box and penguin diagrams



Next generation experiments should
measure these decays for the 1st time

- $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ (NA62, CERN)
- $K^0 \rightarrow \pi^0 \nu \bar{\nu}$ (KOTO, J-PARC)

The need for more precision

- “Imagine if Fitch and Cronin had stopped at the 1% level, how much physics would have been missed”

– A.Soni

- “A special search at Dubna was carried out by Okonov and his group. They did not find a single $K_L^0 \rightarrow \pi^+\pi^-$ event among **600 decays** into charged particles (Anikira et al., JETP 1962). At that stage the search was terminated by the administration of the lab. **The group was unlucky.**”

– L.Okun

(remember: $B(K_L^0 \rightarrow \pi^+\pi^-) \sim 2 \cdot 10^{-3}$)

Summary

- We still don't know:
 - why there are so many fermions in the SM
 - what causes the baryon asymmetry of the Universe
 - where exactly the new physics is ...
 - ... and what its flavour structure is
- Prospects are good for progress in the next few years
- Will have continuing programme of flavour physics into the 2020s and perhaps beyond
 - complementary to the high- p_T programme of the LHC

References and background reading

- Reviews by the Particle Data Group
 - <http://pdg.lbl.gov/>
- Heavy Flavour Averaging Group (HFAG)
 - <http://www.slac.stanford.edu/xorg/hfag/>
- CKMfitter & UTfit
 - <http://ckmfitter.in2p3.fr/> & <http://www.utfit.org/>
- Review journals (e.g. Ann. Rev. Nucl. Part. Phys.)
 - <http://nucl.annualreviews.org>
- Proceedings of CKM workshops
 - Phys.Rept. 494 (2010) 197, eConf C100906
- Books
 - CP violation, I.I.Bigi and A.I.Sanda (CUP)
 - CP violation, G.C.Branco, L.Lavoura & J.P.Silva (OUP)