

Flavour Physics in the LHC Era

Lecture 2 of 3

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HCPSS 2015
2 July 2015



Contents

- Part 1
 - Why is flavour physics interesting?
- Part 2
 - What do we know from previous experiments?
- Part 3
 - What do we hope to learn from current and future heavy flavour experiments?

Today hope to cover Part 2 & start Part 3

(but let's see how we go)

What do we know about heavy quark flavour physics as of today?

CKM Matrix : parametrizations

- Many different possible choices of 4 parameters
- PDG: 3 mixing angles and 1 phase

PRL 53 (1984) 1802

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix}$$

- Apparent hierarchy: $s_{12} \sim 0.2$, $s_{23} \sim 0.04$, $s_{13} \sim 0.004$

– [Wolfenstein parametrization](#) (expansion parameter $\lambda \sim \sin \theta_c \sim 0.22$)

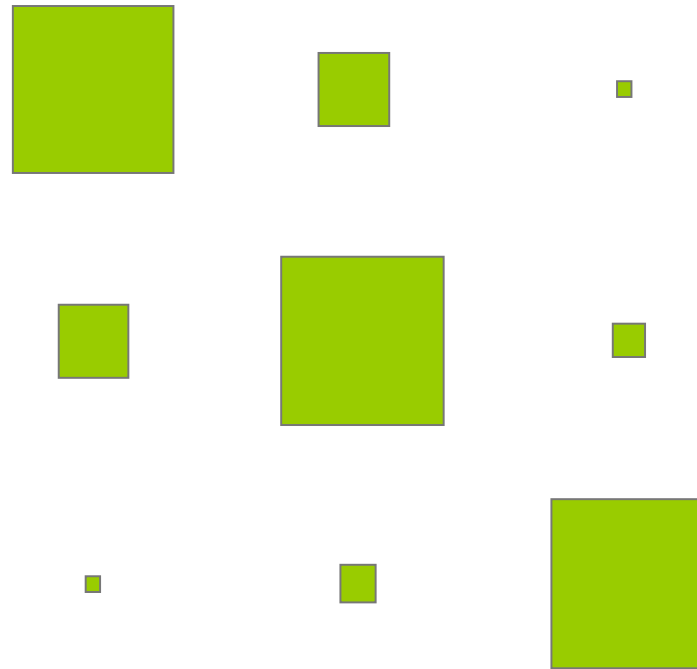
PRL 51 (1983) 1945

$$V = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$

- Other choices, eg. based on CP violating phases

Hierarchy in quark mixing

$$V = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$



Very suggestive pattern
 No known underlying reason
 Situation for leptons (vs) is completely different

CKM matrix to $O(\lambda^5)$

$$V_{\text{CKM}} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda + \frac{1}{2}A^2\lambda^5[1 - 2(\rho + i\eta)] & 1 - \frac{1}{2}\lambda^2 - \frac{1}{8}\lambda^4(1 + 4A^2) & A\lambda^2 \\ A\lambda^3[1 - (1 - \frac{1}{2}\lambda^2)(\rho + i\eta)] & -A\lambda^2 + \frac{1}{2}A\lambda^4[1 - 2(\rho + i\eta)] & 1 - \frac{1}{2}A^2\lambda^4 \end{pmatrix}$$

Diagram illustrating the CKM matrix elements and their imaginary parts:

- Red oval: $-\lambda + \frac{1}{2}A^2\lambda^5[1 - 2(\rho + i\eta)]$ (imaginary part at $O(\lambda^5)$)
- Blue oval: $A\lambda^3(\rho - i\eta)$ (imaginary part at $O(\lambda^3)$)
- Green oval: $-A\lambda^2 + \frac{1}{2}A\lambda^4[1 - 2(\rho + i\eta)]$ (imaginary part at $O(\lambda^4)$)
- Blue oval: $A\lambda^2$ (imaginary part at $O(\lambda^3)$)

Remember – only *relative* phases are observable

Unitarity Tests

- The CKM matrix must be unitary

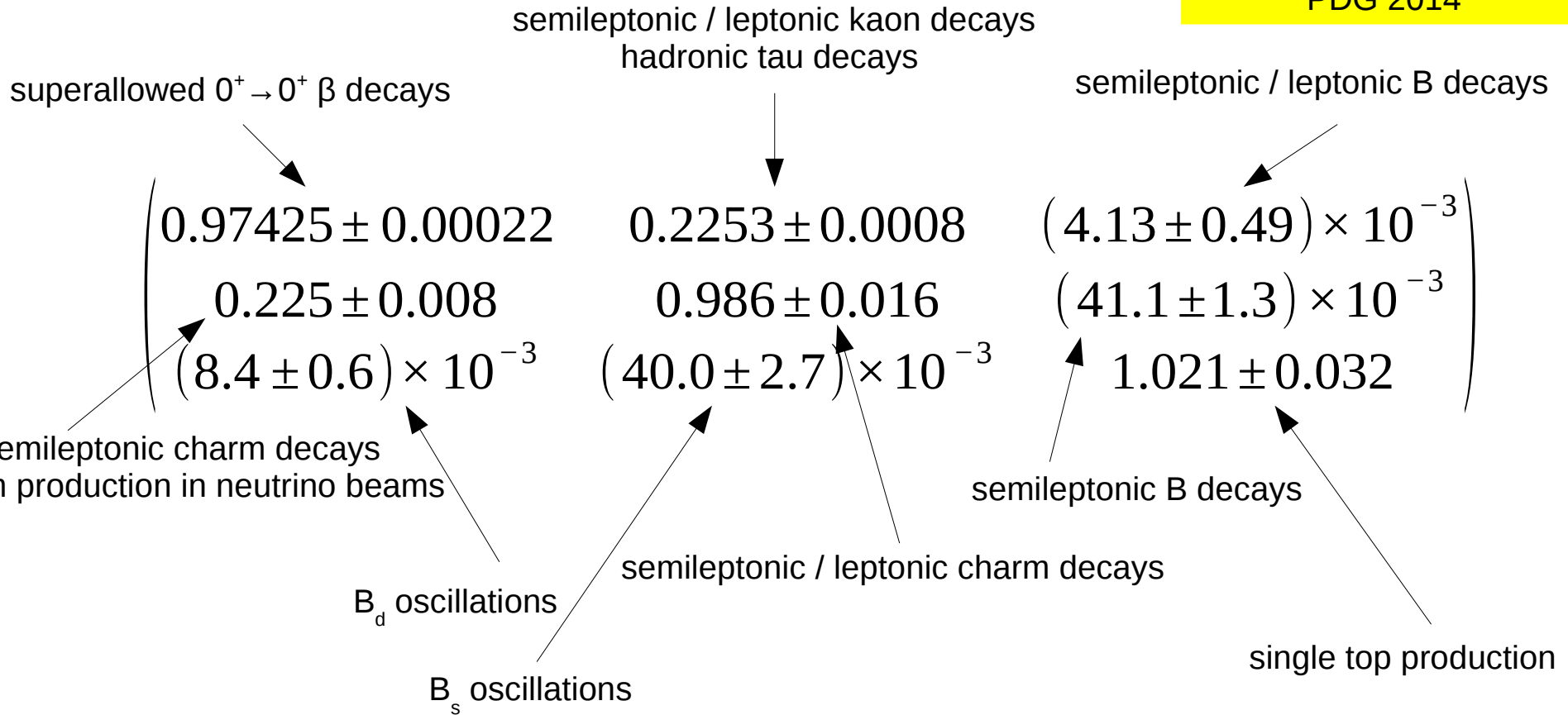
$$V_{CKM}^+ V_{CKM} = V_{CKM} V_{CKM}^+ = 1$$

- Provides numerous tests of constraints between independent observables, such as

$$\begin{aligned} |V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 &= 1 \\ V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* &= 0 \end{aligned}$$

CKM Matrix – Magnitudes

PDG 2014



theory inputs (eg., lattice calculations) required

The Unitarity Triangle

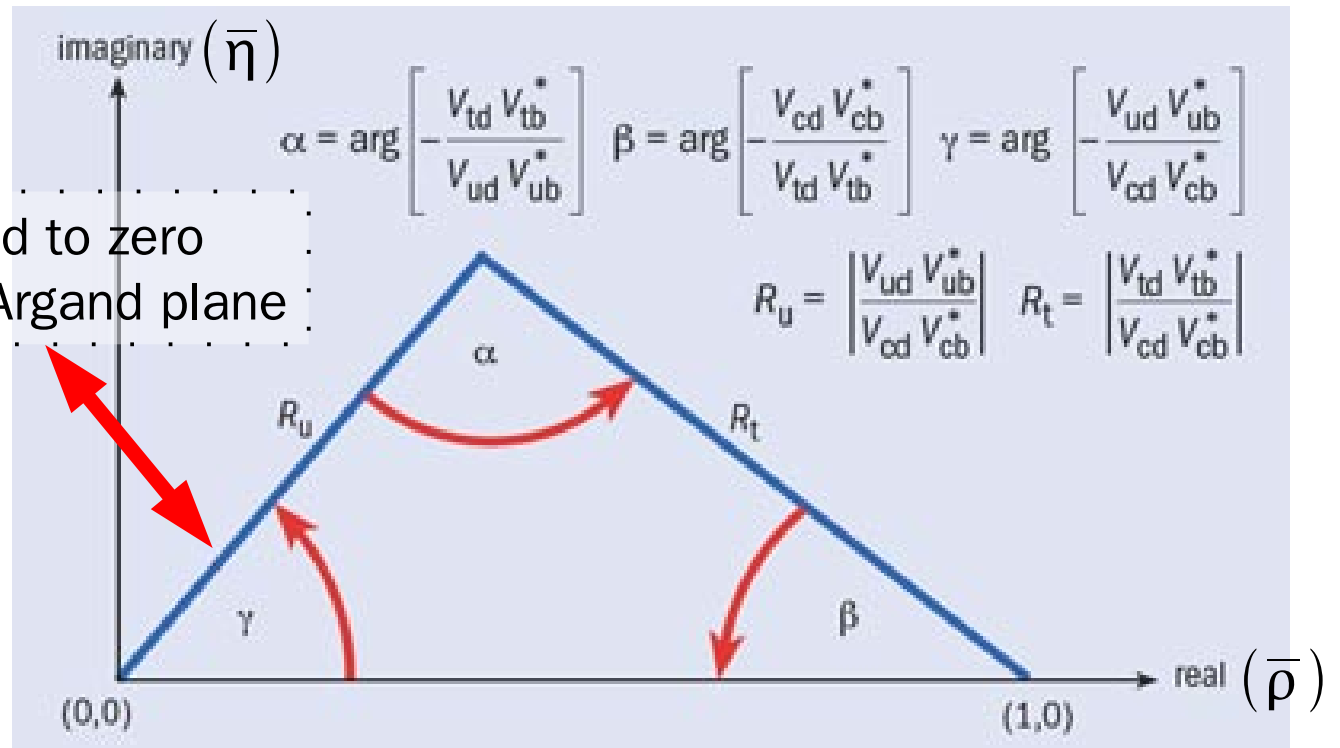
$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$



Three complex numbers add to zero
 \Rightarrow triangle in Argand plane

Axes are $\bar{\rho}$ and $\bar{\eta}$ where

$$\bar{\rho} + i\bar{\eta} \equiv -\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}$$



$$\rho + i\eta = \frac{\sqrt{1 - A^2\lambda^4}(\bar{\rho} + i\bar{\eta})}{\sqrt{1 - \lambda^2} [1 - A^2\lambda^4(\bar{\rho} + i\bar{\eta})]}$$

Predictive nature of KM mechanism

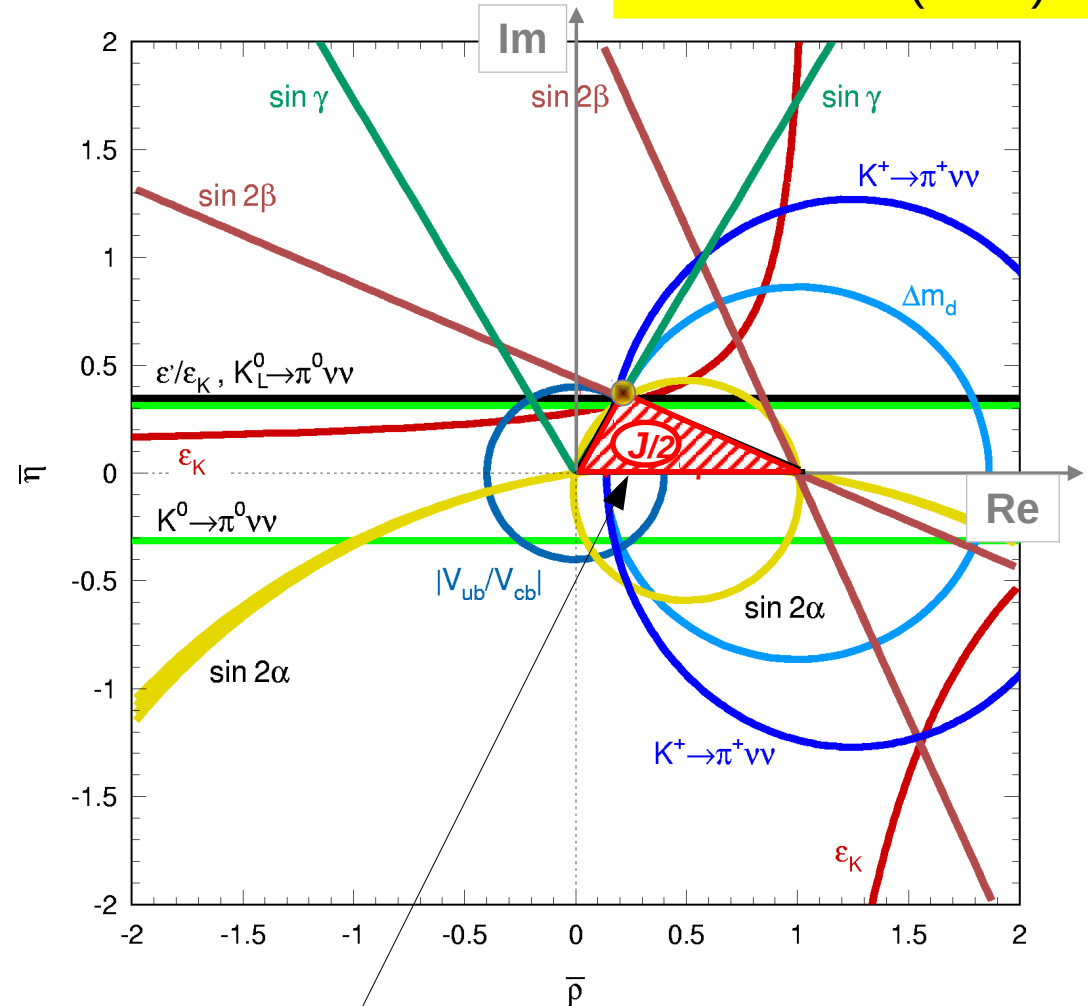
In the Standard Model the KM phase is the **sole origin of CP violation**

Hence:

all measurements must agree on the position of the apex of the Unitarity Triangle

(Illustration shown assumes no experimental or theoretical uncertainties)

EPJC 41 (2005) 1



Area of (all of) the Unitarity Triangle(s) is given by the Jarlskog invariant

Time-Dependent CP Violation in the $B^0-\bar{B}^0$ System

- For a B meson known to be 1) B^0 or 2) \bar{B}^0 at time $t=0$, then at later time t :

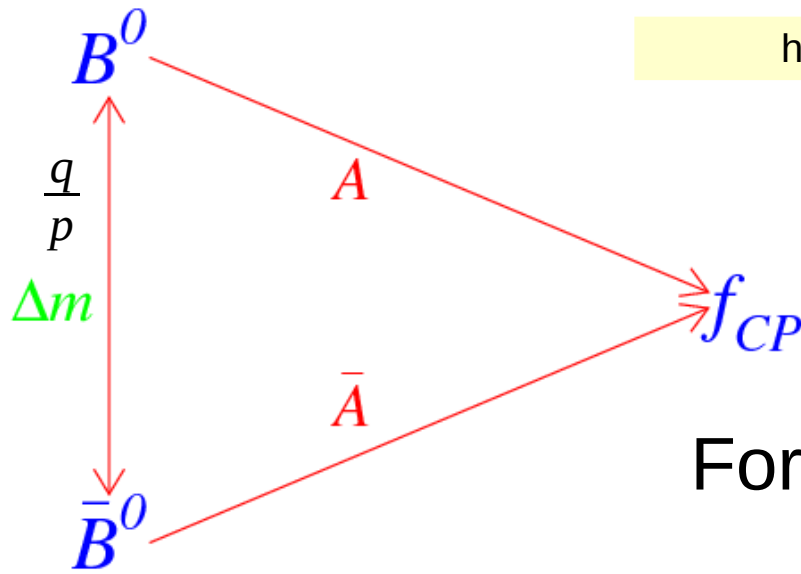
$$\Gamma(B_{phys}^0 \rightarrow f_{CP}(t)) \propto e^{-\Gamma t} (1 - (S \sin(\Delta m t) - C \cos(\Delta m t)))$$

$$\Gamma(\bar{B}_{phys}^0 \rightarrow f_{CP}(t)) \propto e^{-\Gamma t} (1 + (S \sin(\Delta m t) - C \cos(\Delta m t)))$$

here assume $\Delta\Gamma$ negligible – will see full expressions later

$$S = \frac{2\Im(\lambda_{CP})}{1 + |\lambda_{CP}^2|} \quad C = \frac{1 - |\lambda_{CP}^2|}{1 + |\lambda_{CP}^2|} \quad \lambda_{CP} = \frac{q}{p} \frac{\bar{A}}{A}$$

For $B^0 \rightarrow J/\psi K_S$, $S = \sin(2\beta)$, $C=0$

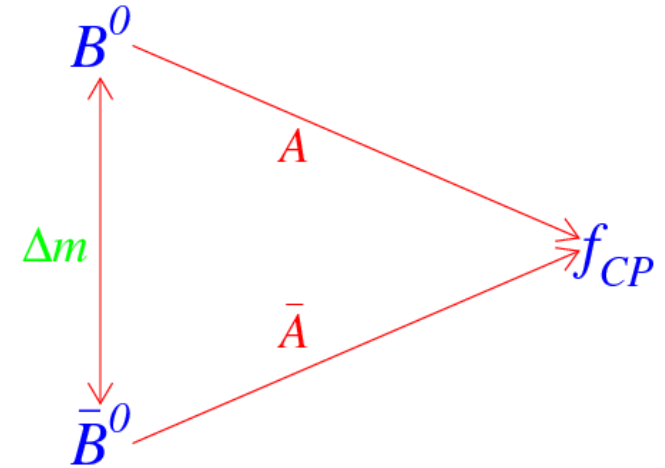


NPB 193 (1981) 85

Categories of CP violation

- Consider decay of neutral particle to a CP eigenstate

$$\lambda_{CP} = \frac{q \bar{A}}{p A}$$



$$\left| \frac{q}{p} \right| \neq 1$$

CP violation in mixing

$$\left| \frac{\bar{A}}{A} \right| \neq 1$$

CP violation in decay

$$\Im \left(\frac{q \bar{A}}{p A} \right) \neq 0$$

CP violation in interference between mixing and decay

Asymmetric B factory principle

To measure t require B meson to be moving

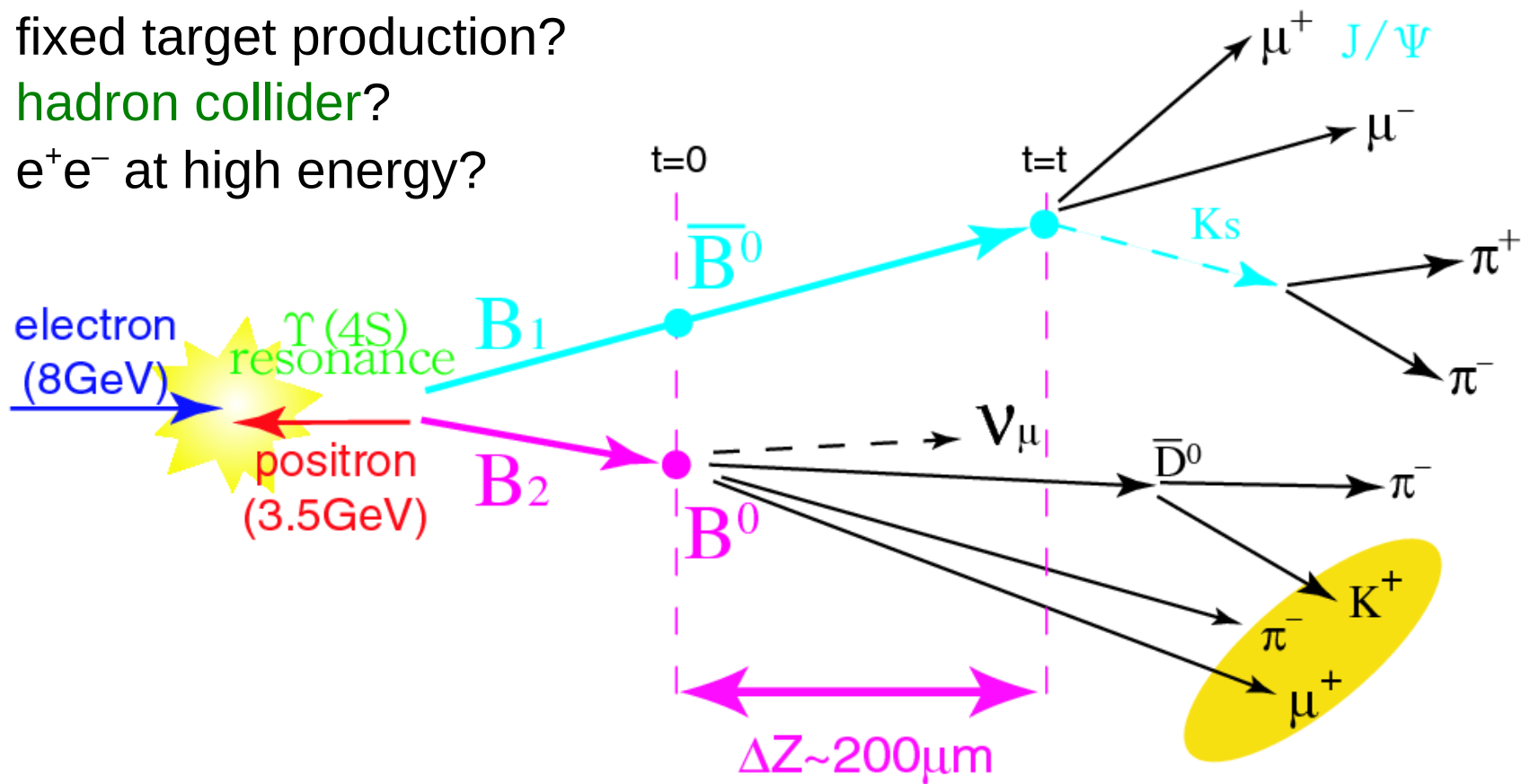
→ e^+e^- at threshold with asymmetric collisions (Odone)

Other possibilities considered

→ fixed target production?

→ hadron collider?

→ e^+e^- at high energy?



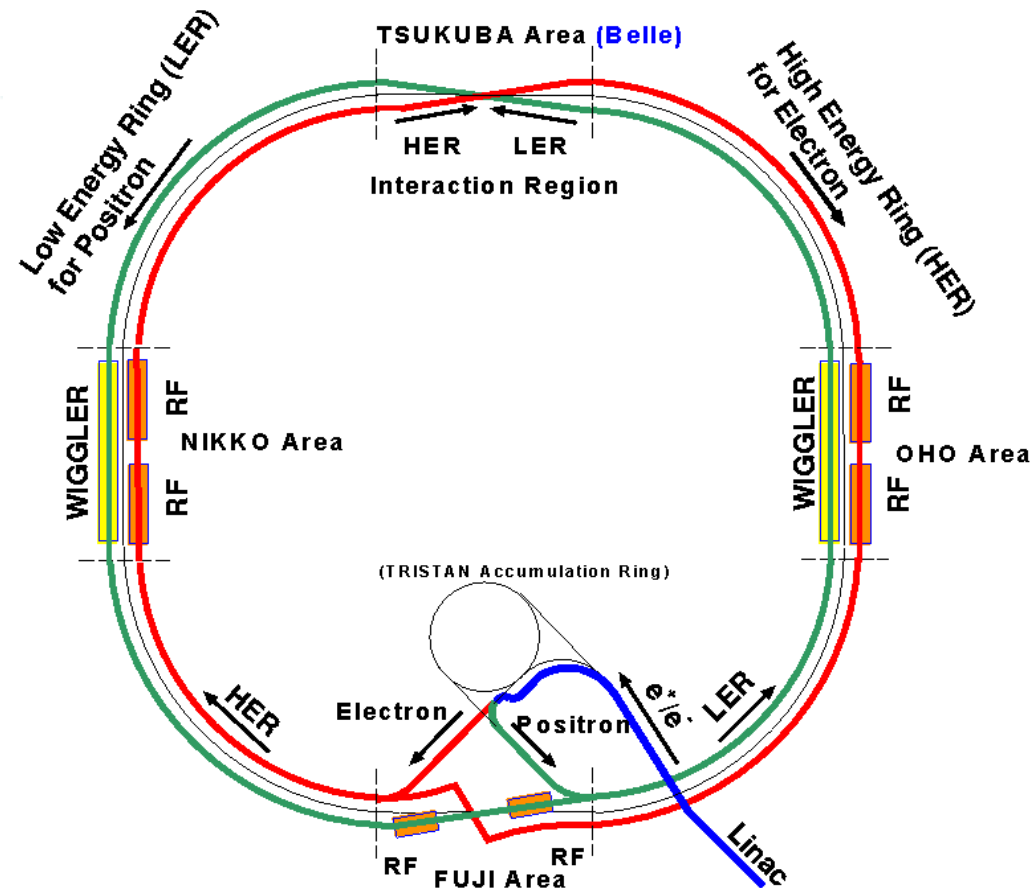
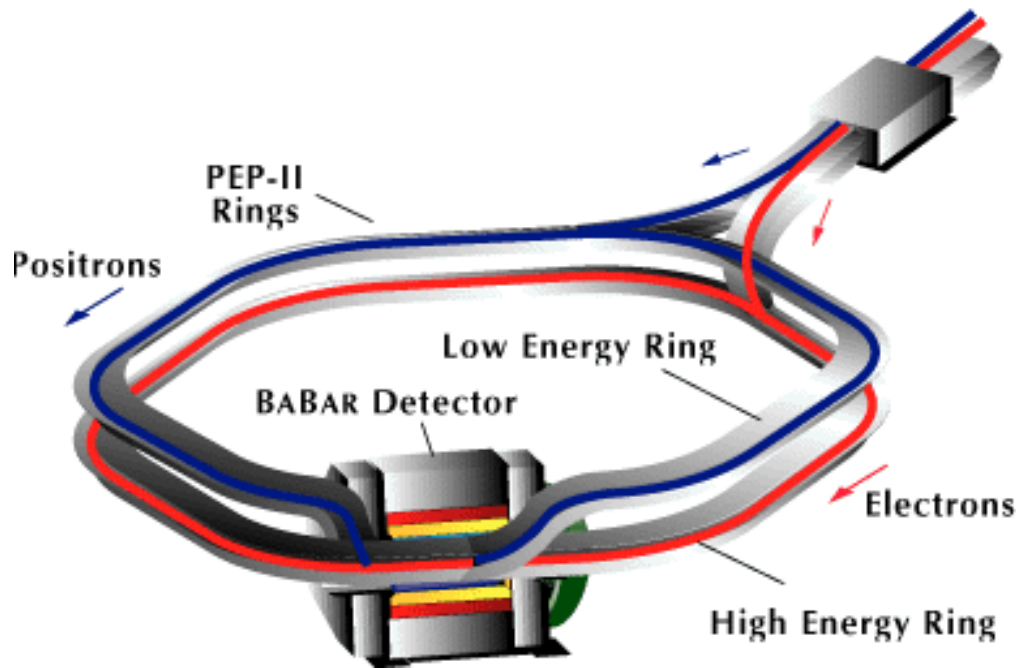
Asymmetric B Factories

PEP-II at SLAC

9.0 GeV e^- on 3.1 GeV e^+

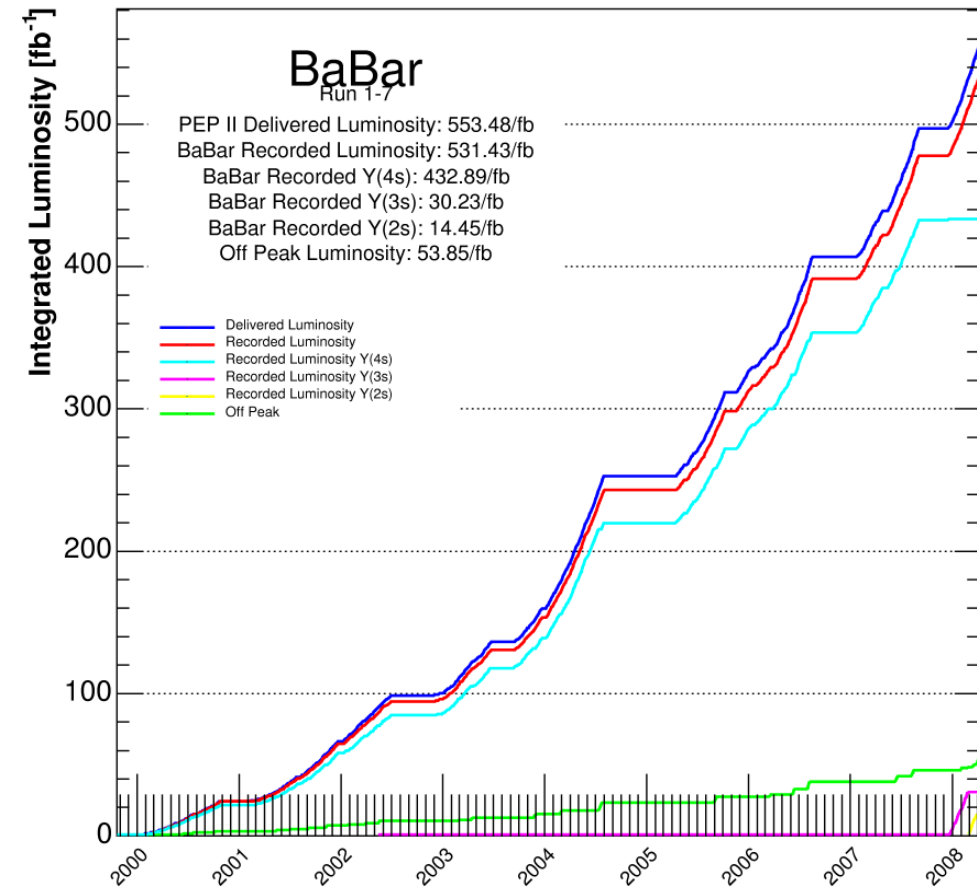
KEKB at KEK

8.0 GeV e^- on 3.5 GeV e^+



B factories – world record luminosities

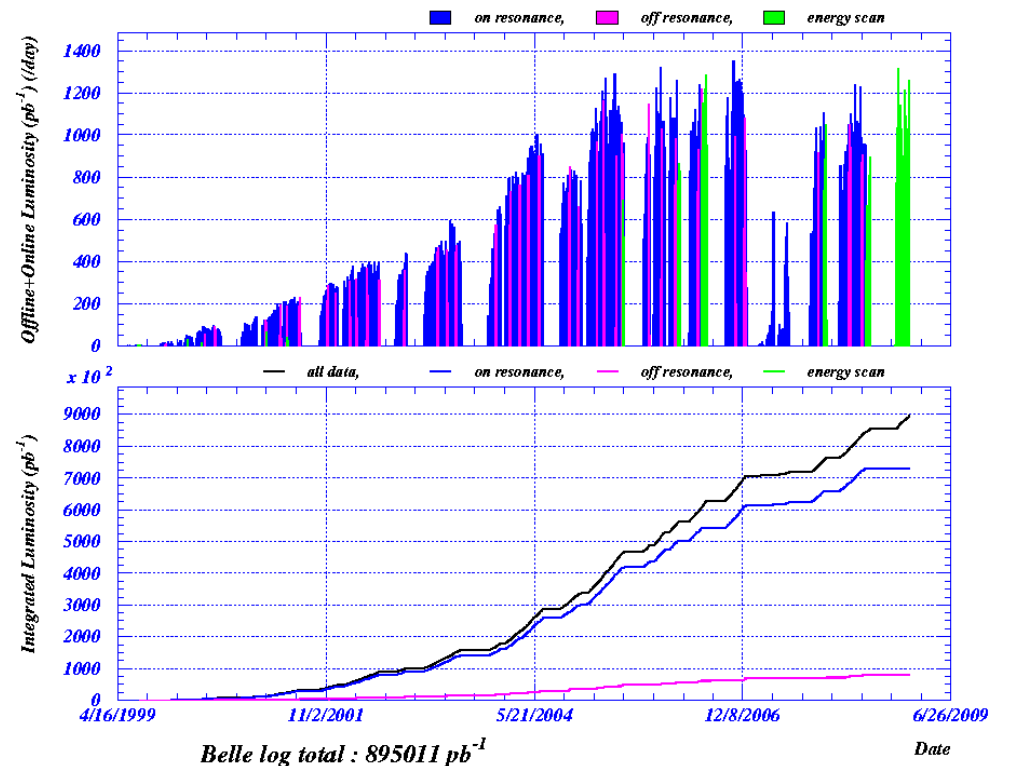
As of 2008/04/09 00:00



~ 433/fb on Y(4S)

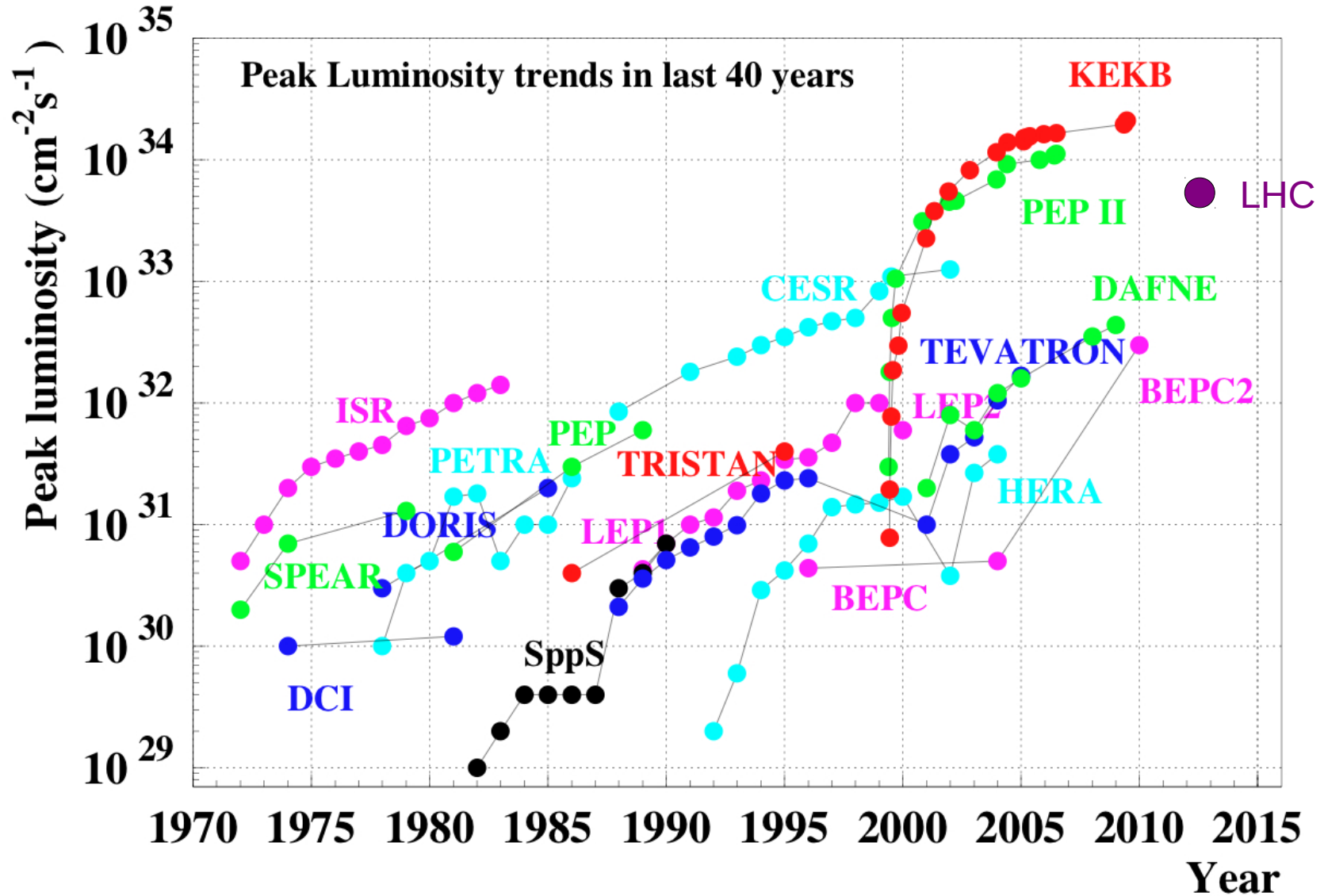
Offline+Online Luminosity (pb^{-1}) (/day)

2008/12/23 14:01

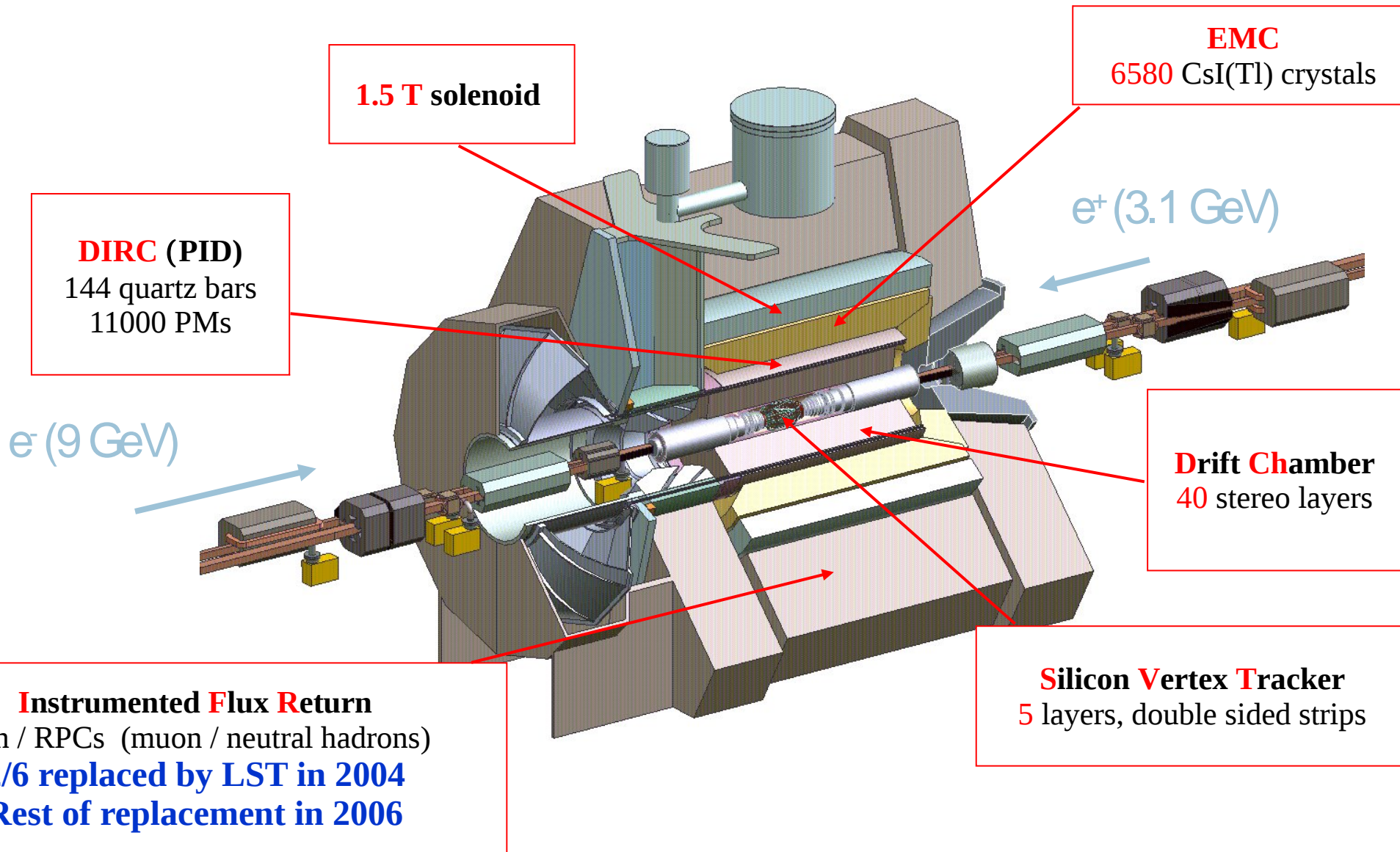


~ 711/fb on Y(4S)

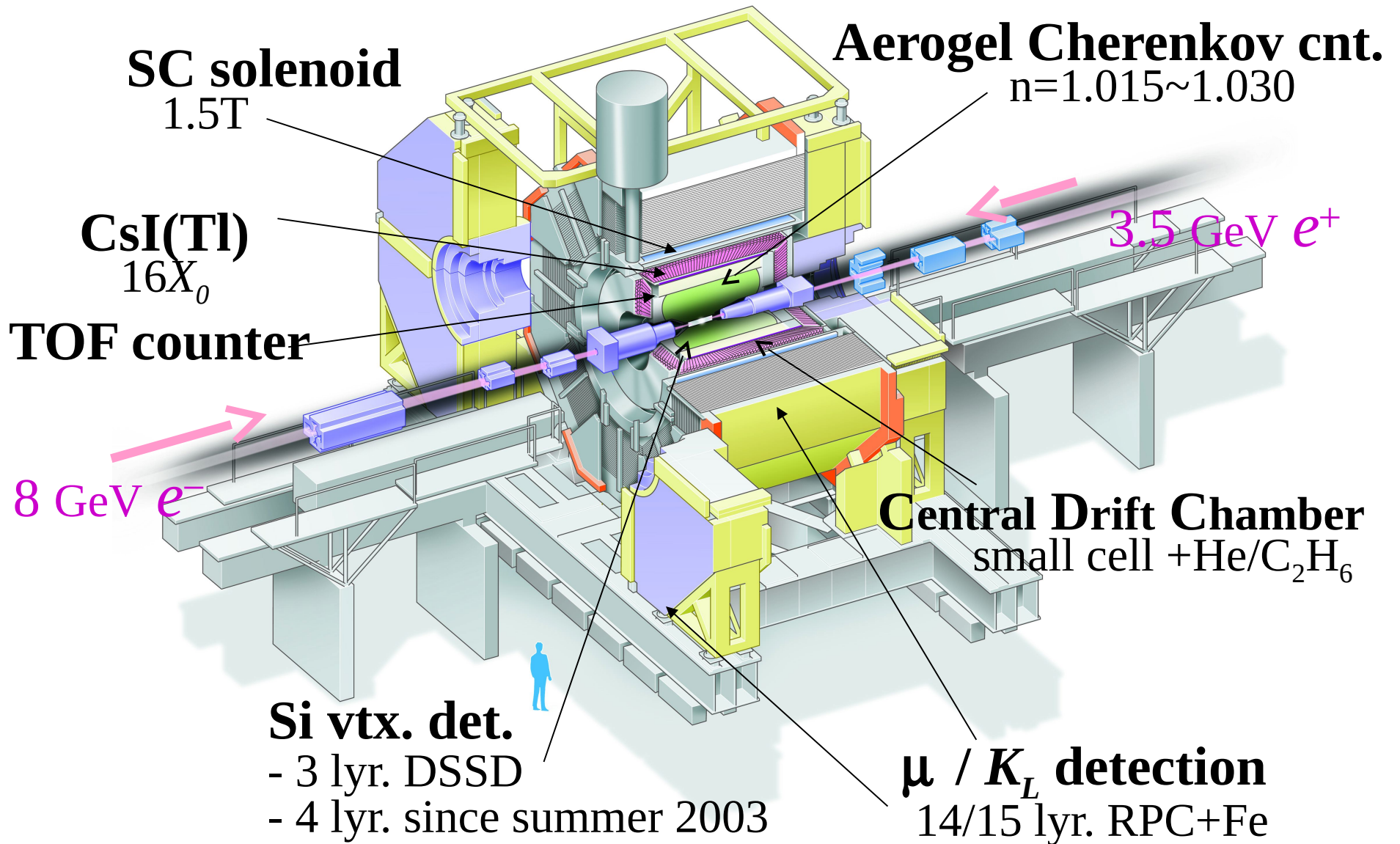
World record luminosities (2)



BaBar Detector



Belle Detector

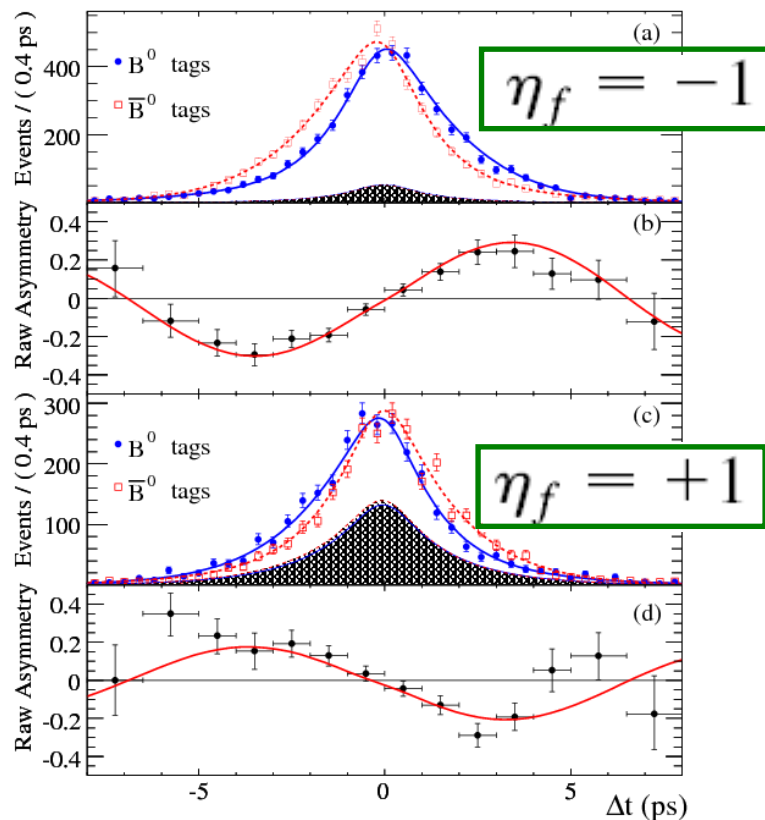


Results for the golden mode

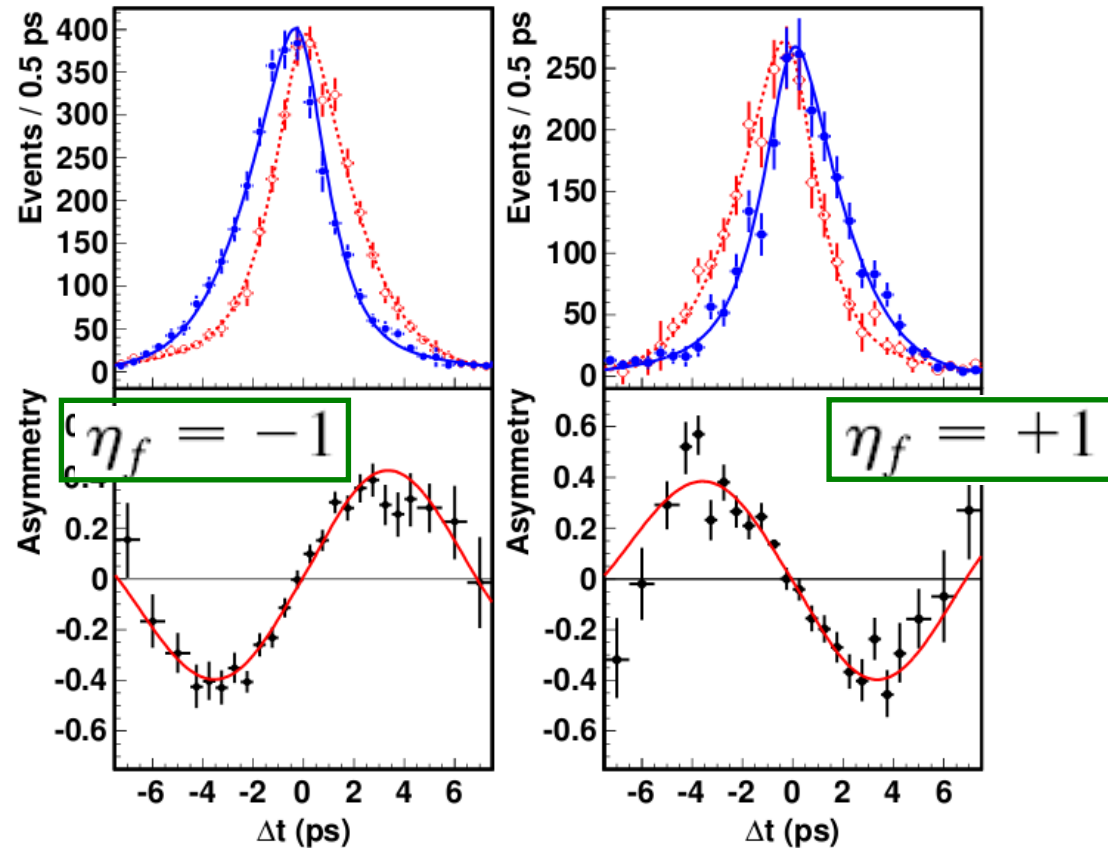


BABAR

BELLE



PRD 79 (2009) 072009



PRL 108 (2012) 171802

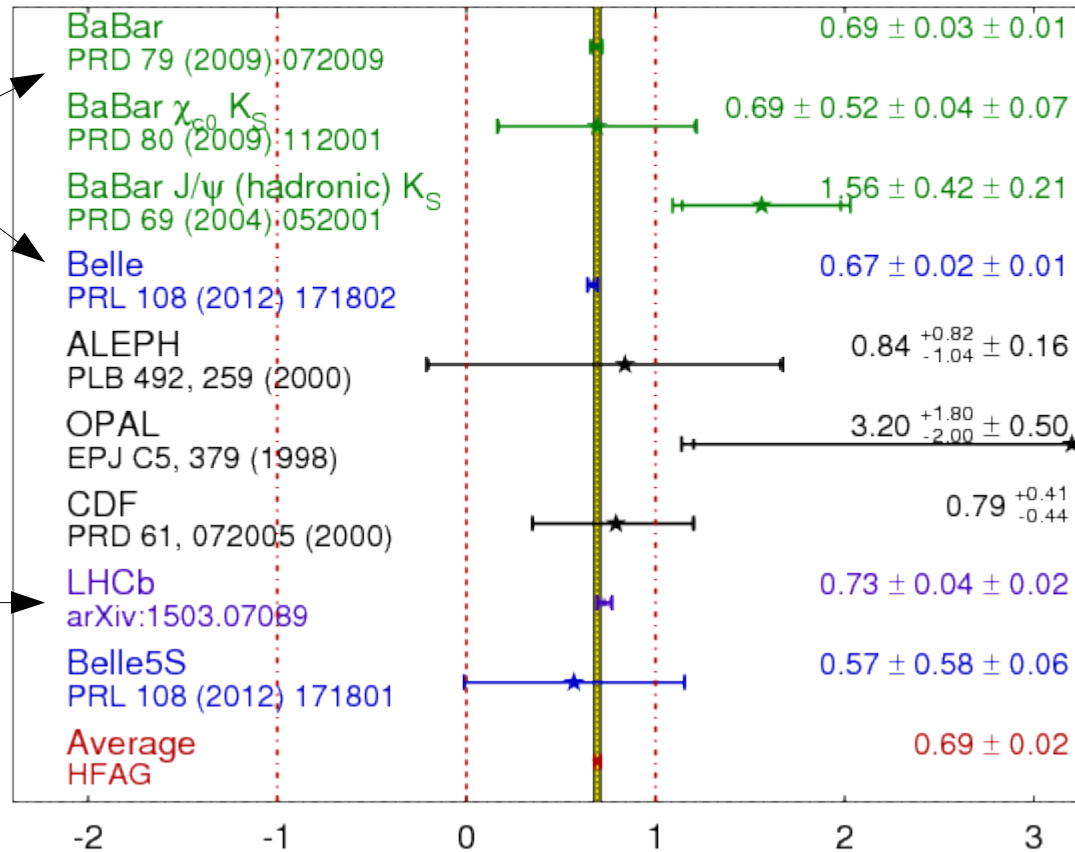
Compilation of results

$$\sin(2\beta) \equiv \sin(2\phi_1)$$

HFAG
Moriond 2015
PRELIMINARY

Results on previous slide

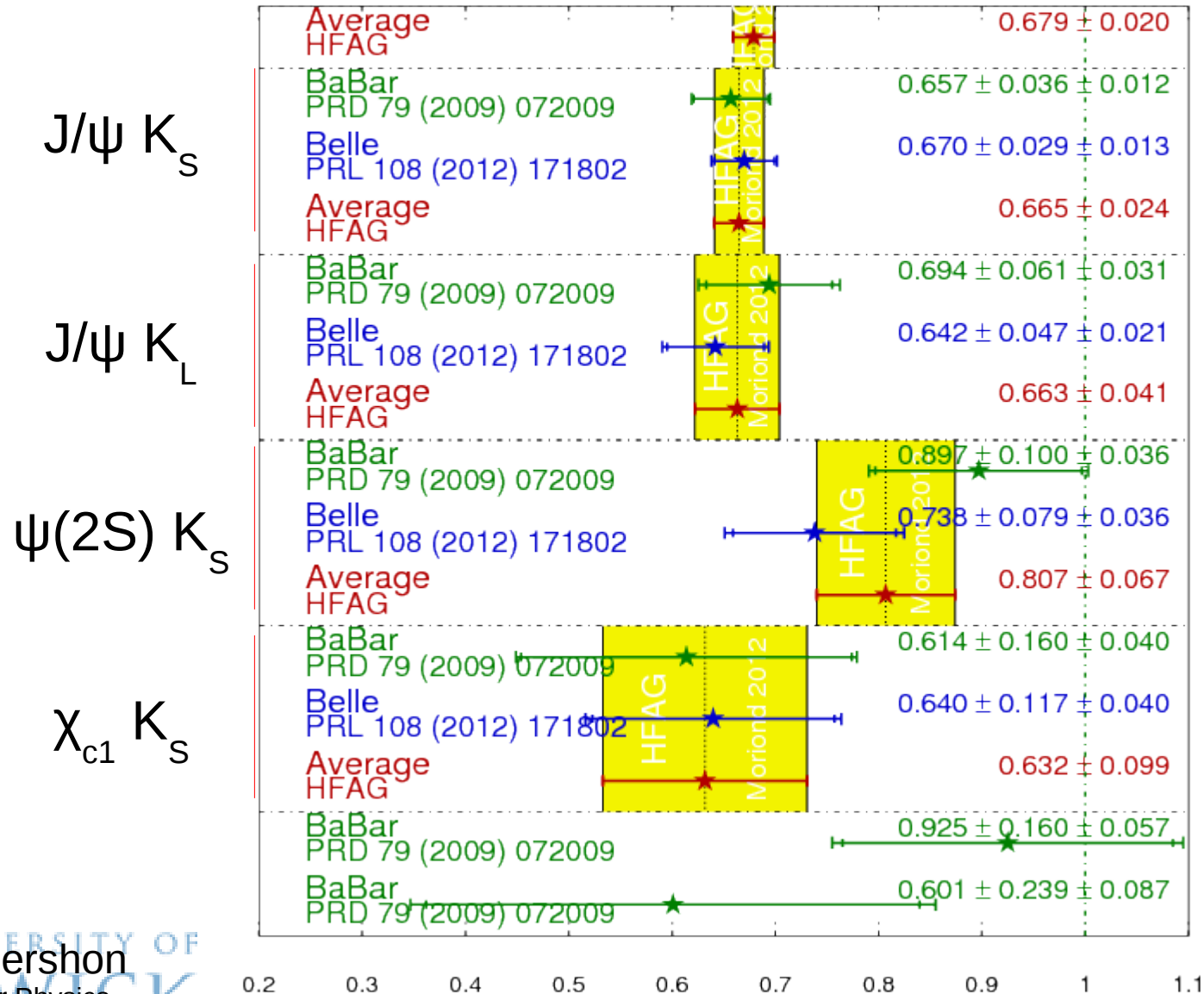
Note LHCb also highly competitive



Compilation of B factory results

$$\sin(2\beta) \equiv \sin(2\phi_1)$$

HFAG
Moriond 2012
PRELIMINARY

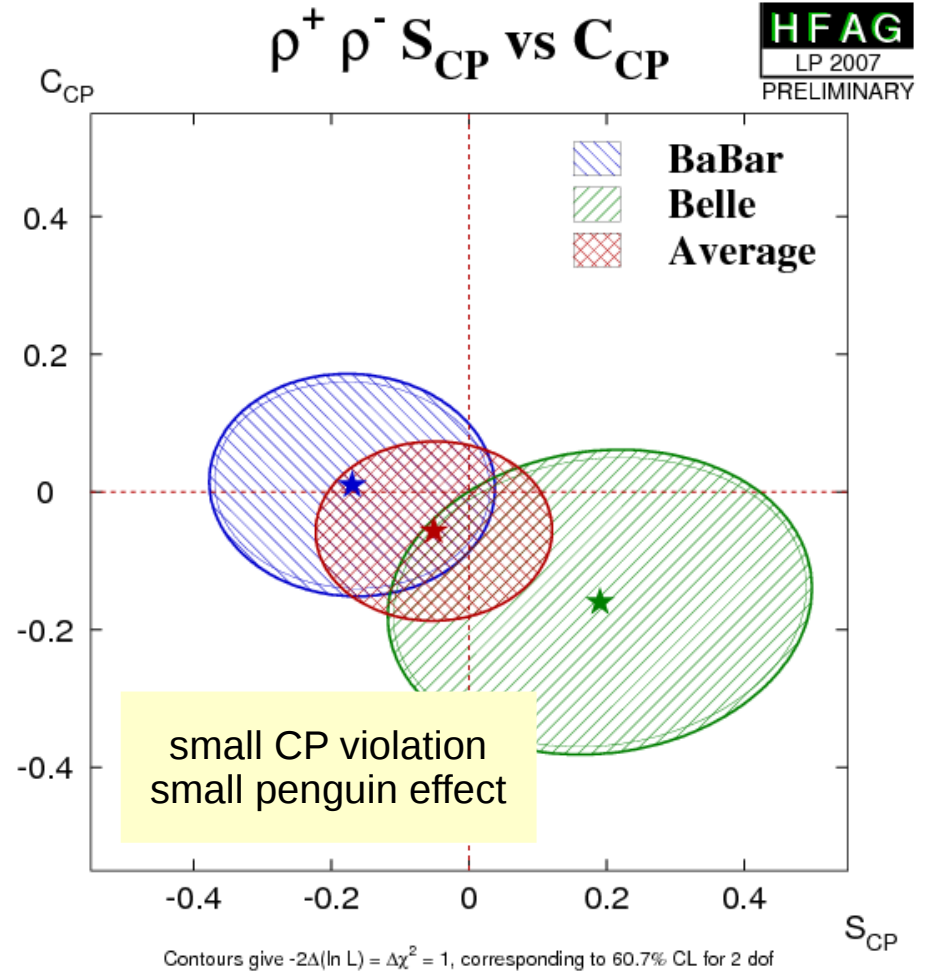
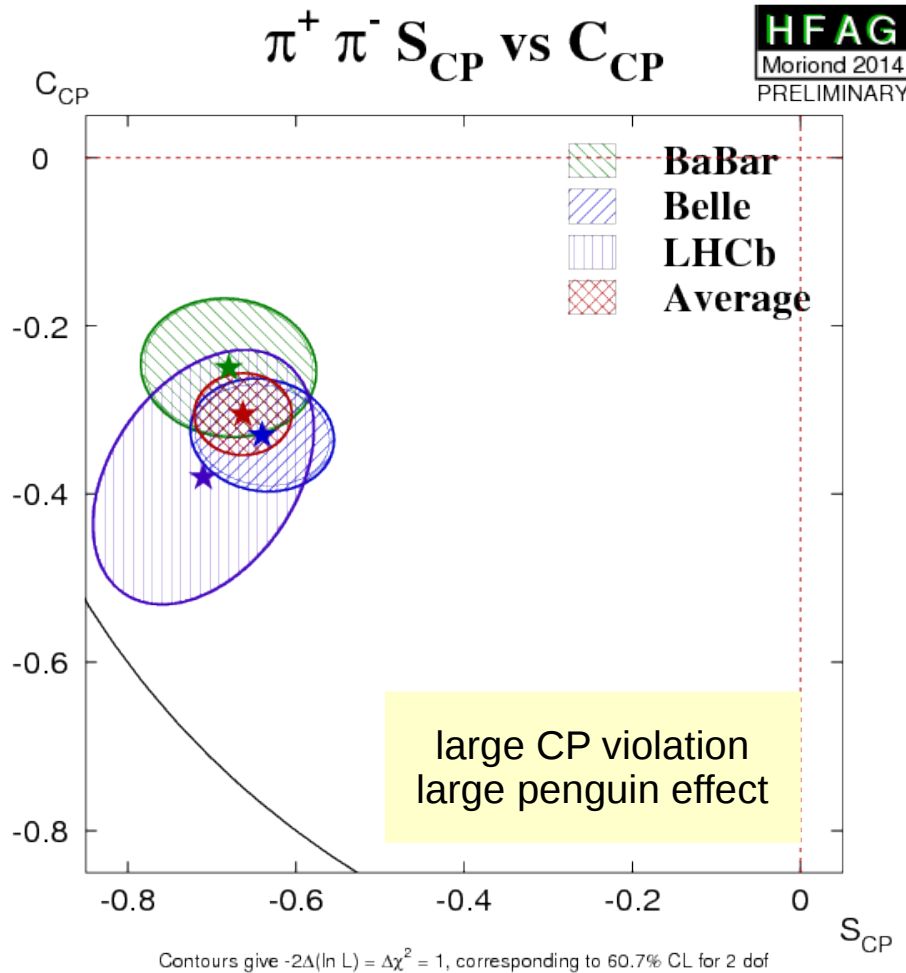


Measurement of α

- Similar analysis using $b \rightarrow u\bar{u}d$ decays (e.g. $B_d^0 \rightarrow \pi^+\pi^-$) probes $\pi-(\beta+\gamma) = \alpha$
 - but $b \rightarrow du\bar{u}$ penguin transitions contribute to same final states \Rightarrow “penguin pollution”
 - $C \neq 0 \Leftrightarrow$ CP violation in decay can occur
 - $S \neq +\eta_{CP} \sin(2\alpha)$
- Two approaches (optimal approach combines both)
 - try to use modes with small penguin contribution
 - correct for penguin effect (isospin analysis)

PRL 65 (1990) 3381

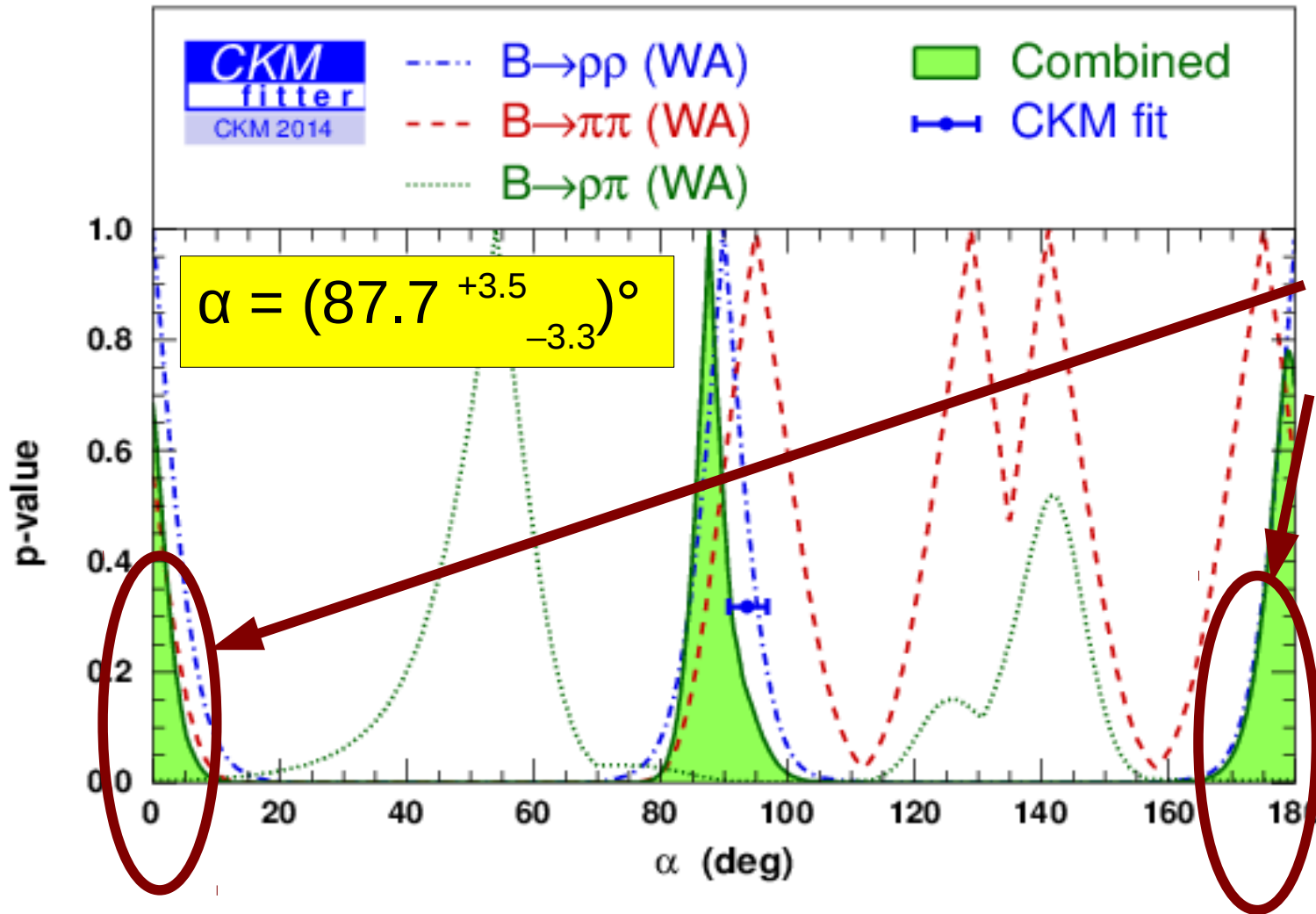
Experimental Situation



improved measurements needed!

Measurement of α

THESE SOLUTIONS RULED OUT BY OBSERVATION OF DIRECT CP VIOLATION IN $B^0 \rightarrow \pi^+ \pi^-$

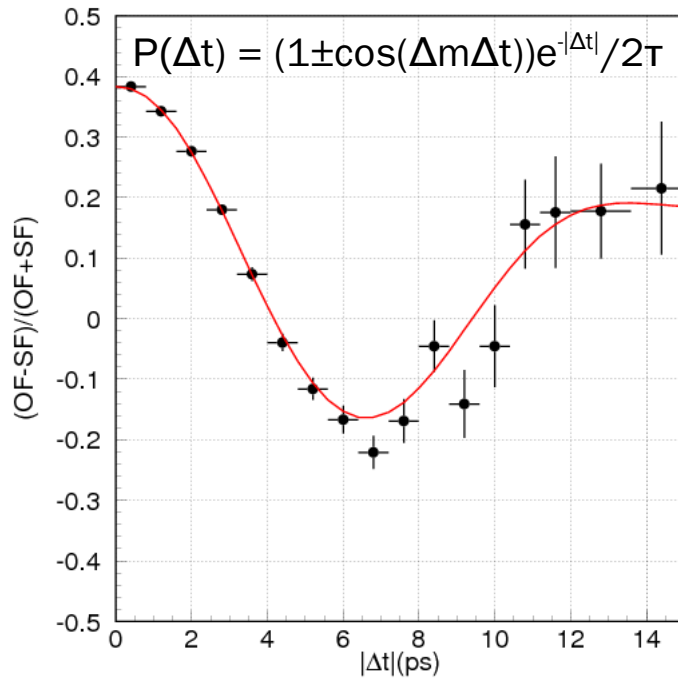


Is there any physical significance in the fact that $\alpha \approx 90^\circ$?

R_t side from B^0-B^0 mixing

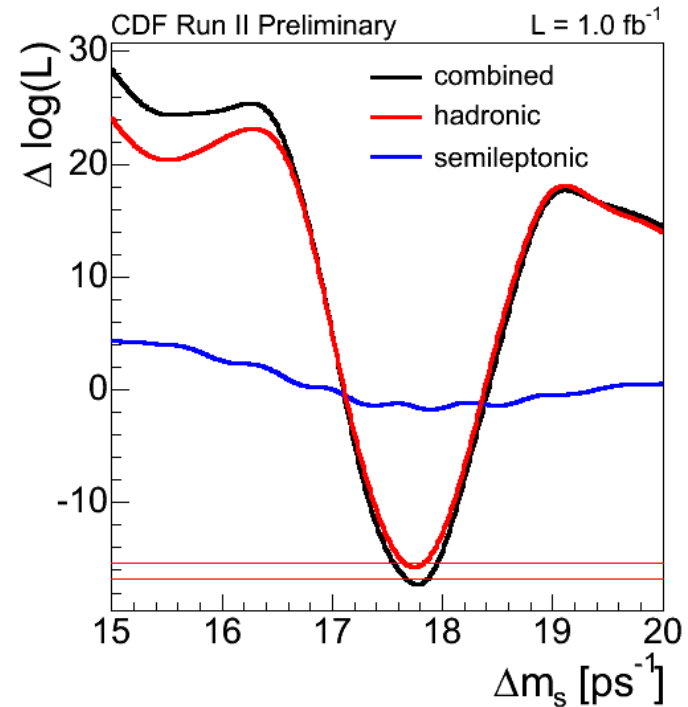
World average based on many measurements

$$R_t = \left| \frac{V_{td} V_{tb}^*}{V_{cd} V_{cb}^*} \right| \quad \& \quad \frac{\Delta m_d}{\Delta m_s} = \frac{m_{B_d} f_{B_d}^2 \hat{B}_{B_d} |V_{td}|^2}{m_{B_s} f_{B_s}^2 \hat{B}_{B_s} |V_{ts}|^2}$$



$$\Delta m_d = (0.511 \pm 0.005 \pm 0.006) \text{ ps}^{-1}$$

PRD 71, 072003 (2005)



$$\Delta m_s = (17.77 \pm 0.10 \pm 0.07) \text{ ps}^{-1}$$

PRL 97, 242003 (2006)

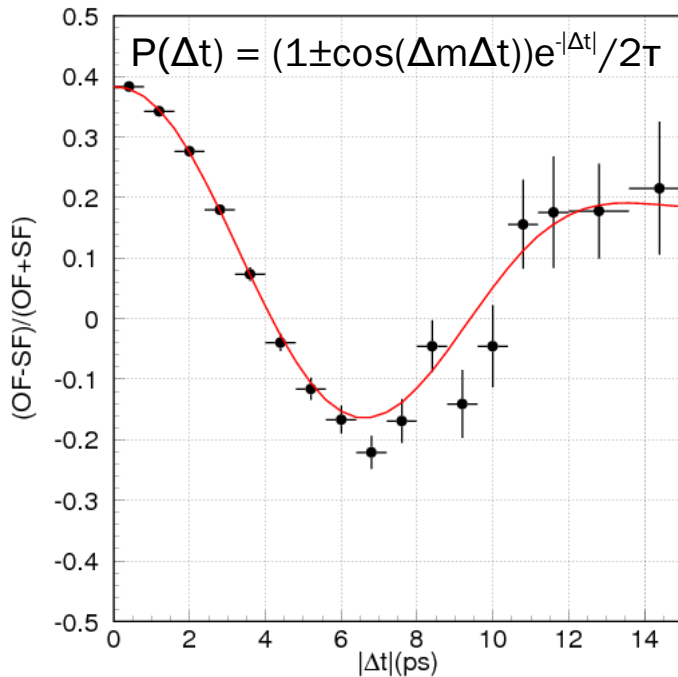
$$\left| V_{td}/V_{ts} \right| = 0.216 \pm 0.001 \pm 0.011$$

↑ experimental uncertainty ↑ theoretical uncertainty

R_t side from B^0-B^0 mixing

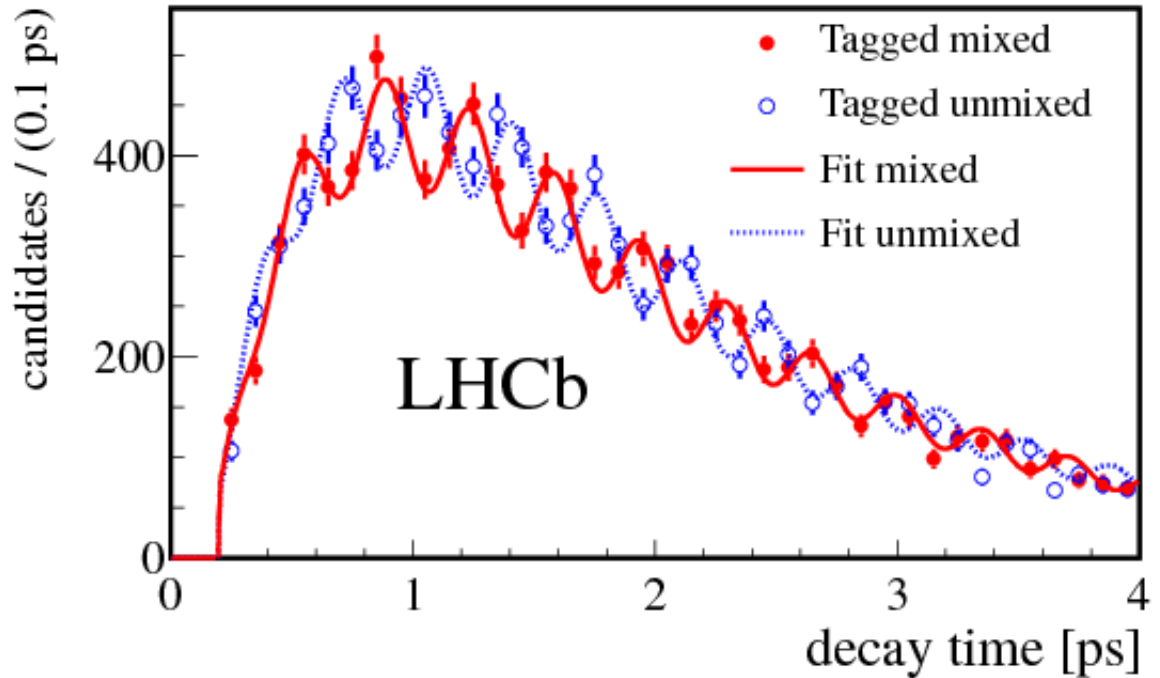
$$R_t = \left| \frac{V_{td} V_{tb}^*}{V_{cd} V_{cb}^*} \right| \quad \& \quad \frac{\Delta m_d}{\Delta m_s} = \frac{m_{B_d} f_{B_d}^2 \hat{B}_{B_d} |V_{td}|^2}{m_{B_s} f_{B_s}^2 \hat{B}_{B_s} |V_{ts}|^2}$$

World average based on many measurements



$$\Delta m_d = (0.511 \pm 0.005 \pm 0.006) \text{ ps}^{-1}$$

PRD 71, 072003 (2005)



$$\Delta m_s = (17.768 \pm 0.023 \pm 0.006) \text{ ps}^{-1}$$

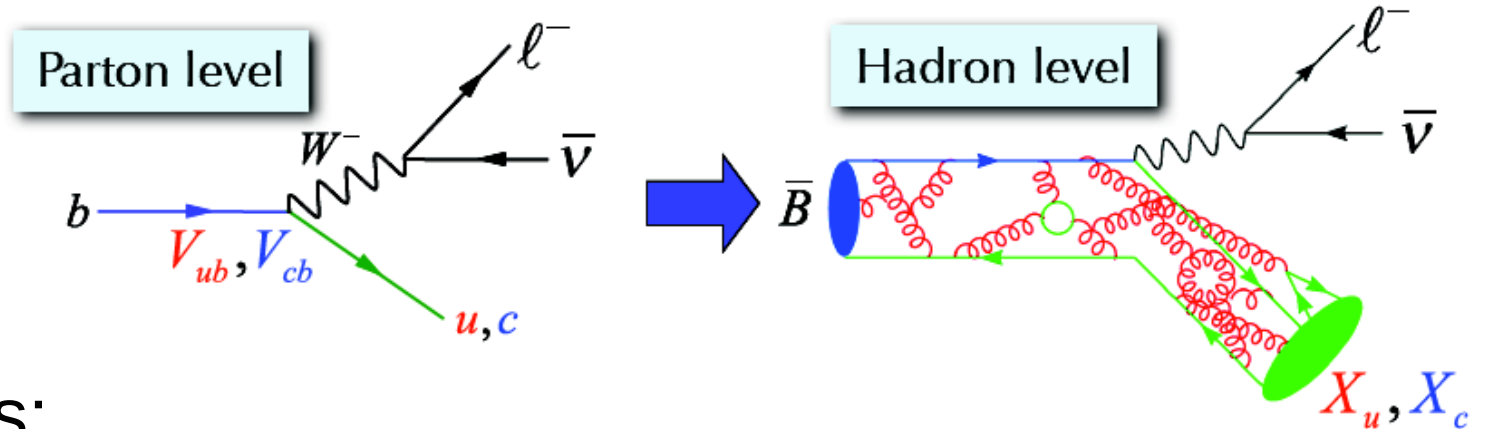
NJP 15 (2013) 053021

$$\left| V_{td} / V_{ts} \right| = 0.216 \pm 0.001 \pm 0.011$$

↑ experimental uncertainty ↑ theoretical uncertainty

R_u side from semileptonic decays

$$R_u = \left| \frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*} \right|$$



- Approaches:

- exclusive semileptonic B decays, eg. $B^0 \rightarrow \pi^- e^+ \nu$

- require knowledge of form factors

- can be calculated in lattice QCD at kinematical limit

- inclusive semileptonic B decays, eg. $B \rightarrow X_u e^+ \nu$

- clean theory, based on Operator Product Expansion

- experimentally challenging:

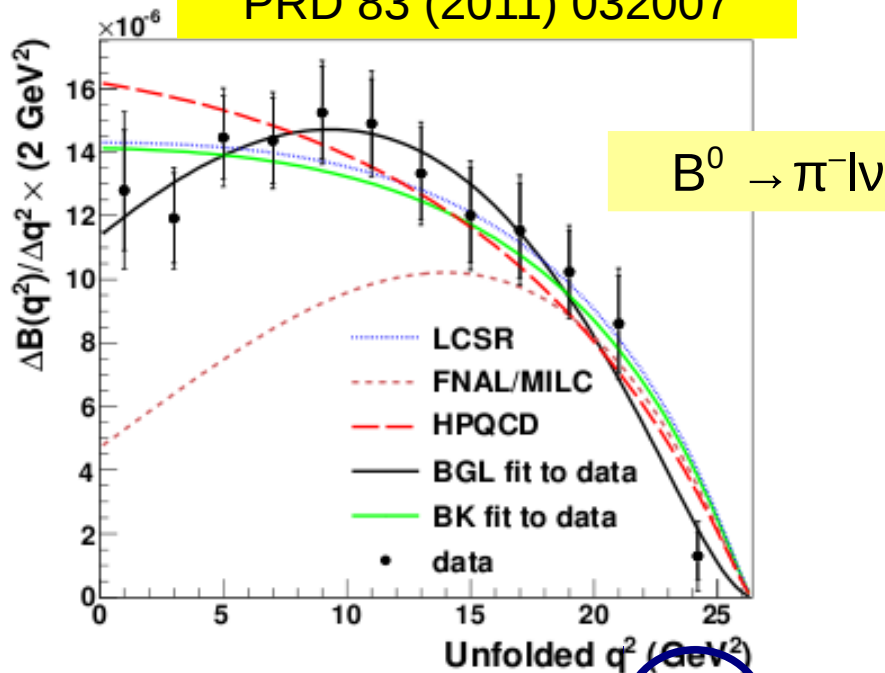
- need to reject $b \rightarrow c$ background

- cuts re-introduce theoretical uncertainties

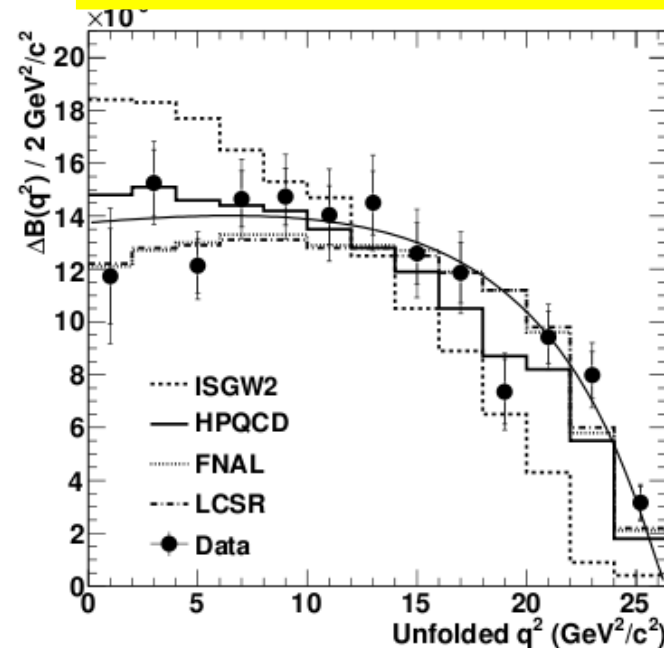
$|V_{ub}|$ from exclusive semileptonic decays

Current best measurements use $B^0 \rightarrow \pi^- l^+ \nu$
 (recent competitive measurement from LHCb with $\Lambda_b \rightarrow p \mu \nu$)

BaBar experiment
 PRD 83 (2011) 052011
 PRD 83 (2011) 032007



Belle experiment
 PRD 83 (2011) 071101(R)

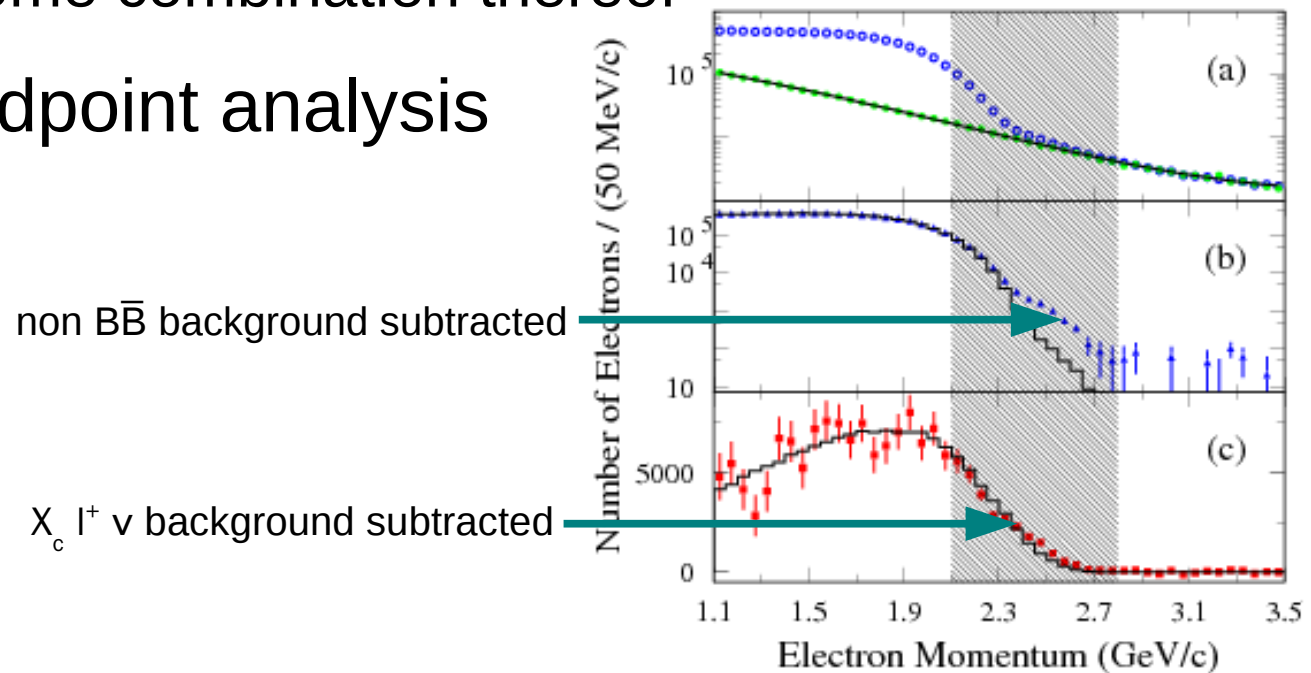


$$|V_{ub}| = (3.09 \pm 0.08 \pm 0.12^{+0.35}_{-0.29}) \times 10^{-3}$$

$$|V_{ub}| = (3.43 \pm 0.33) \times 10^{-3}$$

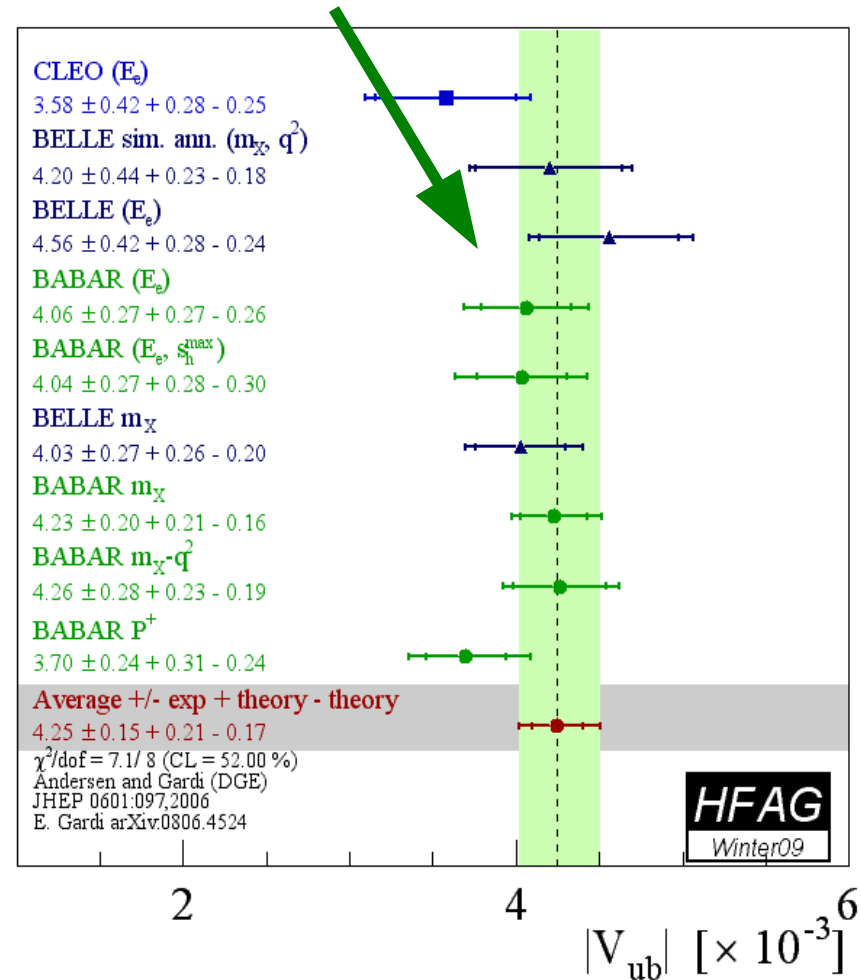
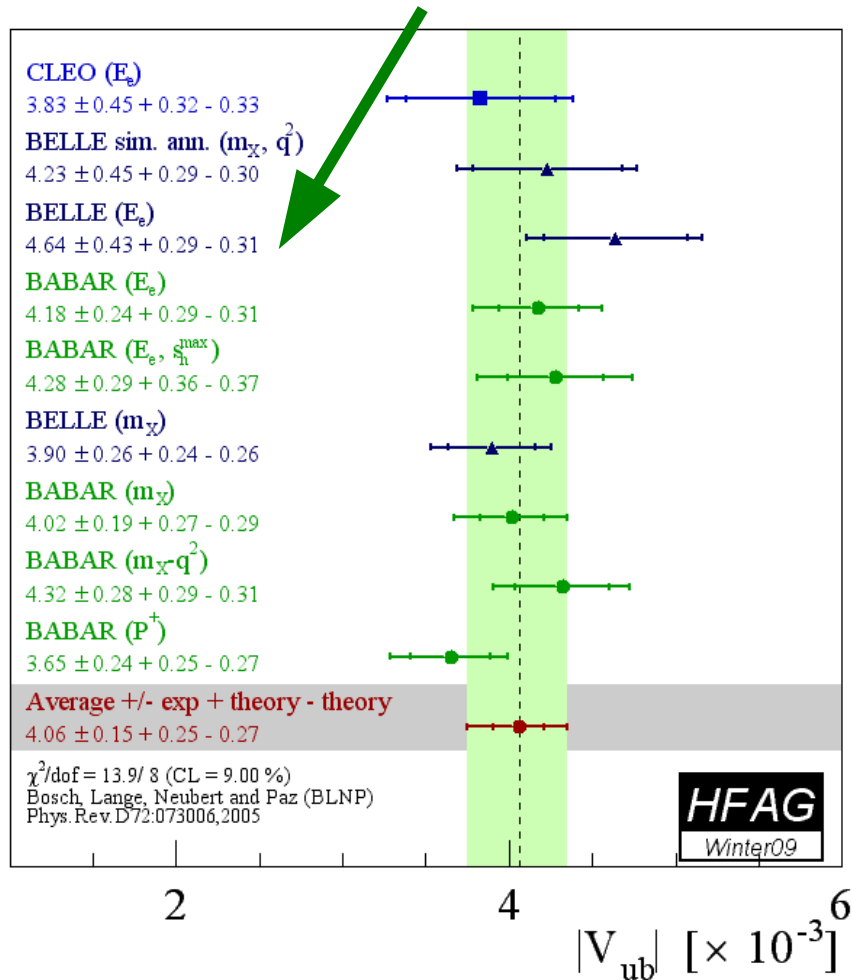
$|V_{ub}|$ from inclusive semileptonic decays

- Main difficulty to measure inclusive $B \rightarrow X_u l^+ \nu$
 - background from $B \rightarrow X_c l^+ \nu$
- Approaches
 - cut on E_l (lepton endpoint), q^2 ($l\nu$ invariant mass squared), $M(X_u)$, or some combination thereof
- Example: endpoint analysis



$|V_{ub}|$ inclusive - compilation

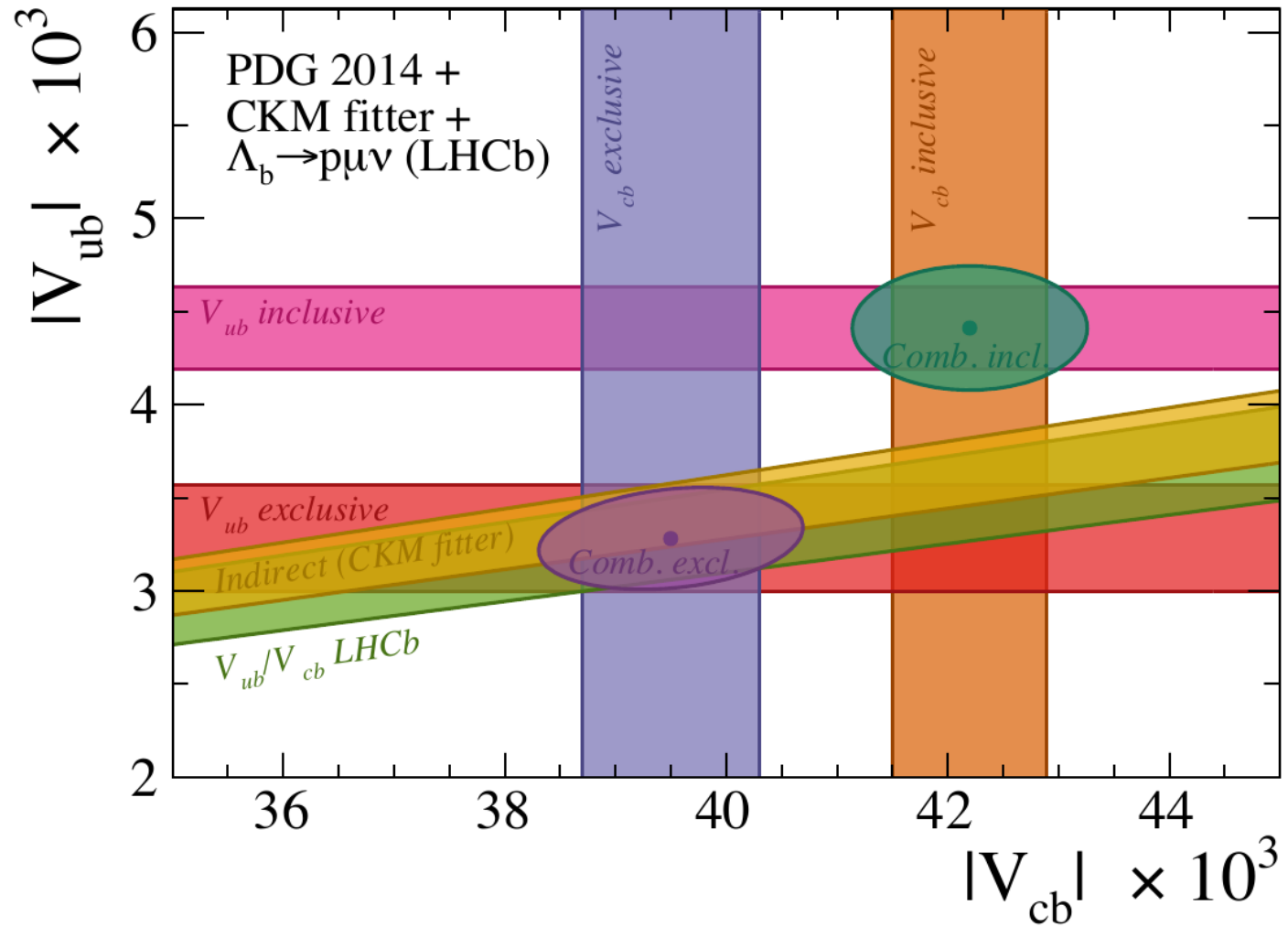
Different theoretical approaches (2 of 4 used by HFAG)



$|V_{ub}|$ average

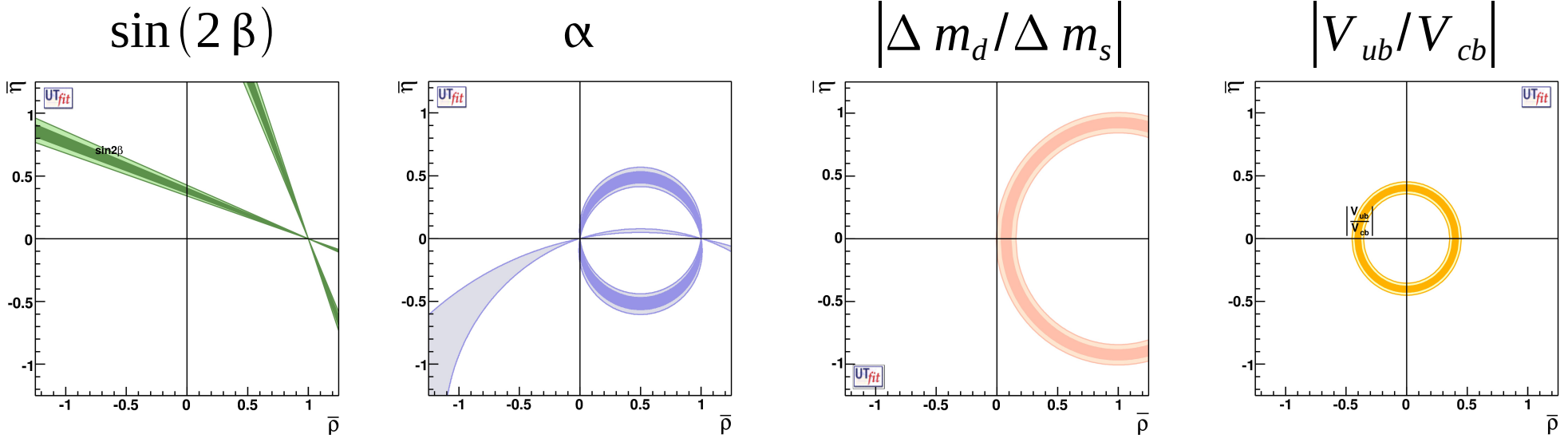
- Averages on $|V_{ub}|$ from both exclusive and inclusive approaches
 - exclusive: $|V_{ub}| = (3.28 \pm 0.29) \times 10^{-3}$
 - inclusive: $|V_{ub}| = (4.41 \pm 0.15^{+0.15}_{-0.19}) \times 10^{-3}$
 - slight tension between these results
 - in both cases theoretical errors are dominant
 - but some “theory” errors can be improved with more data
 - PDG2014 does naïve average rescaling due to inconsistency to obtain $|V_{ub}| = (4.13 \pm 0.49) \times 10^{-3}$

Inclusive vs. exclusive



Discrepancies need to be understood!

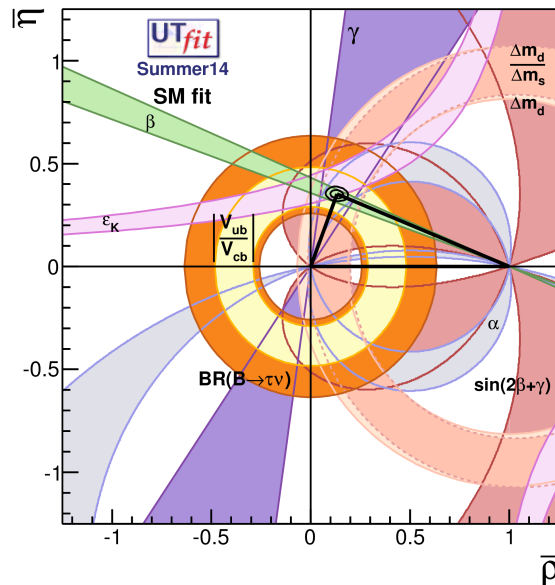
Partial summary



Adding a few other constraints we find

$$\bar{\rho} = 0.132 \pm 0.023$$

$$\bar{\eta} = 0.351 \pm 0.013$$



Consistent with Standard Model fit

- some “tensions”

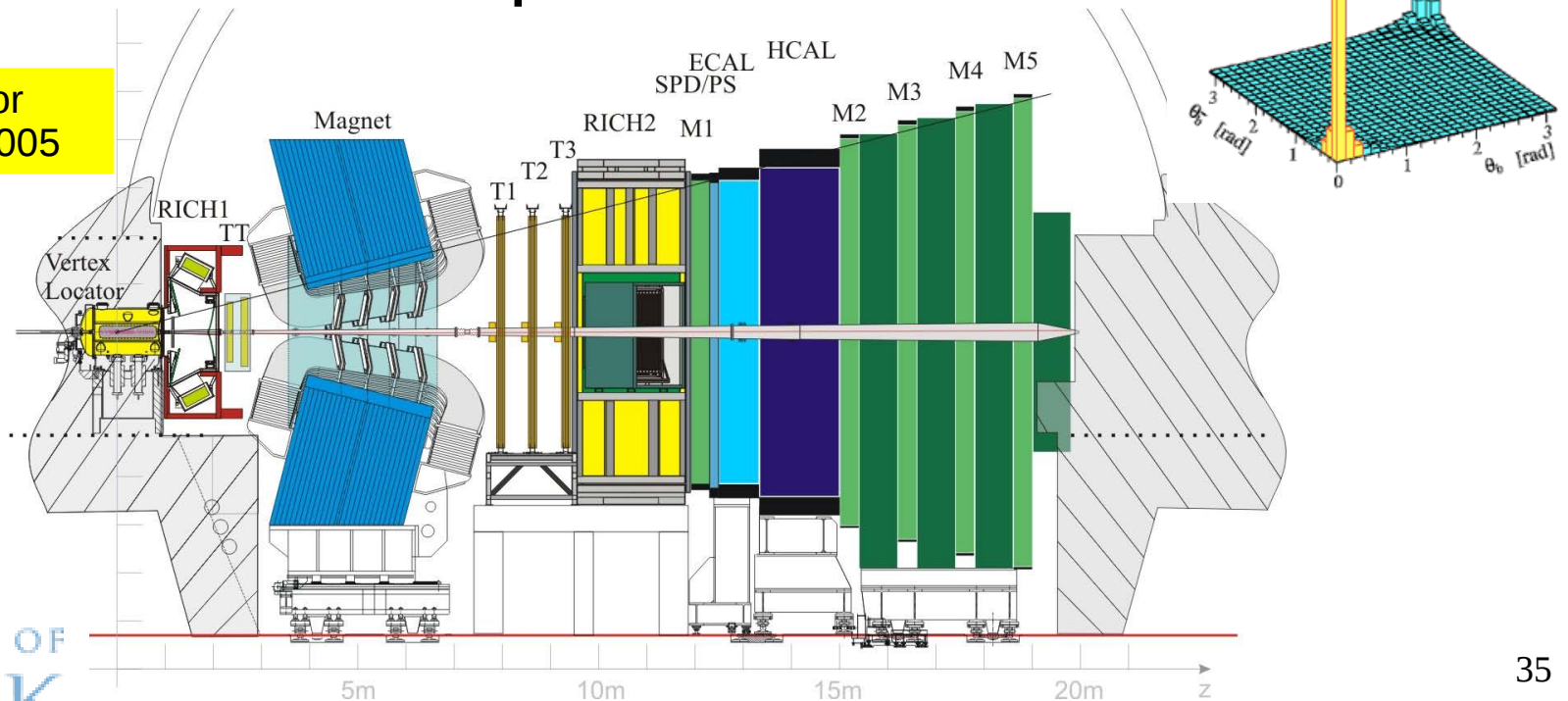
Still plenty of room for new physics

Flavour physics at hadron colliders

	$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$ PEP-II, KEKB	$p\bar{p} \rightarrow b\bar{b}X$ ($\sqrt{s} = 2 \text{ TeV}$) Tevatron	$pp \rightarrow b\bar{b}X$ ($\sqrt{s} = 14 \text{ TeV}$) LHC
Production cross-section	1 nb	$\sim 100 \mu\text{b}$	$\sim 500 \mu\text{b}$
Typical $b\bar{b}$ rate	10 Hz	$\sim 100 \text{ kHz}$	$\sim 500 \text{ kHz}$
Pile-up	0	1.7	0.5–20
b hadron mixture	B^+B^- (50%), $B^0\bar{B}^0$ (50%)	B^+ (40%), B^0 (40%), B_s^0 (10%), Λ_b^0 (10%), others (< 1%)	
b hadron boost	small ($\beta\gamma \sim 0.5$)	large ($\beta\gamma \sim 100$)	
Underlying event	$B\bar{B}$ pair alone	Many additional particles	
Production vertex	Not reconstructed	Reconstructed from many tracks	
$B^0-\bar{B}^0$ pair production	Coherent (from $\Upsilon(4S)$ decay)	Incoherent	
Flavour tagging power	$\epsilon D^2 \sim 30\%$	$\epsilon D^2 \sim 5\%$	

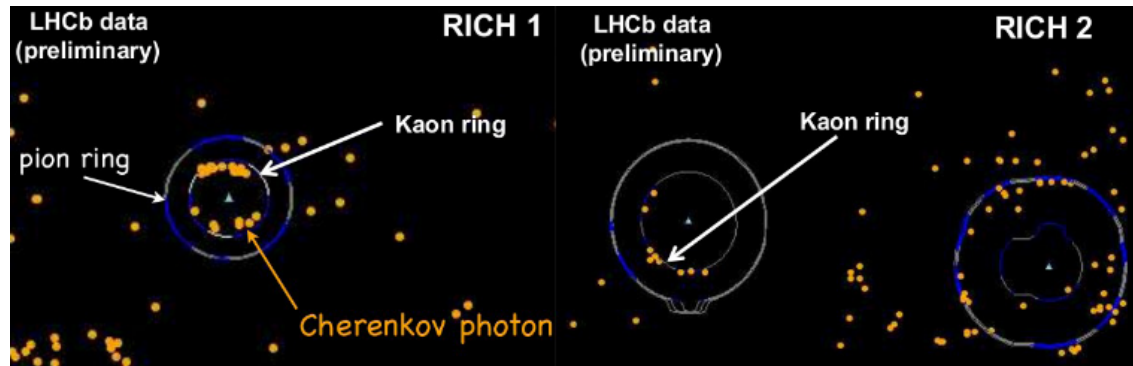
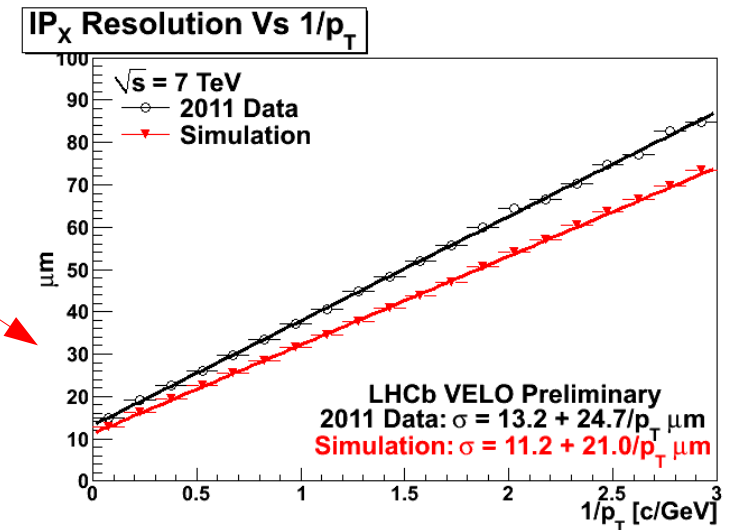
Geometry

- In high energy collisions, $b\bar{b}$ pairs produced predominantly in forward or backward directions
- LHCb is a forward spectrometer

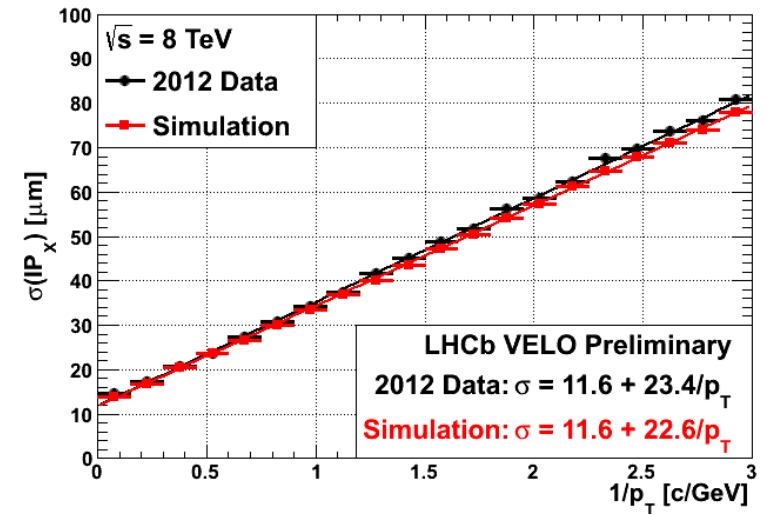
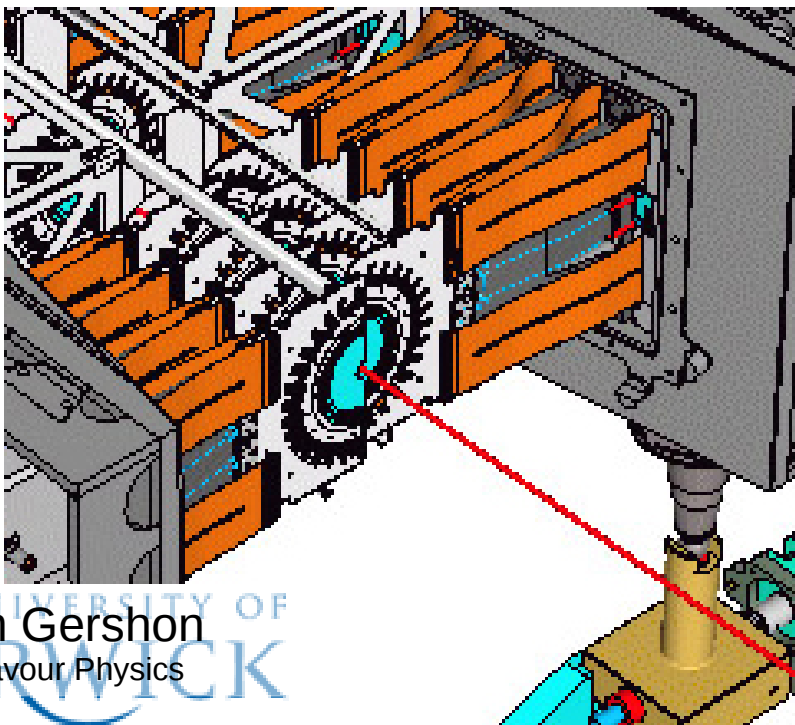


LHCb detector features

- Tracking and calorimetry
 - basic essentials of any collider experiment!
 - muon chambers
- VELO
 - reconstruct displaced vertices
- RICH
 - particle ID (K/ π separation)
- Trigger
 - fast and efficient

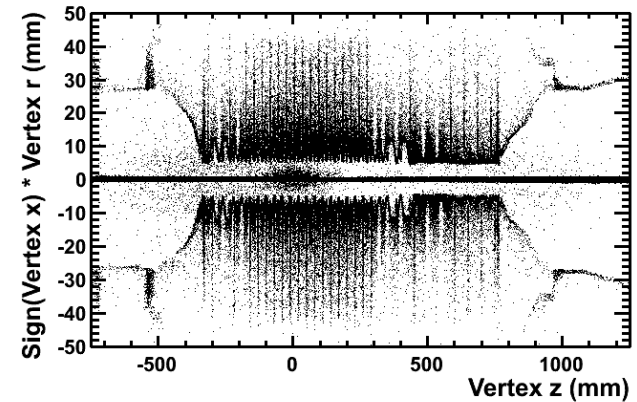


VELO

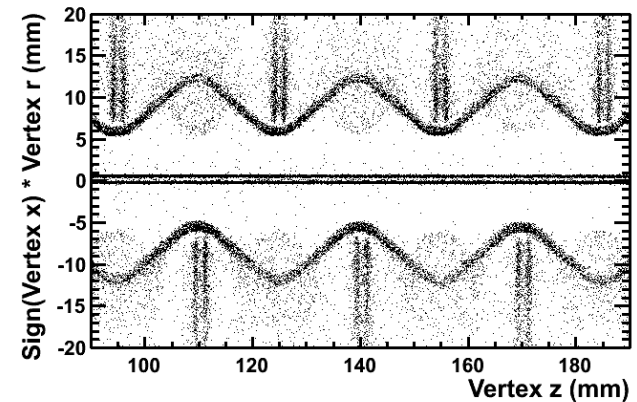


Material imaged used beam gas collisions

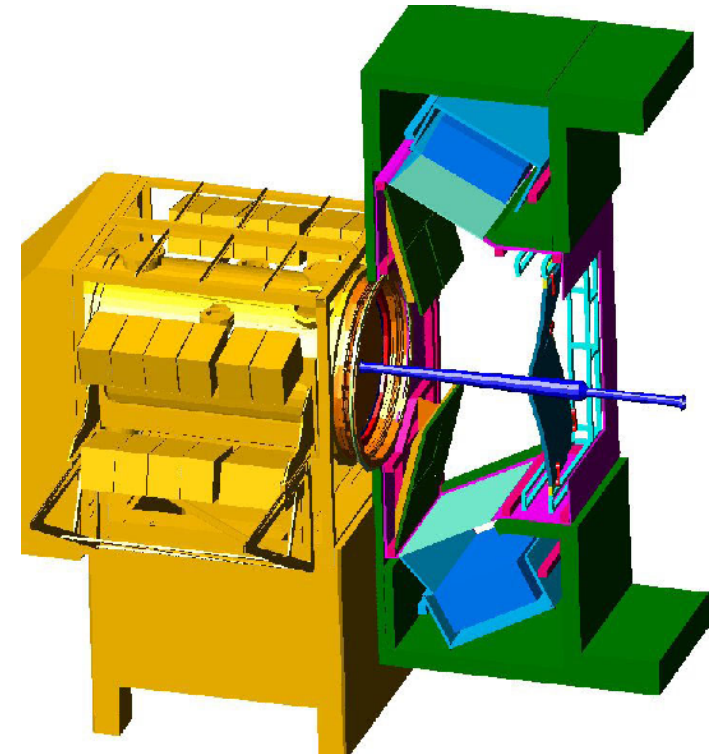
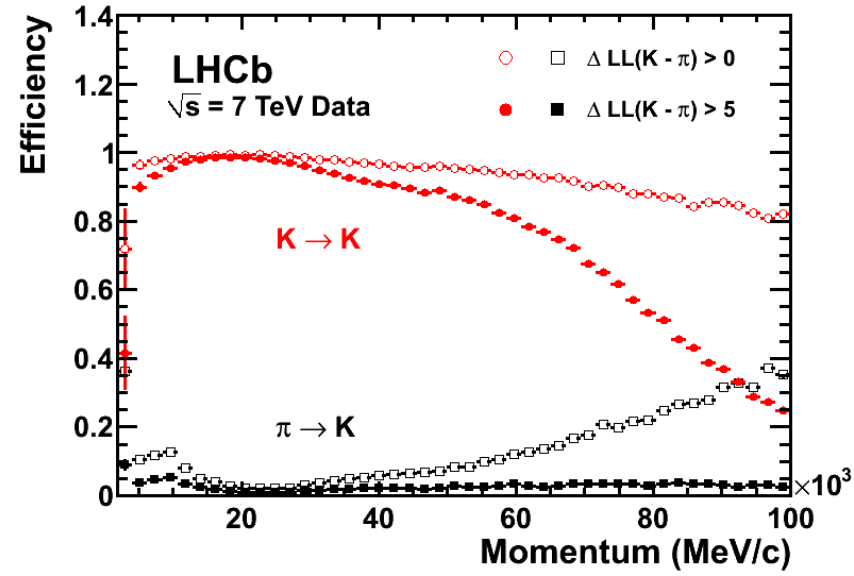
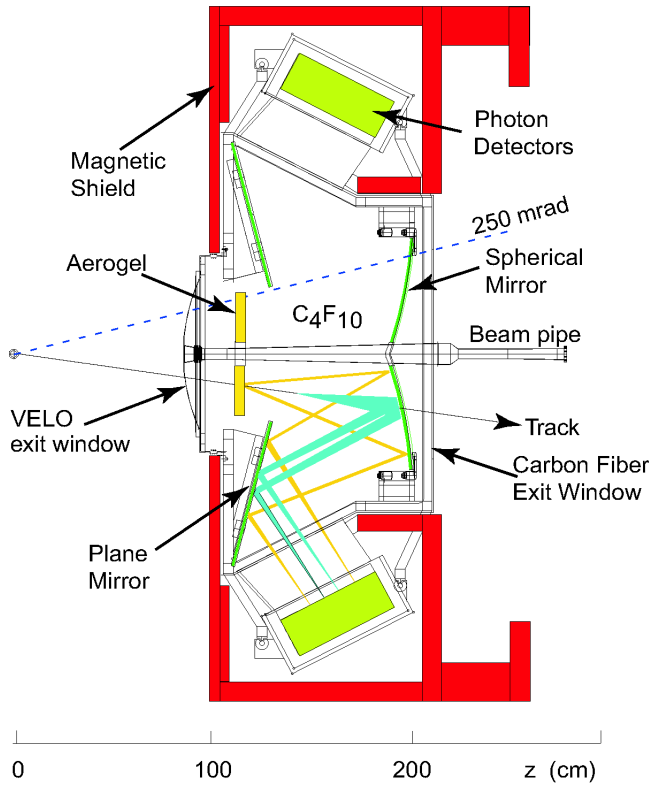
LHCb VELO Preliminary



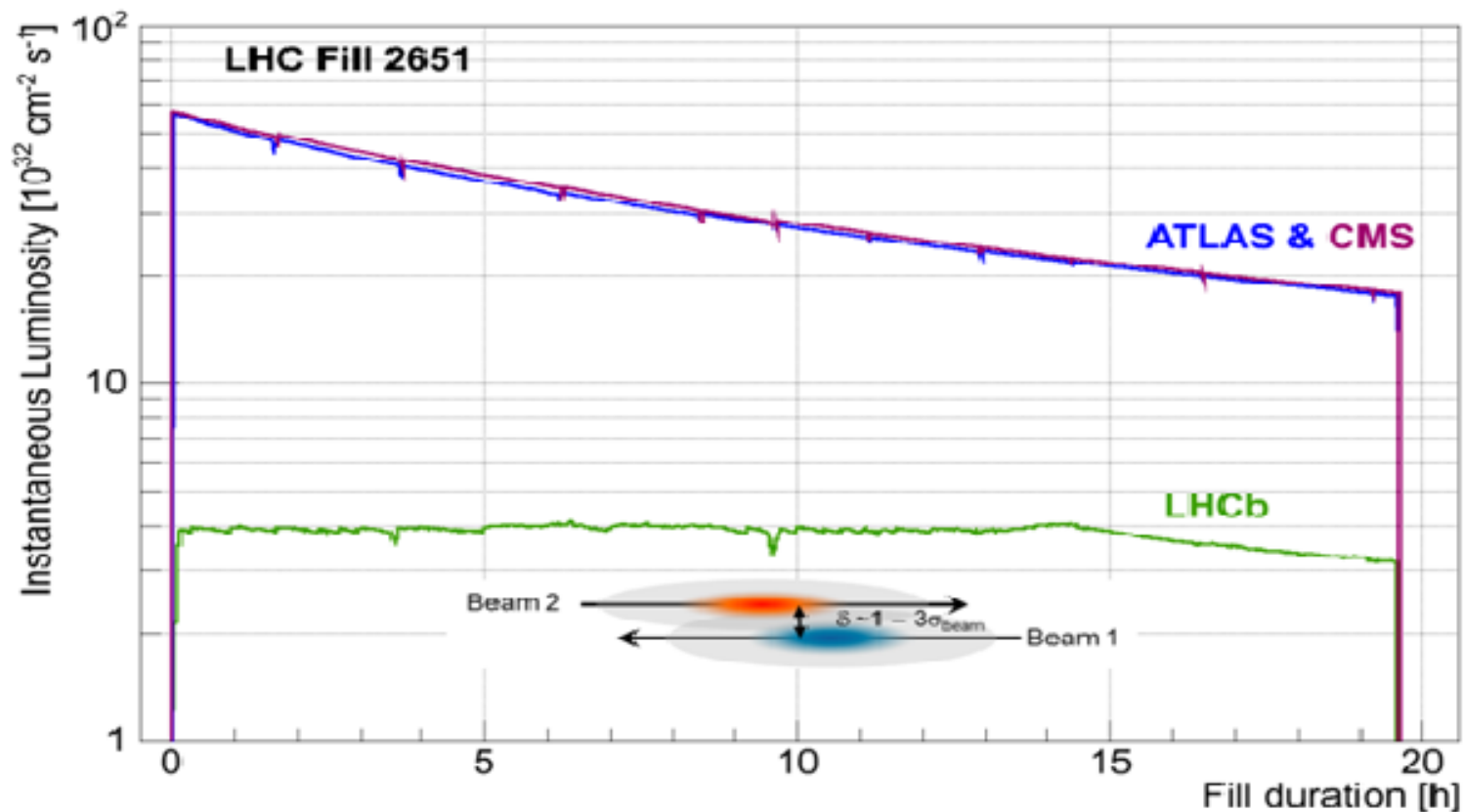
LHCb VELO Preliminary



RICH



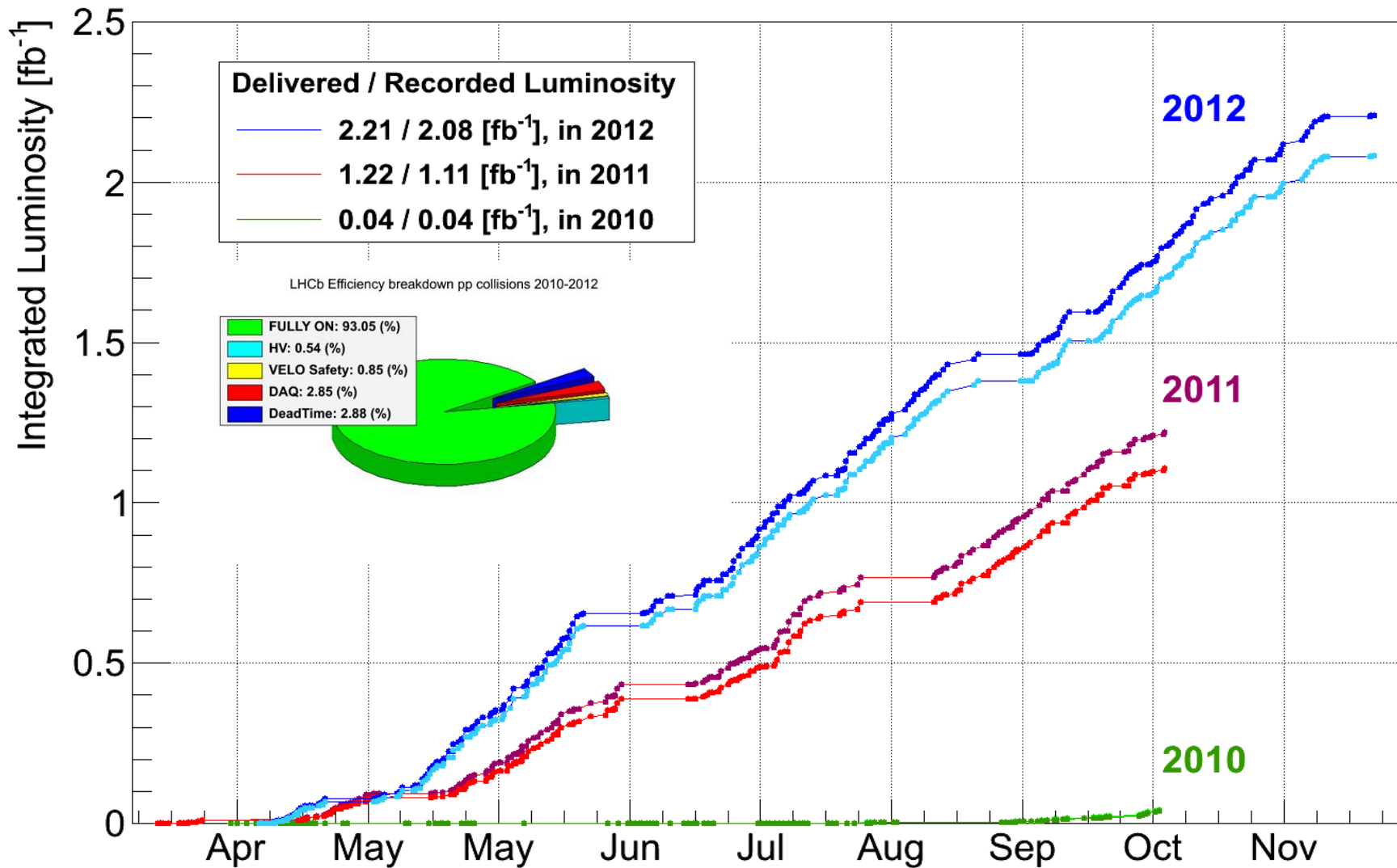
Luminosity levelling in LHCb



luminosity levelling at around $4 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$ via transverse separation (with tilted crossing angle)

from C. Gaspar, via. F. Zimmerman

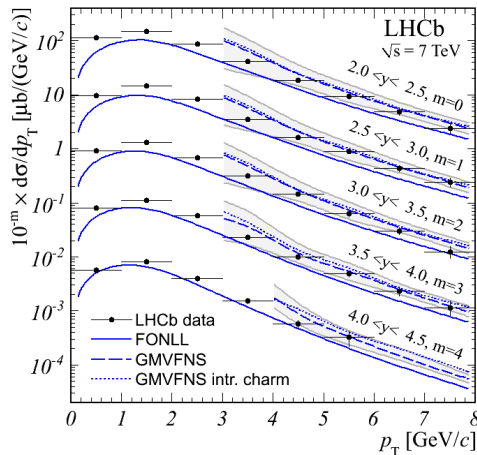
Run 1 data taking



Heavy flavour production @ LHCb

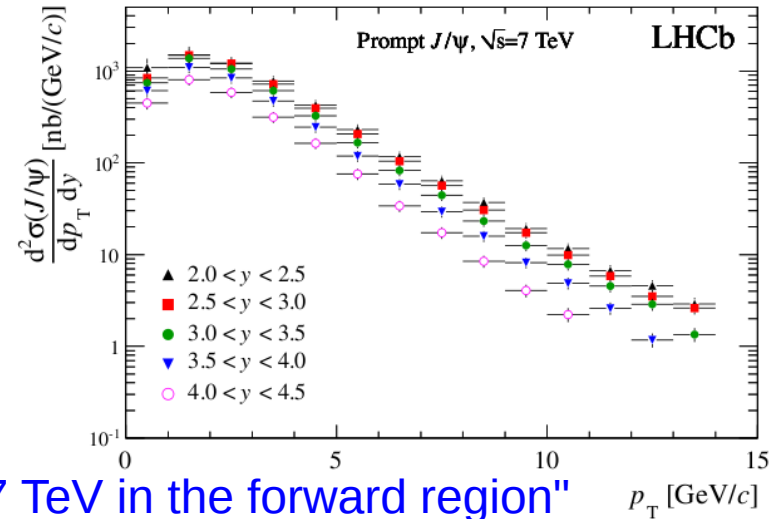
“Prompt charm production in pp collisions at $\sqrt{s} = 7$ TeV”

Nucl. Phys. B 871 (2013) 1



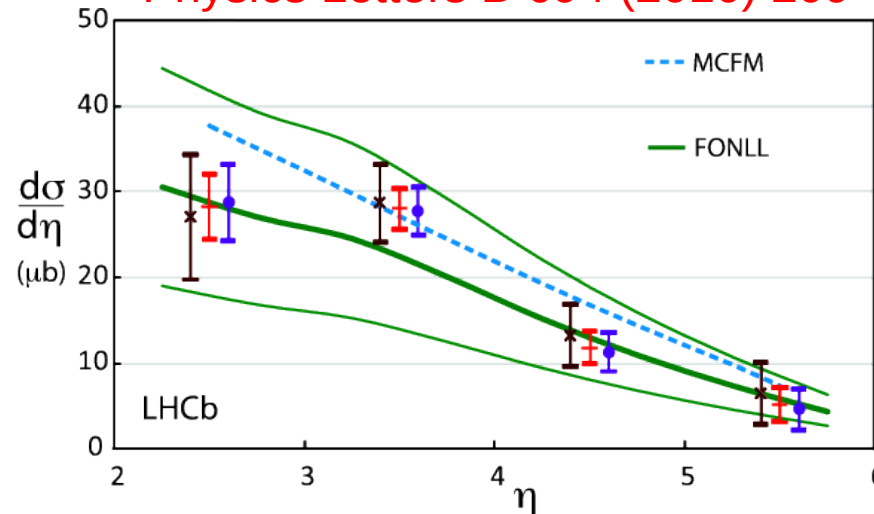
“Measurement of J/ψ production in pp collisions at $\sqrt{s} = 7$ TeV”

Eur. Phys. J. C 71 (2011) 1645



“Measurement of $\sigma(pp \rightarrow b\bar{b}X)$ at $\sqrt{s} = 7$ TeV in the forward region”

Physics Letters B 694 (2010) 209



What does $\int L dt = 1/\text{fb}$ mean?

- Measured cross-section, in LHCb acceptance

$$\sigma(pp \rightarrow b\bar{b}X) = (75.3 \pm 5.4 \pm 13.0) \mu\text{b}$$

PLB 694 (2010) 209

- So, number of $b\bar{b}$ pairs produced

$$10^{15} \times 75.3 \times 10^{-6} \sim 10^{11}$$

- Compare to combined data sample of e^+e^- “B factories” BaBar and Belle of $\sim 10^9$ $B\bar{B}$ pairs

for any channel where the (trigger, reconstruction, stripping, offline) efficiency is not too small, LHCb has world's largest data sample

- p.s.: for charm, $\sigma(pp \rightarrow c\bar{c}X) = (6.10 \pm 0.93) \text{mb}$

LHCb-CONF-2010-013

The all important trigger

JINST 8 (2013) P04022

Challenge is

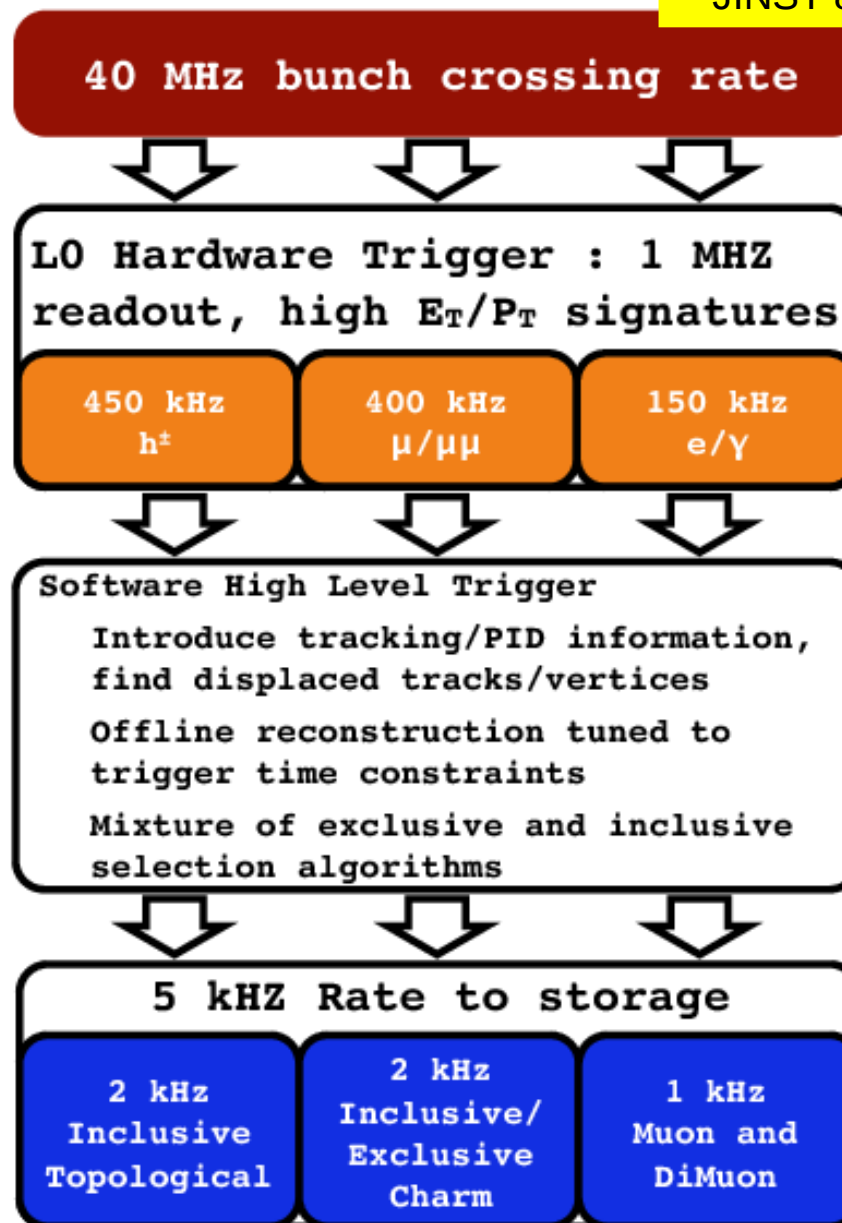
- to efficiently select most interesting B decays
- while maintaining manageable data rates

Main backgrounds

- “minimum bias” inelastic pp scattering
- other charm and beauty decays

Handles

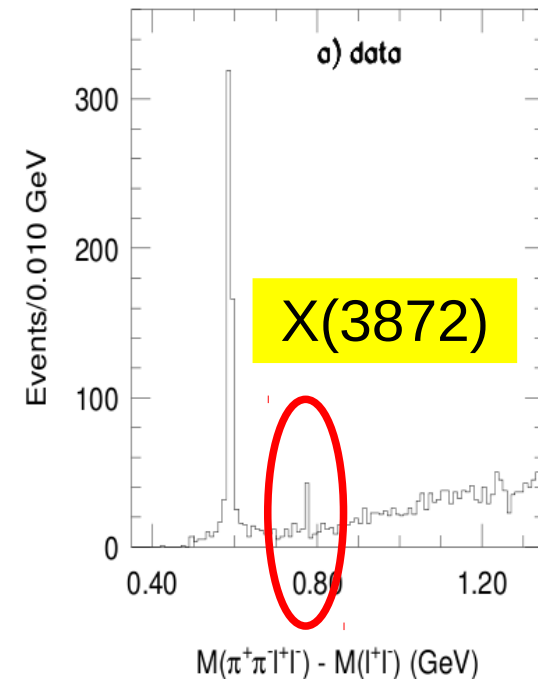
- high p_T signals (muons)
- displaced vertices



Spectroscopy

- I've talked about the headline items of flavour physics
 - CP violation, searches for new physics
 - what we tell the funding agencies, and the press
- But, much of the physics performed by flavour experiments is the study of properties of hadronic states
 - lifetimes, masses, decay channels, quantum numbers
 - and the discoveries of new ones

PRL 91 (2003) 262001
Most highly cited paper (>1000 citations)
from BaBar or Belle



Discovery of the lightest $b\bar{b}$ state – 2008

Observation of the Bottomonium Ground State in the Decay $\Upsilon(3S) \rightarrow \gamma \eta_b$

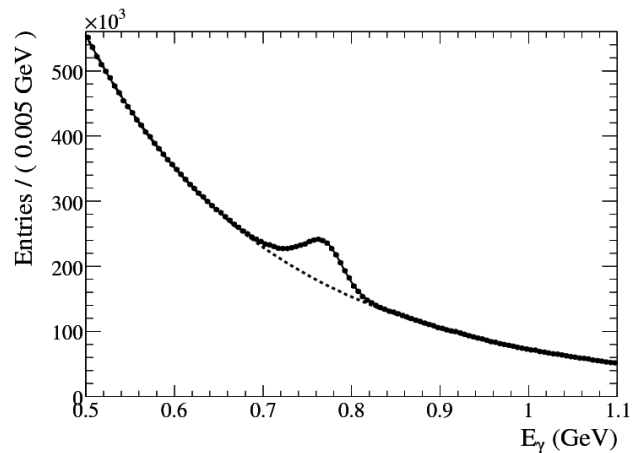
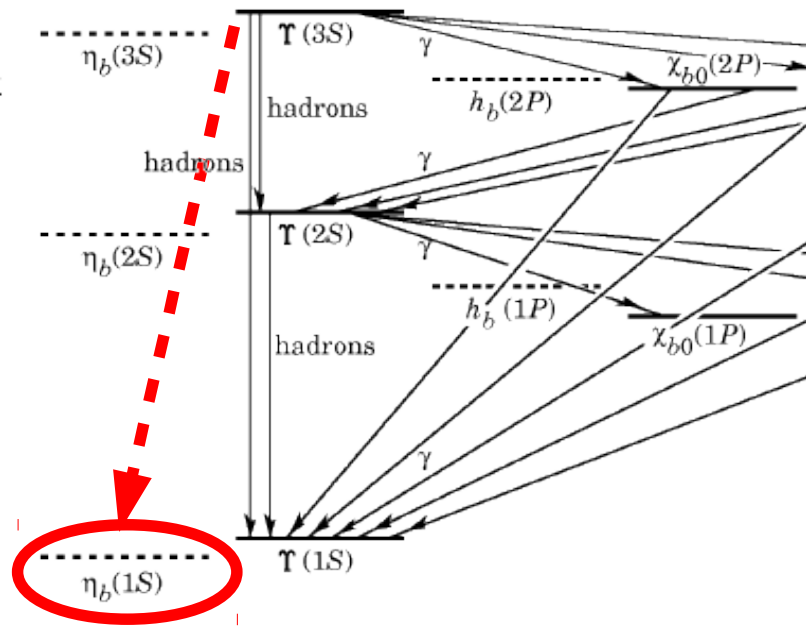
B. Aubert,¹ M. Bona,¹ Y. I. Karasik,¹ J. R. Loy,¹ V. Pojma,¹ E. Preprint,¹ X. Rong,¹ V. Tisserand,¹ J. Garra Tico,² F. Graess,² L. Lopez,³ A. P. ...
The BaBar Collaboration Abrams,⁵ M. Rattalio,⁵

- Only recoil γ is reconstructed

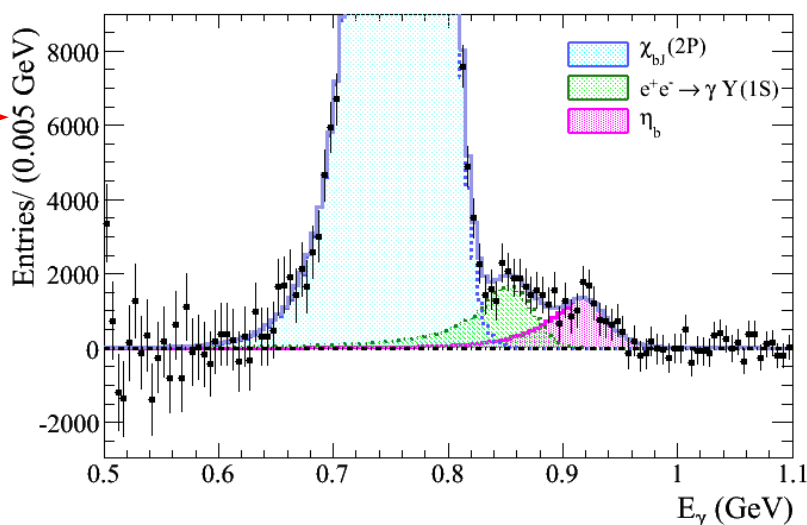
$$m(\eta_b(1S)) = (9388.9^{+3.1}_{-2.3} \pm 2.7) \text{ MeV}/c^2$$

$$m(\Upsilon(1S)) - m(\eta_b(1S)) = (71.4^{+2.3}_{-3.1} \pm 2.7) \text{ MeV}/c^2$$

$$B(\Upsilon(3S) \rightarrow \gamma \eta_b(1S)) = (4.8 \pm 0.5 \pm 1.2) \times 10^{-4}$$



→ subtract smoothly varying background



Why wasn't the η_b discovered at a hadronic experiment?

- Remember: $Y(1S)$ discovered at FNAL in 1977

- fixed target experiment: p on Be

PRL 39 (1977) 252

- η_b is lighter
- Hadron collisions produce all types of b hadrons
- So why couldn't the η_b be discovered, e.g., at the Tevatron?

Why wasn't the η_b discovered at a hadronic experiment?

- Remember: $Y(1S)$ discovered at FNAL in 1977
 - fixed target experiment: p on Be
- η_b is lighter
- Hadron collisions produce all types of b hadrons
- So why couldn't the η_b be discovered, e.g., at the Tevatron?
- **It's all about the trigger!**
 - need clean signature for trigger and reconstruction
 - CDF search used $\eta_b \rightarrow J/\psi J/\psi$ decay, with predicted BF $\sim 0!$

PRL 39 (1977) 252

Digression on a digression: The “Oops Leon”

Observation of High-Mass Dilepton Pairs in Hadron Collisions at 400 GeV

D. C. Hom, L. M. Lederman, H. P. Paar, H. D. Snyder, J. M. Weiss, and J. K. Yoh
Columbia University, New York, New York 10027*

and

J. A. Appel, B. C. Brown, C. N. Brown, W. R. Innes, and T. Yamanouchi
Fermi National Accelerator Laboratory, Batavia, Illinois 60510†

and

D. M. Kaplan
State University of New York at Stony Brook, Stony Brook, New York 11794*
(Received 28 January 1976)

We report preliminary results on the production of electron-positron pairs in the mass range 2.5 to 20 GeV in 400-GeV p -Be interactions. 27 high-mass events are observed in the mass range 5.5–10.0 GeV corresponding to $\sigma = (1.2 \pm 0.5) \times 10^{-35}$ cm² per nucleon. Clustering of 12 of these events between 5.8 and 6.2 GeV suggests that the data contain a new resonance at 6 GeV.

PRL 36 (1976) 1236

Homework exercise:

1. Read this paper
2. Do you find the “discovery” convincing?
3. Explain what's wrong

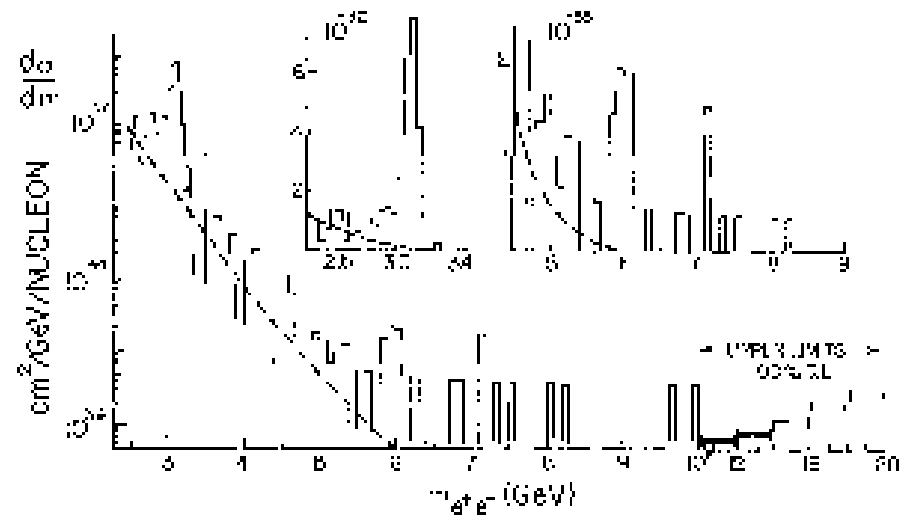
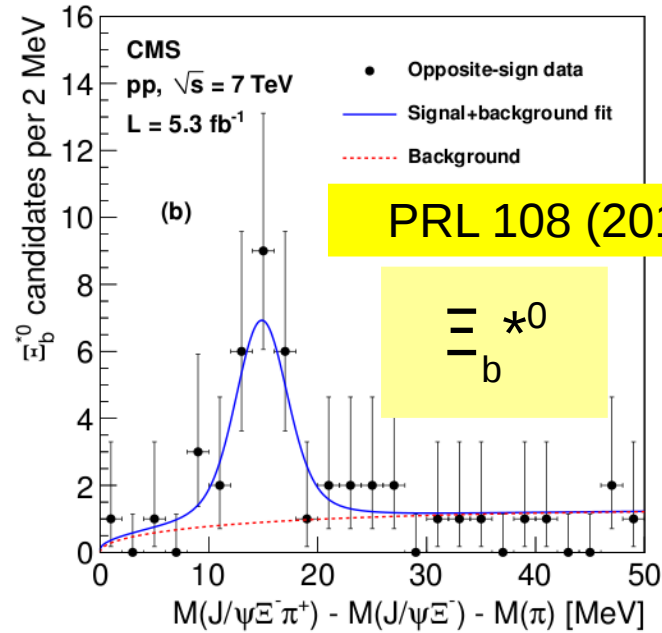
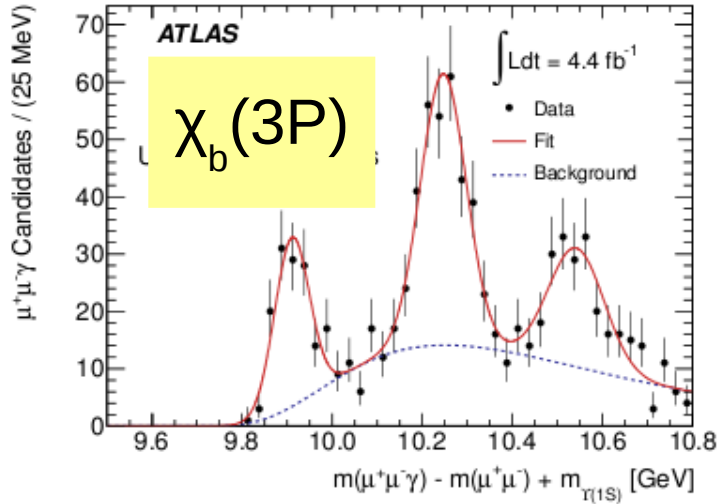


FIG. 2. Electron-positron mass spectrum: $d\sigma/dm$ per nucleon versus the effective mass. A linear Λ dependence is assumed. Note bin-width changes.

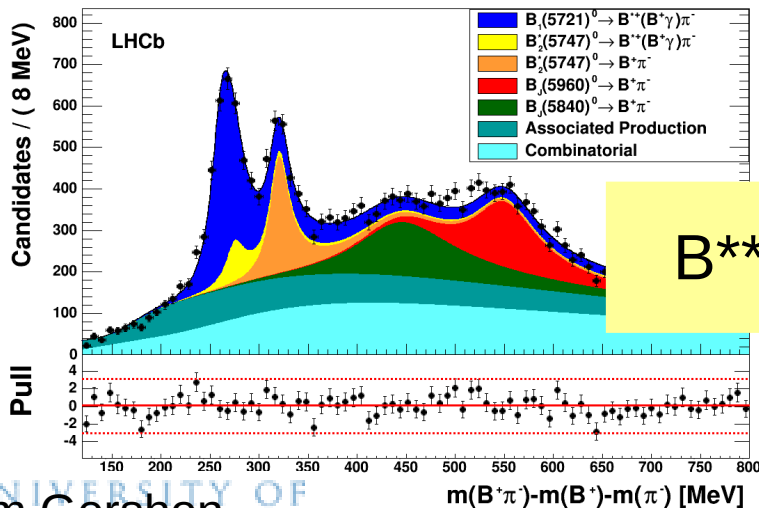
More new particles

PRL 108 (2012) 152001

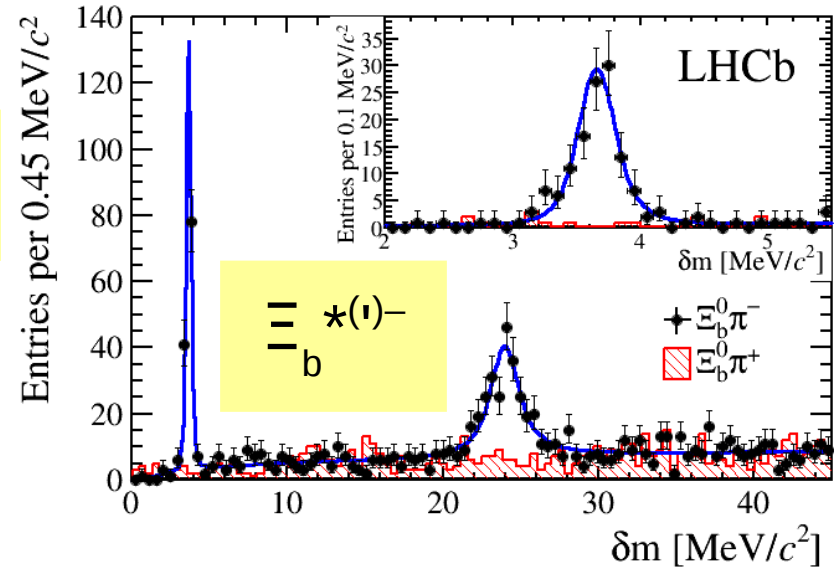


PRL 108 (2012) 252002

JHEP 04 (2015) 024



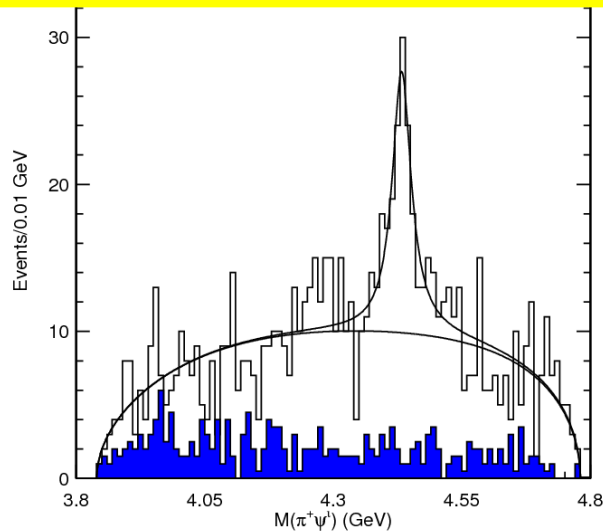
PRL 114 (2015) 062004



The smoking gun exotic hadron: A charged charmonium-like state

$$B^0 \rightarrow Z(4430)^- K^+, Z(4430)^- \rightarrow \psi' \pi^-$$

Belle PRL 100 (2008) 142001

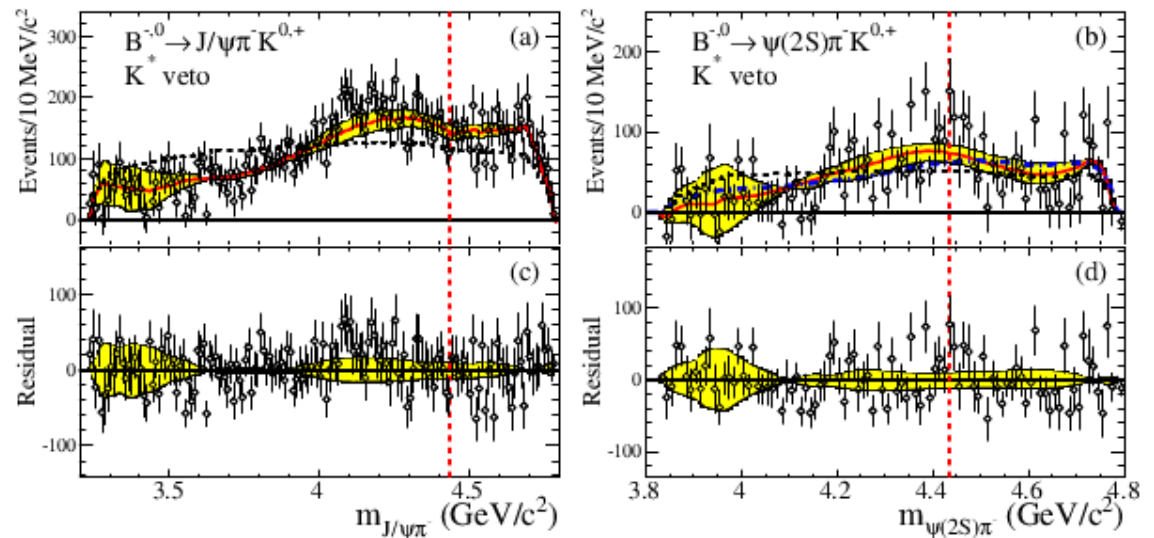


Clear peak

Still there in more detailed analysis

PRD 80 (2009) 031104

BABAR PRD 79 (2009) 112001



Data consistent with $K\pi$ reflections

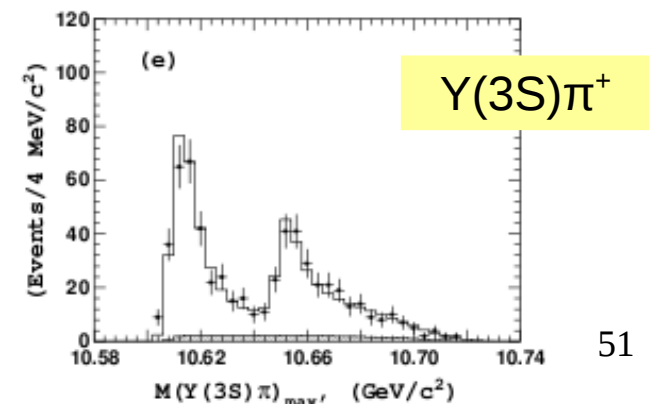
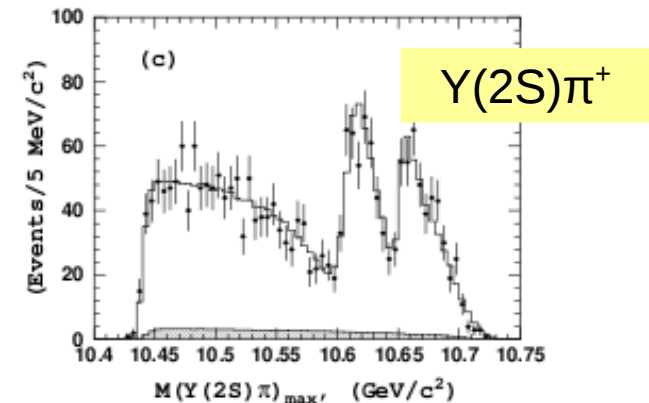
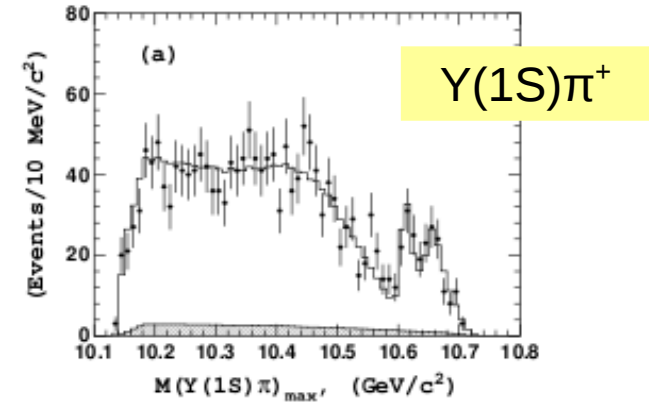
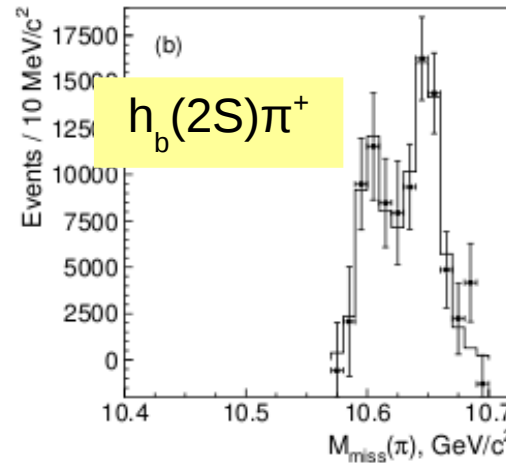
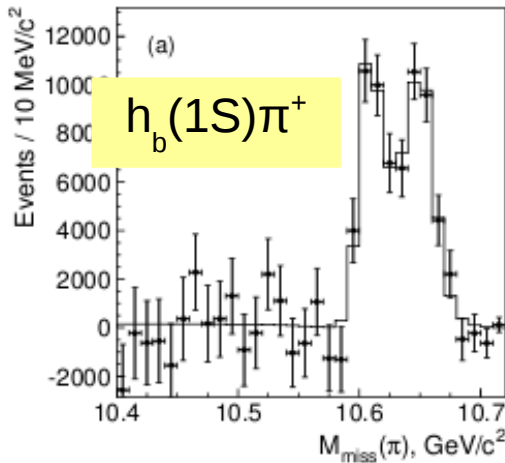
Slight peak but no evidence for new state

But also consistent with Belle

Need more experimental input
(CDF, D0, ATLAS, CMS or LHCb)

Charged bottomonium-like states

Belle
PRL 108 (2012) 122001



Final state	$\Upsilon(1S)\pi^+\pi^-$	$\Upsilon(2S)\pi^+\pi^-$	$\Upsilon(3S)\pi^+\pi^-$	$h_b(1P)\pi^+\pi^-$	$h_b(2P)\pi^+\pi^-$
$M[Z_b(10610)]$, MeV/c^2	$10611 \pm 4 \pm 3$	$10609 \pm 2 \pm 3$	$10608 \pm 2 \pm 3$	$10605 \pm 2^{+3}_{-1}$	10599^{+6+5}_{-3-4}
$\Gamma[Z_b(10610)]$, MeV	$22.3 \pm 7.7^{+3.0}_{-4.0}$	$24.2 \pm 3.1^{+2.0}_{-3.0}$	$17.6 \pm 3.0 \pm 3.0$	$11.4^{+4.5+2.1}_{-3.9-1.2}$	13^{+10+9}_{-8-7}
$M[Z_b(10650)]$, MeV/c^2	$10657 \pm 6 \pm 3$	$10651 \pm 2 \pm 3$	$10652 \pm 1 \pm 2$	$10654 \pm 3^{+1}_{-2}$	10651^{+2+3}_{-3-2}
$\Gamma[Z_b(10650)]$, MeV	$16.3 \pm 9.8^{+6.0}_{-2.0}$	$13.3 \pm 3.3^{+4.0}_{-3.0}$	$8.4 \pm 2.0 \pm 2.0$	$20.9^{+5.4+2.1}_{-4.7-5.7}$	$19 \pm 7^{+11}_{-7}$
Rel. normalization	$0.57 \pm 0.21^{+0.19}_{-0.04}$	$0.86 \pm 0.11^{+0.04}_{-0.10}$	$0.96 \pm 0.14^{+0.08}_{-0.05}$	$1.39 \pm 0.37^{+0.05}_{-0.15}$	$1.6^{+0.6+0.4}_{-0.4-0.6}$
Rel. phase, degrees	$58 \pm 43^{+4}_{-9}$	$-13 \pm 13^{+17}_{-8}$	$-9 \pm 19^{+11}_{-26}$	187^{+44+3}_{-57-12}	$181^{+65+74}_{-105-109}$