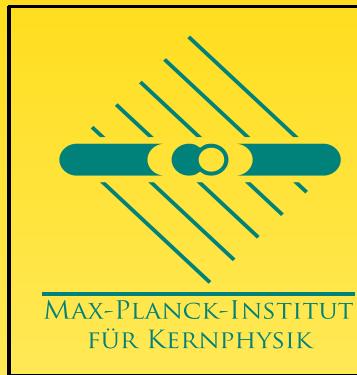
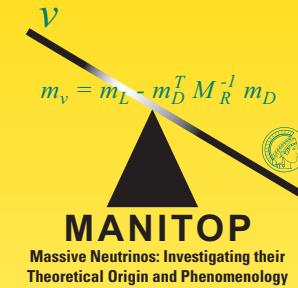


Neutrinoless Double Beta Decay and Particle Physics



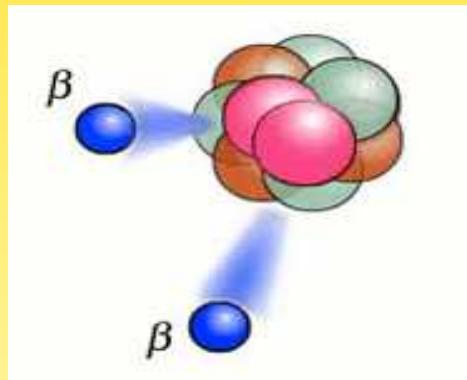
WERNER RODEJOHANN
CONFINEMENT 2016
02/09/16



Neutrinoless Double Beta Decay

$(A, Z) \rightarrow (A, Z + 2) + 2 e^- \quad (0\nu\beta\beta) \Rightarrow \text{Lepton Number Violation}$

- **Standard Interpretation** (neutrino physics)
- **Non-Standard Interpretations** ($\text{BSM} \neq \text{neutrino physics}$)



W.R., Int. J. Mod. Phys. E20, 1833-1930 (2011);

W.R., H. Päs, New J. Phys. 17, 115010 (2015)

Why should we probe Lepton Number Violation?

- L and B accidentally conserved in SM
- effective theory: $\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \mathcal{L}_{\text{LNV}} + \frac{1}{\Lambda^2} \mathcal{L}_{\text{LFV, BNV, LNV}} + \dots$
- baryogenesis: B is violated
- B, L often connected in GUTs
- GUTs have seesaw and Majorana neutrinos
- (chiral anomalies: $\partial_\mu J_{B,L}^\mu = c G_{\mu\nu} \tilde{G}^{\mu\nu} \neq 0$ with $J_\mu^B = \sum \bar{q}_i \gamma_\mu q_i$ and $J_\mu^L = \sum \bar{\ell}_i \gamma_\mu \ell_i$)

⇒ Lepton Number Violation as important as Baryon Number Violation
($0\nu\beta\beta$ is much more than a neutrino mass experiment)

Upcoming/running experiments: exciting time!!

best limit was from 2001, improved 2012

Name	Isotope	Source = Detector; calorimetric with			Source \neq Detector topology
		high ΔE	low ΔE	topology	
AMoRE	^{100}Mo	✓	—	—	—
CANDLES	^{48}Ca	—	✓	—	—
COBRA	^{116}Cd (and ^{130}Te)	—	—	✓	—
CUORE	^{130}Te	✓	—	—	—
CUPID	^{82}Se / ^{100}Mo / ^{116}Cd / ^{130}Te	✓	—	—	—
DCBA/MTD	^{82}Se / ^{150}Nd	—	—	—	✓
EXO	^{136}Xe	—	—	✓	—
GERDA	^{76}Ge	✓	—	—	—
KamLAND-Zen	^{136}Xe	—	✓	—	—
LUCIFER	^{82}Se / ^{100}Mo / ^{130}Te	✓	—	—	—
LUMINEU	^{100}Mo	✓	—	—	—
MAJORANA	^{76}Ge	✓	—	—	—
MOON	^{82}Se / ^{100}Mo / ^{150}Nd	—	—	—	✓
NEXT	^{136}Xe	—	—	✓	—
SNO+	^{130}Te	—	✓	—	—
SuperNEMO	^{82}Se / ^{150}Nd	—	—	—	✓
XMASS	^{136}Xe	—	✓	—	—

Interpretation of Experiments

Master formula:

$$\Gamma^{0\nu} = G_x(Q, Z) |\mathcal{M}_x(A, Z) \eta_x|^2$$

- $G_x(Q, Z)$: phase space factor
- $\mathcal{M}_x(A, Z)$: nuclear physics
- η_x : particle physics

Interpretation of Experiments

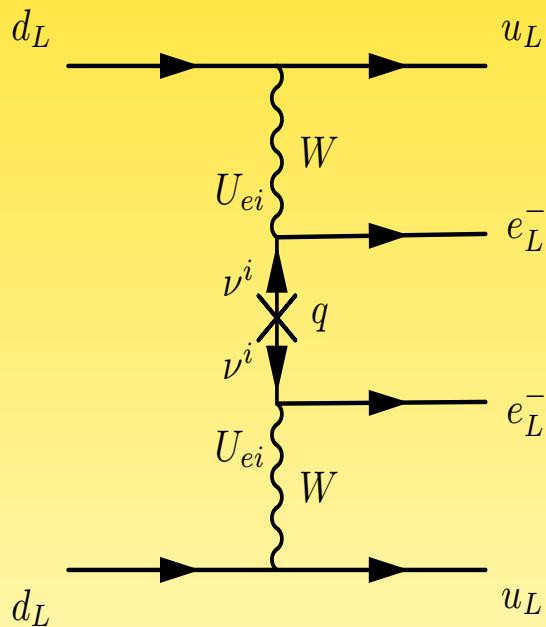
Master formula:

$$\Gamma^{0\nu} = G_x(Q, Z) |\mathcal{M}_x(A, Z) \eta_x|^2$$

- $G_x(Q, Z)$: phase space factor; **calculable**
- $\mathcal{M}_x(A, Z)$: nuclear physics; **problematic**
- η_x : particle physics; **interesting**

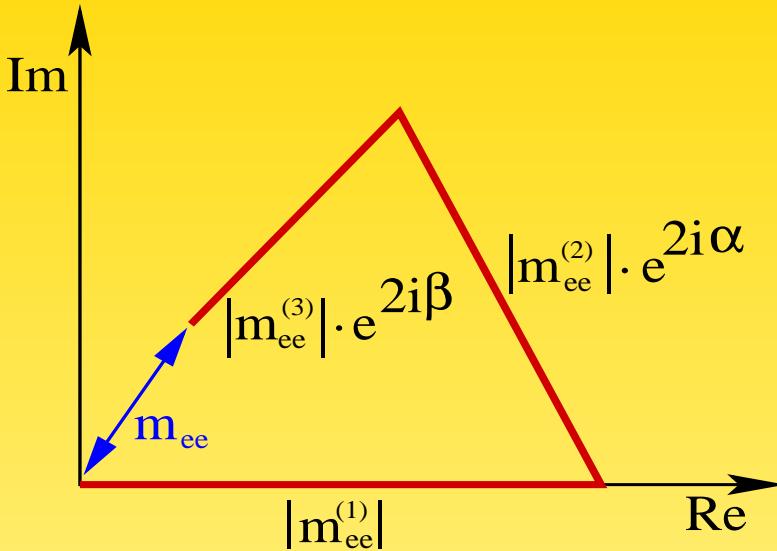
Standard Interpretation

Neutrinoless Double Beta Decay is mediated by light and massive Majorana neutrinos (the ones which oscillate) and all other mechanisms potentially leading to $0\nu\beta\beta$ give negligible or no contribution



prediction of $(100 - \epsilon)\%$ of all neutrino mass mechanisms

The effective mass



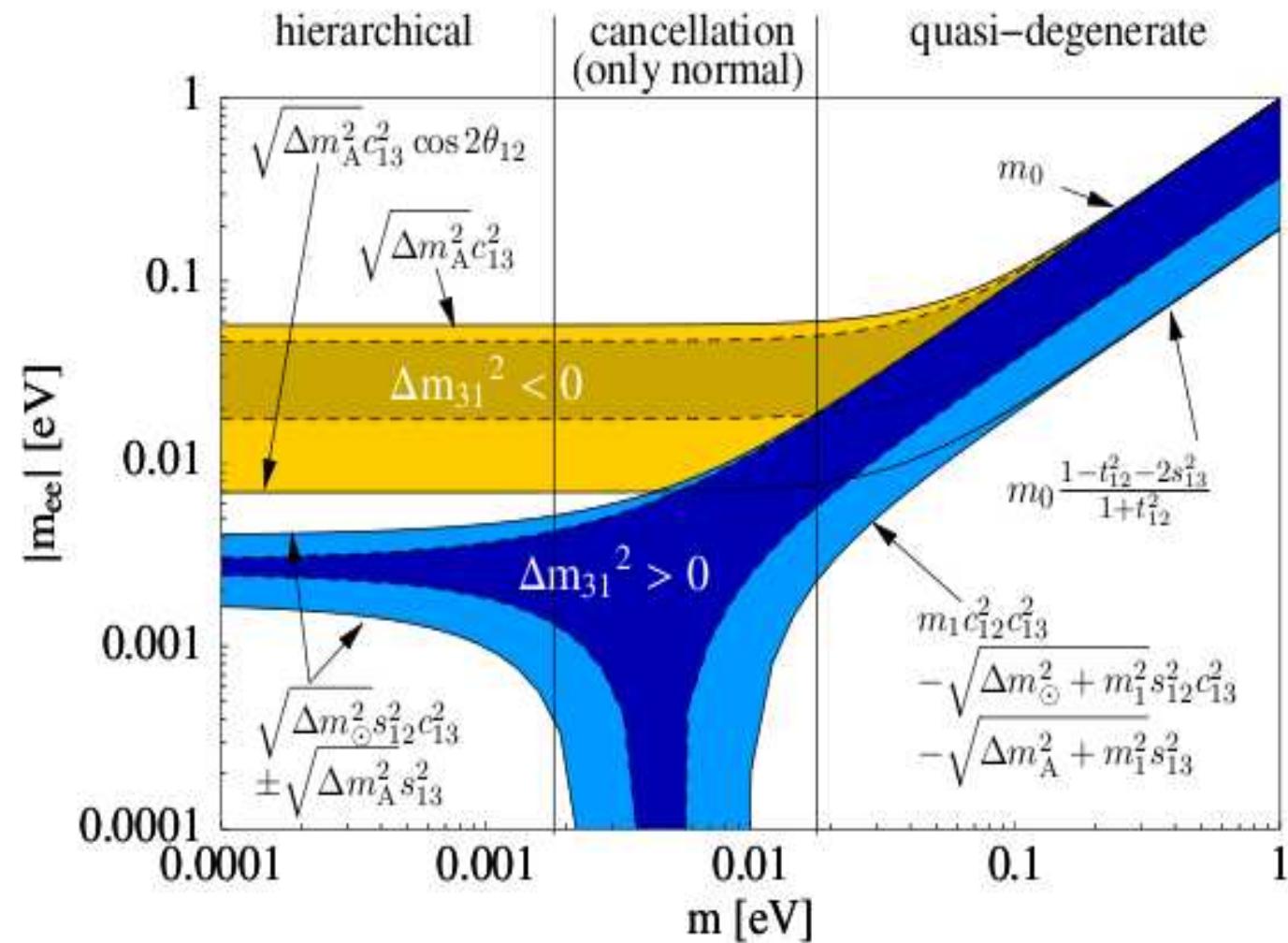
Amplitude proportional to coherent sum ("effective mass"):

$$|m_{ee}| \equiv \left| \sum U_{ei}^2 m_i \right| = \left| |U_{e1}|^2 m_1 + |U_{e2}|^2 m_2 e^{2i\alpha} + |U_{e3}|^2 m_3 e^{2i\beta} \right|$$

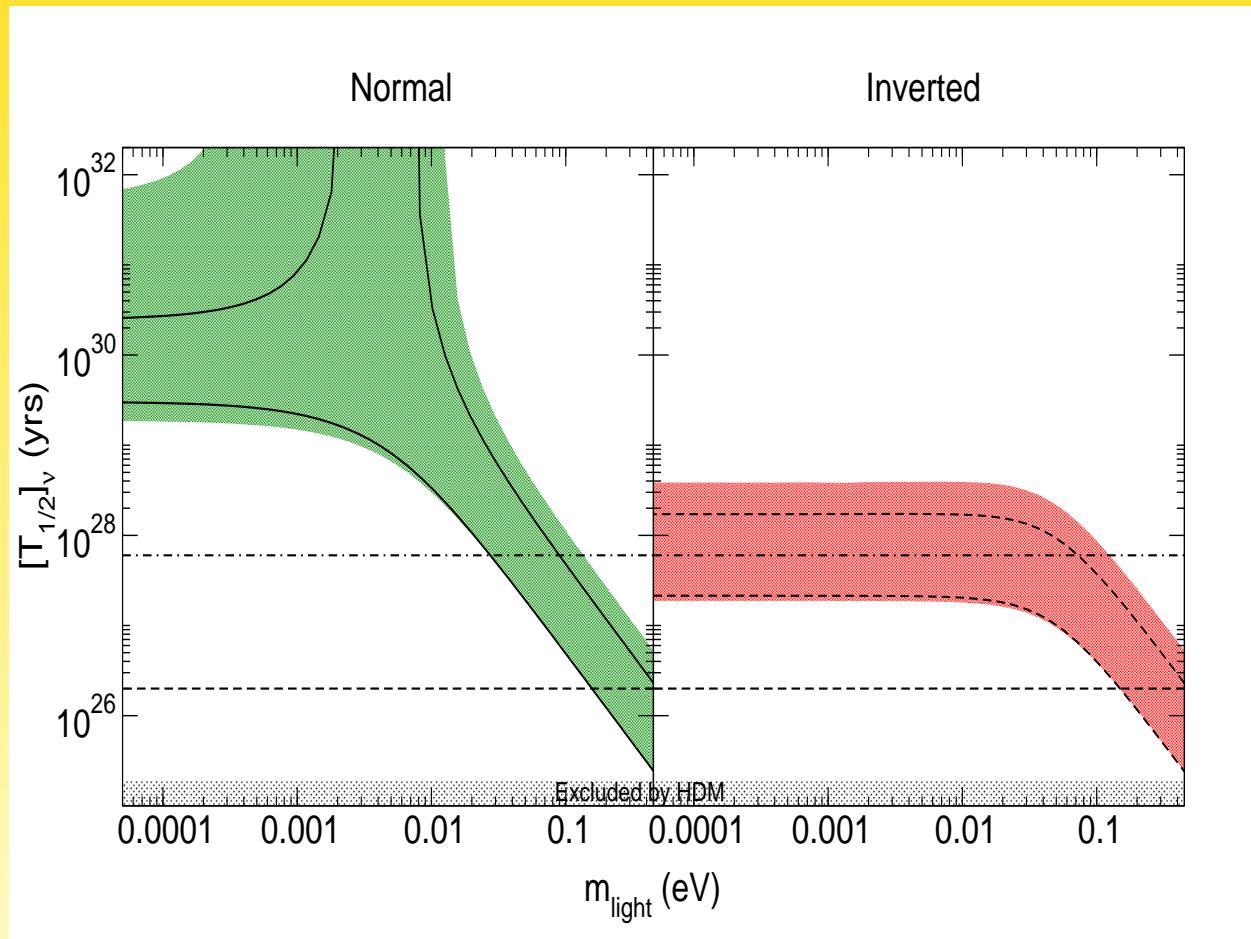
$$= f(\theta_{12}, |U_{e3}|, m_i, \text{sgn}(\Delta m_A^2), \alpha, \beta)$$

7 out of 9 parameters of neutrino physics!

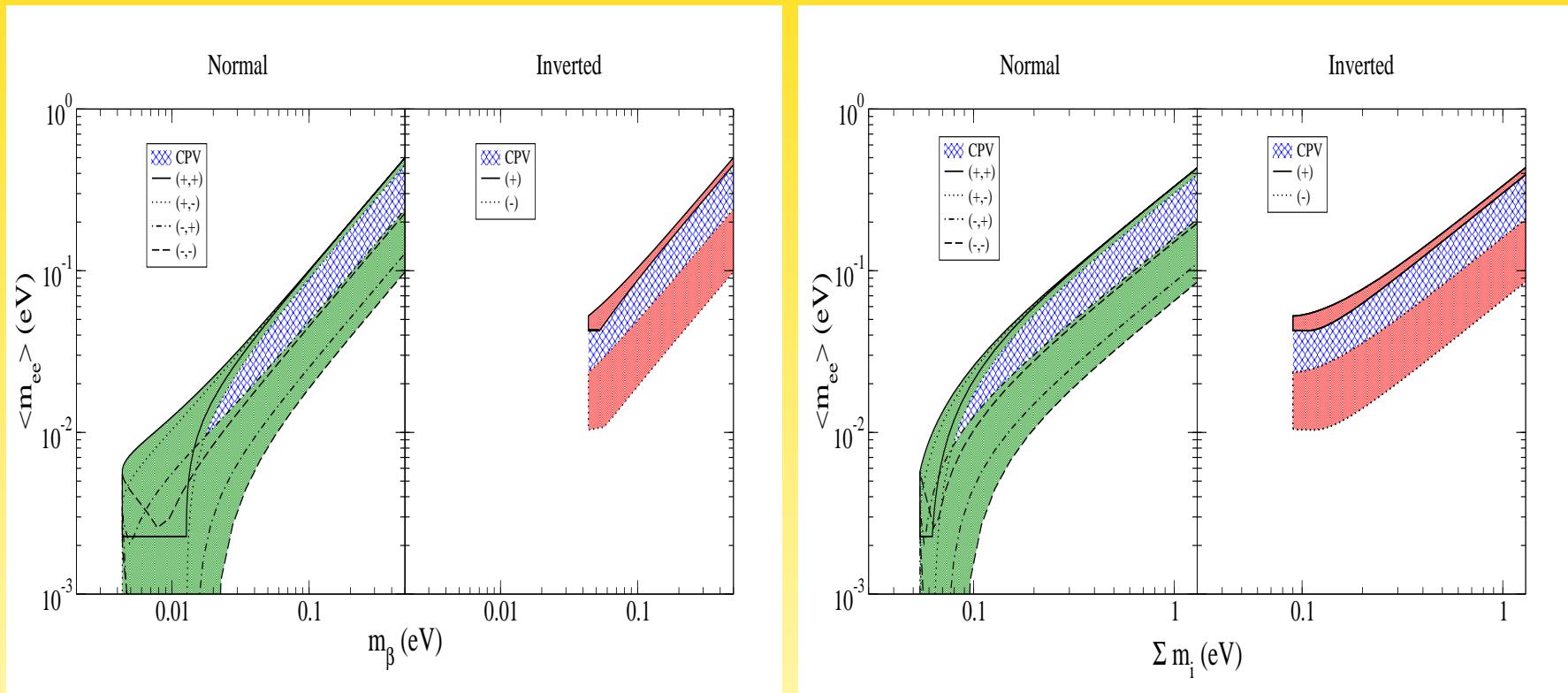
The usual plot



The usual plot (life-time instead of $|m_{ee}|$)



Plot against other observables



Complementarity of $|m_{ee}| = U_{ei}^2 m_i$, $m_\beta = \sqrt{|U_{ei}|^2 m_i^2}$ and $\Sigma = \sum m_i$

Neutrino Mass

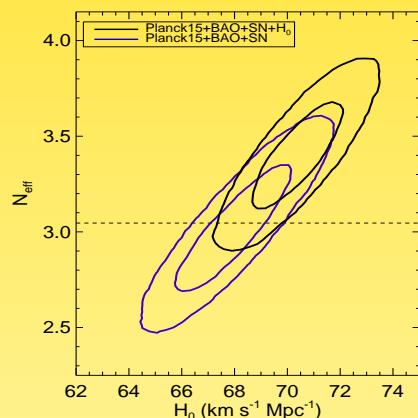
$$m(\text{heaviest}) \geq \sqrt{|m_3^2 - m_1^2|} \simeq 0.05 \text{ eV}$$

3 **complementary** methods to measure neutrino mass:

Method	observable	now [eV]	near [eV]	far [eV]	pro	con
Kurie	$\sqrt{\sum U_{ei} ^2 m_i^2}$	2.3	0.2	0.1	model-indep.; theo. clean	final?; worst
Cosmo.	$\sum m_i$	0.5	0.2	0.05	best; NH/IH	systemat.; model-dep.
$0\nu\beta\beta$	$ \sum U_{ei}^2 m_i $	0.2	0.1	0.05	fundament.; NH/IH	model-dep.; theo. dirty

Cosmological Limits

stacking more and more data sets on top of each other, limits become stronger
(needed to break degeneracies, but induces systematic issues)
including more and more parameters, limits become weaker



Riess *et al.*,

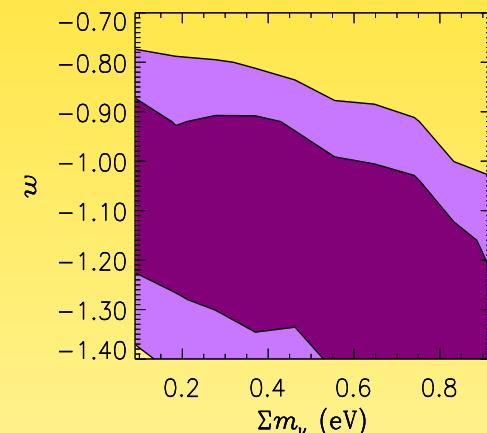
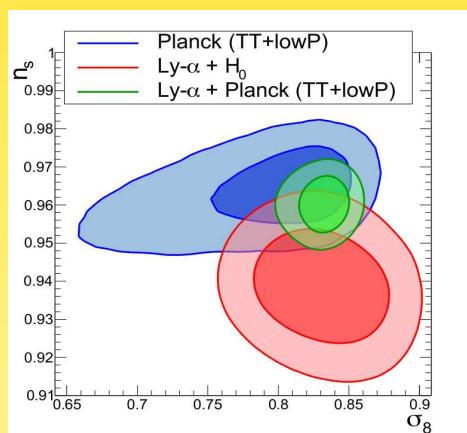
1604.01424

Palanque-Delabrouille *et al.*,

1506.05976

Hannestad,

PRL 95



(most extreme (1410.7244): at 1σ : $\Sigma m_\nu \leq 0.08$ eV, disfavors inverted ordering...)

Sterile Neutrinos and $0\nu\beta\beta$

- LSND/MiniBooNE/gallium/reactor anomalies, $\Delta m^2 \simeq 1 \text{ eV}^2$, $U_{\alpha 4} \simeq 0.1$
- $|m_{ee}| = \underbrace{|U_{e1}|^2 m_1 + |U_{e2}|^2 m_2 e^{2i\alpha} + |U_{e3}|^2 m_3 e^{2i\beta}}_{m_{ee}^{\text{act}}} + \underbrace{|U_{e4}|^2 m_4 e^{2i\Phi_1}}_{m_{ee}^{\text{st}}}$
- sterile contribution to $0\nu\beta\beta$:

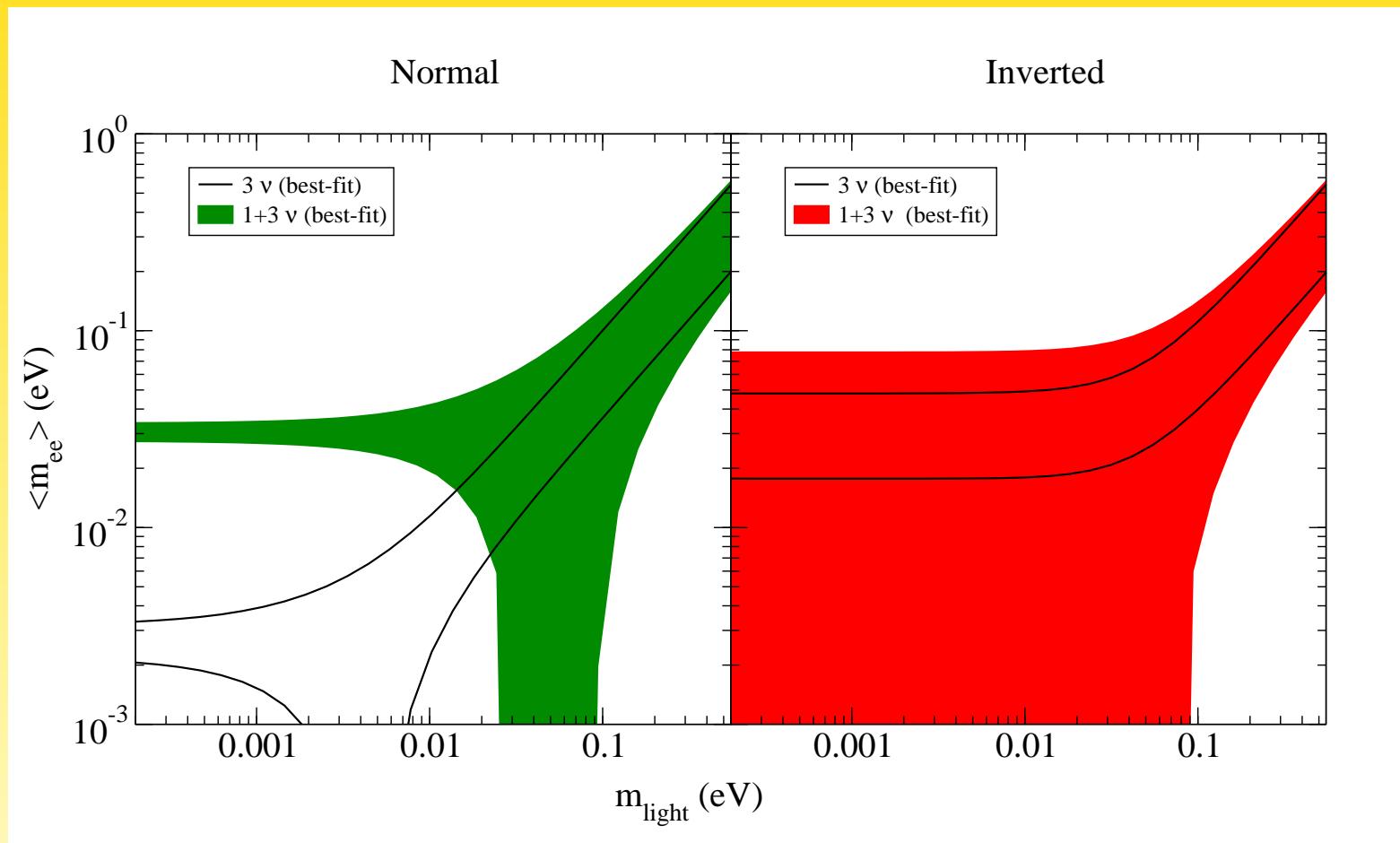
$$|m_{ee}|^{\text{st}} \simeq \sqrt{\Delta m_{\text{st}}^2} |U_{e4}|^2 \left\{ \begin{array}{l} \gg |m_{ee}|_{\text{NH}}^{\text{act}} \\ \simeq |m_{ee}|_{\text{IH}}^{\text{act}} \end{array} \right.$$

$\Rightarrow |m_{ee}|_{\text{NH}}$ cannot vanish and $|m_{ee}|_{\text{IH}}$ can vanish!

\Rightarrow usual phenomenology gets completely turned around!

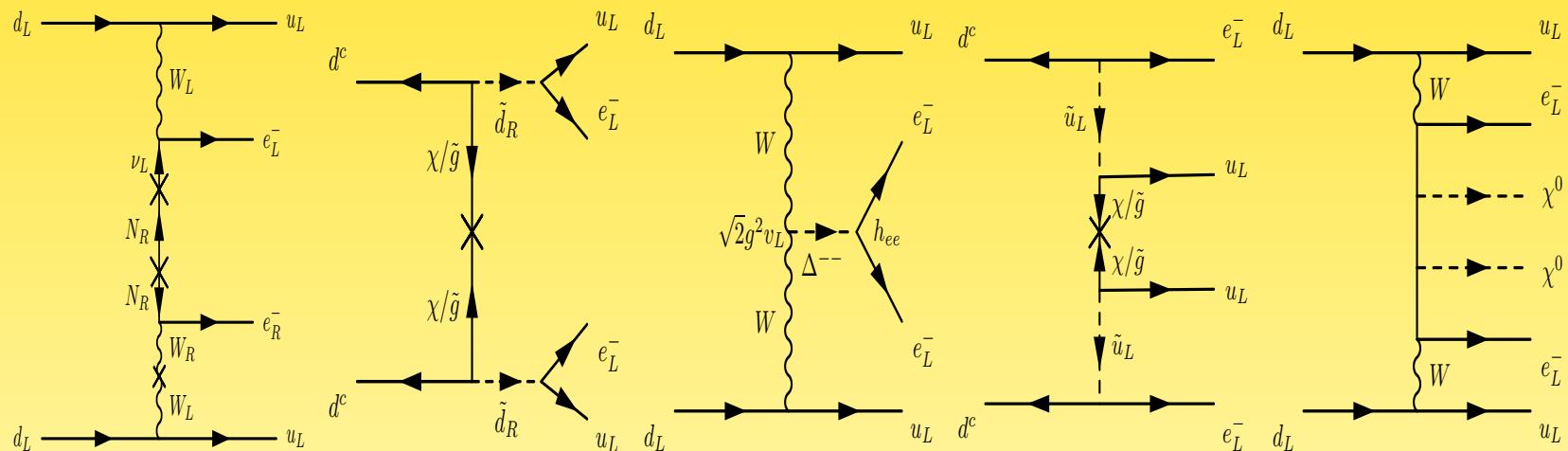
Barry, W.R., Zhang, JHEP **1107**; Giunti *et al.*, PRD **87**; Girardi, Petcov, Meroni, JHEP **1311**

Usual plot gets completely turned around!



Non-Standard Interpretations:

There is at least one other mechanism leading to Neutrinoless Double Beta Decay and its contribution is at least of the same order as the light neutrino exchange mechanism



Clear experimental signature:

KATRIN and/or cosmology see nothing but $0\nu\beta\beta$ does

Energy Scale:

Note: *standard amplitude* for light Majorana neutrino exchange:

$$\mathcal{A}_l \simeq G_F^2 \frac{|m_{ee}|}{q^2} \simeq 7 \times 10^{-18} \left(\frac{|m_{ee}|}{0.5 \text{ eV}} \right) \text{ GeV}^{-5} \simeq (2.7 \text{ TeV})^{-5}$$

if new heavy particles are exchanged:

$$\mathcal{A}_h \simeq \frac{c}{M^5}$$

\Rightarrow for $0\nu\beta\beta$ holds:

$$1 \text{ eV} = 1 \text{ TeV}$$

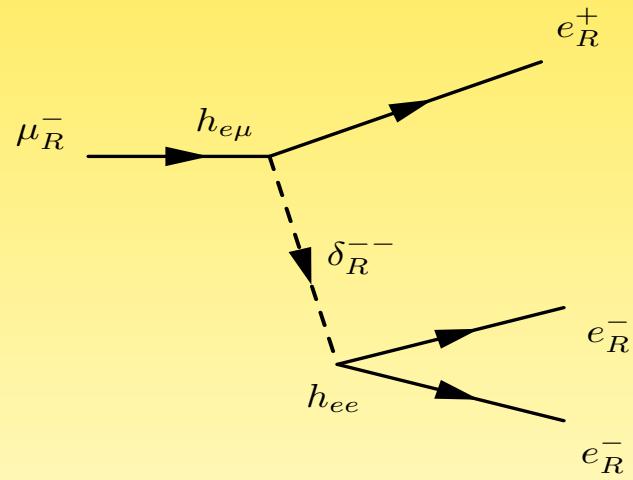
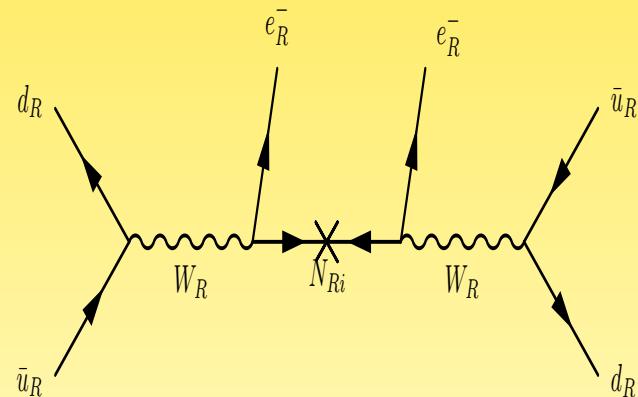
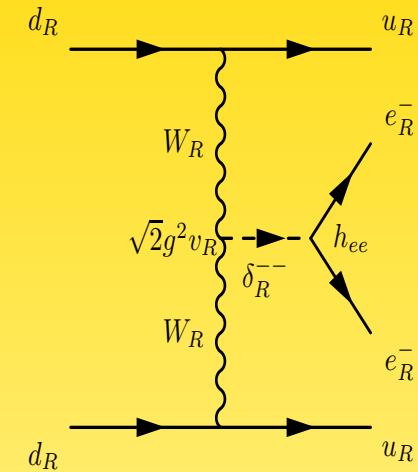
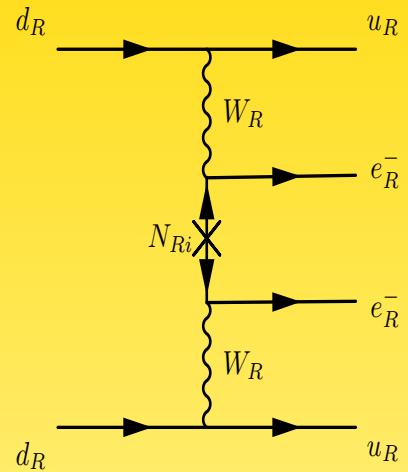
\Rightarrow Phenomenology in colliders, LFV
(cosmology limits decoupled from $0\nu\beta\beta$)

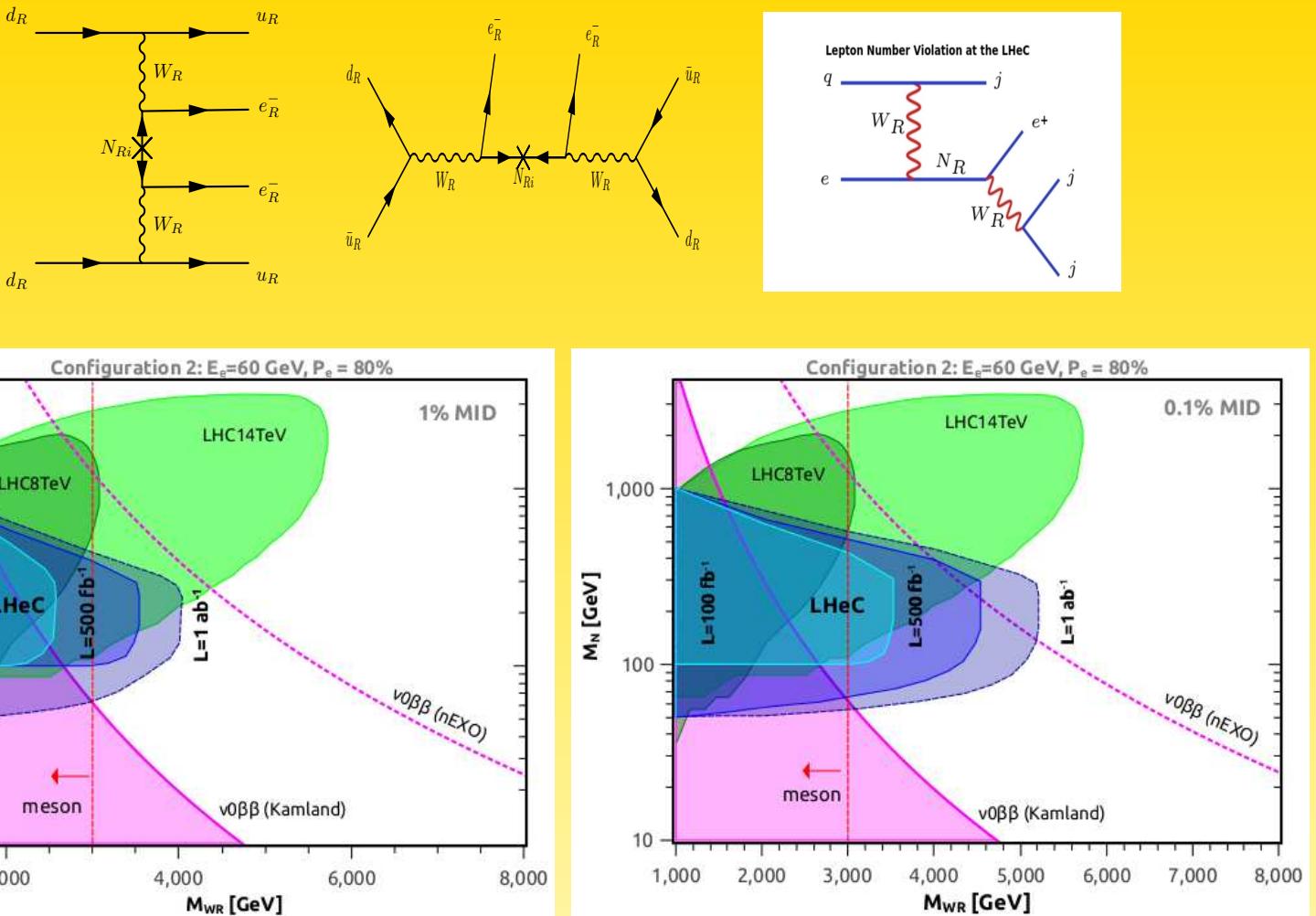
$$T^{0\nu}(1 \text{ eV}) = T^{0\nu}(1 \text{ TeV})$$

- RPV Supersymmetry
- left-right symmetry
- heavy neutrinos
- color octets
- leptoquarks
- effective operators
- extra dimensions
- ...

⇒ need to solve the inverse problem... .

Example: Left-right symmetric theories

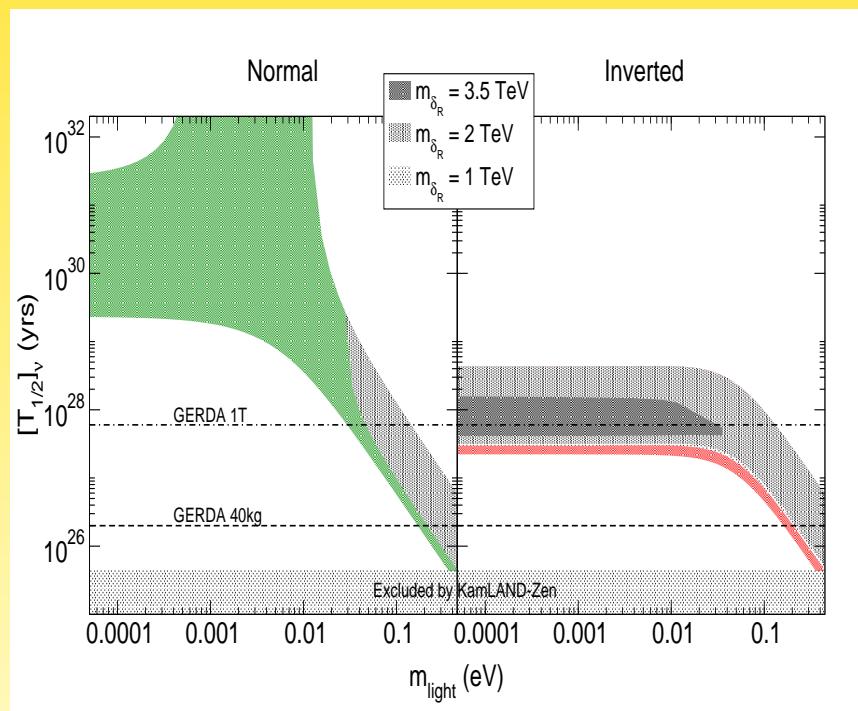
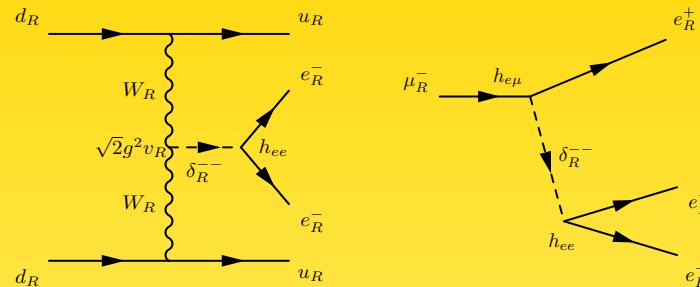




Lindner, Queiroz, W.R., Yaguna, JHEP 1606

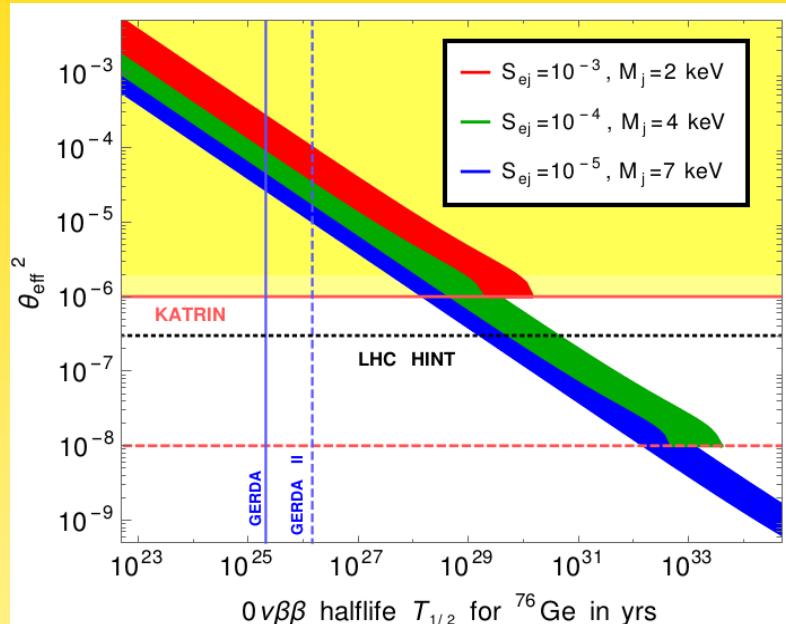
$\text{LHeC} \leftrightarrow$ polarization and complementarity

Constraints from Lepton Flavor Violation



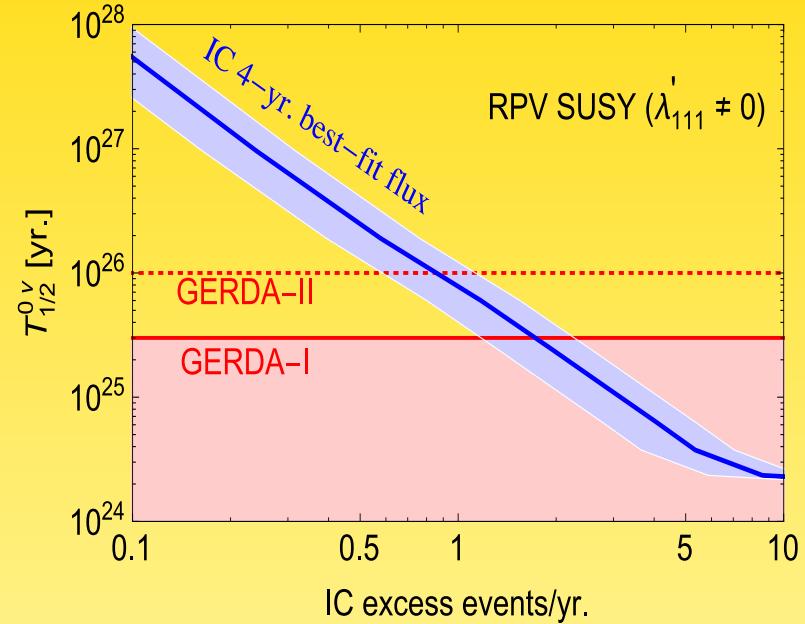
Barry, W.R., JHEP 1309

Surprising correlations in alternative scenarios



keV- ν in KATRIN
(RH interaction)

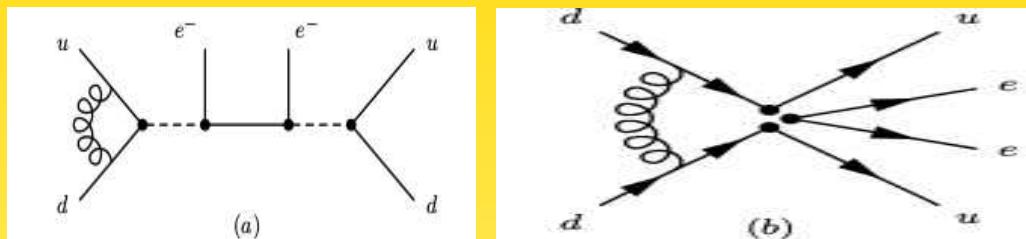
Barry, Heeck, W.R., JHEP **1407**



excess events in IceCube
(RPV SUSY)

Dev, Ghosh, W.R., 1605.09743

QCD corrections



- naive size $\alpha_s/(4\pi) \ln \frac{M_W^2}{(100 \text{ MeV})^2} = 10\%$, true for standard interpretation
- but: creates in non $(V - A) \otimes (V - A)$ mechanisms color non-singlet operators, Fierz them and mix with new operators with different NMEs
- can give for alternative mechanisms large effect in either direction...
- (makes limit on right-handed diagrams slightly weaker)

Mahajan, PRL 112; Gonzalez, Kovalenko, Hirsch, PRD 93; Peng,
Ramsey-Musolf, Winslow, PRD 93

Do Dirac neutrinos mean there is no Lepton Number Violation?

Model based on gauged $B - L$, broken by 4 units

\Rightarrow Neutrinos are Dirac particles, $\Delta L = 2$ forbidden, but $\Delta L = 4$ allowed...

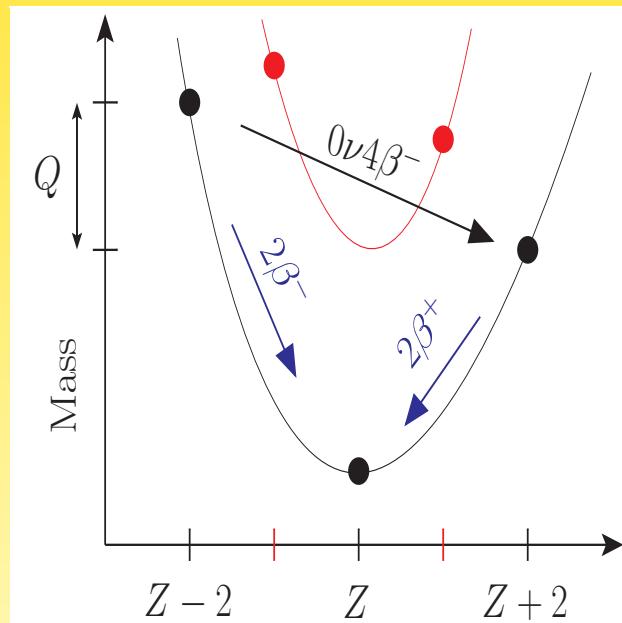
Heeck, W.R., EPL 103

Do Dirac neutrinos mean there is no Lepton Number Violation?

Model based on gauged $B - L$, broken by 4 units

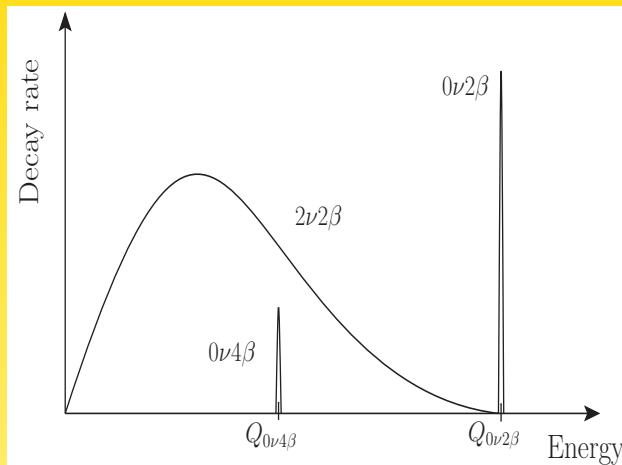
\Rightarrow Neutrinos are Dirac particles, $\Delta L = 2$ forbidden, but $\Delta L = 4$ allowed...

\Rightarrow observable: neutrinoless quadruple beta decay $(A, Z) \rightarrow (A, Z + 4) + 4 e^-$



Heeck, W.R., EPL 103

Candidates for neutrinoless quadruple beta decay



	$Q_{0\nu4\beta}$	Other decays	NA
$^{96}_{40}\text{Zr} \rightarrow ^{96}_{44}\text{Ru}$	0.629	$\tau_{1/2}^{2\nu2\beta} \simeq 2 \times 10^{19}$	2.8
$^{136}_{54}\text{Xe} \rightarrow ^{136}_{58}\text{Ce}$	0.044	$\tau_{1/2}^{2\nu2\beta} \simeq 2 \times 10^{21}$	8.9
$^{150}_{60}\text{Nd} \rightarrow ^{150}_{64}\text{Gd}$	2.079	$\tau_{1/2}^{2\nu2\beta} \simeq 7 \times 10^{18}$	5.6

Heeck, W.R., EPL 103

Summary



- need to pursue all neutrino mass approaches
 - confirm 3 Majorana neutrino paradigm!
 - inconsistencies not unlikely
- LHC and $0\nu\beta\beta$ complementary
- distinguishing mechanisms necessary

Another extreme point of view: Quenching

$T_{1/2}^{0\nu} \propto g_A^{-4}$, where in $2\nu\beta\beta$ -decay ([Iachello](#))

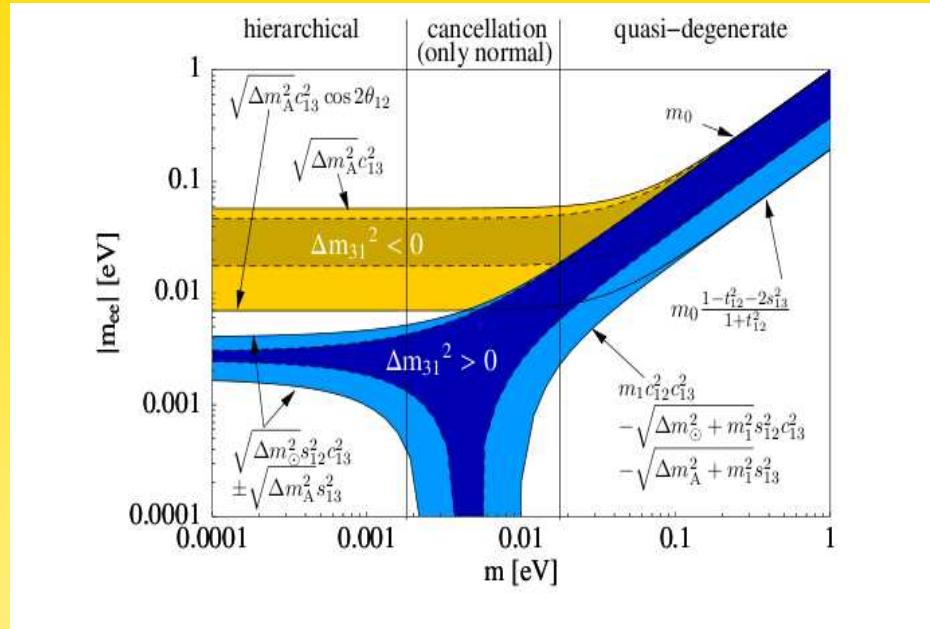
$$g_A^{\text{IBM}} \simeq 1.27 A^{-0.18} = \begin{cases} 0.58 & \text{Ge} \\ 0.53 & \text{Te} \\ 0.52 & \text{Xe} \end{cases}$$

would shift lifetimes an order of magnitude (in wrong direction...)

- model-space truncation (A -dep.)/omission of N^* , Δ (not A -dep.)
- energy scale (no quenching for muon capture)/many multipolarities in 0ν
- include 2 body currents (creation of 2p2h), weaker quenching in 0ν ([Engel](#), [Simkovic](#), [Vogel](#), [PRC89](#))

lots of nuclear theory work on the way, possibly no showstopper (20%?)

Inverted Ordering



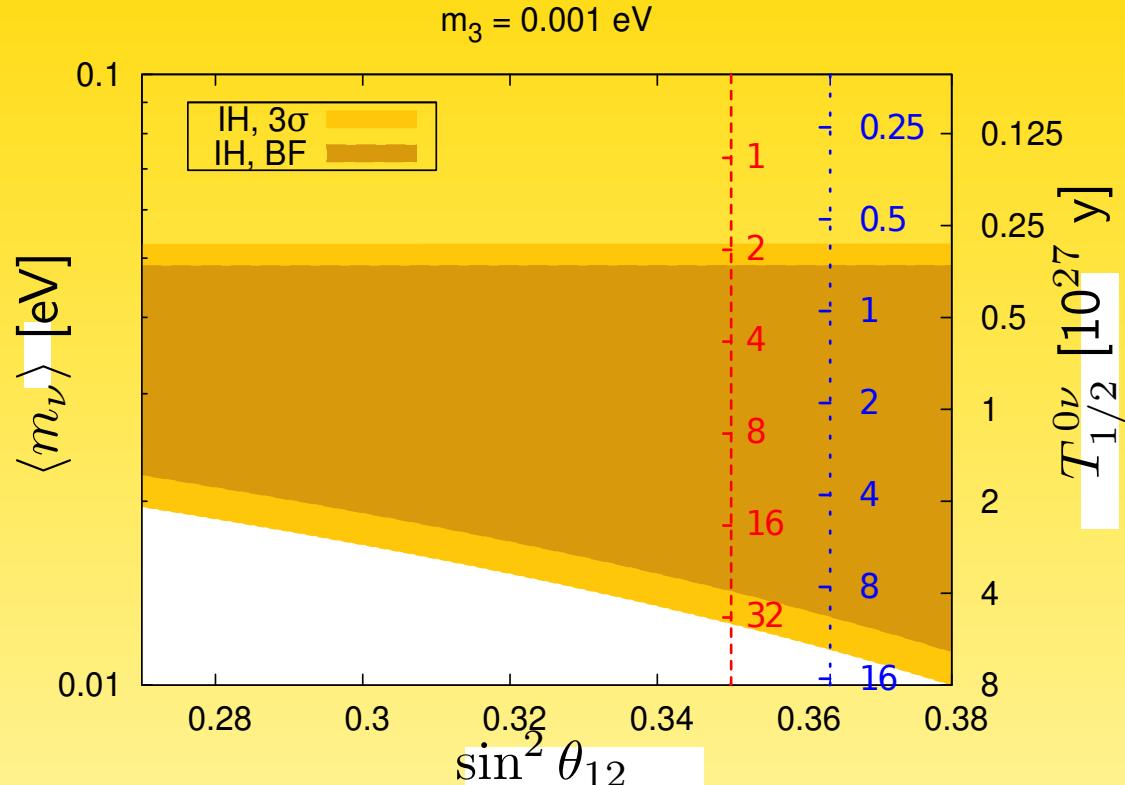
Nature provides 2 scales:

$$|m_{ee}|_{\max}^{\text{IH}} \simeq c_{13}^2 \sqrt{\Delta m_A^2} \quad \text{and} \quad |m_{ee}|_{\min}^{\text{IH}} \simeq c_{13}^2 \sqrt{\Delta m_A^2} \cos 2\theta_{12}$$

requires $\mathcal{O}(10^{26} \dots 10^{27})$ yrs

is the lower limit $|m_{ee}|_{\min}^{\text{IH}}$ fixed?

Inverted Hierarchy

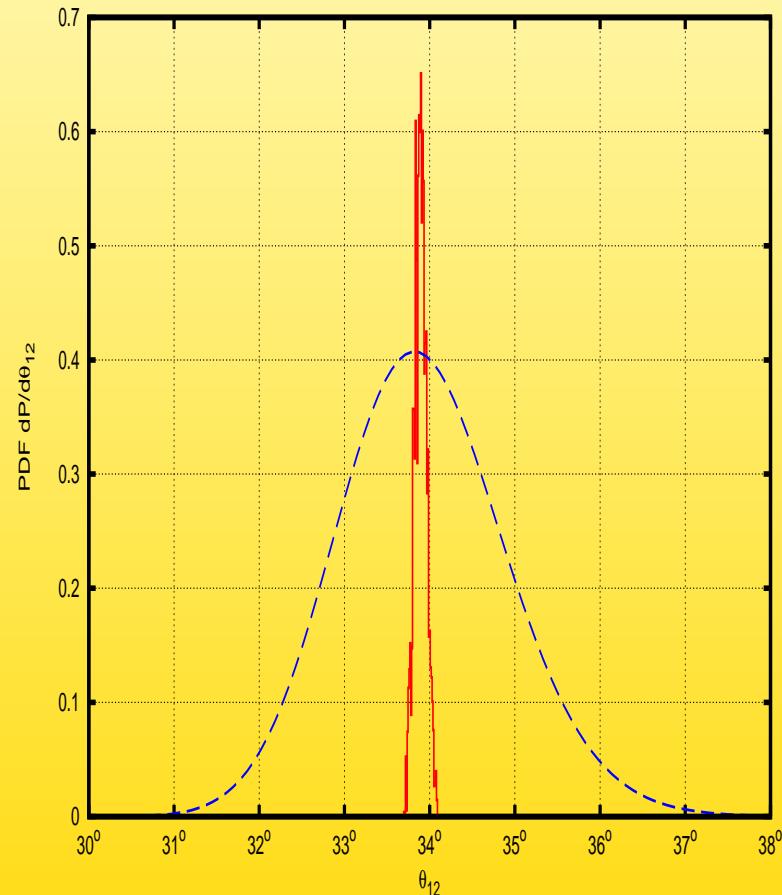
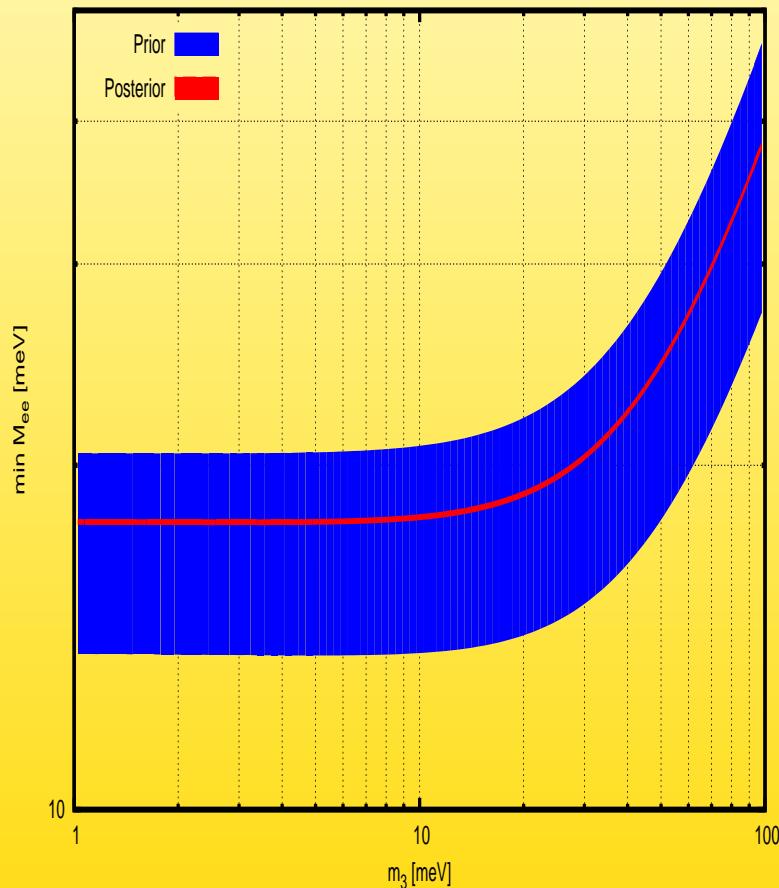


Current 3σ range of $\sin^2 \theta_{12}$ gives factor of ~ 2 uncertainty for $|m_{ee}|_{\min}^{\text{IH}}$

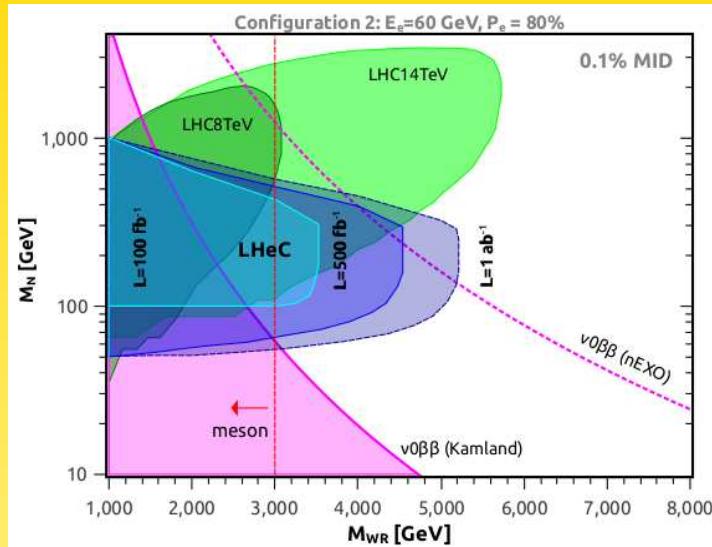
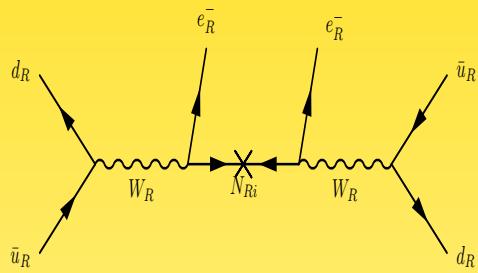
$$(T_{1/2}^{0\nu})^{-1} \propto a \varepsilon \sqrt{\frac{M t}{B \Delta E}} \Rightarrow \text{need precision determination of } \theta_{12}! \leftrightarrow \text{JUNO}$$

Dueck, W.R., Zuber, PRD **83**; Ge, W.R., PRD **92**

Ge, W.R., PRD 92; <http://nupro.hepforge.org>

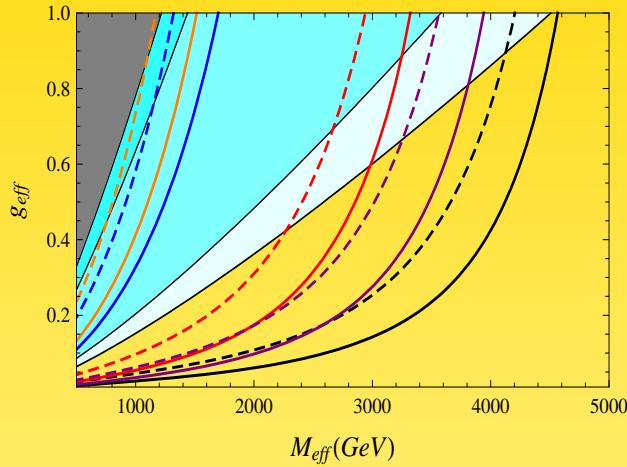
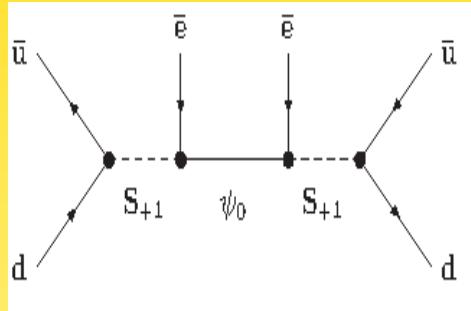


LHC vs. $0\nu\beta\beta$



- LHC assumptions: $M_N < M_{W_R}$, $\text{BR}(M_N \rightarrow ee) = 1$, $g_R = g_L$
- cuts result in weak sensitivities for low M_N
- background processes?
- QCD corrections?
- (LNV at LHC and baryogenesis)

Background



Helo *et al.*, PRD 88

one should include e.g.

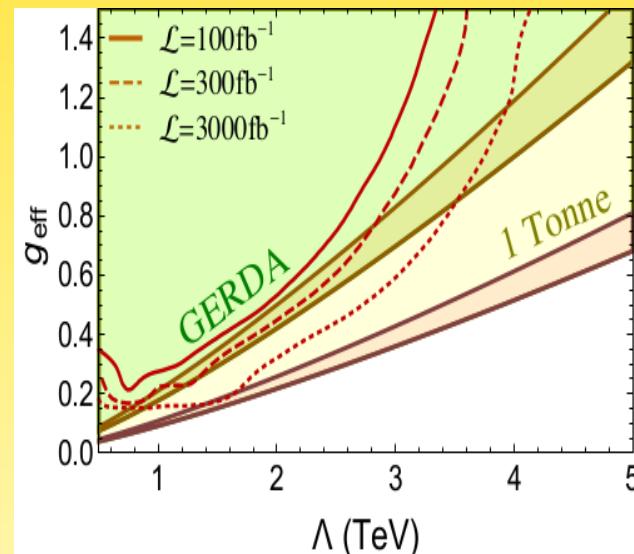
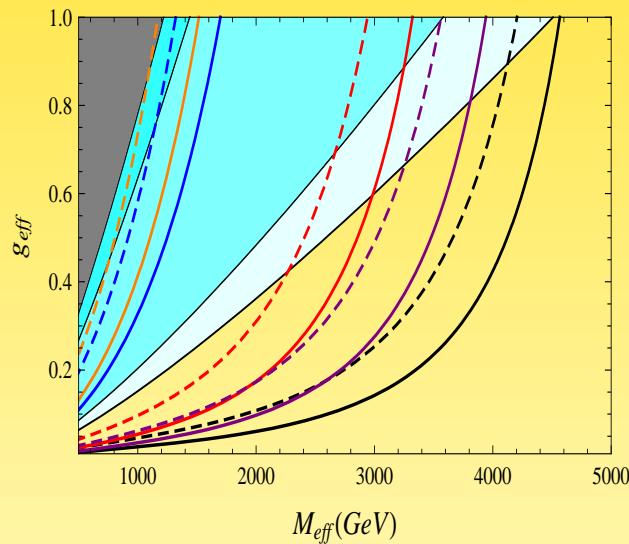
- “jet fake” (high- p_T jet registered as electron)
- “charge flip” (e^- from opposite sign pair transfer p_T to e^+ via conversion)

Peng, Ramsey-Musolf, Winslow, 1508.04444

Background

one should include e.g.

- “jet fake” (high- p_T jet registered as electron)
- “charge flip” (e^- from opposite sign pair transfer p_T to e^+ via conversion)



Peng, Ramsey-Musolf, Winslow, 1508.04444

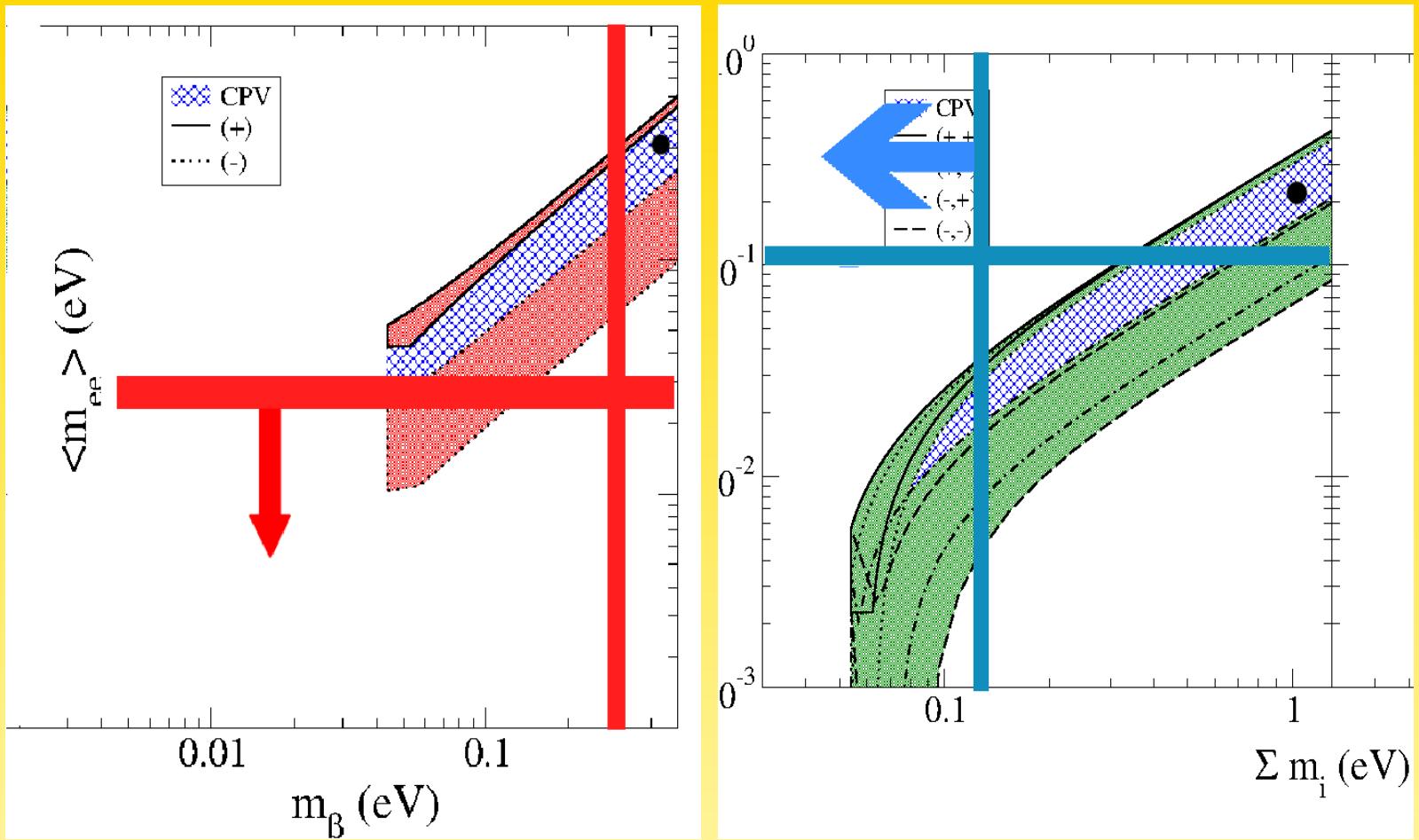
Distinguishing Mechanisms

The inverse problem of $0\nu\beta\beta$

- 1.) Other observables (LHC, LFV, KATRIN, cosmology,...)
- 2.) Decay products (individual e^- energies, angular correlations, spectrum,...)
([SuperNEMO](#), EPJC **70**; Horoi, Neascu, [1511.00670](#))
- 3.) Nuclear physics (multi-isotope, 0ν ECEC, $0\nu\beta^+\beta^+$,...)
([Gehman](#), [Elliott](#), JPG **34,35**)

Complementarity!

- are already in era of complementarity
 - cosmology limits rule out that light neutrinos saturate $0\nu\beta\beta$ -limits
 - * strictest limits start to disfavor inverted ordering
 - $0\nu\beta\beta$ limits rule out that light neutrinos saturate Mainz/Troitsk limit
- interesting possibilities in case inconsistencies arise...



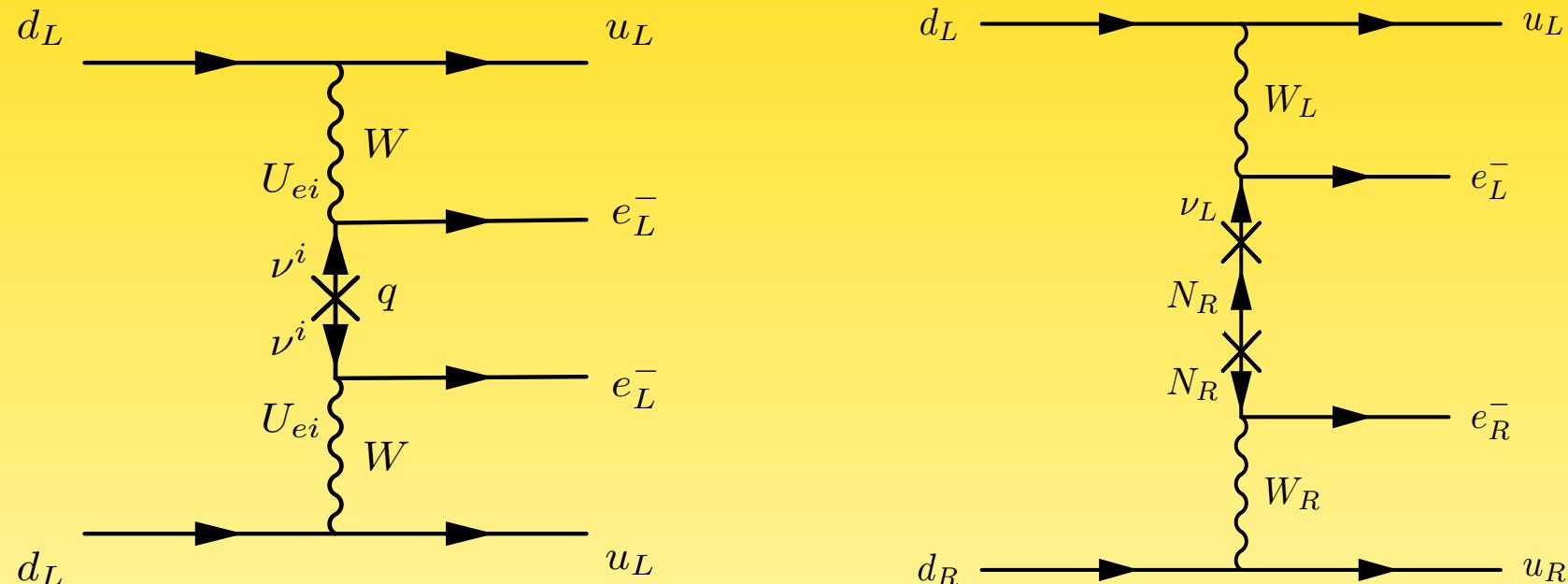
CP violation!

Dirac neutrinos!

something else does $0\nu\beta\beta$!

Distinguishing via decay products

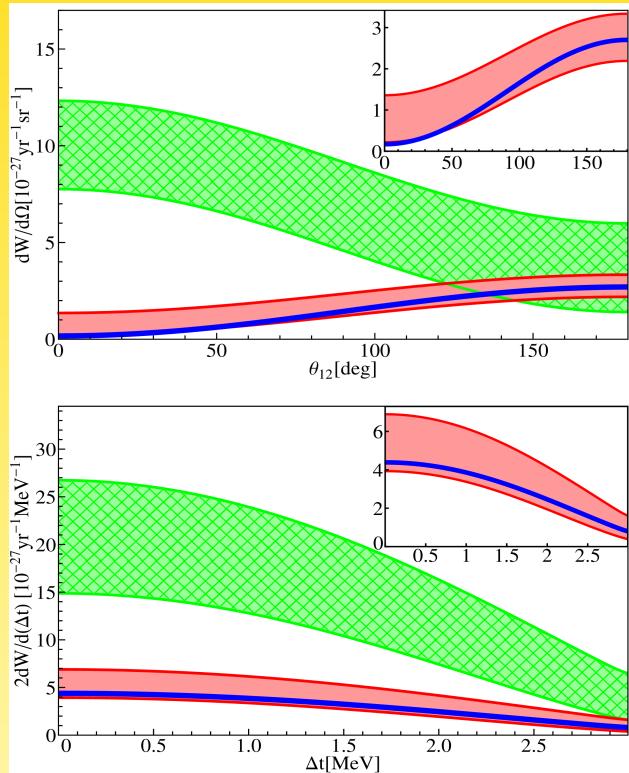
Consider standard plus λ -mechanism



$$\frac{d\Gamma}{dE_1 dE_2 d\cos\theta} \propto (1 - \beta_1 \beta_2 \cos\theta) \quad \frac{d\Gamma}{dE_1 dE_2 d\cos\theta} \propto (E_1 - E_2)^2 (1 + \beta_1 \beta_2 \cos\theta)$$

Arnold *et al.*, EPJC 70

Distinguishing via decay products



$|m_{ee}| = 0.1 \text{ eV}$ and

$$\frac{U_{ei}S_{ei}}{M_{WR}^2} = 0$$

$$\frac{U_{ei}S_{ei}}{M_{WR}^2} = 8 \cdot 10^{-6} \text{ TeV}^{-2}$$

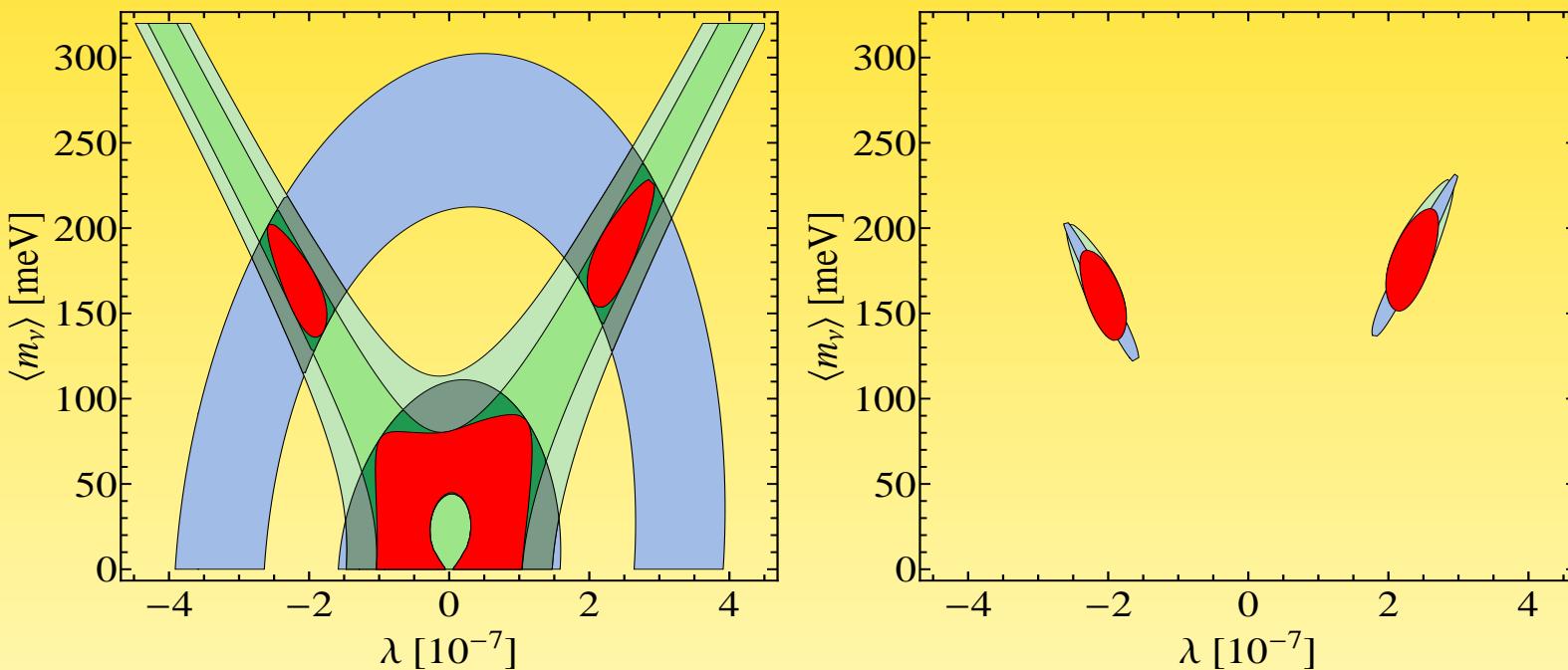
$$\frac{U_{ei}S_{ei}}{M_{WR}^2} = 3 \cdot 10^{-5} \text{ TeV}^{-2}$$

Horoi, Neascu, 1511.00670

Distinguishing via decay products

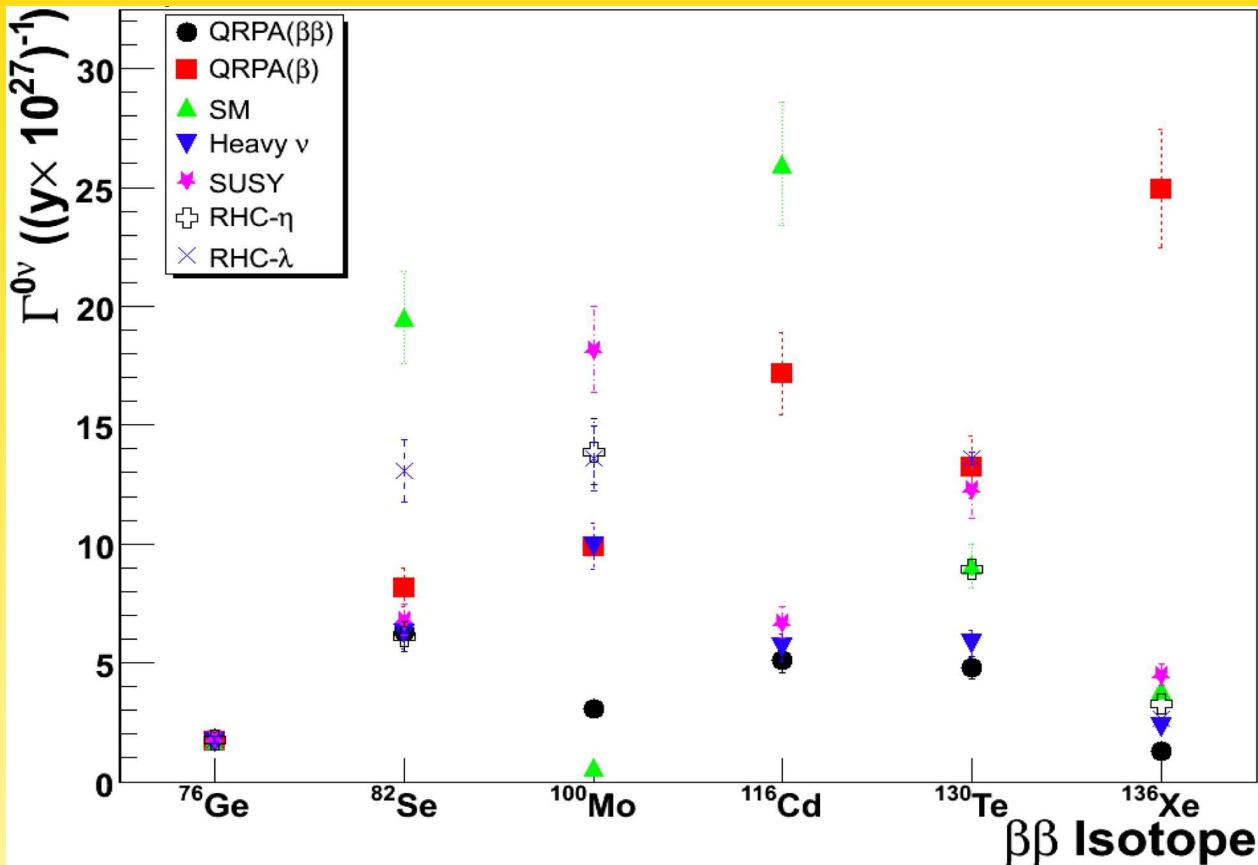
Defining asymmetries

$$A_\theta = (N_+ - N_-)/(N_+ + N_-) \text{ and } A_E = (N_> - N_<)/(N_> + N_<)$$



Arnold *et al.*, EPJC 70

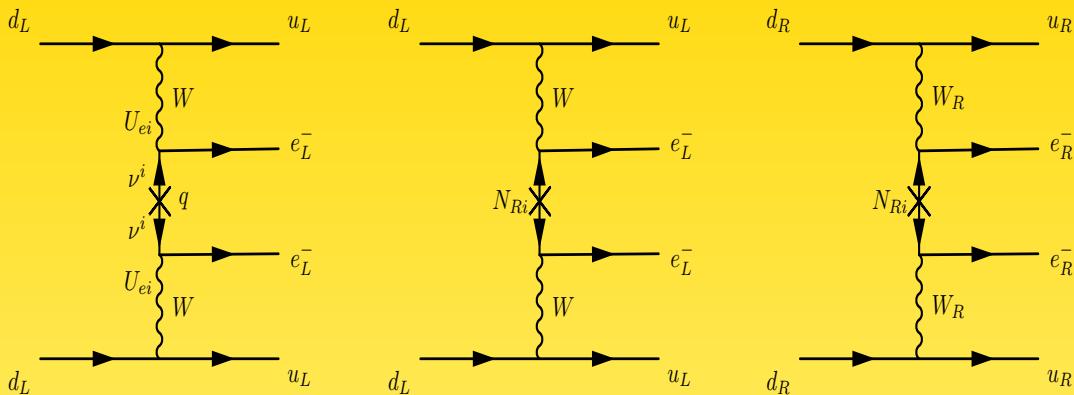
Distinguishing via nuclear physics



Gehman, Elliott, JPG 34,35

3 to 4 isotopes necessary to disentangle mechanism

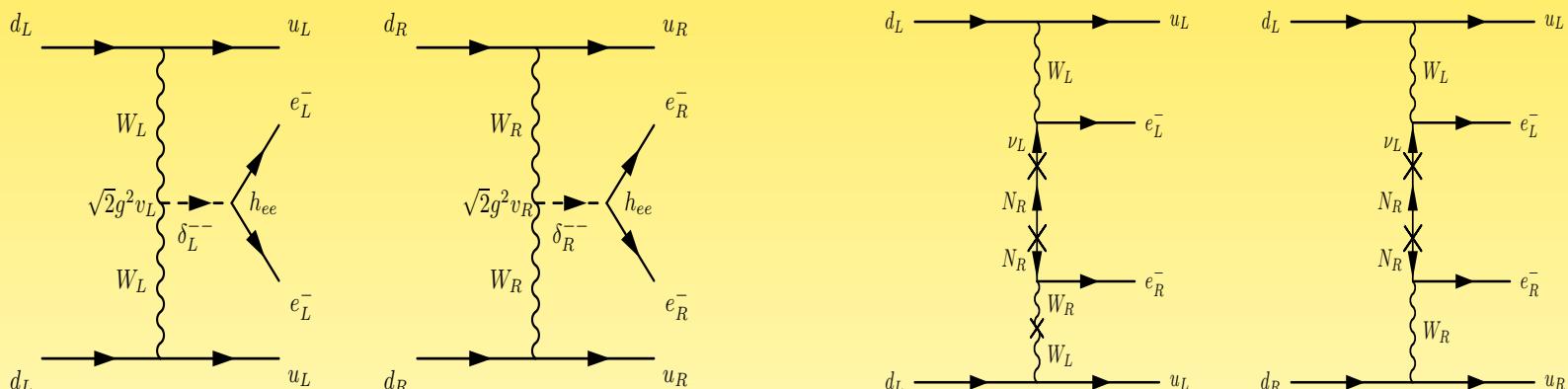
Left-right symmetry



$$U_{ei}^2 m_i$$

$$\frac{S_{ei}^2}{M_i}$$

$$\frac{V_{ei}^2}{M_{W_R}^4 M_i}$$



$$\frac{U_{ei}^2 m_i}{M_{\Delta_L}^2}$$

$$\frac{V_{ei}^2 M_i}{M_{W_R}^4 M_{\Delta_R}^2}$$

$$U_{ei} T_{ei} \tan \zeta$$

$$\frac{U_{ei} T_{ei}}{M_{W_R}^2}$$

Predictions of $SO(10)$ theories

Yukawa structure of $SO(10)$ models depends on Higgs representations

$$10_H \ (\leftrightarrow \textcolor{blue}{H}), \overline{126}_H \ (\leftrightarrow \textcolor{blue}{F}), \ 120_H \ (\leftrightarrow \textcolor{blue}{G})$$

Gives relation for mass matrices:

$$m_{\text{up}} \propto r(H + sF + it_u G)$$

$$m_{\text{down}} \propto H + F + iG$$

$$m_D \propto r(H - 3sF + it_D G)$$

$$m_\ell \propto H - 3F + it_l G$$

$$M_R \propto r_R^{-1} F$$

Numerical fit including RG, Higgs, θ_{13}

$10_H + \overline{126}_H$: 19 free parameters

$10_H + \overline{126}_H + 120_H$: 18 free parameters

20 (19) observables to be fitted

Predictions of $SO(10)$ theories

Model	Fit	$ m_{ee} $ [meV]	m_0 [meV]	M_3 [GeV]	χ^2
$10_H + \overline{126}_H$	NH	0.49	2.40	3.6×10^{12}	23.0
$10_H + \overline{126}_H + SS$	NH	0.44	6.83	1.1×10^{12}	3.29
<hr/>					
$10_H + \overline{126}_H + 120_H$	NH	2.87	1.54	9.9×10^{14}	11.2
$10_H + \overline{126}_H + 120_H + SS$	NH	0.78	3.17	4.2×10^{13}	6.9×10^{-6}
<hr/>					
$10_H + \overline{126}_H + 120_H$	IH	35.52	30.2	1.1×10^{13}	13.3
$10_H + \overline{126}_H + 120_H + SS$	IH	24.22	12.0	1.2×10^{13}	0.6

Dueck, W.R., JHEP 1309

Recent Results

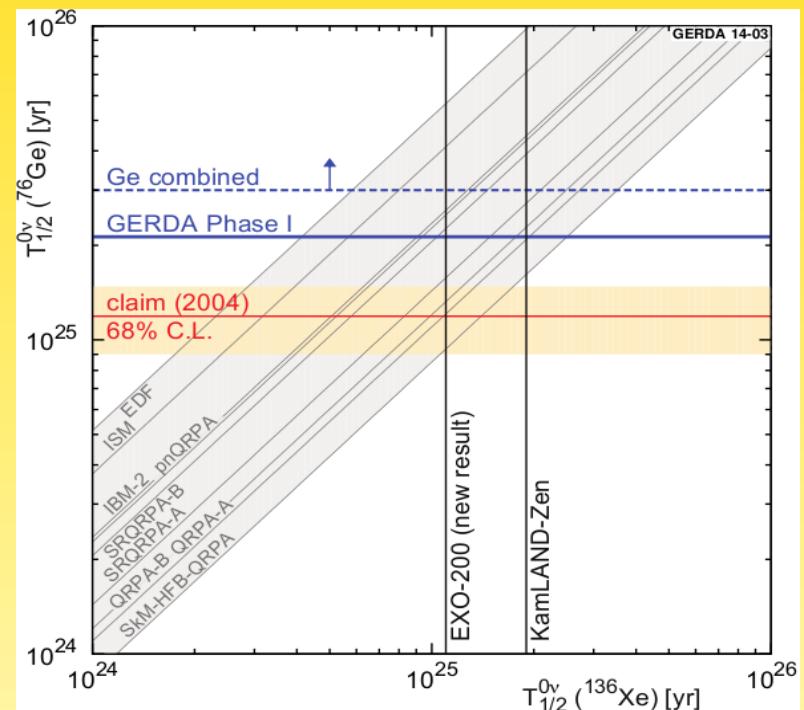
- $^{76}\text{Ge}:$
 - GERDA: $T_{1/2} > 2.1 \times 10^{25}$ yrs
 - GERDA + IGEX + HDM: $T_{1/2} > 3.0 \times 10^{25}$ yrs
- $^{136}\text{Xe}:$
 - EXO-200: $T_{1/2} > 1.1 \times 10^{25}$ yrs (**first run with less exposure**: $T_{1/2} > 1.6 \times 10^{25}$ yrs. . .)
 - KamLAND-Zen: $T_{1/2} > 2.6 \times 10^{25}$ yrs

Xe-limit is stronger than Ge-limit when:

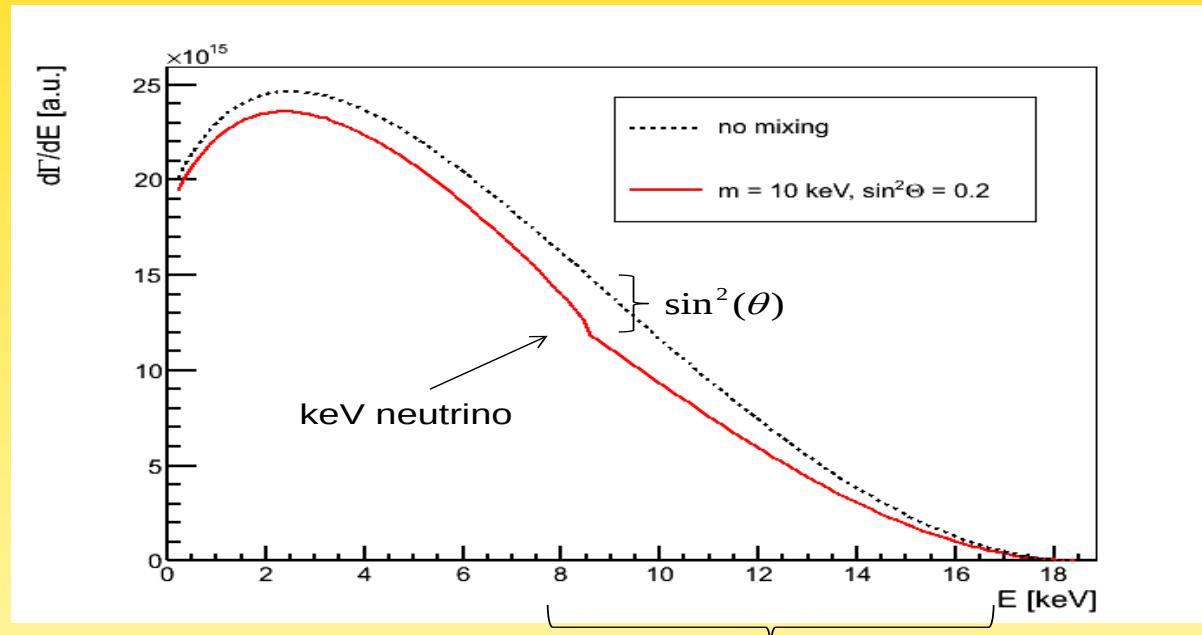
$$T_{\text{Xe}} > T_{\text{Ge}} \frac{G_{\text{Ge}}}{G_{\text{Xe}}} \left| \frac{\mathcal{M}_{\text{Ge}}}{\mathcal{M}_{\text{Xe}}} \right|^2 \text{ yrs}$$

Current new limits on $|m_{ee}|$ (post KamLAND-Zen)

NME	^{76}Ge		^{136}Xe	
	GERDA	comb	KLZ	comb
EDF(U)	0.32	0.27	0.06	—
ISM(U)	0.52	0.44	0.12	—
IBM-2	0.27	0.23	0.08	—
pnQRPA(U)	0.28	0.24	0.08	—
SRQRPA-A	0.31	0.26	0.11	—
QRPA-A	0.28	0.24	0.12	—
SkM-HFB-QRPA	0.29	0.24	0.15	—



Imprint of keV neutrinos on β -spectrum

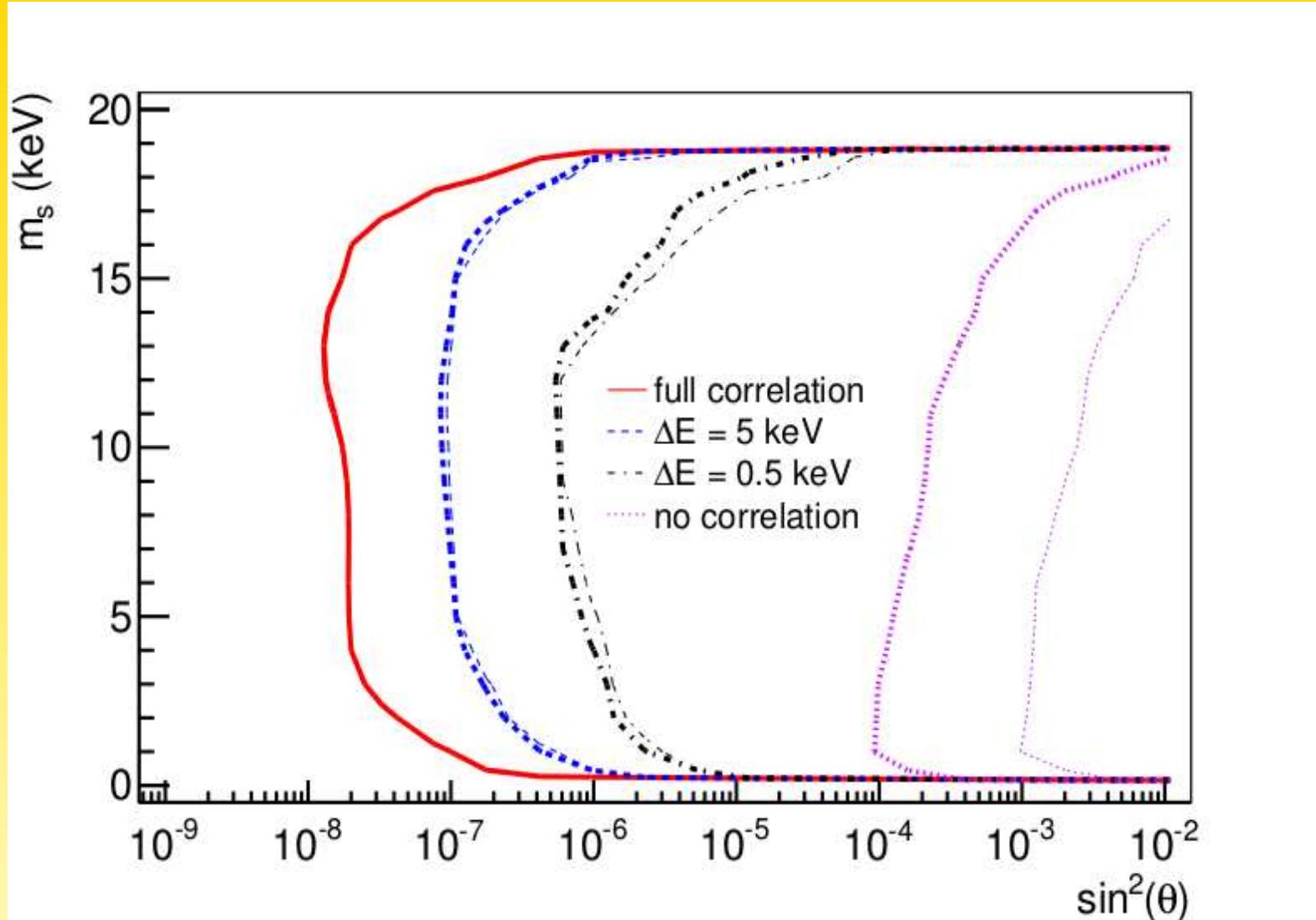


Susanne Mertens

13

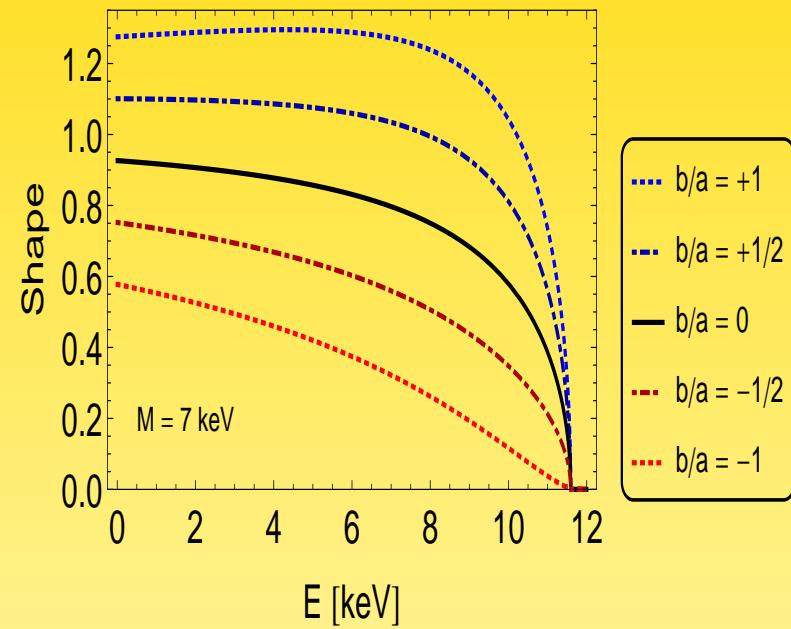
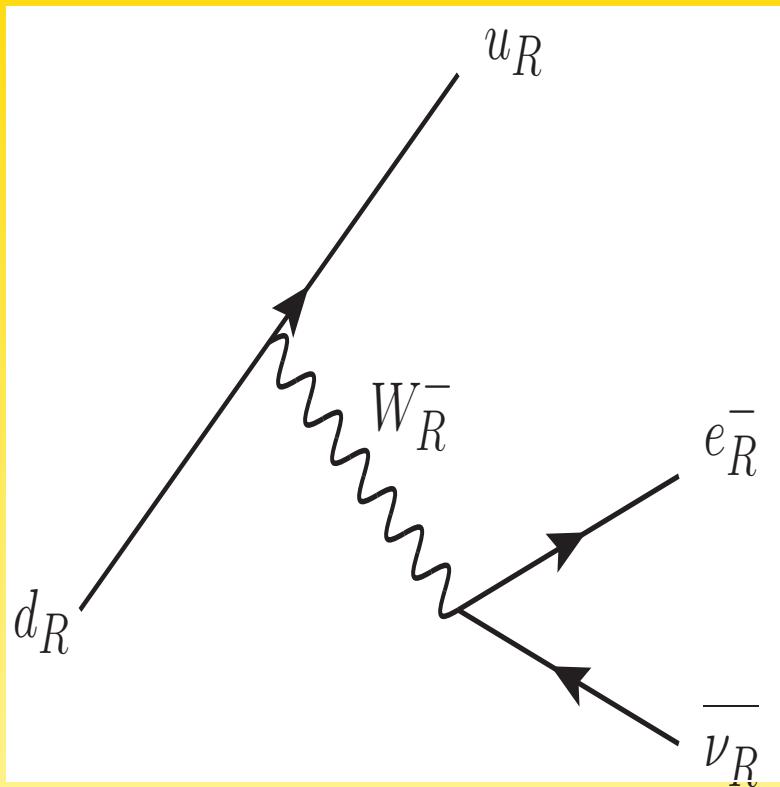


Mertens *et al.*, 1409.0920



⇒ mixing down to 10^{-7} in reach!?

Focus for simplicity on



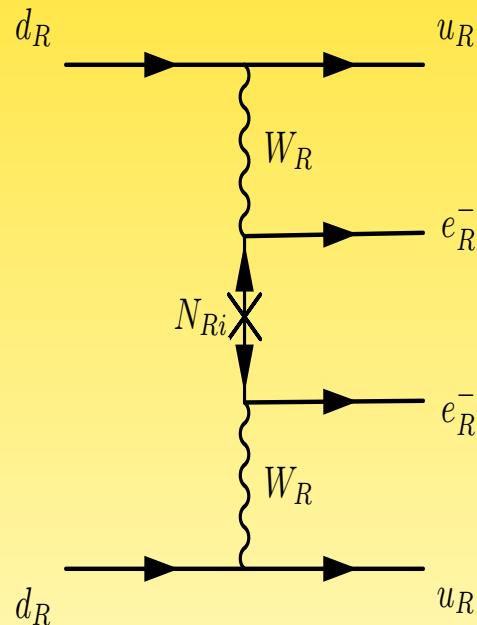
and assume keV neutrino with RH current

$$\frac{d\Gamma/dE - (d\Gamma/dE)_{\text{std}}}{(d\Gamma/dE)_{\text{std}}} \simeq \left(a + b \frac{M}{E_0 - E} \right) \sqrt{1 - \frac{M^2}{(E_0 - E)^2}} \Theta(E_0 - E - M)$$

neglect interference term b :

$$\theta_{\text{eff}}^2 \simeq |S_{ej}|^2 + 1.1 \times 10^{-6} |V_{ej}|^2 \left(\frac{2.5 \text{ TeV}}{m_{W_R}} \right)^4$$

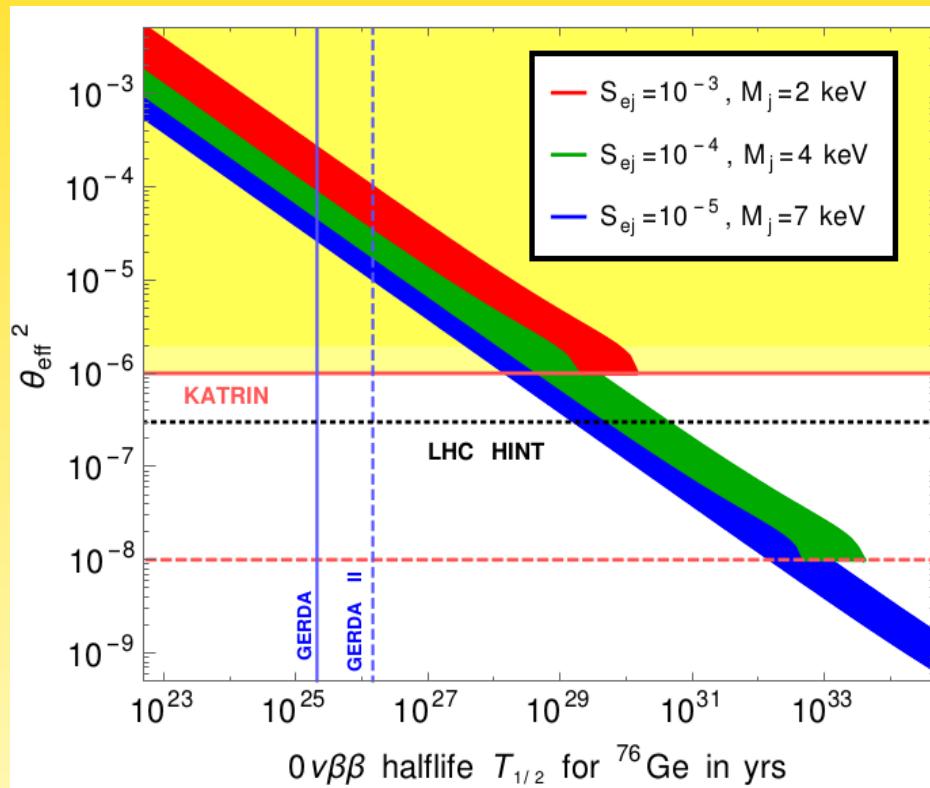
and note that M does $0\nu\beta\beta$ with amplitude $\propto |V_{ej}|^2 (m_W/m_{W_R})^4 M/q^2$



\Rightarrow connection to $0\nu\beta\beta$ constraints!

connection to $0\nu\beta\beta$ constraints:

$$\theta_{\text{eff}}^2 = |S_{ej}|^2 + \frac{m_e}{M_j} \left[|\mathcal{M}_\nu^{0\nu}|^{-2} (G_{01}^{0\nu})^{-1} (T_{1/2}^{0\nu})^{-1} - |S_{ej}^2 M_j / m_e|^2 \right]^{\frac{1}{2}}$$



Barry, Heeck, W.R., 1404.5955

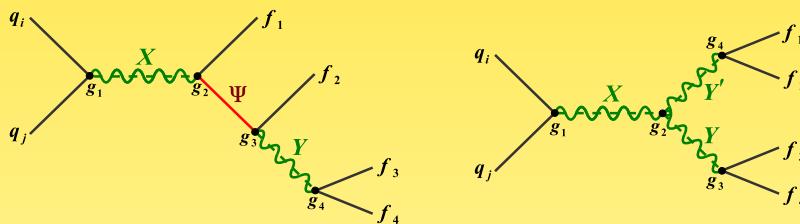
How the additional interactions save the day

- double beta decay without RHC: $\theta^2 M = 7 \times 10^{-10} \text{ keV} = 70 \mu\text{eV}$
- double beta decay with RHC: $(m_{W_L}/m_{W_R})^4 |V_{ei}|^2 M = 8 \text{ meV}$
- decay: $\frac{\Gamma_{\text{RHC}}(N_j \rightarrow \bar{\nu}\gamma)}{\Gamma_{\text{SM}}(N_j \rightarrow \nu\gamma)} \simeq \frac{m_{W_L}^4 |S_{ei}|^2}{m_{W_R}^4 |T_{ei}|^2} \simeq \frac{m_{W_L}^4}{m_{W_R}^4}$
- beta decay: $\theta_{\text{eff}}^2 \simeq |S_{ej}|^2 + 1.1 \times 10^{-6} |V_{ej}|^2 \left(\frac{2.5 \text{ TeV}}{m_{W_R}}\right)^4 > |S_{ej}|^2$

Observation of LNV at LHC implies washout effects in early Universe!

Example TeV-scale W_R : leading to washout $e_R^\pm e_R^\pm \rightarrow W_R^\pm W_R^\pm$ and $e_R^\pm W_R^\mp \rightarrow e_R^\mp W_R^\pm$. Further, $e_R^\pm W_R^\mp \rightarrow e_R^\mp W_R^\pm$ stays long in equilibrium
 (Frere, Hambye, Vertongen; Bhupal Dev, Lee, Mohapatra; U. Sarkar *et al.*)

More model-independent (Deppisch, Harz, Hirsch):



$$\text{washout: } \log_{10} \frac{\Gamma_W(qq \rightarrow \ell^+ \ell^+ qq)}{H} \gtrsim 6.9 + 0.6 \left(\frac{M_X}{\text{TeV}} - 1 \right) + \log_{10} \frac{\sigma_{\text{LHC}}}{\text{fb}}$$

(TeV- $0\nu\beta\beta$, LFV and Y_B : Deppisch, Harz, Huang, Hirsch, Päs)

\leftrightarrow post-Sphaleron mechanisms, τ flavor effects,...