

# XII Quark Confinement & the Hadron Spectrum



X, Y, Z States

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# Lots of X, Y and Z states observed by BaBar, Belle, BESIII, CDF, CLEOIII, CLEO-c, CMS, D0 and LHCb Collaborations

N. Branbilla et al., arXiv:1404.3723

State	$M$ , MeV	$\Gamma$ , MeV	$J^{PC}$	Process (mode)	Experiment ( $\# \sigma$ )	Year	Status
$X(3872)$	$3871.68 \pm 0.17$	$< 1.2$	$1^{++}$	$B \rightarrow K(\pi^+\pi^-J/\psi)$ $p\bar{p} \rightarrow (\pi^+\pi^-J/\psi) \dots$ $pp \rightarrow (\pi^+\pi^-J/\psi) \dots$ $B \rightarrow K(\pi^+\pi^-\pi^0J/\psi)$ $B \rightarrow K(\gamma J/\psi)$  $B \rightarrow K(\gamma\psi(2S))$	Belle [810, 1030] ( $>10$ ), BaBar [1031] (8.6) CDF [1032, 1033] (11.6), D0 [1034] (5.2) LHCb [1035, 1036] (np) Belle [1037] (4.3), BaBar [1038] (4.0) Belle [1039] (5.5), BaBar [1040] (3.5) LHCb [1041] ( $>10$ ) BaBar [1040] (3.6), Belle [1039] (0.2) LHCb [1041] (4.4)	2003	Ok
$Z_c(3885)^+$	$3883.9 \pm 4.5$	$25 \pm 12$	$1^{+-}$	$Y(4260) \rightarrow \pi^-(D\bar{D}^*)^+$	Belle [1042] (6.4), BaBar [1043] (4.9) BES III [1044] (np)	2006	Ok
$Z_c(3900)^+$	$3891.2 \pm 3.3$	$40 \pm 8$	$?^{? -}$	$Y(4260) \rightarrow \pi^-(\pi^+J/\psi)$	BES III [1045] (8), Belle [1046] (5.2) T. Xiao <i>et al.</i> [CLEO data] [1047] ( $>5$ )	2013	NC!
$Y(3915)$	$3918.4 \pm 1.9$	$20 \pm 5$	$0/2^{?+}$	$B \rightarrow K(\omega J/\psi)$ $e^+e^- \rightarrow e^+e^-(\omega J/\psi)$	Belle [1088] (8), BaBar [1038, 1089] (19) Belle [1090] (7.7), BaBar [1091] (7.6)	2004	Ok
$\chi_{c2}(2P)$	$3927.2 \pm 2.6$	$24 \pm 6$	$2^{++}$	$e^+e^- \rightarrow e^+e^-(D\bar{D})$	Belle [1092] (5.3), BaBar [1093] (5.8)	2005	Ok
$X(3940)$	$3942_{-8}^{+9}$	$37_{-17}^{+27}$	$?^{?+}$	$e^+e^- \rightarrow J/\psi(D\bar{D}^*)$	Belle [1086, 1087] (6)	2005	NC!
$Y(4008)$	$3891 \pm 42$	$255 \pm 42$	$1^{--}$	$e^+e^- \rightarrow (\pi^+\pi^-J/\psi)$	Belle [1046, 1094] (7.4)	2007	NC!
$Z_c(4020)^+$	$4022.9 \pm 2.8$	$7.9 \pm 3.7$	$?^{? -}$	$Y(4260, 4360) \rightarrow \pi^-(\pi^+h_c)$	BES III [1048] (8.9)	2013	NC!
$Z_c(4025)^+$	$4026.3 \pm 4.5$	$24.8 \pm 9.5$	$?^{? -}$	$Y(4260) \rightarrow \pi^-(D^*\bar{D}^*)^+$	BES III [1049] (10)	2013	NC!
$\psi(4040)$	$4039 \pm 1$	$80 \pm 10$	$1^{--}$	$e^+e^- \rightarrow (D^{(*)}\bar{D}^{(*)}(\pi))$ $e^+e^- \rightarrow (\eta J/\psi)$	PDG [1] Belle [1095] (6.0)	1978	Ok
$Z(4050)^+$	$4051_{-43}^{+24}$	$82_{-55}^{+51}$	$?^{?+}$	$\bar{B}^0 \rightarrow K^-(\pi^+\chi_{c1})$	Belle [1096] (5.0), BaBar [1097] (1.1)	2008	NC!
$Y(4140)$	$4145.8 \pm 2.6$	$18 \pm 8$	$?^{?+}$	$B^+ \rightarrow K^+(\phi J/\psi)$	CDF [1098] (5.0), Belle [1099] (1.9), LHCb [1100] (1.4), CMS [1101] ( $>5$ ) D0 [1102] (3.1)	2009	NC!

$\psi(4160)$	$4153 \pm 3$	$103 \pm 8$	$1^{--}$	$e^+ e^- \rightarrow (D^{(*)} \bar{D}^{(*)})$ $e^+ e^- \rightarrow (\eta J/\psi)$	PDG [1]	1978	Ok
$X(4160)$	$4156^{+29}_{-25}$	$139^{+113}_{-65}$	$?^{?+}$	$e^+ e^- \rightarrow J/\psi (D^* \bar{D}^*)$	Belle [1095] (6.5)	2013	NC!
$Z(4200)^+$	$4196^{+35}_{-30}$	$370^{+99}_{-110}$	$1^{+-}$	$\bar{B}^0 \rightarrow K^- (\pi^+ J/\psi)$	Belle [1087] (5.5)	2007	NC!
$Z(4250)^+$	$4248^{+185}_{-45}$	$177^{+321}_{-72}$	$?^{?+}$	$\bar{B}^0 \rightarrow K^- (\pi^+ \chi_{c1})$	Belle [1103] (7.2)	2014	NC!
$Y(4260)$	$4250 \pm 9$	$108 \pm 12$	$1^{--}$	$e^+ e^- \rightarrow (\pi\pi J/\psi)$	Belle [1096] (5.0), BaBar [1097] (2.0)	2008	NC!
				$e^+ e^- \rightarrow (f_0(980)J/\psi)$	BaBar [1104] [1105] (8), CLEO [1106] [1107] (11)	2005	Ok
				$e^+ e^- \rightarrow (\pi^- Z_c(3900)^+)$	Belle [1046] [1094] (15), BES III [1045] (np)		
				$e^+ e^- \rightarrow (\gamma X(3872))$	BaBar [1105] (np), Belle [1046] (np)	2012	Ok
$Y(4274)$	$4293 \pm 20$	$35 \pm 16$	$?^{?+}$	$B^+ \rightarrow K^+ (\phi J/\psi)$	BES III [1045] (8), Belle [1046] (5.2)	2013	Ok
					BES III [1108] (5.3)	2013	NC!
					CDF [1098] (3.1), LHCb [1100] (1.0), CMS [1101] (>3), D0 [1102] (np)	2011	NC!
$X(4350)$	$4350.6^{+4.6}_{-5.1}$	$13^{+18}_{-10}$	$0/2^{?+}$	$e^+ e^- \rightarrow e^+ e^- (\phi J/\psi)$	Belle [1109] (3.2)	2009	NC!
$Y(4360)$	$4354 \pm 11$	$78 \pm 16$	$1^{--}$	$e^+ e^- \rightarrow (\pi^+ \pi^- \psi(2S))$	Belle [1110] (8), BaBar [1111] (np)	2007	Ok
$Z(4430)^+$	$4458 \pm 15$	$166^{+37}_{-32}$	$1^{+-}$	$\bar{B}^0 \rightarrow K^- (\pi^+ \psi(2S))$	Belle [1112] [1113] (6.4), BaBar [1114] (2.4)	2007	Ok
					LHCb [1115] (13.9)		
				$\bar{B}^0 \rightarrow K^- (\pi^+ J/\psi)$	Belle [1103] (4.0)	2014	NC!
$X(4630)$	$4634^{+9}_{-11}$	$92^{+41}_{-32}$	$1^{--}$	$e^+ e^- \rightarrow (\Lambda_c^+ \bar{\Lambda}_c^-)$	Belle [1116] (8.2)	2007	NC!
$Y(4660)$	$4665 \pm 10$	$53 \pm 14$	$1^{--}$	$e^+ e^- \rightarrow (\pi^+ \pi^- \psi(2S))$	Belle [1110] (5.8), BaBar [1111] (5)	2007	Ok

in 2014: 23 new states, many not confirmed  
many candidates for exotic states

up to now: 9 reported charged states  
which are not quark-antiquark states

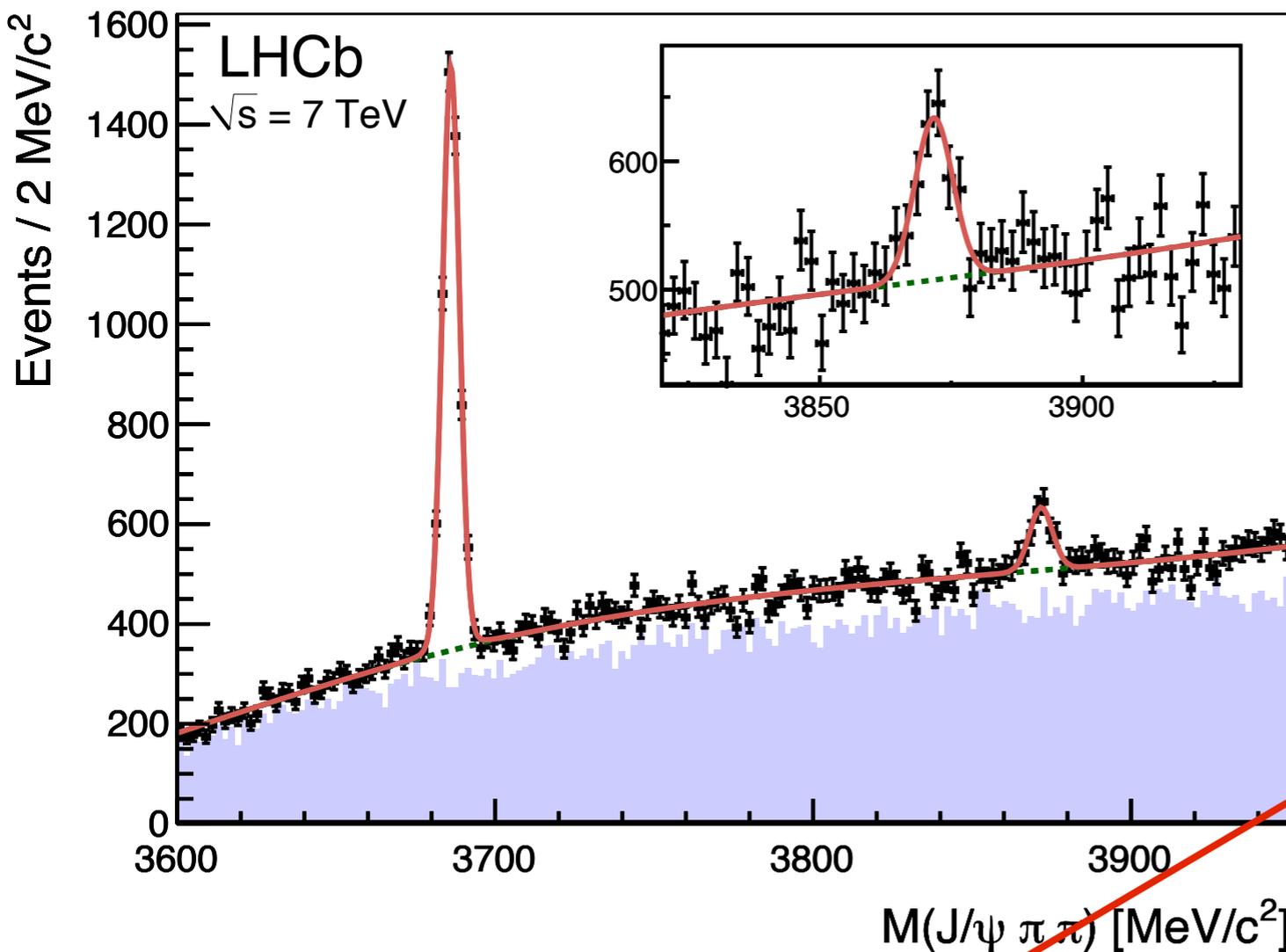
 <p><math>Z^+(4430)</math> 2007</p>	 <p><math>Z_1^+(4050)</math> 2008</p>	 <p><math>Z_2^+(4250)</math> 2008</p>
  		
<p>BES III</p> <p><math>Z_c^+(3900)</math> 2013</p> 	<p><math>Z_c^+(4025)</math> 2013</p> <p>BES III</p>	<p><math>Z_c^+(4020)</math> 2013</p> <p>BES III</p>
<p><math>Z_c^+(3885)</math> 2013</p> <p>BES III</p>	<p><math>Z_c^+(4200)</math> 2014</p> 	<div style="border: 2px dashed orange; padding: 5px;">  <p><math>X^+(5568)</math> 2016</p>   </div>

not a charmonium state ←

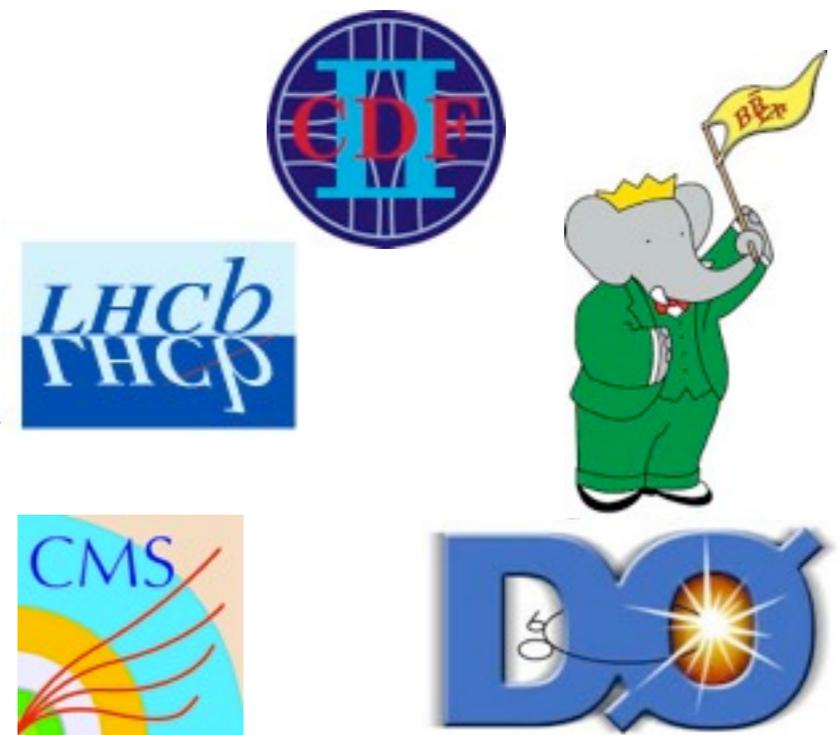
# X(3872) @ KEK (PRL91(2003))

very narrow state observed in the decay:  $B^\pm \rightarrow K^\pm (J/\psi \pi^+ \pi^-)$

best studied charmonium exotic candidate



$M_X = (3872.20 \pm 0.39) \text{ MeV}$   
 $\Gamma < 2.3 \text{ MeV}$



$c\bar{c}$  spec. for  $J^{PC} = 1^{++}$  (Barnes & Godfrey, PRD69 (2004))

- $2^3 P_1$  (3990)
- $3^3 P_1$  (4290)

$$\frac{X \rightarrow J/\psi \pi^+ \pi^- \pi^0}{X \rightarrow J/\psi \pi^+ \pi^-} = 0.8 \pm 0.3 \Rightarrow \text{strong isospin and G parity violation}$$

$$M(D^{*0} \bar{D}^0) = (3871 \pm 1)$$

X(3872): molecular  $(D^{*0} \bar{D}^0 + \bar{D}^{*0} D^0)$  state (Swanson, Close, Voloshin, Wong ...)

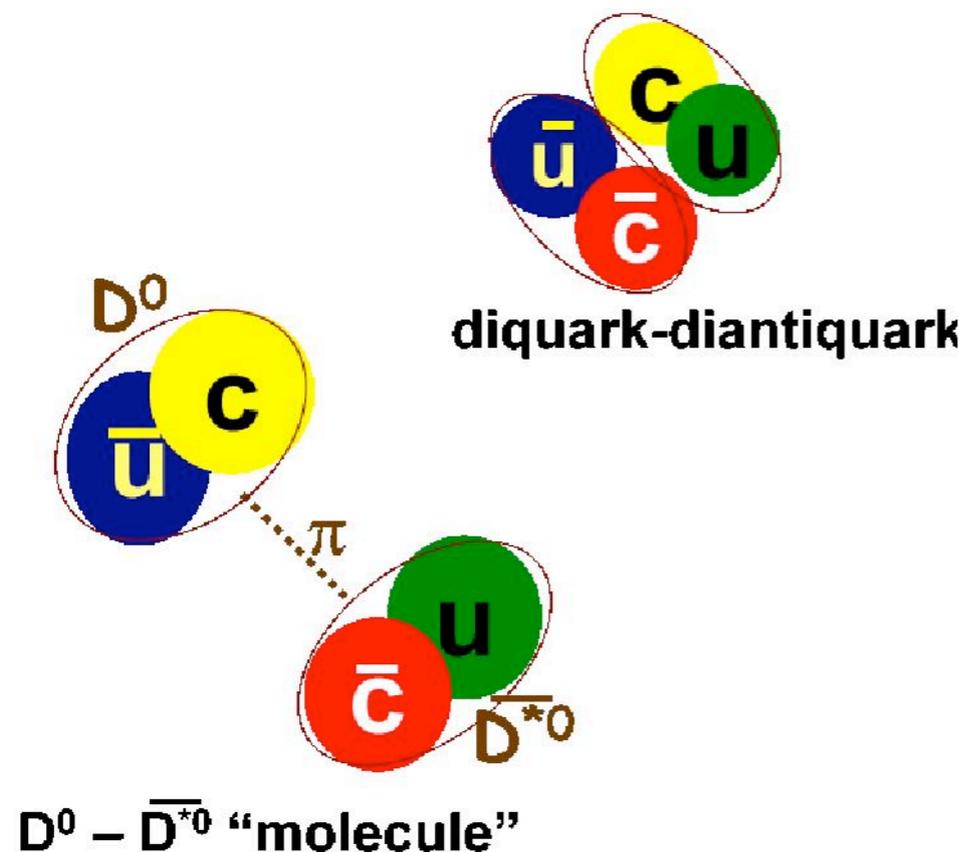
Maiani et al. (PRD71 (05)) tetraquark  $J^{PC} = 1^{++}$  state

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molecular and tetraquark interpretations differ by the way quarks are organized in the state

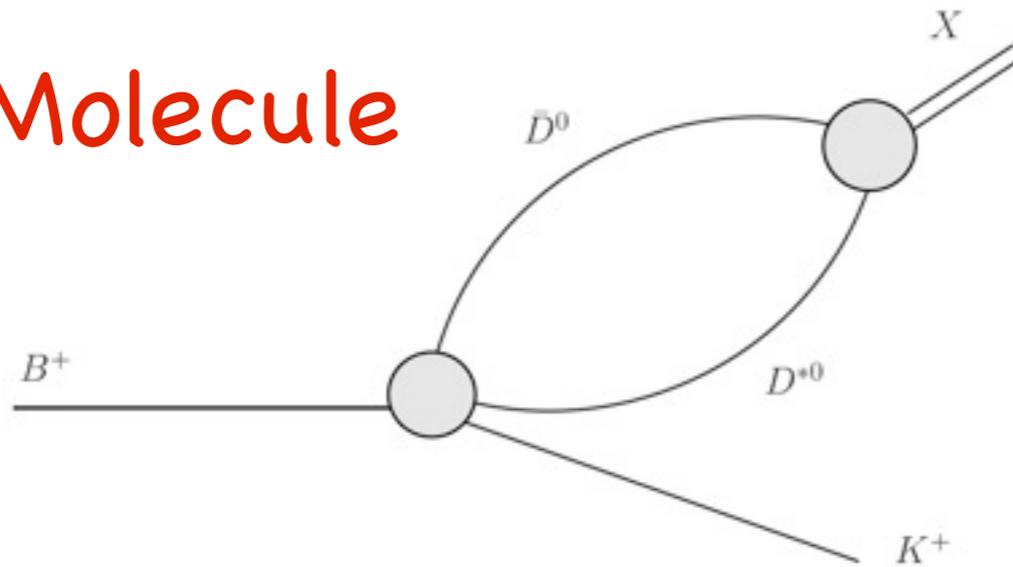
# X(3872) production

B decays at B factories



$$B^{\pm} \rightarrow X(3872)K^{\pm}$$

Meson Molecule



Meson coalescence

Small binding energy

Agreement with data !

E. Braaten, M. Kusunoki, hep-ph/0404161

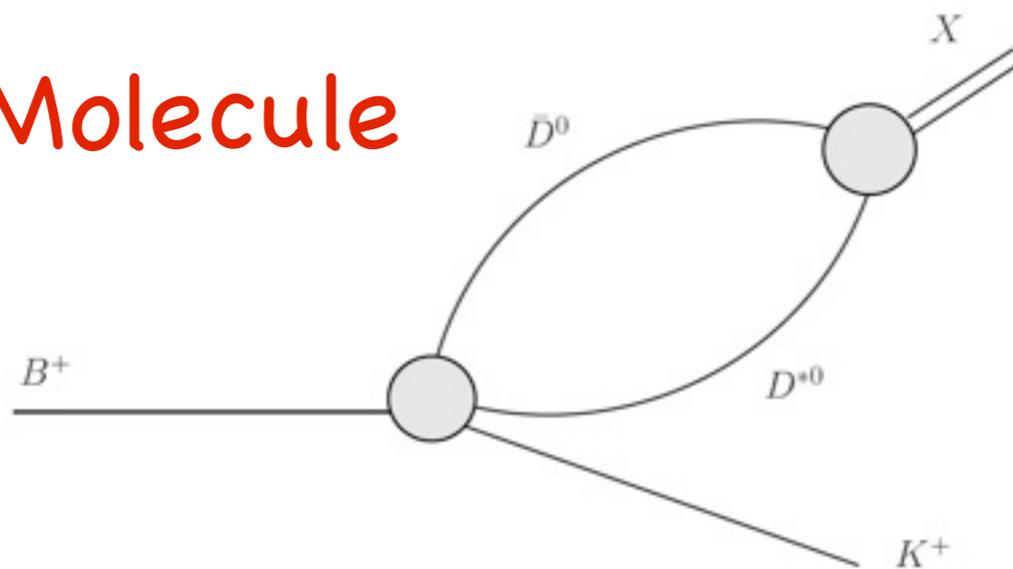
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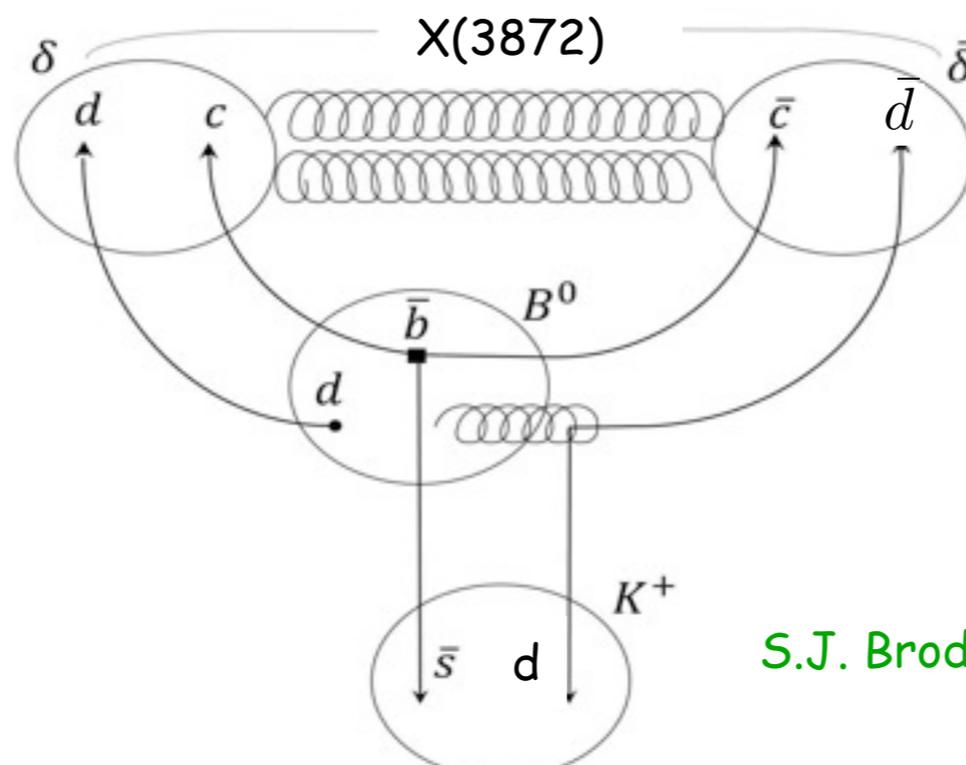
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Tetraquark



Diquark-antidiquark picture

Non-relativistic potential

Agreement with data !

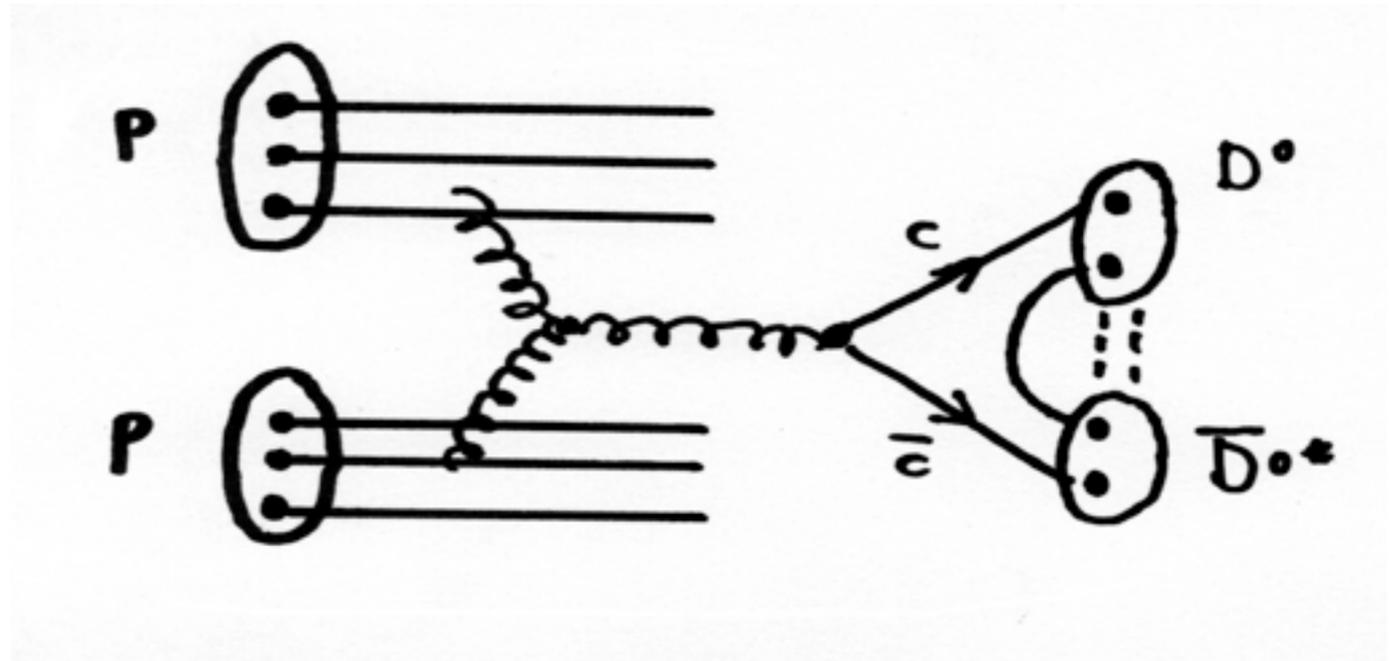
S.J. Brodsky, D.S. Hwang, R.F. Lebed, arXiv:1406.7281

# Proton - (anti)Proton



$$\sigma_{\text{exp}} = 30 \text{ nb (CMS)}$$

Meson molecule



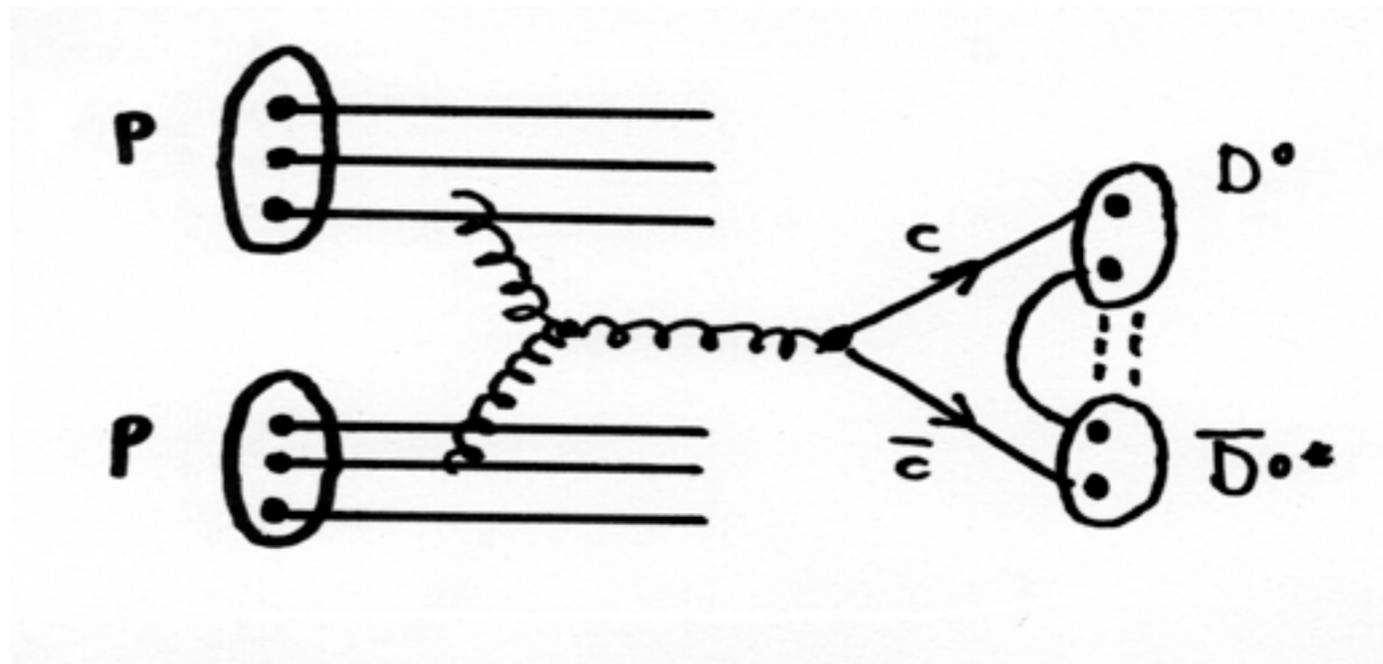
How can a molecule, with small binding energy, be produced in high energy collision with large cross section?

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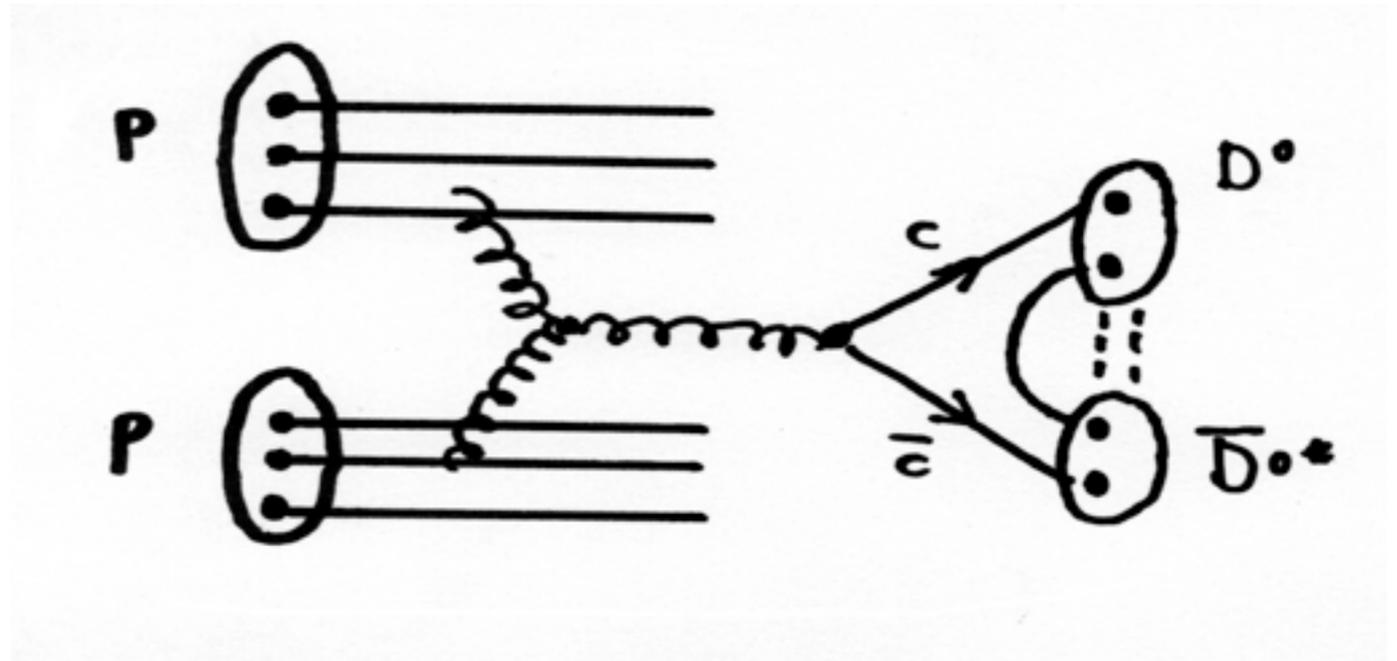
theoretical estimates + MC  $\rightarrow$  production cross section smaller by factor 300! (Bignamini et. al., PRL103(09)162001) Problem for molecular approach

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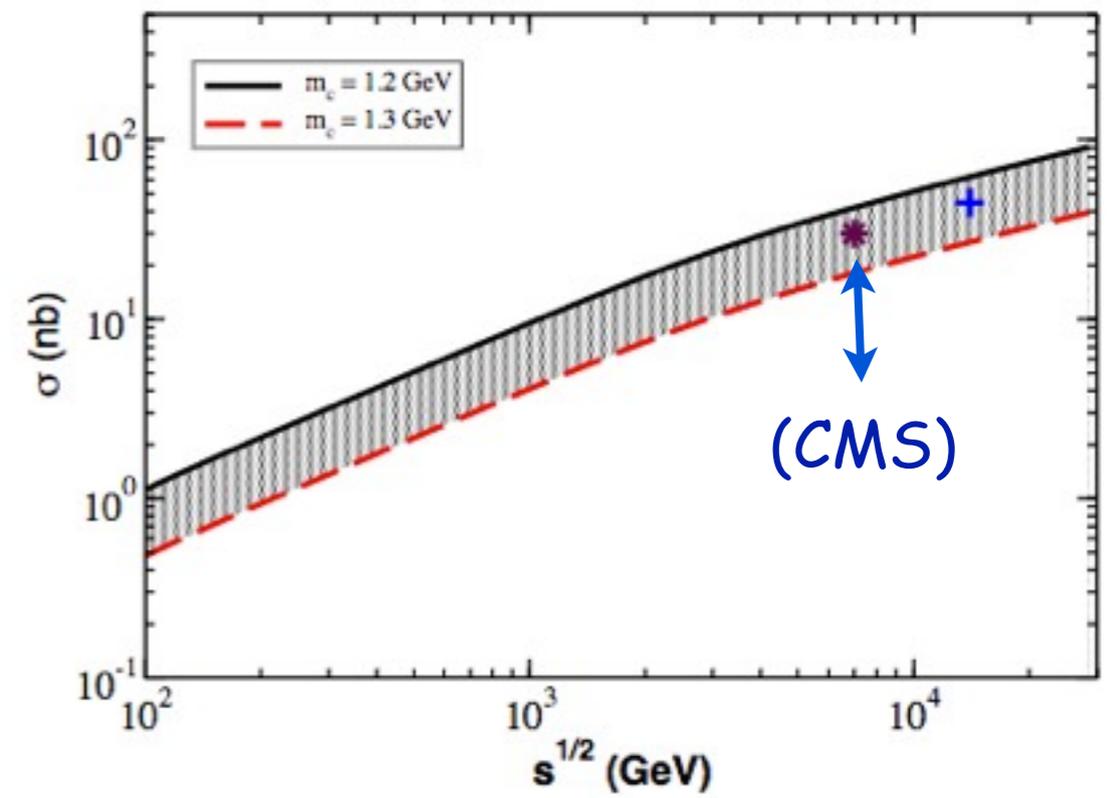
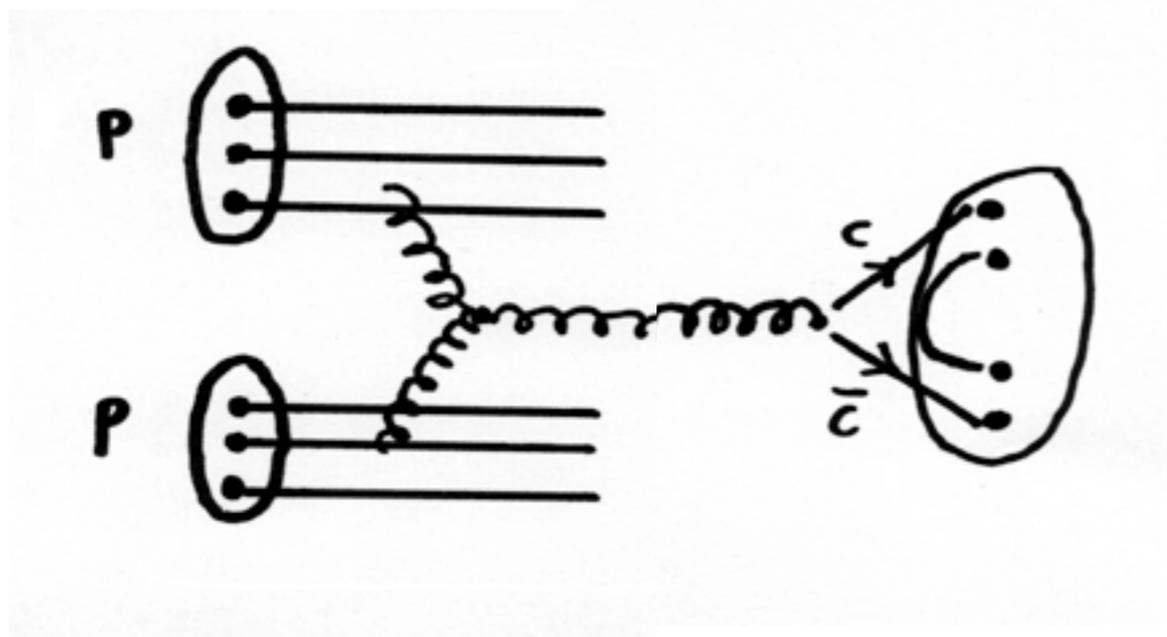


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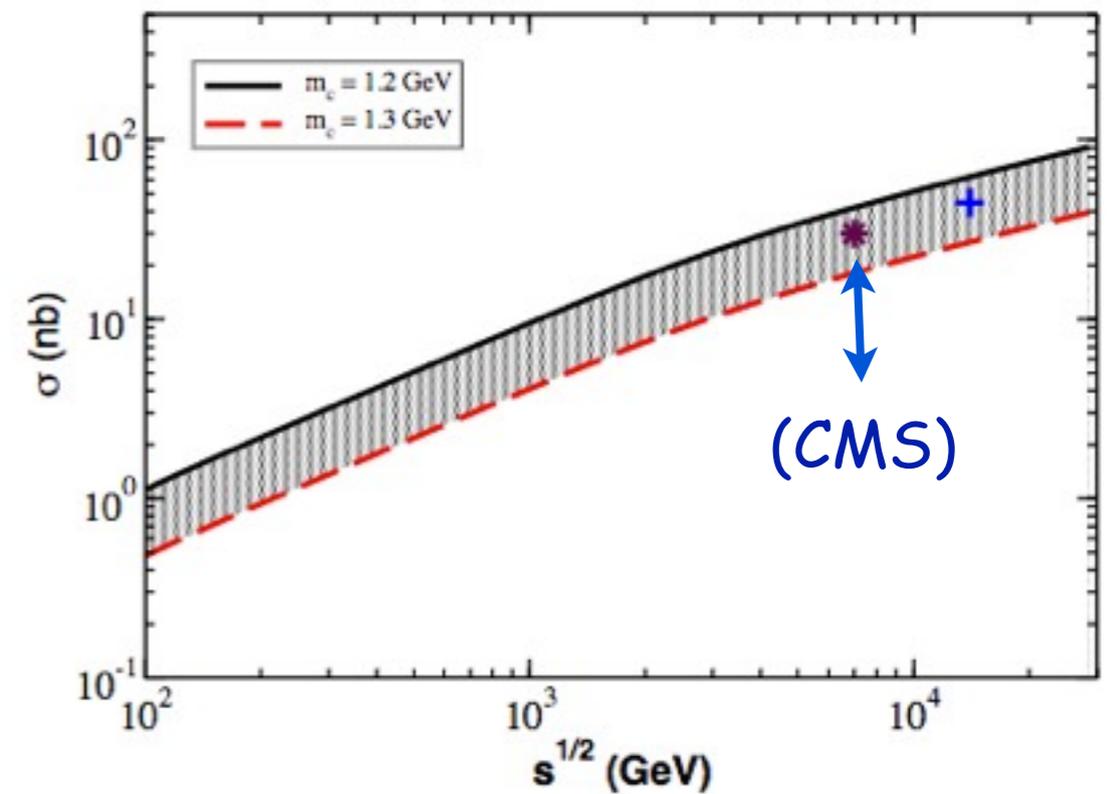
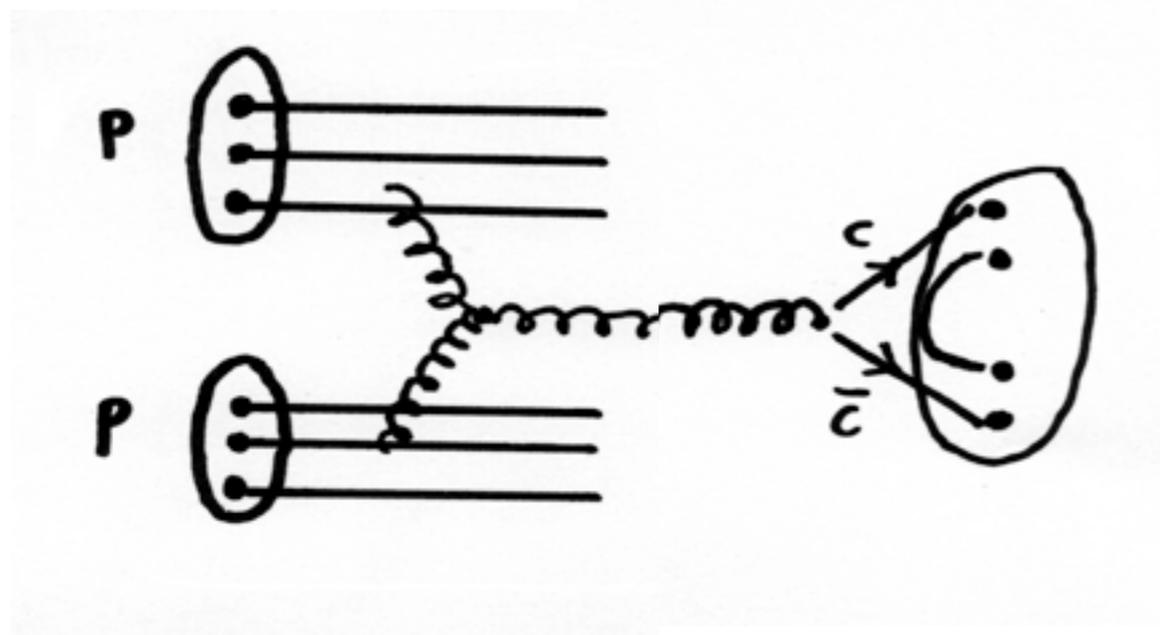
NRQCD plus rescattering in the final state: molecular approach can describe the CDF data ! P. Artoisenet, E. Braaten, arXiv:0911.2016

# Tetraquark



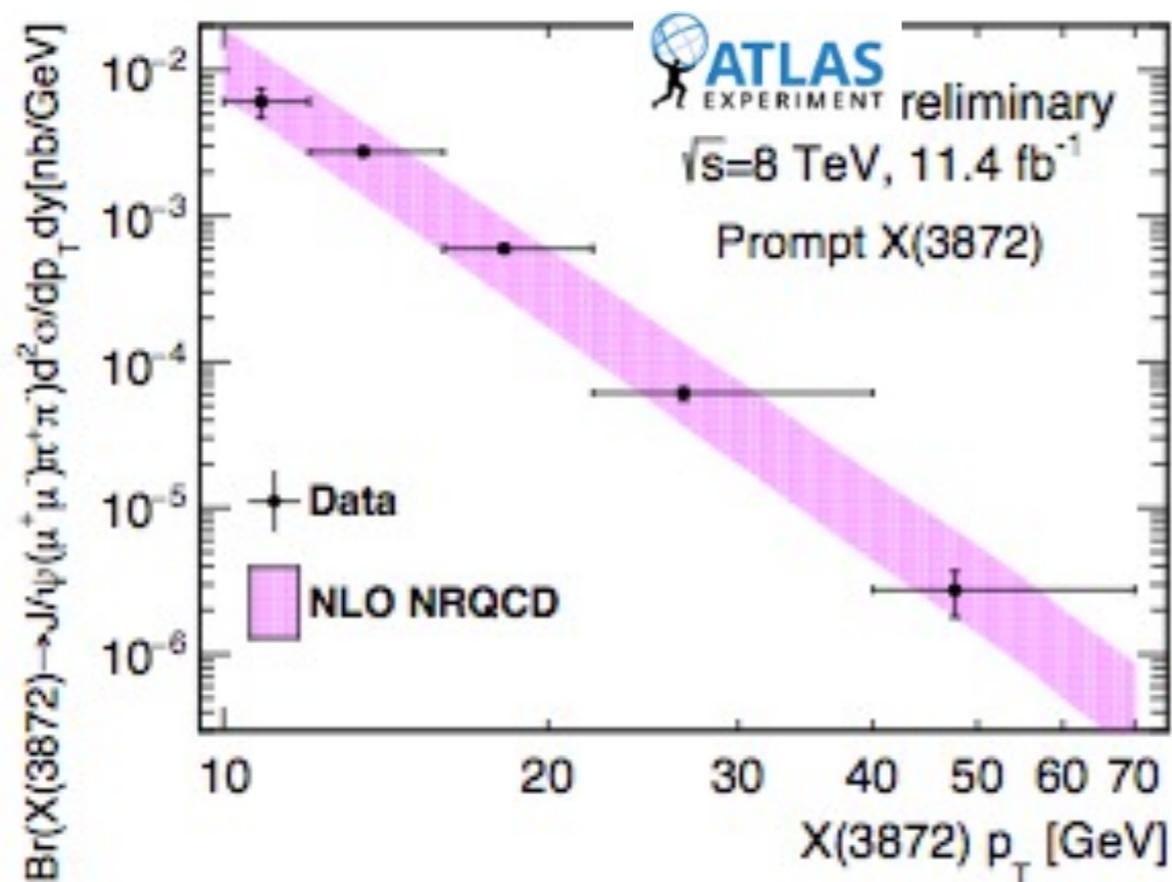
parameters fixed to reproduce CMS data  
(Carvalho et al., arXiv:1511.05209)

# Tetraquark



parameters fixed to reproduce CMS data

(Carvalho et al., arXiv:1511.05209)



The X(3872) is modeled as a mixture of a  $\chi_{c1}(2P)$  and a  $\bar{D}^0 D^{*0}$  molecular state.

from K. Toms talk ICHEP16

Theoretical calculation from Meng et al., arXiv:1304.6710

# QCD Sum Rule

**Fundamental Assumption: Principle of Duality**

$$\Pi(q) = i \int d^4x e^{iq \cdot x} \langle 0 | T[j(x)j^\dagger(0)] | 0 \rangle$$

Theoretical side

- quarks and gluons degrees of freedom
- Operator Product Expansion of the correlator

Phenomenological side

- hadronic degrees of freedom
- Spectral representation for the correlator

$$\Pi^{phen}(Q^2) \leftrightarrow \Pi^{OPE}(Q^2)$$



valid at small  $Q^2$



valid at large  $Q^2$



Borel transform

$$\lambda^2 e^{-m^2/M^2} = \int_{s_{min}}^{s_0} ds e^{-s/M^2} \rho^{OPE}(s)$$

$s_0$ : continuum parameter

$$\Pi^{phen}(Q^2) \leftrightarrow \Pi^{OPE}(Q^2)$$

valid at small  $Q^2$

valid at large  $Q^2$

Borel transform

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$s_0$ : continuum parameter

Good Sum Rule  $\Rightarrow$  Borel window such that:

- pole contribution  $>$  continuum contribution
- good OPE convergence
- good Borel stability

# QCD sum rules calculation for $X(3872)$

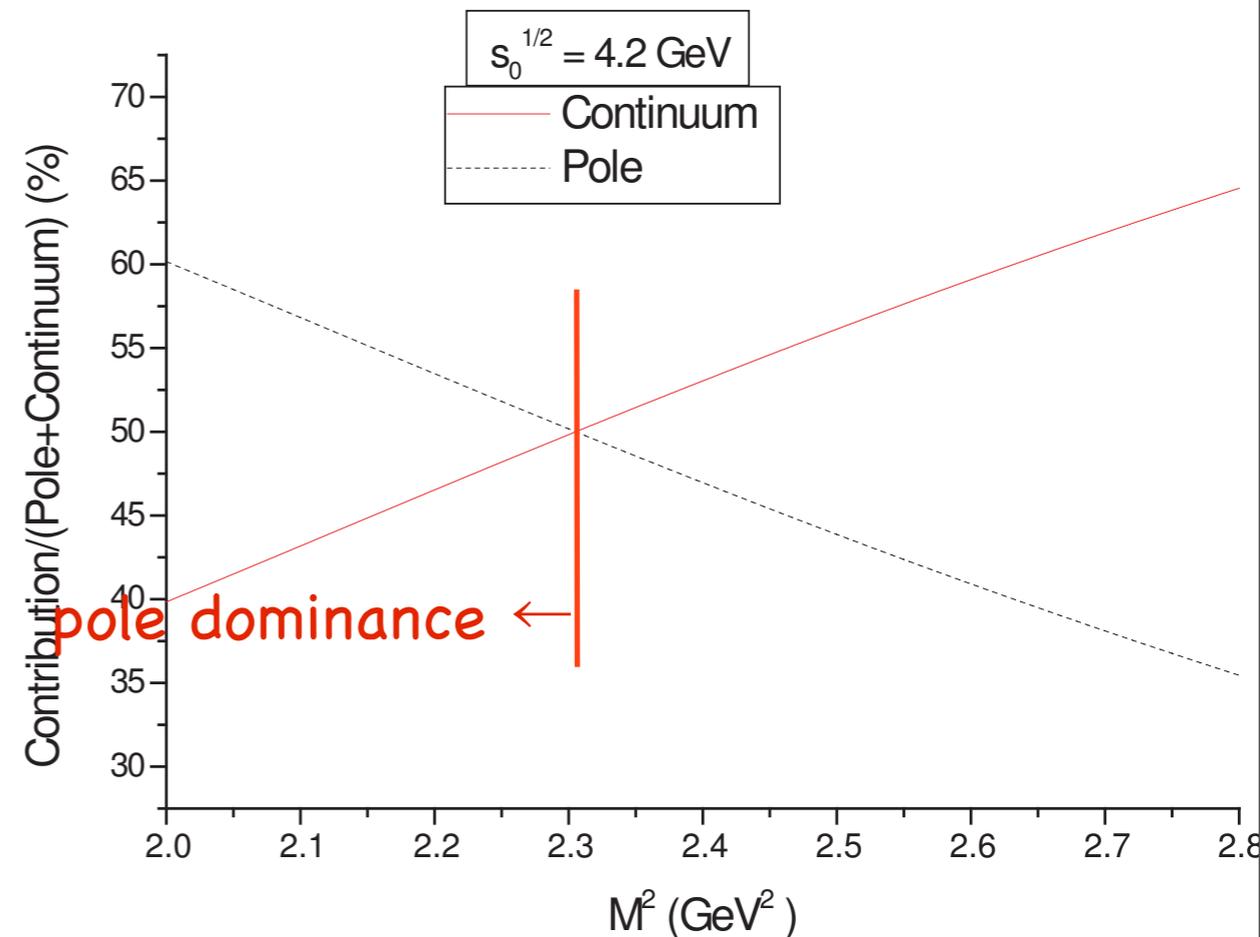
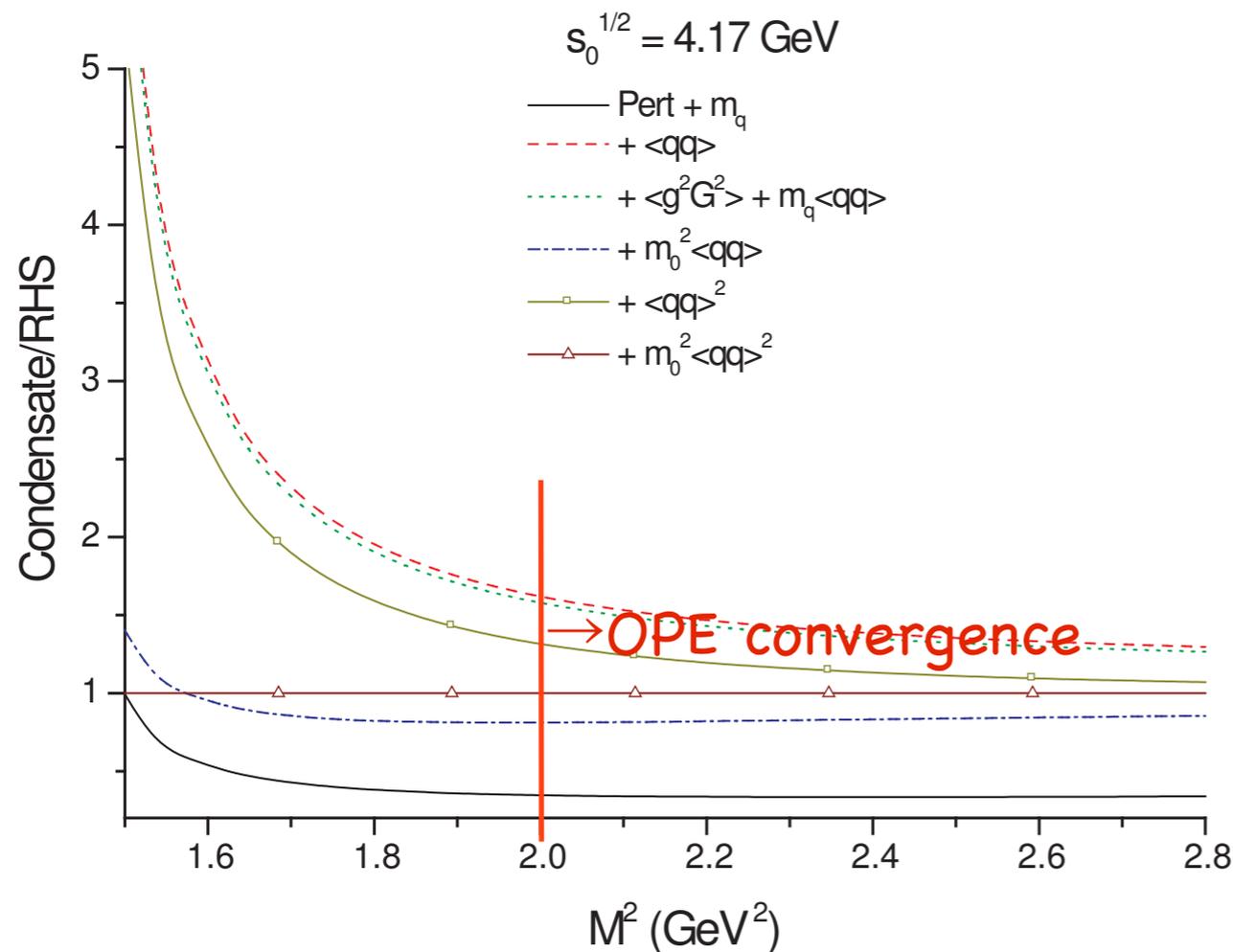
Matheus, Narison, MN, Richard: PRD75 (07)

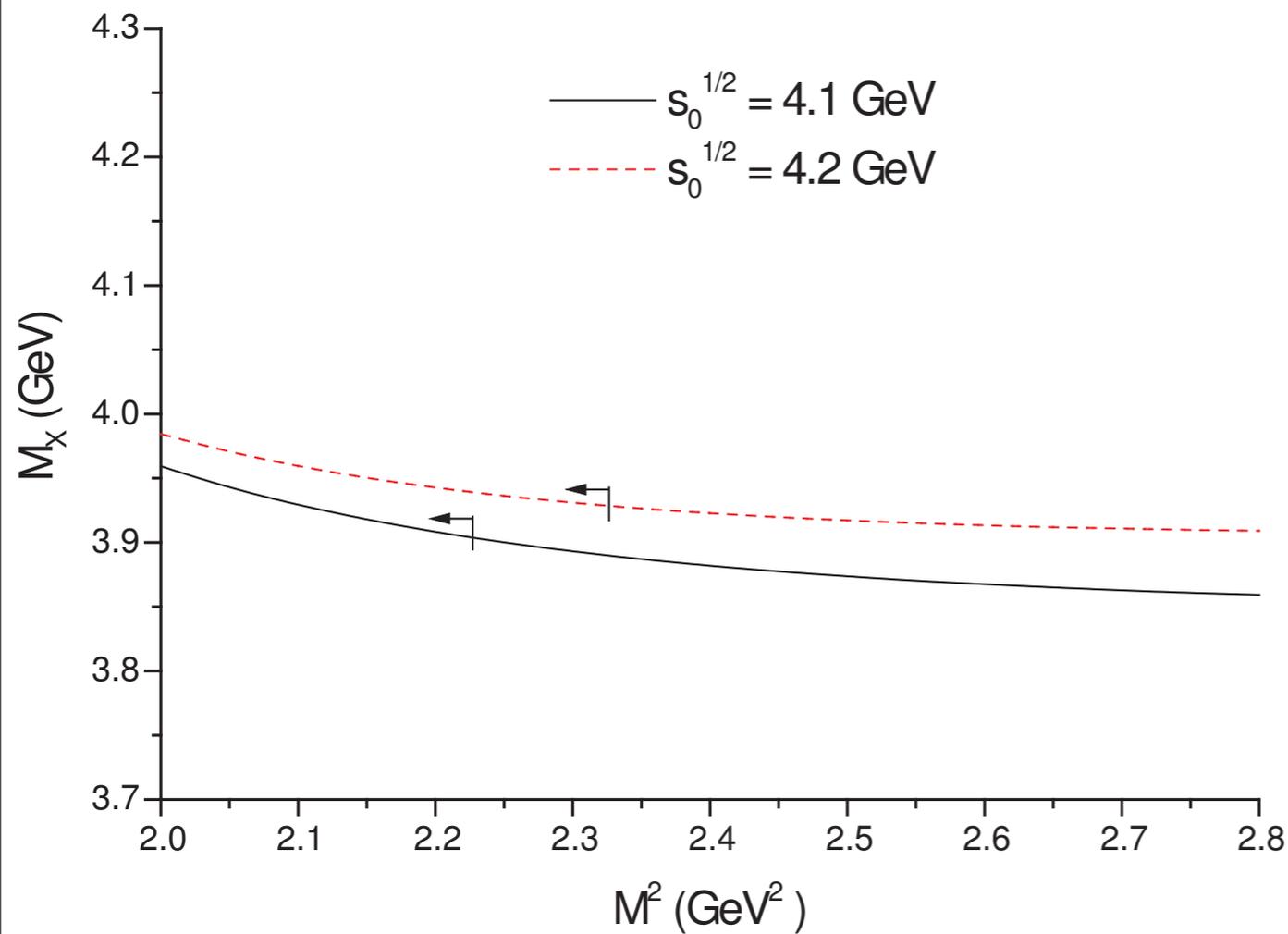
$$j_\mu = \frac{i\epsilon_{abc}\epsilon_{dec}}{\sqrt{2}} [(q_a^T C \gamma_5 c_b)(\bar{q}_d \gamma_\mu C \bar{c}_e^T) + (q_a^T C \gamma_\mu c_b)(\bar{q}_d \gamma_5 C \bar{c}_e^T)]$$

# QCD sum rules calculation for $X(3872)$

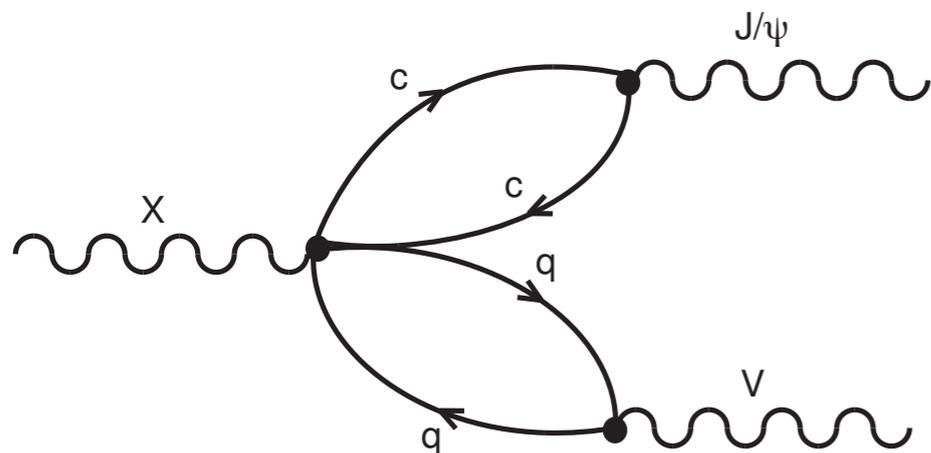
Matheus, Narison, MN, Richard: PRD75 (07)

$$j_\mu = \frac{i\epsilon_{abc}\epsilon_{dec}}{\sqrt{2}} [(q_a^T C \gamma_5 c_b)(\bar{q}_d \gamma_\mu C \bar{c}_e^T) + (q_a^T C \gamma_\mu c_b)(\bar{q}_d \gamma_5 C \bar{c}_e^T)]$$





$$m_X = (3.92 \pm 0.13) \text{ GeV}$$



Problem: decay width  $X \rightarrow J/\psi \pi \pi \pi$   
 $\sim 50 \text{ MeV}$  (Navarra, MN, PLB639 (06)272)

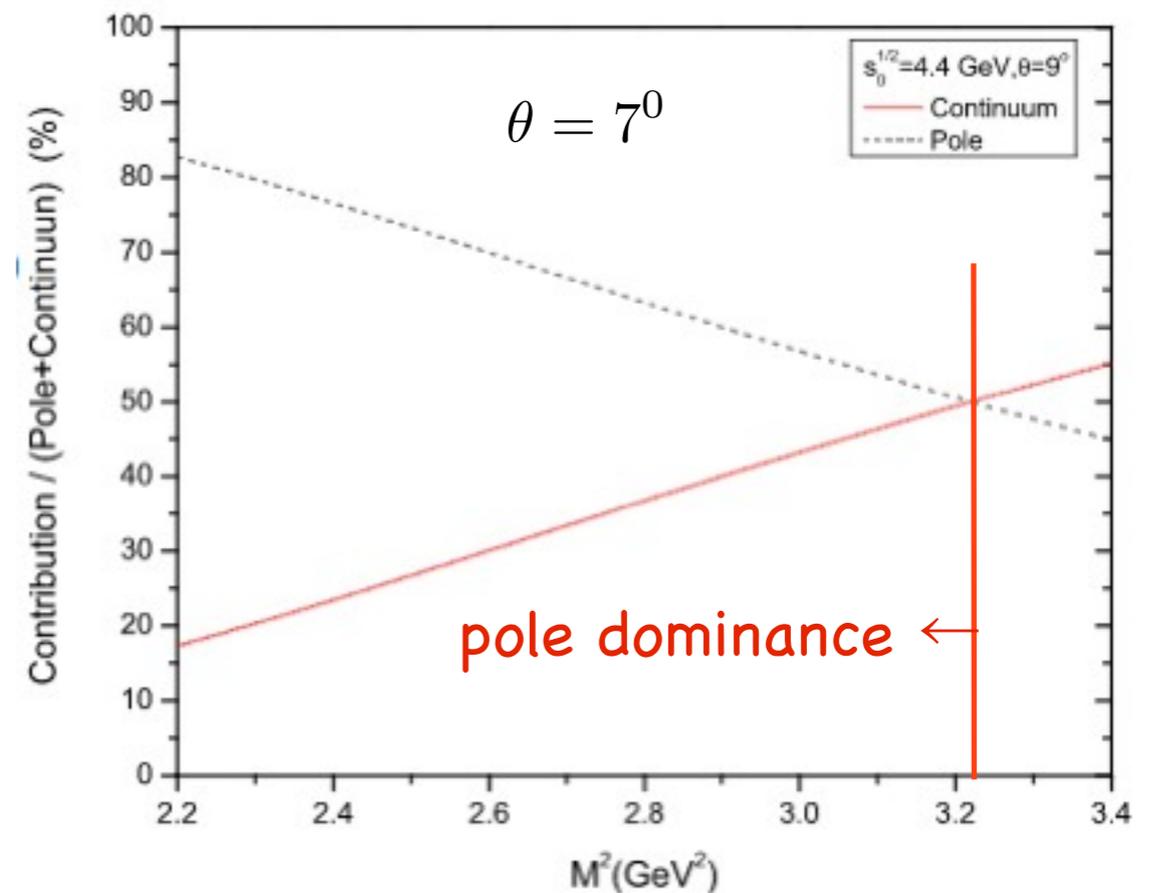
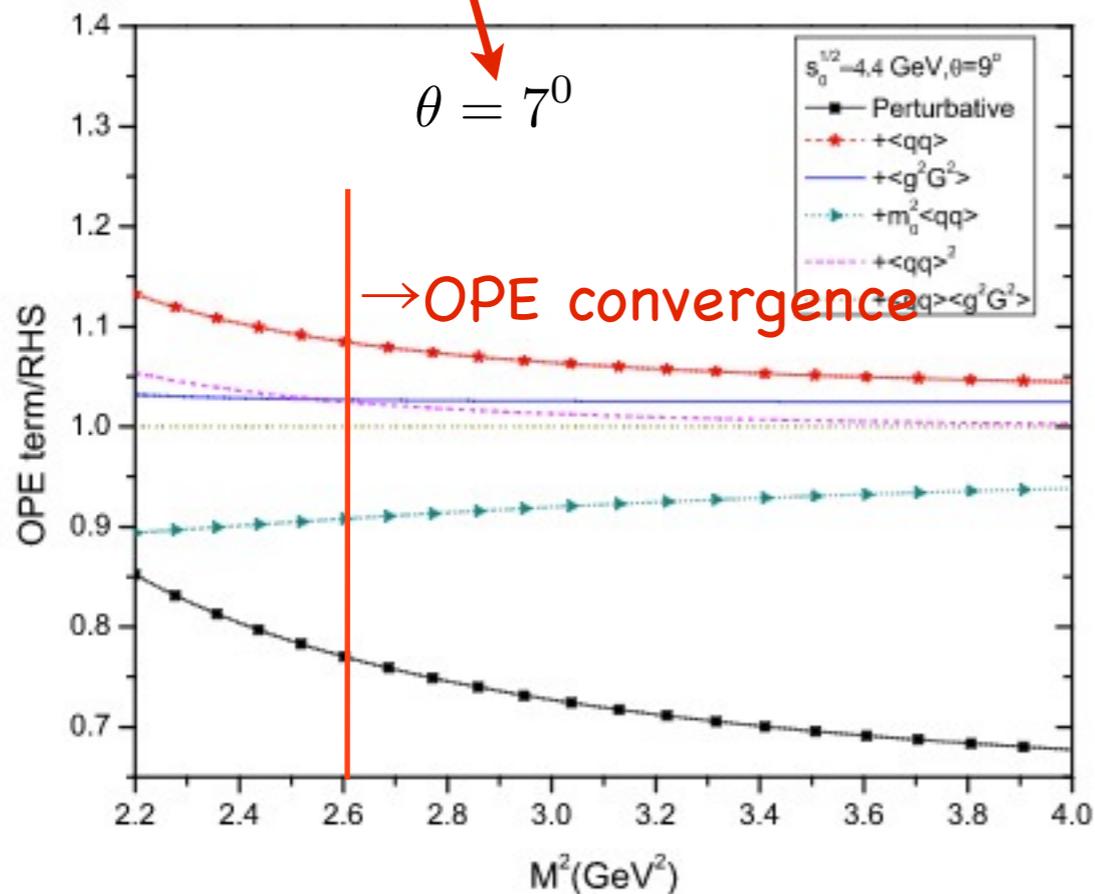
How to solve this problem?

# X(3872) as a mixed charmonium 4-quark state

Matheus, Navarra, MN, Zanetti: PRD80 (09)

$$J_\mu^u(x) = \sin(\theta) j_\mu^{(4u)}(x) + \cos(\theta) j_\mu^{(2u)}(x)$$

$$j_\mu^{(2u)} = \frac{1}{6\sqrt{2}} \langle \bar{u}u \rangle \bar{c}_a(x) \gamma_\mu \gamma_5 c_a(x)$$



$$m_X = (3.77 \pm 0.18) \text{ GeV}$$

$$5^\circ \leq \theta \leq 13^\circ$$

Compatible with the experimental X(3872) mass

# Decay width $X \rightarrow J/\psi V$

$$\Pi_{\mu\nu\alpha}(p, p', q) = \int d^4x d^4y e^{ip' \cdot x} e^{iq \cdot y} \Pi_{\mu\nu\alpha}(x, y)$$

$$\Pi_{\mu\nu\alpha}(x, y) = \langle 0 | T [j_\mu^\psi(x) j_\nu^V(y) j_\alpha^{X^\dagger}(0)] | 0 \rangle \quad j_\mu^\psi = \bar{c}_a \gamma_\mu c_a$$

$$j_\nu^V = \frac{N_V}{2} (\bar{u}_a \gamma_\nu u_a + (-1)^{I_V} \bar{d}_a \gamma_\nu d_a) \begin{array}{l} \rightarrow N_\rho = 1, I_\rho = 1 \\ \rightarrow N_\omega = 1/3 \text{ and } I_\omega = 0 \end{array}$$

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$$\Gamma = (9.3 \pm 6.9) \text{ MeV}, 5^\circ \leq \theta \leq 13^\circ$$

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$$N_\rho = 1, I_\rho = 1$$

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## Decay width $X \rightarrow J/\psi \gamma$

MN, Zanetti: PRD82 (10)

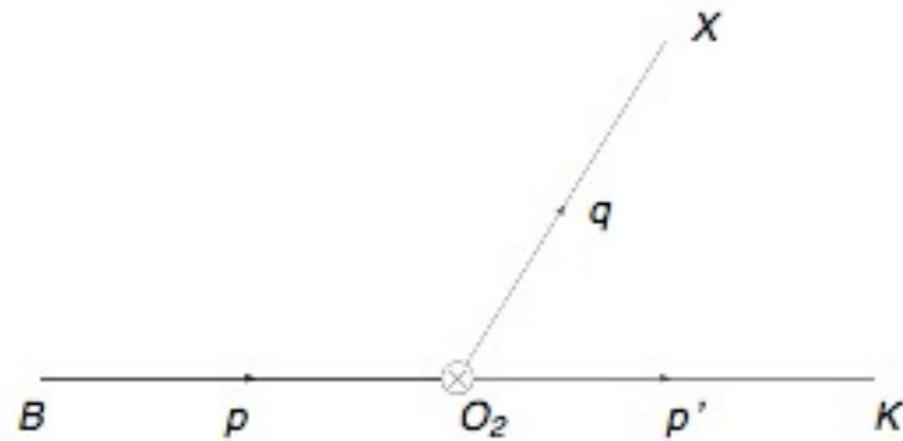
$$\frac{\Gamma(X \rightarrow J/\psi \gamma)}{\Gamma(X \rightarrow J/\psi \pi^+ \pi^-)} = 0.14 \pm 0.05$$

$$\frac{\Gamma(X \rightarrow J/\psi \gamma)}{\Gamma(X \rightarrow J/\psi \pi^+ \pi^-)} = 0.19 \pm 0.13$$

# Production rate $B^+ \rightarrow X(3872)K^+$

$$5^\circ \leq \theta \leq 13^\circ$$

Matheus, MN, Zanetti: PLB702 (11)



$$\mathcal{H}_W = \frac{G_F}{\sqrt{2}} V_{cb} V_{cs}^* \left[ \left( C_2(\mu) + \frac{C_1(\mu)}{3} \right) \mathcal{O}_2 + \dots \right]$$

$$\mathcal{O}_2 = (\bar{c}\Gamma_\mu c)(\bar{s}\Gamma^\mu b), \text{ with } \Gamma_\mu = \gamma_\mu(1-\gamma_5)$$

$$\mathcal{B}(B \rightarrow X(3872)K) = (1.00 \pm 0.68) \times 10^{-5}$$

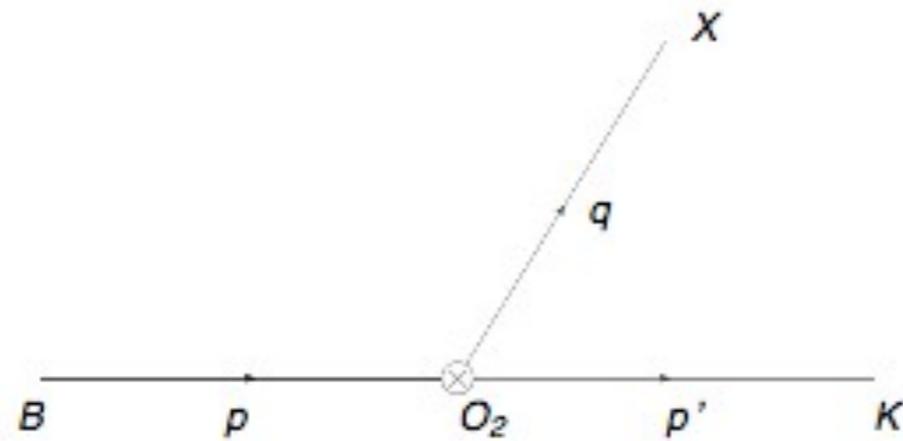


$$\mathcal{B}(B^\pm \rightarrow K^\pm X(3872)) < 3.2 \times 10^{-4}$$

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$$\mathcal{B}(B \rightarrow X(3872)K) = (1.00 \pm 0.68) \times 10^{-5}$$



$$\mathcal{B}(B^\pm \rightarrow K^\pm X(3872)) < 3.2 \times 10^{-4}$$

## Conclusions for $X(3872)$

- $X(3872)$  is probably a mixed multiquark state with a  $\chi_{c1}$  state



$Z^+(4430)$

first observed charged  
charmonium state  $\rightarrow$  not  $c\bar{c}$

PRL100(08)142001

$$\bar{B}^0 \rightarrow K^\mp Z^\pm(4430), Z^\pm(4430) \rightarrow \psi' \pi^\pm$$



$Z^+(4430)$

first observed charged charmonium state  $\rightarrow$  not  $c\bar{c}$

PRL100(08)142001

$$\bar{B}^0 \rightarrow K^{\mp} Z^{\pm}(4430), Z^{\pm}(4430) \rightarrow \psi' \pi^{\pm}$$



searched  $Z^-(4430)$  in 4 decay modes:

no conclusive  
evidence for the existence of  $Z^+(4430)$  seen by  
Belle

arXiv:0905.2869



# $Z^+(4430)$

first observed charged charmonium state  $\rightarrow$  not  $c\bar{c}$

PRL100(08)142001

$$\bar{B}^0 \rightarrow K^\mp Z^\pm(4430), Z^\pm(4430) \rightarrow \psi' \pi^\pm$$



## searched $Z^-(4430)$ in 4 decay modes:

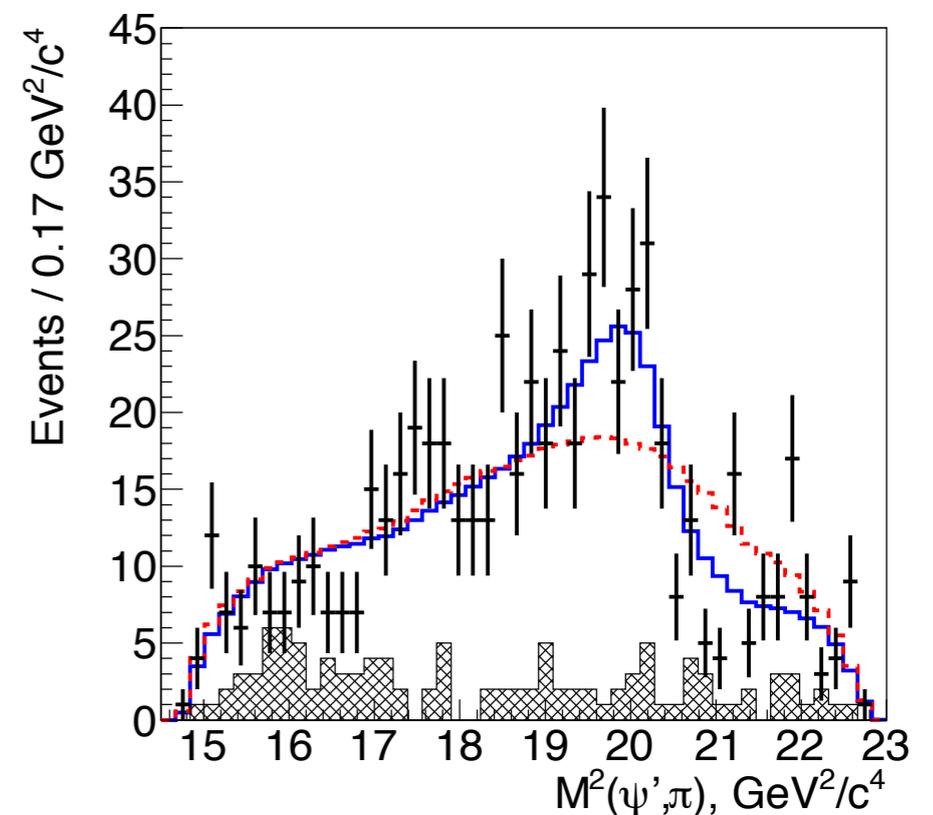
no conclusive evidence for the existence of  $Z^+(4430)$  seen by Belle

arXiv:0905.2869



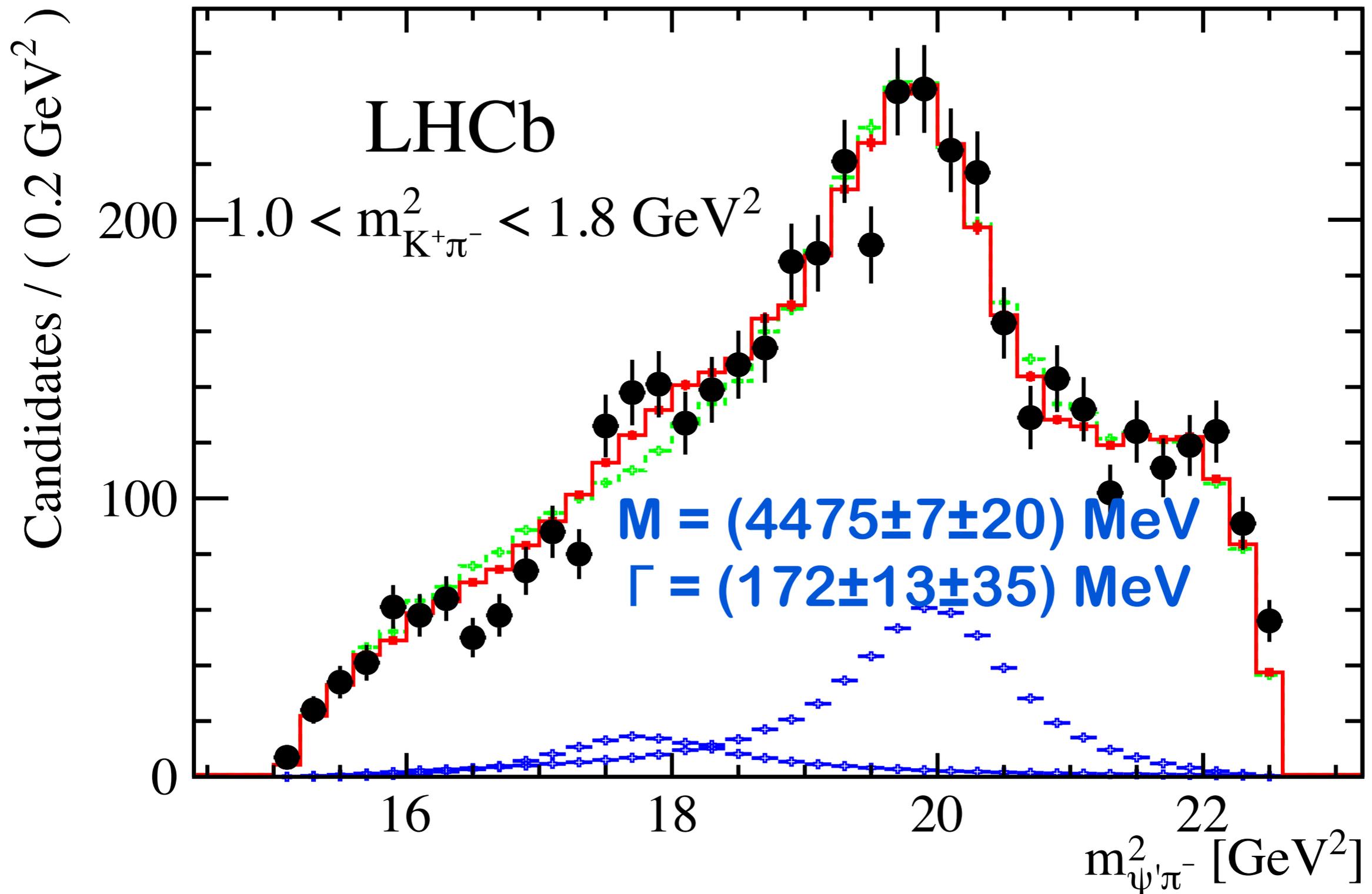
arXiv:1306.4894

confirm the observation of  $Z^+(4430)$  with  $6.1 \sigma$  and  $J^P=1^+$

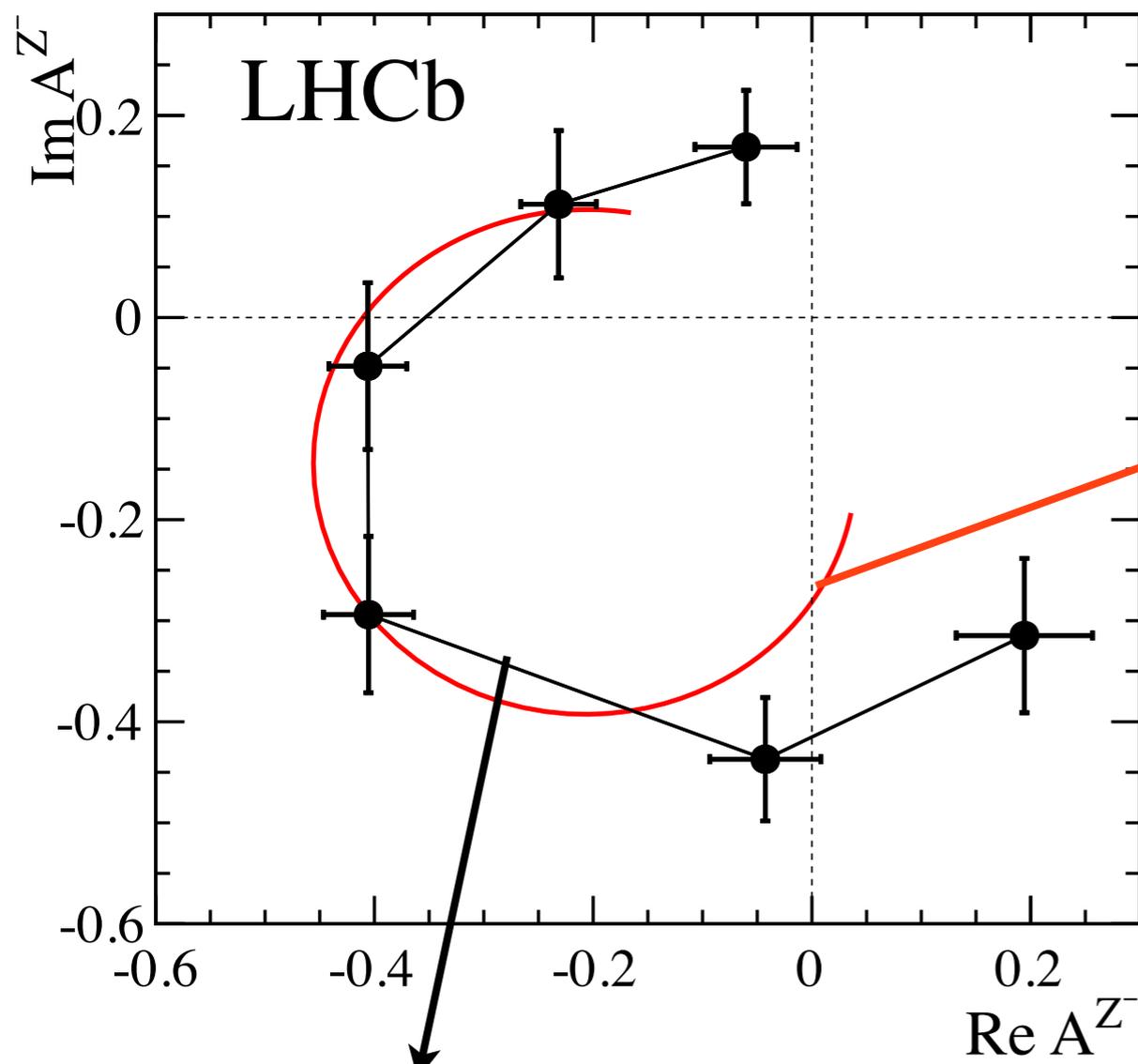


has confirmed the observation of  $Z^+(4430)$  with  $13.9 \sigma$  and  $J^+ = 1^+$

arXiv:1404.1903



LHCb also did the first attempt to demonstrate the resonant behavior of  $Z^+(4430)$  (arXiv:1404.1903): the Breit-Wigner amplitude was replaced by a combination of independent complex amplitudes at six equally spaced points in  $m_{\Psi'\pi}$  range covering the  $Z^+(4430)$  peak region



fitted values of  $Z$   
amplitude in six  $m_{\Psi'\pi}$  bins

Breit-Wigner

the Argand diagram is consistent with a rapid phase transition, as expected for a resonance

$Z^+(4430)$

threshold effect in the  $D_1 D^*$  channel  
Rosner, arXiv:0708.3496

four-quark radial excitation with  $J^{PC} = 1^{+-}$   
Maiani, Polosa & Riquer, arXiv:0708.3997

radial excitation of  $\Lambda_c - \Sigma_c^0$  bound state  
Qiao, arXiv:0709.4066

$D_1 D^*$  molecular state with  $J^P = 0^-, 1^-, 2^-$   
Meng & Cheng, arXiv:0708.4222

cusp in the  $D_1 D^*$  channel  
Bugg, arXiv:0709.1254

$D_1 D^*$  molecular state with  $J^P = 1^+$   
He, arXiv:1410.8645

$D_1 D^*$  or  $D_2 D^*$  molecular state with  $J^P = 1^+$   
Ma, Liu, Liu, Zhu, arXiv:1404.3450; Barnes,  
Close, Swanson, arXiv:1409.6651

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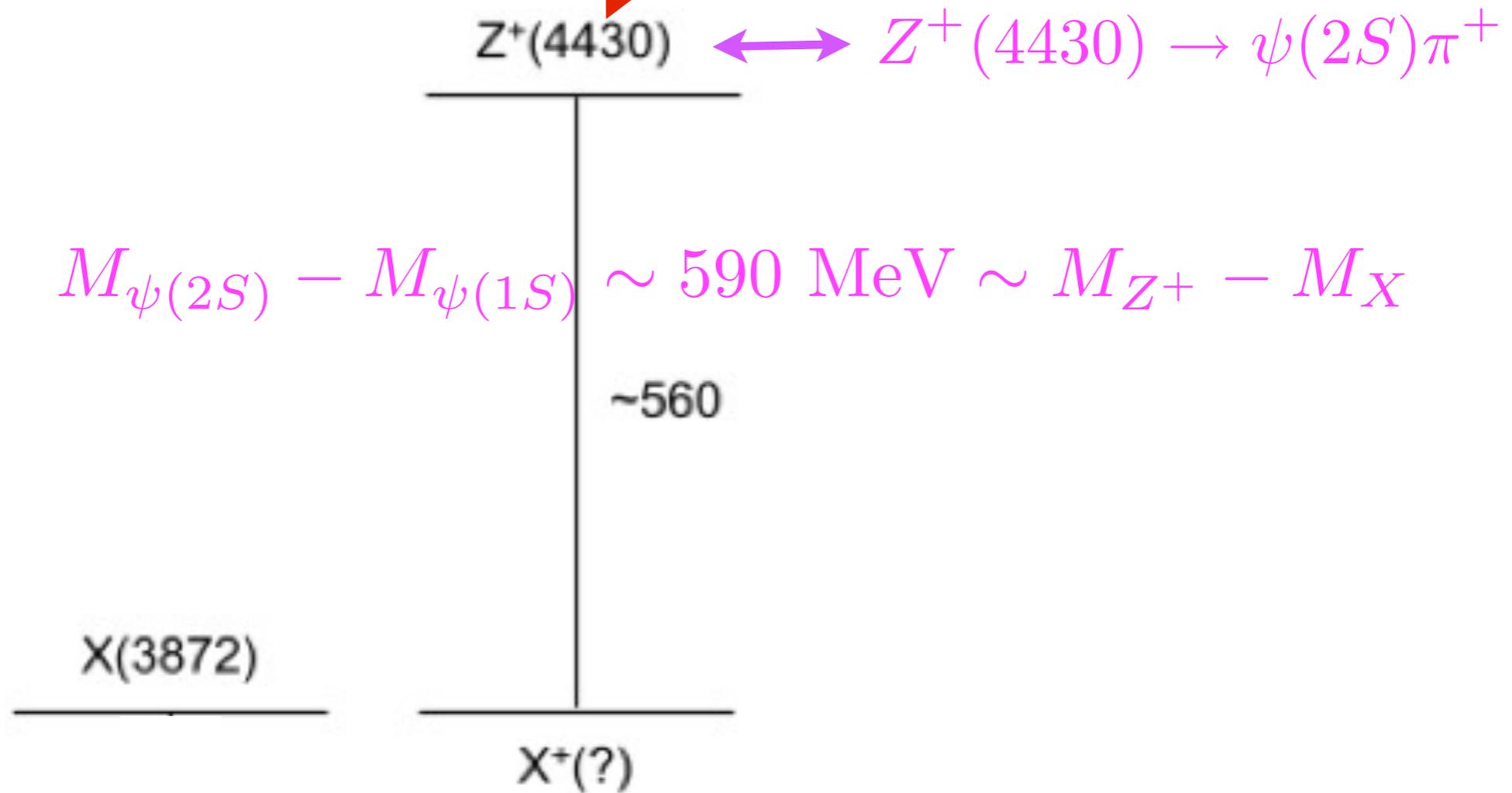
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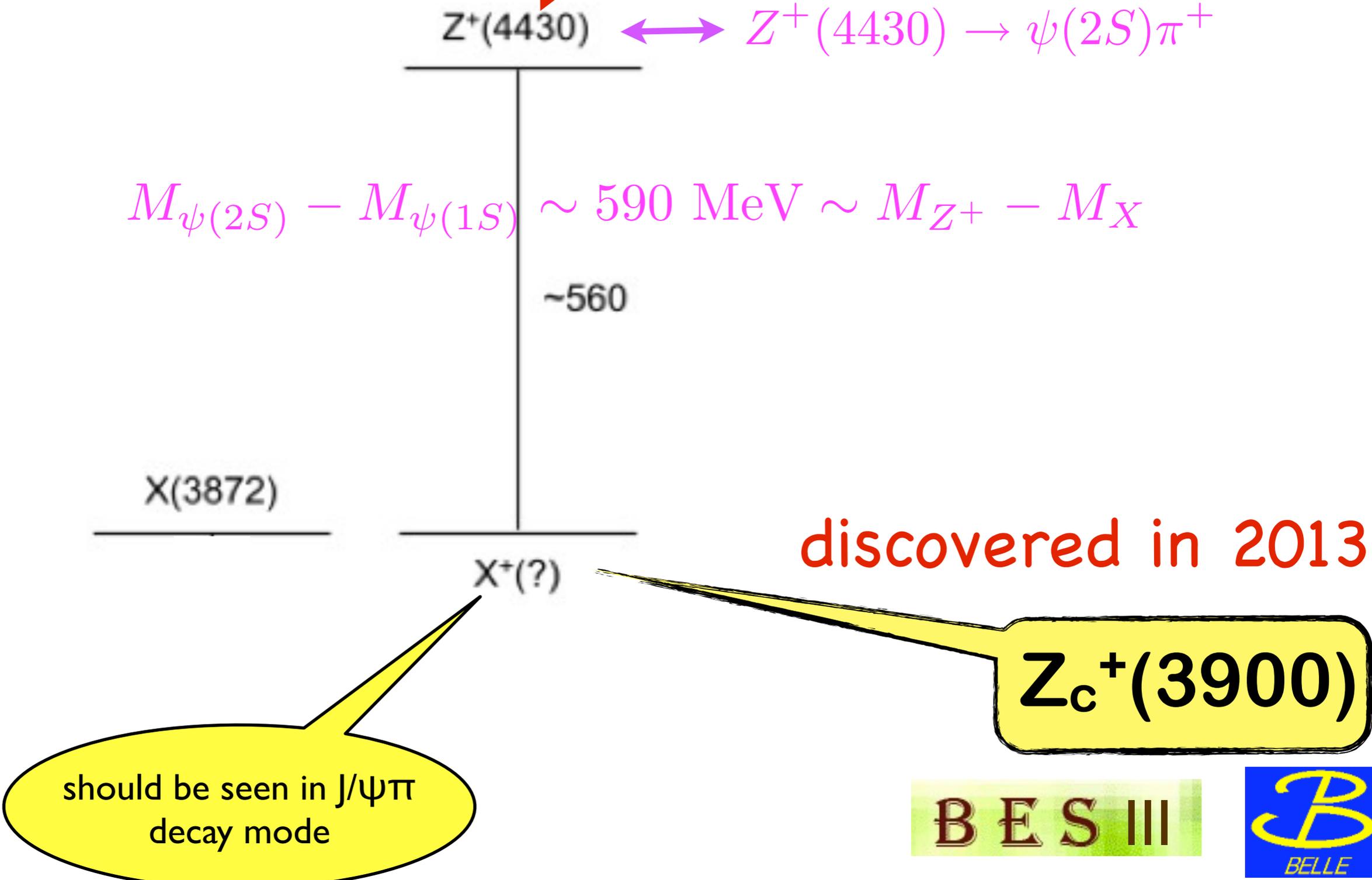
not a real  
state

Maiani et al. (arXiv:0708.3997) : four-quark radial excitation of the  $I^+$  charged state (X(3872) partner)

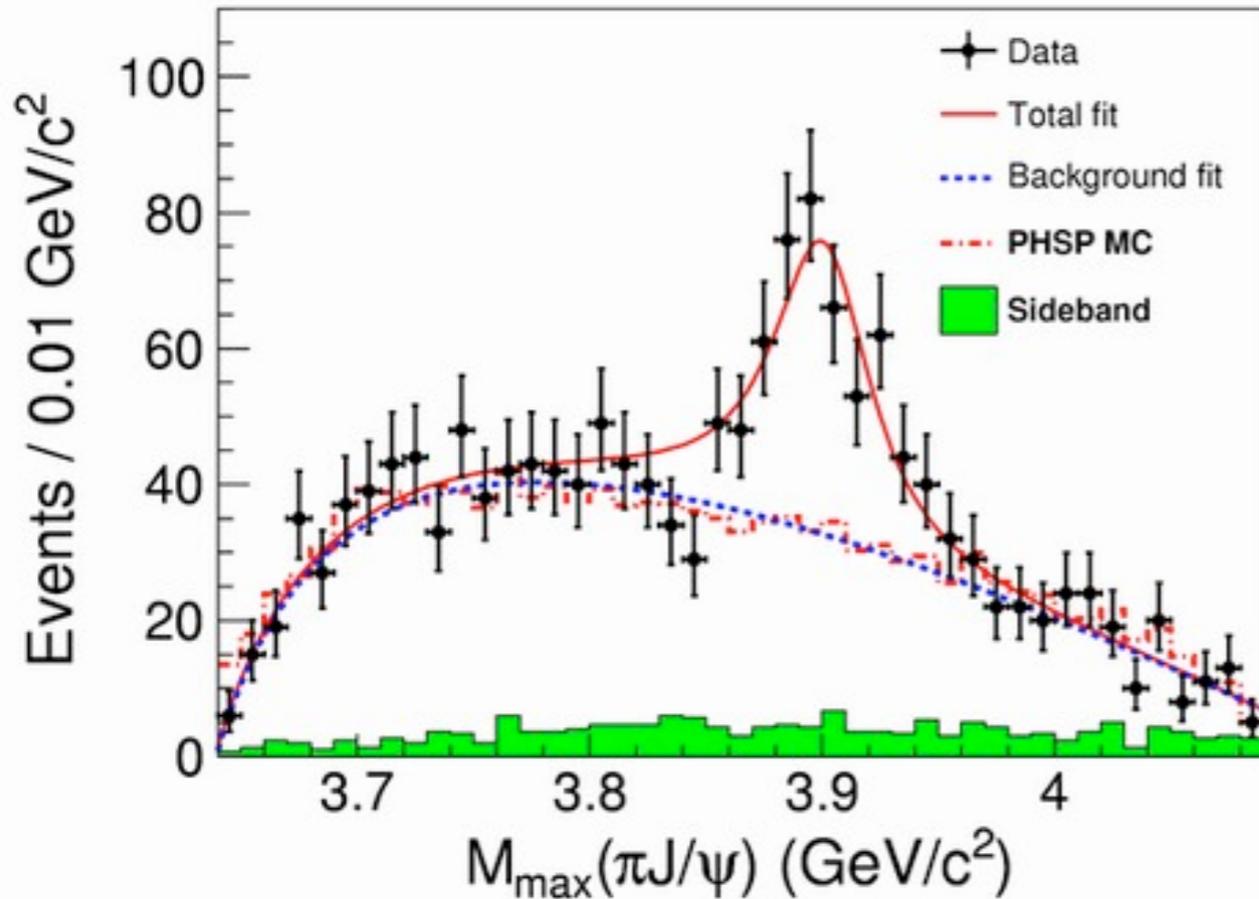


should be seen in  $J/\psi\pi$  decay mode

Maiani et al. (arXiv:0708.3997) : four-quark radial excitation of the  $I^+$  charged state (X(3872) partner)



# Charged Charmonium states discovered in 2013



**$Z_c^+(3900)$**

**BES III**



arXiv:1303.5949

arXiv:1304.0121

$$Y(4260) \rightarrow (J/\psi \pi^+) \pi^-$$

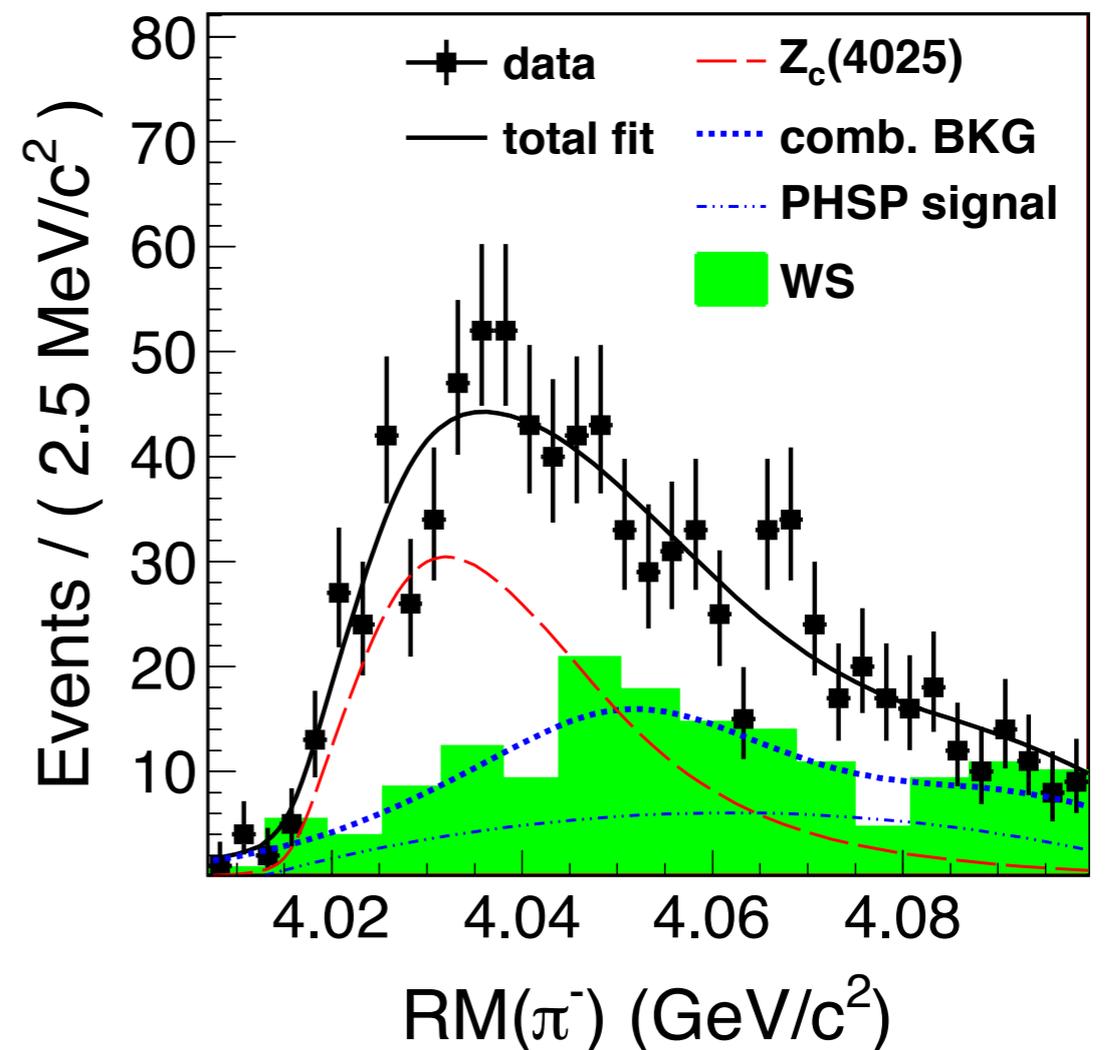
**$Z_c^+(4025)$**

**BES III**

arXiv:1308.2760

$$e^+ e^- \rightarrow (D^* \bar{D}^*)^\pm \pi^\mp$$

$$\sqrt{s} = 4.26 \text{ GeV}$$

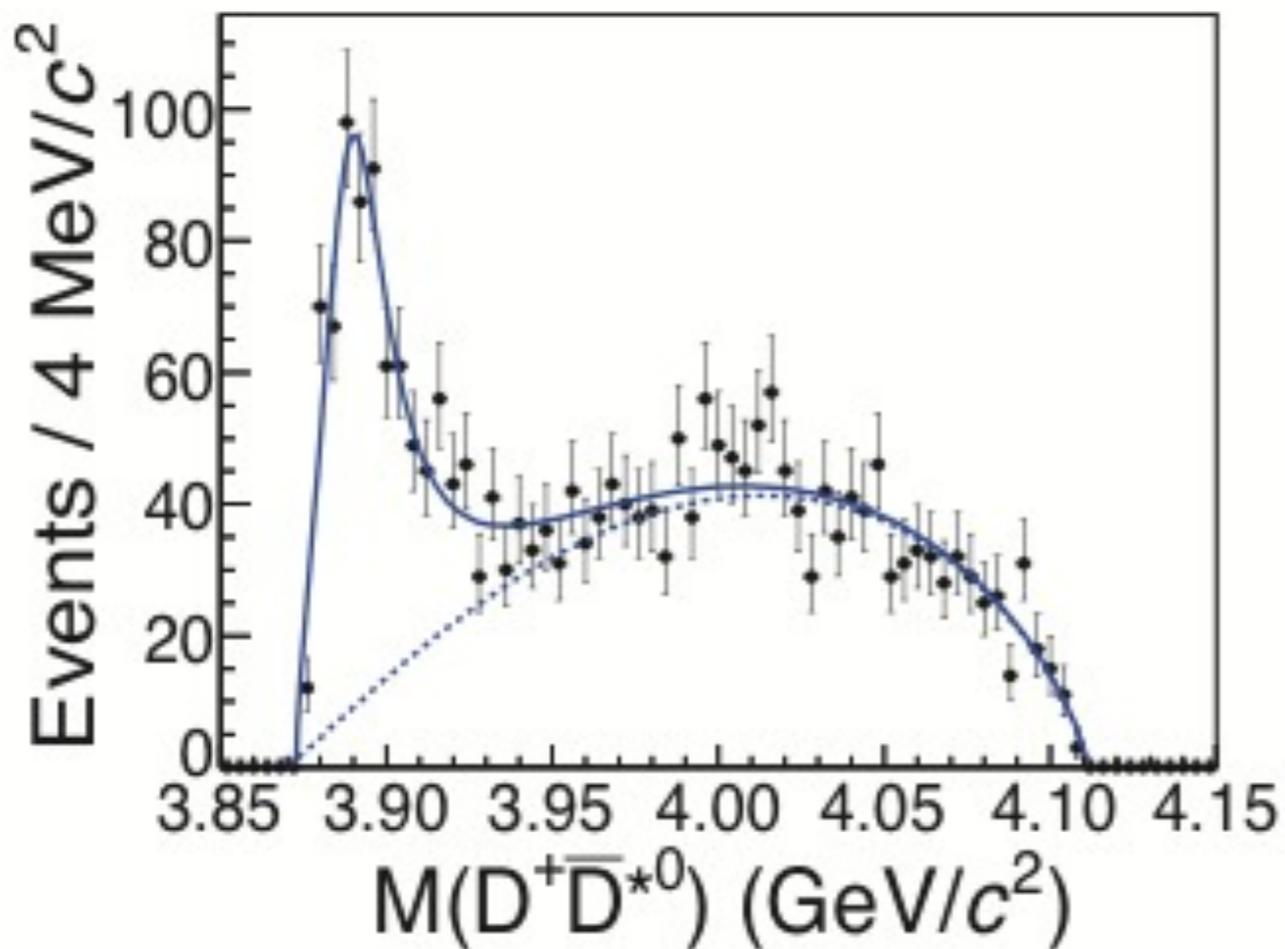
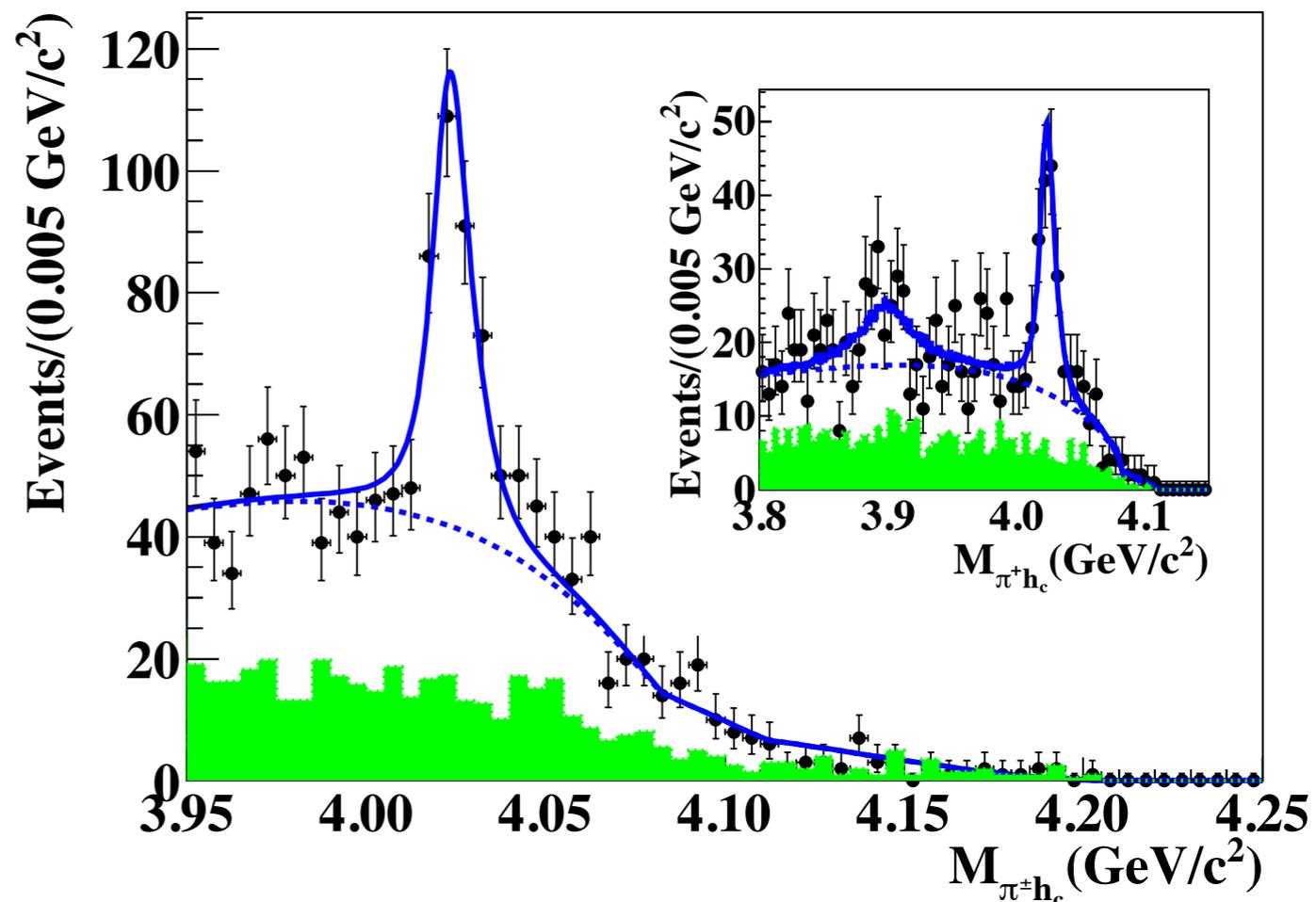


# $Z_c^+(4020)$

# BES III

arXiv:1309.1896

$$e^+e^- \rightarrow \pi^+\pi^-h_c$$
$$\sqrt{s} = (3.90 - 4.42) \text{ GeV}$$



# $Z_c^+(3885)$

# BES III

arXiv:1310.1163

$$e^+e^- \rightarrow \pi^\pm (D\bar{D}^*)^\mp @ \sqrt{s} = 4.26 \text{ GeV}$$

# BESIII: a summary of $Z_c$ observations

$Z_c$	Mass (MeV/c <sup>2</sup> )	Width (MeV)	Decay	Process	[Ref]
$Z_c(3900)^{\pm}$	$3899.0 \pm 3.6 \pm 4.9$	$46 \pm 10 \pm 20$	$\pi^{\pm} J/\psi$	$e^+e^- \rightarrow \pi^+\pi^- J/\psi$	[1]
$Z_c(3900)^0$	$3894.8 \pm 2.3 \pm 2.7$	$29.6 \pm 8.2 \pm 8.2$	$\pi^0 J/\psi$	$e^+e^- \rightarrow \pi^0\pi^0 J/\psi$	[2]
$Z_c(3885)^{\pm}$	$3883.9 \pm 1.5 \pm 4.2$ Single D tag	$24.8 \pm 3.3 \pm 11.0$ Single D tag	$(D\bar{D}^*)^{\pm}$	$e^+e^- \rightarrow (D\bar{D}^*)^{\pm}\pi^{\mp}$	[3]
	$3881.7 \pm 1.6 \pm 2.1$ Double D tag	$26.6 \pm 2.0 \pm 2.3$ Double D tag	$(D\bar{D}^*)^{\pm}$	$e^+e^- \rightarrow (D\bar{D}^*)^{\pm}\pi^{\mp}$	[4]
$Z_c(3885)^0$	$3885.7^{+4.3}_{-5.7} \pm 8.4$	$35^{+11}_{-12} \pm 15$	$(D\bar{D}^*)^0$	$e^+e^- \rightarrow (D\bar{D}^*)^0\pi^0$	[5]
$Z_c(4020)^{\pm}$	$4022.9 \pm 0.8 \pm 2.7$	$7.9 \pm 2.7 \pm 2.6$	$\pi^{\pm} h_c$	$e^+e^- \rightarrow \pi^+\pi^- h_c$	[6]
$Z_c(4020)^0$	$4023.9 \pm 2.2 \pm 3.8$	fixed	$\pi^0 h_c$	$e^+e^- \rightarrow \pi^0\pi^0 h_c$	[7]
$Z_c(4025)^{\pm}$	$4026.3 \pm 2.6 \pm 3.7$	$24.8 \pm 5.6 \pm 7.7$	$D^*\bar{D}^*$	$e^+e^- \rightarrow (D^*\bar{D}^*)^{\pm}\pi^{\mp}$	[8]
$Z_c(4025)^0$	$4025.5^{+2.0}_{-4.7} \pm 3.1$	$23.0 \pm 6.0 \pm 1.0$	$D^*\bar{D}^*$	$e^+e^- \rightarrow (D^*\bar{D}^*)^0\pi^0$	[9]

[1] PRL 110, 252001; [2] PRL 115, 112003; [3] PRL 112, 022001; [4] PRD 92, 092006

[5] PRL 115, 222002; [6] PRL 110, 252001; [7] PRL 113, 212002; [8] PRL 112, 132001

[9] PRL 115, 182002

- Mass and widths of  $Z_c(3900)$  and  $Z_c(3885)$  (also  $Z_c(4020)$  and  $Z_c(4025)$ ) are consistent within  $2\sigma \rightarrow$  the same states?

from Shan Jin talk  
ICHEP16

**$Z_c^+(3900)$**

## Tetraquark state

Maiani et al., PRD87(13); Dias et al., arXiv:1304.6433; Wang & Huang, arXiv:1310.2412; Braaten, arXiv:1305.6905,...

## $D^*\bar{D}$ molecular state

Sun et al., arXiv:1106.2968; Guo et al., arXiv:1303.6608; Voloshin, arXiv:1304.0380; Wang et al., arXiv:1303.6355; Cui et al., arXiv:1304.1850; Zhang, arXiv:1304.5748; Dong et al., arXiv:1306.0824; Ke et al., arXiv:1307.2414; Prelovsek et al., arXiv:1308.2097

to reproduce the measured width  $\Rightarrow \langle r_{\text{eff}} \rangle \approx 0.4 \text{ fm} \Rightarrow$

disfavors molecular interpretation

(Mahajan, arXiv1304.1301)

$D^*\bar{D}$  molecule with  $\langle r^2 \rangle \approx 0.11 \text{ fm}^2$  (Wilbring et al., PLB726(13))

hard to understand since  $\langle r_\psi^2 \rangle \approx 0.16 \text{ fm}^2$

# QCDSR calculation for $Z_c^+(3900)$

two-point calculation for  $Z_c^+(3900)$  with a tetraquark current gives the same result as for  $X(3872)$

Decay width  $Z^+ \rightarrow J/\psi \pi^+$

Dias, Navarra, MN, Zanetti  
arXiv:1304.6433

$$\Pi_{\mu\nu\alpha}(p, p', q) = \int d^4x d^4y e^{ip' \cdot x} e^{iq \cdot y} \Pi_{\mu\nu\alpha}(x, y)$$

$$\Pi_{\mu\nu\alpha}(x, y) = \langle 0 | T [j_\mu^\psi(x) j_{5\nu}^\pi(y) j_\alpha^\dagger(0)] | 0 \rangle$$

$$j_\alpha = \frac{i\epsilon_{abc}\epsilon_{dec}}{\sqrt{2}} [(u_a^T C \gamma_5 c_b)(\bar{d}_d \gamma_\alpha C \bar{c}_e^T) - (u_a^T C \gamma_\alpha c_b)(\bar{d}_d \gamma_5 C \bar{c}_e^T)]$$

tetraquark current

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tetraquark current

$$\Gamma(Z_c^+(3900) \rightarrow J/\psi \pi^+) = (29.1 \pm 8.2) \text{ MeV}$$

# QCDSR Results for decay widths of the $Z_c^+(3900)$

Dias, Navarra, MN, Zanetti  
arXiv:1304.6433

Vertex	coupling constant (GeV)	decay width (MeV)
$Z_c^+(3900) J/\psi \pi^+$	$3.89 \pm 0.56$	$29.1 \pm 8.2$
$Z_c^+(3900) \eta_c \rho^+$	$4.85 \pm 0.81$	$27.5 \pm 8.5$
$Z_c^+(3900) D^+ \bar{D}^{*0}$	$2.5 \pm 0.3$	$3.2 \pm 0.7$
$Z_c^+(3900) \bar{D}^0 D^{*+}$	$2.5 \pm 0.3$	$3.2 \pm 0.7$

$$\Gamma_{Z_c^+} = (63 \pm 18) \text{ MeV}$$

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$$\Gamma_{Z_c^+} = (63 \pm 18) \text{ MeV}$$

$$\Gamma_{Z_c^+}^{BES} = (46 \pm 22) \text{ MeV} \quad \Gamma_{Z_c^+}^{BELLE} = (63 \pm 35) \text{ MeV}$$

Very good agreement

$$\frac{\Gamma(Z_c(3900) \rightarrow D\bar{D}^*)}{\Gamma(Z_c(3900) \rightarrow \pi J/\psi)} = 0.22 \pm 0.12$$

**BES III**

arXiv:1310.1163

$$\frac{\Gamma(Z_c(3885) \rightarrow D\bar{D}^*)}{\Gamma(Z_c(3900) \rightarrow \pi J/\psi)} = 6.2 \pm 1.1 \pm 2.7$$

QCDSR  $\Rightarrow$  not the same state!

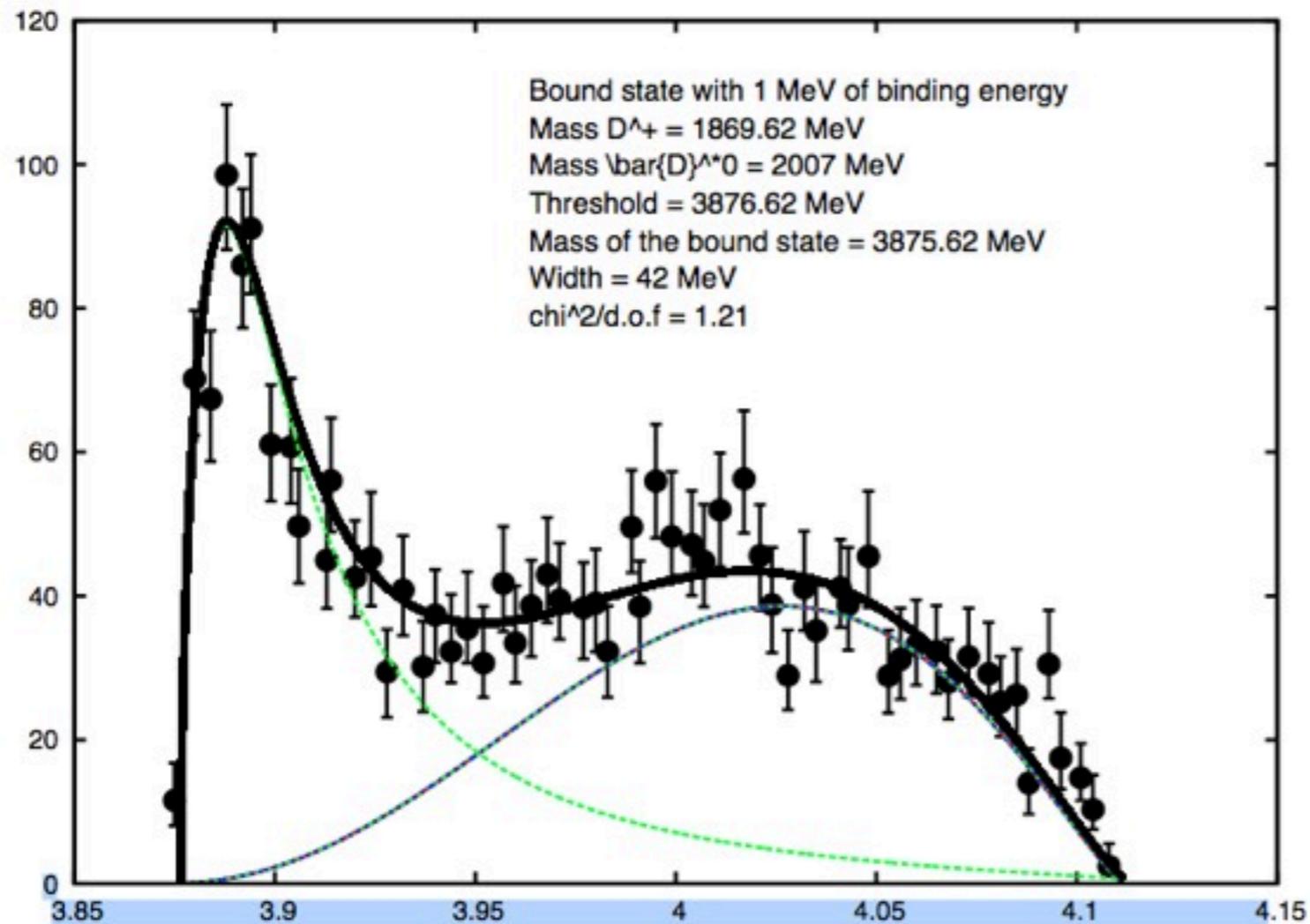
$$\frac{\Gamma(Z_c(3900) \rightarrow D\bar{D}^*)}{\Gamma(Z_c(3900) \rightarrow \pi J/\psi)} = 0.22 \pm 0.12$$

**BES III**

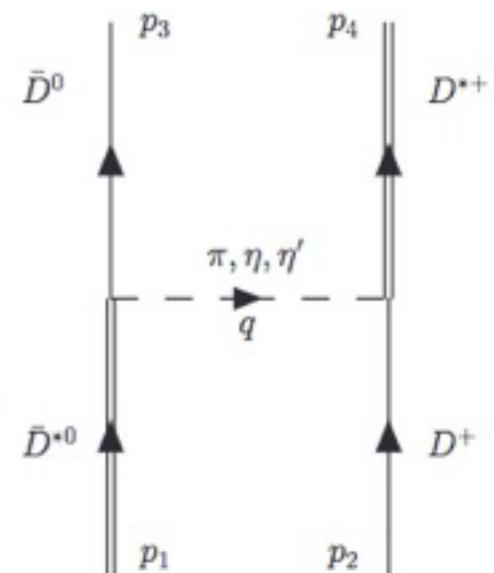
arXiv:1310.1163

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QCDSR  $\Rightarrow$  not the same state!



Aceti et al.,  
arXiv:1401.8216



$Z_c^+(3885)$   
 can be explained as  
 a  $1^+ D\bar{D}^*$  state below  
 the threshold

# Conclusions for $Z_c^+(3900)$ and $Z_c^+(3885)$

- $Z_c^+(3900)$  is probably a  $1^+$  tetraquark state
- $Z_c^+(3885)$  is probably a  $DD^*$   $1^+$  state below threshold

# Conclusions for $Z_c^+(3900)$ and $Z_c^+(3885)$

- $Z_c^+(3900)$  is probably a  $1^+$  tetraquark state
- $Z_c^+(3885)$  is probably a  $DD^*$   $1^+$  state below threshold

## QCDSR for $Z_c^+(4025)$ as a $D^*\bar{D}^*$ molecule

Khemchandani, Martínez, Navarra, MN: arXiv:1310.0862

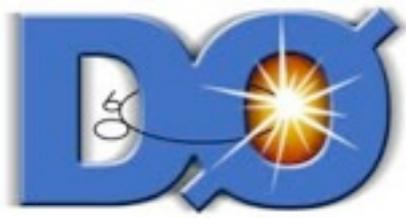
$$M^{S=1} = (3950 \pm 105) \text{ MeV}$$

$$M^{S=2} = (3946 \pm 104) \text{ MeV}$$

Both compatible with  
 $Z_c(4025)$

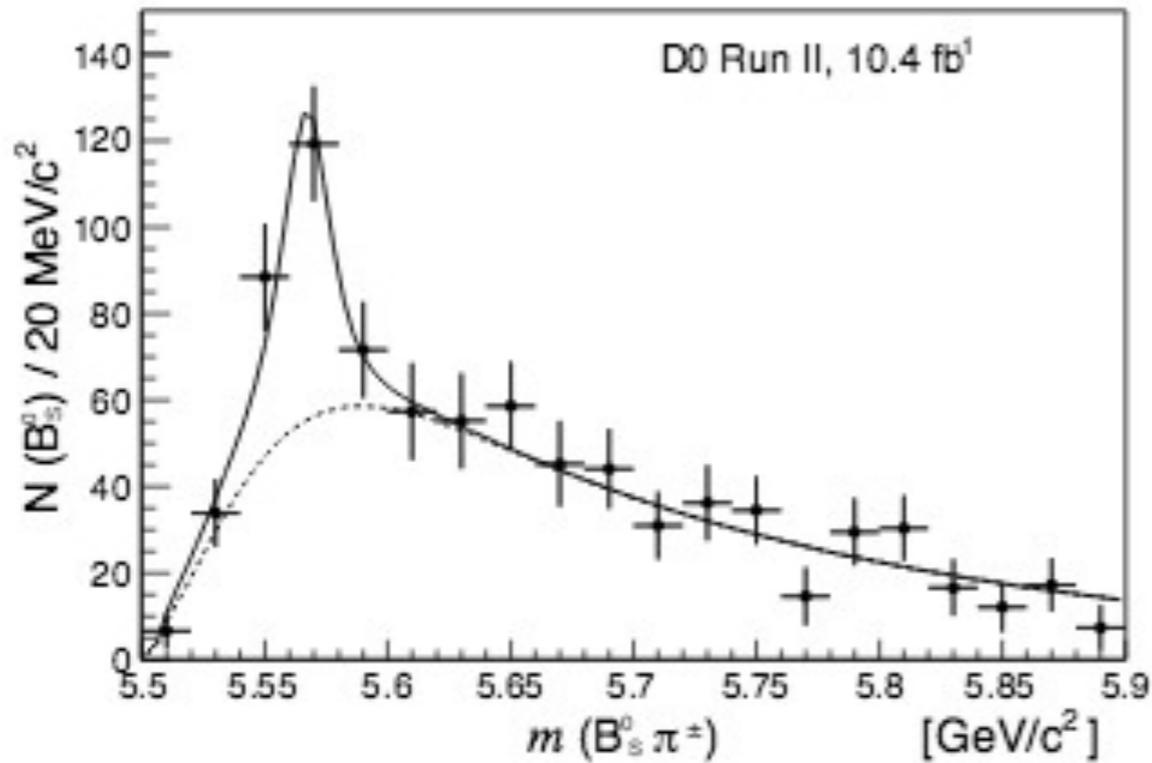
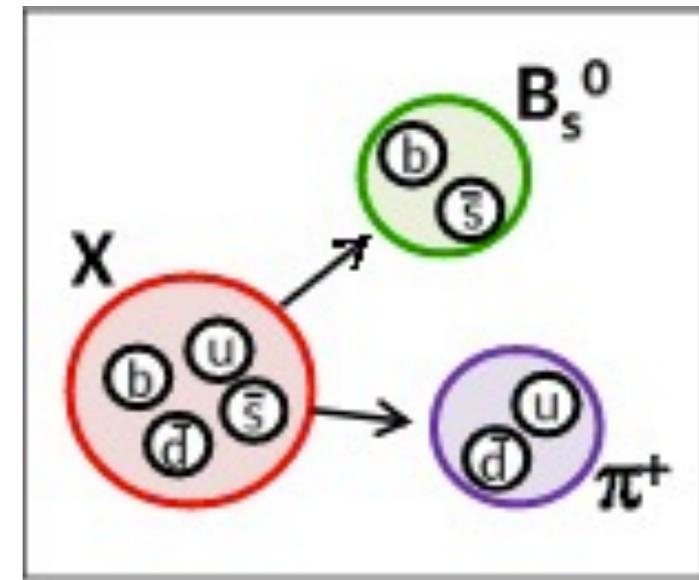
$$M^{exp} = (4026.3 \pm 2.6 \pm 3.7) \text{ MeV}$$

results are also compatible with a spin 2  $D^*\bar{D}^*$  state below threshold ([arXiv:1310.1119](https://arxiv.org/abs/1310.1119)), consistent with prediction from Molina & Oset ([PRD80\(2009\)114013](https://arxiv.org/abs/0904.1140)) doing a coupled channel analysis

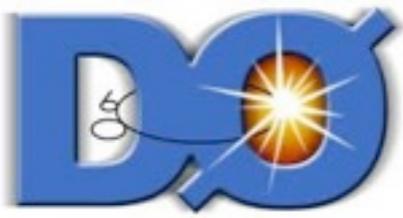


arXiv:1602.07588

# $X^\pm(5568)$ : most recent acquisition

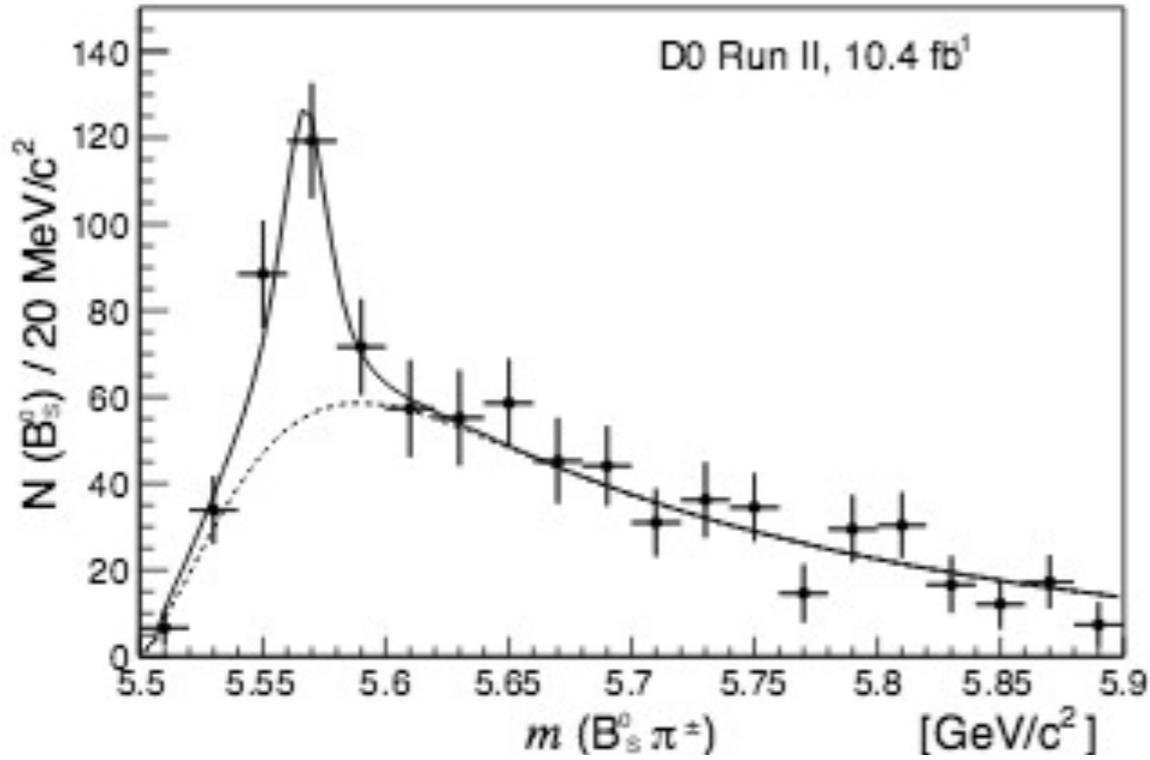
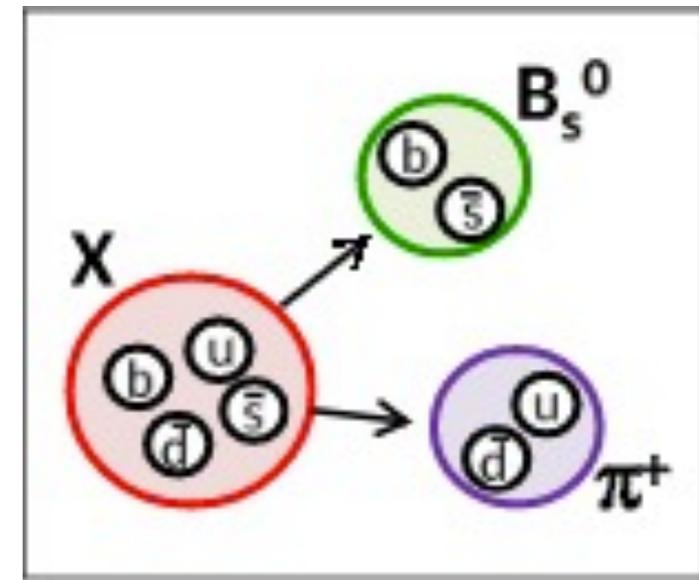


$M = (5567.8 \pm 2.9 \pm 1.2) \text{ MeV}$   
 $\Gamma = (21.9 \pm 6.4 \pm 3.5) \text{ MeV}$   
stat. significance  $5.1\sigma$

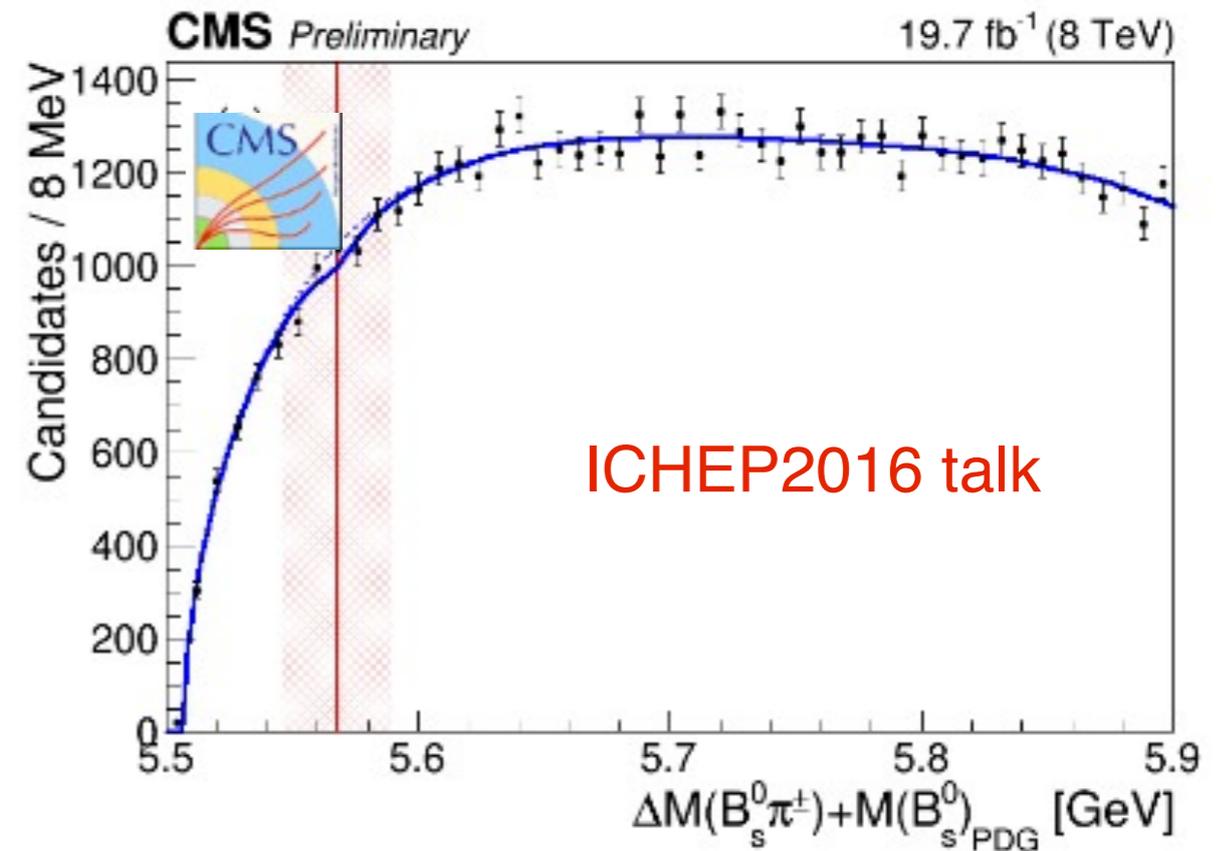
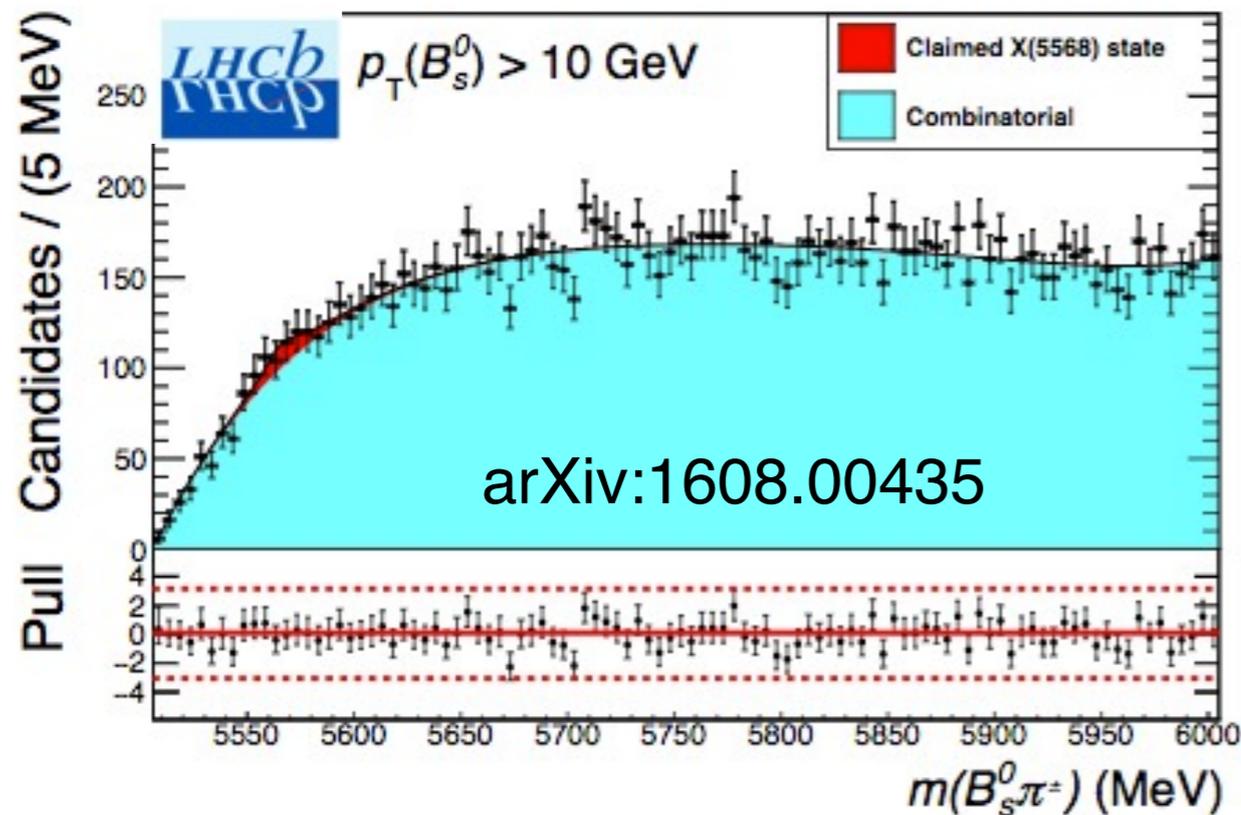


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**X<sup>+</sup>(5568)**

## Tetraquark state

Agaev et al., arXiv:1602.08642; Chen et al., arXiv:1602.08916; Wang, arXiv:1602.08711; Tang & Qiao, arXiv:1603.04761

## B $\bar{K}$ molecular state

Agaev et al., arXiv:1603.02708; Xiao & Chen, arXiv:1603.00228; Albaladejo et al., PLB757

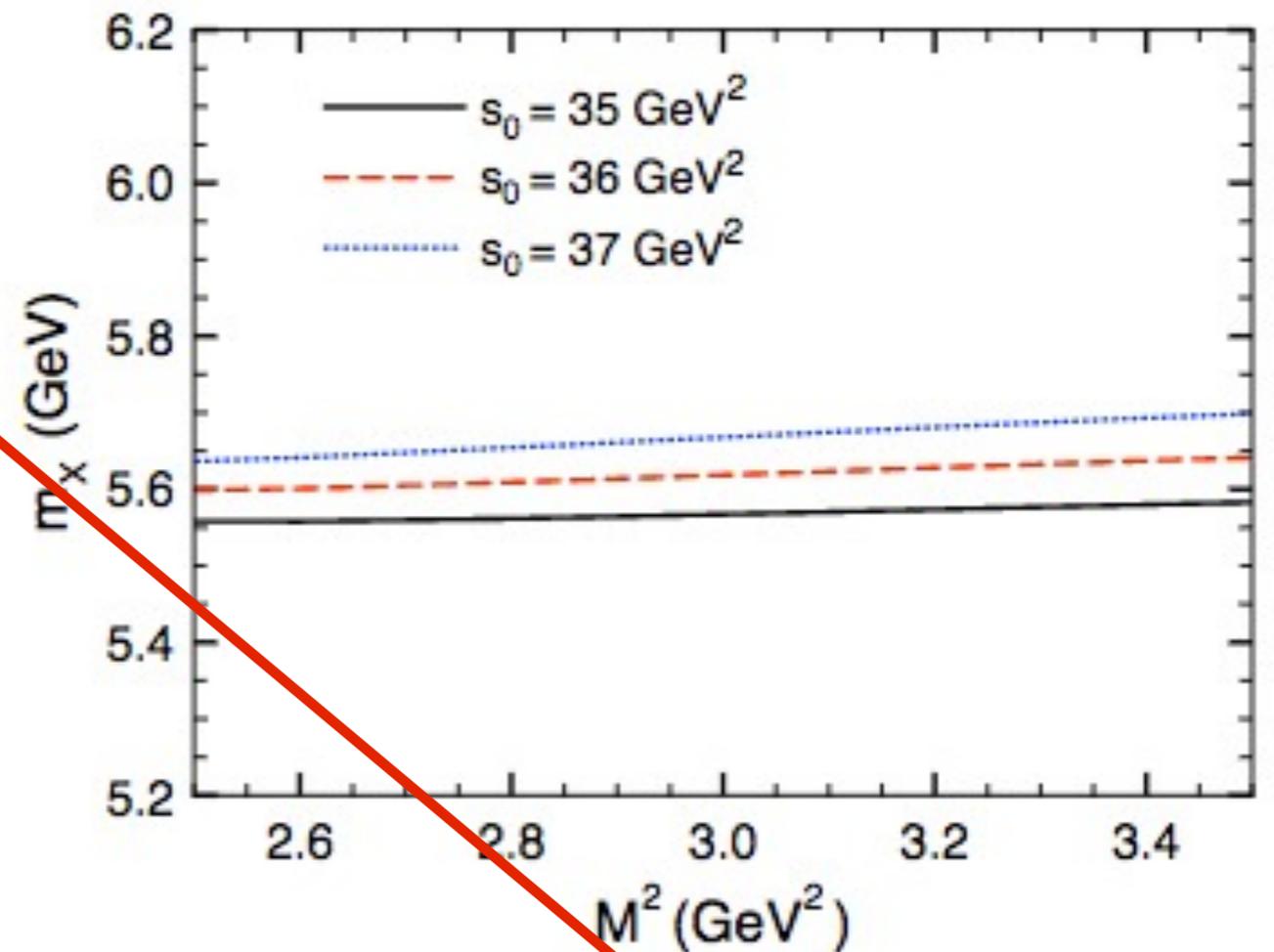
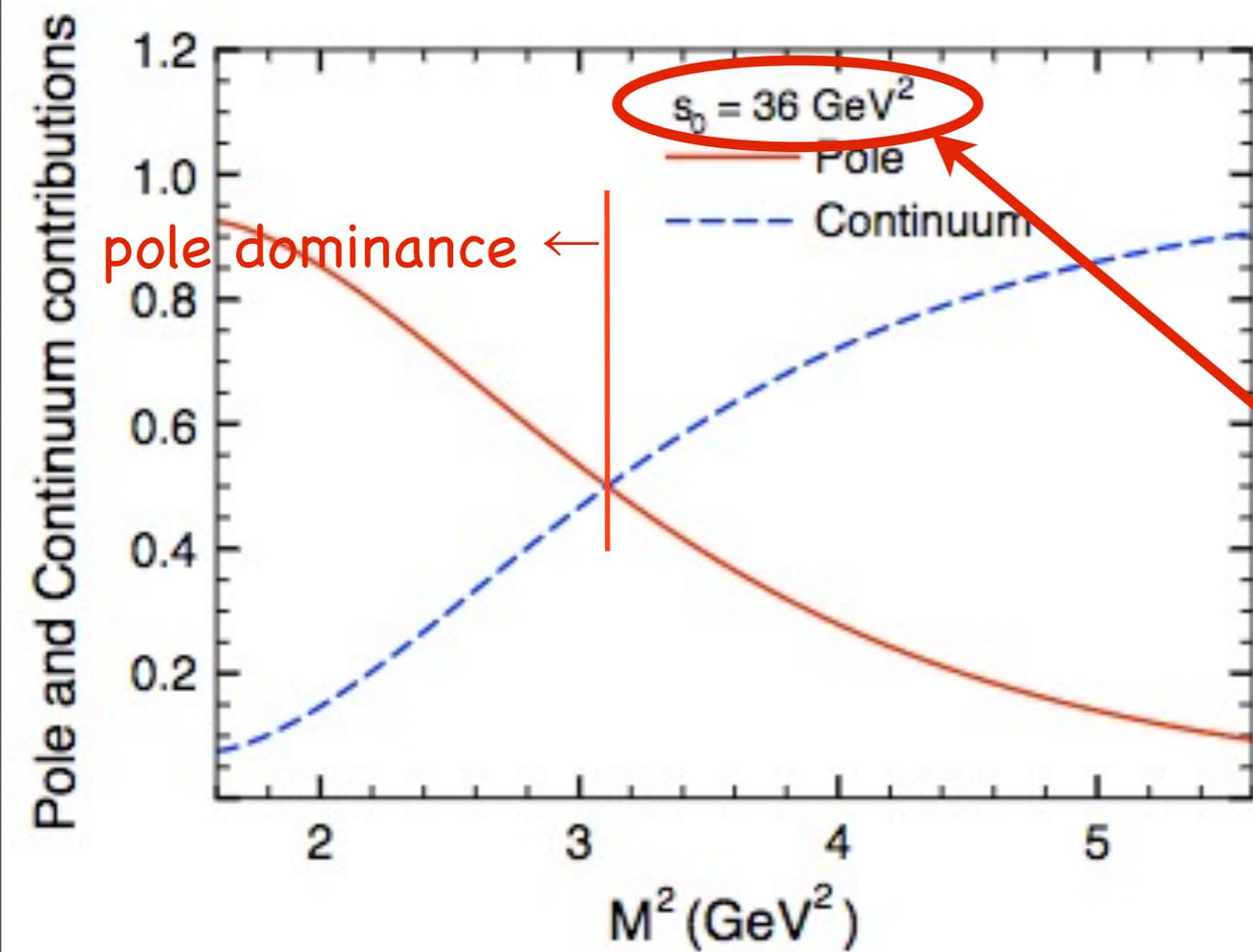
mass not compatible with 4-q or mol.

Burns & Swanson, arXiv:1603.04366; Guo et al., arXiv:1603.06316; Zanetti et al., arXiv:1602.09041; Wang & Zhu, arXiv:1602.08806; Chen & Ping, arXiv:1604.05651; Maiani et al., arXiv:1604.01731; Lu & Dong, arXiv:1603.06417; Albuquerque et al., arXiv:1604.05566

# QCDSR for $X^+(5568)$ as a tetraquark state

Khemchandani, MN, Zanetti: arXiv:1602.09041

$$j_S = \epsilon_{abc}\epsilon_{dec}(u_a^T C \gamma_5 s_b)(\bar{d}_d \gamma_5 C \bar{b}_e^T)$$



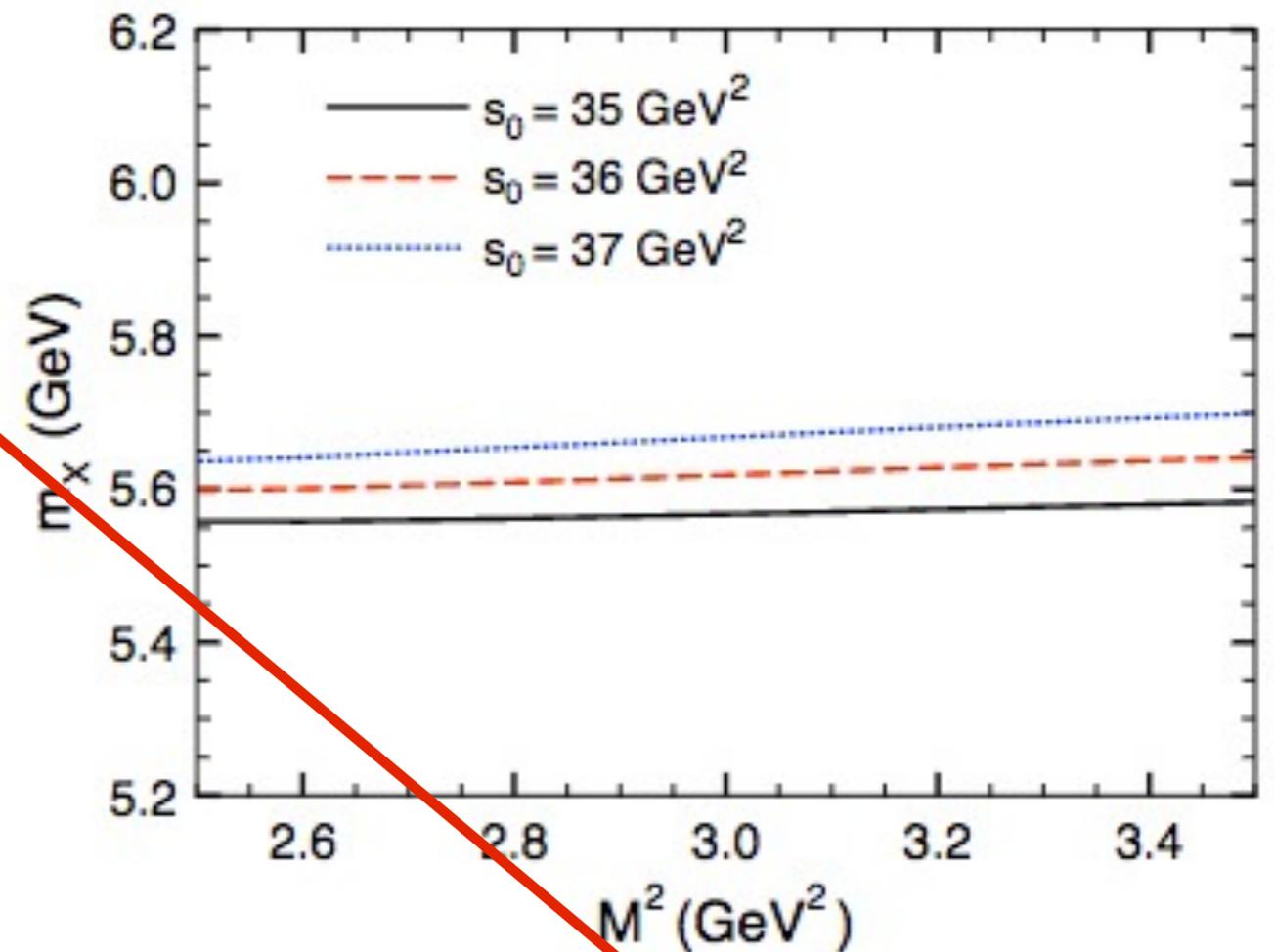
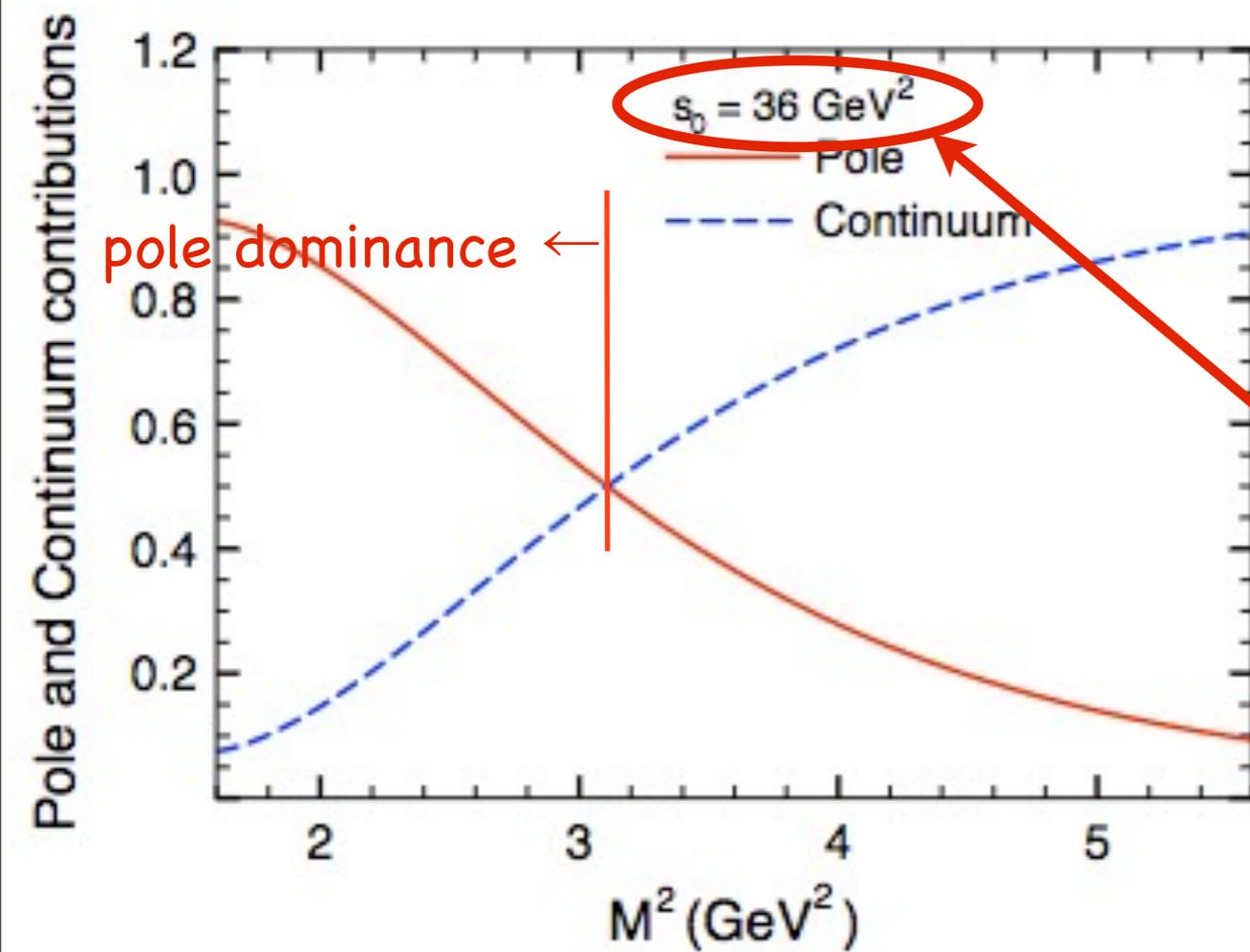
$$m_X = (5.58 \pm 0.17) \text{ GeV}$$

$$s_0 \sim (m + 0.5 \text{ GeV})^2$$

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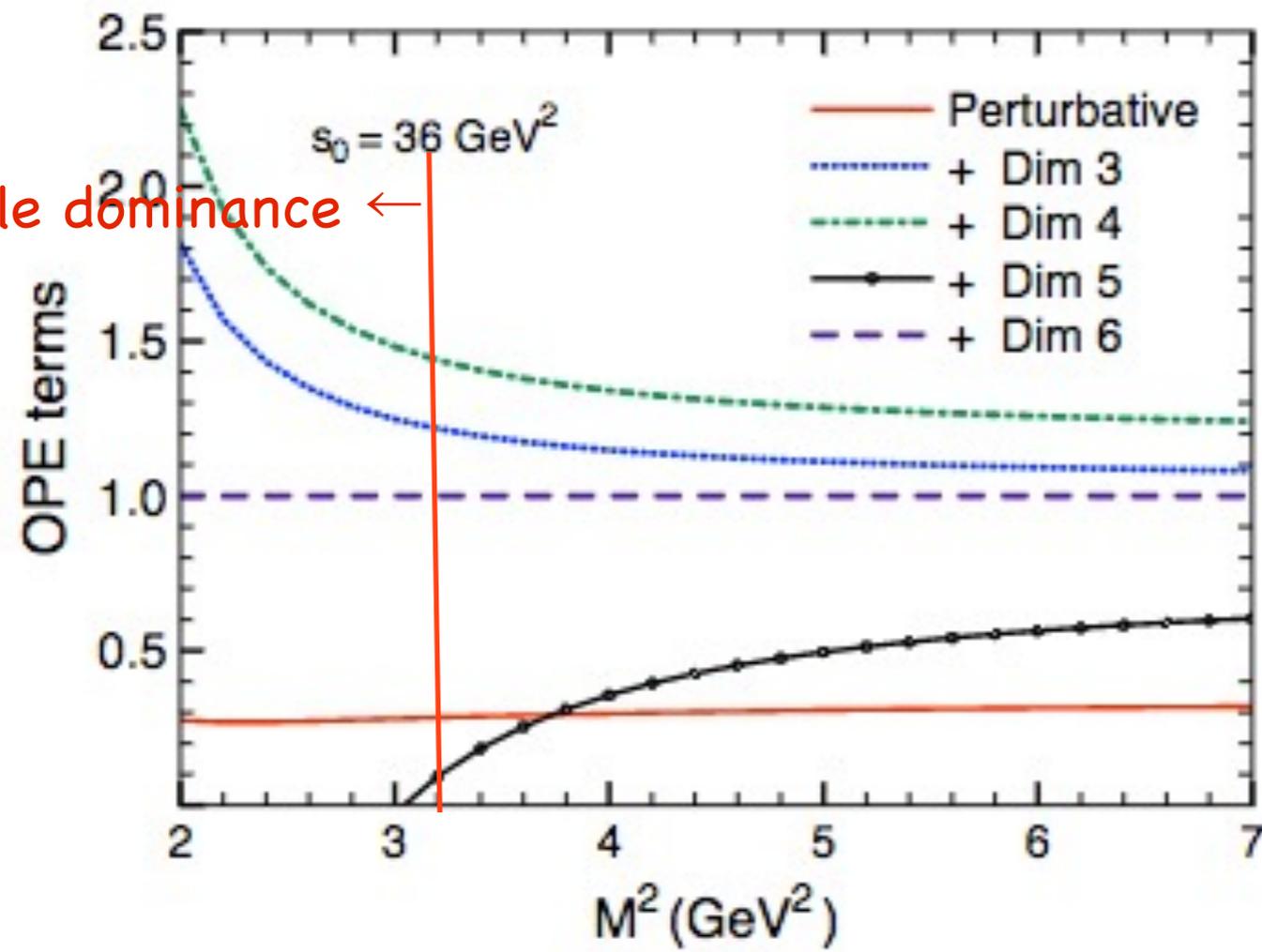


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OPE convergence?

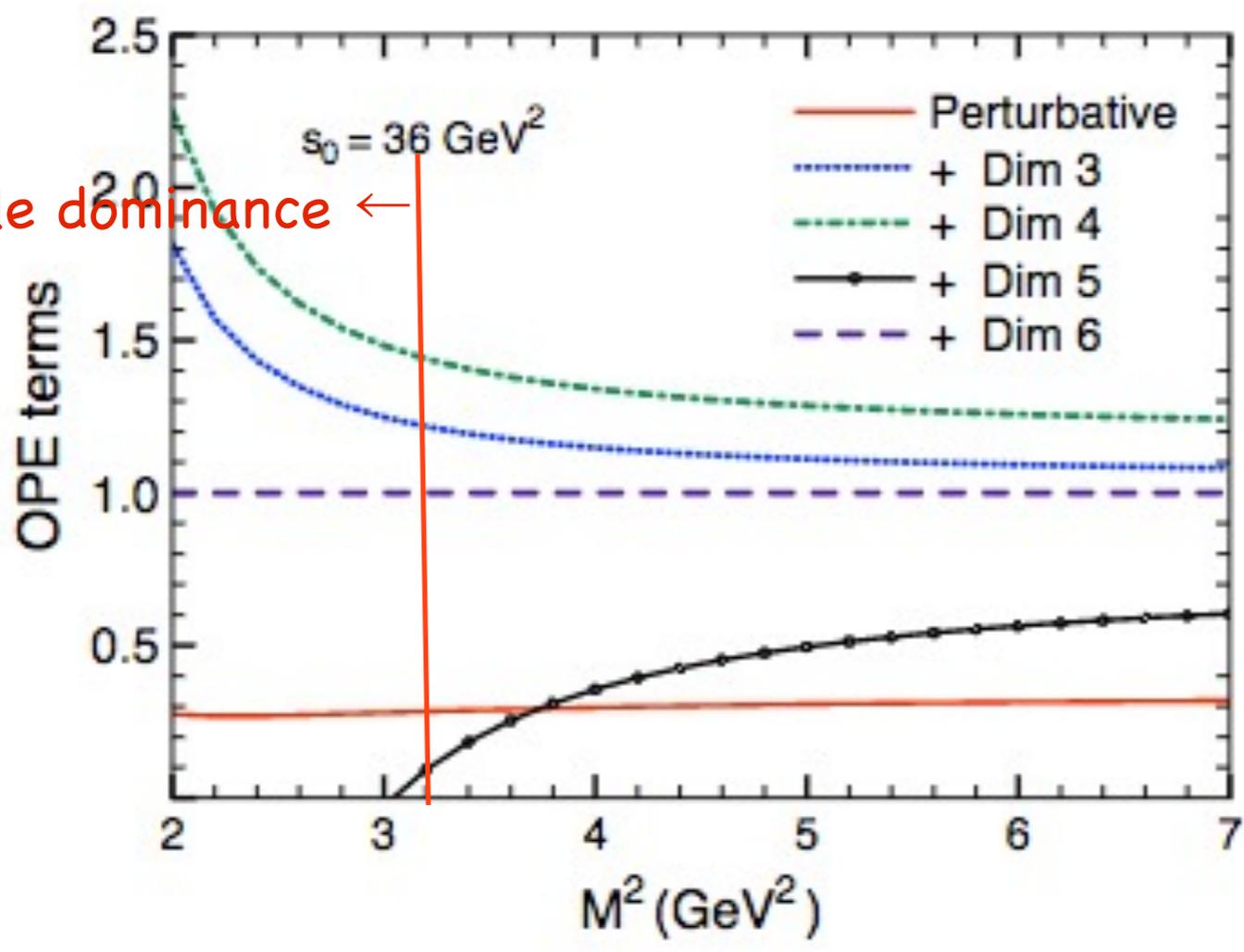
$$s_0 \sim (m + 0.5 \text{ GeV})^2$$

pole dominance ←



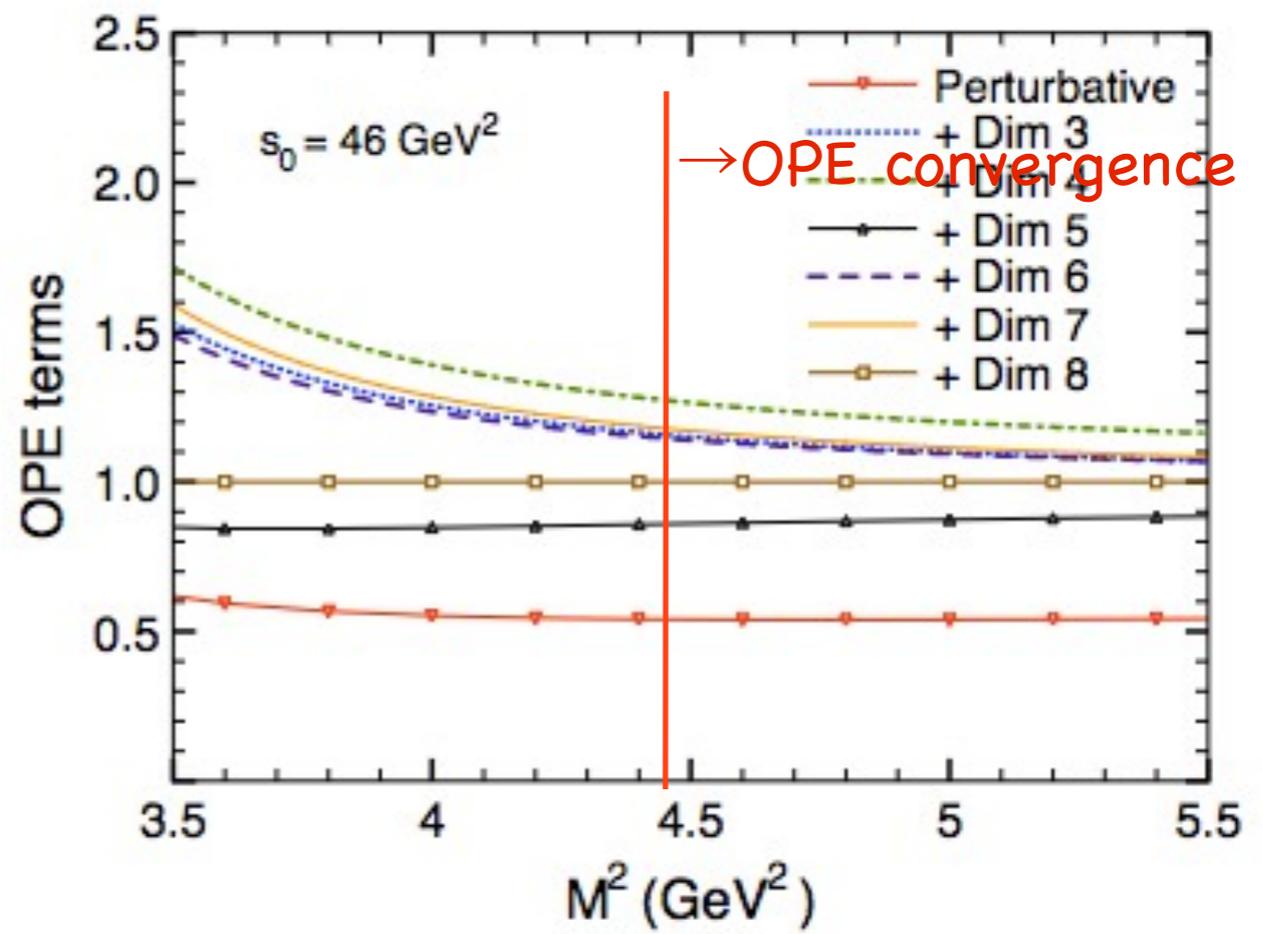
No OPE convergence  
for  $s_0 \approx 3.6 \text{ GeV}^2$

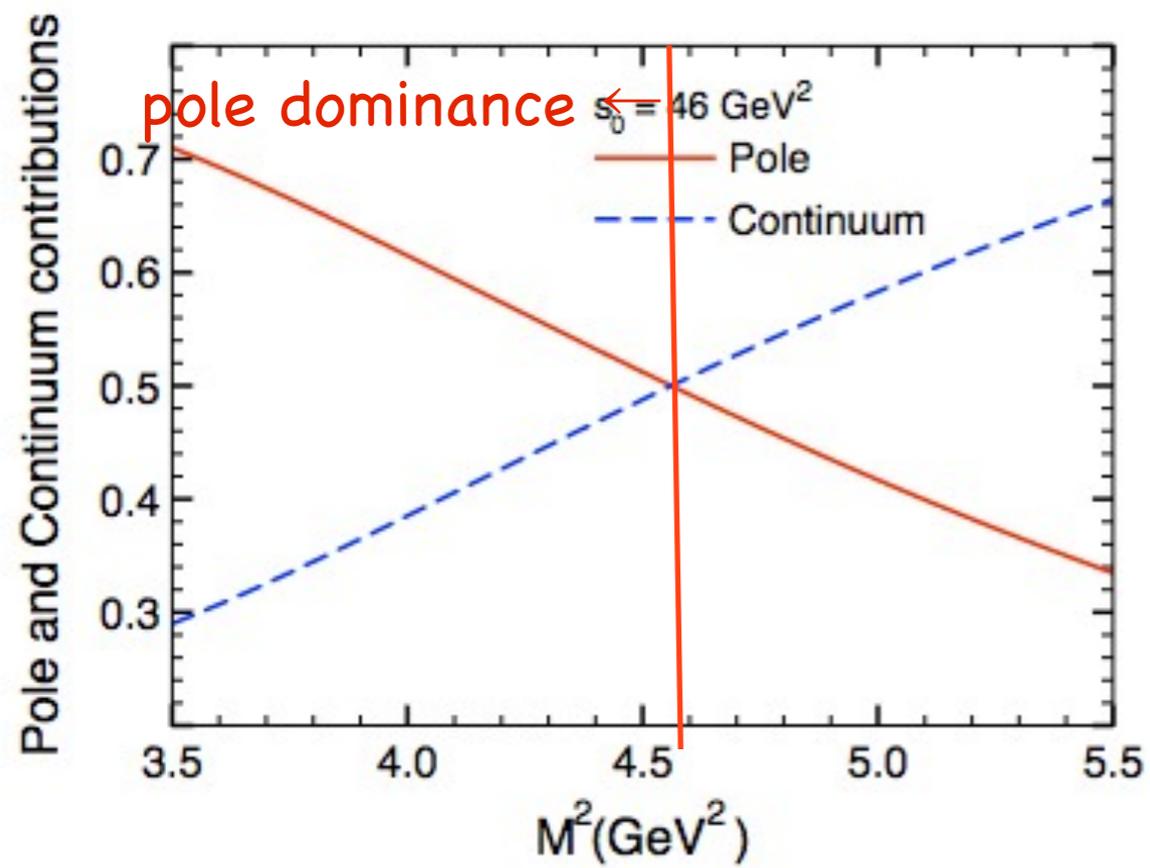
pole dominance ←



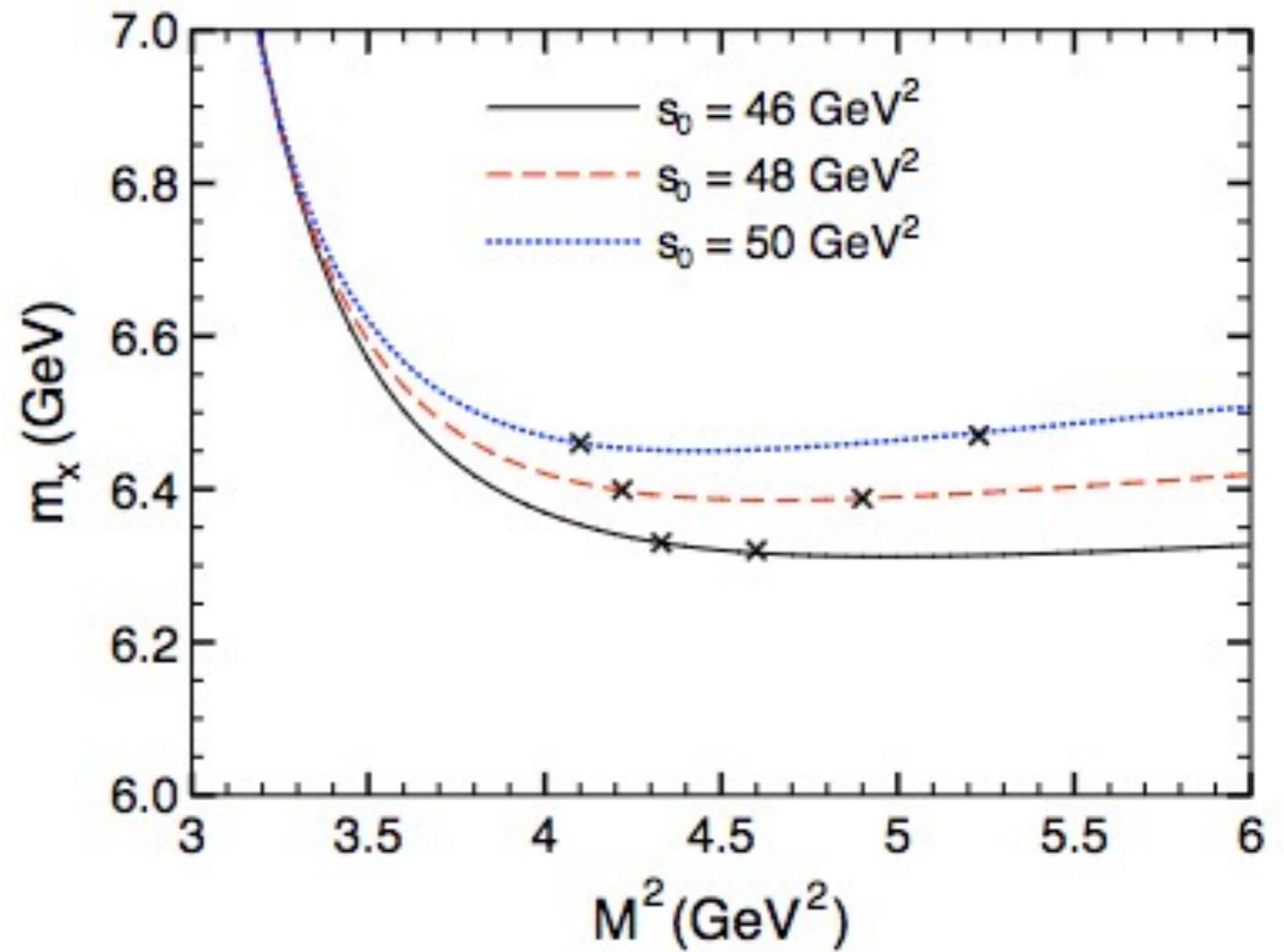
No OPE convergence  
for  $s_0 \approx 3.6$  GeV<sup>2</sup>

OPE convergence  
only for  $s_0 \geq 46$  GeV<sup>2</sup>

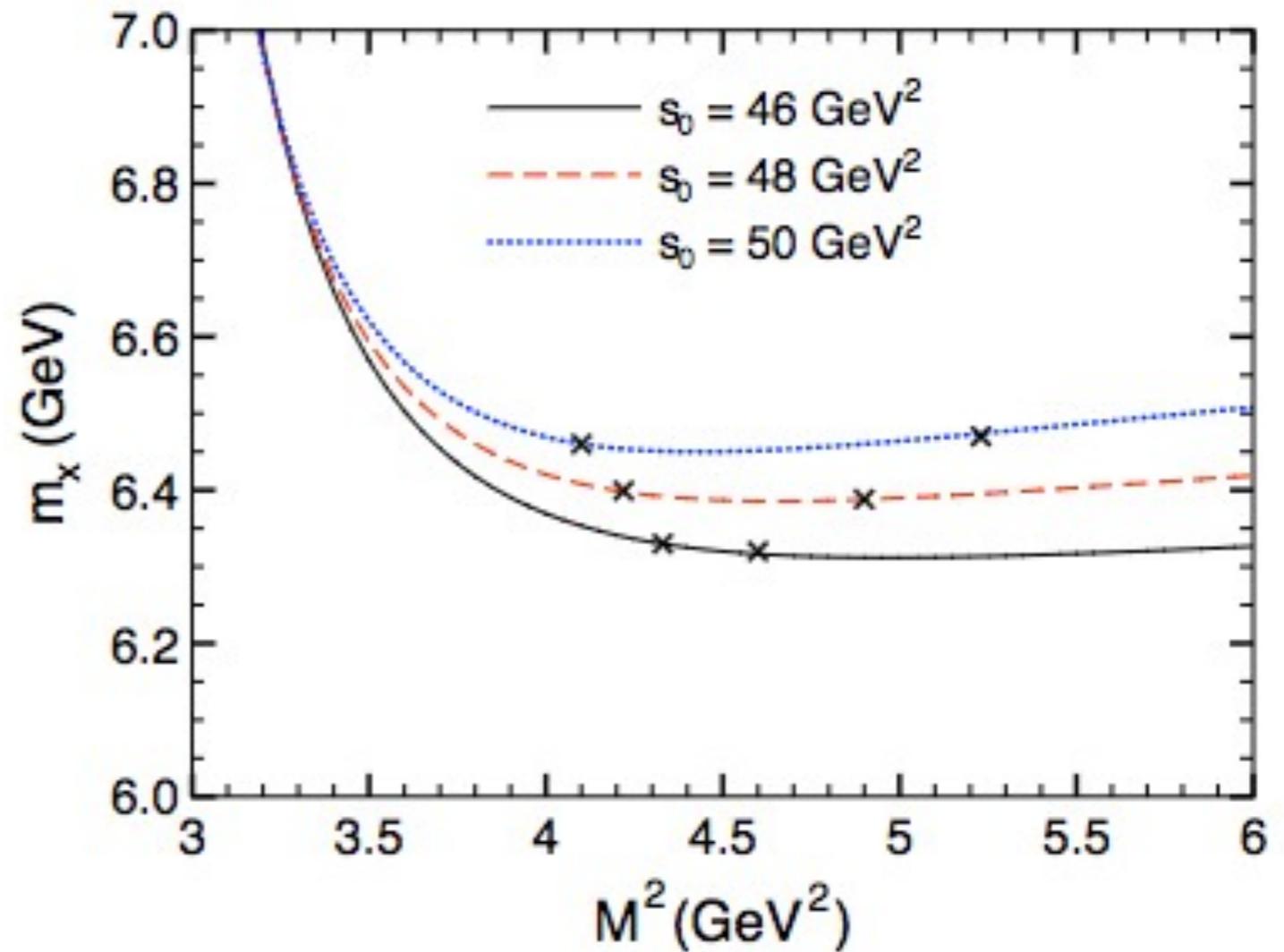
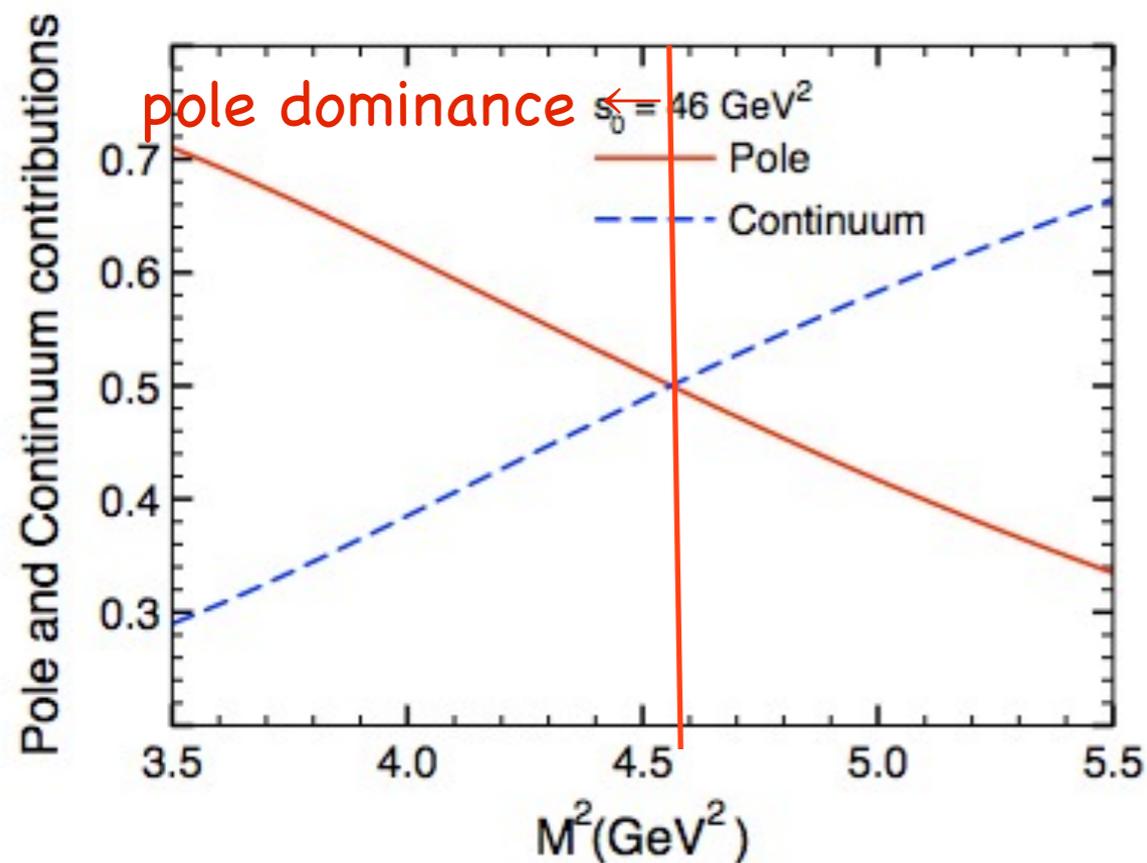




not compatible with  
 $X^+$  (5568) mass



$$m_X = (6.39 \pm 0.10) \text{ GeV}$$



not compatible with  
 $X^+$  (5568) mass

$$m_X = (6.39 \pm 0.10) \text{ GeV}$$

## Conclusions for $X^+(5568)$

- probably not a real state

# Conclusions

$X(3872) \rightarrow$  mixture  $\chi_{c1}$  and a  $D^*\bar{D}$  molecule

$Z_c^+(3900) \rightarrow J^P=1^+$  tetraquark state

$Z_c^+(3900)$  and  $Z_c^+(3885) \rightarrow$  not the same state

$Z_c^+(4025) \rightarrow J^P=1^+,2^+ D^*\bar{D}^*$  resonance, or D-wave background

- $Z^+$  states need confirmation. A bump in the spectra near the threshold does not indicate, necessarily, the existence of a state

$X^+(5568) \rightarrow$  needs confirmation, probably not a real state

Thank you

Θ ε ν κ υ

Questions?

