



# Number and density of quark-gluon strings and collective effects in hadron collisions

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*XXII Quark Confinement and the Hadron Spectrum*

Thessaloniki (Greece) from 29th August to 3rd September 2016, ROOM, Clio, (*Makedonia Palace*), 16:40 – 17:00, Friday 02/09/2016

<https://indico.cern.ch/event/353906/>

# Outline

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1) Introduction (motivation)

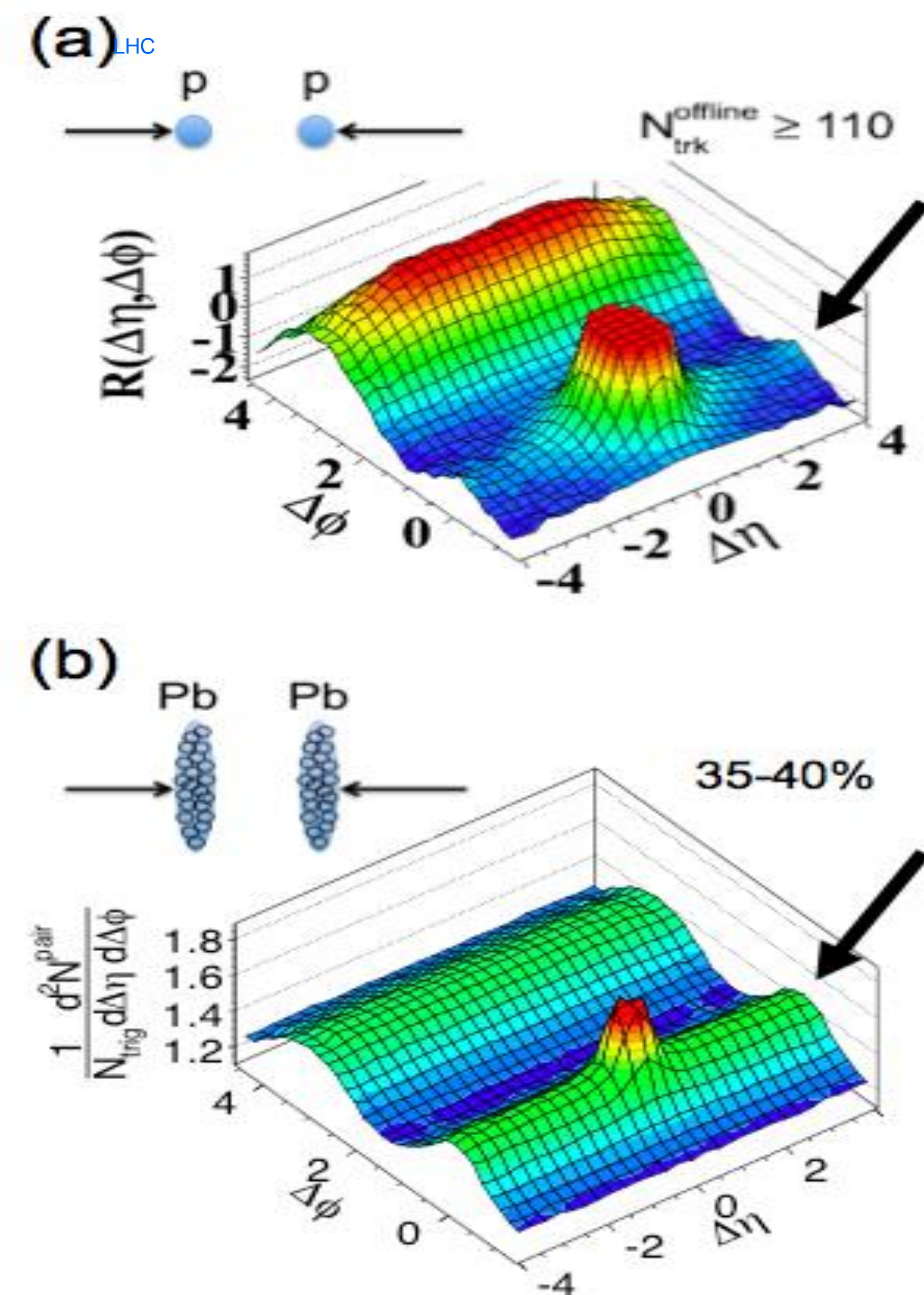
2) Estimates of:

- Number of MPIs from PYTHIA
- Constraints on number of strings in percolation approach basing on the onset of ridge in Au+Au collisions at RHIC
- The multipomeron exchange model with string fusion phenomenon

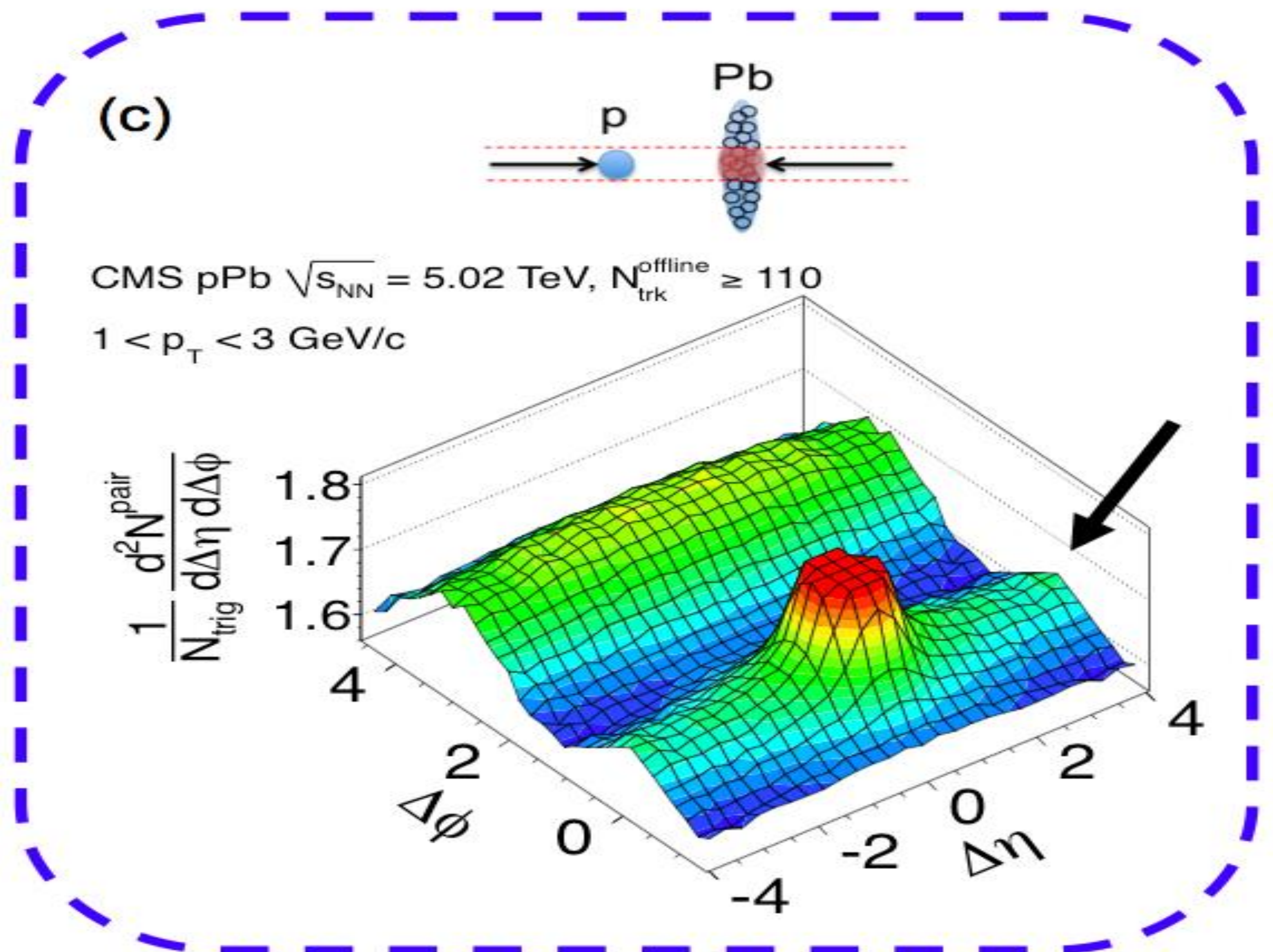
3) Conclusions



# Unexpected long-range correlations observed in pp and p-Pb similar to Pb-Pb collisions



JHEP 09 (2010) 091  
Eur. Phys. J. C 72  
(2012)



Phys. Lett. B 718 (2013) 795

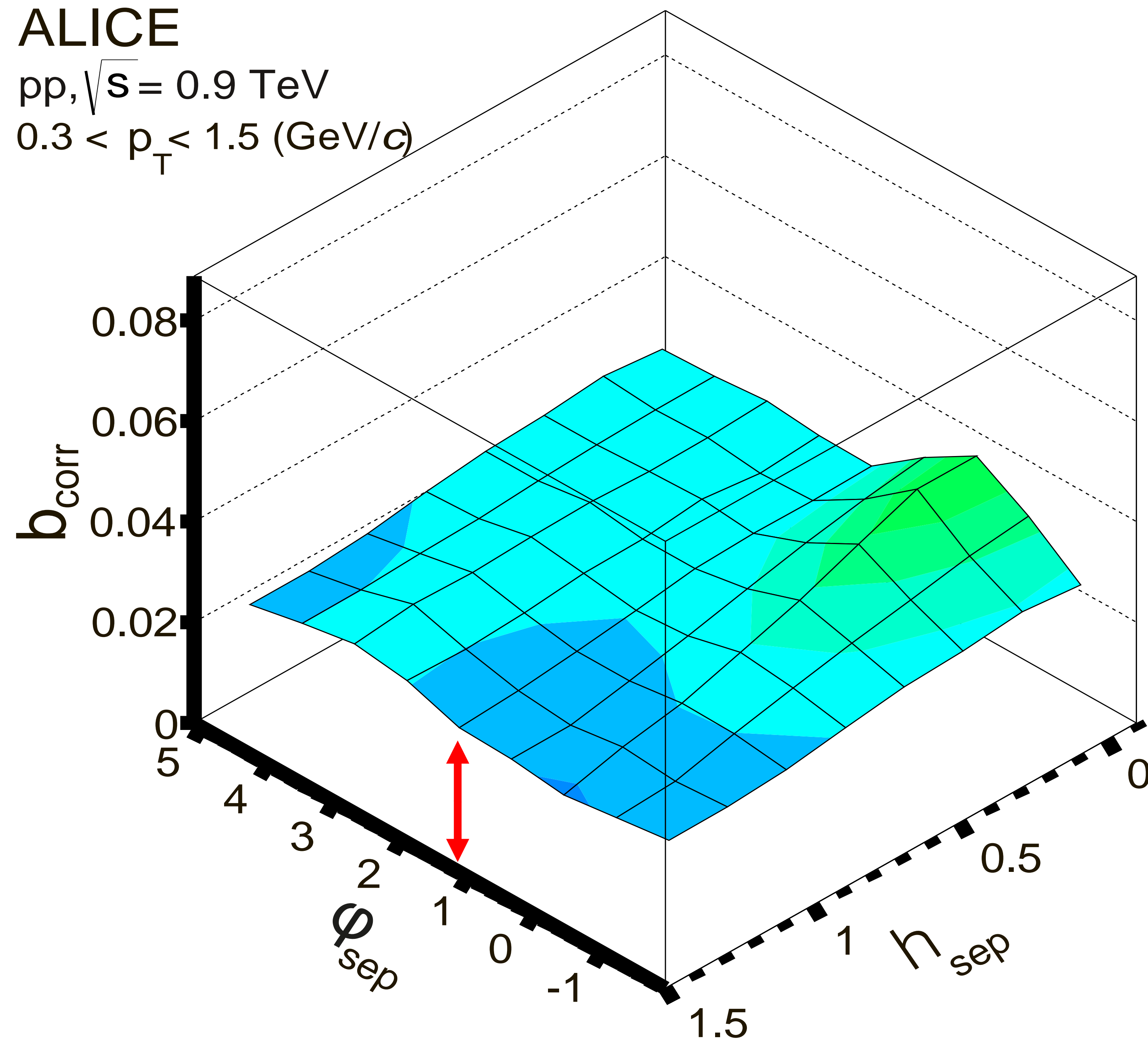
arXiv:1210.5482 [nucl-ex]



# Forward-Backward multiplicity correlations in pp@LHC

ALICE

pp,  $\sqrt{s} = 0.9$  TeV  
 $0.3 < p_T < 1.5$  (GeV/c)

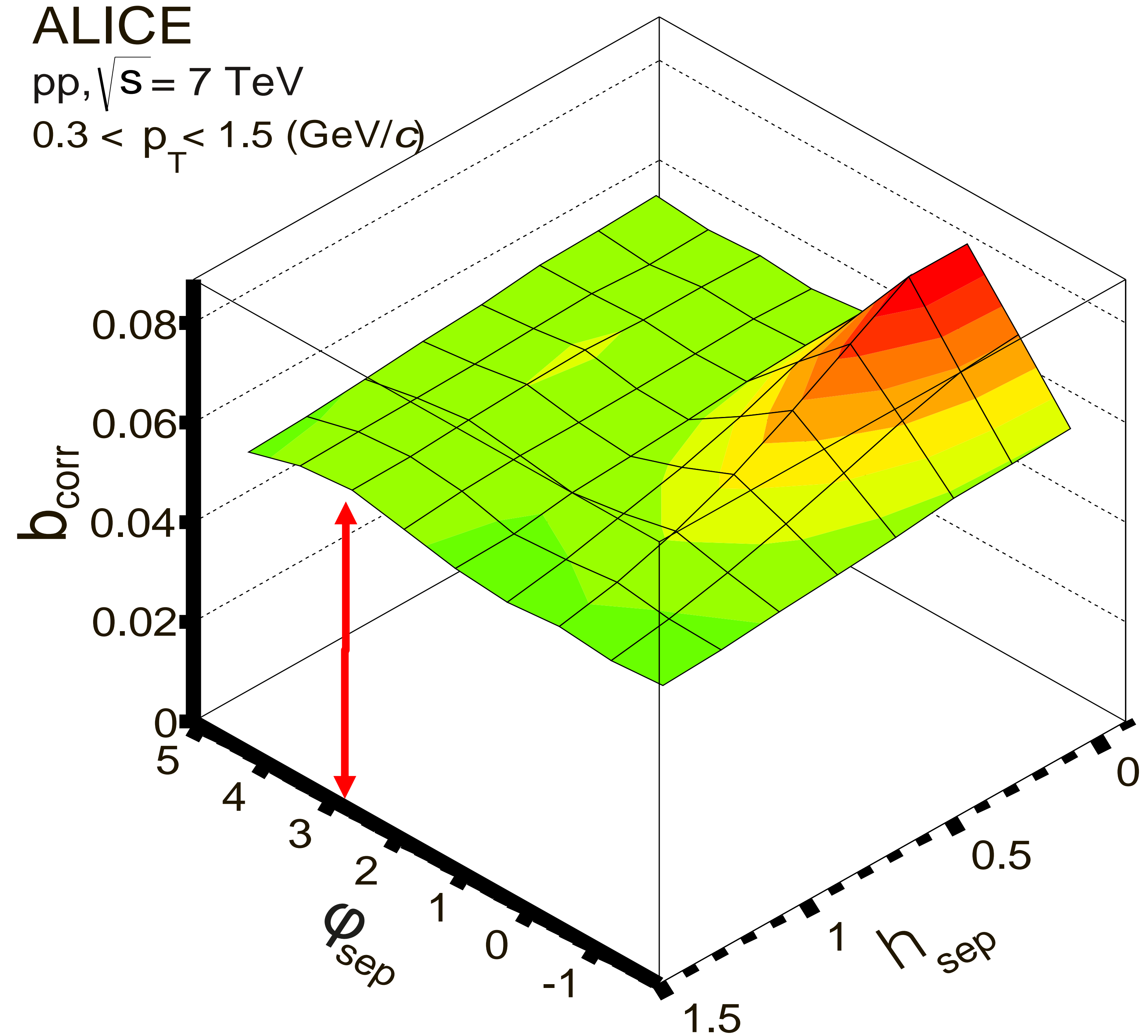


(a)

$\sqrt{s} = 0.9$  TeV

ALICE

pp,  $\sqrt{s} = 7$  TeV  
 $0.3 < p_T < 1.5$  (GeV/c)



(b)

$\sqrt{s} = 7$  TeV

ALICE, JHEP 05 (2015) 097; arxiv:1502.00230

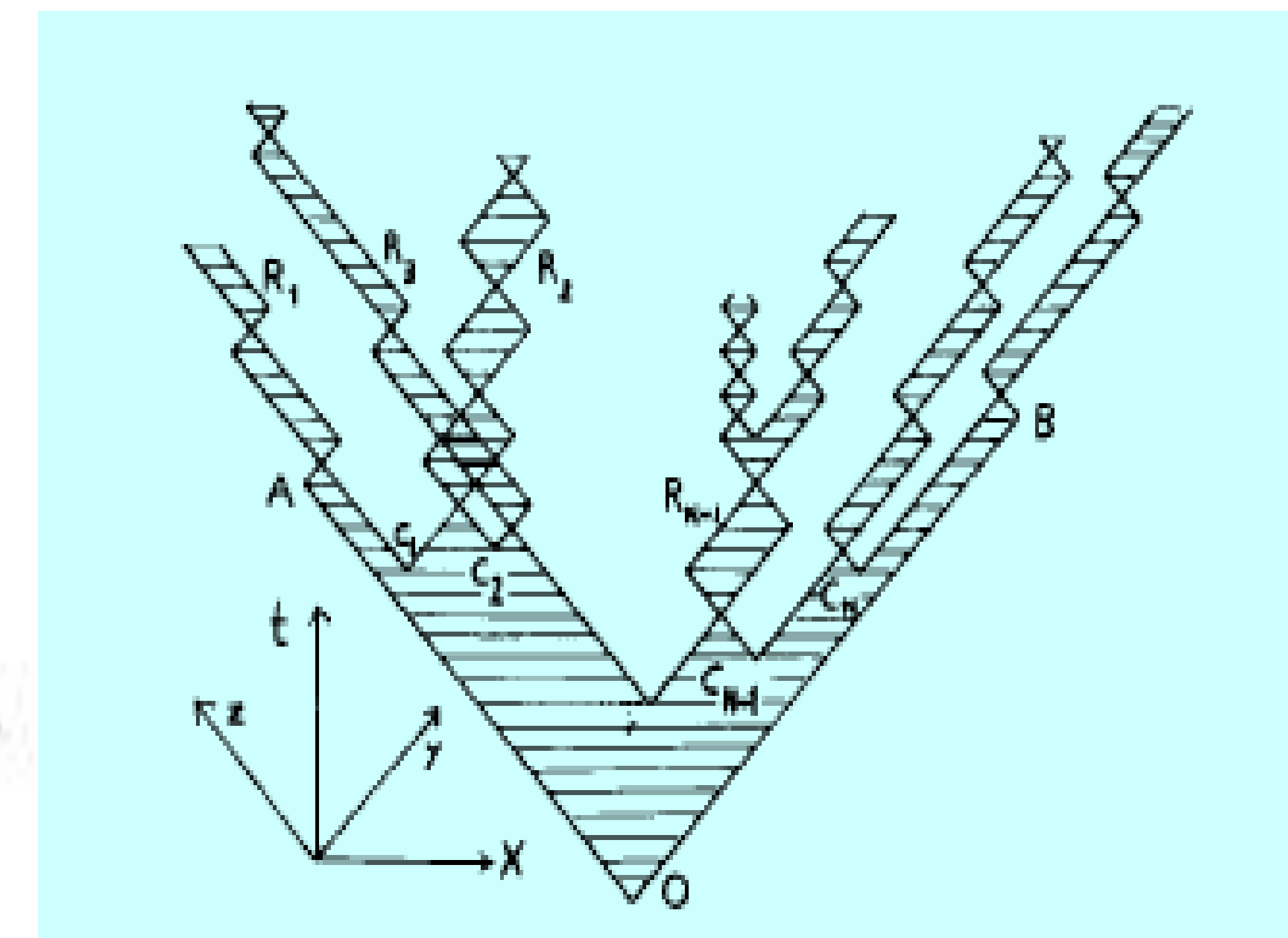
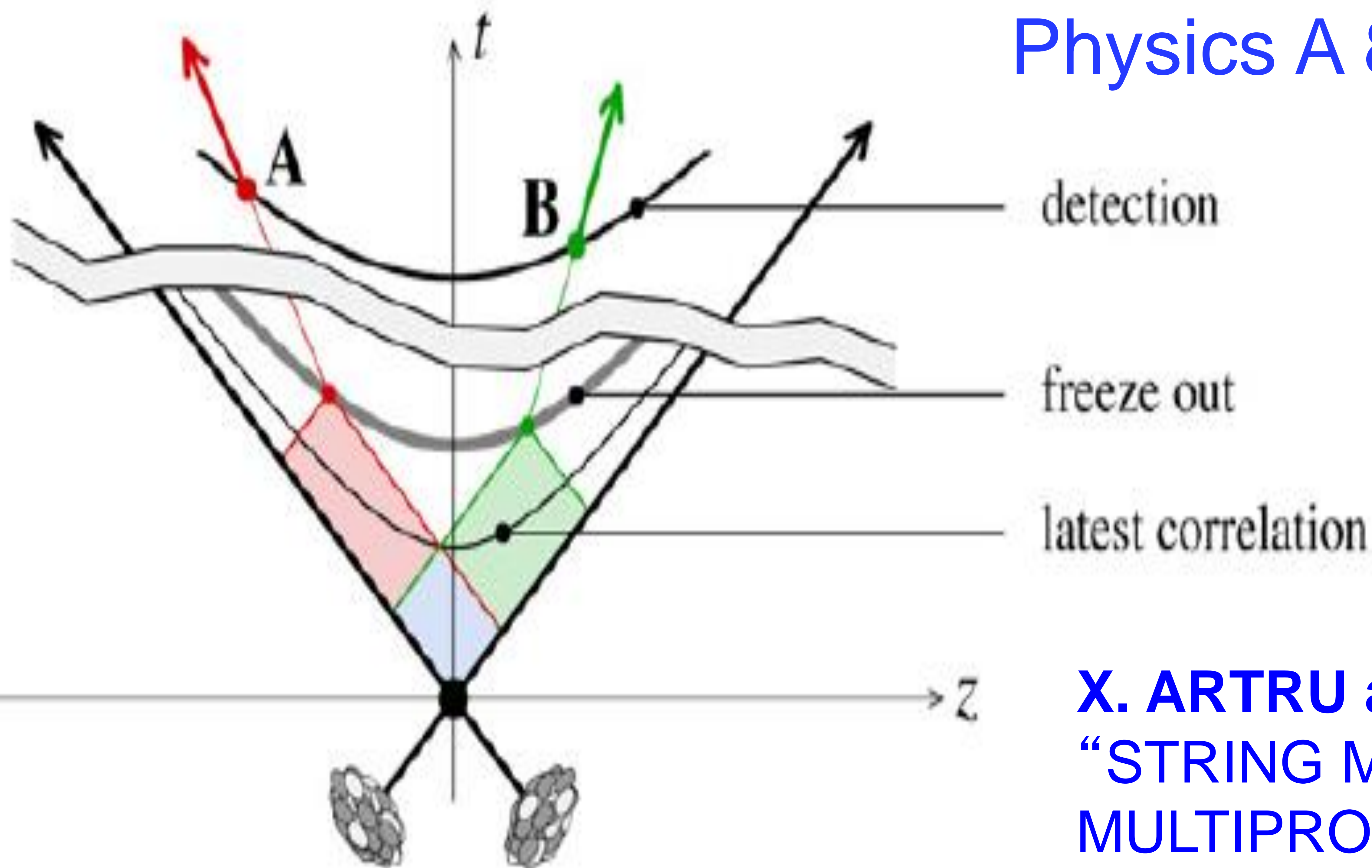
- **Short-Range(SR) and Long-Range(LR) components**
- **Strong energy dependence for LR)**
- **In PYTHIA the LR is dominated by MPI**

$$b_{\text{corr}} = \frac{\langle n_B n_F \rangle - \langle n_B \rangle \langle n_F \rangle}{\langle n_F^2 \rangle - \langle n_F \rangle^2}$$



# Long-Range Correlations: a general question - WHY?

A.Dumitru et al./ Nuclear  
Physics A 810 (2008) 91-108



X. ARTRU and G. MENNESSIER,  
“STRING MODEL AND  
MULTIPRODUCTION”,  
Nuclear Physics B70 (1974) 93-115

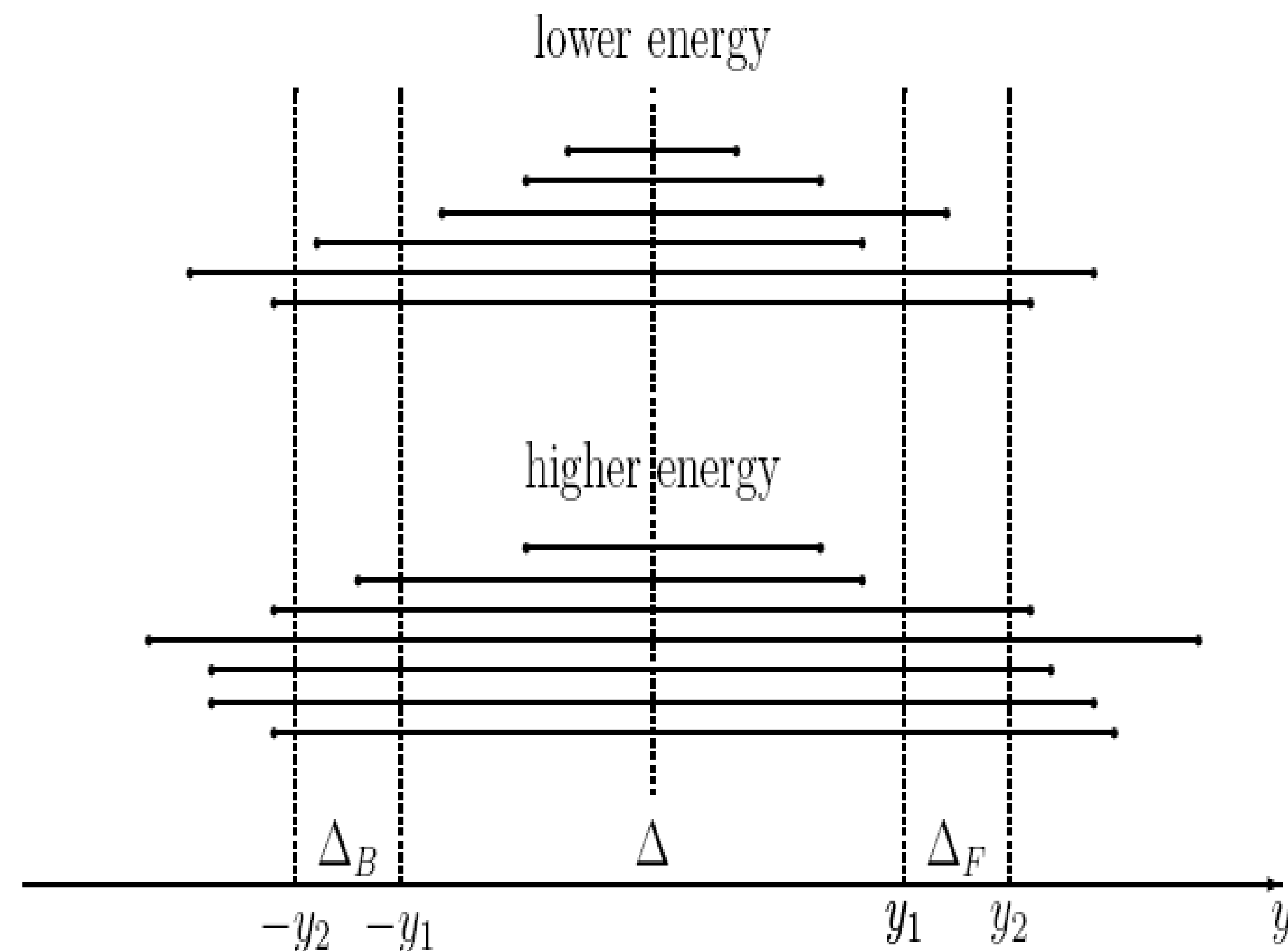
Causality requires that correlations –if they exist - of Long Range in rapidity between particles (A and B) must be made very early



# The initial conditions for the QGP formation in A-A collisions:

## Color string fusion phenomenon (SFM)

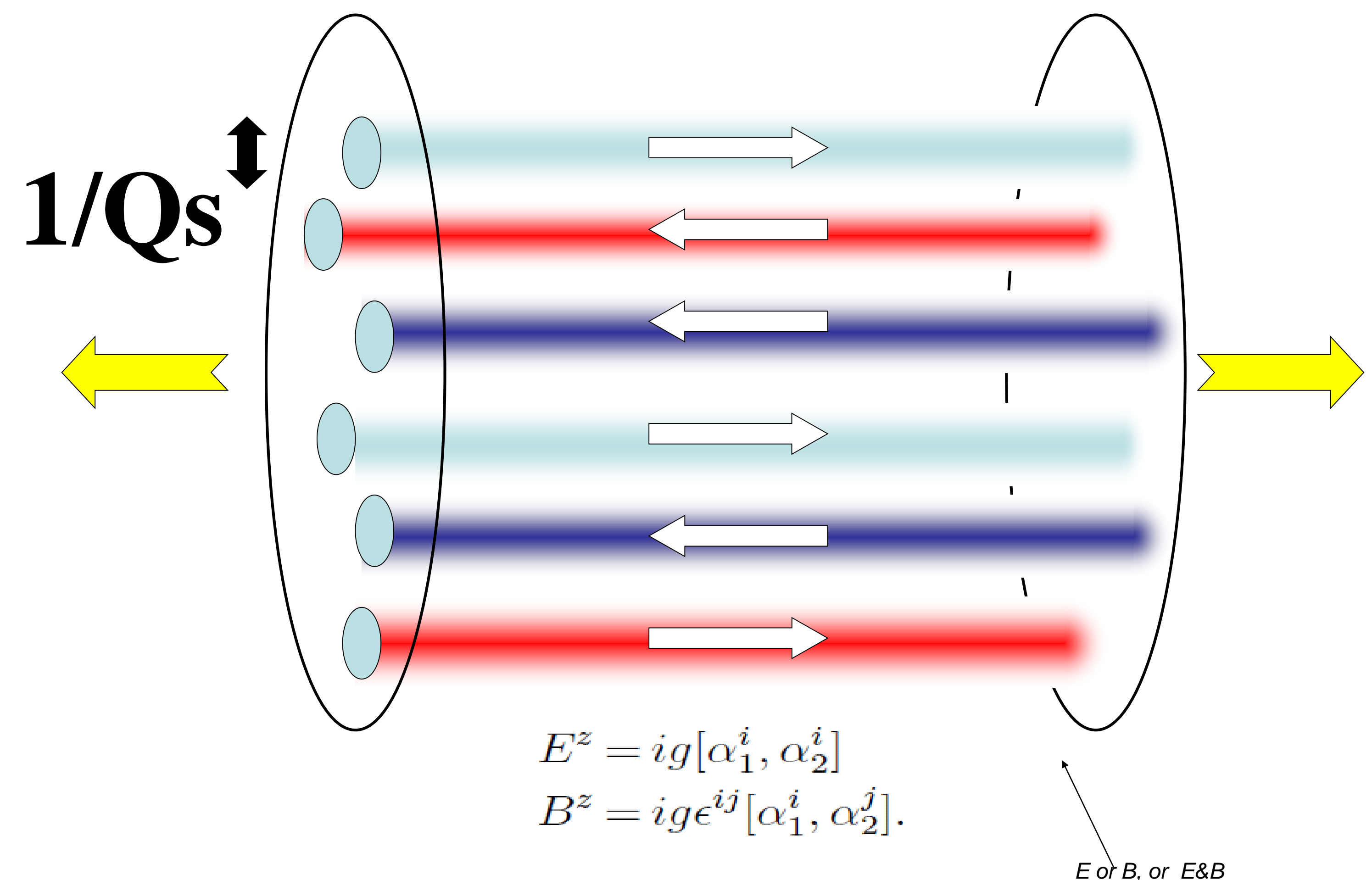
M.A.Braun and C.Pajares  
Phys. Lett. B287 (1992) 154;  
Nucl. Phys. B390 (1993) 542.



Schematics of strings formed just after the collision in cases of lower and of higher energy.

## Color Glass Condensate (CGC) and Glasmaflux tubes, L.McLerran,

Nucl.Phys.A699,73(2002);  
T. Lappi and L. McLerran,  
Nucl. Phys. A772 (2006) 200.



The color electric and magnetic flux tubes just after the collision (see [arXiv:0803.0410](https://arxiv.org/abs/0803.0410))

See talks at this conference%

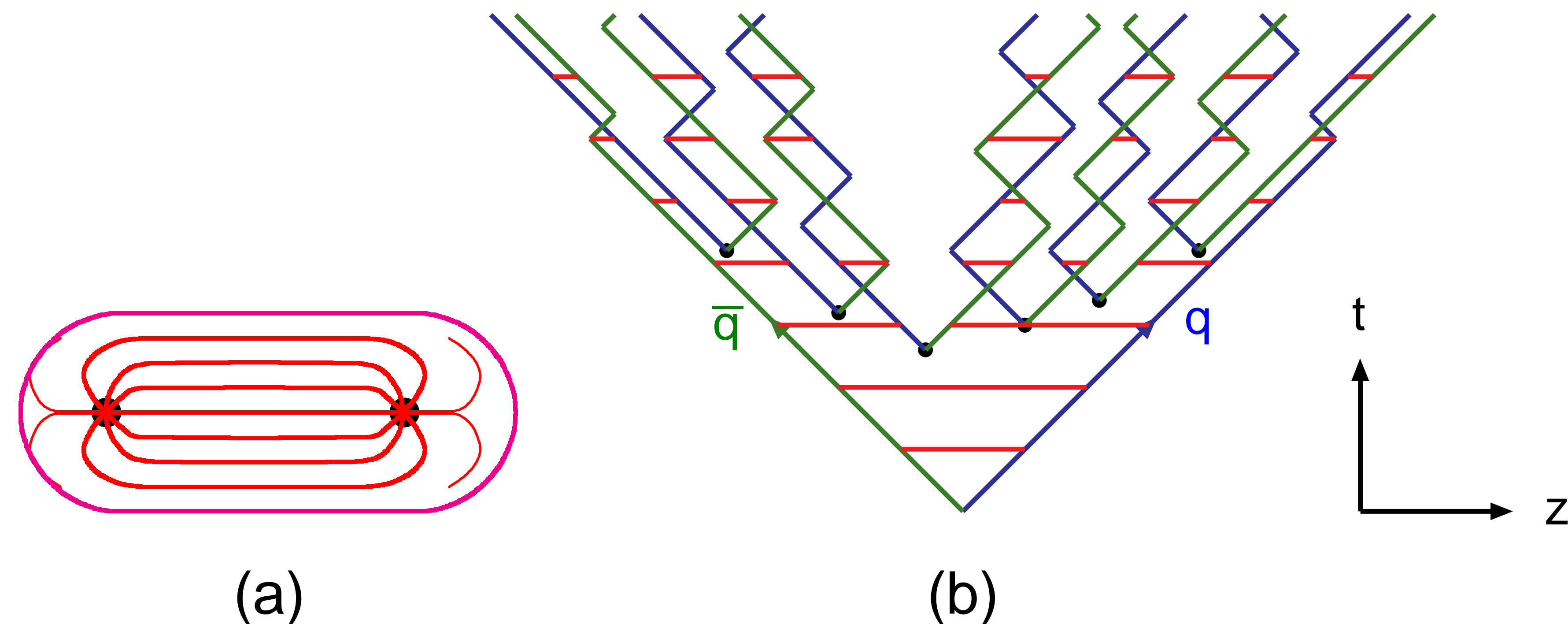
Tuomas Lappi, "Initial conditions in AA and pA collisions"

Soeren Schlichting, "Initial state and pre-equilibrium effects in small systems"

# Color-flux tubes as particle emitting sources: quark-gluon strings

## 2-stage scenario :

- **A.Capella, U.P.Sukhatme, C.-I.Tan and J.Tran Thanh Van,**  
Phys. Lett. **B81** (1979) 68;  
Phys. Rep.,236(1994) 225.
- **A.B.Kaidalov and K.A.Ter-Martirosyan ,**  
Phys.Lett., **117B**(1982)247.



See in: **Andy Buckley et al.,**  
**General-purpose event generators for LHC**  
**physics**

arXiv:1101.2599, 2011

# Application of string models

Investigations of the charged particles long-range multiplicity correlations, measured for well separated rapidity intervals, can give us information on the number of emitting centers and hence on the fusion of colour strings[2,3].

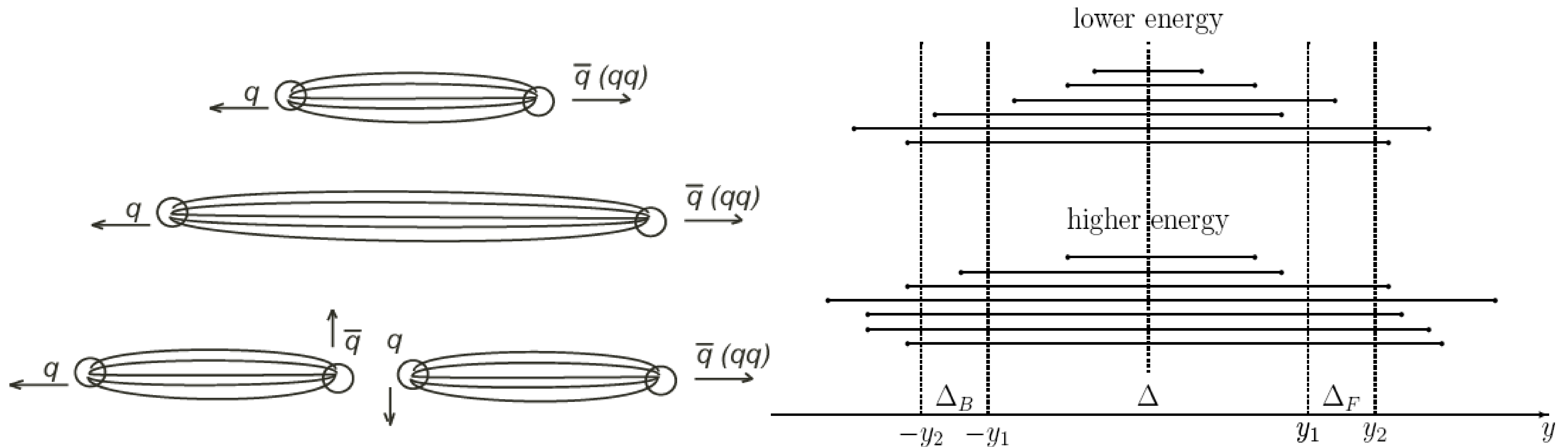


Fig.1. Quark-gluon strings and schematics for studies of Long-Range Correlations (LRC) using forward ( $\Delta_F$ ) and backward ( $\Delta_B$ ) rapidity windows [2]

[2] **M.A.Braun, C.Pajares and V.V.Vechernin**, Low  $p_T$  Distributions in the Central Region and the Fusion of Colour Strings, Internal Note/FMD ALICE-INT-2001-16

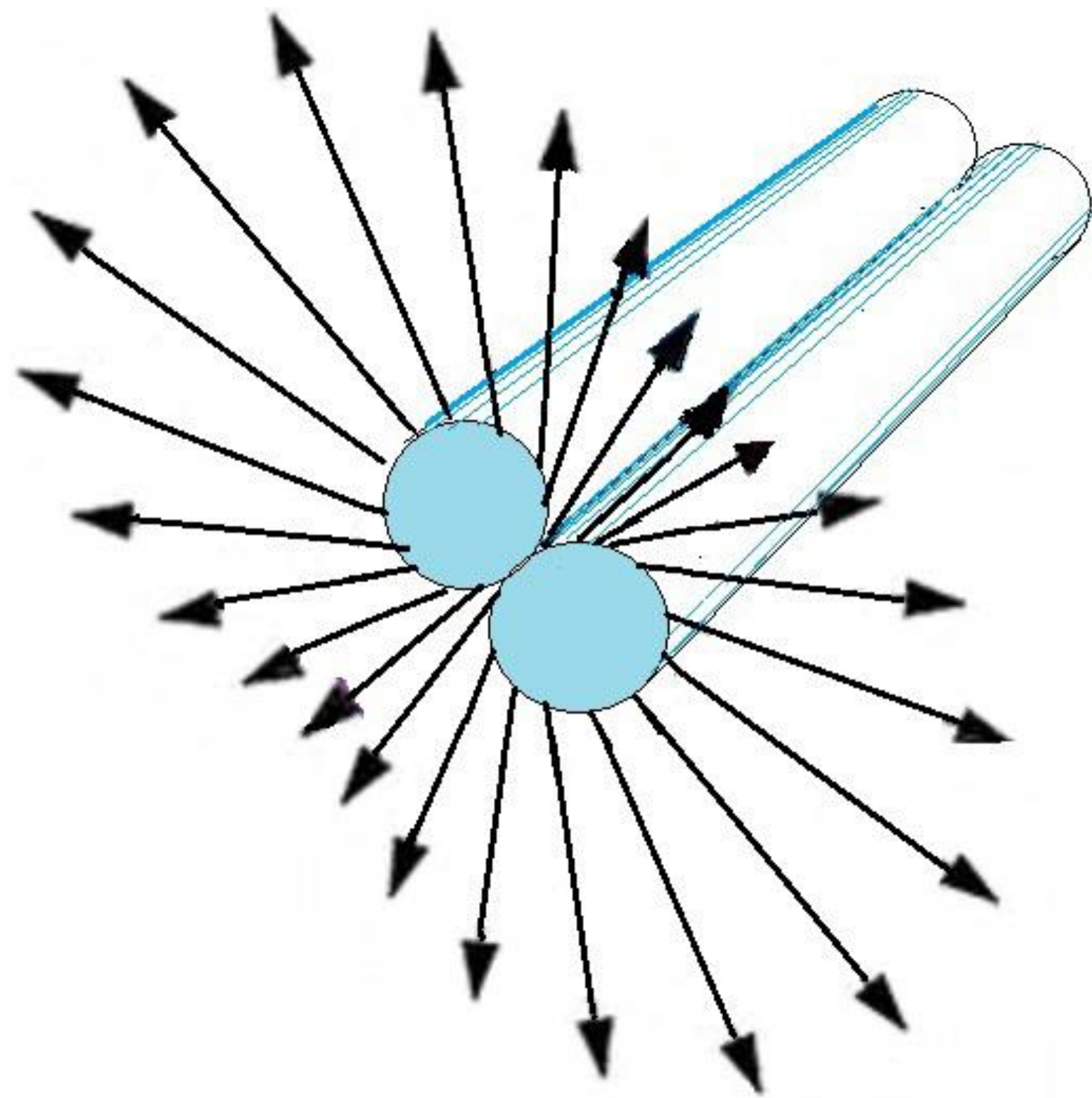
[3] **А. Абрамовский, О.В. Канчели**// Письма в ЖЭТФ, т.31, 566, 1980



# Do these color strings interact ?

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**V.A. Abramovsky, O.V. Kanchely,**  
JETP letters 31, (1980) 566;  
**Abramovskii V. A., Gedalin E. V.,**  
**Gurvich E. G., Kancheli O. V.,**  
JETP Lett., vol.47, 337-339, 1988.



*Attraction or repulsion depending  
on the directions of color fluxes*

*$\mathbf{q}$  -- momentum of particle*

*$\mathbf{k}$  -- momentum of the boosted  
string*

$$F_1(\varphi, y) \sim 1 + a_1(y) \cos^2 \phi,$$



# Color string fusion phenomenon

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**SFM: M.A.Braun and C.Pajares,**

Phys. Lett. B287(1992) 154;

Nucl. Phys. B390} (1993)

542, 549

**Colour rope model**

**Biro, T.S. *et al.*** Nucl.Phys. B245  
(1984) 449-468

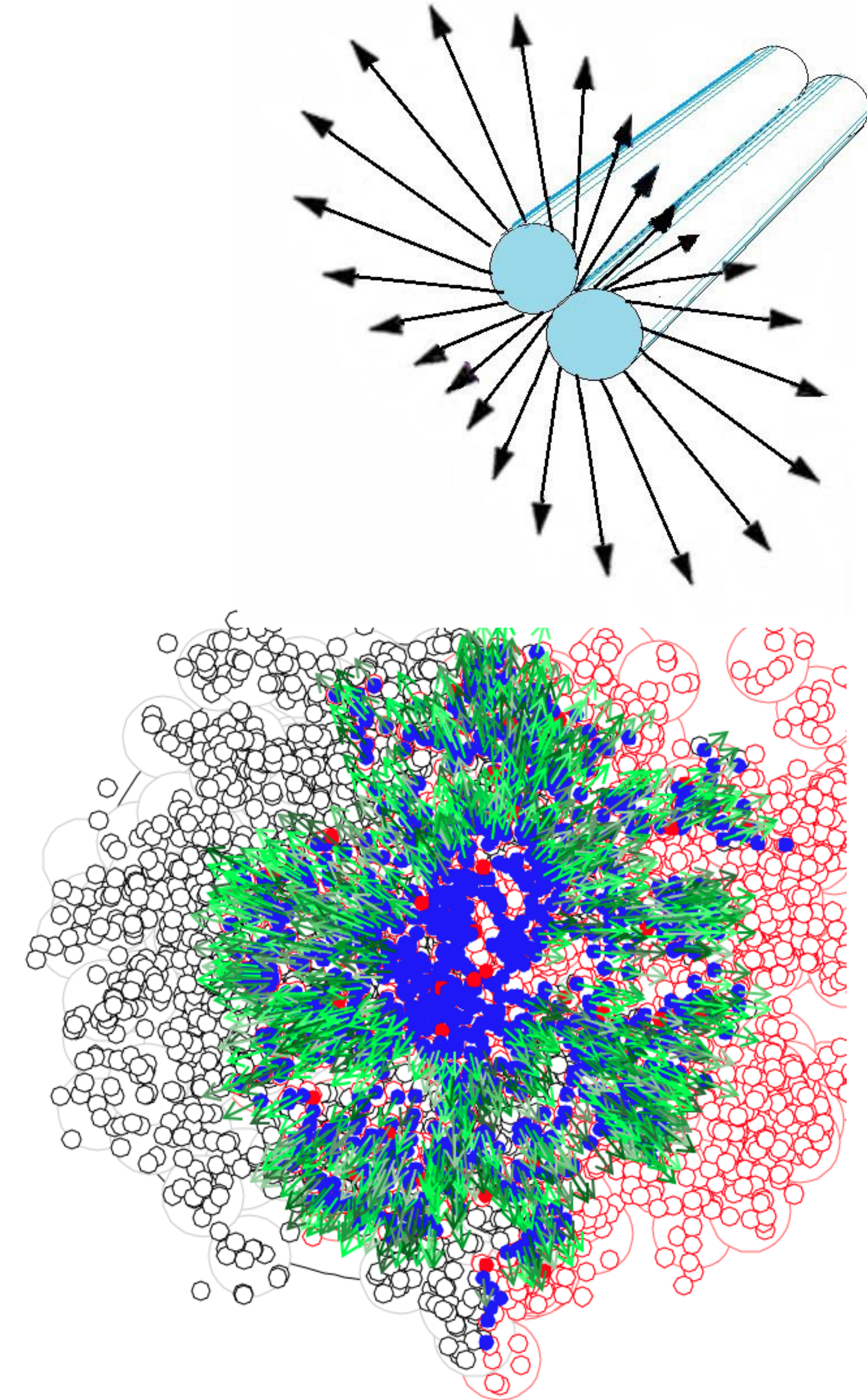
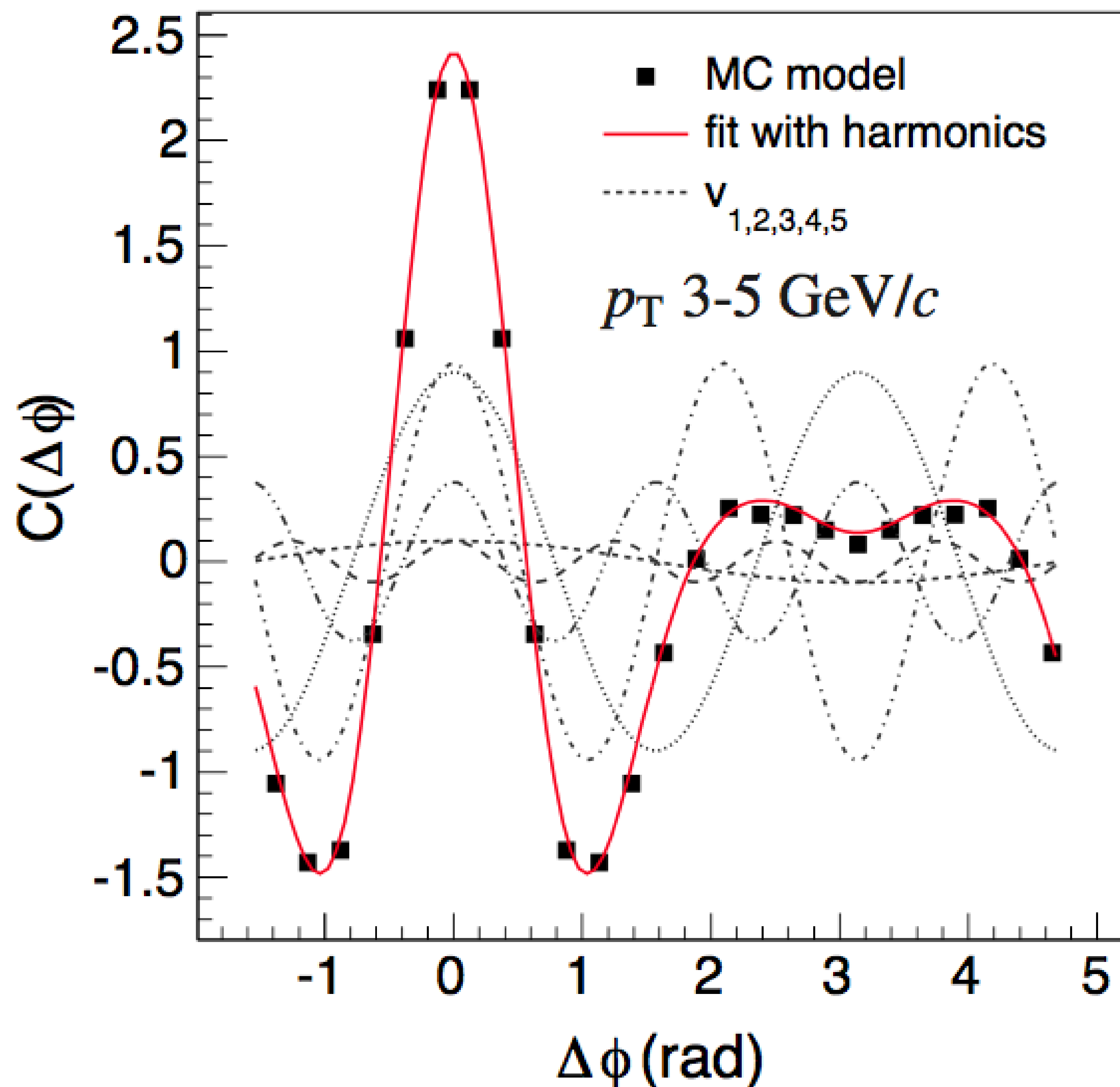
**C.Bierlich et al.,** arXiv:1412.6259  
[hep-ph] (The DIPSY model)

- N.S.Amelin, M.A.Braun and C.Pajares, Phys. Lett. {\bf B306} (1993) 312;\\ Z.Phys. {\bf C63} (1994) 507.
- N.S.Amelin, N.Armesto, M.A.Braun, E.G.Ferreiro and C.Pajares, Phys. Rev. Lett. {\bf 73} (1994) 2813.
- N.Armesto, M.A.Braun, E.G.Ferreiro and C.Pajares, Phys. Rev. Lett. {\bf 77} (1996) 3736.
- M.Nardi and H.Satz, Phys. Lett. {\bf B442} (1998) 14;\\ H.Satz, Nucl. Phys. {\bf A661} (2000) 104c.
- M.A.Braun, C.Pajares and J. Ranft, Int. J. of Mod. Phys. {\bf A14} (1999) 2689.
- M.A.Braun and C.Pajares, Eur. Phys. J. {\bf C16} (2000) 349.
- M.A.Braun, R.S.Kolevatov, C.Pajares, V.V.Vechernin, Eur.Phys.J.C.32.535-546(2004)
- N.Armesto, M.A.Braun, E.G.Ferreiro, C.Pajares, Z.Phys.C., 67, 489-493, (1995),
- M.A.Braun, C.Pajares Phys.Rev.Let, v.85.no.23, 4864-4867, 2000
- M.A.Braun, C.Pajares Eur.Phys.J.C16, 349-359(2000)

See the talk on string fusion by V.Kovalenko at this conference



# Repulsion of quark-gluon strings and flow harmonics: MC model



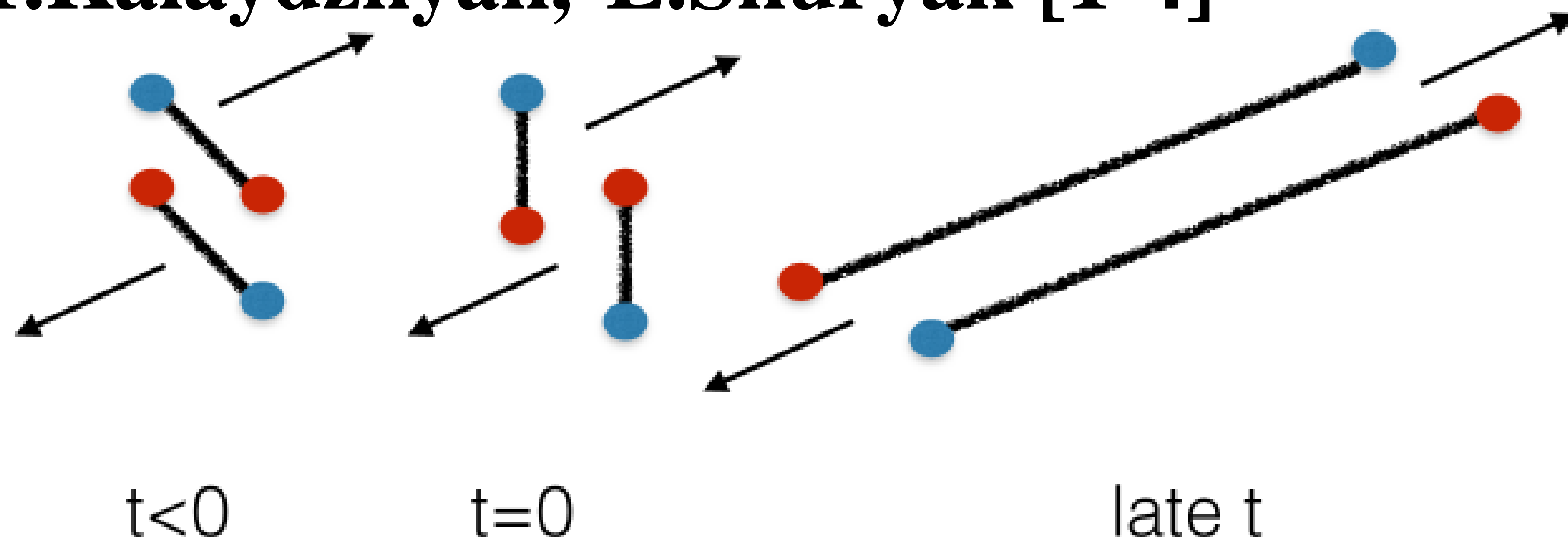
Pb-Pb collision at  $b=4$  fm  
 blue circles – strings  
 green arrows – string boosts

- [1] I.Altshbeev, AIP Conf.Proc. 1701 (2016)  
 [2] I.Altshbeev, G.Feofilov and O.Kochebina, AIP Conf. Proc. 1701, 060011 (2016).



# QCD string-string interactions and “Spaghetti implosion”

T.Kalaydzhyan, E.Shuryak [1-4]



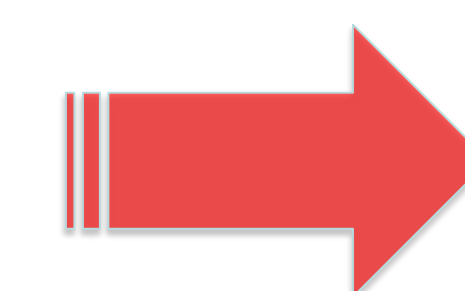
Attraction between strings  
due to  $\sigma$ -meson exchange  
and concept  
of  $\sigma$ -meson cloud[3]

Small sigma-string  
coupling

$$g_N \sigma_T = \frac{\langle \sigma \rangle^2 C^2}{4\sigma_T} \ll 1,$$

in the range  $10^{-1} - 10^{-2}$

is compensated  
by large number  
of strings [3]



flows [3]

- [1] E.Shuryak, ArXiv:1412.8393, 29 Dec. 2014
- [2] T.Kalaydzhyan and E.Shuryak, arXiv:1402.7363,
- [3] T.Kalaydzhyan and E.Shuryak, arXiv:1404.1888.
- [4] T.Kalaydzhyan and E.Shuryak, Phys. Rev. C 91,  
054913 (2015) , [arXiv:1503.05213 \[hep-ph\]](https://arxiv.org/abs/1503.05213)



# QUESTIONS:

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1) What is the number of these sources extended in rapidity and produced

in case of small systems,

*in particular, in pp*

*collisions?*

2) Is the density of these sources sufficient to start overlap and *to interact* producing new kinds of particle production sources?

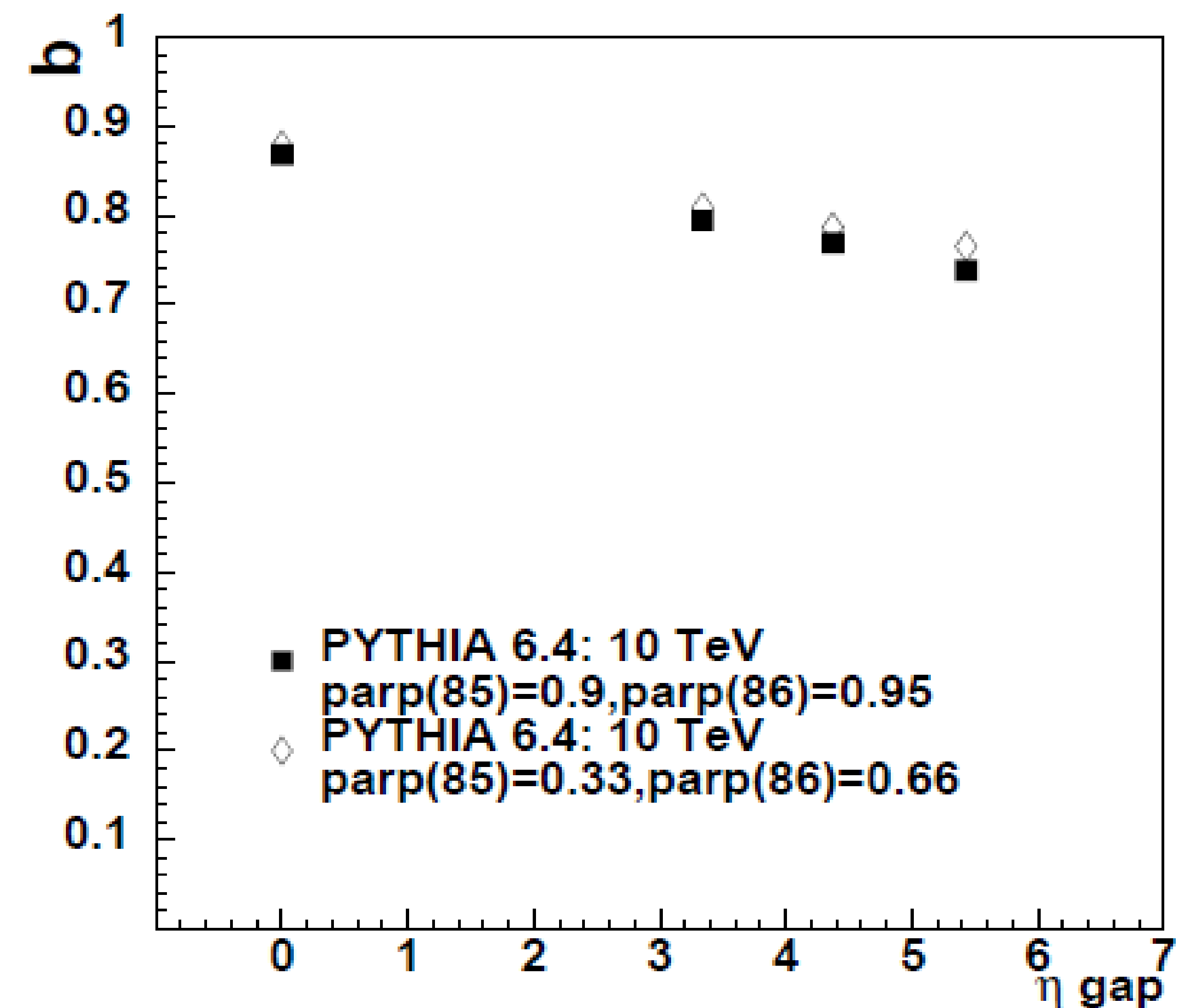
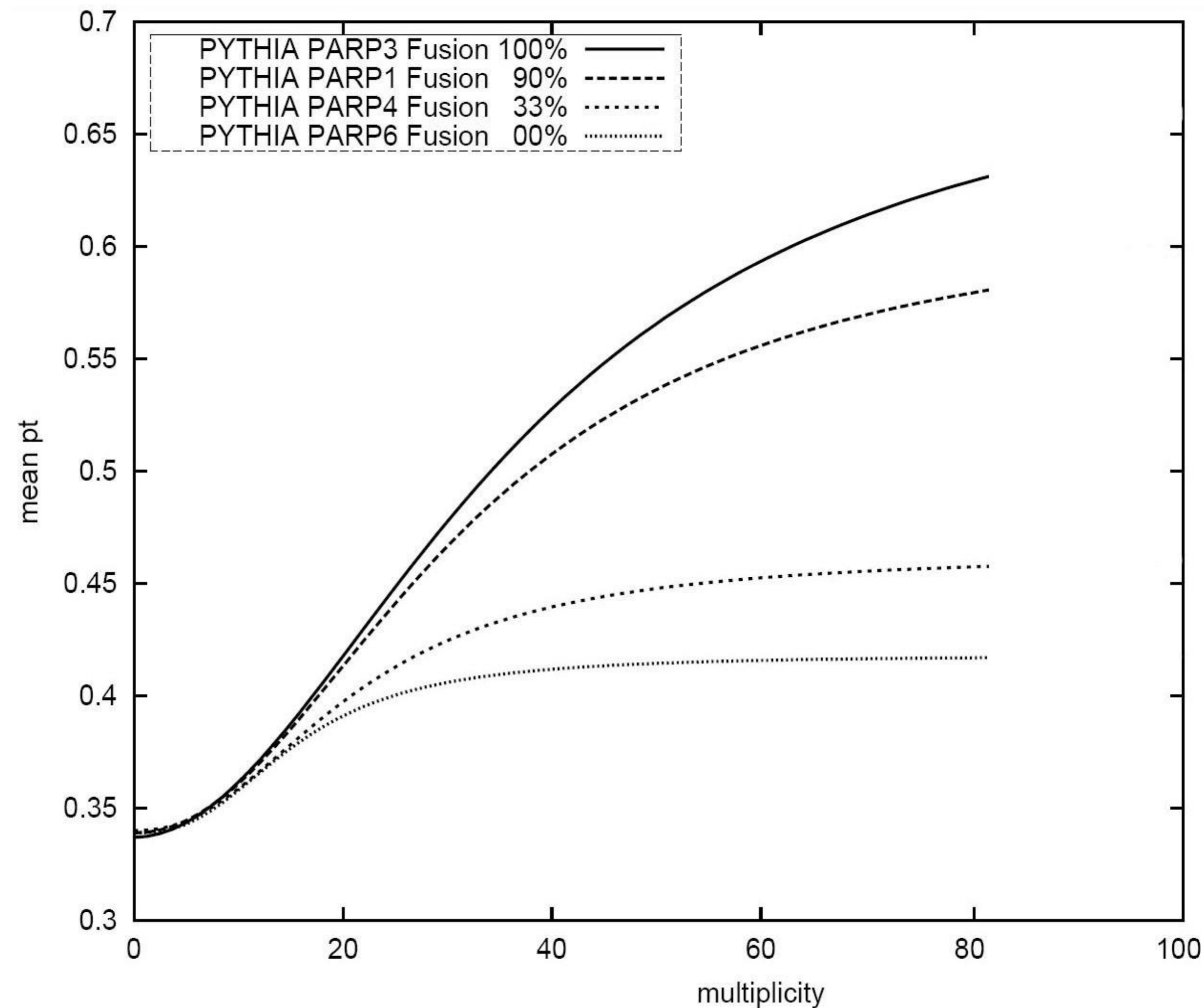


# ESTIMATE-1

## MPI in pp



# Collectivity in PYTHIA: Color Reconnection and Long-Range correlations (LRC)



[1] A. Asryan, G. Feofilov,  
**Studies of pT-Nch correlation**  
in pp collisions in the framework  
of PSM and PYTHIA generators, ALICE Week,  
Physics Forum, CERN, 11 October 2006.

[2] A. Asryan, D. Derkach, G. Feofilov  
“Correlation pT-Nch and collective effects  
in pp and ppbar collisions from ISR up to  
Tevatron and LHC”, Vestnik SPbSU,  
ser.4 ,v.2,2008,3-16, accepted 18 Dec.2007.

Figure 3: PYTHIA: The  $n$ - $n$  correlation strength for pp collisions at  $\sqrt{s}=10$  TeV as a function of the pseudorapidity gap for 2 sets of collectivity parameters: (0.33, 0.63) (open diamonds), (0.9, 0.95) (black squares).

- LRC in PYTHIA due to fluctuating, from event to event, number of strings.
- pT-Nch correlation – due to Color Reconnection



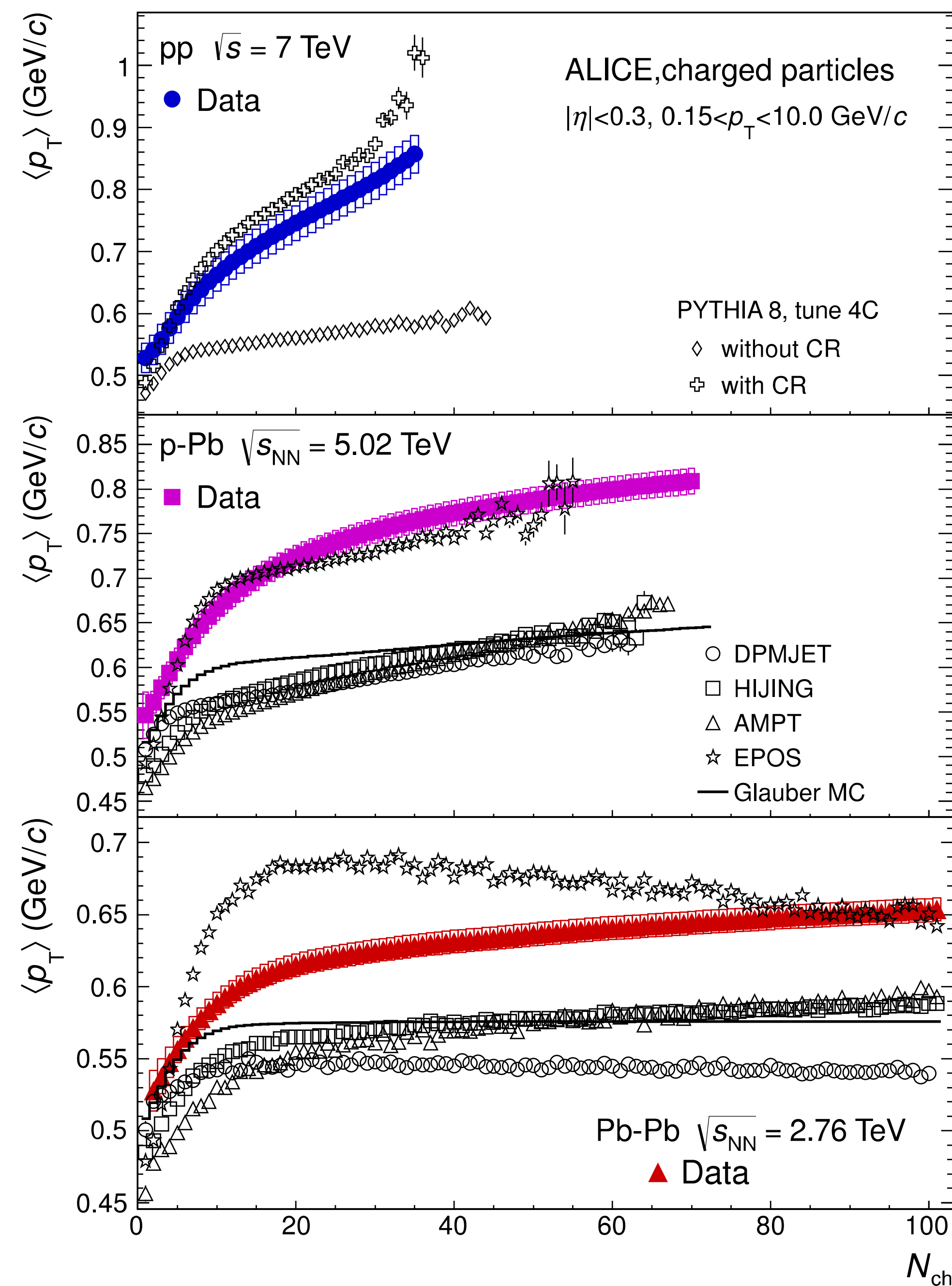
# Collectivity in PYTHIA:

## MPI in pp collisions

2 assumptions:

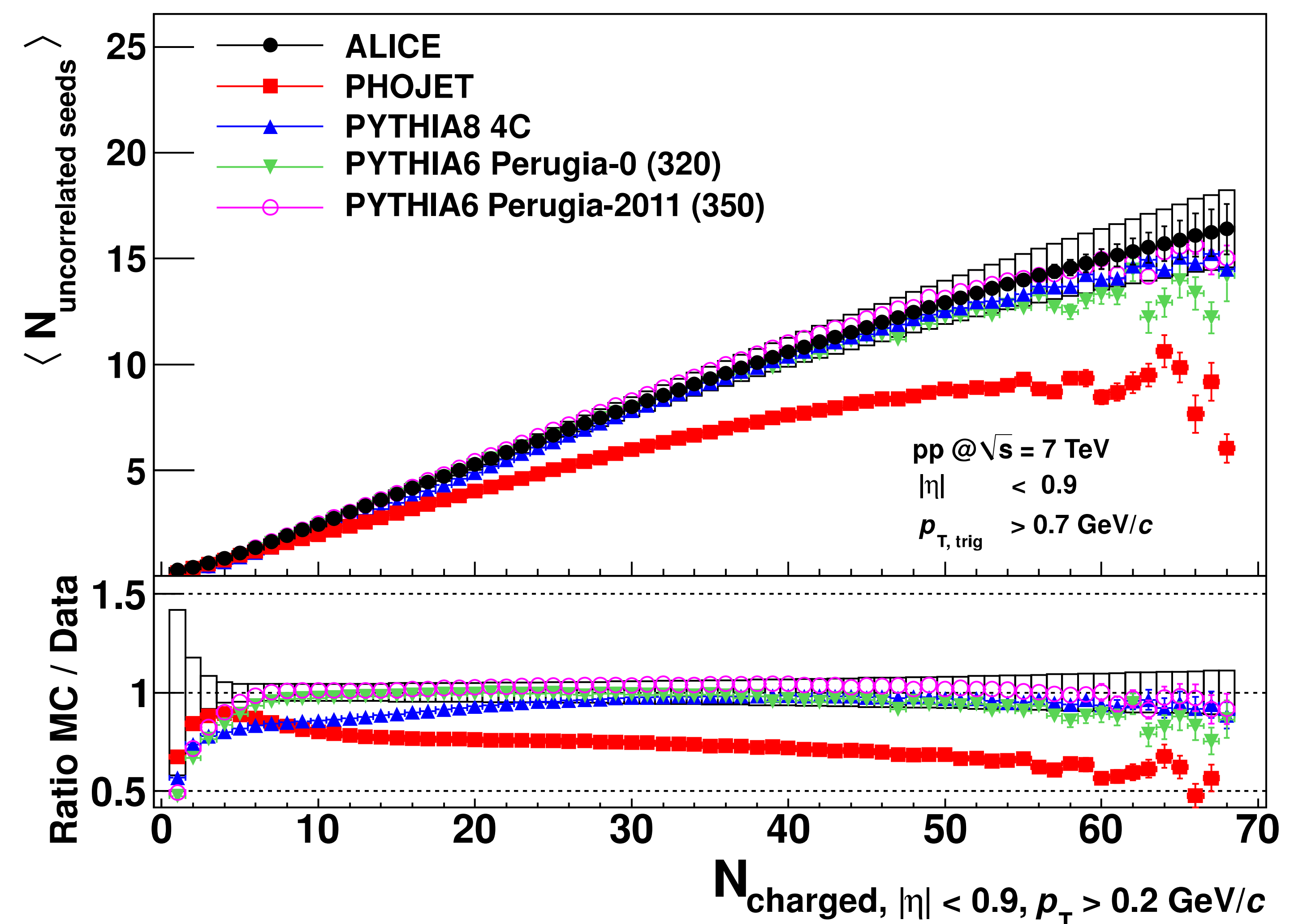
---the number of MPIs is proportional to the hard collisions cross section

-- soft particle multiplicity scales with the number of MPIs



**Figure 2.** The mean particle transverse momentum as a function of multiplicity in  $|\eta| < 0.3$  for pp collisions at  $\sqrt{s} = 7$  TeV (upper panel), p-Pb collisions at  $\sqrt{s_{NN}} = 5.02$  TeV (middle panel) and Pb-Pb collisions at  $\sqrt{s_{NN}} = 2.76$  TeV (lower panel) [11].

Andreas Morsch,  
for the ALICE Collaboration  
Journal of Physics: Conf Seri. **535** (2014) 012012  
arXiv: 1407.3628



ALI-PUB-62528

**Figure 4.** Number of uncorrelated seeds as defined in the text from two-particle azimuthal correlations with  $p_{T,trig}, p_{T,assoc} > 0.7$  GeV/c in pp collisions at  $\sqrt{s} = 7$  TeV [13].

$\langle N_{uncor.seeds} \rangle$  -- up to  $\sim 15$  in pp@7TeV  
for  $p_{T,trig} > 0.7$  GeV/c



# ESTIMATE-2

## based on the onset of ridge in Au-Au@RHIC

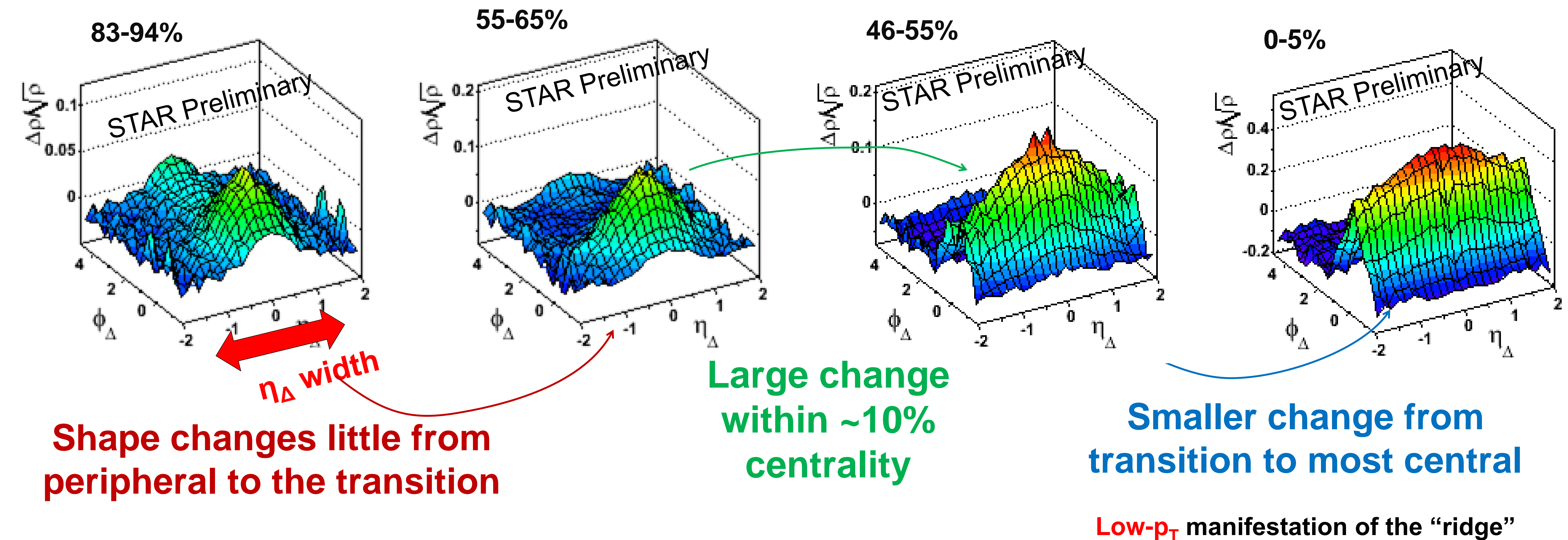
O.Kochebina, G.Feofilov, Arxiv:1012.0173



# Threshold phenomena in AA collisions observed by STAR [1]

Variation of **low- $p_T$**  “ridge” with centrality (Npart).

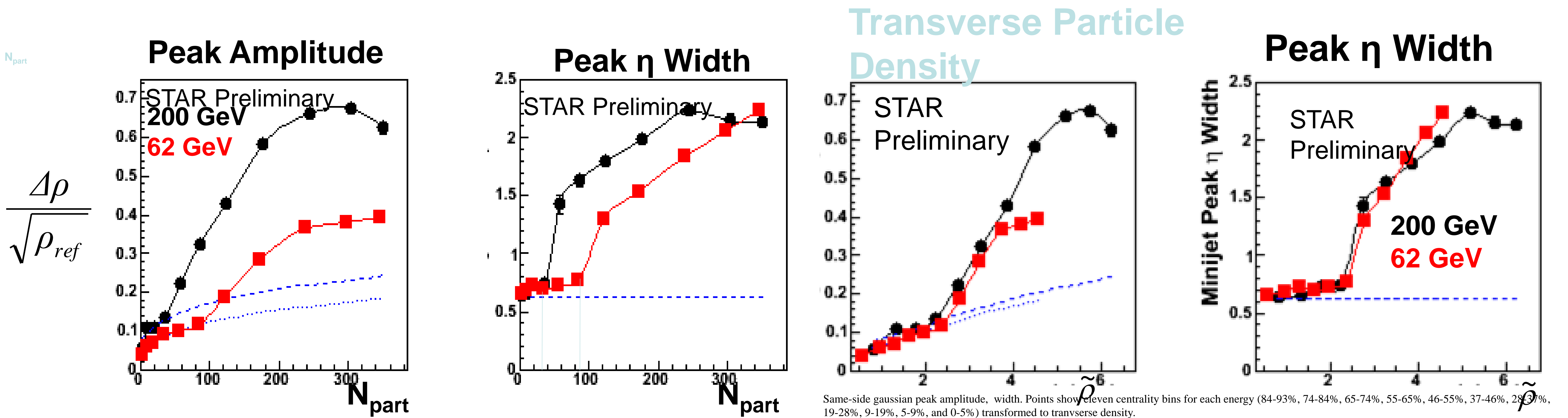
( $p_T > 0.15 \text{ GeV}/c$ )



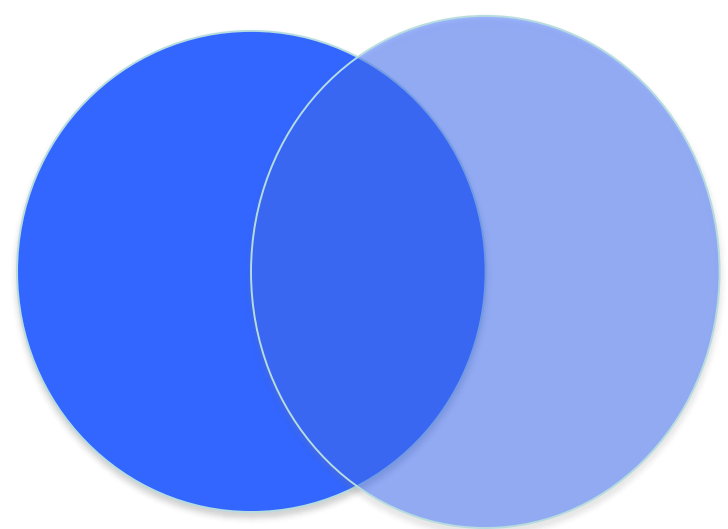
The data showed a sharp transition at some definite energy-dependent centrality: growing of peak amplitude and pseudorapidity stretching of width.



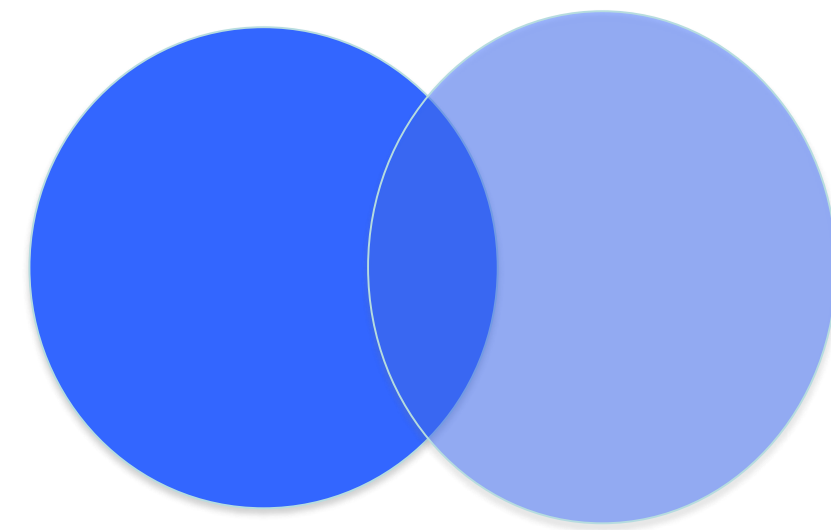
# Variation of low- $p_T$ “ridge” with centrality



**62 GeV**  
**“Critical value”**  
 **$N_{part} \approx 90$**



**200 GeV**  
**“Critical value”**  
 **$N_{part} \approx 40$**



The transverse particle density:

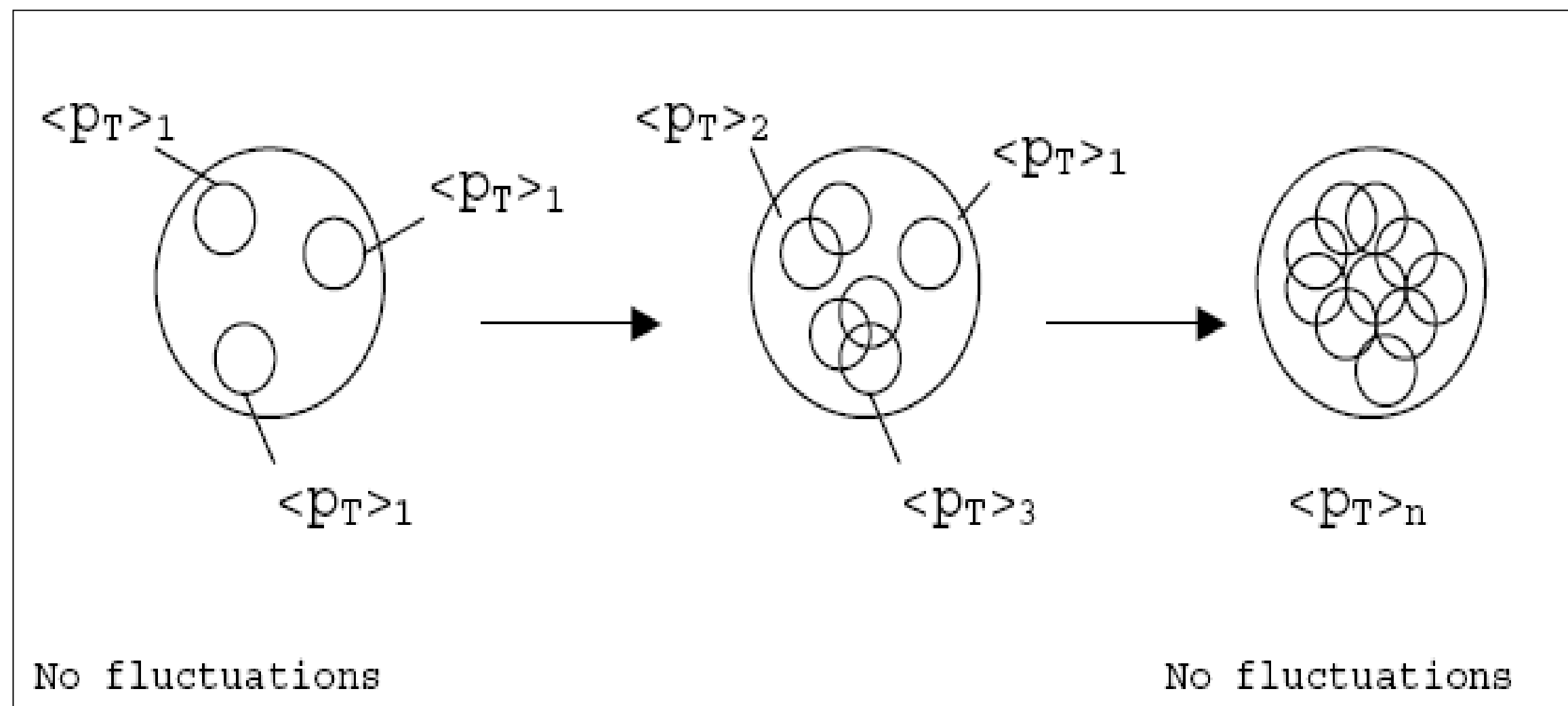
$$\tilde{\rho} = \frac{3}{2} \frac{dN_{ch}}{d\eta} / S(b)$$

$$\tilde{\rho}_{crit} = 2,6 \pm 0,2 fm^{-2}$$

[1] Anomalous centrality variation of minijet angular correlations in Au-Au collisions at 62 and 200 GeV from STAR. M. Daugherty. QM2008.



# String percolation and mean number of strings



Percolation parameter:

$$\eta(b) = N_{str}(b) \pi r_0^2 / S(b)$$

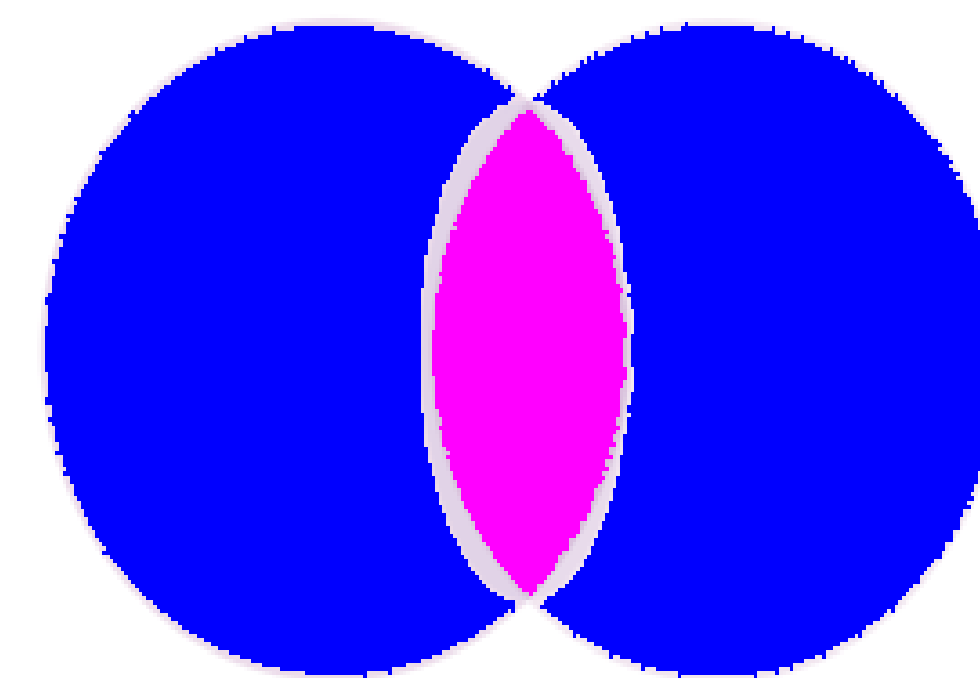
$$\eta(N_{part}) = N_{str}(N_{part}) \pi r_0^2 / S(N_{part})$$

$N_{str}$  -- number of strings,  
 $\pi r_0^2$  -- string transverse area,  
 $S$  -- overlap area

$r_0 = 0,2 - 0,25$  fm -- string radius

$$\tilde{\eta} = \frac{\pi r_0^2 N_{str}}{\langle S \rangle}$$

At some critical density a macroscopic cluster appears that marks the percolation phase transition. [3]



$$\eta_c = 1,15 \text{ ([4])}$$

$$\tilde{\rho} = \frac{3}{2} \frac{dN_{ch}}{d\eta} / S(b)$$

$$\frac{\tilde{\rho}^{crit}(N_{part})}{\tilde{\eta}^{crit}(N_{part})} = \frac{3}{2} \frac{1}{\pi r_0^2} \frac{dN_{ch}}{dy} \frac{1}{N_{str}} = 2.3 \pm 0.2 \text{ fm}^{-2},$$

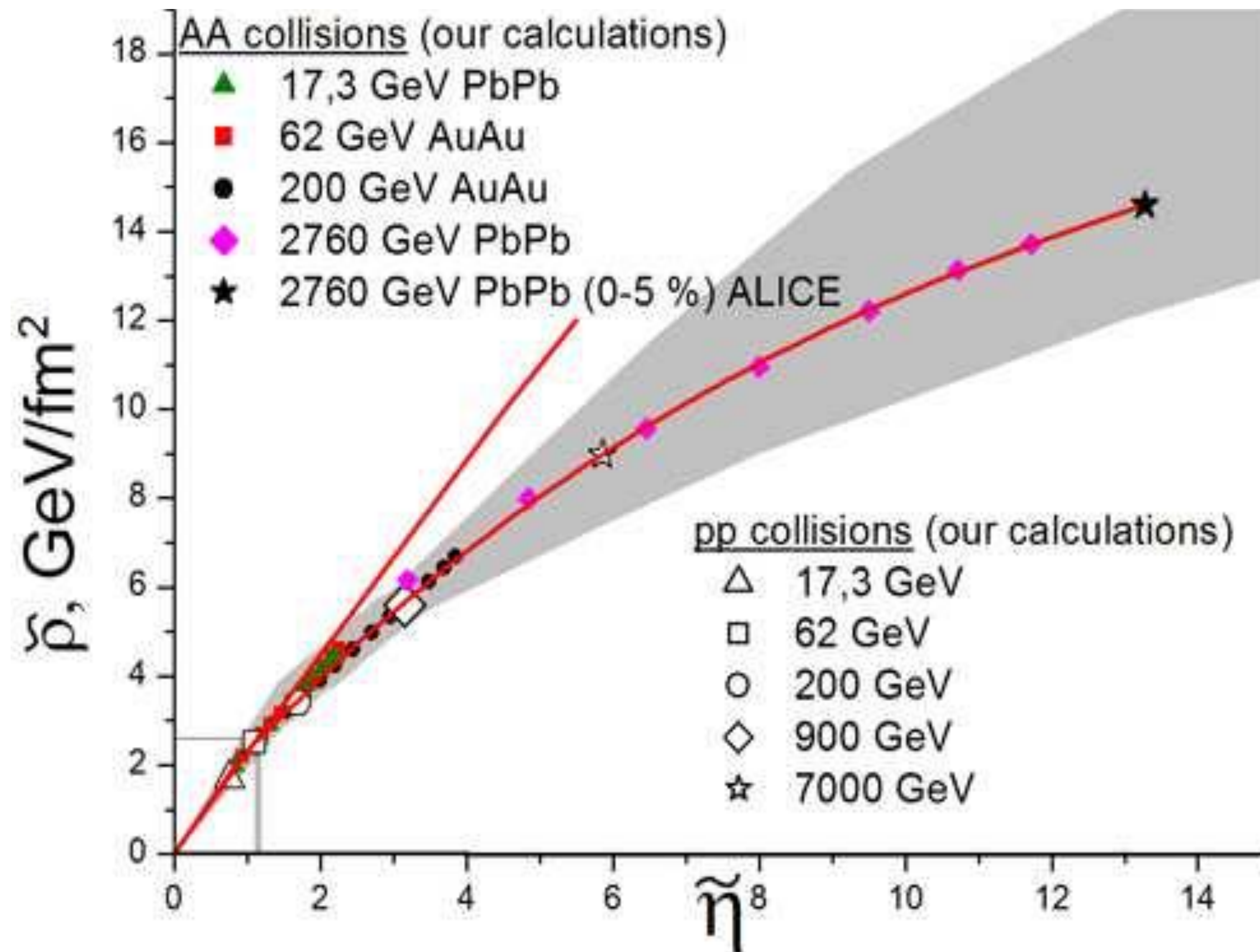
O.Kochebina, G.Feofilov, Arxiv:1012.0173

[4] J.Dias de Deus and A. Rodrigues// Phys. Rev. C 67, 064903 (2003)

[3] C. Pajares // arXiv:hep-ph/0501125v1 14 Jan 2005



# String percolation and number of strings: from A-A collisions to pp



**The transverse particle density vs. string density**

O.Kochebina, G.Feofilov, Arxiv:1012.0173



# From A-A collisions to pp: mean number of strings

Table 1: The total number of strings, the number of sea strings and parameter  $a$  obtained in the "critical" points for AuAu collisions at 62 GeV and 200 GeV collision energies and for PbPb collisions at 17.3 GeV. The calculations are done for  $r_0 = 0.25$  fm.[1].

$\sqrt{s}$ , GeV	$N_{\text{part}}$	$dN_{\text{ch}}/d\eta$	$N_{\text{str}}$	$N_s$	$N_{\text{coll}}$	$a$
200(AuAu)	40	$2.97 \pm 0.30$ [22]	$194 \pm 25$	$155 \pm 23$	$59 \pm 4$	$2.6 \pm 0.4$
62 (AuAu)	90	$2.30 \pm 0.23$ [23]	$352 \pm 28$	$262 \pm 23$	$167 \pm 4$	$1.6 \pm 0.2$
17.3 (PbPb)	110	$1.62 \pm 0.21$ [24]	$302 \pm 45$	$192 \pm 30$	$158 \pm 5$	$1.2 \pm 0.2$

Table 2: The transverse particle density, the string density and number of strings estimated for pp collisions for energies from 17.3 GeV to 7000 GeV.

$\sqrt{s}$ , GeV	$dN_{\text{ch}}/d\eta$	$\tilde{\rho}$ , GeV/f m <sup>2</sup>	$\tilde{\eta}$	$N_{\text{str}}$ our estim.
7000	$6.02 \pm 0.50$ [27]	$9.0 \pm 0.5$	$5 \pm 1$	$30 \pm 12$
900	$3.78 \pm 0.19$ [28]	$5.6 \pm 0.4$	$3.2 \pm 0.8$	$16 \pm 6$
200(pp)	$2.30 \pm 0.20$ [29]	$3.4 \pm 0.2$	$1.7 \pm 0.4$	$9 \pm 4$
62	$1.64 \pm 0.17$ [30]	$2.5 \pm 0.1$	$1.1 \pm 0.6$	$6 \pm 4$
17.3	$1.14 \pm 0.12$ [31]	$1.70 \pm 0.08$	$0.7 \pm 0.4$	$4 \pm 3$

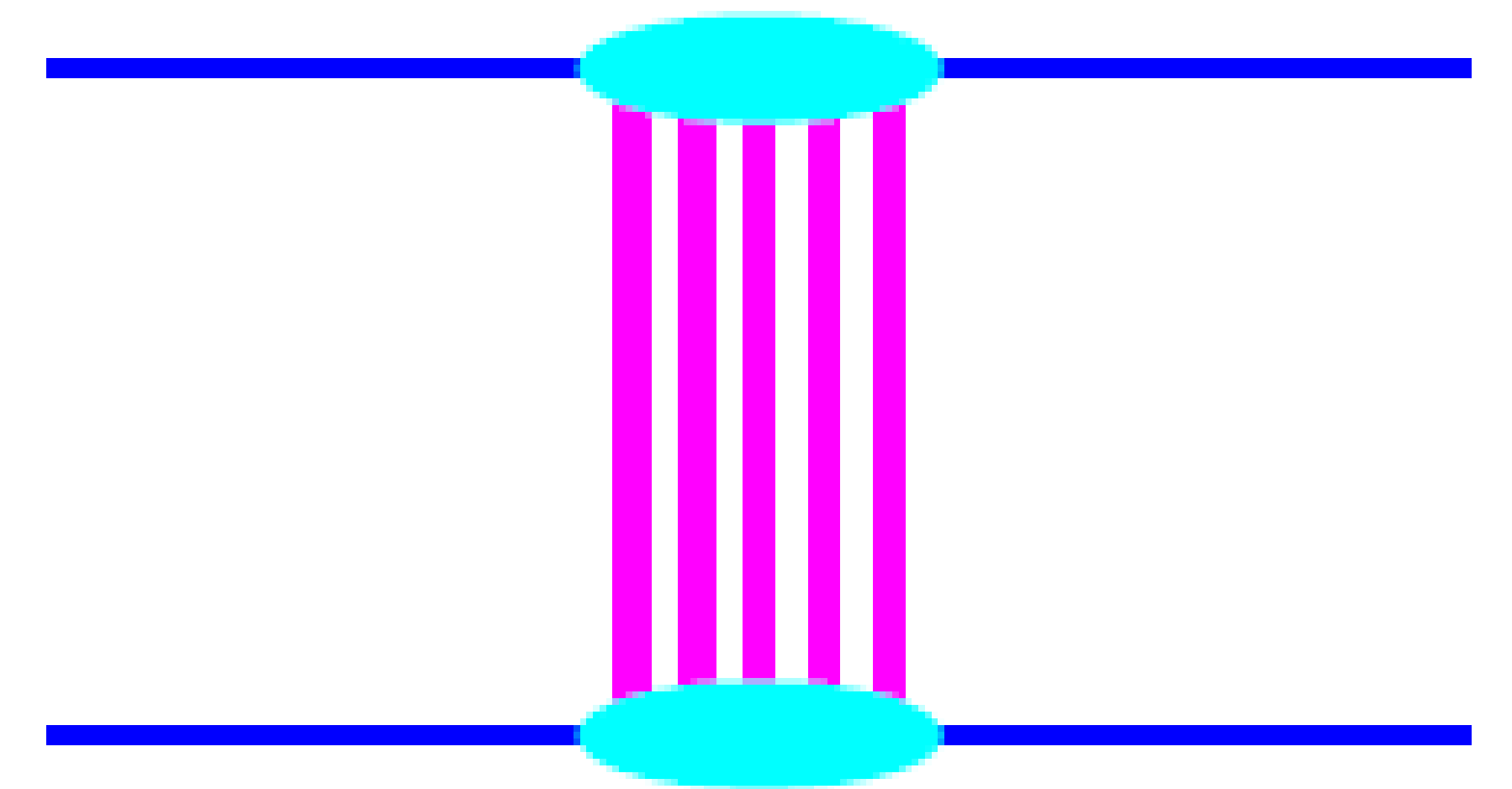
[1] O.Kochebina, G.Feofilov, Arxiv:1012.0173

for pp@7TeV:  $\langle N_{\text{strings}} \rangle \sim 30 \pm 12$



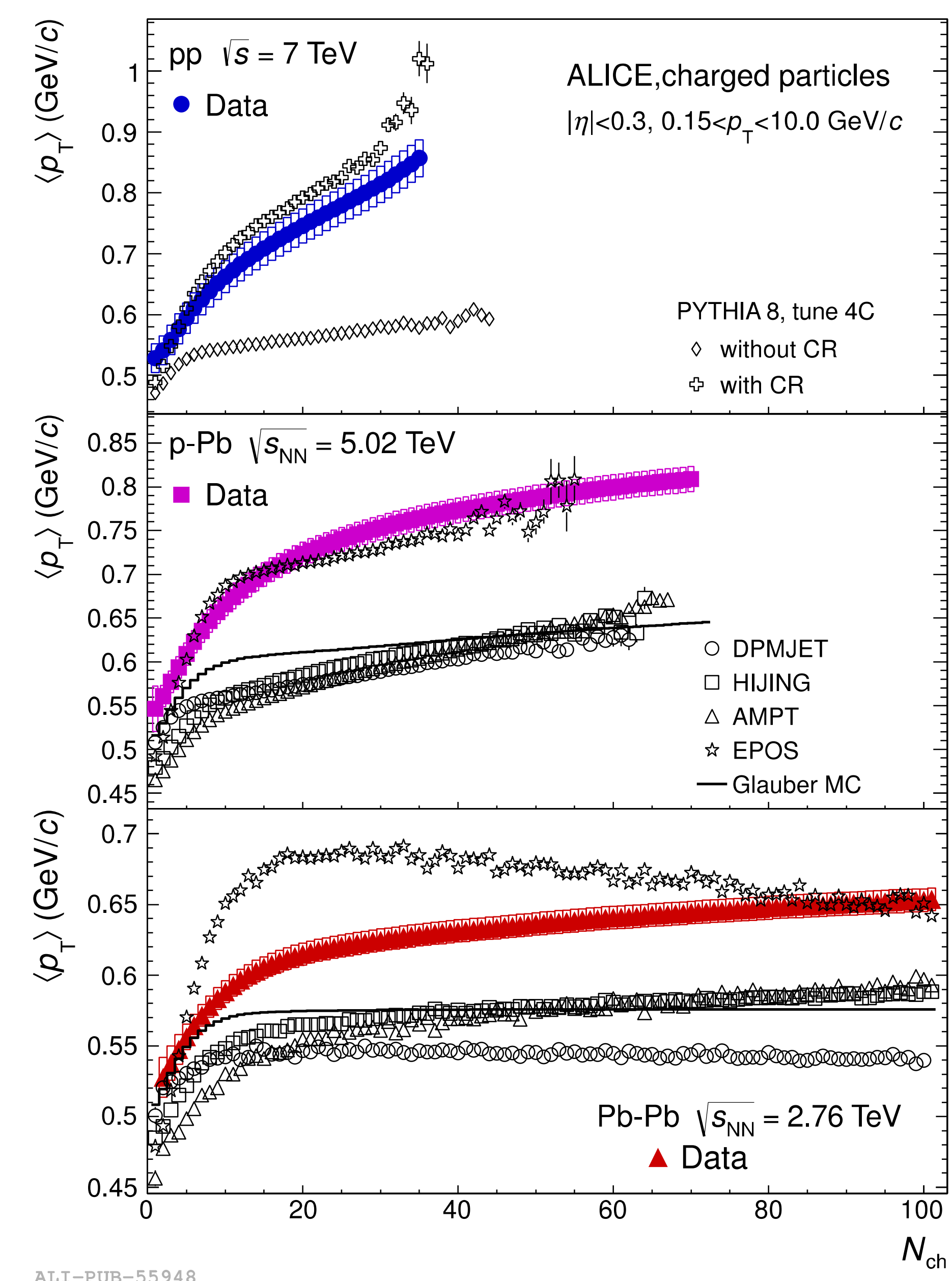
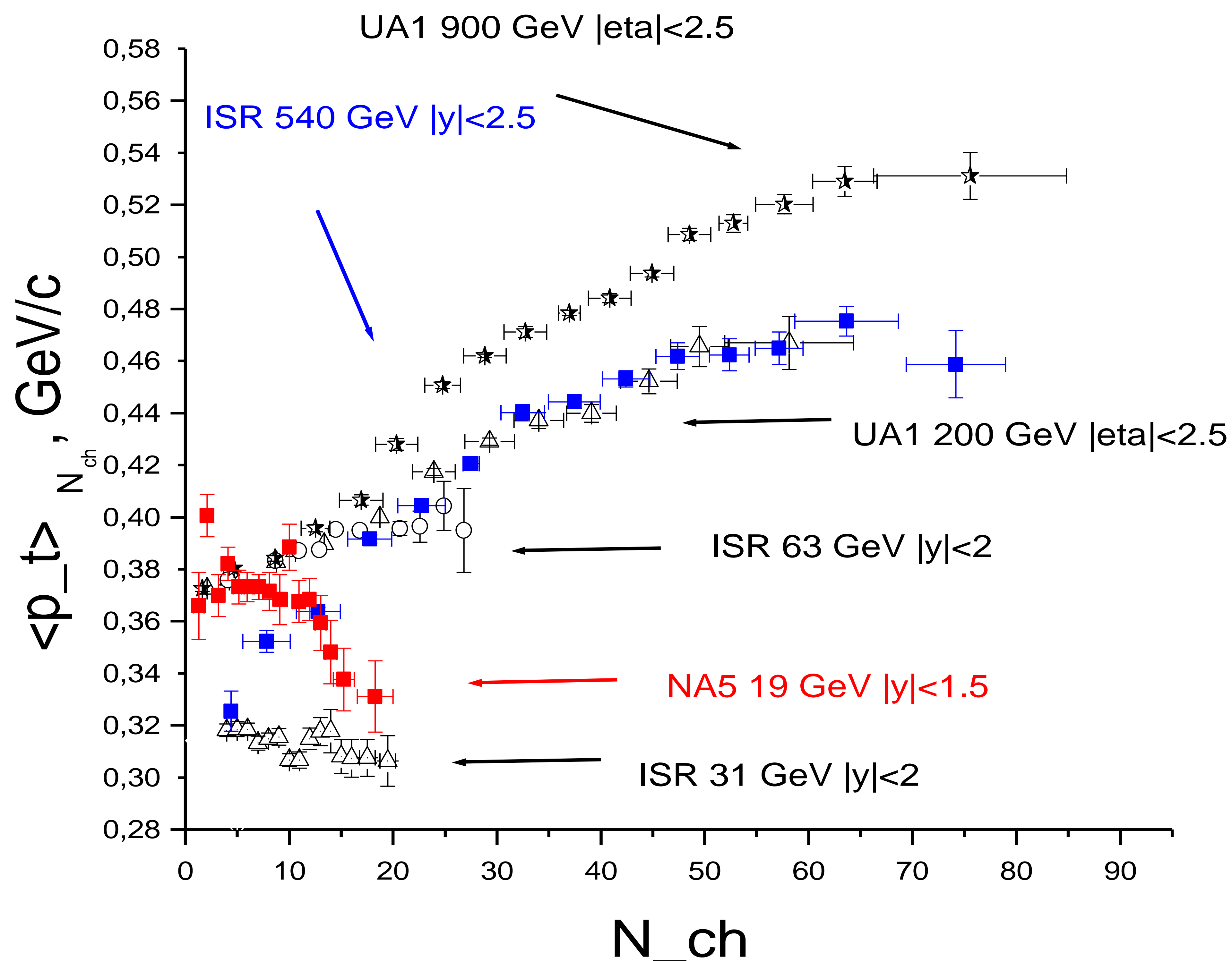
# ESTIMATE-3

Multi-pomeron exchange model with effective  
account of interaction between strings  
(EPEM)



- [1] Armesto, N., Derkach, D., and Feofilov, G., Phys. At. Nucl., 2008, vol. 71, p. 2087.
- [2] Bodnia, E., Derkach, D., Feofilov, G., Kovalenko, V., and Puchkov, A., Proc. QFTHEP 2013, St. Petersburg, 2013. <http://arxiv.org/abs/1310.1627>.
- [3] Bodnia, E.O., Kovalenko, V.N., Puchkov, A.M., and Feofilov, G.A., AIP Conf. Proc., 2014, vol. 1606, p. 273.

# Motivation: Experimentally Observed $p_t$ - $N_{ch}$ correlations in pp and ppbar collisions:



**Figure 2.** The mean particle transverse momentum as a function of multiplicity in  $|\eta| < 0.3$  for pp collisions at  $\sqrt{s} = 7$  TeV (upper panel), p-Pb collisions at  $\sqrt{s_{NN}} = 5.02$  TeV (middle panel) and Pb-Pb collisions at  $\sqrt{s_{NN}} = 2.76$  TeV (lower panel) [11].

Compilation of experimental data in:

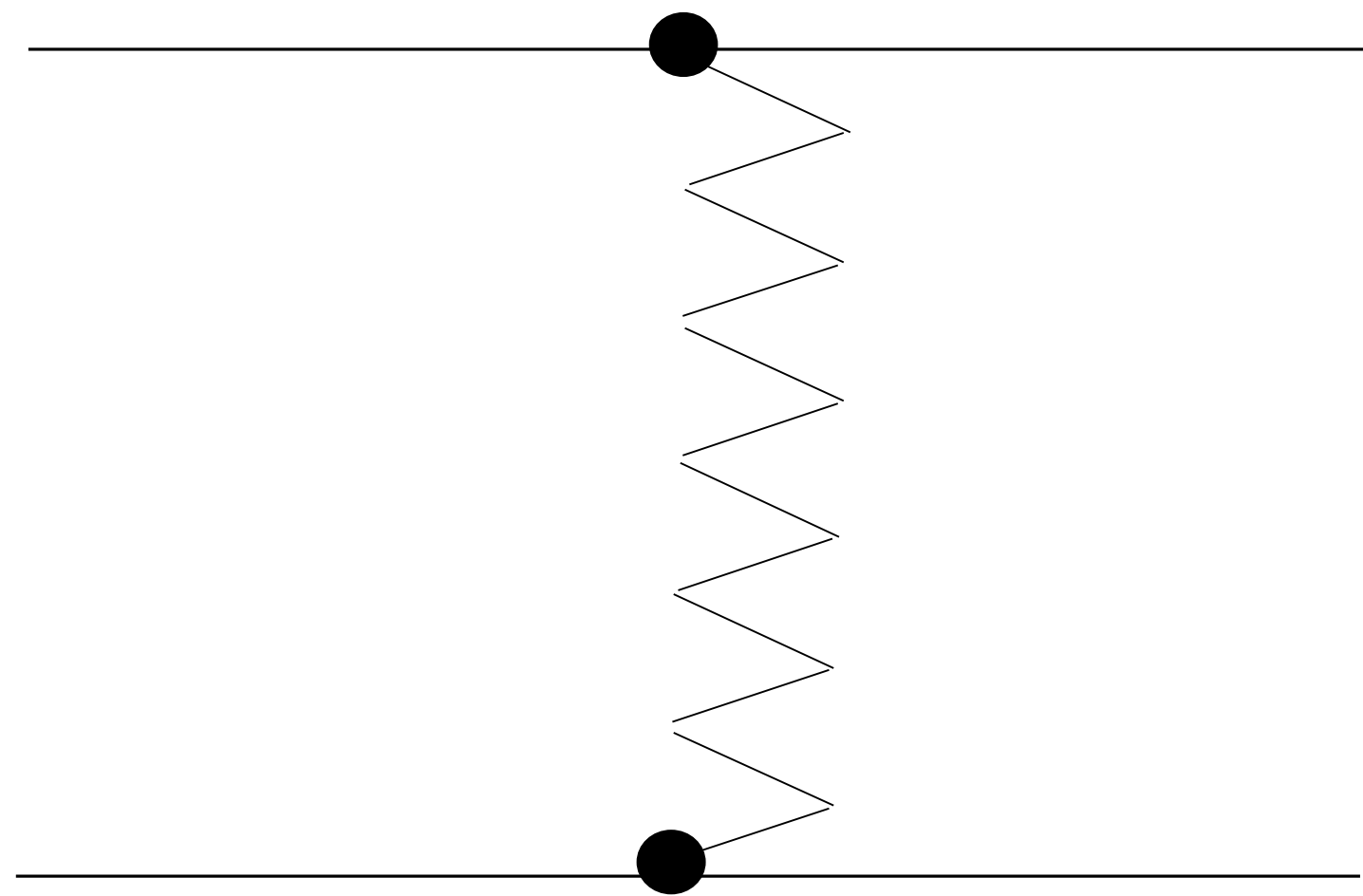
[1] Armesto, N., Derkach, D., and Feofilov, G., Phys. At. Nucl., 2008, vol. 71, p. 2087.

$p_t$ - $N_{ch}$  correlations @LHC



# Classical Multi-Pomeron Exchange Model (Regge-Gribov approach)

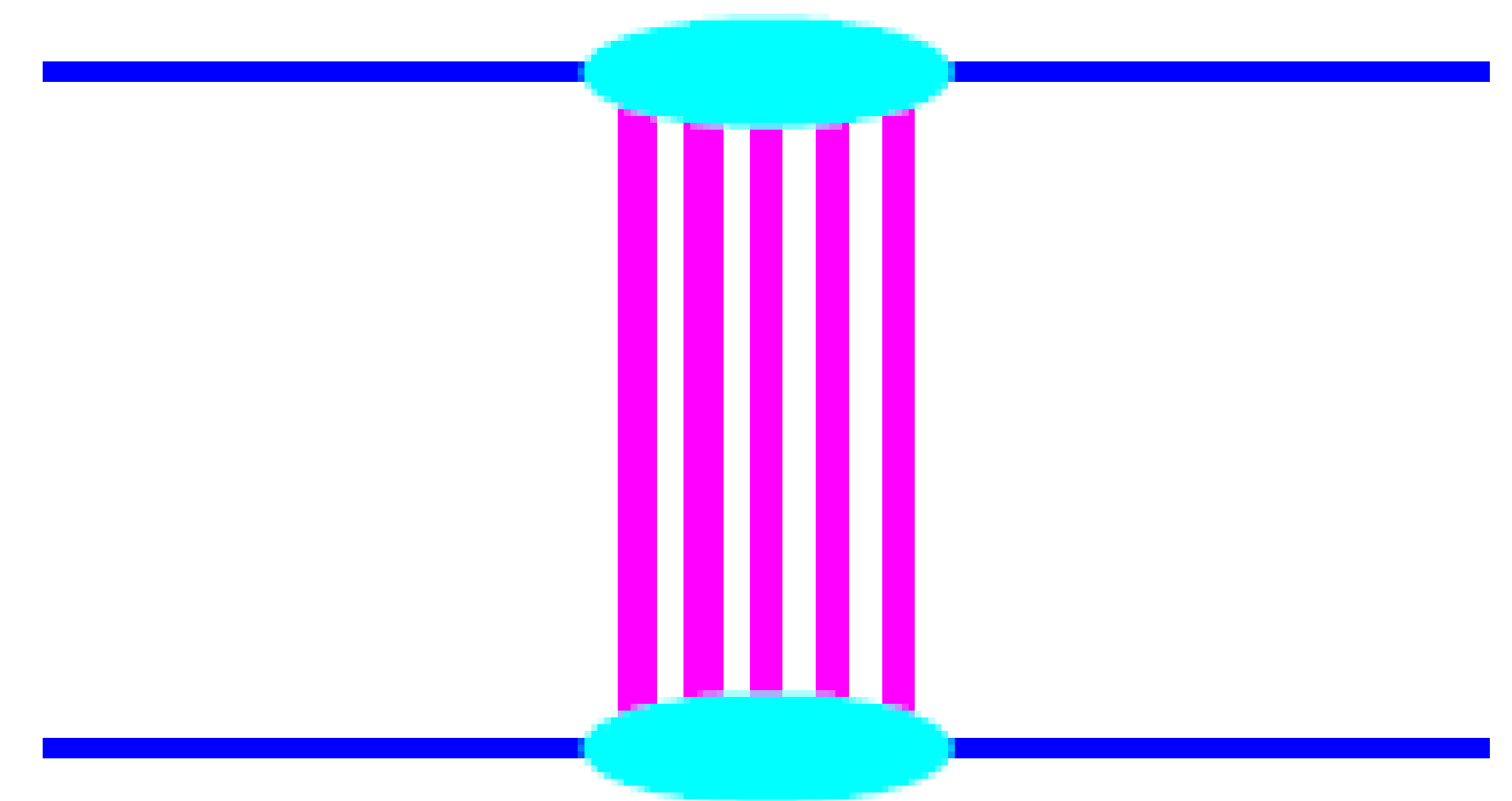
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Pomeron is a virtual particle that is exchanged during the inelastic scattering process with vacuum quantum numbers flow.

It can be considered as a pair of strings.

The number of pomerons exchanged rises with energy.



Collective effects were not included in the model.

**A.Capella, U.P.Sukhatme, C.-I.Tan and J.Tran Thanh Van, Phys. Rep.236(1994)225**

# EPEM[1] Modifications[2]

$\rho(N_{ch}, p_t) =$ $= \frac{C_w}{z} \sum_{n=1}^{\infty} \frac{1}{n} \left( 1 - \exp(-z) \sum_{l=0}^{n-1} \frac{z^l}{l!} \right) \times$ $\times \exp(-2nk\delta) \frac{(2nk\delta)^{N_{ch}}}{N_{ch}!} \times$ $\times \frac{1}{n^{\beta \cdot t}} \exp \left( -\frac{\pi p_t^2}{n^{\beta} t} \right)$	<p>Probability distribution</p> <p>Probability of production of <math>n</math> pomerons</p> <p>Poisson distribution of the charged particles from <math>2n</math> string</p> <p>Modified Schwinger mechanism</p>
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$t$  – average string tension

$k$  – mean number of particles produced per unit rapidity by one string

$\beta$ -- efficient string fusion collective coefficient

[1] Armesto, N., Derkach, D., and Feofilov, G., Phys. At. Nucl., 2008, vol. 71, p. 2087

[2] Bodnia, E., Derkach, D., Feofilov, G., Kovalenko, V., and Puchkov, A.,  
Proc. QFTHEP 2013, St. Petersburg, 2013. <http://arxiv.org/abs/1310.162>

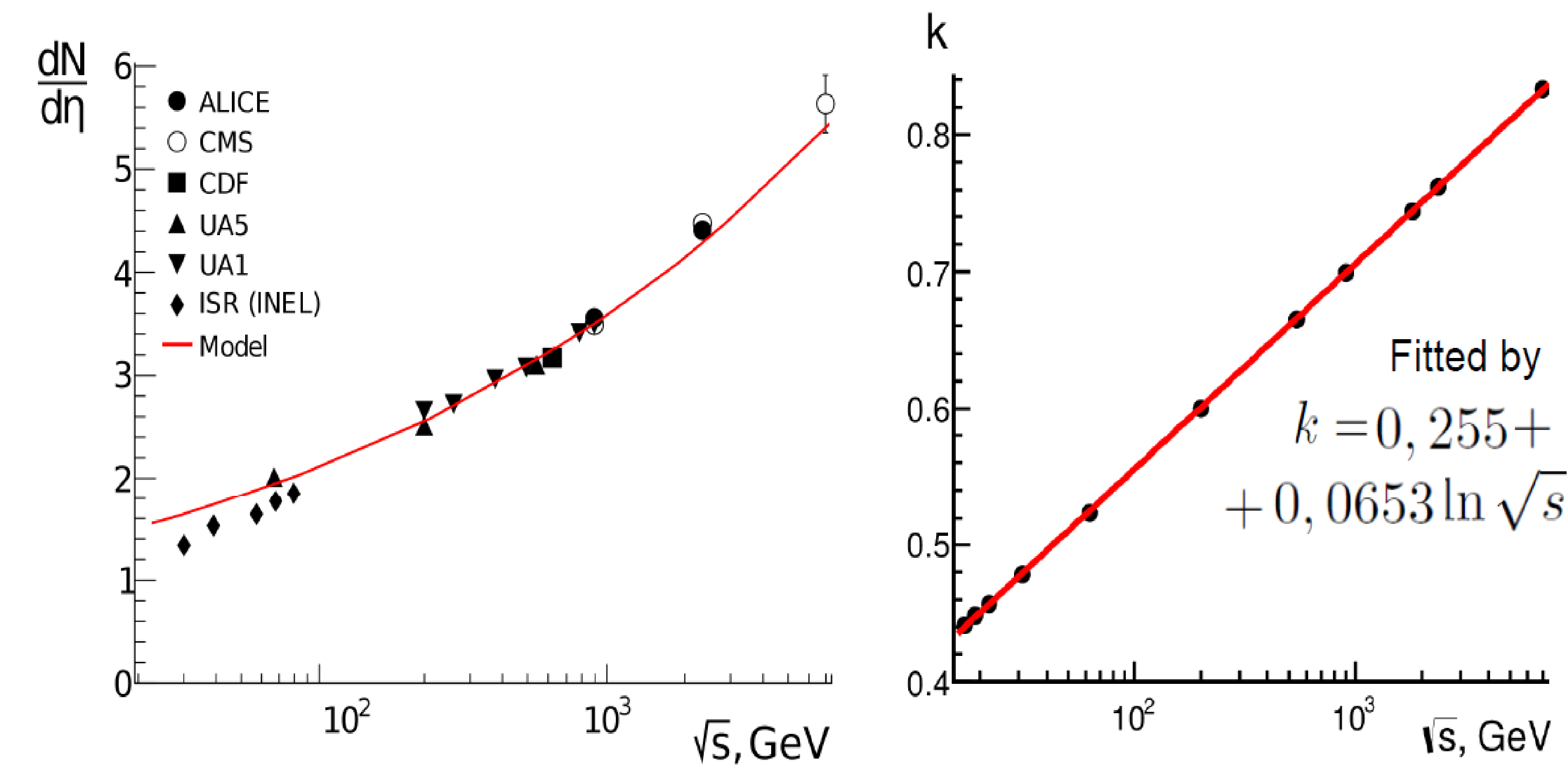


# Parameters and results from ISR to LHC

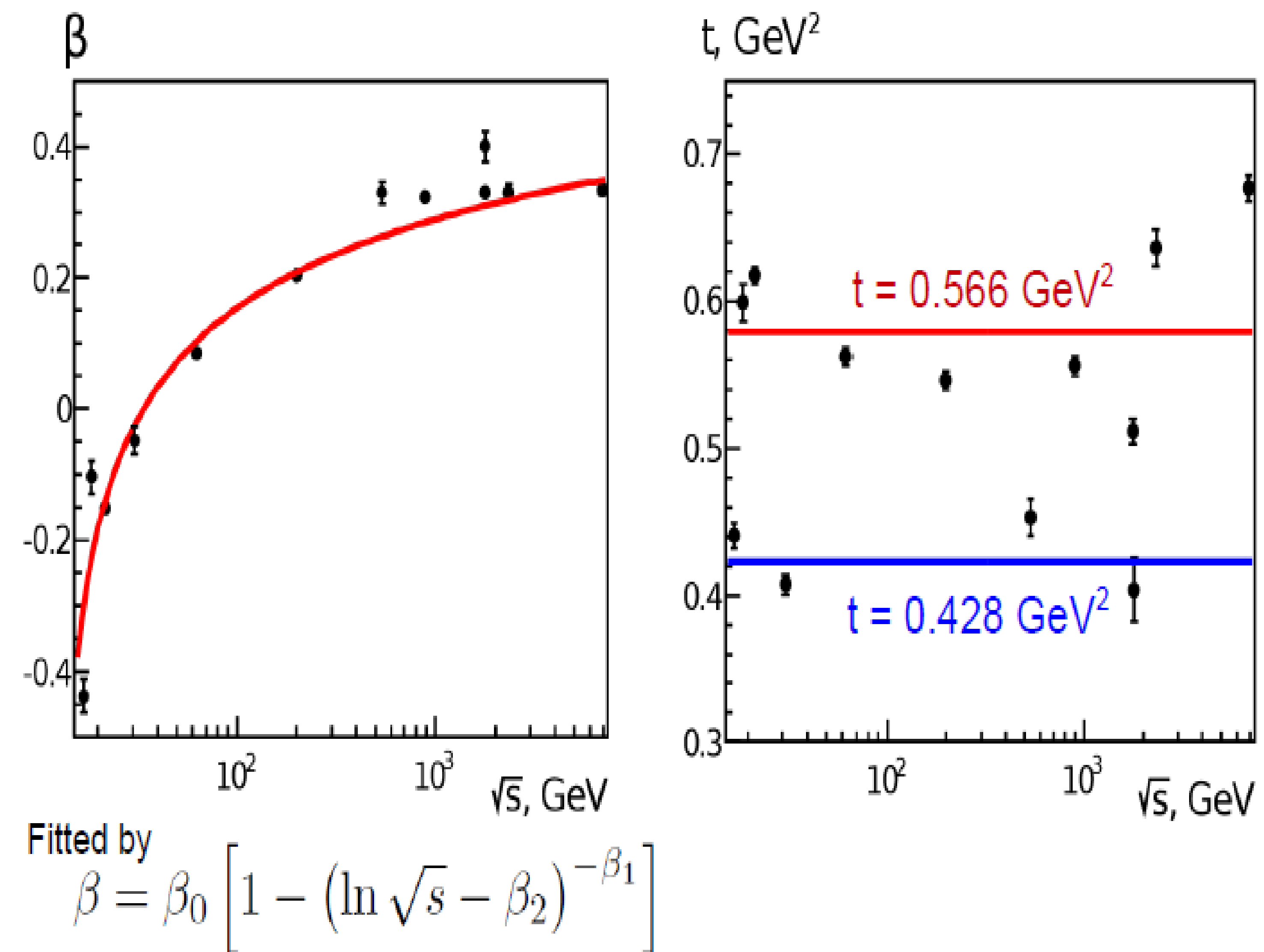
## Determination of the parameter $k$

from experimental data on charged multiplicity:

$$\langle N_{ch} \rangle(s) = \sum_{N_{ch}=0}^{\infty} N_{ch} \mathcal{P}(N_{ch}) = 2\langle n \rangle \cdot k \cdot \delta$$



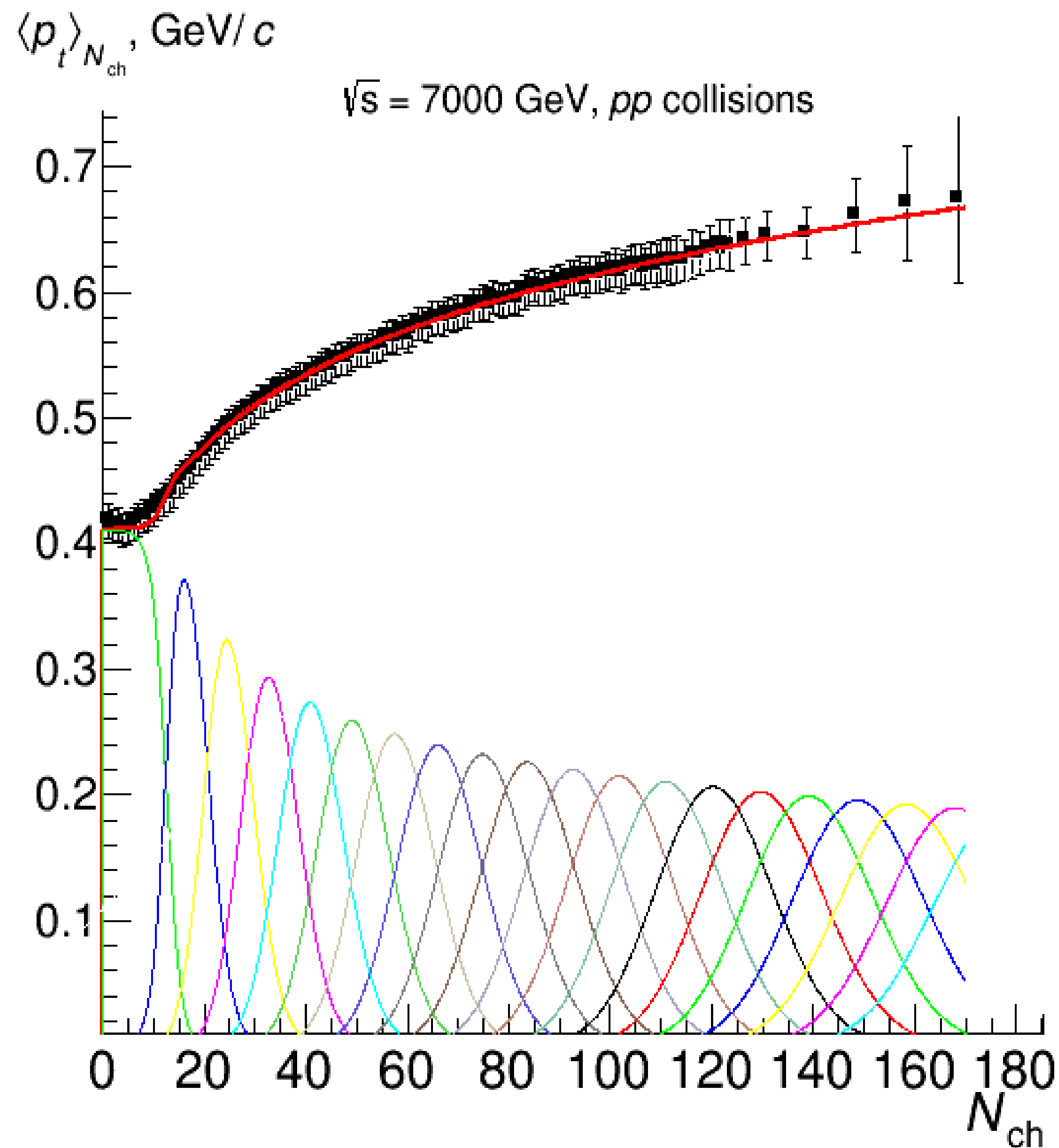
## Dependence of the parameters $\beta$ and $t$ on collision energy



$p_t$ - $N_{ch}$  correlation function in the model is calculated as:

$$\langle p_t \rangle_{N_{ch}}(s) = \frac{\int_0^{\infty} \rho(N_{ch}, p_t) p_t^2 dp_t}{\int_0^{\infty} \rho(N_{ch}, p_t) p_t dp_t}$$

# Number of pomerons involved in pp@7 TeV



For high multiplicity events ( $N_{ch} > 100$ ) we have:  
the number of  $N_{\text{Pomerons}} \sim 12-19$   
the number of  $N_{\text{springs}} \sim 24-38$



# Summary of estimates of number of sources of particle production at midrapidity (in high multiplicity events) in pp@7TeV

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Estimate	N strings
MPI ( $p_{t,TRIG} \sim 0.7$ GeV/c)[1]	$\sim 15$
Percolation [2]	$30 \pm 12$
Multipomeron exchange model [3]	24-38

[1] Andreas Morsch, for the ALICE Collaboration

Journal of Physics: Conf Seri. **535** (2014) 012012 arXiv: 1407.3628

[2] O.Kochebina, G.Feofilov, Arxiv:1012.0173

[3] Bodnia, E., Derkach, D., Feofilov, G., Kovalenko, V., and Puchkov, A., Proc.

QFTHEP 2013, St. Petersburg, 2013. <http://arxiv.org/abs/1310.1627>.; Bodnia, E.O., Kovalenko, V.N., Puchkov, A.M., and Feofilov, G.A., AIP Conf. Proc., 2014, vol. 1606, p. 273.

# Conclusions

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- Concept of **color flux tubes** (quark-gluon strings) as particle production sources is implemented in a number of event generators, phenomenology is tuned and looks feasible for the majority of experimental phenomena at the LHC. It contains some collectivity, manifested in long-range correlations, color-reconnection, flows...
- Independent estimates of number of these sources show that one may expect **formation of  $\sim 20-40$  strings** in high multiplicity pp collisions at the LHC.
- **String-string interaction** between these sources in case of high density is an important factor of investigations of new effects like string fusion, “spaghetti” implosion and /or string repulsion, that are responsible for shaping the initial conditions of systems collisions leading to the QGP formation.