

# Multiquark resonances

Alessandro Pilloni

Joint Physics Analysis Center

Thessaloniki, September 2<sup>nd</sup> 2016

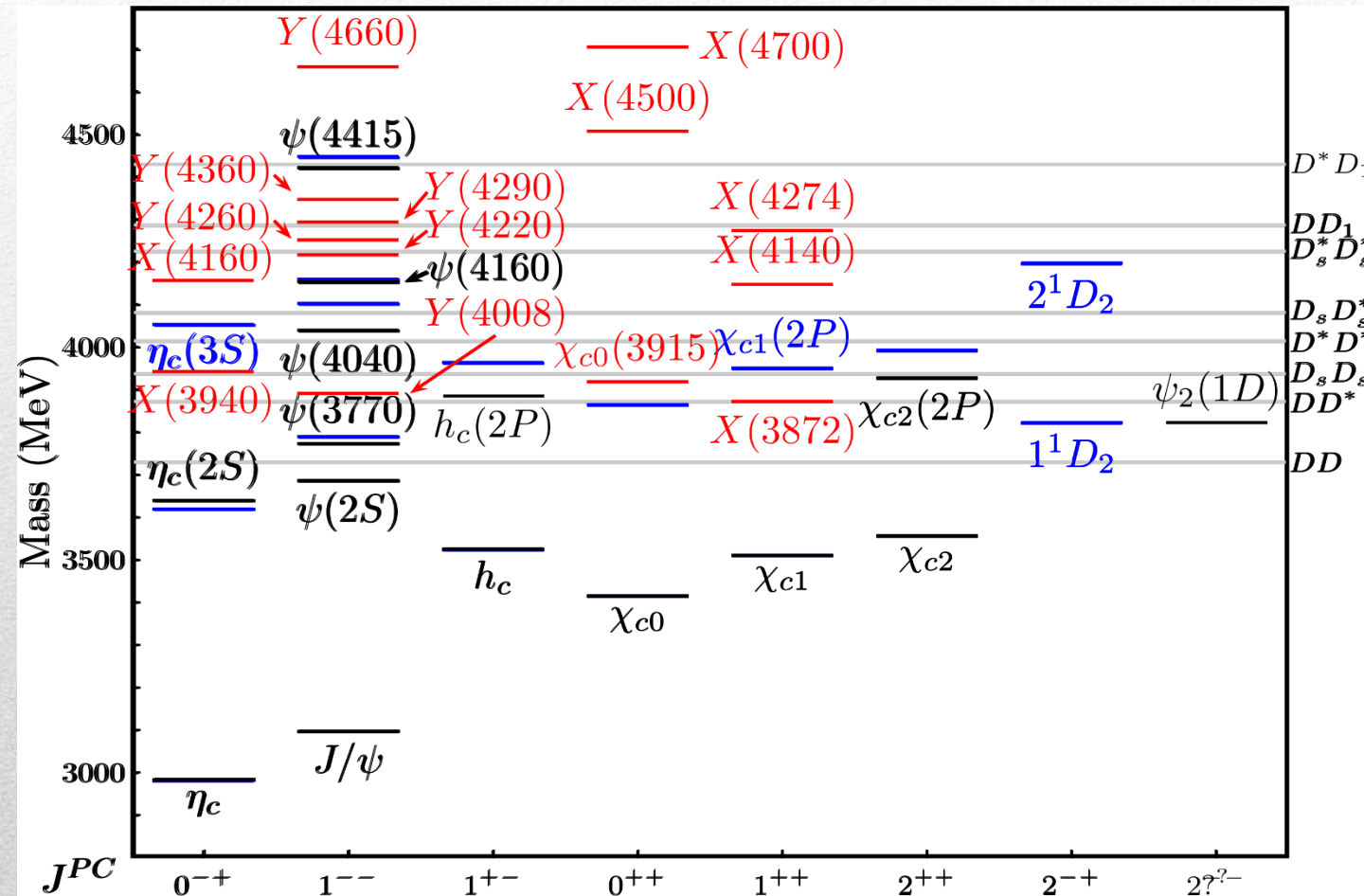


# Outline

- Compact tetraquarks
- Production of exotics at LHC
- Hybridized tetraquarks
- Conclusions



# Exotic landscape



A host of **unexpected resonances** have appeared

decaying mostly into charmonium + light

**Hardly reconciled** with usual charmonium interpretation

# Tetraquark

In a constituent quark model, we can think of a **diquark-antidiquark compact state**

$$[cq]_{S=0}[\bar{c}\bar{q}]_{S=1} + h.c.$$

Maiani, Piccinini, Polosa, Riquer PRD71 014028

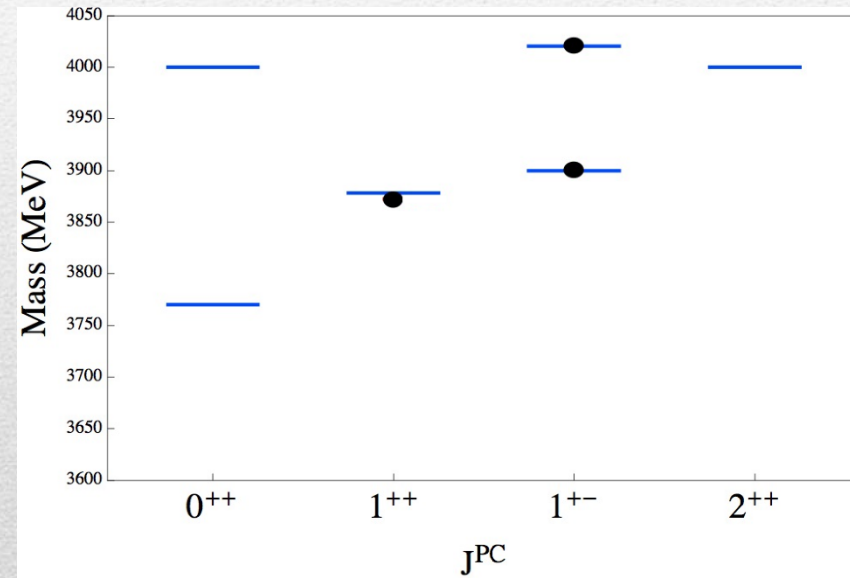
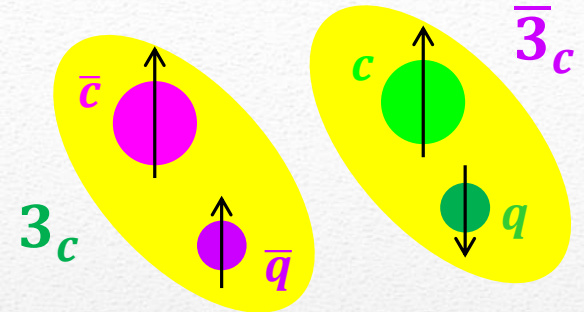
Faccini, Maiani, Piccinini, AP, Polosa, Riquer PRD87 111102

Maiani, Piccinini, Polosa, Riquer PRD89 114010

Spectrum according to **color-spin hamiltonian**  
(all the terms of the Breit-Fermi hamiltonian are absorbed into a constant diquark mass):

$$H = \sum_{dq} m_{dq} + 2 \sum_{i < j} \kappa_{ij} \vec{S}_i \cdot \vec{S}_j \frac{\lambda_i^a}{2} \frac{\lambda_j^a}{2}$$

Decay pattern mostly driven by **HQSS** ✓  
Fair understanding of existing spectrum ✓  
A full nonet for each level is expected ✗



New ansatz: the diquarks are compact objects  
spacially separated from each other,  
**only  $\kappa_{cq} \neq 0$**

Existing spectrum is fitted if  $\kappa_{cq} = 67$  MeV



# Tetraquark at large- $N$

Some discussions about the existence of tetraquark poles in the large- $N$  limit have been recently raised

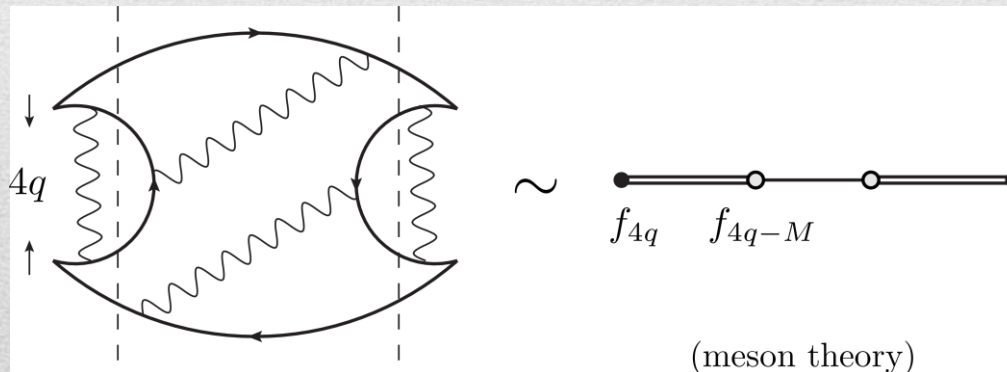
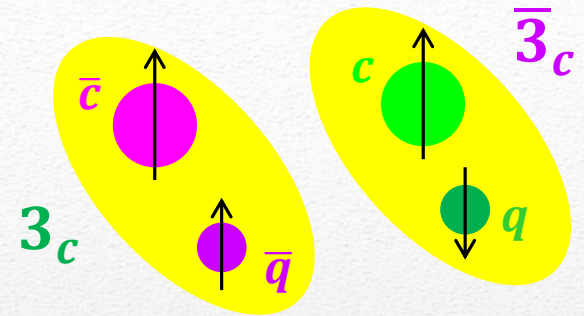
S. Weinberg, PRL110 261601

Kencht and Peris, PRD88, 036016

Cohen and Lebed, PRD89, 054018

Cohen and Lebed, PRD90, 016001

Maiani, Polosa, Riquer, JHEP1606, 160



The poles can appear at subleading order (nonplanar diagrams), and give rise to narrow objects

See T. Cohen's talk on Tuesday 17:30

# Tetraquark: new ansatz

Maiani, Piccinini, Polosa, Riquer PRD89 114010

$J^{PC}$	$cq \bar{c}\bar{q}$	$c\bar{c} q\bar{q}$	Resonance Assig.	Decays
$0^{++}$	$ 0, 0\rangle$	$1/2 0, 0\rangle + \sqrt{3}/2 1, 1\rangle_0$	$X_0(\sim 3770 \text{ MeV})$	$\eta_c, J/\psi + \text{light mesons}$
$0^{++}$	$ 1, 1\rangle_0$	$\sqrt{3}/2 0, 0\rangle - 1/2 1, 1\rangle_0$	$X'_0(\sim 4000 \text{ MeV})$	$\eta_c, J/\psi + \text{light mesons}$
$1^{++}$	$1/\sqrt{2}( 1, 0\rangle +  0, 1\rangle)$	$ 1, 1\rangle_1$	$X_1 = X(3872)$	$J/\psi + \rho/\omega, DD^*$
$1^{+-}$	$1/\sqrt{2}( 1, 0\rangle -  0, 1\rangle)$	$1/\sqrt{2}( 1, 0\rangle -  0, 1\rangle)$	$Z = Z(3900)$	$J/\psi + \pi, h_c/\eta_c + \pi/\rho$
$1^{+-}$	$ 1, 1\rangle_1$	$1/\sqrt{2}( 1, 0\rangle +  0, 1\rangle)$	$Z' = Z(4020)$	$J/\psi + \pi, h_c/\eta_c + \pi/\rho$
$2^{++}$	$ 1, 1\rangle_2$	$ 1, 1\rangle_2$	$X_2(\sim 4000 \text{ MeV})$	$J/\psi + \text{light mesons}$

$$\Delta H = \frac{B_c \vec{L}^2}{2} - 2a \vec{L} \cdot \vec{S}$$

$L = 1$	$P(S_{c\bar{c}} = 1) : P(S_{c\bar{c}} = 0)$	Assignment	Radiative Decay
$Y_1$	3:1	$Y(4008)$	$\gamma + X_0$
$Y_2$	1:0	$Y(4260)$	$\gamma + X$
$Y_3$	1:3	$Y(4290)/Y(4220)$	$\gamma + X'_0$
$Y_4$	1:0	$Y(4630)$	$\gamma + X_2$

actually observed  
BESIII PRL 112,  
092001

Radial excitations

$$Z(2S) = Z(4430)$$

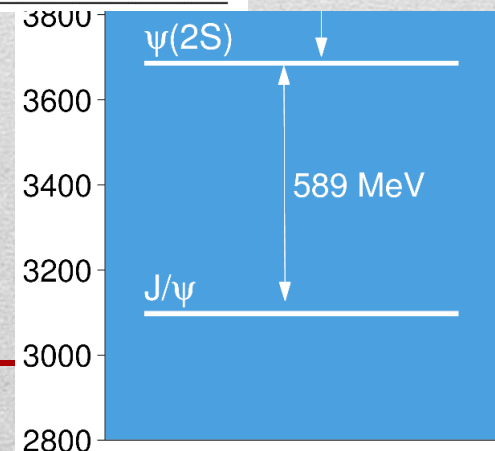
$$Y_1(2P) = Y(4360)$$

$$Y_2(2P) = Y(4660)$$

Decay in  $\psi(2S)$  preferably

$$M_{Z(4430)} - M_{Z_c} = 586^{+17}_{-26} \text{ MeV}$$

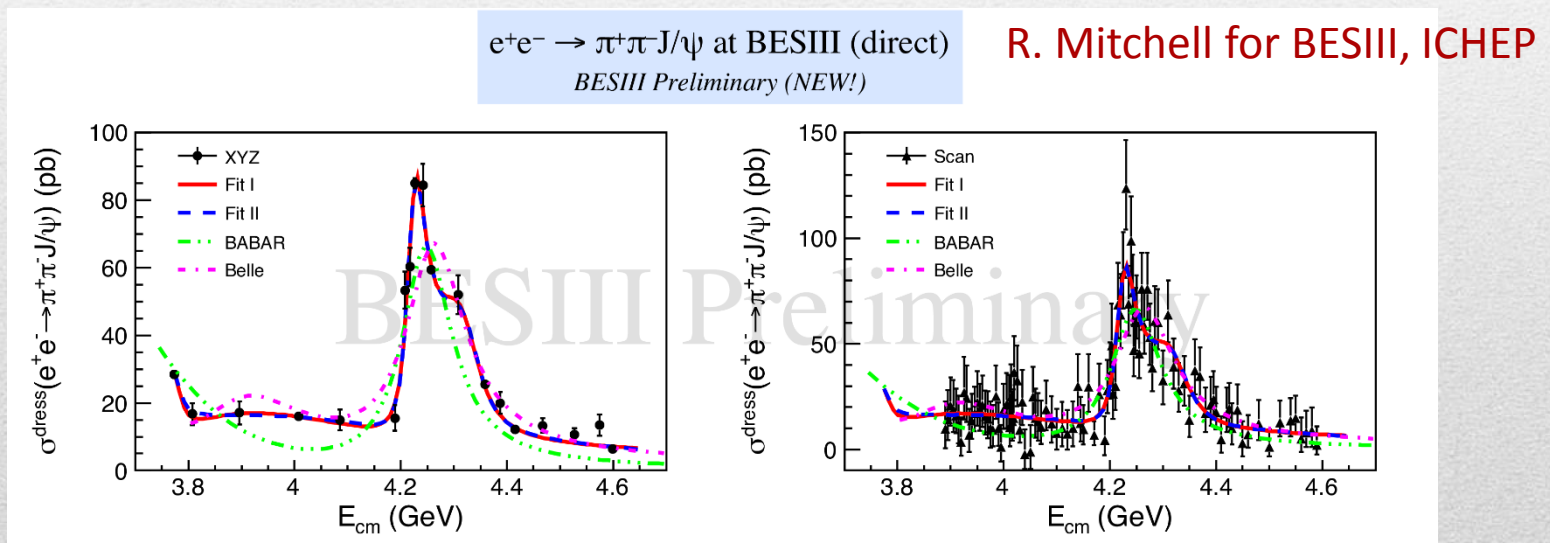
to compare with charmonium





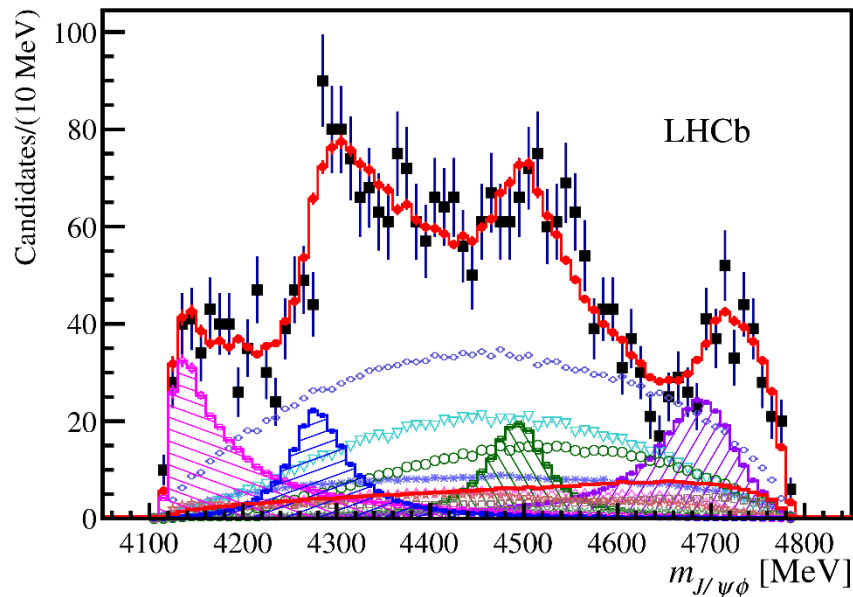
# Tetraquark: the $Y$ states

	$L = 1$	$P(S_{c\bar{c}} = 1) : P(S_{c\bar{c}} = 0)$	Assignment	Radiative Decay
$J/\psi \pi\pi$ ←	$Y_1$	3:1	$Y(4008)$	$\gamma + X_0$
	$Y_2$	1:0	$Y(4260)$	$\gamma + X$
$h_c \pi\pi$ ←	$Y_3$	1:3	$Y(4290)/Y(4220)$	$\gamma + X'_0$
$\Lambda_c^+ \Lambda_c^-$ ←	$Y_4$	1:0	$Y(4630)$	$\gamma + X_2$



New data on the  $Y$  states are going to change this picture, waiting for a clarification

# Tetraquark: the $c\bar{c}s\bar{s}$ states



$$\begin{array}{ccc}
 \frac{0^{++'}}{X(4274)} + \kappa & \frac{1^{+-'}}{+ \kappa} & \frac{2^{++}}{X(4274)} + \kappa \\
 & & \uparrow \\
 \frac{1^{++}}{X(4140)} - \kappa & \frac{1^{+-}}{- \kappa} & + 2 m_{[cs]} = M \\
 \frac{0^{++}}{- 3 \kappa} & & 
 \end{array}$$

$$\begin{aligned}
 J^{PC} = 0^{++} & \quad X_0 = |0, 0\rangle_0, \quad X'_0 = |1, 1\rangle_0 \\
 J^{PC} = 2^{++} & \quad X_2 = |1, 1\rangle_2 \\
 J^{PC} = 1^{++} & \quad X = \frac{1}{\sqrt{2}} (|1, 0\rangle_1 + |0, 1\rangle_1) \\
 J^{PC} = 1^{+-} & \quad Z = \frac{1}{\sqrt{2}} (|1, 0\rangle_1 - |0, 1\rangle_1) \\
 & \quad Z' = |1, 1\rangle_1
 \end{aligned}$$

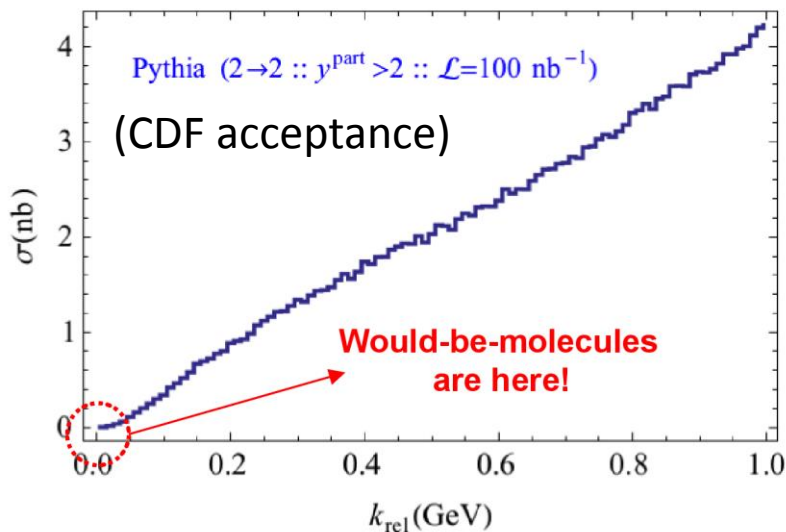
Good description of the spectrum **but** one has to assume the axial assignment for the  $X(4274)$  to be incorrect (two unresolved states with  $0^{++}$  and  $2^{++}$ )

Maiani, Polosa and Riquer, arXiv:1607.02405  
Esposito, AP, Polosa, to appear



# Prompt production of $X(3872)$

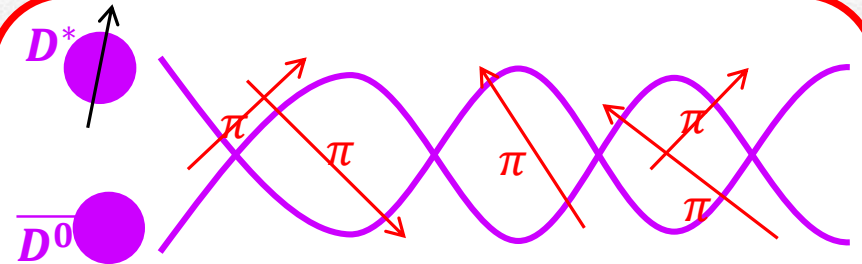
$X(3872)$  is the Queen of exotic resonances, the most popular interpretation is a  $D^0 \bar{D}^{0*}$  **molecule** (bound state, pole in the 1<sup>st</sup> Riemann sheet?) but it is copiously promptly produced at hadron colliders



$$\sigma_{MC}(p\bar{p} \rightarrow DD^* | k < k_{\text{max}}) \approx 0.1 \text{ nb}$$

$$\sigma_{\text{exp}}(p\bar{p} \rightarrow X(3872)) \approx 30 - 70 \text{ nb!!!}$$

Bignamini *et al.* PRL103 (2009) 162001



A solution can be FSI (rescattering of  $DD^*$ ), which allow  $k_{\text{max}}$  to be as large as  $5m_\pi$ ,  
 $\sigma(p\bar{p} \rightarrow DD^* | k < k_{\text{max}}) \approx 230 \text{ nb}$

Artoisenet and Braaten, PRD81, 114018

However, the rescattering is flawed by the presence of pions that interfere with  $DD^*$  propagation. Estimating the effect of these pions increases  $\sigma$ , but not enough

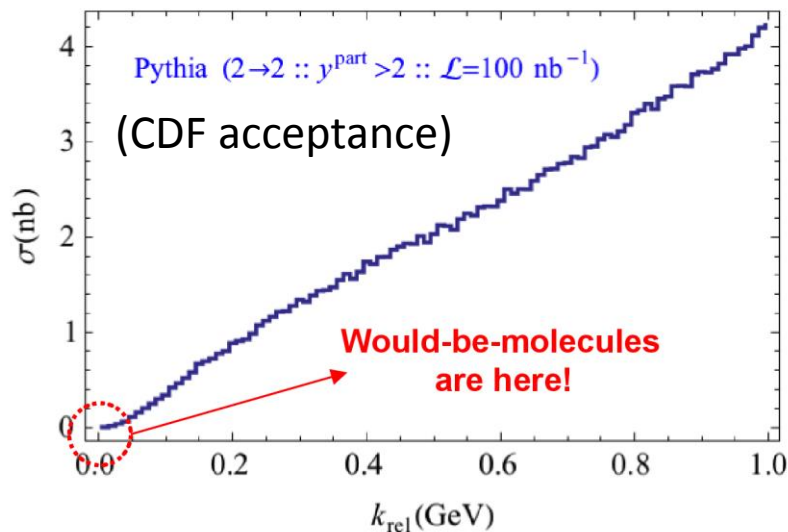
Bignamini *et al.* PLB684, 228-230

Esposito, Piccinini, AP, Polosa, JMP 4, 1569

Guerrieri, Piccinini, AP, Polosa, PRD90, 034003

# Prompt production of $X(3872)$

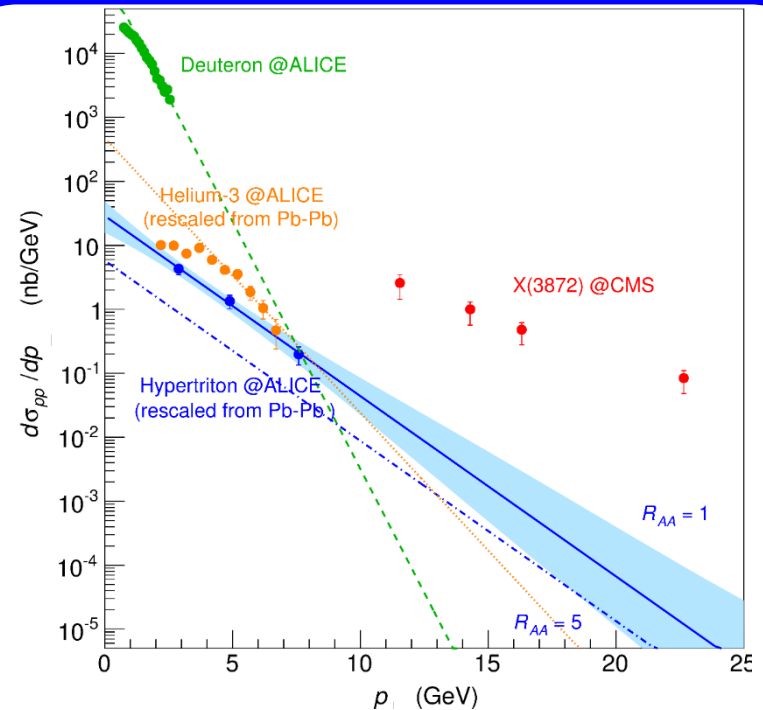
$X(3872)$  is the Queen of exotic resonances, the most popular interpretation is a  $D^0 \bar{D}^{0*}$  molecule (bound state, pole in the 1<sup>st</sup> Riemann sheet?) but it is copiously promptly produced at hadron colliders



$$\sigma_{MC}(p\bar{p} \rightarrow DD^* | k < k_{\text{max}}) \approx 0.1 \text{ nb}$$

$$\sigma_{\text{exp}}(p\bar{p} \rightarrow X(3872)) \approx 30 - 70 \text{ nb!!!}$$

Bignamini *et al.* PRL103 (2009) 162001



Also, a comparison to light nuclei does not favor the  $X(3872)$  to share the same nature

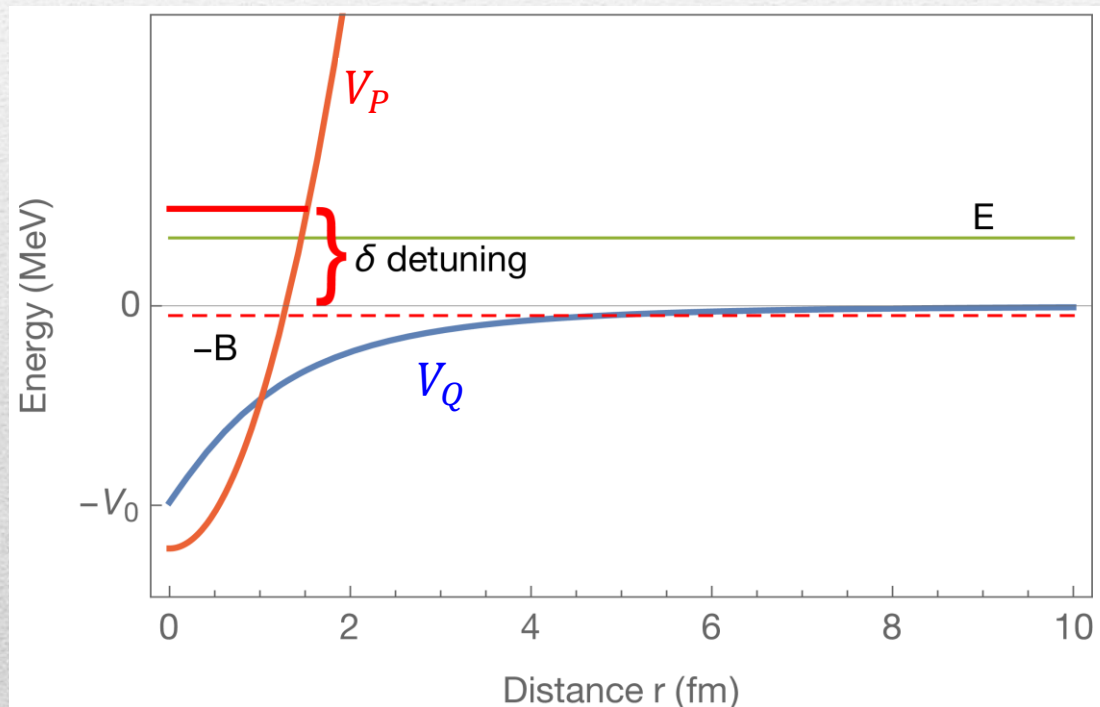
Esposito, Guerrieri, Maiani,  
Piccinini, AP, Polosa, Riquer, PRD92, 034028



# Hybridized tetraquarks

Esposito, AP, Polosa, PLB758, 292

Feshbach mechanism occurs when two atoms can interact with **two potentials**, resp. with **continuum** ("molecule") and **discrete (4q)** spectrum  $\rightarrow$  **hybridization**



Let  $P$  and  $Q$  be orthogonal subspaces of the Hilbert space

$$H = H_{PP} + H_{QQ}$$

We have the (weak) scattering length  $a_P$  in the open channel.

We add an off-diagonal  $H_{QP}$

$$a = a_P - c \sum \frac{|\langle \psi_n | H_{QP} | \psi_P \rangle|^2}{E_n - E + i\epsilon}$$

$$\simeq a_P \left( 1 - \frac{\kappa}{\delta - E + i\epsilon} \right)$$

# Hybridized tetraquarks

Esposito, AP, Polosa, PLB758, 292

$X(3872)$  should be a  $I = 0$  state, but  $M(1^{++}) < M(D^{*+}D^-)$

$\delta < 0$ , so  $a > 0 \rightarrow$  Repulsive interaction

No charged component, isospin violation!

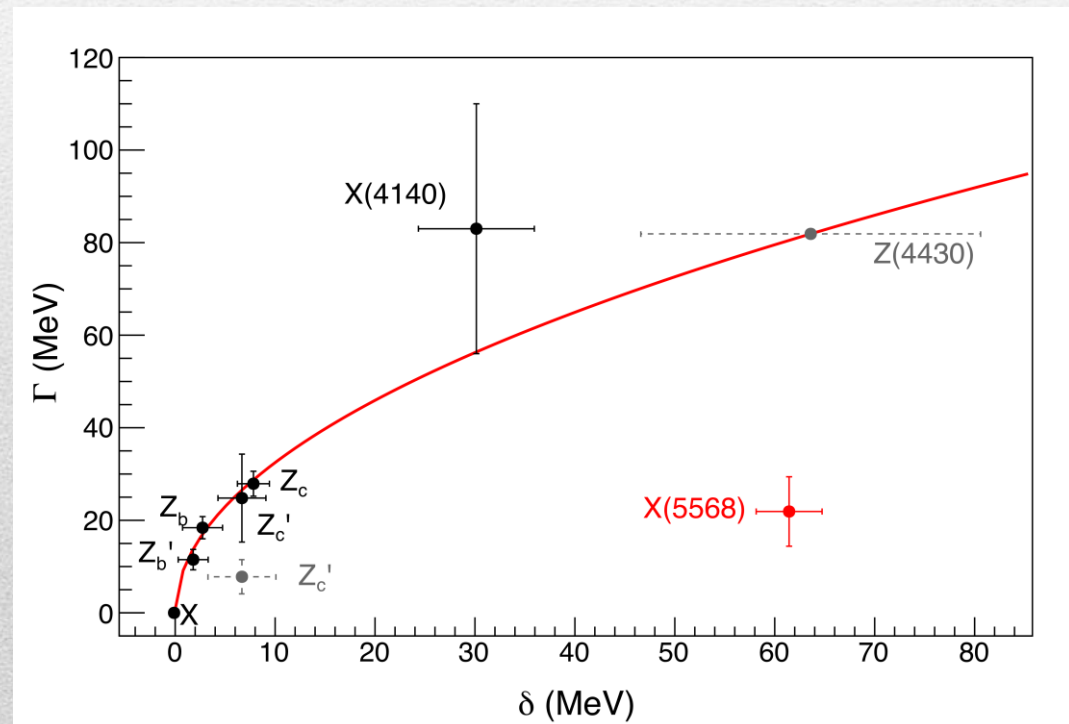
$$d\Gamma = \rho v \sigma_{inel} \sim \delta(E - \delta) |\kappa a_p| \frac{d^3p}{m}$$

$$\Gamma \sim \sqrt{2m} |\kappa a_p| \sqrt{\delta} \equiv A\sqrt{\delta}$$

$E < E_{max}$ , with  $E_{max}$  estimated by diquarkonium potential to be

- $\sim 20$  MeV for charmonium
- $\sim 40$  MeV for bottomonium

The closest threshold below the state dominates the interaction





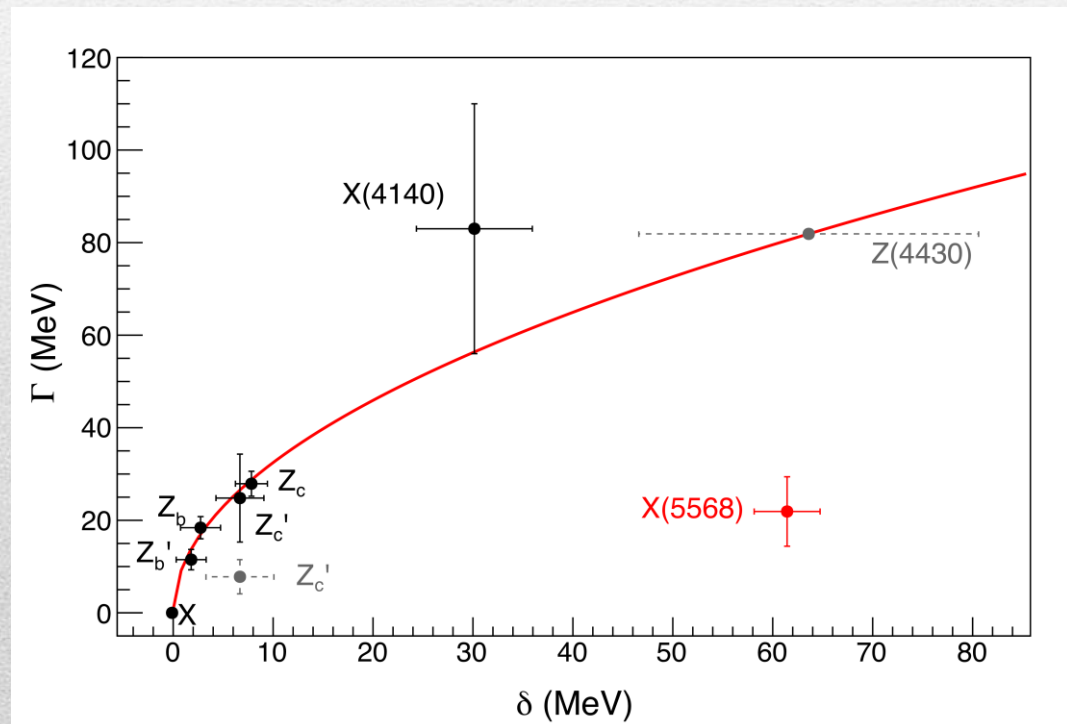
# Hybridized tetraquarks

Esposito, AP, Polosa, PLB758, 292

The model works only if no direct transition between closed channel levels can occur  
This prevents the straightforward generalization to  $L = 1$  and radially excited states  
(like the  $Y$ s or the  $Z(4430)$ )

In this picture, a  $[bu][\bar{s}\bar{d}]$  state with resonance parameters of the  $X(5568)$  observed by D0 is not likely

Also, one has to ensure the orthogonality between the two Hilbert subspaces  $P$  and  $Q$ .  
This might affect the estimate for the  $X(4140)$




# Production & Feshbach?

Going back to  $pp(\bar{p})$  collisions, we can imagine hadronization to produce a state

$$|\psi\rangle = \alpha|[qQ][\bar{q}\bar{Q}]\rangle_c + \beta|(\bar{q}q)(\bar{Q}Q)\rangle_o + \gamma|(\bar{q}Q)(\bar{Q}q)\rangle_o$$

If  $\beta, \gamma \gg \alpha$ , an initial tetraquark state is not likely to be produced

The open channel mesons fly apart  
(see MC simulations)



If Feshbach mechanism is at work, an open state can resonate in a closed one

## No prompt production without Feshbach resonances!

Note that only the  $X(3872)$  has been observed promptly so far...

...and a narrow  $X(4140)$  not compatible with the LHCb one → **needs confirmation**



# Conclusions & prospects

The study of **exotic heavy quark sector** is a **challenging task**

Experiments are very prolific! **Constant feedback on predictions**

- Study of spectra and decay patterns will improve our understanding, **new data** expected by BESIII, LHCb, Belle II, JLab
- **Nuclei observation at hadron colliders** can give an unexpected help in testing some phenomenological hypotheses for the XYZ states
- Search for exotic states in **prompt production** is a necessary step to improve our understanding of the sector
- Feshbach mechanism might be effective in **reducing the number of states** predicted by the tetraquark picture

**Thank you**

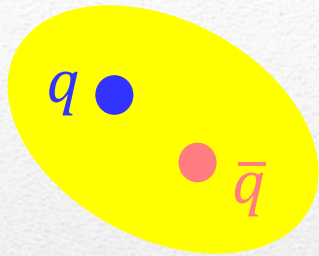
---

# BACKUP





# Quarkonium orthodoxy



Heavy quarkonium sector is extremely useful  
for the understanding of QCD

$$\alpha_s(M_Q) \sim 0.3$$

(perturbative regime)

OZI-rule, QCD multipole

Heavy quark spin flip suppressed by quark mass,  
approximate heavy quark spin symmetry (HQSS)

## Potential models

(meaningful when  $M_Q \rightarrow \infty$ )

$$V(r) = -\frac{C_F \alpha_s}{r} + \sigma r$$

(Cornell potential)

Solve NR Schrödinger eq.  $\rightarrow$  spectrum

## Effective theories

(HQET, NRQCD...)

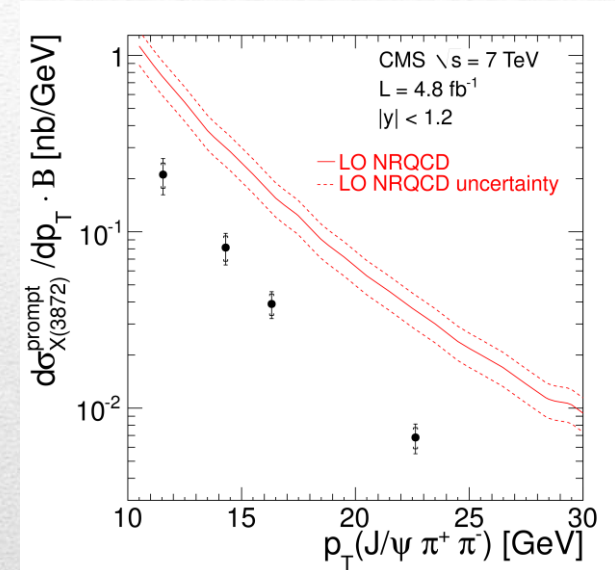
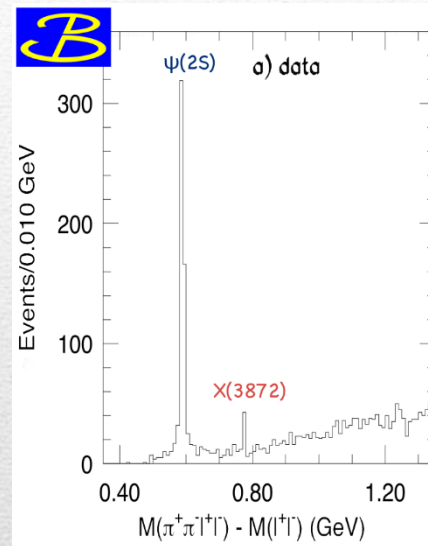
Integrate out heavy DOF



(spectrum), decay & production rates

# X(3872)

- Discovered in  
 $B \rightarrow K X \rightarrow J/\psi \pi\pi$
- Very close to  $DD^*$  threshold
- Too narrow for an above-threshold charmonium
- Isospin violation too big  
 $\frac{\Gamma(X \rightarrow J/\psi \omega)}{\Gamma(X \rightarrow J/\psi \rho)} \sim 0.8 \pm 0.3$
- Mass prediction not compatible with  $\chi_{c1}(2P)$



Unexpected large prompt production  
at hadron colliders

$$\sigma_B/\sigma_{TOT} = (26.3 \pm 2.3 \pm 1.6)\%$$

$$\sigma_{PR} \times B(X \rightarrow J/\psi \pi\pi) = (1.06 \pm 0.11 \pm 0.15) \text{ nb}$$

CMS, JHEP 1304, 154

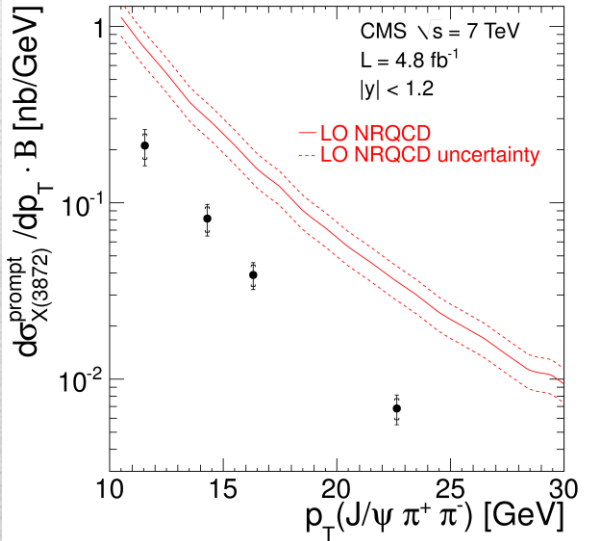
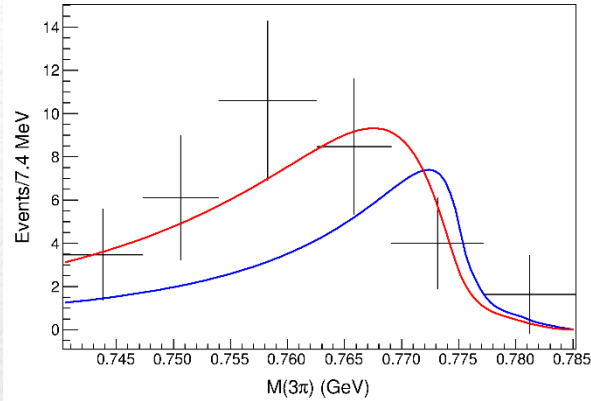
$$M = 3871.68 \pm 0.17 \text{ MeV}$$

$$M_X - M_{DD^*} = -3 \pm 192 \text{ keV}$$

$$\Gamma < 1.2 \text{ MeV @90\%}, J^{PC} = 1^{++}$$



# X(3872)

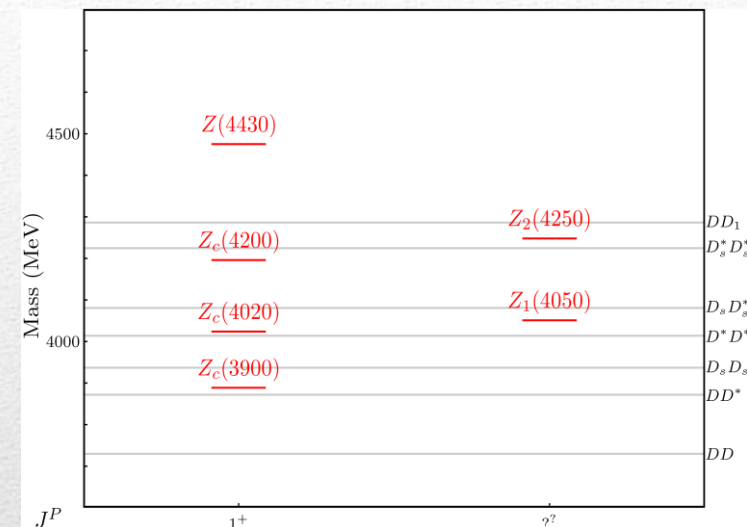


B decay mode	X decay mode	product branching fraction ( $\times 10^5$ )		$B_{fit}$	$R_{fit}$
$K^+ X$	$X \rightarrow \pi\pi J/\psi$	<b><math>0.86 \pm 0.08</math></b>	(BABAR <sup>[26]</sup> Belle <sup>[25]</sup> )	$0.081^{+0.019}_{-0.031}$	1
		$0.84 \pm 0.15 \pm 0.07$	BABAR <sup>[26]</sup>		
		$0.86 \pm 0.08 \pm 0.05$	Belle <sup>[25]</sup>		
$K^0 X$	$X \rightarrow \pi\pi J/\psi$	<b><math>0.41 \pm 0.11</math></b>	(BABAR <sup>[26]</sup> Belle <sup>[25]</sup> )		
		$0.35 \pm 0.19 \pm 0.04$	BABAR <sup>[26]</sup>		
		$0.43 \pm 0.12 \pm 0.04$	Belle <sup>[25]</sup>		
$(K^+\pi^-)_{NR} X$	$X \rightarrow \pi\pi J/\psi$	$0.81 \pm 0.20^{+0.11}_{-0.14}$	Belle <sup>[106]</sup>		
$K^{*0} X$	$X \rightarrow \pi\pi J/\psi$	$< 0.34$ , 90% C.L.	Belle <sup>[106]</sup>		
$K X$	$X \rightarrow \omega J/\psi$	$R = 0.8 \pm 0.3$	BABAR <sup>[33]</sup>	$0.061^{+0.024}_{-0.036}$	$0.77^{+0.28}_{-0.32}$
$K^+ X$		$0.6 \pm 0.2 \pm 0.1$	BABAR <sup>[33]</sup>		
$K^0 X$		$0.6 \pm 0.3 \pm 0.1$	BABAR <sup>[33]</sup>		
$K X$	$X \rightarrow \pi\pi\pi^0 J/\psi$	$R = 1.0 \pm 0.4 \pm 0.3$	Belle <sup>[32]</sup>		
$K^+ X$	$X \rightarrow D^{*0} \bar{D}^0$	<b><math>8.5 \pm 2.6</math></b>	(BABAR <sup>[38]</sup> Belle <sup>[37]</sup> )	$0.614^{+0.166}_{-0.074}$	$8.2^{+2.3}_{-2.8}$
		$16.7 \pm 3.6 \pm 4.7$	BABAR <sup>[38]</sup>		
		$7.7 \pm 1.6 \pm 1.0$	Belle <sup>[37]</sup>		
$K^0 X$	$X \rightarrow D^{*0} \bar{D}^0$	<b><math>12 \pm 4</math></b>	(BABAR <sup>[38]</sup> Belle <sup>[37]</sup> )		
		$22 \pm 10 \pm 4$	BABAR <sup>[38]</sup>		
		$9.7 \pm 4.6 \pm 1.3$	Belle <sup>[37]</sup>		
$K^+ X$	$X \rightarrow \gamma J/\psi$	<b><math>0.202 \pm 0.038</math></b>	(BABAR <sup>[35]</sup> Belle <sup>[34]</sup> )	$0.019^{+0.005}_{-0.009}$	$0.24^{+0.05}_{-0.06}$
$K^+ X$		$0.28 \pm 0.08 \pm 0.01$	BABAR <sup>[35]</sup>		
		$0.178^{+0.048}_{-0.044} \pm 0.012$	Belle <sup>[34]</sup>		
$K^0 X$		$0.26 \pm 0.18 \pm 0.02$	BABAR <sup>[35]</sup>		
		$0.124^{+0.076}_{-0.061} \pm 0.011$	Belle <sup>[34]</sup>		
$K^+ X$	$X \rightarrow \gamma\psi(2S)$	<b><math>0.44 \pm 0.12</math></b>	BABAR <sup>[35]</sup>	$0.04^{+0.015}_{-0.020}$	$0.51^{+0.13}_{-0.17}$
$K^+ X$		$0.95 \pm 0.27 \pm 0.06$	BABAR <sup>[35]</sup>		
		$0.083^{+0.198}_{-0.183} \pm 0.044$	Belle <sup>[34]</sup>		
		$R' = 2.46 \pm 0.64 \pm 0.29$	LHCb <sup>[36]</sup>		
$K^0 X$		$1.14 \pm 0.55 \pm 0.10$	BABAR <sup>[35]</sup>		
		$0.112^{+0.357}_{-0.290} \pm 0.057$	Belle <sup>[34]</sup>		
$K^+ X$	$X \rightarrow \gamma\chi_{c1}$	$< 9.6 \times 10^{-3}$	Belle <sup>[23]</sup>	$< 1.0 \times 10^{-3}$	$< 0.014$
$K^+ X$	$X \rightarrow \gamma\chi_{c2}$	$< 0.016$	Belle <sup>[23]</sup>	$< 1.7 \times 10^{-3}$	$< 0.024$
$K X$	$X \rightarrow \gamma\gamma$	$< 4.5 \times 10^{-3}$	Belle <sup>[111]</sup>	$< 4.7 \times 10^{-4}$	$< 6.6 \times 10^{-3}$
$K X$	$X \rightarrow \eta J/\psi$	$< 1.05$	BABAR <sup>[112]</sup>	$< 0.11$	$< 1.55$
$K^+ X$	$X \rightarrow p\bar{p}$	$< 9.6 \times 10^{-4}$	LHCb <sup>[110]</sup>	$< 1.6 \times 10^{-4}$	$< 2.2 \times 10^{-3}$

# Charged Z states...

Charged quarkonium-like resonances have been found, **4q needed**

Two states  $J^{PC} = 1^{+-}$  appear slightly above  $D^{(*)}D^*$  thresholds



$e^+e^- \rightarrow Z_c(3900)^+\pi^- \rightarrow J/\psi \pi^+\pi^-$  and  $\rightarrow (DD^*)^+\pi^-$

$M = 3888.7 \pm 3.4 \text{ MeV}, \Gamma = 35 \pm 7 \text{ MeV}$

$e^+e^- \rightarrow Z'_c(4020)^+\pi^- \rightarrow h_c \pi^+\pi^-$  and  $\rightarrow \bar{D}^{*0}D^{*+}\pi^-$

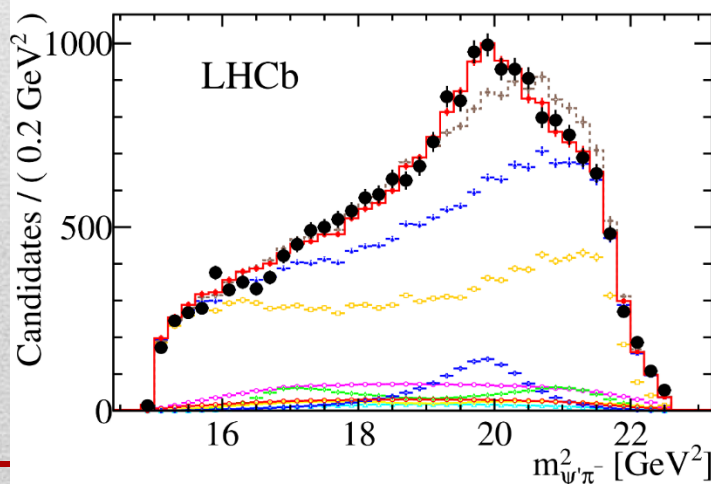
$M = 4023.9 \pm 2.4 \text{ MeV}, \Gamma = 10 \pm 6 \text{ MeV}$

Similar system in bottomonium

$Z(4430)^+ \rightarrow \psi(2S) \pi^+$   
 $I^G J^{PC} = 1^+ 1^{+-}$

$M = 4475 \pm 7_{-25}^{+15} \text{ MeV}$   
 $\Gamma = 172 \pm 13_{-34}^{+37} \text{ MeV}$

Far from open charm thresholds

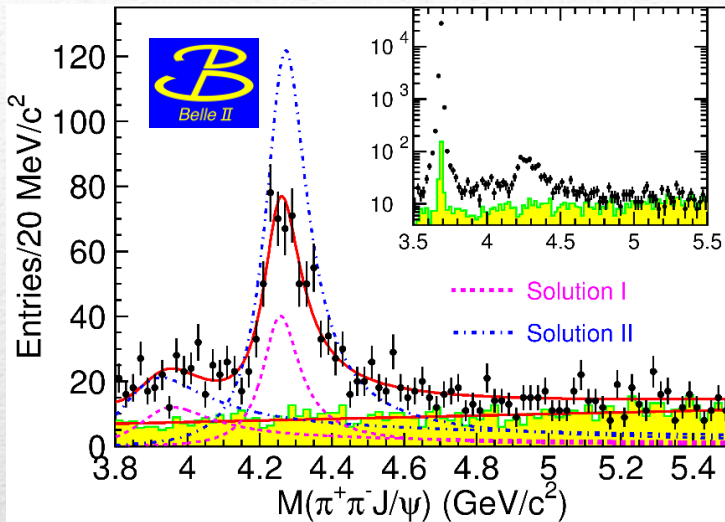


...Y vectors,  
pentaquarks...



# Vector $Y$ states

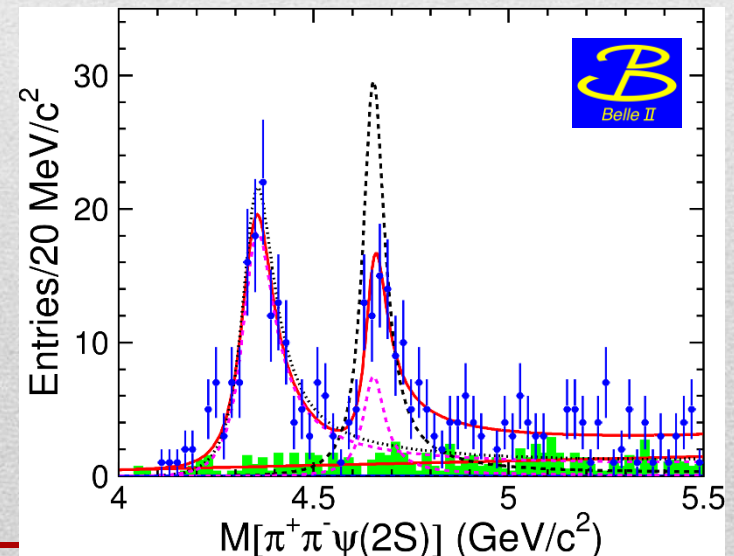
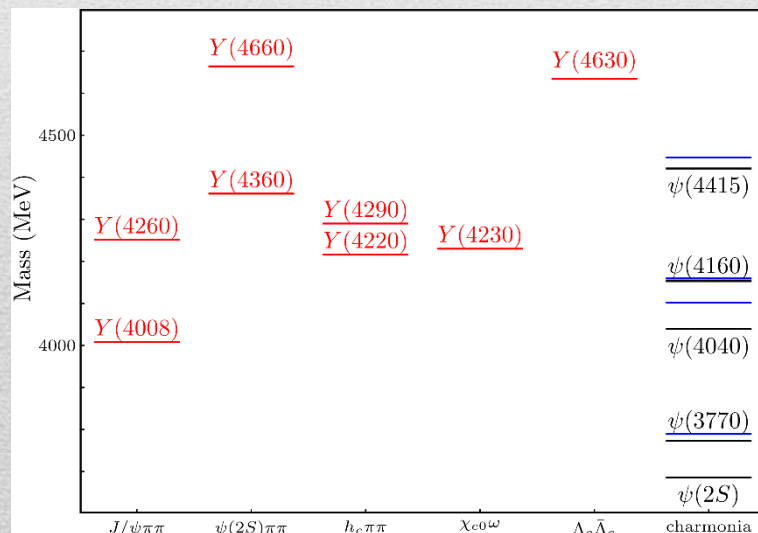
Lots of unexpected  $J^{PC} = 1^{--}$  states found in ISR analyses (and nowhere else!)



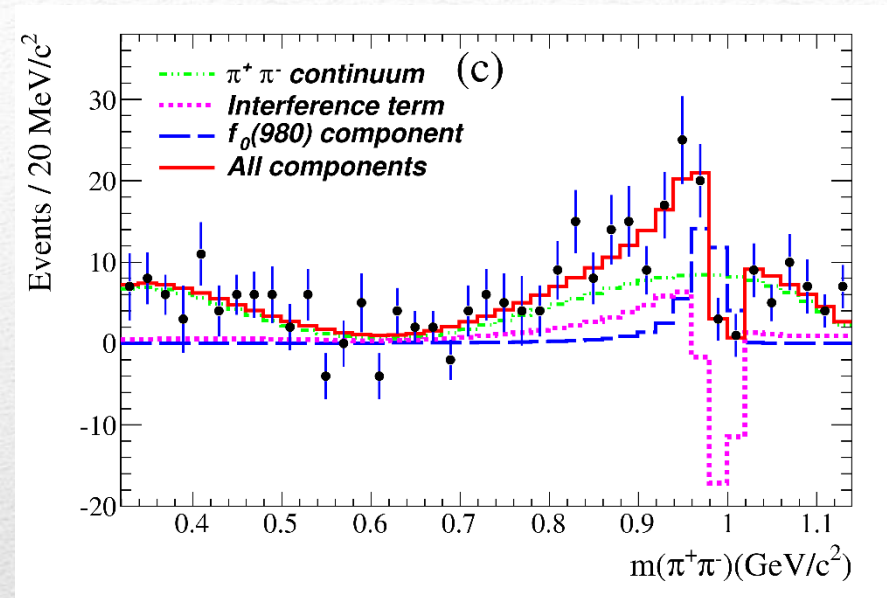
Seen in **few final states**,  
mostly  $J/\psi \pi\pi$  and  $\psi(2S) \pi\pi$

**Not seen decaying into open charm pairs**,  
to compare with

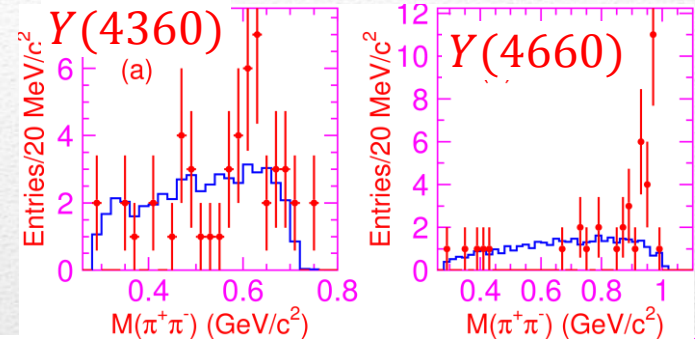
$$\frac{B(\psi(3770) \rightarrow D\bar{D})}{B(\psi(3770) \rightarrow J/\psi \pi\pi)} > 480$$



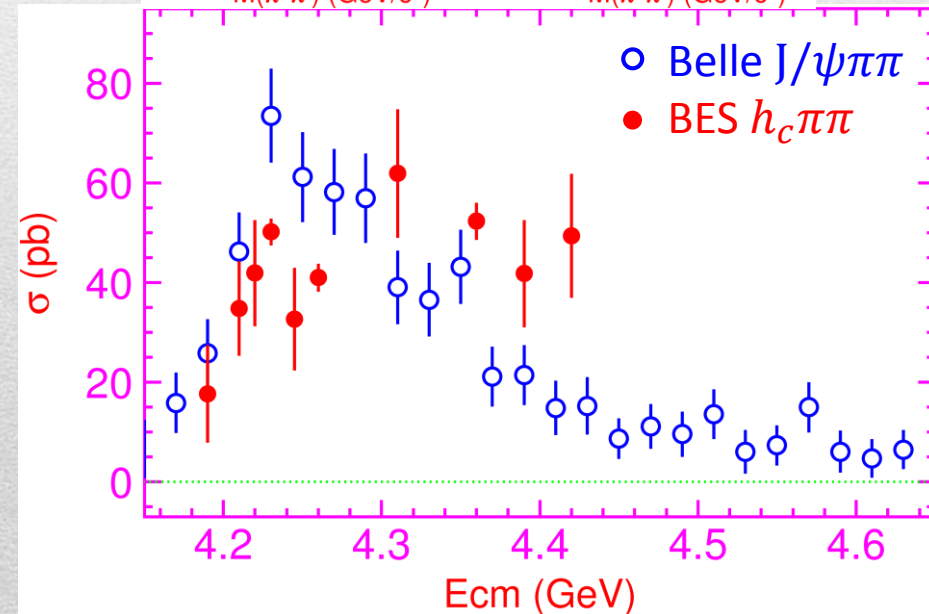
# Vector $Y$ states



A component  $Y(4260) \rightarrow J/\psi f_0(980)$   
might explain why  $Y(4260) \rightarrow \psi(2S)\pi\pi$

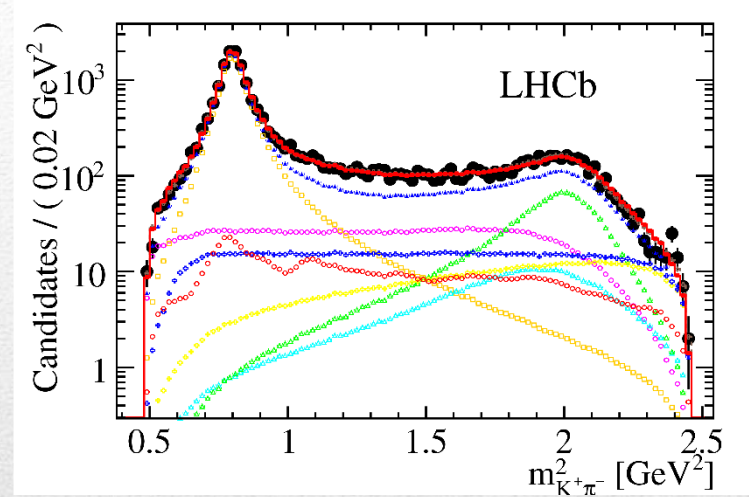
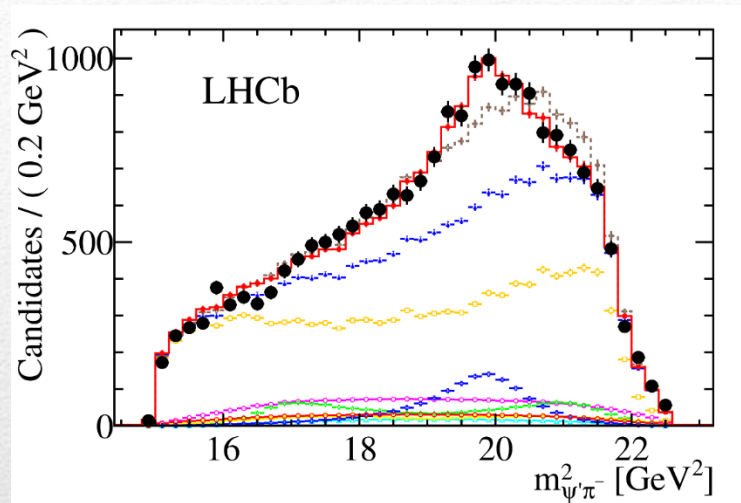


The lineshape in  $h_c \pi\pi$  looks pretty different  
Different states contributing?





# Charged Z states: Z(4430)



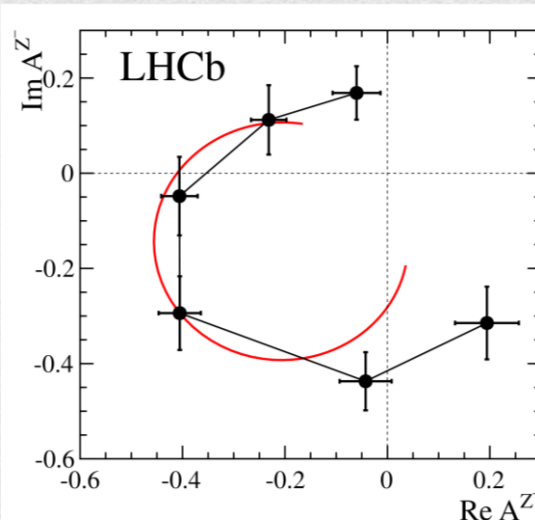
$$Z(4430)^+ \rightarrow \psi(2S) \pi^+$$

$$I^G J^{PC} = 1^+ 1^{+-}$$

$$M = 4475 \pm 7_{-25}^{+15} \text{ MeV}$$

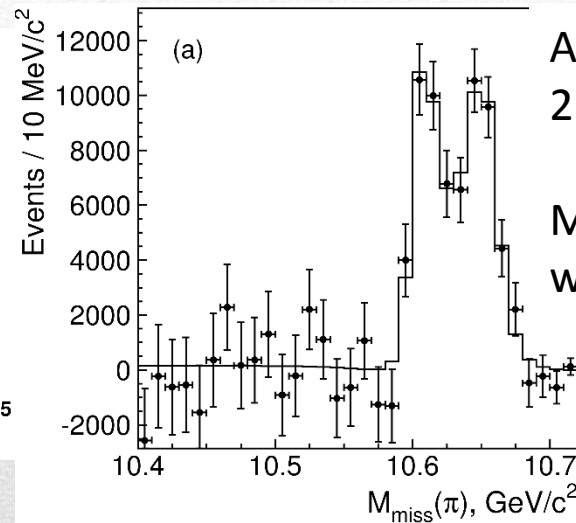
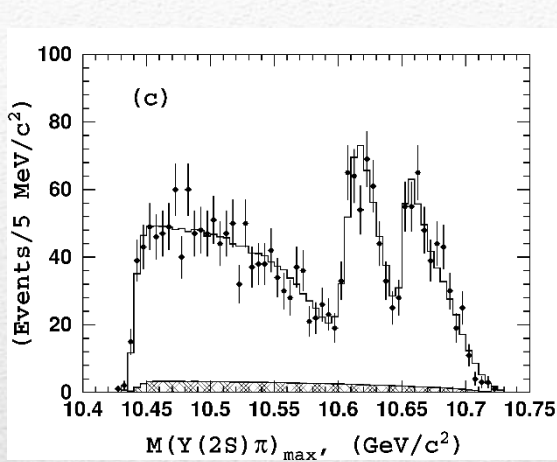
$$\Gamma = 172 \pm 13_{-34}^{+37} \text{ MeV}$$

Far from open charm thresholds



If the amplitude is a free complex number, in each bin of  $m_{\psi'\pi^-}^2$ , the resonant behaviour appears as well

# Charged Z states: $Z_b(106010)$ , $Z'_b(10650)$



Anomalous dipion width in  $\Upsilon(5S)$ ,  
2 orders of magnitude larger than  $\Upsilon(nS)$

Moreover, observed  $\Upsilon(5S) \rightarrow h_b(nP)\pi\pi$   
which violates HQSS

2 twin resonances!

$$\Upsilon(5S) \rightarrow Z_b(10610)^+\pi^- \rightarrow \Upsilon(nS)\pi^+\pi^-, h_b(nP)\pi^+\pi^-$$

$$\text{and } \rightarrow (BB^*)^+\pi^-$$

$$M = 10607.2 \pm 2.0 \text{ MeV}, \Gamma = 18.4 \pm 2.4 \text{ MeV}$$

$$\Upsilon(5S) \rightarrow Z'_b(10650)^+\pi^- \rightarrow \Upsilon(nS)\pi^+\pi^-, h_b(nP)\pi^+\pi^-$$

$$\text{and } \rightarrow \bar{B}^{*0}B^{*+}\pi^-$$

$$M = 10652.2 \pm 1.5 \text{ MeV}, \Gamma = 11.5 \pm 2.2 \text{ MeV}$$



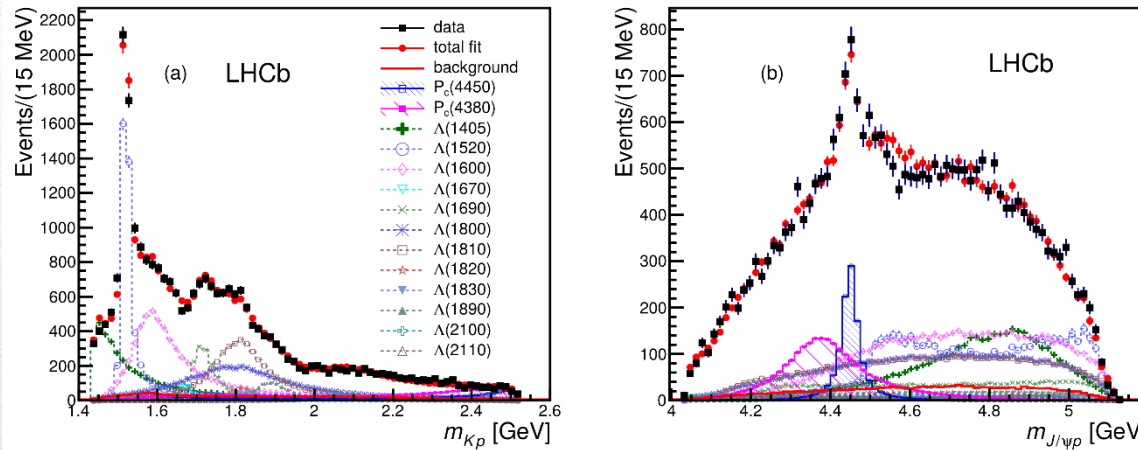
State	$M$ (MeV)	$\Gamma$ (MeV)	$J^{PC}$	Process (mode)	Experiment ( $\# \sigma$ )
$X(3823)$	$3823.1 \pm 1.9$	$< 24$	$?^{-}$	$B \rightarrow K(\chi_{c1} \gamma)$	Belle <sup>[23]</sup> (4.0)
$X(3872)$	$3871.68 \pm 0.17$	$< 1.2$	$1^{++}$	$B \rightarrow K(\pi^+ \pi^- J/\psi)$	Belle <sup>[24,25]</sup> ( $>10$ ), BABAR <sup>[26]</sup> (8.6)
				$p\bar{p} \rightarrow (\pi^+ \pi^- J/\psi) \dots$	CDR <sup>[27,28]</sup> (11.6), D0 <sup>[29]</sup> (5.2)
				$pp \rightarrow (\pi^+ \pi^- J/\psi) \dots$	LHCb <sup>[30,31]</sup> (np)
				$B \rightarrow K(\pi^+ \pi^- \pi^0 J/\psi)$	Belle <sup>[32]</sup> (4.3), BABAR <sup>[33]</sup> (4.0)
				$B \rightarrow K(\gamma J/\psi)$	Belle <sup>[34]</sup> (5.5), BABAR <sup>[35]</sup> (3.5)
					LHCb <sup>[36]</sup> ( $>10$ )
				$B \rightarrow K(\gamma \psi(2S))$	BABAR <sup>[35]</sup> (3.6), Belle <sup>[34]</sup> (0.2)
					LHCb <sup>[36]</sup> (4.4)
				$B \rightarrow K(D\bar{D}^*)$	Belle <sup>[37]</sup> (6.4), BABAR <sup>[38]</sup> (4.9)
$Z_c(3900)^+$	$3888.7 \pm 3.4$	$35 \pm 7$	$1^{+-}$	$Y(4260) \rightarrow \pi^- (D\bar{D}^*)^+$	BES III <sup>[39]</sup> (np)
				$Y(4260) \rightarrow \pi^- (\pi^+ J/\psi)$	BES III <sup>[40]</sup> (8), Belle <sup>[41]</sup> (5.2)
					CLEO data <sup>[42]</sup> ( $>5$ )
$Z_c(4020)^+$	$4023.9 \pm 2.4$	$10 \pm 6$	$1^{+-}$	$Y(4260) \rightarrow \pi^- (\pi^+ h_c)$	BES III <sup>[43]</sup> (8.9)
				$Y(4260) \rightarrow \pi^- (D^* \bar{D}^*)^+$	BES III <sup>[44]</sup> (10)
$Y(3915)$	$3918.4 \pm 1.9$	$20 \pm 5$	$0^{++}$	$B \rightarrow K(\omega J/\psi)$	Belle <sup>[45]</sup> (8), BABAR <sup>[33,46]</sup> (19)
				$e^+ e^- \rightarrow e^+ e^- (\omega J/\psi)$	Belle <sup>[47]</sup> (7.7), BABAR <sup>[48]</sup> (7.6)
$Z(3930)$	$3927.2 \pm 2.6$	$24 \pm 6$	$2^{++}$	$e^+ e^- \rightarrow e^+ e^- (D\bar{D})$	Belle <sup>[49]</sup> (5.3), BABAR <sup>[50]</sup> (5.8)
$X(3940)$	$3942_{-8}^{+9}$	$37_{-17}^{+27}$	$?^{?+}$	$e^+ e^- \rightarrow J/\psi (D\bar{D}^*)$	Belle <sup>[51,52]</sup> (6)
$Y(4008)$	$3891 \pm 42$	$255 \pm 42$	$1^{--}$	$e^+ e^- \rightarrow (\pi^+ \pi^- J/\psi)$	Belle <sup>[41,53]</sup> (7.4)
$Z(4050)^+$	$4051_{-43}^{+24}$	$82_{-55}^{+51}$	$?^{?+}$	$\bar{B}^0 \rightarrow K^- (\pi^+ \chi_{c1})$	Belle <sup>[54]</sup> (5.0), BABAR <sup>[55]</sup> (1.1)
$Y(4140)$	$4145.6 \pm 3.6$	$14.3 \pm 5.9$	$?^{?+}$	$B^+ \rightarrow K^+ (\phi J/\psi)$	CDR <sup>[56,57]</sup> (5.0), Belle <sup>[58]</sup> (1.9), LHCb <sup>[59]</sup> (1.4), CMS <sup>[60]</sup> ( $>5$ ) D0 <sup>[61]</sup> (3.1)
$X(4160)$	$4156_{-25}^{+29}$	$139_{-65}^{+113}$	$?^{?+}$	$e^+ e^- \rightarrow J/\psi (D^* \bar{D}^*)$	Belle <sup>[52]</sup> (5.5)
$Z(4200)^+$	$4196_{-30}^{+35}$	$370_{-110}^{+99}$	$1^{+-}$	$\bar{B}^0 \rightarrow K^- (\pi^+ J/\psi)$	Belle <sup>[62]</sup> (7.2)

State	$M$ (MeV)	$\Gamma$ (MeV)	$J^{PC}$	Process (mode)	Experiment ( $\# \sigma$ )
$Y(4220)$	$4196_{-30}^{+35}$	$39 \pm 32$	$1^{--}$	$e^+ e^- \rightarrow (\pi^+ \pi^- h_c)$	BES III data <sup>[63,64]</sup> (4.5)
$Y(4230)$	$4230 \pm 8$	$38 \pm 12$	$1^{--}$	$e^+ e^- \rightarrow (\chi_{c0} \omega)$	BES II <sup>[65]</sup> ( $>9$ )
$Z(4250)^+$	$4248_{-45}^{+185}$	$177_{-72}^{+321}$	$?^{?+}$	$\bar{B}^0 \rightarrow K^- (\pi^+ \chi_{c1})$	Belle <sup>[54]</sup> (5.0), BABAR <sup>[55]</sup> (2.0)
$Y(4260)$	$4250 \pm 9$	$108 \pm 12$	$1^{--}$	$e^+ e^- \rightarrow (\pi \pi J/\psi)$	BABAR <sup>[66,67]</sup> (8), CLEO <sup>[68,69]</sup> (11) Belle <sup>[41,53]</sup> (15), BES III <sup>[40]</sup> (np)
				$e^+ e^- \rightarrow (f_0(980) J/\psi)$	BABAR <sup>[67]</sup> (np), Belle <sup>[41]</sup> (np)
				$e^+ e^- \rightarrow (\pi^- Z_c(3900)^+)$	BES III <sup>[40]</sup> (8), Belle <sup>[41]</sup> (5.2)
				$e^+ e^- \rightarrow (\gamma X(3872))$	BES II <sup>[70]</sup> (5.3)
$Y(4290)$	$4293 \pm 9$	$222 \pm 67$	$1^{--}$	$e^+ e^- \rightarrow (\pi^+ \pi^- h_c)$	BES III data <sup>[63,64]</sup> (np)
$X(4350)$	$4350.6_{-5.1}^{+4.6}$	$13_{-10}^{+18}$	$0/2^{?+}$	$e^+ e^- \rightarrow e^+ e^- (\phi J/\psi)$	Belle <sup>[58]</sup> (3.2)
$Y(4360)$	$4354 \pm 11$	$78 \pm 16$	$1^{--}$	$e^+ e^- \rightarrow (\pi^+ \pi^- \psi(2S))$	Belle <sup>[71]</sup> (8), BABAR <sup>[72]</sup> (np)
$Z(4430)^+$	$4478 \pm 17$	$180 \pm 31$	$1^{+-}$	$\bar{B}^0 \rightarrow K^- (\pi^+ \psi(2S))$	Belle <sup>[73,74]</sup> (6.4), BABAR <sup>[75]</sup> (2.4) LHCb <sup>[76]</sup> (13.9)
				$\bar{B}^0 \rightarrow K^- (\pi^+ J/\psi)$	Belle <sup>[62]</sup> (4.0)
$Y(4630)$	$4634_{-11}^{+9}$	$92_{-32}^{+41}$	$1^{--}$	$e^+ e^- \rightarrow (\Lambda_c^+ \bar{\Lambda}_c^-)$	Belle <sup>[77]</sup> (8.2)
$Y(4660)$	$4665 \pm 10$	$53 \pm 14$	$1^{--}$	$e^+ e^- \rightarrow (\pi^+ \pi^- \psi(2S))$	Belle <sup>[71]</sup> (5.8), BABAR <sup>[72]</sup> (5)
$Z_b(10610)^+$	$10607.2 \pm 2.0$	$18.4 \pm 2.4$	$1^{+-}$	$\Upsilon(5S) \rightarrow \pi(\pi \Upsilon(nS))$	Belle <sup>[78,79]</sup> ( $>10$ )
				$\Upsilon(5S) \rightarrow \pi^- (\pi^+ h_b(nP))$	Belle <sup>[78]</sup> (16)
				$\Upsilon(5S) \rightarrow \pi^- (B\bar{B}^*)^+$	Belle <sup>[80]</sup> (8)
$Z_b(10650)^+$	$10652.2 \pm 1.5$	$11.5 \pm 2.2$	$1^{+-}$	$\Upsilon(5S) \rightarrow \pi^- (\pi^+ \Upsilon(nS))$	Belle <sup>[78]</sup> ( $>10$ )
				$\Upsilon(5S) \rightarrow \pi^- (\pi^+ h_b(nP))$	Belle <sup>[78]</sup> (16)
				$\Upsilon(5S) \rightarrow \pi^- (B^* \bar{B}^*)^+$	Belle <sup>[80]</sup> (6.8)

Guerrieri, AP, Piccinini, Polosa,  
IJMPA 30, 1530002

# Pentaquarks... and so on

LHCb, PRL 115, 072001



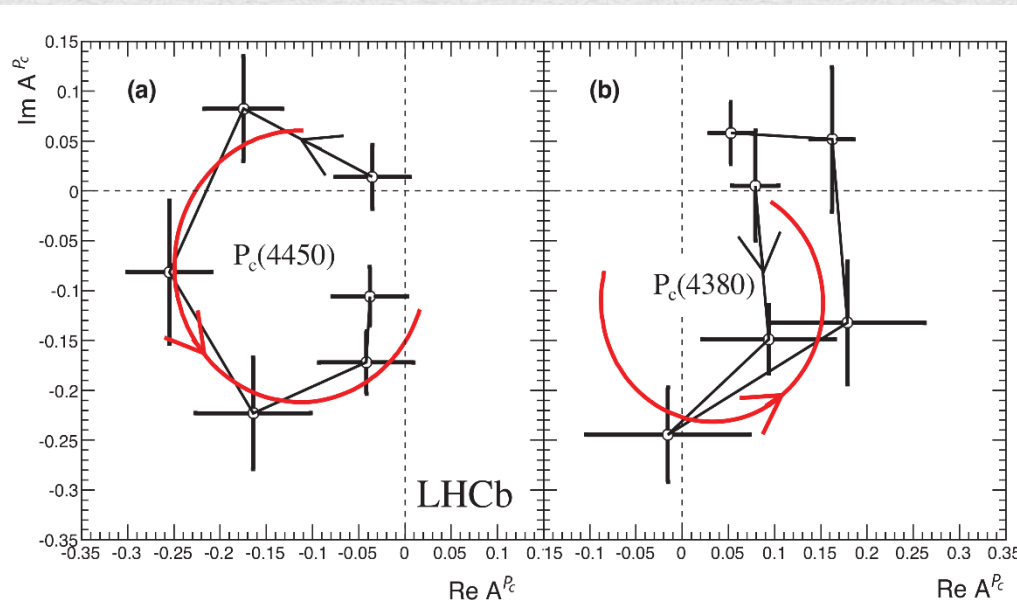
Two states seen in  $\Lambda_b \rightarrow (J/\psi p) K^-$

$$M_1 = 4380 \pm 8 \pm 29 \text{ MeV}$$

$$\Gamma_1 = 205 \pm 18 \pm 86 \text{ MeV}$$

$$M_2 = 4449.8 \pm 1.7 \pm 2.5 \text{ MeV}$$

$$\Gamma_2 = 39 \pm 5 \pm 19 \text{ MeV}$$



Quantum numbers

$$J^P = \left( \frac{3}{2}^-, \frac{5}{2}^+ \right) \text{ or } \left( \frac{3}{2}^+, \frac{5}{2}^- \right) \text{ or } \left( \frac{5}{2}^+, \frac{3}{2}^- \right)$$

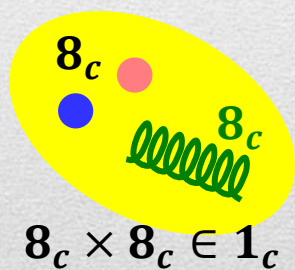
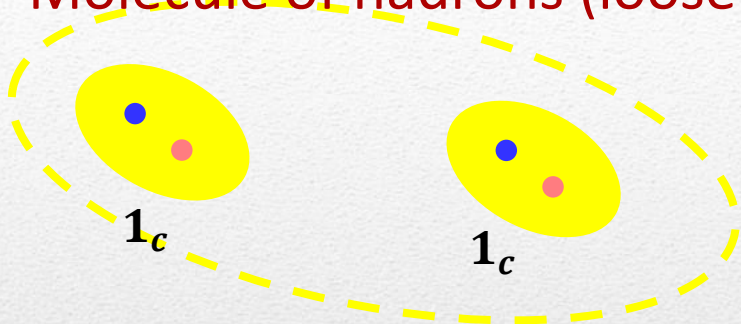
Opposite parities needed for the interference to correctly describe angular distributions

No obvious threshold nearby

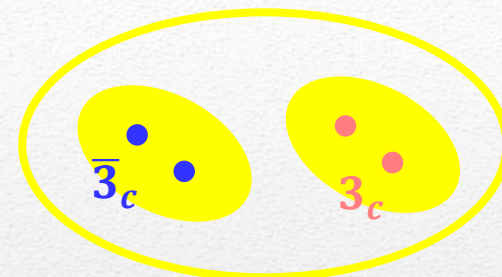


# Proposed models

Molecule of hadrons (loosely bound)



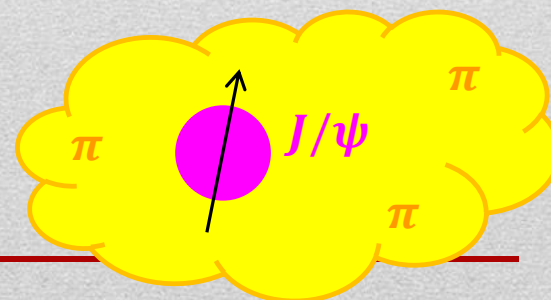
Glueball, Hybrids  
(with valence gluons),  
Born-Oppenheimer 4q



$$3_c \times \bar{3}_c \in 1_c$$

Diquark-antidiquark  
(tetraquark)

Hadrocharmonium  
(Van der Waals forces)



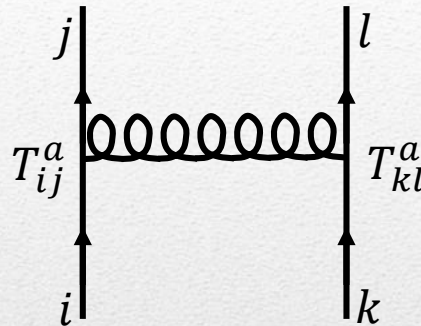
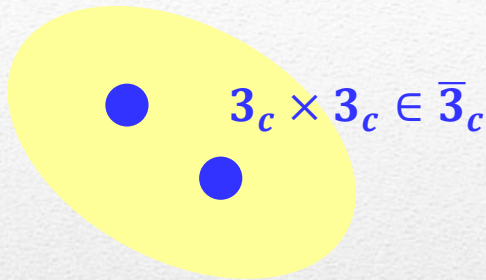
$$1_c \times 1_c \in 1_c$$

Cusp (kinematical effect)



# Diquarks

Attraction and repulsion in 1-gluon exchange approximation is given by



$$R = \frac{1}{2} (C_2(R_{12}) - C_2(R_1) - C_2(R_2))$$

$$R_1 = -\frac{4}{3}, R_8 = +\frac{1}{6}$$

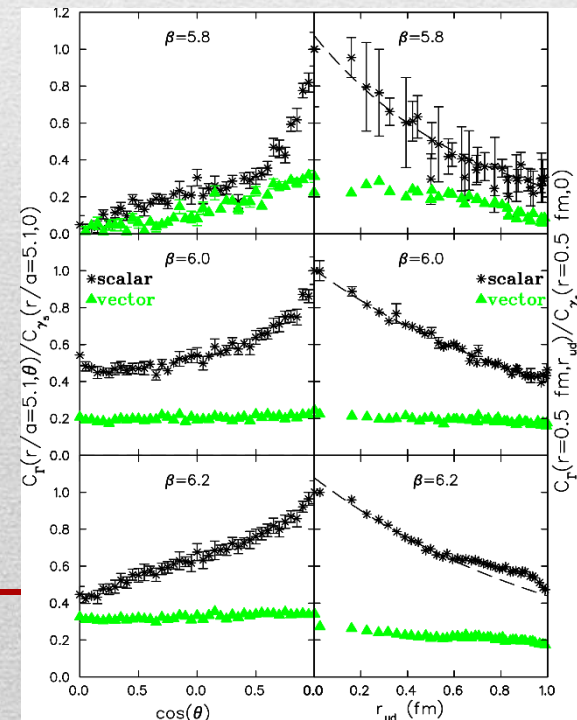
$$R_3 = -\frac{2}{3}, R_6 = +\frac{1}{3}$$

The singlet  $\mathbf{1}_c$  is an attractive combination

A diquark in  $\bar{\mathbf{3}}_c$  is an attractive combination

A diquark is colored, so it can stay into hadrons but cannot be an asymptotic state

Evidence (?) of diquarks in lattice QCD,  
Alexandrou, de Forcrand, Lucini, PRL 97, 222002



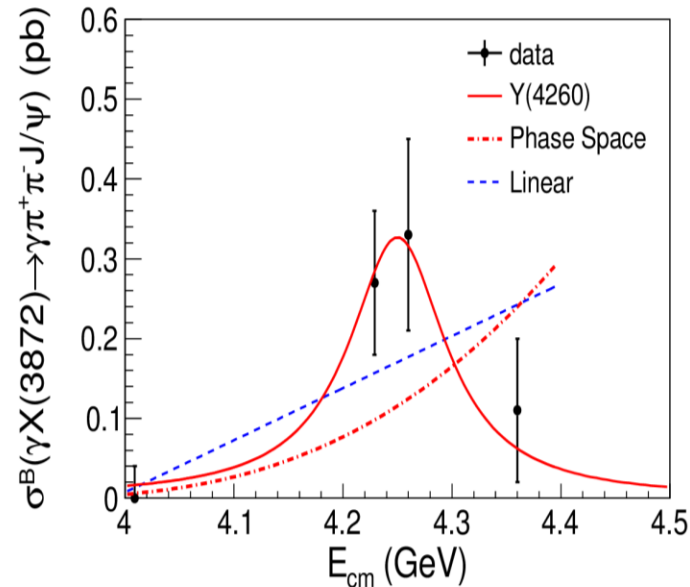
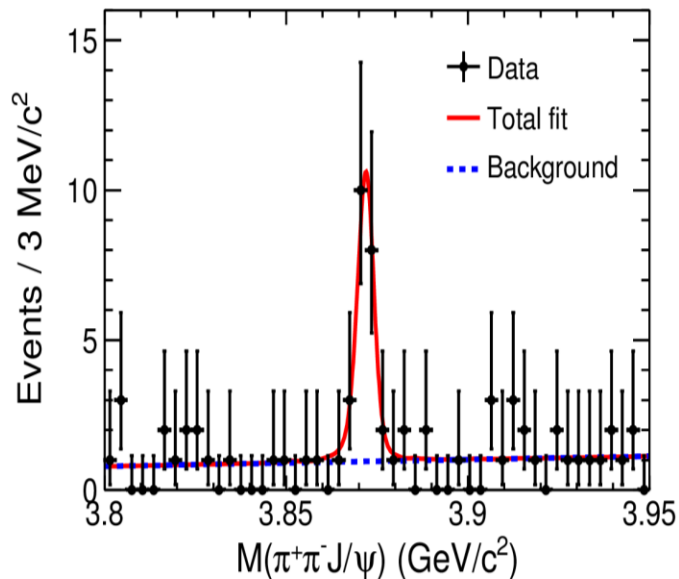


# $Y(4260) \rightarrow \gamma X(3872)$

M. Ablikim et al., Phys. Rev. Lett. 112 (2014) 092001

F. Piccinini

BESIII:  $e^+e^- \rightarrow Y(4260) \rightarrow X(3872)\gamma$



With  $\mathcal{B}[X(3872) \rightarrow \pi^+\pi^-J/\psi] = 5\%$

$$\frac{\mathcal{B}[Y(4260) \rightarrow \gamma X(3872)]}{\mathcal{B}(Y(4260) \rightarrow \pi^+\pi^-J/\psi)} = 0.1$$

Strong indication that  $Y(4260)$  and  $X(3872)$  share a similar structure

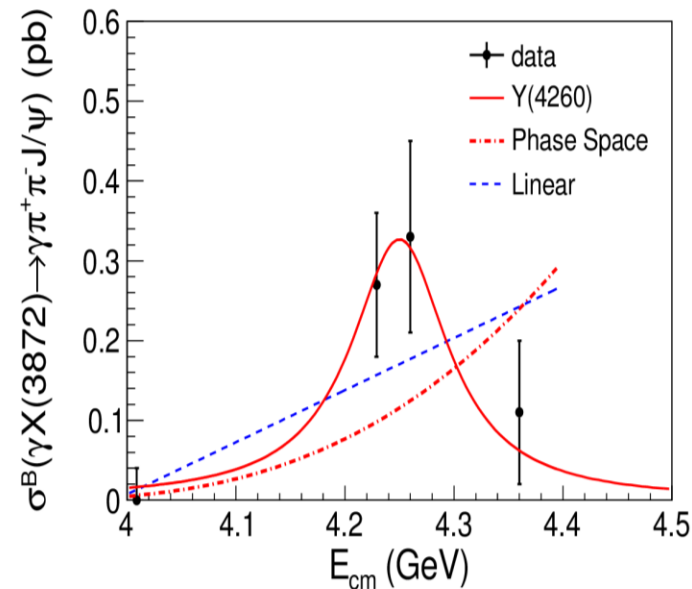
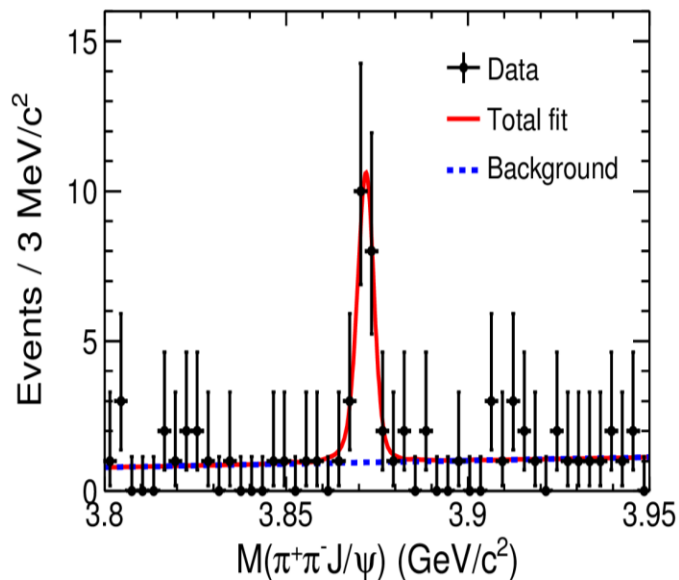
Chen, Maiani, Polosa, Riquer EPJC75 11, 550

# $Y(4260) \rightarrow \gamma X(3872)$

M. Ablikim et al., Phys. Rev. Lett. 112 (2014) 092001

F. Piccinini

BESIII:  $e^+e^- \rightarrow Y(4260) \rightarrow X(3872)\gamma$



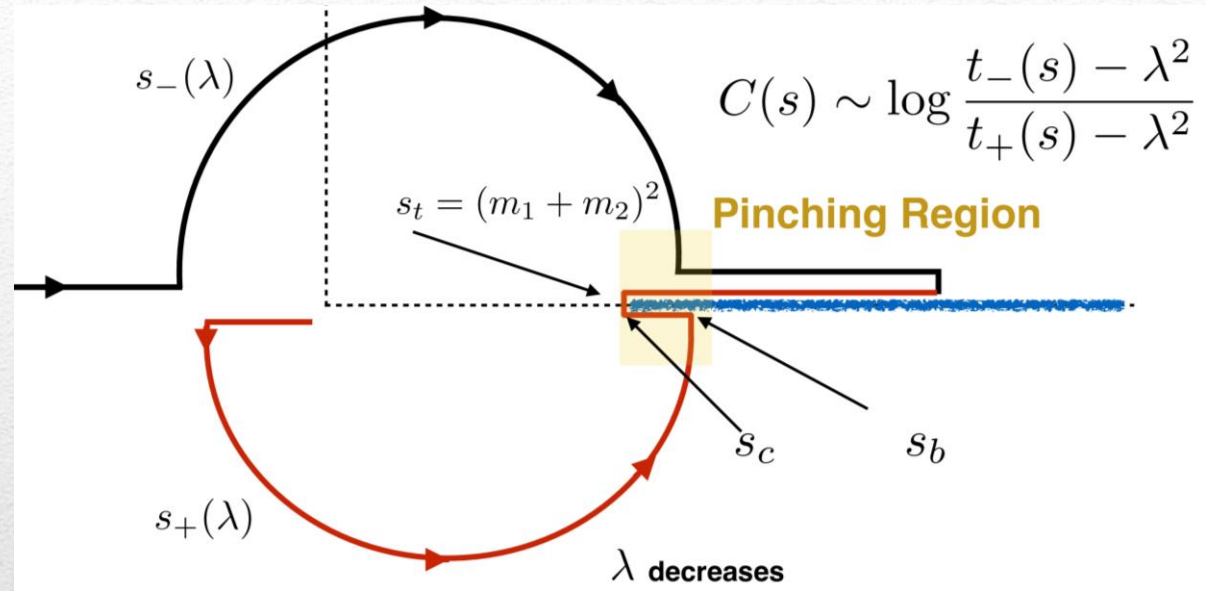
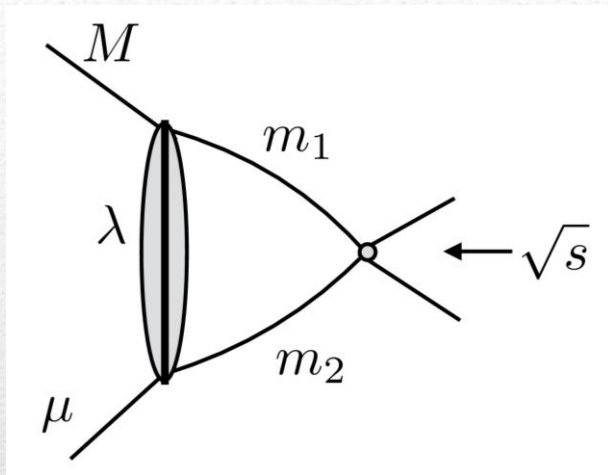
With  $\mathcal{B}[X(3872) \rightarrow \pi^+\pi^-J/\psi] = 5\%$

$$\frac{\mathcal{B}[Y(4260) \rightarrow \gamma X(3872)]}{\mathcal{B}(Y(4260) \rightarrow \pi^+\pi^-J/\psi)} = 0.1$$

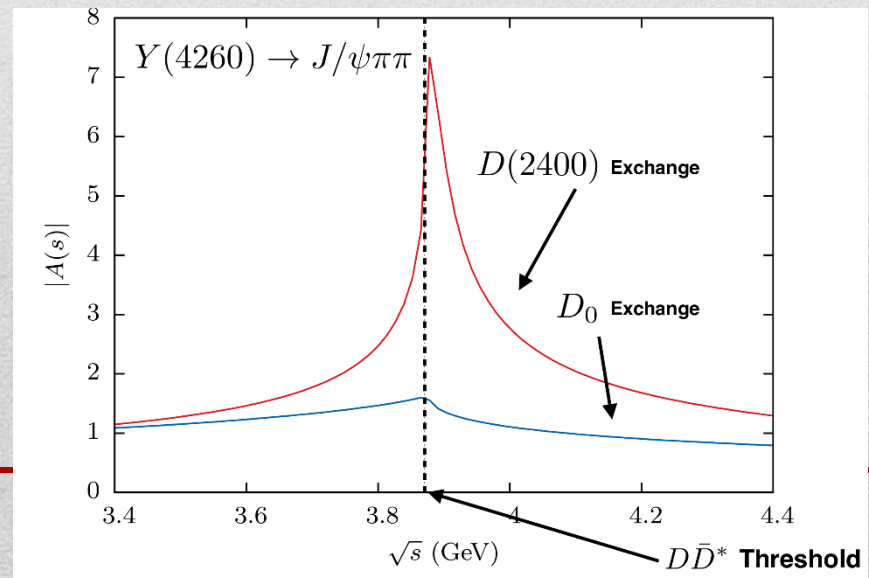
Strong indication that  $Y(4260)$  and  $X(3872)$  share a similar structure



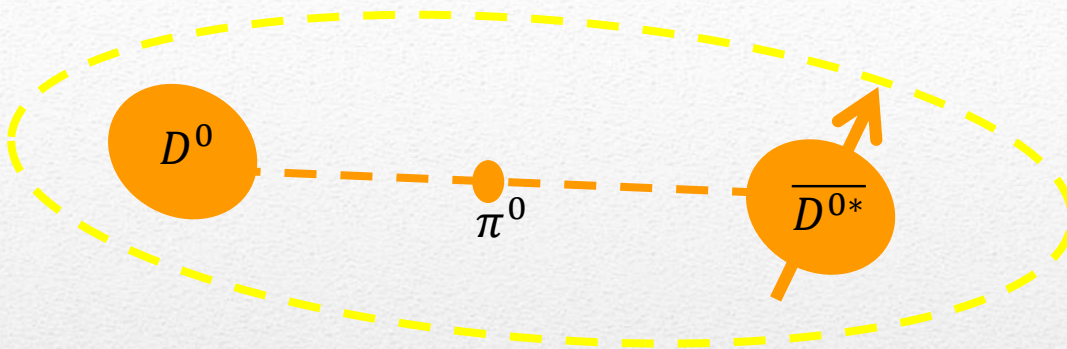
# Triangle singularity (cusps)



Bugg, PLB598, 8-14  
 Szczepaniak, PLB747, 410-416  
 Szczepaniak, 1510.01789



# Molecule



Tornqvist, Z.Phys. C61, 525  
Braaten and Kusunoki, PRD69 074005  
Swanson, Phys.Rept. 429 243-305

$$\begin{aligned} X(3872) &\sim \bar{D}^0 D^{*0} \\ Z_c(3900) &\sim \bar{D}^0 D^{*+} \\ Z'_c(4020) &\sim \bar{D}^{*0} D^{*+} \\ Y(4260) &\sim \bar{D} D_1 \end{aligned}$$

A **deuteron-like meson pair**, the interaction is mediated by the exchange of light mesons

- Some model-independent relations (**Weinberg's theorem**) ✓
- Good description of **decay patterns** (mostly to constituents) and X(3872) **isospin violation** ✓
- States appear **close to thresholds** ✓ (but **Z(4430)** ✗)
- Lifetime of constituents has to be  $\gg 1/m_\pi$ , (but why  $\Gamma_Y \gg \Gamma_{D_{-1}}$ ?)
- Binding energy varies from  $-70$  to  $-0.1$  MeV, or even **positive** (repulsive interaction) ✗
- **Unclear spectrum** (a state for each threshold?) – **depends on potential models** ✗

$$V_\pi(r) = \frac{g_{\pi N}^2}{3} (\vec{\tau}_1 \cdot \vec{\tau}_2) \left\{ [3(\vec{\sigma}_1 \cdot \hat{r})(\vec{\sigma}_2 \cdot \hat{r}) - (\vec{\sigma}_1 \cdot \vec{\sigma}_2)] \left( 1 + \frac{3}{(m_\pi r)^2} + \frac{3}{m_\pi r} \right) + (\vec{\sigma}_1 \cdot \vec{\sigma}_2) \right\} \frac{e^{-m_\pi r}}{r}$$

Needs regularization, cutoff dependence



# Weinberg theorem

Resonant scattering amplitude

$$f(ab \rightarrow c \rightarrow ab) = -\frac{1}{8\pi E_{CM}} g^2 \frac{1}{(p_a + p_b)^2 - m_c^2}$$

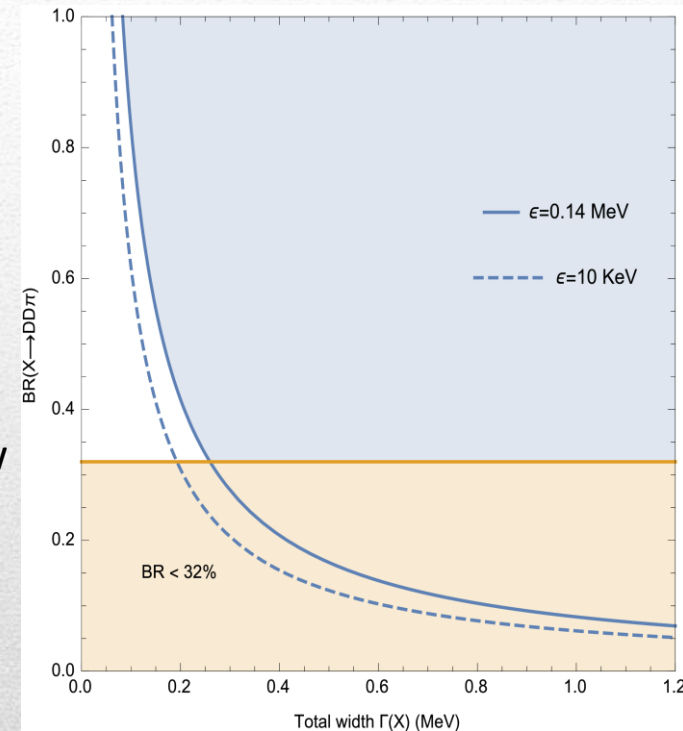
with  $m_c = m_a + m_b - B$ , and  $B, T \ll m_{a,b}$

$$f(ab \rightarrow c \rightarrow ab) = -\frac{1}{16\pi(m_a + m_b)^2} g^2 \frac{1}{B + T}$$

This has to be compared with the potential scattering for slow particles ( $kR \ll 1$ , being  $R \sim 1/m_\pi$  the range of interaction) in an attractive potential  $U$  with a superficial level at  $-B$

$$f(ab \rightarrow ab) = -\frac{1}{\sqrt{2\mu}} \frac{\sqrt{B} - i\sqrt{T}}{B + T}$$

$$B = \frac{g^4}{512\pi^2} \frac{\mu^5}{(m_a m_b)^2}$$



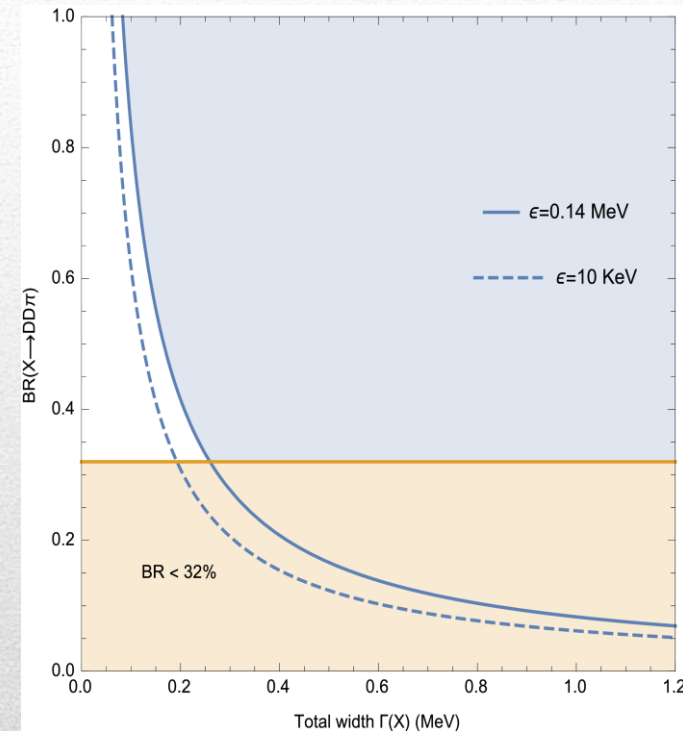
Weinberg, PR 130, 776  
Weinberg, PR 137, B672  
Polosa, PLB 746, 248

# Weinberg theorem

$$B = \frac{g^4}{512\pi^2} \frac{\mu^5}{(m_a m_b)^2}, \quad kR \ll 1$$

This has to be fulfilled by **EVERY molecular state**, but:

- $X(3872)$ ,  $B = 0$ ,  $g \neq 0$
- $Z_s$ ,  $B < 0$ , repulsive interaction!
- $Y(4260)$ ,  $kR \sim 1.4$



Weinberg, PR 130, 776  
Weinberg, PR 137, B672  
Polosa, PLB 746, 248



# Estimating $k_{max}$

The binding energy is  $E_B \approx -0.16 \pm 0.31$  MeV (PDG): **very small!**

In a simple square well model this corresponds to:

$$\sqrt{\langle k^2 \rangle} \approx 50 \text{ MeV}, \sqrt{\langle r^2 \rangle} \approx 10 \text{ fm}$$

$$\left( \begin{array}{l} \text{binding energy reported by NU, PRD91, 011102} \\ E_B \approx -0.003 \pm 0.192 \text{ MeV: } \sqrt{\langle k^2 \rangle} \approx 20 \text{ MeV}, \sqrt{\langle r^2 \rangle} \approx 60 \text{ fm} \end{array} \right)$$

to compare with deuteron:  $E_B = -2.2$  MeV

$$\sqrt{\langle k^2 \rangle} \approx 80 \text{ MeV}, \sqrt{\langle r^2 \rangle} \approx 4 \text{ fm}$$

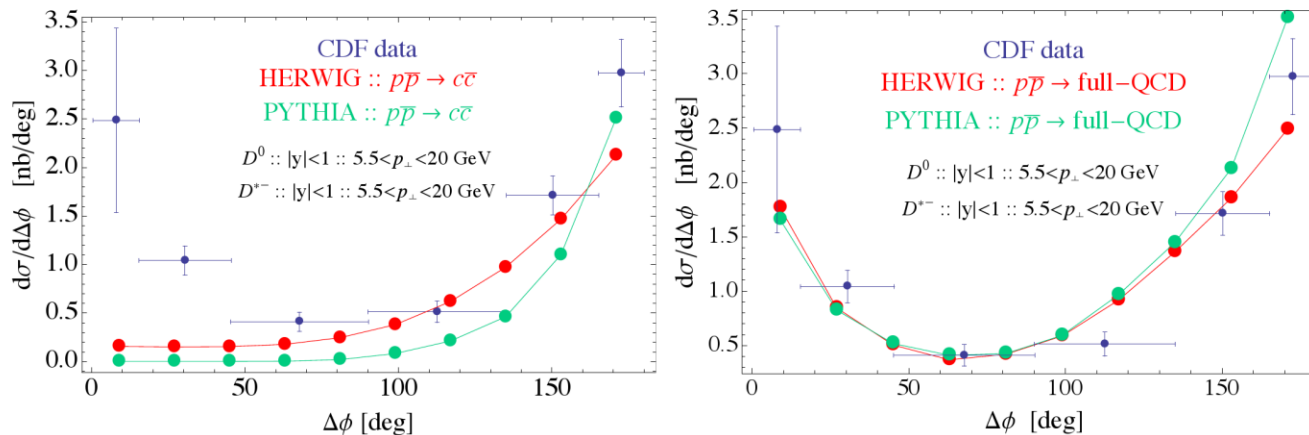
We assume  $k_{max} \sim \sqrt{\langle k^2 \rangle} \approx 50 \text{ MeV}$ , some other choices are commented later

# Tuning of MC

## Monte Carlo simulations

A. Esposito

- We compare the  $D^0 D^{*-}$  pairs produced as a function of relative azimuthal angle with the results from CDF:



*The c-cbar run underestimate the low angles (low- $k_{\theta}$ ) region!*

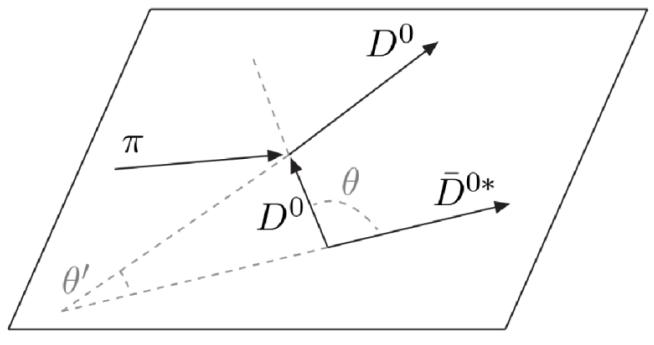
Such distributions of charm mesons are available at Tevatron  
No distribution has been published (yet) at LHC



# A new mechanism?

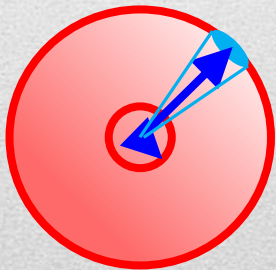
In a more **billiard-like** point of view, the comoving pions can **elastically interact** with  $D(D^*)$ , and **slow down** the  $DD^*$  pairs

Esposito, Piccinini, AP, Polosa, JMP 4, 1569  
Guerrieri, Piccinini, AP, Polosa, PRD90, 034003



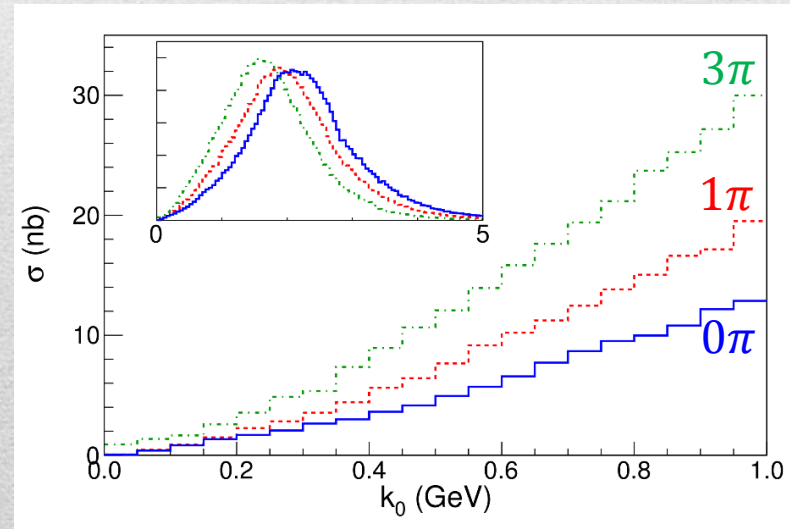
The mechanism also implies:  $D$  mesons actually **“pushed”** **inside** the potential well (the **classical 3-body problem!**)

$X(3872)$  is a **real, negative energy bound state** (stable)  
It also explains a small width  $\Gamma_X \sim \Gamma_{D^*} \sim 100$  keV



By comparing hadronization times of heavy and light mesons, we estimate up to  $\sim 3$  collisions can occur before the heavy pair to fly apart

We get  $\sigma(p\bar{p} \rightarrow X(3872)) \sim 5$  nb, **still not sufficient** to explain all the experimental cross section



# Light nuclei at ALICE

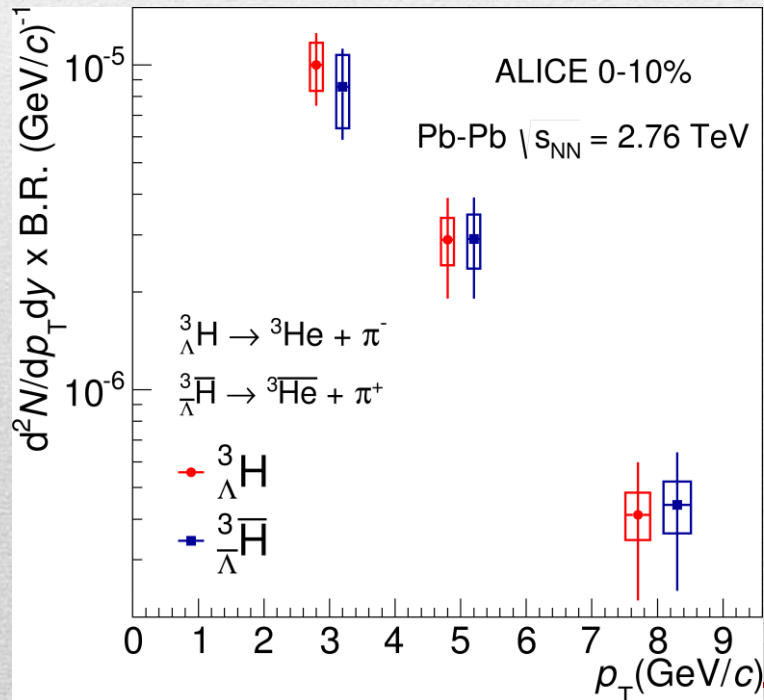
Recently, ALICE published data on production of light nuclei in Pb-Pb and  $pp$  collisions

These might provide a benchmark for  $X(3872)$  production



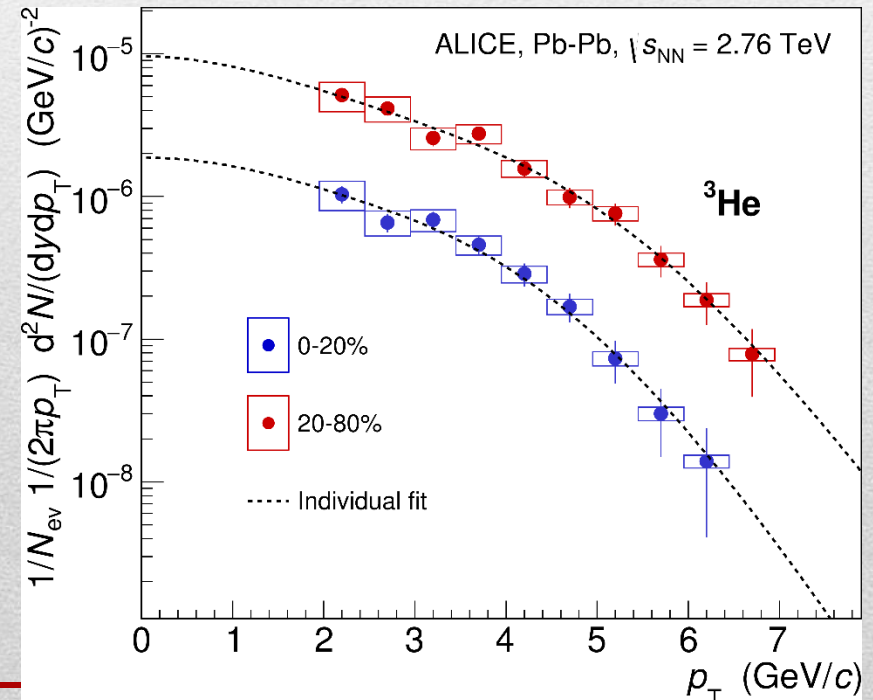
Hypertriton

arXiv:1506.08453



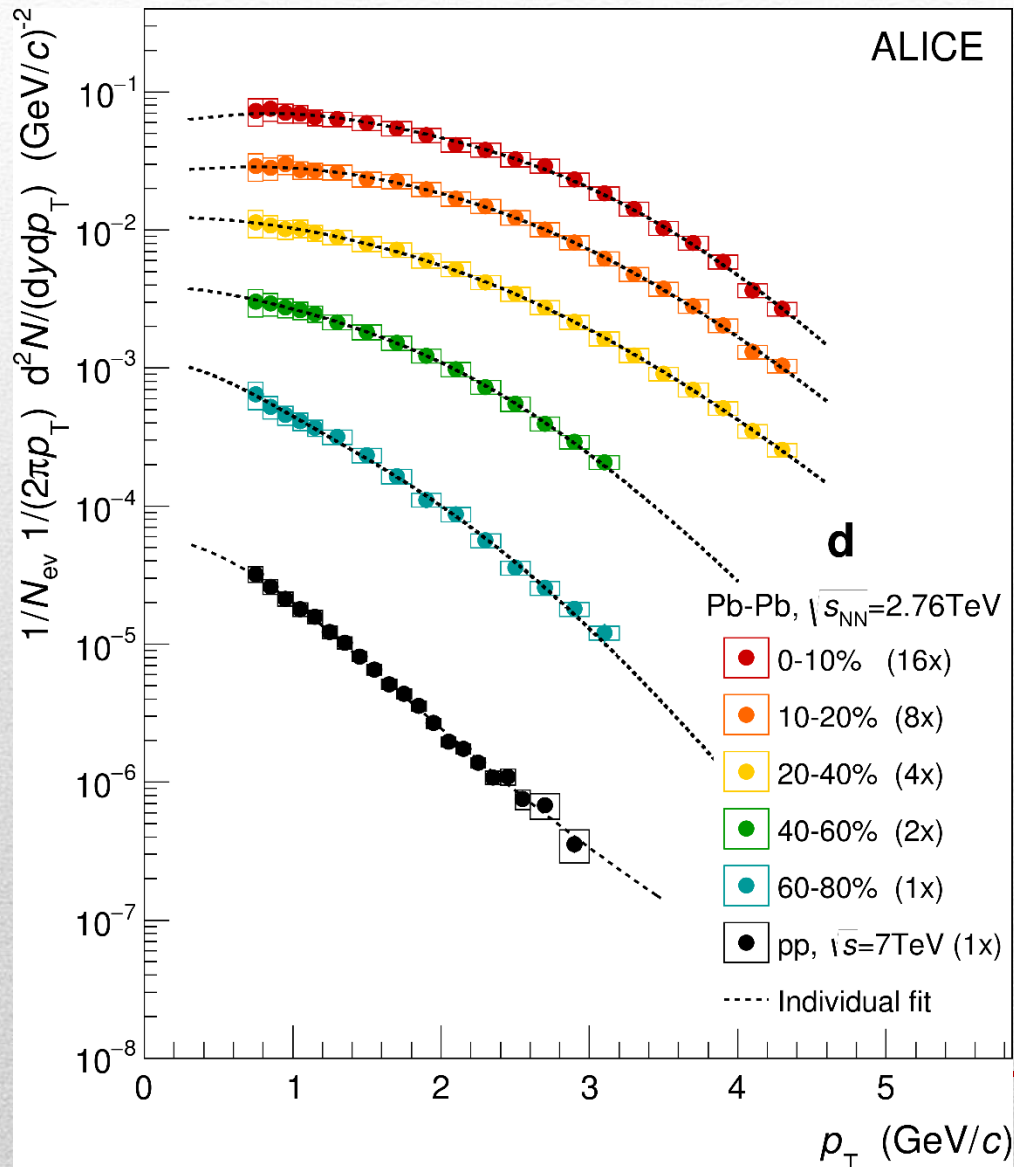
Helium-3

arXiv:1506.08951





# Light nuclei at ALICE



Deuteron

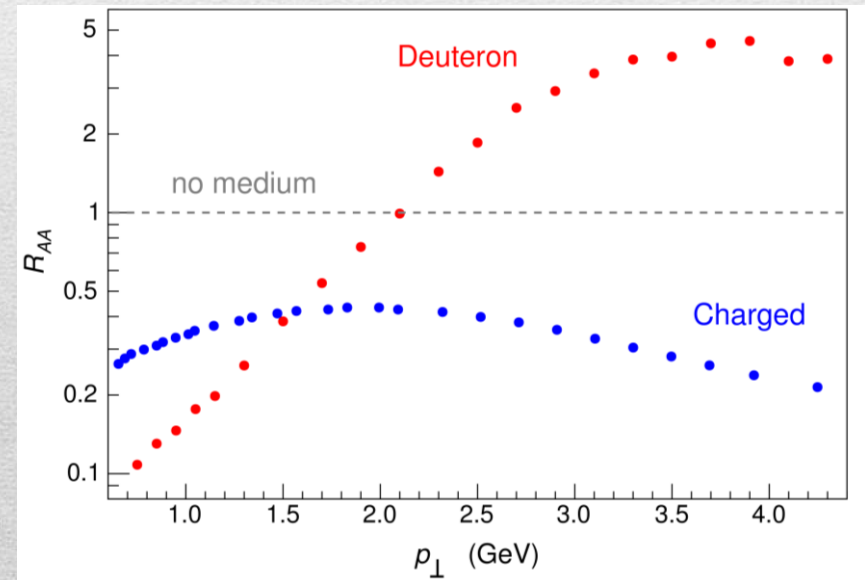
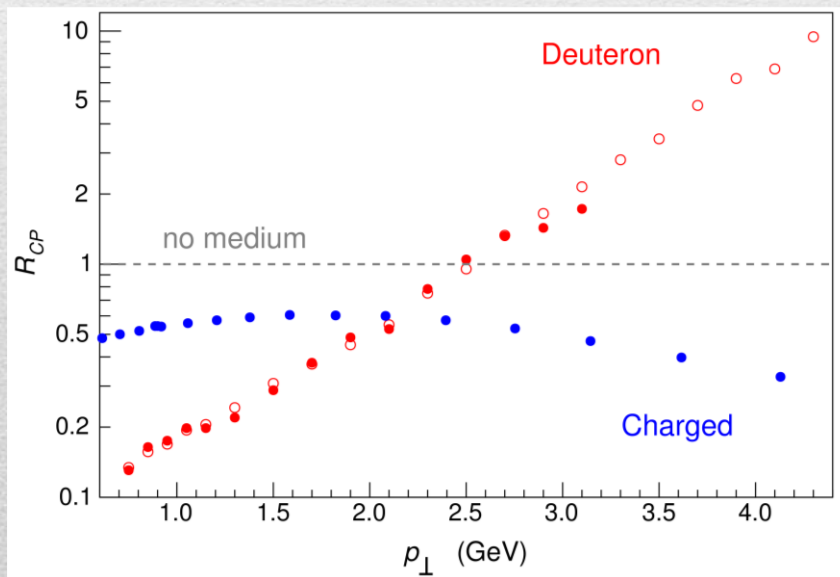
[arXiv:1506.08951](https://arxiv.org/abs/1506.08951)

# Nuclear modification factors

We can use deuteron data to extract the values of the nuclear modification factors  
(caveat: for RAA data have different  $\sqrt{s}$ )

$$R_{CP} = \frac{N_{coll}^P \left( \frac{dN}{dp_T} \right)_C}{N_{coll}^C \left( \frac{dN}{dp_T} \right)_P}$$

$$R_{AA} = \frac{\left( \frac{dN}{dp_T} \right)_{Pb-Pb}}{N_{coll} \left( \frac{dN}{dp_T} \right)_{pp}}$$



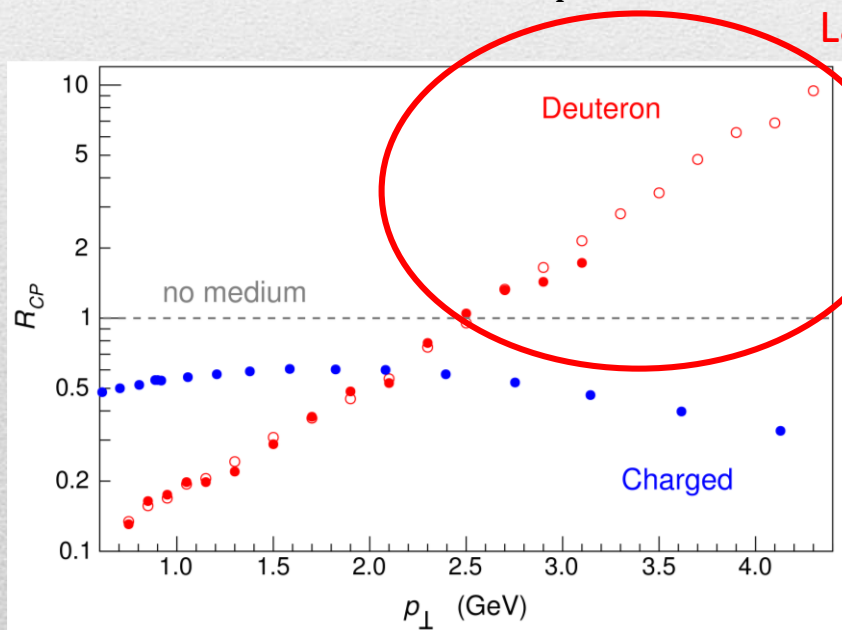


# Nuclear modification factors

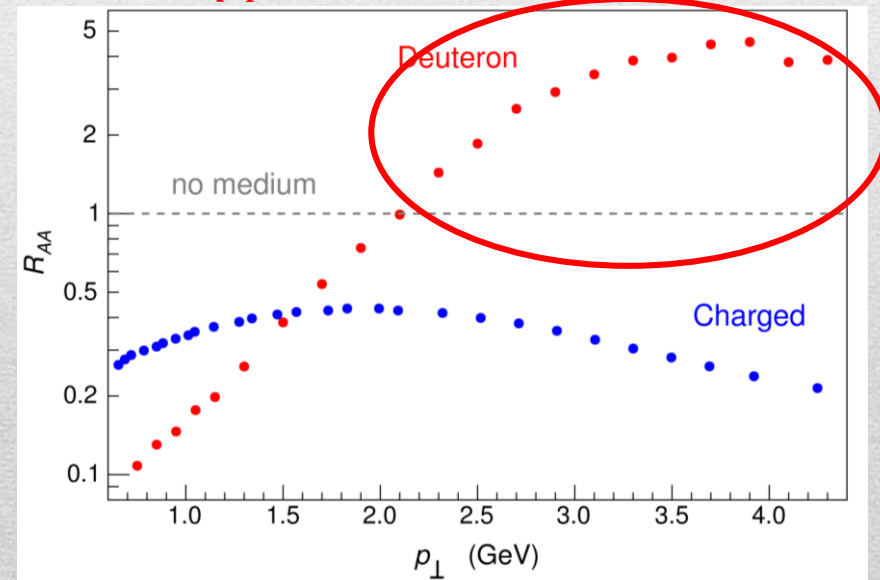
We can use deuteron data to extract the values of the nuclear modification factors  
(caveat: for RAA data have different  $\sqrt{s}$ )

$$R_{CP} = \frac{N_{coll}^P \left( \frac{dN}{dp_T} \right)_C}{N_{coll}^C \left( \frac{dN}{dp_T} \right)_P}$$

$$R_{AA} = \frac{\left( \frac{dN}{dp_T} \right)_{Pb-Pb}}{N_{coll} \left( \frac{dN}{dp_T} \right)_{pp}}$$



Larger than 1 at  $p_T > 2.5$  GeV



# Light nuclei at ALICE

Esposito, Guerrieri, Maiani, Piccinini, AP, Polosa, Riquer, PRD92, 034028

We assume a **pure Glauber** model ( $RAA = 1$ ) and a value  $RAA = 5$  to rescale Pb-Pb data to pp

Constant  $RAA \rightarrow$  same shape in Pb-Pb and pp

$$\left( \frac{d\sigma(^3\Lambda\text{H})}{dp_\perp} \right)_{pp} = \frac{\Delta y}{\mathcal{B}(^3\text{He}\pi)} \times \frac{\sigma_{pp}^{\text{inel}}}{N_{\text{coll}}} \left( \frac{1}{N_{\text{evt}}} \frac{d^2 N(^3\text{He}\pi)}{dp_\perp dy} \right)_{\text{Pb-Pb}}$$

We **extrapolate** this data at higher  $p_T$  either by assuming an **exponential law**, or with a **blast-wave** function, which describes the emission of particles in an expanding medium

The blast-wave function is

$$\frac{dN}{dp_\perp} \propto p_\perp \int_0^R r dr m_\perp I_0 \left( \frac{p_\perp \sinh \rho}{T_{\text{kin}}} \right) K_1 \left( \frac{m_\perp \cosh \rho}{T_{\text{kin}}} \right),$$

where  $m_\perp$  is the transverse mass,  $R$  is the radius of the fireball,  $I_0$  and  $K_1$  are the Bessel functions,  $\rho = \tanh^{-1} \left( \frac{(n+2)\langle\beta\rangle}{2} (r/R)^n \right)$ , and  $\langle\beta\rangle$  the averaged speed of the particles in the medium.



# Light nuclei at ALICE vs. $X(3872)$

Esposito, Guerrieri, Maiani, Piccinini, AP, Polosa, Riquer, PRD92, 034028

We assume a pure Glauber model ( $R_{AA} = 1$ ) and a value  $R_{AA} = 5$  to rescale Pb-Pb data to pp

The  $X(3872)$  is way larger than the extrapolated cross section

