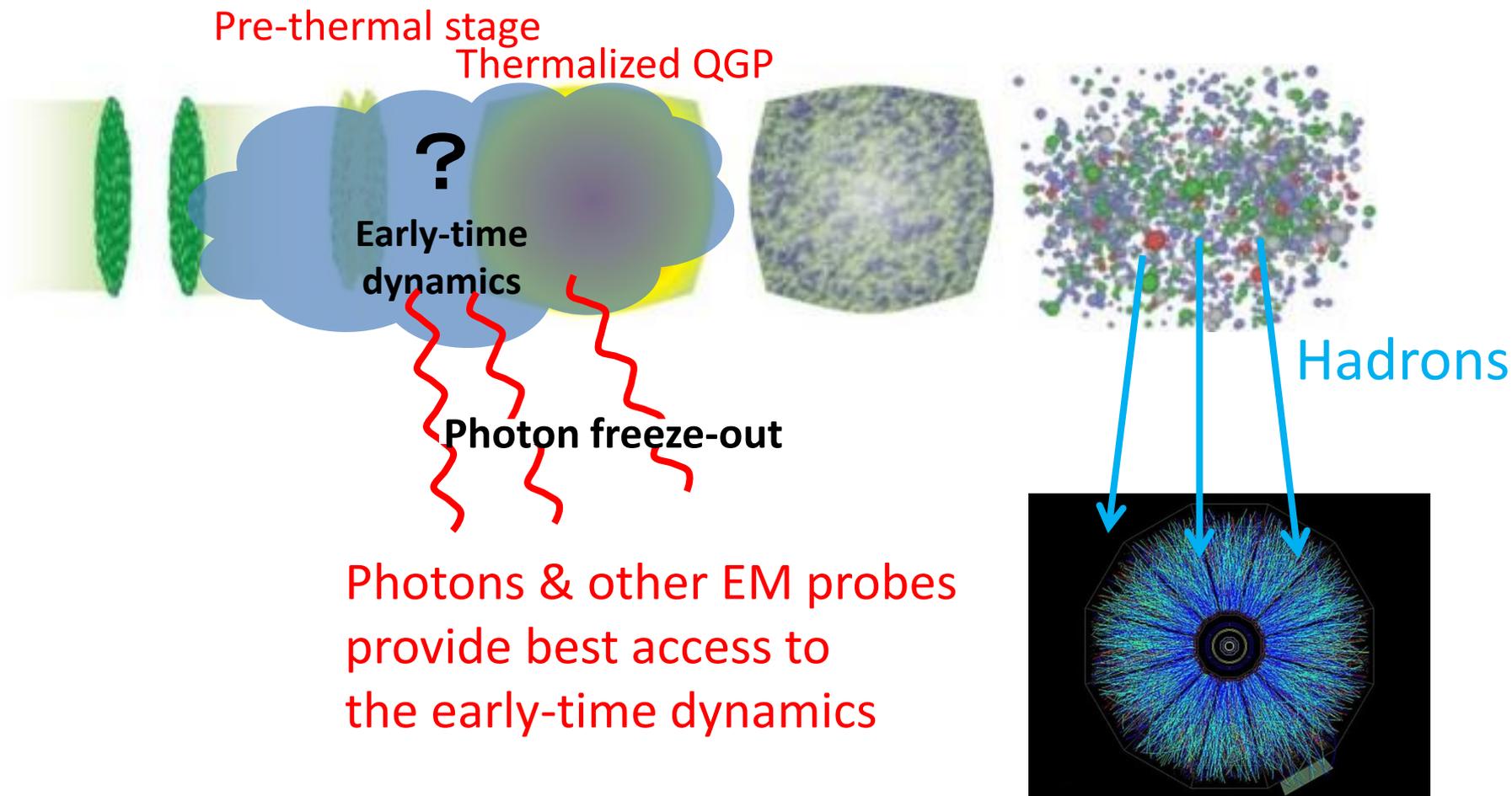


Jet fragmentation photons in ultrarelativistic heavy-ion collisions

Koichi Hattori, Larry McLerran, Bjoern Schenke

Quark Matter 2015@Kobe, Sep. 18 - Oct. 3, 2015

EM probes as messengers of early-time dynamics



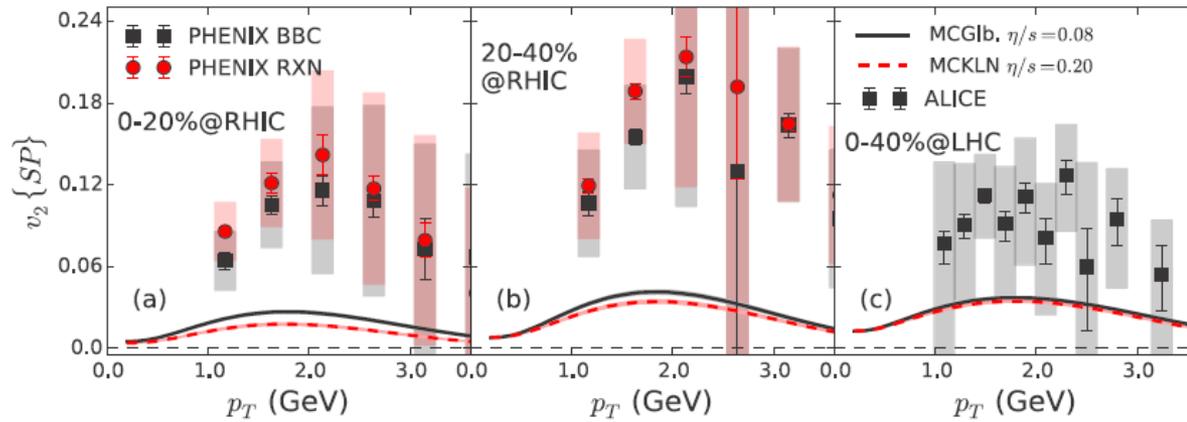
Shuryak (1978), McLerran & Toimela (1985), etc

Photon yield, v_2 , and v_3 measured in RHIC and LHC!!

See next talks.

Recent theoretical progresses

Still small v_2 in 2015 (Shen, et al., 2015.)



- + Bulk viscosity, etc. (J.-F. Paquet, et al. See his talk.)
- + NLO HTL photon rate (Ghiglieri, et al.)
- + Nonperturbative background in semi-QGP (BNL)
- + B-field (Basar, et al., Tuchin, HK, Itakura, etc.)
- +

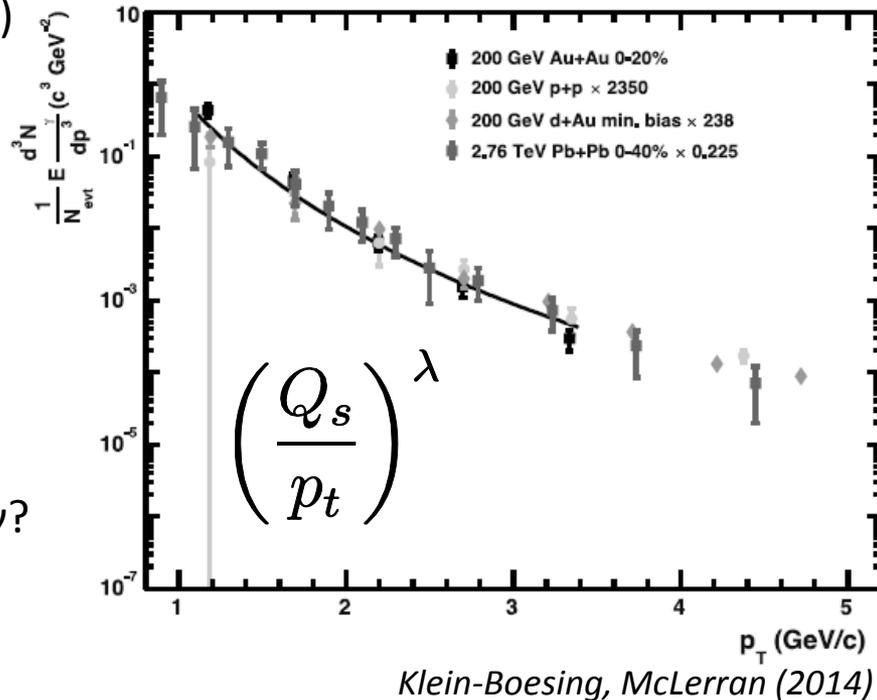
Geometrical scaling of photons in pp, dA, AA @ RHIC & LHC

Suggests an early-time emission?

→ How is the information of Q_s transferred to γ ?

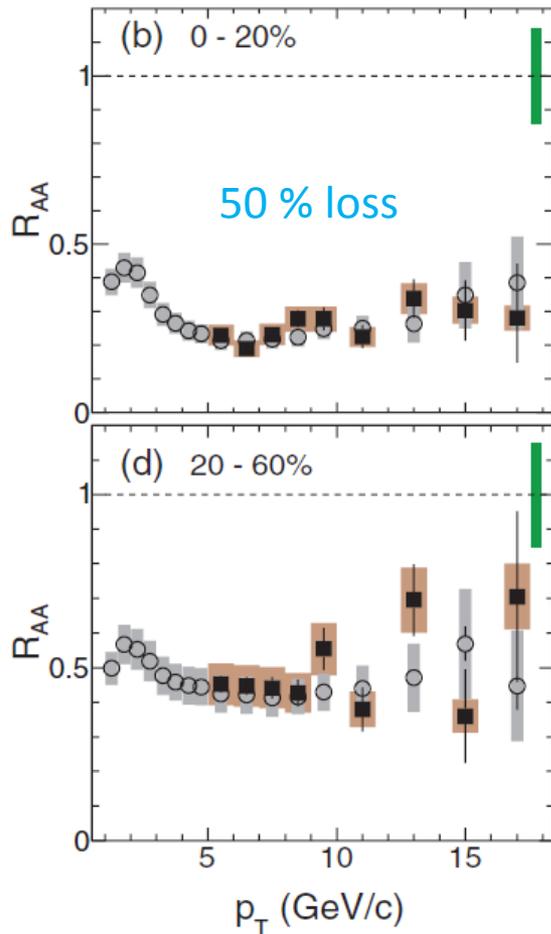
→ Is the large v_2 again puzzling?

- + Glasma? (McLerran, Schenke; Tanji)
- + Jet fragmentation? → This talk

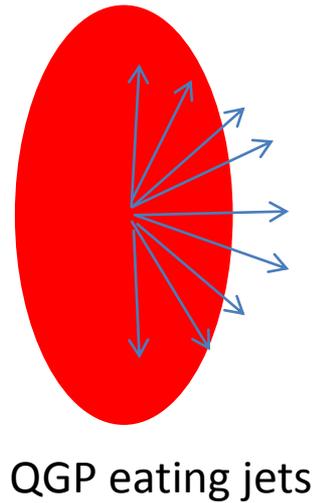
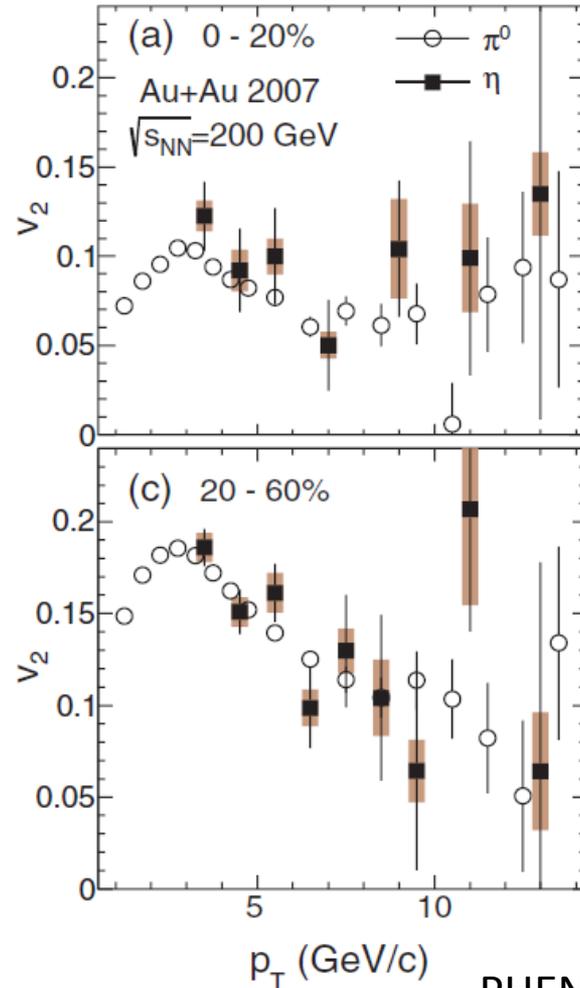


v_2 of jets generated by energy loss \rightarrow Can be transferred to photon v_2 ?

R_{AA} of high- p_T π^0



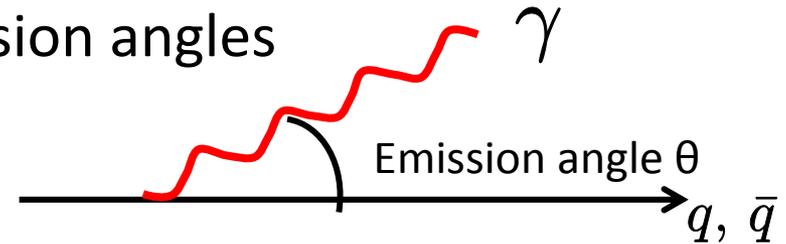
v_2 of π^0 and η at high p_T
 -- Almost species independent



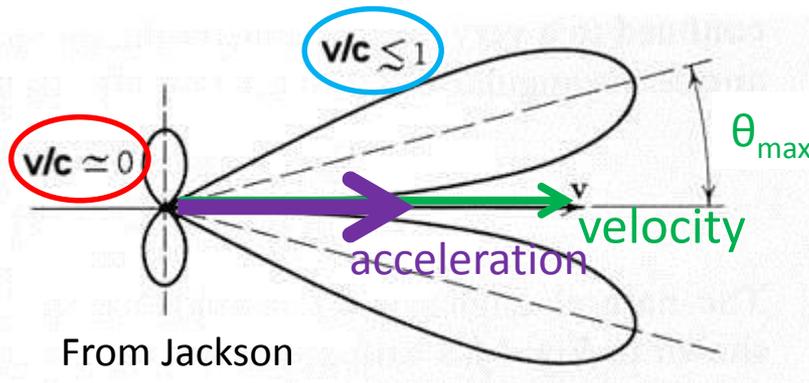
Estimates by classical electrodynamics

Provides a good approximation when kinematics is properly treated.

Velocity-dependence of emission angles



Bremsstrahlung from relativistic and nonrelativistic particles



- + Relativistic particles
Forward-dominant emission
→ Collimation btw the jet & photon momenta.
- + Non-relativistic particles
Isotropic emission from
→ Uncollimated emission

Radiation in the linear acceleration

$$\theta \rightarrow \frac{1}{2\gamma} \text{ as } v \rightarrow 1$$

c.f. “Dead-cone effect” in the heavy-quark jet energy loss, Dokshitzer, Kharzeev (2001)

Bremsstrahlung from a quark (antiquark) jet

Photon emission rate from quark current

$$2\epsilon_{\mathbf{p}} \frac{dn_{\gamma}}{d^3\mathbf{p}} = -\frac{1}{(2\pi)^3} \tilde{j}^{\mu}(p) \tilde{j}_{\mu}^*(p) \Big|_{p^0=|\mathbf{p}|}$$

Quark (antiquark) current

$$j^{\mu}(x) = e \{ v_{\text{ini}}^{\mu} \delta^{(3)}(\mathbf{x} - \mathbf{v}_{\text{ini}} t) \theta(-t) + v_{\text{fin}}^{\mu} \delta^{(3)}(\mathbf{x} - \mathbf{v}_{\text{fin}} t) \theta(t) \}$$

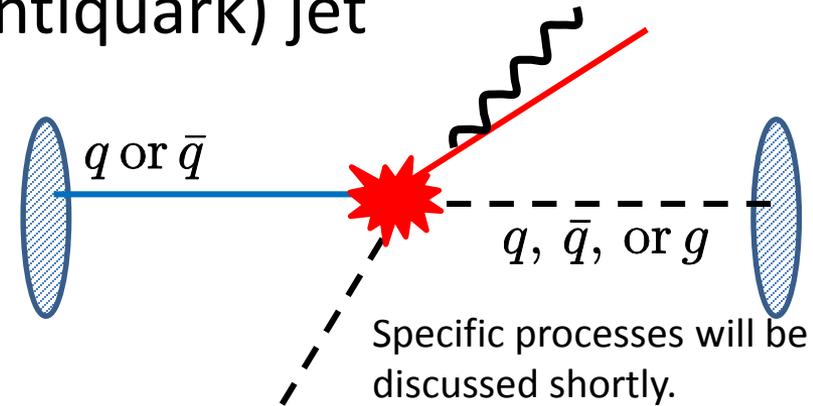
Classical trajectory after the scattering

Before the scattering $\mathbf{v}_{\text{ini}} = (0, 0, 1)$

After the scattering $\epsilon_{\text{jet}}^2 - \mathbf{k}_{\text{jet}}^2 = Q_{\text{jet}}^2$

$$v_{\perp} = \frac{k_t}{\epsilon_{\text{jet}}} = \frac{k_t}{\sqrt{k_t^2 + Q_{\text{jet}}^2} \cosh Y_{\text{jet}}} = \frac{\kappa}{\cosh Y_{\text{jet}}} \quad v_z = \tanh Y_{\text{jet}}$$

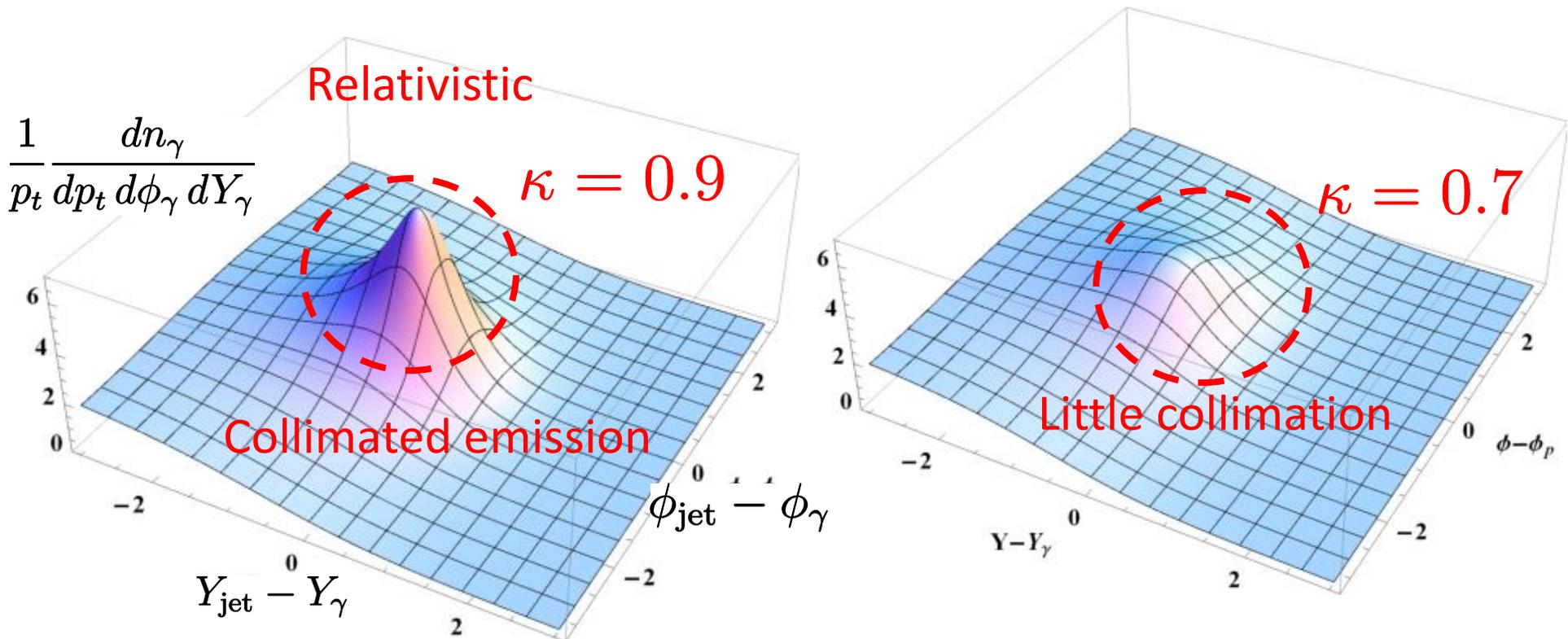
$$\begin{aligned} \kappa &\rightarrow 1 \quad \text{Relativistic limit} && (k_t \gg Q_{\text{jet}}) \\ &\rightarrow 0 \quad \text{Non-relativistic limit} && (k_t \ll Q_{\text{jet}}) \end{aligned}$$



Degree of the collimation in the bremsstrahlung

Photon emission rate

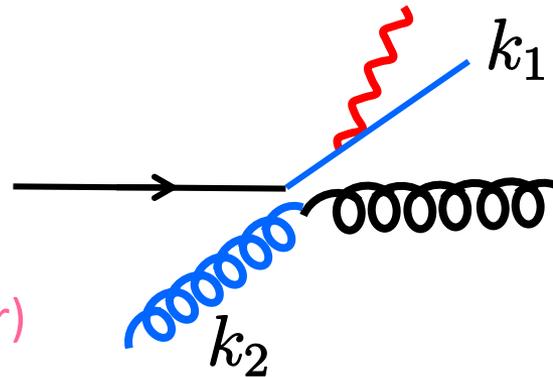
$$2\epsilon_p \frac{dn_\gamma}{d^3\mathbf{p}} = \frac{\alpha_{\text{em}}}{p_\perp^2} \frac{(\dots)}{\{ \cosh(Y_{\text{jet}} - Y_\gamma) - \kappa \cos(\phi_{\text{jet}} - \phi_\gamma) \}^2} \rightarrow \frac{1}{1 - \kappa} \text{ when } \begin{matrix} Y_{\text{jet}} = Y_\gamma \\ \phi_{\text{jet}} = \phi_\gamma \end{matrix}$$



Convolution of jet distribution and photon emission rate

$$\epsilon_{\mathbf{p}} \frac{dN_{\gamma}}{d^3\mathbf{p}} = \mathcal{N}_{\text{jet}} \int d^4k_1 \int d^4k_2 \frac{dn_{\text{jet}}}{d^4k_1 d^4k_2} \cdot \epsilon_{\mathbf{p}} \frac{dn_{\gamma}}{d^3\mathbf{p}_{\gamma}}$$

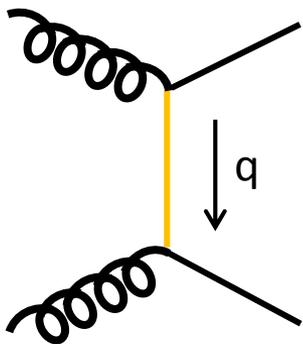
Overall normalization includes contributions of u, d, s , and their anti-quarks; left- and right-moving q ($q\bar{q}$)
 -- Fitted to the LO pQCD calculation from J. Fries, et al., (2003)



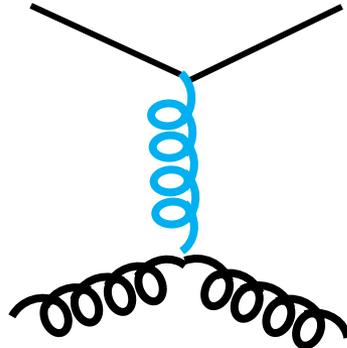
What is the dominant quark-jet production process?

→ Gluon Compton scattering

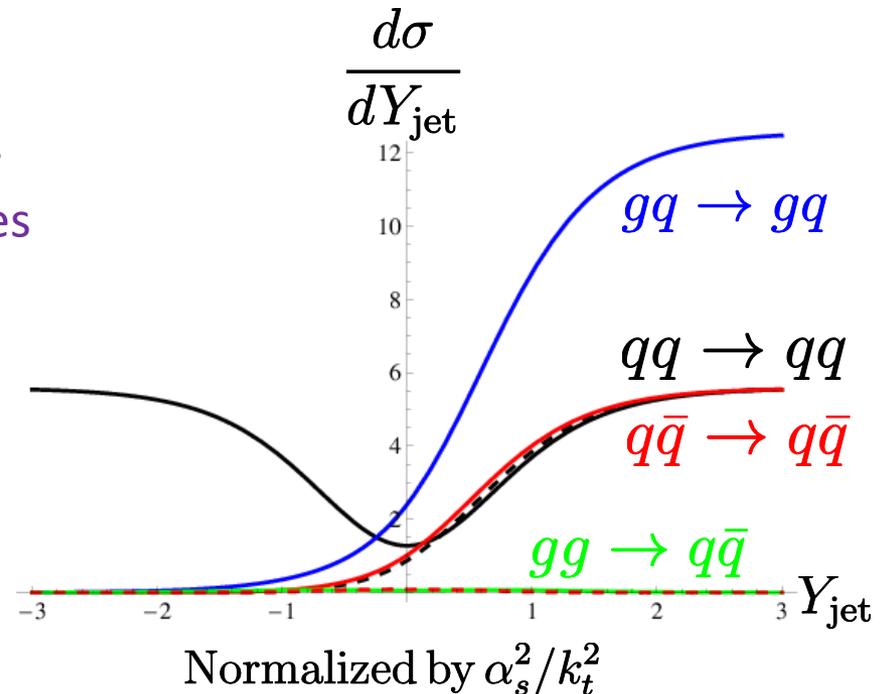
1. Gluon-dominant PDF
 → Take processes involving at least one gluon.
2. Dominant diagrams from gluon exchanges



Enhanced by $1/q$



✓ Enhanced by $1/q^2$



Transverse jet momentum distribution

Assuming the boost invariance,

$$\epsilon_{\mathbf{p}} \frac{dN_{\gamma}}{d^3\mathbf{p}} = \mathcal{N}_{\text{jet}} \int dY_{\text{com}} dY \int d\phi_{\text{jet}} \int_{k_{\text{min}}}^{k_{\text{max}}} dk_t k_t \frac{dn_{\text{jet}}}{k_t dk_t d\phi_{\text{jet}} dY} \cdot \epsilon_{\mathbf{p}} \frac{dn_{\gamma}}{d^3\mathbf{p}}$$

$$Y_{\text{com}} = Y_1 + Y_2$$

$$Y = (Y_1 - Y_2)/2$$

$$\frac{dn_{\text{jet}}}{k_t dk_t d\phi_{\text{jet}} dY} = \frac{\alpha_s^2}{k_t^2} \frac{d\sigma_{gq}}{dY} \left(\frac{1}{1 + k_t/Q_{\text{sat}}} \right)^{\beta} \left(1 + 2v_{\text{jet}}^{(2)} \cos 2\phi_{\text{jet}} + \dots \right)$$

+ Phenomenological parameters

ϕ_{jet} is measured from the reaction plane.

$$\beta \sim 6, v_{\text{jet}}^{(2)} \sim v_2 \text{ of high-}p_t \pi^0$$

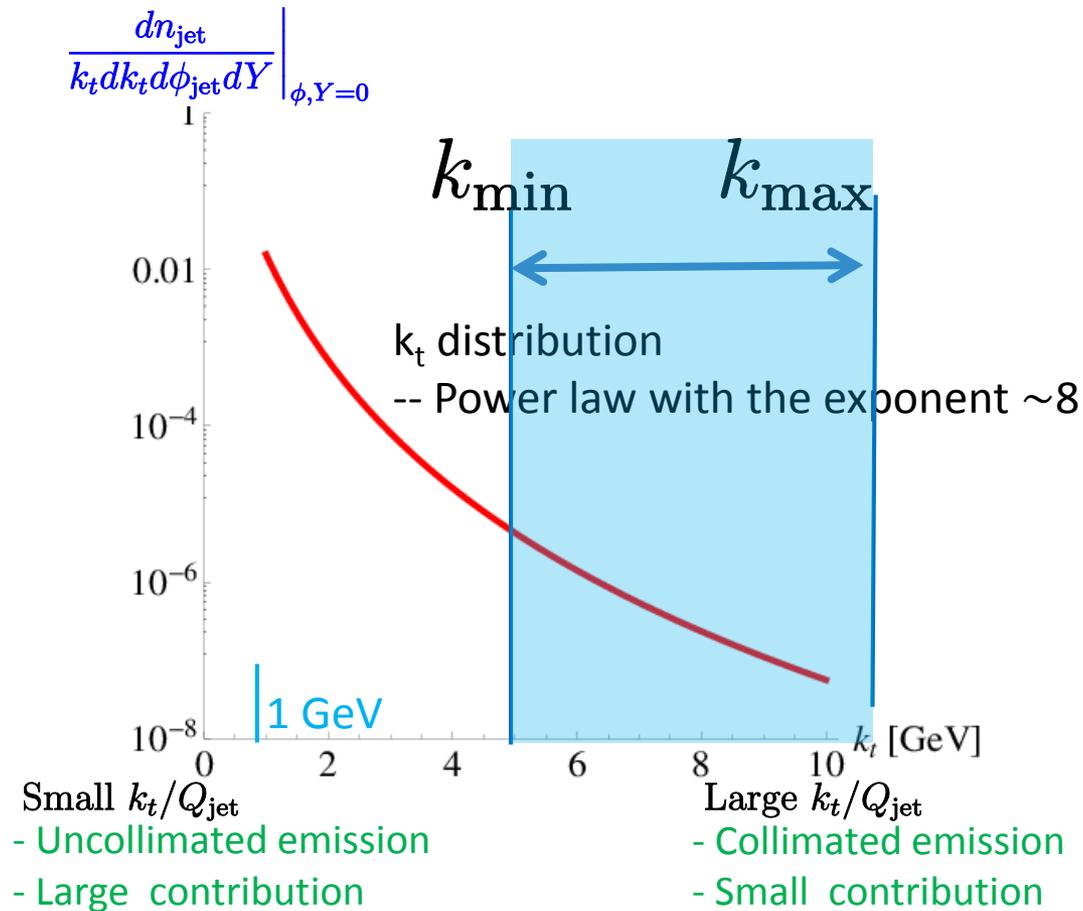
Cutoffs of the transverse jet momentum

Maximum jet momentum should be smaller than the beam energy: $S_{gq} < S_{NN}$

Minimum jet momentum should be larger than the photon momentum: $\epsilon_{\text{jet}} > \epsilon_{\mathbf{p}_{\gamma}}$

If this condition allows for less 1 GeV, the momentum is cutoff sharply at 1 GeV.

Expectations for photon yield and v2

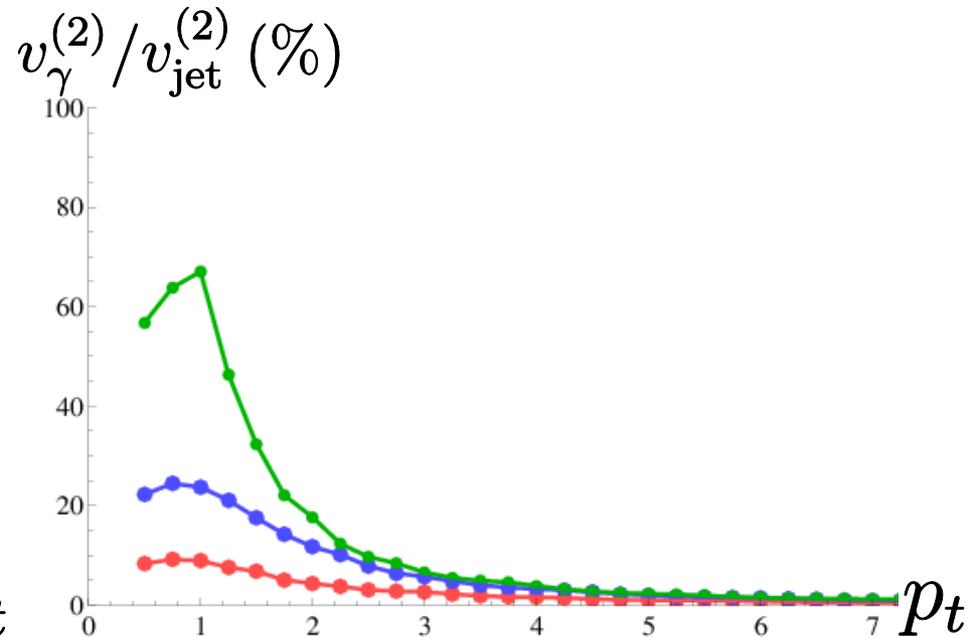
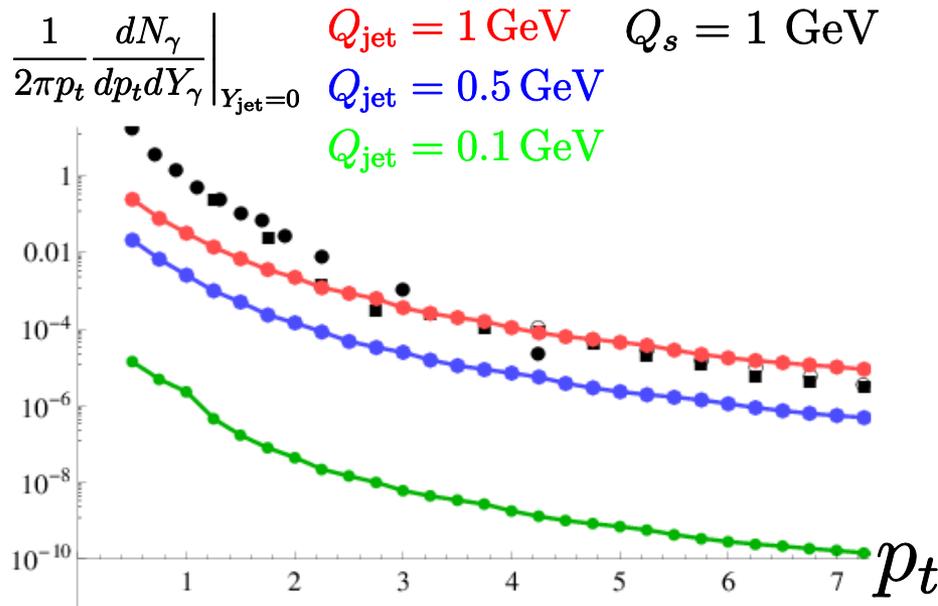


Results: RHIC energy

$$\epsilon_p \frac{dN_\gamma}{d^3\mathbf{p}} = \frac{1}{2\pi p_t} \frac{dN_\gamma}{dp_t dY_\gamma} \left(1 + 2v_\gamma^{(2)} \cos 2\phi_p + \dots \right)$$

Photon yield
from the jet fragmentation

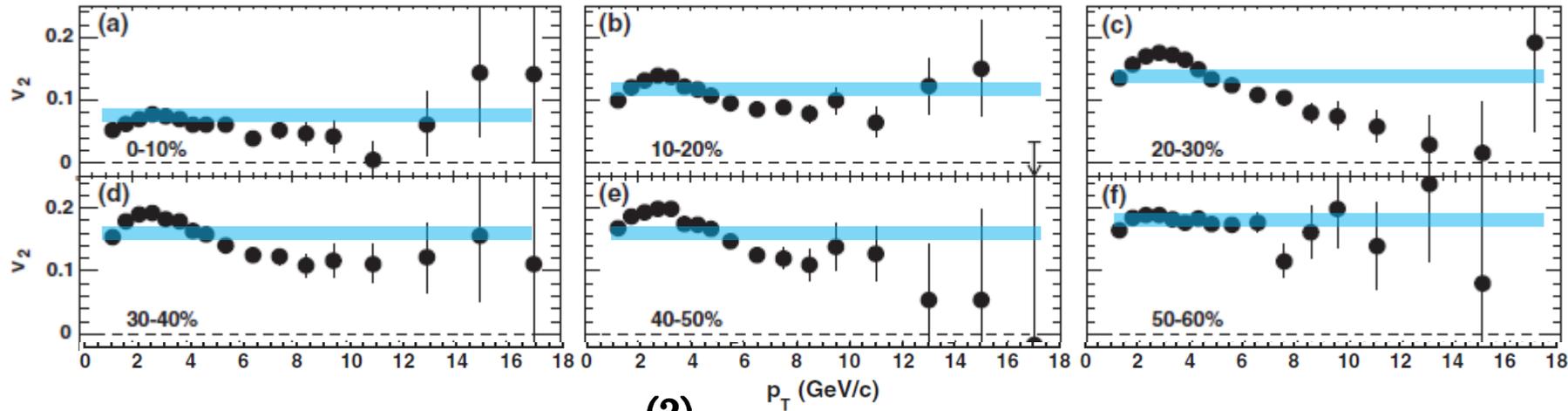
Ratio of the anisotropies: $v_\gamma^{(2)} / v_{\text{jet}}^{(2)}$ (%)
-- Momentum anisotropy transferred
from jets to photons.



Converting the jet v_2 to the photon v_2

High p_t pion v_2

PHENIX, 2010, 2013



P_t averaged jet v_2

0-10%: 0.066

10-20%: 0.097

20-30%: 0.12

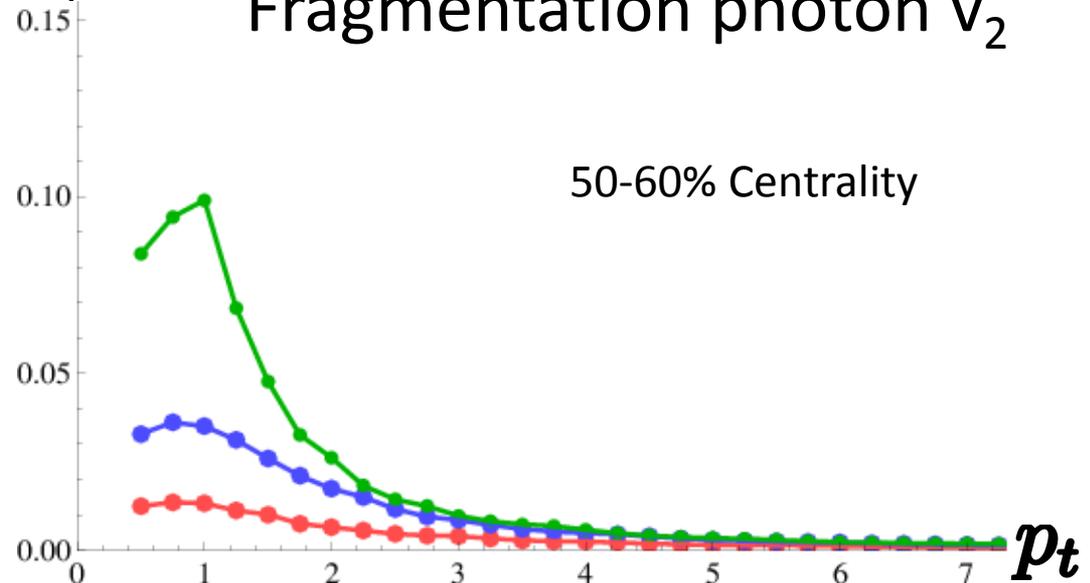
30-40%: 0.148

40-50%: 0.136

50-60%: 0.173

$v_\gamma^{(2)}$

Fragmentation photon v_2



Summary

We investigated the jet fragmentation photons by the simplest and clearest setup, which captures the importance of kinematics and jet mass.

Conclusion for the first estimate:

Large $v_2 \Leftrightarrow$ Small yield

Small $v_2 \Leftrightarrow$ Large yield

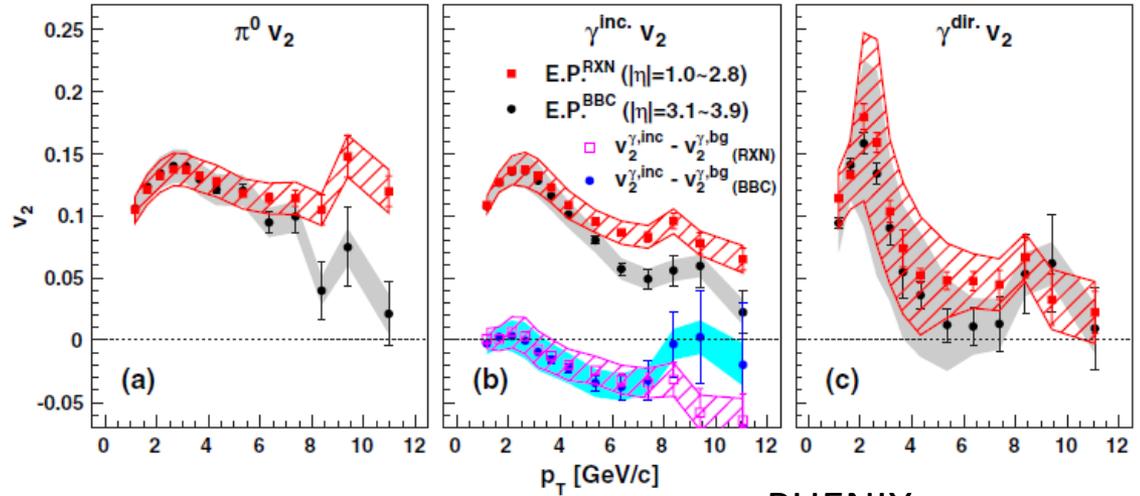
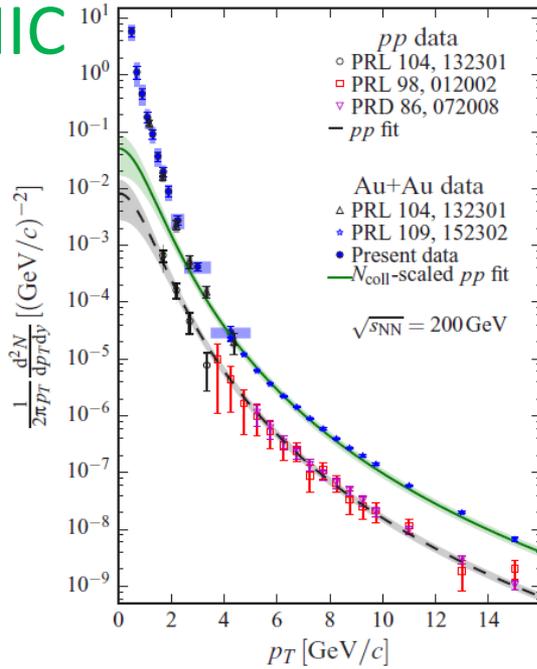
What about the medium-induced photon radiation?

c.f., Turbide, et al.

Need to pursue mechanisms of the geometrical scaling of photons.

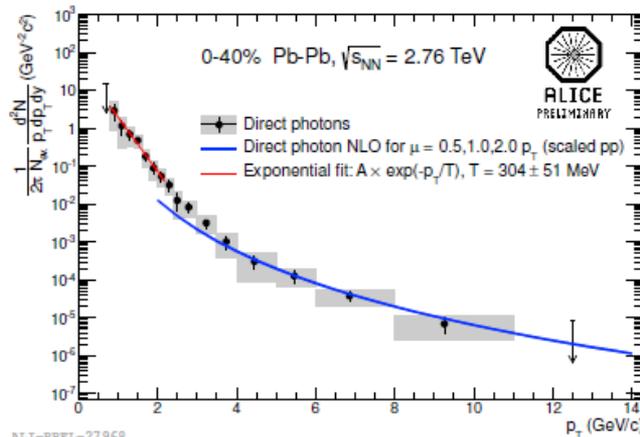
Recent photon measurements See next talks.

RHIC

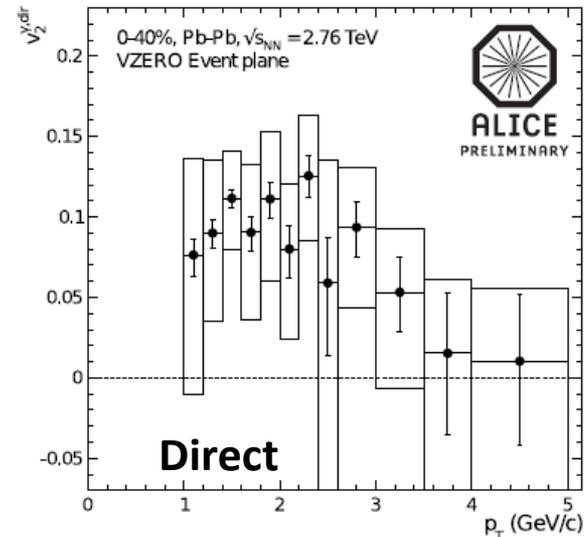


PHENIX

LHC



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ALICE

How precisely do we know photon sources?

$$N_{\text{dir}} = N_{\text{prompt}} + N_{\text{jet}} + N_{\text{QGP}} + N_{\text{Had}} + \dots$$

Hard

Semi-hard

Soft

High T

Low T

1D expansion \rightarrow 3D expansion
(Transverse-flow development)

$$v_{\text{dir}}^{(2)} = N_{\text{prompt}} v_{\text{prompt}}^{(2)} + N_{\text{jet}} v_{\text{jet}}^{(2)} + N_{\text{QGP}} v_{\text{QGP}}^{(2)} + N_{\text{Had}} v_{\text{Had}}^{(2)} + \dots$$

Small

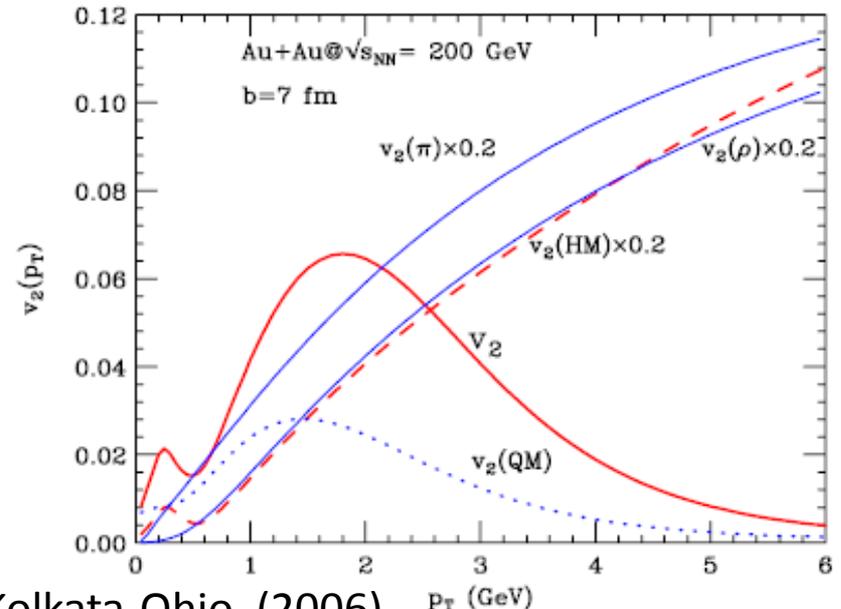
???

Small

Large

Ellipsis includes other sources such as Glasma, strong B-fields, etc.

Early theoretical observations:
+ Small v_2 in QGP phase
+ Large v_2 in hadron phase
 \rightarrow On average, small v_2 of direct photons



Kolkata-Ohio, (2006)

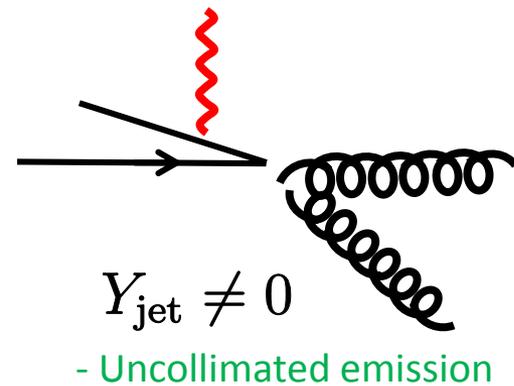
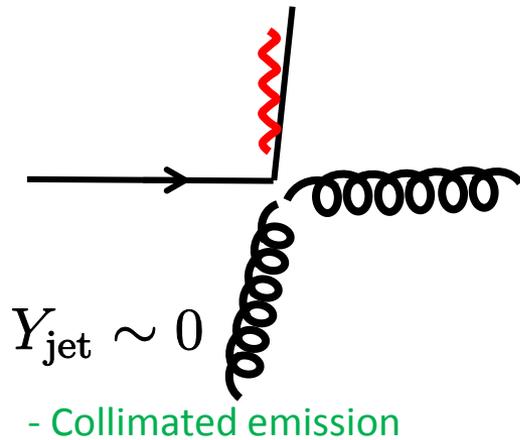
Consistent results from McGill-BNL, (2011)

$$\frac{dn_{\text{jet}}}{k_t dk_t d\phi_{\text{jet}} dY} = \frac{\alpha_s^2}{k_t^2} \frac{d\sigma_{gq}}{dY} \left(\frac{1}{1 + k_t/Q_{\text{sat}}} \right)^\beta \{ 1 + 2v_{\text{jet}}^{(2)} \cos 2\phi_{\text{jet}} + \dots \}$$

$$\epsilon_{\mathbf{p}} \frac{dN_\gamma}{d^3\mathbf{p}} = \frac{1}{2\pi p_t} \frac{dN_\gamma}{dp_t dY_\gamma} \{ 1 + 2v_\gamma^{(2)} \cos 2\phi_p + \dots \}$$

$$\frac{v_\gamma^{(2)}}{v_{\text{jet}}^{(2)}} = \frac{\int \cos(2\phi) f_0(k_t, Y) \cdot \epsilon_{\mathbf{p}} \frac{dn_\gamma}{d^3\mathbf{p}}}{\int f_0(k_t, Y) \cdot \epsilon_{\mathbf{p}} \frac{dn_\gamma}{d^3\mathbf{p}}}$$

Rapidity distribution of jets emitting photons in mid-rapidity



Bremsstrahlung from a quark (antiquark) jet

Photon emission rate from quark current

$$2\epsilon_p \frac{dn_\gamma}{d^3p} = -\frac{1}{(2\pi)^3} \tilde{j}^\mu(p) \tilde{j}_\mu^*(p) \Big|_{p^0=|p|}$$

Quark (antiquark) current

$$j^\mu(x) = e \{ v_{\text{ini}}^\mu \delta^{(3)}(\mathbf{x} - \mathbf{v}_{\text{ini}} t) \theta(-t) + v_{\text{fin}}^\mu \delta^{(3)}(\mathbf{x} - \mathbf{v}_{\text{fin}} t) \theta(t) \}$$

$$v_{\text{ini}} = (0, 0, 1)$$

Classical trajectory after the scattering

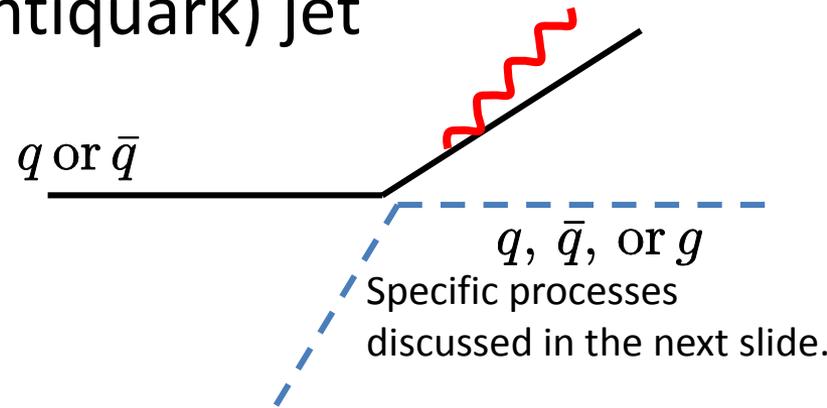
$$\epsilon_{\text{jet}}^2 - \mathbf{k}_{\text{jet}}^2 = Q_{\text{jet}}^2$$

$$v_\perp = \frac{k_t}{\epsilon_{\text{jet}}} = \frac{k_t}{\sqrt{k_t^2 + Q_{\text{jet}}^2} \cosh Y_{\text{jet}}}$$

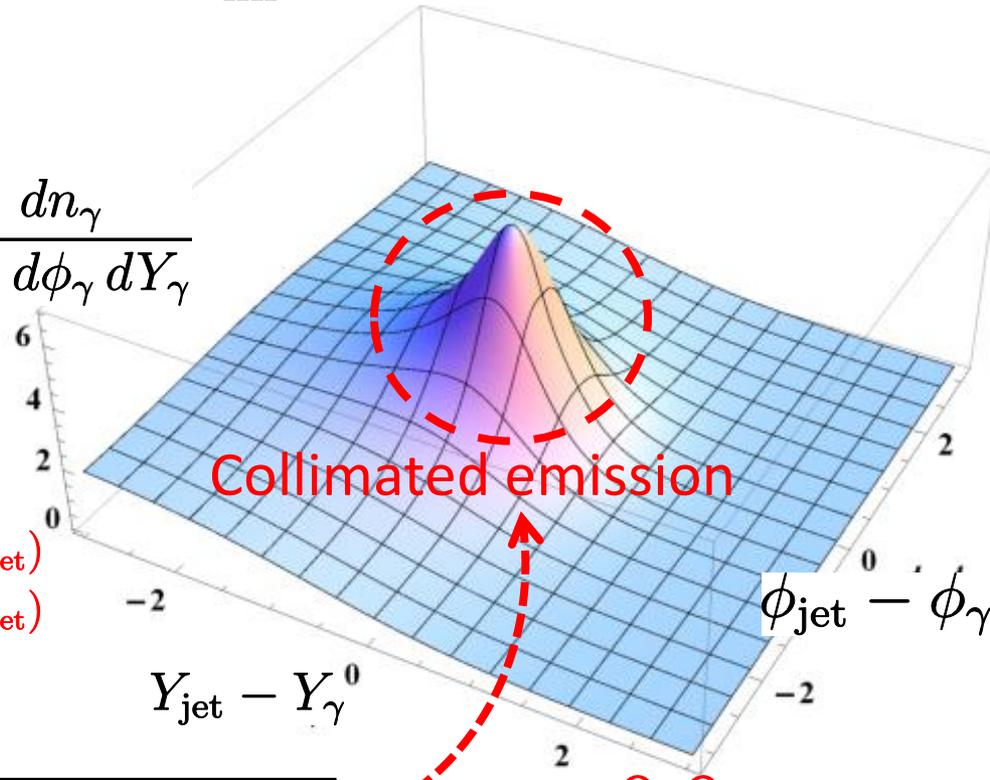
$$\begin{aligned} \mathcal{K} &\rightarrow 1 \quad \text{Relativistic limit} && (k_t \gg Q_{\text{jet}}) \\ &\rightarrow 0 \quad \text{Non-relativistic limit} && (k_t \ll Q_{\text{jet}}) \end{aligned}$$

Photon emission rate

$$2\epsilon_p \frac{dn_\gamma}{d^3p} \propto \frac{\alpha_{\text{em}}}{p_\perp^2} \frac{1}{\{ \cosh(Y_{\text{jet}} - Y_\gamma) - \mathcal{K} \cos(\phi_{\text{jet}} - \phi_\gamma) \}^2}$$



$$\frac{1}{p_t} \frac{dn_\gamma}{dp_t d\phi_\gamma dY_\gamma}$$



$\mathcal{K} = 0.9$

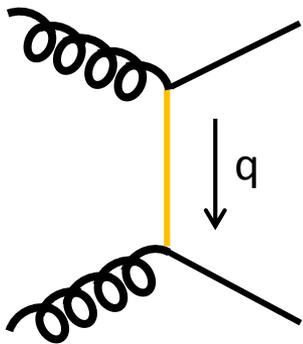
What is the dominant quark-jet production process?

→ Gluon Compton scattering

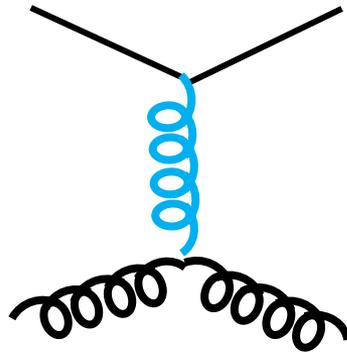
1. Gluon-dominant PDF

→ Take processes involving at least one gluon.

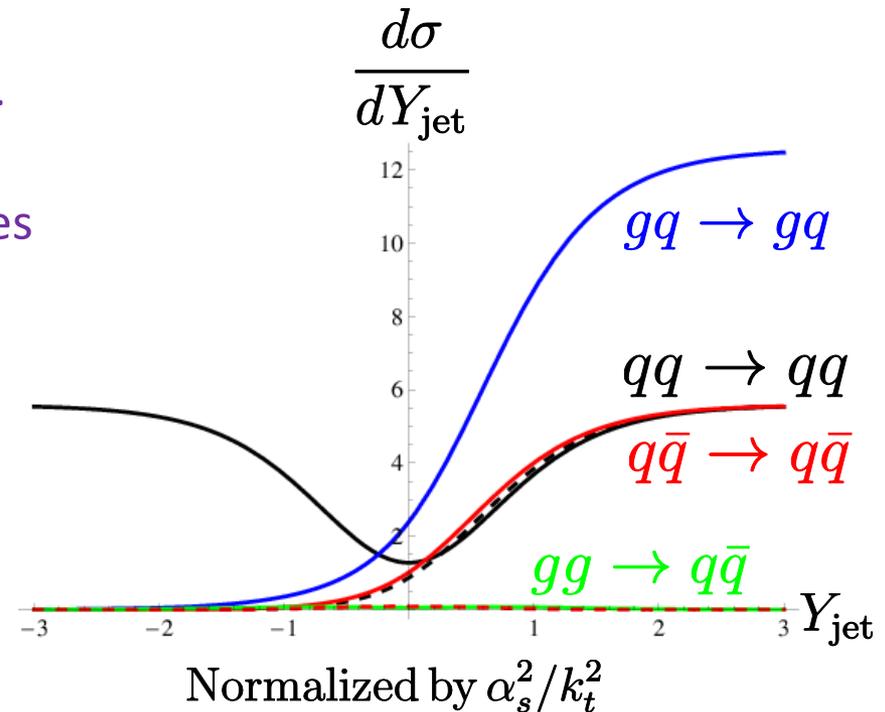
2. Dominant diagrams from gluon exchanges



Enhanced by $1/q$



✓ Enhanced by $1/q^2$



Leading-order results

$$\frac{d\sigma_{gq}}{d\hat{t}} = \frac{\pi\alpha_s^2}{\hat{s}^2} \left[-\frac{4}{9} \left(\frac{\hat{s}}{\hat{u}} + \frac{\hat{u}}{\hat{s}} \right) + \frac{\hat{s}^2 + \hat{u}^2}{\hat{t}^2} \right]$$

$$\frac{d\sigma_{gg}}{d\hat{t}} = \frac{\pi\alpha_s^2}{\hat{s}^2} \left[\frac{1}{6} \left(\frac{\hat{t}}{\hat{u}} + \frac{\hat{u}}{\hat{t}} \right) - \frac{3\hat{t}^2 + \hat{u}^2}{8\hat{s}^2} \right]$$

$$\hat{s} = (2k_t \cosh Y)^2$$

$$\hat{t} = -\hat{s}(1 - \tanh Y)/2$$

$$\hat{u} = -\hat{s}(1 + \tanh Y)/2$$

Suppressed by COM energy