

# Saturation or collectivity in p+A collisions at RHIC and LHC

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Situation

Observables

Long-range longitudinal fluctuations / correlations

Conclusions

# The situation in p+A:

$C_2(\Delta\varphi)$	hydro	CGC	
$v_2(p_t)$	hydro	CGC	
$v_3(p_t)$	hydro		CGC for quarks
$v_{2,3}$ vs $N_{track}$	hydro		
$\langle p_t \rangle$ vs $N_{track}$	hydro	geom. scaling	
$v_2$ mass splitting	hydro		
$v_2\{2,4,6,8\}$	hydro	CGC ?	>0 up to 6 GeV [CMS]
$v_2(p_t)$ in d+Au	hydro		
$v_3(p_t)$ in He3+Au	hydro		
p+p	ampt	CGC ?	

Hydro is running strong. At high  $p_t > 1 - 2$  GeV it is questionable.

Uncertain status of hydro in p+p. AMPT describes well p+p ridge.

Local sources of correlations (domains etc.) seem to have problem with d+Au and He3+Au (the more sources the smaller  $v_n$ ).

in my opinion

**Successful hydro ?**  
**Unconvincing CGC ?**

CGC  $\Leftrightarrow$  dense partonic system  $\Rightarrow$  scatterings of partons  $\Rightarrow$  “hydro” ?

hydro-like behavior

P. Bozek, PRC 85 (2012) 014911

E. Shuryak, I. Zahed, PRC 88 (2013) 044915

K. Dusling, R. Venugopalan, PRD 87 (2013), 094034

A. Dumitru, A.V. Giannini, NPA 933 (2014) 212

V. Skokov, PRD 91 (2015) 054014

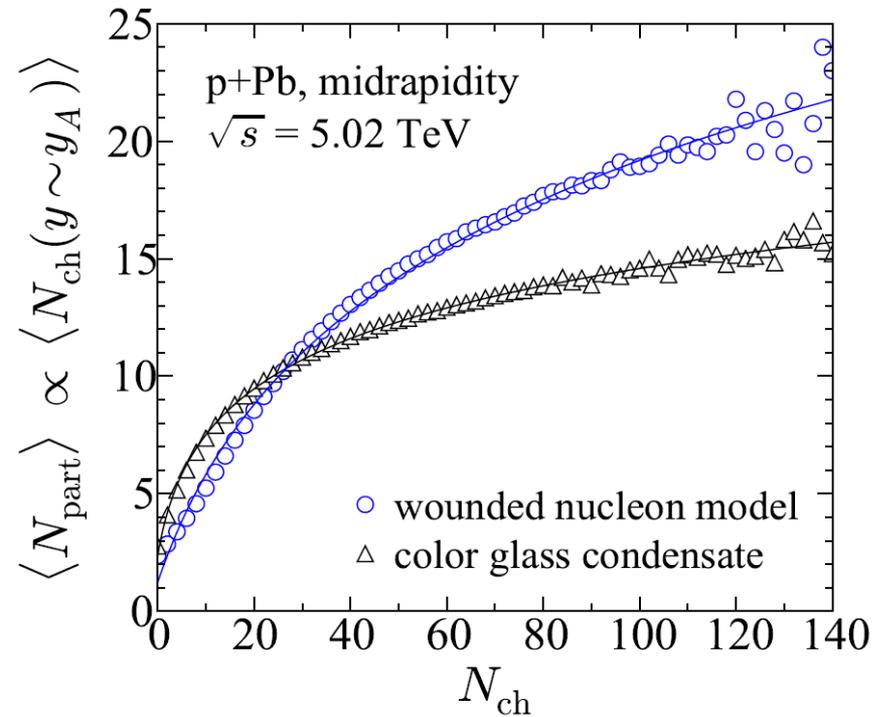
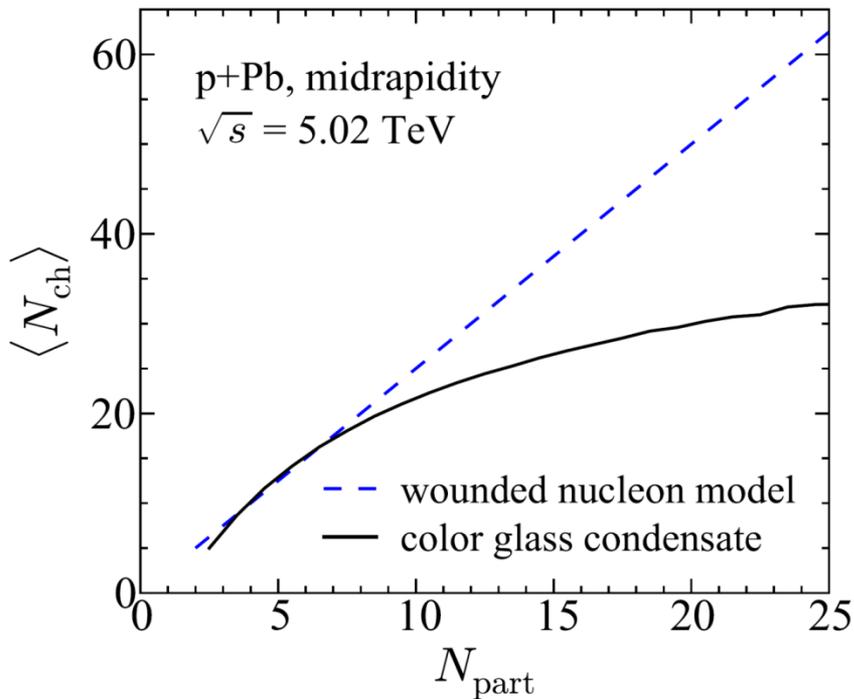
G.L. Ma, AB, PLB 739 (2014) 209

# Possible tests of initial vs. final state physics.

CGC:  $\langle N_{pA} \rangle \sim \ln(N_{part})$  checked in rcBK, IP-Glasma, KLN

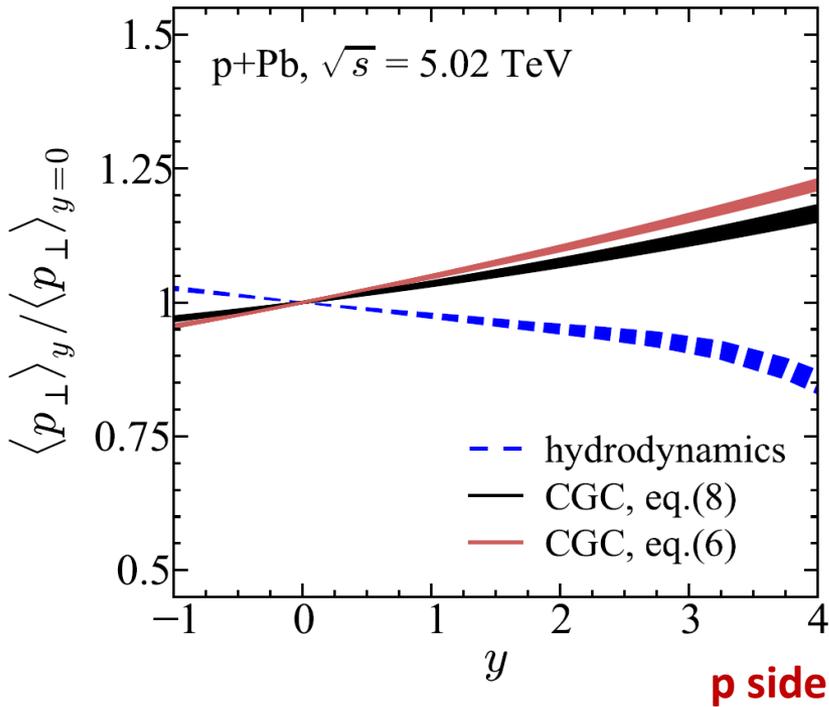
WNM:  $\langle N_{pA} \rangle \sim N_{part}$

↑  
thanks to B.Schenke

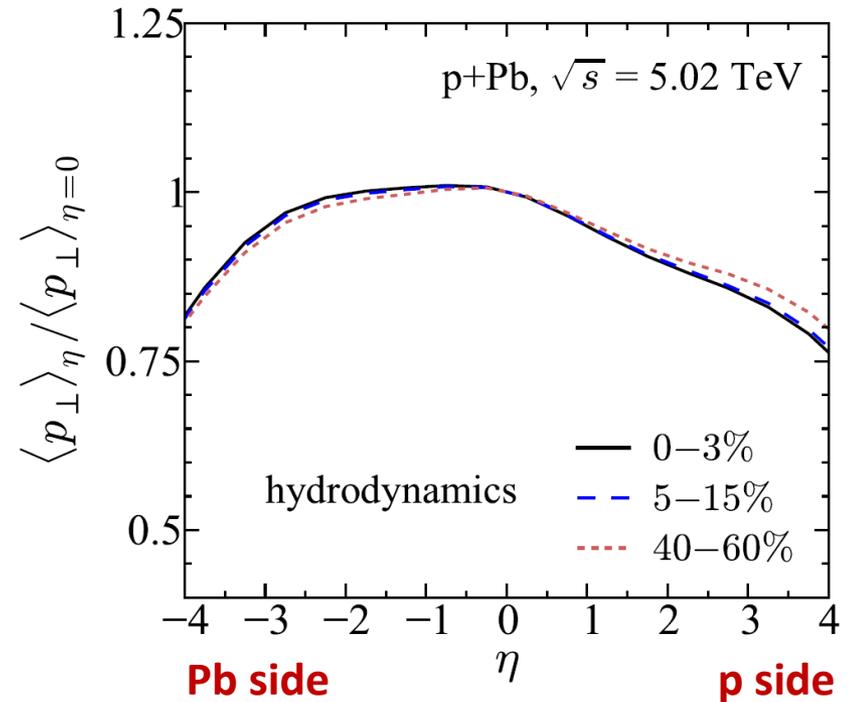


# $\langle p_T \rangle$ versus $\eta$ on proton side

$\langle p_t \rangle \sim Q_s^A$ ,  $Q_s^A$  is growing with  $y$

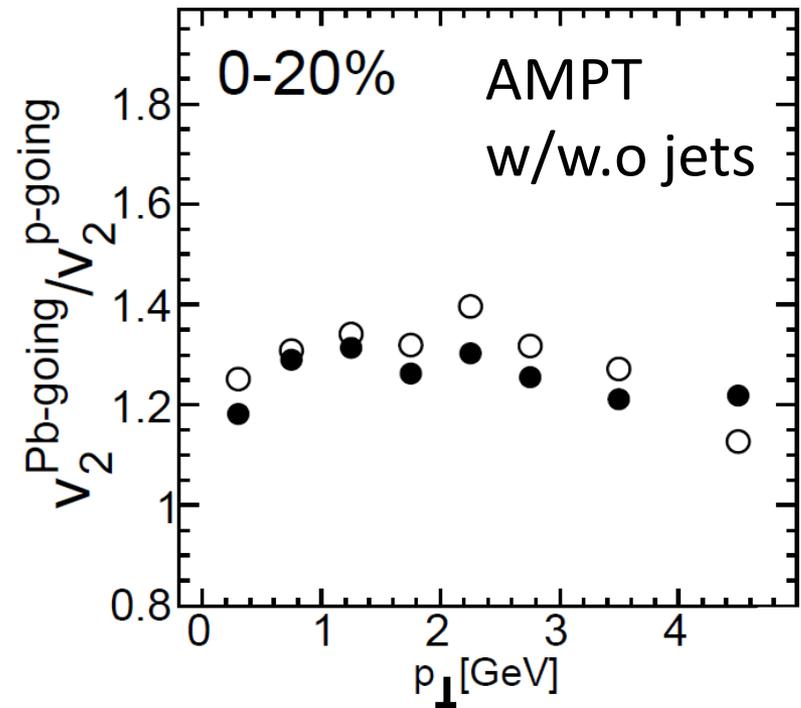
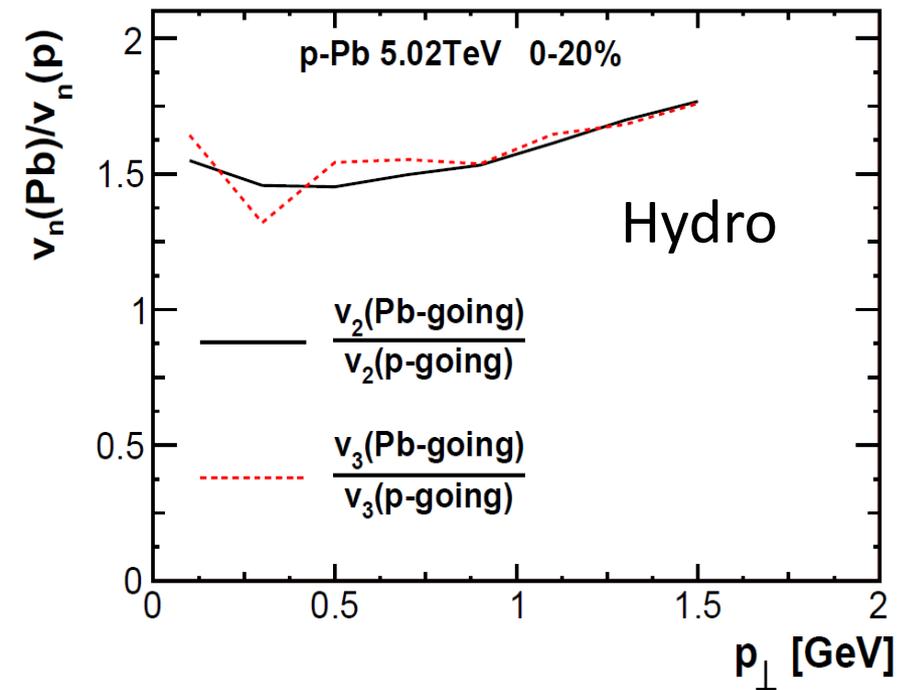


less stuff on proton side



CGC predictions are not so clear, many uncertainties.

$v_n$  on proton ( $-4 < \eta < -2.5$ ) and nucleus ( $2.5 < \eta < 4$ ) sides



for 40-60% the ratio is 1

CGC predictions are welcomed!

# Correlations:

N.Borghini, P.M.Dinh, J.-Y.Ollitrault,  
PRC 63 (2001) 054906

$$\begin{aligned}(v_2\{2\})^2 &= \langle e^{i2(\varphi_1 - \varphi_2)} \rangle \\ &= \langle v_2^2 \rangle + c_2\end{aligned}$$

$c_m$  is non-flow

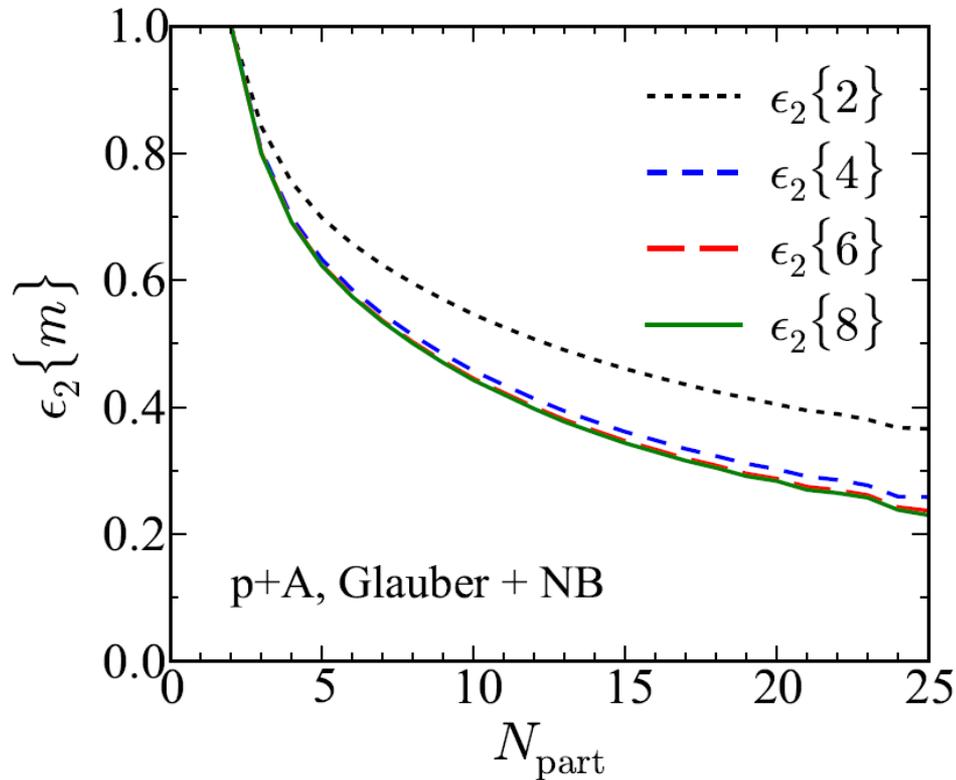
$$\begin{aligned}(v_2\{4\})^4 &= -\langle e^{i2(\varphi_1 + \varphi_2 - \varphi_3 - \varphi_4)} \rangle + 2\langle e^{i2(\varphi_1 - \varphi_2)} \rangle^2 \\ &= -\langle v_2^4 \rangle + 2\langle v_2^2 \rangle^2 + c_4\end{aligned}$$

etc.

if in each event  $v_2 = \overline{v_2}$   
and no non-flow  $\rightarrow$   $v_2\{2\} = \overline{v_2}$   
 $v_2\{m\} = \overline{v_2}$

# p+A with negative binomial distribution

for many other implementations  
it looks similar



$$v_2\{2\} > v_2\{4\} \approx v_2\{6\} \approx v_2\{8\}$$

AB, P. Bozek, L. McLerran, NPA 927 (2014) 15  
L. Yan, J.-Y. Ollitrault, PRL 112 (2014) 082301  
AB, V. Skokov, NPA 943 (2015) 1

$$\langle \epsilon_2^{2n} \rangle = \frac{n! \lim_{z \rightarrow 0} \frac{d^n}{dz^n} \langle I_0(2\sqrt{z}r^2) \rangle^N}{\lim_{z \rightarrow 0} \frac{d^{2n}}{dz^{2n}} \langle e^{-r^2 z} \rangle^N}$$

# Long-range (pseudo)rapidity correlations

AB, D. Teaney,  
PRC 87 (2013) 024906

average single  
particle distribution



$$\rho_{\text{event}}(y) = \langle \rho(y) \rangle \left[ 1 + \sum_{i=0} a_i T_i(y/Y) \right]$$

↑  
single particle distribution  
in an event

↑  
orthogonal polynomial  
Chebyshev, Legendre, etc. ?

$a_i$  - coefficients analogous to elliptic, triangular etc. flow

$y$  - rapidity or pseudorapidity

$Y$  - measurement is from  $-Y$  to  $Y$

## Long-range (pseudo)rapidity correlations

$$\rho_{\text{event}}(y) = \langle \rho(y) \rangle \left[ 1 + a_0 + a_1 \frac{y}{Y} + \dots \right]$$

$a_1$  could be driven by asymmetry in the number of left- and right-going wounded nucleons,  $w_L$  and  $w_R$

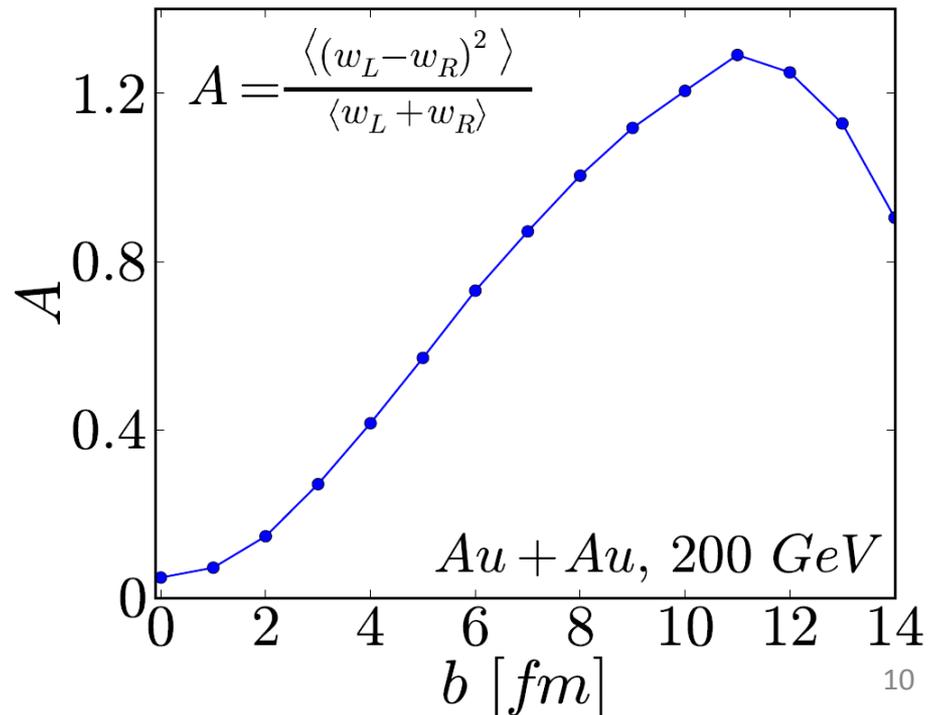
$a_0$  is rapidity independent fluctuation of fireball as a whole

see also

J.Jia, S.Radhakrishnan, M.Zhou

arXiv:1506.03496 (2015)

for more practical discussion



$$\rho_{\text{event}}(y) = \langle \rho(y) \rangle \left[ 1 + \sum_{i=0} a_i T_i(y/Y) \right]$$



$$\frac{C_2(y_1, y_2)}{\langle \rho(y_1) \rangle \langle \rho(y_2) \rangle} = \sum_{i,k} \langle a_i a_k \rangle T_i(y_1/Y) T_k(y_2/Y)$$

Long-range two-particle correlation function

$$\frac{C_2(y_1, y_2)}{\langle \rho(y_1) \rangle \langle \rho(y_2) \rangle} \sim \langle a_0^2 \rangle + \langle a_1^2 \rangle \frac{y_1 y_2}{Y^2} + \dots$$

## First hydro calculations reported recently

P.Bozek, W.Broniowski, A.Olszewski, arXiv:1509.04124

A.Monnai, B.Schenke, arXiv:1509.04103

New ATLAS results reported at this QM → J. Jia

It would be interesting to calculate  $\langle a_i a_k \rangle$  in CGC related models.

New nontrivial tests for all models in p+p, p+A, A+A collisions

It is important to remove the short-range correlations related to resonances, jets, etc. → **multi-particle rapidity correlations**

$$\frac{C_n(y_1, \dots, y_n)}{\langle \rho(y_1) \rangle \dots \langle \rho(y_n) \rangle}$$

AB, P. Bozek,  
arXiv:1509.02967

AB, D. Teaney,  
PRC 87 (2013) 024906

For example the genuine 4-particle correlation function

$$\frac{C_4(y_1, y_2, y_3, y_4)}{\langle \rho(y_1) \rangle \dots \langle \rho(y_4) \rangle} = \sum_{i,k,m,n=0} \langle a_i a_k a_m a_n \rangle_{[4]} T_i(y_1) T_k(y_2) T_m(y_3) T_n(y_4)$$

$$\begin{aligned} \langle a_i a_k a_m a_n \rangle_{[4]} &\equiv \langle a_i a_k a_m a_n \rangle - \langle a_i a_k \rangle \langle a_m a_n \rangle \\ &\quad - \langle a_i a_m \rangle \langle a_k a_n \rangle - \langle a_i a_n \rangle \langle a_k a_m \rangle \end{aligned}$$

In particular

$$\langle a_i^4 \rangle_{[4]} \equiv \langle a_i^4 \rangle - 3 \langle a_i^2 \rangle^2$$

For more details see: AB, P. Bozek,  
arXiv:1509.02967

## Conclusions

Hydro can fit all data in p+Pb, d+Au and He3+Au

CGC less successful

New tests:  $\langle p_t \rangle$ ,  $v_2$ ,  $v_3$  vs. (pseudo)rapidity  
 $\langle N_{ch} \rangle$  vs.  $N_{part}$

Multi-particle long-range rapidity correlations could shed more light on physics in small systems