

A Challenge to Lepton Universality

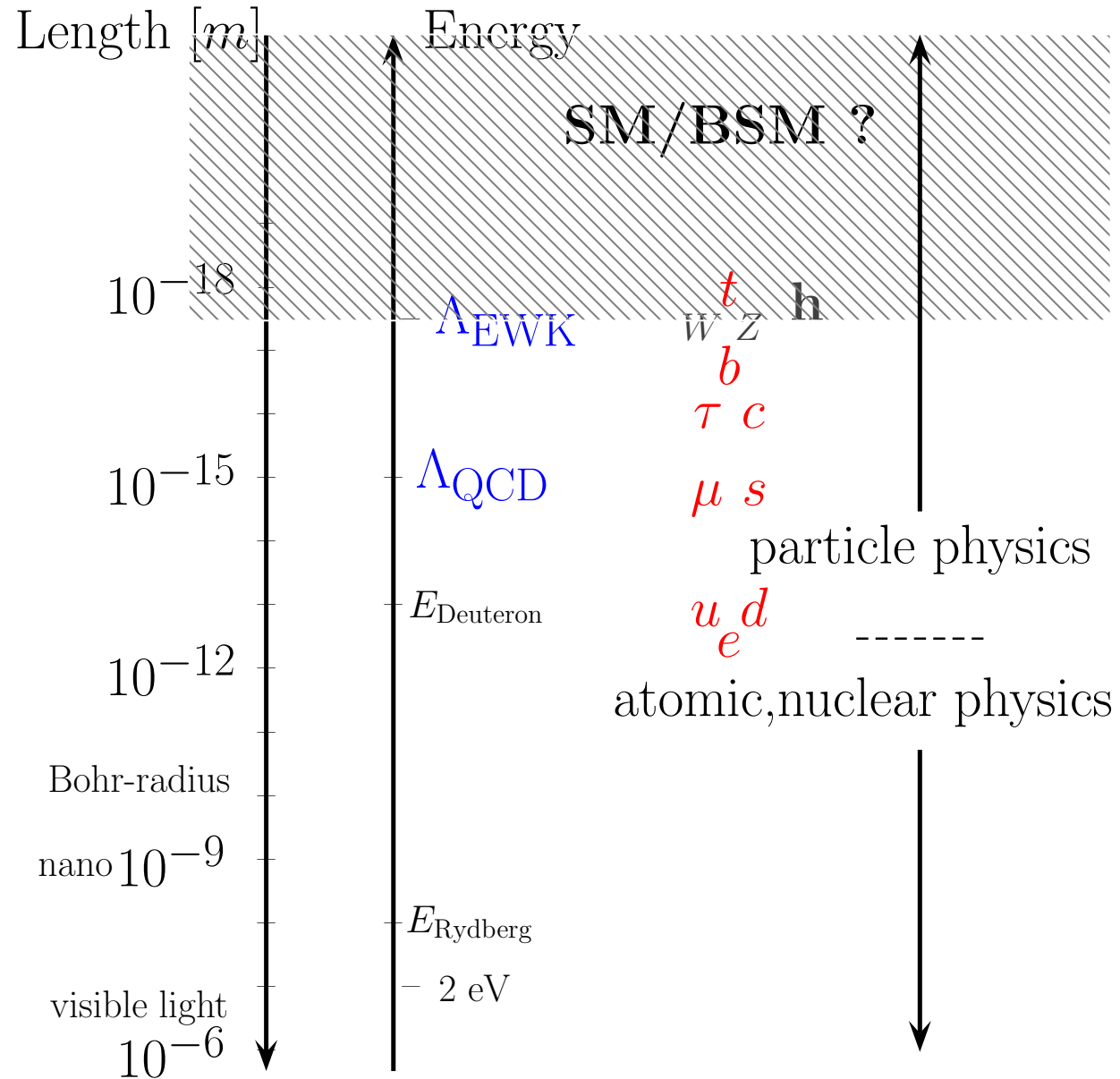
$$R_K @ \text{LHCb} \neq 1$$

<http://journals.aps.org/prl/abstract/10.1103/PhysRevLett.113.151601>,
arXiv:1406.6482 [hep-ex]

physics highlight: <http://physics.aps.org/articles/v7/102>

Gudrun Hiller, Dortmund

Exploring Physics at Highest Energies



FCNCs are suppressed in SM by i) weak loop, ii) CKM and iii) GIM. These mechanisms do not have to be at work in BSM, so FCNCs are a great place to look for BSM effects.

$$s \rightarrow d: K^0 - \bar{K}^0, K \rightarrow \pi \nu \bar{\nu}$$

$$c \rightarrow u: D^0 - \bar{D}^0, \Delta A_{CP}$$

$$b \rightarrow d: B^0 - \bar{B}^0, B \rightarrow \rho \gamma, b \rightarrow d \gamma, B \rightarrow \pi \mu \mu$$

$$b \rightarrow s: B_s - \bar{B}_s, b \rightarrow s \gamma, B \rightarrow K_s \pi^0 \gamma, b \rightarrow s l l, B \rightarrow K^{(*)} l l \text{ (precision, angular analysis, } R_K), B_s \rightarrow \mu \mu$$

$$t \rightarrow c, u, l \rightarrow l': \text{ not observed}$$

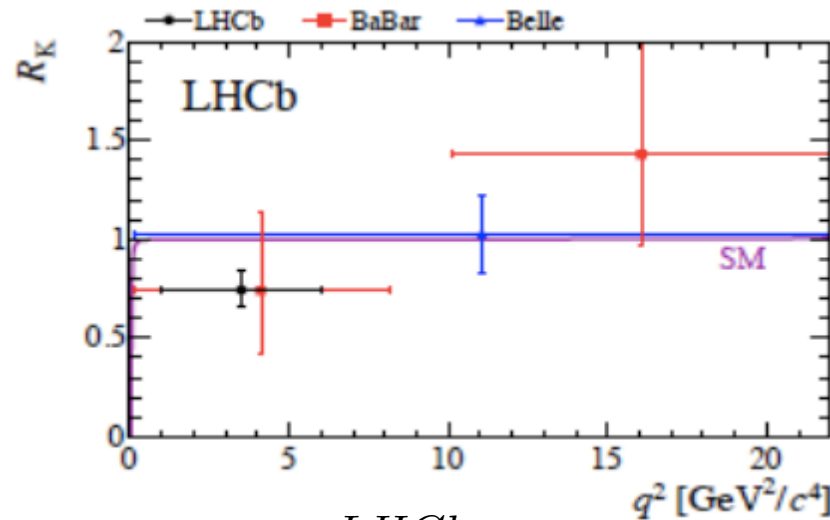
in red: **THIS TALK!**

$$R_K = \frac{\mathcal{B}(\bar{B} \rightarrow \bar{K} \mu \mu)}{\mathcal{B}(\bar{B} \rightarrow \bar{K} e e)}$$

idea: $R_H^{\text{SM}} = 1 + \text{tiny}$ for $H = K, K^*, X_s, \dots$ GH, Krüger, hep-ph/0310219

refined, cuts, correlations, models: 0709.4174 Bobeth et al

early data: Belle 0904.0770, BaBar 1204.3933, consistent with SM



latest data: LHCb 1406.6482 $R_K^{\text{LHCb}} \simeq 3/4 \pm 0.1$: **2.6 σ , BSM huge!**

theory: 1406.6681 1407.7044 1408.1627 1408.4097 1409.0882

$B^\pm \rightarrow K^\pm ee$ and $B^\pm \rightarrow K^\pm \mu\mu$ events at LHCb. Full data set, 3fb^{-1} , from 7 and 8 TeV LHC run.

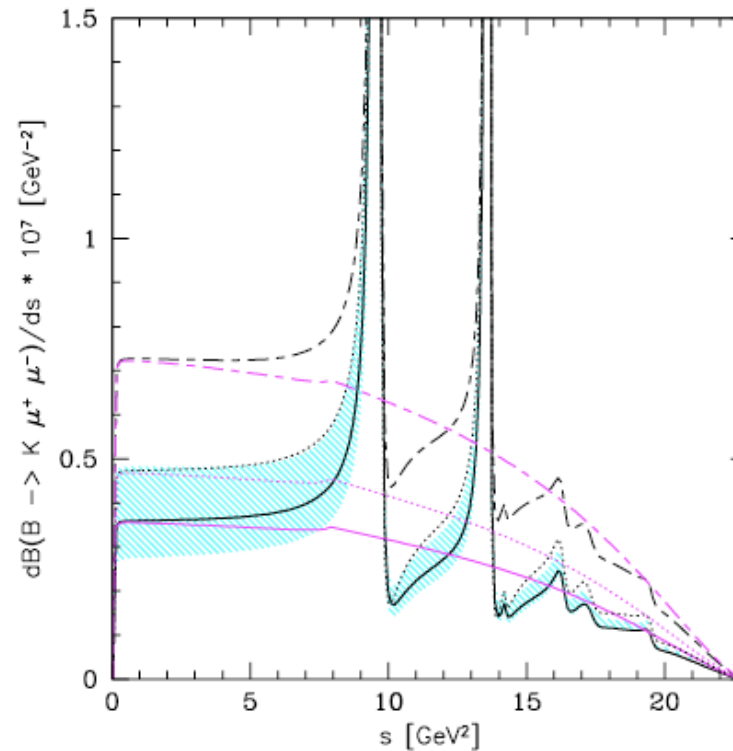


Fig from 9910221, solid: SM, dotted and dot-dashed: susy

Select low dilepton mass window: $1 \leq q^2 < 6 \text{ GeV}^2$ below J/Ψ .

situation for numerator $\mu\mu$ and denominator ee of R_K separately:

	LHCb ^a	SM ^b
$\mathcal{B}(B \rightarrow K\mu\mu)_{[1,6]}$	$(1.21 \pm 0.09 \pm 0.07) \cdot 10^{-7}$	$(1.75^{+0.60}_{-0.29}) \cdot 10^{-7}$
$\mathcal{B}(B \rightarrow Kee)_{[1,6]}$	$(1.56^{+0.19+0.06}_{-0.15-0.04}) \cdot 10^{-7}$	same
$R_K _{[1,6]}$	$0.745 \pm_{0.074}^{0.090} \pm 0.036$	$\simeq 1$

^a 1209.4284 (μ) and 1406.6482 (e) ^b Bobeth, GH, van Dyk '12, form factors from 1006.4945

Individual branching ratios make presently no case for new physics, although muons are a bit below SM. The Ratio R_K is much cleaner.

Probing Lepton e vs μ universality with R_K

.. which was the idea behind R_K in first place:

Lepton-universal effects – including hadronic ones – drop out in ratios of branching fractions GH,Krüger'03

$$R_K^{LHCb} = \frac{\mathcal{B}(\bar{B} \rightarrow \bar{K} \mu \mu)}{\mathcal{B}(\bar{B} \rightarrow \bar{K} e e)}$$

$R_K^{\text{SM}} = 1$ up to kinematic corrections $\mathcal{O}(m_\mu^2/m_b^2)$ and electromagnetic logs (depending on exp. cuts) $\mathcal{O}(\frac{\alpha_e}{4\pi} \text{Log}(m_e/m_b))$ at O(per mille) level.

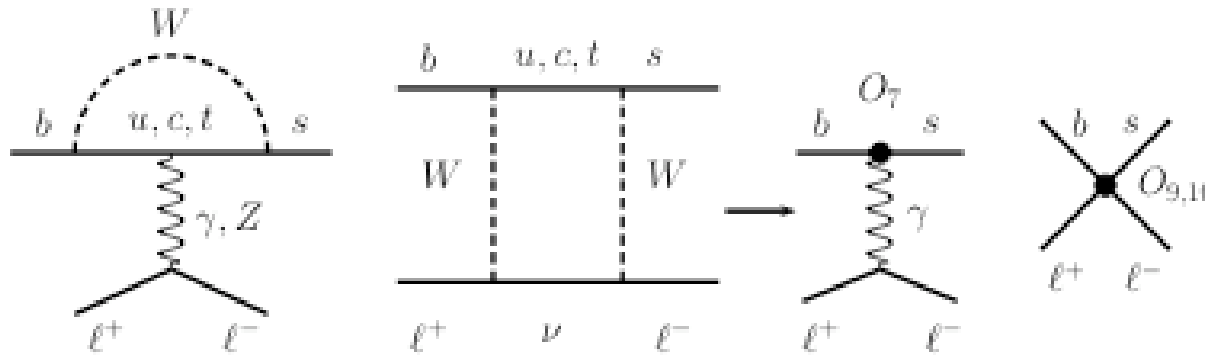
$$R_K^{LHCb} = 0.745 \pm_{0.074}^{0.090} \pm 0.036, \quad \text{1406.6482 hep-ex}$$

2.6σ : if taken at face value this implies lepton-nonuniversal new physics in the flavor sector.

Probing Lepton e vs μ universality with R_K

Comments:

- $R_K = 0.745 \pm_{0.074}^{0.090} \pm 0.036 < 1$ implies suppressed muons and/or enhanced electrons, that is, BSM in electrons, or muons, or both.
- $R_K \simeq 3/4$ is almost an order 1 effect. Yet, it is not excluded by other data essentially because R_K is so clean and the effect, lepton-nonuniversality in $b \rightarrow s$, is quite specific.
- Ongoing precision fits in $B \rightarrow K^{(*)} \ell \ell$ decays (Babar, Belle, CDF, ATLAS, CMS, LHCb) [1307.5683](#), [1308.1501](#), [1310.2478](#) dominated from hadron colliders hence give essentially lepton-specific constraints for $\ell = \mu$.
- Electrons much more difficult for LHCb than muons:
 $B \rightarrow K \mu \mu$: ~ 1226 events, $B \rightarrow K e e$: $\sim O(200)$ events.



Construct EFT $\mathcal{H}_{\text{eff}} = -4 \frac{G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i C_i(\mu) O_i(\mu)$ at dim 6

V,A operators $\mathcal{O}_9 = [\bar{s} \gamma_\mu P_L b] [\bar{\ell} \gamma^\mu \ell]$, $\mathcal{O}'_9 = [\bar{s} \gamma_\mu P_R b] [\bar{\ell} \gamma^\mu \ell]$

$\mathcal{O}_{10} = [\bar{s} \gamma_\mu P_L b] [\bar{\ell} \gamma^\mu \gamma_5 \ell]$, $\mathcal{O}'_{10} = [\bar{s} \gamma_\mu P_R b] [\bar{\ell} \gamma^\mu \gamma_5 \ell]$

S,P operators $\mathcal{O}_S = [\bar{s} P_R b] [\bar{\ell} \ell]$, $\mathcal{O}'_S = [\bar{s} P_L b] [\bar{\ell} \ell]$, **ONLY $\mathcal{O}_9, \mathcal{O}_{10}$ are SM, all other BSM**

$\mathcal{O}_P = [\bar{s} P_R b] [\bar{\ell} \gamma_5 \ell]$, $\mathcal{O}'_P = [\bar{s} P_L b] [\bar{\ell} \gamma_5 \ell]$

and tensors $\mathcal{O}_T = [\bar{s} \sigma_{\mu\nu} b] [\bar{\ell} \sigma^{\mu\nu} \ell]$, $\mathcal{O}_{T5} = [\bar{s} \sigma_{\mu\nu} b] [\bar{\ell} \sigma^{\mu\nu} \gamma_5 \ell]$

lepton specific $C_i O_i \rightarrow C_i^\ell O_i^\ell$, $\ell = e, \mu, \tau$

Barring the presence of several different types of operators, hence allowing for tuning, there are the following model-independent explanations for R_K :

- i)* V,A operators with muons
- ii)* V,A operators with electrons
- iii)* S,P operators electrons (disfavored at 1σ and requires cancellations, testable with $\bar{B} \rightarrow \bar{K} ee$ angular distributions)

Tensors and S,P muons are excluded.

Model-independent interpretations with V,A interactions: [arXiv:1408.1627](#),

[1406.6681](#)

$$0.7 \lesssim \text{Re}[X^e - X^\mu] \lesssim 1.5 ,$$

$$X^\ell = C_9^{\text{NP}\ell} + C_9^{\prime\ell} - (C_{10}^{\text{NP}\ell} + C_{10}^{\prime\ell}) , \quad \ell = e, \mu .$$

- The required NP is large, almost $O(1)$ of SM $C_9^{\text{SM}} \simeq -C_{10}^{\text{SM}} \simeq 4.2$.
- Since the SM couples V-A-like, the leading constraints on X^ℓ from SM-NP-interference have V-A structure for the leptons; there's no sensitivity to V+A (right-handed) leptons at this level.

Lets use the chiral basis:

$$\begin{aligned}\mathcal{O}_{LL}^\ell &\equiv (\mathcal{O}_9^\ell - \mathcal{O}_{10}^\ell)/2, & \mathcal{O}_{LR}^\ell &\equiv (\mathcal{O}_9^\ell + \mathcal{O}_{10}^\ell)/2, \\ \mathcal{O}_{RL}^\ell &\equiv (\mathcal{O}'_9{}^\ell - \mathcal{O}'_{10}{}^\ell)/2, & \mathcal{O}_{RR}^\ell &\equiv (\mathcal{O}'_9{}^\ell + \mathcal{O}'_{10}{}^\ell)/2.\end{aligned}$$

R_K sensitive to left-handed leptons:

$$C_{LL}^\ell = C_9^\ell - C_{10}^\ell, \quad C_{RL}^\ell = C'_9{}^\ell - C'_{10}{}^\ell.$$

right-handed leptons: $C_{LR}^\ell = C_9^\ell + C_{10}^\ell$, $C_{RR}^\ell = C'_9{}^\ell + C'_{10}{}^\ell$

This suggests to use in global fits invariant-constraints such as

$$C_9^{\text{NP}\ell} = -C_{10}^{\text{NP}\ell}, \quad C_9^{\text{NP}'\ell} = -C_{10}^{\text{NP}'\ell}.$$

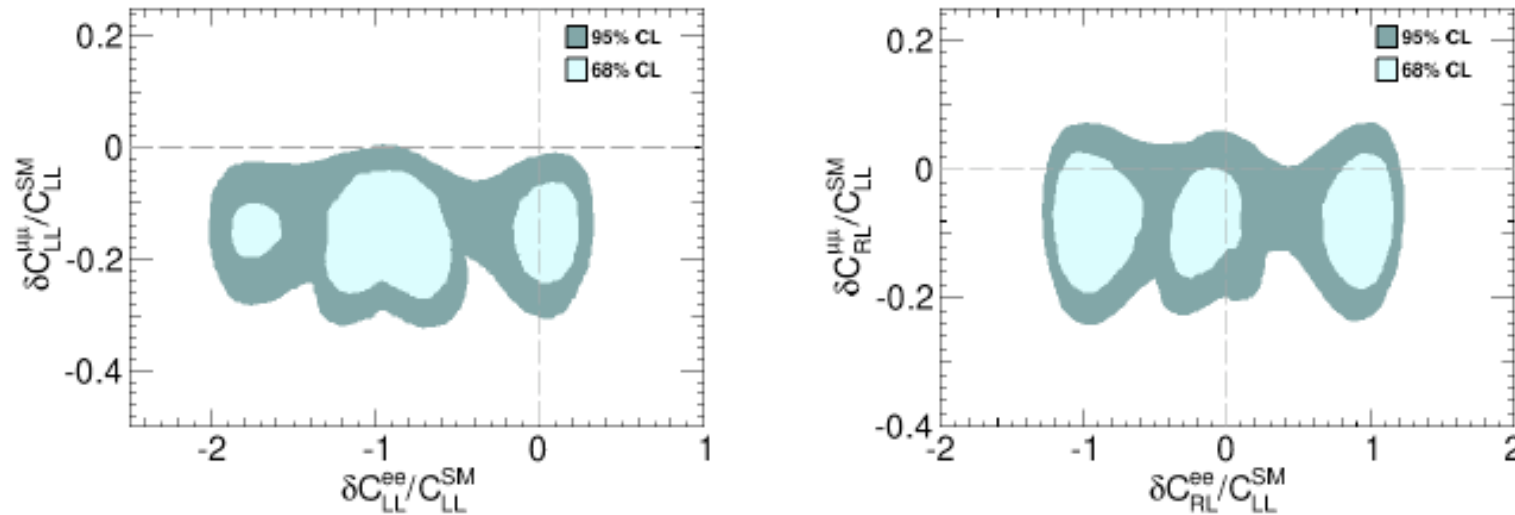


Fig from 1410.4545 – global fit including R_K

- Bounds stronger for $\mu\mu$ (y -axis) than for ee (x -axis).
- Both left-handed quarks C_{LL} (left-handed plot) and right-handed quarks C_{RL} (right-handed plot) can be sizable.

If we assume new physics in muons alone employ $\mathcal{B}(\bar{B}_s \rightarrow \mu\mu)$

$$\frac{\mathcal{B}(\bar{B}_s \rightarrow ee)^{\text{exp}}}{\mathcal{B}(\bar{B}_s \rightarrow ee)^{\text{SM}}} < 3.3 \cdot 10^6, \quad \frac{\mathcal{B}(\bar{B}_s \rightarrow \mu\mu)^{\text{exp}}}{\mathcal{B}(\bar{B}_s \rightarrow \mu\mu)^{\text{SM}}} = 0.79 \pm 0.20 \quad \text{is suppressed currently.}$$

$$0.0 \lesssim \text{Re}[C_{LR}^\mu + C_{RL}^\mu - C_{LL}^\mu - C_{RR}^\mu] \lesssim 1.9, \quad (\mathcal{B}(B_s \rightarrow \mu\mu))$$

$$0.7 \lesssim -\text{Re}[C_{LL}^\mu + C_{RL}^\mu] \lesssim 1.5. \quad (R_K)$$

This isolates C_{LL}^μ as the only single operator (particle) interpretation of R_K . Note: this is V-A. Iff $\mathcal{B}(\bar{B}_s \rightarrow \mu\mu)$ would be enhanced this would isolate $C_{RL}^\mu \simeq -1$, V+A! $b \rightarrow see$ way less constrained.

V,A muons and V,A electrons can be realized with leptoquark models

GH, Schmaltz arXiv:1408.1627, Phys. Rev. D 90, 054014 (2014)

A model with C_{RL}^e (includes R-parity violating MSSM):

$\mathcal{L} = -\lambda_{d\ell} \varphi (\bar{d} P_L \ell)$ with leptoquark $\varphi(3, 2)_{1/6}$ with mass M .

$$\mathcal{H}_{\text{eff}} = -\frac{|\lambda_{d\ell}|^2}{M^2} (\bar{d} P_L \ell) (\bar{\ell} P_R d) = \frac{|\lambda_{d\ell}|^2}{2M^2} [\bar{d} \gamma^\mu P_R d] [\bar{\ell} \gamma_\mu P_L \ell]$$

from tree level φ exchange and fierzing.

In terms of the usual Wilson coefficients:

$$C_{10}^{\prime e} = -C_9^{\prime e} = \frac{\lambda_{se} \lambda_{be}^*}{V_{tb} V_{ts}^*} \frac{\pi}{\alpha_e} \frac{\sqrt{2}}{4M^2 G_F} = -\frac{\lambda_{se} \lambda_{be}^*}{2M^2} (24\text{TeV})^2$$

R_K -benchmark: $C_9^{\prime e} = -C_{10}^{\prime e} \simeq 1/2$ follows $M^2 / \lambda_{se} \lambda_{be}^* \simeq (24\text{TeV})^2$

Viable parameters of the (scalar) leptoquarks read

$$\begin{aligned} 1 \text{ TeV} &\lesssim M \lesssim 48 \text{ TeV} \\ 2 \cdot 10^{-3} &\lesssim |\lambda_{se}\lambda_{be}^*| \lesssim 4 \\ 4 \cdot 10^{-4} &\lesssim |\lambda_{qe}| \lesssim 5 \end{aligned}$$

- $SU(2)$ implies corresponding effects in $b \rightarrow s\nu\nu$ (only electron-neutrinos affected, signal diluted over 3 species).
 $\mathcal{B}(B \rightarrow K\nu\nu)$ reduced by 5 %, $\mathcal{B}(B \rightarrow K^*\nu\nu)$ enhanced by 5 %, F_L enhanced by 2 % w.r.t SM.
- Further correlation with B_s mixing, $b \rightarrow s\gamma$, and direct searches.
- Decay modes of φ -doublet: $\varphi^{2/3} \rightarrow b e^+$, $\varphi^{-1/3} \rightarrow b \nu$

A LL muon leptoquark model

$$\mathcal{L} = -\lambda_{b\mu} \varphi^* q_3 \ell_2 - \lambda_{s\mu} \varphi^* q_2 \ell_2, \quad \varphi(3, 3)_{-1/3}$$

$$\mathcal{H}_{\text{eff}} = -\frac{\lambda_{s\mu}^* \lambda_{b\mu}}{M^2} \left(\frac{1}{4} [\bar{q}_2 \tau^a \gamma^\mu P_L q_3] [\bar{\ell}_2 \tau^a \gamma_\mu P_L \ell_2] + \frac{3}{4} [\bar{q}_2 \gamma^\mu P_L q_3] [\bar{\ell}_2 \gamma_\mu P_L \ell_2] \right)$$

gives $C_9^{\text{NP}\mu} = -C_{10}^{\text{NP}\mu} = \frac{\pi}{\alpha_e} \frac{\lambda_{s\mu}^* \lambda_{b\mu}}{V_{tb} V_{ts}^*} \frac{\sqrt{2}}{2M^2 G_F} \simeq -0.5$ and similar mass range as other model.

Decay modes of φ -triplet:

$$\begin{aligned} \varphi^{2/3} &\rightarrow t \nu \\ \varphi^{-1/3} &\rightarrow b \nu, t \mu^- \\ \varphi^{-4/3} &\rightarrow b \mu^- \end{aligned}$$

The $U(1)_{\tau-\mu}$ -extension of SM [1403.1269 Altmannshofer et al](#) also violates lepton-universality. (V,A-muons-type i) model, no BSM in ee .)

C (LH-quark currents) versus
 C' (RH quark currents)?

Long story in interpreting $B \rightarrow K^{(*)} \mu\mu$ data/global fits as hadronic uncertainties (power corrections, resonances) could shadow BSM.

e.g. Camalich, Jäger '12, Lyon, Zwicky'14, .. in global fits 1307.5683, 1308.1501, 1310.2478, ...

Diagnosing lepton-nonuniversality

By parity and lorentz invariance, the C, C' enter decay amplitudes $B \rightarrow K \ell \ell$ etc as [GH, Schmaltz 1411.4773 \(today\)](#)

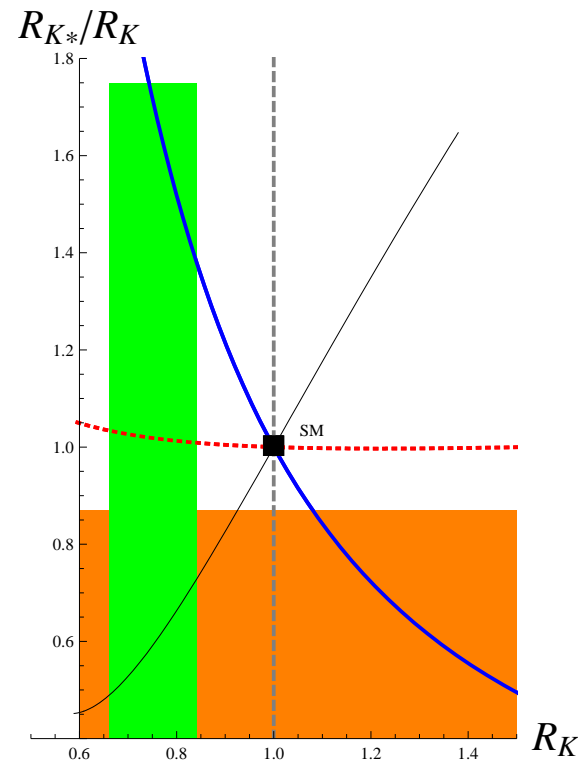
$$C + C' : K, K_{\perp}^*, \dots$$

$$C - C' : K_0(1430), K_{0,\parallel}^*, \dots$$

so different ratios R_K, R_{K^*} etc are complementary. It follows that double ratios R_{K^*}/R_K are cleanly probing right-handed currents! In addition, since K^* is dominated by '0' and '||' polarization, the complementarity between R_K and R_{K^*} (similarly R_{φ}) is maximal.

predictions: $R_K = R_{\eta}, R_{K^*} = R_{\varphi}$, and correlations between R_H .
Measure two R_H (with $C \pm C'$) and predict all of them !

Diagnosing lepton-nonuniversality



Green band: R_K 1 sigma LHCb. Curves: different BSM scenarios. red dashed: pure C_{LL} . Black solid: $C_{LL} = -2C_{RL}$. Blue: C_{RL} . Orange band is prediction for R_{K^*} (not significantly measured) based on R_K and $B \rightarrow X_s \ell \ell$: $R_{X_s}^{\text{Belle}'09} = 0.42 \pm 0.25$, $R_{X_s}^{\text{BaBar}'13} = 0.58 \pm 0.19$.

- If LHCb's measurement of R_K substantiates it implies that there is more difference between a muon and an electron than their mass. Lepton-universality, a feature of the $SU(3)_C \times SU(2)_L \times U(1)_Y$ SM appears to be violated in $b \rightarrow s$ FCNC transitions.
- Current data allow for model-independent explanations, as well as model frameworks such as leptoquarks. There is no conflict with other measurements nor with model-building.
- Explanations imply correlations with other FCNC processes as well as predictions for direct searches, that can be tested in the future.

STAY TUNED