



Measurement of the
 $D^0 \rightarrow \pi^- e^+ \nu$ BR, form factor and
implications for V_{ub}

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On behalf of the BaBar Collaboration

Outline

[PRD 91, 052022 (2015)]

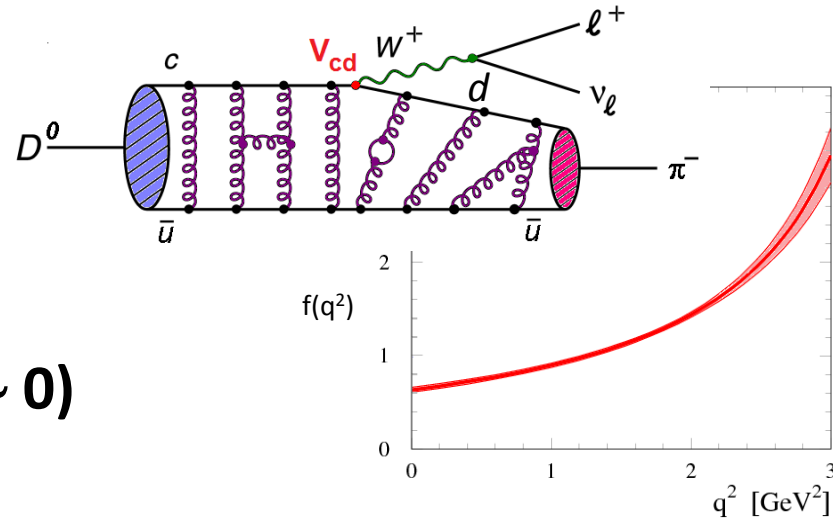
- Motivation
- Analysis of $D^0 \rightarrow \pi^- e^+ \nu$ events at BaBar
- Measurement of the branching fraction
- Form factor interpretation
- Application: V_{ub} extraction
- Conclusions

Motivation

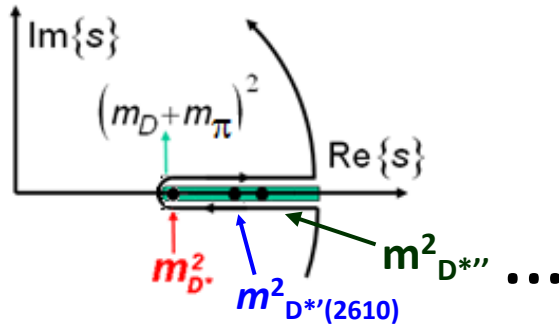
$$q^2 = (p_e + p_{\nu_e})^2 = (p_D - p_\pi)^2$$

- The $D^0 \rightarrow \pi^- e^+ \nu$ decay channel:

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{cd}|^2 p_\pi^3(q^2) |f_+(q^2)|^2$$



- Only one form factor: $f_+(q^2)$ ($m_e \sim 0$)



$$f_{+,D}^\pi(q^2) \simeq \sum_i \frac{\text{Res}(f_{+,D}^\pi) D_i^*}{m_{D_i^*}^2 - q^2}$$

D_i^* are $J^P = 1^-$ states ($\rightarrow D\pi$)

- Partially known: contributions from the D^* and $D^{*'}$ poles
- Can be related to the $B \rightarrow \pi$ form factor at the same $E_\pi \rightarrow V_{ub}$

Analysis method

- Based on similar techniques as in other BaBar analyses

$D^0 \rightarrow K^- e^+ \nu$ (PRD 76 (07) 052005), $D_s \rightarrow K^+ K^- e^+ \nu$ (PRD78 (08) 051101 (RC)), $D^+ \rightarrow K^- \pi^+ e^+ \nu$ (PRD 83 (11) 072001)

- $D^0 \rightarrow \pi^- e^+ \nu$: Cabibbo suppressed (BR~0.3%); large backgrounds from π 's

- From 347.2 fb^{-1} of $e^+ e^- \rightarrow c\bar{c}$ events at the $Y(4S)$ reconstruct $D^{*+} \rightarrow D^0 \pi^+$, $D^0 \rightarrow \pi^- e^+ \nu$:

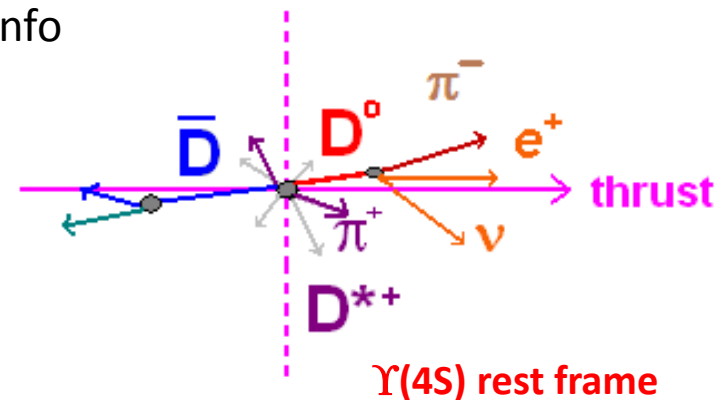
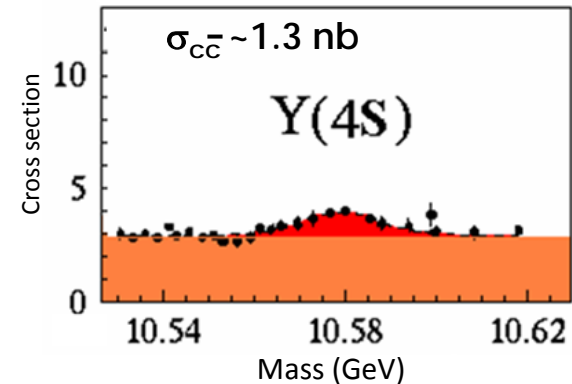
→ Partially reconstructed: π^+ , π^- and e^+ in the same hemisphere

→ Require tight PID signal pions and veto against kaons

→ Reconstruct $p_{D^0} = p_{\pi^-} + p_{e^+} + p_{\nu}$ using E_{miss} and info of the rest of the event

→ Constraints using m_{D^0} and $m_{D^{*+}}$

- Control channel from data: $D^0 \rightarrow K^- \pi^+$



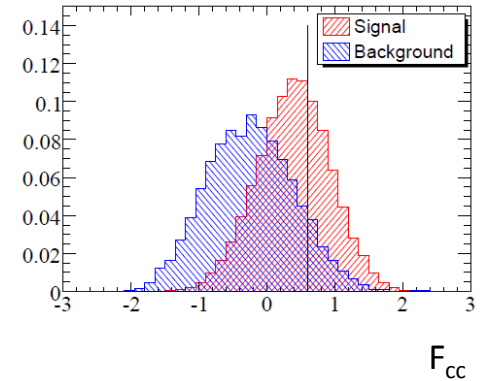
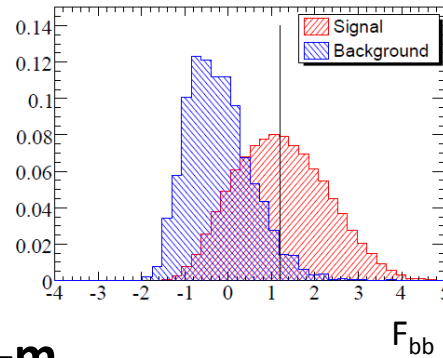
$Y(4S)$ rest frame

Analysis method

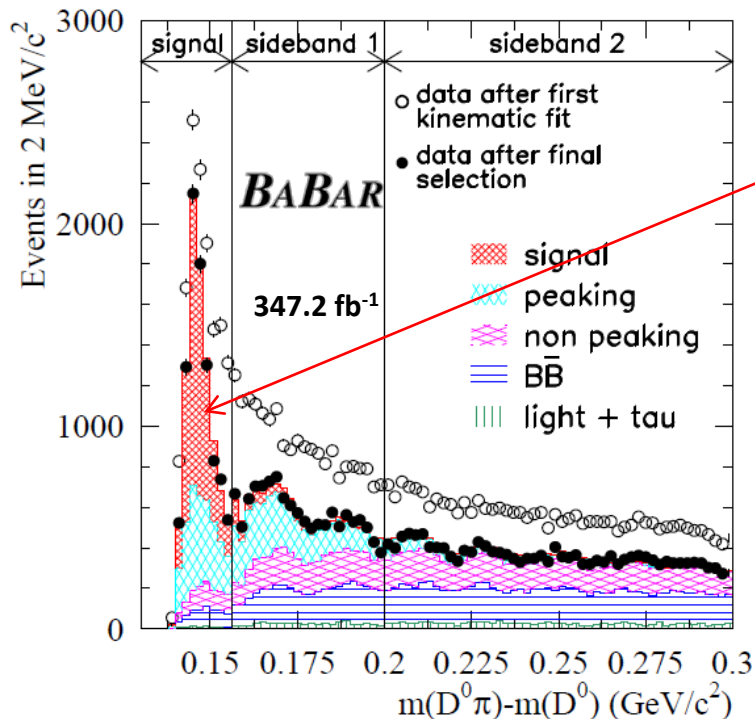
- The background is reduced using Fisher discriminant variables

- F_{bb} : against $B\bar{B}$ events (event shape)
- F_{cc} : against non-signal $c\bar{c}$ events (additional tracks topology)

ϵ : 1.8%, $S/B \sim 1.2$



- Signal events selected in $\delta m = m_{D^{*+}} - m_{D^0}$



~ 10000 candidates
50 % background

Background sources:

- $B\bar{B}$ background
- Charm non-peaking (π not from D^*)
- Charm peaking (13 subcategories)
- Light quarks

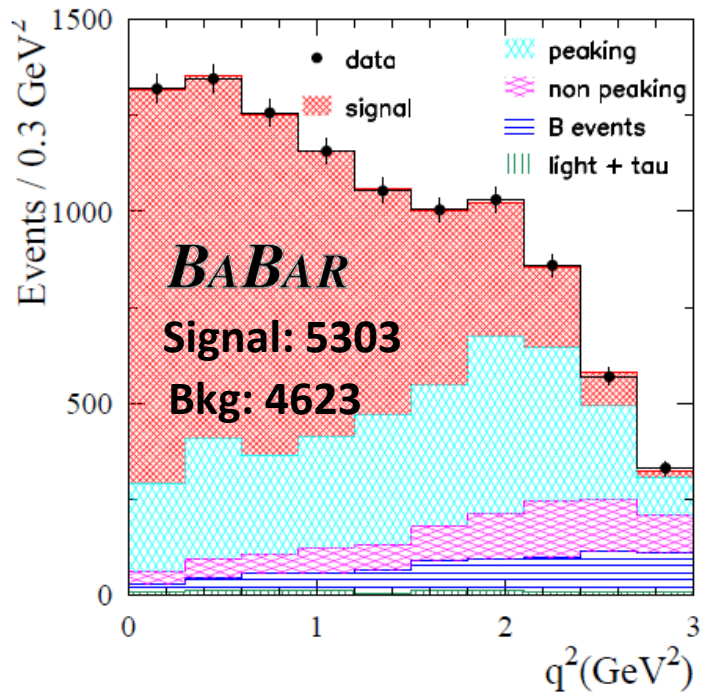
- Use $\delta m = m_{D^{*+}} - m_{D^0}$ sidebands from on-peak ($B\bar{B} + c\bar{c}$ +light) and off-peak (37fb^{-1} ; $c\bar{c}$ +light) data samples to determine the different backgrounds (fit E_{miss} vs p_π)

→ Main systematic uncertainty in the analysis assessed using data

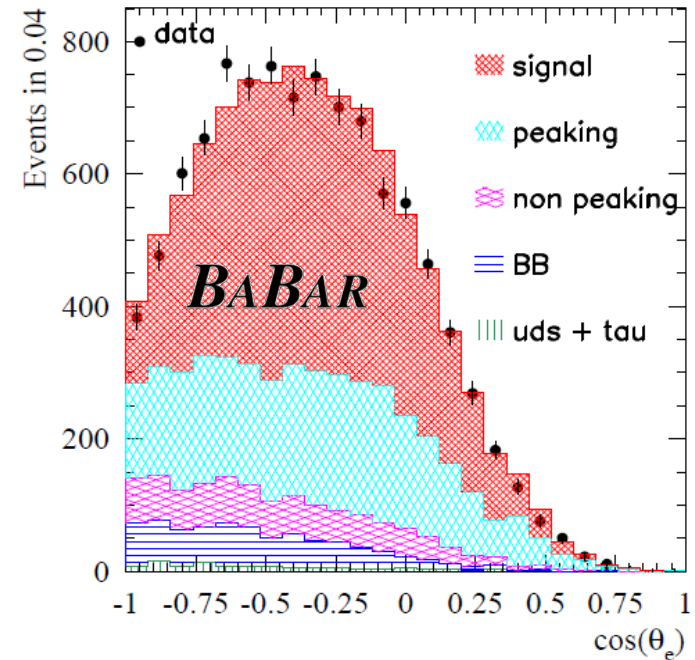
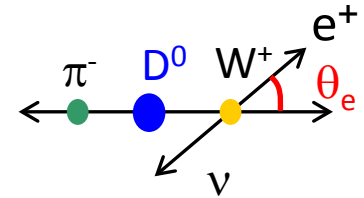
Analysis method

- The $q^2 = (\mathbf{p}_{D^0} - \mathbf{p}_{\pi})^2 = (\mathbf{p}_{e^+} + \mathbf{p}_{\nu})^2$ distribution is measured in 10 bins:

$$\delta m = m(D^0\pi) - m(D^0) < 0.150 \text{ GeV}$$



Cross-check: Pseudoscalar, known angular distribution



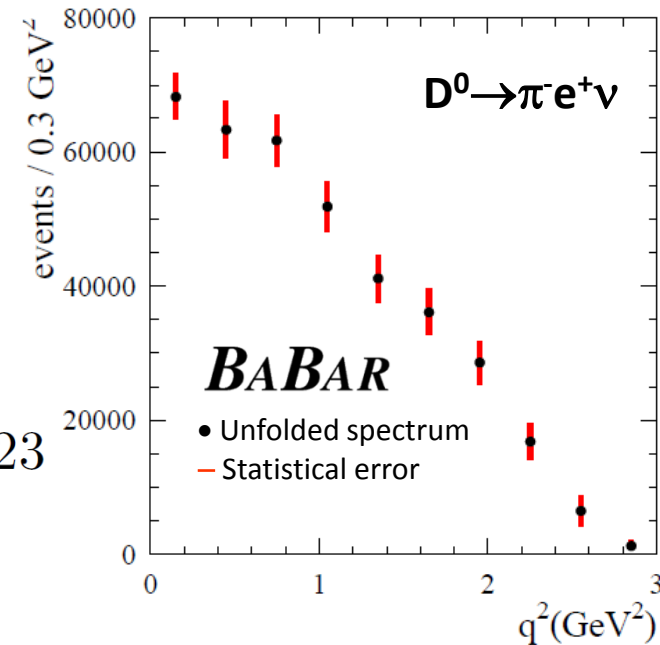
→ Resolution $\sigma(q^2) \sim 0.085 \text{ GeV}^2$ (50%) and 0.311 GeV^2 (50%)

Measurement of the Branching Fraction

- **Normalization: relative to the $D^0 \rightarrow K^- \pi^+$ decay channel**

- ▶ Try to have a selection as similar as possible for the $D^0 \rightarrow \pi^- e^+ \nu$ and $D^0 \rightarrow K^- \pi^+$ channels
- ▶ Measure $B(D^0 \rightarrow \pi^- e^+ \nu) / B(D^0 \rightarrow K^- \pi^+)$ in data and in MC
- ▶ From the unfolded number of signal events:

$$R_D = \frac{B(D^0 \rightarrow \pi^- e^+ \nu)_{data}}{B(D^0 \rightarrow K^- \pi^+)_{data}} = 0.0702 \pm 0.0017 \pm 0.0023$$



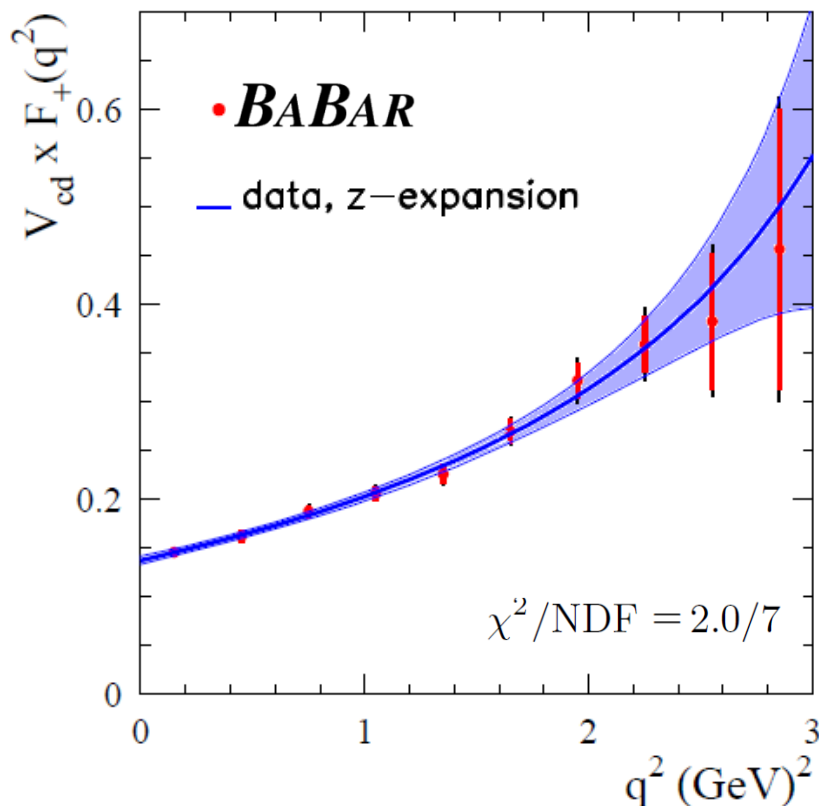
Using the world average for $BR(D^0 \rightarrow K^- \pi^+)$:

$$B(D^0 \rightarrow \pi^- e^+ \nu) = (2.770 \pm 0.068 \pm 0.092 \pm 0.037) \times 10^{-3}$$

PDG 2014 : $BR(D^0 \rightarrow \pi^- e^+ \nu) = (2.89 \pm 0.08) \times 10^{-3}$

Form factor interpretation

- Form factor fit in the z-expansion formalism:



z-expansion

$$F(t) = \frac{1}{P(t)\phi(t, t_0)} \sum_{k=0}^{\infty} a_k(t_0) z(t, t_0)^k$$

$$t \equiv q^2 \quad |z| \ll 1$$

$$z(t, t_0) = \frac{\sqrt{t_+ - t} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - t} + \sqrt{t_+ - t_0}} \quad t_0 = t_+(1 - \sqrt{1 - t_-/t_+})$$

$$t_{\pm} = (m_{D^0} \pm m_{\pi^+})^2$$

$$\sum_{k=0}^{\infty} a_k^2(t_0) \leq 1 \quad P(t)=1 \text{ for } D \rightarrow \pi e \nu$$

- Model independent, based on QCD properties
- a_k parameters (fitted) have no physics interpretation

Fitted parameters:

$$r_k = a_k/a_0 \quad \begin{cases} r_1 = -1.31 \pm 0.70 \pm 0.43 \\ r_2 = -4.2 \pm 4.0 \pm 1.9 \end{cases}$$

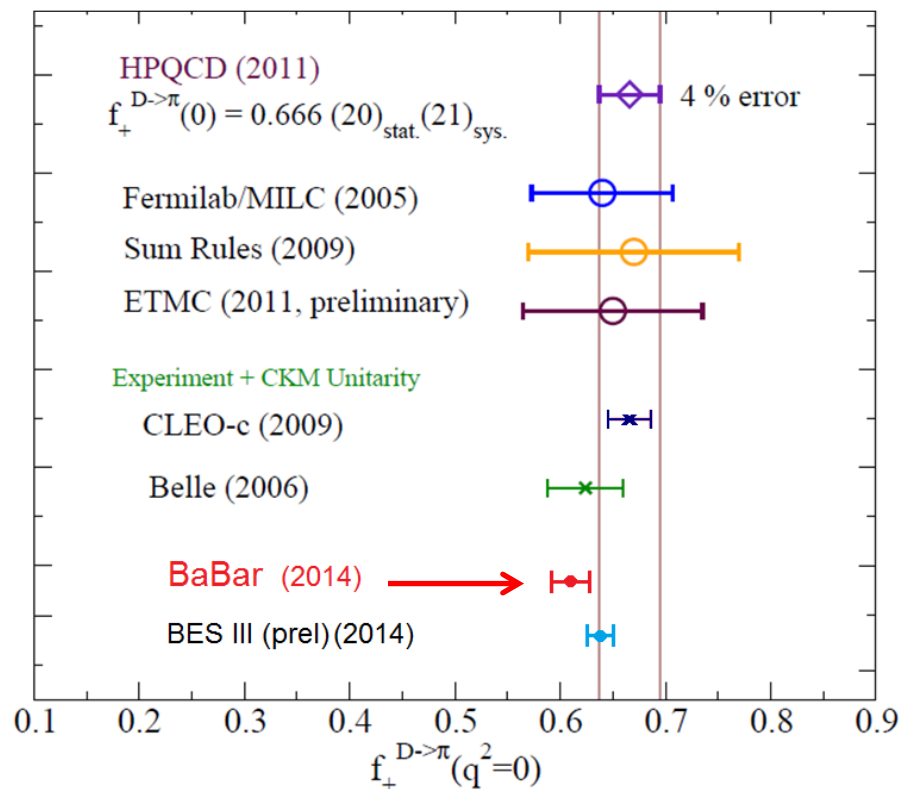
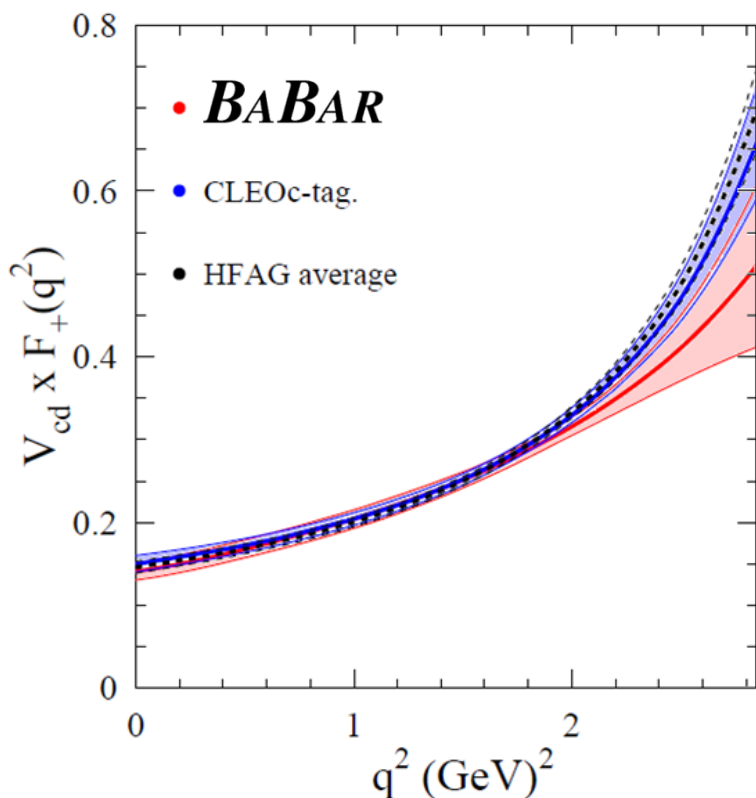
- Normalization:

$$|V_{cd}| f_{+,D}^{\pi}(0) = 0.1374 \pm 0.0038_{\text{stat.}} \pm 0.0022_{\text{syst.}} \pm 0.0009_{\text{ext.}}$$

Form factor interpretation

- Comparison with other results:

NEW Lattice 2015 (ETMC) $f_+(0)=0.610(23)(?)$
(N. Carrasco *et al.*)



$$|V_{cd}| = |V_{us}| = 0.2252 \pm 0.0009 \quad \longrightarrow$$

$$f_{+,D}^{\pi}(0) = 0.610 \pm 0.017 \pm 0.010 \pm 0.005$$

$$f_{+,D}^{\pi}(0) = 0.666 \pm 0.029 \quad \longrightarrow$$

$$|V_{cd}| = 0.206 \pm 0.007_{\text{exp.}} \pm 0.009_{\text{LQCD}}$$

Lattice average (arXiv:1310.8555)

Form factor interpretation

- Going further in the understanding of the form factor:

Burdman and Kambor [PRD55 (1997) 2817] (and before)

Becirevic and Kaidalov [PLB(2000) 417]

$$f_{+,H}^{\pi}(q^2) \simeq \sum_i \frac{\text{Res}(f_{+,H}^{\pi})_{H_i^*}}{m_{H_i^*}^2 - q^2}$$

being $H^* = D^*, D^{*'}, D^{*''}, \dots$ (or $B^*, B^{*'}, B^{*''}, \dots$) ($J^P=1^-$)

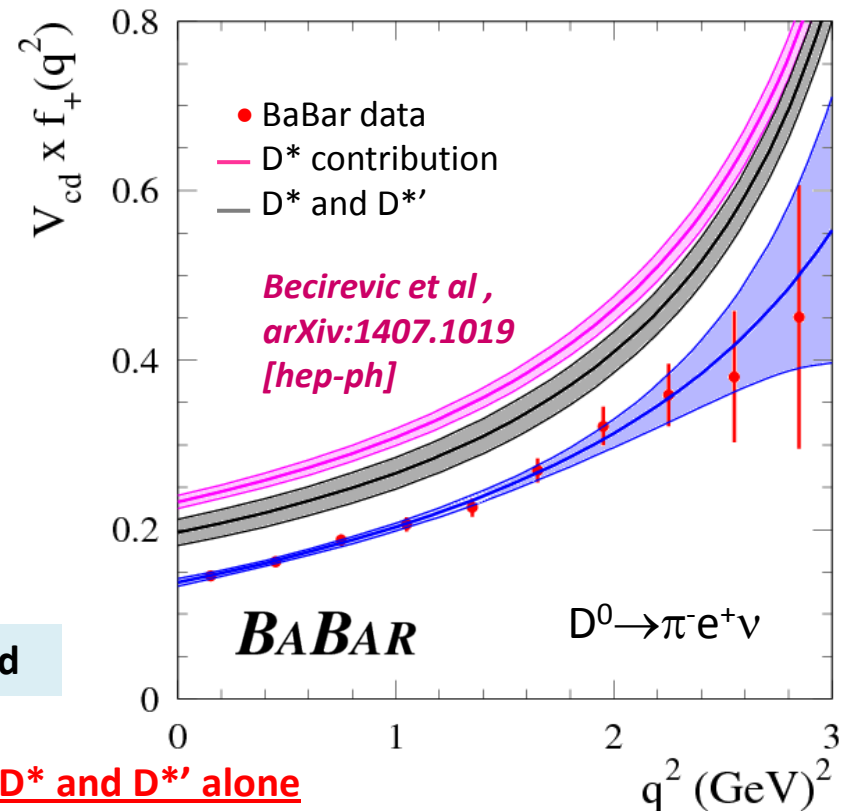
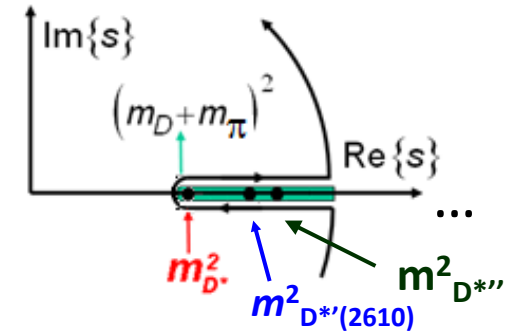
$$\text{Res}(f_{+,H}^{\pi})_{H^*} = \frac{1}{2} m_{H^*} f_{H^*} g_{H^* H \pi}$$

$f_{H^*}, g_{H^* H \pi}$ are the decay constant and coupling

- For $D^0 \rightarrow \pi^- e^+ \nu$: - $f_{D^*}, f_{D^{*'}}$ determined by Lattice
- $g_{H^* H \pi}, g_{H^{*'} H \pi}$ from $D^*, D^{*'}$ widths measured at BaBar

→ D^* and $D^{*'}$ contributions constrained

→ The form factor cannot be explained by the D^* and $D^{*'}$ alone

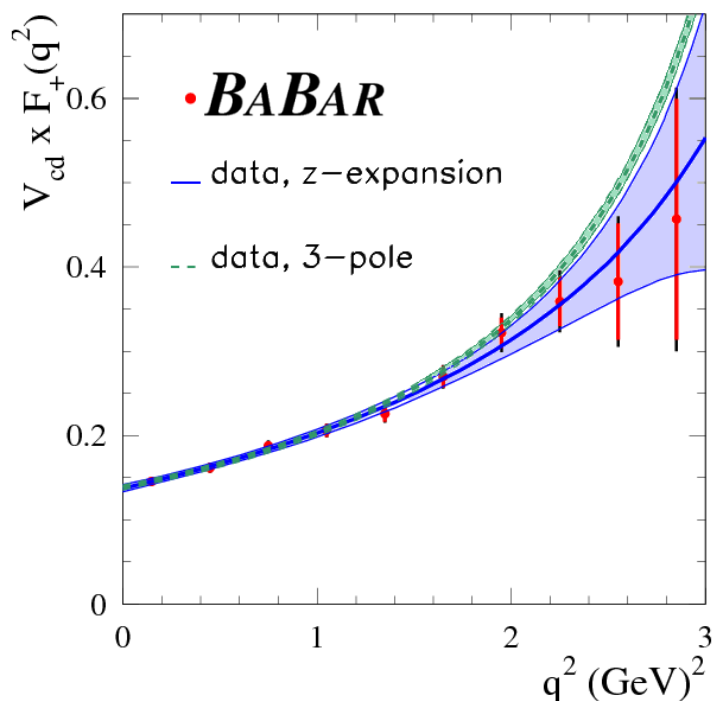


Form factor interpretation

“Three” poles ansatz (multipole) *Becirevic et al (arXiv:1407.1019 [hep-ph])*

$$f_{+,D}^{\pi}(q^2) = \frac{f_{+,D}^{\pi}(0)}{1 - c_2 - c_3} \left(\frac{1}{1 - \frac{q^2}{m_{D^*}^2}} - \sum_{i=2}^3 \frac{c_i}{1 - \frac{q^2}{m_{D_i^*}^2}} \right)$$

c_i given by the residues of the poles (relative to D^*) in terms of decay constants and couplings



Data is well described by this ansatz
if one fits a 3rd pole effective mass with the condition (*superconvergence*):

$$\sum_i \text{Res}(f_{+,D}^{\pi})_{D_i^{*(\prime)}} \simeq 0$$

$$m_{pole3} = (3.6 \pm 0.3) \text{ GeV}/c^2$$

→ larger than the predicted third $J^P=1^-$ state by quark models $\sim 3.1 \text{ GeV}$,
(as expected since it is effective)

→ a unique 3rd contribution from $m_{D^{*\prime}}=3.1 \text{ GeV}$ is excluded by data

Application: V_{ub} extraction

- Having measured $d\Gamma_{D \rightarrow \pi \ell \nu} / dq^2$ we can extract V_{ub} from the relation between the $D \rightarrow \pi \ell \nu$ and $B \rightarrow \pi \ell \nu$ channels:

Using $w_{B,D} = v_{B,D} \cdot v_{\pi} = E_{\pi}^* / m_{\pi}$ instead of q^2

$$w_{B,D} = \frac{M_{B,D}^2 + m_{\pi}^2 - q^2}{2M_{B,D}m_{\pi}}$$

At $w_B = w_D$:

$$\frac{d\Gamma(B \rightarrow \pi \ell \nu) / dw_B}{d\Gamma(D \rightarrow \pi \ell \nu) / dw_D} = \left| \frac{V_{ub}}{V_{cd}} \right|^2 \left(\frac{M_B}{M_D} \right) \left| \frac{f_+^{B \rightarrow \pi}}{f_+^{D \rightarrow \pi}} \right|^2$$

1) From Lattice
2) From a phenomenological model

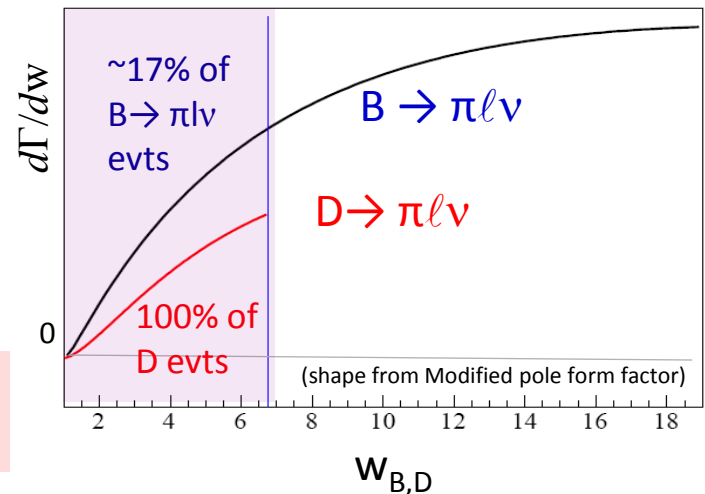
→ Kinematic factors cancel (same E_{π})

Experimentally, the common range in $w_{B,D}$

$$w_{B,D} \in [1, 6.7] :$$

$$q_D^2 \in [0; 2.975] \text{ GeV}^2$$

$$q_B^2 \in [18; 26.4] \text{ GeV}^2$$



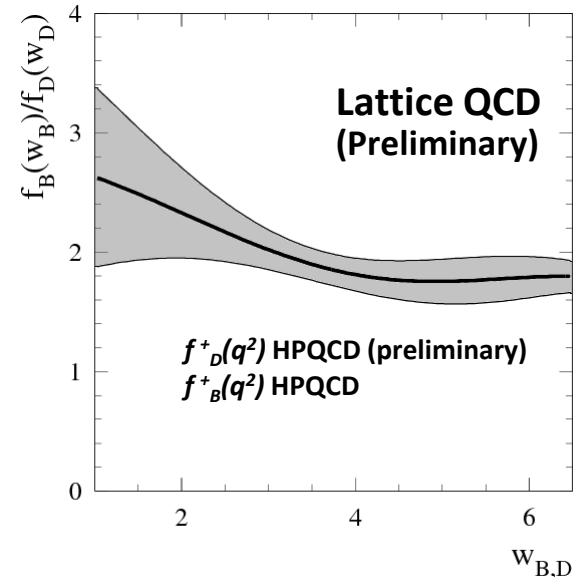
A physics interpretation of the charm form factor may allow to use it outside the D physical region

→ Aim to extract V_{ub} with a different approach, different uncertainties

Application: V_{ub} extraction

- 1) V_{ub} extraction (from Lattice):

- Using BaBar $D^0 \rightarrow \pi^- e^+ \nu$ and $B^0 \rightarrow \pi^- e^+ \nu$ data
- the “three” poles form factor fitted on $D^0 \rightarrow \pi^- e^+ \nu$
- extrapolated to the unphysical region
- assuming a constant ratio of $f_B^+(w_B)/f_D^+(w_D)$

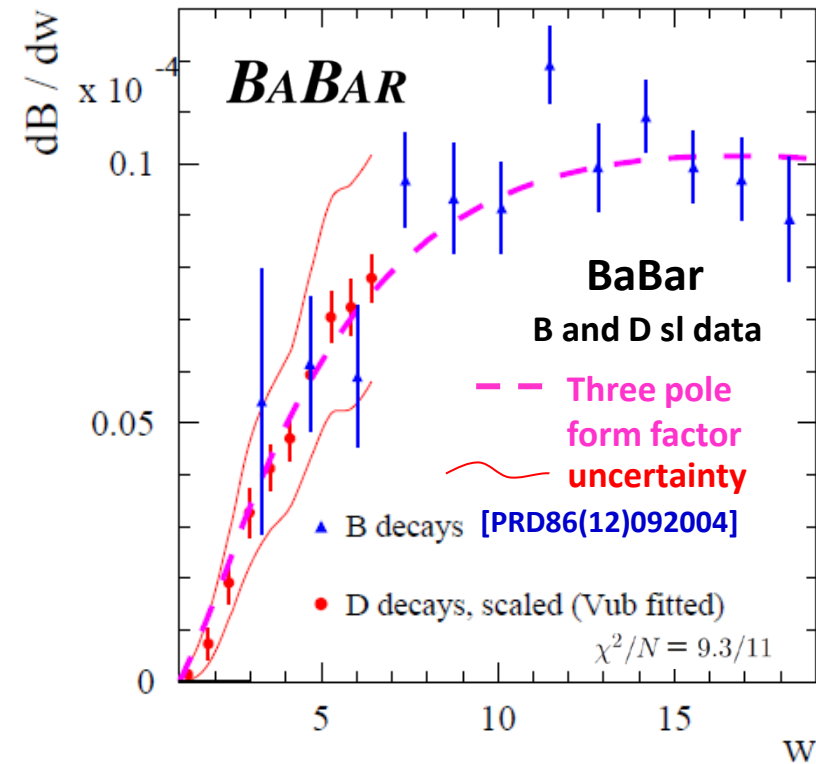


→ good fit for several considered ranges in w :
data are compatible with a constant $f_B(w_B)/f_D(w_D)$

$$|V_{ub}| = (3.65 \pm 0.18 \pm 0.40) \times 10^{-3}$$

Experimental \nearrow Form factor ratio = 1.8 ± 0.2

It can be improved by LQCD, providing values for this ratio with better accuracy and for several values of q^2 .



Application: V_{ub} extraction

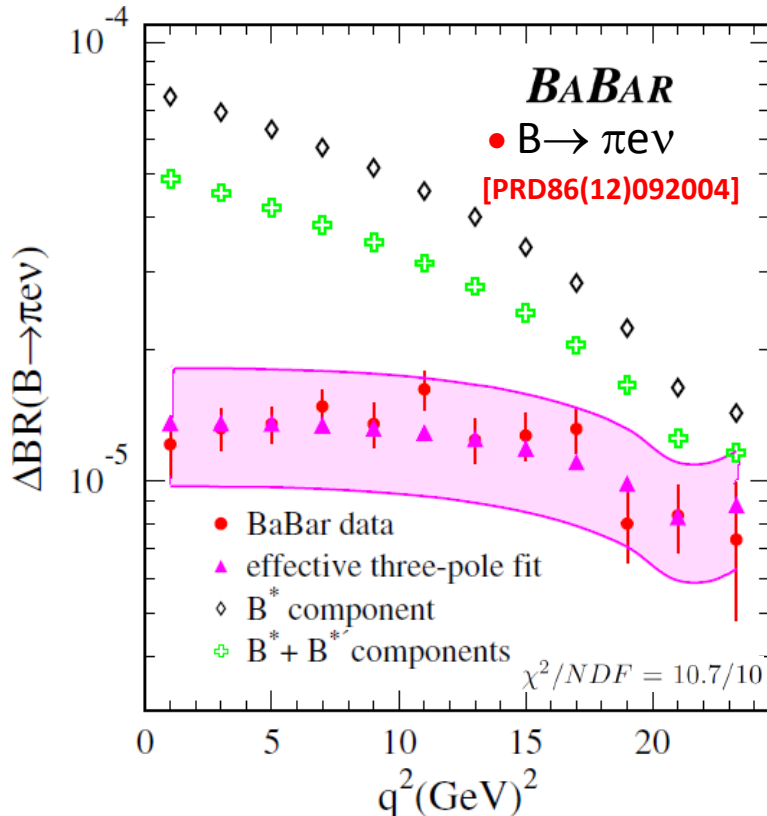
- **2) V_{ub} extraction (from the “three” poles model):**

[Becirevic et al, arXiv:1407.1019]

→ Having tested the “three” poles model in $D^0 \rightarrow \pi^- e^+ \nu$

→ We can use it for fitting only $B^0 \rightarrow \pi^- e^+ \nu$ data

→ Constraints from the residues of the first two poles (B^* , $B^{*'}$) and fitting the **third pole with an effective mass**



$$f_{+,B}^{\pi}(q^2) \simeq \sum_i \frac{\text{Res}(f_{+,B}^{\pi})_{B_i^*}}{m_{B_i^*}^2 - q^2}$$

Result on the third pole (effective):

$$m_{B^{*''}} = (7.4 \pm 0.4) \text{ GeV}/c^2$$

$$|V_{ub}| = (2.6 \pm 0.2 \pm 0.4) \times 10^{-3}$$

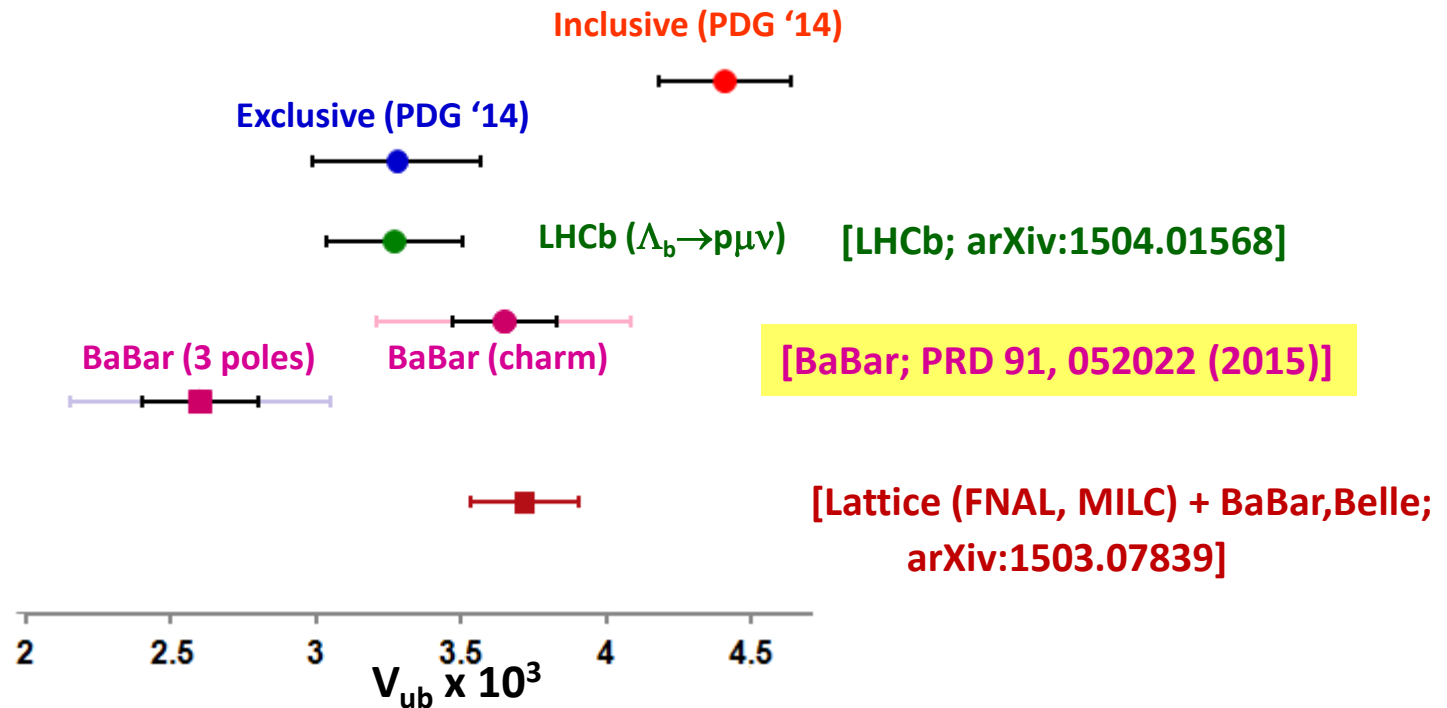
Experimental

$g_{H^*H\pi}$ couplings entering in the residues

It can be improved by Lattice QCD

Application: V_{ub} extraction

- Comparison with other V_{ub} determinations:



- BaBar systematics of different origin, expected to be reduced by Lattice calculations:

→ ● $f_B(q^2)/f_D(q^2)$ form factor ratio as function of E_π (or w)

→ ■ $g_{H^*H\pi}$ couplings

Conclusions

- **Measurement of the $D^0 \rightarrow \pi^- e^+ \nu_e$ form factor and branching fraction at BaBar, in agreement with CLEO-c, BELLE, and preliminary results from BES III.**

[Phys. Rev. D 91, 052022 (2015)]

$$|V_{cd}| f_{+,D}^{\pi}(0) = 0.1374 \pm 0.0038_{\text{stat.}} \pm 0.0022_{\text{syst.}} \pm 0.0009_{\text{ext.}}$$

$$\mathcal{B}(D^0 \rightarrow \pi^- e^+ \nu_e) = (2.770 \pm 0.068 \pm 0.092 \pm 0.037) \times 10^{-3}$$

→ Experimental results more accurate than Lattice calculations

- **Physics interpretation of the form factor:** [Becirevic *et al*, arXiv:1407.1019 [hep-ph]]
 - The form factor cannot be explained by the D^* and $D^{*'}$ contributions alone.
 - The description in terms of an **effective third-pole ansatz** agrees well with data.
- V_{ub} can be extracted using charm semileptonic data, using alternative approaches:
 - Using the constant form factor ratio from Lattice (assumed to be constant at present).
 - Using the “three” poles model

competitive when new lattice QCD calculations become available

Thank you!

B and D spectroscopy

- From Godfrey and Isgur [PRD32 (85)189]

$J^P = 1^-$ states

Measurement
(GeV)

Prediction: D mesons

(PDG) **2.0103(1)** → $m_0 = 2.037$ GeV (L=0)
 (BaBar) **2.609(4)** }
 (LHCb) **2.649(5)** } $m_1 = 2.645$ GeV (L=0)
 $m_2 = 2.816$ GeV (L=2)
 $m_3 = 3.11$ GeV (L=0)

$J^P = 1^-$ states

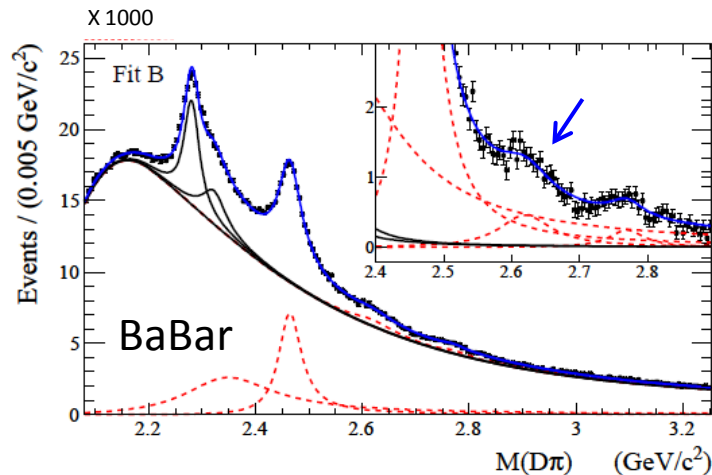
Measurement
(GeV)

Prediction: B mesons

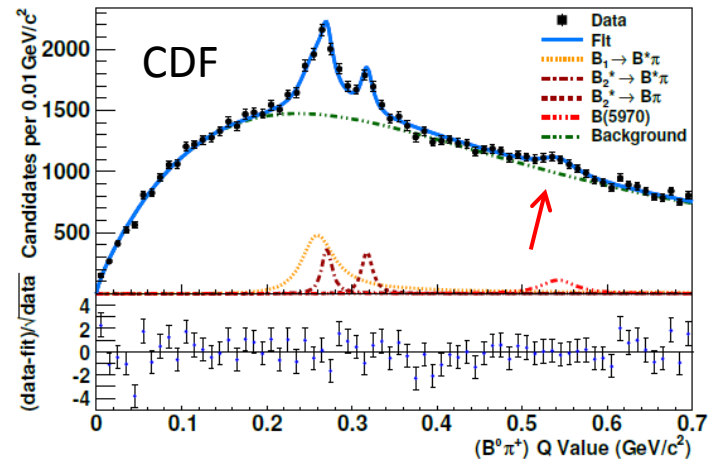
$m_0 = 5.37$ GeV (L=0) ← **5.325(1)** (PDG)
 $m_1 = 5.93$ GeV (L=0) ← **5.970(13)** (CDF)
 $m_2 = 6.11$ GeV (L=2)
 $m_3 = 6.355$ GeV (L=0) (A. Le Yaouanc)

→ Lowest lying state: D^* , B^*

→ Radially excited states: observed by BaBar and LHCb ($D^{*'}$), and CDF ($B^{*'}$)



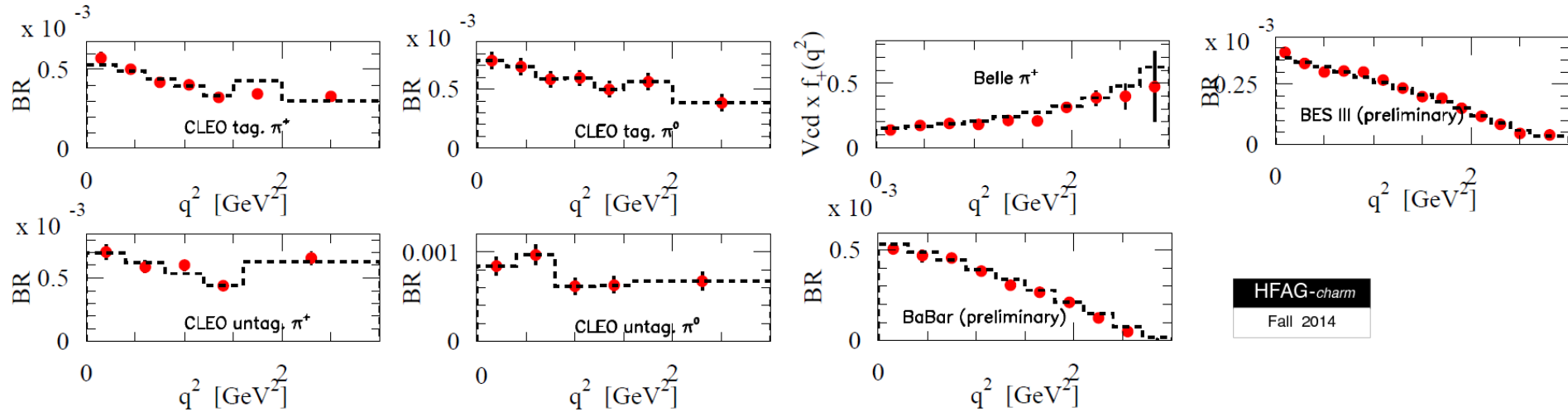
[PRD82(10)111101]



[arXiv:1309.5961 [hep-ex]]

Form factor interpretation

"Three" poles ansatz (multipole) *Becirevic et al (arXiv:1407.1019 [hep-ph])*



HFAG-*charm*
Fall 2014

It works well for all experimental data.