

Z'-induced FCNC Decays of Top, Beauty and Strange Quarks


$$t \rightarrow c Z'$$

Masaya Kohda
(Chung Yuan Christian Univ., Taiwan)

Based on works with:

Kaori Fuyuto (Nagoya U.), Wei-Shu Hou (Nat'l Taiwan U.)
[PRL114, 171802, and work in progress]

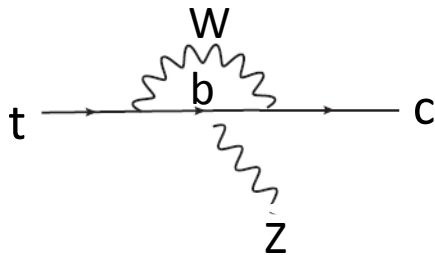
EPS HEP 2015 @ Vienna, July 24, 2015

Introduction

- Rare decays of top quark are good probes to see New Physics

1) Flavor Changing Neutral Current (FCNC) decays

ex.) $t \rightarrow c Z$, $t \rightarrow c h$



◆ Tiny SM rate due to

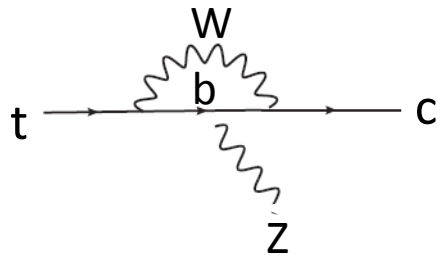
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- CKM suppression
- GIM (perfectly works)

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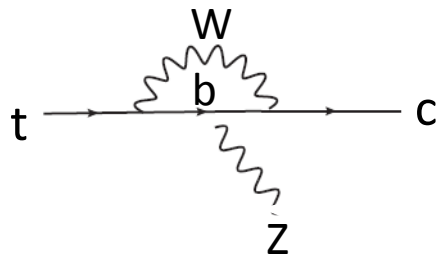
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3) New particle production in top FCNC decay

$t \rightarrow c Z'$ Z' : new massive gauge boson

Hints from B physics

- $b \rightarrow s \mu^+ \mu^-$ transitions are being precisely measured at LHC
- Overall agreement with SM, but two tantalizing hints

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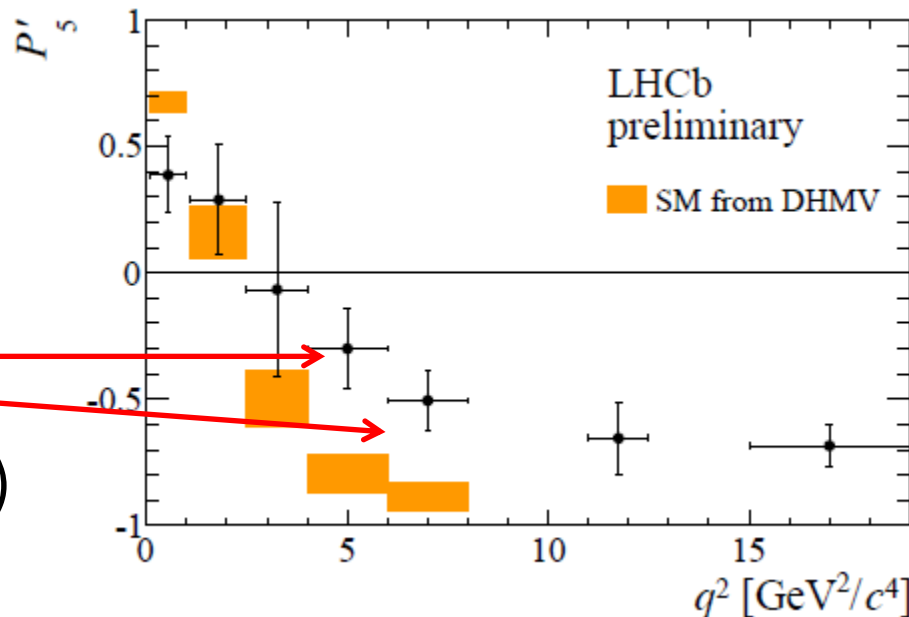
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1) P_5' anomaly in $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ decay angular distribution

LHCb, PRL 111, 191801 (2013) [1/fb]; LHCb-CONF-2015-002 [3/fb]

➤ P_5' : a form-factor free observable made from angular coefficients

➤ measured spectrum:
($q^2 = m_{\mu\mu}^2$)



2.9 σ tensions

--> 3.7 σ tension (combo)

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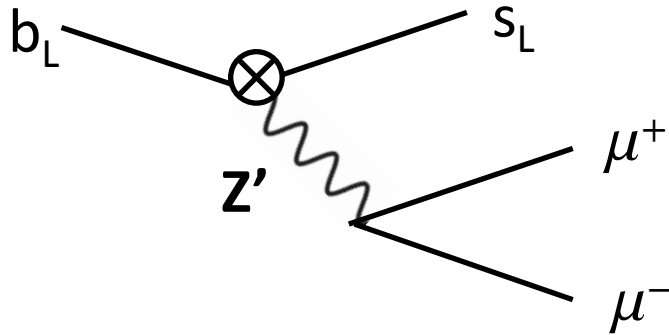
$$R_K = \frac{\Gamma(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\Gamma(B^+ \rightarrow K^+ e^+ e^-)} = 0.745_{-0.074}^{+0.090}(\text{stat}) \pm 0.036(\text{sys})$$

➤ 2.6σ deviation from SM: $R_K^{SM} = 1 + \mathcal{O}(\frac{m_\mu^2}{m_b^2})$

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- Both anomalies can be nicely explained by adding New Physics contribution to C_9 for muon, but not for electron
 - C_9 : Wilson coefficient in $\mathcal{H}_{\text{eff}} \supset C_9 (\bar{s} \gamma_\alpha P_L b) (\bar{\mu} \gamma^\alpha \mu)$
 - A global analysis tells: $\Delta C_9 \simeq -\frac{1}{(34 \text{ TeV})^2}$ ($\sim -25\%$ of SM)
Altmannshofer and Straub, 1411.3161

A new muon-specific gauge boson Z'

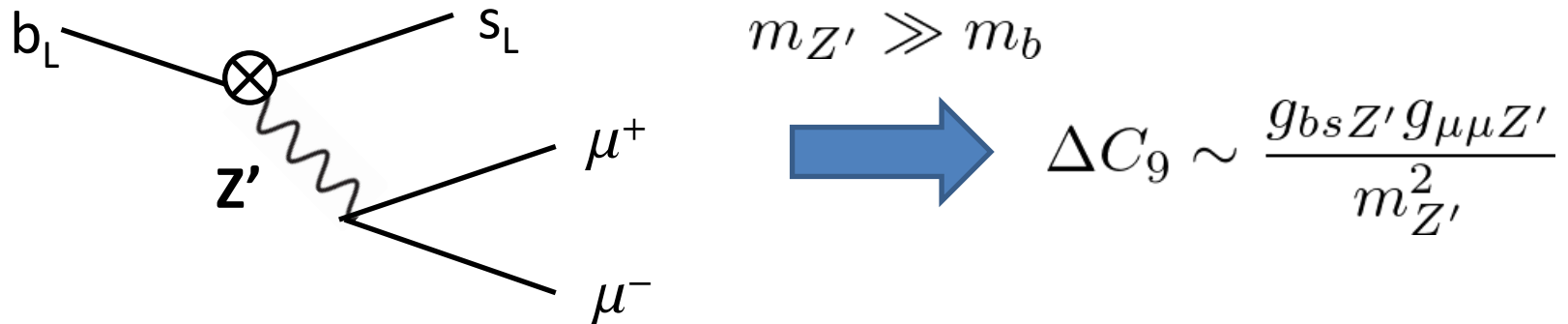


$$m_{Z'} \gg m_b$$



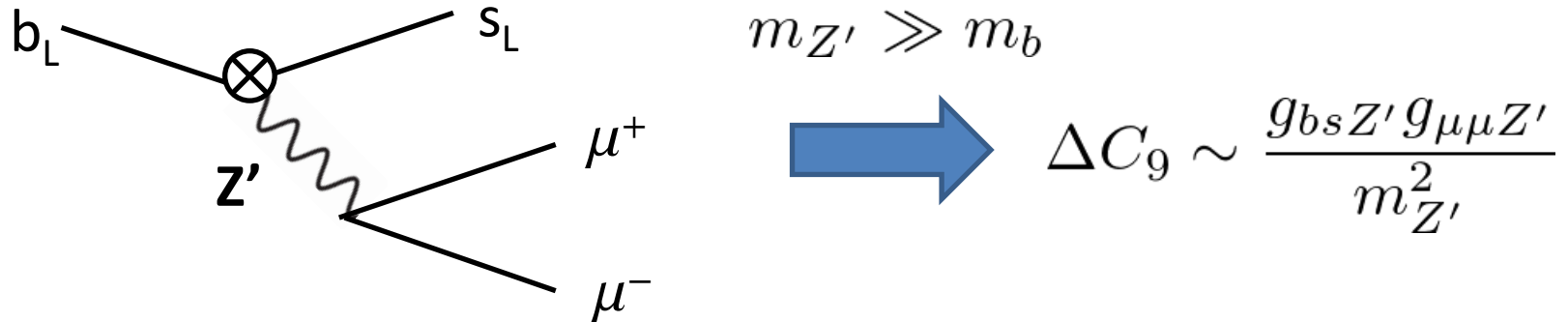
$$\Delta C_9 \sim \frac{g_{bsZ'} g_{\mu\mu Z'}}{m_{Z'}^2}$$

A new muon-specific gauge boson Z'



- A nice candidate is a Z' boson of gauged $L_\mu - L_\tau$ symmetry (μ -number minus τ -number) [Altmannshofer et al., PRD89, 095033\(2014\)](#)
- anomaly free [He, Joshi, Lew and Volkas, PRD43,22\(1991\)](#)

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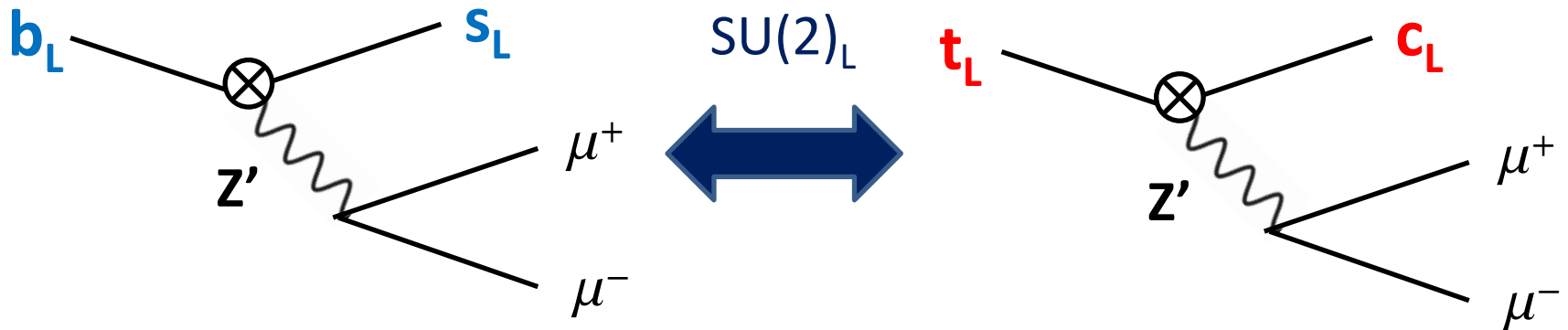
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 - anomaly free [He, Joshi, Lew and Volkas, PRD43,22\(1991\)](#)
 - Z' may couple to $b \rightarrow s$ current via higher dim. operator including $U(1)'$ Higgs field Φ

$$\frac{i}{\Lambda^2} (\Phi^* \overleftrightarrow{D}_\alpha \Phi) (\bar{s} \gamma^\alpha P_L b) \quad \longrightarrow \quad -\frac{g' v_\Phi^2}{\Lambda^2} Z'_\alpha \bar{s} \gamma^\alpha P_L b$$

$\langle \Phi \rangle = v_\Phi / \sqrt{2}$

“ $b \rightarrow s$ ” to “ $t \rightarrow c$ ”

- Nonzero $b_L s_L Z'$ coupling implies nonzero $t_L c_L Z'$



- If $m_{Z'} < m_t - m_c$, the 2-body decay $t \rightarrow c Z'$ can happen!
 - This mass range is compatible with experimental data in the gauged $L_\mu - L_\tau$ model

Altmannshofer et al., PRD89, 095033(2014)

Plan of this talk

- Introduction
- The explicit mode for bsZ' and tcZ' couplings
- $t \rightarrow c Z'$ for $m_{Z'} \gg m_b$ (motivated by P_5' and R_K)
- $t \rightarrow c Z'$ for $m_{Z'} \ll m_b$ (motivated by muon $g-2$)
- Discussion and summary

The model for bsZ' and tcZ' coupling

Altmannshofer, Gori, Pospelov and Yavin, PRD89, 095033(2014)

New matter fields

$U(1)'$ Higgs

$$\Phi : (\mathbf{1}, \mathbf{1})_0$$

Vector-like quarks

$$Q : (\mathbf{3}, \mathbf{2})_{+1/6} \quad U : (\mathbf{3}, \mathbf{1})_{+2/3} \quad D : (\mathbf{3}, \mathbf{1})_{-1/3}$$

$$Q_{U(1)'} = +1$$

$$+1$$

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- Q mixes with SM quarks via

$$\mathcal{L}_{\text{int}} \supset Y_{Qq_i} \Phi \bar{Q}_R q_{iL}$$

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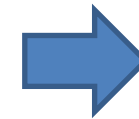
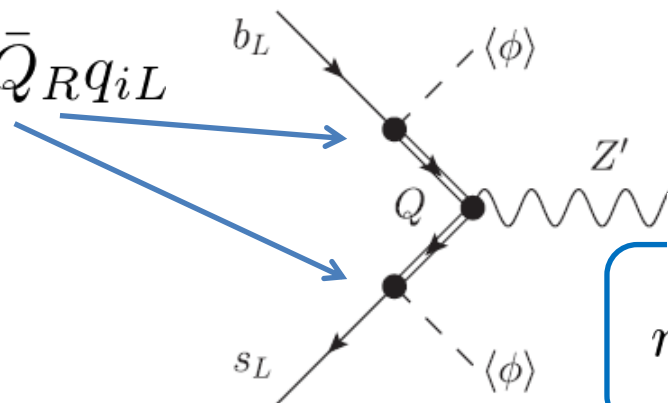
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$$\Delta C_9 \simeq \frac{Y_{Qs}^* Y_{Qb}}{2m_Q^2}$$

P_5' & R_K anomalies

$$m_Q \simeq 24 \text{ TeV} \times |Y_{Qb} Y_{Qs}^*|^{1/2}$$

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Two major constraints on the model

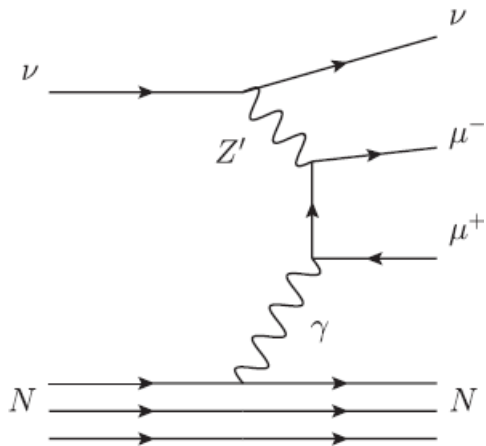
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1) Neutrino Trident Production: $\nu N \rightarrow \nu N \mu^+ \mu^-$

Altmannshofer, Gori, Pospelov and Yavin, PRL113, 091801(2014)



$$\propto \frac{g'^2}{m_{Z'}^2} = \frac{1}{v_{\Phi}^2}$$

CCFR experiment

PRL66, 3117 (1991)

$$v_{\Phi} \gtrsim 540 \text{ GeV}$$

N.B.: $m_{Z'} \gtrsim 10 \text{ GeV}$ is assumed

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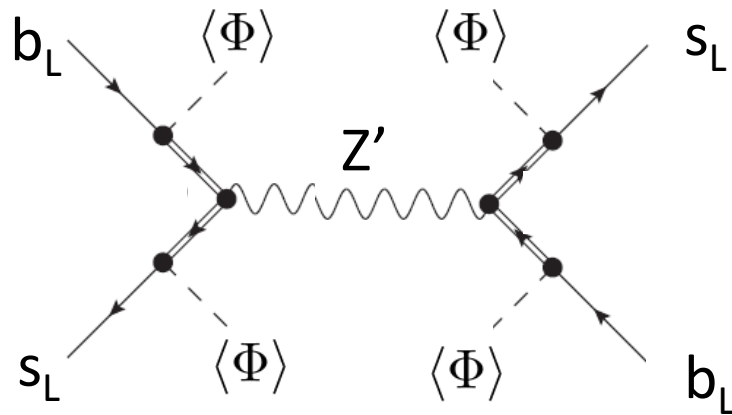
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2) B_s mixing:

Altmannshofer et al. (2014); Crivellin et al. (2015)

P_5' & R_K anomalies

$$\frac{|Y_{Qs}^* Y_{Qb}|}{2m_Q^2} \simeq \frac{1}{(34 \text{ TeV})^2}$$



$$\propto \frac{(Y_{Qs}^* Y_{Qb})^2}{m_Q^4} v_\Phi^2$$

➤ Demanding NP effect < 15%

$$v_\Phi \lesssim 5.6 \text{ TeV}$$

Naïve experimental sensitivity for $t \rightarrow c Z'$

- A similar process $t \rightarrow c Z(\rightarrow l^+ l^-)$ was searched at LHC in

$$t\bar{t} \rightarrow qZ(\rightarrow \ell^+ \ell^-) + bW(\rightarrow \ell\nu) \quad (\ell = e, \mu, \tau)$$

- The 95% CL upper limits for $t \rightarrow q Z$ ($q = c, u$):

- CMS (full Run1) [PRL112, 171802\(2014\)](#)

$$\mathcal{B}(t \rightarrow qZ) < 5 \times 10^{-4}$$

- ATLAS (2.1/fb, 7TeV) [JHEP1209.139](#)

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$$\mathcal{B}(Z' \rightarrow \ell^+ \ell^-) \simeq 2/3 \quad \gg \quad \mathcal{B}(Z \rightarrow \ell^+ \ell^-) \simeq 3 \times 3.4\% \simeq 10\%$$

(for $m_{Z'} > 2m_\tau$)

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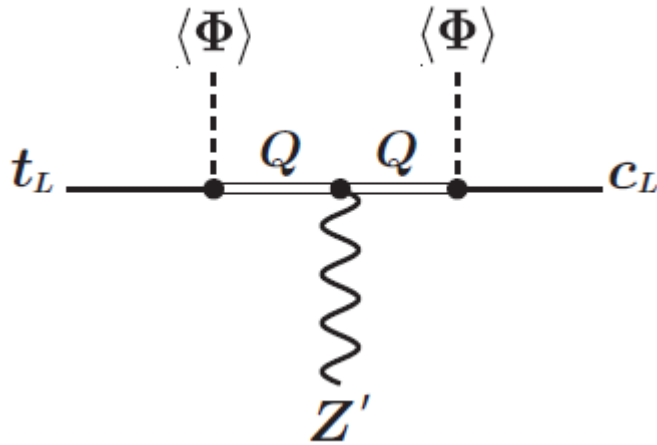
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- Naïve expectation for CMS sensitivity on $t \rightarrow c Z'$

$$\mathcal{B}(t \rightarrow cZ') \lesssim 8 \times 10^{-5} \quad \longrightarrow \quad \lesssim 2 \times 10^{-6}$$

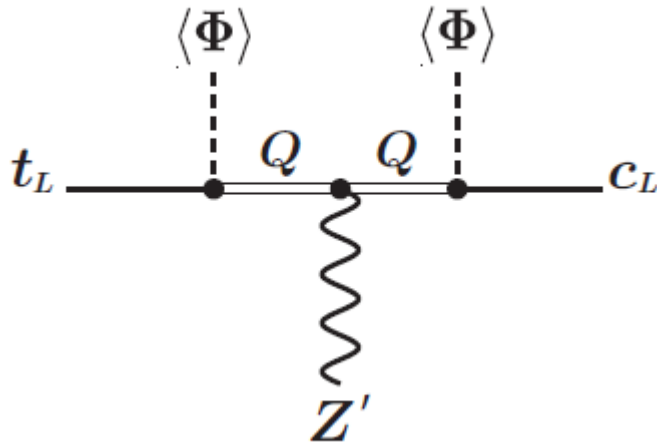
$t \rightarrow c Z'$ rate predicted by P_5' & R_K



$$\mathcal{B}(t \rightarrow c Z')_{\text{LH}} \simeq \frac{(1 - x')^2 (1 + 2x')}{2(1 - x_W)^2 (1 + 2x_W)} \frac{|Y_{Qt} Y_{Qc}^*|^2}{4m_Q^4} v^2 v_\Phi^2$$

$$\text{with } x' = \frac{m_{Z'}^2}{m_t^2} \quad x_W = \frac{m_W^2}{m_t^2}$$

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P_5' & R_K anomalies

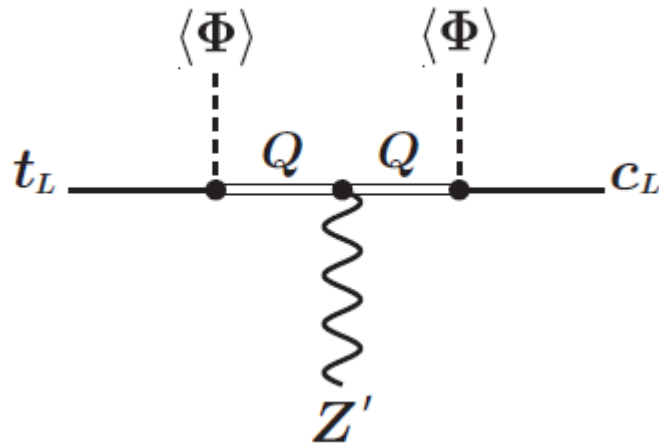
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- Applying constraints on v_Φ ,

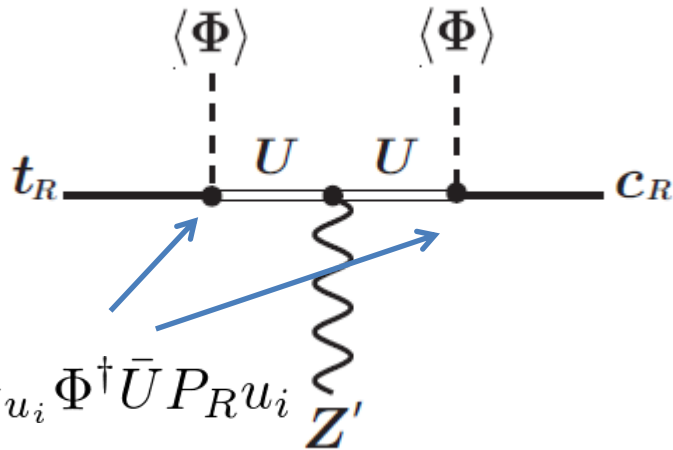
$$\text{with } x' = \frac{m_{Z'}^2}{m_t^2} \quad x_W = \frac{m_W^2}{m_t^2}$$

$$0.8 \times 10^{-8} \lesssim \mathcal{B}(t \rightarrow c Z')_{\text{LH}} \lesssim 0.8 \times 10^{-6}$$

slightly below CMS (300/fb)

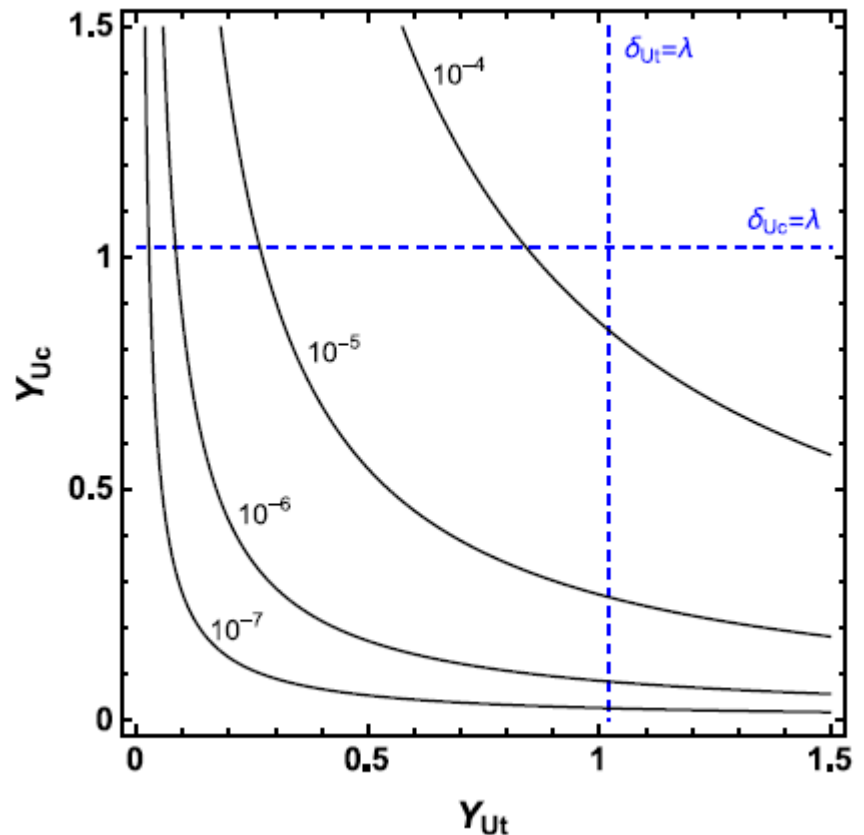
$t \rightarrow c Z'$ via RH current

- Right-Handed tcZ' coupling, mediated by SU(2) singlet quark U, is unconstrained by $b \rightarrow s$ data



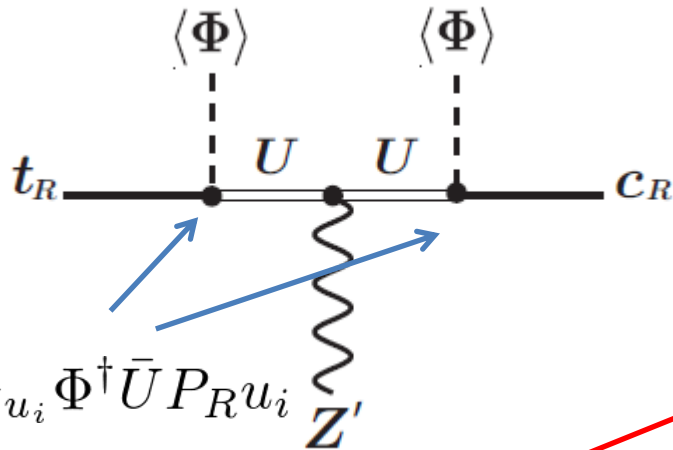
$$\mathcal{L}_{\text{int}} \supset Y_{Uu_i} \Phi^\dagger \bar{U} P_R u_i Z'$$

- BR($t \rightarrow c Z'$) contours for $m_{Z'} = 50$ GeV, $g' = 0.064$, $v_\Phi = 780$ GeV, $m_U = 2.5$ TeV

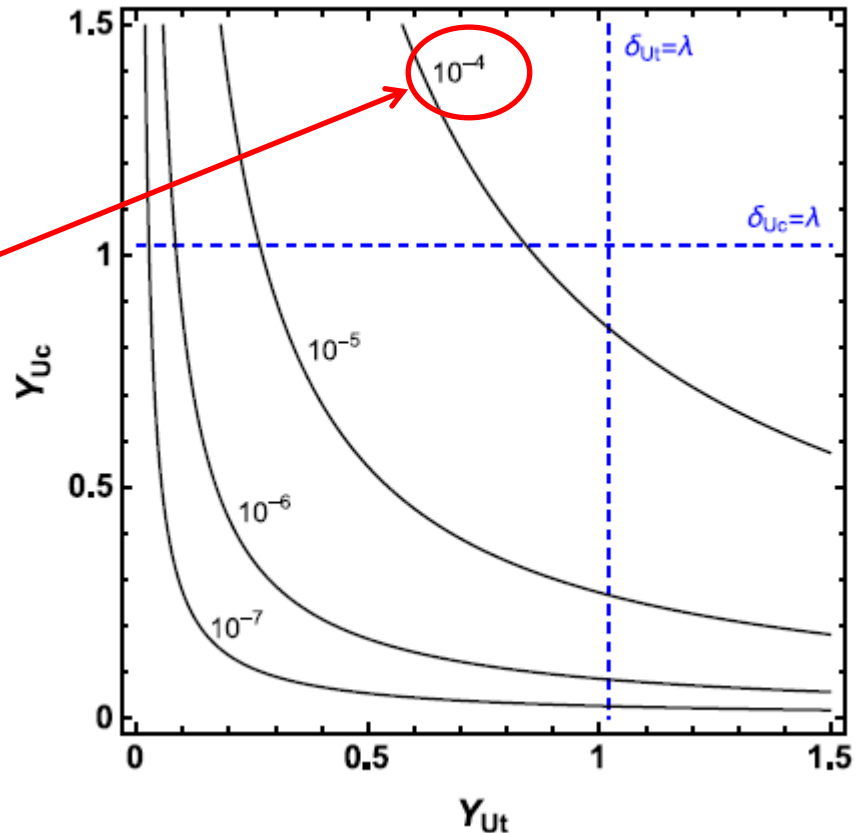


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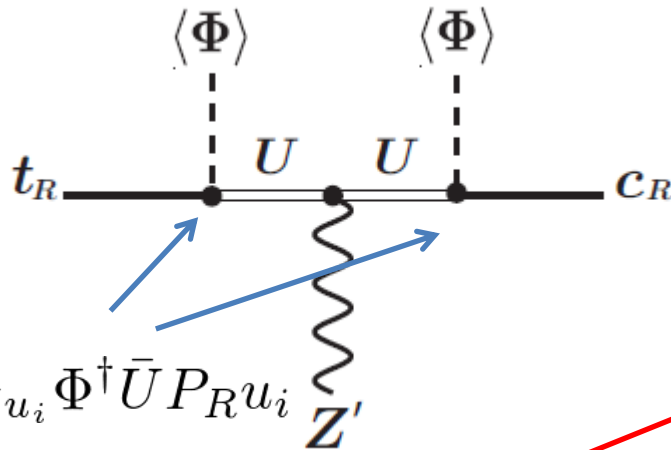


- BR($t \rightarrow c Z'$) $\sim 10^{-4}$ is possible, but not more to keep **small mixing angle** for U-t and U-c

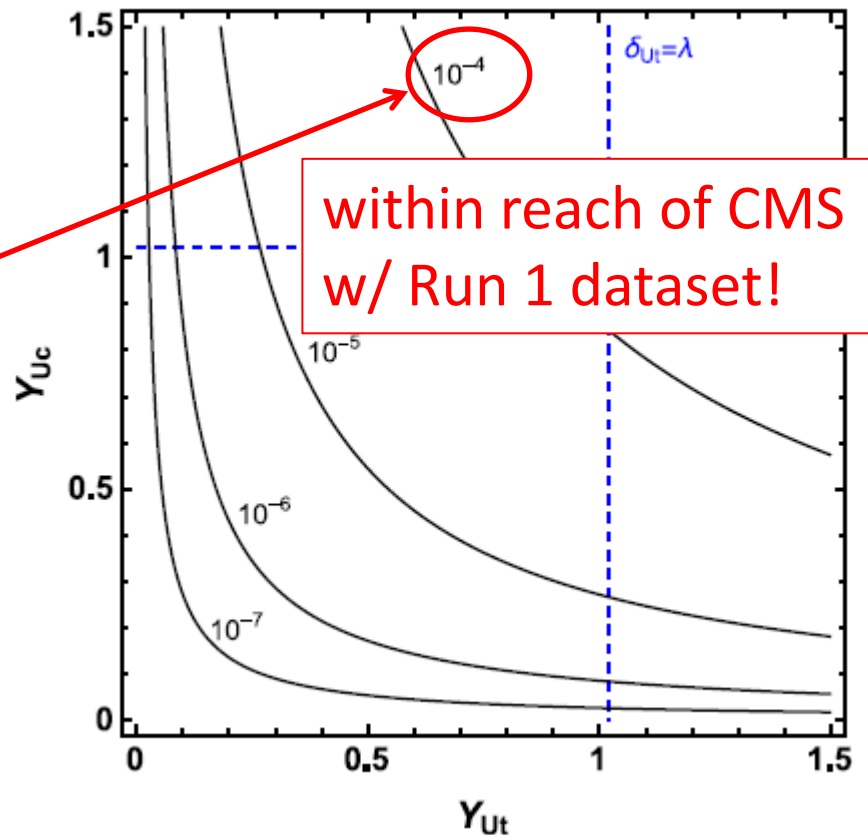
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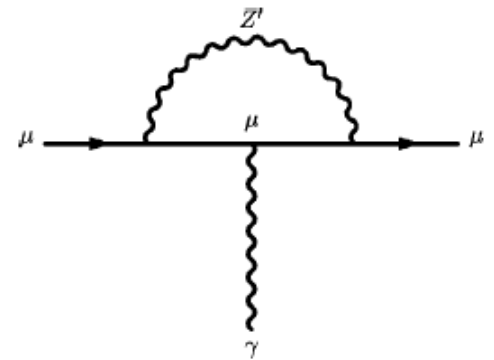
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What if the Z' is extremely light?

- Cannot explain P_5' and R_K anomalies
- But, motivated by the muon $g-2$ anomaly

Baek, Deshpande, He and Ko (2001)

$$m_{Z'} \ll m_b$$



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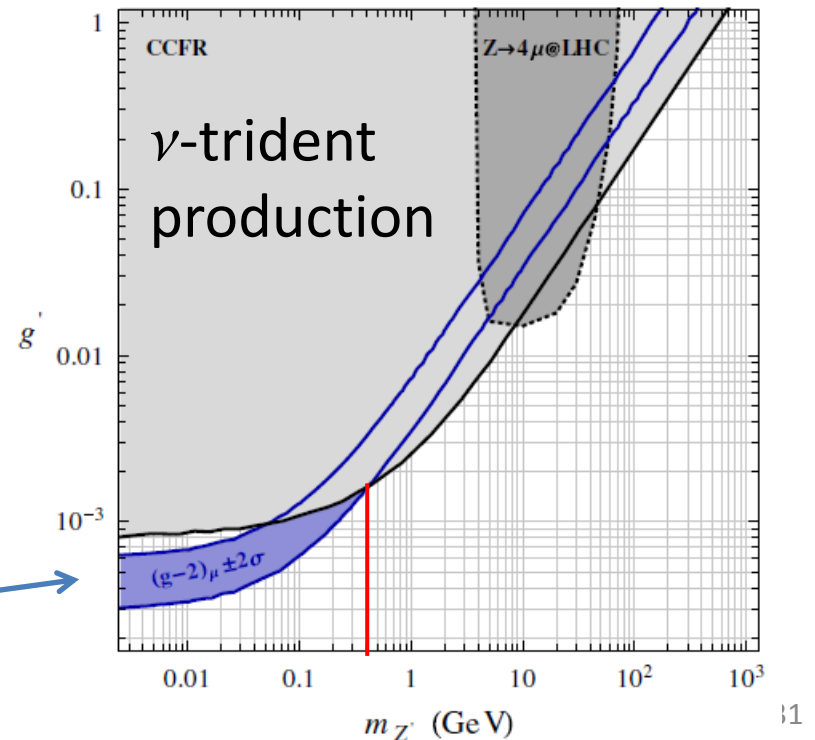
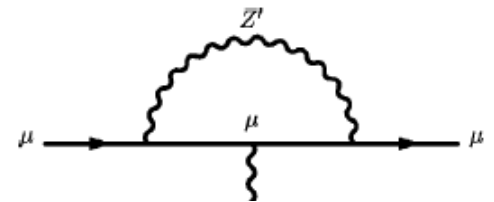
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- The Z' can explain the anomaly only if

$$m_{Z'} \lesssim 400 \text{ MeV}$$

Altmannshofer et al., PRL113, 091801(2014)

favored by $(g-2)_\mu$



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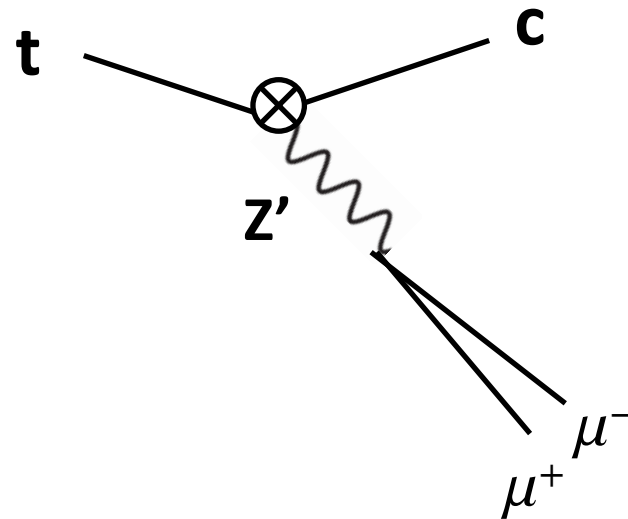
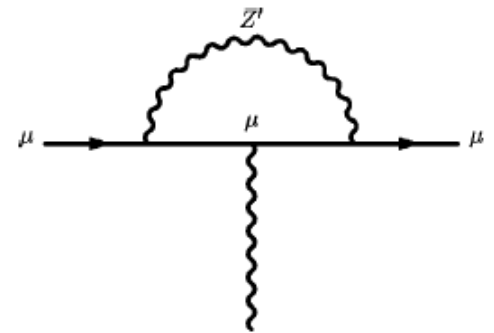
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- Striking collider signature:
muon pairs from $t \rightarrow c Z'$
are collimated

$$m_{Z'} \ll m_b$$

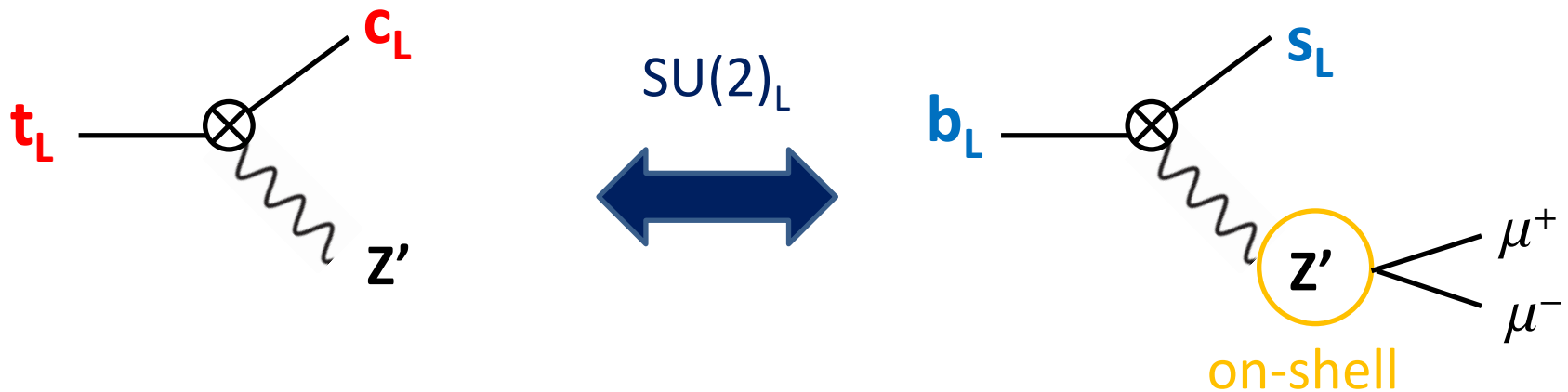
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Muon g-2 motivated $t \rightarrow c Z'$ via LH current

- For the light Z' , left-handed tcZ' coupling is strongly constrained, as $b \rightarrow s \mu^+ \mu^-$ goes through the 2-body decay $b \rightarrow s Z' (\rightarrow \mu^+ \mu^-)$, with on-shell Z' , and LH bsZ' coupling is tightly bounded



- B-factories and LHCb data imply

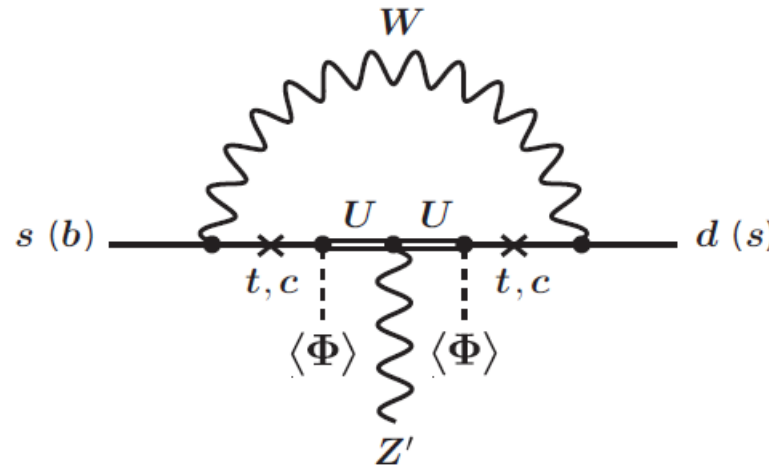
$$\mathcal{B}(t \rightarrow c Z')_{\text{LH}} \lesssim 2 \times 10^{-14} \quad \leftarrow \text{far below CMS (300/fb)}$$

Fuyuto, Hou and MK, in preparation

Muon $g-2$ motivated $t \rightarrow c Z'$ via **RH** current

Fuyuto, Hou and MK, arXiv:1412.4397

- For the light Z' , the right-handed tcZ' coupling is also constrained by meson decays
- At one-loop, U - t and U - c mixing induces effective bsZ'/sdZ' coupling



- The loop suppression is compensated by the two-body enhancement in the B and K decays, e.g., $B \rightarrow K Z' (\rightarrow \mu\mu)$

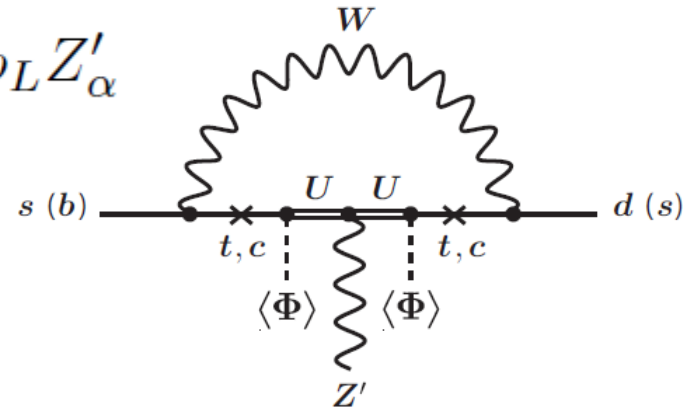
Loop-induced bsZ'/sdZ' couplings

- Some assumptions:

- For simplicity, the mixings with Q, D quarks are turned off
- U-u mixing is also turned off to satisfy D-meson mixing/decay constraints

- Loop induced bsZ' coupling: $g_{sb}\bar{s}_L\gamma^\alpha b_L Z'_\alpha$

$$g_{sb} = \frac{g'v_\Phi^2}{32\pi^2 v^2} [c_{cc}f_{cc} + (c_{tc} + c_{ct})f_{ct} + c_{tt}f_{tt}]$$



with $c_{ij} = V_{ib}V_{js}^* Y_{Ui}Y_{Uj}^* m_i m_j / m_U^2$

$$\begin{cases} f_{ct} \simeq 1 + \log \frac{m_U^2}{m_t^2} + \frac{3m_W^2}{m_t^2 - m_W^2} \log \frac{m_t^2}{m_W^2}, & f_{tt} \simeq \frac{3m_W^2}{m_t^2 - m_W^2} \left(1 - \frac{m_W^2}{m_t^2 - m_W^2} \log \frac{m_t^2}{m_W^2} \right) + \log \frac{m_U^2}{m_t^2}, \\ f_{cc} \text{ is obtained by } m_c^2 \ll m_W^2 \end{cases}$$

Relevant measurements for $b \rightarrow s Z'$ & $s \rightarrow d Z'$

Bottom FCNC decays

[mass range]

- Binned $B^+ \rightarrow K^+ \mu^+ \mu^-$ spectrum by LHCb (1/fb, 7 TeV) [JHEP1302.105](#) $m_{Z'} \gtrsim 224 \text{ MeV}$

N.B.: Full Run1 results by LHCb cover only the half of $(g-2)_\mu$ region ($m_{Z'} > 316 \text{ MeV}$)

[JHEP1406.133](#)

- $B^+ \rightarrow K^* X(\rightarrow \mu^+ \mu^-)$ search by Belle [PRL105, 091801\(2010\)](#) $m_{Z'} \in (212, 300) \text{ MeV}$
- Binned $B \rightarrow K^{(*)} \nu \nu$ search by BaBar [PRD87, 112005\(2013\)](#) $m_{Z'} \geq 0$

Strange FCNC decays

- Binned $K^+ \rightarrow \pi^+ \mu^+ \mu^-$ spectrum by NA48/2 [PLB697, 107\(2011\)](#) $m_{Z'} \in (211, 354) \text{ MeV}$
- $K_L \rightarrow \pi^0 \mu^+ \mu^-$ search by KTeV [PRL84, 5279\(2000\)](#) $m_{Z'} \in (211, 350) \text{ MeV}$
- $K^+ \rightarrow \pi^+ X(\rightarrow \nu \nu)$ search by E949 [PRD79, 092004\(2009\)](#) $m_{Z'} \in (0, 125) \text{ or } (150, 260) \text{ MeV}$
- $K_L \rightarrow \pi^0 \nu \nu$ search by E391a [PRD81, 072004\(2010\)](#) $m_{Z'} \lesssim 363 \text{ MeV}$

Relevant measurements for $b \rightarrow s Z'$ & $s \rightarrow d Z'$

Bottom FCNC decays

[mass range]

- Binned $B^+ \rightarrow K^+ \mu^+ \mu^-$ spectrum by LHCb (1/fb, 7 TeV) [JHEP1302.105](#) $m_{Z'} \gtrsim 224 \text{ MeV}$

N.B.: Full Run1 results by LHCb cover only the half of $(g-2)_\mu$ region ($m_{Z'} > 316 \text{ MeV}$)

[JHEP1406.133](#)

- $B^+ \rightarrow K^* X(-)$ $m_{Z'} \gtrsim 100 \text{ MeV}$
- Binned $B \rightarrow K \mu^+ \mu^-$
 - Z' with mass around m_π can evade K^+ decay experiments, while it is sensed by K_L decay
 - This leads to the apparent violation of Grossman-Nir bound [Fuyuto, Hou and MK, PRL114, 171802](#)
 - See talk by W.-S. Hou in flavor session (7/24, 11:50~)

Strange FCNC

- Binned $K^+ \rightarrow \pi^+ \mu^+ \mu^-$ $m_{Z'} \gtrsim 100 \text{ MeV}$
- $K_L \rightarrow \pi^0 \mu^+ \mu^-$ search by KTeV [PRL84, 5279\(2000\)](#) $m_{Z'} \in (211, 350) \text{ MeV}$
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- $K_L \rightarrow \pi^0 \nu \nu$ search by E391a [PRD81, 072004\(2010\)](#) $m_{Z'} \lesssim 363 \text{ MeV}$

Constraint from $B^+ \rightarrow K^+ \mu^+ \mu^-$

- Z' would show up as a spike in $q^2 = m_{\mu\mu}^2$ distribution
- 1 fb⁻¹ result of LHCb probes down to

$$q^2 > 0.05 \text{ GeV}^2 \simeq (224 \text{ MeV})^2 \quad \text{JHEP 02 (2013) 105}$$

target range

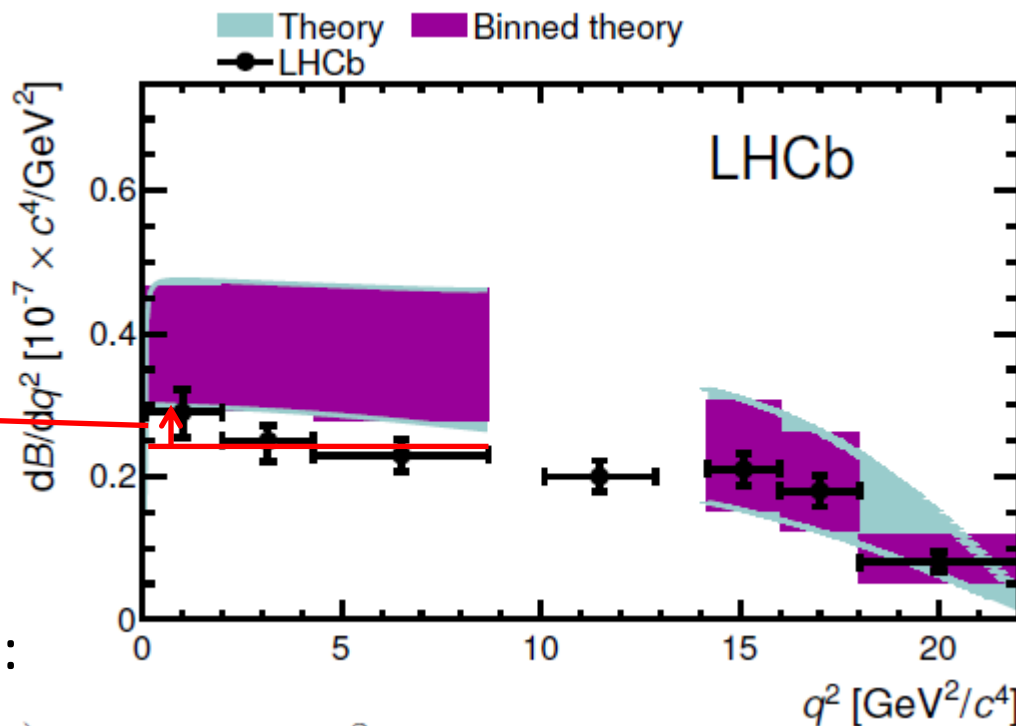
$$q^2 \in (0.05, 2.00) \text{ GeV}^2$$

$$m_{Z'} \in (224, 1414) \text{ MeV}$$

$$\Delta\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-) = (0.86 \pm 0.59) \times 10^{-8}$$

- We obtain 2 σ upper limit:

$$\mathcal{B}(B^+ \rightarrow K^+ Z') \mathcal{B}(Z' \rightarrow \mu^+ \mu^-) < 2.04 \times 10^{-8}$$



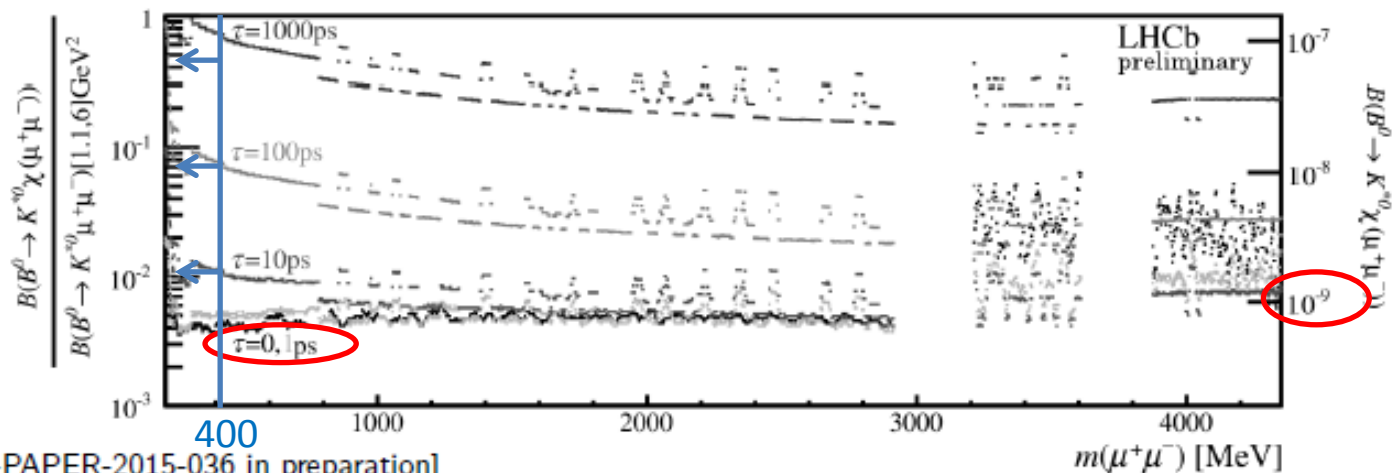
$B^0 \rightarrow K^{*0} \chi(\rightarrow \mu\mu)$ search by LHCb

Talk by A. Mauri in this conference

Exclusion limit

No deviation from the background only hypothesis is observed

- We set a 95% CL upper limit as function of mass and lifetime of the new particle (in the LHCb accessible range)
- The new particle is assumed to be a scalar
- Lower lifetimes have better limit due to higher reconstruction efficiency



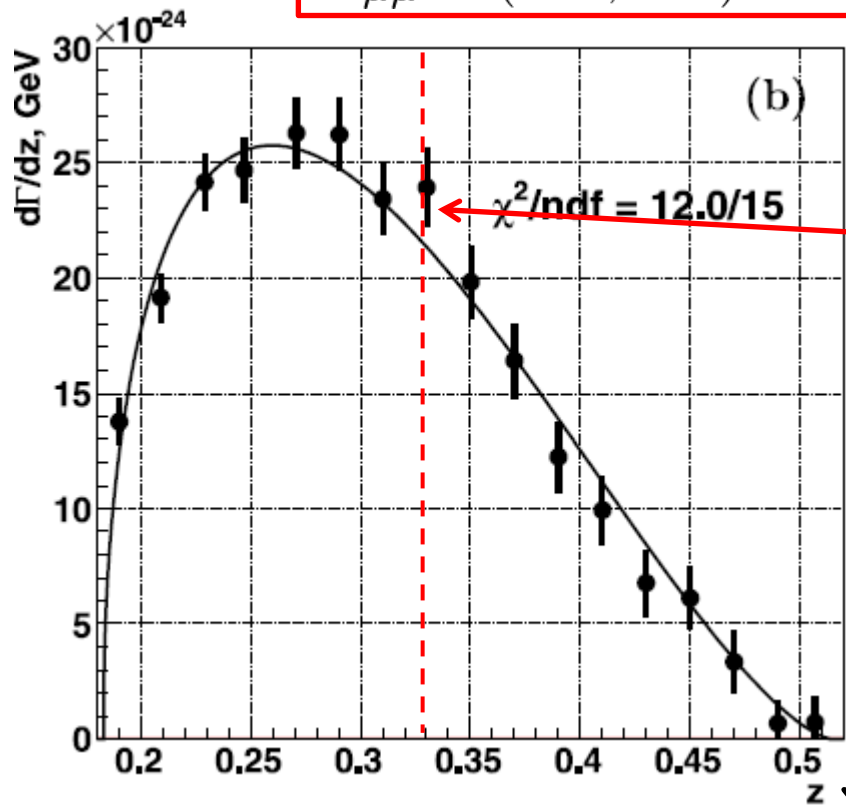
[LHCb-PAPER-2015-036 in preparation]

Constraint from $K^+ \rightarrow \pi^+ \mu^+ \mu^-$

- NA48/2@CERN SPS: most precise single measurement

$$m_{\mu\mu} \in (279, 288) \text{ MeV}$$

PLB697, 107(2011)



- take most tolerant case

$$\Delta\mathcal{B}(K^+ \rightarrow \pi^+ \mu^+ \mu^-) \simeq (9.4 \pm 5.6) \times 10^{-10}$$

- We obtain 2σ upper limit:

$$\mathcal{B}(K^+ \rightarrow \pi^+ Z') \mathcal{B}(Z' \rightarrow \mu^+ \mu^-) < 2.1 \times 10^{-9}$$

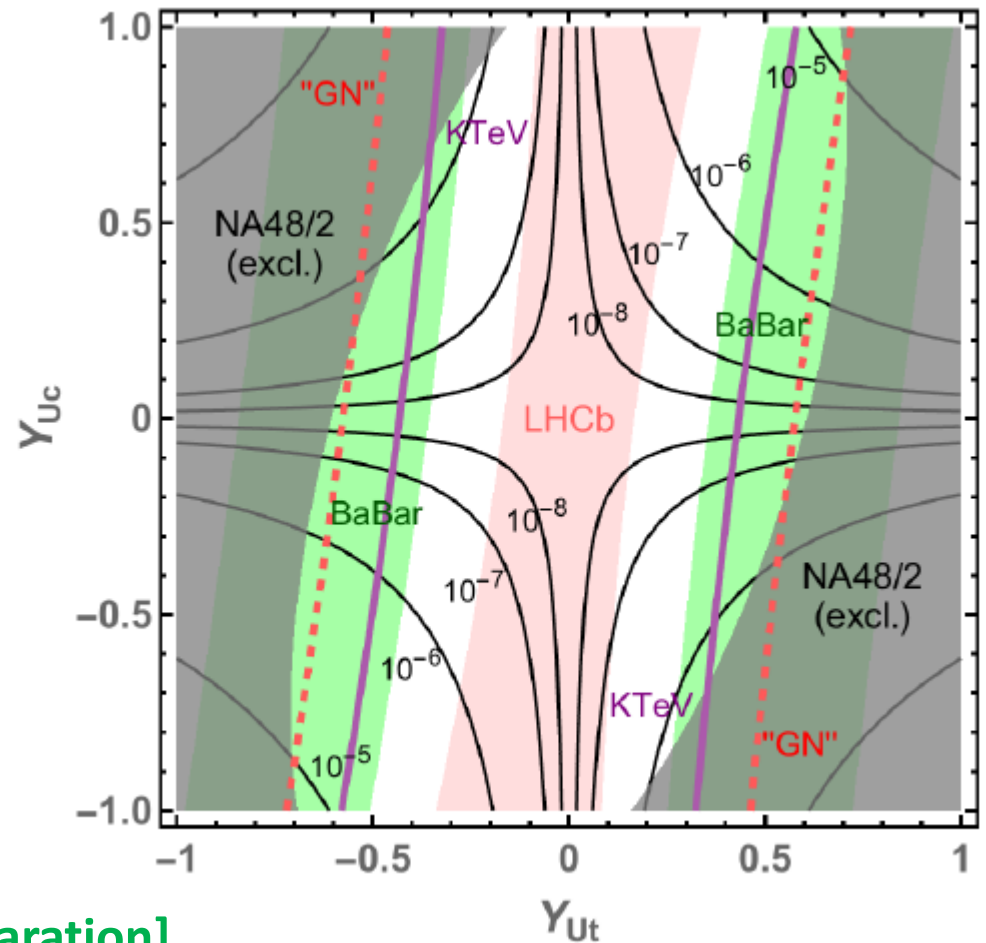
$$z \equiv q^2/m_{K^+}^2$$

- fit by linear form factor $W(z) = G_F M_K^2 f_0(1 + \delta z)$

Constraints on Y_{Ut} and Y_{Uc}

$$Y_{Uu_i} \Phi^\dagger \bar{U} P_R u_i$$

Benchmark $m_{Z'} = 285 \text{ MeV}$, $g' = 1.3 \times 10^{-3}$, $m_U = 2 \text{ TeV}$



[Fuyuto, Hou and MK, in preparation]

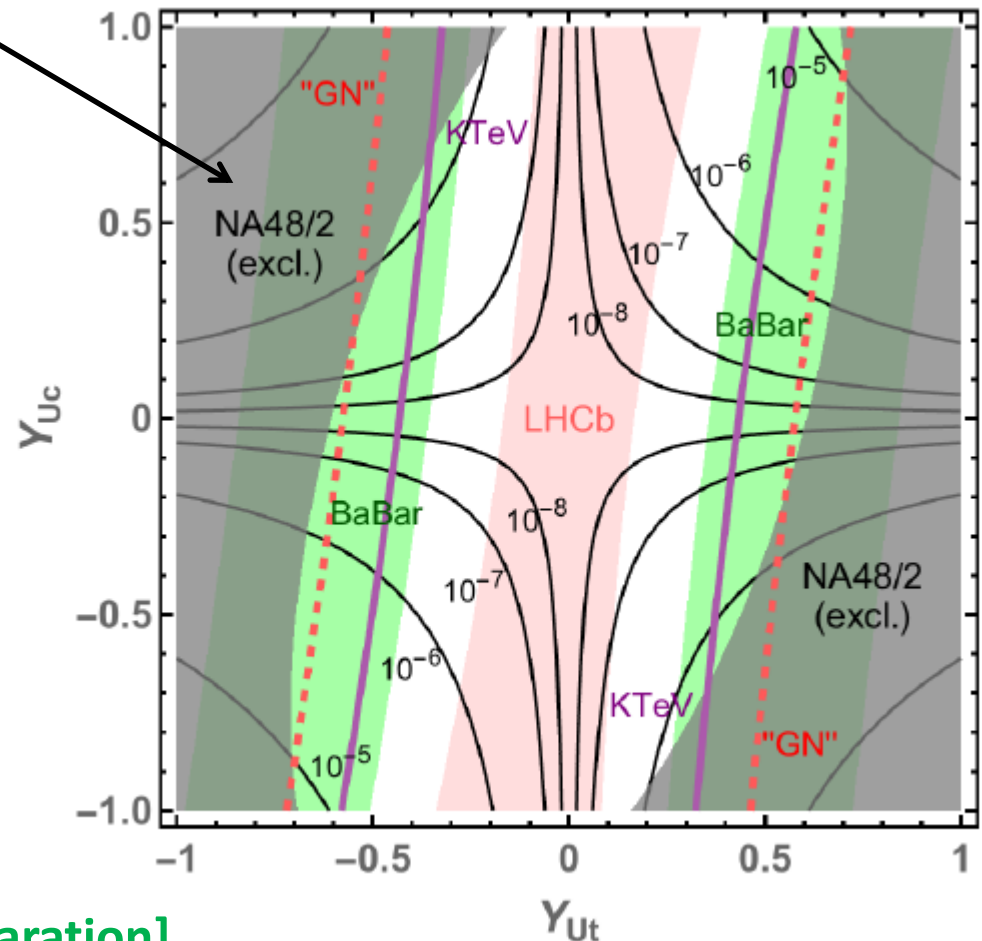
Constraints on Y_{Ut} and Y_{Uc}

$$Y_{Uu_i} \Phi^\dagger \bar{U} P_R u_i$$

Benchmark $m_{Z'} = 285 \text{ MeV}$, $g' = 1.3 \times 10^{-3}$, $m_U = 2 \text{ TeV}$

Excluded by $K^+ \rightarrow \pi^+ \mu^+ \mu^-$ at 2σ

➤ weakest at $m_{Z'} = 285 \text{ MeV}$



[Fuyuto, Hou and MK, in preparation]

Constraints on Y_{Ut} and Y_{Uc}

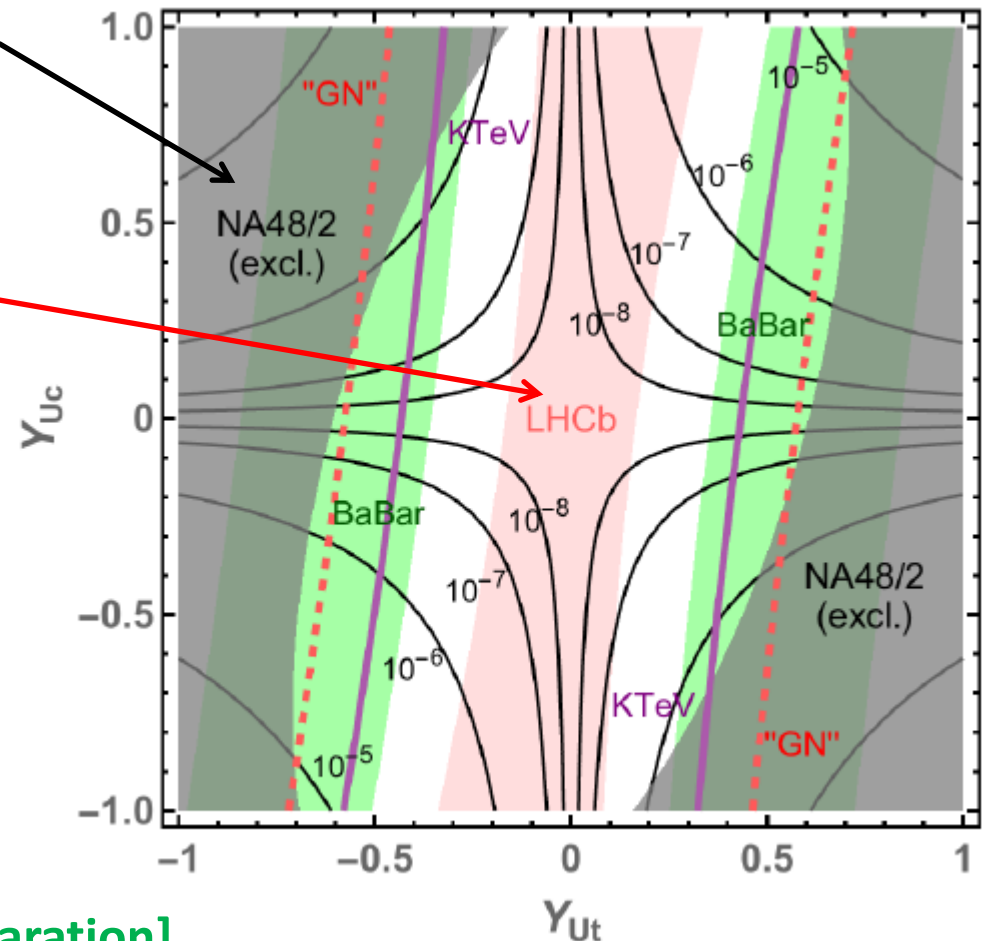
$$Y_{Uu_i} \Phi^\dagger \bar{U} P_R u_i$$

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➤ weakest at $m_{Z'} = 285 \text{ MeV}$

Allowed by $B^+ \rightarrow K^+ \mu^+ \mu^-$ at 2σ



[Fuyuto, Hou and MK, in preparation]

Constraints on Y_{Ut} and Y_{Uc}

$$Y_{Uu_i} \Phi^\dagger \bar{U} P_R u_i$$

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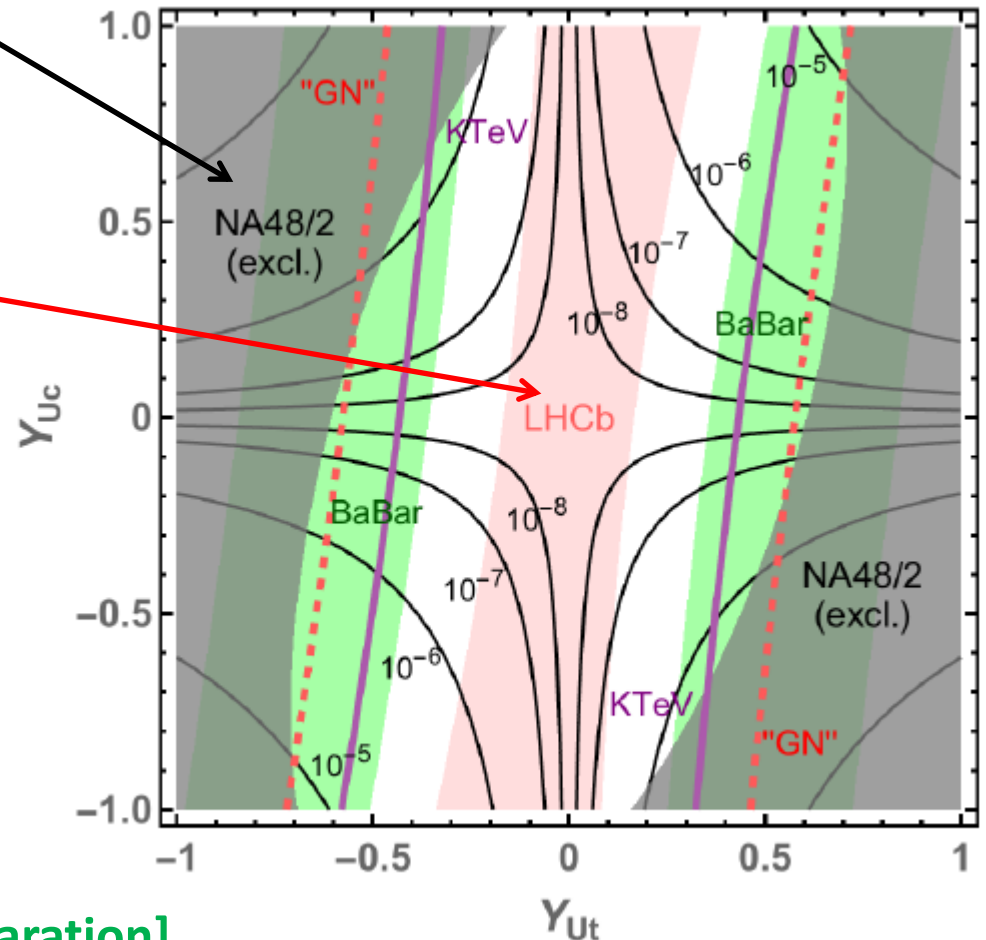
Excluded by $K^+ \rightarrow \pi^+ \mu^+ \mu^-$ at 2σ

➤ weakest at $m_{Z'} = 285 \text{ MeV}$

Allowed by $B^+ \rightarrow K^+ \mu^+ \mu^-$ at 2σ

- More sensitive to Y_{Ut} than Y_{Uc} , due to chiral factor m_t/m_c in the loop-induced bsZ'/sdZ' coupling

- $\text{BR}(t \rightarrow c Z')$ contours are shown by solid-black lines



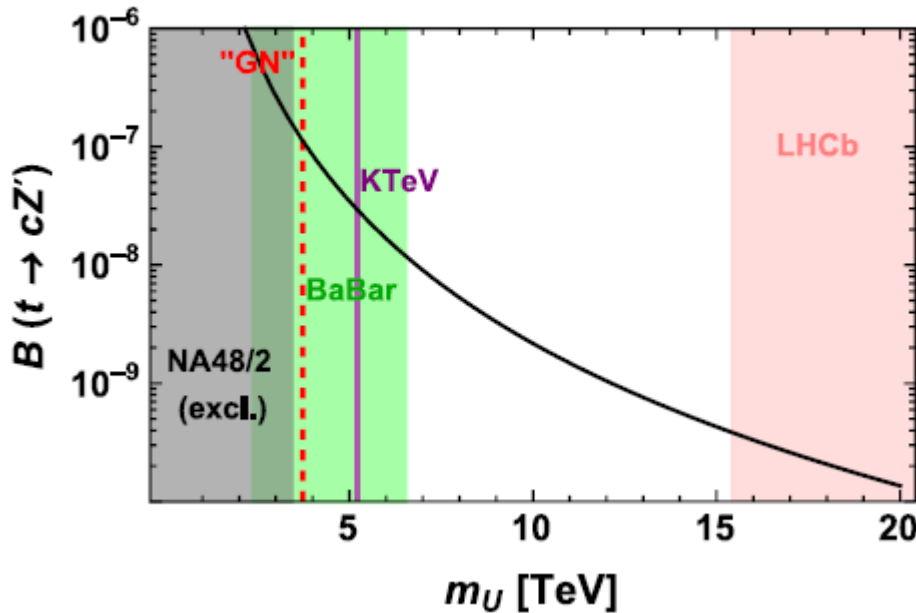
[Fuyuto, Hou and MK, in preparation]

RH-current induced $t \rightarrow c Z'$ rates

Fuyuto, Hou and MK, in preparation

(1) Normal Yukawa hierarchy

$$Y_{Ut}=1, Y_{Uc}=\lambda$$



➤ $B^+ \rightarrow K^+ \mu\mu$ data pushes down to $\text{BR}(t \rightarrow c Z') < 10^{-9}$

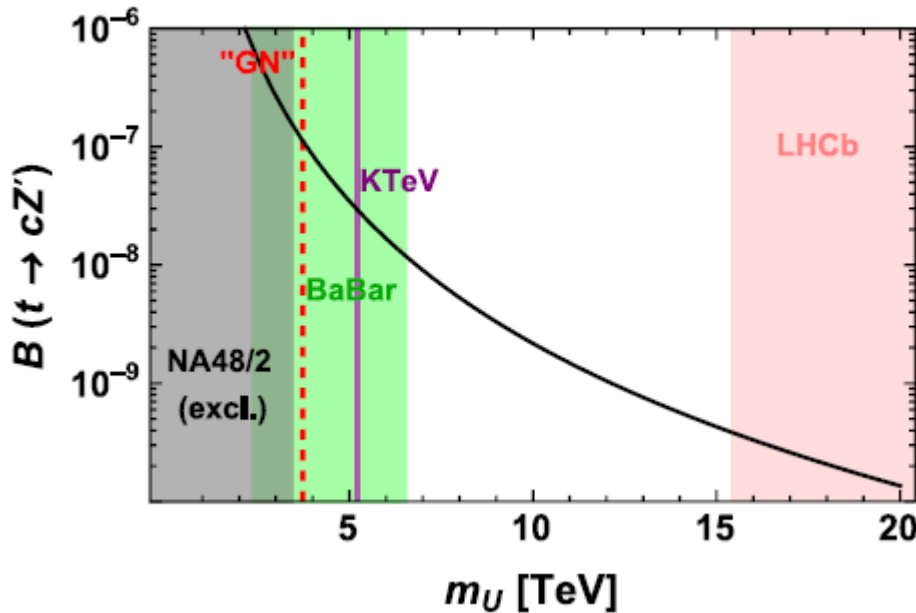
-> far below sensitivity of CMS (300/fb)

RH-current induced $t \rightarrow c Z'$ rates

Fuyuto, Hou and MK, in preparation

(1) Normal Yukawa hierarchy

$$Y_{Ut}=1, Y_{Uc}=\lambda$$

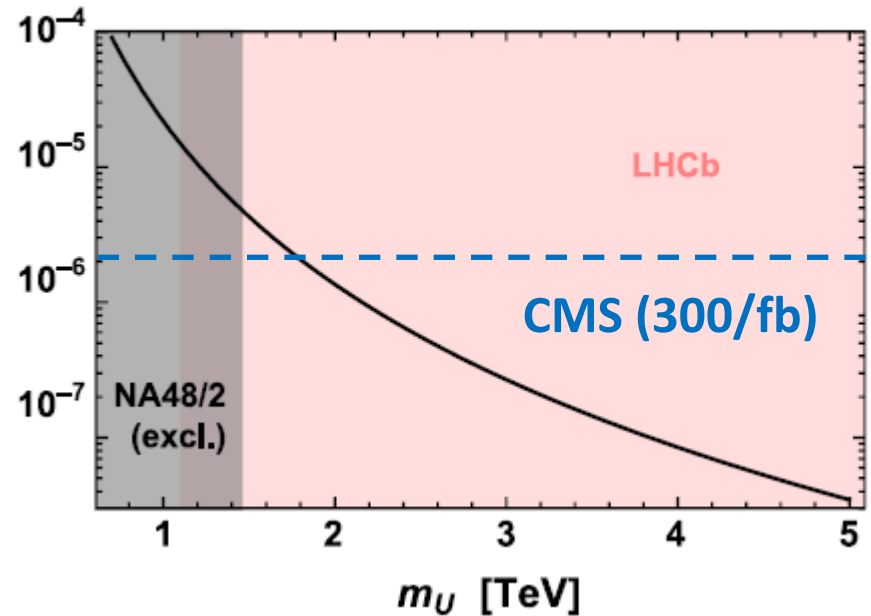


➤ $B^+ \rightarrow K^+ \mu\mu$ data pushes down to $\text{BR}(t \rightarrow c Z') < 10^{-9}$

-> far below sensitivity of CMS (300/fb)

(2) Flipped Yukawa hierarchy

$$Y_{Ut}=\lambda, Y_{Uc}=1$$



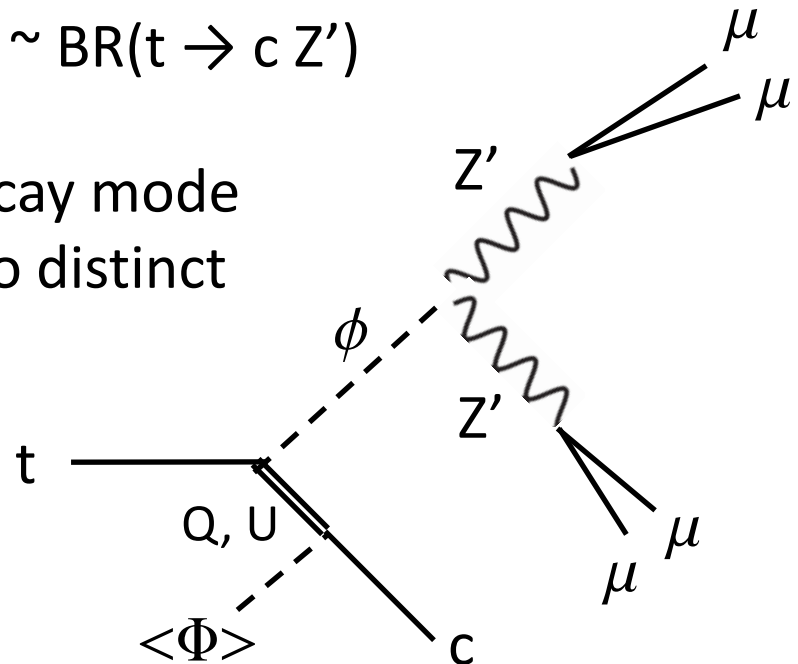
➤ $K^+ \rightarrow \pi^+ \mu\mu$ data imposes $\text{BR}(t \rightarrow c Z') < 10^{-5}$

-> CMS (300/fb) sensitivity is barely attained

Discussion: $t \rightarrow c \phi$

Hou and MK, in preparation

- The model predicts FCNC couplings with $U(1)'$ Higgs ϕ
- This leads to $t \rightarrow c \phi \rightarrow c Z' Z' \rightarrow c + 4\mu$
- For $m_\phi, m_{Z'} \ll m_t$, $BR(t \rightarrow c \phi) \sim BR(t \rightarrow c Z')$
- If ϕ is lighter than top, this decay mode may be more promising due to distinct signature



Summary

- We studied allowed ranges for the $t \rightarrow c Z'$ rate based on a gauged $L_\mu - L_\tau$ model

- 2 scenarios are considered

$B(t \rightarrow c Z')$ range

- (1) Heavy Z' : $m_b \ll m_{Z'} (< m_t - m_c)$
motivated by P_5' & R_K anomalies

$< 10^{-3}$

- Within reach of CMS with Run 1 dataset!

- (2) Light Z' : $m_{Z'} < 400$ MeV
motivated by muon $g-2$ anomaly

$< 10^{-9}$ (normal)

$< 10^{-5}$ (flipped)

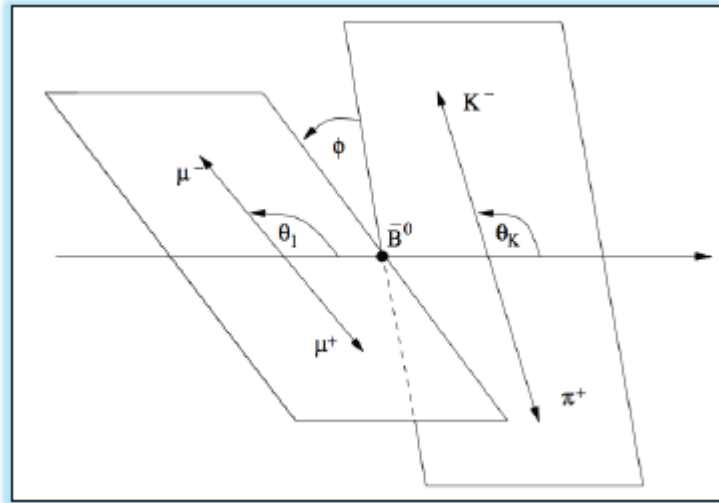
- Seemingly beyond reach of near future LHC in most parts of the parameter space

Back Up Slides

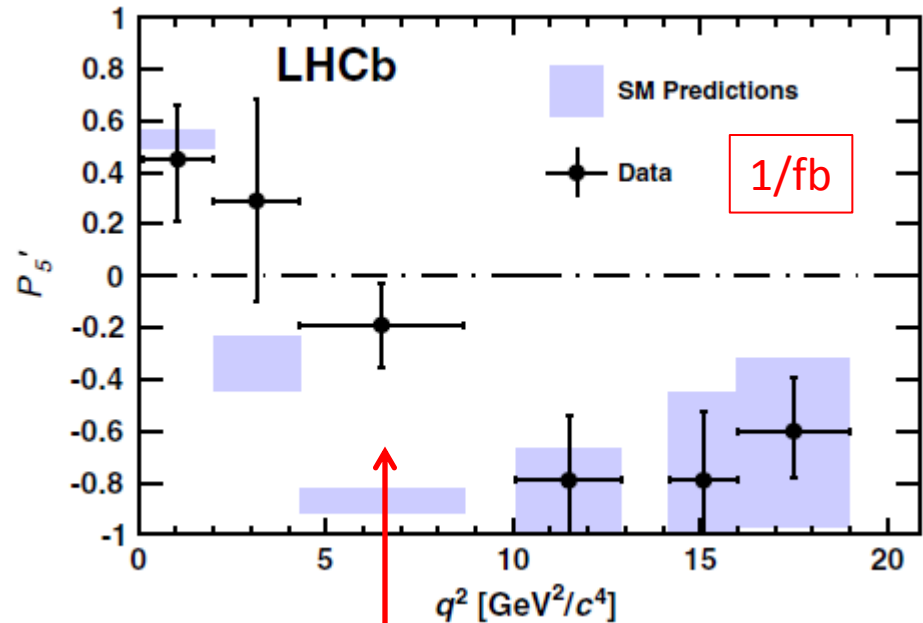
Some hints of NP in $b \rightarrow s$ transitions

- P_5' anomaly in angular distribution of

$$B \rightarrow K^*(\rightarrow K^+\pi^-) \mu^+\mu^-$$



LHCb, PRL 111, 191801 (2013)



3.7 σ discrepancy

* 2.5 σ in better controlled 1 - 6 GeV 2

$$\frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{d\cos\theta_\ell d\cos\theta_K d\phi dq^2}$$

$$= \frac{9}{32\pi} \left[\frac{3}{4} (1 - F_L) \sin^2\theta_K + F_L \cos^2\theta_K + \frac{1}{4} (1 - F_L) \sin^2\theta_K \cos 2\theta_\ell \right.$$

$$- F_L \cos^2\theta_K \cos 2\theta_\ell + S_3 \sin^2\theta_K \sin^2\theta_\ell \cos 2\phi + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi$$

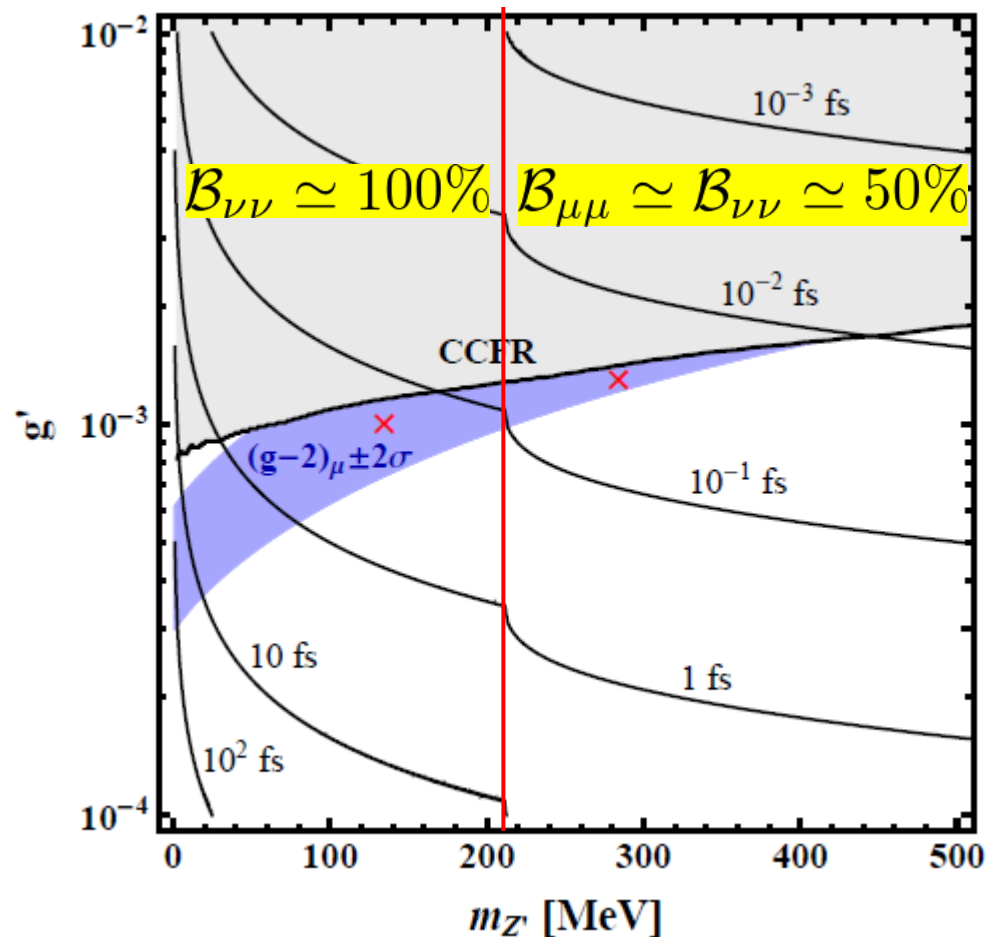
$$+ S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi + S_6 \sin^2\theta_K \cos \theta_\ell + S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi$$

$$+ S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2\theta_K \sin^2\theta_\ell \sin 2\phi \left. \right]$$

$$P_{i=4,5,6,8}' = \frac{S_{j=4,5,7,8}}{\sqrt{F_L(1 - F_L)}}$$

Lifetime and BR for light Z' , motivated by $(g-2)_\mu$

K. Fuyuto, W.-S. Hou, MK, in preparation



$b \rightarrow s Z'$ formulas

Fuyuto, Hou and MK, arXiv:1412.4397

- Loop induced bsZ' coupling: $g_{sb} \bar{s}_L \gamma^\alpha b_L Z'_\alpha$

$$g_{sb} = \frac{g' v_\Phi^2}{32\pi^2 v^2} [c_{cc} f_{cc} + (c_{tc} + c_{ct}) f_{ct} + c_{tt} f_{tt}] \quad (b) \quad \begin{array}{c} \text{Diagram: A loop diagram showing a top quark line (t) and a charm quark line (c) connected by a W boson loop. The loop is labeled with U and U. The external lines are labeled d(s) and Z'. The loop is also labeled with t, c and t, c. The loop is also labeled with \langle \Phi \rangle and \langle \Phi \rangle. The loop is also labeled with Z' and Z'.$$

with $c_{ij} = V_{ib} V_{js}^* Y_{Ui} Y_{Uj}^* m_i m_j / m_U^2$

$$\begin{cases} f_{ct} \simeq 1 + \log \frac{m_U^2}{m_t^2} + \frac{3m_W^2}{m_t^2 - m_W^2} \log \frac{m_t^2}{m_W^2}, & f_{tt} \simeq \frac{3m_W^2}{m_t^2 - m_W^2} \left(1 - \frac{m_W^2}{m_t^2 - m_W^2} \log \frac{m_t^2}{m_W^2} \right) + \log \frac{m_U^2}{m_t^2}, \\ f_{cc} \text{ is obtained by } m_c^2 \ll m_W^2 \end{cases}$$

- $B \rightarrow K Z'$ branching ratio (similar for Kaon decays):

$$\mathcal{B}(\bar{B} \rightarrow \bar{K} Z') = \tau_B \frac{|g_{sb}|^2}{64\pi} \frac{m_B^3}{m_{Z'}^2} \lambda^{3/2} \left(1, \frac{m_K^2}{m_B^2}, \frac{m_{Z'}^2}{m_B^2} \right) [f_+^{B \rightarrow K}(m_{Z'}^2)]^2$$

where $\lambda(x, y, z) \equiv x^2 + y^2 + z^2 - 2(xy + xz + yz)$

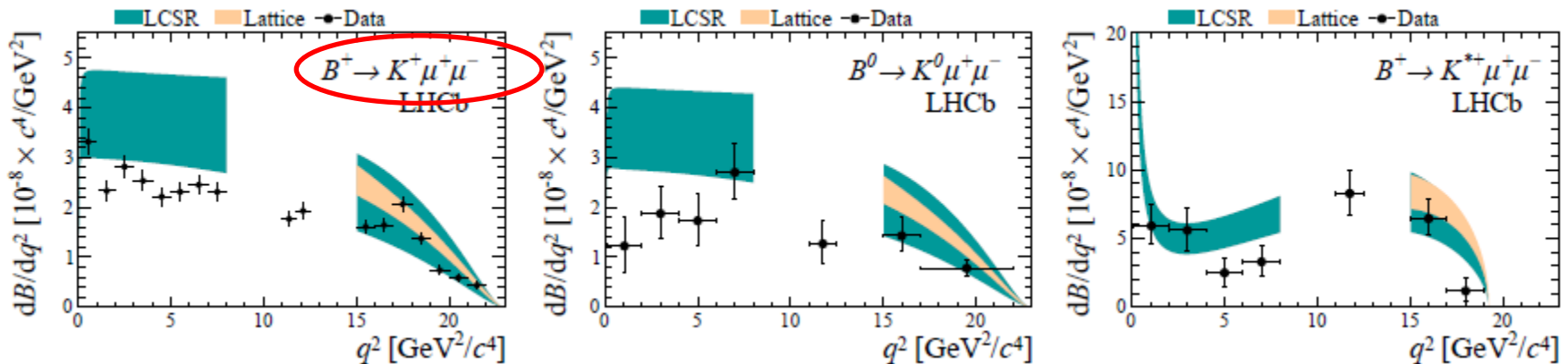
$f_+^{B \rightarrow K}$: $B \rightarrow K$ form factor **Ball and Zwicky, PRD71, 014015(2005)**

Constraint from $B \rightarrow K \mu^+ \mu^-$

- Z' would show up as a spike in $q^2 = m_{\mu\mu}^2$ distribution

- 3 fb⁻¹ results by LHCb **JHEP 06 (2014) 133**

$$q^2 \lesssim 0.16 \text{ GeV}^2$$

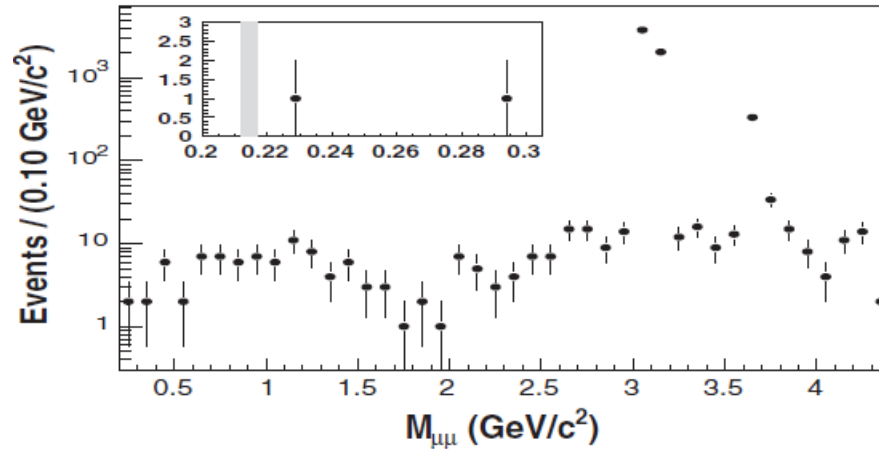


- best place to search Z'
- less statistics
- photon peak pollution

- However, LHCb sets the cut $q^2 > 0.1 \text{ GeV}^2 \simeq (316 \text{ MeV})^2$

=> This constraint can be avoided if $m_{Z'} < 316 \text{ MeV}$

Belle's search for $B \rightarrow K^* X (\rightarrow \mu^+ \mu^-)$



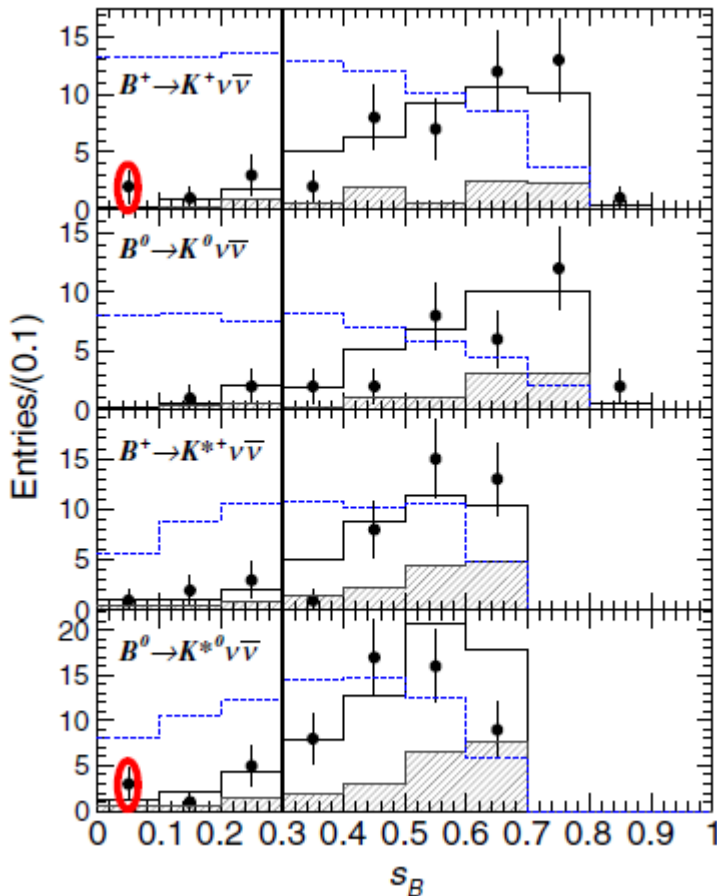
PRL105, 091801(2010)

$M_{\mu\mu}$ (MeV/ c^2)	$B^0 \rightarrow K^{*0} X, K^{*0} \rightarrow K^+ \pi^-, X \rightarrow \mu^+ \mu^-$				
	N_{obs}	N_{bg}	ϵ	S_{90}	U.L. (10^{-8})
212.0	0	$0.03^{+0.01}_{-0.01}$ ($0.03^{+0.01}_{-0.01}$)	23.8 (23.7)	2.43 (2.43)	2.34 (2.34)
214.3	0	$0.13^{+0.04}_{-0.03}$ ($0.13^{+0.04}_{-0.03}$)	23.6 (23.5)	2.33 (2.33)	2.26 (2.27)
220.0	0	$0.13^{+0.02}_{-0.02}$ ($0.13^{+0.02}_{-0.02}$)	23.0 (22.9)	2.33 (2.33)	2.31 (2.33)
230.0	1	$0.24^{+0.02}_{-0.02}$ ($0.25^{+0.02}_{-0.02}$)	21.4 (21.4)	4.09 (4.12)	4.37 (4.40)
240.0	0	$0.38^{+0.02}_{-0.02}$ ($0.39^{+0.02}_{-0.02}$)	20.0 (20.0)	2.09 (2.09)	2.40 (2.39)
250.0	0	$0.51^{+0.01}_{-0.01}$ ($0.51^{+0.01}_{-0.01}$)	18.0 (18.4)	1.92 (1.94)	2.43 (2.41)
260.0	0	$0.63^{+0.01}_{-0.01}$ ($0.63^{+0.01}_{-0.01}$)	16.5 (17.2)	1.83 (1.83)	2.54 (2.43)
270.0	0	$0.75^{+0.02}_{-0.02}$ ($0.75^{+0.02}_{-0.02}$)	15.4 (16.4)	1.76 (1.76)	2.61 (2.45)
280.0	0	$0.69^{+0.03}_{-0.03}$ ($0.86^{+0.04}_{-0.04}$)	14.6 (15.8)	1.78 (1.69)	2.78 (2.45)
290.0	1	$0.98^{+0.06}_{-0.06}$ ($0.97^{+0.06}_{-0.06}$)	14.0 (15.5)	3.35 (3.37)	5.47 (4.99)
300.0	1	$1.08^{+0.08}_{-0.08}$ ($1.08^{+0.08}_{-0.08}$)	13.6 (15.1)	3.28 (3.28)	5.53 (4.97)

<-- 90%CL upper limit

Constraint from $B \rightarrow K \nu \nu$

- Belle & BaBar's sensitivities are $\sim 10 \times \text{BR}(\text{SM})$
- BaBar's result is sensitive to low mass Z' PRD87, 112005(2013)



constraint on New Physics effect in [1st bin](#)

$$s_B \equiv \frac{m_{\nu\nu}^2}{m_B^2} \in (0, 0.1) \quad m_{Z'} \in (0, 1670) \text{ MeV}$$

$$\Delta\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu})_{(0,0.1)} = (0.35^{+0.60}_{-0.15}) \times 10^{-5}$$

$$\Delta\mathcal{B}(B^0 \rightarrow K^0 \nu \bar{\nu})_{(0,0.1)} = (-0.2^{+1.8}_{-0.1}) \times 10^{-5}$$

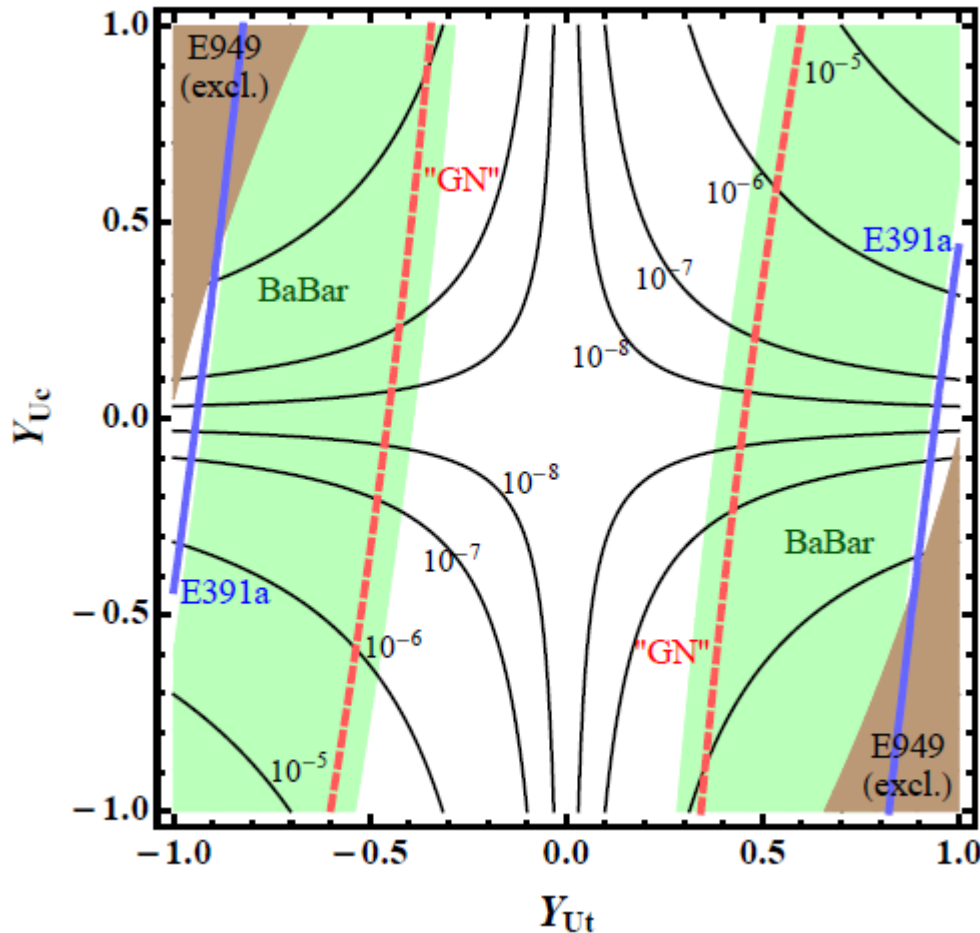
$$\Delta\mathcal{B}(B^+ \rightarrow K^{*+} \nu \bar{\nu})_{(0,0.1)} = (-0.1^{+1.9}_{-0.3}) \times 10^{-5}$$

$$\Delta\mathcal{B}(B^0 \rightarrow K^{*0} \nu \bar{\nu})_{(0,0.1)} = (1.1^{+1.9}_{-0.6}) \times 10^{-5}$$

N.B. These are supplied by genuine experiments

Allowed Region: $m_{Z'} = 135 \text{ MeV}$

$$g' = 10^{-3}, \quad v_\Phi = 135 \text{ GeV}, \quad m_U = 2 \text{ TeV}$$



- **E391a** set better limit than E949 in some region
- **"GN"** is usual GN bound, which should not be applied in this case
 $\mathcal{B}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \lesssim 1.4 \times 10^{-9}$
- $K_L \rightarrow \pi^0 Z'$ can go beyond **"GN"** bound (favored by the **BaBar** data)