



# Leptonic and Radiative B Meson Decays at Belle

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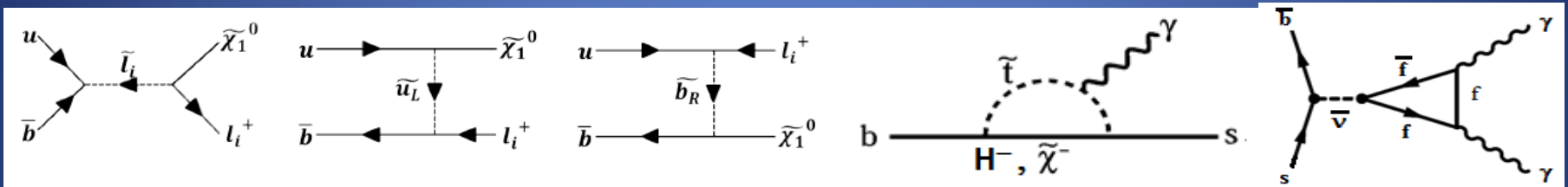
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# Introduction

- Leptonic and radiative B decays are sensitive to new physics in tree or penguin loop.



- Small SM branching fraction ( $\mathcal{B}$ )
- More precise theoretical predictions
- Topics covered in this talk
  - Search for massive invisible particles
  - Search for  $B^+ \rightarrow \ell^+ \nu \gamma$ , ( $\ell = e, \mu$ )
  - Update on  $B_s^0 \rightarrow \phi \gamma$  and search for  $B_s^0 \rightarrow \gamma \gamma$

# KEKB and Belle Detector

Tsukuba, Japan

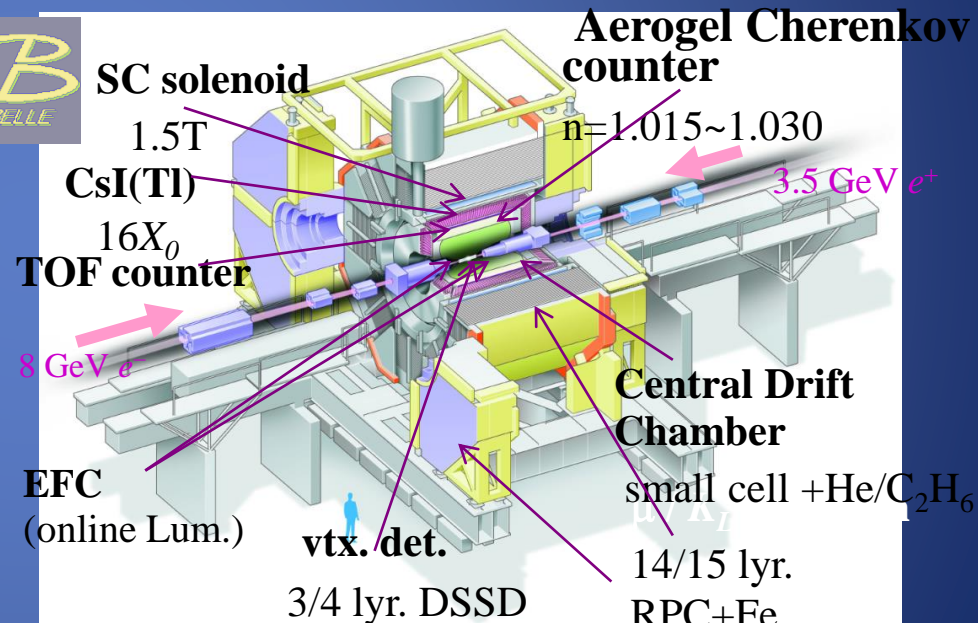
Belle 測定器

$$L_{\text{peak}} = 2.1 \times 10^{34} / \text{cm}^2 / \text{s}^2$$

加速空洞

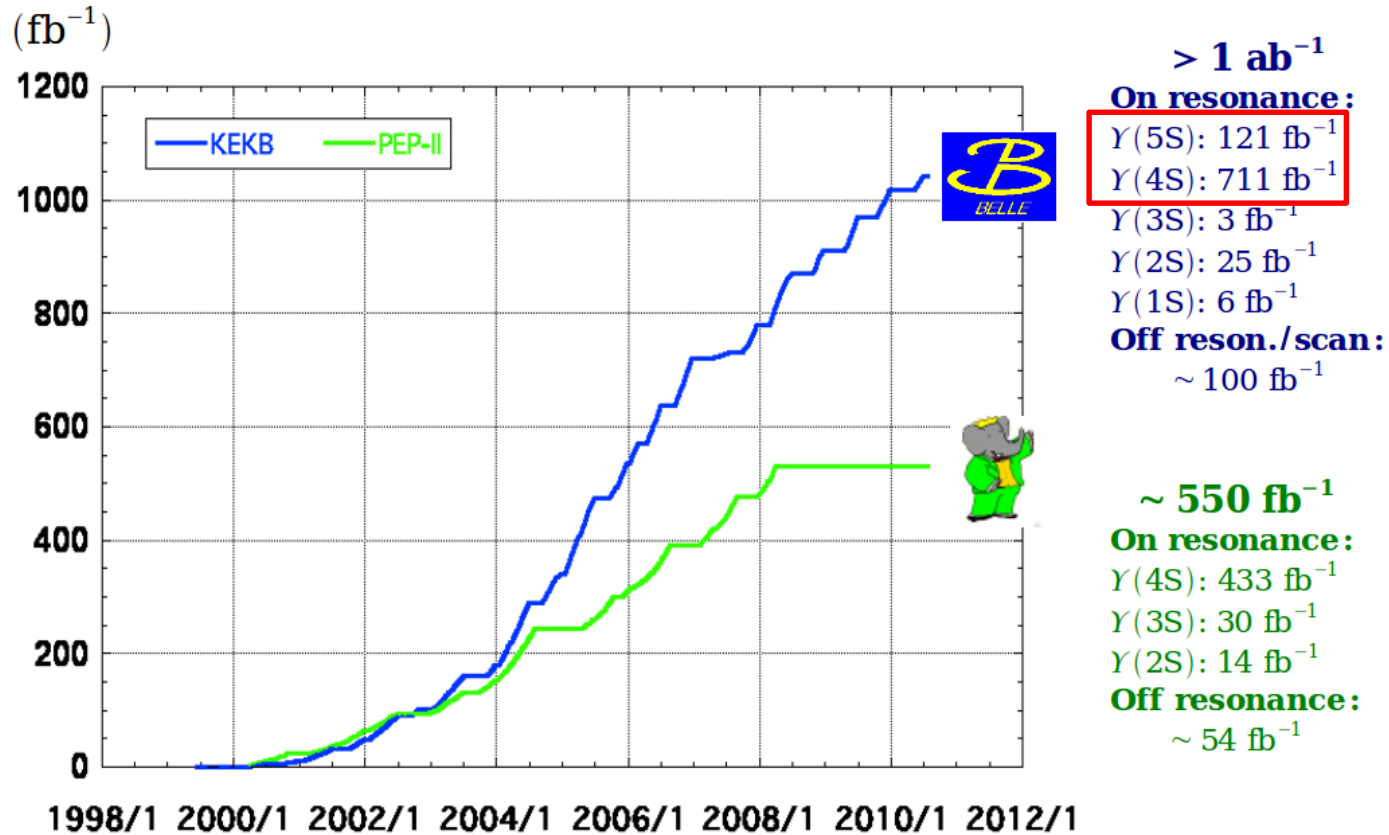
3.5 GeV  $e^+$  on 8 GeV  $e^-$   
 $W_{\text{CM}} = M(\Upsilon(4S, 5S))$   
 3km circumference  
 ~11mrad crossing angle

陽電子源



# Data samples

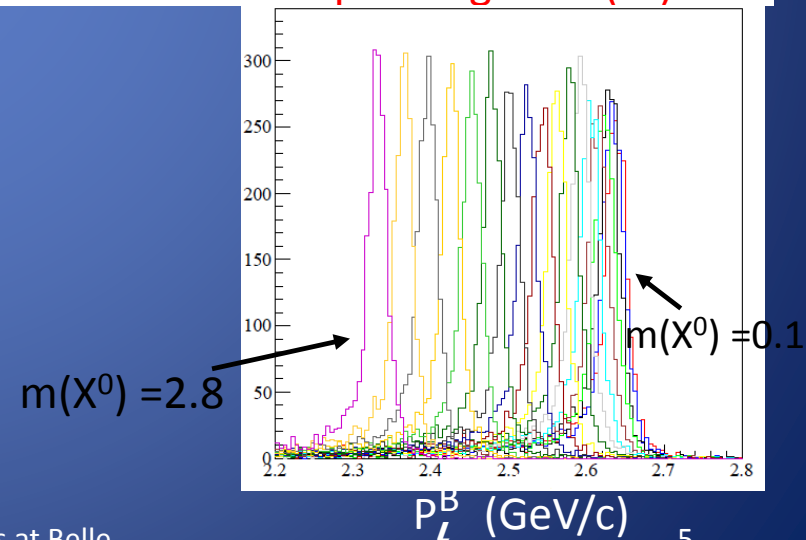
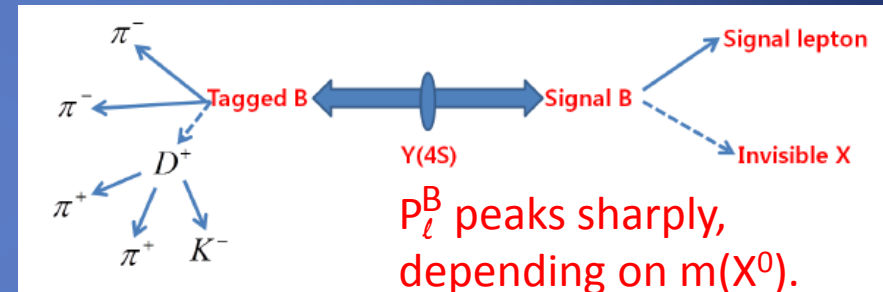
## Integrated luminosity of B factories





# Search for massive invisible spin-1/2 particle $X^0$ in $B^+ \rightarrow \ell^+ X^0$

- Analysis strategy:
  - Require hadronic  $B_{\text{tag}}$  (1104 modes) using NeuroBayes.
  - Select  $1.8 < P_{\ell}^B < 3.0 \text{ GeV}/c$  ( $\ell = e$  or  $\mu$ )
  - Apply  $|\cos\theta_T| < 0.9$  (0.8) for  $e^+ X^0$  ( $\mu^+ X^0$ ) to suppress continuum background.
  - Demand  $E_{\text{Ecl}} < 0.5 \text{ GeV}$



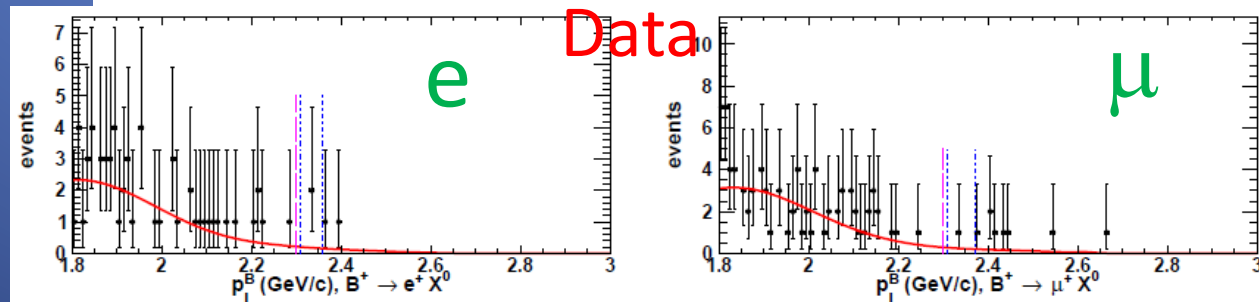
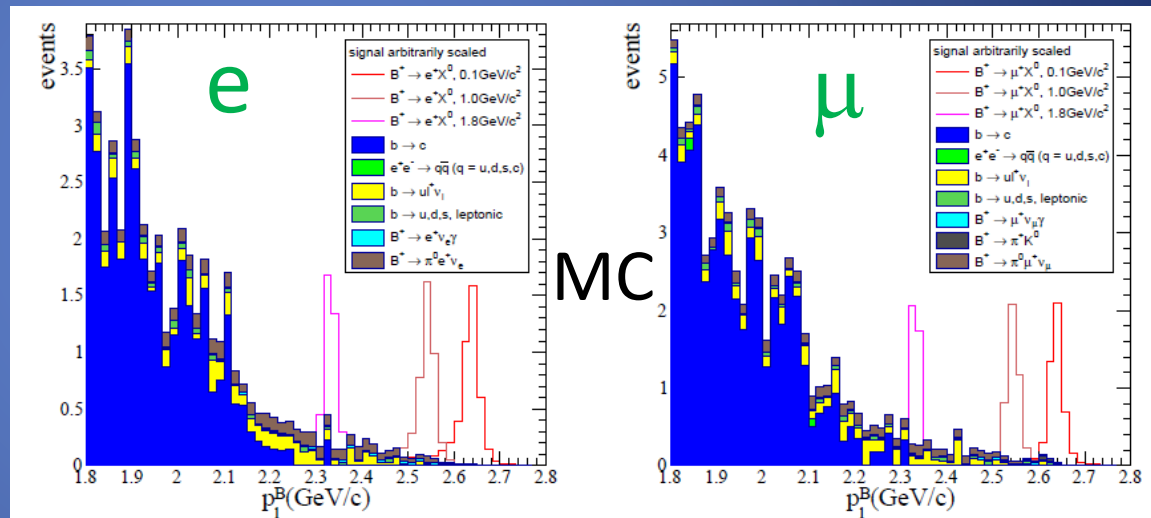
# Signal Extraction, $B^+ \rightarrow \ell^+ X^0$

- Use MC and data to estimate the numbers of bkg.
  - Fit MC  $P_{\ell}^B$  distribution in side-band region (1.8–2.3 GeV/c) to estimate yields in signal regions.
  - Correct for data-MC difference

$$N_{\text{sig}} = N_{\text{obs}} - N_{\text{exp}}^{\text{bkg}}$$

• Backgrounds:

- $b \rightarrow c$
- $e^+e^- \rightarrow qq$
- $b \rightarrow u \ell^+ \nu$
- $b \rightarrow u, d, s, \text{leptonic}$
- $b \rightarrow \ell^+ \nu \gamma$
- $b \rightarrow \pi^0 \ell^+ \nu$



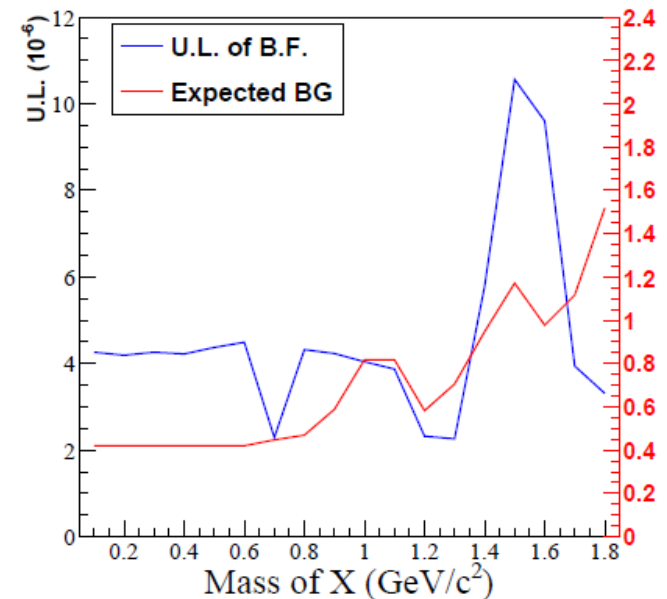
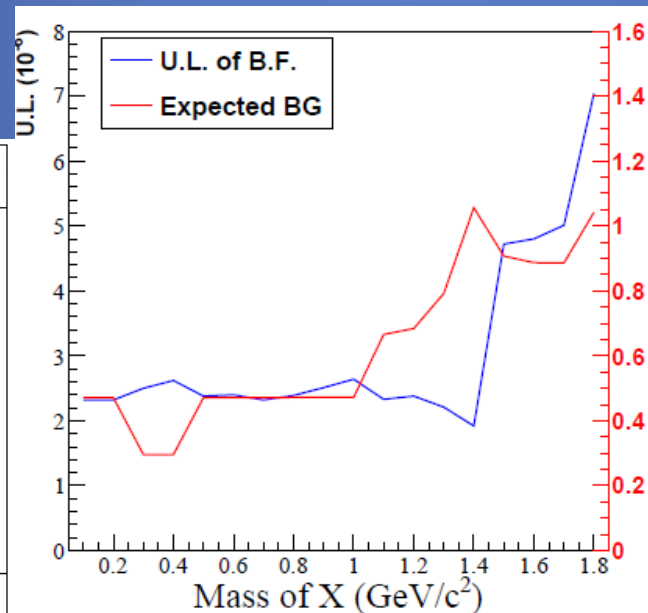
Leptonic and Radiative B decays at Belle

# Preliminary Results of $B^+ \rightarrow \ell^+ X^0$

- No significant signals are observed; the obtained  $\mathcal{B}(B^+ \rightarrow \ell^+ X^0)$  upper limits @90% C.L. using POLE package are  $(2-11) \times 10^{-6}$  for  $0.1 < m(X^0) < 1.8 \text{ GeV}/c^2$

## Syst. errors.

Source	$B^+ \rightarrow e^+ X^0$	$B^+ \rightarrow \mu^+ X^0$
$N_{B^+B^-}$	1.8%	1.8%
Tracking	0.35%	0.35%
$\epsilon_{tag}$ correction	6.4%	6.4%
$p_l^B$ shape	3.6%	3.6%
Lepton ID	1.0-1.1%	0.8-0.9%
MC statistics	1.8-2.0%	1.8-1.9%
Total	7.9%	7.8%

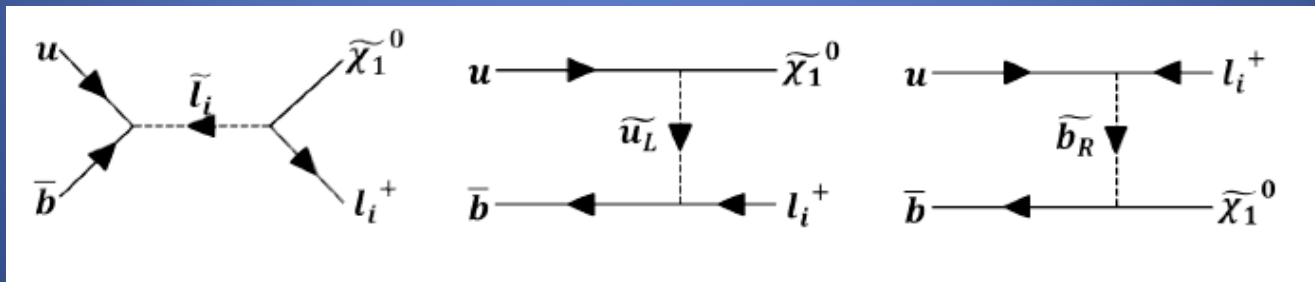


# Bound on SUSY-related parameter

- Assume R-parity violation,  $\xi_i$  can be expressed as,

$$\xi_i = \lambda'^2_{i13} \left( \frac{1}{2M_{\tilde{l}_i}^2} + \frac{1}{12M_{\tilde{u}_L}^2} + \frac{1}{6M_{\tilde{b}_R}^2} \right)^2 = \frac{8\pi(m_u + m_b)^2 \mathcal{B}(B^+ \rightarrow l_i^+ X^0)}{\tau_{B^+} g'^2 f_B^2 m_{B^+}^2 p_{l_i}^B (m_{B^+}^2 - m_{l_i}^2 - m_{X^0}^2)}$$

$\lambda'$ : R-parity violating coupling constant;  $g'$ : weak decay coupling c.



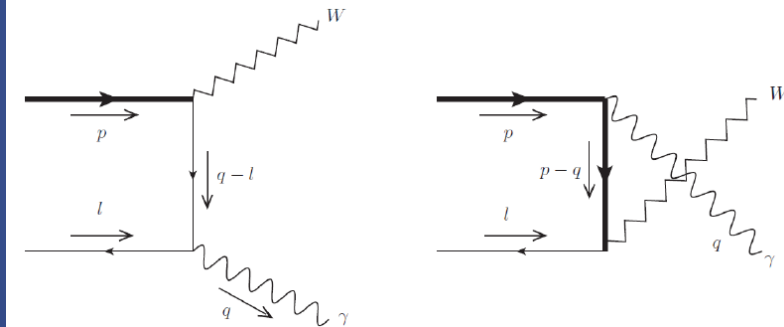
- Best limits:  $\xi_i < 4 \times 10^{-14}$  for  $m(X^0) = 0.1 \text{ GeV}/c^2$  (for e)  
 $\xi_i < 4 \times 10^{-14}$  for  $m(X^0) = 0.7 \text{ GeV}/c^2$  (for  $\mu$ )



# Search for in $B^+ \rightarrow \ell^+ \nu \gamma$

- The differential branching fraction is expressed as ,

$$\frac{d\Gamma}{dE_\gamma} = \frac{\alpha_{em} G_F^2 |V_{ub}|^2}{48\pi^2} m_B^4 (1 - x_\gamma) x_\gamma^3 [F_A^2 + F_V^2]$$



1.  $x_\gamma = 2E_\gamma/m_B$

2.  $F_A$  and  $F_V$  are form factors

3.  $\lambda_B$ , the  $B$  meson light-cone parameter, in  $F_A$  and  $F_V$  is a key param. for charmless  $B$  decays.

- Compared to  $B^+ \rightarrow \ell^+ \nu$ ,

1. no helicity suppression

2. additional  $\alpha_{em}$

- SM branching fraction  $\sim 0(10^{-6})$  M. Beneke and J. Rohrwild  
Eur. Phys. J. C. 71, 1818 (2011)

- Best limits from BaBar  $\mathcal{B}(B^+ \rightarrow e^+ \nu \gamma) < 17 \times 10^{-6}$

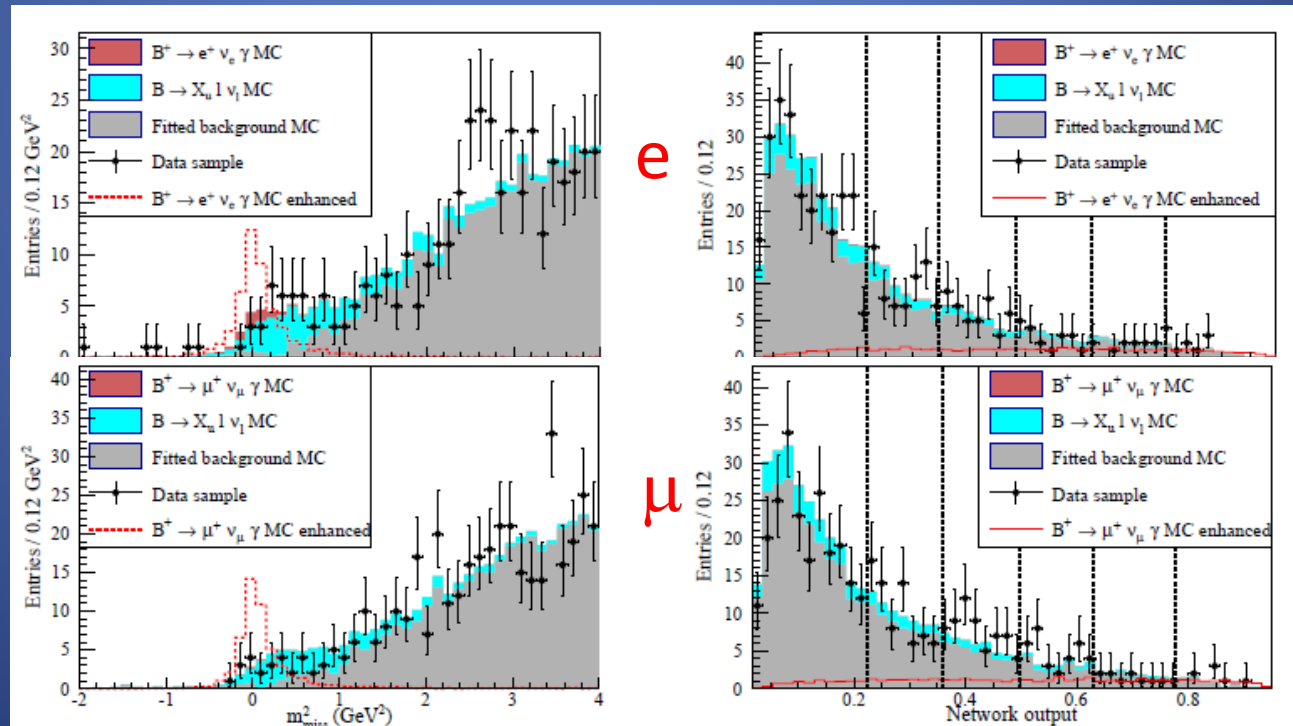
PRD 80, 111105 (2009)  $\mathcal{B}(B^+ \rightarrow \mu^+ \nu \gamma) < 26 \times 10^{-6}$

# Analysis strategy, $B^+ \rightarrow \ell^+ \nu \gamma$

- Require a hadronic B tag with a lepton and a photon.
  - $P_{\text{miss}} > 800 \text{ MeV}/c$ ,  $\cos\Theta_{\gamma\ell} < 0.6$ ,  $\cos\Theta_{\gamma\nu} > -0.9$
  - Two thresholds on  $E_{\gamma}^{\text{sig}}$ , 400 MeV & 1 GeV (nominal).
  - Signal-background separation:  $m_{\text{miss}}^2$  & other variables
    - Remaining ECL energy
    - $\cos\Theta_{\gamma\ell}$  &  $\cos\Theta_{\gamma\nu}$
    - $m(\gamma\gamma)$  with  $E_{\gamma}$  threshold from 0-100 MeVto distinguish  $\gamma$ s from  $B^+ \rightarrow \ell^+ \nu \pi^0$  and  $\ell^+ \nu \eta$
- ➡ Neural Network

# Signal Extraction, $B^+ \rightarrow \ell^+ \nu \gamma$

- Perform unbinned likelihood fit on  $m_{\text{miss}}^2$  in 6 NN bins with 3 components: signal, measured  $B \rightarrow X_u \ell^+ \nu$ , other backgrounds.



# Results, $B^+ \rightarrow \ell^+ \nu \gamma$

PRD 91, 112009 (2015)

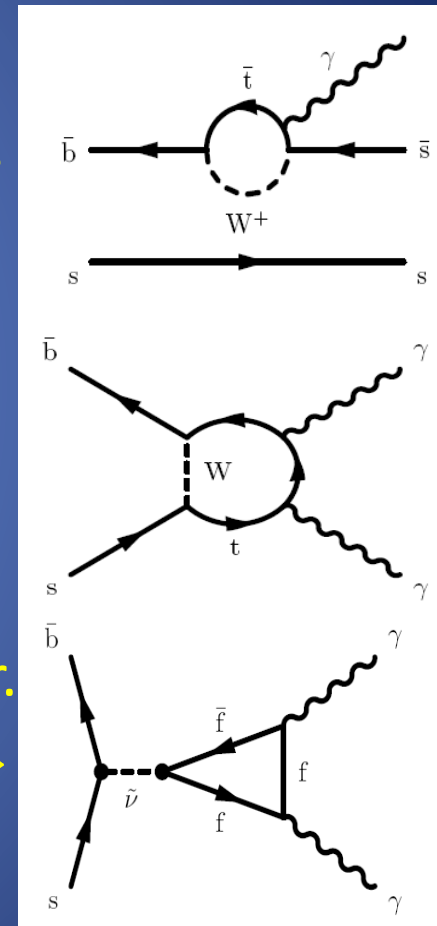
- No significant signals are observed. Provide best limits.
- $\lambda_B > 260$  MeV at 90% C.L.

Nominal analysis with $E_\gamma^{\text{sig}} > 1$ GeV							
MC expectation				Data measurement			
Mode	Yield	Significance ( $\sigma$ )	$\mathcal{B}$ limit ( $10^{-6}$ )	Yield	$\mathcal{B}$ ( $10^{-6}$ )	Significance ( $\sigma$ )	$\mathcal{B}$ limit ( $10^{-6}$ )
$B^+ \rightarrow e^+ \nu_e \gamma$	$8.0 \pm 4.5^{+1.1}_{-1.4}$	2.1	$< 7.5$	$6.1^{+4.9+1.1}_{-3.9-1.4}$	$3.8^{+3.0+0.5}_{-2.4-0.6}$	1.7	$< 6.1$
$B^+ \rightarrow \mu^+ \nu_\mu \gamma$	$8.7 \pm 4.6^{+1.1}_{-1.6}$	2.2	$< 6.9$	$0.9^{+3.6+1.1}_{-2.6-1.6}$	$0.6^{+2.1+0.1}_{-1.5-0.1}$	0.4	$< 3.4$
$B^+ \rightarrow \ell^+ \nu_\ell \gamma$	$16.5 \pm 6.5^{+1.8}_{-2.3}$	2.9	$< 4.8$	$6.6^{+5.7+1.8}_{-4.7-2.3}$	$2.0^{+1.7+0.2}_{-1.4-0.3}$	1.4	$< 3.5$

Secondary analysis with $E_\gamma^{\text{sig}} > 400$ MeV							
MC expectation				Data measurement			
Mode	Yield	Significance ( $\sigma$ )	$\mathcal{B}$ limit ( $10^{-6}$ )	Yield	$\mathcal{B}$ ( $10^{-6}$ )	Significance ( $\sigma$ )	$\mathcal{B}$ limit ( $10^{-6}$ )
$B^+ \rightarrow e^+ \nu_e \gamma$	$12.4 \pm 6.2^{+1.9}_{-2.4}$	2.1	$< 6.8$	$11.9^{+7.0+1.9}_{-6.0-2.4}$	$4.9^{+2.9+0.8}_{-2.5-1.0}$	2.0	$< 9.3$
$B^+ \rightarrow \mu^+ \nu_\mu \gamma$	$11.9 \pm 6.0^{+1.9}_{-2.3}$	2.2	$< 6.2$	$-0.1^{+5.2+1.9}_{-4.1-2.3}$	-	-	$< 4.3$
$B^+ \rightarrow \ell^+ \nu_\ell \gamma$	$24.9 \pm 8.7^{+3.1}_{-3.6}$	2.9	$< 4.3$	$11.3^{+8.4+3.1}_{-7.4-3.6}$	$2.3^{+1.7+0.3}_{-1.5-0.3}$	1.5	$< 5.0$

# Search for $B_s^0 \rightarrow \gamma\gamma$ & update on $B_s^0 \rightarrow \phi\gamma$

- Update  $\mathcal{B}(B_s^0 \rightarrow \phi\gamma)$  with full Belle data.
  - Stringent constraint by  $B \rightarrow X_s \gamma$  & exclusive decays
  - SM  $\mathcal{B} = 4 \times 10^{-5}$  with 30% theory error
  - Best  $\mathcal{B} = (35.1 \pm 3.5 \pm 1.2) \times 10^{-6}$  is provided by LHCb, Nucl. Phys. B867, 1 (2013)
- The decay  $B_s^0 \rightarrow \gamma\gamma$  has not been observed.
  - Belle previous limit,  $\mathcal{B} < 8.7 \times 10^{-6}$  @90% C.L.
  - $\mathcal{B}$  is also constrained by  $B \rightarrow X_s \gamma$  in R-parity conser. SUSY, but may not in R-parity violating case.  $\Rightarrow$
- At  $\Upsilon(5S)$ ,  $f_{B_s^* \bar{B}_s^*} = (87.0 \pm 0.7)\%$ ,  $f_{B_s^* \bar{B}_s} = (7.3 \pm 1.4)\%$



PRD70, 035008(2004)



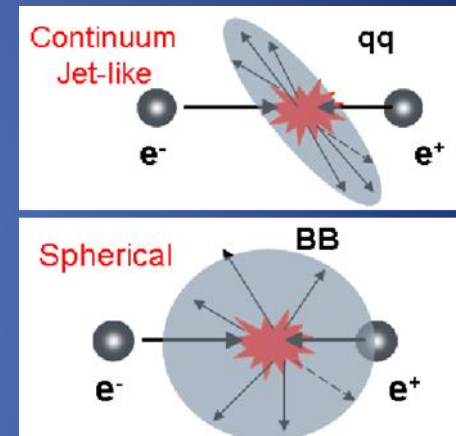
# Analysis method, $B_s^0 \rightarrow \phi\gamma, \gamma\gamma$

- Select  $\phi \rightarrow K^+K^-$ , good quality photon with  $\pi^0$  veto.
- Identify B candidates with  $M_{bc}$  and  $\Delta E$ .

$$\Delta E = E_B - E_{beam}$$

$$M_{bc} = \sqrt{E_{beam}^2 - |\vec{P}_B|^2}$$

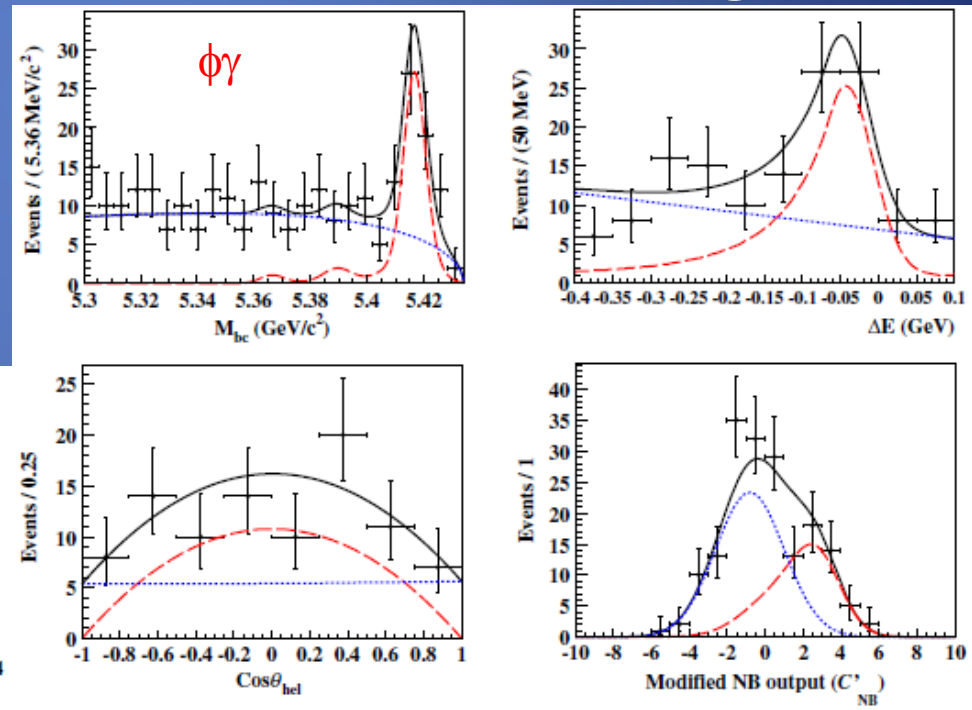
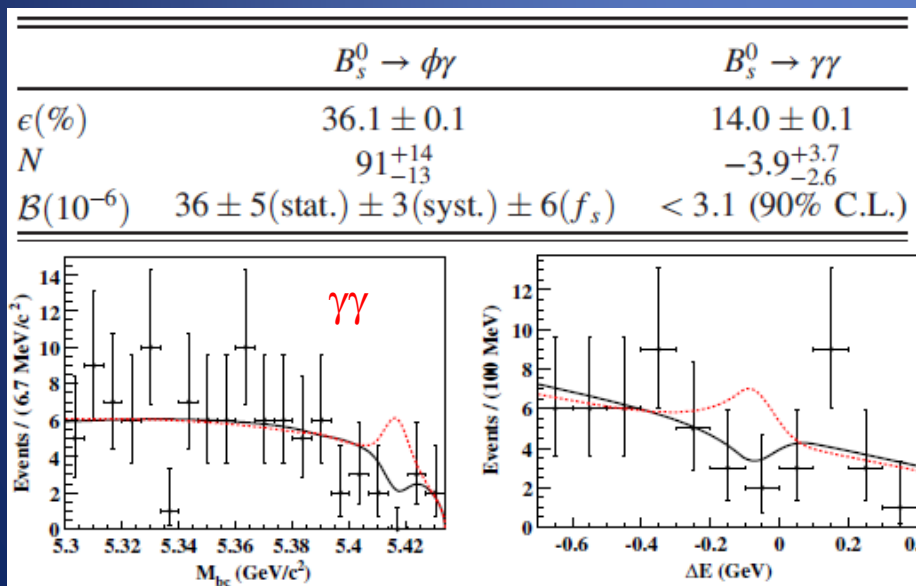
- Distinguish signals from background using shape variables: FWM and  $\cos\theta_T$  in NN  $\Rightarrow C_{NB}$ 
  - $\gamma\gamma$ : tighter cut on  $C_{NB}$ . Perform 2-D  $M_{bc}-\Delta E$  fit.
  - $\phi\gamma$ : loose cut on  $C_{NB}$  and modify it as  $C'_{NB} = \log \left( \frac{C_{NB} - C_{NBmin}}{C_{NBmax} - C_{NB}} \right)$   
Perform 4-D fit on  $M_{bc}, \Delta E, \cos\theta_{hel}, C'_{NB}$



# Results, $B_s^0 \rightarrow \phi\gamma, \gamma\gamma$

PRD 91, 011101 (2015)

- Calibrate signal PDFs using  $B^0 \rightarrow K^*\gamma$  and  $B_s \rightarrow D_s\pi$
- Signal PDFs =  $(f_{B_s^* \bar{B}_s^*}) \times (B^* \bar{B}_s^* \text{ PDF}) + (f_{B_s^* \bar{B}_s}) \times (B_s^* \bar{B}_s \text{ PDF}) + (f_{B_s \bar{B}_s}) \times (B_s \bar{B}_s \text{ PDF})$
- Background PDFs includes continuum and  $b\bar{b}$  bkg.



# Summary

- We present search results for leptonic and radiative B decays using full  $\Upsilon(4S)$  and  $\Upsilon(5S)$  samples:
  - No massive  $X^0$  particles are observed between 0.1 and 1.8 GeV/c<sup>2</sup>.  $\mathcal{B}(B^+ \rightarrow \ell^+ X^0) < (1.96-10.56) \times 10^{-6}$
  - No significant  $B^+ \rightarrow \ell^+ \nu \gamma$  signals are observed.  
 $\mathcal{B}(B^+ \rightarrow e^+ \nu \gamma) < 6.1 \times 10^{-6}$ ;  $\mathcal{B}(B^+ \rightarrow \mu^+ \nu \gamma) < 3.4 \times 10^{-6}$
  - $\mathcal{B}(B_s \rightarrow \phi \gamma) = (36 \pm 5(\text{stat}) \pm 3(\text{syst}) \pm 6(\text{fs})) \times 10^{-6}$   
consistent with LHCb result and SM expectation.
  - No  $B_s \rightarrow \gamma \gamma$  signal is observed,  $\mathcal{B} < 3.1 \times 10^{-6}$

# BACK UP

# $\mathcal{B} (B^+ \rightarrow \ell^+ X^0)$ Upper limits

	$p_l^B$ selection (GeV/c)	$\epsilon_s[\%]$	$N_{\text{obs}}$	$N_{\text{exp}}^{\text{bkg}}$	$\mathcal{B}^{90}$	selection (GeV/c)	$\epsilon_s[\%]$	$N_{\text{obs}}$	$N_{\text{exp}}^{\text{bkg}}$	$\mathcal{B}^{90}$
$M_{X^0}$	$B^+ \rightarrow e^+ X^0$ for $M_{X^0}$					$B^+ \rightarrow \mu^+ X^0$ for $M_{X^0}$				
0.1 GeV/ $c^2$	2.52-2.70	0.11	0	$0.471 \pm 0.173$	$< 2.32 \times 10^{-6}$	2.58-2.68	0.12	1	$0.420 \pm 0.151$	$< 4.26 \times 10^{-6}$
0.2	2.52-2.70	0.11	0	$0.471 \pm 0.173$	$< 2.32 \times 10^{-6}$	2.58-2.68	0.12	1	$0.420 \pm 0.151$	$< 4.19 \times 10^{-6}$
0.3	2.55-2.68	0.11	0	$0.296 \pm 0.115$	$< 2.50 \times 10^{-6}$	2.58-2.68	0.12	1	$0.420 \pm 0.151$	$< 4.26 \times 10^{-6}$
0.4	2.55-2.68	0.11	0	$0.296 \pm 0.115$	$< 2.62 \times 10^{-6}$	2.58-2.68	0.12	1	$0.420 \pm 0.151$	$< 4.22 \times 10^{-6}$
0.5	2.52-2.70	0.11	0	$0.471 \pm 0.173$	$< 2.38 \times 10^{-6}$	2.58-2.68	0.11	1	$0.420 \pm 0.151$	$< 4.37 \times 10^{-6}$
0.6	2.52-2.70	0.11	0	$0.471 \pm 0.173$	$< 2.40 \times 10^{-6}$	2.58-2.68	0.11	1	$0.420 \pm 0.151$	$< 4.49 \times 10^{-6}$
0.7	2.52-2.70	0.11	0	$0.471 \pm 0.173$	$< 2.32 \times 10^{-6}$	2.56-2.63	0.11	0	$0.447 \pm 0.153$	$< 2.29 \times 10^{-6}$
0.8	2.51-2.62	0.11	0	$0.472 \pm 0.163$	$< 2.39 \times 10^{-6}$	2.54-2.61	0.11	1	$0.469 \pm 0.162$	$< 4.32 \times 10^{-6}$
0.9	2.51-2.62	0.10	0	$0.472 \pm 0.163$	$< 2.51 \times 10^{-6}$	2.52-2.60	0.11	1	$0.588 \pm 0.201$	$< 4.23 \times 10^{-6}$
1.0	2.51-2.62	0.096	0	$0.472 \pm 0.163$	$< 2.64 \times 10^{-6}$	2.49-2.58	0.11	1	$0.817 \pm 0.266$	$< 4.04 \times 10^{-6}$
1.1	2.47-2.57	0.099	0	$0.666 \pm 0.207$	$< 2.33 \times 10^{-6}$	2.49-2.58	0.12	1	$0.817 \pm 0.266$	$< 3.87 \times 10^{-6}$
1.2	2.45-2.53	0.096	0	$0.684 \pm 0.206$	$< 2.38 \times 10^{-6}$	2.48-2.53	0.10	0	$0.582 \pm 0.179$	$< 2.32 \times 10^{-6}$
1.3	2.43-2.51	0.098	0	$0.792 \pm 0.237$	$< 2.21 \times 10^{-6}$	2.45-2.50	0.10	0	$0.705 \pm 0.211$	$< 2.26 \times 10^{-6}$
1.4	2.41-2.51	0.10	0	$1.056 \pm 0.318$	$< 1.92 \times 10^{-6}$	2.42-2.48	0.11	2	$0.947 \pm 0.282$	$< 5.78 \times 10^{-6}$
1.5	2.39-2.46	0.093	1	$0.907 \pm 0.277$	$< 4.72 \times 10^{-6}$	2.40-2.47	0.11	5	$1.171 \pm 0.351$	$< 10.56 \times 10^{-6}$
1.6	2.37-2.43	0.092	1	$0.887 \pm 0.277$	$< 4.80 \times 10^{-6}$	2.37-2.42	0.10	4	$0.977 \pm 0.295$	$< 9.60 \times 10^{-6}$
1.7	2.34-2.39	0.088	1	$0.886 \pm 0.283$	$< 5.01 \times 10^{-6}$	2.34-2.39	0.10	1	$1.116 \pm 0.337$	$< 3.94 \times 10^{-6}$
1.8	2.31-2.36	0.087	2	$1.042 \pm 0.335$	$< 7.04 \times 10^{-6}$	2.31-2.37	0.11	1	$1.518 \pm 0.452$	$< 3.31 \times 10^{-6}$



# Form factors to compute $\mathcal{B}(B^+ \rightarrow \ell^+ \nu \gamma)$

$$\frac{d\Gamma}{dE_\gamma} = \frac{\alpha_{em} G_F^2 |V_{ub}|^2}{48\pi^2} m_B^4 (1 - x_\gamma) x_\gamma^3 [F_A^2 + F_V^2]$$

where

$$F_V(E_\gamma) = \frac{Q_u m_B f_B}{2E_\gamma \lambda_B(\mu)} R(E_\gamma, \mu) + \left[ \xi(E_\gamma) + \frac{Q_b m_B f_B}{2E_\gamma m_b} + \frac{Q_u m_B f_B}{(2E_\gamma)^2} \right]$$

and

$$F_A(E_\gamma) = \frac{Q_u m_B f_B}{2E_\gamma \lambda_B(\mu)} R(E_\gamma, \mu) + \left[ \xi(E_\gamma) - \frac{Q_b m_B f_B}{2E_\gamma m_b} - \frac{Q_u m_B f_B}{(2E_\gamma)^2} + \frac{Q_l f_B}{E_\gamma} \right].$$