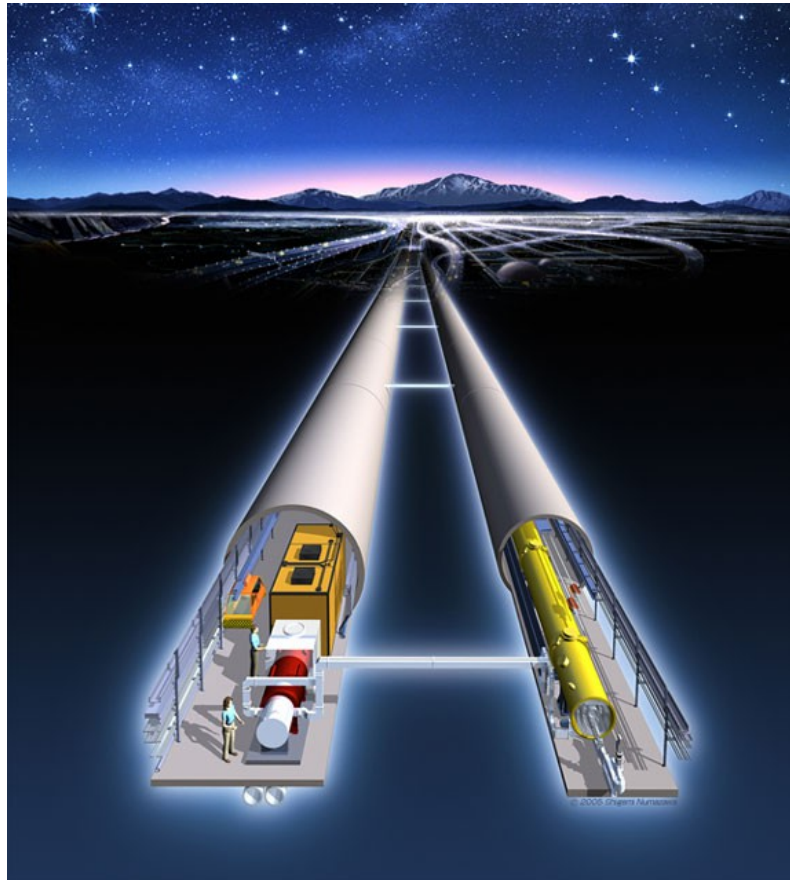


Top quark physics at Linear Colliders



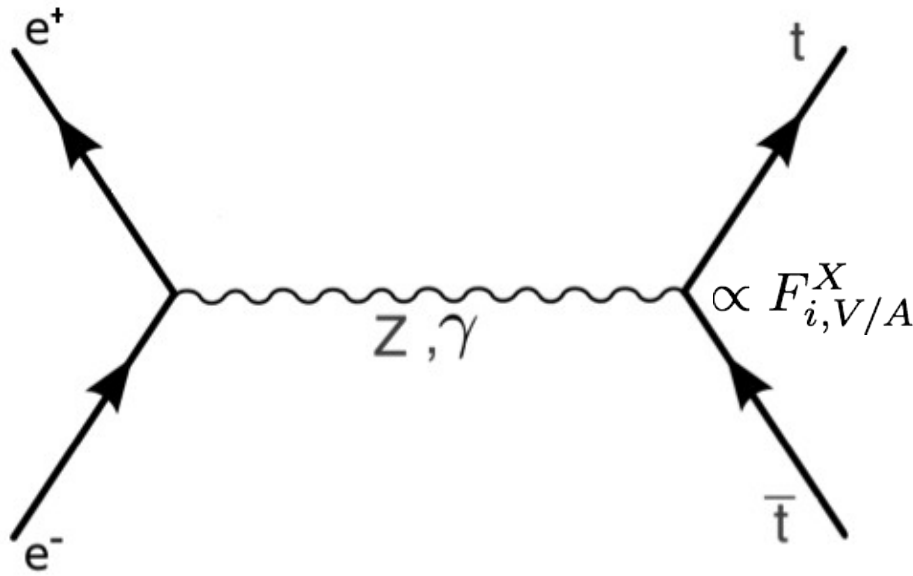
Roman Pöschl



On behalf of ...
... many people contributing to
top physics at the LC
... the LC Collaboration

Latest reference document:

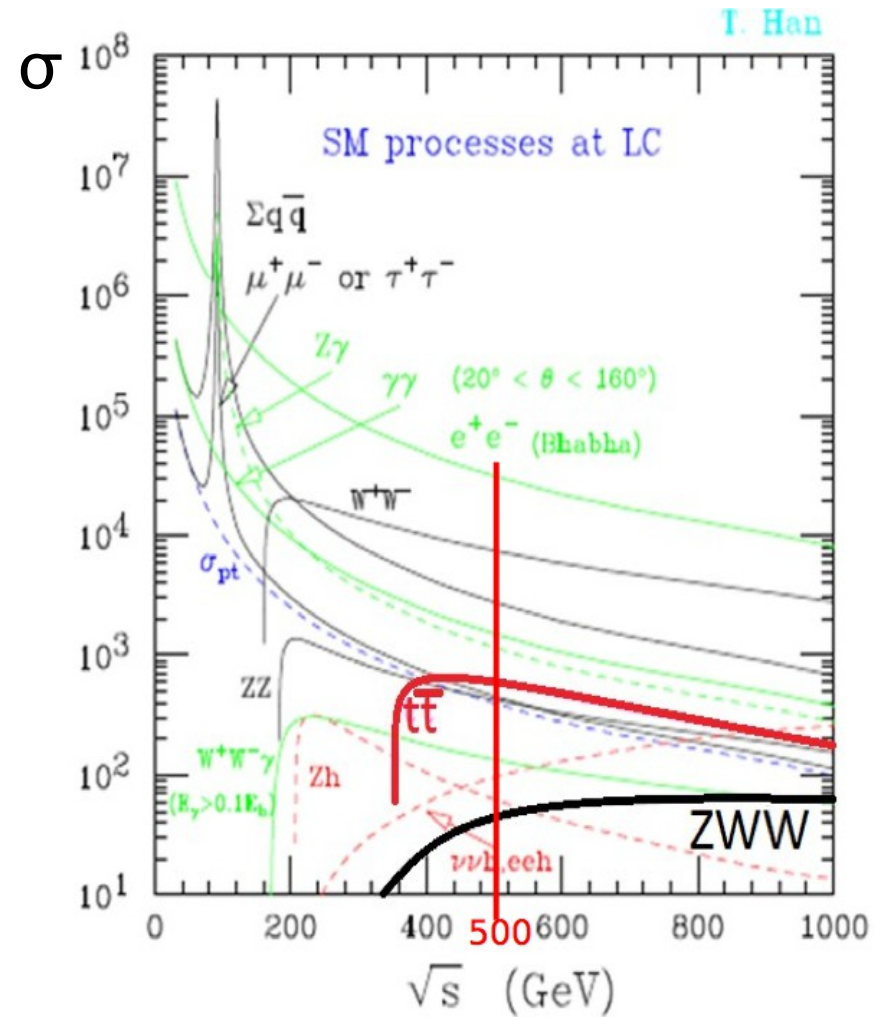
[arxiv:1506.05992](https://arxiv.org/abs/1506.05992) – ILC Physics case

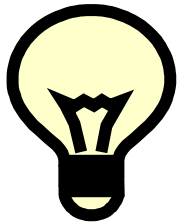


- Top quark production through electroweak processes
no competing QCD production => Small theoretical errors!

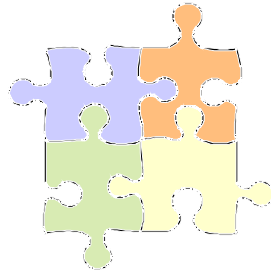
- High precision measurements

- Top quark mass at ~ 350 GeV through threshold scan
- Polarised beams allow testing chiral structure at $t\bar{t}X$ vertex
=> Precision on form factors F and/or couplings g



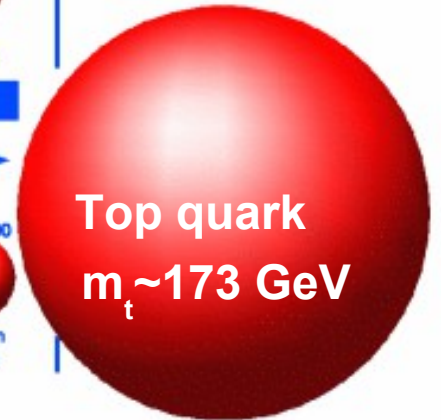


Elementary Scalar?



Composite object?

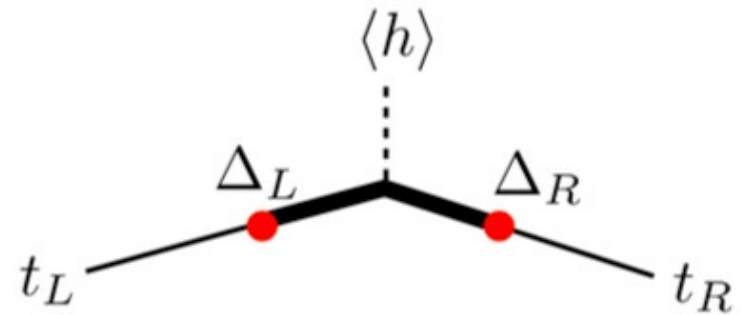
LEPTONS		
Electron Neutrino Mass -0	Muon Neutrino -0	Tau Neutrino -0
Electron .511	Muon 105.7	Tau 1 777
QUARKS		
Up Mass: 5	Charm 1 500	Top ~180 000
Down 8	Strange 160	Bottom 4 250



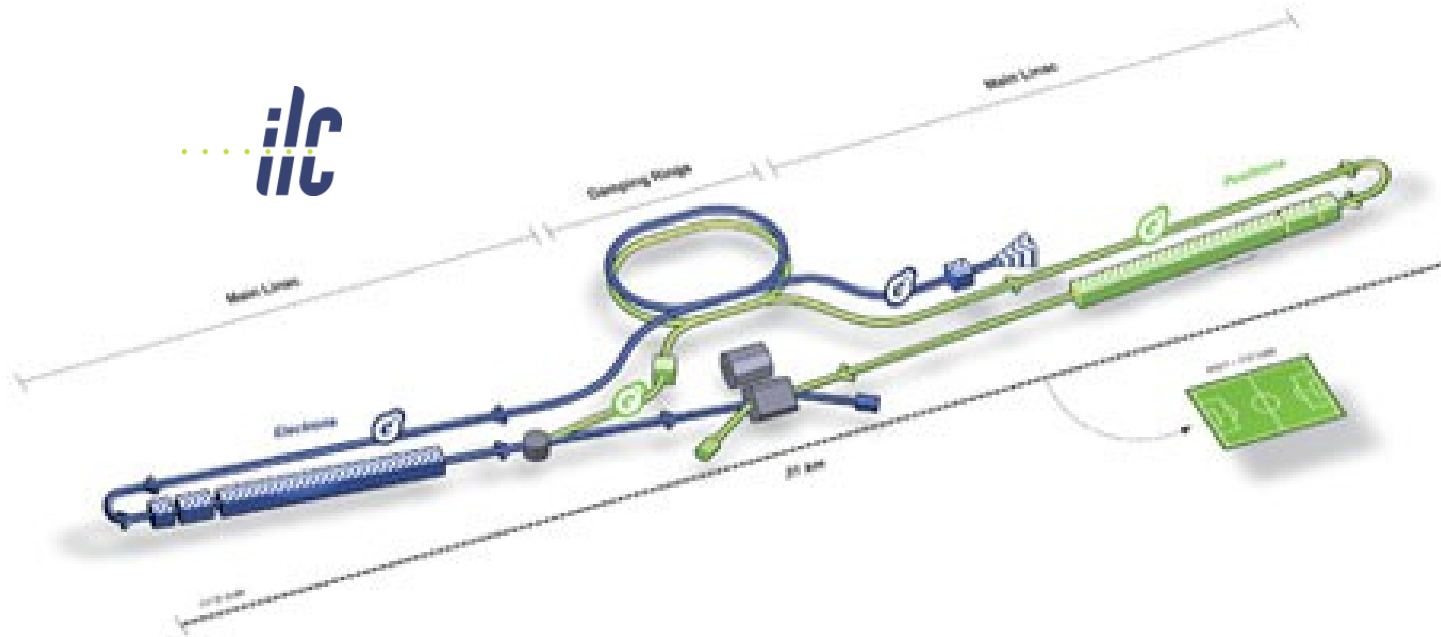
- Higgs and top quark are intimately coupled!
Top Yukawa coupling $O(1)$!
=> Top mass important SM Parameter

- New physics by compositeness?
Higgs and top composite objects?

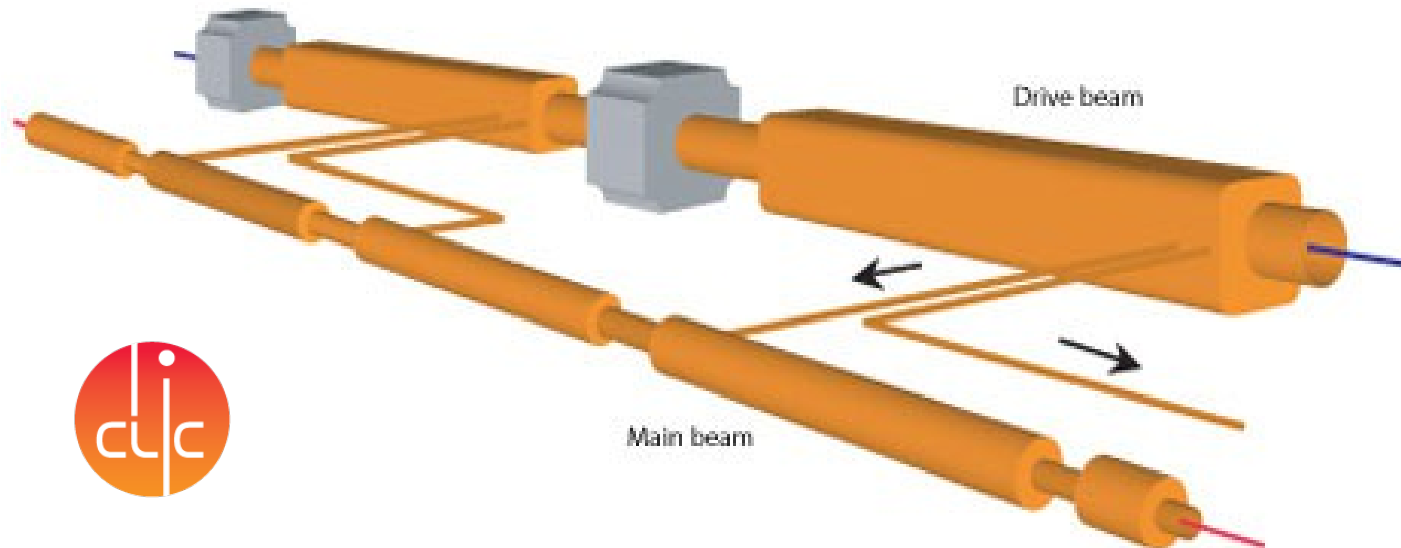
- High energy lepton colliders perfectly suited to decipher both particles



Courtesy of S. Rychkov



Energy: 0.1 - 1 TeV
Electron (and positron)
polarisation
TDR in 2013
+ DBD for detectors
 Footprint 31 km



Energy: 0.5 - 3 TeV
CDR in 2012
 Footprint 48km

Track momentum: $\sigma_{1/p} < 5 \times 10^{-5}/\text{GeV}$ (1/10 x LEP)

(e.g. Measurement of Z boson mass in Higgs Recoil)

Impact parameter: $\sigma_{d_0} < [5 \oplus 10/(p[\text{GeV}]\sin^{3/2}\theta)] \mu\text{m}$ (1/3 x SLD)

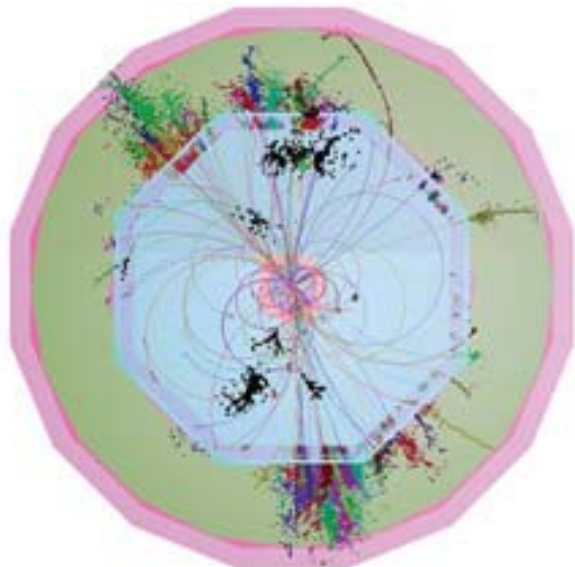
(Quark tagging c/b)

Jet energy resolution : $dE/E = 0.3/(E(\text{GeV}))^{1/2}$ (1/2 x LEP)

(W/Z masses with jets)

Hermeticity : $\theta_{\min} = 5 \text{ mrad}$

(for events with missing energy e.g. SUSY)



Final state will comprise events with a large number of charged tracks and jets(6+)

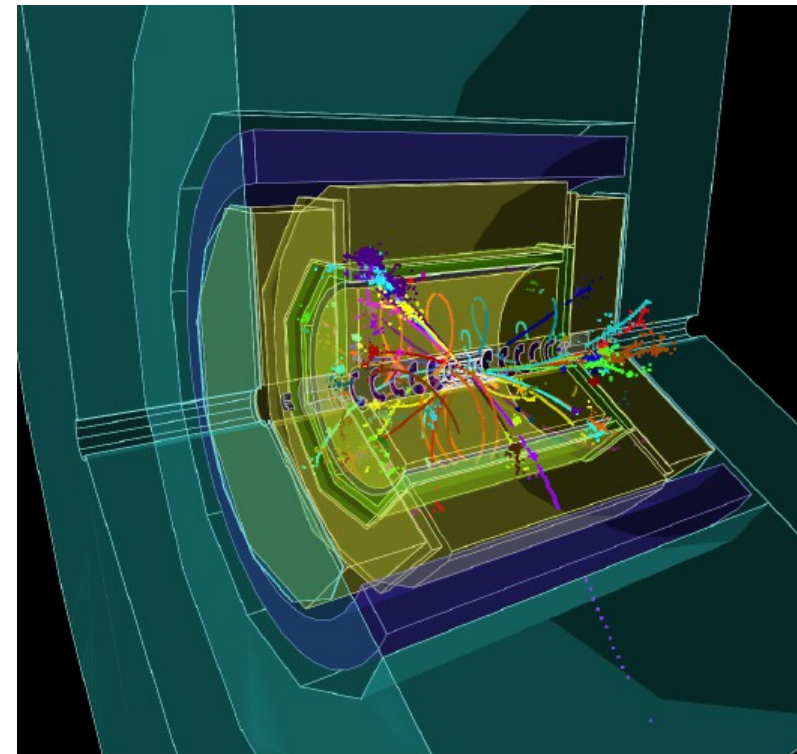
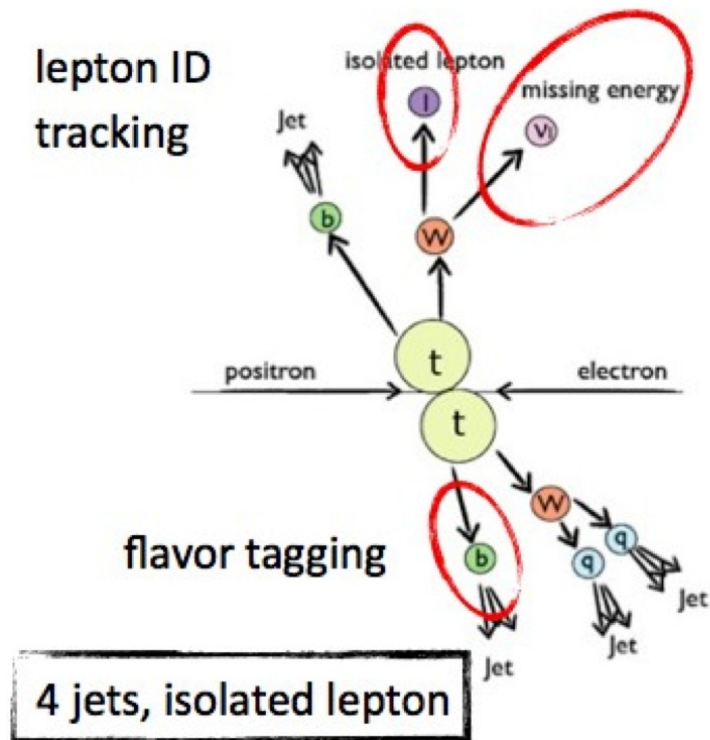
- High granularity
- Excellent momentum measurement
- High separation power for particles
- **Particle Flow Detectors**

Advanced concepts: ILD, SiD and CLIC Detector

Three different final states:

- 1) Fully hadronic (46.2%) → 6 jets
- 2) Semi leptonic (43.5%) → 4 jets + 1 charged lepton and a neutrino
- 3) Fully leptonic (10.3%) → 2 jets + 4 leptons

$$t\bar{t} \rightarrow (bW)(bW) \rightarrow (bqq')(bl\nu)$$



Final state reconstruction uses all detector aspects

Results shown in the following are based on full simulation of LC Detectors

ILC:

	Stage	500			500 LumiUP		
Scenario	\sqrt{s} [GeV]	500	350	250	500	350	250
G-20	$\int \mathcal{L} dt$ [fb^{-1}]	1000	200	500	4000	-	-
	time [years]	5.5	1.3	3.1	8.3	-	-
H-20	$\int \mathcal{L} dt$ [fb^{-1}]	500	200	500	3500	-	1500
	time [years]	3.7	1.3	3.1	7.5	-	3.1
I-20	$\int \mathcal{L} dt$ [fb^{-1}]	500	200	500	3500	1500	-
	time [years]	3.7	1.3	3.1	7.5	3.4	-

	Stage	500			500 LumiUP		
Scenario	\sqrt{s} [GeV]	250	500	350	250	350	500
Snow	$\int \mathcal{L} dt$ [fb^{-1}]	250	500	200	900	-	1100
	time [years]	4.1	1.8	1.3	3.3	-	1.9

For details see: [arxiv: 1506.07830](https://arxiv.org/abs/1506.07830)

CLIC:

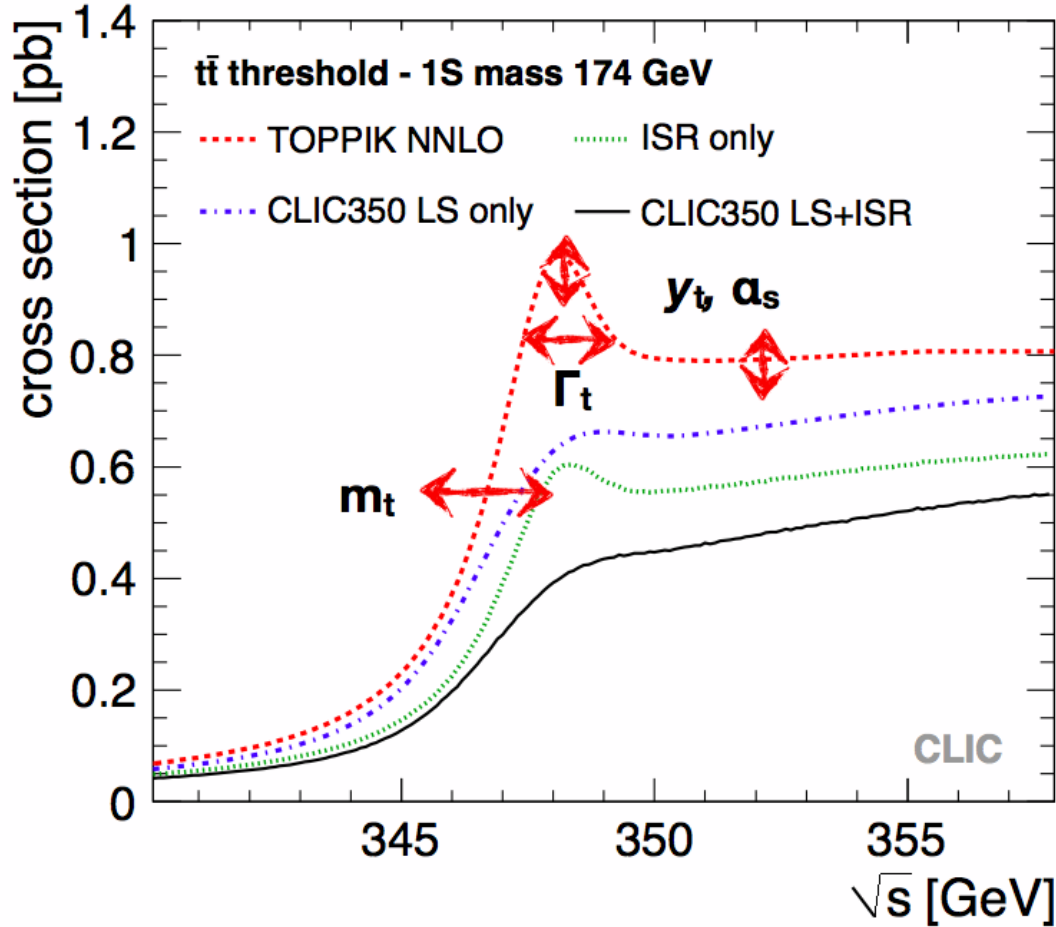
~380 GeV 500 fb^{-1} : precision Higgs and **top physics**

~1.4 TeV 1.5 ab^{-1} : BSM physics, precision Higgs physics and **top physics**

~ 3 TeV, 2 ab^{-1} : BSM physics, precision Higgs

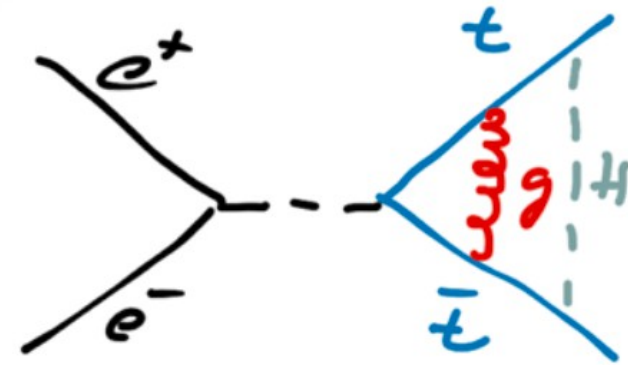
Running scenarios favour early start of top physics programme

Small size of $t\bar{t}$ “bound state” at threshold ideal remise for precision physics



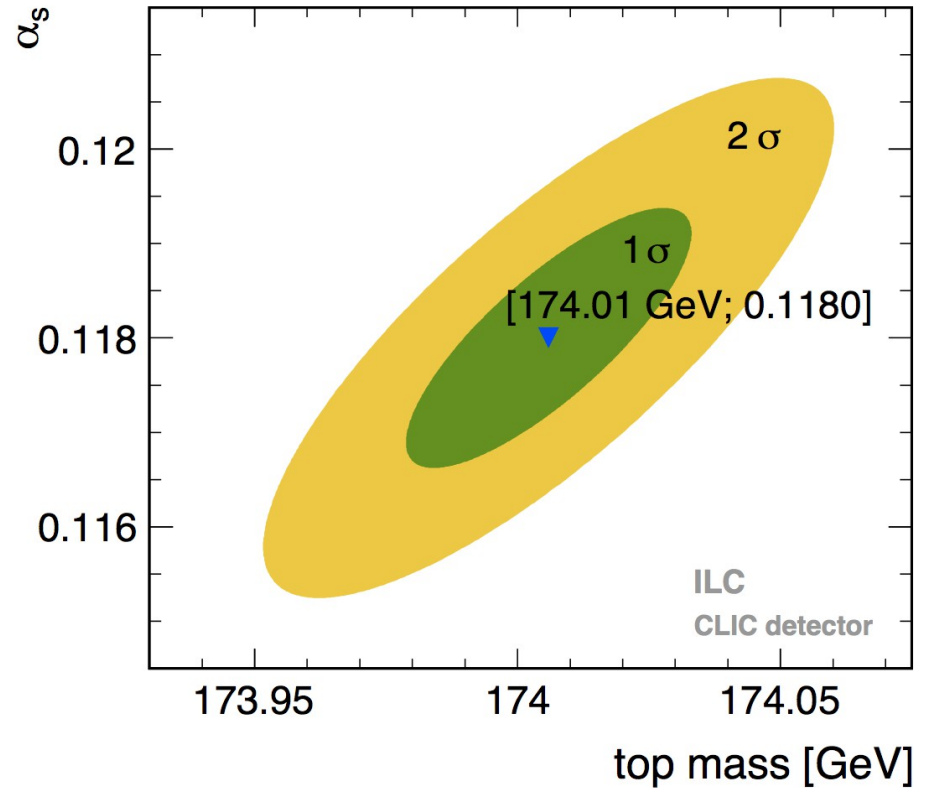
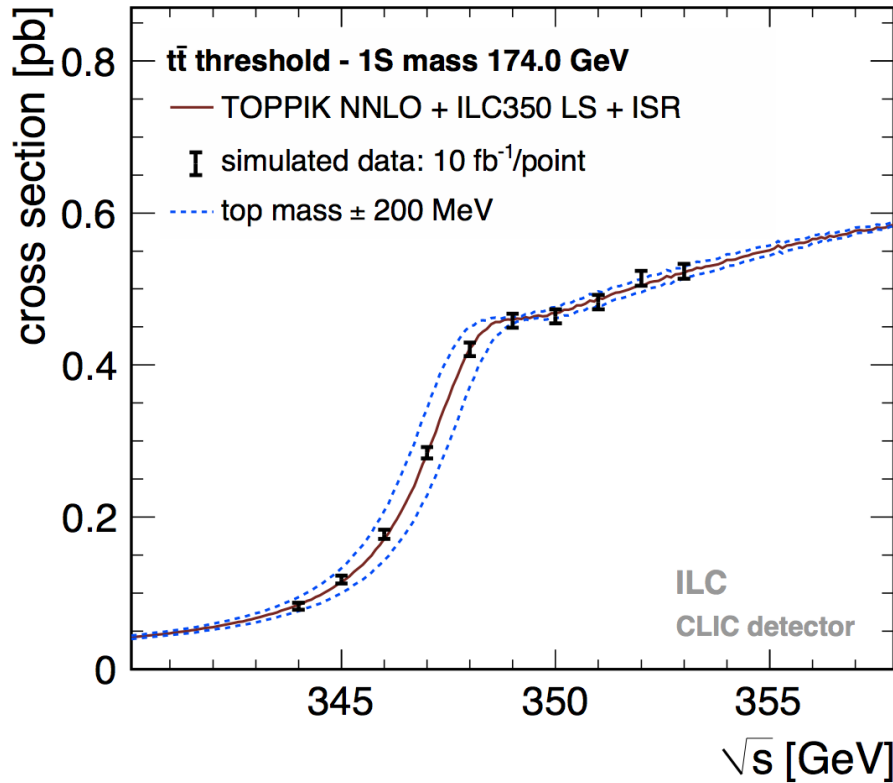
Cross section around threshold is affected by several properties of the top quark and by QCD

- Top mass, width Yukawa coupling
- Strong coupling constant



Effects of some parameters are correlated:
Dependence on Yukawa coupling rather weak,
Precise external α_s helps

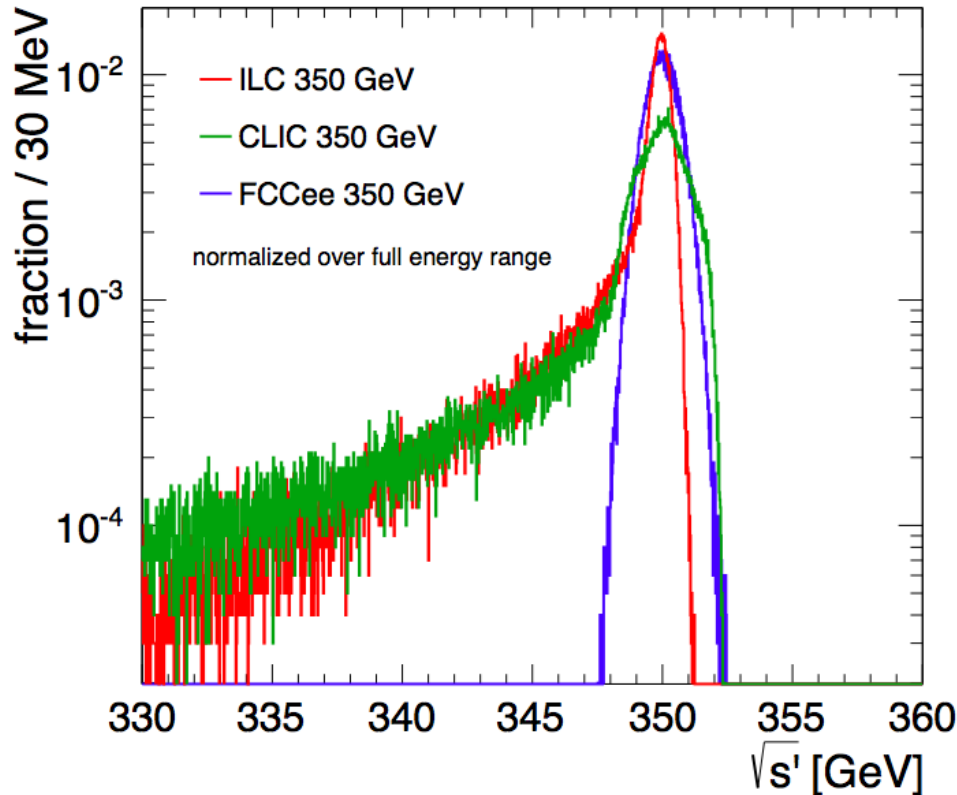
Mass and α_s



~100 MeV

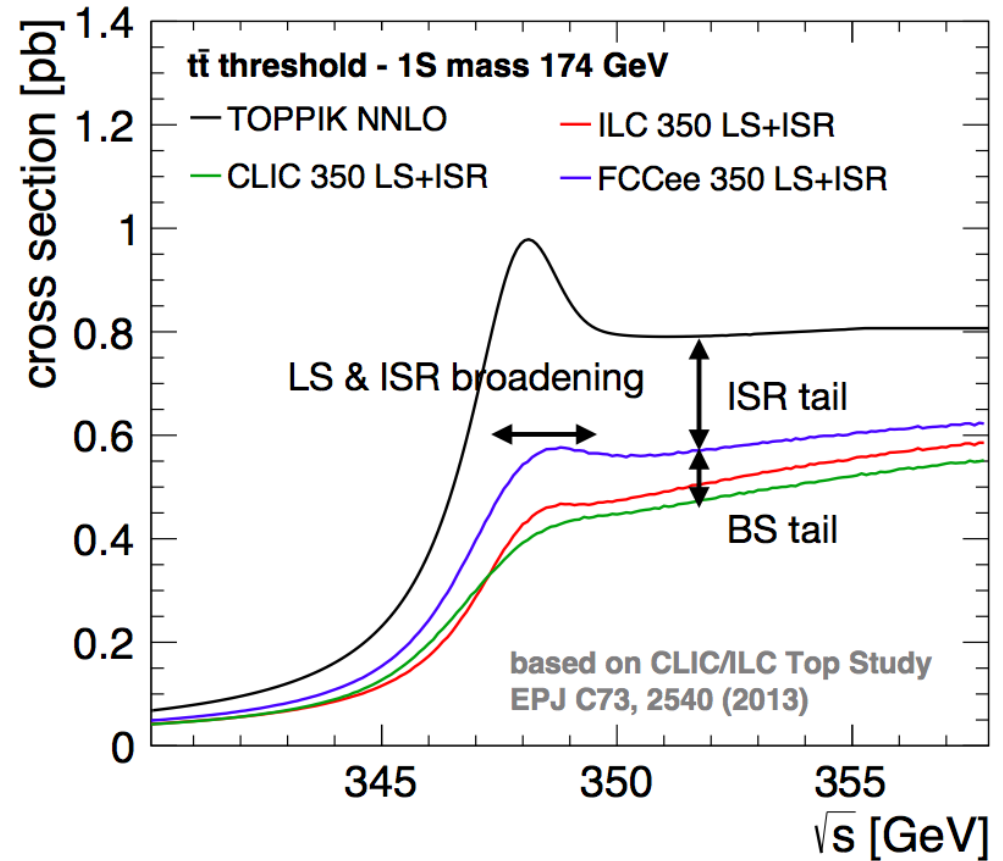
1S top mass and α_s combined 2D fit

m_t stat. error	27 MeV
m_t theory syst. (1%/3%)	5 MeV / 9 MeV
α_s stat. error	0.0008
α_s theory syst. (1%/3%)	0.0007 / 0.0022



- Slight changes in statistics due to cross section, changes in sensitivity due to steepness of threshold turn on
- For 100 fb⁻¹, no polarisation, 1D mass fit
 16 MeV → 18 MeV → 21 MeV (stat.)
 FCCee ILC CLIC

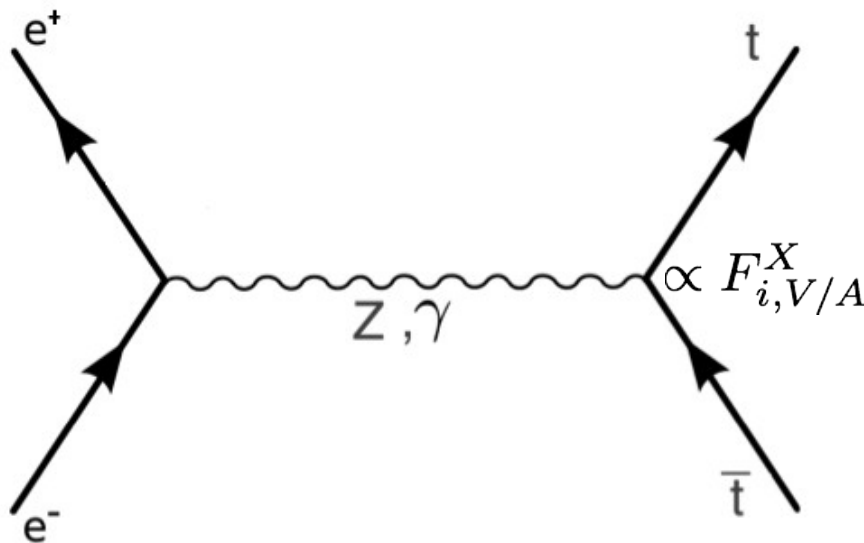
- Somewhat different luminosity spectra for different machines
- No beamstrahlung in storage ring
- Sharper main peak at ILC broader for CLIC



- Expected statistical uncertainty **10 – 30 MeV**
- Experimental systematics
 - Beam energy: **~30 MeV** or lower
 - Non-ttbar background, selection efficiencies: **~ 15 MeV**
 - Luminosity spectrum: **10 MeV**
 - Single top contamination: **< 30 MeV**
- Theory uncertainties
 - Normalisation: **~55 MeV (naive estimate)** much smaller due to recent NNNLO calculations arxiv: 1506.06864, arxiv:1506.06542
 - When not included in the fit: $\sim 3 \text{ MeV per } 10^{-4}$ uncertainty on α_s today \rightarrow **~18 MeV**
 - Conversion from 1S/PS masses to MSbar mass Currently: **~50 MeV**
However conversion now known to N⁴LO (arxiv:1502.01030)
 - Now at point where results become sensitive to effects other than QCD



- Fermion mass generation closely related to the origin electroweak symmetry breaking
- Expect residual effects for particles with masses closest to symmetry breaking scale



Manifestation of New Physics:

- Modification of Ztt coupling
Mixing between top and partners
Mixing Z/Z'
- s-channel exchange of New Z'
Including interference effects

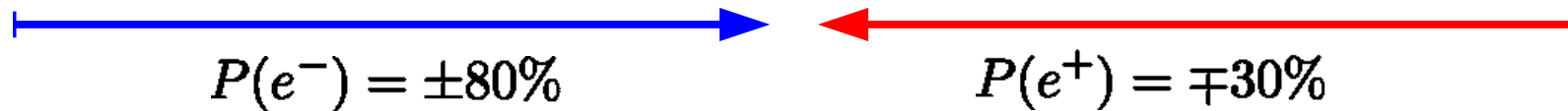
$$\Gamma_{\mu}^{ttX}(k^2, q, \bar{q}) = -ie \left\{ \gamma_{\mu} (F_{1V}^X(k^2) + \gamma_5 F_{1A}^X(k^2)) + \frac{\sigma_{\mu\nu}}{2m_t} (q + \bar{q})^{\nu} (iF_{2V}^X(k^2) + \gamma_5 F_{2A}^X(k^2)) \right\}, \quad (2)$$

Pure γ or pure Z^0 : $\sigma \sim (F_i)^2 \Rightarrow$ No sensitivity to sign of Form Factors

Z^0/γ interference : $\sigma \sim (F_i) \Rightarrow$ Sensitivity to sign of Form Factors

At ILC **no** separate access to ttZ or $t\bar{t}\gamma$ vertex, but ...

ILC 'provides' two beam polarisations



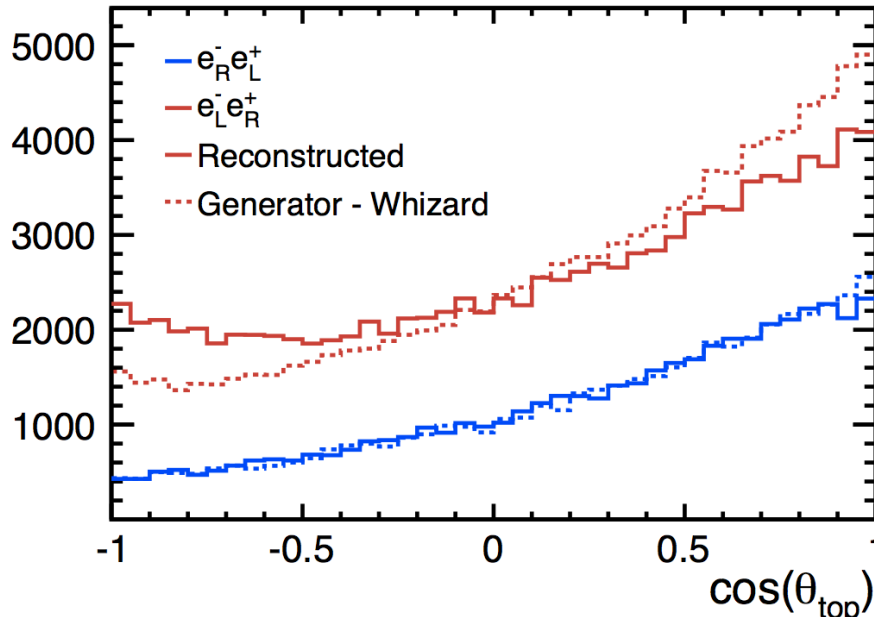
There exists a number of observables sensitive to chiral structure, e.g.

σ_I	$A_{FB,I}^t = \frac{N(\cos\theta > 0) - N(\cos\theta < 0)}{N(\cos\theta > 0) + N(\cos\theta < 0)}$	$(F_R)_I = \frac{(\sigma_R)_I}{\sigma_I}$
x-section	Forward backward asymmetry	Fraction of right handed top quarks



Extraction of relevant unknowns

$$\begin{array}{c}
 F_{1V}^\gamma, F_{1V}^Z, F_{1A}^\gamma = 0, F_{1A}^Z \\
 F_{2V}^\gamma, F_{2V}^Z
 \end{array}
 \quad \text{or equivalently} \quad
 g_L^\gamma, g_R^\gamma, g_L^Z, g_R^Z$$

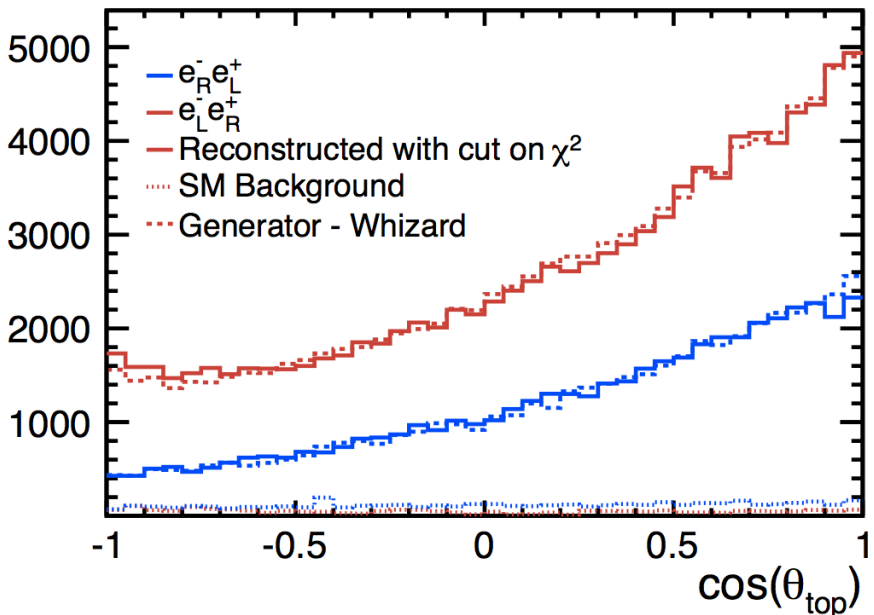


Ambiguities in case of
left handed electron beams
Due to V-A structure at ttX vertex

Precise reconstruction of θ_{top}
in case of **right** handed electron beams

Remedy to address ambiguities:
Select cleanly reconstructed
events by χ^2 analysis

or
Reconstruction of b quark charge



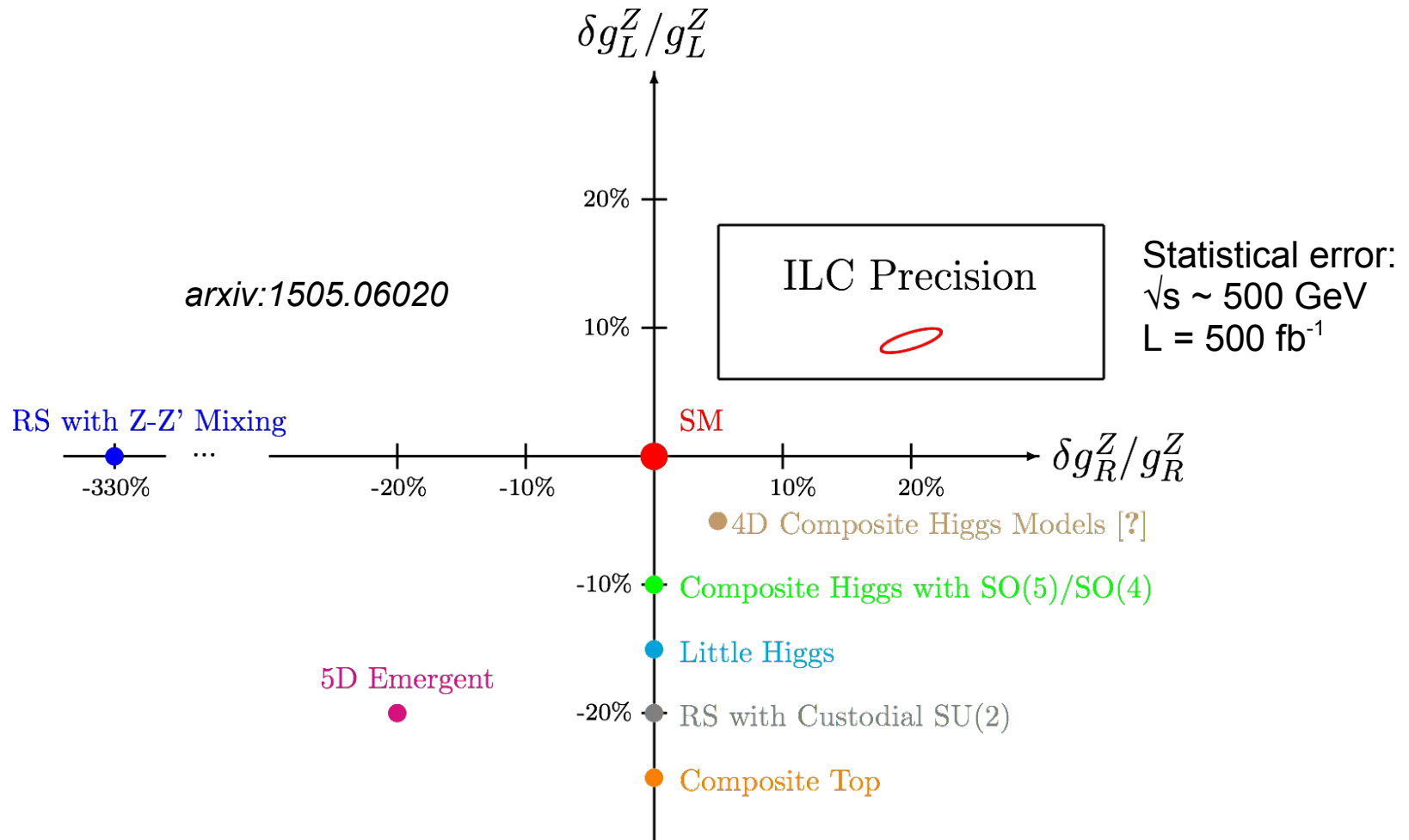
Precise reconstruction for both
beam polarisations

- Efficiency Penalty for e_L
- ϵ_{tot} : $e_R \sim 50\%$, $e_L \sim 30\%$

Results:

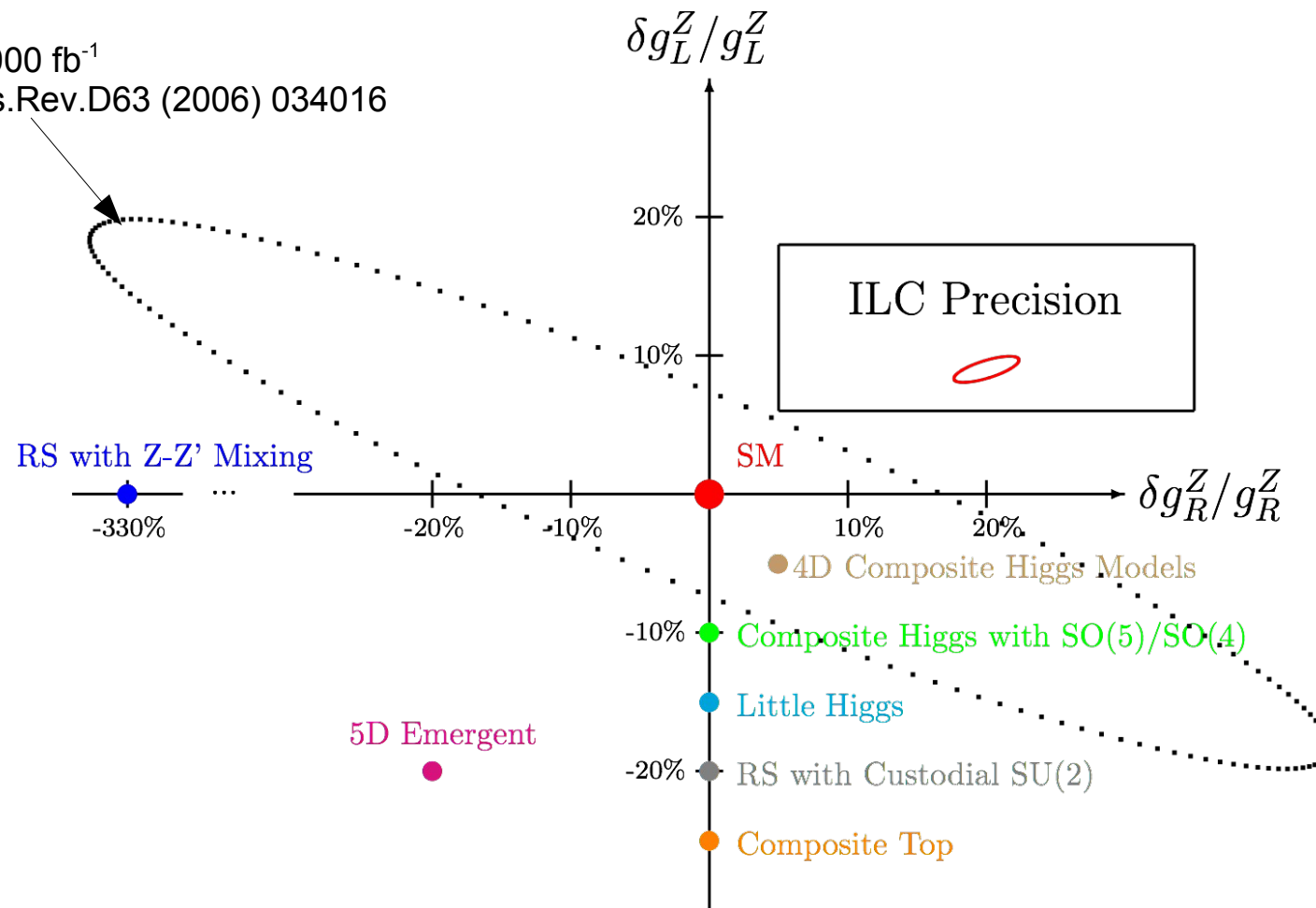
$\mathcal{P}_{e^-}, \mathcal{P}_{e^+}$	$(\delta\sigma/\sigma)_{\text{stat.}} [\%]$	$(\delta A_{FB}^t/A_{FB}^t)_{\text{stat.}} [\%]$
-0.8, +0.3	0.47	1.8
+0.8, -0.3	0.63	1.3

Top is primary candidate to be a messenger new physics in many BSM models
Incorporating compositeness and/or extra dimensions



Precision expected for top quark couplings will allow to distinguish between models

Remark: All presented models are compatible with LEP elw. precision data

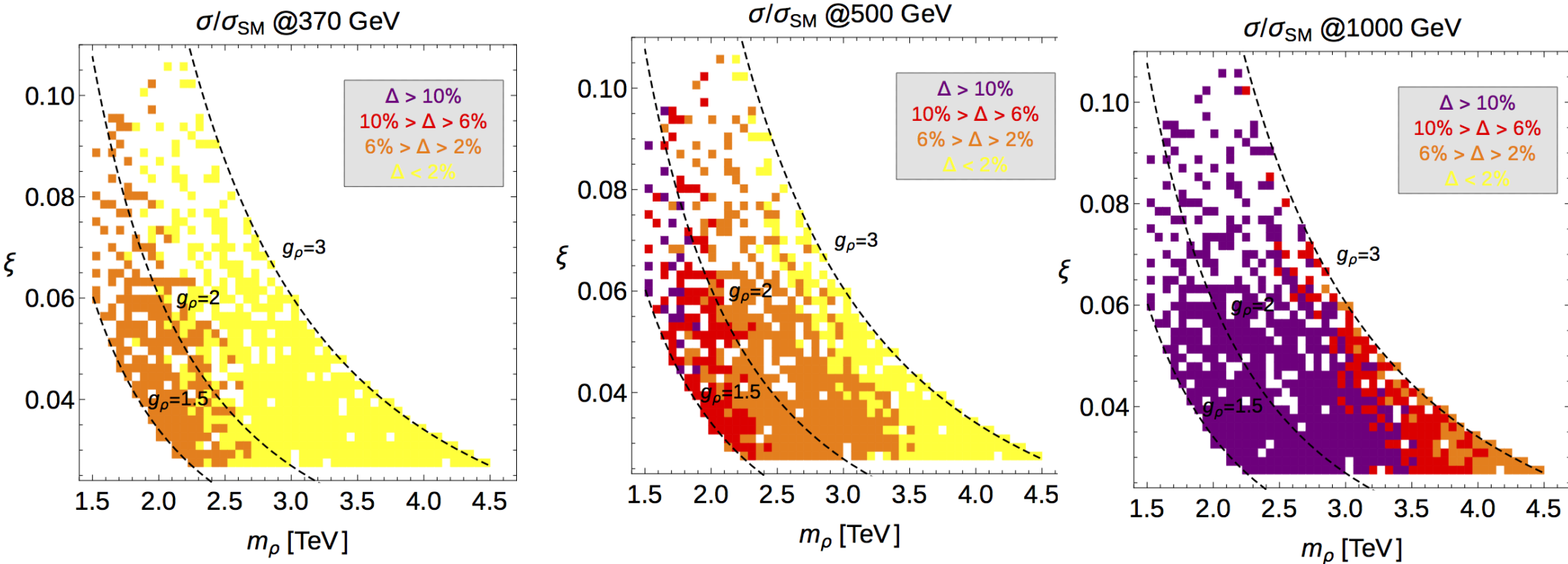


Linear Collider will outperform LHC results

- Particular poor constraint on g_R (this holds also for flavor physics results)
- LHC LO QCD analysis, ~30% improvement through NLO QCD
- LHC may still be capable to exclude models

Example: Sensitivity to $M_{Z'} = M_\rho$ in 4D Higgs Composite Model, arxiv: 1504.05407

$$\frac{\delta g_I}{g_I} \sim \xi \sim \left(\frac{v g_\rho}{M_\rho} \right)^2$$

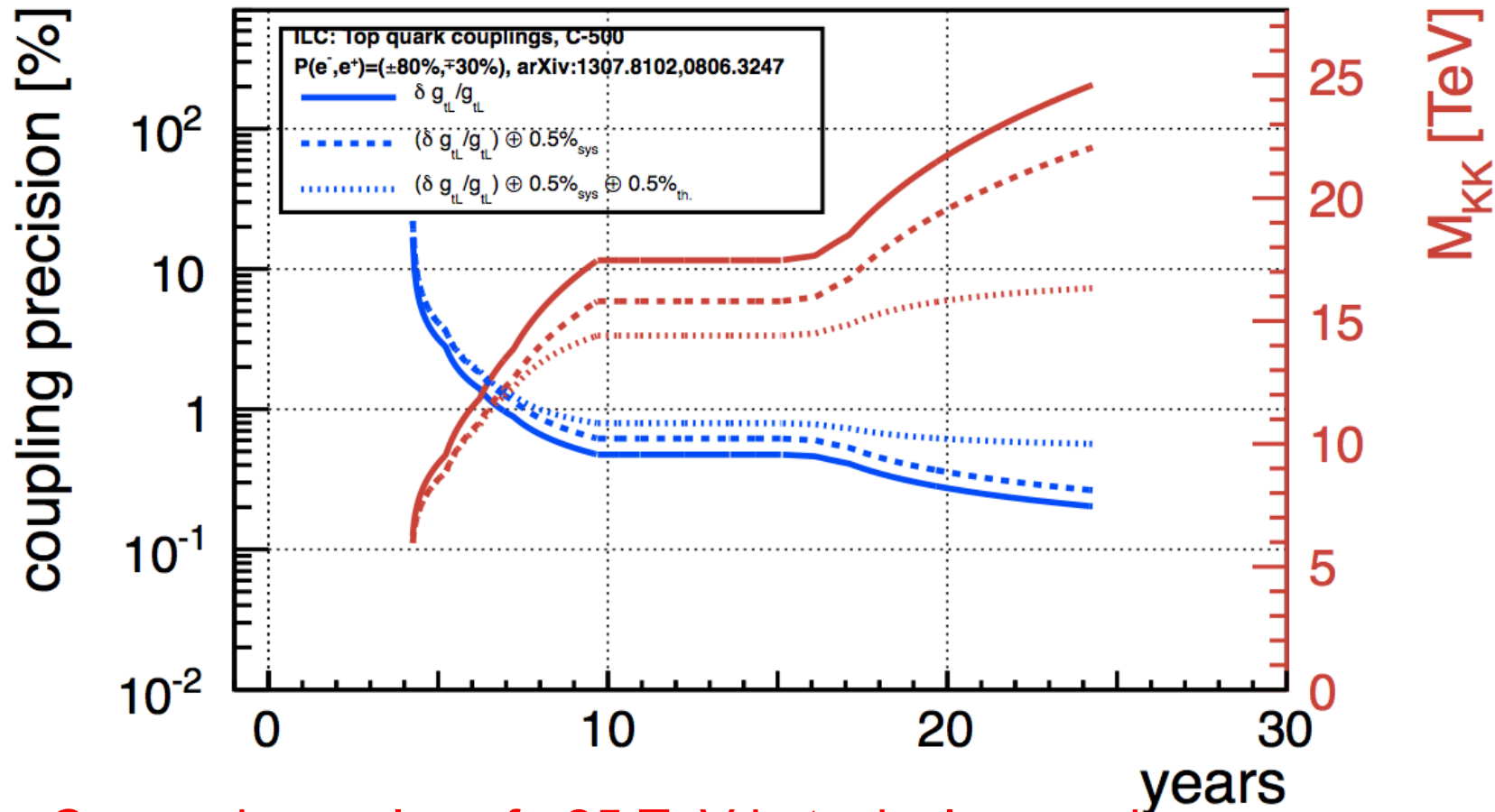


\sqrt{s}

Effects observed at smaller energies may be amplified at higher energies

New physics reach for typical BSM scenarios with composite Higgs/Top and or extra dimensions

Based on phenomenology described in Pomerol et al. arXiv:0806.3247

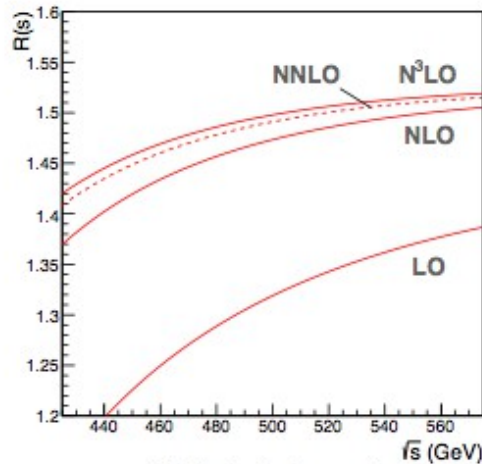


Can probe scales of ~25 TeV in typical scenarios

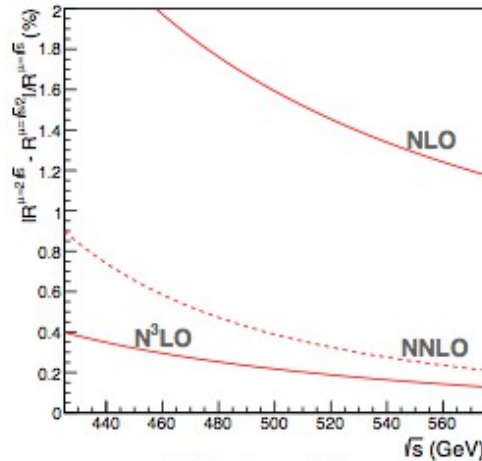
(... and up to 80 TeV for extreme scenarios)

=> Important guidance for e.g. 100 TeV pp-collider

*QCD corrections are known up to N³LO



(a) Perturbation series

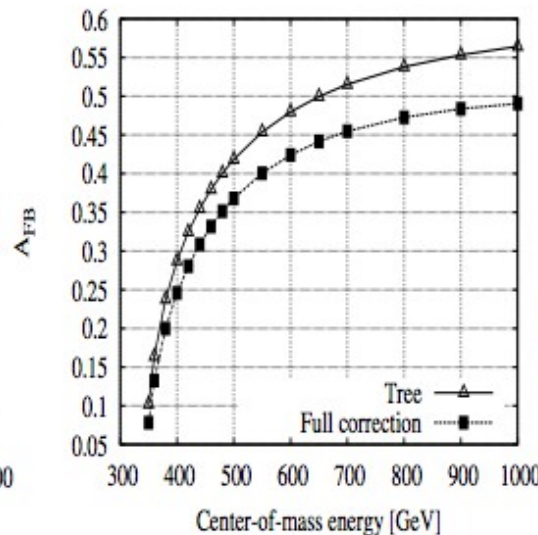
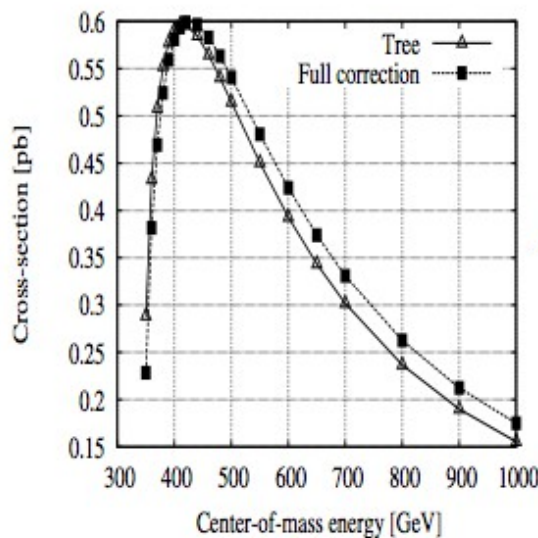


(b) Scale variations

QCD correction (N³LO) is
at the per mil level

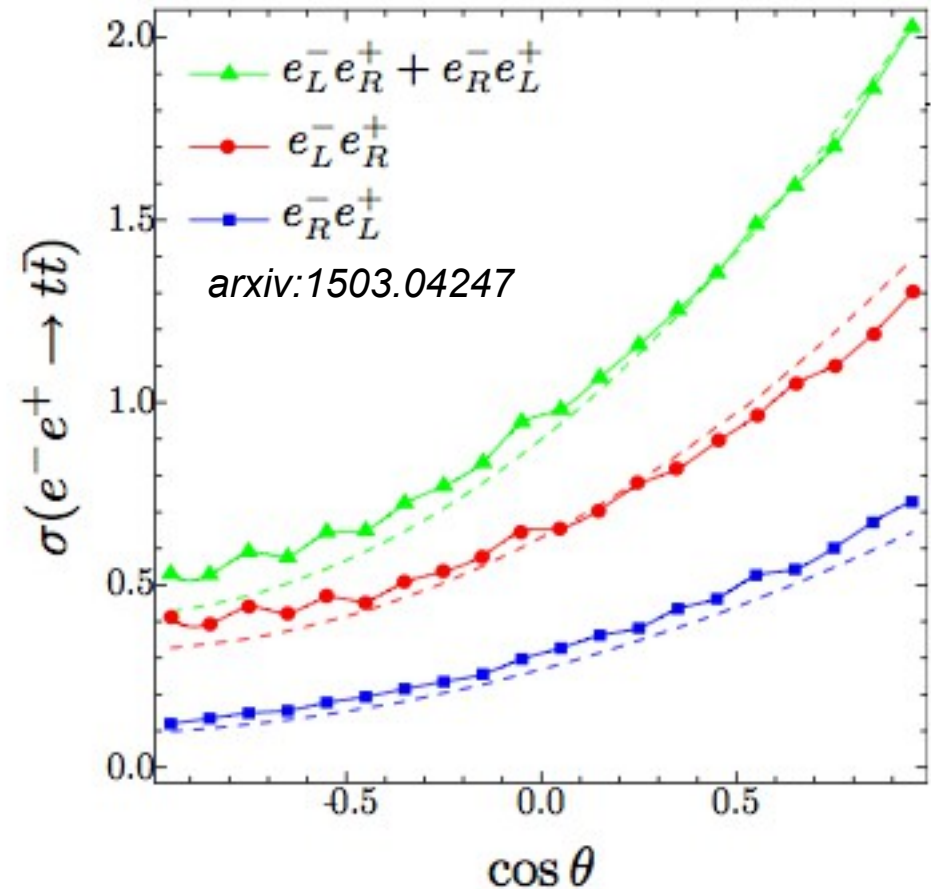
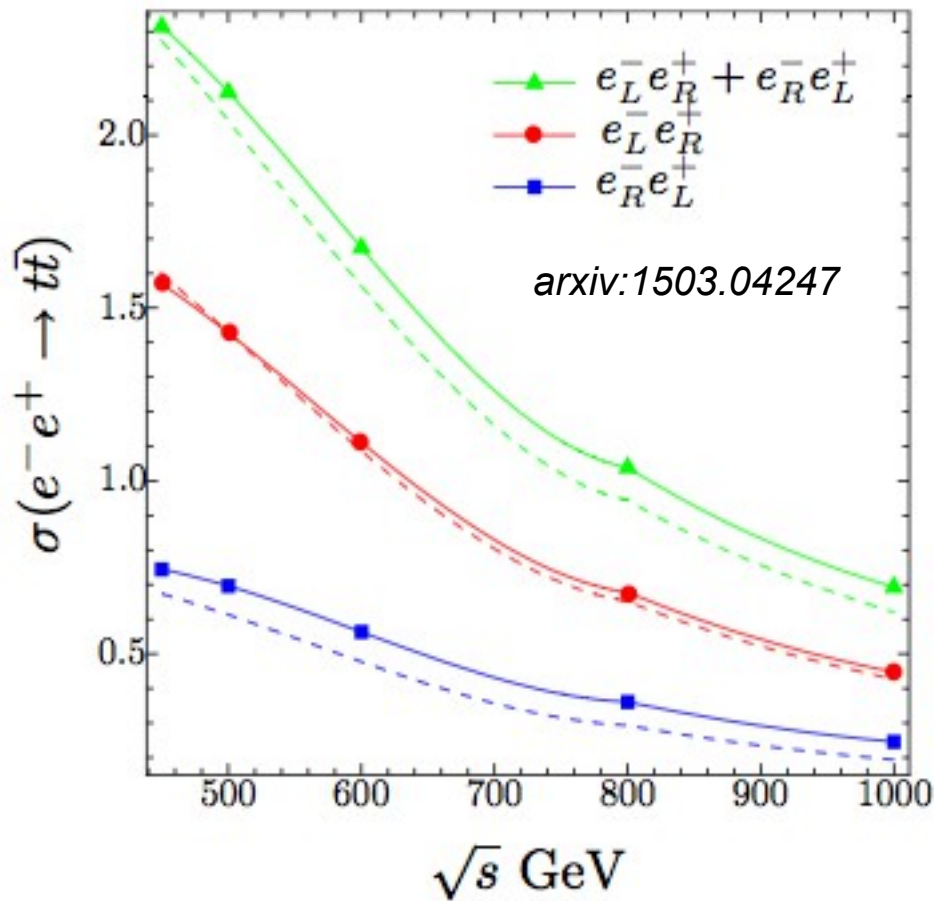
Kiyo, Maier, Maierhofer, Marquard, NCP B823 ('09)
*Bernreuther, Bonciani, Gehrmann, Heinesch,
Leineweber. NPB750 ('06)*
Hoang, Mateu, Zebarjad, NPB813 ('09)

*Electroweak corrections are known at one-loop level



EW correction at one-loop is
~5% for cross section
~10% for A_{FB}

Fleischer, Leike, Riemann, Werthenbach, EJPC31 ('03)
*Kheim, Fujimoto, Ishikawa, Kaneko, Kato,
arXiv:1211.1112*



- Electroweak corrections manifest themselves differently for different beam polarisations

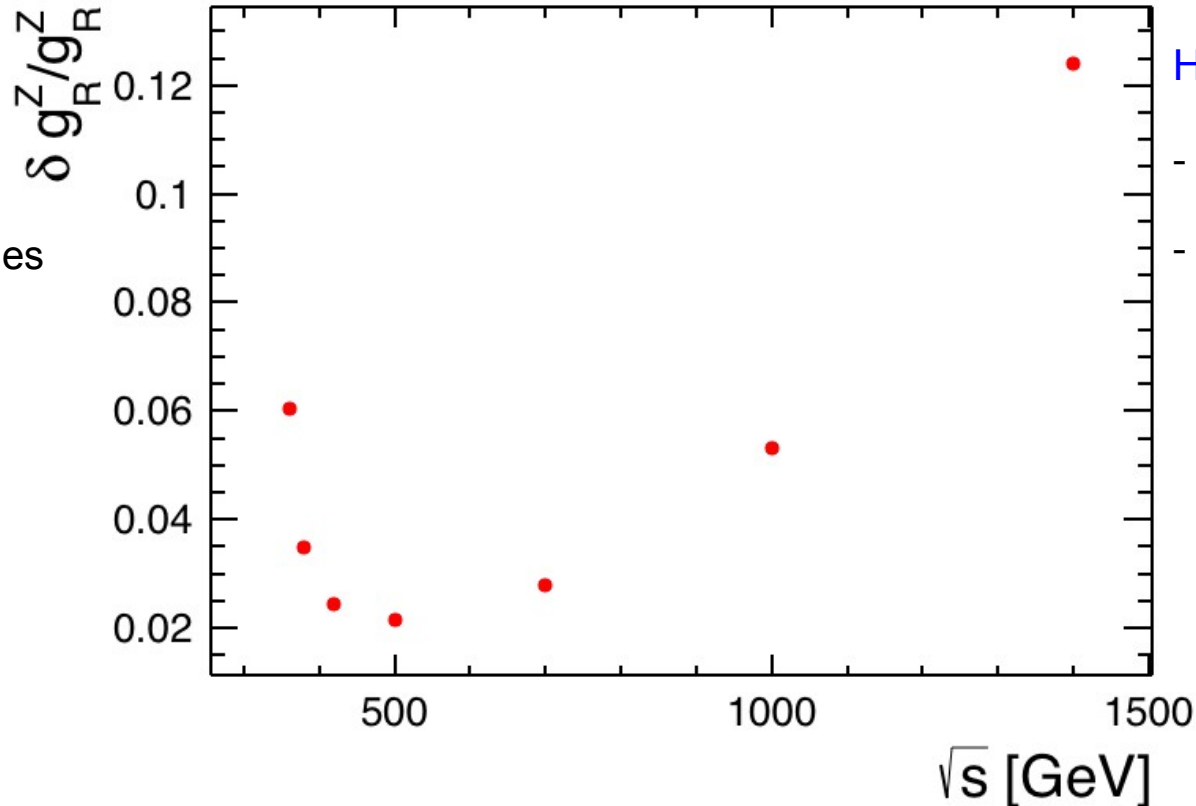
Beam polarisation important asset to disentangle SM and effects of new physics

Configuration $e_R^-e_L^+$ seems to lead to “simpler” corrections

... simplified discussion

Small cms energies:

- Vanishing axial vector coupling
- large QCD uncertainties ... and
- Lumi decreases at linear colliders



High cms energies:

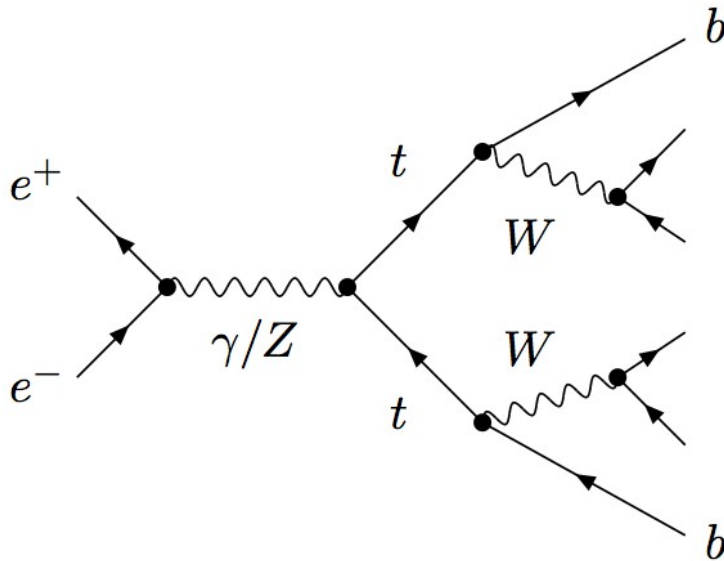
- Quickly decreasing cross section
- ... partially compensated by increasing luminosity

Broad minimum between 400 and 700 GeV

$\sqrt{s} \sim 500$ GeV is “sweet spot” for coupling measurements

However:

- Sensitivity to CP violating Higgs at smaller cms energies
- New physics at higher energies may increase cross section (see above)



Top pair production is effectively $ee \rightarrow 6f$ process

- Role of (indistinguishable) single top production (Eur. Phys. J. C (2015) **75**: 223)
Only relevant for e_L
- QCD and electroweak corrections for top decay chain
- Effects of finite top width and V_{tb} instead of Γ_t
- Exploitation of information of final state by matrix element method (arxiv: 1503.04247)
Unbiased access to tensorial CP violating form factors !?
- Exotic decays as e.g. $t \rightarrow ch$

- A LC is the right machine for **rediscovery of the top quark** by precision physics
 - Production top pairs in electroweak production!!!
 - Essential pillar of LC physics program
 - Experimental programme can take full advantage of flexible running (cms energy)
- Full simulation available for LC detectors
 - => Great deal of realism and confidence in perspectives
- Precision on top mass reach 50 MeV regime (200 fb⁻¹ or less needed)
 - Effort was driven by experimental study, now need to feedback newest theory insights
- Precision on form factors and couplings of the order of 1% with minimal ILC running scenario
 - Sensitivity to new physics up to several 10 TeV
 - Main experimental challenge is control of migrations in A_{FB}
 - Beam polarisation is major asset for control of theoretical and experimental ambiguities
- Start to address full 6 fermion final state instead of tt only
- Keeping all the promises is hardest task in coming years
 - Need full understanding of systematics for optimal detector and machine design

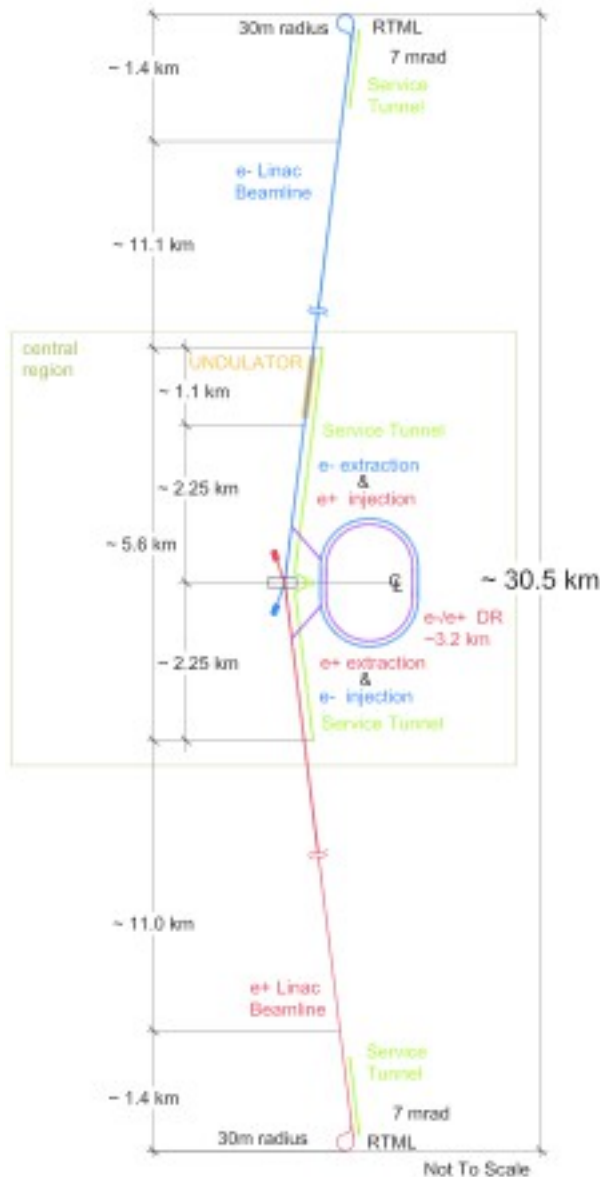
Backup

ILC design parameters	
\sqrt{s}	91-500 GeV
\mathcal{L}	$2 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
P_{e^-}	>80%
P_{e^+}	upto 30%
Length	~31 km

Comment

- 500 GeV is baseline
Option to upgrade to 1 TeV
- ~Factor 4 technically possible
- Proven by SLC
- ~Conservative estimate
- Current site allows for 50km

- Discussion on possible running scenarios has started
- Luminosity and running time to achieve at a ~25 years research programme
That includes running at 250 GeV, 350 GeV, 500 GeV and 1 TeV
- No official statement yet but integrated luminosities indicated in following transparencies are realistic



• SCRF Technology

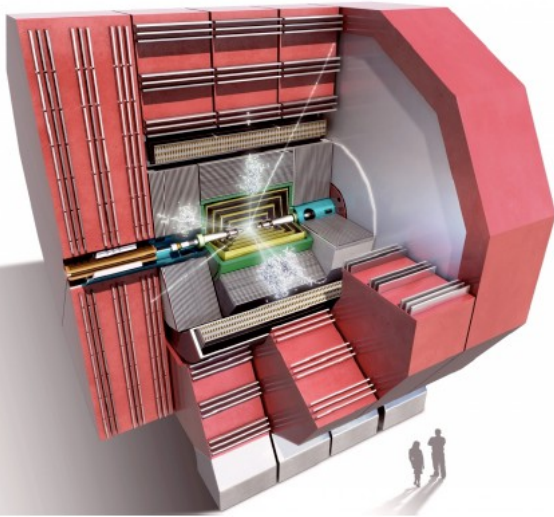
- 1.3GHz SCRF with 31.5 MV/m
- 17,000 cavities
- 1,700 cryomodules
- 2×11 km linacs

Luminosity

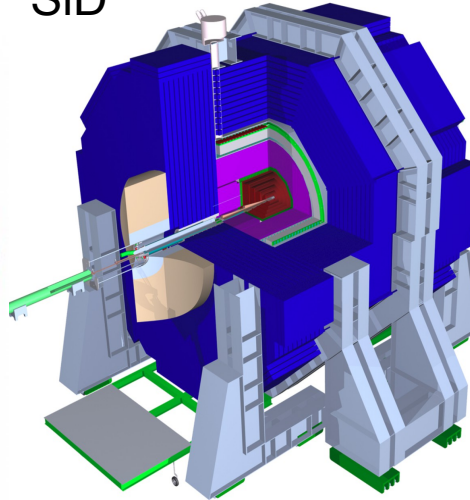
$$L \propto \frac{\eta_{RF} P_{RF}}{E_{cm}} \sqrt{\frac{\delta_{BS}}{\epsilon_{n,y}}} H_D$$

$\eta_{RF} \sim 40\%$ for SCRF technology
-> efficient technology

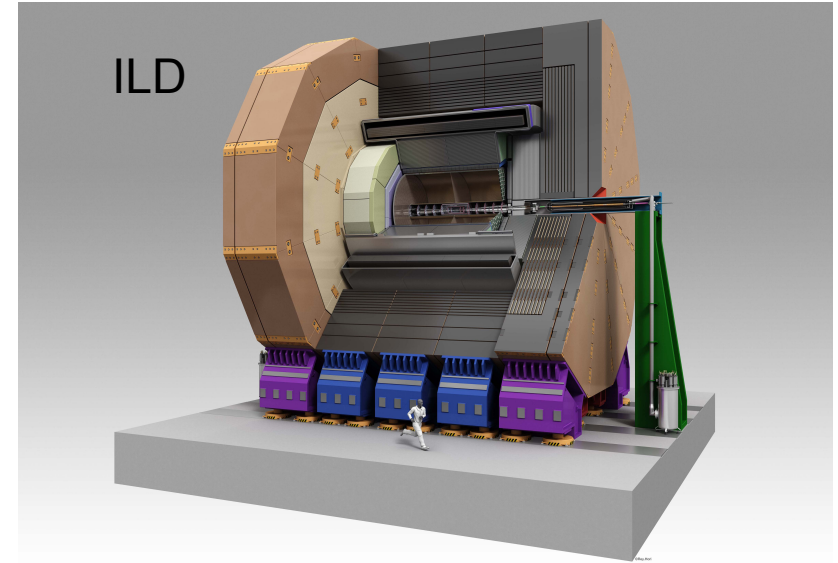
CLIC Detector



SiD



ILD



Highly granular calorimeters
 Central tracking
 with silicon
 Inner tracking with silicon

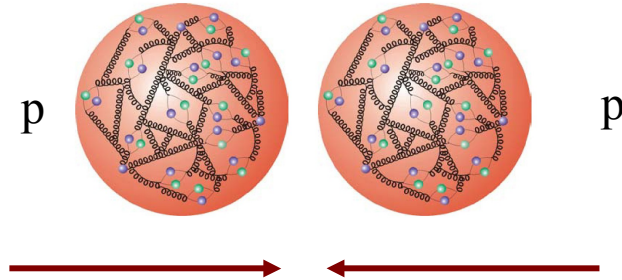
Central tracking
 with TPC

- CDR 2012
 Revised since

- LOI's Validated by IDAG in 2009
 - Publication of **D**etector **B**aseline **D**esign in 2013, together with TDR

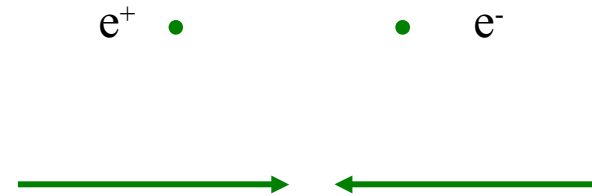
Concepts based on input from physics studies and detector R&D organised in R&D collaborations

- Event generator **WHIZARD** interfaced to **PYTHIA**
Alternative generators **PYTHIA** or **PHYSIM**
- **LC Detectors** benefit from a complete software suite
 - **GEANT4** for event simulation
 - e.g. **Mokka/DD4HEP** as geometry interface to **GEANT4**
 - **MARLIN** for event reconstruction and analysis framework
 - Interface to toolkits such as **PandoraPFA** or **LCFIVertex**
 - Extensive use of grid resources
- Detector simulation is based on input from worldwide detector R&D



Proton:

Composed particle (hadron)
 Unknown energy of collision partners
 Parasitic reactions
 Strong interaction
 => Considerable physics background
 Advantage: Scan of energy
 Range within one experiment



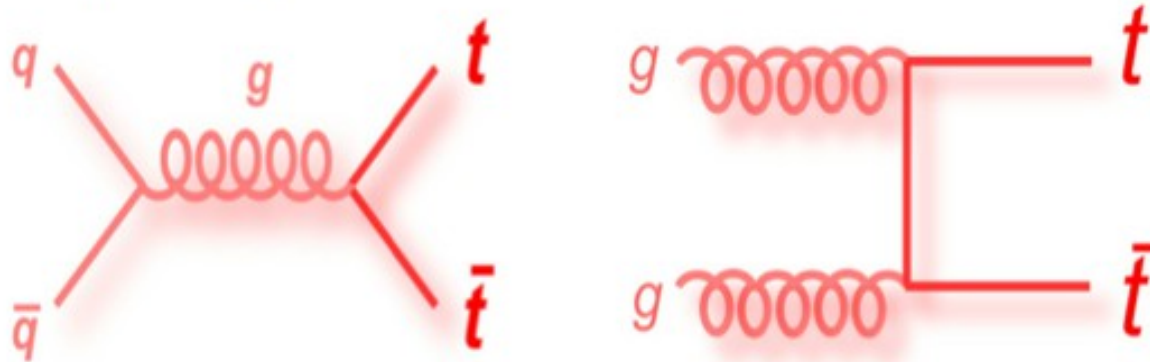
Electron:

Elementary particle
 Well known and adjustable energy of collision partners

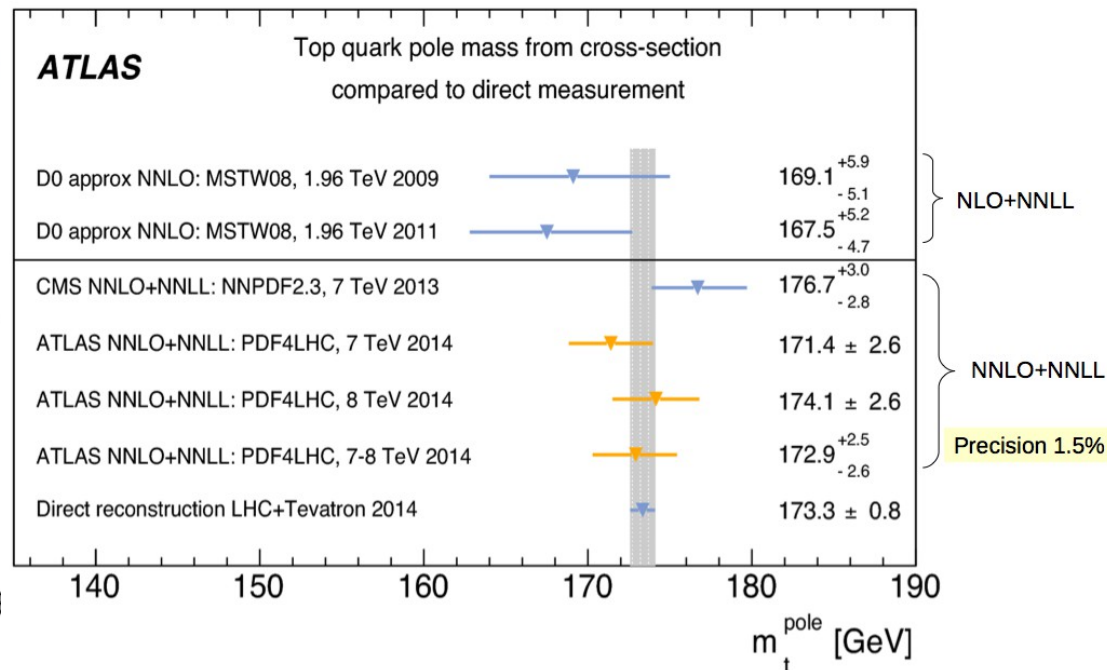
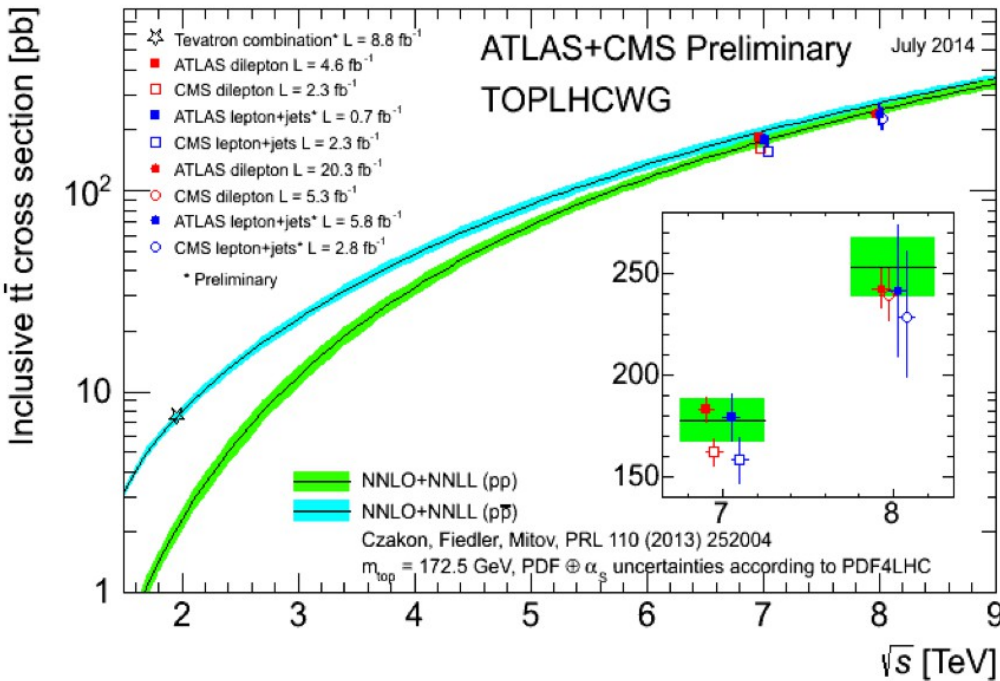
 Each energy point needs a New set of machine parameters

High precision measurements

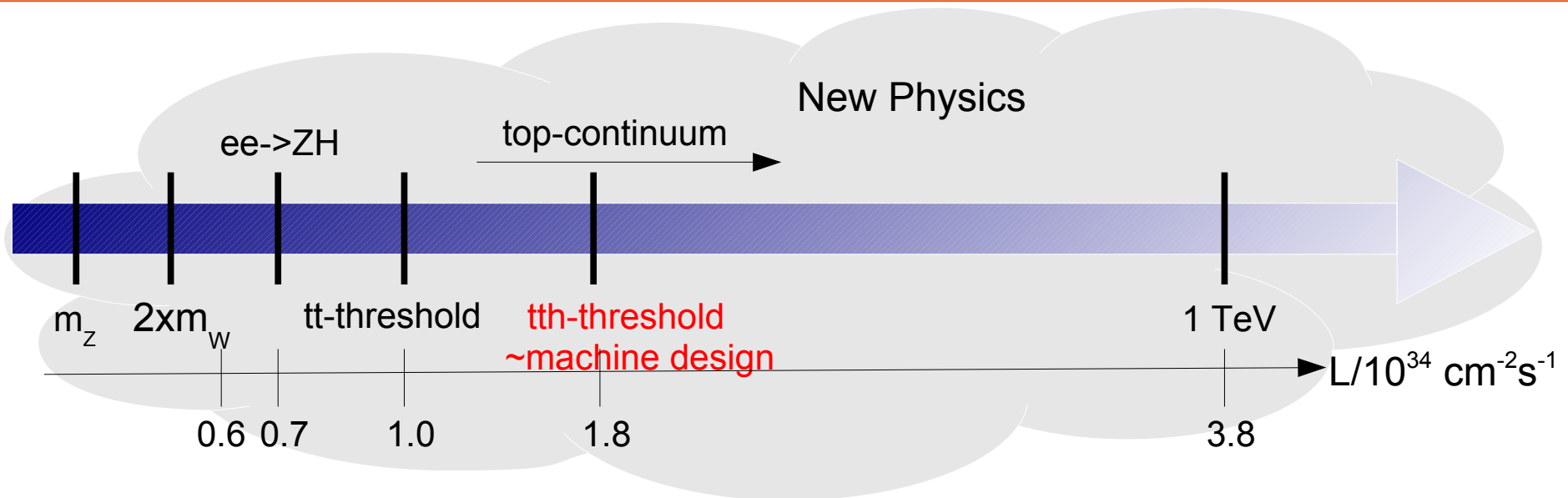
Example diagrams:



	σ_{gg}/σ_{tot}
Tevatron	$\approx 15\%$
LHC 7 TeV	$\approx 85\%$
LHC 14 TeV	$\approx 90\%$



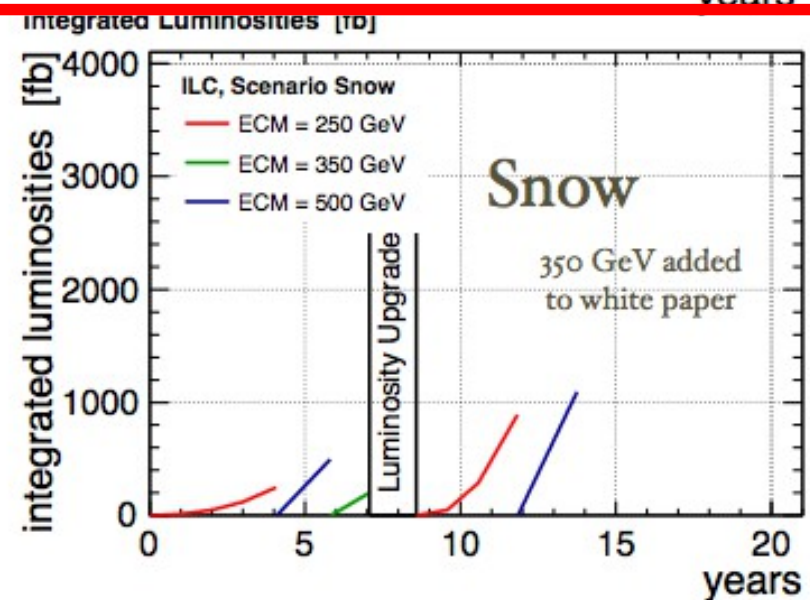
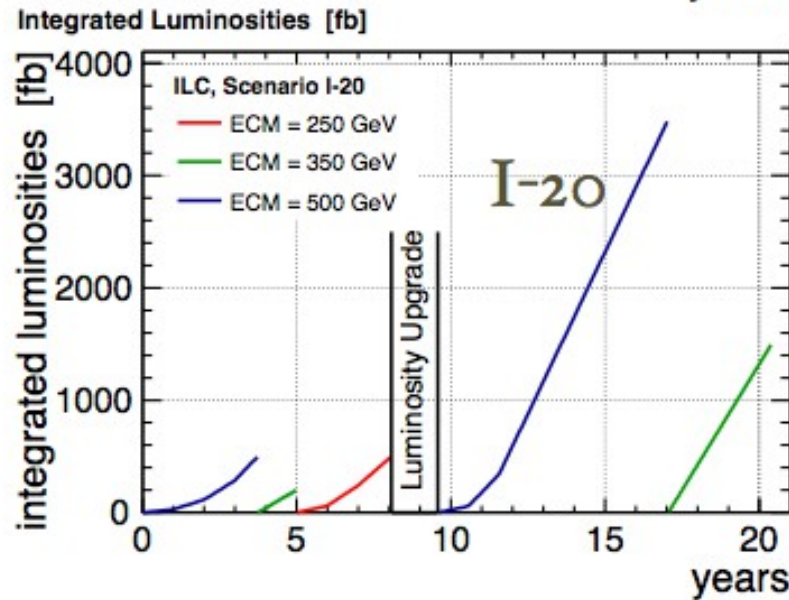
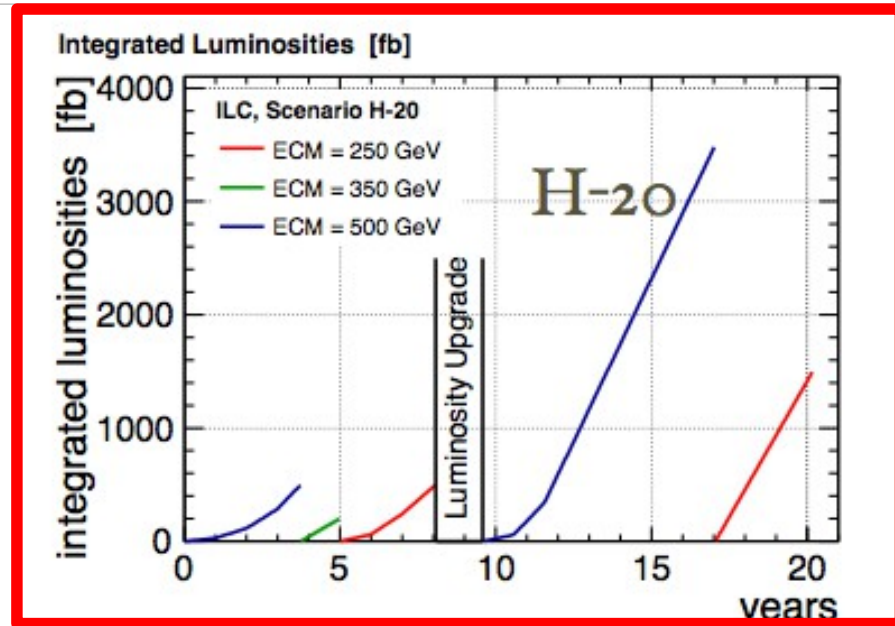
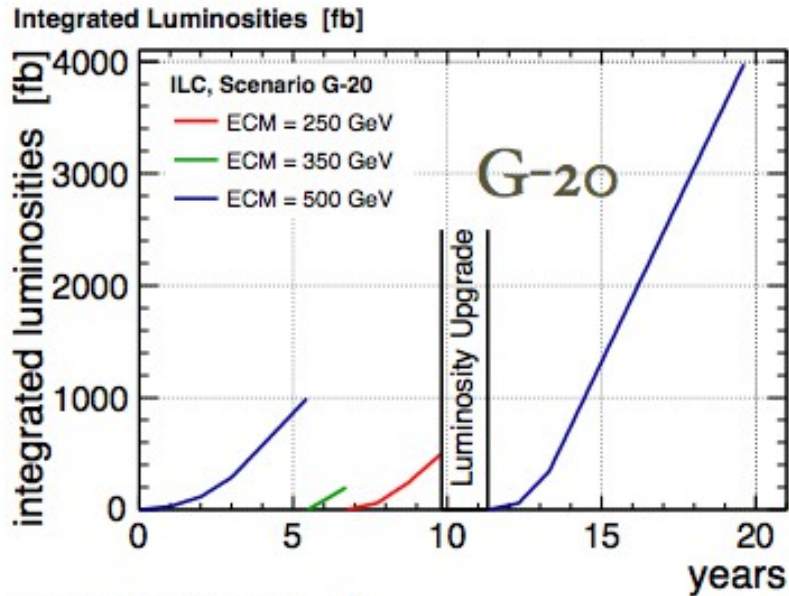
=> High time to see them at lepton colliders!



- All Standard Model particles within reach of ILC
 - High precision tests of Standard Model over wide range to detect onset of New Physics
- Machine settings can be “tailored” for specific processes
 - Centre-of-Mass energy
 - Beam polarisation

$$\sigma_{P,P'} = \frac{1}{4} [(1 - PP')(\sigma_{LR} + \sigma_{RL}) + (P - P')(\sigma_{RL} - \sigma_{LR})]$$

- “Background free” searches for BSM through beam polarisation



type	final state	σ 500 GeV	σ 352 GeV
Signal ($m_{\text{top}} = 174$ GeV)	$t\bar{t}$	530 fb	450 fb
Background	WW	7.1 pb	11.5 pb
Background	ZZ	410 fb	865 fb
Background	$q\bar{q}$	2.6 pb	25.2 pb
Background	WWZ	40 fb	10 fb

Remarks:

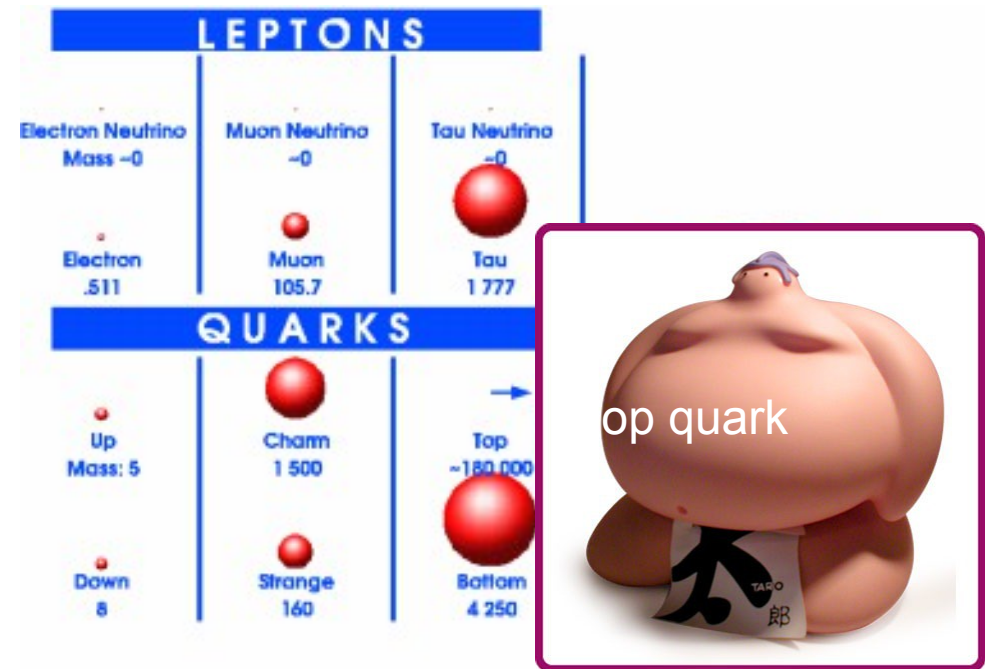
- LC will have polarised beams

=> $(\sigma_{t\bar{t}})_L \sim 1565\text{fb}^{-1}$, $(\sigma_{t\bar{t}})_R \sim 724\text{fb}^{-1}$ at 500 GeV

- Background varies differently with polarisations

e.g. WW-Background $\rightarrow 26000\text{fb}^{-1}$ for e_L and 150fb^{-1} for e_R

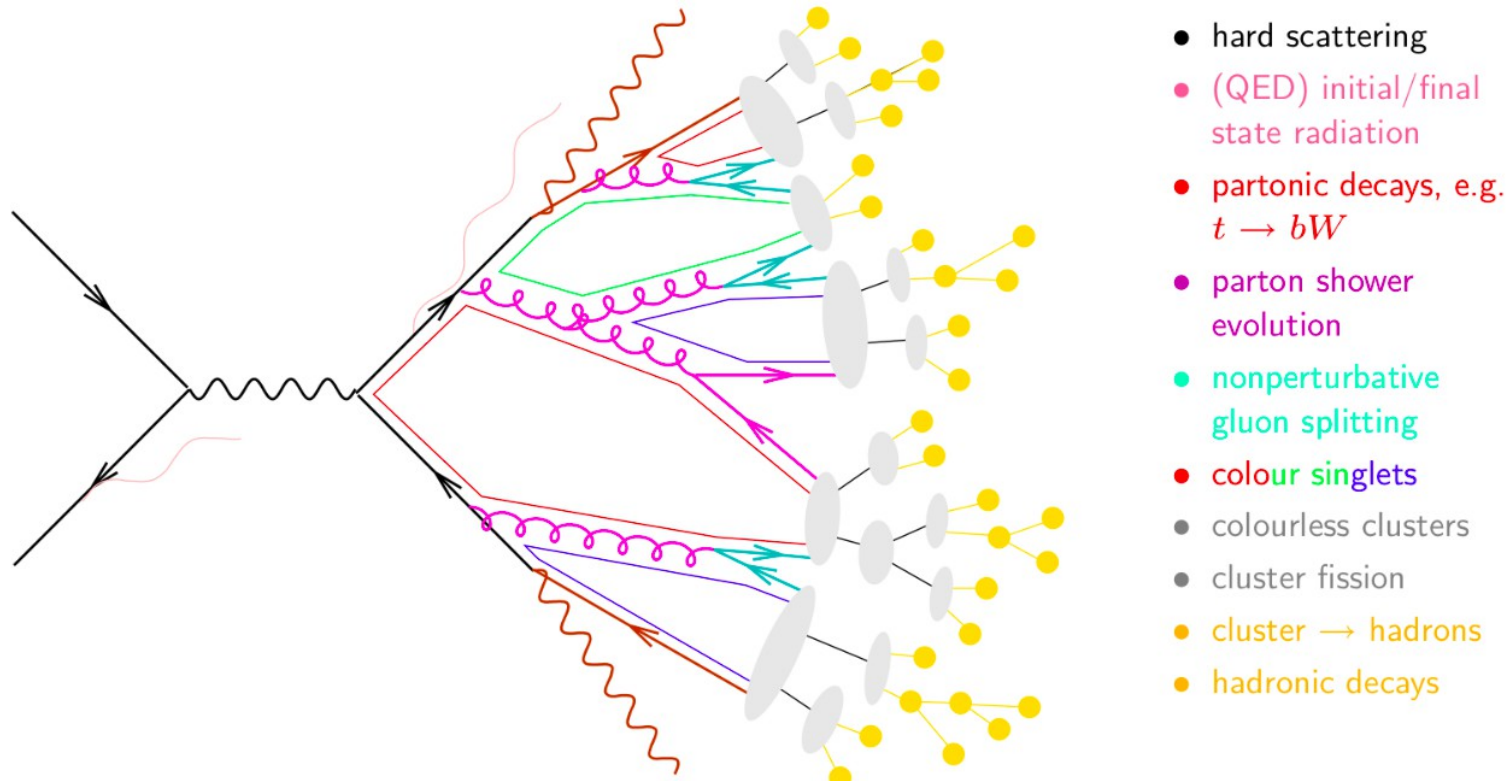
- The top quark is the heaviest known elementary particle
Discovery in 1995 at Tevatron
- $m_t \sim 173 \text{ GeV}$ ($\sim m$ of Gold atom)
- Electrical charge $Q_t = 2/3$
- Spin $1/2 \Rightarrow$ fermion
- Lifetime $\tau \sim 5 \times 10^{-25} \text{ s}$
(SM decays)
- Total width $\Gamma_t \sim 1.5 \text{ GeV}$
- No hadronisation, behaves like a free quark
- Predominant decays
 $t \rightarrow Wb$ (BR $\sim 100\%$)



*Ideal object for
a machine in Japan ;-)*

*Slide inspired by Lecture of
Prof. K. Jakobs, Uni Freiburg*

Extraction of top mass from invariant jet masses (Typical for hadron colliders)



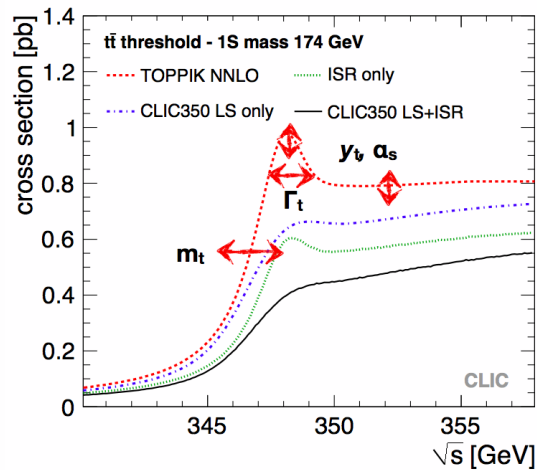
- MC Mass: Mass of (on-shell) top propagator prior to decay \Rightarrow Pole mass

- Pole mass theoretically unsafe when precision reaches $O(\Lambda_{\text{QCD}} \sim 1 \text{ GeV})$

(Non absorption of soft virtual corrections)

Stat. Error (m_t, Γ_t :MeV/ y_t :%)	6-Jet			4-Jet		
	m_t^{PS}	Γ_t	y_t	m_t^{PS}	Γ_t	y_t
Left(50fb ⁻¹)	47	65	9.6	52	71	11
Right(50fb ⁻¹)	68	94	14	75	106	16
Left (50fb ⁻¹) + Right(50fb ⁻¹)	39	53	7.9	43	59	9.1

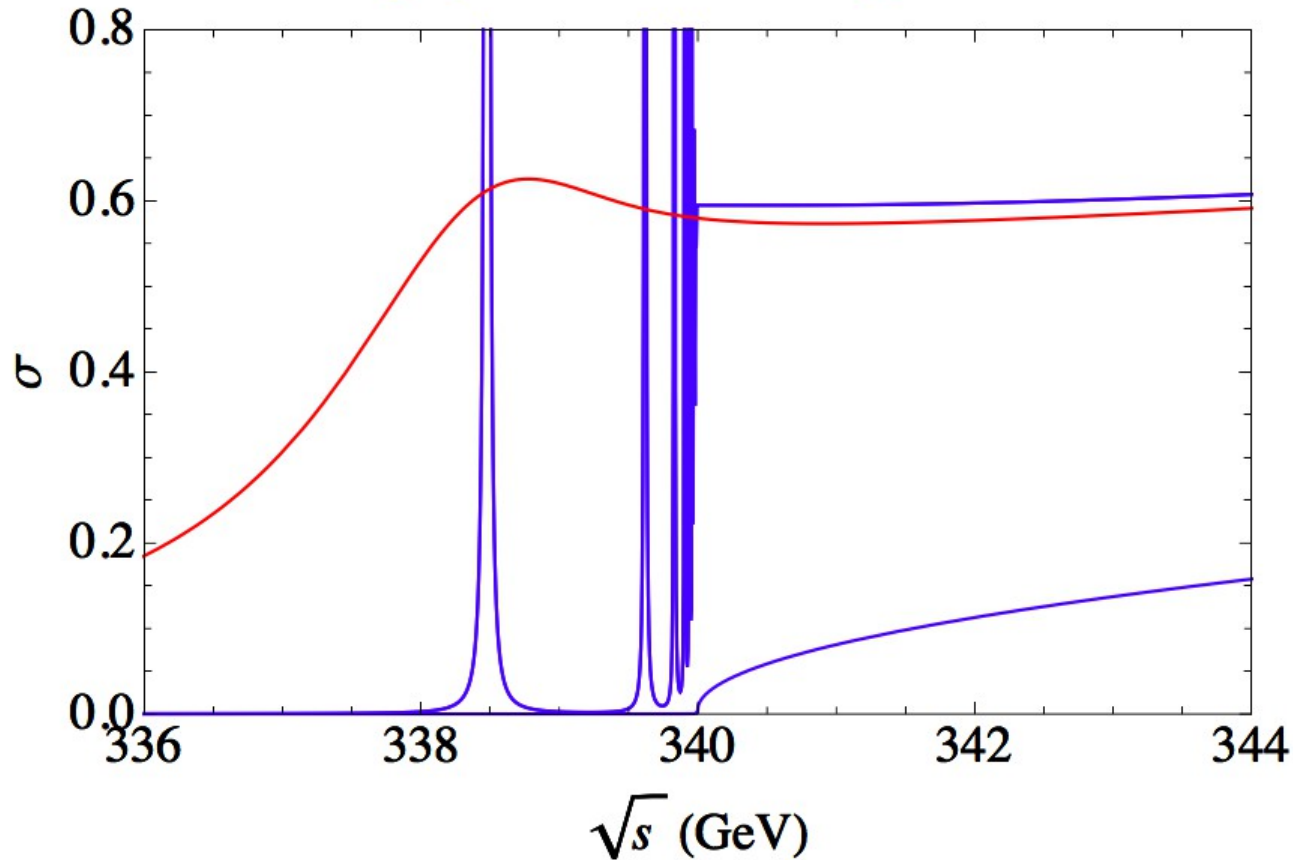
Update of: arxiv 1310.0563



Combined ALL		
m_t^{PS} (GeV)	Γ_t (GeV)	y_t
172 ± 0.029	1.4 ± 0.039	5.9 %

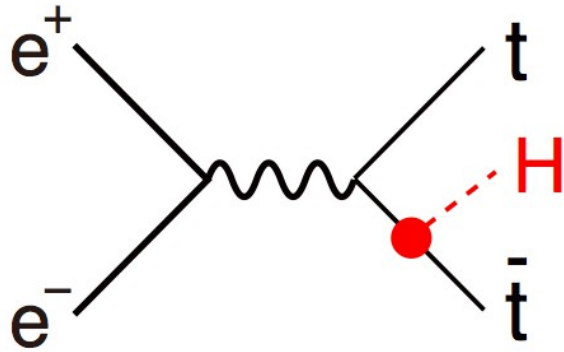
- Competitive determination of three parameters
- y_t suffers however from large theory uncertainties (~20%)
=> Indirect determination may not be conclusive
- Systematic studies on e.g. beam spectrum ongoing
Important for top width

“Bound states” at tt threshold
Hydrogen atom of strong interaction

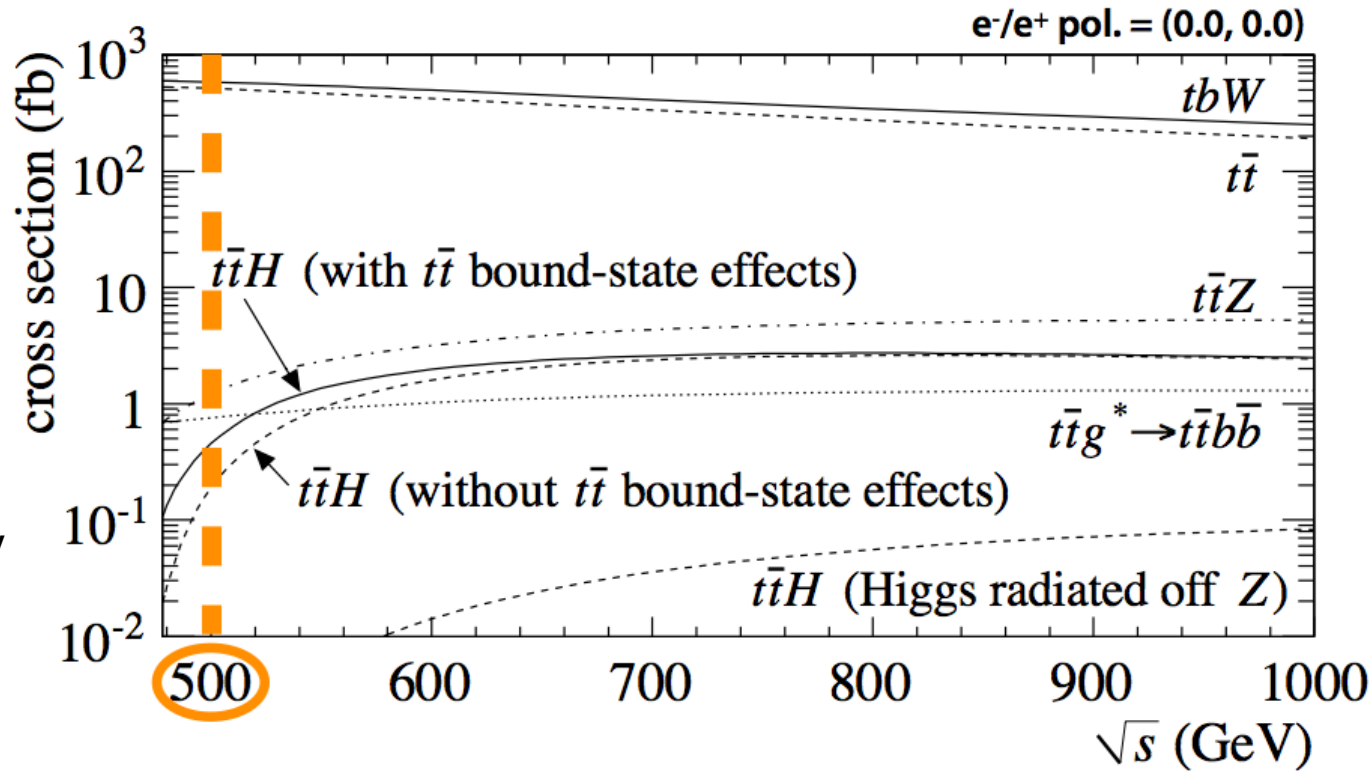


- Size $O(10^{-17}\text{m})$, **smallest object known in particle physics**
 Small scale => Free of confinement effects => Ideal premise for precision calculations
 Measurement of (a hypothetical) 1^3S_1 State
- Decay of top quark smears out resonances in a well defined way

- Expected statistical uncertainty **10 – 30 MeV**
- Experimental systematics
 - Beam energy: **~30 MeV** or lower
 - Non- $t\bar{t}$ background, selection efficiencies (Assuming $< 5\%$ background uncertainty, 0.5% knowledge on signal selection): **~ 15 MeV**
 - Luminosity spectrum (studied for CLIC LS with reconstruction of spectrum via Bhabha Scattering, scaling from 3 TeV studies, full study on the way): **10 MeV**
 - Single top contamination: **< 30 MeV**
- Theory uncertainties
 - Normalisation: **~55 MeV (naive estimate)** much smaller due to recent NNNLO calculations arxiv: 1506.06864, arxiv:1506.06542
 - When not included in the fit: ~ 3 MeV per 10^{-4} uncertainty on α_s today \rightarrow **~18 MeV**
 - Conversion from 1S/PS masses to \overline{MS} mass Currently: **~50 MeV**
However conversion now known to N^4 LO (arxiv:1502.01030)
 - Now at point where results become sensitive to effects other than QCD



- Coupling of Higgs to heaviest particle known today
- Up to eight final state jets



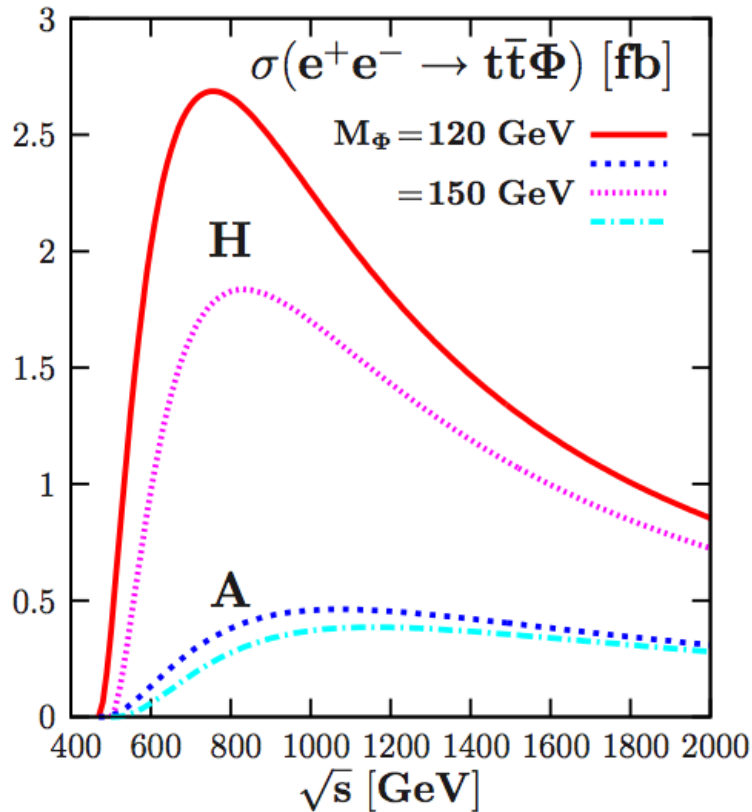
$\Delta g_{ttH}/g_{ttH}$	H20 - 500	H20 - 500 Lumi Up
Standard ILC	18%	6.3%
ILC @ $\sqrt{s} = 550$ GeV	~9%	~3%

← ILC 2015
← Technically possible

Running at 1 TeV would allow precision at the 1 – 2% level

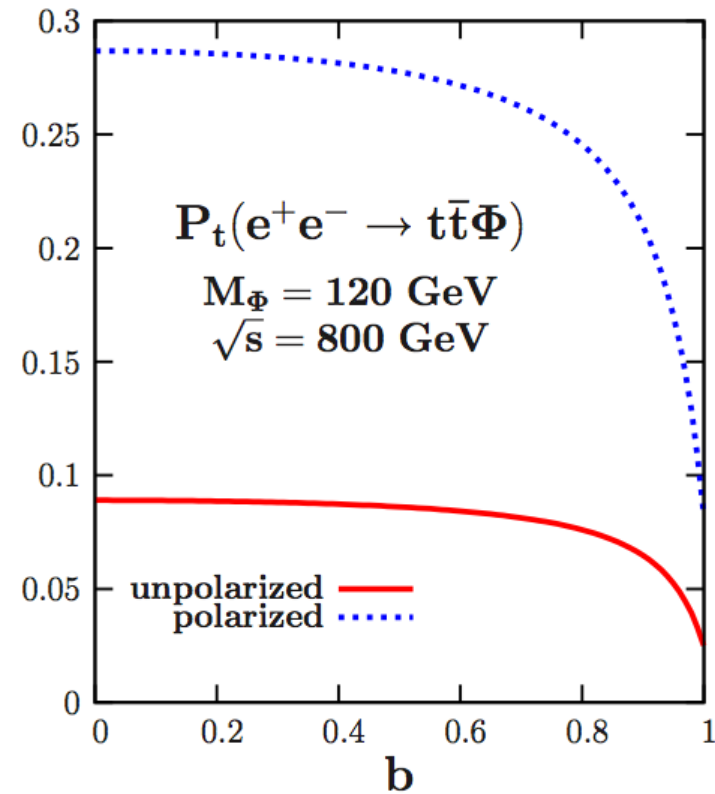
Direct coupling of top quark to CP odd and CP even scalar

Cross section



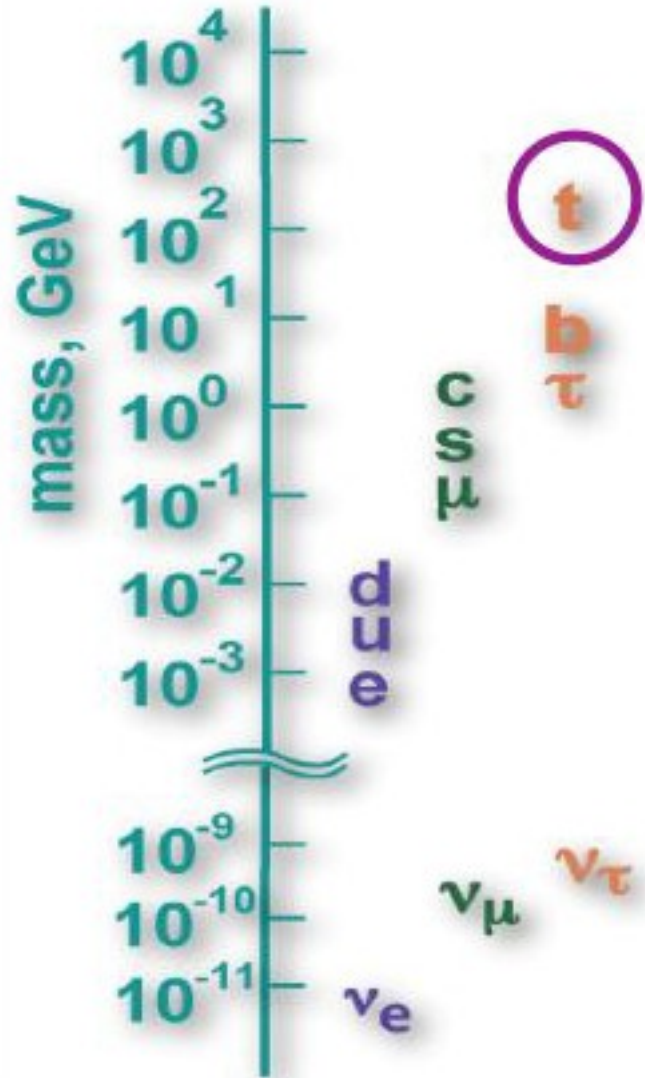
Dramatic differences for
CP odd and CP even scalar

Top quark polarisation



Sensitivity to CP odd admixture b
Merit of beam polarisation

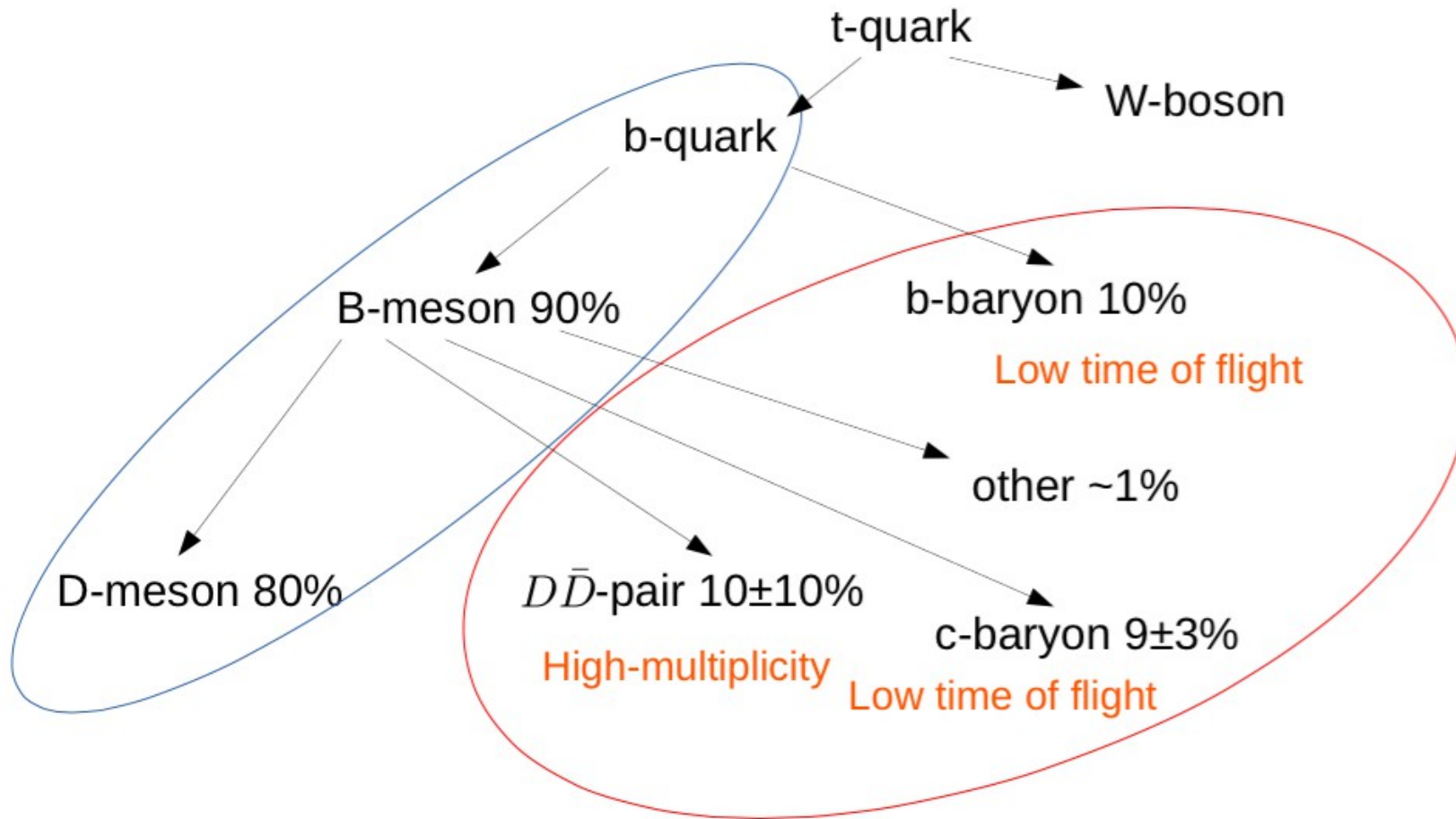
Determination of CP nature of scalar boson in an unambiguous way



- SM does not provides no explanation for mass spectrum of fermions (and gauge bosons)
- Fermion mass generation closely related to the origin electroweak symmetry breaking
- Expect residual effects for particles with masses closest to symmetry breaking scale
 - A_{FB} anomaly at LEP for b quark

Strong motivation to study chiral structure of top vertex in high energy e+e- collisions

- Hadronization and decay modes of b-quark:

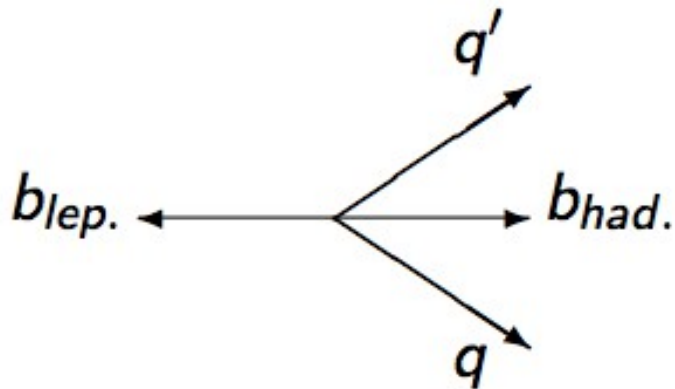


4

> 70% of the tops lead to “straightforward” reconstructable final states
Exploiting this observation is subject of PhD thesis at LAL

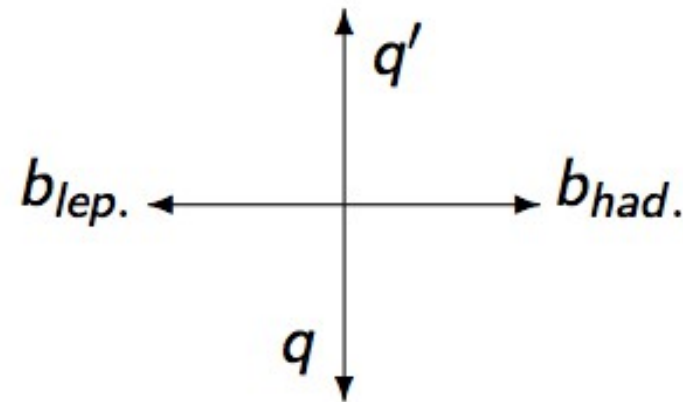
Collaboration within French-Japanese TYL/FJPPL research programme

- To measure A_{FB} in fully hadronic decays there is no choice
- In semi-leptonic decays there is the charged lepton but



Right handed electron beam:

- mainly right handed tops
In final state (V-A)
- Hard W in flight direction of Top and soft b's
- Flight direction of t from flight direction of W

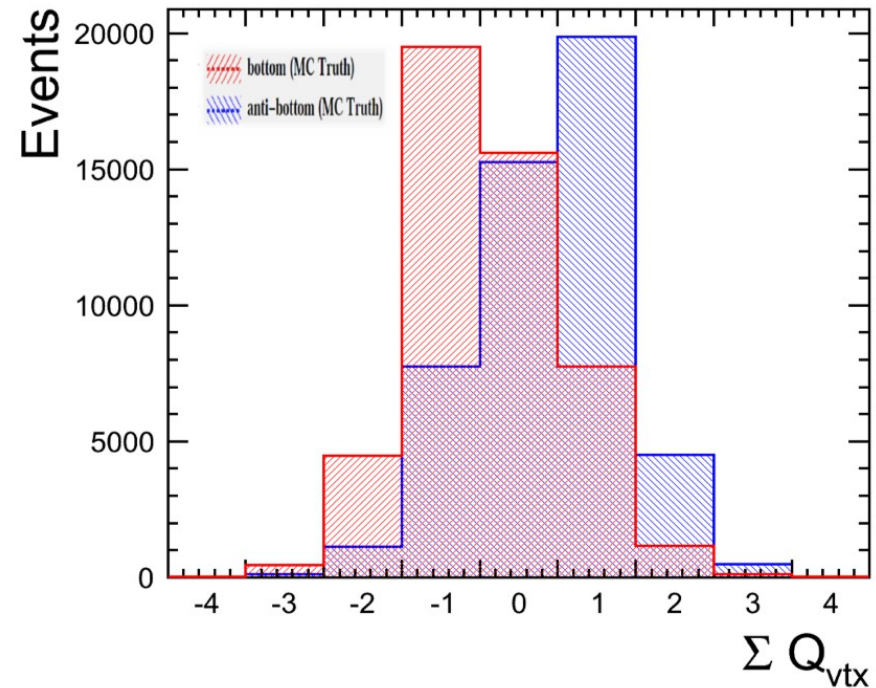
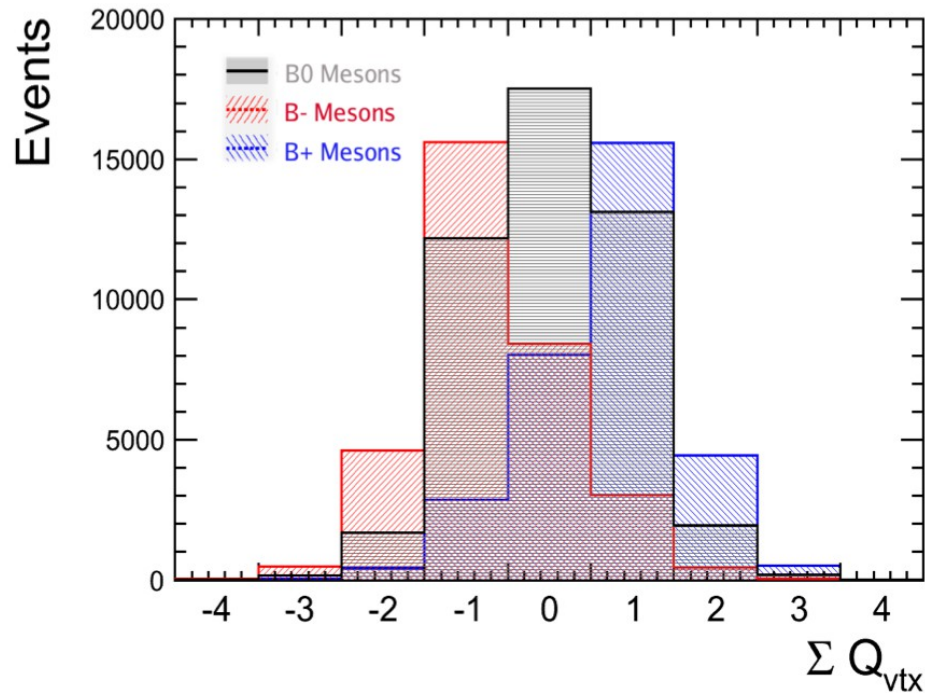


Left handed electron beam:

- mainly left handed tops
- Hard b in flight direction of Top and soft W's
- Flight direction of t from flight direction of b
=> Wrong association ↔ top flip

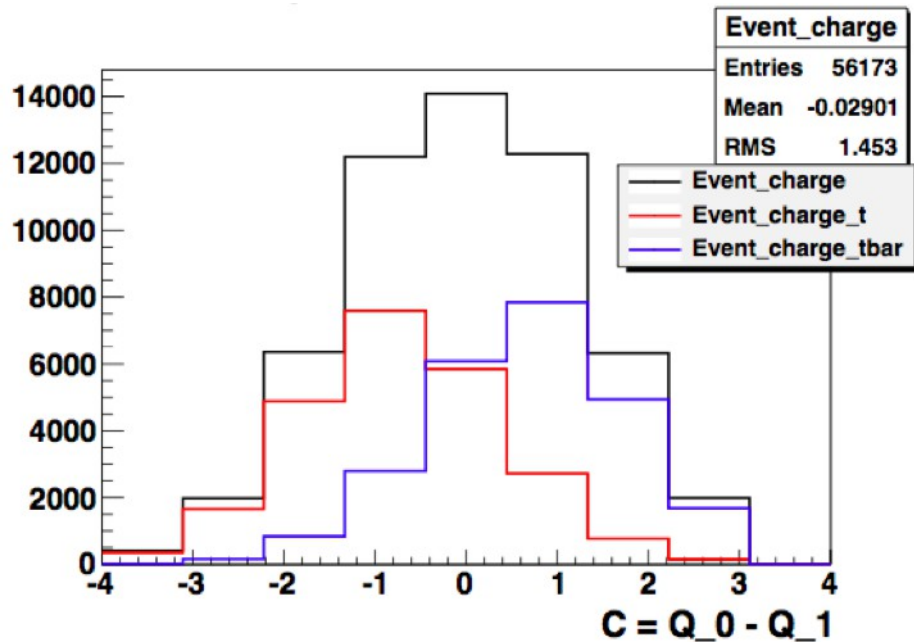
Measurement of b-charge to resolve ambiguities

(N.B. At example of fully hadronic analysis, PhD M.S. Amjad)



- LC vertex and tracking system should allow for determination of b-meson (b-quark) charge
- B-quark charge measured correctly in about 60% of the cases
Can be increased to 'arbitrary' purity on the expense of smaller statistics
- However ~25% are “accidentally” correct measurements
- LC software (LCFIPlus package) not yet optimised for vertex charge measurement

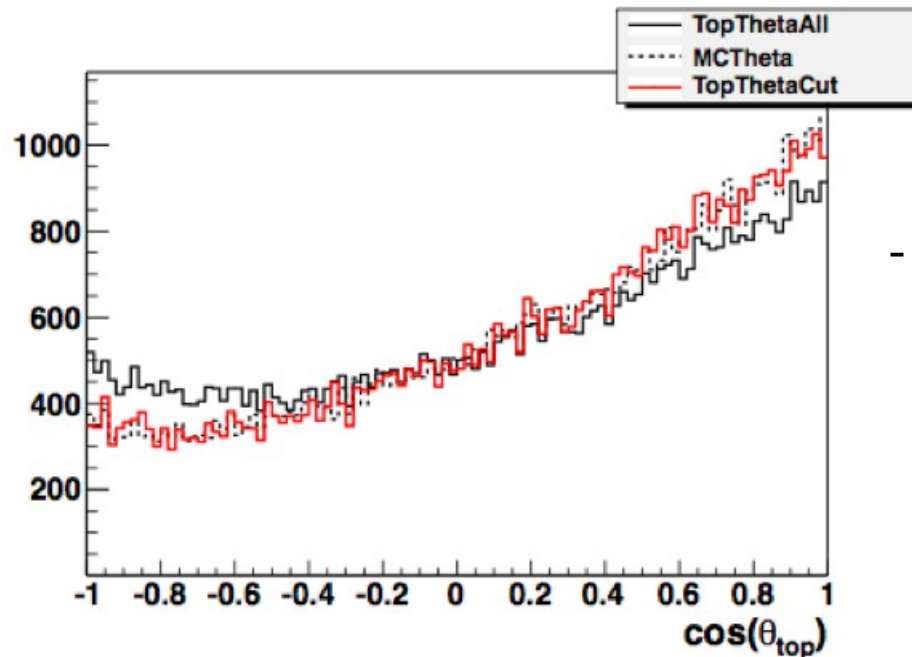
Optimisation of b-quark charge is major topic in ongoing studies and real challenge of LC detectors



Event charge $C = b_1 - b_2$

In SL can compare charge C with lepton charge to select clean sample

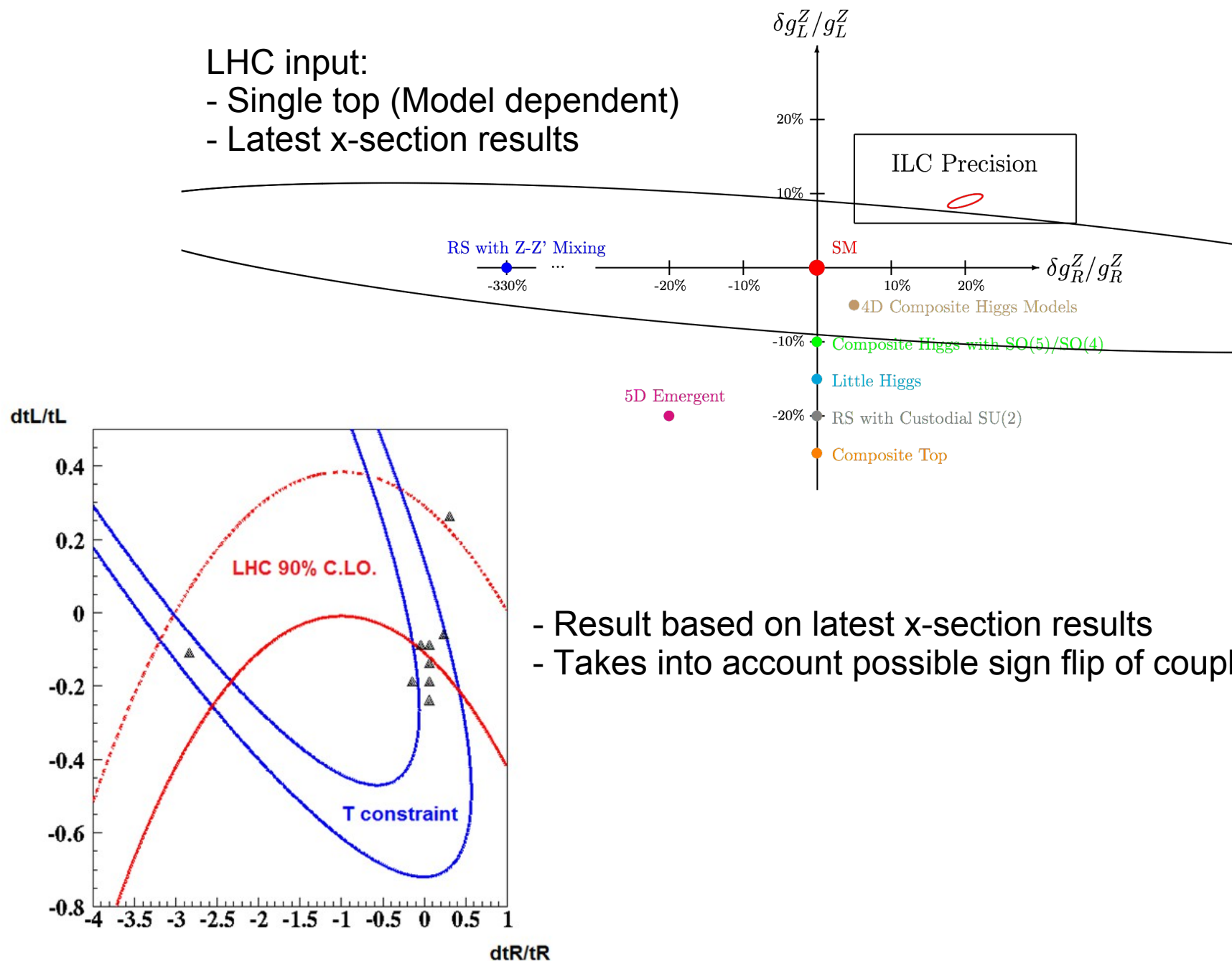
Use only events with correct C or $C=0$
(plus another cut on the Lorentz Factor)



- Clean reconstruction of top quark direction
 $\epsilon \sim 30\%$
Will improve with improving charge reconstruction

Comparison with current LHC results

LHC input:
- Single top (Model dependent)
- Latest x-section results



- Result based on latest x-section results
- Takes into account possible sign flip of couplings

Study by Francois Richard

Higgs sector

- It should be noted that for what concerns the Higgs sector (non-minimal) contribution there could be a much larger enhancement for the 3d generation $\mathbf{df} \sim \mathbf{m}^3 \mathbf{f}$ at one-loop
- Higgs exchange is larger near threshold and the sensitivity for $\text{Re}(F2A)$ drops to 0 at 500 GeV

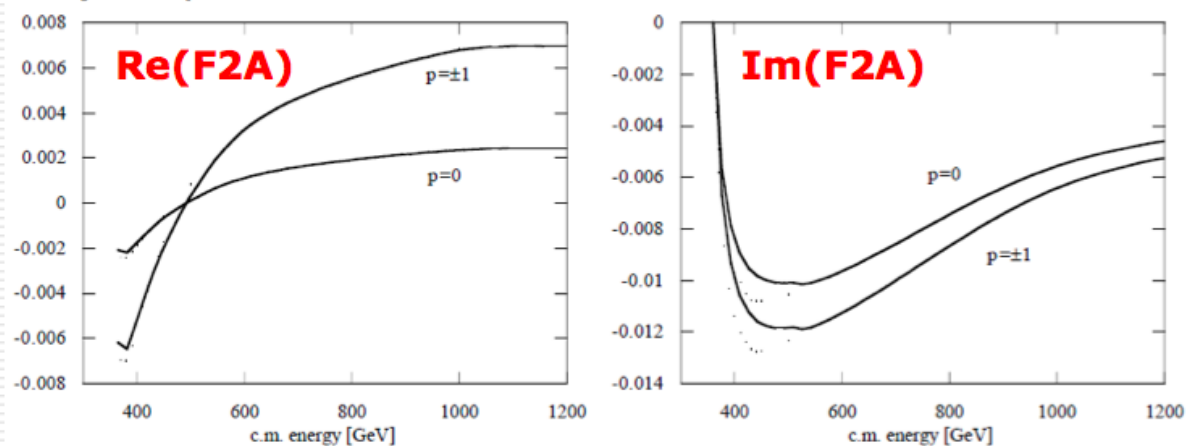


Fig 1: Ratios r_1 (left figure) and r_2 (right figure) for the optimized dispersive and absorptive observables $\mathcal{O}_{\pm}(i)$, $i = 1, 2$ defined in [6] for $m_t = 180$ GeV, $m_{\varphi_1} = 100$ GeV, and $\gamma_{CP} = 1$.

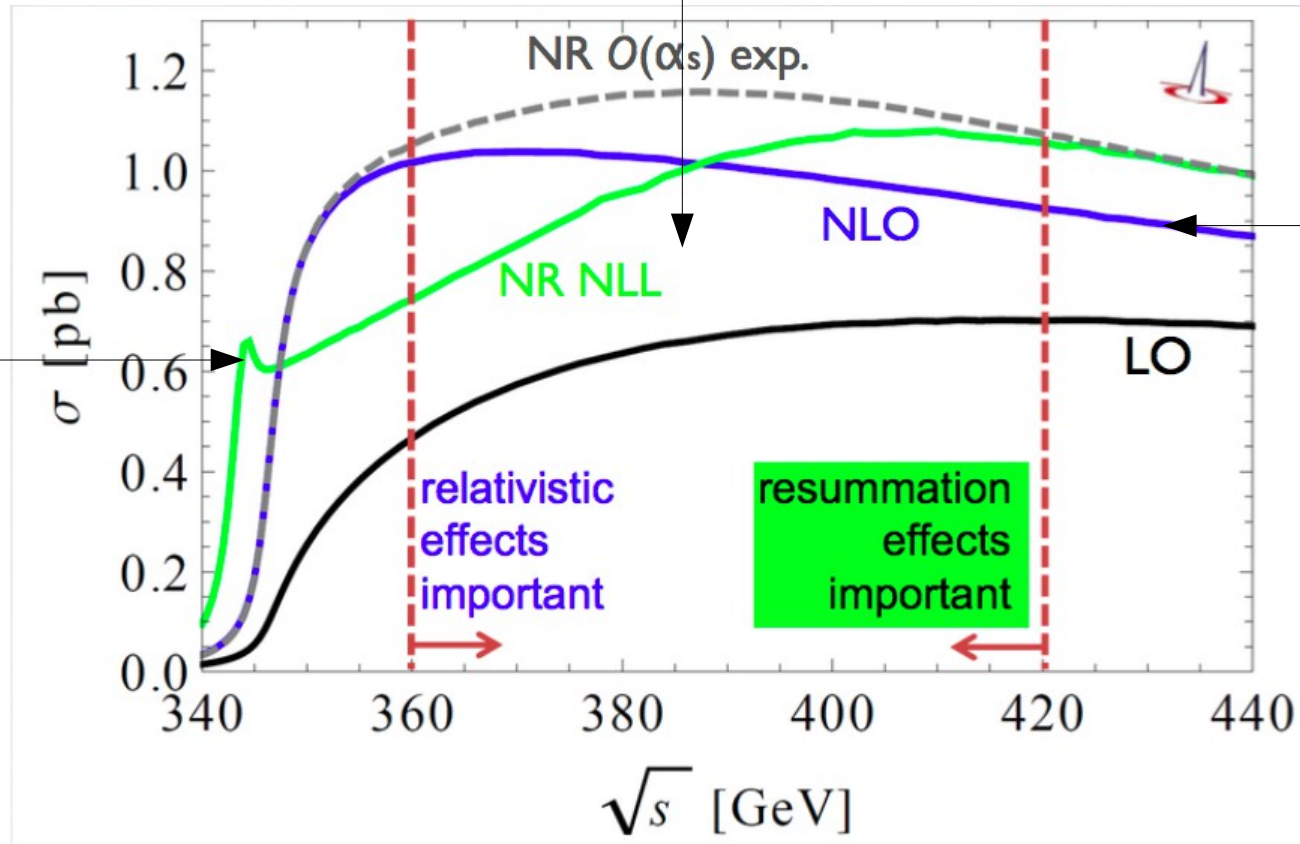
8

Exchange of CP Violating Higgs is most probable source of CP violation
In $t\bar{t}$ production (dixit Werner Bernreuther)

Complicated transition region

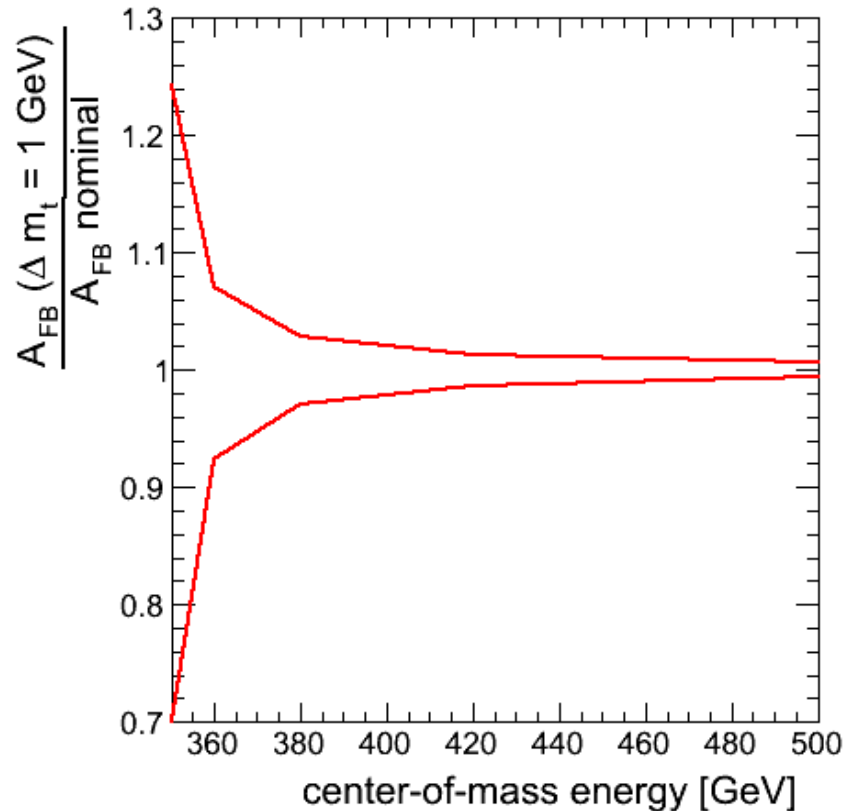
Transition region
Difficult to match non-relativistic QCD at threshold
With relativistic QCD in continuum

Threshold region
Theoretically
well under control



Continuum
Theoretically
well under control

Considerable theory uncertainties suggest
to avoid transition region for precision physics



Influence of the top quark mass on x-sec and A_{FB}

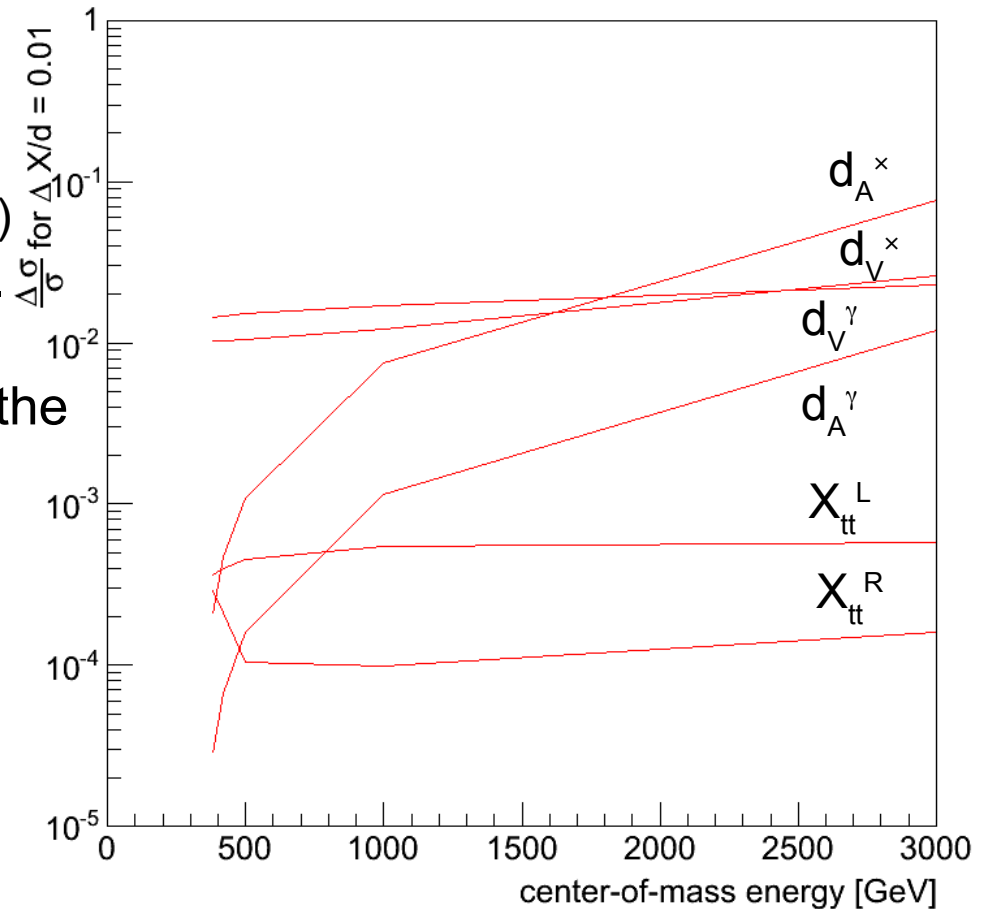
- very pronounced below $\sqrt{s} = 360$ GeV
- 2.9%/GeV at $\sqrt{s} = 380$ GeV
- 1.3%/GeV at $\sqrt{s} = 420$ GeV
- 0.6%/GeV at $\sqrt{s} = 500$ GeV

With the assumption of a 100 MeV pole mass measurement at threshold, the remaining uncertainty is one per mil or less above 420 GeV

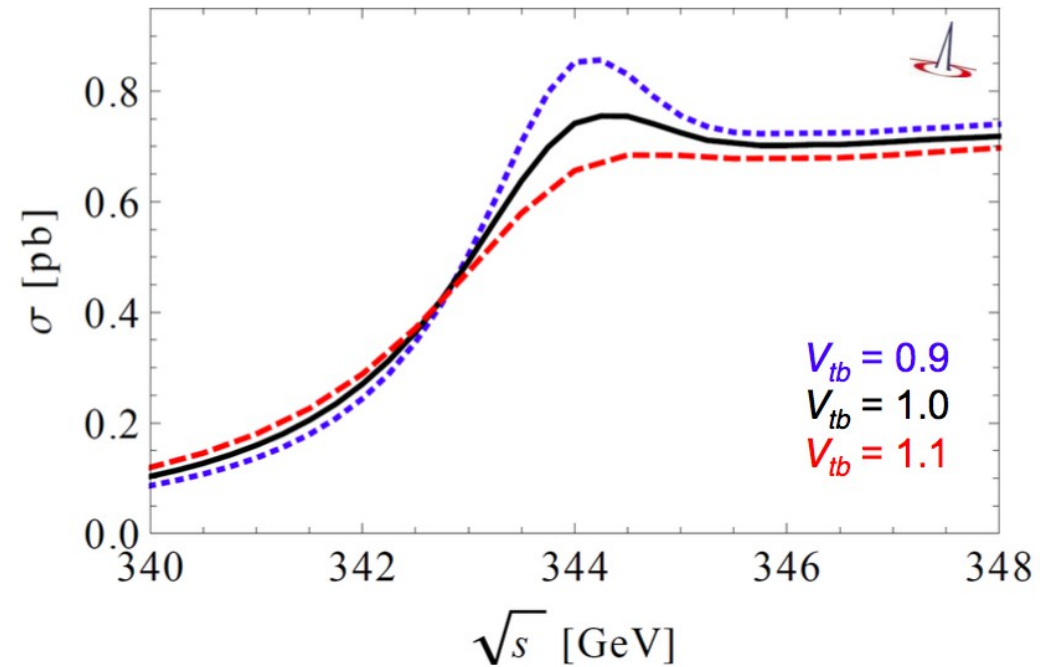
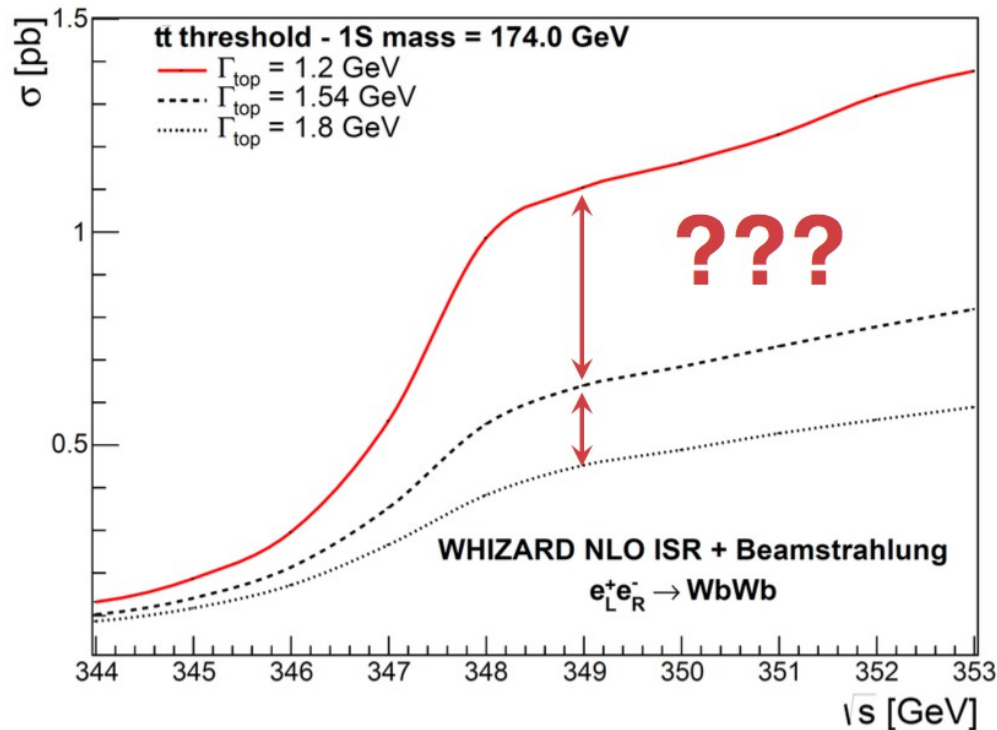
Dimension 6 effective operators
(~equivalent role to anomalous form factors)
have been implemented in WHIZARD...

Allow to map the dependence on \sqrt{s} of the
impact of new physics on given
observable

May help to explore the sensitivity of
new/additional observables



Study with WHIZARD generator



- “Erratic” behaviour of theory prediction when using Γ_t as free parameter
- Using V_{tb} as free parameter leads to more benign behaviour

Experimentally observable final state requires proper definition of theory parameters

For details see arxiv: 1503.04247

Basic idea: Final state top polarisation contains information about factors

$$\begin{aligned}
 \mathcal{M}(e_L \bar{e}_R \rightarrow t_L \bar{t}_R)^{\gamma/Z} &= c_L^{\gamma/Z} [F_{1V}^{\gamma/Z} - \beta F_{1A}^{\gamma/Z} + F_{2V}^{\gamma/Z}] (1 + \cos \theta) e^{-i\phi} \\
 \mathcal{M}(e_L \bar{e}_R \rightarrow t_R \bar{t}_L)^{\gamma/Z} &= c_L^{\gamma/Z} [F_{1V}^{\gamma/Z} + \beta F_{1A}^{\gamma/Z} + F_{2V}^{\gamma/Z}] (1 - \cos \theta) e^{-i\phi} \\
 \mathcal{M}(e_L \bar{e}_R \rightarrow t_L \bar{t}_L)^{\gamma/Z} &= c_L^{\gamma/Z} \gamma^{-1} [F_{1V}^{\gamma/Z} + \gamma^2 (F_{2V}^{\gamma/Z} + \beta F_{2A}^{\gamma/Z})] \sin \theta e^{-i\phi} \\
 \mathcal{M}(e_L \bar{e}_R \rightarrow t_R \bar{t}_R)^{\gamma/Z} &= c_L^{\gamma/Z} \gamma^{-1} [F_{1V}^{\gamma/Z} + \gamma^2 (F_{2V}^{\gamma/Z} - \beta F_{2A}^{\gamma/Z})] \sin \theta e^{-i\phi} \\
 \mathcal{M}(e_R \bar{e}_L \rightarrow t_L \bar{t}_R)^{\gamma/Z} &= -c_R^{\gamma/Z} [F_{1V}^{\gamma/Z} - \beta F_{1A}^{\gamma/Z} + F_{2V}^{\gamma/Z}] (1 - \cos \theta) e^{i\phi} \\
 \mathcal{M}(e_R \bar{e}_L \rightarrow t_R \bar{t}_L)^{\gamma/Z} &= -c_R^{\gamma/Z} [F_{1V}^{\gamma/Z} + \beta F_{1A}^{\gamma/Z} + F_{2V}^{\gamma/Z}] (1 + \cos \theta) e^{i\phi} \\
 \mathcal{M}(e_R \bar{e}_L \rightarrow t_L \bar{t}_L)^{\gamma/Z} &= c_R^{\gamma/Z} \gamma^{-1} [F_{1V}^{\gamma/Z} + \gamma^2 (F_{2V}^{\gamma/Z} + \beta F_{2A}^{\gamma/Z})] \sin \theta e^{i\phi} \\
 \mathcal{M}(e_R \bar{e}_L \rightarrow t_R \bar{t}_R)^{\gamma/Z} &= c_R^{\gamma/Z} \gamma^{-1} [F_{1V}^{\gamma/Z} + \gamma^2 (F_{2V}^{\gamma/Z} - \beta F_{2A}^{\gamma/Z})] \sin \theta e^{i\phi}
 \end{aligned}$$

=> different sensitivities in different individual matrix elements:

$$\omega_i = \frac{\partial |\mathcal{M}|^2(\alpha)}{\partial \alpha_i} \Big|_{\alpha^0} \frac{1}{|\mathcal{M}|^2(\alpha^0)} \quad \text{For each } \alpha_i \text{ (=FF) there is one (measurable) } \omega_i$$

Using full matrix element information -> Full event reconstruction

$$d\text{Lips} \propto d \cos \theta_t \, d \cos \theta_b \, d\phi_b \, d \cos \theta_{\bar{b}} \, d\phi_{\bar{b}} \, d \cos \theta_{l+} \, d\phi_{l+} \, d \cos \theta_{l-} \, d\phi_{l-} \, dq_t^2 \, dq_{\bar{t}}^2 \, dq_W^2$$

Parton level analysis (with GRACE generator) using fully leptonic final state

Simultaneous extraction of 10 FF **including CP violating FFs**

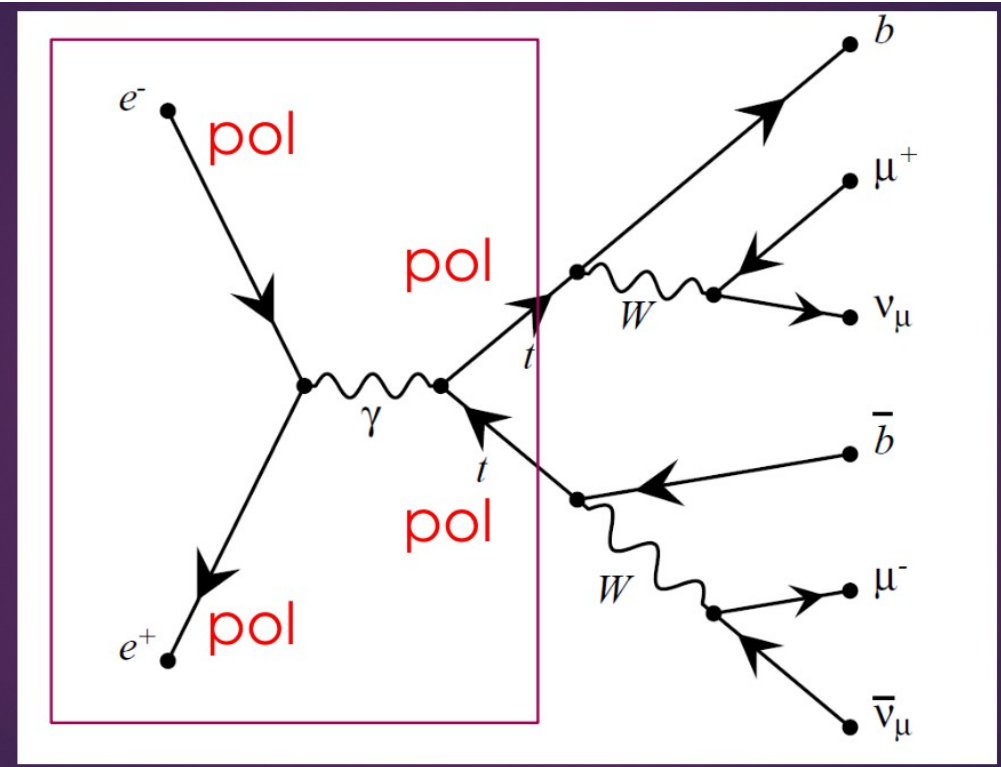
$\mathcal{R}e \delta \tilde{F}_{1V}^\gamma$	$\mathcal{R}e \delta \tilde{F}_{1V}^Z$	$\mathcal{R}e \delta \tilde{F}_{1A}^\gamma$	$\mathcal{R}e \delta \tilde{F}_{1A}^Z$	$\mathcal{R}e \delta \tilde{F}_{2V}^\gamma$	$\mathcal{R}e \delta \tilde{F}_{2V}^Z$	$\mathcal{R}e \delta \tilde{F}_{2A}^\gamma$	$\mathcal{R}e \delta \tilde{F}_{2A}^Z$	$\mathcal{I}m \delta \tilde{F}_{2A}^\gamma$	$\mathcal{I}m \delta \tilde{F}_{2A}^Z$
0.0037	-0.18	-0.09	+0.14	+0.62	-0.15	0	0	0	0
	0.0063	+0.14	-0.06	-0.13	+0.61	0	0	0	0
		0.0053	-0.15	-0.05	+0.09	0	0	0	0
			0.0083	+0.06	-0.04	0	0	0	0
				0.0105	-0.19	0	0	0	0
					0.0169	0	0	0	0
						0.0068	-0.15	0	0
							0.0118	0	0
								0.0069	-0.17
									0.0100

No particular improvement through beam polarisation

- No background, no smearing
- Needs experimental study – You?

Collaboration within French-Japanese TYL/FJPPL research programme

Elw. Corrections for polarised beams



Target:

- $e^+e^- \rightarrow t\bar{t} \rightarrow b\bar{b}f\bar{f}f\bar{f}$ @ ILC
- Full $O(\alpha)$ electroweak corrections
- Beam polarization effects
- Finite width effects of top-quarks
- Matrix elements
- Event generation ?
- $O(\alpha^2)$ electroweak corrections ???

Goal for accuracy < 1%

Collaboration within French-Japanese TYL/FJPPL research programme

- **Luminosity:** Critical for cross section measurements
Expected precision 0.1% @ 500 GeV
- **Beam polarisation:** Critical for asymmetry measurements
Expected to be known to 0.1% for e- beam
and 0.35% for e+ beam
- **Migrations/Ambiguities:** Critical for A_{FB} :
PFLOW important for selection of 'clean events' but maybe subleading w.r.t. jet clustering
Control of b charge is most relevant topic !!!!
- **Other effects:** b-tagging, passive material etc.
LEP1 claims 0.2% error on R_b -> guiding line for LC

Under discussion with theory groups:

- Consideration full 6f final state (Interference with single top and ZWW)
- Electroweak NLO predictions (Correction LO \rightarrow NLO \sim 15%)
- Update and maintenance of event generators (WHIZARD, MADGRAPH etc.)