



Dalitz Plot Analyses with $B \rightarrow Dhh$ decays at LHCb

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Outline

- **General view of Dalitz plot analyses with $B \rightarrow Dhh$**
- **Results of excited D mesons**
- **Light meson structure studies**
- **Conclusion**

Analyses with $B \rightarrow Dhh$

Decay Channels	Branching fractions ($\times 10^{-4}$)	
$B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$	$8.46 \pm 0.14 \pm 0.29 \pm 0.40$	arXiv: 1505.01710; 3 fb ⁻¹
$B_s^0 \rightarrow \bar{D}^0 f_0(980)$	$0.017 \pm 0.010 \pm 0.005 \pm 0.001$	arXiv: 1505.01654; 3 fb ⁻¹
$B^0 \rightarrow \bar{D}^0 K^+ \pi^-$	$0.92 \pm 0.06 \pm 0.07 \pm 0.06$	arXiv: 1505.01505; 3 fb ⁻¹
$B_s^0 \rightarrow \bar{D}^0 K^- \pi^+$	$10.0 \pm 0.4 \pm 1.0 \pm 1.0$	PRD 90, 072003 (2014); 3 fb ⁻¹
$B^0 \rightarrow \bar{D}^0 K^- K^+$	$0.47 \pm 0.09 \pm 0.06 \pm 0.05$	PRL 109, 131801 (2012); 0.62 fb ⁻¹
$B_s^0 \rightarrow \bar{D}^0 K^- K^+$	0.42 ± 0.19	
$B^- \rightarrow D^+ K^- \pi^-$	$0.731 \pm 0.019 \pm 0.022 \pm 0.039$	PRD 91, 092002 (2015); 3 fb ⁻¹
.....	

Rich physics programs with $B \rightarrow Dhh$ decays at LHCb:

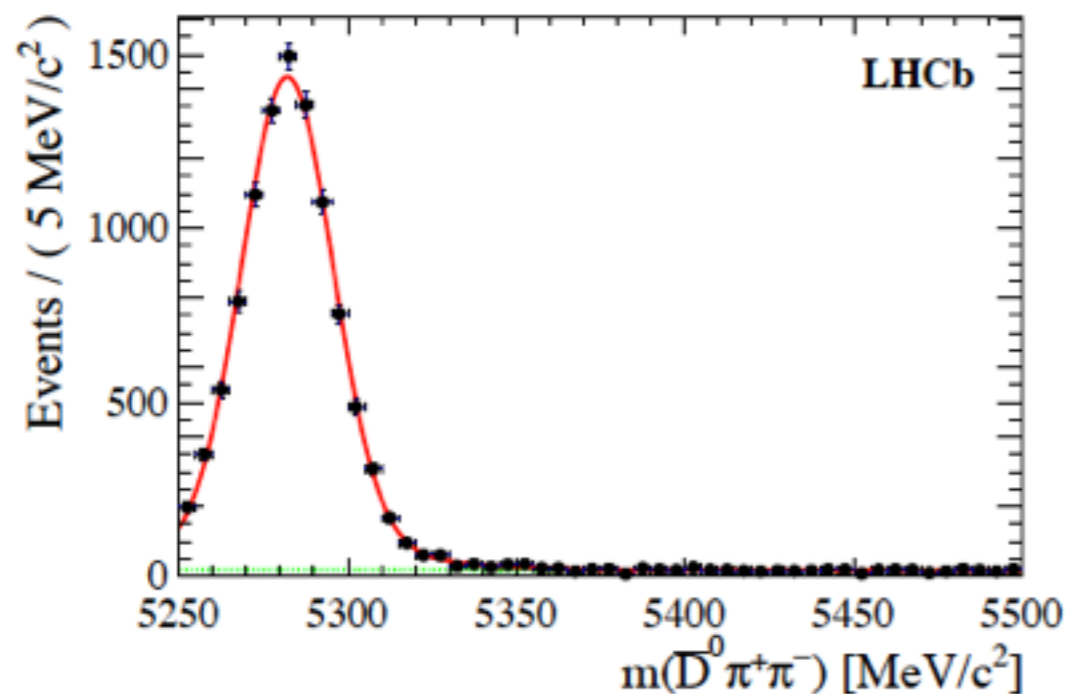
- Understand excited D meson spectroscopy
- Understand $\pi\pi$, $K\pi$, KK spectrum
- can be used for further studies to extract CKM angle γ , $\beta_{(s)}$

Dalitz plot analyses strategy (1)

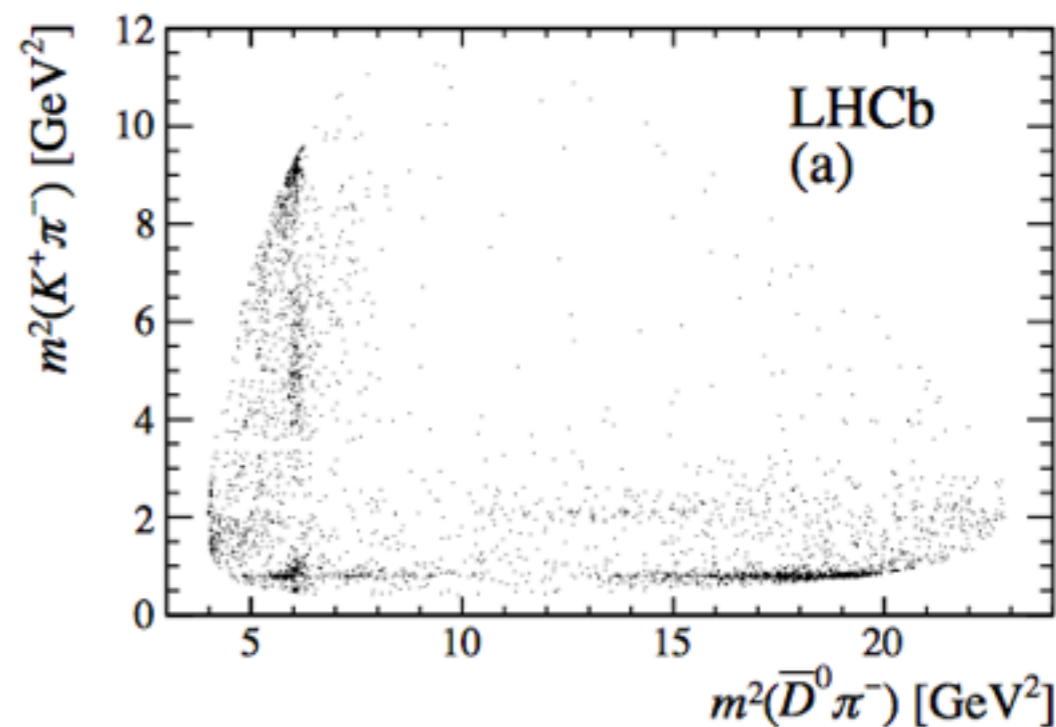
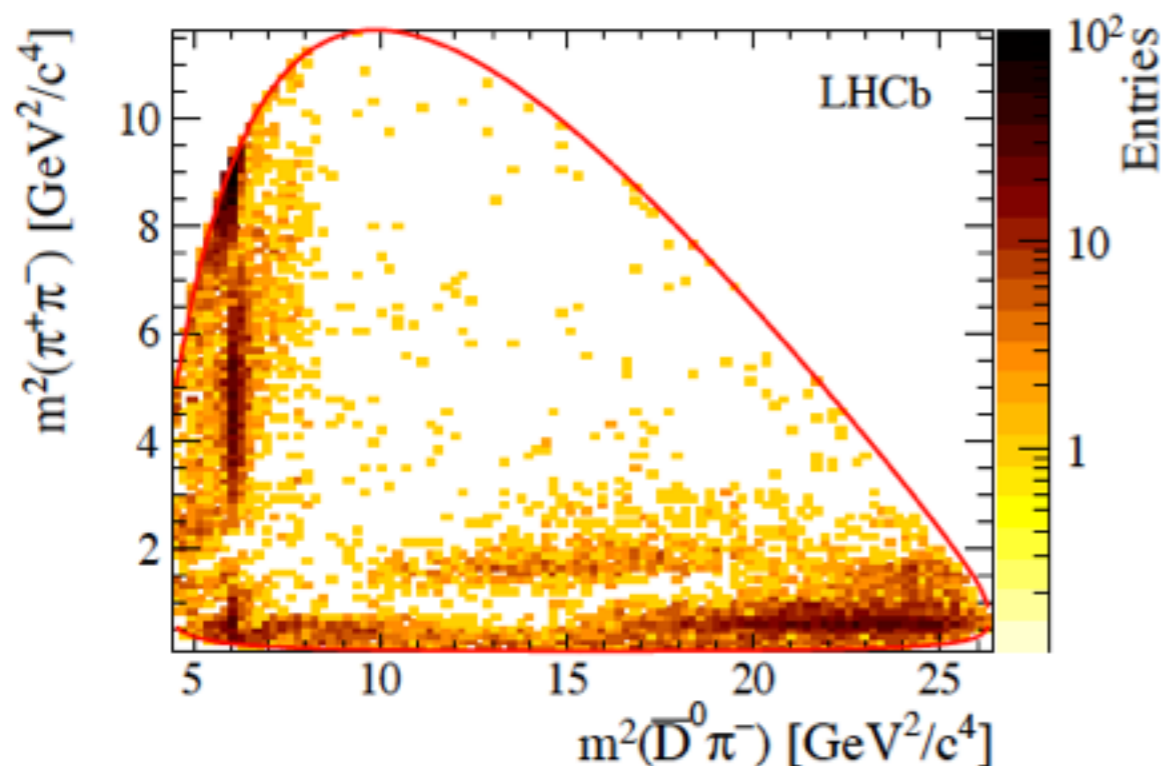
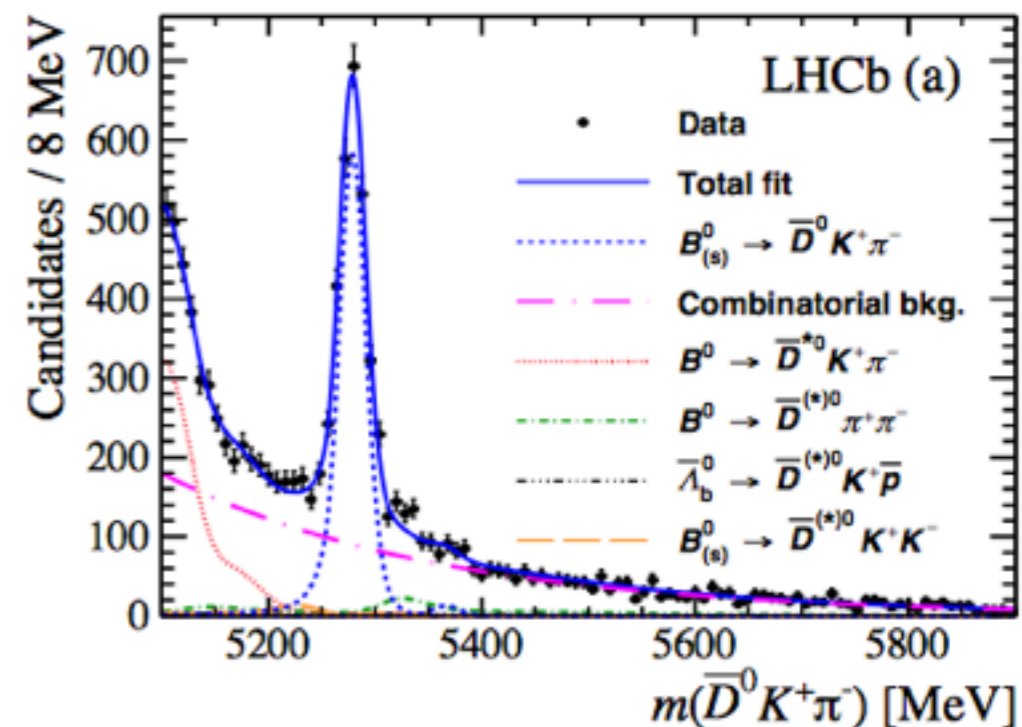
Similar Dalitz plot analysis strategy applied:

➤ Optimized selection to achieve clean environment for Dalitz plot analyses

arXiv: 1505.01710; 3 fb⁻¹



arXiv: 1505.01505; 3 fb⁻¹

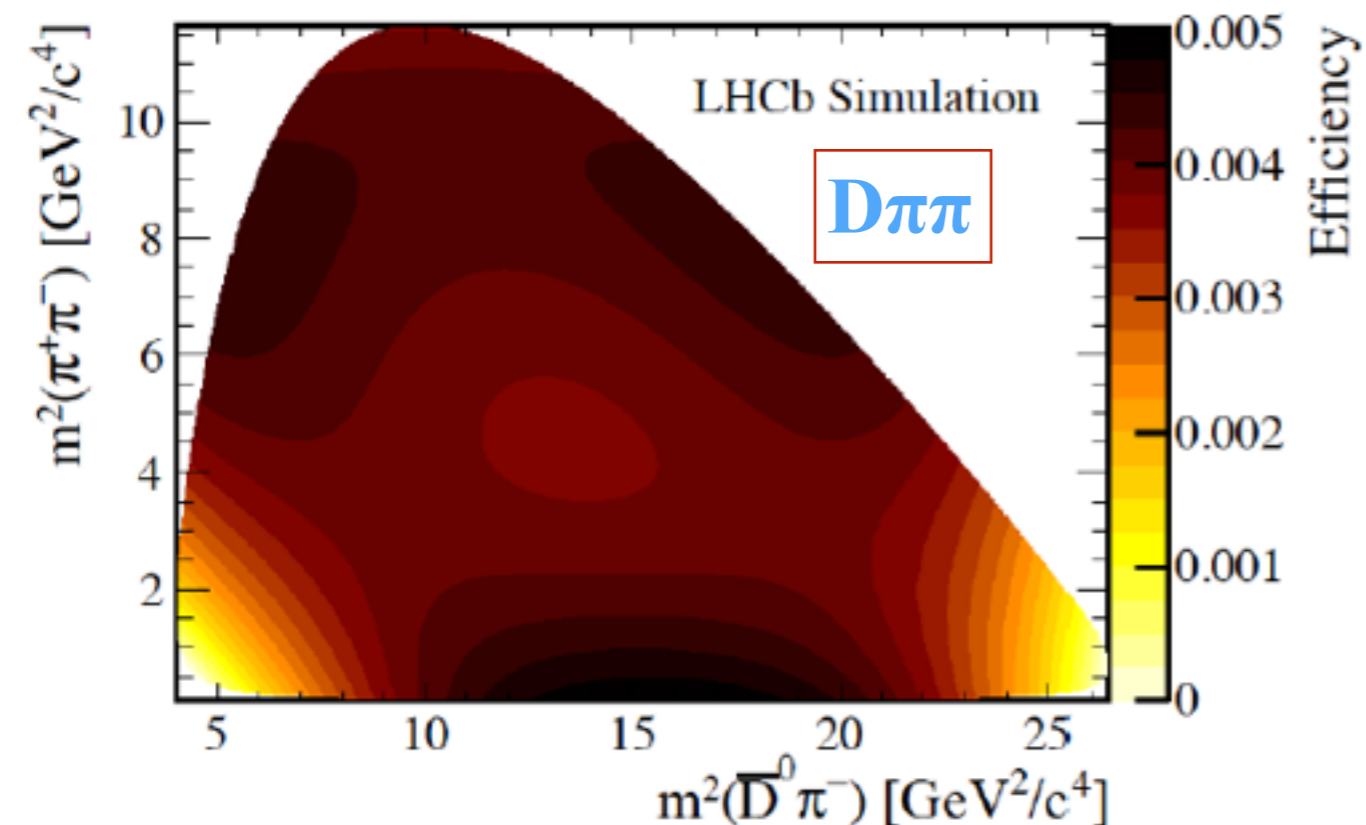


Dalitz plot analyses strategy (2)

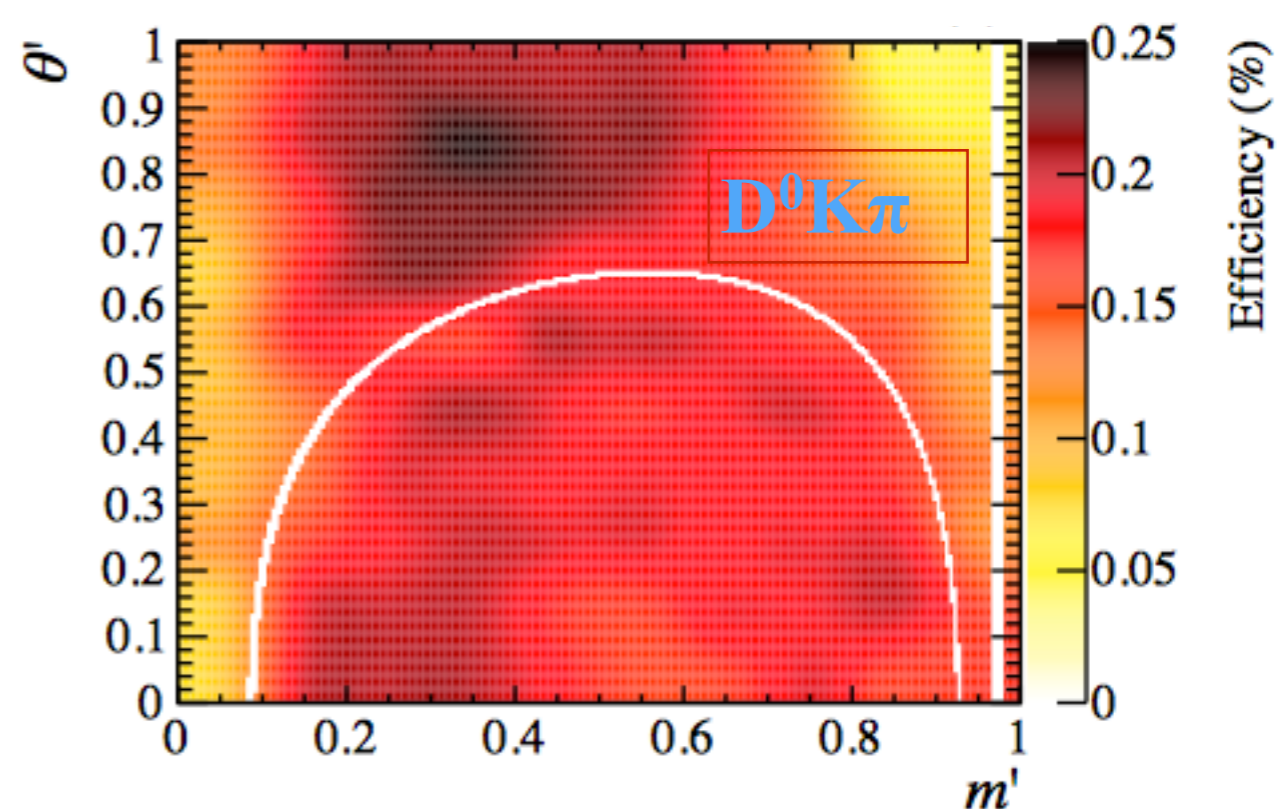
Similar Dalitz plot analysis strategy applied:

- Efficiency obtained from Monte Carlo with data-driven method to correct for data and Monte Carlo difference

arXiv: 1505.01710; 3 fb⁻¹ $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$



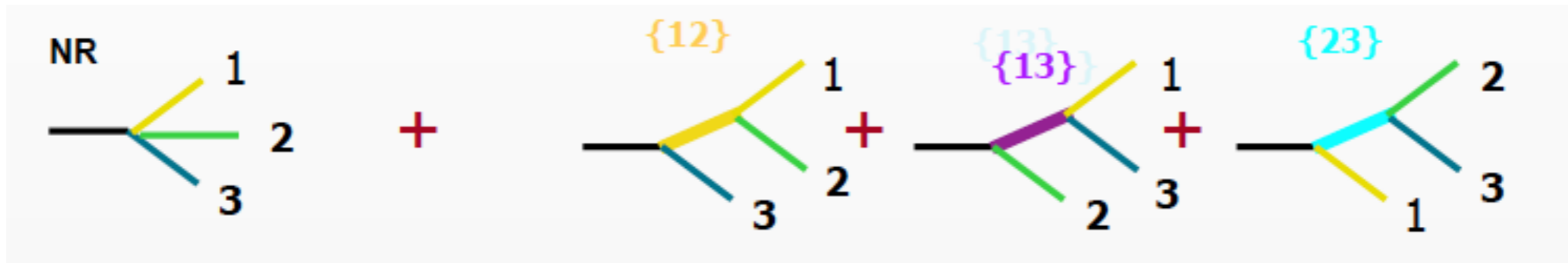
arXiv: 1505.01505; 3 fb⁻¹ $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$



- Combinatorial background modeled from sidebands
- Peaking background either suppressed to negligible level or modeled using Dalitz model obtained from other analyses

Dalitz formalism with $B \rightarrow Dh\bar{h}$

Modeled by Isobar formalism: total amplitude as coherent sum of quasi-two-body contributions ($\pi\pi$ S-wave also uses K-matrix formalism)



$$A(s_{12}, s_{23}) = \sum_j A_j = \sum_j a_j F_j(s_{12}, s_{23})$$

CP violation effect negligible in current analyses

- s_{12}, s_{23} are the invariant mass squared of two of the three decay particles
- sum over all resonant contributions
- a_j : complex fit parameters to describe relative contributions between resonances
- $F_j(s_{12}, s_{23})$: strong dynamics including resonant line shapes, angular distributions etc.

Output of Dalitz plot analyses

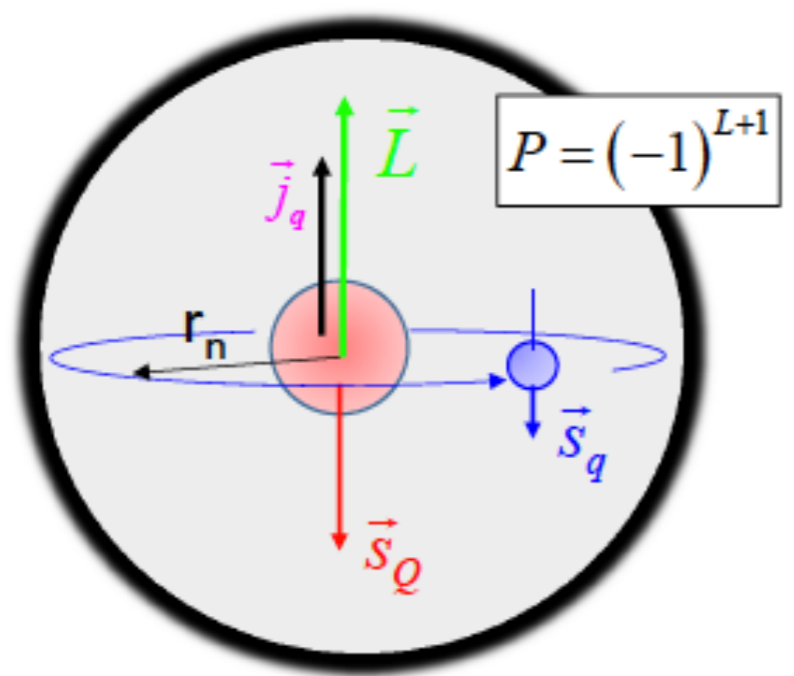
- Resonant contributions, relative amplitudes and phases of resonances, fit fractions, resonant properties etc.

Spectroscopy of charmed mesons

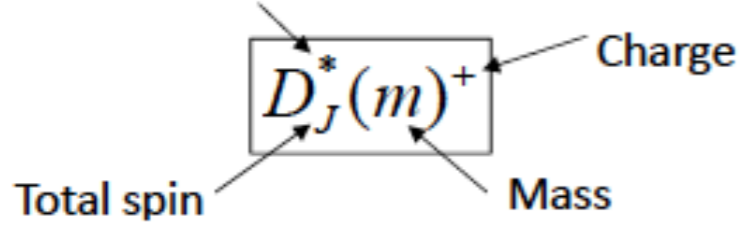
- Tests of HQET, potential models, Lattice QCD, ...
- Inputs for other studies, exotic states, $R(D^{(*)})$, ...

J^P $Q\bar{q}$ meson

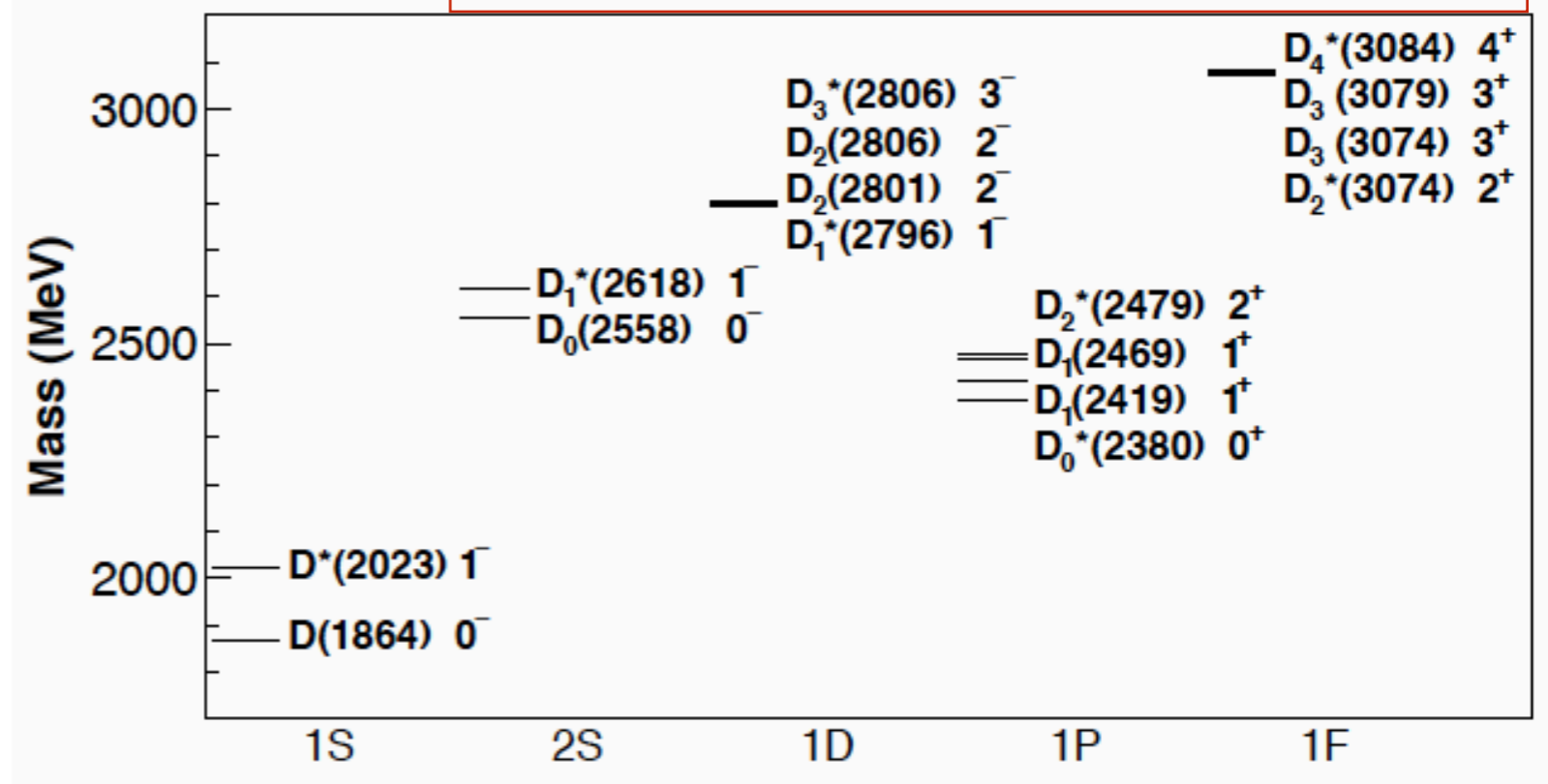
$$\vec{J} = \vec{j}_q + \vec{s}_Q = \vec{L} + \vec{s}_q$$



* Indicates "natural" parity ($0^+, 1^-, 2^+, \dots$)



S. Godfrey, N. Isgur, Phys. Rev. D32, 189 (1985)



States appear in doublet with similar widths: one with "natural" parity ($0^+, 1^-, 2^+, \dots$) and one with "unnatural" parity ($0^-, 1^+, 2^-, \dots$)

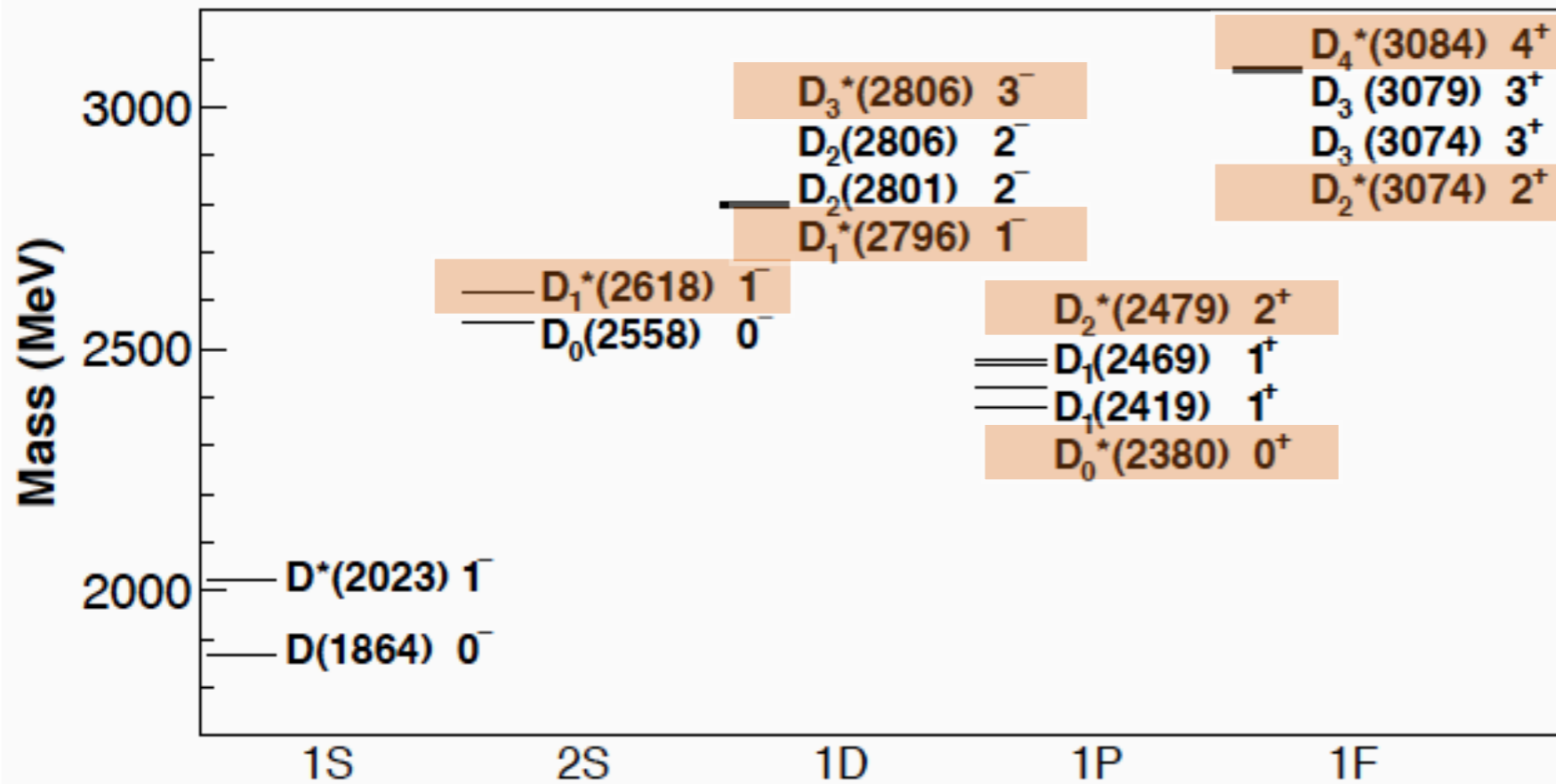
Similar for D^{*0}, D^{*+}, D_s^{*+}

Excited D meson states

arXiv: 1505.01710; 3 fb⁻¹

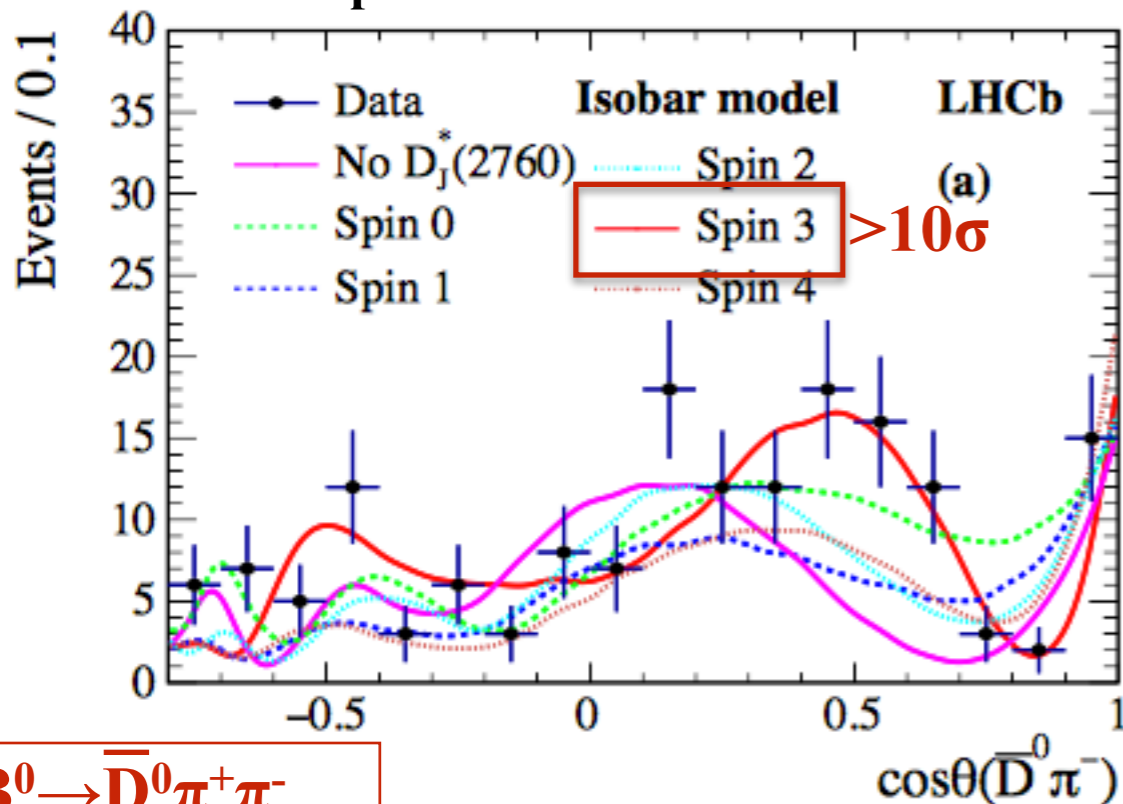
PRD 91, 092002 (2015); 3 fb⁻¹

JHEP 09, 145 (2013); 3 fb⁻¹



States in $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$,
 $B^0 \rightarrow \bar{D}^0 K^+ \pi^-$, $B^- \rightarrow D^+ K^- \pi^-$,
 Dalitz plot analysis

$\theta(D\pi)$ is helicity angle defined between directions of two pions in the rest frame of resonance



- $D_0(2400)$, $D_2(2460)$ dominant in all analyses
- Many new D^* states observed in inclusive D spectroscopy: $D^*(2650)$, $D^*(2760)$, $D^*(3000)$
- A D^* with spin 3 and mass around 2800 MeV observed in $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$ analysis
- A D^* with spin 1 and mass around 2791 MeV observed in $B^- \rightarrow D^+ K^- \pi^-$ analysis

$B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$

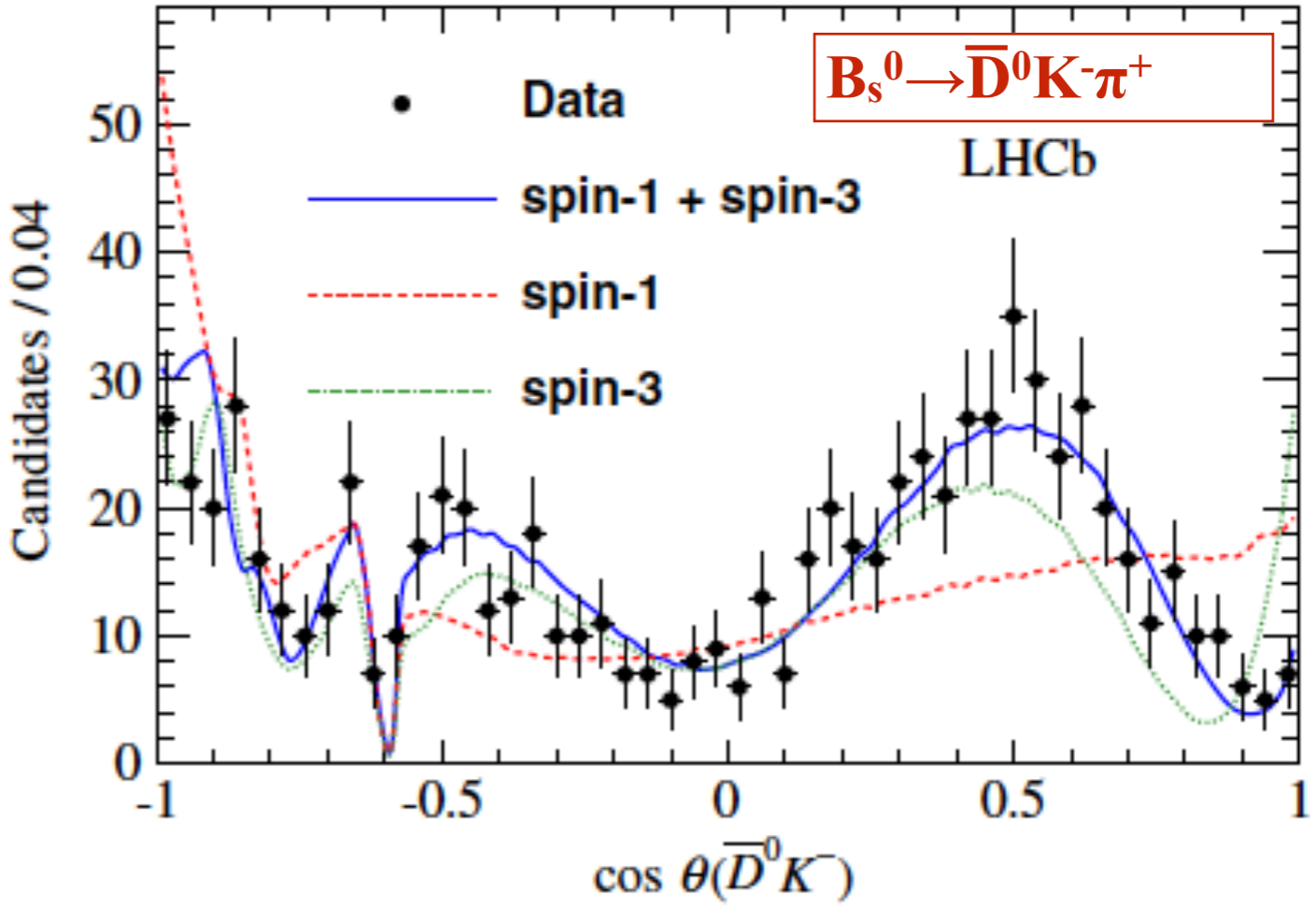
Excited D_s meson states

LHCb, PRD 90, 072003 (2014); 3 fb⁻¹
 LHCb, JHEP 10, 151 (2012); 1 fb⁻¹
 Babar, PRD 80, 092003 (2009)

State	Mass	Width	Comment
		<i>BABAR</i>	
$D_{s1}^*(2700)^-$	$2710 \pm 2_{-7}^{+12}$	$149 \pm 7_{-52}^{+39}$	Seen in DK and D^*K
$D_{sJ}^*(2860)^-$	$2862 \pm 2_{-2}^{+5}$	$48 \pm 3 \pm 6$	Seen in DK and D^*K
$D_{sJ}^*(3040)^-$	$3044 \pm 8_{-5}^{+30}$	$239 \pm 35_{-42}^{+46}$	Seen in D^*K only
		<i>LHCb</i>	
$D_{s1}^*(2700)^-$	$2709.2 \pm 1.9 \pm 4.5$	$115.8 \pm 7.3 \pm 12.1$	Only DK studied
$D_{sJ}^*(2860)^-$	$2866.1 \pm 1.0 \pm 6.3$	$69.9 \pm 3.2 \pm 6.6$	

➤ Many new D_s^* states also observed in inclusive D_s spectroscopy: $D_s^*(2700)$, $D_s^*(2860)$, $D_s^*(3040)$

➤ A structure around 2860 MeV with both spin 1 and spin 3 resonant contributions is found



Excited D meson masses and widths

➤ Spin 3 D* meson around 2800 MeV from $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$

		Isobar				K-matrix			
$D_3^*(2760)$	m	$2798 \pm 7 \pm 1 \pm 7$			$2802 \pm 11 \pm 10 \pm 3$				
	Γ	$105 \pm 18 \pm 6 \pm 23$			$154 \pm 27 \pm 13 \pm 9$				

➤ Spin 1 D* meson around 2791 MeV from $B^- \rightarrow D^+ K^- \pi^-$

$D_1^*(2760)$	m	$2791 \pm 18 \pm 11 \pm 6$
	Γ	$177 \pm 32 \pm 20 \pm 7$

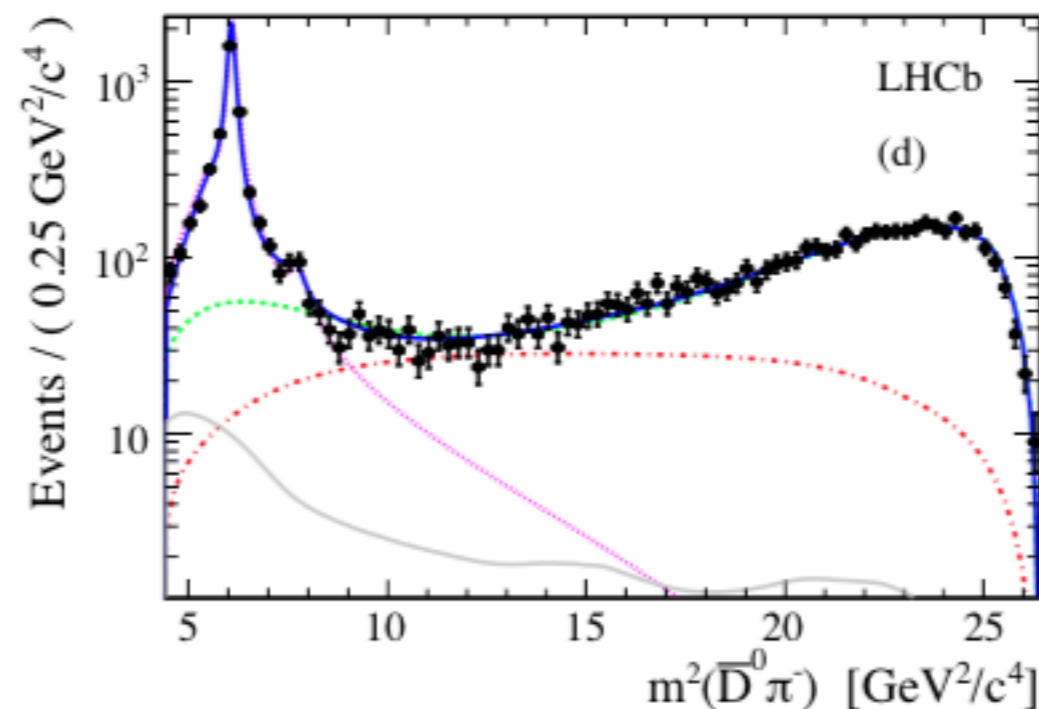
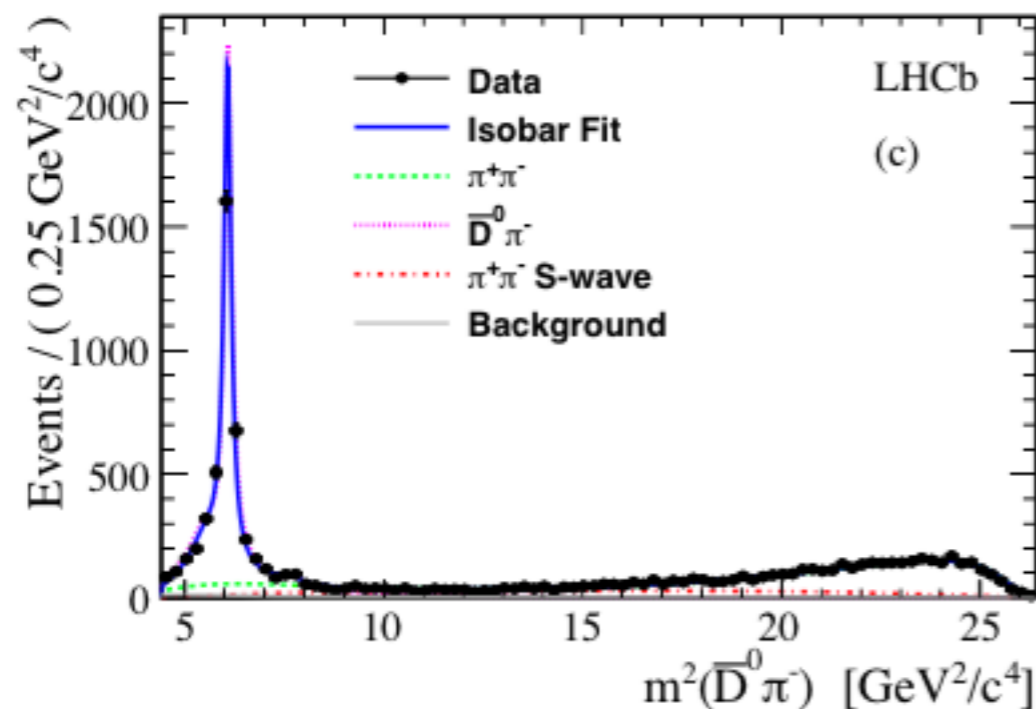
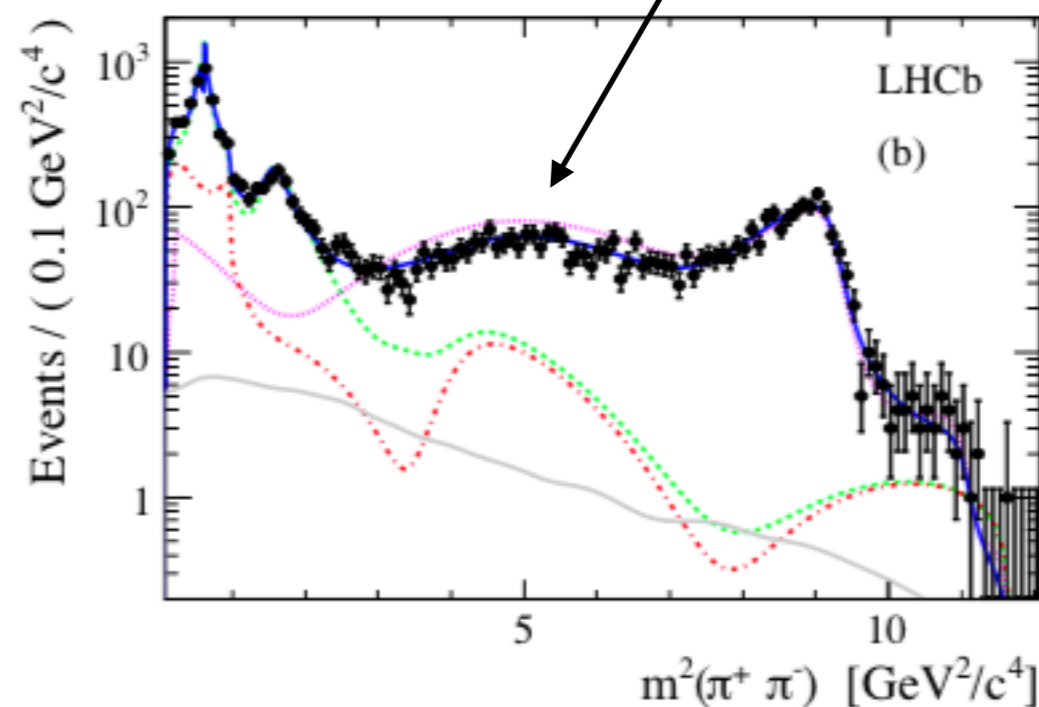
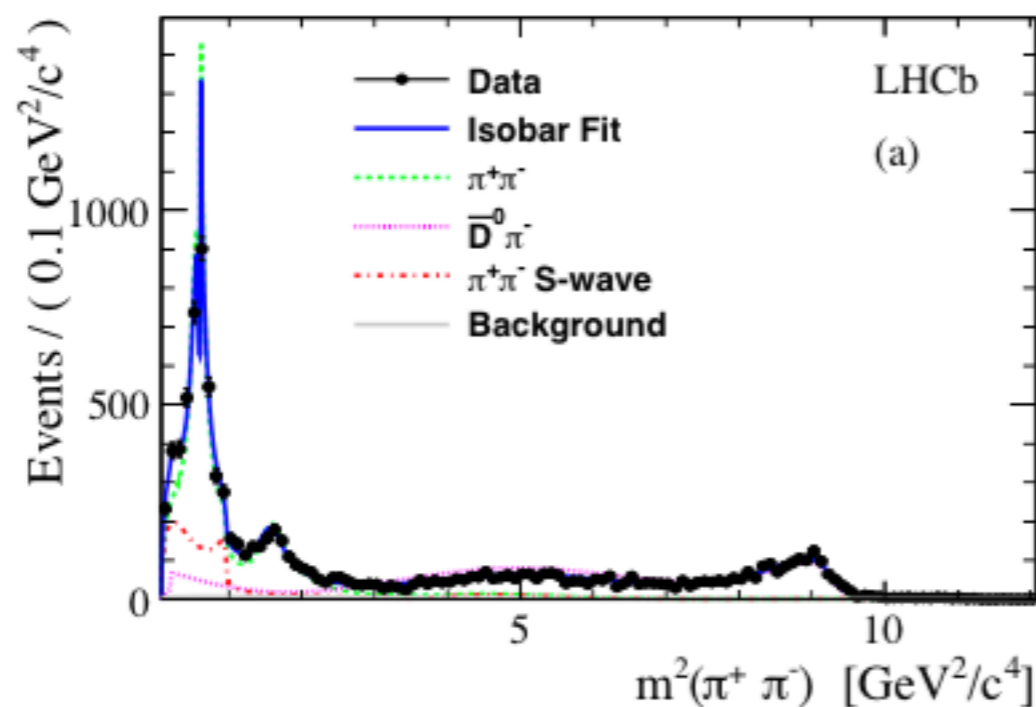
➤ Spin 1 and spin 3 mixture of D_s^* meson around 2860 MeV from $B_s^0 \rightarrow \bar{D}^0 K^- \pi^+$

$D_{s1}^*(2860)$	m	$2859 \pm 12 \pm 6 \pm 23$
	Γ	$159 \pm 23 \pm 27 \pm 72$
$D_{s3}^*(2860)$	m	$2860.5 \pm 2.6 \pm 2.5 \pm 6.0$
	Γ	$53 \pm 7 \pm 4 \pm 6$

➤ More precise and accurate also for other D* states like $D_0^*(2400)$, $D_2^*(2460)$ etc compared to previous measurements

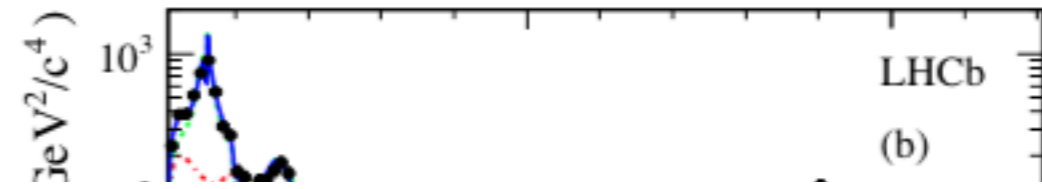
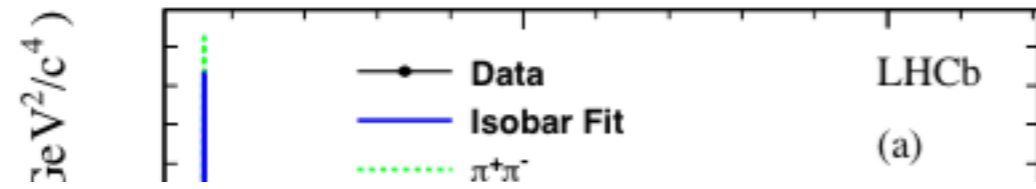
Dalitz fit display: $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$

larger subcomponent due to interference

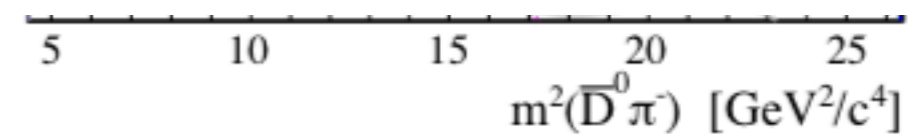
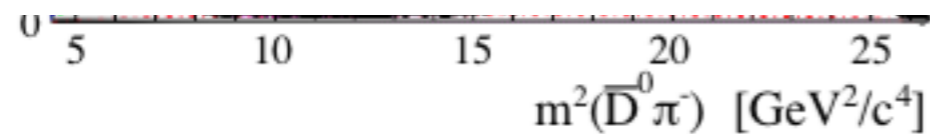


linear

log

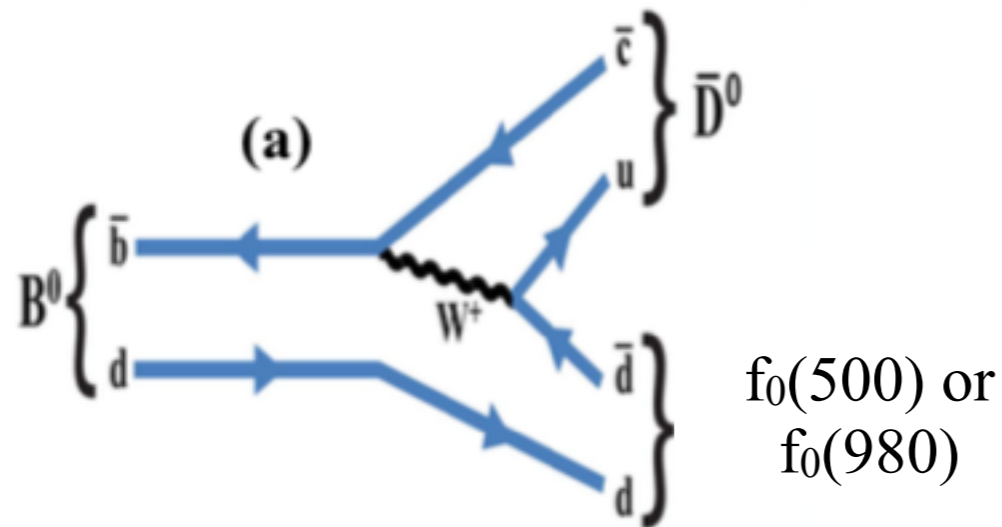
Dalitz fit display: $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$ 

Resonance	Isobar ($\times 10^{-5}$)					K-matrix ($\times 10^{-5}$)				
$f_0(500)$	11.2 ± 0.8	0.5 ± 0.5	2.1 ± 0.5	0.8 ± 0.5	0.5 ± 0.5	n/a				
$f_0(980)$	1.34 ± 0.25	0.10 ± 0.06	0.46 ± 0.06	0.25 ± 0.06	0.10 ± 0.06	n/a				
$f_0(2020)$	1.35 ± 0.31	0.14 ± 0.06	0.85 ± 0.06	0.31 ± 0.06	0.14 ± 0.06	n/a				
S-wave	14.1 ± 0.5	0.6 ± 0.7	1.3 ± 0.7	0.5 ± 0.7	0.6 ± 0.7	14.2 ± 0.6	1.5 ± 0.9	0.9 ± 0.7	0.6 ± 0.7	1.5 ± 0.9
$\rho(770)$	32.1 ± 1.0	1.2 ± 1.5	0.9 ± 1.5	1.0 ± 1.5	1.2 ± 1.5	31.0 ± 1.0	2.1 ± 0.7	0.7 ± 1.5	1.0 ± 1.5	2.1 ± 0.7
$\omega(782)$	0.42 ± 0.11	0.02 ± 0.02	0.03 ± 0.02	0.11 ± 0.02	0.02 ± 0.02	0.43 ± 0.11	0.02 ± 0.02	0.02 ± 0.02	0.11 ± 0.02	0.02 ± 0.02
$\rho(1450)$	1.36 ± 0.28	0.08 ± 0.06	0.19 ± 0.06	0.28 ± 0.06	0.08 ± 0.06	1.91 ± 0.37	0.73 ± 0.19	0.19 ± 0.09	0.37 ± 0.09	0.73 ± 0.19
$\rho(1700)$	0.33 ± 0.11	0.06 ± 0.02	0.05 ± 0.02	0.11 ± 0.02	0.06 ± 0.02	0.73 ± 0.18	0.53 ± 0.10	0.10 ± 0.03	0.18 ± 0.03	0.53 ± 0.10
$f_2(1270)$	9.5 ± 0.5	0.4 ± 0.4	1.0 ± 0.4	0.5 ± 0.4	0.4 ± 0.4	9.1 ± 0.6	0.8 ± 0.5	0.5 ± 0.4	0.6 ± 0.4	0.8 ± 0.5
$D_0^*(2400)^-$	7.7 ± 0.5	0.3 ± 0.4	0.3 ± 0.4	0.5 ± 0.4	0.3 ± 0.4	8.0 ± 0.5	0.8 ± 0.4	0.4 ± 0.4	0.5 ± 0.4	0.8 ± 0.4
$D_2^*(2460)^-$	24.4 ± 0.7	1.0 ± 1.2	0.4 ± 1.2	0.7 ± 1.2	1.0 ± 1.2	23.8 ± 0.7	1.2 ± 0.5	0.5 ± 1.1	0.7 ± 1.1	1.2 ± 0.5
$D_3^*(2760)^-$	1.03 ± 0.16	0.07 ± 0.05	0.08 ± 0.05	0.16 ± 0.05	0.07 ± 0.05	1.34 ± 0.19	0.16 ± 0.06	0.06 ± 0.06	0.19 ± 0.06	0.16 ± 0.06



Light meson structure (1)

2-q model



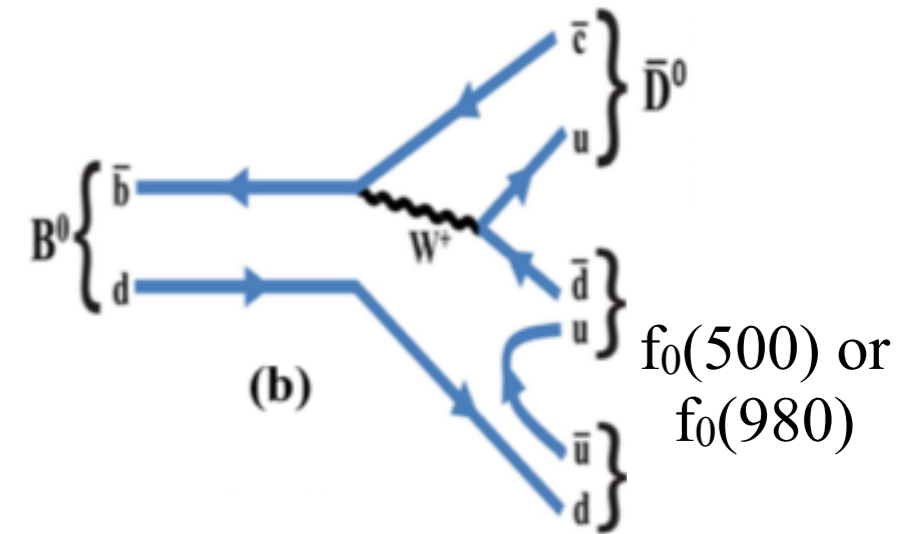
$$|f_0(500)\rangle = \frac{1}{\sqrt{2}}(|\bar{u}u\rangle + |\bar{d}d\rangle) \equiv |\bar{n}n\rangle$$

$$|f_0(980)\rangle = |\bar{s}s\rangle$$

$$|f_0(980)\rangle = |\bar{s}s\rangle \cos \theta + |\bar{n}n\rangle \sin \theta,$$

$$|f_0(500)\rangle = -|\bar{s}s\rangle \sin \theta + |\bar{n}n\rangle \cos \theta.$$

4-q model



$$|f_0(500)\rangle = |\bar{u}u\bar{d}d\rangle$$

$$|f_0(980)\rangle = |\bar{n}n\bar{s}s\rangle$$

$$|f_0(980)\rangle = |\bar{n}n\bar{s}s\rangle \cos \phi + |\bar{u}u\bar{d}d\rangle \sin \phi,$$

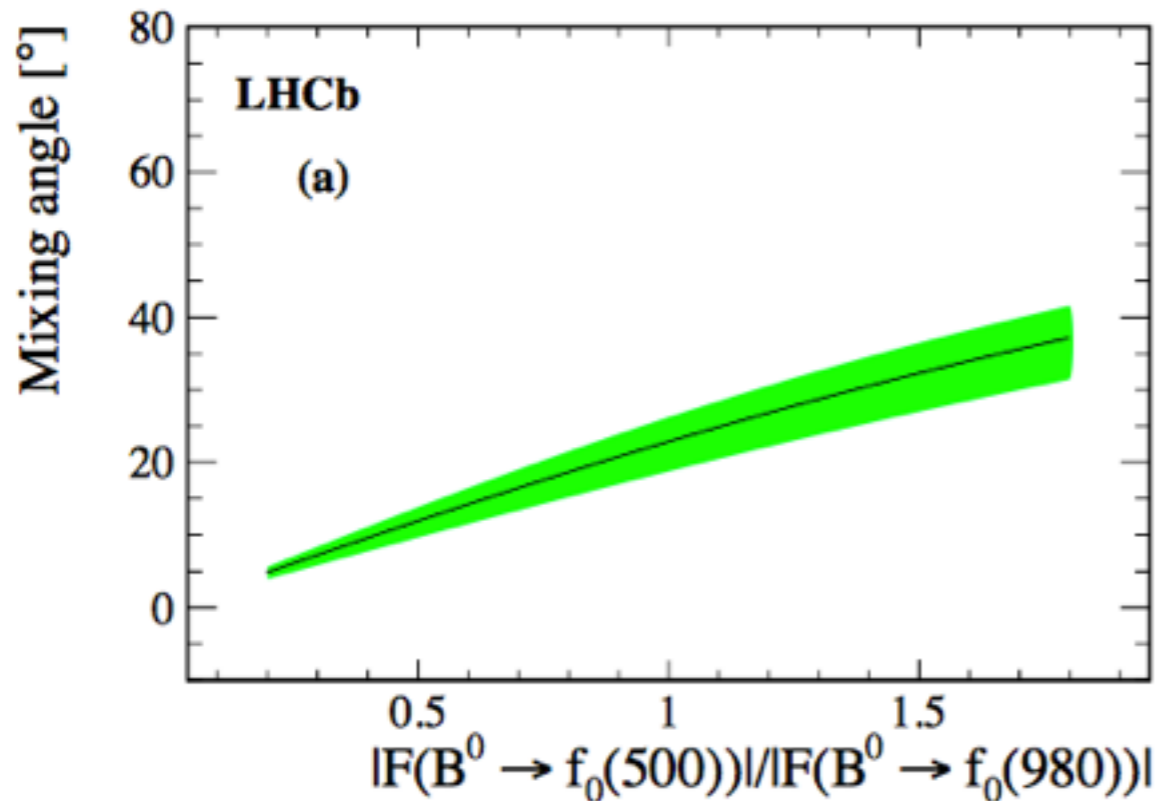
$$|f_0(500)\rangle = -|\bar{n}n\bar{s}s\rangle \sin \phi + |\bar{u}u\bar{d}d\rangle \cos \phi,$$

➤ Proposals given to use $B_{(s)} \rightarrow J/\psi \pi \pi$ to understand nature of light mesons $f_0(500)$ and $f_0(980)$ and has been performed by LHCb to set upper limits on mixing angles

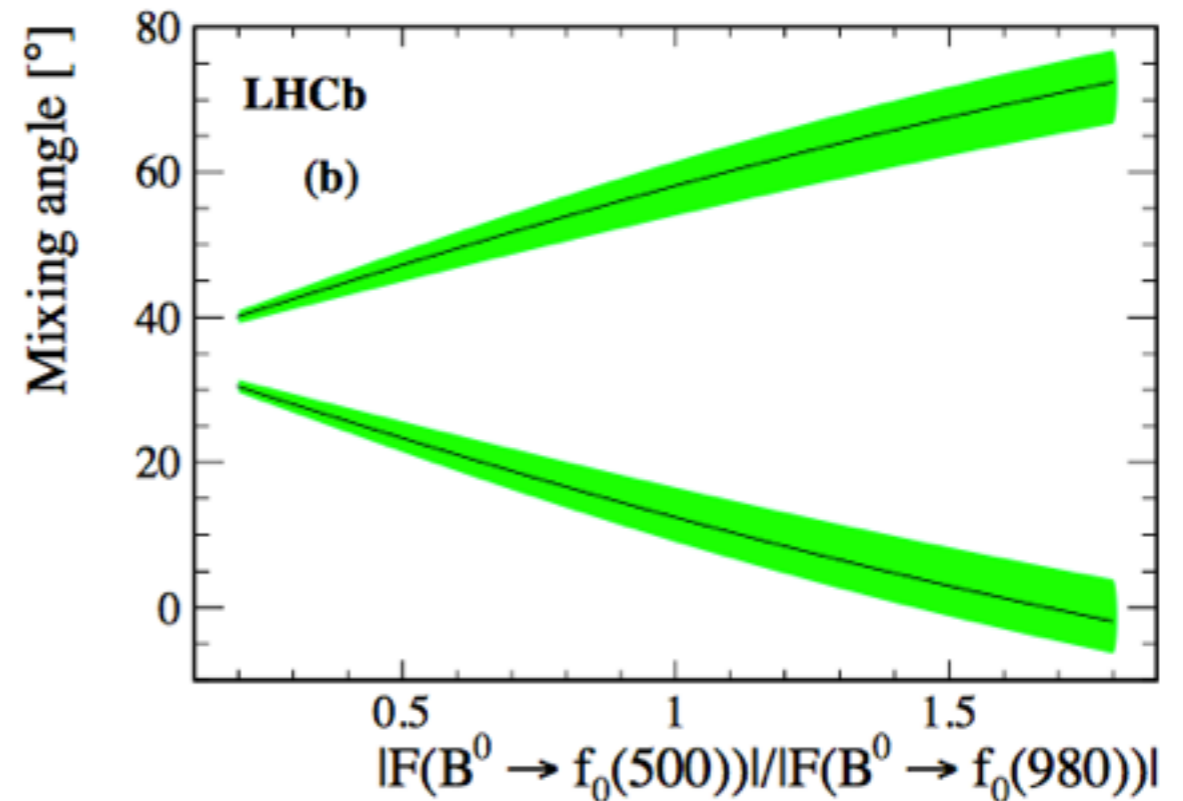
➤ Similar studies can also be done for $B_{(s)} \rightarrow \bar{D}^0 \pi \pi$ decays

	$\mathcal{B}(B^0 \rightarrow \bar{D}^0 f_0)$	$\mathcal{B}(B_s^0 \rightarrow \bar{D}^0 f_0)$
$f_0(500)$	$(11.2 \pm 0.8 \pm 0.5 \pm 2.1 \pm 0.5) \times 10^{-5}$	—
$f_0(980)$	$(1.34 \pm 0.25 \pm 0.10 \pm 0.46 \pm 0.06) \times 10^{-5}$	$(1.7 \pm 1.0 \pm 0.5 \pm 0.1) \times 10^{-6}$

2-q model



4-q model



➤ Mixing angles of 2-q and 4-q model given as a function of form factor ratios

➤ Results from $B_s^0 \rightarrow \bar{D}^0 f_0(980)$, $B^0 \rightarrow \bar{D}^0 f_0(980)$ and $B^0 \rightarrow \bar{D}^0 f_0(500)$ indicate complicated nature of the system

Other results

Channels	Isobar $\times 10^{-5}$	K-Matrix
$\rho(770)(\pi^+\pi^-)$	$32.1 \pm 1.4 \pm 1.2 \pm 0.9 \pm 1.5$	$31.0 \pm 1.4 \pm 2.1 \pm 0.7 \pm 1.5$

➤ **Isospin symmetry between three decays: $B^+ \rightarrow D^0 \rho^+$, $B^0 \rightarrow D^- \rho^+$, $B^0 \rightarrow \bar{D}^0 \rho^0$,**

$$A(\bar{D}^0 \rho^+) = \sqrt{3} A_{3/2},$$

$$A(D^- \rho^+) = \sqrt{1/3} A_{3/2} + \sqrt{2/3} A_{1/2},$$

$$A(\bar{D}^0 \rho^0) = \sqrt{2/3} A_{3/2} - \sqrt{1/3} A_{1/2},$$

In factorization approximation:

$$R_{D\rho} = \frac{|A_{1/2}|}{\sqrt{2}|A_{3/2}|} = 1 + \mathcal{O}(\Lambda_{QCD}/m_b) \quad \delta_{D\rho} = \arg\left(\frac{A_{1/2}}{A_{3/2}}\right) \sim \mathcal{O}(\Lambda_{QCD}/m_b)$$

Model	$R_{D\rho}$	$\cos \delta_{D\rho}$
Isobar	0.69 ± 0.15	$0.984^{+0.113}_{-0.048}$
K-matrix	0.69 ± 0.15	$0.987^{+0.114}_{-0.048}$

➤ **Uncertainties mainly from Br of $D^+ \rho^+$ and $D^0 \rho^-$**

➤ **The results are not different from the prediction of factorization**

Conclusion

- **Rich physics in $B \rightarrow Dhh$ systems using Dalitz plot techniques**
- **Studies have been performed to understand their resonant contributions, excited D^* spectroscopy, light meson structures etc.**
- **Stay tuned for more analyses in the $B \rightarrow Dhh$ system**

Thank You