Flavour changing top decays in the aligned two-Higgs-doublet model

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- $t \rightarrow ch$ in the aligned two-Higgs-doublet model (A2HDM).
- $t \to cV (= \gamma, Z)$ in the aligned two-Higgs-doublet model (A2HDM).
- The 2HDM provides a minimal extension of the scalar sector with a second Higgs doublet, (ϕ_1, ϕ_2) .
- A global SU(2) transformation in the scalar space (ϕ_1, ϕ_2) takes to the so-called Higgs basis (Φ_1, Φ_2)

$$
\left(\begin{array}{c}\Phi_1\\-\Phi_2\end{array}\right)\equiv\frac{1}{v}\left[\begin{array}{cc}v_1&v_2\\v_2&-v_1\end{array}\right]\left(\begin{array}{c}\phi_1\\e^{-i\theta}\phi_2\end{array}\right).
$$
 (1)

• In this basis,

$$
\Phi_1 = \left[\begin{array}{c} G^+ \\ \frac{1}{\sqrt{2}} \left(v + S_1 + iG^0 \right) \end{array} \right] , \qquad \Phi_2 = \left[\begin{array}{c} H^+ \\ \frac{1}{\sqrt{2}} \left(S_2 + iS_3 \right) \end{array} \right] , \qquad (2)
$$

where G^{\pm} , G^0 are the Goldstone fields and $\langle H^+\rangle = \langle G^+\rangle = \langle G^0\rangle = \langle S_i\rangle = 0.$

- The five physical scalars are two charged fields $H^{\pm}(x)$ and three neutral ones $\varphi_i^0(x) = \{h(x), H(x), A(x)\}.$
- The neutral scalars are related to the S_i fields through an orthogonal transformation $\varphi_i^0(x) = \mathcal{R}_{ij} S_j(x)$.
- The form of \mathcal{R}_{ii} depends on the scalar potential.

• In the CP-conserving limit

$$
\left(\begin{array}{c} h \\ H \end{array}\right) \; = \; \left[\begin{array}{cc} \cos \tilde{\alpha} & \sin \tilde{\alpha} \\ -\sin \tilde{\alpha} & \cos \tilde{\alpha} \end{array}\right] \left(\begin{array}{c} S_1 \\ S_2 \end{array}\right) \; . \tag{3}
$$

- The CP-odd field A corresponds to S_3 .
- In the generic 2HDM, however, tree-level FCNC interactions generally exist, through non-diagonal couplings of neutral scalars to fermions.

• In the Higgs basis

$$
\mathcal{L}_Y = -\frac{\sqrt{2}}{v} \left[\bar{Q}'_L (M'_d \Phi_1 + Y'_d \Phi_2) d'_R + \bar{Q}'_L (M'_u \tilde{\Phi}_1 + Y'_u \tilde{\Phi}_2) u'_R + \bar{L}'_L (M'_\ell \Phi_1 + Y'_\ell \Phi_2) \ell'_R \right] + \text{h.c.} \,,
$$
\nwhere $\tilde{\Phi}_i(x) = i\tau_2 \Phi_i^*(x)$ are the charge-conjugated scalar doublets. (4)

• In general, the Yukawa matrices M'_f and Y'_f cannot be simultaneously diagonalized in flavour space.

- An elegant solution is to use an appropriately chosen \mathcal{Z}_2 symmetries. Glashow and S. Weinberg 1977
- This guarantees the absence of FCNCs in the Yukawa sector.

• Flavour conservation in the neutral scalar couplings can be enforced in a rather trivial way requiring the Yukawa coupling matrices to be aligned in flavour space.

Pich and Tuzón 2009

• In the A2HDM, the interactions of scalar fields with fermions are described by

$$
Y_{d,\ell} = s_{d,\ell} M_{d,\ell}, \qquad Y_u = s_u^* M_u. \qquad (5)
$$

• In the A2HDM the mass-eigenstate Yukawa Lagrangian reads

$$
\mathcal{L}_Y = -\frac{\sqrt{2}}{v} H^+(x) \left\{ \bar{u}(x) \left[c_d V M_d \mathcal{P}_R - c_u M_u^{\dagger} V \mathcal{P}_L \right] d(x) + c_l \bar{\nu}(x) M_l \mathcal{P}_R I(x) \right\} - \frac{1}{v} \sum_{\varphi, f} y_f^{\varphi_i^0} \varphi_i^0(x) \bar{f}(x) M_f \mathcal{P}_R f(x) + \text{h.c.}, \tag{6}
$$

where V denotes the CKM matrix.

• The couplings of the neutral scalar fields are given by:

$$
y_{d,l}^{\varphi_i^0} = \mathcal{R}_{i1} + (\mathcal{R}_{i2} + i \mathcal{R}_{i3}) \varsigma_{d,l}, \qquad \qquad y_u^{\varphi_i^0} = \mathcal{R}_{i1} + (\mathcal{R}_{i2} - i \mathcal{R}_{i3}) \varsigma_u^* \,.
$$
 (7)

- Quantum corrections induce some misalignment of the Yukawa coupling matrices, generating small FCNC effects suppressed by the corresponding loop factors.
- However, the special structure of the A2HDM strongly constrains the possible FCNC interactions. Pich and Tuzón 2009

• The one-loop gauge corrections preserve the alignment while the only FCNC structures induced by the scalar contributions take the form

$$
\mathcal{L}_{\text{FCNC}} = \frac{C(\mu)}{4\pi^2 \nu^3} (1 + \varsigma_u^* \varsigma_d) \times
$$

$$
\times \sum_i \varphi_i^0(x) \left\{ (\mathcal{R}_{i2} + i \mathcal{R}_{i3}) (\varsigma_d - \varsigma_u) \left[\bar{d}_L V^\dagger M_u M_u^\dagger V M_d d_R \right] - \right. \\ \left. - (\mathcal{R}_{i2} - i \mathcal{R}_{i3}) (\varsigma_d^* - \varsigma_u^*) \left[\bar{u}_L V M_d M_d^\dagger V^\dagger M_u u_R \right] \right\}
$$

 $+$ h.c.

Jung, Pich and Tuzón 2010

• The renormalization of the coupling constant C is determined, using dimensional regularization, to be

$$
C = C_R(\mu) + \frac{1}{2} \left\{ \frac{2\mu^{D-4}}{D-4} + \gamma_E - \ln(4\pi) \right\},
$$
 (8)

Li, Lu and Pich 2014

• The renormalized coupling satisfies

$$
C_R(\mu) = C_R(\mu_0) - \ln(\mu/\mu_0).
$$
 (9)

• Assuming Yukawa alignment to be exact at a given energy scale Λ_A , so that $C_R(\Lambda_A) = 0$, implies that $C_R(\mu) = \ln(\Lambda_A/\mu)$.

Model	ς_d	ς_{tt}	ς_I
Type I	$\cot \beta$	$\cot \beta$	$\cot \beta$
Type II	$-$ tan β	$\cot \beta$	$-$ tan β
Type X	$\cot \beta$	$\cot \beta$	$-$ tan β
Type Y	– tan β	$\cot \beta$	$\cot \beta$

Table: Two-Higgs-doublet models with natural flavour conservation.

$t \to ch, cV$ decay

- The flavour-changing top decays $t \to ch, cV$ occur at the one-loop level in the SM.
- The decay rates is suppressed by the loop factor and also receives a strong CKM and GIM suppression. Eilam, Hewett and Soni 1991, Mele, Petrarca and Soddu 1998, Aguilar-Saavedr 2004
- Fixing the Higgs mass at $M_h \simeq 125$ GeV, one obtains the SM branching ratios: $Br(t \to ch) \sim \mathcal{O}(10^{-15})$, $Br(t \to c\gamma) \sim \mathcal{O}(10^{-14})$ and $Br(t \to cZ) \sim \mathcal{O}(10^{-14})$.
- Within the A2HDM these decay rates can be enhanced due to additional charged Higgs contributions at the loop level. Celis, Li, Lu, Pich and GA 2015
- The ATLAS and CMS collaborations have searched for flavour-changing decays of the top quark.
- The ATLAS has set the bound $Br(t \rightarrow qZ) < 0.73\%$ at the 95% confidence leve. Aad et al 2012
- The CMS has set a better limit, $Br(t \rightarrow qZ) < 0.05\%$. Chatrchyan et al 2013

$t \to ch, cV$ decays

- The strongest current bound on $t \to c\gamma$ decay by the CMS is $Br(t \to c\gamma) < 0.182\%$. CMS 2014
- The ATLAS collaboration sets the limit $Br(t \rightarrow gh) < 0.79\%$. Aad et al 2014
- A slightly stronger limit, $Br(t \rightarrow qh) < 0.56\%$, has been obtained by the CMS collaboration. CMS 2014
- One expects to improve the limits to $10^{-4} 10^{-5}$ level for $Br(t \to ch)$.

Figure: Penguin diagrams contributing to $t\to c\varphi_j^0$ in the Feynman gauge.

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- The CP-conserving A2HDM contains 12 free real parameters: μ_2 , λ_k $(k = 1, \ldots, 7)$, the three alignment constants ς_f $(f = u, d, l)$ and the counter-term coupling $C_R(\mu)$.
- Some of the parameters of the scalar potential can be traded by the physical scalar masses and the mixing angle $\tilde{\alpha}$.
- \bullet The decays $t\to c\,\varphi^0_j, cZ$ are only sensitive to $\{M_{\varphi^0_j},\,M_{H^\pm},\, \cos\tilde\alpha,\,\lambda_3,\,\lambda_7,\,\varsigma_u,\,\varsigma_d,\,\ldots\}$ $C_R(M_W)$.
- We assume that the 125 GeV Higgs boson corresponds to the lightest CP-even state h; i.e., we fix $M_h \simeq 125$ GeV.
- The LHC data imply that it couples to the massive gauge vector bosons with a SM-like strength so that cos $\tilde{\alpha} \simeq 1$.

We analyze the parameter space of the A2HDM, subject to the following assumptions and constraints:

- The LHC and Tevatron Higgs data imply that $\cos \tilde{\alpha} > 0.9$ (68% CL) and $|y_f^h| \sim 1$ $(f = u, d, l).$
- We work in the limit cos $\tilde{\alpha} = 1$ so that no constraints on the alignment parameters are obtained from the 125 GeV Higgs data. Celis, Ilisie and Pich 2013
- We take into account constraints in the $\varsigma_u \varsigma_d$ plane derived from the measurement of $Br(\bar{B}\to X_s\gamma)$. Jung, Pich and Tuzón 2010, Jung, Li and Pich 2012
- We restrict the alignment parameter $|\varsigma_u| \leq 2$, in order to satisfy the constraints from $Z\rightarrow \bar{b}b$ decay and $\mathcal{B}^{0}_{s,d}-\bar{\mathcal{B}}^{0}_{s,d}$ mixings.
- The parameters $\varsigma_{d,l}$ are much less constrained phenomenologically; we take $|S_{d,\ell}| \leq 50$. Jung, Pich and Tuzón 2010, Jung, Li and Pich 2012
- The LEP has searched for pair-produced charged Higgs bosons in the framework of 2HDMs, excluding $M_{H\pm} \lesssim 80$ GeV (95% CL) under the assumption that H^{\pm} decays dominantly into fermions. G. Abbiendi et al. 2013
- Searches for a light charged Higgs via the decay $t \rightarrow H^+b$ performed by the ATLAS and CMS collaborations, together with the limits on a charged Higgs from the Tevatron are taken into account. Aad et. al 2013, 2014, CMS 2014, Gutierrez et. al 2010
- These direct searches give an upper bound on the Yukawa combination $|\varsigma_u \varsigma_d|$, which, although being weaker than the one from $Br(\bar{B}\to X_s\gamma)$, basically exclude one of the two possible strips allowed by the latter. Celis, Ilisie and Pich 2013
- We consider the perturbativity bound on the quartic scalar couplings $|\lambda_{3,7}| \leq 4\pi$. Additionally, the loop-induced decay $h \to \gamma\gamma$ is sensitive to λ_3 and λ_7 through the charged Higgs contribution to this process. Celis, Ilisie and Pich 2013
- We take into account the latest measurements of the Higgs signal strengths in the $h \to \gamma\gamma$ channel by ATLAS and CMS. ATLAS, CMS 2015

$t \to ch, cV$ decays

- In the limit cos $\tilde{\alpha} = 1$, the decay rate for $t \to ch$ does not depend on $C_R(M_W)$ and λ_7 . In particular, for cos $\tilde{\alpha} = 1$ we have $\lambda^h_{H^+H^-} = \lambda_3$.
- The measured Higgs signal strengths by ATLAS and CMS in the di-photon channel are then only sensitive to λ_3 and $M_{H^{\pm}}$.

• One can write the Higgs signal strength in the di-photon channel as

$$
\mu_{\gamma\gamma}^h = \frac{\sigma(pp \to h) \times Br(h \to 2\gamma)}{\sigma(pp \to h)_{\rm SM} \times Br(h \to 2\gamma)_{\rm SM}} \simeq \left(1 - 0.15 \, C_{H^\pm}^h\right)^2, \qquad (10)
$$

where $\mathcal{C}_{H^\pm}^h$ encodes the charged Higgs contribution to $h\to 2\gamma$ and is given by

$$
C_{H^{\pm}}^{h} = \frac{v^2}{2M_{H^{\pm}}^2} \lambda_{H^+H^-}^{h} \mathcal{A}(x_{H^{\pm}}).
$$
 (11)

Celis, Ilisie and Pich 2013

• Here

$$
\mathcal{A}(x) = -x - \frac{x^2}{4} f(x), \qquad f(x) = -4 \arcsin^2(1/\sqrt{x}), \qquad (12)
$$

with $x_{H^{\pm}} = 4M_{H^{\pm}}^2/M_h^2$.

- We require that the Higgs signal strength lies within the 2σ range of the experimental measurements.
- The latest results by ATLAS $\mu_{\gamma\gamma}^h = 1.17^{+0.28}_{-0.26}$, and by CMS $\mu_{\gamma\gamma}^h = 1.12 \pm 0.24$, are consistent with the SM. ATLAS, CMS 2015
- Performing a scan over $\{\varsigma_u, \varsigma_d, \lambda_3\}$, subject to the restrictions specified, while fixing the charged Higgs mass to benchmark values, we obtain the upper bounds on $Br(t \to ch)$ and $Br(t \to cV)$. Celis, Li, Lu, Pich and GA 2015
- In the window 90 GeV $< M_{H\pm} < 150$ GeV the alignment parameter ς_d is constrained to be small by the direct charged Higgs searches at the LHC via top decays, $|s_d| \leq 10$, implying a very strong suppression on the decay rates. Celis, Ilisie and Pich 2013
- For $M_{H\pm}$ < 90 GeV a weaker bound on $|\varsigma_d|$ is obtained by a combination of LHC and Tevatron limits, $|\varsigma_d| \lesssim 25$. Celis, Ilisie and Pich 2013
- For $M_{H^\pm} > 150$ GeV the largest decay rates for $t \to ch, cV$ are obtained for $|s_u| < 1$ and $|s_d| \approx 50$.
- The decay rate for $t \to ch$ can receive much larger enhancements, due to the intermediate charged Higgs contribution involving the cubic Higgs coupling $\lambda_{H^+H^-}^h$.
- The maximum values for $Br(t \to ch)$ are obtained when the cubic scalar coupling $\lambda^h_{H^+H^-}$ saturates either the $h\to 2\gamma$ limits or the perturbativity bound.

- Diagram 3 dominates the corresponding decay amplitude in this case.
- The contribution from this diagram to the decay amplitude is proportional to $\int \int \int H + H$ and $\int \int \int \int H + H$.
- While the product $\varsigma_u\varsigma_d$ is constrained to be small in magnitude by $\text{Br}(\bar{B}\to X_s\gamma)$, the term proportional to ς_d^2 becomes greatly enhanced for large $|\varsigma_d|$ values.
- Such large values of $|S_d|$ can be obtained outside the window 90 GeV $< M_{H^{\pm}} < 160$ GeV.
- The measurement of the Higgs signal strengths in the di-photon channel restrict the allowed size of the cubic Higgs coupling $\lambda_{H^+H^-}^h$ for a light charged Higgs.
- Taking into account the measurements of the 125 GeV Higgs properties, all constraints specified earlier, we find that the decay rate for $t \to ch, cV$ lie beyond the reach of the high luminosity LHC in 2HDMs without tree-level FCNCs.
- Under the constraints considered the largest decay rate is obtained for $M_{H\pm}$ being slightly below 90 GeV, $\mathrm{Br}(t\to ch)\lesssim 2\times 10^{-7}.$

$M_{H^{\pm}}$ [GeV]	$Br(t \to c\gamma)$	$Br(t \to cZ)$	$Br(t \rightarrow ch)$
100	$\lesssim 2\times10^{-12}$	\lesssim 2 \times 10 ⁻¹³	$\lesssim 6 \times 10^{-9}$
200	$\lesssim 10^{-10}$	\lesssim 3 \times 10 $^{-11}$	$\lesssim 3\times 10^{-8}$
300	$\lesssim 10^{-11}$	$\lesssim 5\times 10^{-12}$	$\lesssim 2\times 10^{-8}$
400	$\lesssim 2\times 10^{-12}$	$\lesssim 2\times 10^{-12}$	$\lesssim 5\times 10^{-9}$
500	$\lesssim 10^{-12}$	$\lesssim 10^{-12}$	$\lesssim 2\times10^{-9}$
Exp. limit	$< 1.8 \times 10^{-3}$ CMS, 2014	$<$ 5 \times 10 $^{-4}$ Chatrchyan et al 2013 \parallel	$< 5.6 \times 10^{-3}$ CMS, 2014

Table: Upper bounds for $Br(t \to ch, cV)$ in the CP-conserving A2HDM.

- If small deviations from the limit cos $\tilde{\alpha} = 1$ are considered, the LHC Higgs data gives rise to strong bounds on the magnitude of the alignment parameters.
- Since $|y_f^h| = |\cos \tilde{\alpha} + \varsigma_f \sin \tilde{\alpha}| (f = u, d, l)$ is constrained to be close to one, one obtains $|\varsigma_f| \lesssim \mathcal{O}(1)$ when $\cos \tilde{\alpha} < 1$. Celis, Ilisie and Pich 2013
- This implies in particular that $|\varsigma_d|$ should be small and large enhancements of $Br(t \rightarrow ch)$ are not possible.
- Allowing for CP violation would not led to any significant enhancement either, given the strong constraints on CP-violating couplings derived from electric dipole moment experiments.

Jung, Pich and Tuzón 2010

$t \rightarrow ch$ decay

The direct counter term contribution

- The direct counter-term contribution to $t \to ch$ decay is not present in 2HDMs with NFC.
- The flavour structure of the A2HDM counter-term implies a strong suppression of its effects, due to the explicit powers of quark masses and the unitarity of the quark mixing matrix.
- Neglecting the loop contribution (at $\mu = M_W$),

$$
Br(t \to ch)_{\text{tree}} \approx \frac{\alpha^2 \pi^2 |V_{cb}|^2 m_b^4}{2 \sin^4 \theta_W M_W^4} \frac{(1 - M_h^2/m_t^2)^2}{(1 - M_W^2/m_t^2)^2 (1 + 2M_W^2/m_t^2)} \sin^2 \tilde{\alpha} |E_d|^2
$$

$$
\approx 2 \times 10^{-11} \sin^2 \tilde{\alpha} |E_d|^2, \tag{13}
$$

where

$$
E_d = \frac{1}{4\pi^2} C_R(M_W) (1 + \varsigma_u \varsigma_d) (\varsigma_d - \varsigma_u).
$$
 (14)

- The size of E_d is constrained by the mixing between the neutral B_s^0 meson and its antiparticle, which receives also contributions from the three neutral scalars $\varphi_i^0 = \{h, H, A\}.$
- This process allows for $|E_d| \sim \mathcal{O}(1)$, even when the masses of the neutral scalars are of $\mathcal{O}(100 \text{ GeV})$, but this is far too small to generate any observable signal in $t \rightarrow ch$. Braeuninger, Ibarra and Simonett 2010

• The charged Higgs gives the following finite correction to the hH^+H^- vertex, at the one-loop level:

$$
(\lambda_{H^+H^-}^h)_{\text{eff}} = \lambda_{H^+H^-}^h \left[1 + \frac{v^2 (\lambda_{H^+H^-}^h)^2}{16\pi^2 M_{H^\pm}^2} \mathcal{Z}\left(\frac{M_h^2}{M_{H^\pm}^2}\right) \right] \equiv \lambda_{H^+H^-}^h (1 + \Delta) , \tag{15}
$$

where

$$
\mathcal{Z}(X) = \int_0^1 dy \int_0^{1-y} dz \, [(y+z)^2 + X(1-y-z-yz)]^{-1} \,. \tag{16}
$$

• We allow this correction to be at most 50% ($\Delta \leq 0.5$).

$t \rightarrow ch$ decay Impact of perturbative bound

Figure: Allowed region by measurements of the Higgs signal strengths in the di-photon channel (blue-meshed) together with the perturbativity limits $|\lambda_3| \leq 4\pi$ (light gray) or $\Delta \leq 0.5$ (dark gray). See text for details.

• In figure we show the region allowed at 2σ by the measurement of the Higgs signal strengths in the di-photon channel, together with the bounds extracted with the perturbativity limits $|\lambda_3| \leq 4\pi$ and $\Delta \leq 0.5$.

- The constraints from $h \to \gamma \gamma$ give rise to a large allowed region, centered around $\lambda_3 = 0$, whose width increases for higher values of $M_{H^{\pm}}$.
- In this area the $h \to \gamma\gamma$ decay amplitude is dominated by the W-boson and top-quark loop contributions, as in the SM; the charged Higgs contribution remains subdominant.
- For light charged Higgs masses a small disjoint allowed region appears with $\lambda_3 \geq 6$.
- The perturbativity limit $\Delta \leq 0.5$, being more stringent for light charged Higgs masses, excludes this small region.
- For a light charged Higgs the maximum values of $Br(t \to ch)$ are obtained precisely in this separate region, where the value for $|\lambda^h_{H^+H^-}|$ reaches its maximum allowed value.
- After concidering perturbative limit, we get the limit $\mathrm{Br}(t\to ch)\lesssim 6\times 10^{-8}.$

Summary

- We perform a complete one-loop computation of the two-body flavour-changing top decays $t \to ch$ and $t \to cV$ ($V = \gamma$, Z), within the aligned two-Higgs-doublet model.
- We evaluate the impact of the model parameters on the associated branching ratios, taking into account constraints from flavour data and measurements of the Higgs properties.
- Assuming that the 125 GeV Higgs corresponds to the lightest CP-even scalar of the CP-conserving aligned two-Higgs-doublet model, we find that the rates for such flavour-changing top decays lie below the expected sensitivity of the future high-luminosity phase of the LHC.
- Measurements of the Higgs signal strength in the di-photon channel are found to play an important role in limiting the size of the $t \rightarrow ch$ decay rate when the charged scalar of the model is light.