Flavour changing top decays in the aligned two-Higgs-doublet model

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- $t \rightarrow ch$ in the aligned two-Higgs-doublet model (A2HDM).
- $t \rightarrow cV(=\gamma, Z)$ in the aligned two-Higgs-doublet model (A2HDM).

- The 2HDM provides a minimal extension of the scalar sector with a second Higgs doublet, (φ₁, φ₂).
- A global SU(2) transformation in the scalar space (ϕ_1, ϕ_2) takes to the so-called Higgs basis (Φ_1, Φ_2)

$$\begin{pmatrix} \Phi_1 \\ -\Phi_2 \end{pmatrix} \equiv \frac{1}{\nu} \begin{bmatrix} \nu_1 & \nu_2 \\ \nu_2 & -\nu_1 \end{bmatrix} \begin{pmatrix} \phi_1 \\ e^{-i\theta}\phi_2 \end{pmatrix} .$$
 (1)

In this basis,

$$\Phi_1 = \begin{bmatrix} G^+ \\ \frac{1}{\sqrt{2}} \left(\mathbf{v} + S_1 + iG^0 \right) \end{bmatrix}, \qquad \Phi_2 = \begin{bmatrix} H^+ \\ \frac{1}{\sqrt{2}} \left(S_2 + iS_3 \right) \end{bmatrix}, \qquad (2)$$

where G^{\pm} , G^0 are the Goldstone fields and $\langle H^+ \rangle = \langle G^+ \rangle = \langle G^0 \rangle = \langle S_i \rangle = 0$.

- The five physical scalars are two charged fields $H^{\pm}(x)$ and three neutral ones $\varphi_i^0(x) = \{h(x), H(x), A(x)\}.$
- The neutral scalars are related to the S_i fields through an orthogonal transformation φ⁰_i(x) = R_{ij}S_j(x).
- The form of \mathcal{R}_{ij} depends on the scalar potential.

• In the CP-conserving limit

$$\left(\begin{array}{c}h\\H\end{array}\right) = \left[\begin{array}{c}\cos\tilde{\alpha} & \sin\tilde{\alpha}\\-\sin\tilde{\alpha} & \cos\tilde{\alpha}\end{array}\right] \left(\begin{array}{c}S_1\\S_2\end{array}\right).$$
(3)

- The CP-odd field A corresponds to S_3 .
- In the generic 2HDM, however, tree-level FCNC interactions generally exist, through non-diagonal couplings of neutral scalars to fermions.

• In the Higgs basis

$$\mathcal{L}_{Y} = -\frac{\sqrt{2}}{v} \left[\bar{Q}'_{L} (M'_{d} \Phi_{1} + Y'_{d} \Phi_{2}) d'_{R} + \bar{Q}'_{L} (M'_{u} \tilde{\Phi}_{1} + Y'_{u} \tilde{\Phi}_{2}) u'_{R} + \bar{L}'_{L} (M'_{\ell} \Phi_{1} + Y'_{\ell} \Phi_{2}) \ell'_{R} \right] + \text{h.c.} ,$$

$$(4)$$
where $\tilde{\Phi}_{i}(x) = i\tau_{2} \Phi^{*}_{i}(x)$ are the charge-conjugated scalar doublets.

 In general, the Yukawa matrices M'_f and Y'_f cannot be simultaneously diagonalized in flavour space.

- An elegant solution is to use an appropriately chosen \mathcal{Z}_2 symmetries. Glashow and S. Weinberg 1977
- This guarantees the absence of FCNCs in the Yukawa sector.

 Flavour conservation in the neutral scalar couplings can be enforced in a rather trivial way requiring the Yukawa coupling matrices to be aligned in flavour space.

Pich and Tuzón 2009

• In the A2HDM, the interactions of scalar fields with fermions are described by

$$Y_{d,\ell} = \varsigma_{d,\ell} M_{d,\ell}, \qquad Y_u = \varsigma_u^* M_u.$$
(5)

• In the A2HDM the mass-eigenstate Yukawa Lagrangian reads

$$\mathcal{L}_{Y} = -\frac{\sqrt{2}}{v} H^{+}(x) \left\{ \bar{u}(x) \left[\varsigma_{d} V M_{d} \mathcal{P}_{R} - \varsigma_{u} M_{u}^{\dagger} V \mathcal{P}_{L} \right] d(x) + \varsigma_{l} \bar{\nu}(x) M_{l} \mathcal{P}_{R} l(x) \right\} - \frac{1}{v} \sum_{\varphi, f} y_{f}^{\varphi_{i}^{0}} \varphi_{i}^{0}(x) \bar{f}(x) M_{f} \mathcal{P}_{R} f(x) + \text{h.c.}, \qquad (6)$$

where V denotes the CKM matrix.

• The couplings of the neutral scalar fields are given by:

$$y_{d,l}^{\varphi_i^0} = \mathcal{R}_{i1} + (\mathcal{R}_{i2} + i\,\mathcal{R}_{i3})\,\varsigma_{d,l}\,, \qquad \qquad y_u^{\varphi_i^0} = \mathcal{R}_{i1} + (\mathcal{R}_{i2} - i\,\mathcal{R}_{i3})\,\varsigma_u^*\,.$$
(7)

- Quantum corrections induce some misalignment of the Yukawa coupling matrices, generating small FCNC effects suppressed by the corresponding loop factors.
- However, the special structure of the A2HDM strongly constrains the possible FCNC interactions.
 Pich and Tuzón 2009

• The one-loop gauge corrections preserve the alignment while the only FCNC structures induced by the scalar contributions take the form

$$\mathcal{L}_{\text{FCNC}} = \frac{C(\mu)}{4\pi^2 v^3} \left(1 + \varsigma_u^* \varsigma_d\right) \times \\ \times \sum_i \varphi_i^0(x) \left\{ \left(\mathcal{R}_{i2} + i \,\mathcal{R}_{i3}\right) \left(\varsigma_d - \varsigma_u\right) \left[\bar{d}_L \,V^{\dagger} M_u M_u^{\dagger} \,V M_d \,d_R\right] - \\ - \left(\mathcal{R}_{i2} - i \,\mathcal{R}_{i3}\right) \left(\varsigma_d^* - \varsigma_u^*\right) \left[\bar{u}_L \,V M_d \,M_d^{\dagger} \,V^{\dagger} M_u \,u_R\right] \right\}$$

+ h.c.

Jung, Pich and Tuzón 2010

 $\bullet\,$ The renormalization of the coupling constant ${\cal C}$ is determined, using dimensional regularization, to be

$$C = C_R(\mu) + \frac{1}{2} \left\{ \frac{2\mu^{D-4}}{D-4} + \gamma_E - \ln(4\pi) \right\} , \qquad (8)$$

Li, Lu and Pich 2014

• The renormalized coupling satisfies

$$C_R(\mu) = C_R(\mu_0) - \ln(\mu/\mu_0).$$
 (9)

• Assuming Yukawa alignment to be exact at a given energy scale Λ_A , so that $C_R(\Lambda_A) = 0$, implies that $C_R(\mu) = \ln(\Lambda_A/\mu)$.

Model	Sd	ςu	51
Type I	$\cot \beta$	$\cot \beta$	$\cot \beta$
Type II	- aneta	$\cot \beta$	- aneta
Type X	$\cot \beta$	$\cot \beta$	$-\tan\beta$
Type Y	- aneta	$\cot \beta$	$\cot \beta$

Table: Two-Higgs-doublet models with natural flavour conservation.

- The flavour-changing top decays $t \rightarrow ch, cV$ occur at the one-loop level in the SM.
- The decay rates is suppressed by the loop factor and also receives a strong CKM and GIM suppression.
 Eilam, Hewett and Soni 1991, Mele, Petrarca and Soddu 1998, Aguilar-Saavedr 2004
- Fixing the Higgs mass at $M_h \simeq 125$ GeV, one obtains the SM branching ratios: Br $(t \to ch) \sim \mathcal{O}(10^{-15})$, Br $(t \to c\gamma) \sim \mathcal{O}(10^{-14})$ and Br $(t \to cZ) \sim \mathcal{O}(10^{-14})$.
- Within the A2HDM these decay rates can be enhanced due to additional charged Higgs contributions at the loop level. Celis, Li, Lu, Pich and GA 2015

- The ATLAS and CMS collaborations have searched for flavour-changing decays of the top quark.
- The ATLAS has set the bound ${
 m Br}(t o qZ) < 0.73\%$ at the 95% confidence leve. Aad et al 2012
- The CMS has set a better limit, ${\rm Br}(t o qZ) < 0.05\%$. Chatrchyan et al 2013

- The strongest current bound on $t\to c\gamma$ decay by the CMS is ${\rm Br}(t\to c\gamma)<$ 0.182%. CMS 2014
- The ATLAS collaboration sets the limit ${\rm Br}(t o qh) < 0.79\%$. Aad et al 2014
- A slightly stronger limit, ${\rm Br}(t\to qh)<$ 0.56%, has been obtained by the CMS collaboration. CMS 2014
- One expects to improve the limits to $10^{-4} 10^{-5}$ level for $Br(t \to ch)$.



Figure: Penguin diagrams contributing to $t \to c\varphi_i^0$ in the Feynman gauge.



Figure: Penguin diagrams contributing to $t \to c\varphi_j^0$ in the Feynman gauge.



Figure: Penguin diagrams contributing to $t \to c\varphi_j^0$ in the Feynman gauge.

- The CP-conserving A2HDM contains 12 free real parameters: μ₂, λ_k (k = 1,...,7), the three alignment constants ς_f (f = u, d, l) and the counter-term coupling C_R(μ).
- Some of the parameters of the scalar potential can be traded by the physical scalar masses and the mixing angle $\tilde{\alpha}$.
- The decays $t \to c \varphi_j^0, cZ$ are only sensitive to $\{M_{\varphi_j^0}, M_{H^{\pm}}, \cos \tilde{\alpha}, \lambda_3, \lambda_7, \varsigma_u, \varsigma_d, C_R(M_W)\}$.
- We assume that the 125 GeV Higgs boson corresponds to the lightest CP-even state h; i.e., we fix $M_h\simeq 125$ GeV.
- The LHC data imply that it couples to the massive gauge vector bosons with a SM-like strength so that $\cos \tilde{\alpha} \simeq 1$.

We analyze the parameter space of the A2HDM, subject to the following assumptions and constraints:

- The LHC and Tevatron Higgs data imply that $\cos \tilde{\alpha} > 0.9$ (68% CL) and $|y_f^h| \sim 1$ (f = u, d, l).
- We work in the limit $\cos \tilde{\alpha} = 1$ so that no constraints on the alignment parameters are obtained from the 125 GeV Higgs data. Celis, Ilisie and Pich 2013
- We take into account constraints in the $\varsigma_u \varsigma_d$ plane derived from the measurement of $\operatorname{Br}(\bar{B} \to X_s \gamma)$. Jung, Pich and Tuzón 2010, Jung, Li and Pich 2012

- We restrict the alignment parameter $|\varsigma_u| \leq 2$, in order to satisfy the constraints from $Z \to \bar{b}b$ decay and $B^0_{s,d} \bar{B}^0_{s,d}$ mixings.
- The parameters $\varsigma_{d,l}$ are much less constrained phenomenologically; we take $|\varsigma_{d,\ell}| \leq 50$. Jung, Pich and Tuzón 2010, Jung, Li and Pich 2012
- The LEP has searched for pair-produced charged Higgs bosons in the framework of 2HDMs, excluding $M_{H^{\pm}} \lesssim 80$ GeV (95% CL) under the assumption that H^{\pm} decays dominantly into fermions. G. Abbiendi et al. 2013

- Searches for a light charged Higgs via the decay $t \rightarrow H^+ b$ performed by the ATLAS and CMS collaborations, together with the limits on a charged Higgs from the Tevatron are taken into account. Aad et. al 2013, 2014, CMS 2014, Gutierrez et. al 2010
- These direct searches give an upper bound on the Yukawa combination $|\varsigma_{u}\varsigma_{d}|$, which, although being weaker than the one from $\operatorname{Br}(\bar{B} \to X_{s}\gamma)$, basically exclude one of the two possible strips allowed by the latter. Celis, Ilisie and Pich 2013

- We consider the perturbativity bound on the quartic scalar couplings $|\lambda_{3,7}| \leq 4\pi$. Additionally, the loop-induced decay $h \rightarrow \gamma \gamma$ is sensitive to λ_3 and λ_7 through the charged Higgs contribution to this process. Celis, Ilisie and Pich 2013
- We take into account the latest measurements of the Higgs signal strengths in the $h \rightarrow \gamma \gamma$ channel by ATLAS and CMS. ATLAS, CMS 2015

- In the limit cos α̃ = 1, the decay rate for t → ch does not depend on C_R(M_W) and λ₇. In particular, for cos α̃ = 1 we have λ^h_{H+H−} = λ₃.
- The measured Higgs signal strengths by ATLAS and CMS in the di-photon channel are then only sensitive to λ_3 and M_{H^\pm} .

• One can write the Higgs signal strength in the di-photon channel as

$$\mu_{\gamma\gamma}^{h} = \frac{\sigma(pp \to h) \times \operatorname{Br}(h \to 2\gamma)}{\sigma(pp \to h)_{\text{SM}} \times \operatorname{Br}(h \to 2\gamma)_{\text{SM}}} \simeq \left(1 - 0.15 C_{H^{\pm}}^{h}\right)^{2}, \quad (10)$$

where $C^h_{H^\pm}$ encodes the charged Higgs contribution to $h o 2\gamma$ and is given by

$$C_{H^{\pm}}^{h} = \frac{v^{2}}{2M_{H^{\pm}}^{2}} \lambda_{H^{+}H^{-}}^{h} \mathcal{A}(x_{H^{\pm}}).$$
(11)

Celis, Ilisie and Pich 2013

• Here

$$\mathcal{A}(x) = -x - \frac{x^2}{4} f(x), \qquad f(x) = -4 \arcsin^2(1/\sqrt{x}), \qquad (12)$$

with $x_{H^{\pm}} = 4M_{H^{\pm}}^2/M_h^2$.

- We require that the Higgs signal strength lies within the 2σ range of the experimental measurements.
- The latest results by ATLAS $\mu^h_{\gamma\gamma}=1.17^{+0.28}_{-0.26}$, and by CMS $\mu^h_{\gamma\gamma}=1.12\pm0.24$, are consistent with the SM. ATLAS, CMS 2015
- Performing a scan over {ς_u, ς_d, λ₃}, subject to the restrictions specified, while fixing the charged Higgs mass to benchmark values, we obtain the upper bounds on Br(t → ch) and Br(t → cV).
 Celis, Li, Lu, Pich and GA 2015

- In the window 90 GeV $< M_{H^\pm} <$ 150 GeV the alignment parameter ς_d is constrained to be small by the direct charged Higgs searches at the LHC via top decays, $|\varsigma_d| \lesssim$ 10, implying a very strong suppression on the decay rates. Celis, Ilisie and Pich 2013
- For $M_{H^{\pm}} < 90$ GeV a weaker bound on $|\varsigma_d|$ is obtained by a combination of LHC and Tevatron limits, $|\varsigma_d| \lesssim 25$. Celis, Ilisie and Pich 2013

- For $M_{H^{\pm}} > 150$ GeV the largest decay rates for $t \to ch, cV$ are obtained for $|\varsigma_u| < 1$ and $|\varsigma_d| \simeq 50$.
- The decay rate for $t \to ch$ can receive much larger enhancements, due to the intermediate charged Higgs contribution involving the cubic Higgs coupling $\lambda_{H^+H^-}^h$.
- The maximum values for ${\rm Br}(t\to ch)$ are obtained when the cubic scalar coupling $\lambda^h_{H^+H^-}$ saturates either the $h\to 2\gamma$ limits or the perturbativity bound.



- Diagram 3 dominates the corresponding decay amplitude in this case.
- The contribution from this diagram to the decay amplitude is proportional to $\varsigma_{u}\varsigma_{d}\lambda^{h}_{H+H-}$ and $\varsigma^{2}_{d}\lambda^{h}_{H+H-}$.
- While the product $\varsigma_u\varsigma_d$ is constrained to be small in magnitude by $\operatorname{Br}(\bar{B} \to X_s \gamma)$, the term proportional to ς_d^2 becomes greatly enhanced for large $|\varsigma_d|$ values.
- Such large values of $|\varsigma_d|$ can be obtained outside the window 90 GeV $< M_{H^\pm} < 160$ GeV.

- The measurement of the Higgs signal strengths in the di-photon channel restrict the allowed size of the cubic Higgs coupling $\lambda_{H^+H^-}^h$ for a light charged Higgs.
- Taking into account the measurements of the 125 GeV Higgs properties, all constraints specified earlier, we find that the decay rate for $t \rightarrow ch, cV$ lie beyond the reach of the high luminosity LHC in 2HDMs without tree-level FCNCs.
- Under the constraints considered the largest decay rate is obtained for $M_{H^{\pm}}$ being slightly below 90 GeV, $\operatorname{Br}(t \to ch) \lesssim 2 \times 10^{-7}$.

$M_{H\pm}$ [GeV]	${ m Br}(t ightarrow c \gamma)$	$Br(t \rightarrow cZ)$	$Br(t \rightarrow ch)$
100	$\leq 2 \times 10^{-12}$	$\lesssim 2 \times 10^{-13}$	$\lesssim 6 \times 10^{-9}$
200	$\lesssim 10^{-10}$	$\lesssim 3 imes 10^{-11}$	$\lesssim 3 imes 10^{-8}$
300	$\lesssim 10^{-11}$	$\lesssim 5 imes 10^{-12}$	$\lesssim 2 imes 10^{-8}$
400	$\lesssim 2 \times 10^{-12}$	$\lesssim 2 \times 10^{-12}$	$\lesssim 5 imes 10^{-9}$
500	$\lesssim 10^{-12}$	$\lesssim 10^{-12}$	$\lesssim 2 imes 10^{-9}$
Exp. limit	$< 1.8 imes 10^{-3}$ CMS, 2014	$< 5 imes 10^{-4}$ Chatrchyan et al 2013	$< 5.6 imes 10^{-3}$ CMS, 2014

Table: Upper bounds for $Br(t \rightarrow ch, cV)$ in the CP-conserving A2HDM.

 $t \rightarrow ch, cV$ decays

Rbustness of the predictions

- If small deviations from the limit $\cos \tilde{\alpha} = 1$ are considered, the LHC Higgs data gives rise to strong bounds on the magnitude of the alignment parameters.
- Since |y_f^h| = | cos α̃ + ς_f sin α̃| (f = u, d, l) is constrained to be close to one, one obtains |ς_f| ≲ O(1) when cos α̃ < 1.
 Celis, Ilisie and Pich 2013
- This implies in particular that $|\varsigma_d|$ should be small and large enhancements of ${
 m Br}(t o ch)$ are not possible.
- Allowing for CP violation would not led to any significant enhancement either, given the strong constraints on CP-violating couplings derived from electric dipole moment experiments.

Jung, Pich and Tuzón 2010

t ightarrow ch decay

The direct counter term contribution

- The direct counter-term contribution to $t \rightarrow ch$ decay is not present in 2HDMs with NFC.
- The flavour structure of the A2HDM counter-term implies a strong suppression of its effects, due to the explicit powers of quark masses and the unitarity of the quark mixing matrix.
- Neglecting the loop contribution (at $\mu = M_W$),

$$Br(t \to ch)_{tree} \approx \frac{\alpha^2 \pi^2 |V_{cb}|^2 m_b^4}{2 \sin^4 \theta_W M_W^4} \frac{(1 - M_h^2/m_t^2)^2}{(1 - M_W^2/m_t^2)^2 (1 + 2M_W^2/m_t^2)} \sin^2 \tilde{\alpha} |E_d|^2$$

$$\approx 2 \times 10^{-11} \sin^2 \tilde{\alpha} |E_d|^2, \qquad (13)$$

where

$$E_d = \frac{1}{4\pi^2} C_R(M_W) \left(1 + \varsigma_u \varsigma_d\right) \left(\varsigma_d - \varsigma_u\right) \,. \tag{14}$$

- The size of E_d is constrained by the mixing between the neutral B⁰_s meson and its antiparticle, which receives also contributions from the three neutral scalars φ⁰_i = {h, H, A}.
- This process allows for |E_d| ~ O(1), even when the masses of the neutral scalars are of O(100 GeV), but this is far too small to generate any observable signal in t → ch.
 Braeuninger, Ibarra and Simonett 2010

t ightarrow ch decay Impact of perturbative bound

• The charged Higgs gives the following finite correction to the hH^+H^- vertex, at the one-loop level:

$$(\lambda_{H^+H^-}^h)_{\text{eff}} = \lambda_{H^+H^-}^h \left[1 + \frac{v^2 (\lambda_{H^+H^-}^h)^2}{16\pi^2 M_{H^\pm}^2} \, \mathcal{Z}\left(\frac{M_h^2}{M_{H^\pm}^2}\right) \right] \equiv \lambda_{H^+H^-}^h \, (1+\Delta) \,,$$
(15)

where

$$\mathcal{Z}(X) = \int_0^1 dy \, \int_0^{1-y} dz \, \left[(y+z)^2 + X \left(1 - y - z - yz \right) \right]^{-1} \, . \tag{16}$$

• We allow this correction to be at most 50% ($\Delta \leqslant 0.5$).

t ightarrow ch decay Impact of perturbative bound



Figure: Allowed region by measurements of the Higgs signal strengths in the di-photon channel (blue-meshed) together with the perturbativity limits $|\lambda_3| \leq 4\pi$ (light gray) or $\Delta \leq 0.5$ (dark gray). See text for details.

• In figure we show the region allowed at 2σ by the measurement of the Higgs signal strengths in the di-photon channel, together with the bounds extracted with the perturbativity limits $|\lambda_3| \leq 4\pi$ and $\Delta \leq 0.5$.



- The constraints from $h \rightarrow \gamma \gamma$ give rise to a large allowed region, centered around $\lambda_3 = 0$, whose width increases for higher values of $M_{H^{\pm}}$.
- In this area the $h \rightarrow \gamma \gamma$ decay amplitude is dominated by the W-boson and top-quark loop contributions, as in the SM; the charged Higgs contribution remains subdominant.
- + For light charged Higgs masses a small disjoint allowed region appears with $\lambda_3\gtrsim 6.$
- The perturbativity limit $\Delta\leqslant$ 0.5, being more stringent for light charged Higgs masses, excludes this small region.
- For a light charged Higgs the maximum values of Br(t → ch) are obtained precisely in this separate region, where the value for |λ^h_{H+H−}| reaches its maximum allowed value.
- After concidering perturbative limit, we get the limit ${\rm Br}(t \to ch) \lesssim 6 \times 10^{-8}$.

- We perform a complete one-loop computation of the two-body flavour-changing top decays t → ch and t → cV (V = γ, Z), within the aligned two-Higgs-doublet model.
- We evaluate the impact of the model parameters on the associated branching ratios, taking into account constraints from flavour data and measurements of the Higgs properties.
- Assuming that the 125 GeV Higgs corresponds to the lightest CP-even scalar of the CP-conserving aligned two-Higgs-doublet model, we find that the rates for such flavour-changing top decays lie below the expected sensitivity of the future high-luminosity phase of the LHC.
- Measurements of the Higgs signal strength in the di-photon channel are found to play an important role in limiting the size of the $t \rightarrow ch$ decay rate when the charged scalar of the model is light.