

# Neutrino oscillation experiments: Future Prospects

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# Neutrino Oscillations

- Standard three-flavour oscillation framework:

$$U = U_{23} \times U_{13,\delta} \times U_{12}$$

$$= \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & \sin \theta_{23} \\ 0 & -\sin \theta_{23} & \cos \theta_{23} \end{pmatrix} \begin{pmatrix} \cos \theta_{13} & 0 & e^{i\delta} \sin \theta_{13} \\ 0 & 1 & 0 \\ -e^{i\delta} \sin \theta_{13} & 0 & \cos \theta_{13} \end{pmatrix} \begin{pmatrix} \cos \theta_{12} & \sin \theta_{12} & 0 \\ -\sin \theta_{12} & \cos \theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

**Atmospheric + LBL**

**Reactor + LBL**

**Solar + reactor**

$$\Delta m^2_{31}$$

$$\Delta m^2_{21}$$

- Three mixing angles, two independent mass-squared differences, one CP-violating phase

# Known measurements

	Normal Ordering ( $\Delta\chi^2 = 0.97$ )		Inverted Ordering (best fit)		Any Ordering
	bf $\mu$ $\pm 1\sigma$	$3\sigma$ range	bf $\mu$ $\pm 1\sigma$	$3\sigma$ range	$3\sigma$ range
$\sin^2 \theta_{12}$	$0.304^{+0.013}_{-0.012}$	0.270 $\rightarrow$ 0.344	$0.304^{+0.013}_{-0.012}$	0.270 $\rightarrow$ 0.344	0.270 $\rightarrow$ 0.344
$\theta_{12}/^\circ$	$33.48^{+0.78}_{-0.75}$	31.29 $\rightarrow$ 35.91	$33.48^{+0.78}_{-0.75}$	31.29 $\rightarrow$ 35.91	31.29 $\rightarrow$ 35.91
$\sin^2 \theta_{23}$	$0.452^{+0.052}_{-0.028}$	0.382 $\rightarrow$ 0.643	$0.579^{+0.025}_{-0.037}$	0.389 $\rightarrow$ 0.644	0.385 $\rightarrow$ 0.644
$\theta_{23}/^\circ$	$42.3^{+3.0}_{-1.6}$	38.2 $\rightarrow$ 53.3	$49.5^{+1.5}_{-2.2}$	38.6 $\rightarrow$ 53.3	38.3 $\rightarrow$ 53.3
$\sin^2 \theta_{13}$	$0.0218^{+0.0010}_{-0.0010}$	0.0186 $\rightarrow$ 0.0250	$0.0219^{+0.0011}_{-0.0010}$	0.0188 $\rightarrow$ 0.0251	0.0188 $\rightarrow$ 0.0251
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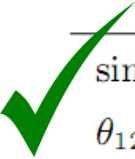
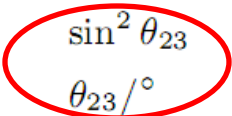
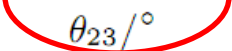
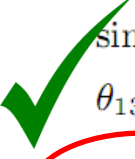
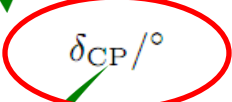

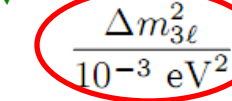
1409.5439: Gonzalez-Garcia, Maltoni, Schwetz

See also:

1405.7540: Forero, Tortola, Valle

1312.2878: Capozzi et al.

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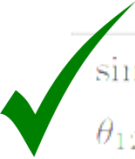
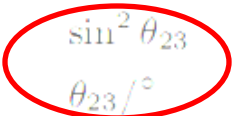

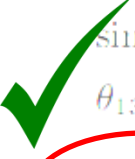
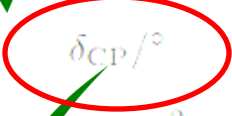
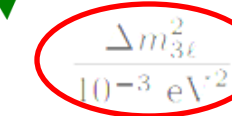
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LO or HO?

$\delta_{CP}=?$

NH or IH?

1409.5439: Gonzalez-Garcia, Maltoni, Schwetz

See also:

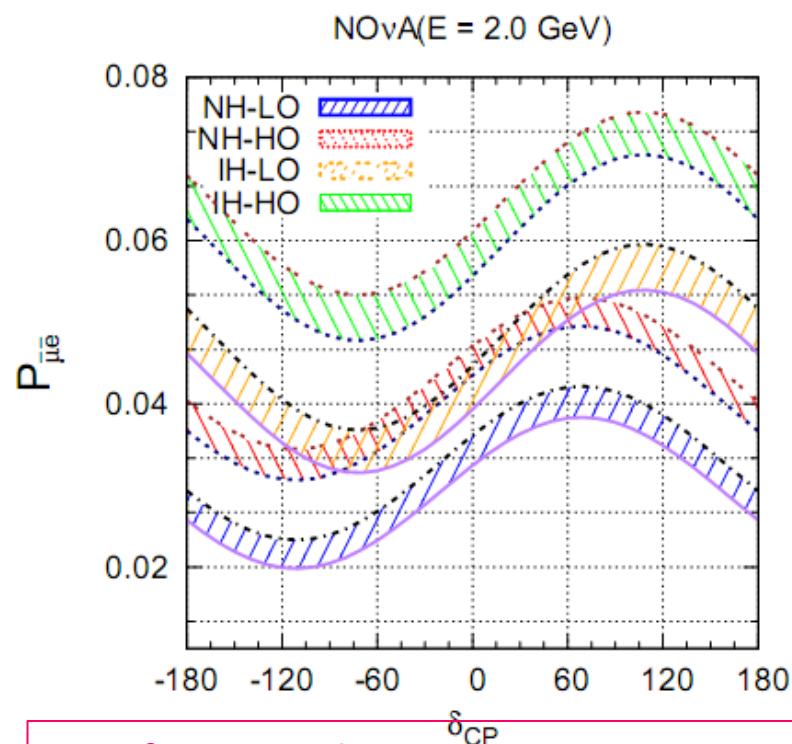
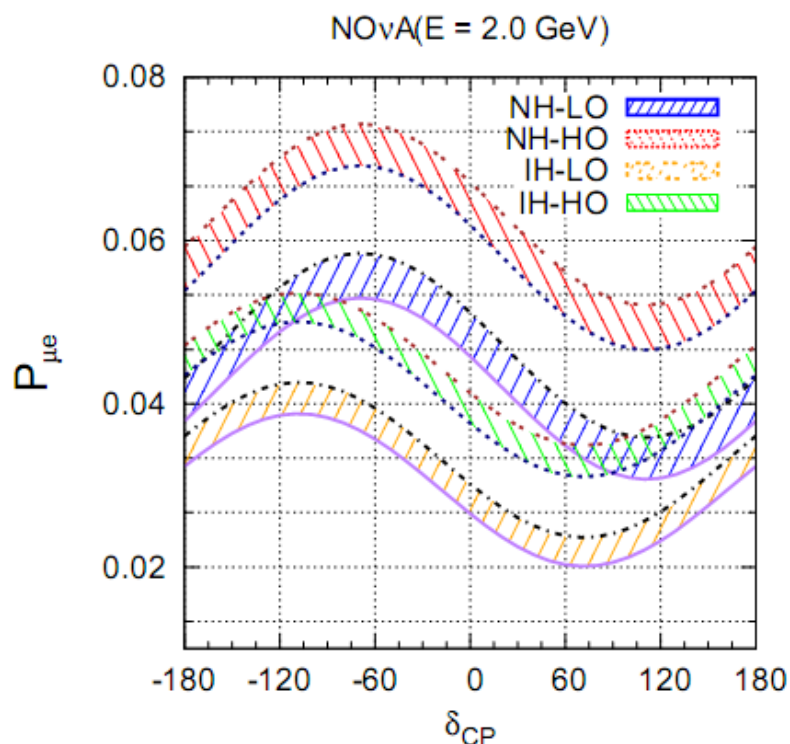
1405.7540: Forero, Tortola, Valle

1312.2878: Capozzi et al.

# Why do we not know what we don't know?

- Parameter degeneracies:

$$P(\text{NH}, \delta_{\text{CP}}) = P(\text{IH}, \delta_{\text{CP}}') \quad ; \quad P(\theta_{23}) = P(90-\theta_{23})$$



See, for example:

1504.06283: Ghosh, Ghoshal, Goswami, Nath, SR

1406.2551: Coloma, Minakata, Parke

# Parameter degeneracies

- Certain combinations of hierarchy and  $\delta_{CP}$  suffer from degeneracies

	NH	IH
Upper half-plane (UHP): $\delta_{CP} = (0, 180^\circ)$	Degeneracy (Unfavourable)	No degeneracy (Favourable)
Lower half-plane (LHP): $\delta_{CP} = (-180^\circ, 0)$	No degeneracy (Favourable)	Degeneracy (Unfavourable)

- For octant determination, the favourable and unfavourable combinations are different for neutrinos and antineutrinos

1301.2574: Agarwalla, Prakash, UmaSankar

# A chronology of experiments

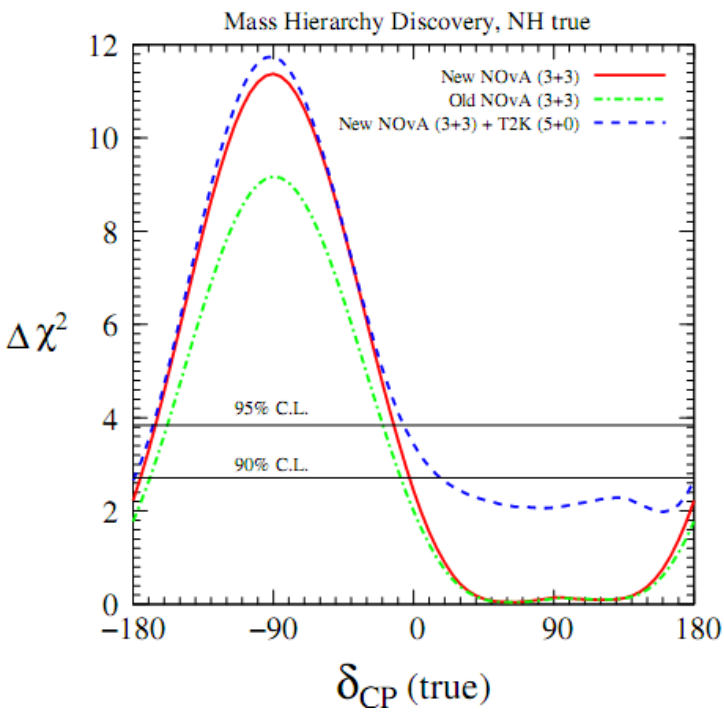
	Current expts	Upcoming (near future) expts	Future expts
<b>Beam-based</b>	T2K, NOvA, MINOS+		DUNE/LBNF/LBNE, T2HK, ESSnuSB
<b>Atmospheric</b>	SK, MINOS+	ICAL@INO	HK, PINGU
<b>Reactor</b>	D-Chooz, DayaBay, RENO	JUNO, RENO50	
<b>Extra-terrestrial</b>	Antares, IceCube		KM3NET

  
time

Far future:  
Neutrino factory?  
Beta-beam?



# Current experiments



## A1: Current expts: Hierarchy

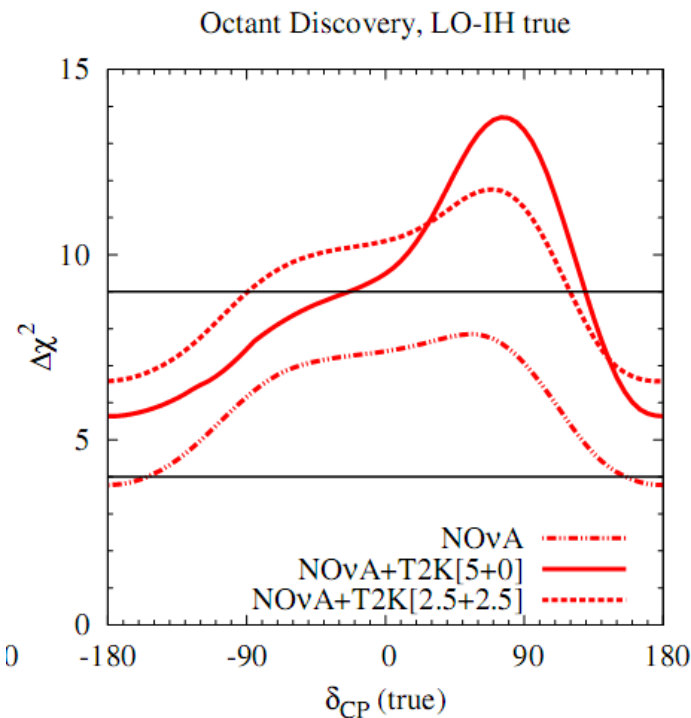
Hierarchy: For favourable combinations of parameters, NOvA and T2K can determine the hierarchy very well

1208.3644: Agarwalla, Prakash, SR, UmaSankar

## A2: Current expts: Octant

Octant: Depending on the true parameters, NOvA + T2K may determine the octant

1301.2574: Agarwalla, Prakash, UmaSankar



# Current experiments

## A3: Current expts: CP

$\delta_{CP}$ : Does the existing T2K data already give a hint for  $\delta_{CP} = -90^\circ$ ?

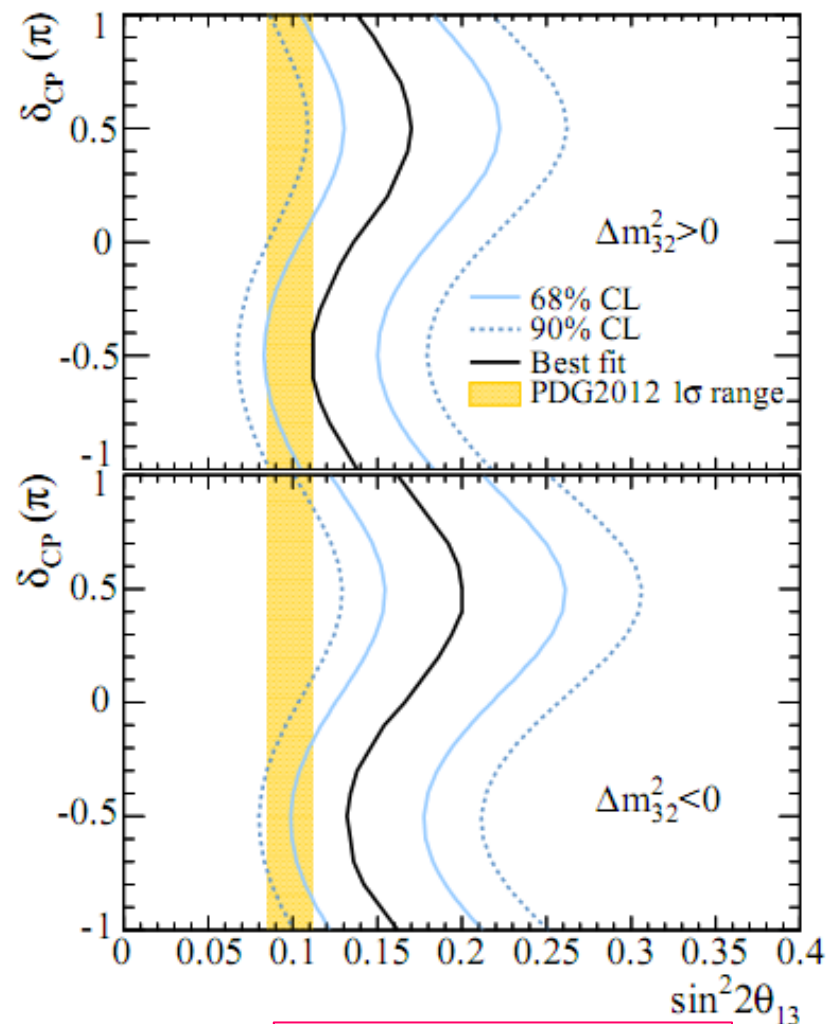
Can we use this hint to draw conclusions about the hierarchy and octant?

	NH	IH	Sum
$\sin^2 \theta_{23} \leq 0.5$	0.179	0.078	0.257
$\sin^2 \theta_{23} > 0.5$	0.505	0.238	0.743
Sum	0.684	0.316	1.0

1502.01550: Abe et al.

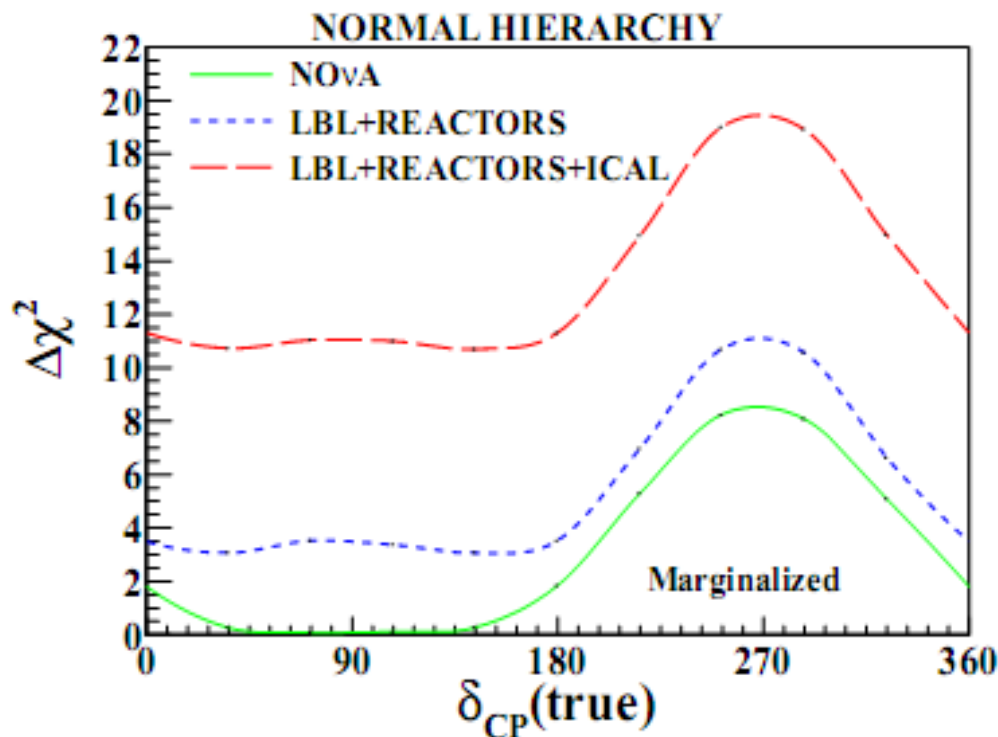
See also:

1409.5046: Ghosh, Goswami, SR



1311.4750: Abe et al.

# Upcoming experiments



## B1: Upcoming expts: Hierarchy

NOvA + T2K + reactors + ICAL can improve the hierarchy sensitivity even for unfavourable combinations of parameters

1212.1305: Choubey, Ghosh, Thakore

See also:

1203.3388: Blenow, Schwetz

Reactor experiments like JUNO are also sensitive to the hierarchy through spectral effects

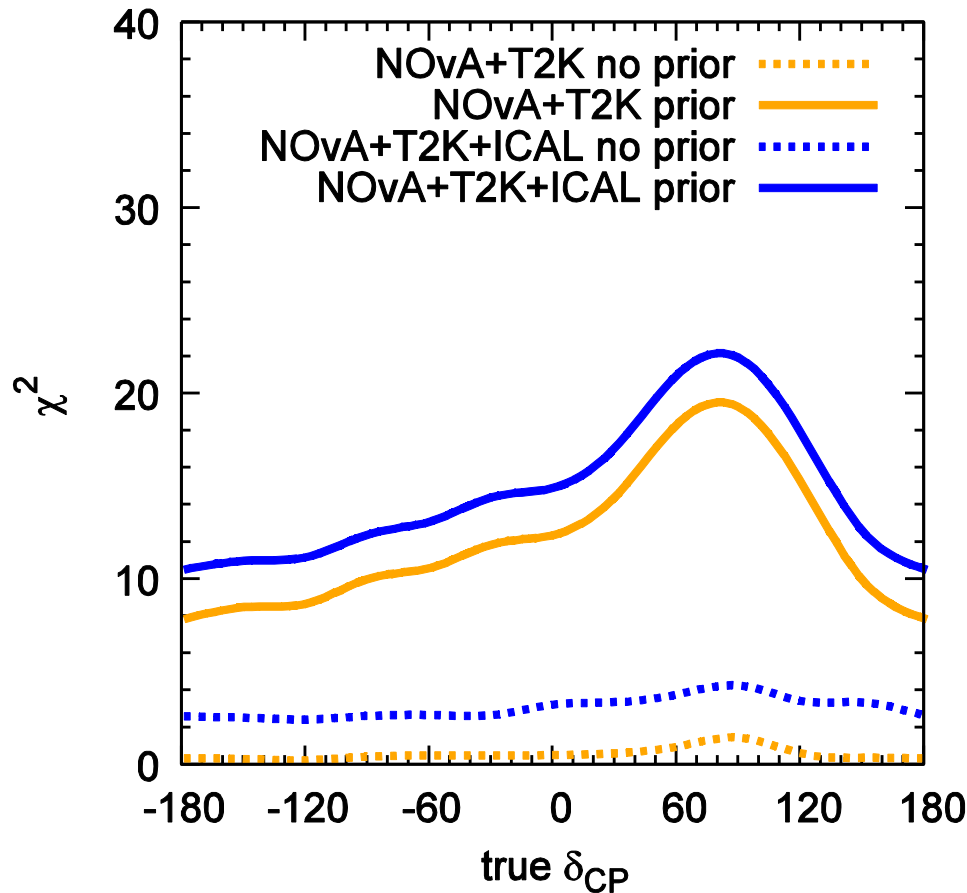
1303.6733: Li, Cao, Wang, Zhan

# Upcoming experiments

## B2: Upcoming expts: Octant

Adding information from reactors + ICAL can improve the octant sensitivity dramatically

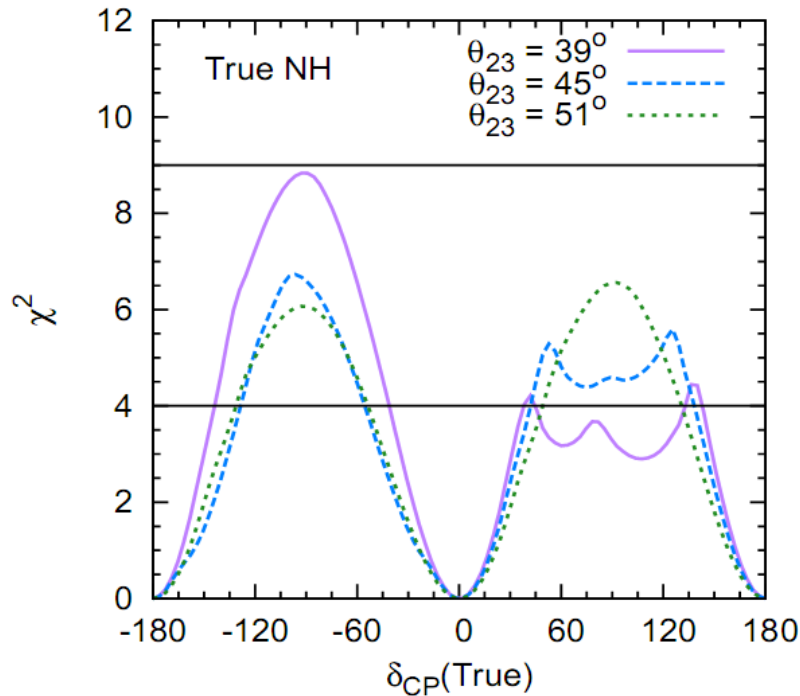
Note the role of the reactors (represented by priors on  $\theta_{13}$ ): synergy between long-baseline and reactor experiments



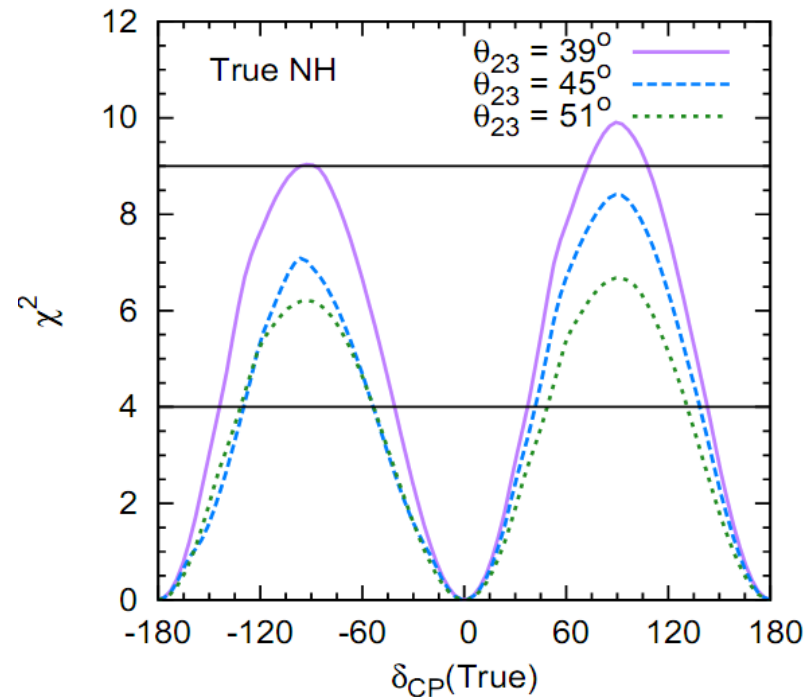
# Upcoming experiments

## B3: Upcoming expts: CP

T2K + NOvA



T2K + NOvA + ICAL

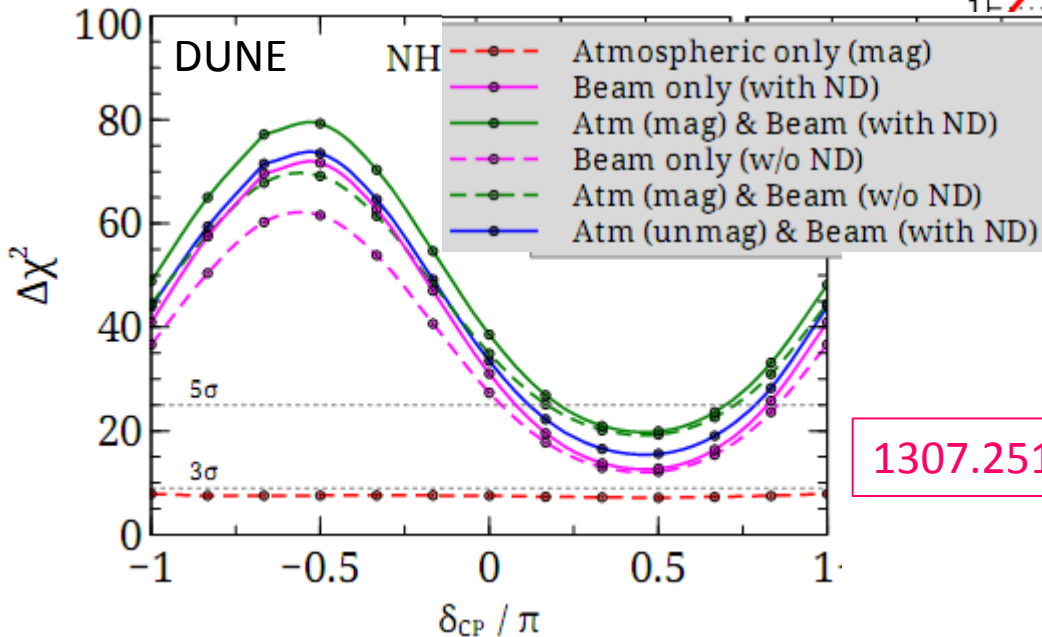
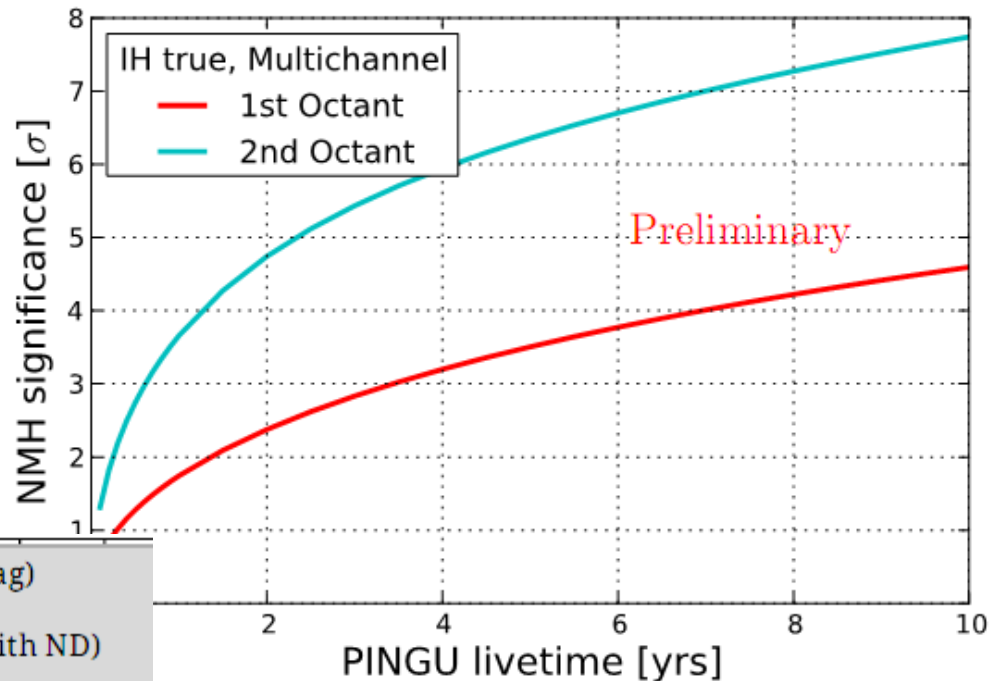


ICAL does not have any intrinsic CP sensitivity, but it is sensitive to the hierarchy. Thus, it helps the discovery of CP violation indirectly, by breaking the hierarchy-  $\delta_{CP}$  degeneracy. [1306.2500: Ghosh, Ghoshal, Goswami, SR](#)

# Future experiments

## C1: Future expts: Hierarchy

1401.2046: Aartsen et al.



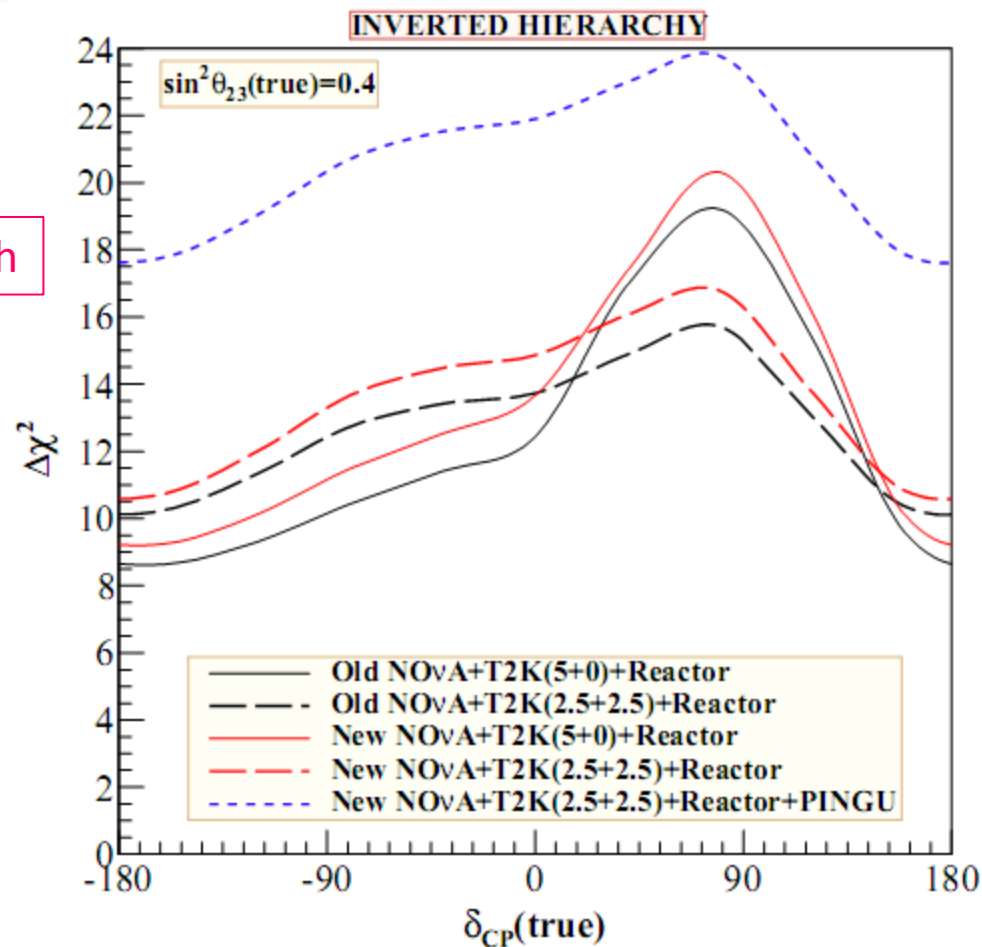
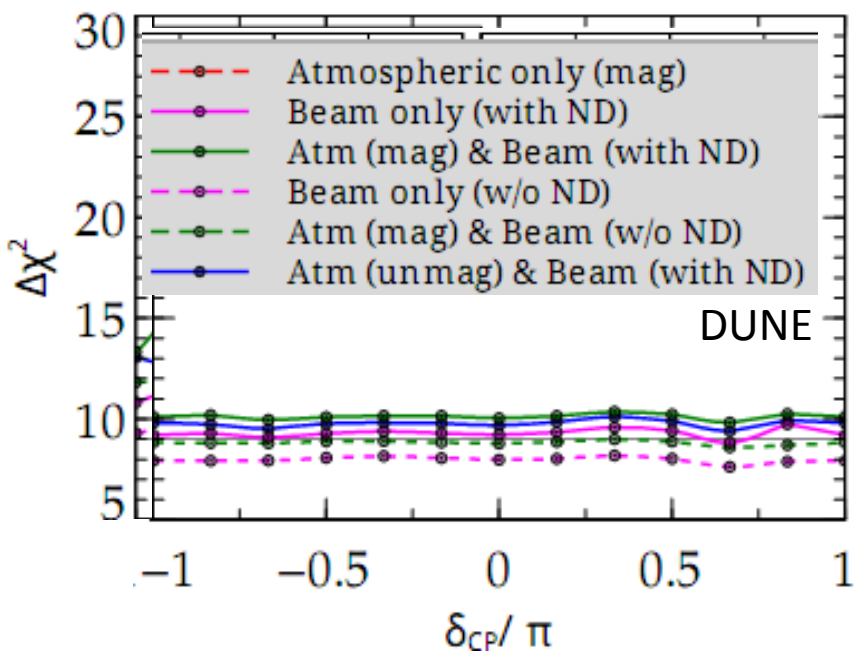
1307.2519: Barger et al.

# Future experiments

## C2: Future expts: Octant

1309.5760: Choubey, Ghosh

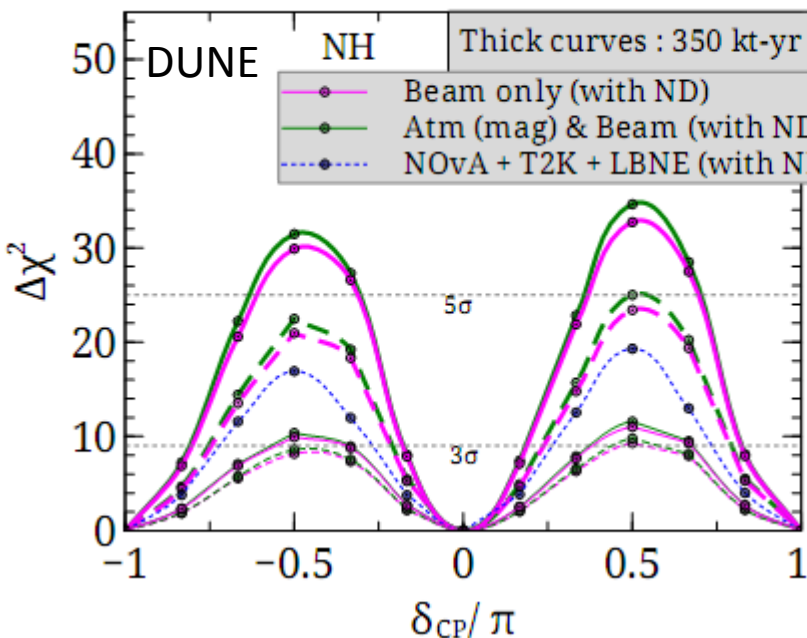
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**Caveat: Octant sensitivity depends on the value of  $\theta_{23}$  in nature**

# Future experiments

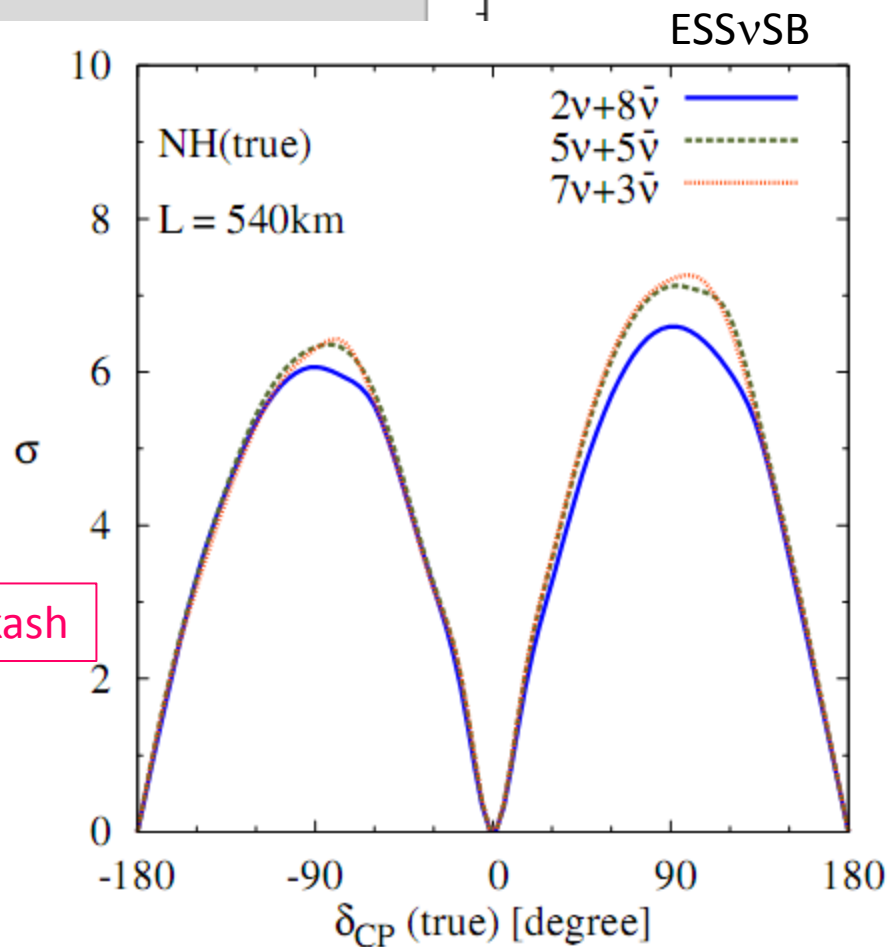
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1307.2519: Barger et al.

1406.2219: Agarwalla, Choubey, Prakash

Also: DAR experiments





# Summary

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- If the combinations are unfavourable, the upcoming experiments like ICAL will conclusively determine the hierarchy, and possibly the octant (depending on  $\theta_{23}$  )
- The discovery of CP violation and a precise measurement of the phase may have to wait until the next generation of experiments like DUNE and ESS $\nu$ SB.

# Some questions for the future

- Is the standard three-flavour oscillation scenario enough?  
Steriles? NSIs?
- How precise is precise? Look to models for answers?
- Are we motivated enough to invest in new and technologically challenging facilities like neutrino factories and beta beams?
- Statistics: Frequentist vs Bayesian. How should we interpret our chi-squared?
- What other physics can we do with neutrino oscillations?  
Supernovae, UHE physics, tomography?