

# Standard Model Theory for Collider Physics

Massimiliano Grazzini\*

University of Zurich



Universität  
Zürich<sup>UZH</sup>

EPS-HEP 2015  
Vienna, July 27 2015

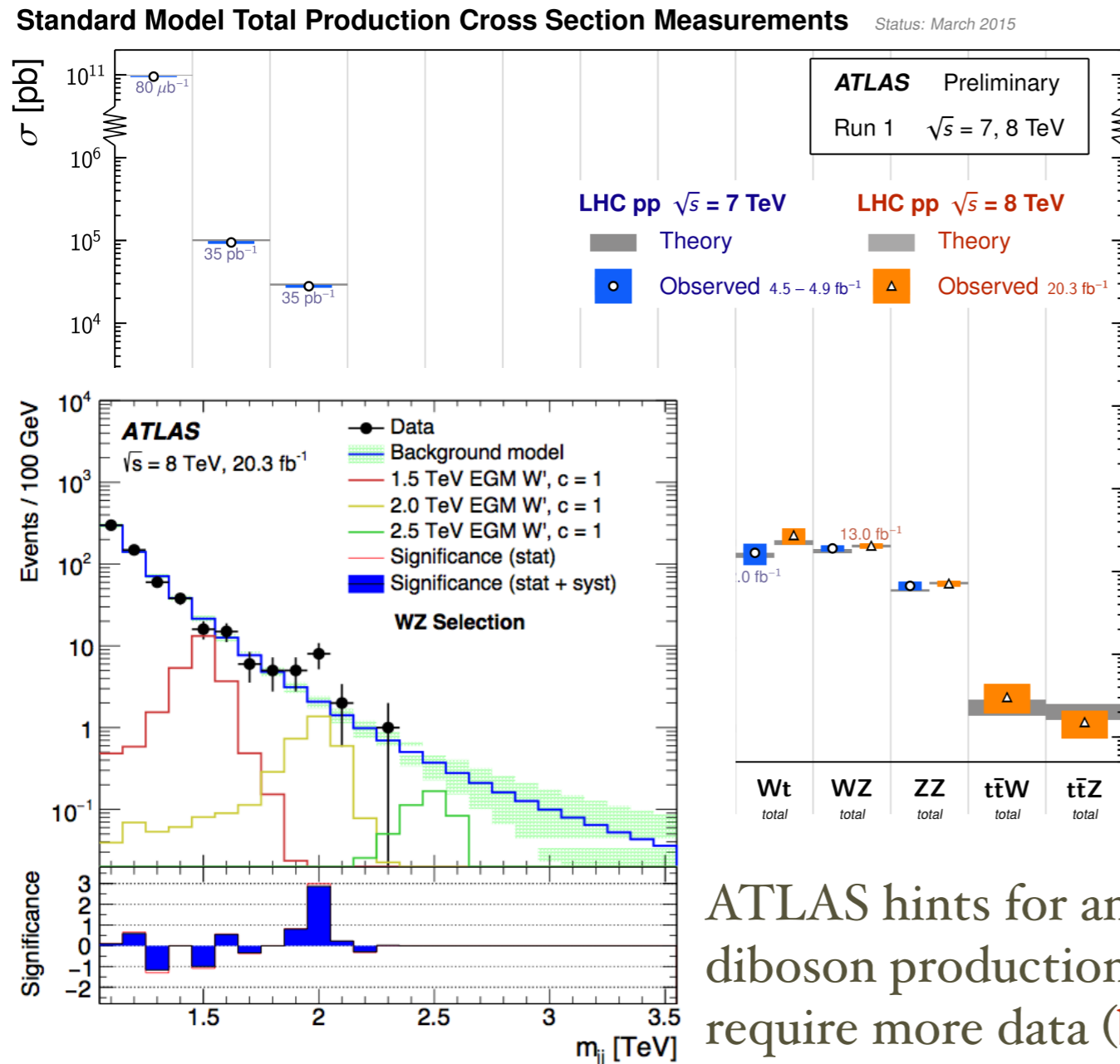


\*On leave of absence from INFN, Sezione di Firenze

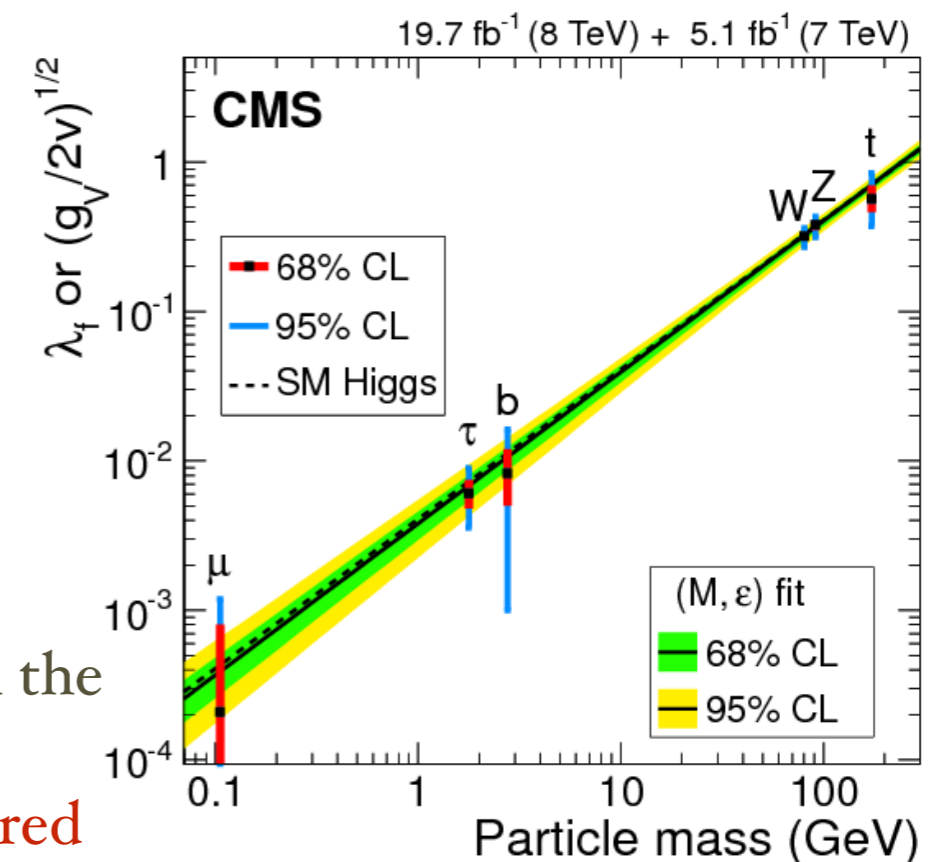
# Introduction

Run 1 at the LHC was a great success for the Standard Model (SM)

No evidence for a new physics signal has been observed



The newly discovered Higgs particle appears SM like

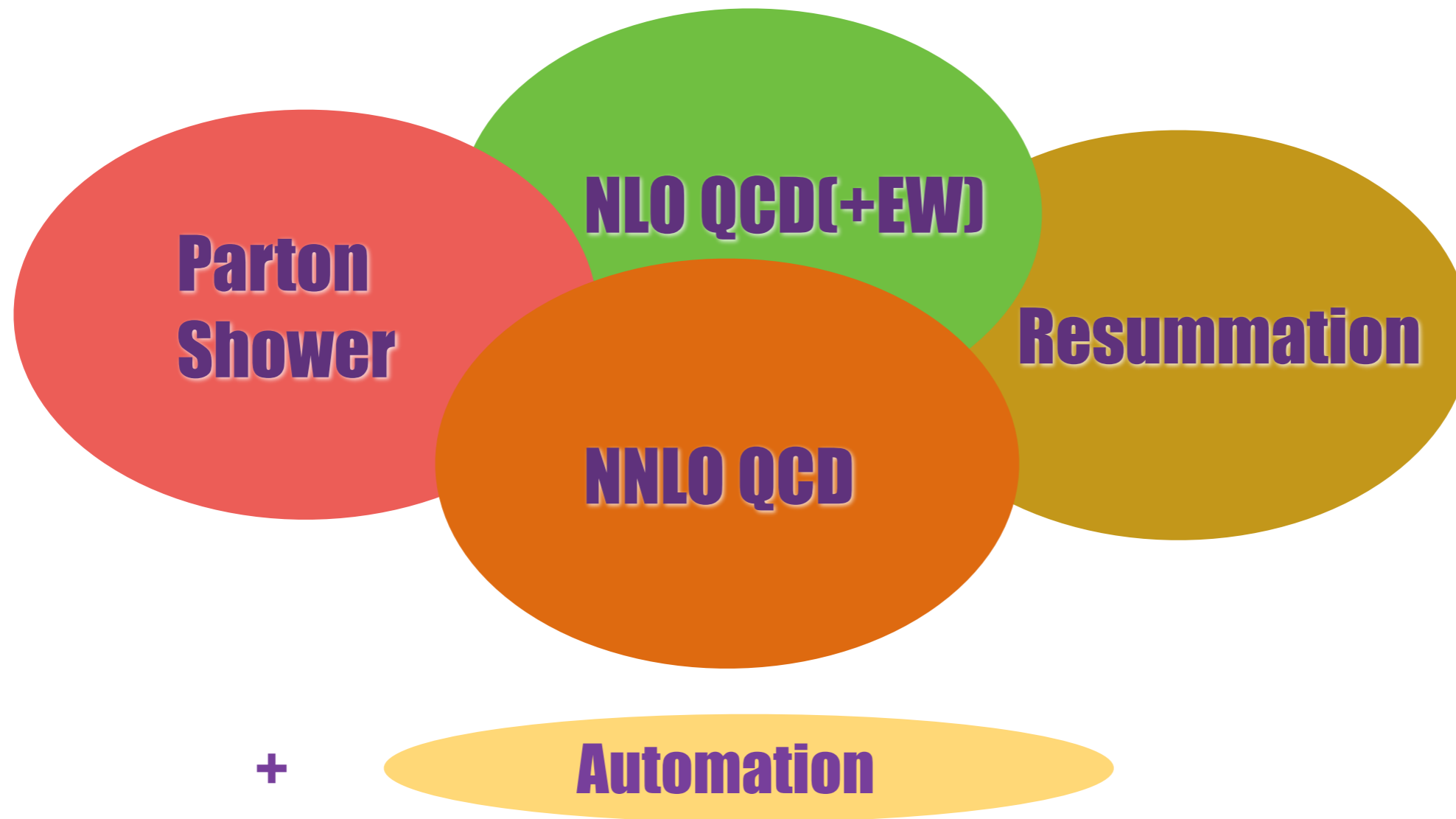


ATLAS hints for an excess in the diboson production at 2 TeV require more data (but triggered more than 30 TH papers !)

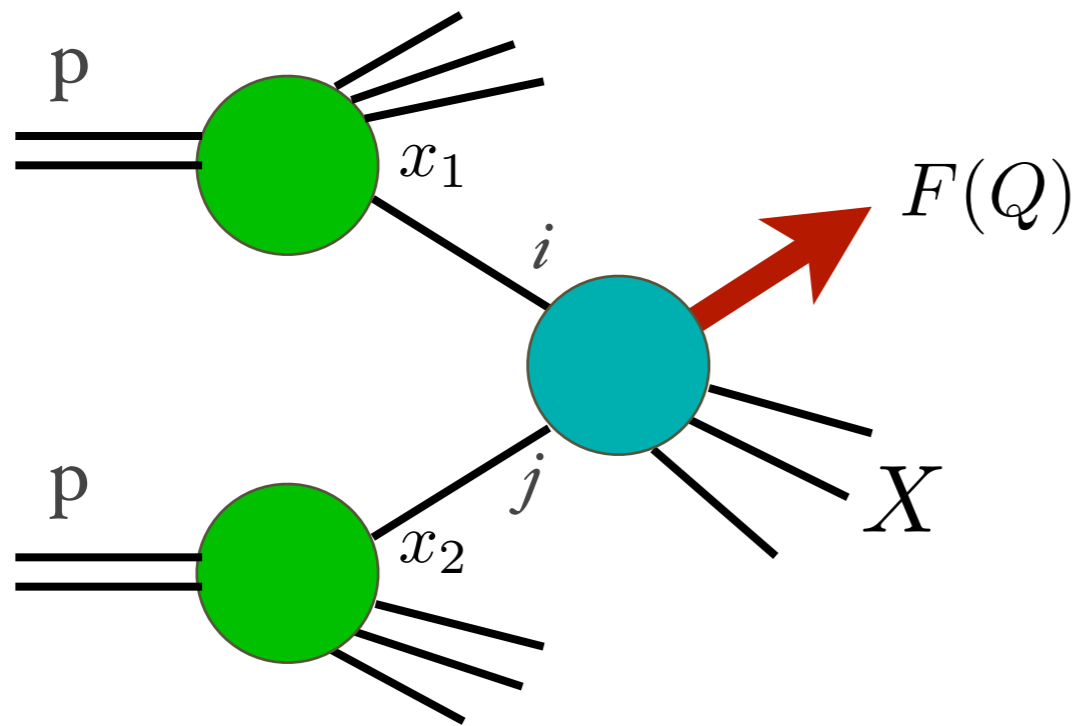
# Introduction

Precise theoretical predictions maybe not crucial for Higgs discovery but essential to interpret the Higgs signal in the SM

→ this talk: quick overview of the progress and tools used in SM physics



# Theoretical framework



High- $p_T$  interactions are characterised by the presence of a hard scale  $Q$  (invariant mass of a lepton pair, high- $p_T$  jet, heavy-quark....)

They can be controlled through the factorisation theorem

The corresponding cross section can be written as

$$\sigma(P_1, P_2) = \sum_{i,j} \int dx_1 dx_2 f_i(x_1, \mu_F^2) f_j(x_2, \mu_F^2) \times \hat{\sigma}_{ij}(p_1, p_2, \alpha_S(\mu_R), Q^2; \mu_F^2, \mu_R^2) + \left(\frac{\Lambda}{Q}\right)^p$$

Parton distributions (PDFs)      Partonic cross section

Accurate predictions for hadronic cross section depend on good knowledge of both  $f_{i,h}(x, \mu_F^2)$  and  $\hat{\sigma}_{ij}$

Power suppressed terms

# PDFs

Determined by global fits to different data sets

## Standard procedure:

- Parametrise at input scale  $Q_0 = 1 - 4 \text{ GeV}$

$$xf(x, Q_0^2) = Ax^\alpha(1-x)^\beta(1 + \epsilon\sqrt{x} + \gamma x + \dots)$$

MMHT14 (CT14) uses instead Chebyshev (Bernstein) polynomials

- Impose momentum sum rule:  $\sum_a \int_0^1 dx x f_a(x, Q_0^2) = 1$

NNPDF generates replicas of the data and fits using a set of neural networks on each replica

- Evolve to desired  $Q^2$  through DGLAP equation

$$Q^2 \frac{\partial f_a(x, Q^2)}{\partial Q^2} = \int_x^1 \frac{dz}{z} P_{ab}(\alpha_S(Q^2), z) f_b(x/z, Q^2)$$

$$P_{ab}(\alpha_S, z) = \frac{\alpha_S}{2\pi} P_{ab}^{(0)}(z) + \left(\frac{\alpha_S}{2\pi}\right)^2 P_{ab}^{(1)}(z) + \left(\frac{\alpha_S}{2\pi}\right)^3 P_{ab}^{(2)}(z) + \dots$$

↑  
LO (1974)

↑  
NLO (1980)

↑  
NNLO (2004: Moch et al.)

- Compute observables and then fit to data to obtain the parameters

# PDFs

set	data	errors	comments
MMHT <sub>14</sub>	DIS+DY+jets+LHC	hessian	$\alpha_s$ fixed
CT <sub>14</sub>	DIS+DY+jets+LHC	hessian	$\alpha_s$ fixed
NNPDF <sub>3.0</sub>	DIS+DY+jets+LHC	Montecarlo	$\alpha_s$ fixed
HeraPDF <sub>2.0</sub>	DIS	hessian	$\alpha_s$ fixed
ABM <sub>12</sub>	DIS+DY+LHC	hessian	$\alpha_s$ fitted
(G)JR	DIS+DY (ft) +some jets	hessian	valence-like $\alpha_s$ fitted

} global fits

“outliers”

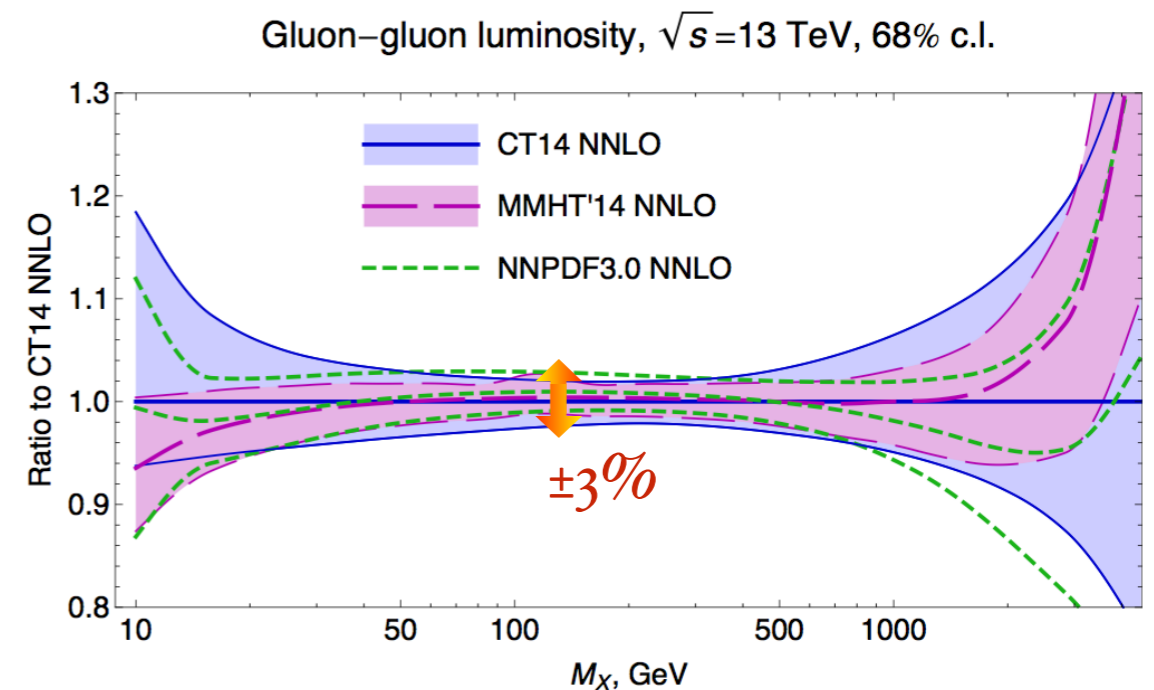
→  $\alpha_s(m_Z) = 0.1132 \pm 0.0011$

→  $\alpha_s(m_Z) = 0.1136 \pm 0.0004$

All fits now up to NNLO

Latest PDF sets from global fits display a nice agreement for the gluon luminosity

→ Good news for Higgs production !



# The value of $\alpha_s(m_Z)$

The current world average from PDG2014 is  $\alpha_s(m_Z)=0.1185 \pm 0.0006$  ↑ quoted error is 0.5 %!

- Recent reassessment of lattice result leads to  $0.1184 \pm 0.0012$  (double error with respect to what used in the PDG) FLAG working group (2013)
- Determination from EW fit (at N<sup>3</sup>LO) gives  $\alpha_s(m_Z)=0.1197 \pm 0.0028$
- Some (maybe controversial) extractions point to much lower  $\alpha_s(m_Z)$ 
  - See e.g. thrust distribution  $\alpha_s(m_Z)=0.1135 \pm 0.0011$  R. Abbate et al (2010)
  - “Outliers” PDF+ $\alpha_s$  fits lead to  $\alpha_s(m_Z) \sim 0.113$  S. Alekhin et al. (2013, 2014)  
P. Jimenez-Delgado, Reja (2014)

➔ **A more conservative error estimate on  $\alpha_s(m_Z)$  is desirable**

**New PDF<sub>4</sub>LHC agreement:** PDFs all evaluated at the same  $\alpha_s(m_Z)=0.118$

Uncertainty for Higgs cross sections evaluated in steps of  $\Delta\alpha_s(m_Z)=0.001-0.0015$

Combined PDF<sub>4</sub>LHC15 sets close to be released

S. Forte, HXSWG meeting, July 2015

Theoretical uncertainties?

# Partonic cross section

The partonic cross section for high- $p_T$  processes can be computed as a series expansion in the QCD coupling  $\alpha_S$

$$\hat{\sigma} = \alpha_S^k \left( \underset{\substack{\uparrow \\ \text{LO}}}{\hat{\sigma}^{(0)}} + \frac{\alpha_S}{\pi} \underset{\substack{\uparrow \\ \text{NLO}}}{\hat{\sigma}^{(1)}} + \left(\frac{\alpha_S}{\pi}\right)^2 \underset{\substack{\uparrow \\ \text{NNLO}}}{\hat{\sigma}^{(2)}} + \dots \right)$$

Leading order (LO) calculations typically give only the order of magnitude of cross sections and distributions

- the scale of  $\alpha_S$  is not defined

- jets  $\leftrightarrow$  partons: jet structure starts to appear only beyond LO

To obtain reliable predictions at least next-to leading order (NLO) is needed

→ NNLO allows to quantify uncertainties

Furthermore

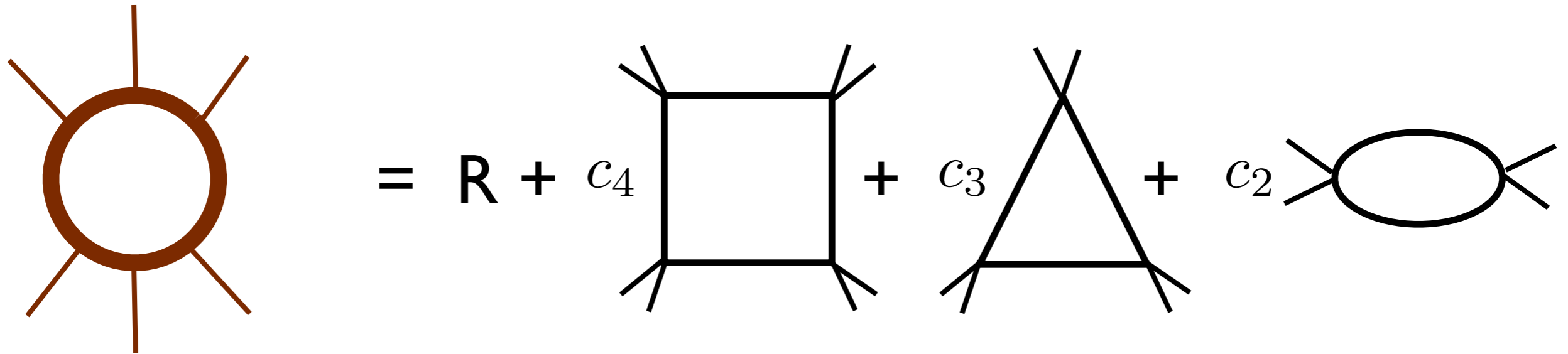
- Resummation of the large logarithmic terms at phase space boundaries
- NLO Electroweak corrections



# The NLO automation

For many years the bottleneck has been the computation of the relevant one-loop amplitudes → Enormous progress in the last 10 years

The traditional approach based on Feynman diagrams is now complemented with new powerful methods based on recursion relations and unitarity



General one-loop amplitude expressed as a sum of known boxes, triangles and bubble integrals plus a remainder term

Coefficient of these integrals can be computed by taking suitable multiple cuts

For example  $c_4$  → Simple product of four tree-level amplitudes evaluated at complex momenta

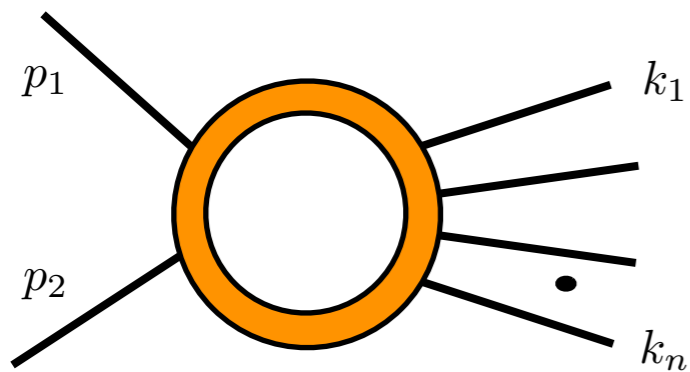
# The NLO automation

For many years the bottleneck has been the computation of the relevant one-loop amplitudes → Enormous progress in the last years

## Automation of NLO corrections

Combine available methods to compute real corrections.....

with most efficient techniques for virtual corrections:

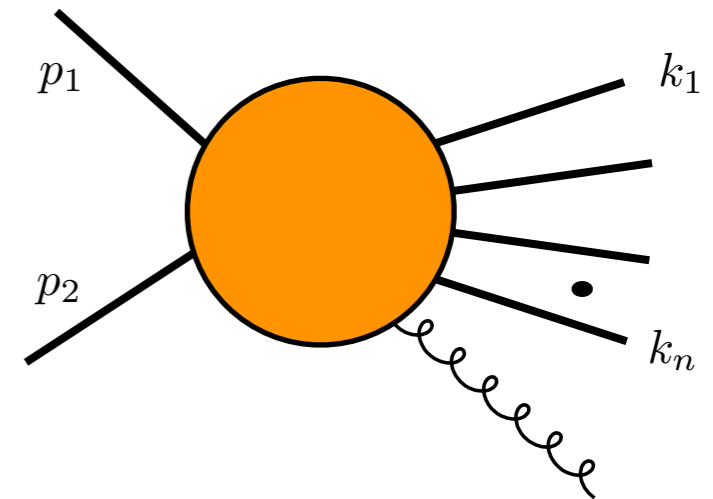


- “traditional” methods to evaluate tensor and scalar integrals

A.Denner, S.Dittmaier (2006,2011)

- fully numerical evaluation based on reduction at the integrand level

G.Ossola, C.Papadopoulos, R.Pittau (2007)  
K.Ellis, W.Giele, Z.Kunszt (2007)



# The NLO automation

- Unitarity and on-shell methods

MadGraph5\_aMC@NLO

BlackHat+Sherpa

NJet

GoSam+Sherpa

Helac-NLO

- Numerical off-shell methods

Combine efficiency of the numerically stable tensor-integral reduction with the automation made possible by a completely recursive approach

OpenLoops+Sherpa

Recola

see also Van Hameren (2009)

The final goal is really automatic NLO calculations

Specify process (input card),  
define cuts/distributions



run and get the results

**The problem is “in principle” solved**

# The NLO automation

Process		Syntax	Cross section (pb)			
Single Higgs production			LO 13 TeV		NLO 13 TeV	
g.1	$pp \rightarrow H$ (HEFT)	p p > h	$1.593 \pm 0.003 \cdot 10^1$	+34.8% +1.2% -26.0% -1.7%	$3.261 \pm 0.010 \cdot 10^1$	+20.2% +1.1% -17.9% -1.6%
g.2	$pp \rightarrow H j$ (HEFT)	p p > h j	$8.367 \pm 0.003 \cdot 10^0$	+39.4% +1.2% -26.4% -1.4%	$1.422 \pm 0.006 \cdot 10^1$	+18.5% +1.1% -16.6% -1.4%
g.3	$pp \rightarrow H j j$ (HEFT)	p p > h j j	$3.020 \pm 0.002 \cdot 10^0$	+59.1% +1.4% -34.7% -1.7%	$5.124 \pm 0.020 \cdot 10^0$	+20.7% +1.3% -21.0% -1.5%
g.4	$pp \rightarrow H j j$ (VBF)	p p > h j j \$\$ w+ w- z	$1.987 \pm 0.002 \cdot 10^0$	+1.7% +1.9% -2.0% -1.4%	$1.900 \pm 0.006 \cdot 10^0$	+0.8% +2.0% -0.9% -1.5%
g.5	$pp \rightarrow H j j j$ (VBF)	p p > h j j j \$\$ w+ w- z	$2.824 \pm 0.005 \cdot 10^{-1}$	+15.7% +1.5% -12.7% -1.0%	$3.085 \pm 0.010 \cdot 10^{-1}$	+2.0% +1.5% -3.0% -1.1%
g.6	$pp \rightarrow HW^\pm$	p p > h wpm	$1.195 \pm 0.002 \cdot 10^0$	+3.5% +1.9% -4.5% -1.5%	$1.419 \pm 0.005 \cdot 10^0$	+2.1% +1.9% -2.6% -1.4%
g.7	$pp \rightarrow HW^\pm j$	p p > h wpm j	$4.018 \pm 0.003 \cdot 10^{-1}$	+10.7% +1.2% -9.3% -0.9%	$4.842 \pm 0.017 \cdot 10^{-1}$	+3.6% +1.2% -3.7% -1.0%
g.8*	$pp \rightarrow HW^\pm j j$	p p > h wpm j j	$1.198 \pm 0.016 \cdot 10^{-1}$	+26.1% +0.8% -19.4% -0.6%	$1.574 \pm 0.014 \cdot 10^{-1}$	+5.0% +0.9% -6.5% -0.6%
g.9	$pp \rightarrow HZ$	p p > h z	$6.468 \pm 0.008 \cdot 10^{-1}$	+3.5% +1.9% -4.5% -1.4%	$7.674 \pm 0.027 \cdot 10^{-1}$	+2.0% +1.9% -2.5% -1.4%
g.10	$pp \rightarrow HZ j$	p p > h z j	$2.225 \pm 0.001 \cdot 10^{-1}$	+10.6% +1.1% -9.2% -0.8%	$2.667 \pm 0.010 \cdot 10^{-1}$	+3.5% +1.1% -3.6% -0.9%
g.11*	$pp \rightarrow HZ j j$	p p > h z j j	$7.262 \pm 0.012 \cdot 10^{-2}$	+26.2% +0.7% -19.4% -0.6%	$8.753 \pm 0.037 \cdot 10^{-2}$	+4.8% +0.7% -6.3% -0.6%
g.12*	$pp \rightarrow HW^+W^-$ (4f)	p p > h w+ w-	$8.325 \pm 0.139 \cdot 10^{-3}$	+0.0% +2.0% -0.3% -1.6%	$1.065 \pm 0.003 \cdot 10^{-2}$	+2.5% +2.0% -1.9% -1.5%
g.13*	$pp \rightarrow HW^\pm \gamma$	p p > h wpm a	$2.518 \pm 0.006 \cdot 10^{-3}$	+0.7% +1.9% -1.4% -1.5%	$3.309 \pm 0.011 \cdot 10^{-3}$	+2.7% +1.7% -2.0% -1.4%
g.14*	$pp \rightarrow HZW^\pm$	p p > h z wpm	$3.763 \pm 0.007 \cdot 10^{-3}$	+1.1% +2.0% -1.5% -1.6%	$5.292 \pm 0.015 \cdot 10^{-3}$	+3.9% +1.8% -3.1% -1.4%
g.15*	$pp \rightarrow HZZ$	p p > h z z	$2.093 \pm 0.003 \cdot 10^{-3}$	+0.1% +1.9% -0.6% -1.5%	$2.538 \pm 0.007 \cdot 10^{-3}$	+1.9% +2.0% -1.4% -1.5%
g.16	$pp \rightarrow Ht\bar{t}$	p p > h t t~	$3.579 \pm 0.003 \cdot 10^{-1}$	+30.0% +1.7% -21.5% -2.0%	$4.608 \pm 0.016 \cdot 10^{-1}$	+5.7% +2.0% -9.0% -2.3%
g.17	$pp \rightarrow Htj$	p p > h tt j	$4.994 \pm 0.005 \cdot 10^{-2}$	+2.4% +1.2% -4.2% -1.3%	$6.328 \pm 0.022 \cdot 10^{-2}$	+2.9% +1.5% -1.8% -1.6%
g.18	$pp \rightarrow Hb\bar{b}$ (4f)	p p > h b b~	$4.983 \pm 0.002 \cdot 10^{-1}$	+28.1% +1.5% -21.0% -1.8%	$6.085 \pm 0.026 \cdot 10^{-1}$	+7.3% +1.6% -9.6% -2.0%
g.19	$pp \rightarrow Ht\bar{t}j$	p p > h t t~ j	$2.674 \pm 0.041 \cdot 10^{-1}$	+45.6% +2.6% -29.2% -2.9%	$3.244 \pm 0.025 \cdot 10^{-1}$	+3.5% +2.5% -8.7% -2.9%
g.20*	$pp \rightarrow Hb\bar{b}j$ (4f)	p p > h b b~ j	$7.367 \pm 0.002 \cdot 10^{-2}$	+45.6% +1.8% -29.1% -2.1%	$9.034 \pm 0.032 \cdot 10^{-2}$	+7.9% +1.8% -11.0% -2.2%

MadGraph5\_aMC@NLO: sample from 172 processes

# NLO+PS matching

Parton Shower Monte Carlo provide a simulation of all the stages of the hadronic collision: merge QCD matrix element + shower in the soft collinear approximation +hadronization model

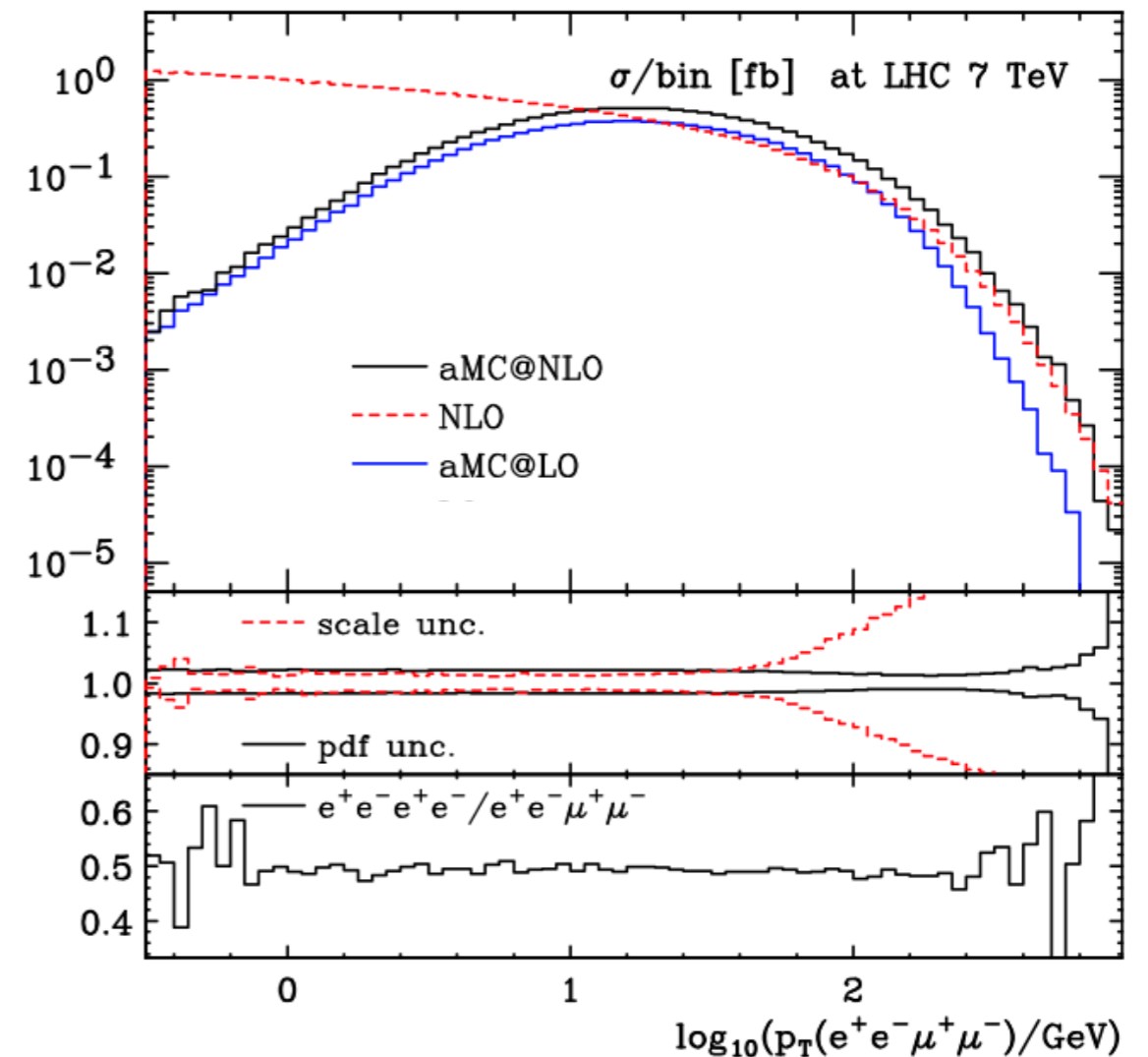
The MC@NLO and POWHEG methods allow us to combine NLO calculations with existing MC like PYTHIA, HERWIG, SHERPA....

- MC@NLO method

- MadGraph5\_aMC@NLO
- Sherpa+OpenLoops
- Herwig++Matchbox+Openloops/Gosam

- Powheg method

- Madgraph4+Powheg+MCFM/Gosam
- Herwig++Matchbox+Openloops/Gosam



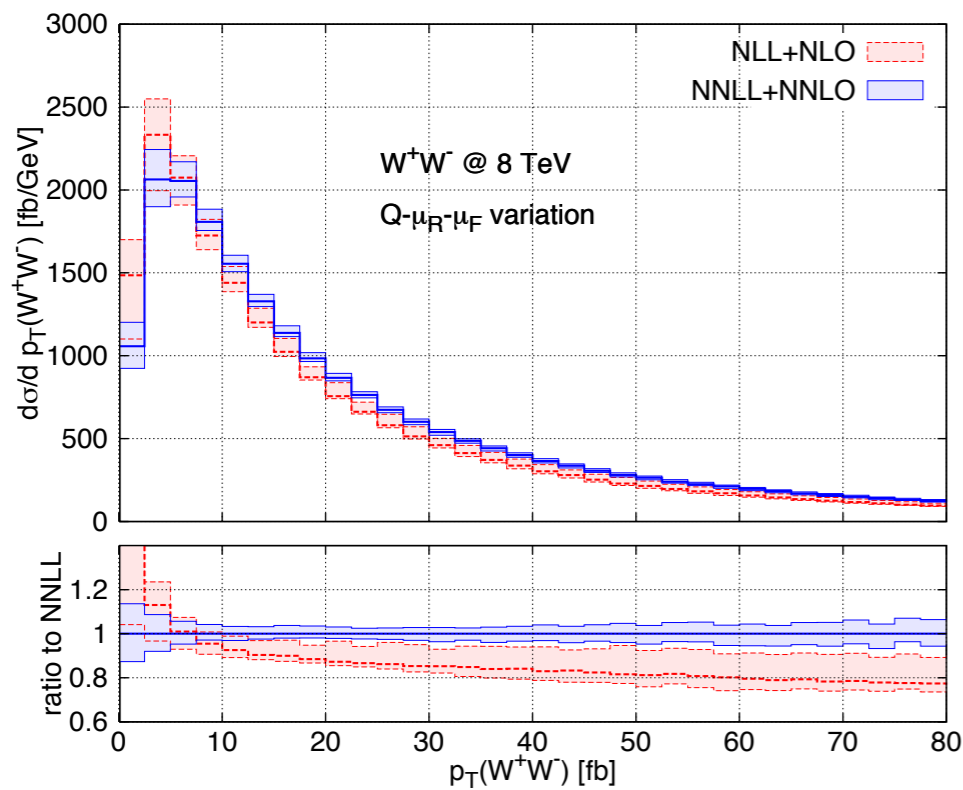
POWHEG and MC@NLO implementations have same formal accuracy but differ in the amount of radiation that is exponentiated → Main issue now is to assess uncertainties

# NLO and PS: what else ?

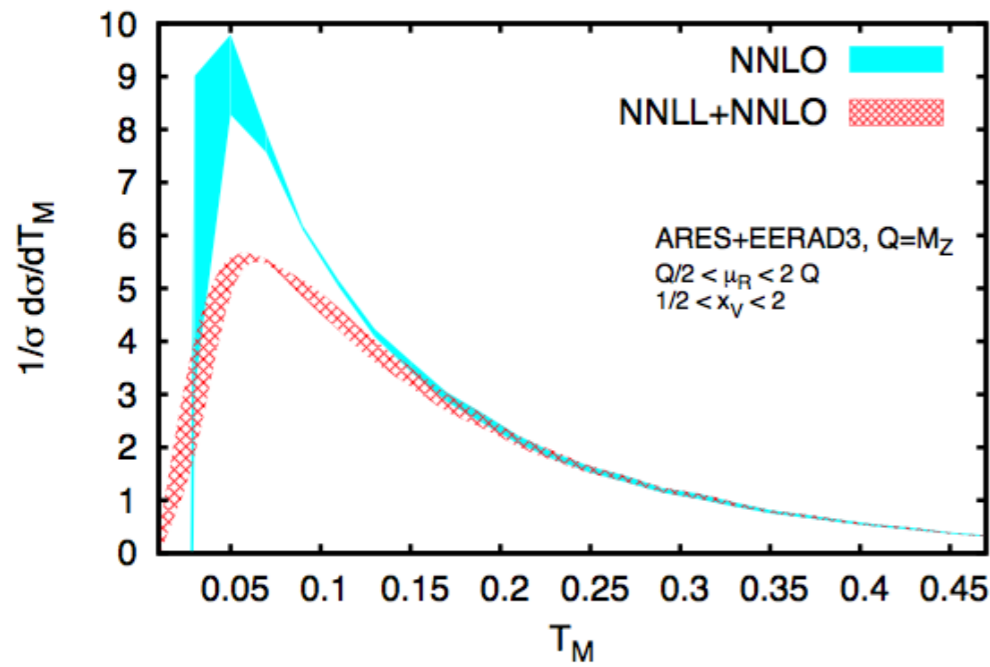
- MENLOPS: Start from a definite NLO+PS and add higher multiplicities tree level ME  
K.Hamilton, P.Nason (2010)
- MEPS@NLO (UNLOPS) merge two NLO+PS simulations with different multiplicities  
R.Frederix, S.Frixione (2011)  
S.Hoeche, F.Krauss, M.Schonherr, F.Siegert (2012)  
L.Lonnblad, S.Prestel (2012), S.Platzer (2012)
- MINLO, Geneva Merge two NLO+PS without merging scale (improving Sudakov form factor)  
K.Hamilton, P.Nason, G.Zanderighi (2012)  
S.Alioli et al (2012)
- Alternative NLO+PS scheme: KrKNLO (requires PDFs in a dedicated scheme)  
S.Jadach et al. (2015)
- Attempts to go beyond Leading Color approximation
  - Deductor (talk by M.Kraus for application to  $t\bar{t}$ )  
Z.Nagy, D.Soper (2012,2015)  
M.Czakon et al. (2015)
  - $qq \rightarrow qq$  evolution matrix elements  
S.Platzer (2013)
- NLO+PS EW implementation in  $H \rightarrow ZZ \rightarrow 4$  leptons  
S.Boselli et al. (2015)

# Resummation

For specific observables, analytic resummation provides predictions with higher logarithmic accuracy and an important validation of MC tools



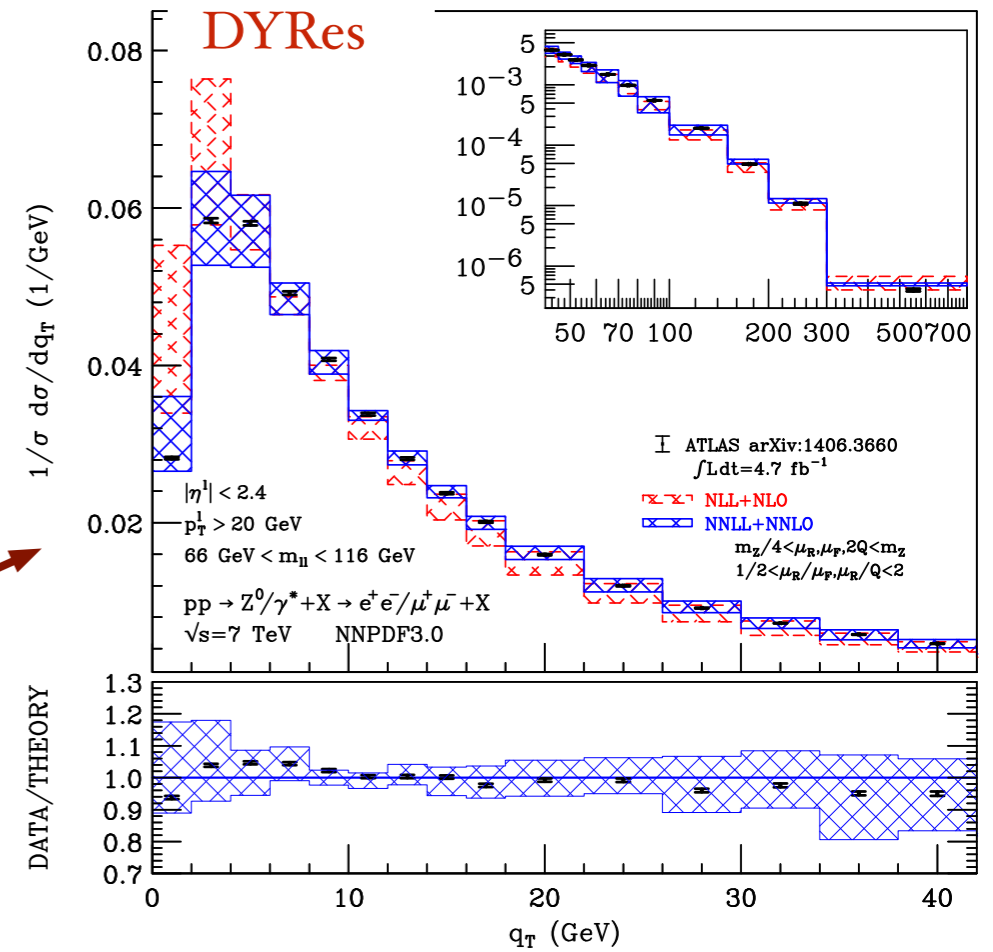
S.Kallweit, D.Rathlev, M. Wiesemann, MG (2015)



Resummed  $p_T$  spectra at full NNLL+NNLO:

WW (and ZZ)

Z (and W) including leptonic cuts



S.Catani, D. de Florian, G.Ferrera, MG (2015)

Automatic resummation for event-shape variables in  $e^+e^-$  annihilation at NNLL

Valid for a specific class of IR safe observables (recursive IR safe): method potentially applicable to hadron collisions

P.Monni, A.Banfi, G.Zanderighi (2015)

# Resummation

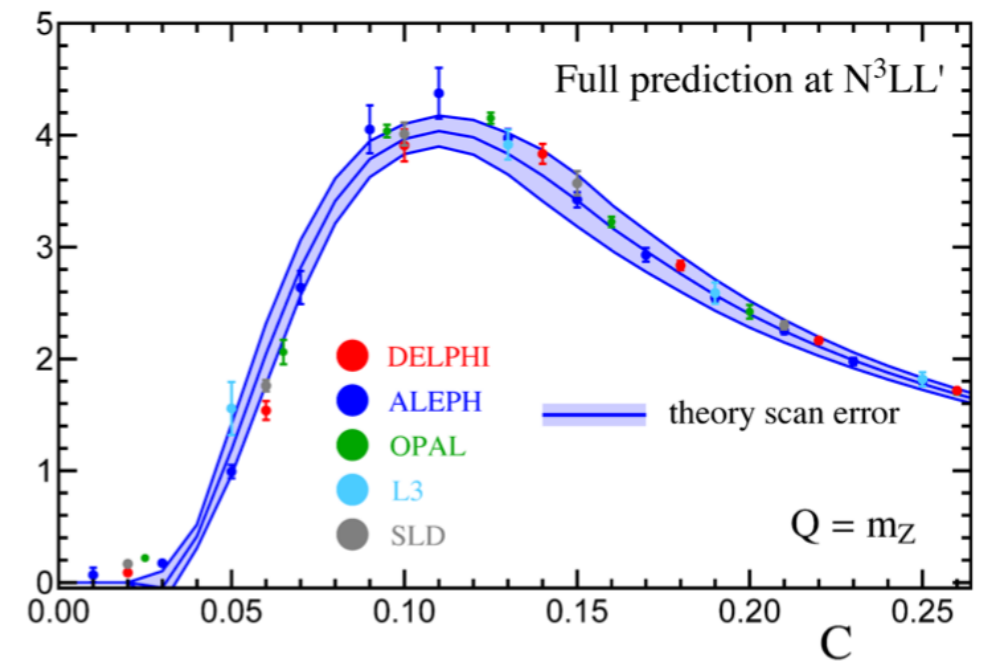
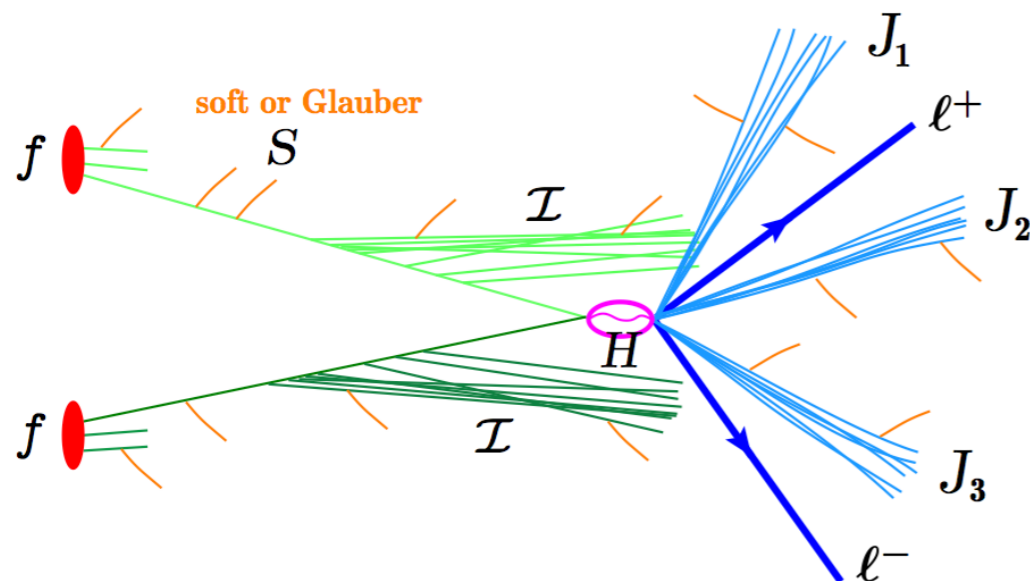
Soft collinear effective theory (SCET) complements traditional QCD approach to derive new interesting results

- Resummation for the C-parameter and fit to  $\alpha_s(m_Z)$

Result for  $\alpha_s(m_Z) = 0.1123 \pm 0.0015$  consistent with analogous fit from Thrust

- Resummation as a way to get further insight into fixed order calculations

Example: N-jettiness:  $\tau_N \rightarrow 0$  when exactly N jets



A.Hoang et al (2015)

I.Stewart,F.Tackmann,W.Waalewijn (2010)

$$\tau_N = \frac{2}{Q^2} \sum_k \min\{q_a \cdot p_k, q_b \cdot p_k, q_1 \cdot p_k, \dots, q_N \cdot p_k\}$$

Jet and beam functions computed to NNLO

T.Becher, M.Neubert (2006); T.Becher, M.Neubert, G.Bell (2010)

J.Gaunt, M.Stahlhofen,F.Tackmann (2014)

Soft function for  $\tau_1$  to NNLO

R.Boughezal, X.Liu, F.Petriello (2015)



# The NNLO revolution

NNLO calculations important at least for the following cases:

1) Benchmark processes measured with high accuracy

✓  $e^+e^- \rightarrow 3 \text{ jets}$

✓  $pp \rightarrow W, Z$

✓  $pp \rightarrow t\bar{t}$

(✓)  $pp \rightarrow 2 \text{ jets}$

↘ towards completion

2) Processes with large NLO corrections

✓  $pp \rightarrow H$

↘ even N<sup>3</sup>LO known now

✓  $pp \rightarrow H + \text{jet}$

✓  $pp \rightarrow HH$

3) Important backgrounds for Higgs and NP searches

✓  $pp \rightarrow \gamma\gamma$

✓  $pp \rightarrow W\gamma, Z\gamma$

✓  $pp \rightarrow WW$

↘ NNLO reduces tension with ATLAS data

✓  $pp \rightarrow ZZ$

✗  $pp \rightarrow WZ$

✓  $pp \rightarrow W(Z) + \text{jet}$

**It is essential to provide fiducial cross sections and distributions with which the data can be directly compared**

( for more processes see also Les Houches 2013 NNLO wish list)

# NNLO methods

Broadly speaking there are two approaches that we can follow:

- Organise the calculation from scratch so as to cancel all the singularities
  - sector decomposition T. Binoth, G.Heinrich (2000,2004)  
C.Anastasiou, K.Melnikov, F.Petriello (2004)
  - antenna subtraction A. & T. Gehrmann, N. Glover (2005)
  - “colourful” subtraction (**talk by Z.Trocsanyi**) G, Somogyi, Z. Trocsanyi,  
V. Del Duca (2005, 2007)
  - joint use of subtraction and sector decomposition M.Czakon (2010,2011)  
R.Boughezal, K.Melnikov, F.Petriello (2011)
- Start from an inclusive NNLO calculation (sometimes obtained through resummation) and combine it with an NLO calculation for n+1 parton process
  - $q_T$  subtraction S.Catani, MG (2007)
  - “N-jettiness” method R.Boughezal, C.Focke,X.Liu, F.Petriello (2015)  
F.Tackmann et al. (2015)
  - recently introduced “Born projection” method for VBF (**talk by A. Karlberg**) M.Cacciari, F.Dreyer, A.Karlberg, G.Salam,G.Zanderighi (2015)

...and then we need the relevant two-loop amplitudes !

C.Anastasiou, F.Caola, M.Czakon, T.Gehrmann, N.Glover, M.Jaquier, A. Koukoutsakis  
C.Oleari, K.Melnikov, L.Tancredi, M.E. Tejeda-Yeomans, A. von Manteuffel and many others

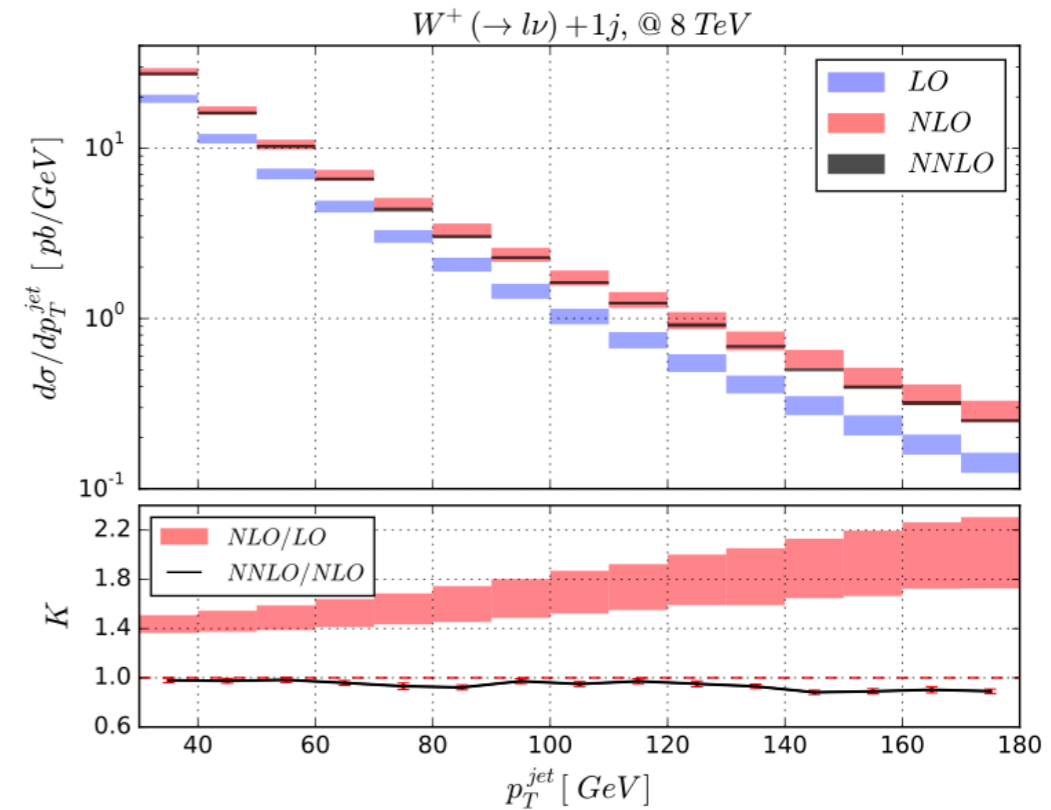
# W and Z+jet at NNLO

## ● W<sub>+jet</sub>

First application of new “*N-jettiness*” method: relatively flat NNLO correction

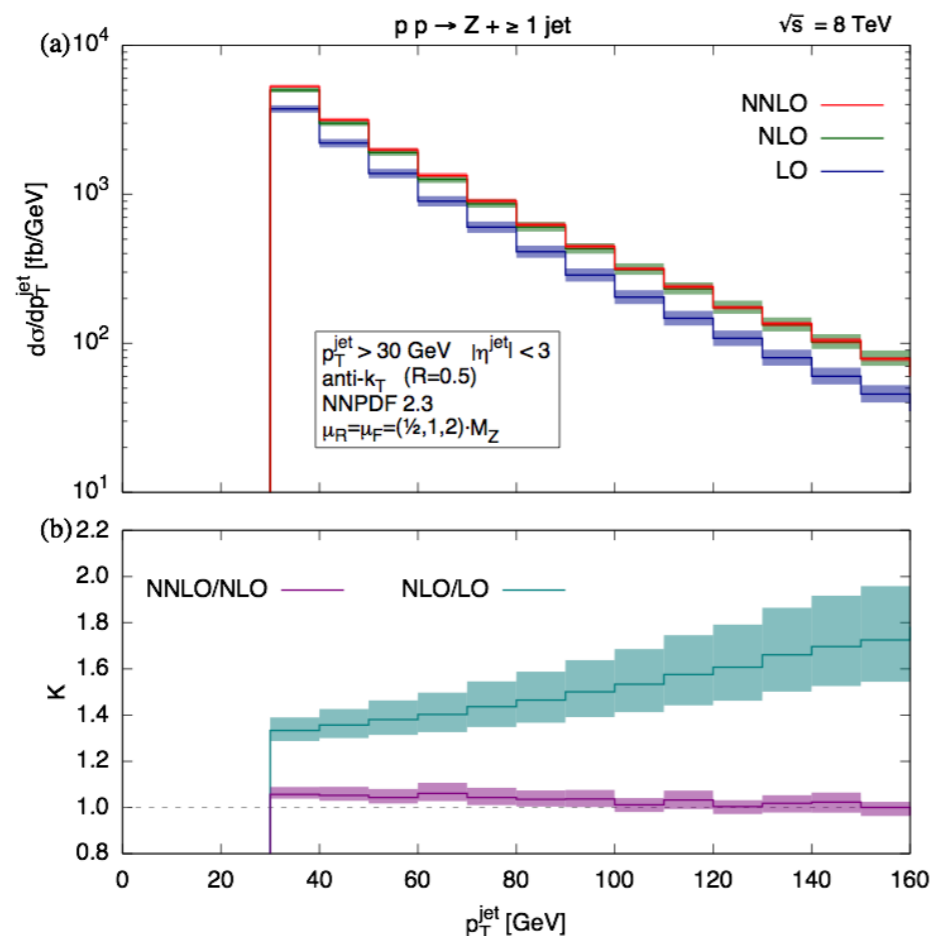
$p_T^{jet} > 30 \text{ GeV},  \eta_{jet}  < 2.4$	
Leading order:	$533^{+39}_{-38} \text{ pb}$
Next-to-leading order:	$798^{+63}_{-48} \text{ pb}$
Next-to-next-to-leading order:	$775^{+0}_{-8} \text{ pb}$

Small NNLO effect and significant reduction of scale uncertainties



R.Boughezal, C.Focke, X.Liu, F.Petriello (2015)

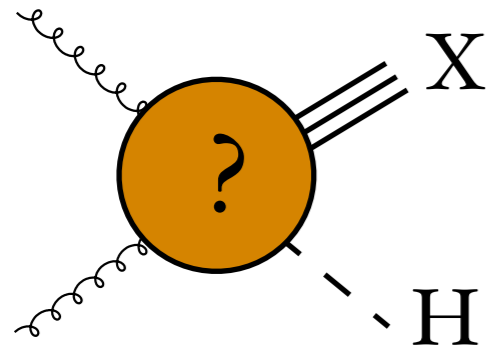
## ● Z+jet



Similar effects for Z+jet: *antenna subtraction* (large  $N_C$  approximation for the dominant channels)

A and T. Gehrmann, N. Glover, T.Morgan, A.Huss (2015)

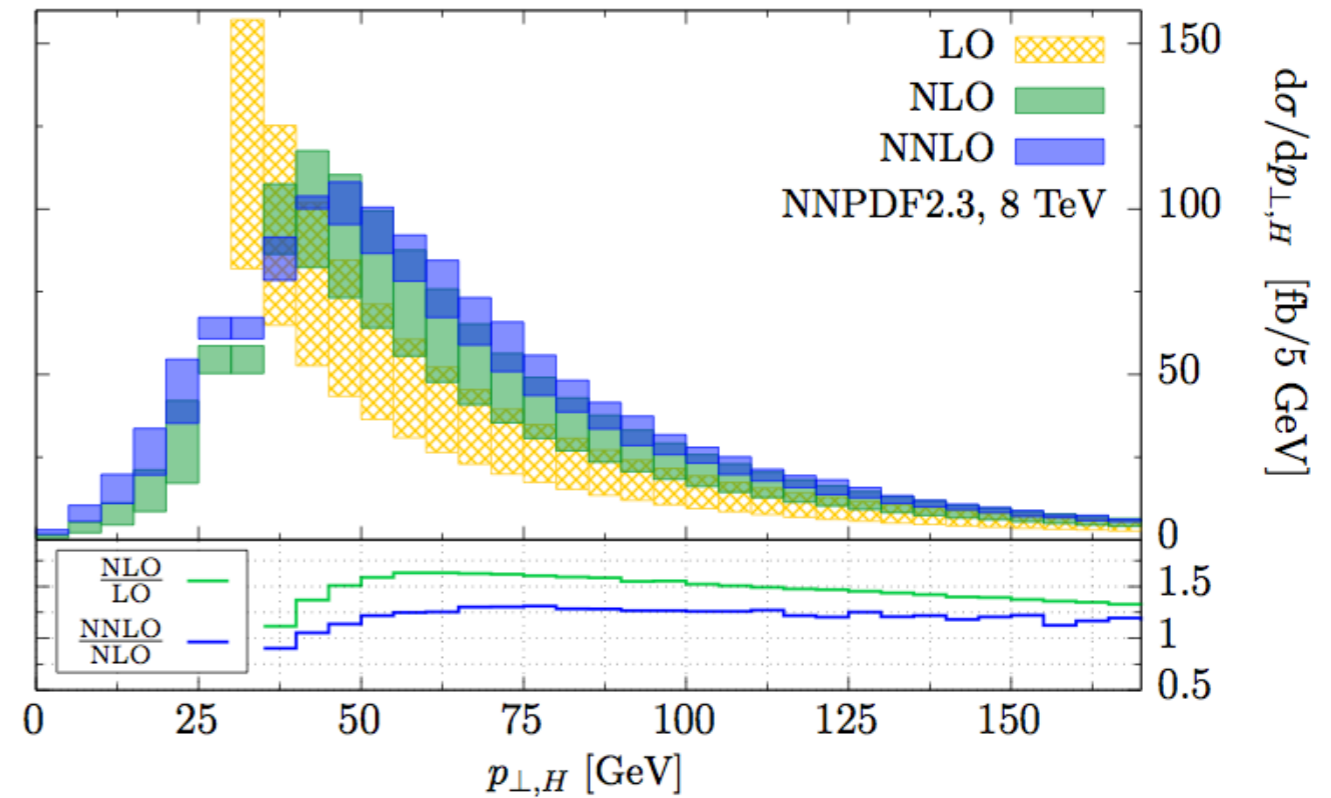
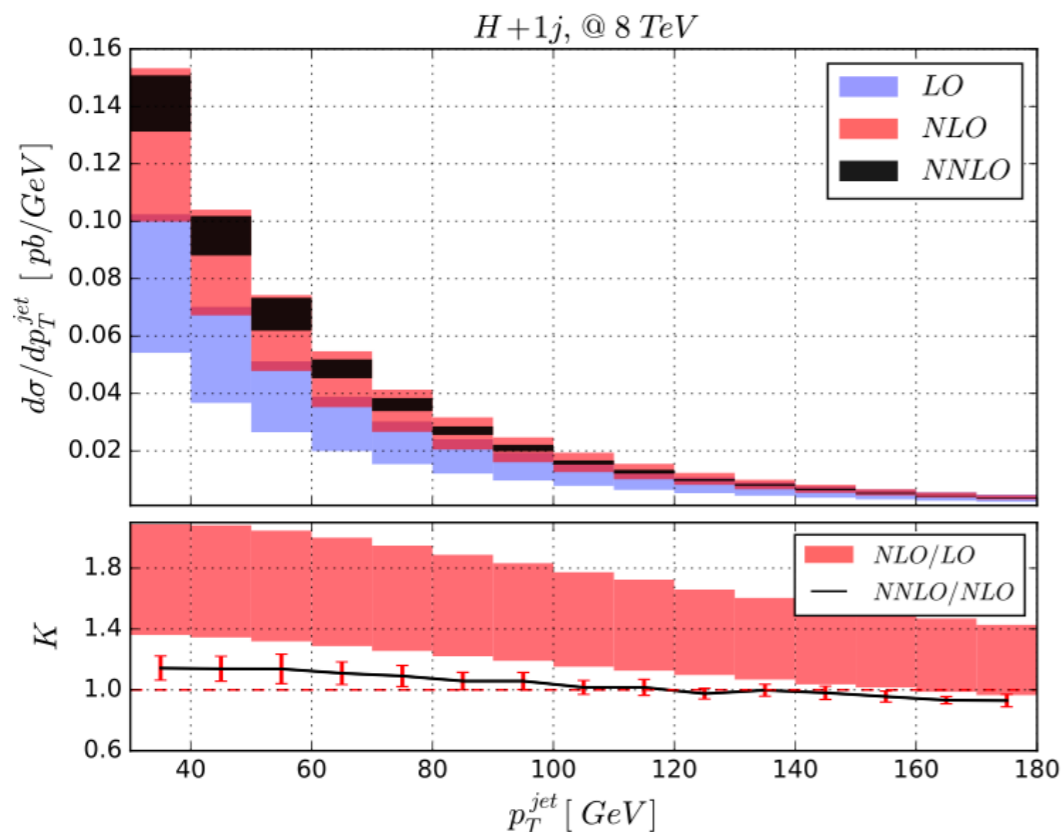
# H+jet at NNLO



Higgs production at high- $p_T$  is useful to test new physics scenarios and better resolve the structure of the heavy-quark loop

X. Chen, T. Gehrmann, N. Glover, M. Jaquier (2014)  
 R. Boughezal, F. Caola, K. Melnikov, F. Petriello, M. Schulze (2015)  
 R. Boughezal, C. Focke, W. Giele, X. Liu, F. Petriello (2015)

NNLO calculation carried out with three independent methods (*antenna subtraction, subtraction+sector, N-jettiness*)!



Still in the large  $m_{\text{top}}$  approximation  
 quantitative effect smaller than previously anticipated from gg only:  
 at the 20% level ( $\mu=m_H$ )

# ZZ at NNLO: lepton decays and off-shell effects

S. Kallweit, D. Rathlev, MG (2015)

Consider  $pp \rightarrow ZZ \rightarrow 4$  leptons at 8 TeV

Use ATLAS cuts to define fiducial region:

$$p_{T1} > 7 \text{ GeV} \quad |\eta_1| < 2.7 \quad \Delta R(1,1) > 0.2$$

$$66 \text{ GeV} < m_{11} < 116 \text{ GeV}$$

Channel	$\sigma_{\text{LO}}$ (fb)	$\sigma_{\text{NLO}}$ (fb)	$\sigma_{\text{NNLO}}$ (fb)	$\sigma_{\text{exp}}$ (fb)
$e^+e^-e^+e^-$	$3.547(1)^{+2.9\%}_{-3.9\%}$	$5.047(1)^{+2.8\%}_{-2.3\%}$	$5.79(2)^{+3.4\%}_{-2.6\%}$	$4.6^{+0.8}_{-0.7}(\text{stat})^{+0.4}_{-0.4}(\text{syst.})^{+0.1}_{-0.1}(\text{lumi.})$
$\mu^+\mu^-\mu^+\mu^-$				$5.0^{+0.6}_{-0.5}(\text{stat})^{+0.2}_{-0.2}(\text{syst.})^{+0.2}_{-0.2}(\text{lumi.})$
$e^+e^-\mu^+\mu^-$	$6.950(1)^{+2.9\%}_{-3.9\%}$	$9.864(2)^{+2.8\%}_{-2.3\%}$	$11.31(2)^{+3.2\%}_{-2.5\%}$	$11.1^{+1.0}_{-0.9}(\text{stat})^{+0.5}_{-0.5}(\text{syst.})^{+0.3}_{-0.3}(\text{lumi.})$

**+15%** (60% comes from gg fusion)

NNLO corrections improve agreement with ATLAS data in the  $2e2\mu$  channel but make the agreement worse in the other channels (but experimental uncertainties still large)

Done with new code **MATRIX**: *q<sub>T</sub>subtraction* +Munich+amplitudes from Openloops

# ZZ at NNLO: lepton decays and off-shell effects

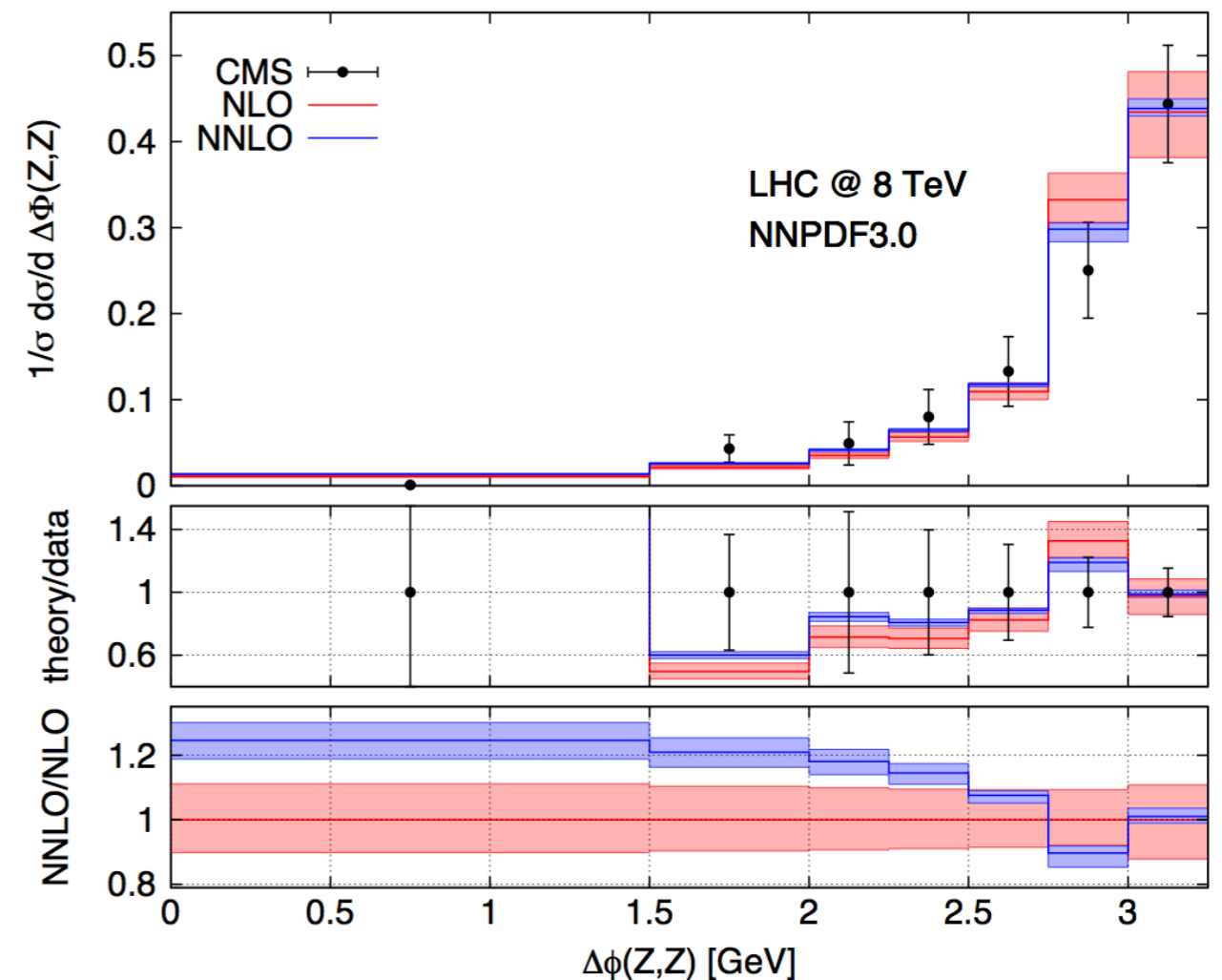
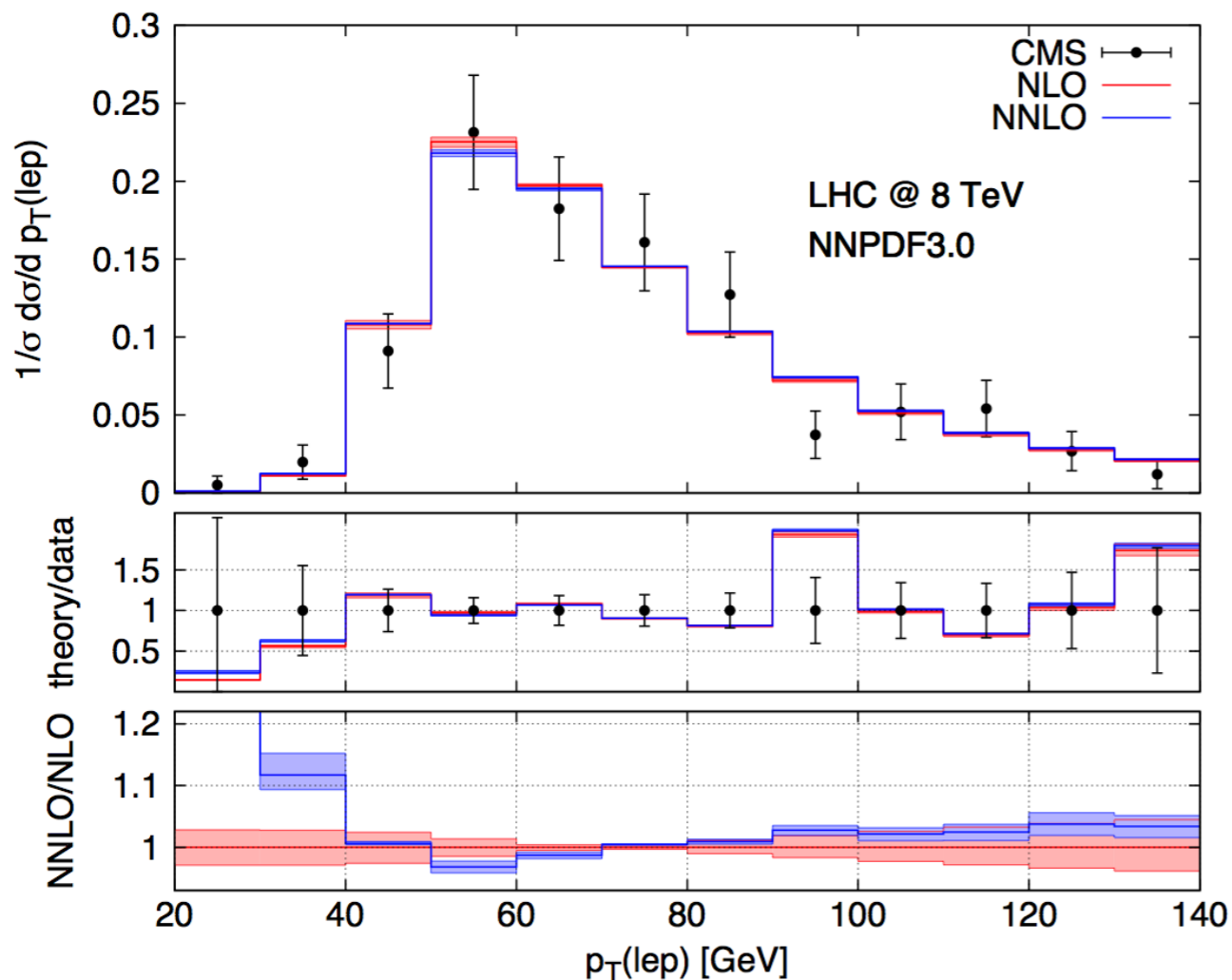
S. Kallweit, D. Rathlev, MG (2015)

Now CMS cuts:  $60 \text{ GeV} < m_{ll} < 120 \text{ GeV}$

$p_{T1} > 20 \text{ GeV}$   $p_{T2} > 10 \text{ GeV}$   $m_{ll} > 4 \text{ GeV}$

$p_{T_e} > 7 \text{ GeV}$   $|\eta_e| < 2.5$

$p_{T_\mu} > 5 \text{ GeV}$   $|\eta_\mu| < 2.4$



NNLO effects improve agreement with data for the  $\Delta\phi$  distribution

# NNLO+PS matching

NLO matching well established, while NNLO matching still in its infancy

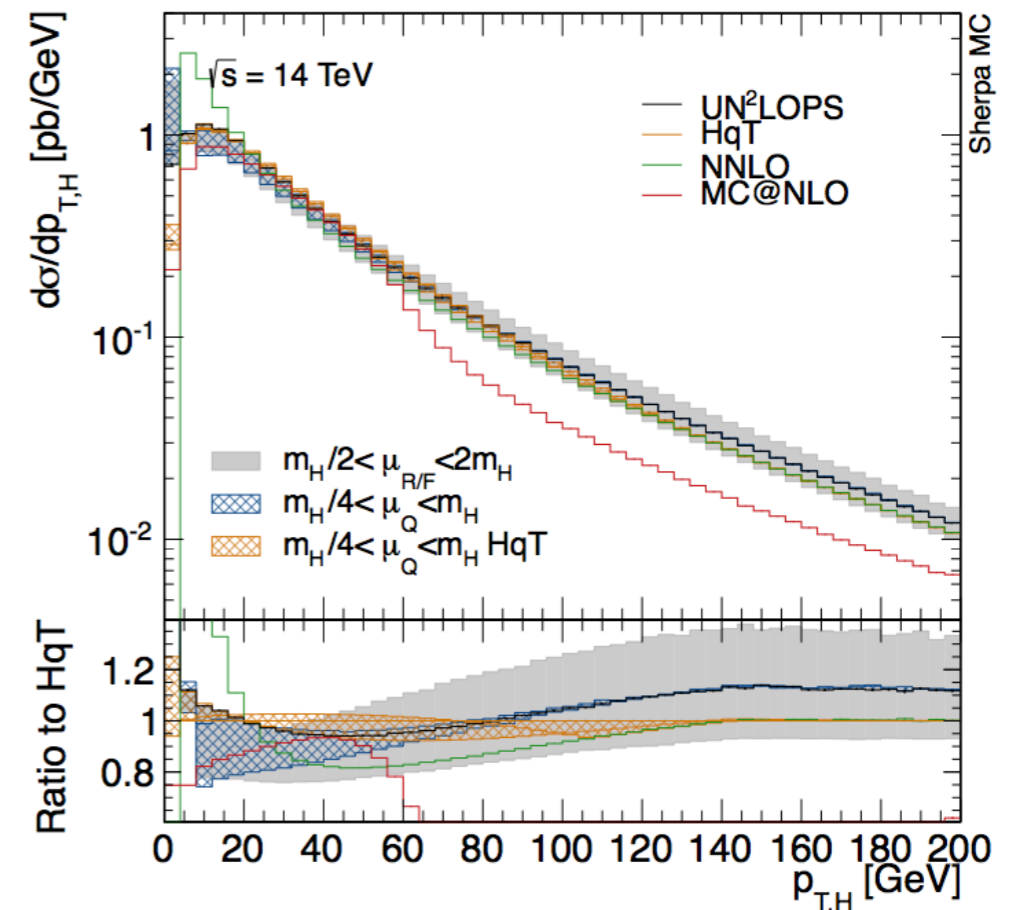
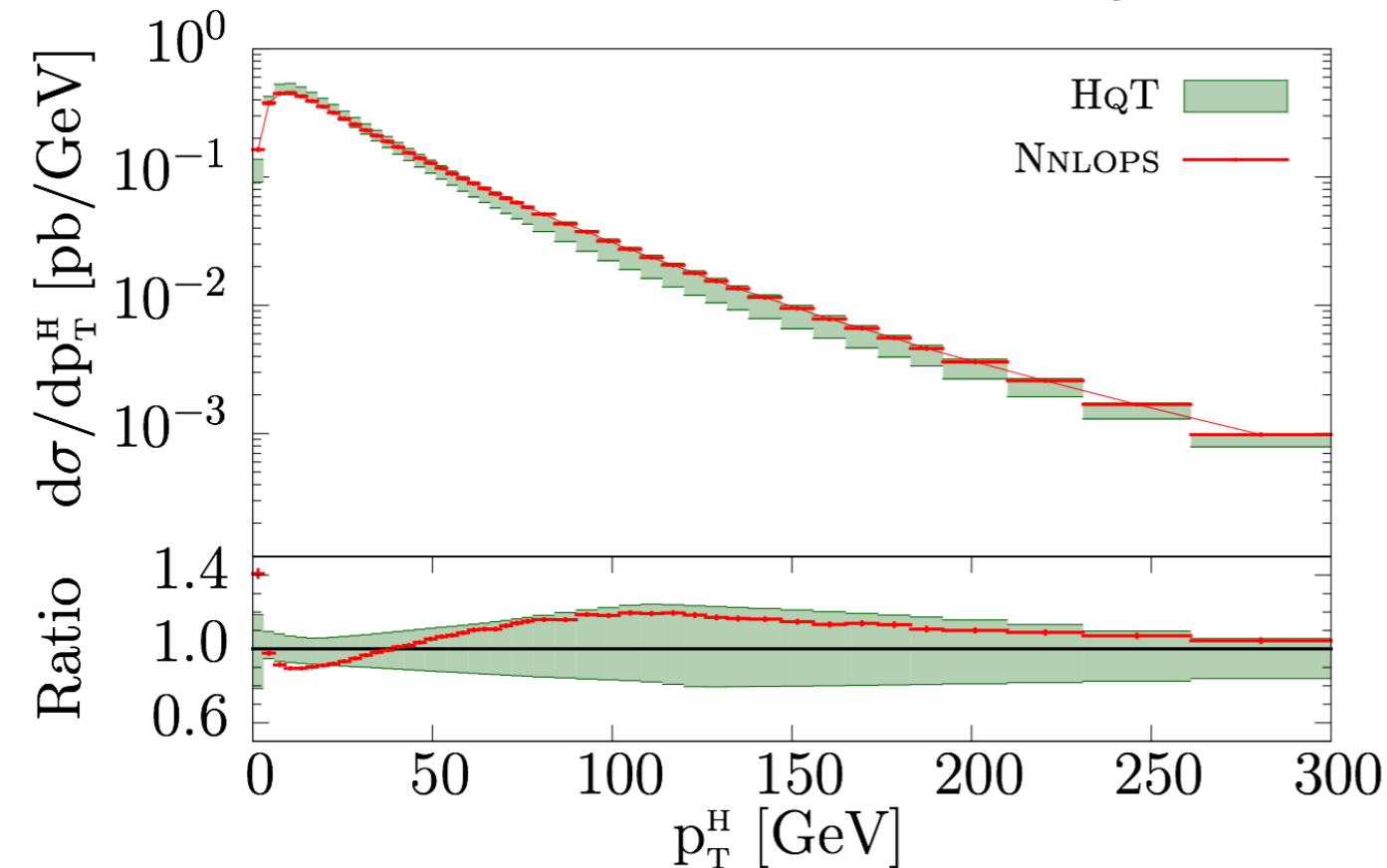
1) **NNLOPS**: use MINLO to obtain a NLO generator for both H and H+jet(s)

2) **UN<sup>2</sup>LOPS**: use S-MC@NLO + UNLOPS + q<sub>T</sub> slicing

K.Hamilton, P.Nason, G.Zanderighi (2014, 2015)

N.Lavesson, L.Lonnblad (2008)

S.Hoeche, Y.Li, S.Prestel (2014)



Enforce correct NNLO normalisation by reweighing the inclusive rapidity distribution to the NNLO calculation

NNLO virtual corrections confined in the low  $p_T$  region while in the POWHEG-MINLO approach they are spread over the whole  $p_T$  region

Current applications limited to vector and Higgs boson production

# Electroweak corrections

Since  $O(\alpha) \sim O(\alpha_s^2)$  we expect NLO EW  $\sim$  NNLO QCD but enhancements due to

- EW Sudakov logs: important at high  $p_T$
- photon emission from “bare” leptons

NLO EW corrections automation in  
Openloops+Munich+Sherpa.....

-  $W$ +multijet

S. Kallweit, J.Lindert, P.Maierhofer,  
S.Pozzorini M.Shonherr (2014)

.....and in MG5\_aMC@NLO

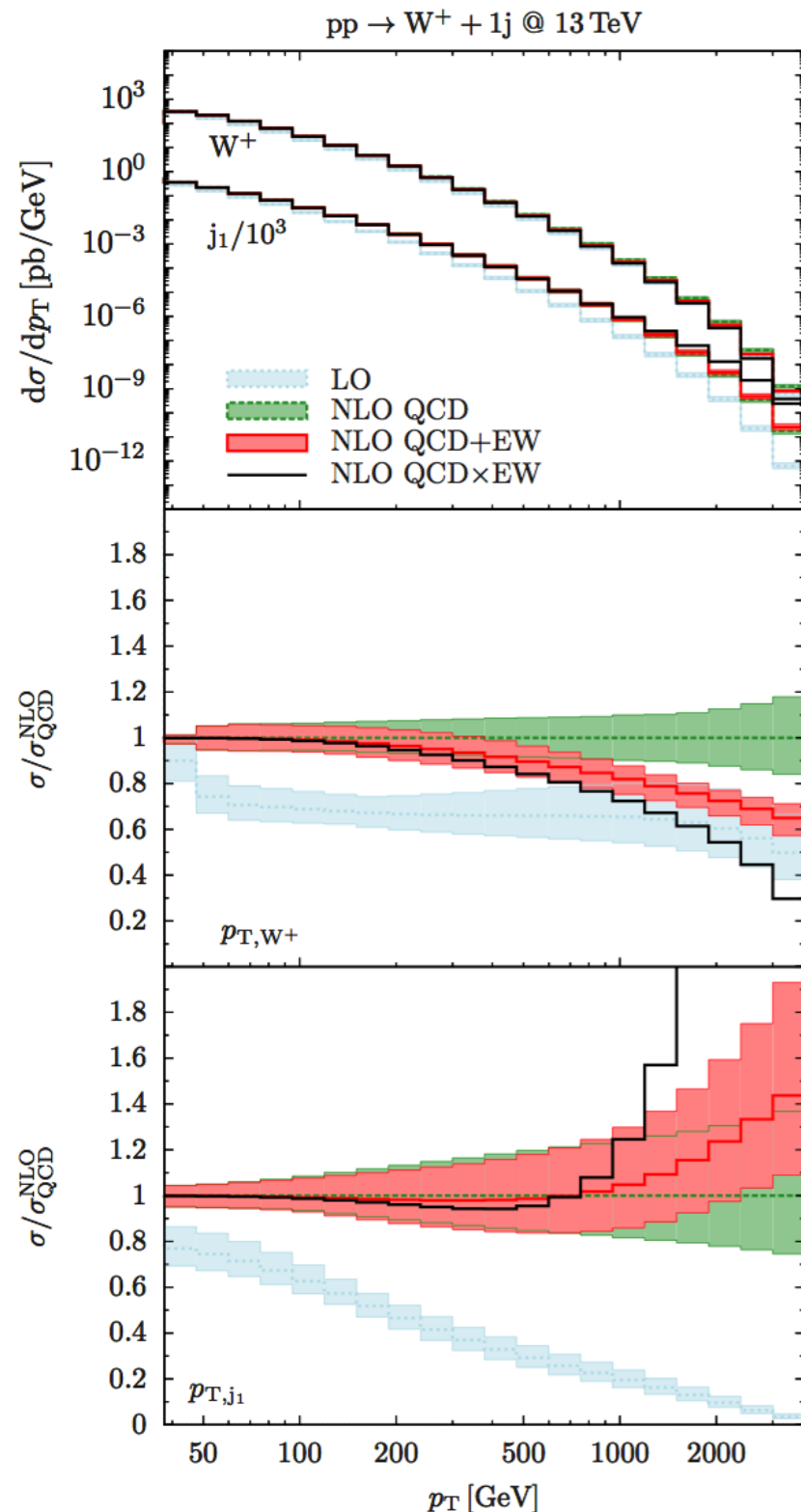
-  $t\bar{t}$ +heavy bosons

S. Frixione et al. (2015)

See also Gosam, Recola...

Progress in the computation of mixed QCD-EW  
 $O(\alpha\alpha_s)$  corrections for the Drell-Yan process: important  
for a precise  $W$  mass measurement

S.Dittmaier, A.Huss, C.Schwinn (2014)

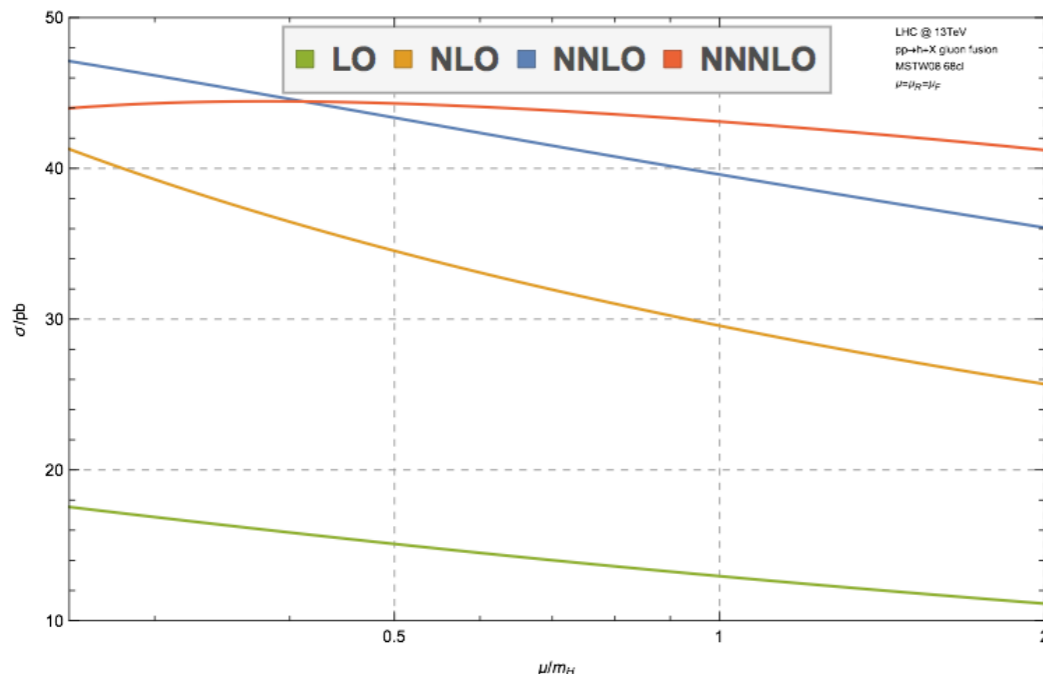




# N<sup>3</sup>LO for Higgs production

C.Anastasiou, C.Duhr, F.Dulat, F.Herzog, B.Mistlberger (2015)

Full calculation for the  $gg \rightarrow H$  completed through the evaluation of 30 terms in the soft-expansion: first complete calculation at N<sup>3</sup>LO in hadronic collisions !



Nice stabilisation of scale dependence around  $\mu=m_H/2$

$\sigma/\text{pb}$	2 TeV	7 TeV	8 TeV	13 TeV	14 TeV
$\mu = \frac{m_H}{2}$	$0.99^{+0.43\%}_{-4.65\%}$	$15.31^{+0.31\%}_{-3.08\%}$	$19.47^{+0.32\%}_{-2.99\%}$	$44.31^{+0.31\%}_{-2.64\%}$	$49.87^{+0.32\%}_{-2.61\%}$
$\mu = m_H$	$0.94^{+4.87\%}_{-7.35\%}$	$14.84^{+3.18\%}_{-5.27\%}$	$18.90^{+3.08\%}_{-5.02\%}$	$43.14^{+2.71\%}_{-4.45\%}$	$48.57^{+2.68\%}_{-4.24\%}$

results in the large  $m_{\text{top}}$  approximation

N<sup>3</sup>LO effect +2.2% at  $\mu=m_H/2$

Corresponding new results for the Higgs cross section including mass effects at NLO and the other known corrections at 13 TeV expected soon

Significant reduction of uncertainties from missing higher orders and PDF+ $\alpha_s$

Together with H+jet at NNLO will help improve predictions in jet categories

# Summary

- The first run at the LHC has been a triumph for the Standard Model, with the discovery of its last missing ingredient, the Higgs boson
- Accurate theoretical predictions are essential to further sharpen our picture of the Higgs boson and to control SM backgrounds in new physics searches
- The last 10 years have witnessed a revolution in NLO calculations that are now the standard and have reached a high level of automation
- NLO matching and merging to parton shower well established: main issue now is to properly assess uncertainties
- In the last 2 years an enormous progress in NNLO calculations has been achieved with many  $2 \rightarrow 2$  computations completed
- First NNLO+PS matched applications for Higgs and vector boson production
- The automation of NLO EW corrections is following



We are doing our best to be ready for the LHC Run 2 !

# Thanks for your attention !

Many thanks to:

*Stefano Catani , Daniel de Florian, Stefano Forte, Stefano Frixione, Thomas Gehrmann, Pier Monni, Stefano Pozzorini, Gavin Salam, Marek Schonherr*

for various useful discussions on the topics presented here....

....and apologies for having left out many important results !

Backup

# Motivations for accurate SM predictions

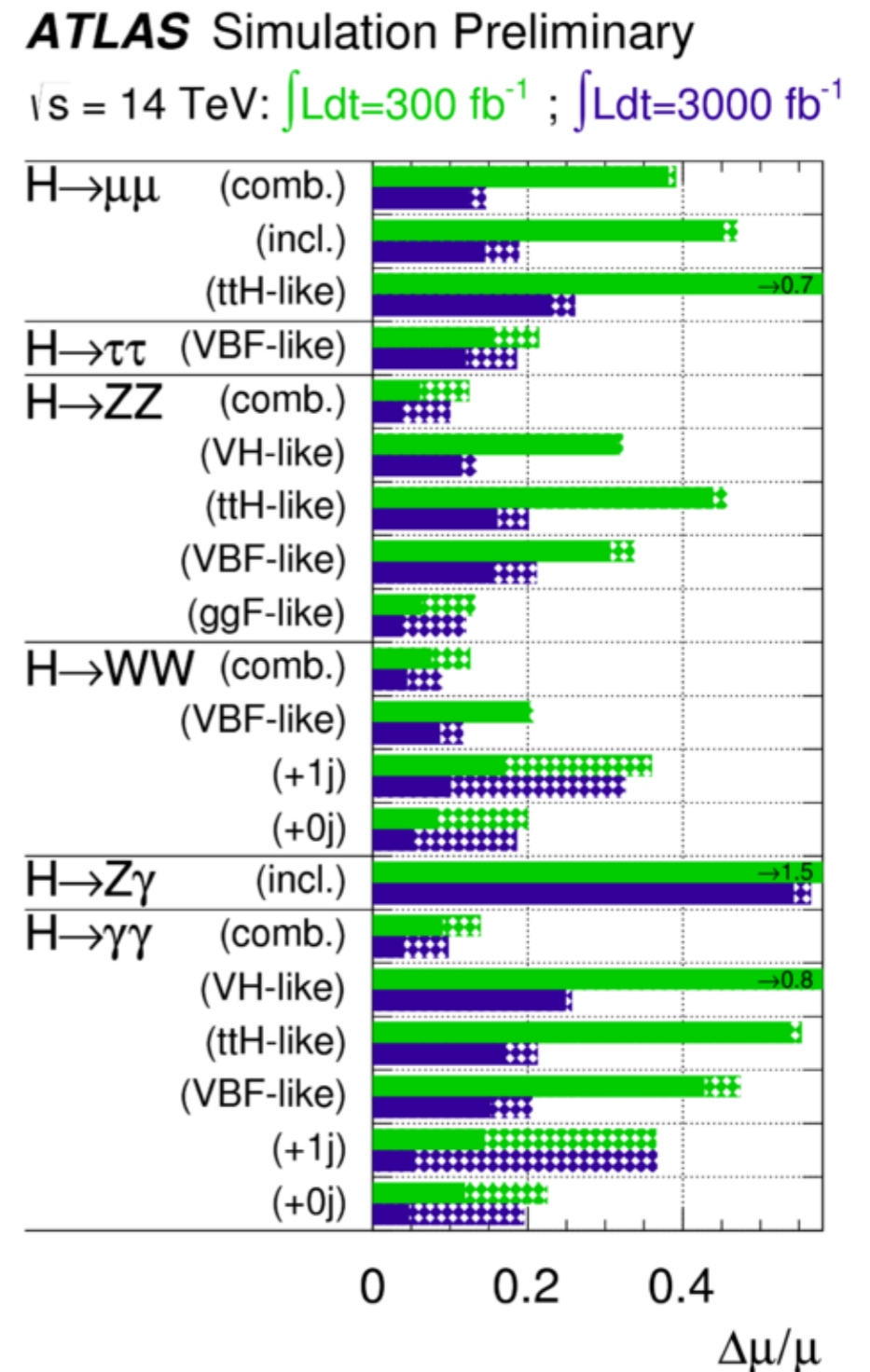
ATL-PHYS-PUB-2013-014

Estimated uncertainty on the total signal strength  $\mu$  for all Higgs final states in the different experimental categories used in the combination, assuming a SM Higgs boson with a mass of 125 GeV

Hashed areas show the impact of theory uncertainties



NNLO Les Houches 2013 wishlist includes processes with Higgs, vector bosons, heavy quarks and jets



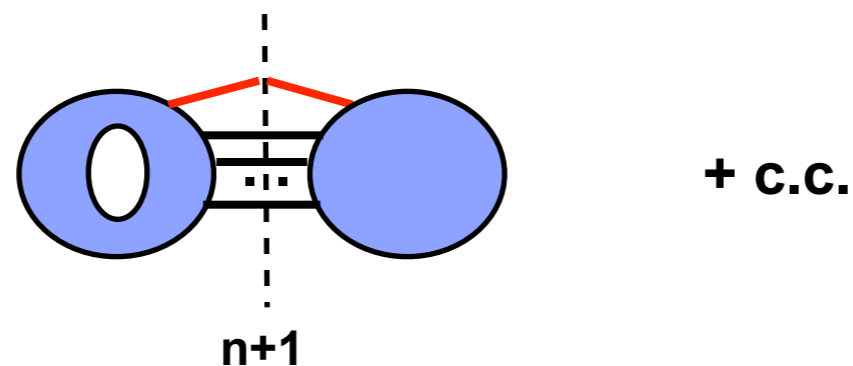
# Ingredients of NNLO calculations

Let us assume that the process involves  $n$  partons at LO  $\rightarrow$  we need:

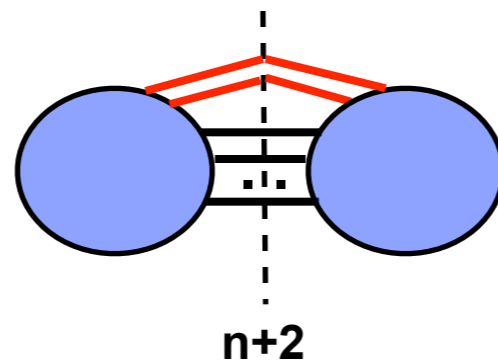
- Double virtual contribution with  $n$  resolved partons



- Real-virtual contribution with 1 unresolved parton



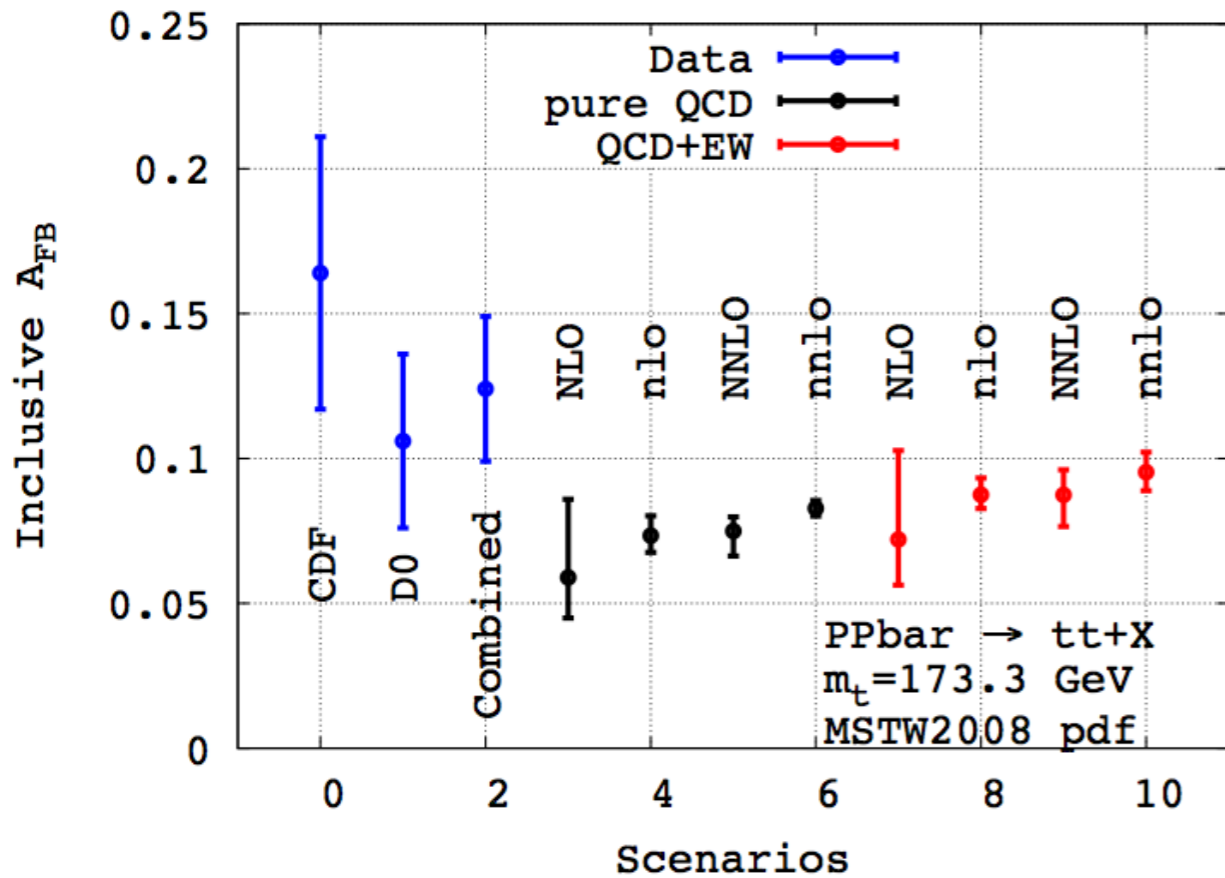
- Double-real contribution with 2 unresolved partons



All the three contributions are divergent: how can we handle IR singularities ?

# Top production at NNLO

NNLO calculation for  $t\bar{t}$  supplemented with soft-gluon resummation: residual scale uncertainties at the few % level  
(*subtraction+sector decomposition*)



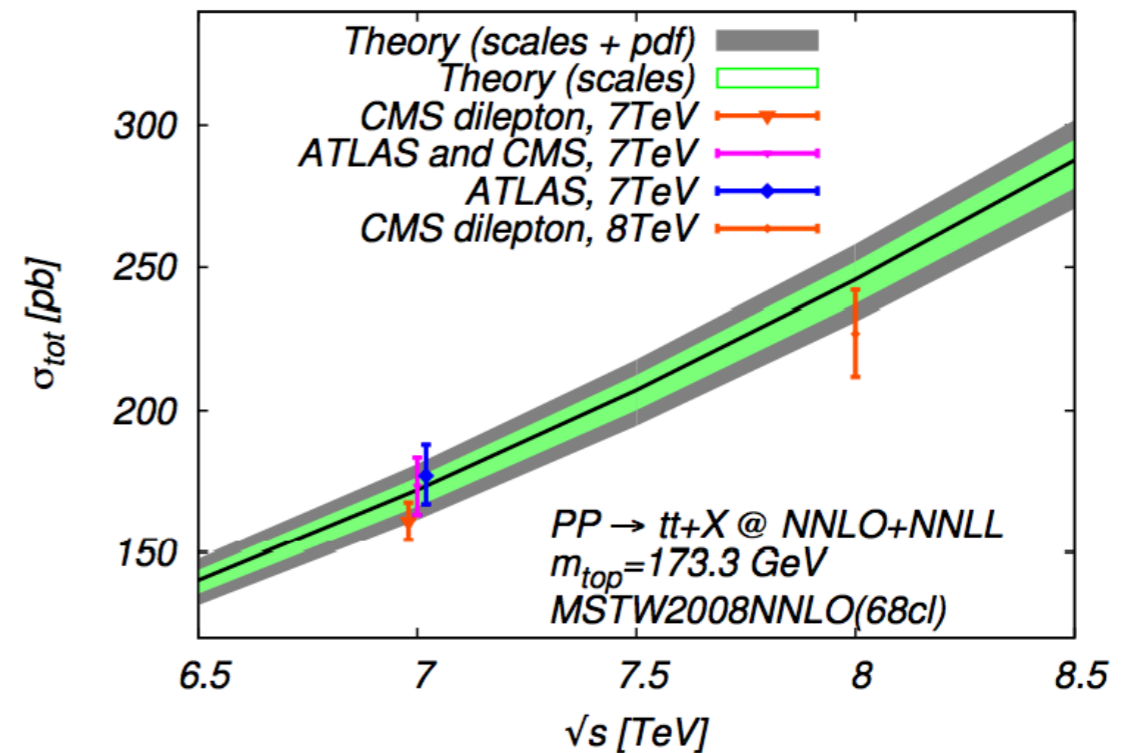
Further results expected soon

Parallel work done with antenna subtraction

A.Gehrmann et al. (2014,2015)

P.Bernreuther, M.Czakon, A.Mitov (2012)

M.Czakon, A.Mitov; M.Czakon, P.Fielder, A.Mitov (2013)



Forward-backward asymmetry at NNLO

M.Czakon, P.Fielder, A.Mitov (2014)

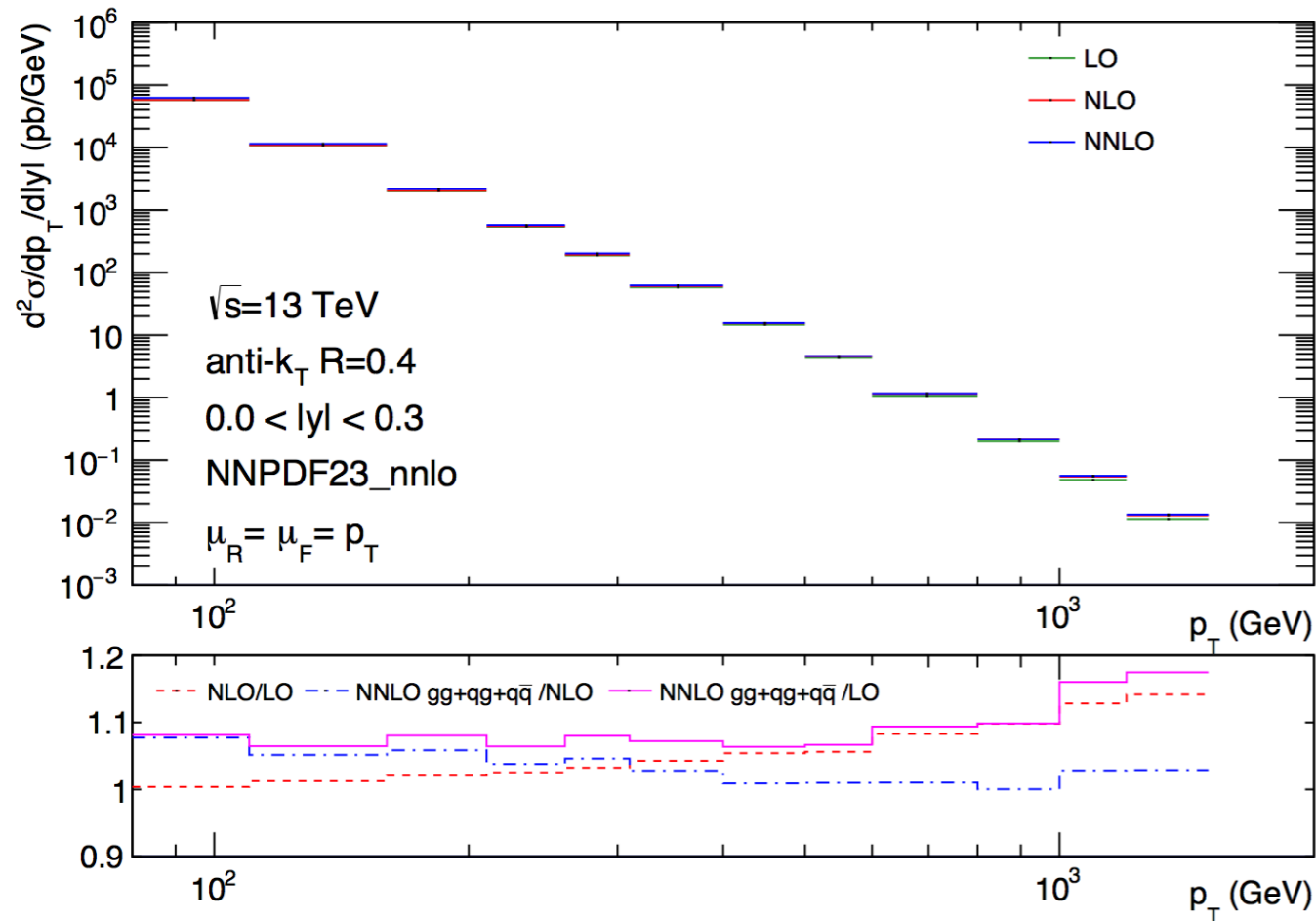
Single top

$p_{\perp}$	$\sigma_{LO}, \text{pb}$	$\sigma_{NLO}, \text{pb}$	$\delta_{NLO}$	$\sigma_{NNLO}, \text{pb}$	$\delta_{NNLO}$
0 GeV	$53.8^{+3.0}_{-4.3}$	$55.1^{+1.6}_{-0.9}$	+2.4%	$54.2^{+0.5}_{-0.2}$	-1.6%
20 GeV	$46.6^{+2.5}_{-3.7}$	$48.9^{+1.2}_{-0.5}$	+4.9%	$48.3^{+0.3}_{-0.02}$	-1.2%
40 GeV	$33.4^{+1.7}_{-2.5}$	$36.5^{+0.6}_{-0.03}$	+9.3%	$36.5^{+0.1}_{+0.1}$	-0.1%
60 GeV	$22.0^{+1.0}_{-1.5}$	$25.0^{+0.2}_{+0.3}$	+13.6%	$25.4^{+0.1}_{+0.2}$	+1.6%

M.Brucherseifer, F.Caola, K.Melnikov (2014)

# Dijets

A. & T. Gehrmann, N. Glover,  
J. Currie, J. Pires (2013, 2014)



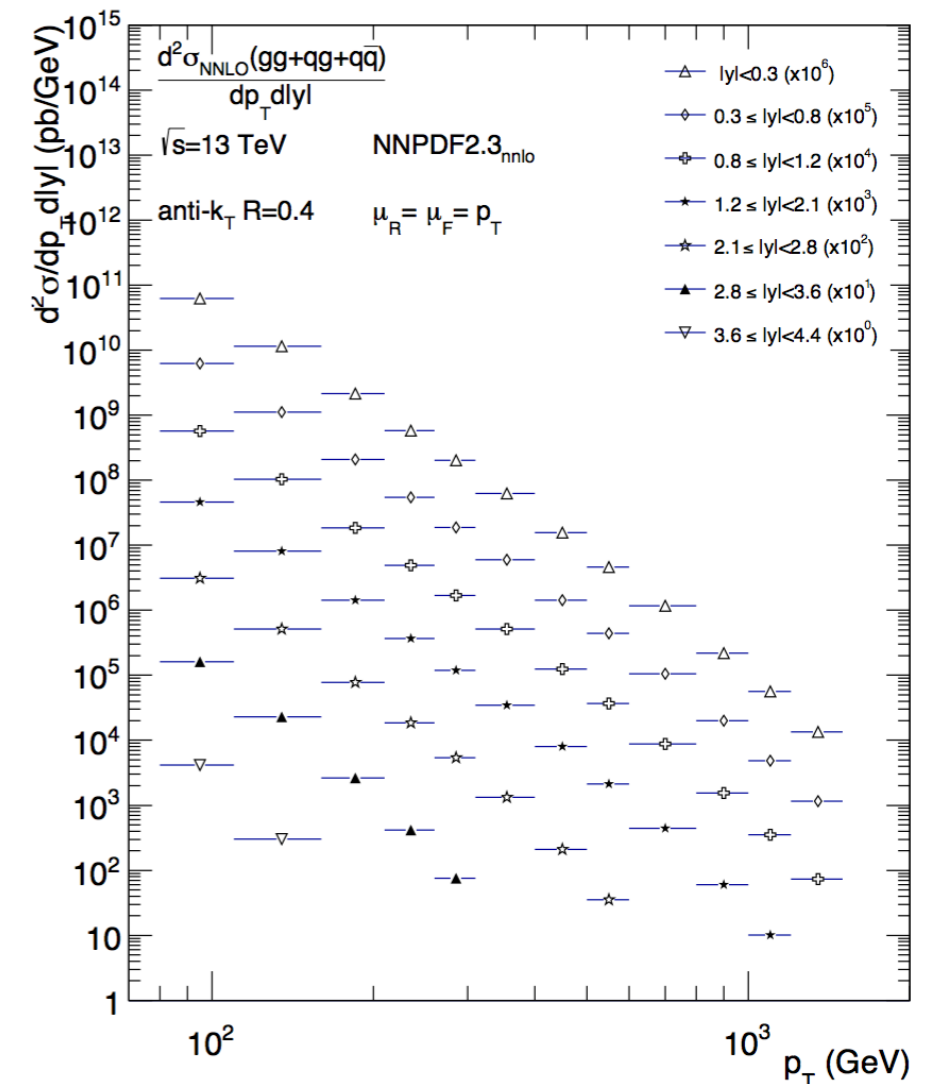
J. Currie, Radcor 2015

This should be already a good approximation for not too large jet  $p_T$

The NNLO impact seems relatively small

The qq channel becomes important at  $p_T > 1$  TeV

gg channel completed in 2013  
 new results include qg and qqbar channel at leading color





# WW at NNLO

T. Gehrmann, S. Kallweit, P. Maierhofer, A. von Manteuffel,  
S. Pozzorini, D. Rathlev, L. Tancredi, MG (2014)

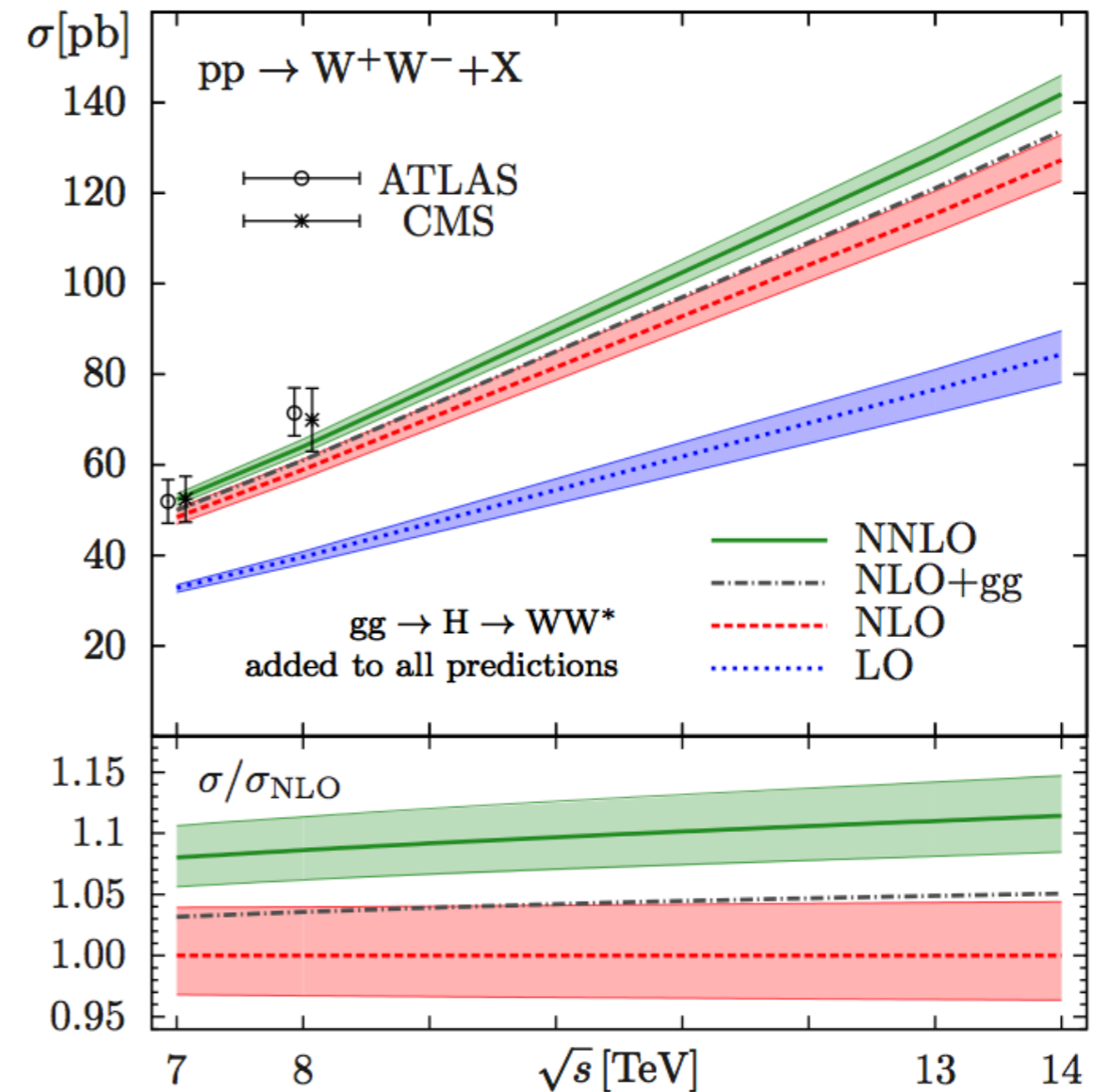
The NNLO effect in the 4FS ranges from 9 to 12 % when  $\sqrt{s}$  varies from 7 to 14 TeV

gg contribution 35% of the full NNLO effect

Comparing with 5FS with subtraction of tt and Wt contribution we find agreement at the 1(2)% level

NNLO result significantly reduces the tension with the ATLAS measurement and is in good agreement with recent result from CMS

Done with  $q_T$  subtraction +Munich+tree and one-loop amplitudes from Openloops



Scale uncertainties computed by varying  $\mu_F$  and  $\mu_R$  simultaneously and independently with  $1/2 m_W < \mu_F, \mu_R < 2m_W$  and  $1/2 < \mu_F/\mu_R < 2$

# W $\gamma$ at NNLO

S.Kallweit, D.Rathlev, MG (2015)

ATLAS cuts (arXiv:1302.1283)

photon isolation:  $\epsilon = 0.5$   
smooth cone  $R = 0.4$

+19%

$p_T^\gamma > 15$  GeV  $p_T^l > 25$  GeV  $\Delta R(l, \gamma) > 0.3$

$|\eta^\gamma| < 2.37$   $|\eta^l| < 2.47$   $\Delta R(l, \gamma) > 0.7$

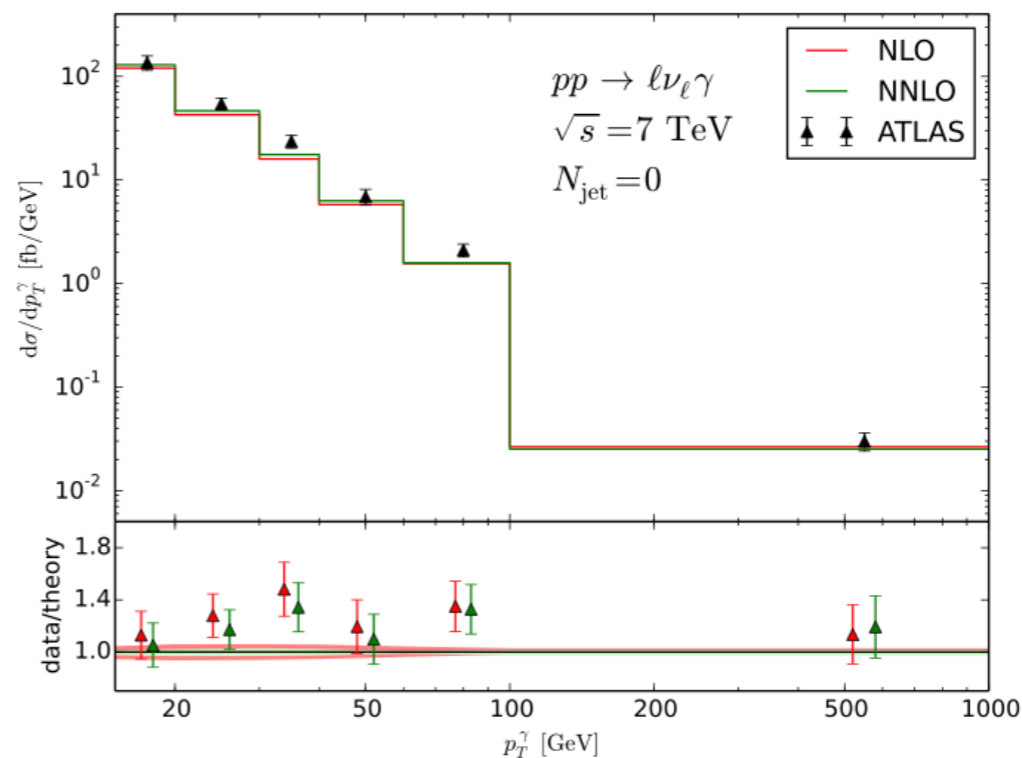
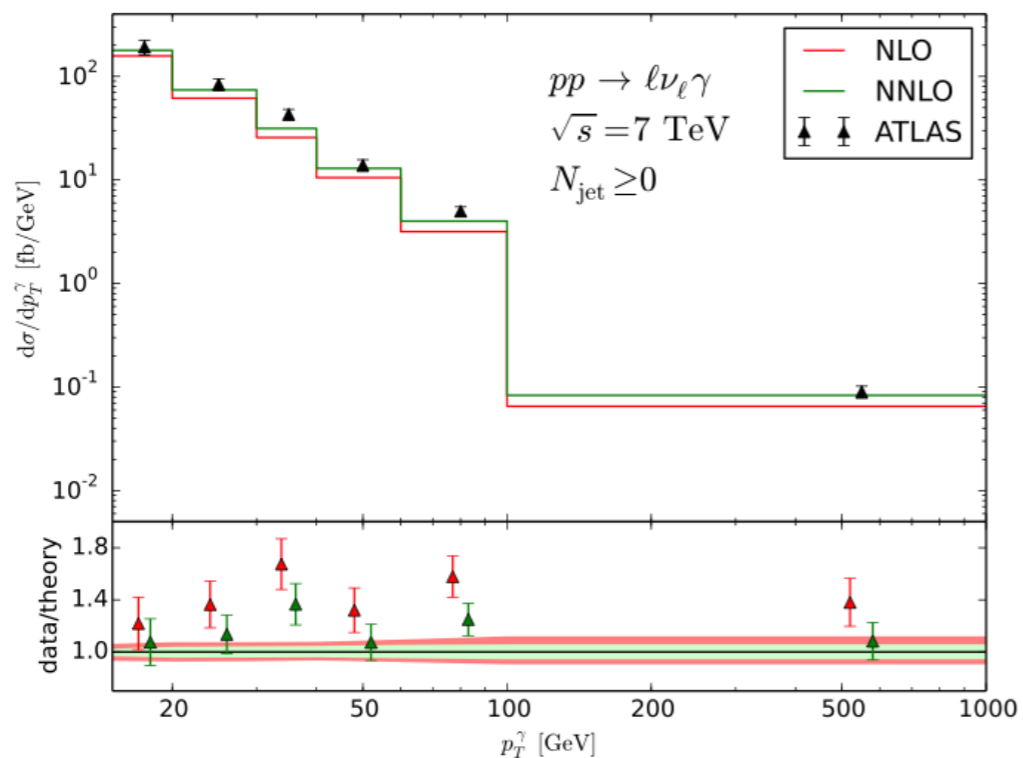
$p_T^{\text{miss}} > 35$  GeV jets: anti-kt with  $D=0.4$

$p_T^{\text{jet}} > 15$  GeV  $|\eta^{\text{jet}}| < 2.47$

$N_{\text{jet}} \geq 0$

$N_{\text{jet}} = 0$

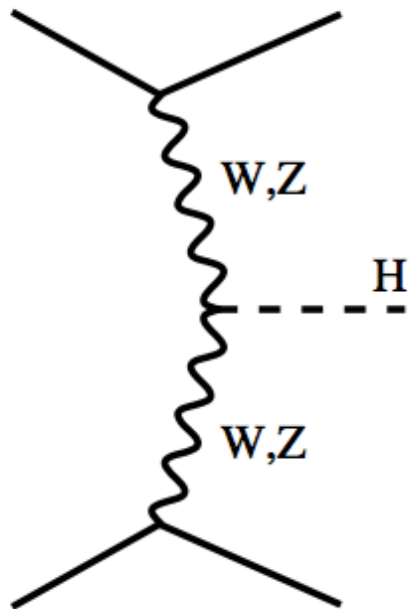
$\sigma_{\text{NLO}}$ [pb]	$\sigma_{\text{NNLO}}$ [pb]	$\sigma_{\text{ATLAS}}$ [pb]
$2.058^{+6.8\%}_{-6.8\%}$	$2.453^{+4.1\%}_{-4.1\%}$	$2.77 \pm 0.03$ (stat) $\pm 0.33$ (syst) $\pm 0.14$ (lumi)
$1.395^{+5.2\%}_{-5.8\%}$	$1.493^{+1.7\%}_{-2.7\%}$	$1.76 \pm 0.03$ (stat) $\pm 0.21$ (syst) $\pm 0.08$ (lumi)



$q_T$  subtraction + Munich+tree and one-loop amplitudes from Openloops

# VBF Higgs production

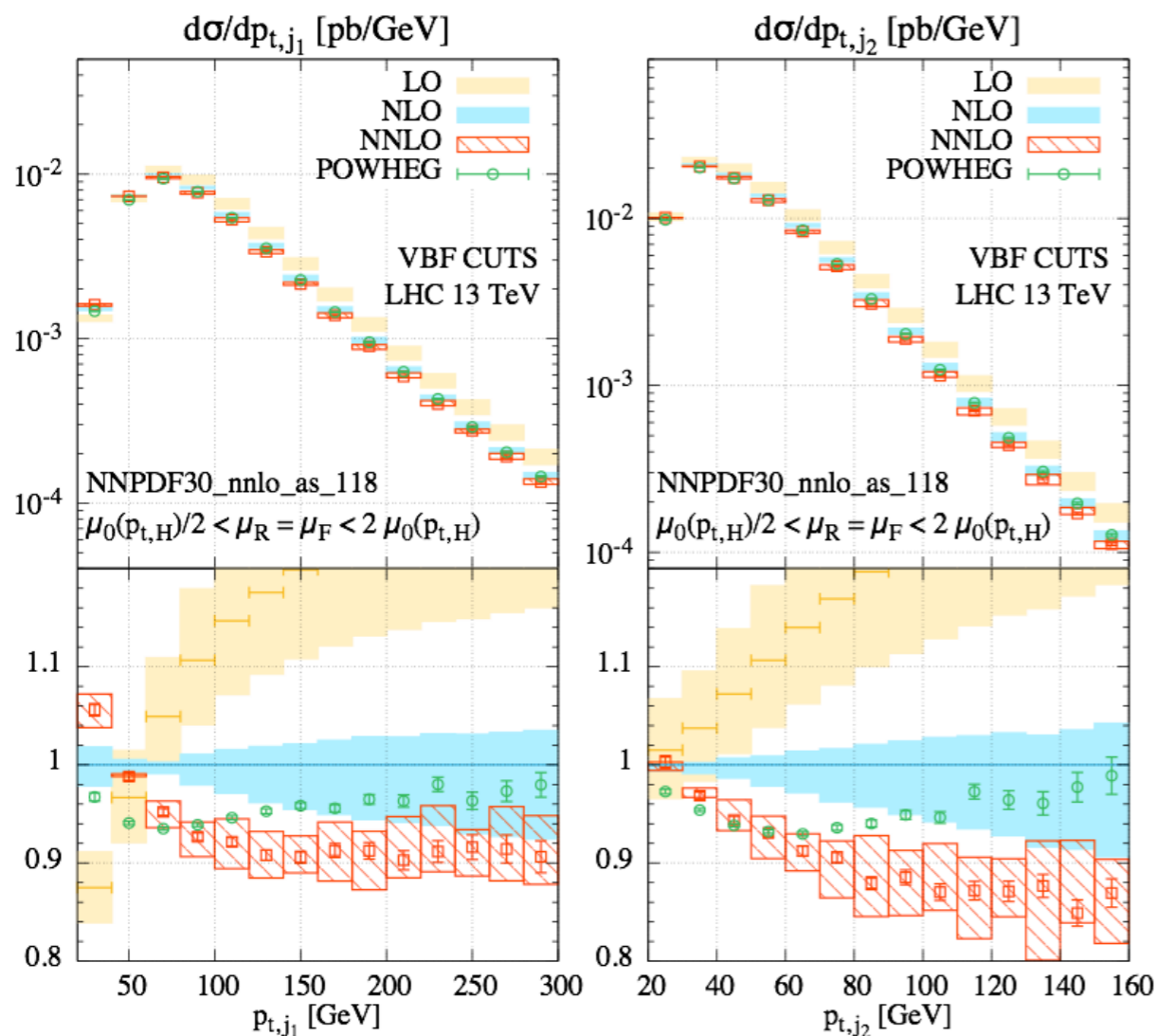
M.Cacciari, F.Dreyer, A.Karlberg, G.Salam, G.Zanderighi (2015)



Vector boson fusion (VBF) is an important production channel for the Higgs boson: distinctive signature with little jet activity in the central rapidity region

Fully inclusive NNLO corrections known since quite some time in the structure function approach:  $O(1\%)$  effect

P.Bolzoni, F.Maltoni, S.Moch, M.Zaro (2010)



Fully exclusive NNLO computation recently completed (still neglecting color exchanges between quark lines)

NNLO corrections make  $p_T$  spectra softer  $\rightarrow$  larger impact when VBF cuts are applied

	$\sigma^{(\text{no cuts})}$ [pb]	$\sigma^{(\text{VBF cuts})}$ [pb]
LO	$4.032^{+0.057}_{-0.069}$	$0.957^{+0.066}_{-0.059}$
NLO	$3.929^{+0.024}_{-0.023}$	$0.876^{+0.008}_{-0.018}$
NNLO	$3.888^{+0.016}_{-0.012}$	$0.826^{+0.013}_{-0.014}$

-1%

-6%