

ERL designs based on FFAG arcs (eRHIC, LHeC, Cornell)

Dejan Trbojevic

Abstract.

*The future Electron Ion Collider (EIC) LHeC will be able to collide electrons with protons/ions. Electron acceleration is based on a concept of Energy Recovery Linacs (ERL) with maximum energies of 60 GeV and almost completely recovering the energy during deceleration to the initial energy. We present: eRHIC, an ERL for LHeC (an example **with almost double reduction in size of the linac**, from 2×10 GeV to 2×5.345 GeV) from the present solution, using two Non-Scaling Fixed Field Alternating Gradient beam lines. This **would reduce the three beam lines to two, and** raise the luminosity for 34% from the electron current of 6.6 mA to 8.9 mA, for the synchrotron radiation limit of 15 MW.*

OUTLINE

**Electron Ion Colliders
eRHIC and LHeC**

**NS-FFAG: Introduction
to the concept**

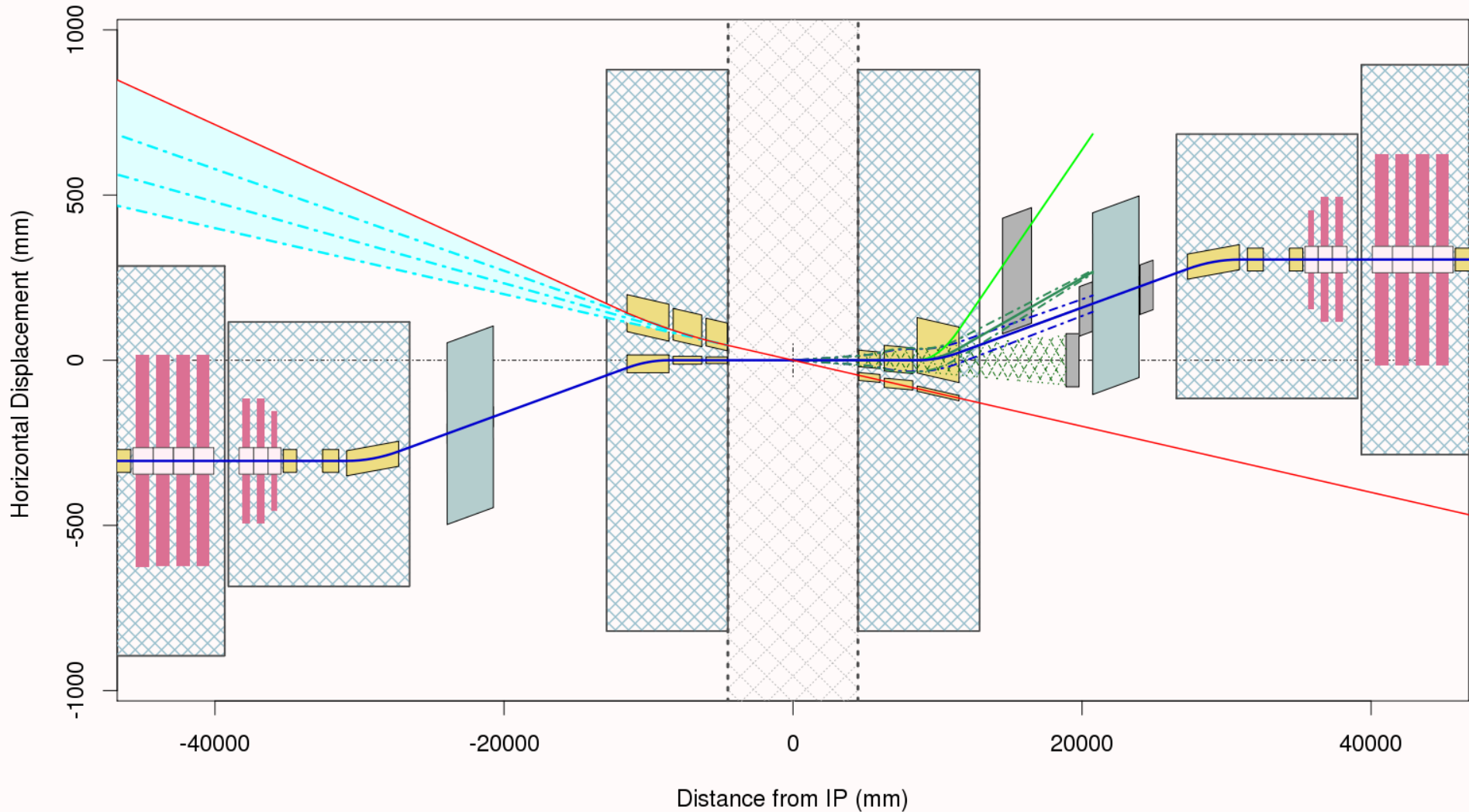
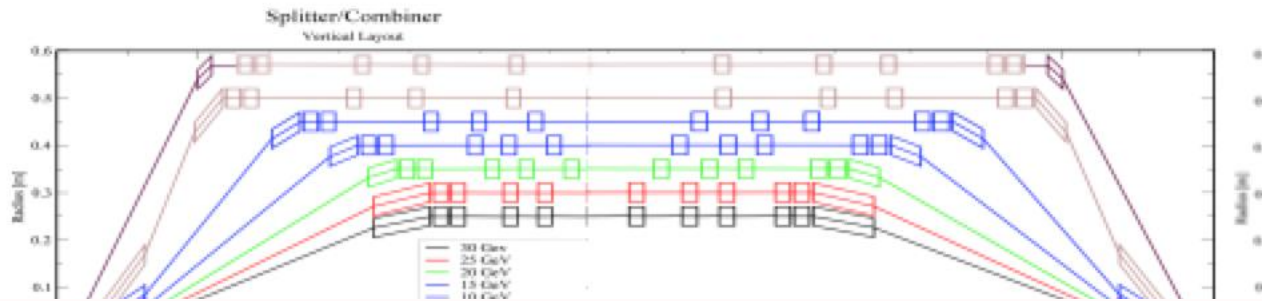
**Lattice examples of the
eRHIC and ERL LHeC**

SUMMARY:

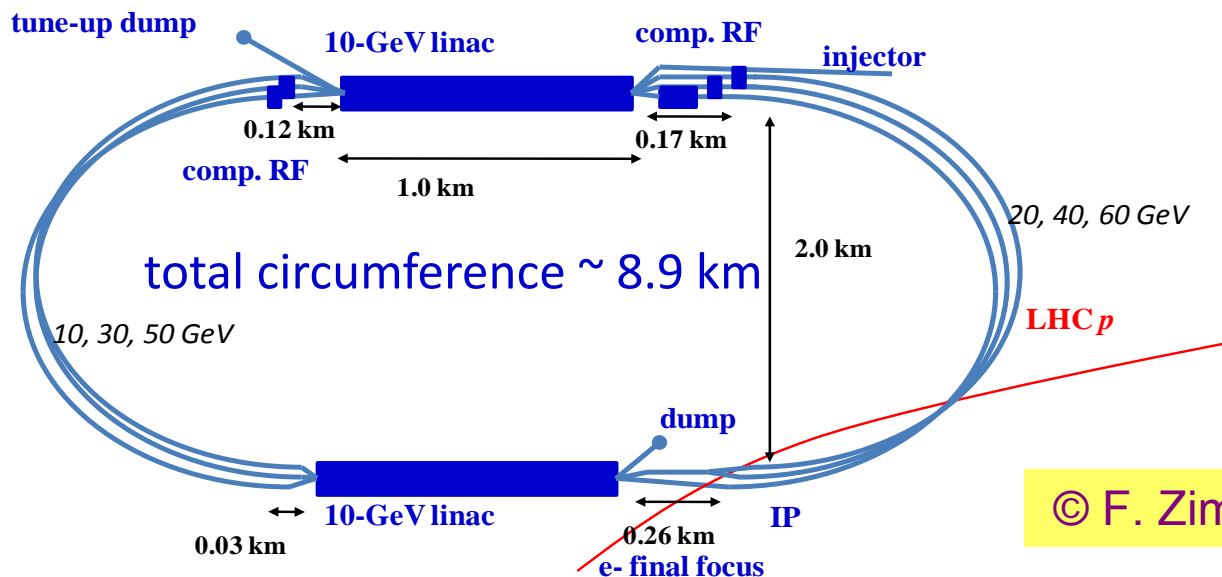
Advantages come from multiple passes through the linac bring reduction in the linac size and of three beam circulating lines to two, reducing the synchrotron radiation – raising 42% the luminosity

Layout

FFAG Recirculating



Linac-Ring Option – LHeC Recirculator



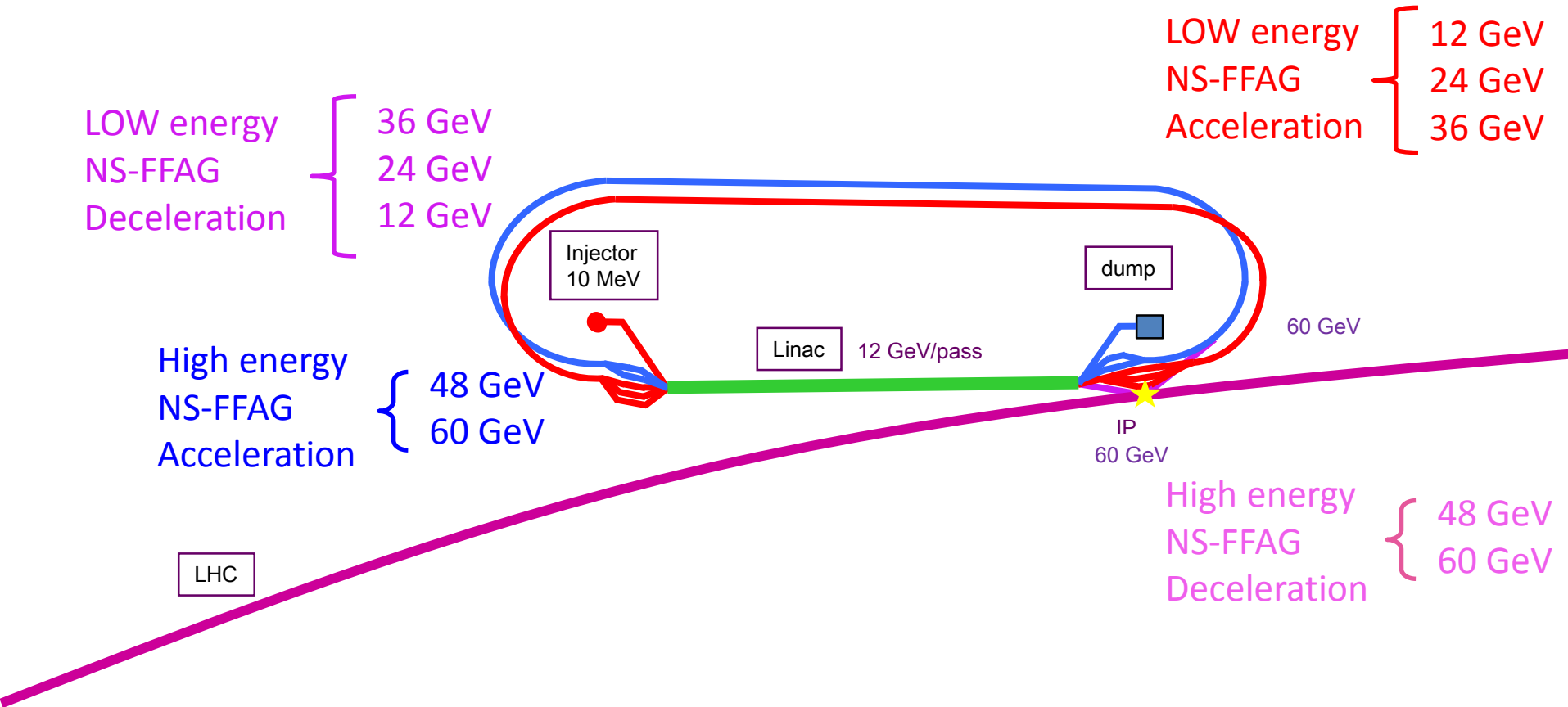
RECIRCULATOR COMPLEX

1. 0.5 GeV injector
2. Two SCRF linacs (10 GeV per pass)
3. Six 180° arcs, each arc 1 km radius
4. Re-accelerating stations
5. Switching stations
6. Matching optics
7. Extraction dump at 0.5 GeV

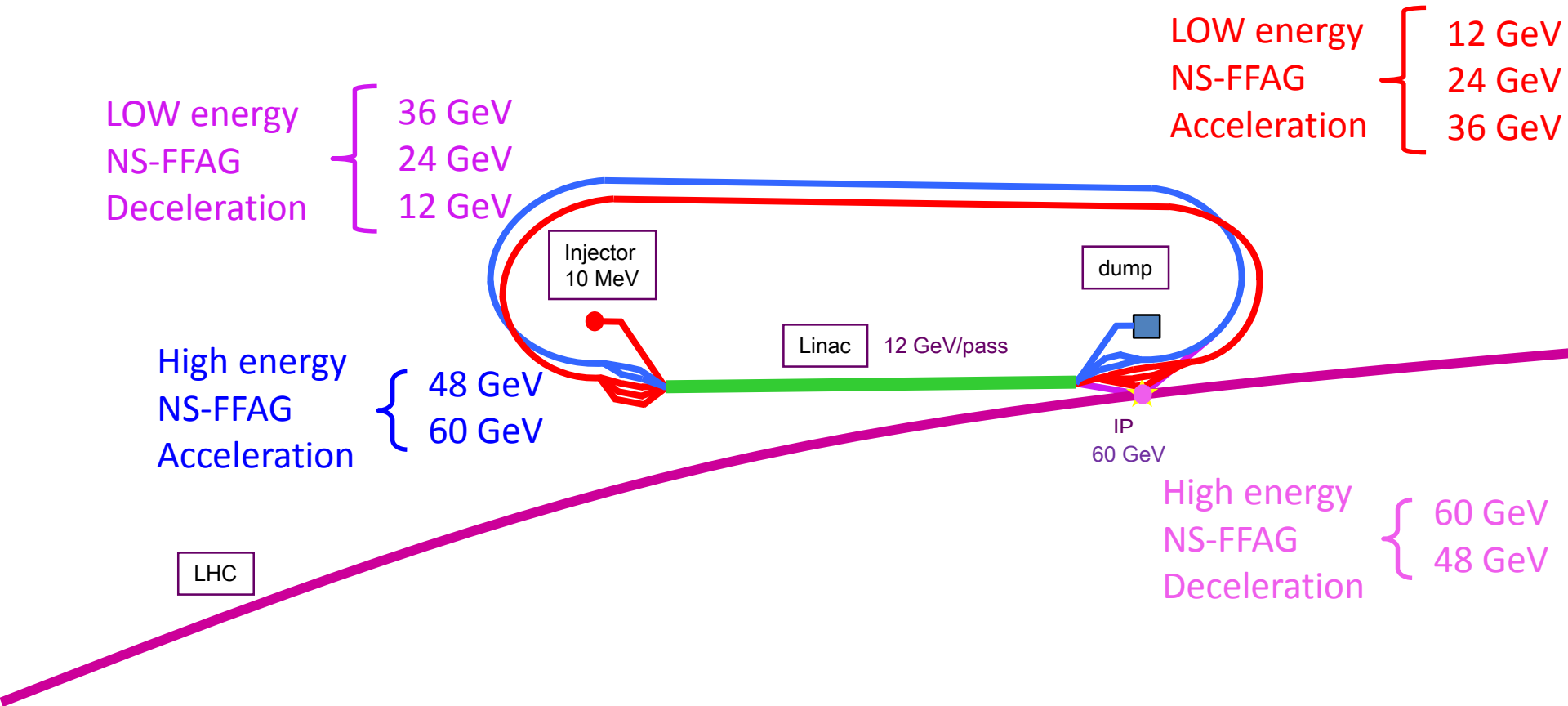
	PROTONS	ELECTRONS
Beam Energy [GeV]	7000	60
Luminosity [$10^{33} \text{cm}^{-2}\text{s}^{-1}$]	1	1
Normalized emittance $\nu\epsilon_{x,y}$ [μm]	3.75	50
Beta Function $\beta_{x,y}^*$ [m]	0.10	0.12
rms Beam size $\sigma_{x,y}^*$ [μm]	7	7
rms Divergence $\sigma'_{x,y}$ [μrad]	70	58
Beam Current [mA]	(860) 430	6.6
Bunch Spacing [ns]	25 (50)	25 (50)
Bunch Population	$1.7 \cdot 10^{11}$	$(1 \cdot 10^9) 2 \cdot 10^9$

The baseline 60 GeV ERL option proposed can give an e-p luminosity of $10^{33} \text{cm}^{-2}\text{s}^{-1}$ (extensions to $10^{34} \text{cm}^{-2}\text{s}^{-1}$ and beyond are being considered)

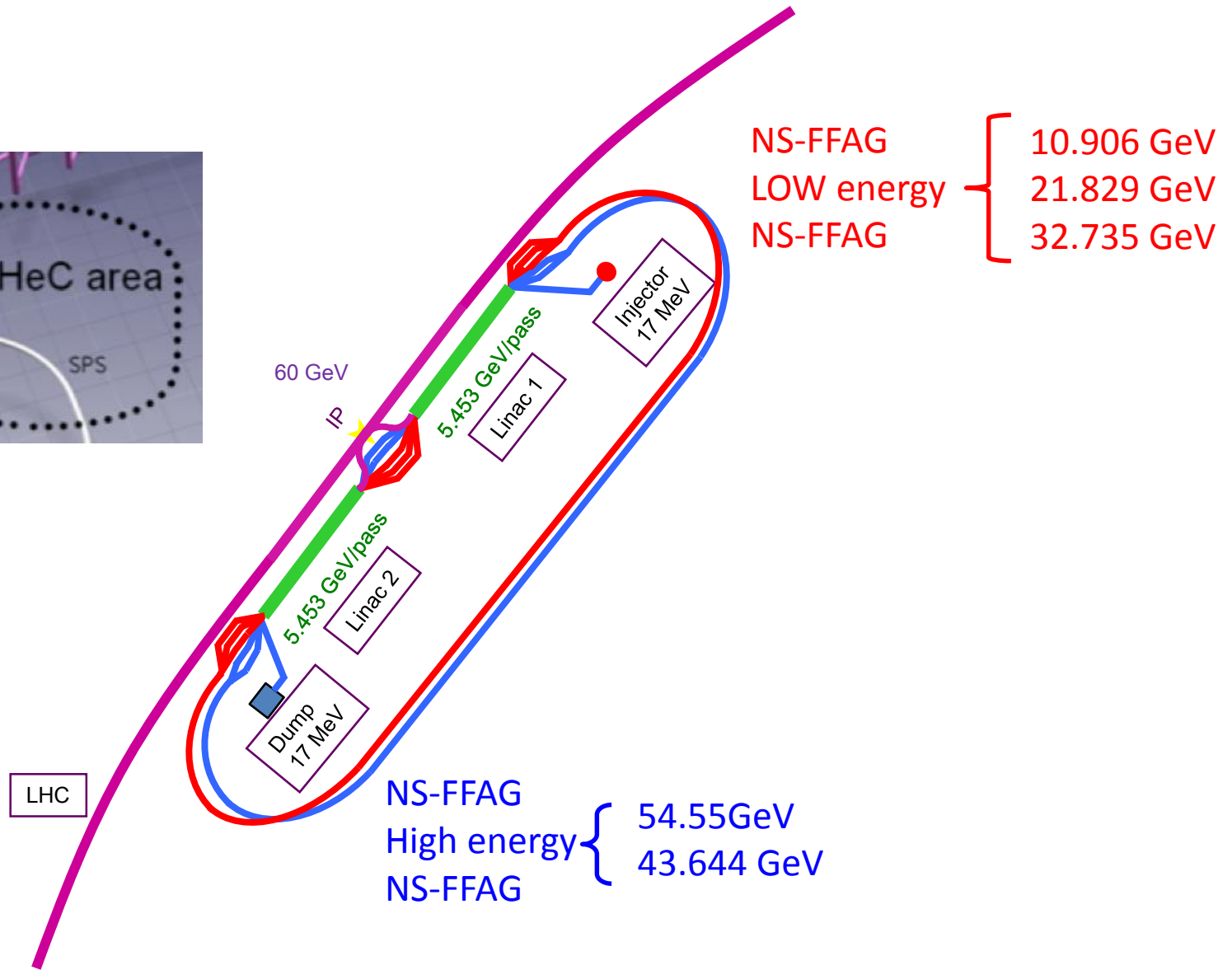
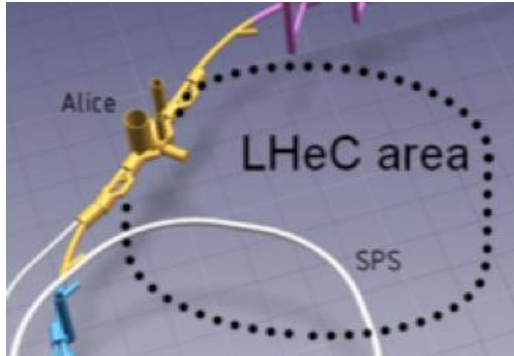
NS-FFAG LHeC Recirculator with 12 GeV ER



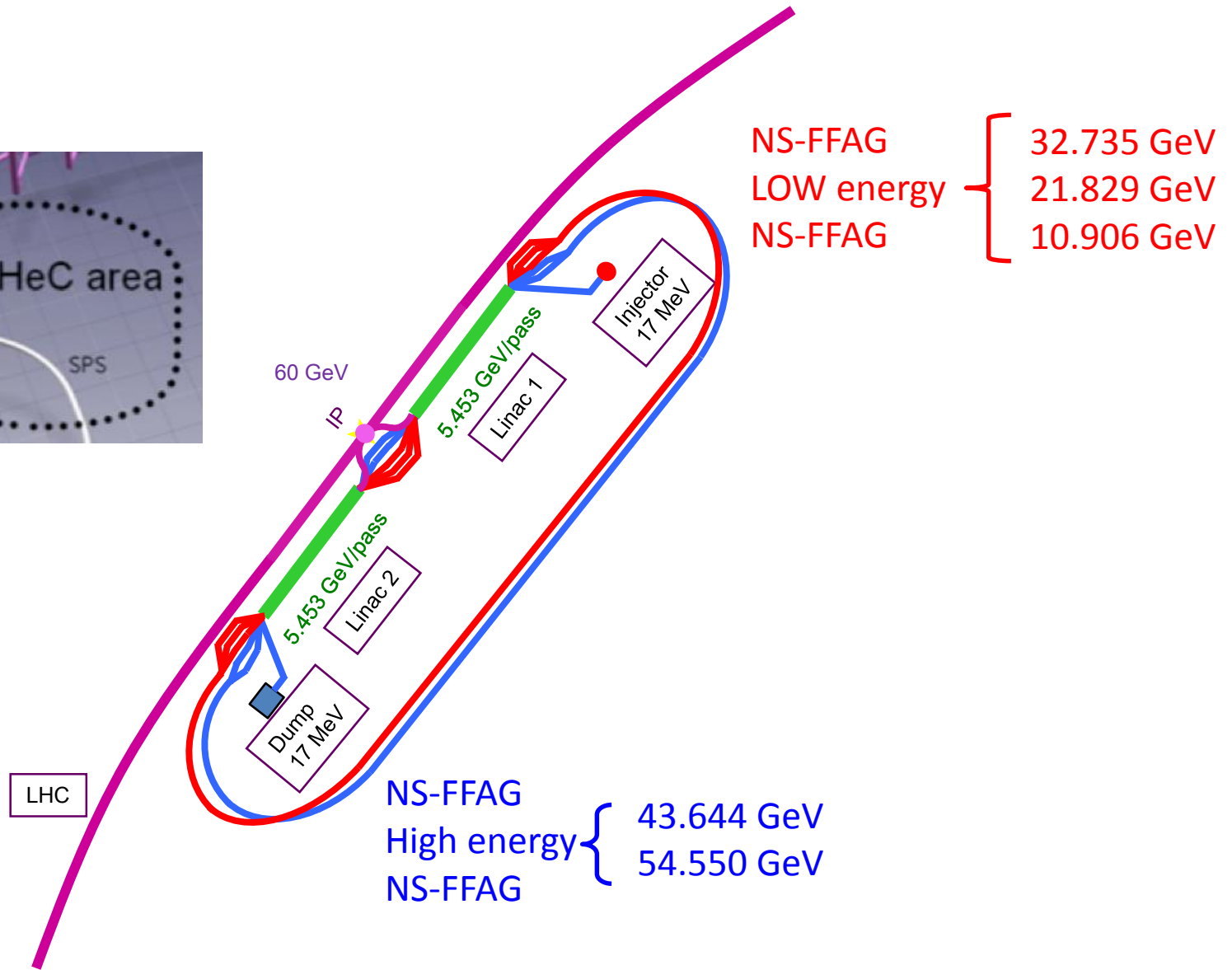
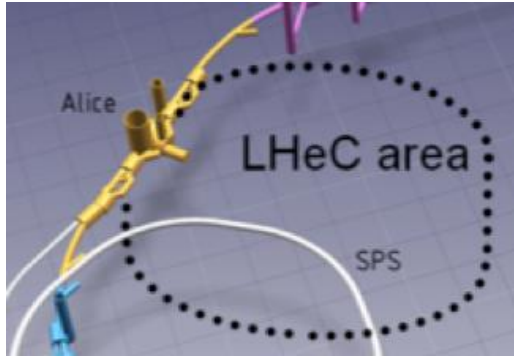
NS-FFAG LHeC Recirculator with 12 GeV ER



NS-FFAG LHeC Recirculator with ER



NS-FFAG LHeC Recirculator with ER



WHAT IS Non-Scaling FFAG?

OUTLINE: NS-FFAG for eRHIC and LHeC

Orbits in NS-FFAG cells

Tune dependence on
momentum

Path length dependence
on energy

Straight section design

By pass design

The AGS NS-

match the degraded
alternating A and B
the field which, ac
1 1/2 strong focuss
reverse the dispers
ly cancel it.

$$\delta p/p = -55, 25 \%$$

NIM 179(1981) 95-103

TRIUMF Vancouver π - μ channel

D. Trbojevic, E.D. Courant, and A. A. Garren

Fall 1999, "FFAG Lattice Without Opposite Bends",

HEMC'99 Workshop, $\delta p/p = -30, 50 \%$

HISTOGRAM NO 9
DISTRIBUTION OF DE/F

3 M FROM THE TARGET

TOR.. 100 X'S EQUAL 272 ENTRIES

INTERVAL

INTERVAL	NUMBER OF ENTRIES
LESS THAN -75.000	0
-75.000 TO -65.000	0
-65.000 TO -55.000	0
-55.000 TO -45.000	0
-45.000 TO -35.000	0
-35.000 TO -25.000	0
-25.000 TO -15.000	0
-15.000 TO -5.000	0
-5.000 TO 5.000	0
5.000 TO 15.000	0
15.000 TO 25.000	0
25.000 TO 35.000	0
35.000 TO 45.000	0
45.000 TO 55.000	0
55.000 TO 65.000	0
65.000 TO 75.000	0
GREATER THAN 75.000	0

$$\delta p/p = -55, -45\%$$

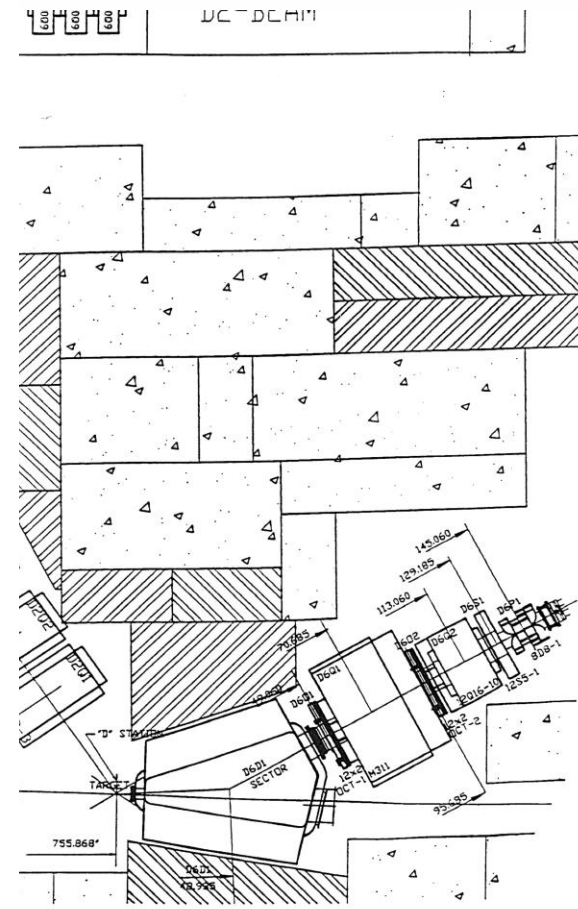
$$\delta p/p = -15, -25\%$$

$$\delta p/p = -5, -5\%$$

Ion Channel

"channel" set of
sets was tuned for
JRTLE, would produce
channel. This will
D2 will approximate-

TOTAL NUMBER OF ENTRIES = 1245 INCLUDING UNDERFLOW AND OVERFLOW
CENTER = -13.049 RMS HALF WIDTH = 20.066



Low energy cell (N=160.1888 cells per arc), $L_{\text{CELL}}=2.2242$ m

$B_{F_{\text{max,min}}}=[0.1211, -0.1744]$ T

$B_D=0.05941$,

$B_{D_{\text{max,min}}}=[0.0047, 0.2442]$ T

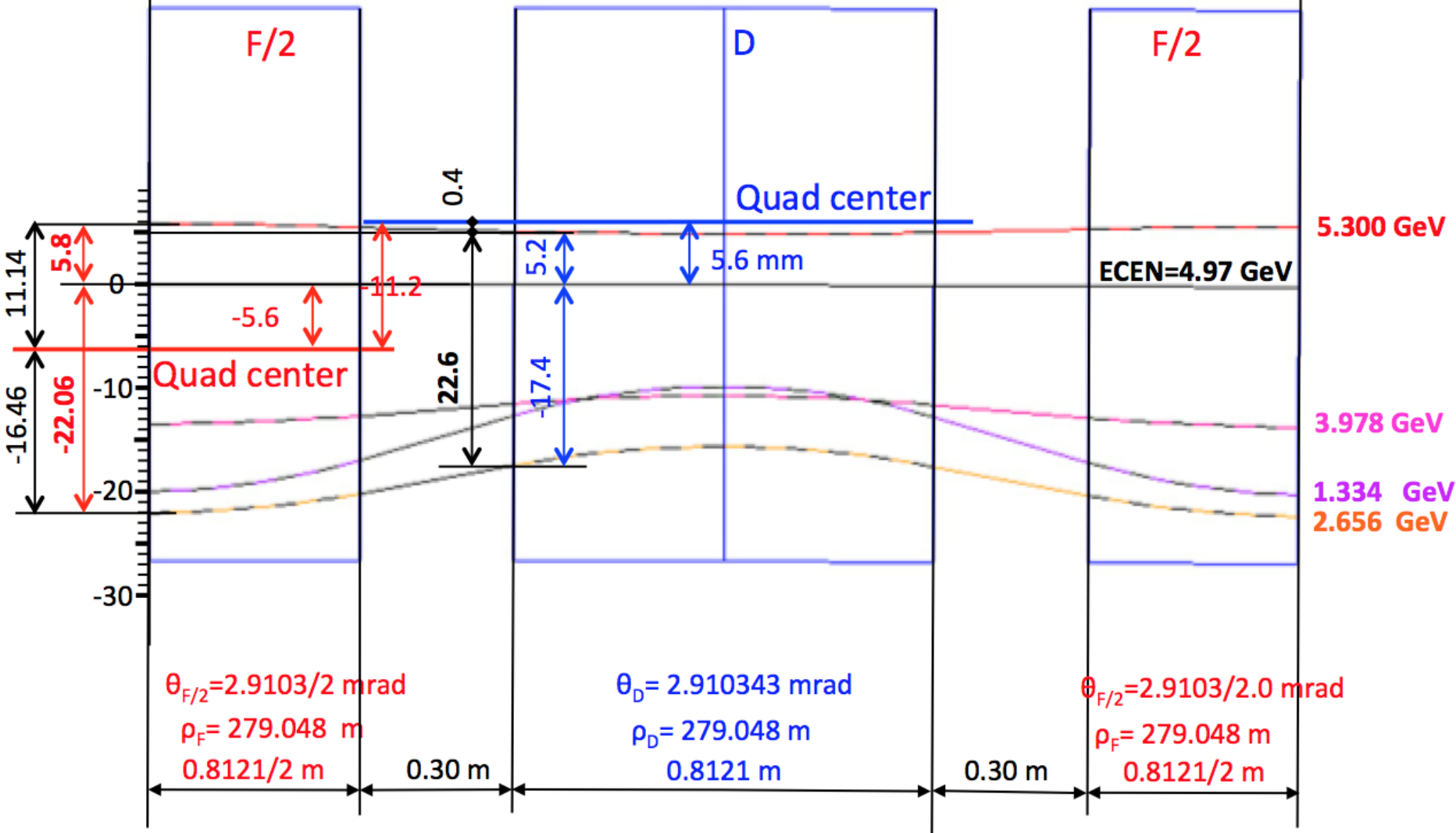
$B_f=0.05941$ T,

$G_d=-10.6$ T/m

$G_f=10.6$ T/m $x_{\text{Offset}}=-5.6$ mm

$x_{\text{Offset}}=+5.6$ mm

x(mm)



nature physics

MARCH 2012 VOL 8 NO 3
www.nature.com/naturephysics

POLARITONS
A quantum pendulum

SPACE WEATHER
Disappearing act revealed

CORRELATED FERMIONS
Transport out of equilibrium

**Acceleration
without scaling**

6.622 – 15.876 GeV

Energy

#1	1.334 GeV
#2	2.565 GeV
#3	3.978 GeV
#4	5.300 GeV

Option #2 Energy

10 mA

Linac 1.322 GeV

#1 6.622 GeV

#2 7.944 GeV

#3 9.266 GeV

#4 10.588 GeV

#5 11.910 GeV

#6 13.232 GeV

#7 14.554 GeV

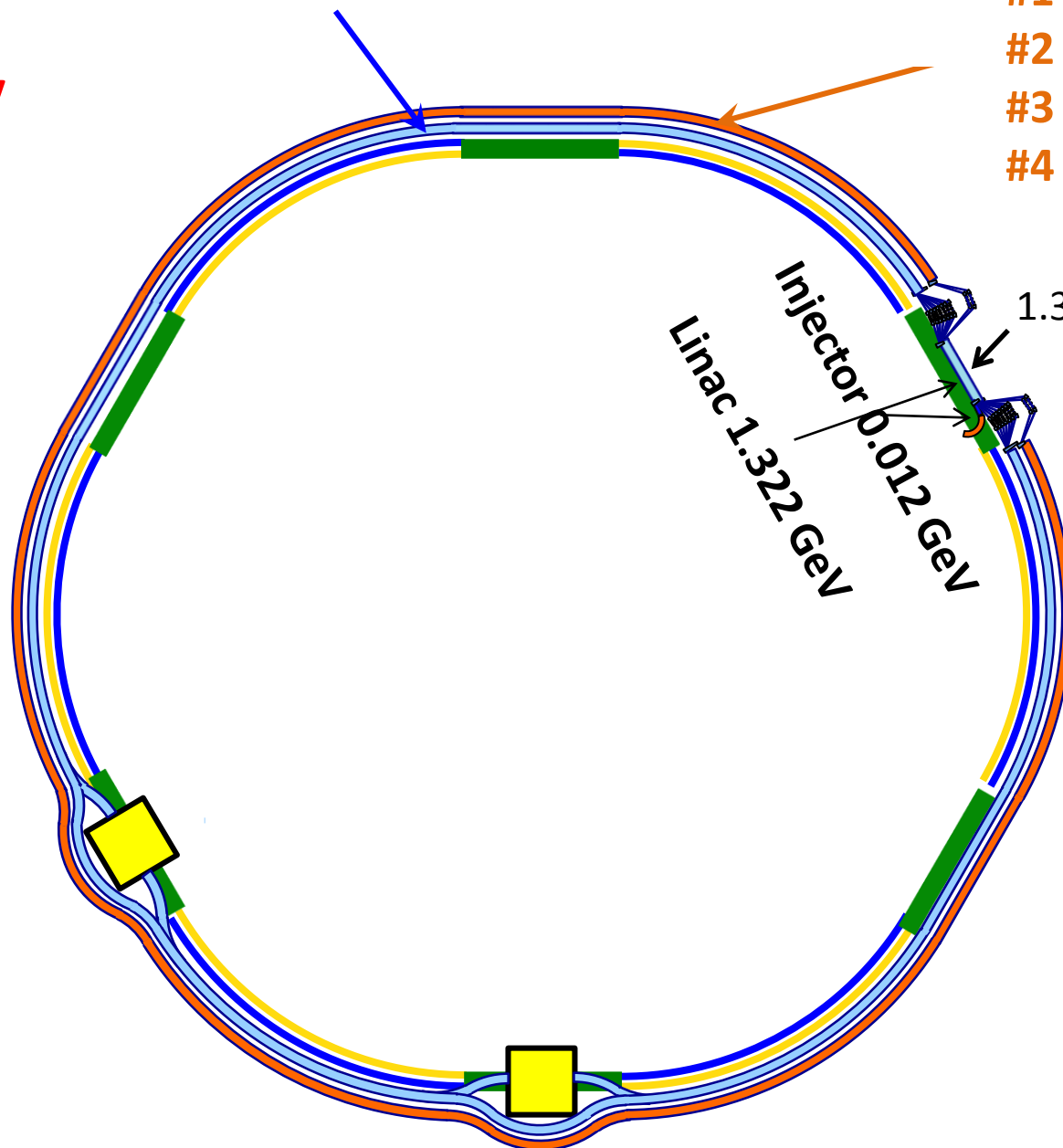
#8 15.876 GeV

#9 17.198 GeV

#10 18.520 GeV

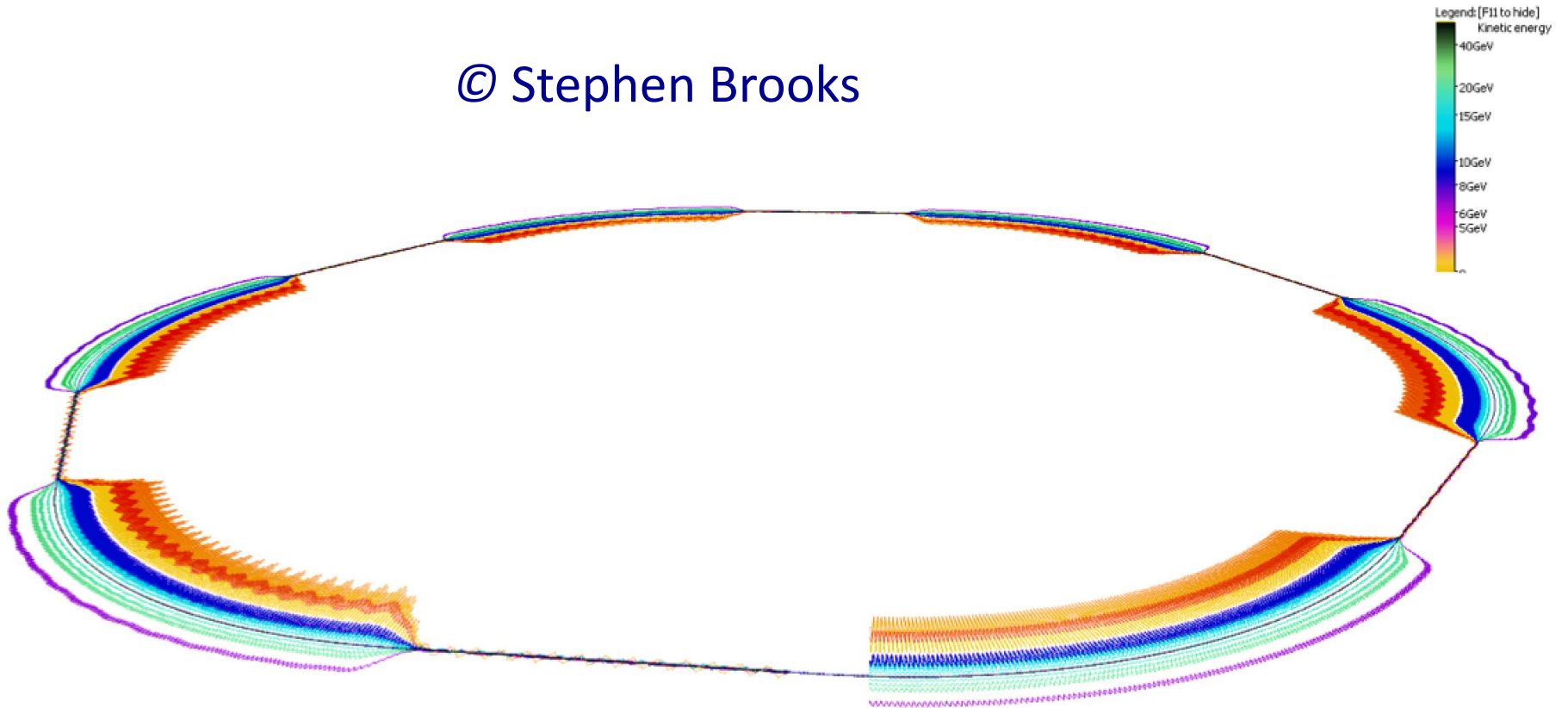
#11 19.842 GeV

#12 21.164 GeV

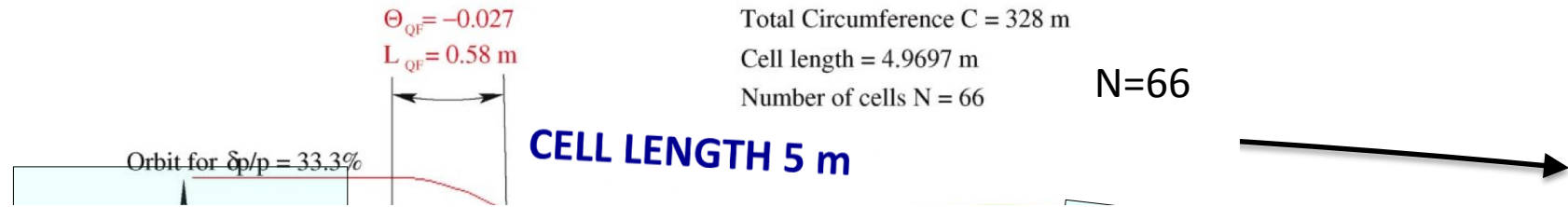


eRHIC FFAG Rings in Perspective

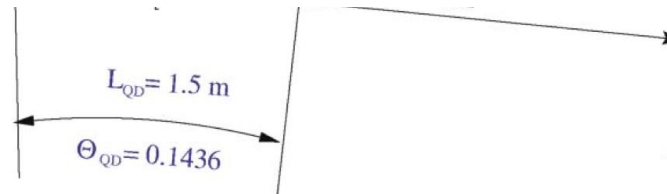
© Stephen Brooks



Non-scaling FFAG for Muon Acceleration



- Extremely strong focusing with a small dispersion function
- Tunes vary
- Orbit offsets are small
- Magnets are small
- Large energy acceptance



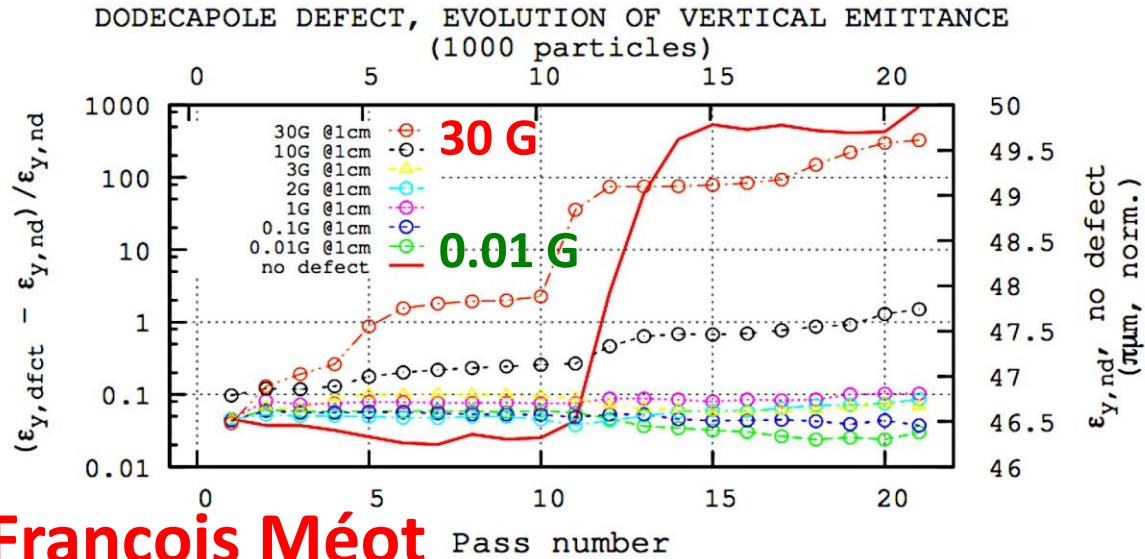
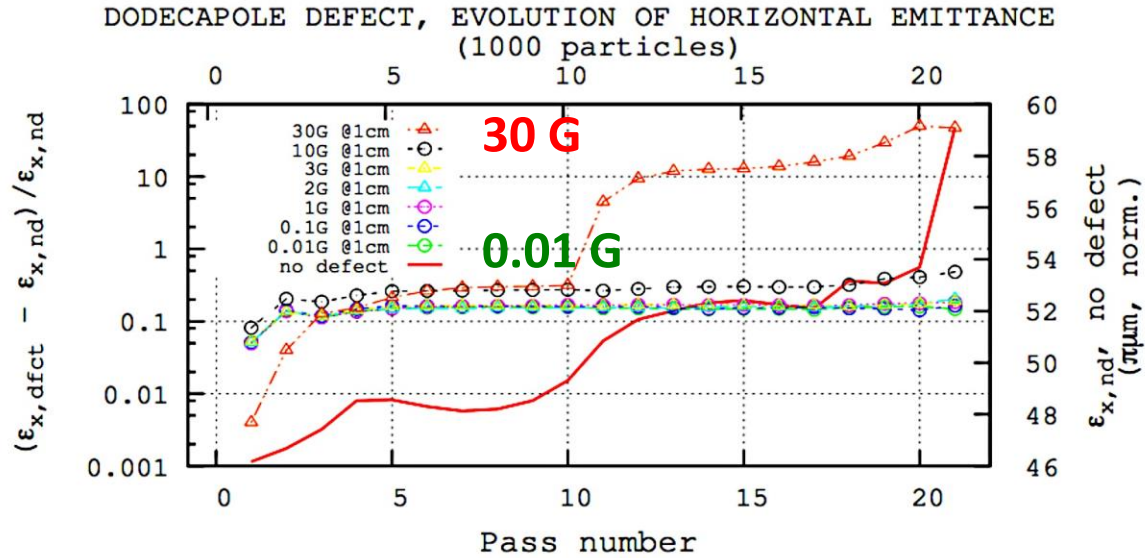
PHYSICAL REVIEW SPECIAL TOPICS - ACCELERATORS AND BEAMS 8, 050101 (2005)

Design of a nonscaling fixed field alternating gradient accelerator

D. Trbojevic,* E. D. Courant, and M. Blaskiewicz
BNL, Upton, New York 11973, USA

Dejan Trbojevic, Workshop on the LHeC, June 24-26, 2015

Defect value, following from prior study of emittance growth over single ring turn : ± 3 Gauss at 1 cm



François Méot Pass number

The prototype of eRHIC will be built at Cornell

Some of the most important risk items for eRHIC:

- 1) FFAG loops with a factor of 4 in momentum aperture.
 - a) Precision, reproducibility, alignment during magnet and girder production.
 - b) Stability of magnetic fields in a radiation environment.
 - c) Matching and correction of multiple simultaneous orbits.
 - d) Matching and correction of multiple simultaneous optics.
 - e) Path length control for all orbits.

- 2) Multi-turn ERL operation with a large number of turns.
 - a) HOM damping.
 - b) BBU limits.
 - c) LLRF control.
 - d) ERL startup from low-power beam.

76 – 286 MeV NS-FFAG Cornell Lattice

100 cells : Orbits and magnets in the 10.5 m diameter

GF = 42.54 T/m

ByF = -0.104 T

GD = -27.493 T/m

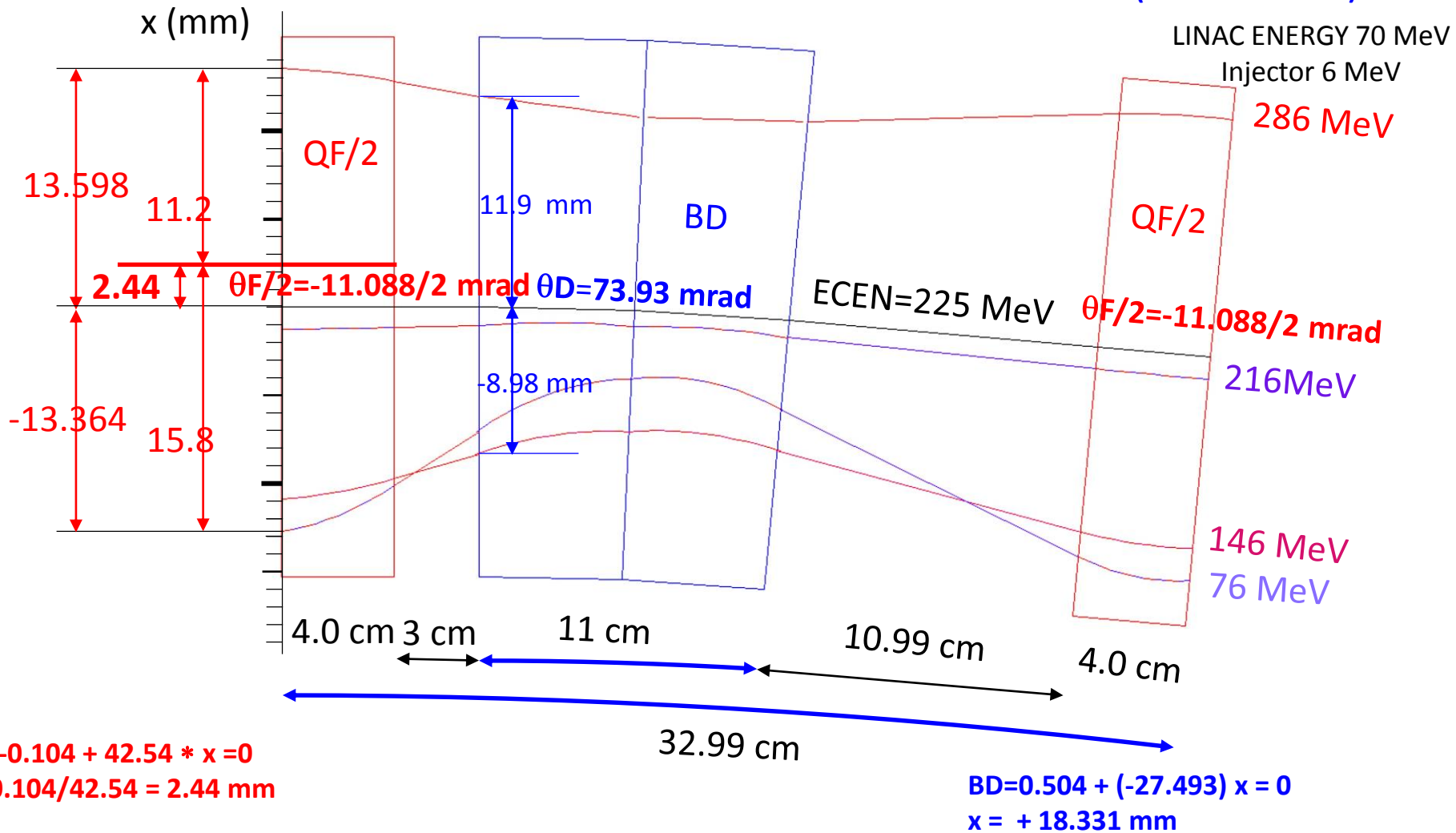
ByD = 0.5044 T

BFmin = -0.104 + 42.54 * (-13.364 mm) = -0.673 T

BFmax = -0.104 + 42.54 * (13.598 mm) = 0.4745 T

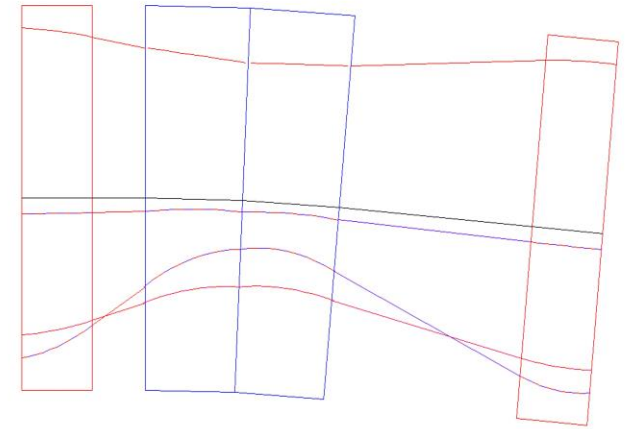
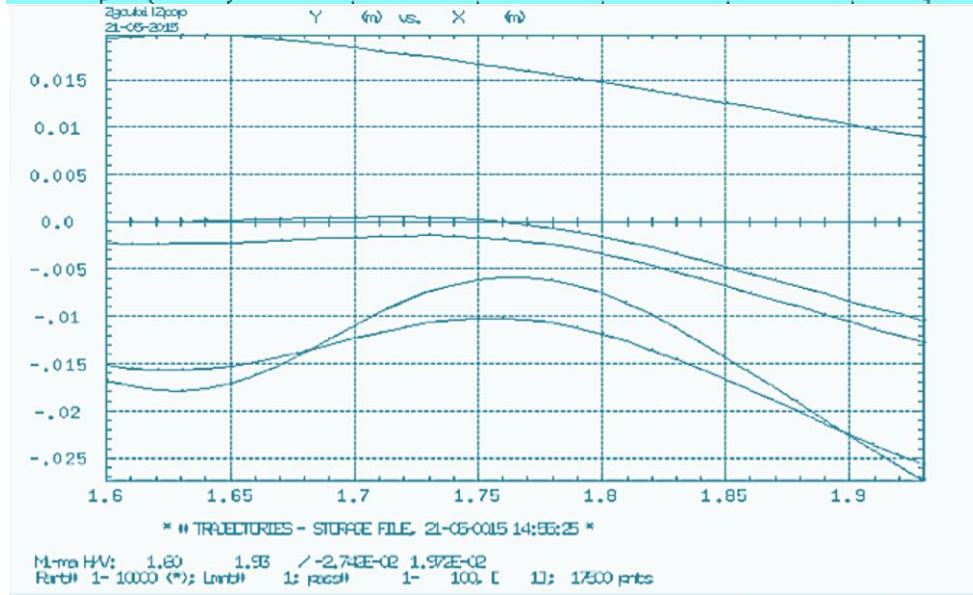
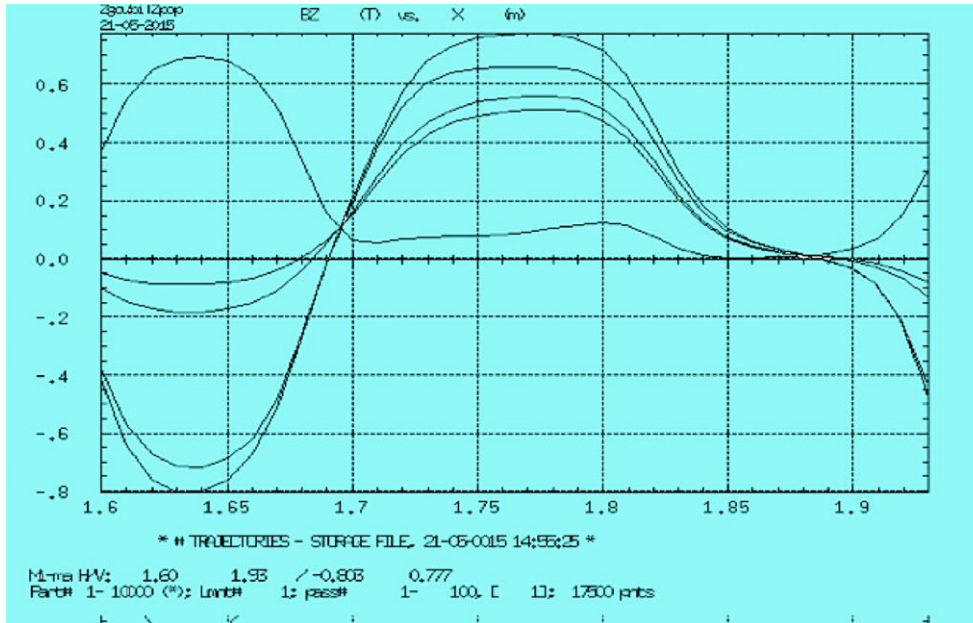
BDmin = 0.504 + (-27.49 * 11.9 mm) = 0.177 T

BDmax = 0.504 + (-27.49 * -8.98 mm) = 0.751 T



OPERA cell is QF-QD-drift. Axis is straight.

$E = 76, 146, 216, 225$ (reference) 286 MeV

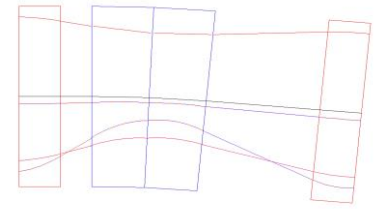


FIELD

From Francois Meot
and Nick Tsoupas

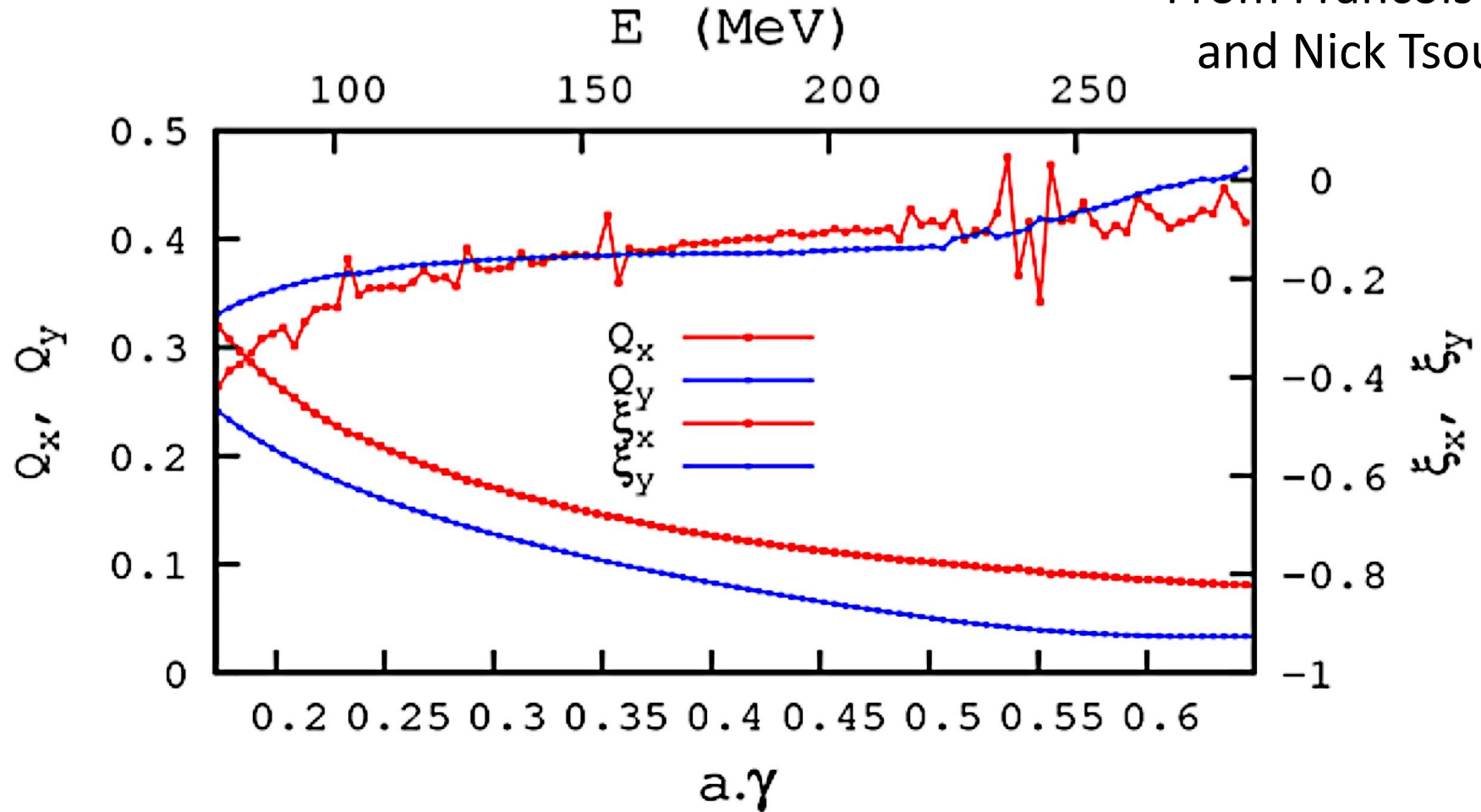
TRAJECTORIES

OPERA cell is QF-QD-drift. Axis is straight.



OPERA map QF-Displaced_QD-CFM
Cell tunes and chroma

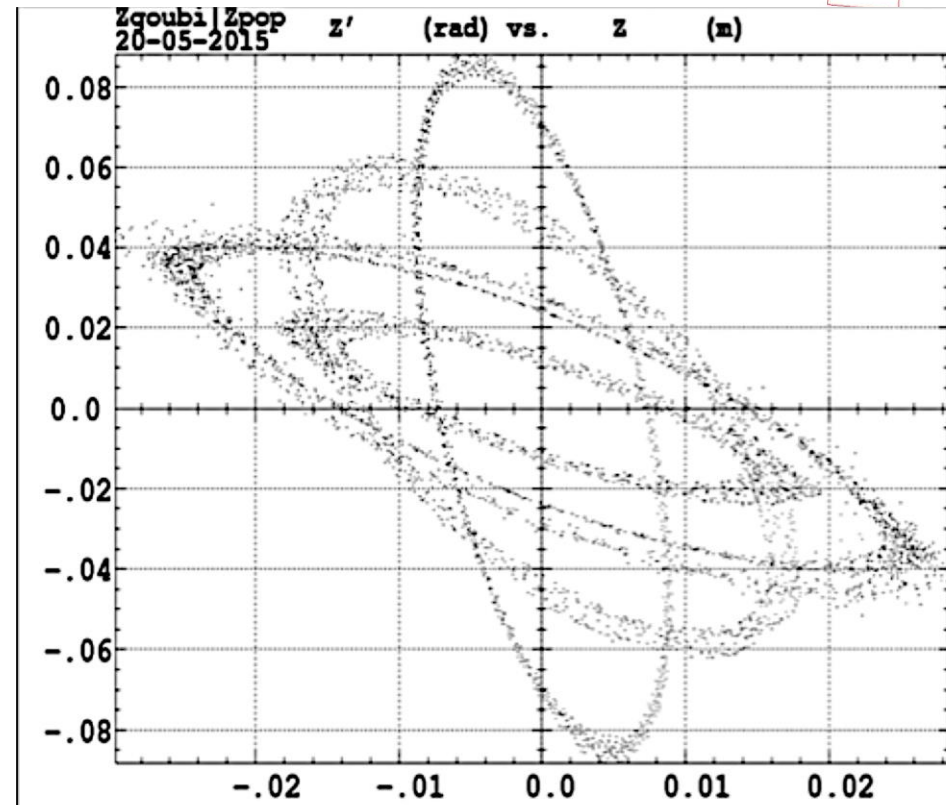
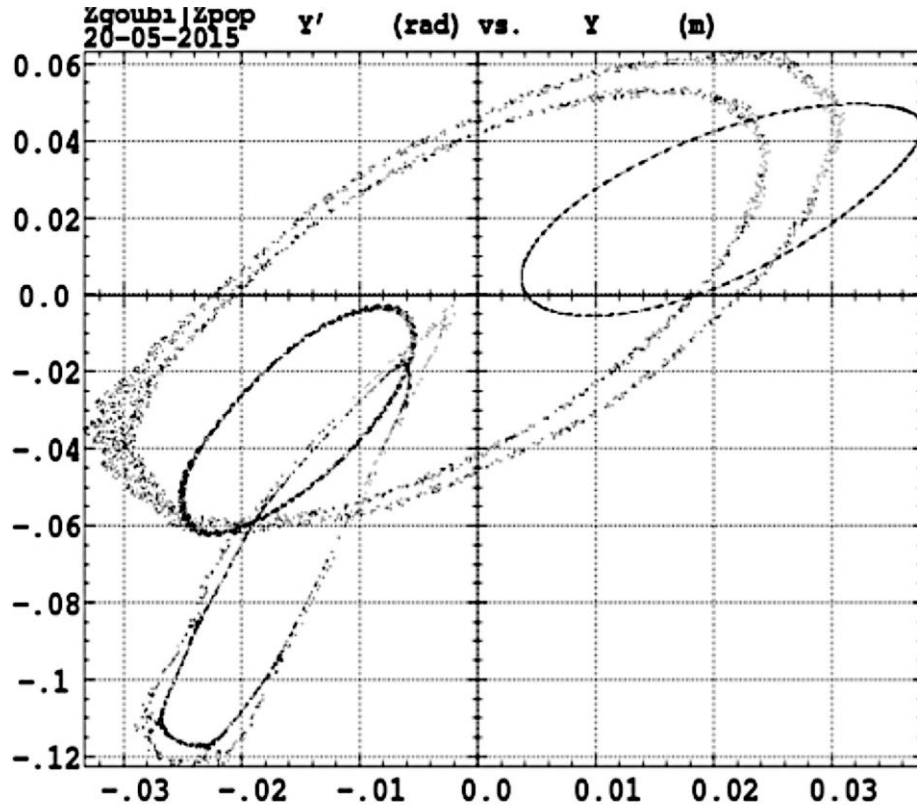
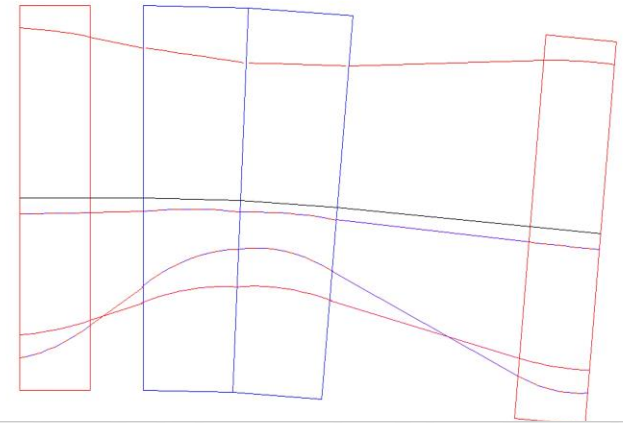
From Francois Meot
and Nick Tsoupas



OPERA cell is QF-QD-drift. Axis is straight.

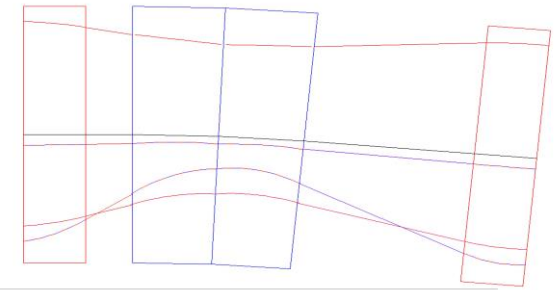
MAXIMAL STABLE AMPLITUDES, H, V :

From Francois Meot
and Nick Tsoupas



OPERA cell is QF-QD-drift. Axis is straight.

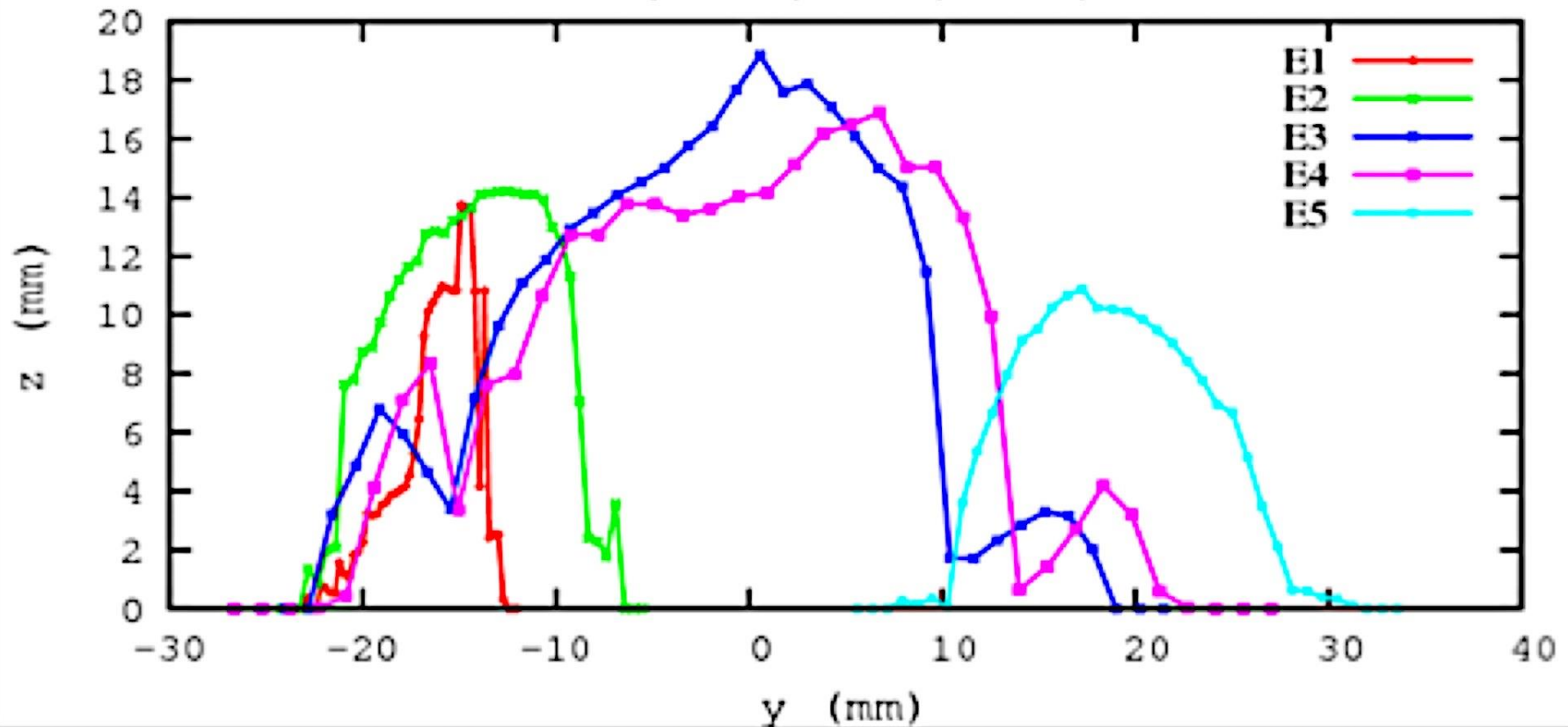
DYNAMICAL ACCEPTANCE



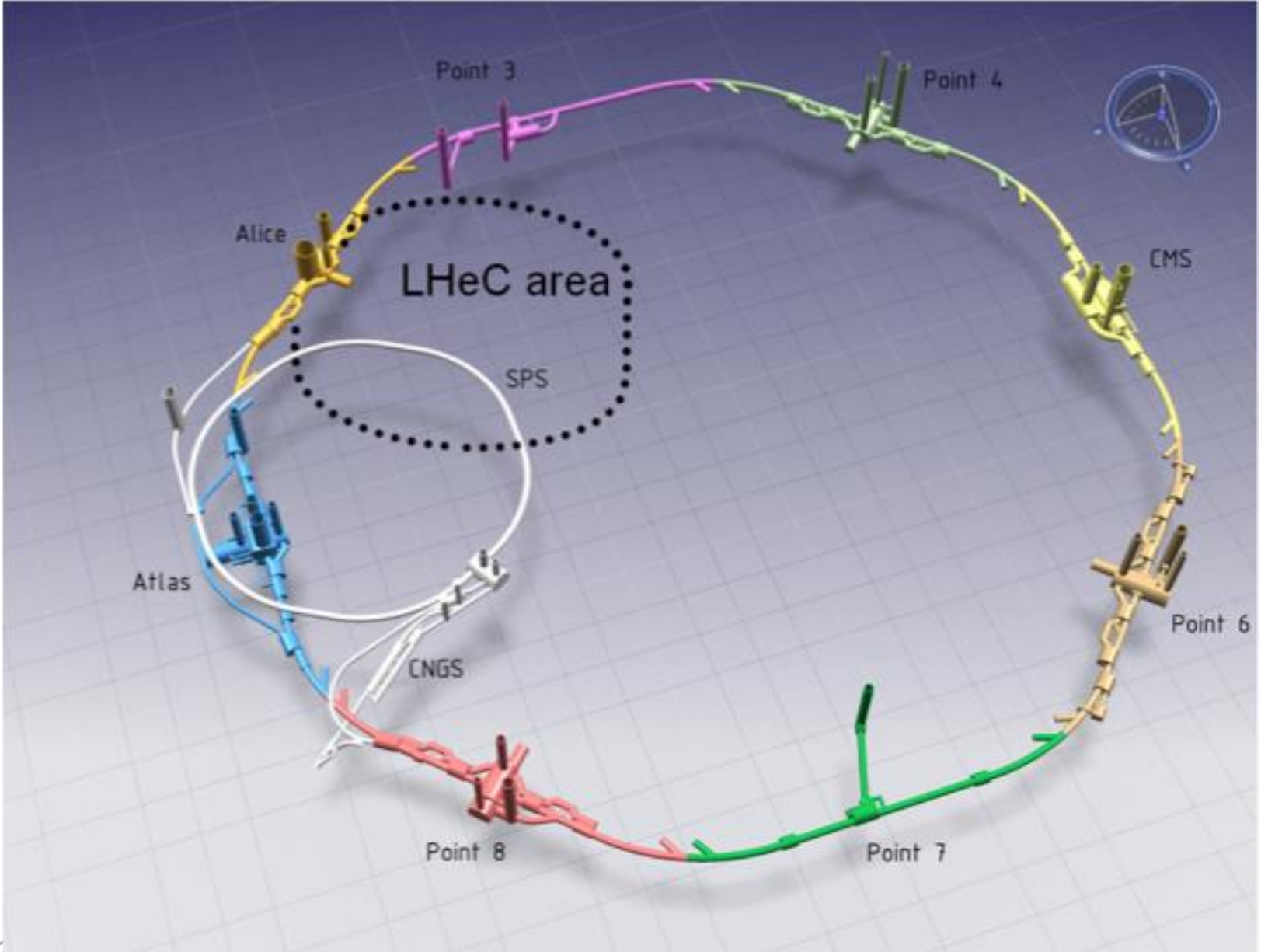
From Francois Meot

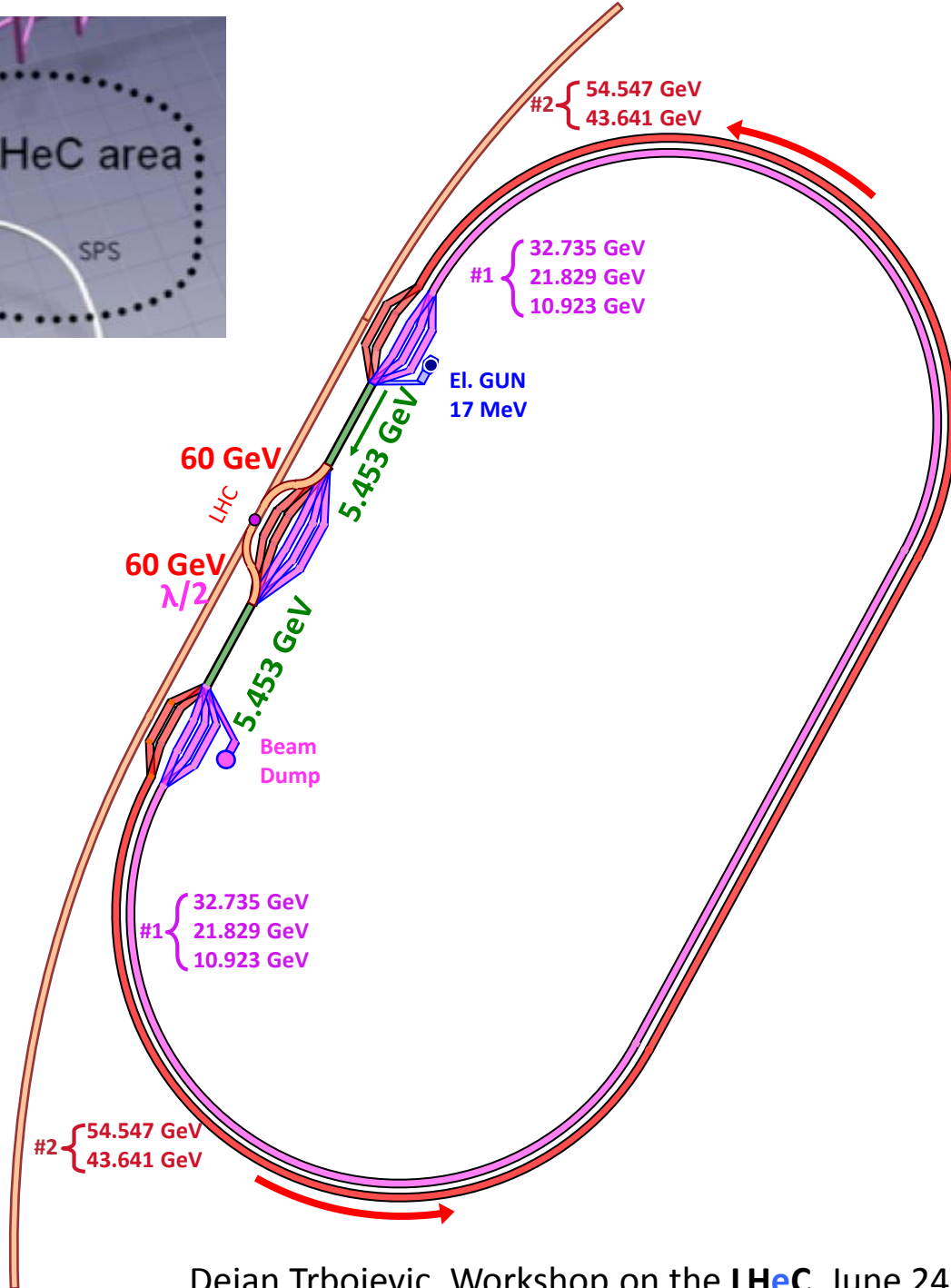
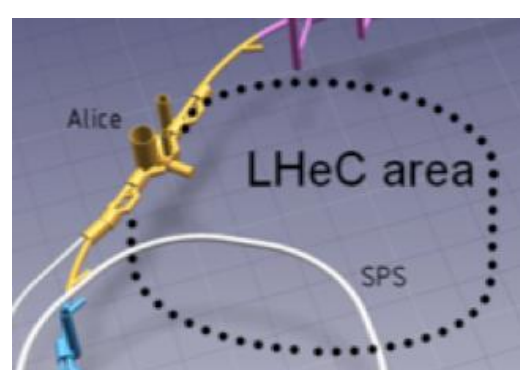
and Nick Tsoupas

$C\beta$ cell, 1000-cell DA
(QF-Displaced_QD-CFM.table field map)
E1-5 : 76, 146, 216, 225, 286 MeV



From Oliver Brüning **Layout of the LHeC-LHC-SPS**





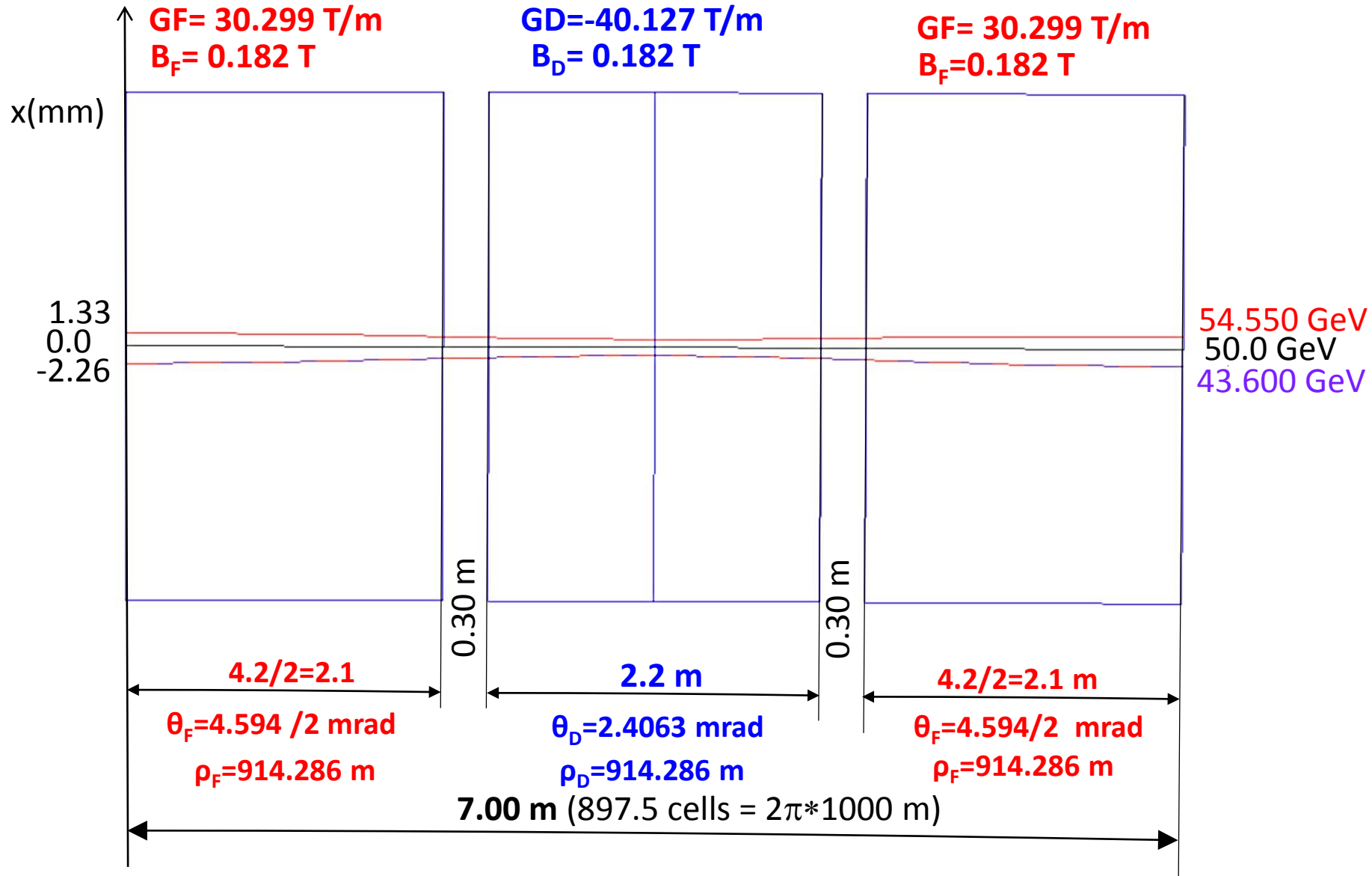
Thomas Roser's idea

1 NS-FFAG beam line:
3 passes for acceleration
3 passes for recovery

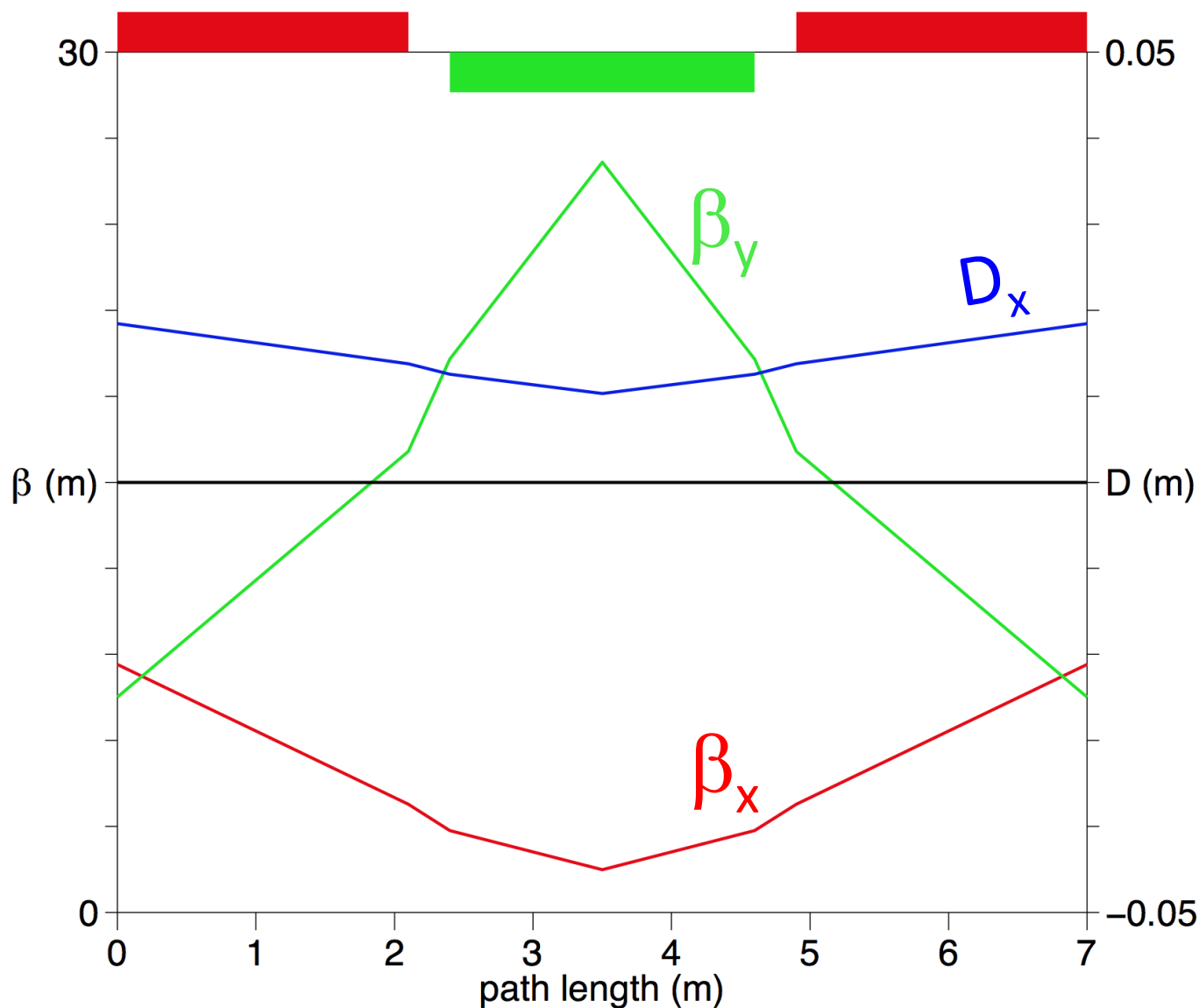
2 NS-FFAG beam line:
2 passes for acceleration
2 passes for recovery

LHeC ARC– 2 x 5.453 GeV linacs:

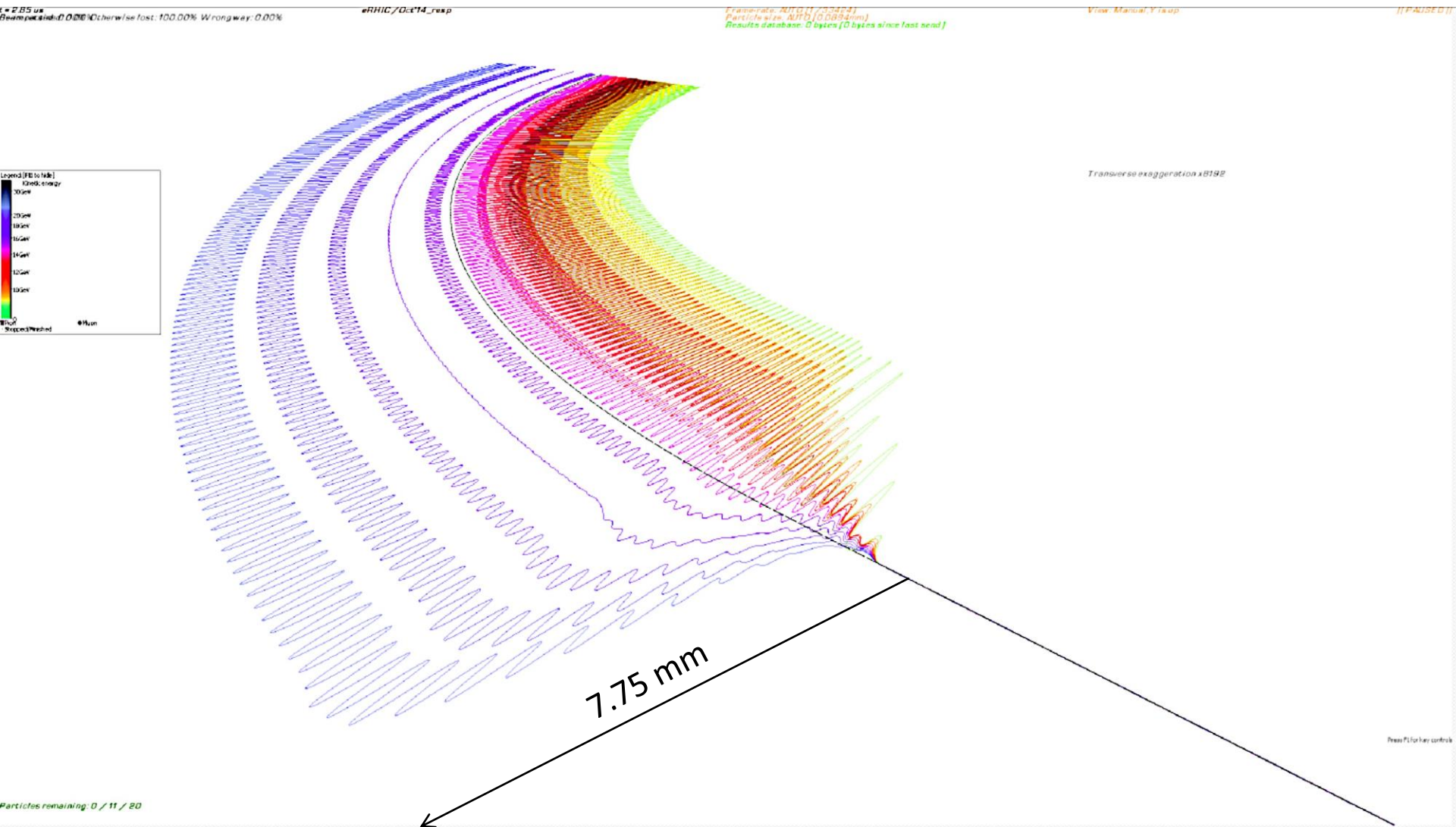
Orbits in the basic cell of the High energy NS-FFAG 54.55 - 43.644 GeV



Betatron Functions for $E_c=50$ GeV, 2 x 5.453 GeV linacs

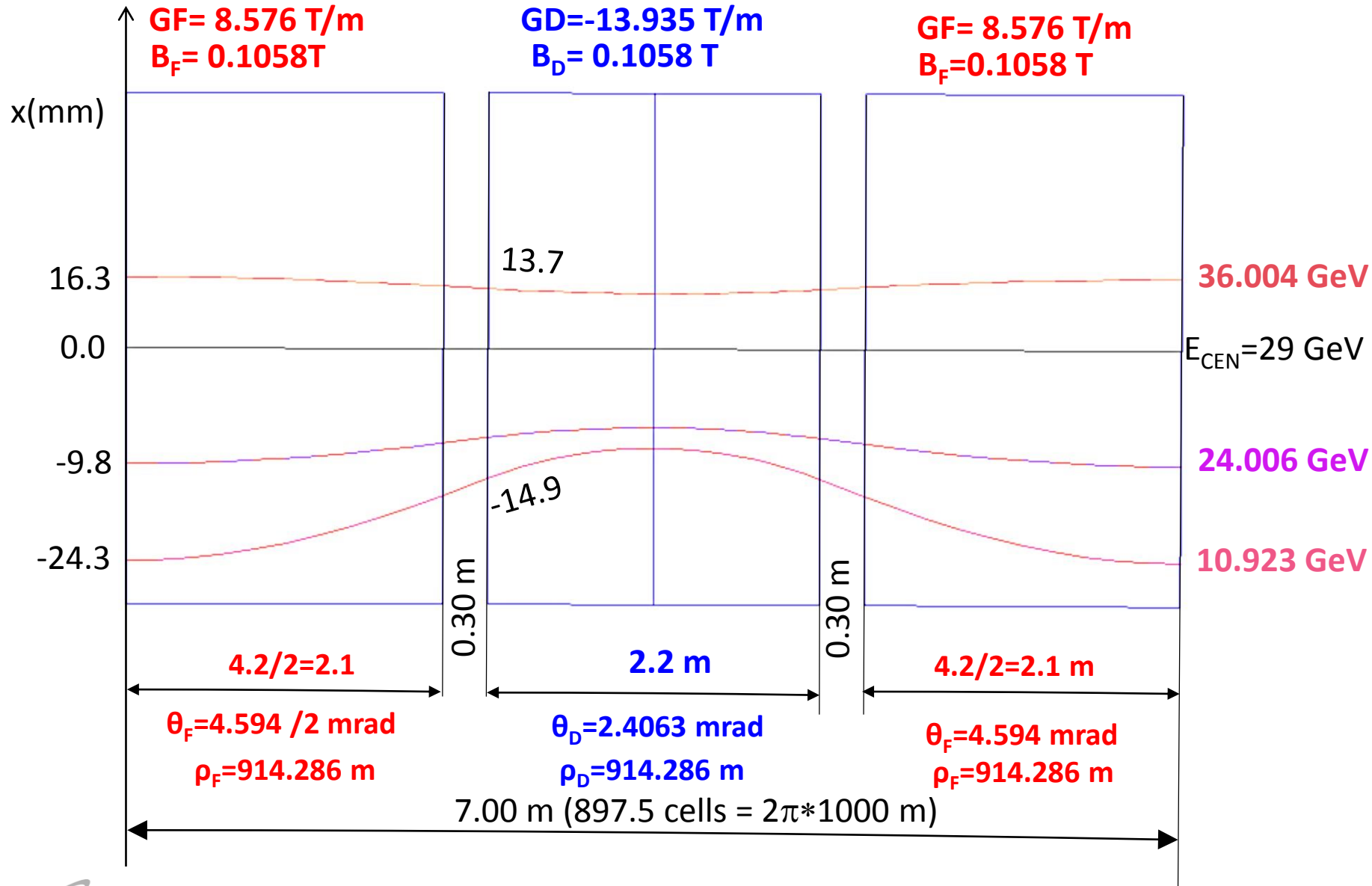


Merging FFAG arcs to the straight section in eRHIC

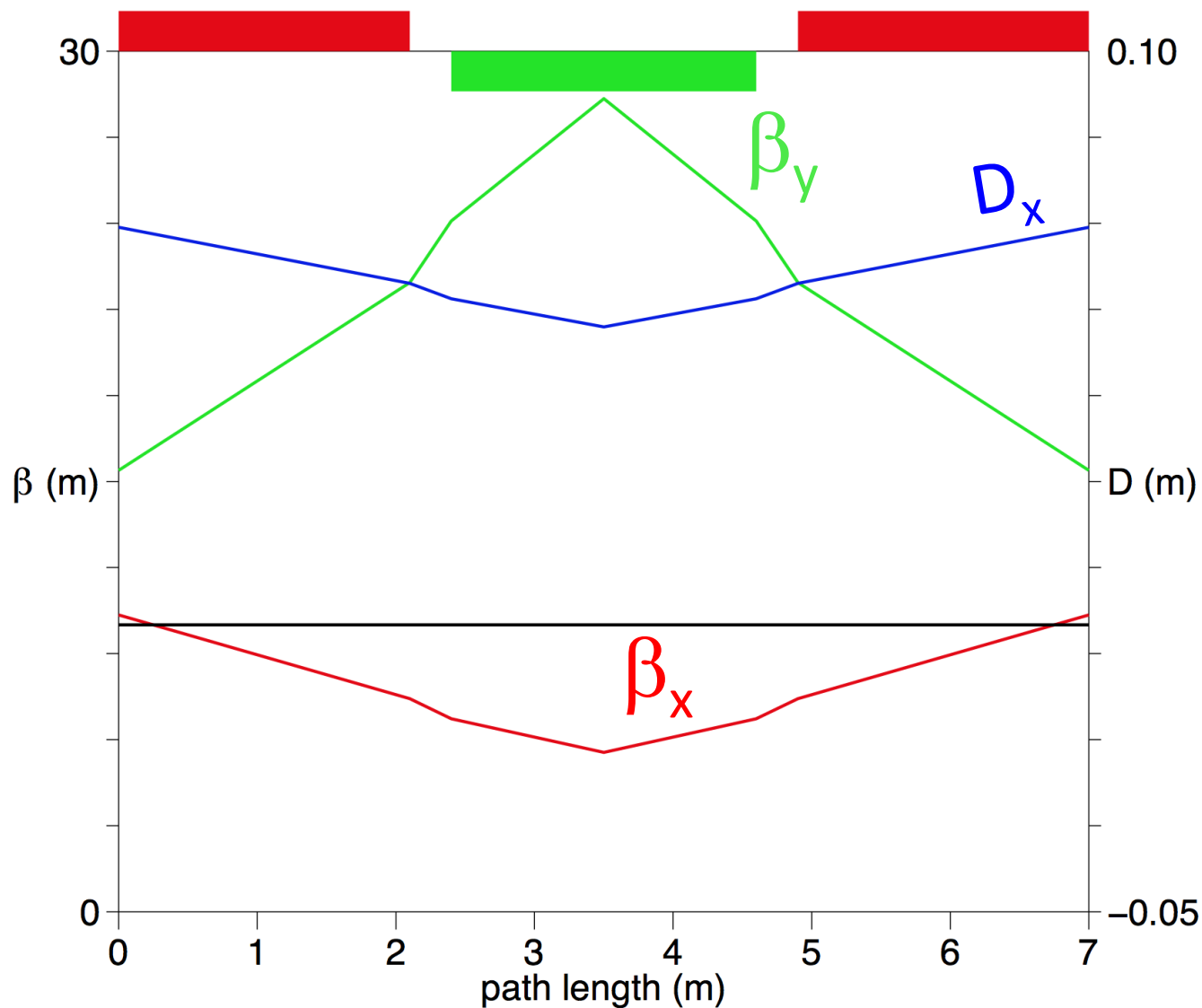


LHeC-ERL with 2 x 5.453 GeV linacs

Orbits in the basic cell of the Low energy NS-FFAG **10.923 - 32.735 GeV**



Betatron Functions for $E_c=29$ GeV, 2 x 5.453 GeV linacs



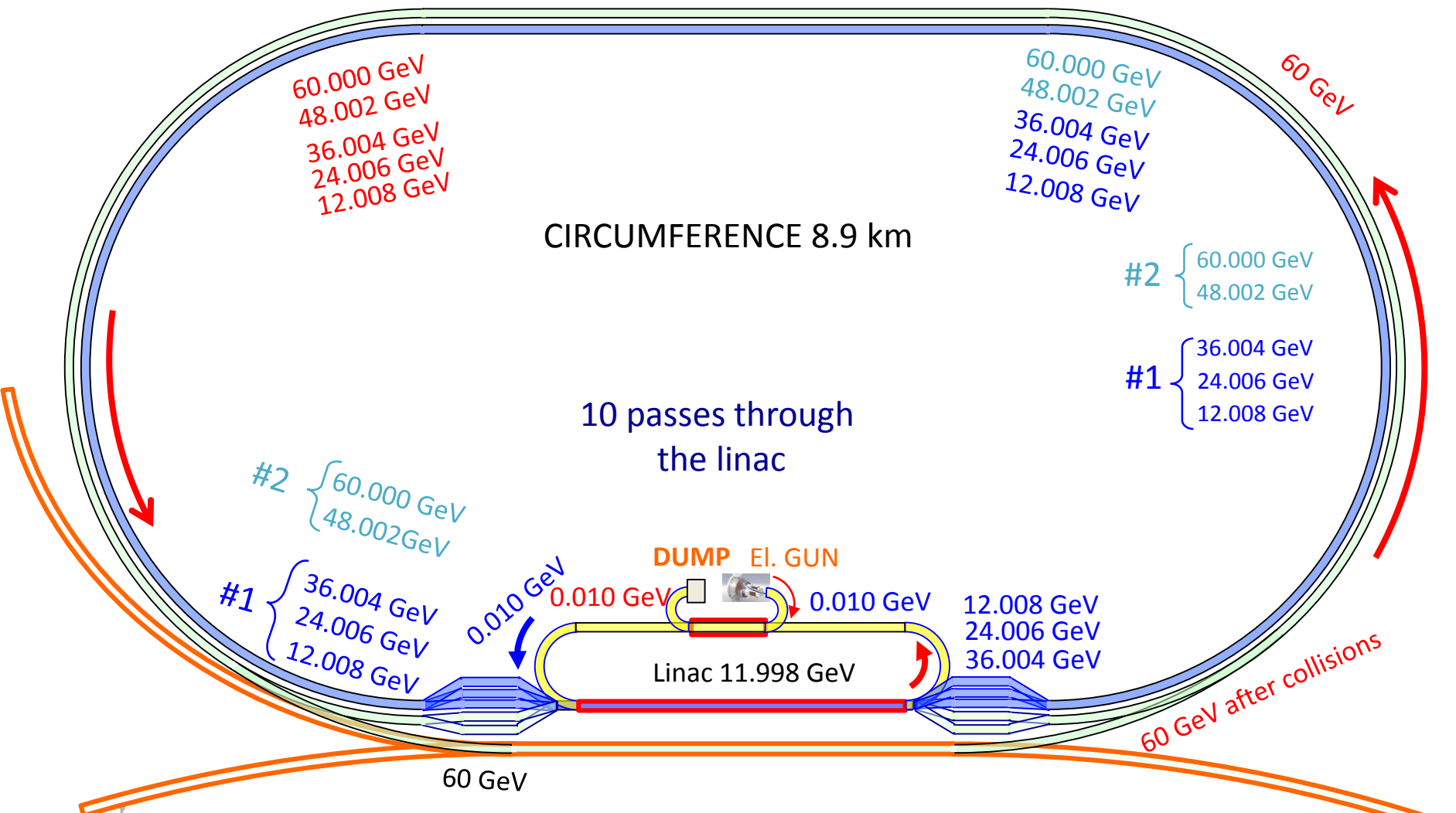
Synchrotron Radiation in LHeC with 2 x 5.453 GeV linacs

Two NS-FFAG 43.6-54.6 GeV and 10.9-32.7 GeV

Maximum Collision Energy 60 GeV

E(GeV)	Total Power (MW) 8.87035 mA	Total Power (MW) 6.6 mA
54.550	7.5779	5.6383
43.644	4.2080	3.1310
32.735	1.3902	1.0344
21.829	1.2881	0.9584
10.923	0.5359	0.3987
TOTAL	15.000	11.1608

NS-FFAG for the LHeC ERL-ONE 12 GeV LINAC



Synchrotron Radiation in LHeC with **one 12 GeV linac**

Two NS-FFAG 48-60 GeV and 12-36 GeV

Maximum Collision Energy 60 GeV

E(GeV)	Total Power (MW) 6.7834 mA	Total Power (MW) 6.6 mA
54.550	6.4562	6.2816
43.644	4.6537	4.5279
32.735	2.5812	2.5115
21.829	0.8544	0.8313
10.923	0.4546	0.4423
TOTAL	15.000	14.5945

$$G_F = 37.37 \text{ T/m}$$

$$B_{yF} = -0.0762 \text{ T}$$

$$B_{Fmin} = -0.0762 + 37.37 * (11.82 \text{ mm}) = 0.371 \text{ T}$$

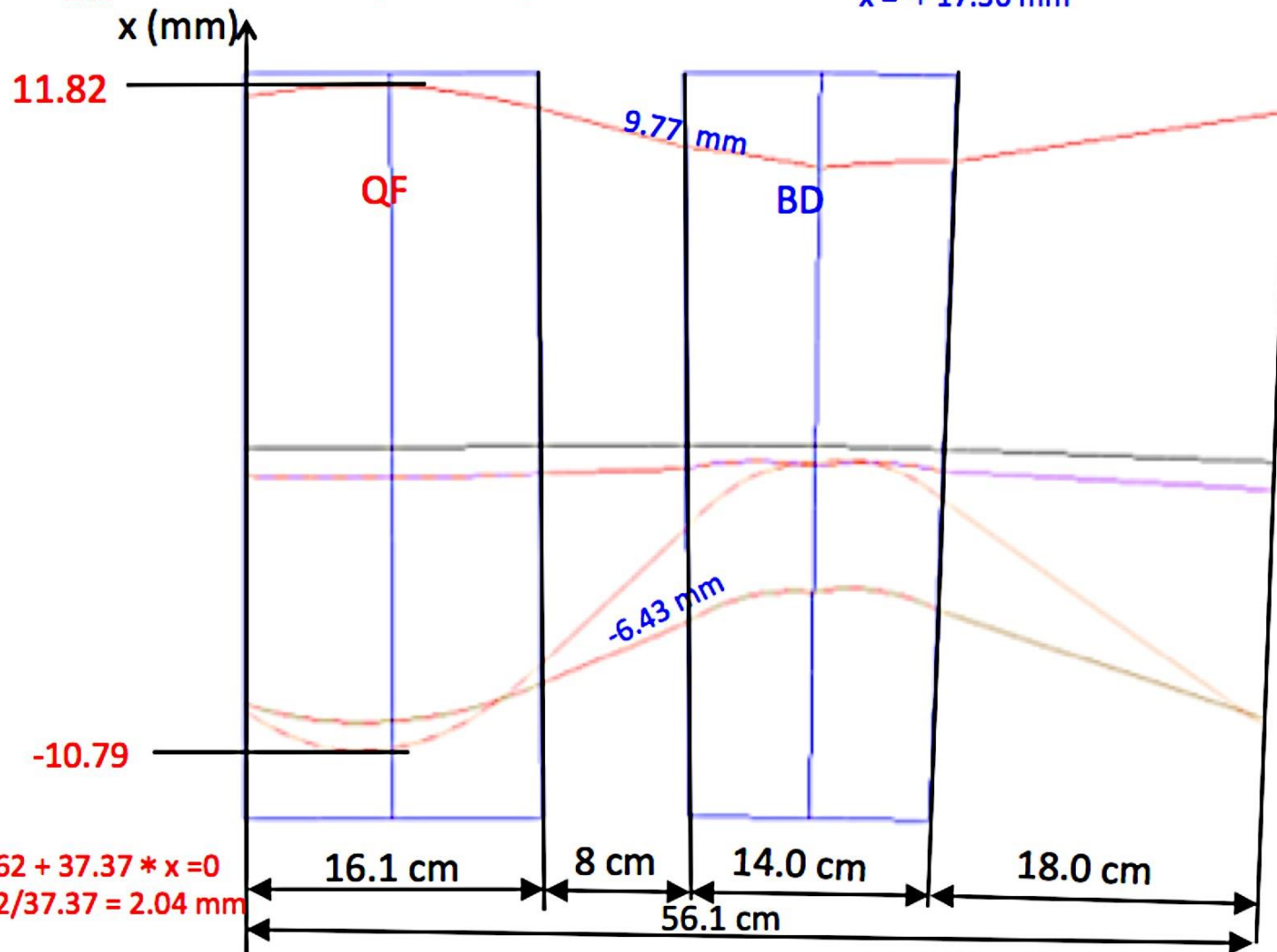
$$B_{Fmax} = -0.0762 + 37.37 * (-10.79 \text{ mm}) = -0.479 \text{ T}$$

$$G_D = -37.37 \text{ T/m} \quad B_{Dmin} = 0.649 + (-37.37 * 9.77 \text{ mm}) = 0.283 \text{ T}$$

$$B_{yD} = 0.649 \text{ T} \quad B_{Dmax} = 0.649 + (-37.37 * -6.43) = 0.889 \text{ T}$$

$$BD = 0.649 + (-37.37) x = 0$$

$$x = +17.36 \text{ mm}$$



CONCLUSION

- A cost effective eRHIC design with 1.332 GeV linac and maximum energy of 21.2 GeV is shown.
- A proposal for replacement of the 2 x 10 GeV linacs and three arcs, with 2 x 5.453 GeV linacs and two NS-FFAG arcs, respectively.
- A cost-effective solution with lower synchrotron radiation, hence 34 % larger luminosity for the same limit on the value of 15 MW for the total loss from synchrotron radiation.

Scaling down LHeC energies

Circumference of the LHC: $C_{\text{LHC}} = 26,658.88320 \text{ m}$

- ① $1/3 C_{\text{LHC}} = 8,886.29440 \text{ m}$ [60 GeV - Linacs $2 \times 10 \times 3$] 10 GeV Linac $\sim 2 \times 1 \text{ km} + 6.283 + 4 \times 0.151$
- ② $1/4 C_{\text{LHC}} = 6,664.72080 \text{ m}$ [45 GeV - Linacs $2 \times 7.5 \times 3$] 7.5 GeV linac 0.75 km
- ③ $1/5 C_{\text{LHC}} = 5,331.77664 \text{ m}$ [36 GeV - Linacs $2 \times 6 \times 3$]

FFAG solutions:

- ① $1/3 C_{\text{LHC}} = 8,886.29440 \text{ m}$ [60 GeV - Linacs $2 \times 5.453 \times 2$]
 - ① Or [60 GeV - one linac 12 GeV $\times 2$ FFAG lines]
- ② $1/4 C_{\text{LHC}} = 6,664.72080 \text{ m}$ [45 GeV - Linacs $2 \times 4.125 \text{ GeV}$]
 - ① Or [45 GeV one linac 11.245 GeV]
- ③ $1/5 C_{\text{LHC}} = 5,331.77664 \text{ m}$ [36 GeV - one linac 8.99 GeV]