

Double Higgs Production at the FCC-he

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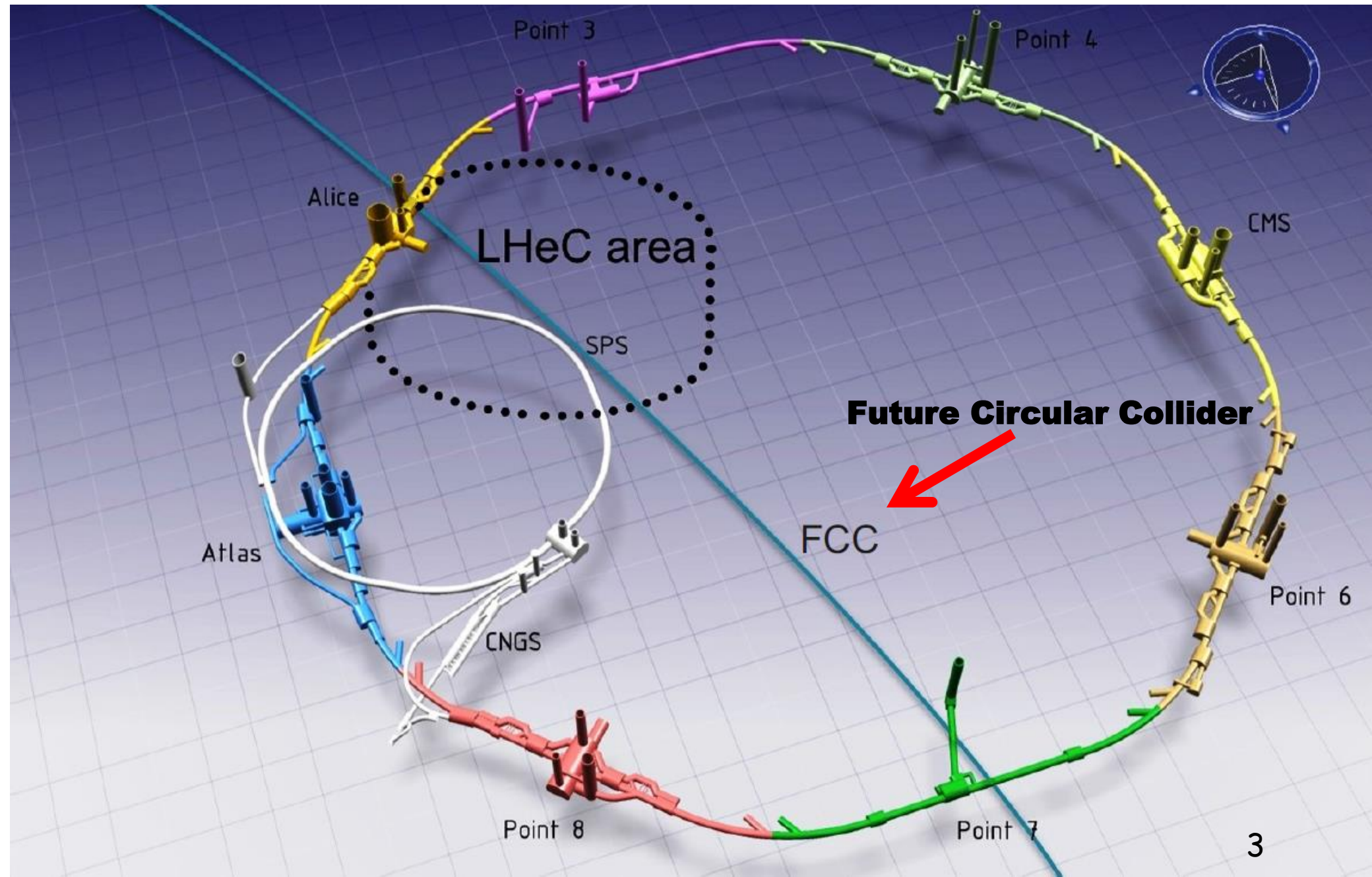
LHeC Workshop, Chavannes-de-Bogis, 26/06/15

LHeC, a Higgs Facility

Demonstrated ability to identify the Higgs boson. No Underlying event, pile up and excellent S/B

LHeC Higgs		CC (e^-p)	NC (e^-p)	CC (e^+p)
Polarisation		-0.8	-0.8	0
Luminosity [ab^{-1}]		1	1	0.1
Cross Section [fb]		196	25	58
Decay	BrFraction	$N_{CC}^H e^-p$	$N_{NC}^H e^-p$	$N_{CC}^H e^+p$
$H \rightarrow b\bar{b}$	0.577	113 100	13 900	3 350
$H \rightarrow c\bar{c}$	0.029	5 700	700	170
$H \rightarrow \tau^+\tau^-$	0.063	12 350	1 600	370
$H \rightarrow \mu\mu$	0.00022	50	5	–
$H \rightarrow 4l$	0.00013	30	3	–
$H \rightarrow 2l2\nu$	0.0106	2 080	250	60
$H \rightarrow gg$	0.086	16 850	2 050	500
$H \rightarrow WW$	0.215	42 100	5 150	1 250
$H \rightarrow ZZ$	0.0264	5 200	600	150
$H \rightarrow \gamma\gamma$	0.00228	450	60	15
$H \rightarrow Z\gamma$	0.00154	300	40	10

What about the FCC-he option?

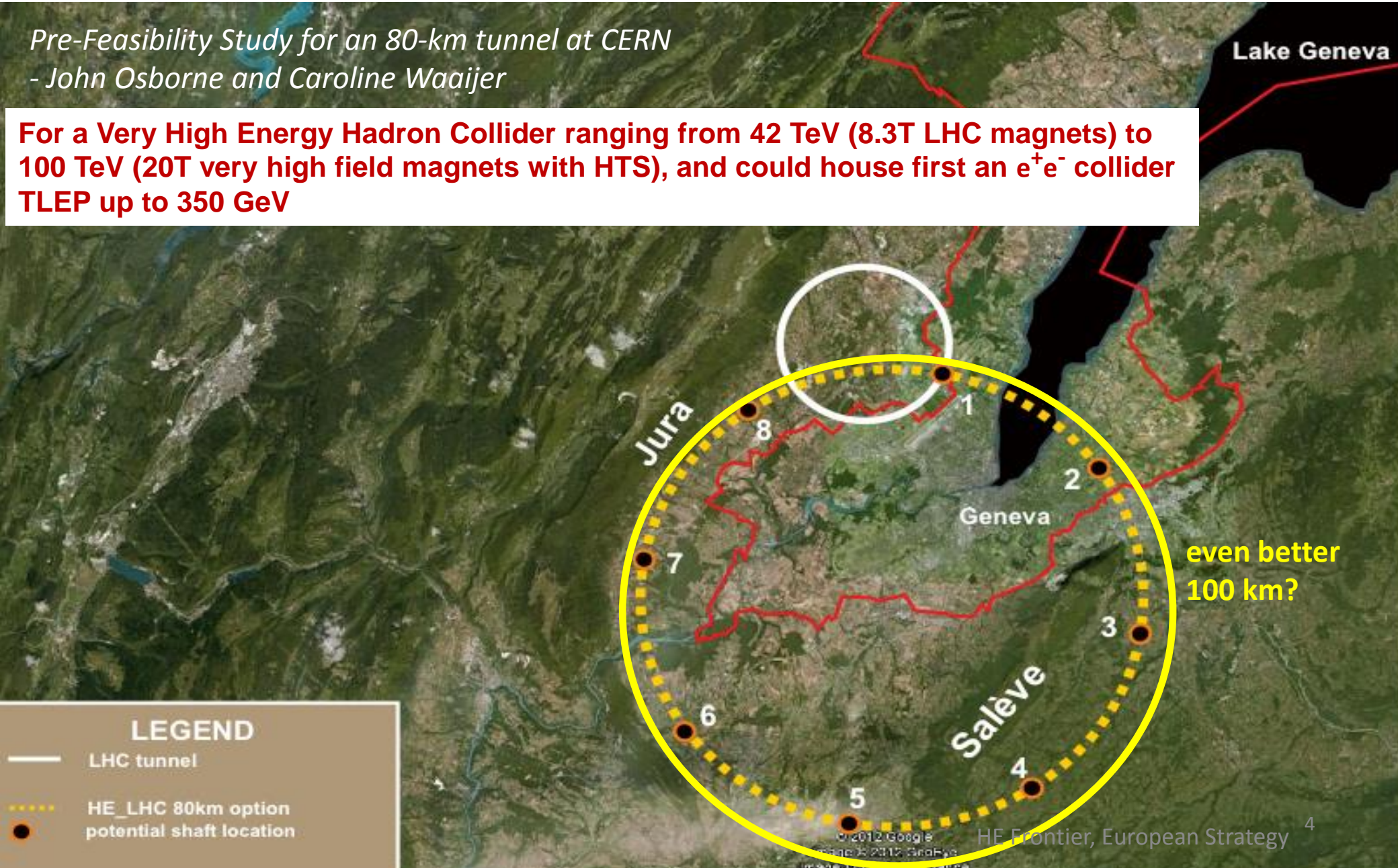


Lake-side option kept for further studies

P. Jenni

*Pre-Feasibility Study for an 80-km tunnel at CERN
- John Osborne and Caroline Waaijer*

For a Very High Energy Hadron Collider ranging from 42 TeV (8.3T LHC magnets) to 100 TeV (20T very high field magnets with HTS), and could house first an e^+e^- collider TLEP up to 350 GeV



collider parameters	FCC ERL	FCC-ee ring		protons
species	$e^-(e^+?)$	e^\pm	e^\pm	p
beam energy [GeV]	60	60	120	50000
bunches/beam	-	10600	1360	10600
bunch intensity [10^{11}]	0.05	0.94	0.46	1.0
beam current [mA]	25.6	480	30	500
rms bunch length [cm]	0.02	0.15	0.12	8
rms emittance [nm]	0.17	1.9 (x)	0.94 (x)	0.04 [0.02 y]
$\beta_{x,y}^*$ [mm]	94	8, 4	17, 8.5	400 [200 y]
$\sigma_{x,y}^*$ [μ m]	4.0	4.0, 2.0		equal
beam-b. parameter ξ	($D = 2$)	0.13	0.13	0.022 (0.0002)
hourglass reduction	0.92 ($H_D = 1.35$)	0.21	0.39	
CM energy [TeV]	3.5	3.5	4.9	
luminosity [10^{34} cm $^{-2}$ s $^{-1}$]	1.0	6.2	0.7	

Feynman rules for the interactions of the scalar boson with gauge bosons, fermions and self-interactions.

Gauge	Self-interaction	Fermion
$HW_{\mu}^{+}W_{\nu}^{-} : (-ig_{\mu\nu})2\frac{m_W^2}{\nu}$	$HHH : (i)3\frac{m_H^2}{\nu}$	$H\bar{f}f : (i)\frac{m_f}{\nu}$
$HZ_{\mu}Z_{\nu} : (-ig_{\mu\nu})2\frac{m_Z^2}{\nu}$	$HHHH : (i)3\frac{m_H^2}{\nu^2}$	
$HHW_{\mu}^{+}W_{\nu}^{-} : (-ig_{\mu\nu})2\frac{m_W^2}{\nu^2}$		
$HHZ_{\mu}Z_{\nu} : (-ig_{\mu\nu})2\frac{m_Z^2}{\nu^2}$		

Exploring the feasibility of the HHH coupling via double-Higgs boson production

HWW coupling well probed at LHeC. However, physics in hh production can also be due to HHWW, which is not constrained.

$$\mathcal{L}_{hhh}^{(3)} = \frac{m_h^2}{2v} (1 - g_{hhh}^{(1)}) h^3 + \frac{1}{2} g_{hhh}^{(2)} h \partial_\mu h \partial^\mu h,$$

$$\begin{aligned} \mathcal{L}_{hWW}^{(3)} = & -\frac{g}{2m_W} g_{hWW}^{(1)} W^{\mu\nu} W_{\mu\nu}^\dagger h - \frac{g}{m_W} \left[g_{hWW}^{(2)} W^\nu \partial^\mu W_{\mu\nu}^\dagger h + \text{h.c.} \right] \\ & - \frac{g}{2m_W} \tilde{g}_{hWW} W^{\mu\nu} \tilde{W}_{\mu\nu}^\dagger h, \end{aligned}$$

$$\begin{aligned} \mathcal{L}_{hhWW}^{(4)} = & -\frac{g^2}{4m_W^2} g_{hhWW}^{(1)} W^{\mu\nu} W_{\mu\nu}^\dagger h^2 - \frac{g^2}{2m_W^2} \left[g_{hhWW}^{(2)} W^\nu \partial^\mu W_{\mu\nu}^\dagger h^2 + \text{h.c.} \right] \\ & - \frac{g^2}{4m_W^2} \tilde{g}_{hhWW} W^{\mu\nu} \tilde{W}_{\mu\nu}^\dagger h^2. \end{aligned}$$

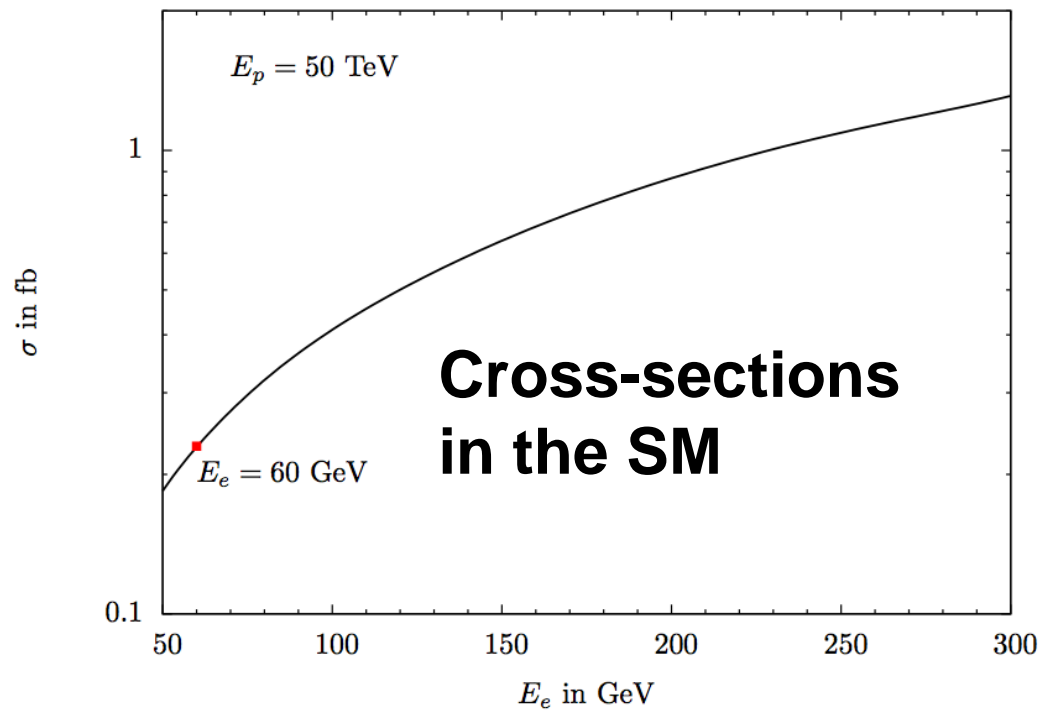
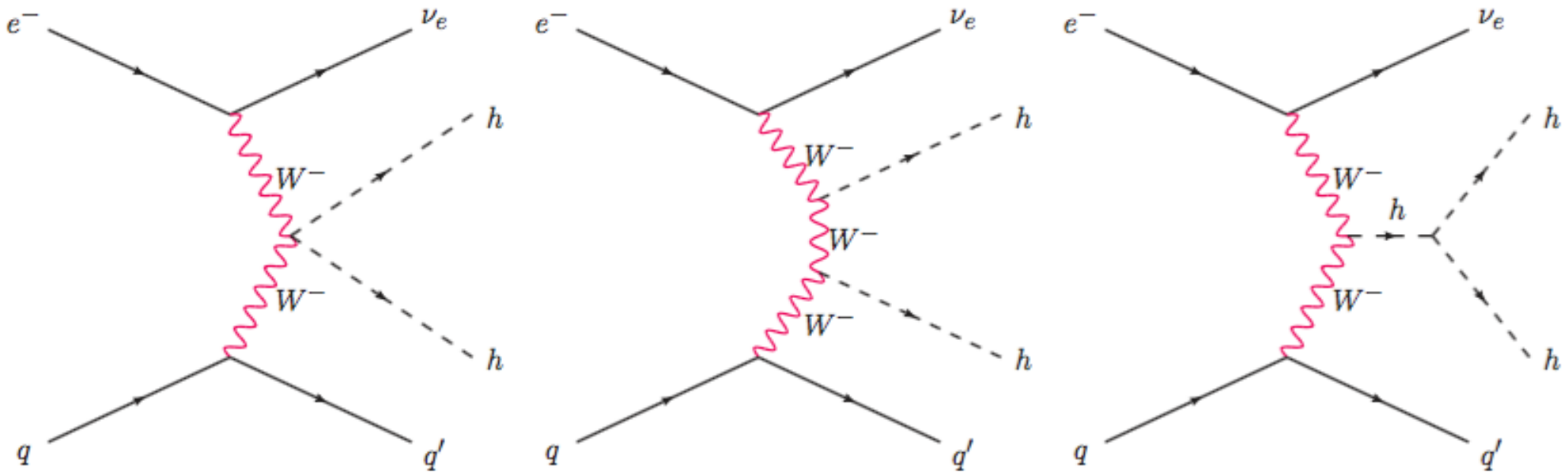
$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{hhh}^{(3)} + \mathcal{L}_{hWW}^{(3)} + \mathcal{L}_{hhWW}^{(4)}$$

Effective vertices. Note the dependence on momenta in non-SM vertices. This induces significant impact on scattering kinematics.

$$i\Gamma_{hhh} = -6iv\lambda g_{hhh}^{(1)} - ig_{hhh}^{(2)}(p_1 \cdot p_2 + p_2 \cdot p_3 + p_3 \cdot p_1),$$

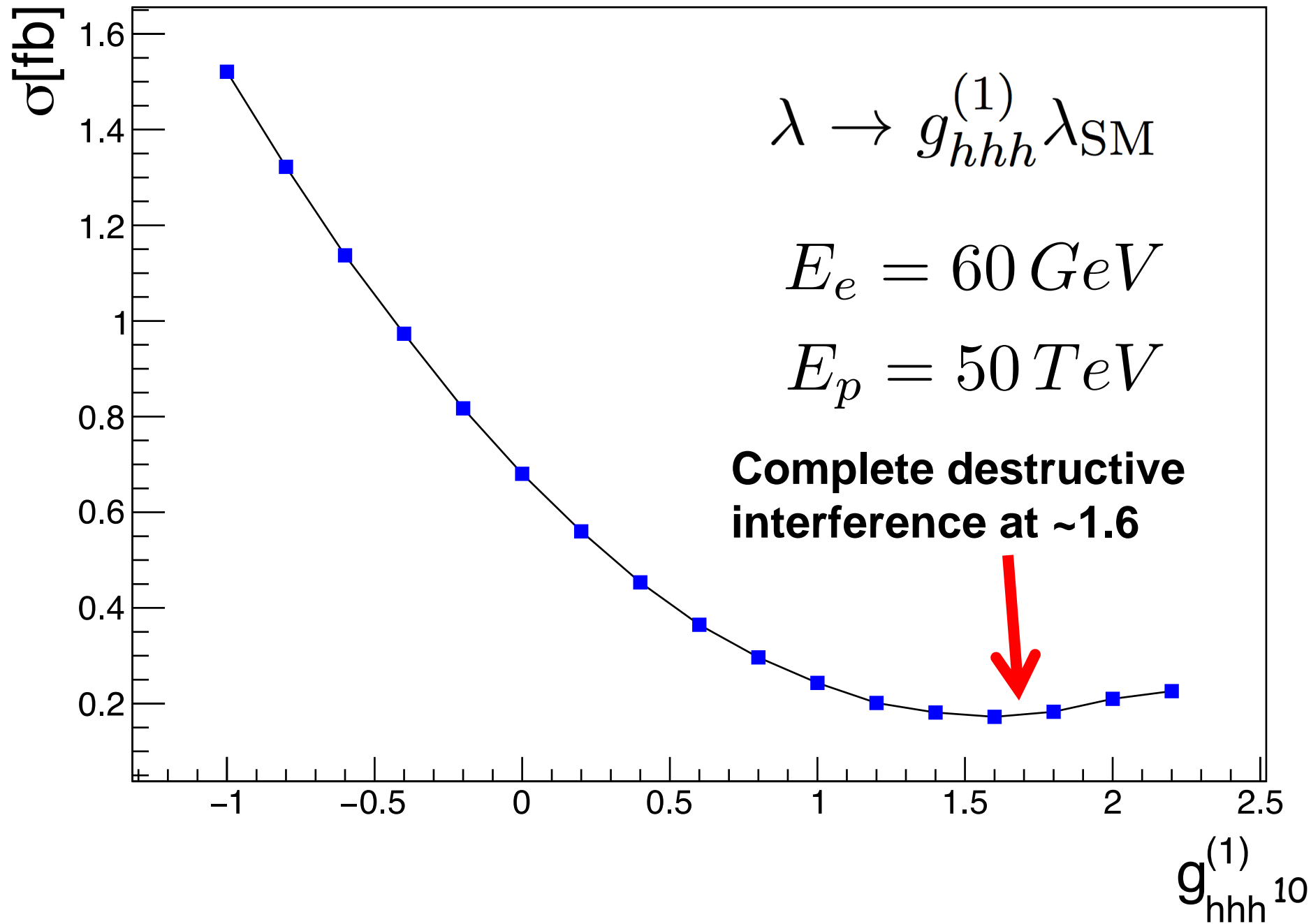
$$i\Gamma_{hW^-W^+} = i \left[\left\{ \frac{g^2}{2}v + \frac{g}{m_W}g_{hWW}^{(1)}p_2 \cdot p_3 + \frac{g}{m_W}g_{hWW}^{(2)}(p_2^2 + p_3^2) \right\} \eta^{\mu_2\mu_3} \right. \\ \left. - \frac{g}{m_W}g_{hWW}^{(1)}p_2^{\mu_3}p_3^{\mu_2} - \frac{g}{m_W}g_{hWW}^{(2)}(p_2^{\mu_2}p_2^{\mu_3} + p_3^{\mu_2}p_3^{\mu_3}) \right. \\ \left. - i\frac{g}{m_W}\tilde{g}_{hWW}\epsilon_{\mu_2\mu_3\mu\nu}p_2^\mu p_3^\nu \right],$$

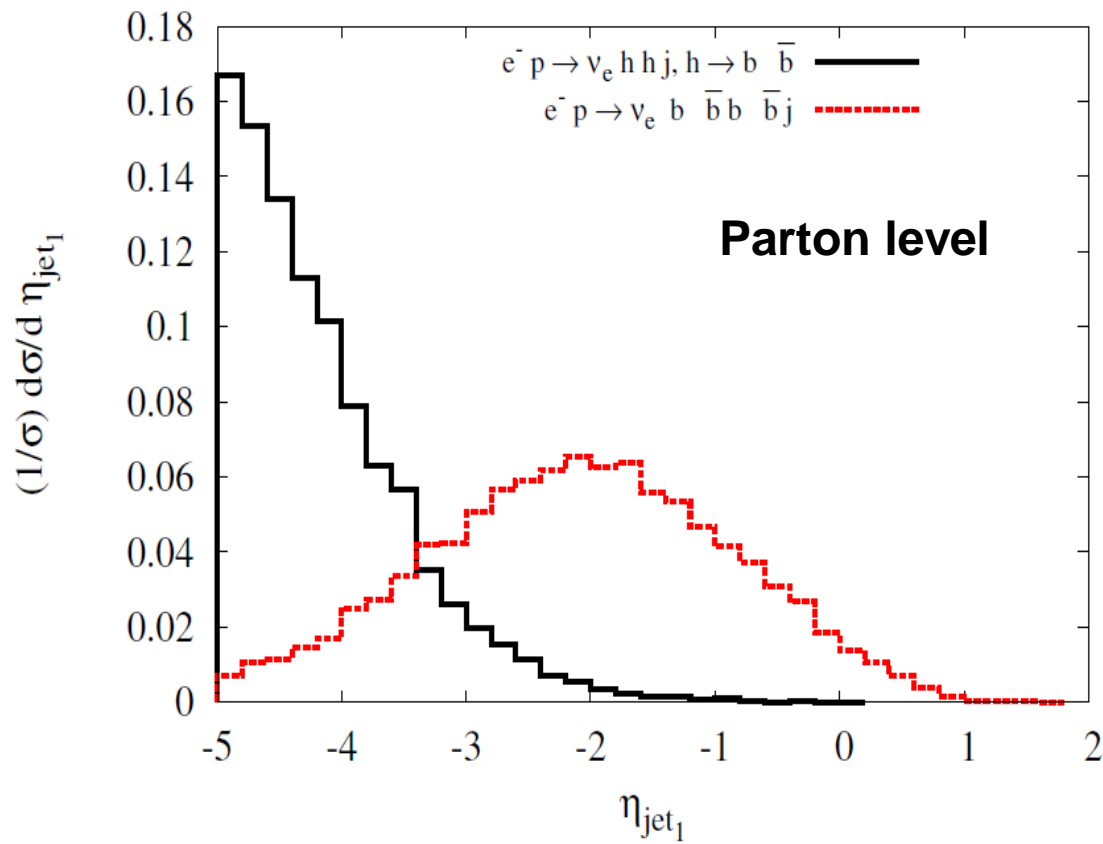
$$i\Gamma_{hhW^-W^+} = i \left[\left\{ \frac{g^2}{2} + \frac{g^2}{m_W^2}g_{hhWW}^{(1)}p_3 \cdot p_4 + \frac{g^2}{m_W^2}g_{hhWW}^{(2)}(p_3^2 + p_4^2) \right\} \eta^{\mu_3\mu_4} \right. \\ \left. - \frac{g^2}{m_W^2}g_{hhWW}^{(1)}p_3^{\mu_4}p_4^{\mu_3} - \frac{g^2}{m_W^2}g_{hhWW}^{(2)}(p_3^{\mu_3}p_3^{\mu_4} + p_4^{\mu_3}p_4^{\mu_4}) \right. \\ \left. - i\frac{g^2}{m_W^2}\tilde{g}_{hhWW}\epsilon_{\mu_3\mu_4\mu\nu}p_3^\mu p_4^\nu \right].$$



**Cross-sections
in the SM**

**Considering highly
asymmetric
collisions**

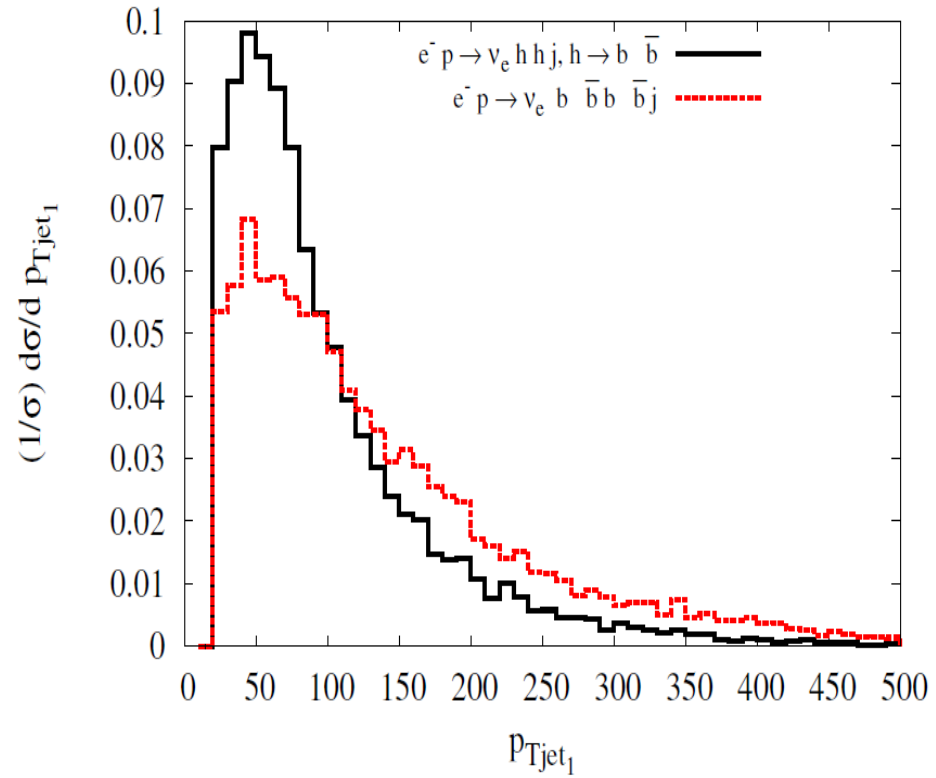




This is an important discriminator to distinguish EW from QCD multi-jet production

Scattered quark is more forward in signal

This is an important characteristic of SM production in VBF that is, in turn, sensitive to coupling structures. **Strong advantage of the LHeC**



Background classification

(Charm and light partons also considered)

• CC processes:

$$pe^- \rightarrow \left\{ \begin{array}{l} b\bar{b}b\bar{b}j\nu_e; \\ b\bar{b}jjj\nu_e; \\ zzj\nu_e, z \rightarrow b\bar{b}; \\ t\bar{t}j\nu_e, (\text{hadronic/semi-leptonic}); \end{array} \right.$$

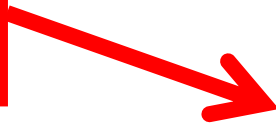
• NC processes:

$$pe^- \rightarrow \left\{ \begin{array}{l} b\bar{b}b\bar{b}je^-; \\ b\bar{b}jjje^-; \\ zzje^-, z \rightarrow b\bar{b}; \\ t\bar{t}je^-, (\text{hadronic/semi-leptonic}); \end{array} \right.$$

• PHOTO-production:

$$p\gamma \rightarrow \left\{ \begin{array}{l} b\bar{b}b\bar{b}j; \\ b\bar{b}jjj; \\ zzj, z \rightarrow b\bar{b}; \\ t\bar{t}j, (\text{hadronic/semi-leptonic}). \end{array} \right.$$

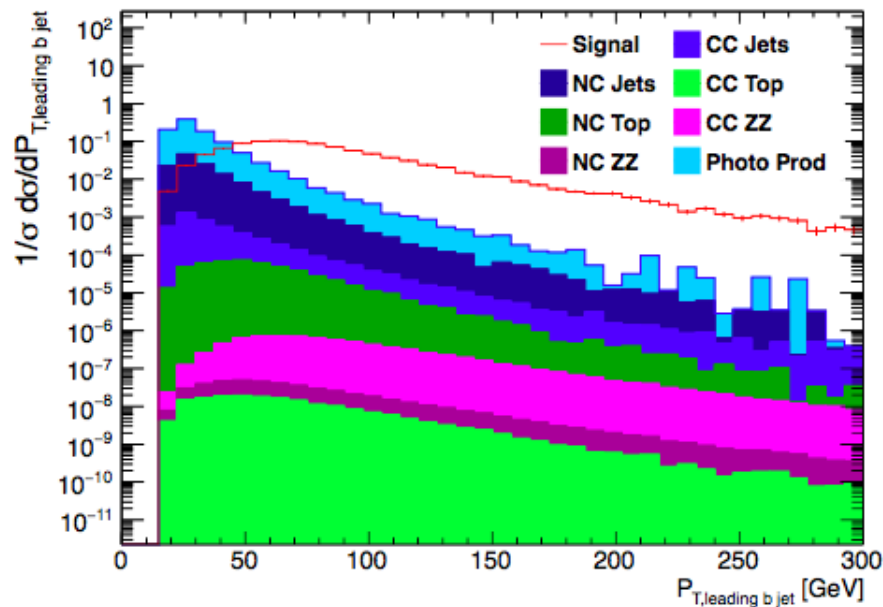
**Particularly
dangerous
background**



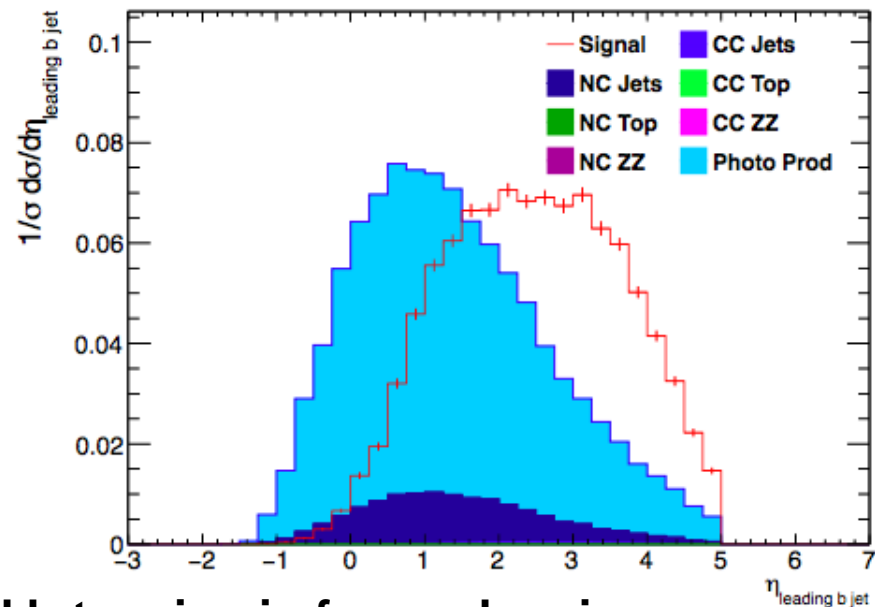
Tree-level cross-sections with Madgraph. Generation requires $p_T > 10$ GeV for partons and MET, $\Delta R_{jj} > 0.4$, $\Delta R_{ll} > 0.2$.

Process	CC (fb)	NC (fb)	PHOTO (fb)
Signal:	2.40×10^{-1}	3.95×10^{-2}	3.30×10^{-6}
$b\bar{b}b\bar{b}j$:	8.20×10^{-1}	$3.60 \times 10^{+3}$	$2.85 \times 10^{+3}$
$b\bar{b}jjj$:	$6.50 \times 10^{+3}$	$2.50 \times 10^{+4}$	$1.94 \times 10^{+6}$
$zzj(z \rightarrow b\bar{b})$:	7.40×10^{-1}	1.65×10^{-2}	1.73×10^{-2}
$t\bar{t}j$ (hadronic):	3.30×10^{-1}	$1.40 \times 10^{+2}$	$3.27 \times 10^{+2}$
$t\bar{t}j$ (semi-leptonic):	1.22×10^{-1}	$4.90 \times 10^{+1}$	$1.05 \times 10^{+2}$

Use Pythia + Delphes



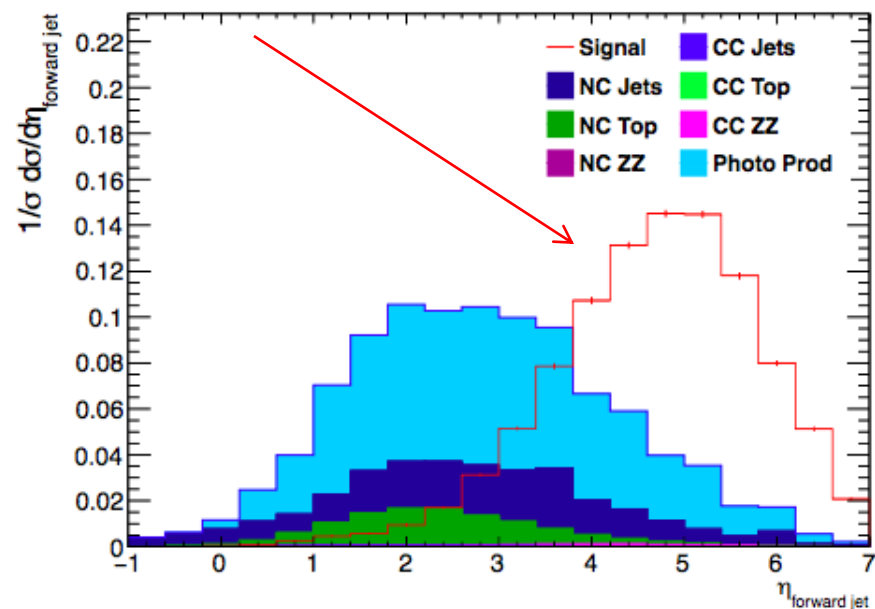
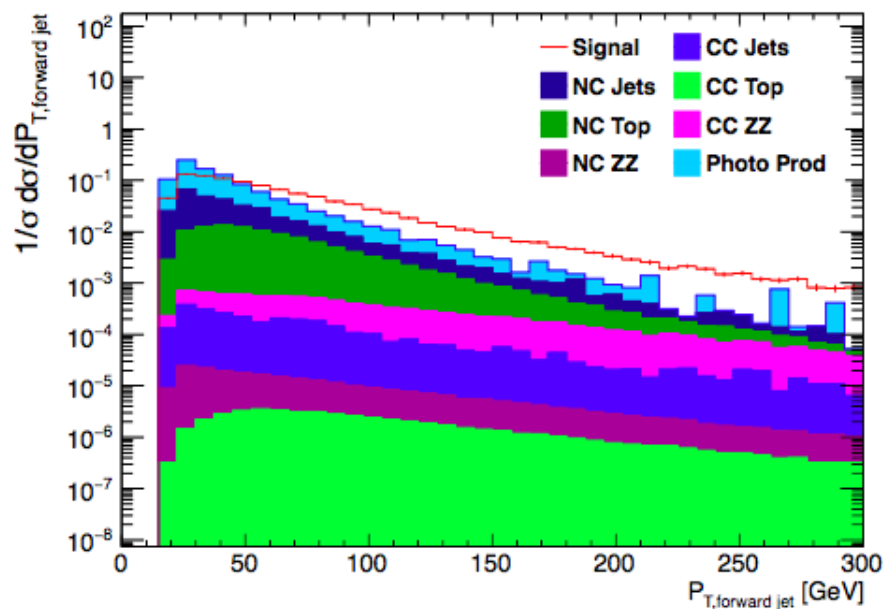
(a)



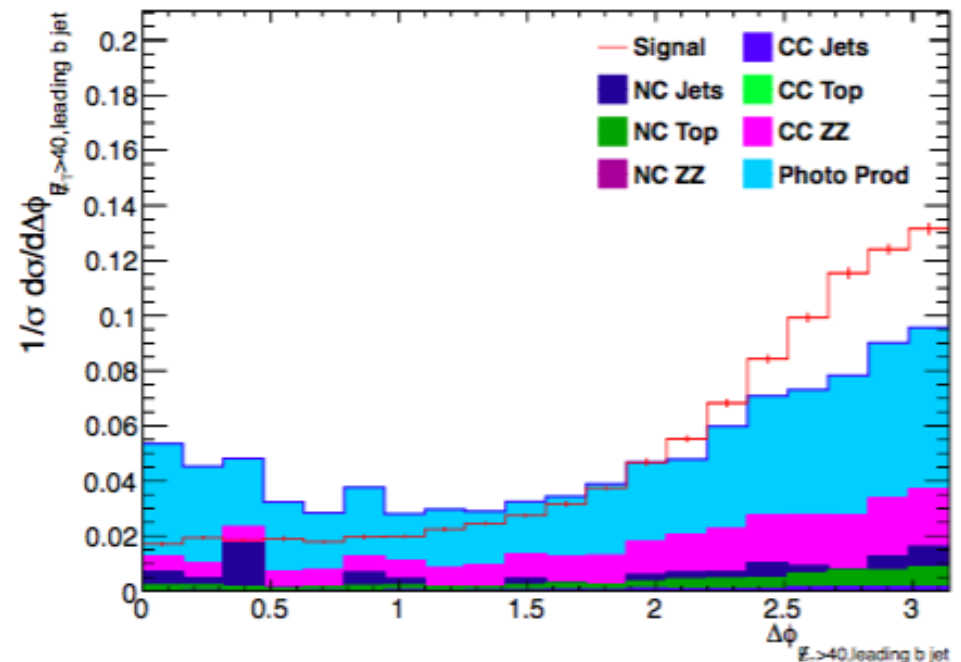
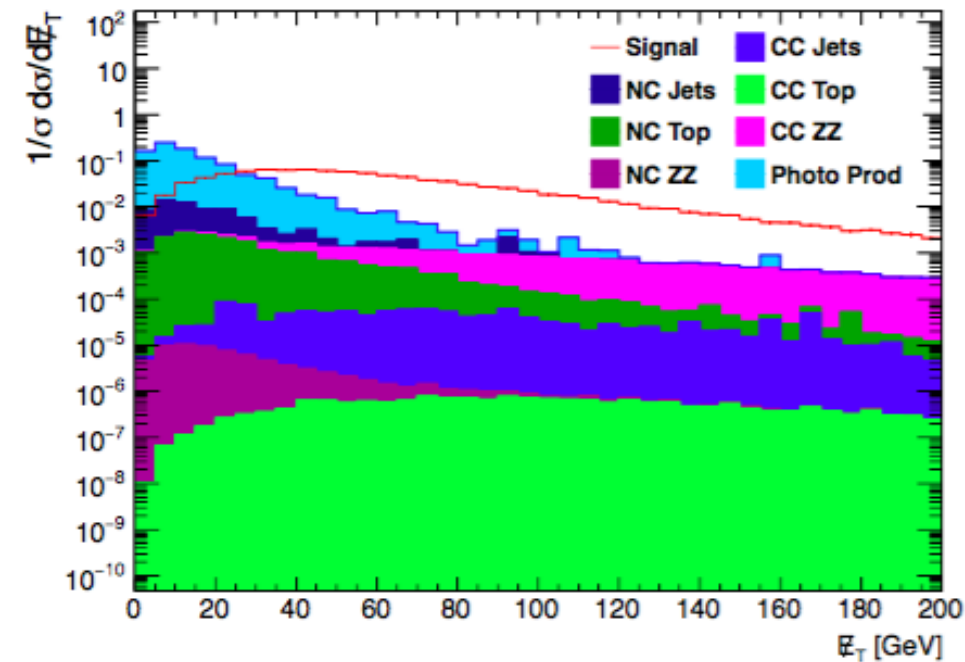
(b)

Need b-tagging in forward region

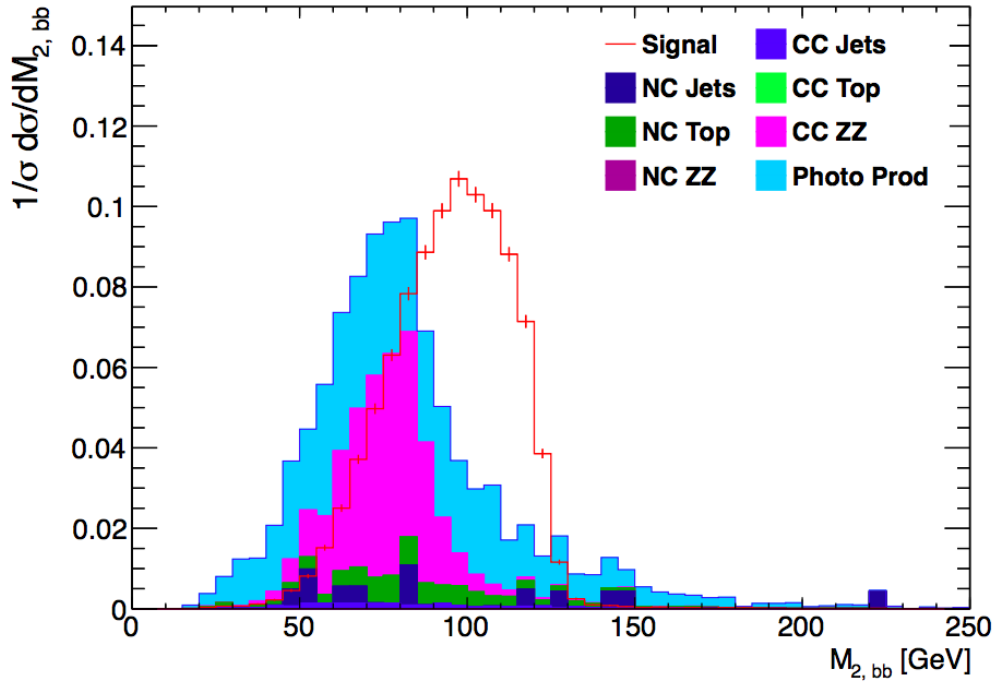
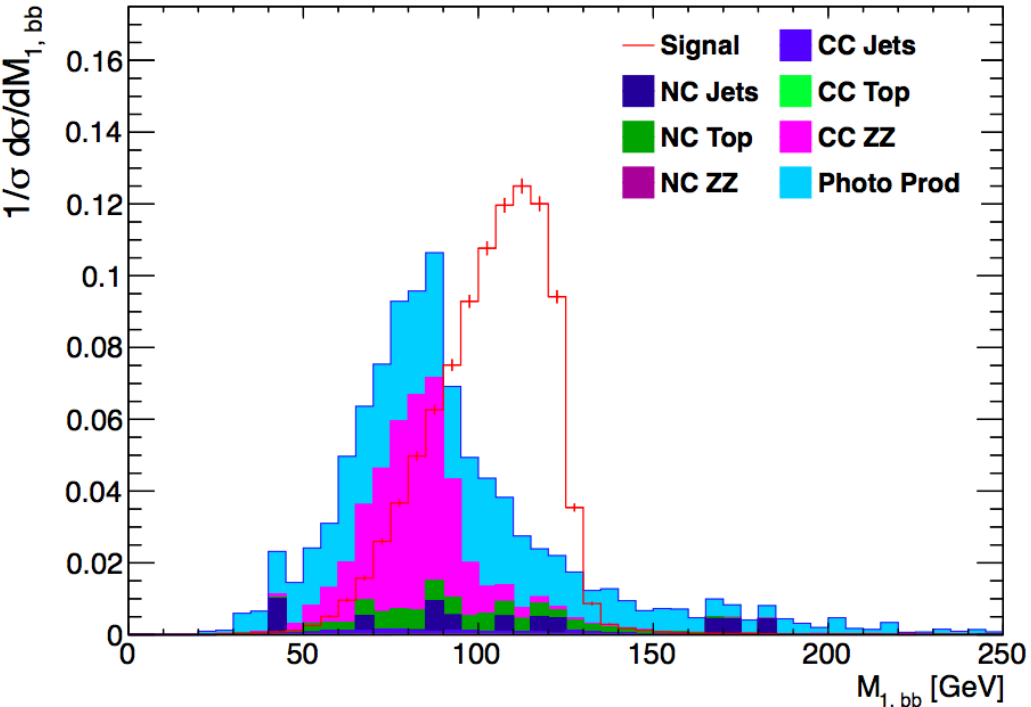
Note how forward the scattered quark is



The reconstruction of Missing E_T is critical to the suppression of the photo-production background. Lack of pile-up in ep collisions is critical to search feasibility.



B-jet invariant mass distributions are used to further suppress background. Mass windows are defined following optimization procedure



Final event selection

Require 4-btags. Forward jet is leading non-b-jet.

$$p_{Tb}, p_{Tj} > 20 \text{ GeV}$$

Leading b-jet pair contains leading b-jet.

$$|\eta_j| < 7, |\eta_b| < 5, \Delta R > 0.7$$

$$p_T^{e^-} < 10 \text{ GeV}$$

$$\eta_{Tag} > 4$$

$$MET > 40 \text{ GeV}, \Delta\Phi_{MET, b_1}, \Delta\Phi_{MET, b_2} > 0.4$$

$$90 < M_1 < 125 \text{ GeV}, 75 < M_2 < 125 \text{ GeV}$$

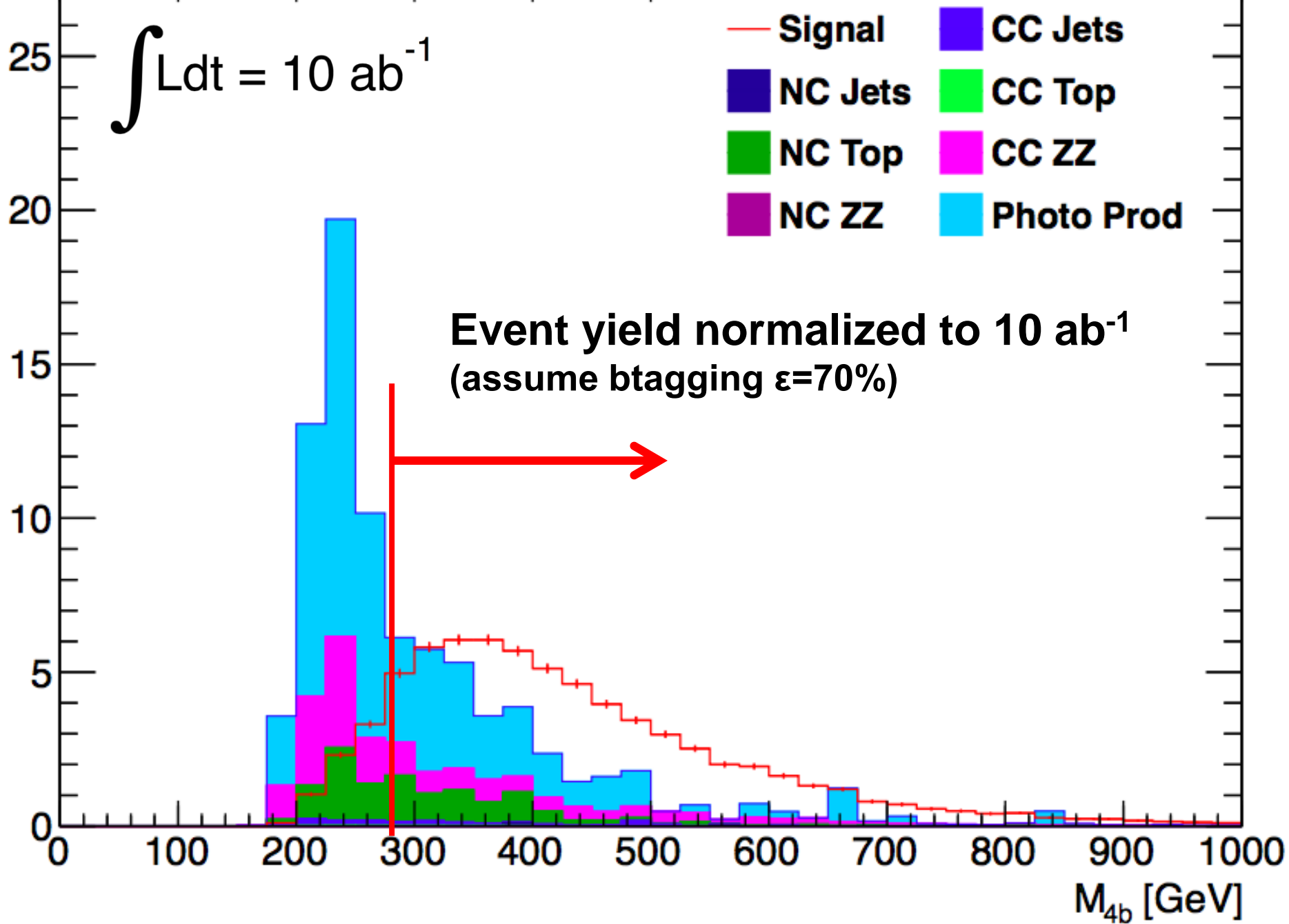
$$M_{4b} > 280 \text{ GeV}$$

Entries / 25 GeV

$$\int L dt = 10 \text{ ab}^{-1}$$

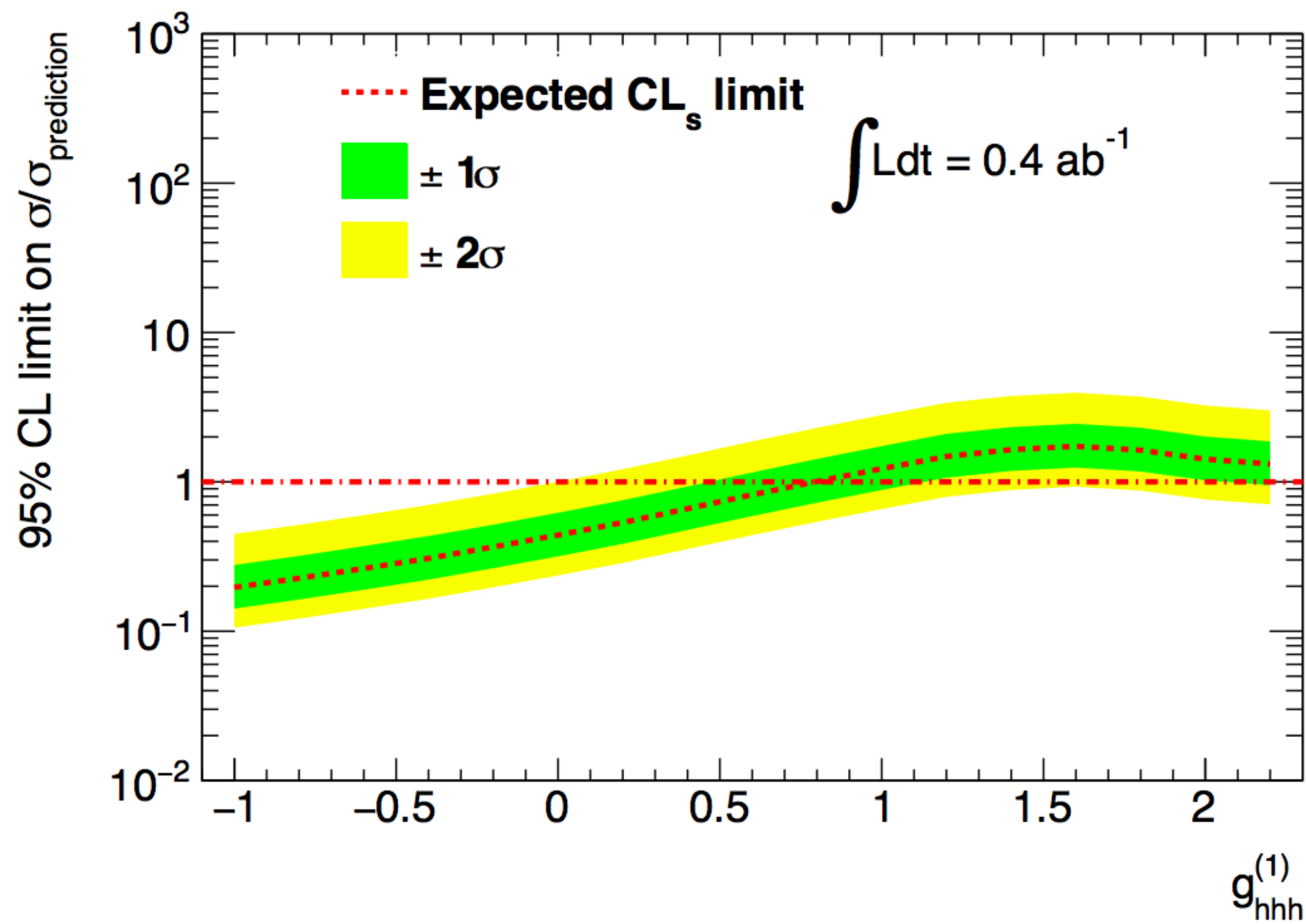
- Signal
- CC Jets
- NC Jets
- CC Top
- NC Top
- CC ZZ
- NC ZZ
- Photo Prod

Event yield normalized to 10 ab^{-1}
(assume btagging $\epsilon=70\%$)

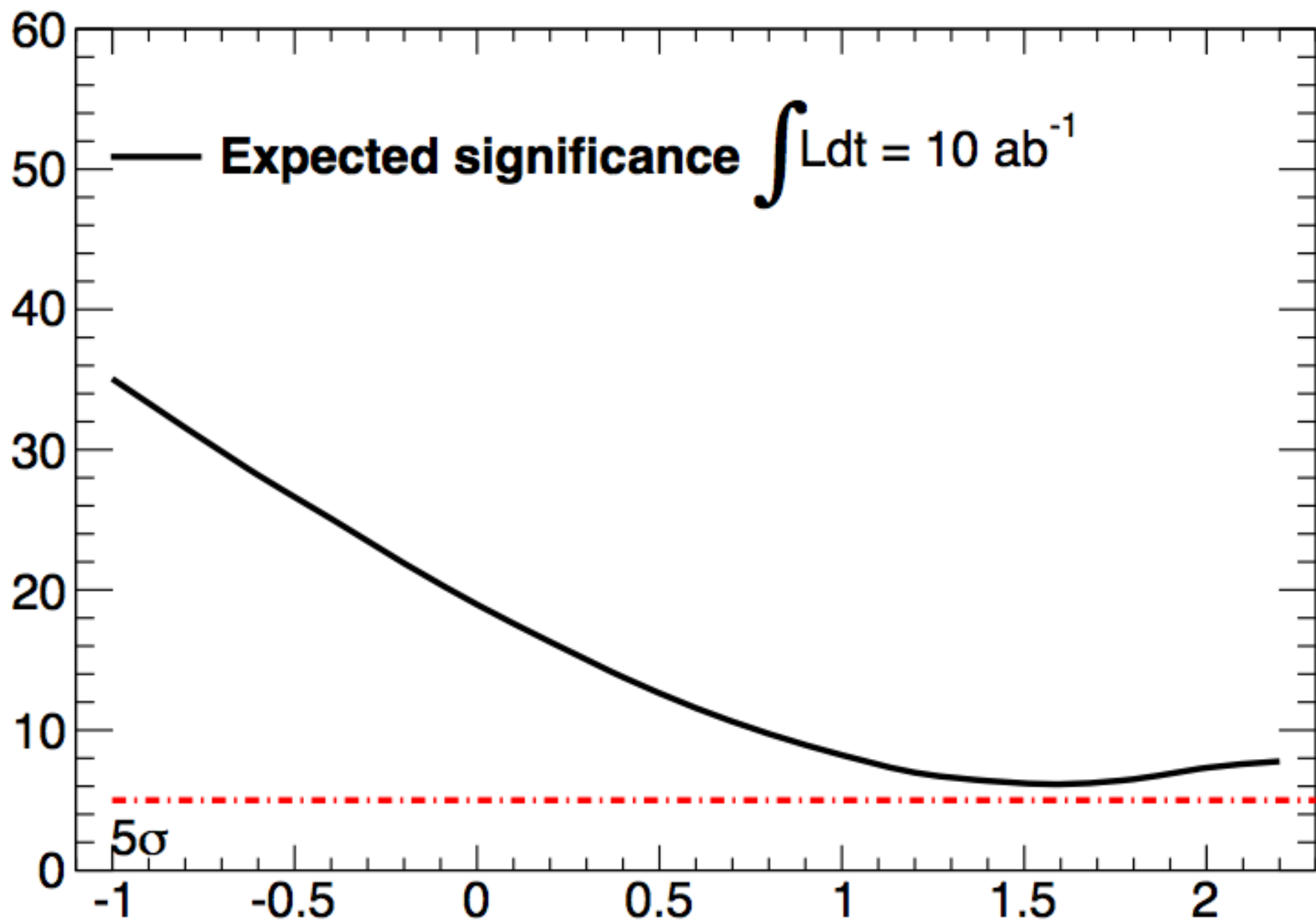


Samples	Signal	CC Jets	NC Jets	CC Top	NC Top
Initial	$2.36 \times 10^3 \pm 4.82$	$6.45 \times 10^6 \pm 9.3 \times 10^3$	$2.5 \times 10^8 \pm 4.26 \times 10^5$	$4.49 \times 10^3 \pm 5.03$	$7.4 \times 10^6 \pm 6.86 \times 10^3$
4 b and 1 light jets	299 ± 1.16	293 ± 7.56	$2.23 \times 10^4 \pm 678$	5.72 ± 0.023	$9.87 \times 10^3 \pm 31.1$
Electron rejection	299 ± 1.16	293 ± 7.56	$6.84 \times 10^3 \pm 385$	5.66 ± 0.0229	$6.43 \times 10^3 \pm 28$
Forward jet	224 ± 1.01	22.9 ± 1.39	864 ± 65.1	0.399 ± 0.00537	307 ± 5.8
\cancel{E}_T	149 ± 0.823	18.7 ± 0.981	93.9 ± 26.7	0.372 ± 0.00524	85.4 ± 2.86
$\cancel{E}_T - \phi$ rejection	128 ± 0.76	16.8 ± 0.957	45.3 ± 14	0.326 ± 0.00493	63.6 ± 2.48
$M_1 M_2$	71 ± 0.568	1.49 ± 0.216	0.151 ± 0.0866	0.06 ± 0.00212	11.1 ± 1.08
M_{4b}	63.4 ± 0.536	0.849 ± 0.191	0.151 ± 0.0866	0.0346 ± 0.00141	5.4 ± 0.776
Samples	CC ZZ	NC ZZ	Photo Prod	Total background	Significance
Initial	$7.36 \times 10^3 \pm 10.6$	338 ± 0.426	$2.1 \times 10^9 \pm 3.43 \times 10^6$	$2.36 \times 10^9 \pm 3.5 \times 10^6$	0.049
4 b and 1 light jets	678 ± 2.19	21.7 ± 0.0707	$7.36 \times 10^4 \pm 4.21 \times 10^3$	$1.07 \times 10^5 \pm 4.3 \times 10^3$	0.92
Electron rejection	678 ± 2.19	14 ± 0.0614	$6.23 \times 10^4 \pm 1.29 \times 10^3$	$7.65 \times 10^4 \pm 1.4 \times 10^3$	1.1
Forward jet	380 ± 1.64	1.04 ± 0.014	$1.43 \times 10^4 \pm 297$	$1.59 \times 10^4 \pm 3 \times 10^2$	1.8
\cancel{E}_T	342 ± 1.55	0.18 ± 0.00575	980 ± 21.9	$1.52 \times 10^3 \pm 35$	3.8
$\cancel{E}_T - \phi$ rejection	287 ± 1.42	0.1 ± 0.00427	440 ± 10.4	853 ± 18	4.3
$M_1 M_2$	16.8 ± 0.344	0.00613 ± 0.00117	54.4 ± 1.21	84.00 ± 1.68	6.9
M_{4b}	7.43 ± 0.229	0.00239 ± 0.000661	21.9 ± 0.63	35.78 ± 1.05	8.7

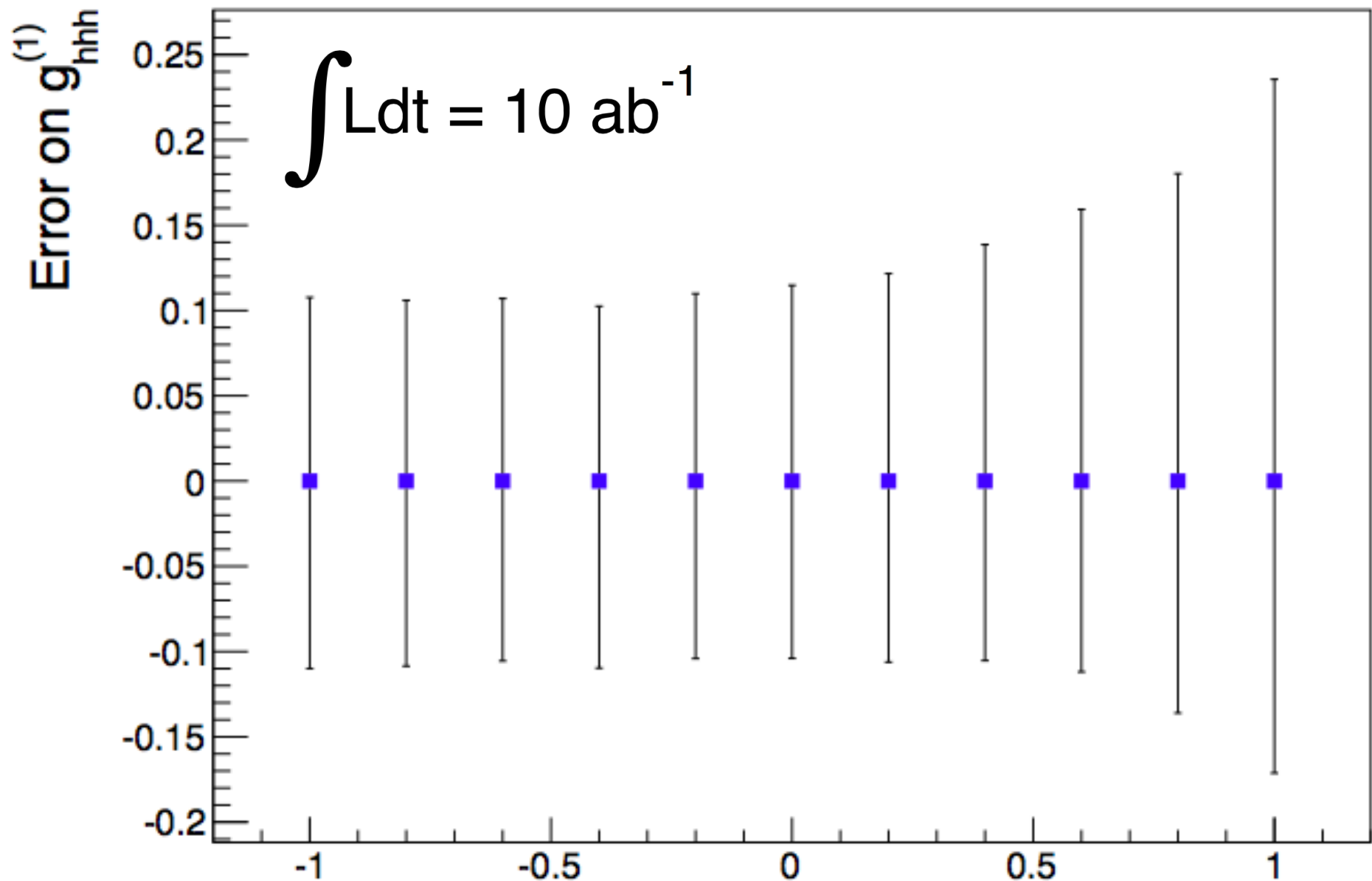
Table 6: Number of events after optimisation, and weighted with luminosity $\mathcal{L} = 10 \text{ ab}^{-1}$. The abbreviations CC(NC)Jet and CC(NC)Top accounts for the weighted sum of CC(NC) backgrounds 1, 2 and 4, 5 as given in Table 4. NCPhotoProd refer to weighted sums of all PHOTO-production.



significance



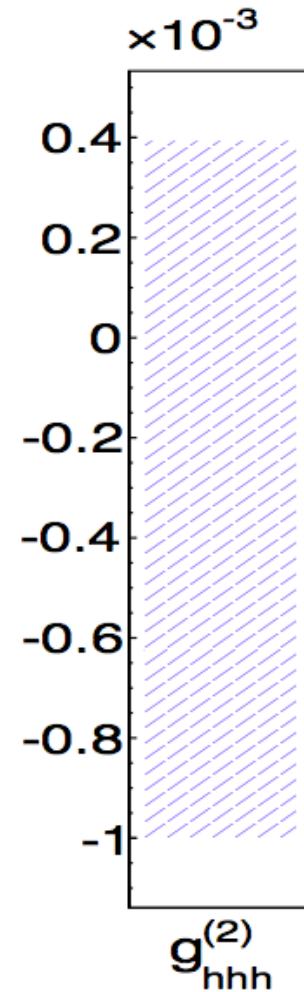
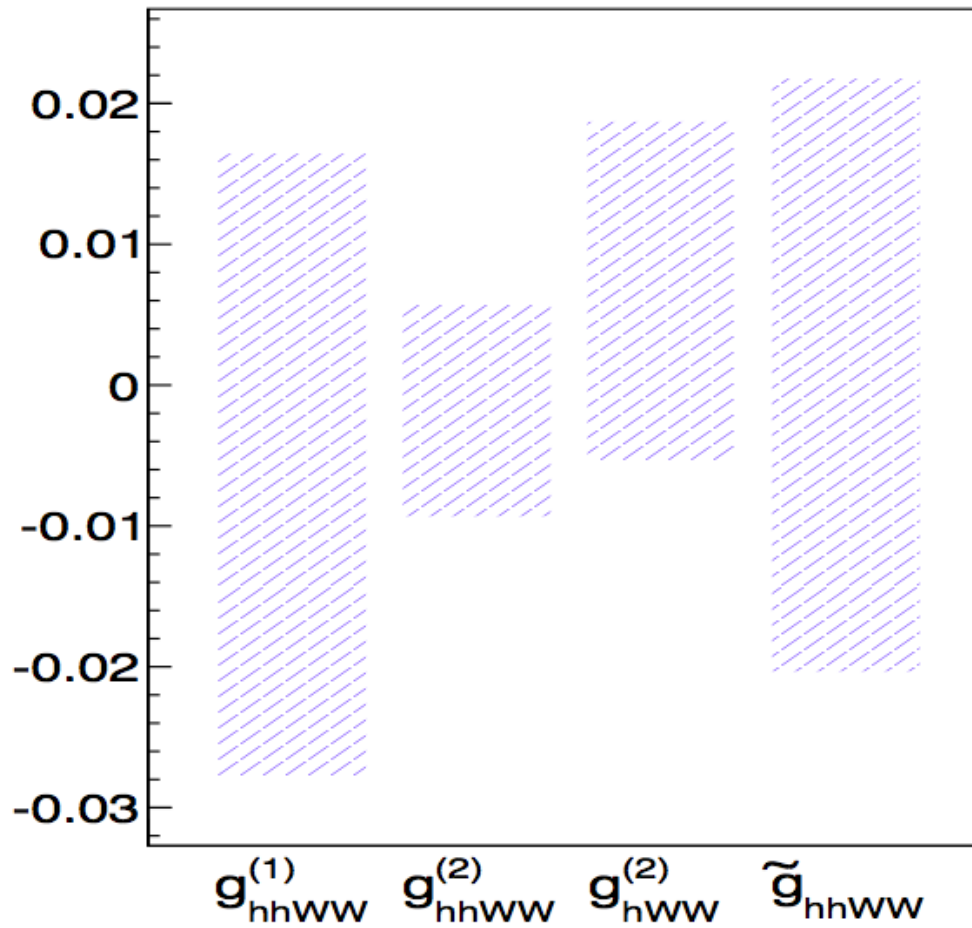
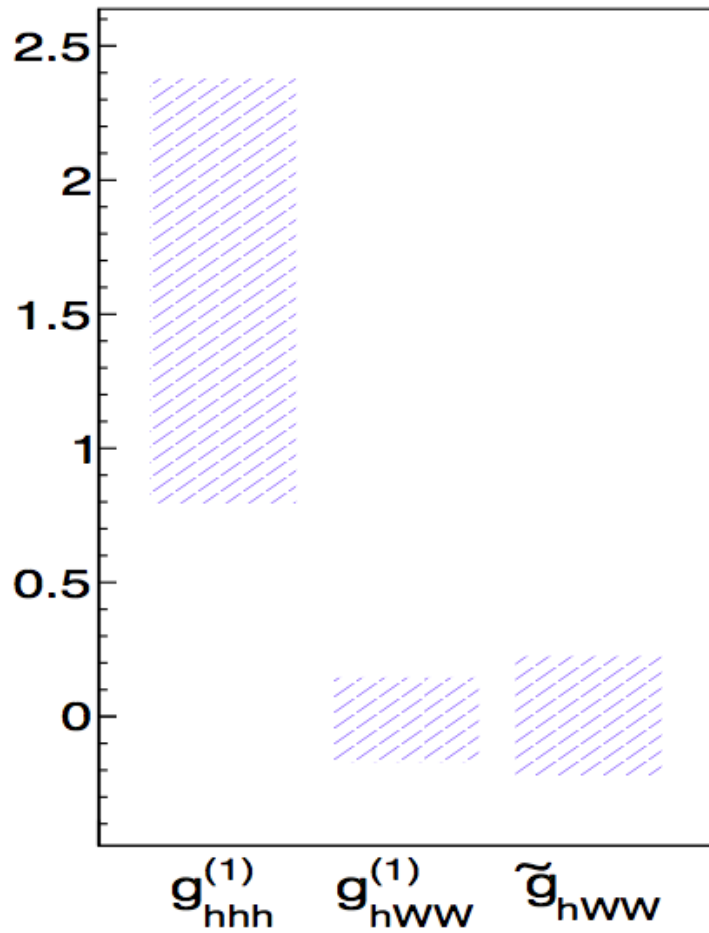
$g_{hhh}^{(1)}$



Error determination of λ , 20% for SM

$g_{hhh}^{(1)}$

$$\int \mathcal{L} dt = 0.4 \text{ ab}^{-1}$$



95% CL limits on different couplings

Outlook and Conclusions

- **First look at search for double Higgs boson production at high-energy collisions ep collisions**
 - **$E_e=60$ GeV, $E_p=50$ TeV. Highly asymmetric collisions. Requires very forward jet tagging and b-tagging**
 - **May achieve $S/B > 1$**
 - **May reach more than 5σ effect with 20% measurement of λ for 10 ab^{-1}**
 - **ep offers possibility of exploring structure of hhh , $hhWW$ couplings**
 - **Sensitivity to non-SM couplings explored**
- **Promising results, to be validated with full simulation studies**