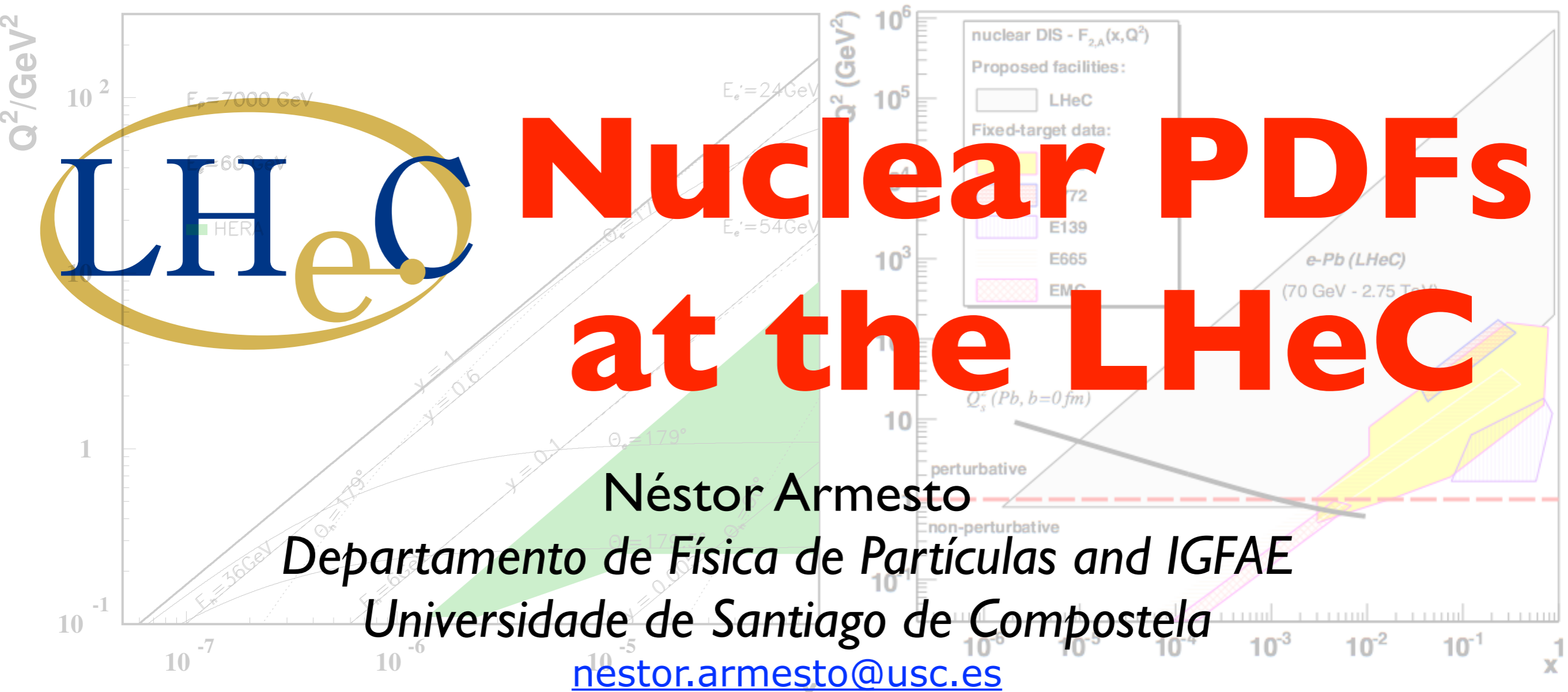


2015 LHeC Workshop
Chavannes-de-Bogis, June 26th 2015

LHeC - Low x Kinematics



with Hannu Paukkunen (Jyväskylä) and Max Klein (Liverpool)
for the LHeC Study group, <http://cern.ch/lhec>

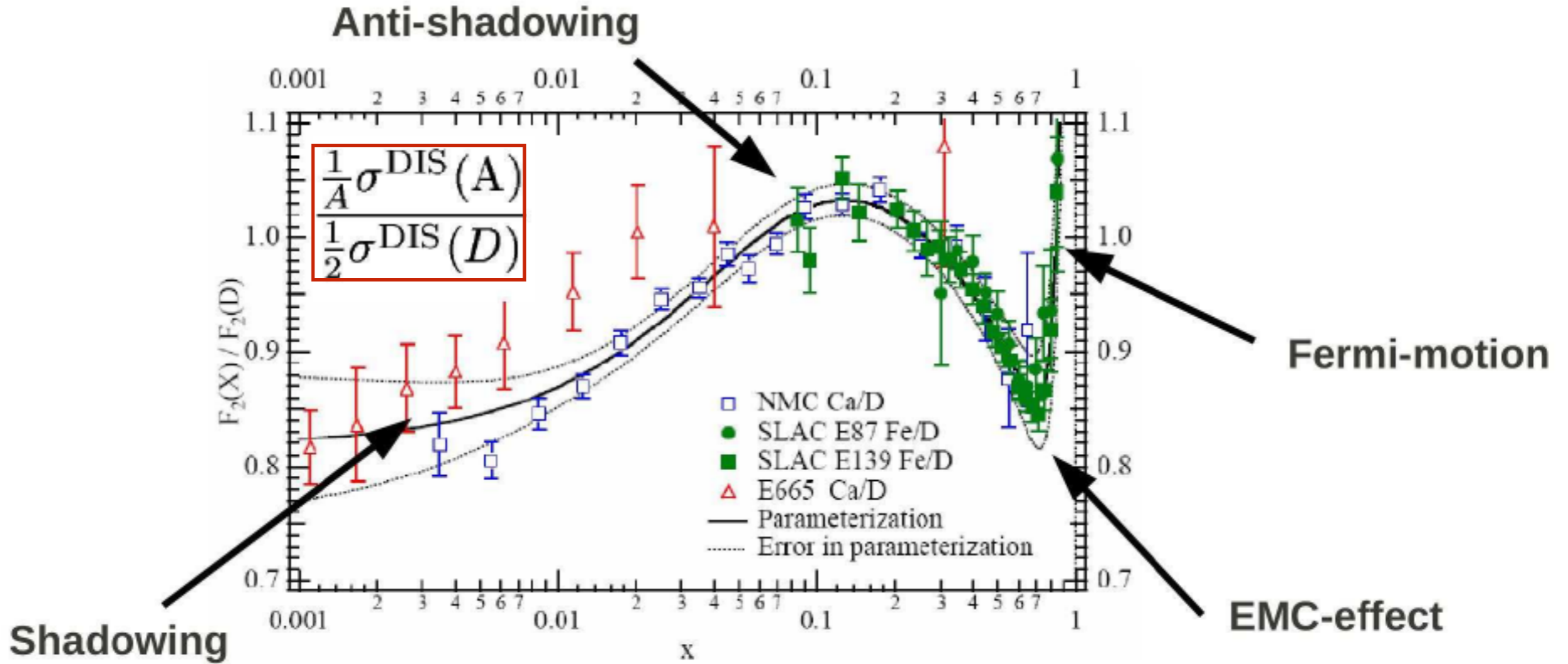
1. Present status.

2. The issue of the initial conditions.

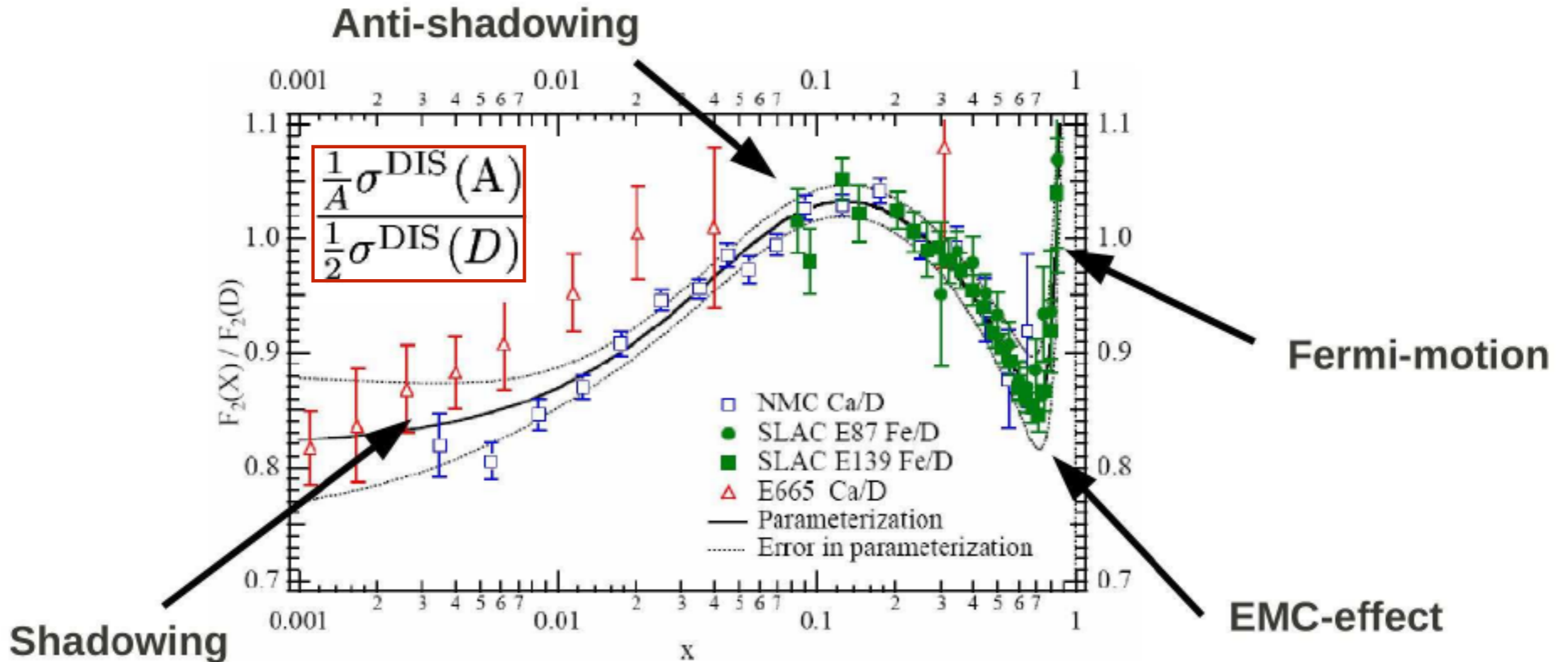
3. Results of the inclusion of LHeC pseudodata.

4. Conclusions and outlook.

Motivation:



Motivation:



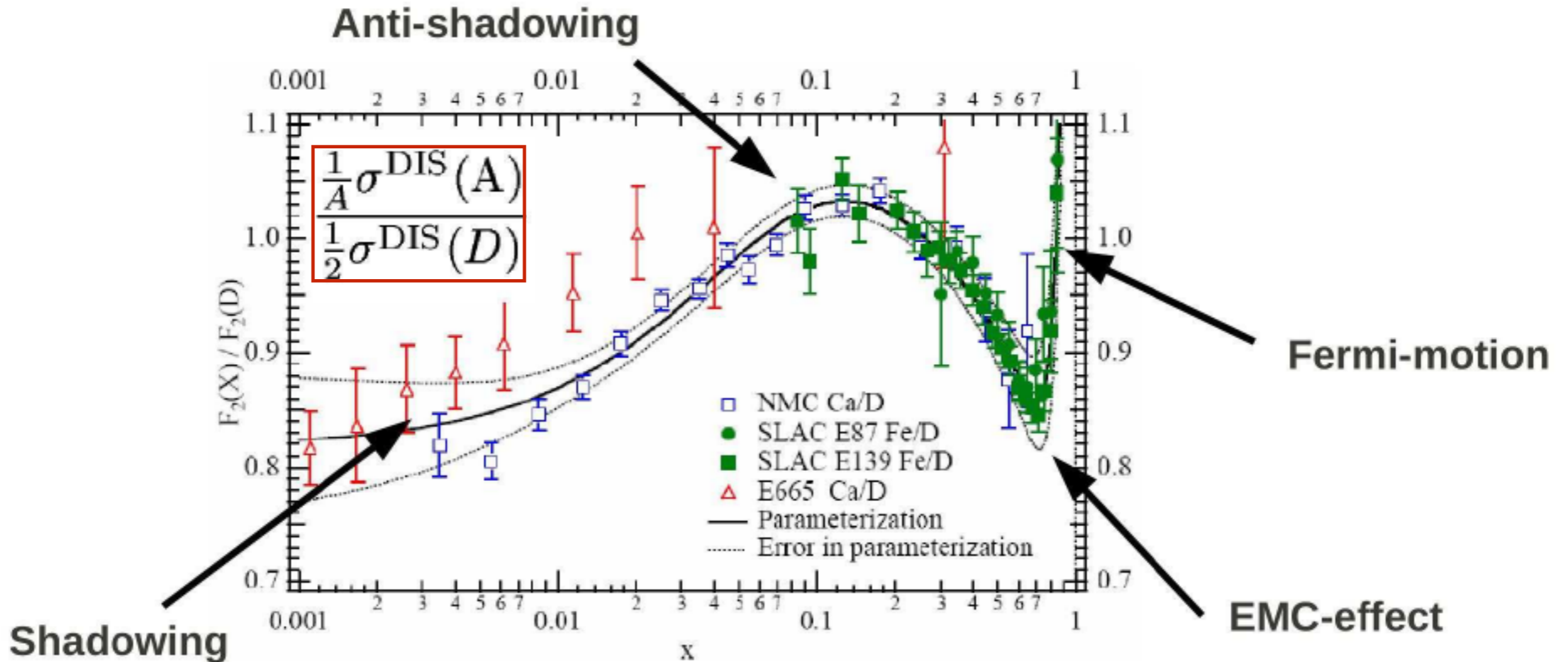
- Bound nucleon \neq free nucleon: search for process independent nPDFs that realise this condition.

$$\sigma_{\text{DIS}}^{\ell+A \rightarrow \ell+X} = \sum_{i=q, \bar{q}, g} \underbrace{f_i^A(\mu^2)}_{\text{Nuclear PDFs, obeying the standard DGLAP}} \otimes \underbrace{\hat{\sigma}_{\text{DIS}}^{\ell+i \rightarrow \ell+X}(\mu^2)}_{\text{Usual perturbative coefficient functions}}$$

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Usual perturbative coefficient functions

Motivation:



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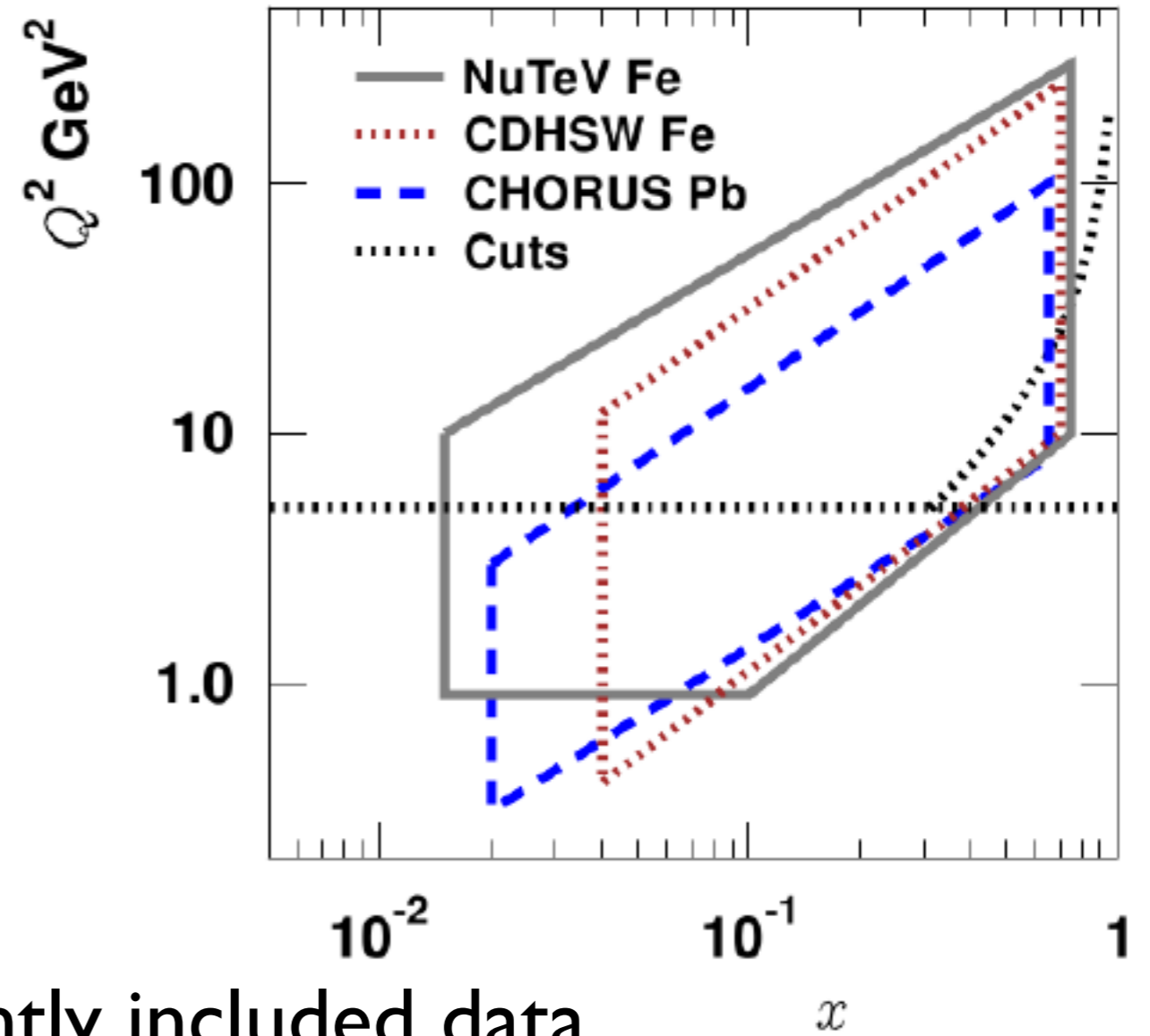
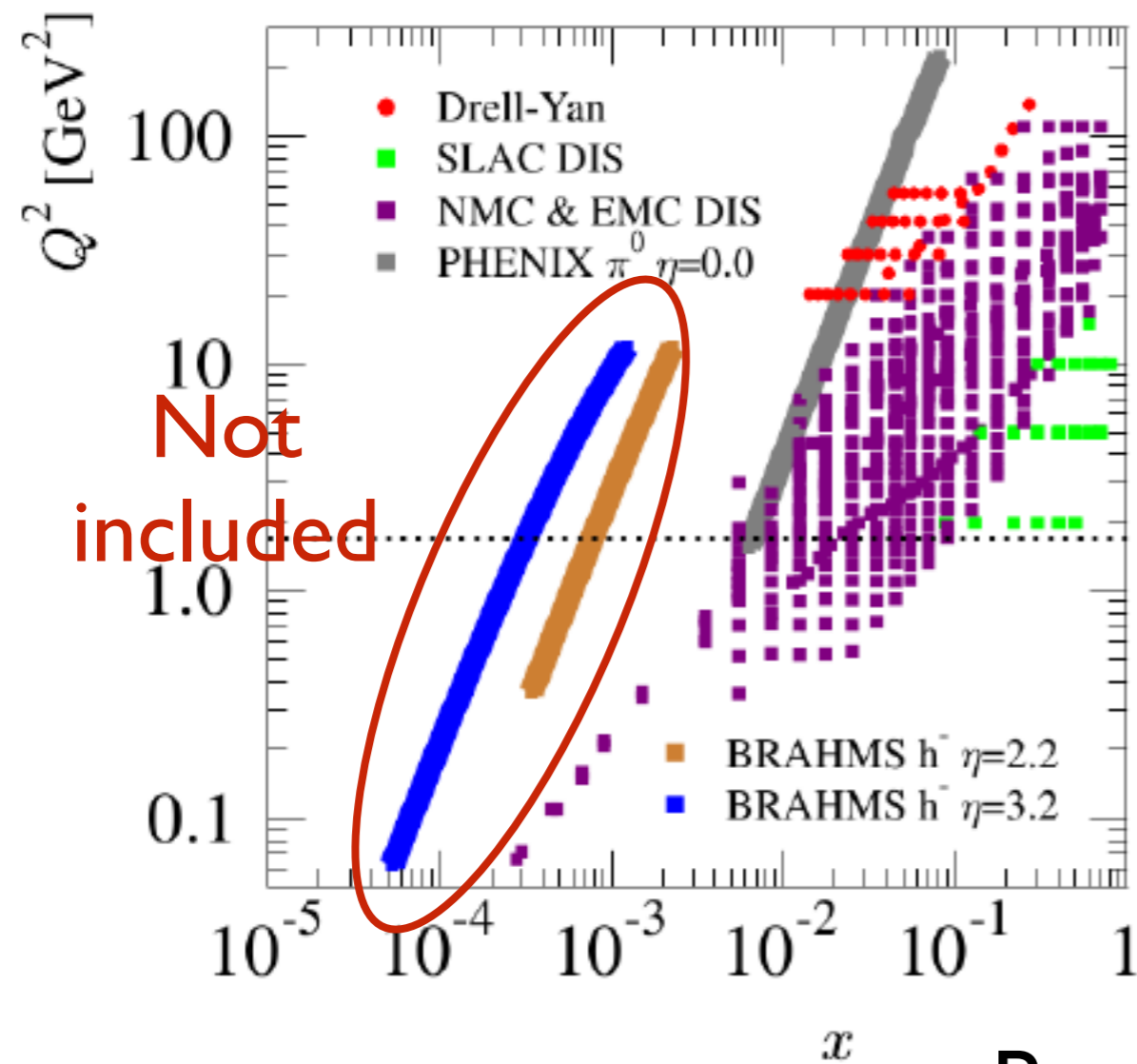
$$f_i^{p,A}(x, Q^2) = \underbrace{R_i^A(x, Q^2)} f_i^p(x, Q^2)$$

Contemporary sets:

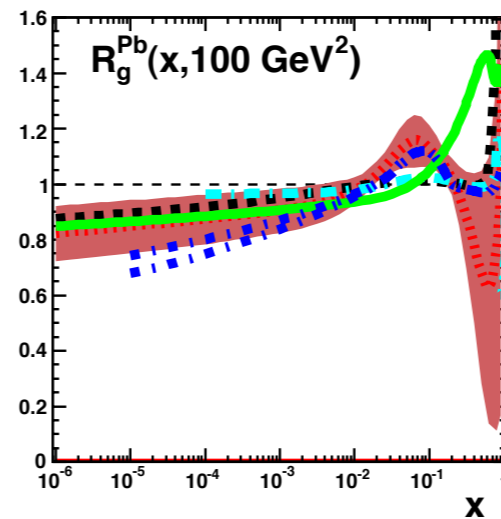
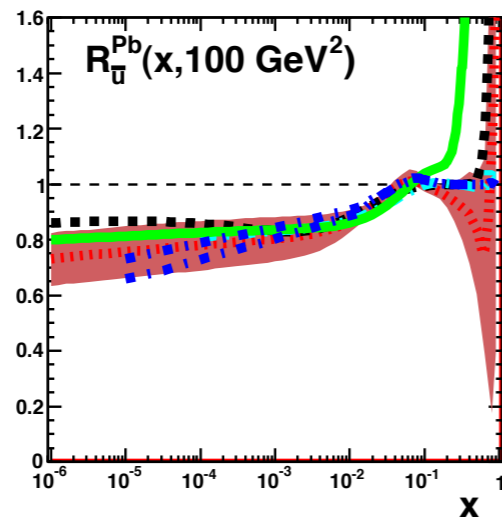
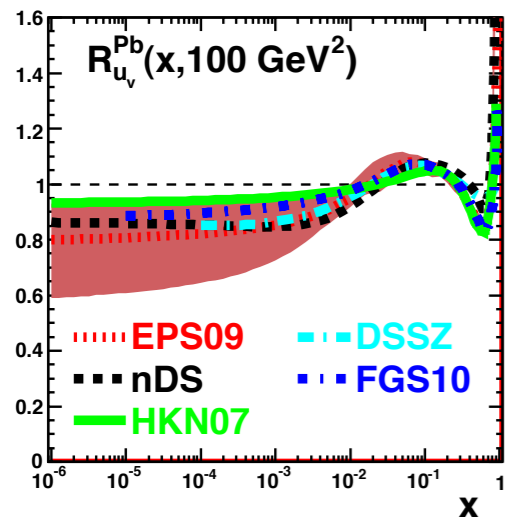
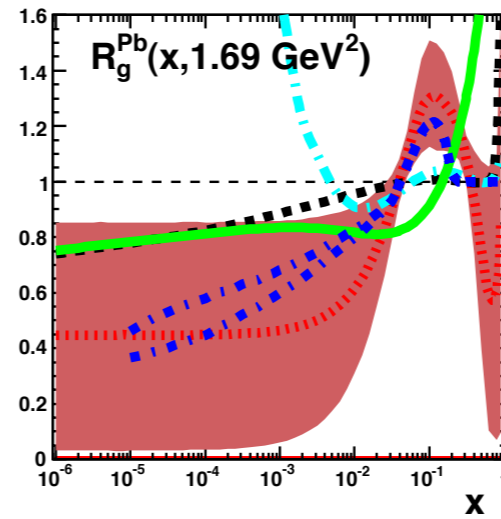
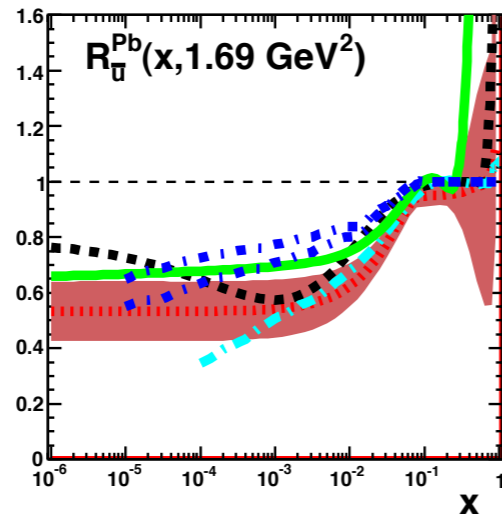
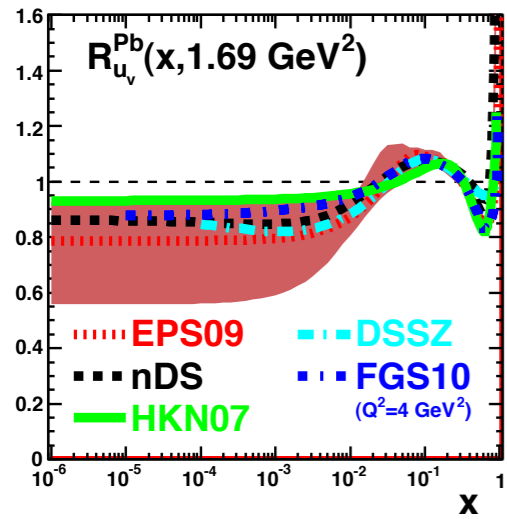
- Most commonly used sets:

	HKN07	EPS09	DSSZ	nCTEQ prelim.
Ref.	Phys. Rev. C76 (2007) 065207	JHEP 0904 (2009) 065	Phys.Rev. D85 (2012) 074028	arXiv:1307.3454
Order	LO & NLO	LO & NLO	NLO	NLO
Neutral current e+A / e+d DIS	√	√	√	√
Drell-Yan dileptons in p+A / p+d	√	√	√	√
RHIC pions in d+Au / p+p		√	√	
Neutrino-nucleus DIS			√	
Q ² cut in DIS	1GeV	1.3GeV	1GeV	2GeV
# of data points	1241	929	1579	708
Free parameters	12	15	25	17
Error sets available		√	√	√
Error tolerance $\Delta\chi^2$	13.7	50	30	35
Baseline	MRST98	CTEQ6.1	MSTW2008	CTEQ6M
Heavy quark treatment	ZM_VFNS	ZM_VFNS	GM_VFNS	GM_VFNS

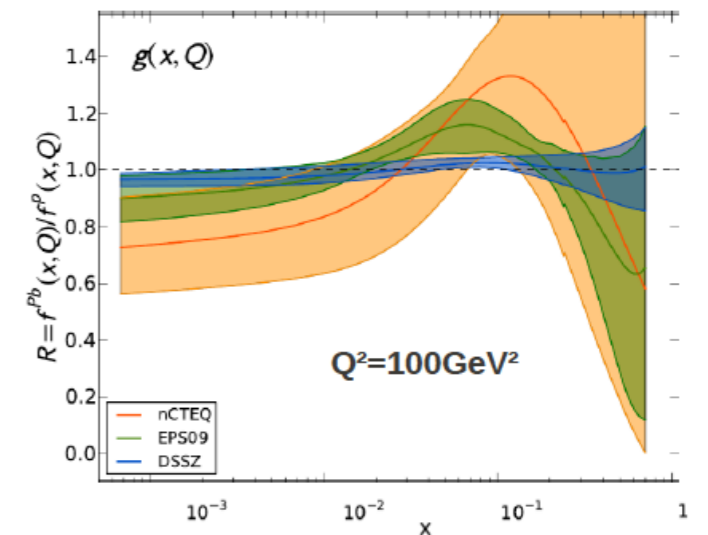
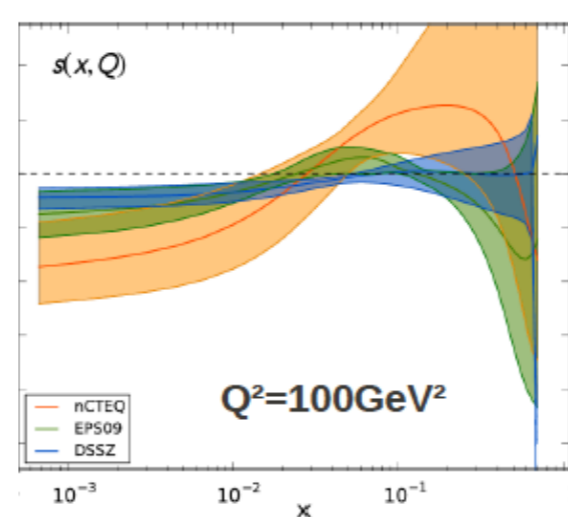
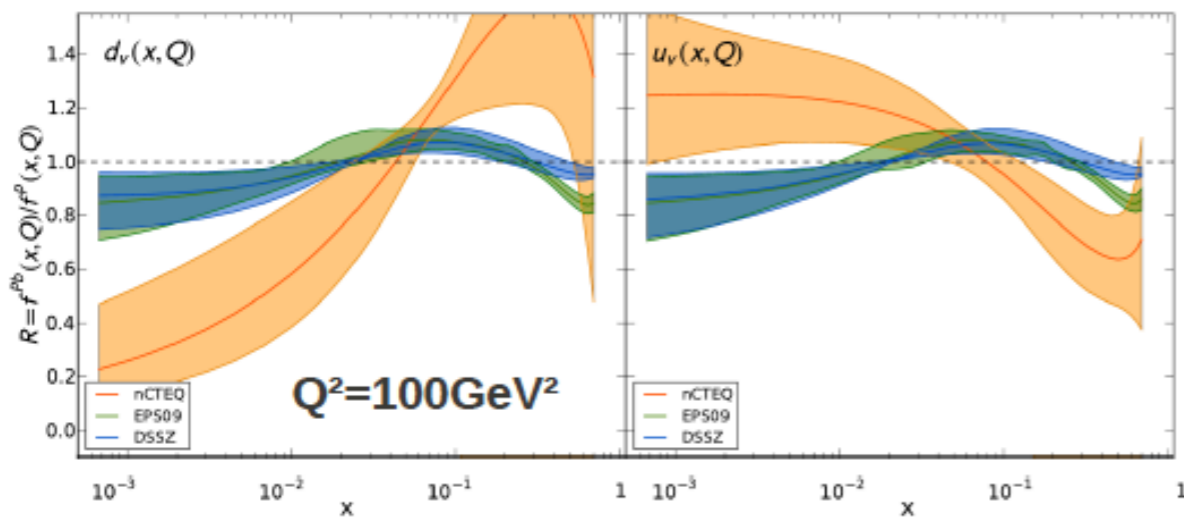
- Most commonly used sets:



Contemporary sets:



- Uncertainties where there are no data.
- Differences (valence with nCTEQ: d_v, u_v) due to assumptions and data included.



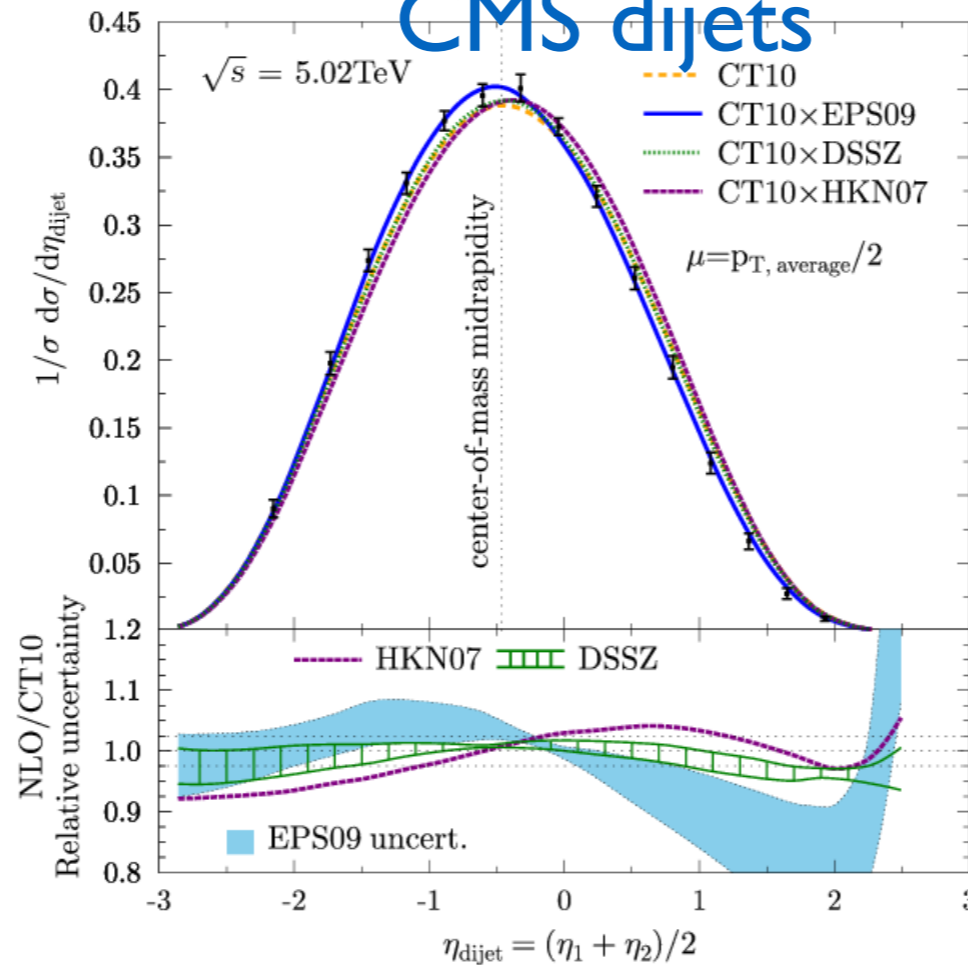
● **Jets and EW bosons:** at present used to test factorisation in pA/AA, and they offer some constrains to nPDFs (pPb@5 TeV/n).

● No sizeable in-medium effects e.g. energy loss.

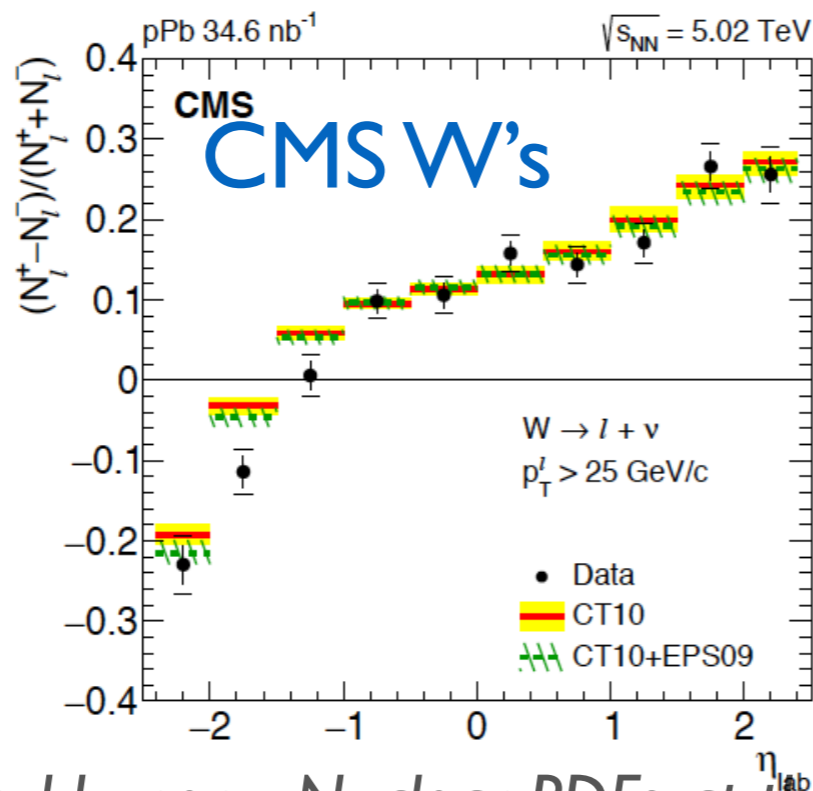
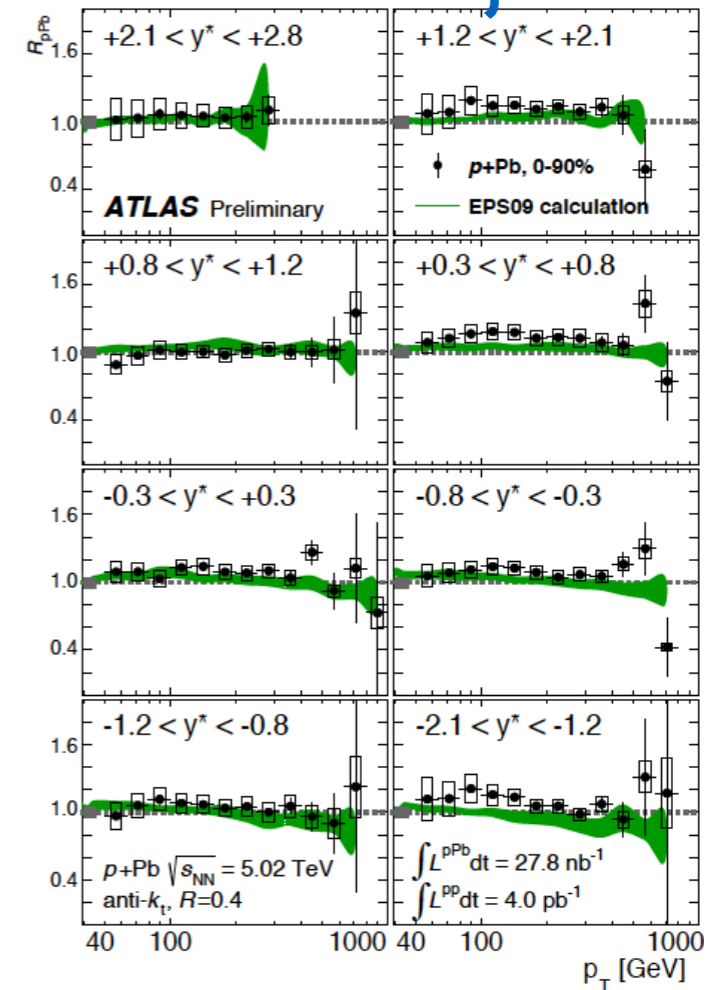
● Delicate centrality issues!!!

LHC?

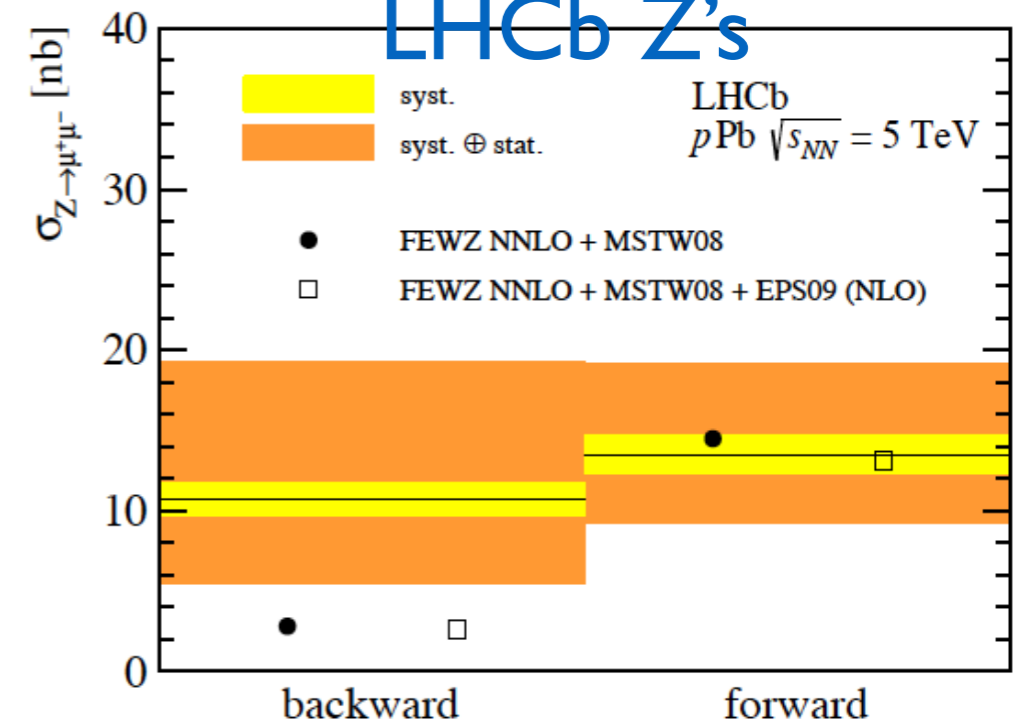
CMS dijets



ATLAS jets



LHCb Z's



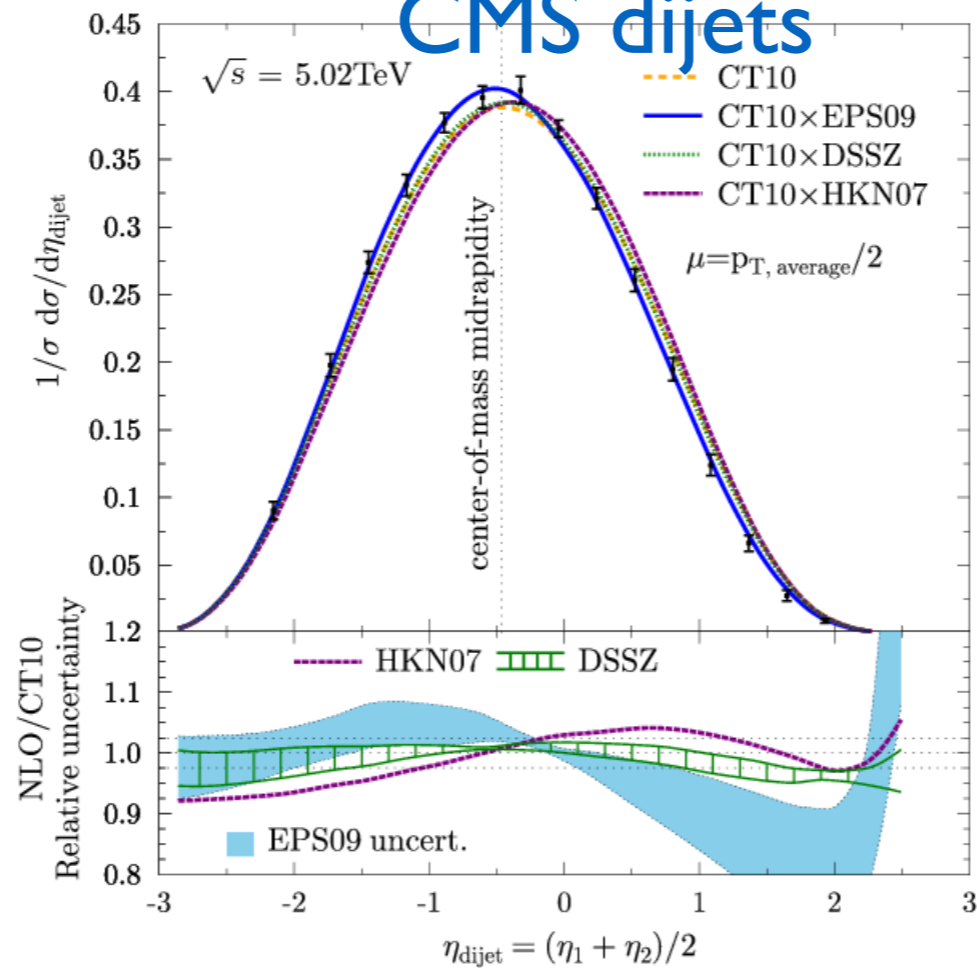
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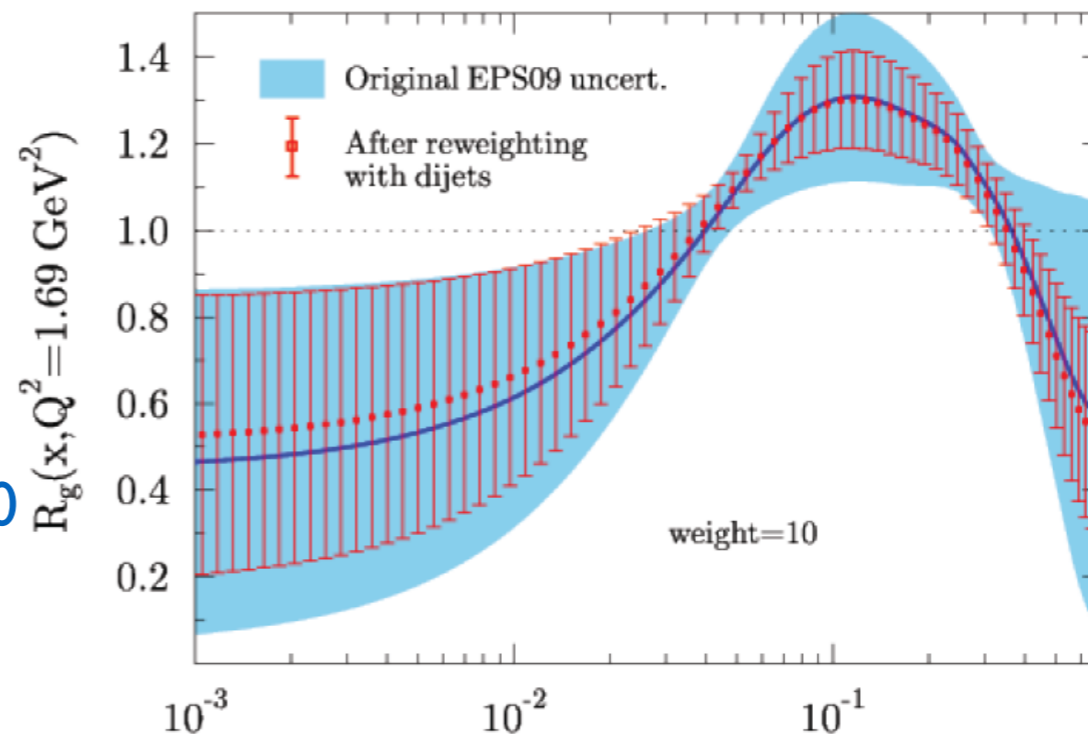
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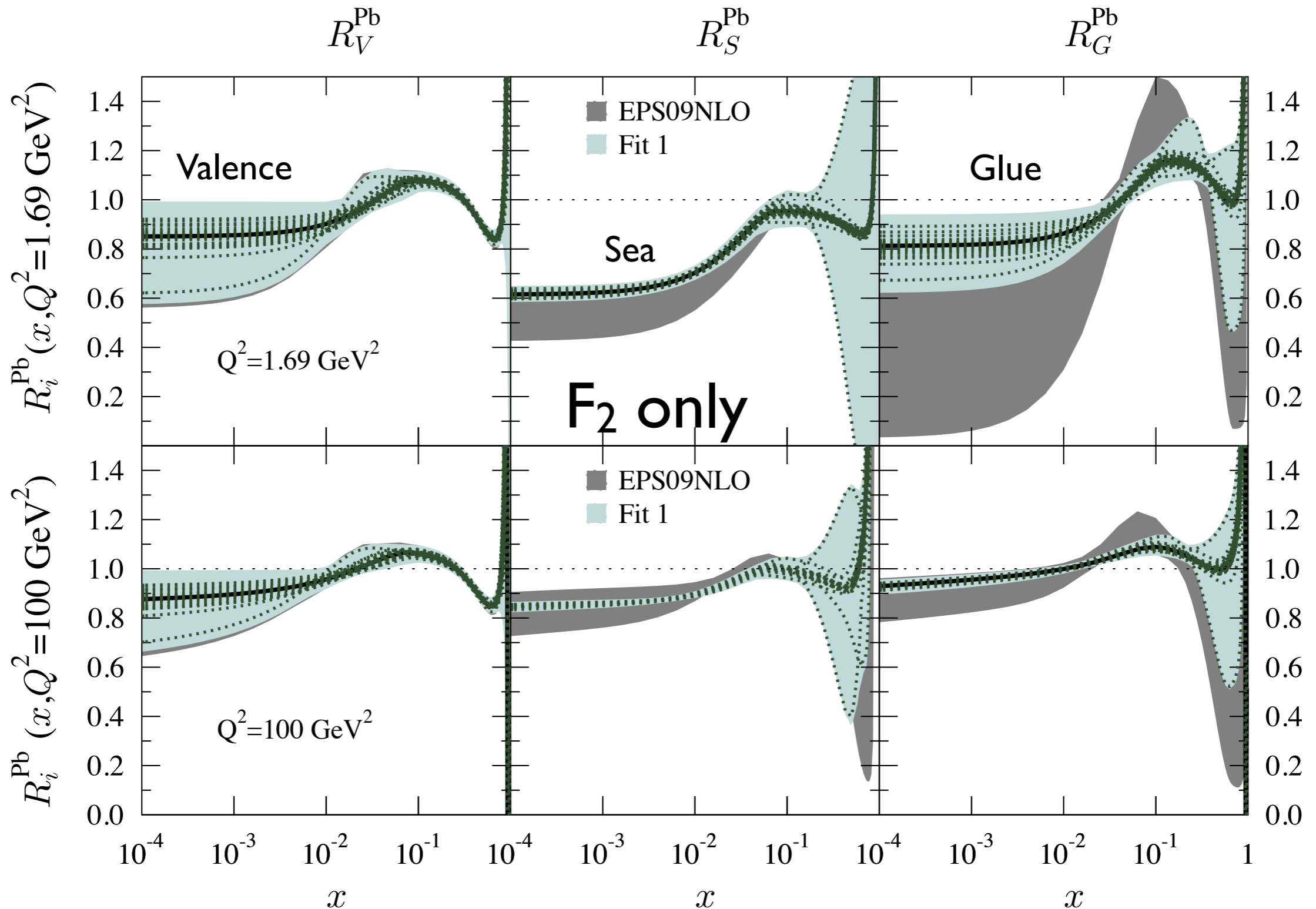
Hessian reweighting!!!
 Note: W's, Z's demands modifying assumptions in ICs.

1408.4563,
w=10 as RHIC π^0



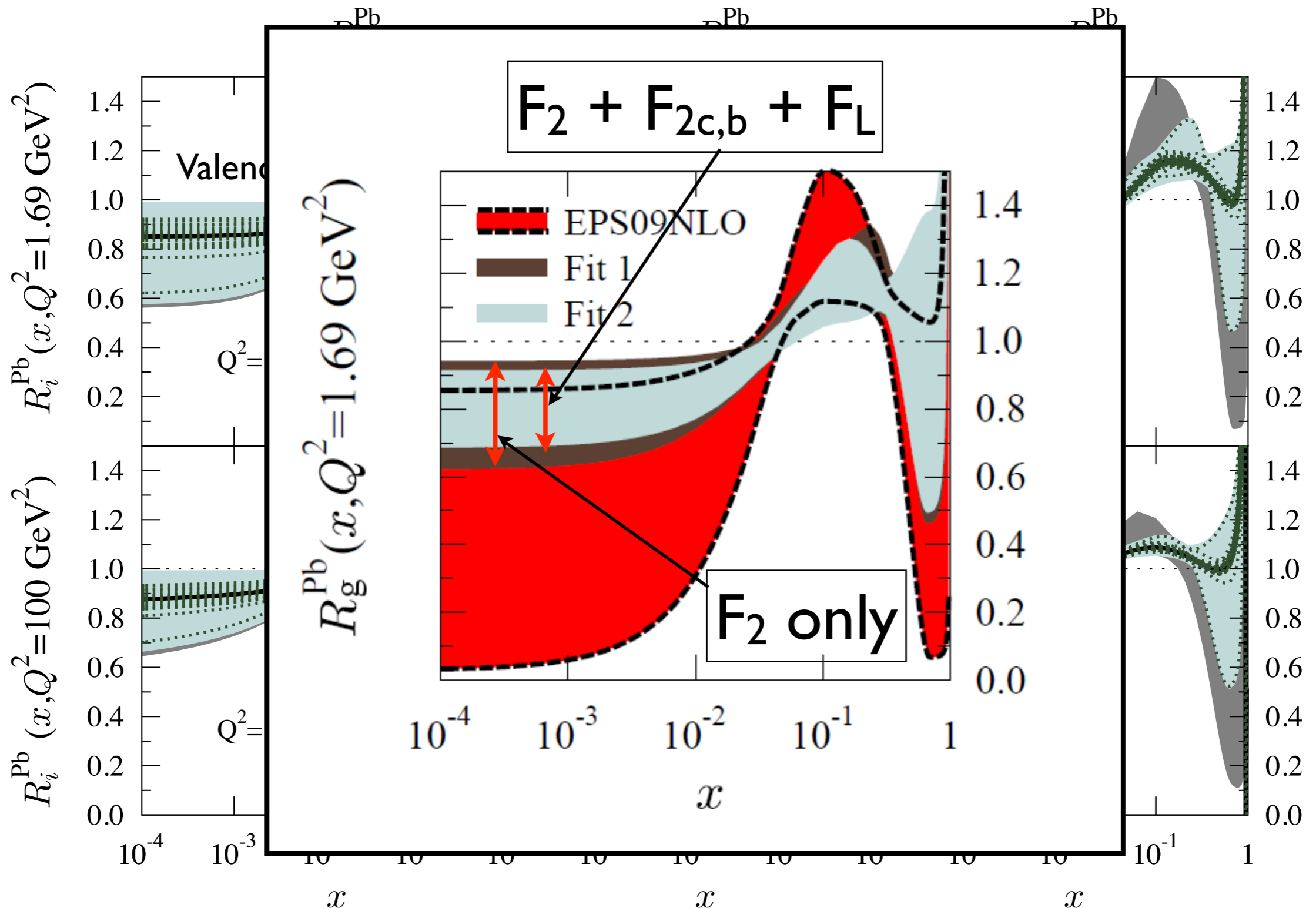
Previous LHeC studies: CDR

- Original EPS09 fit with one additional free parameter, small- x pseudodata.



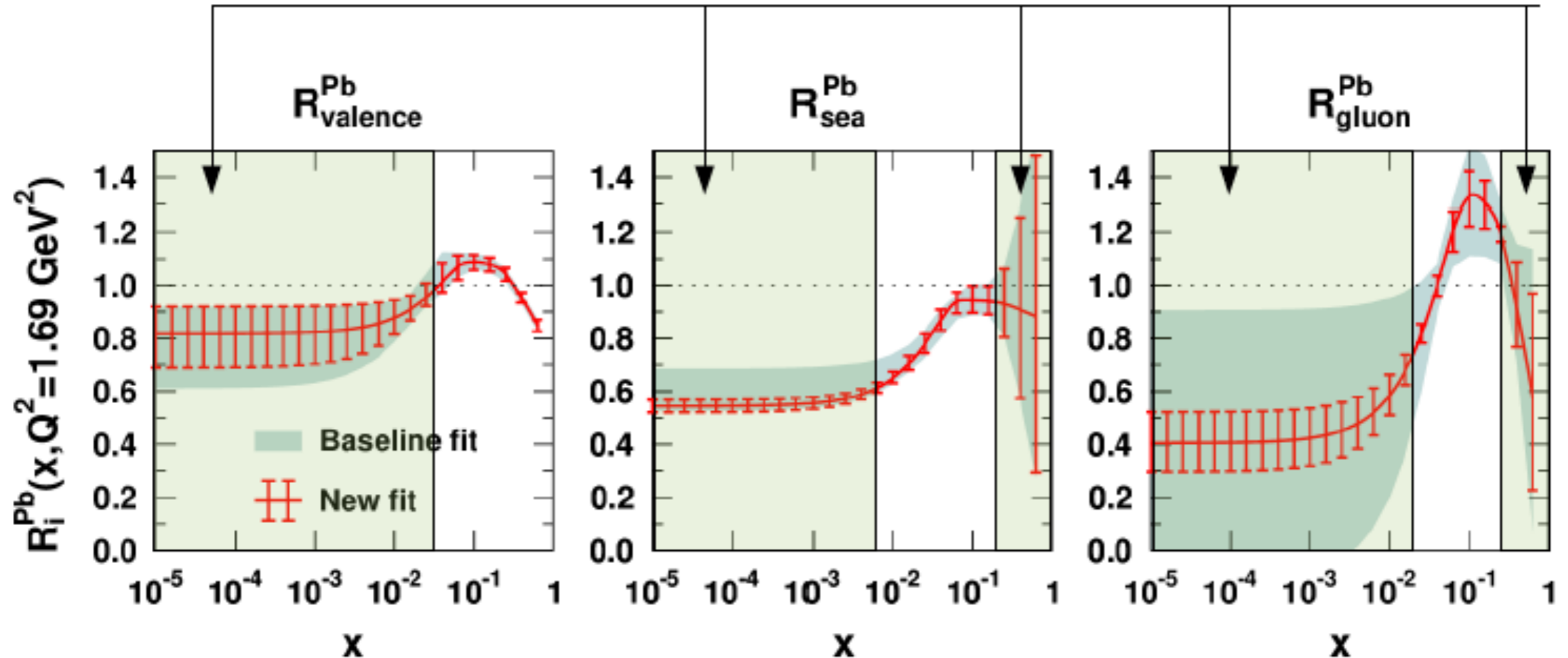
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- Reduced cross sections only, different energies, all x .

Currently no real data constraints!

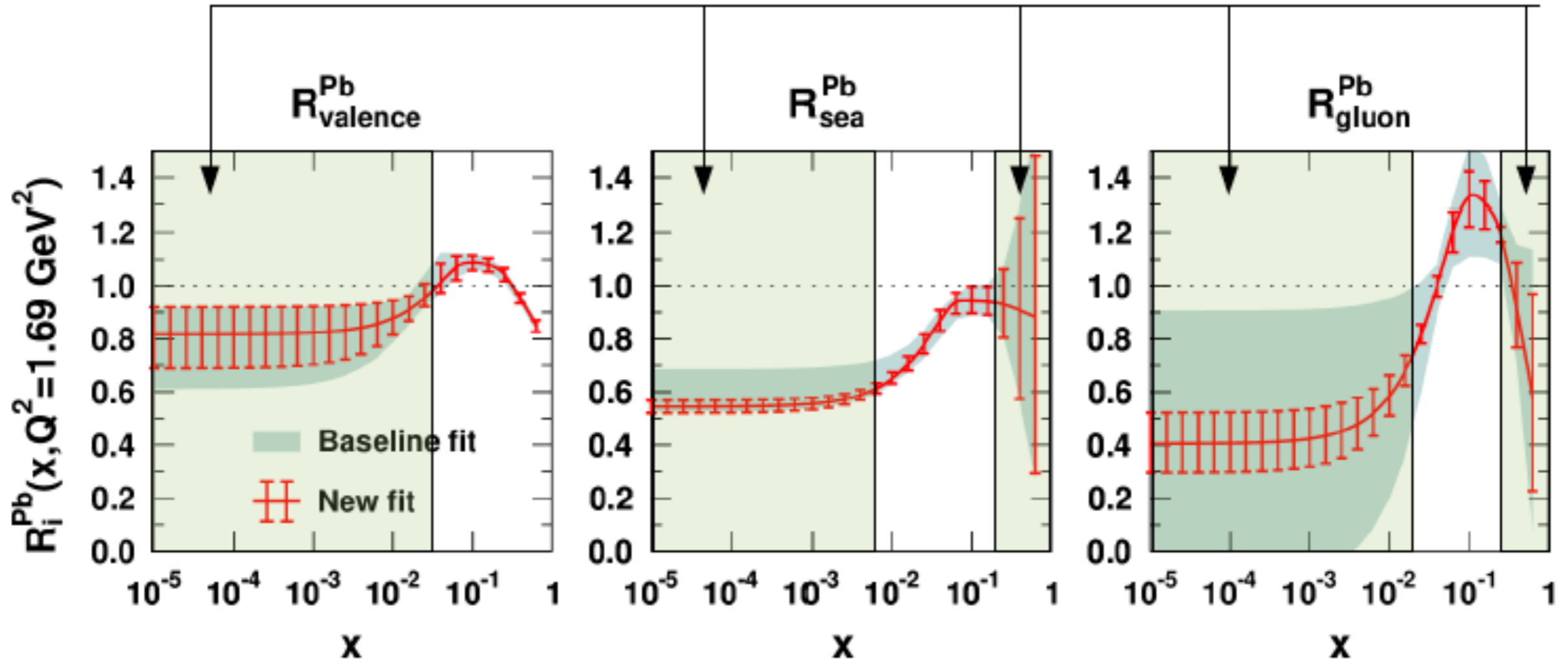


Hannu Paukkunen, LHeC workshop 140I

- **A drastic reduction in the small- x gluon and sea quark uncertainties**
- **More freedom in the fit function should be allowed – the baseline uncertainty probably underestimated**
- **Addition of charged-current data should give a handle on the flavor dependence, which is currently (practically) unconstrained**

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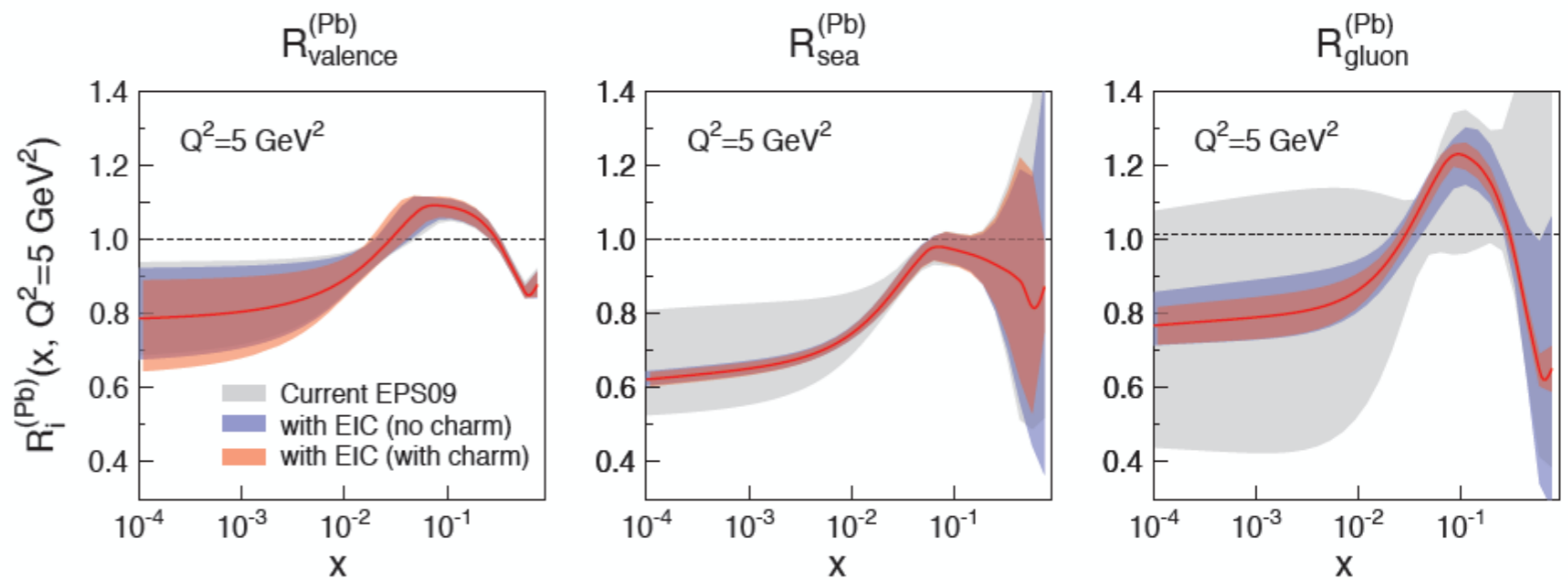
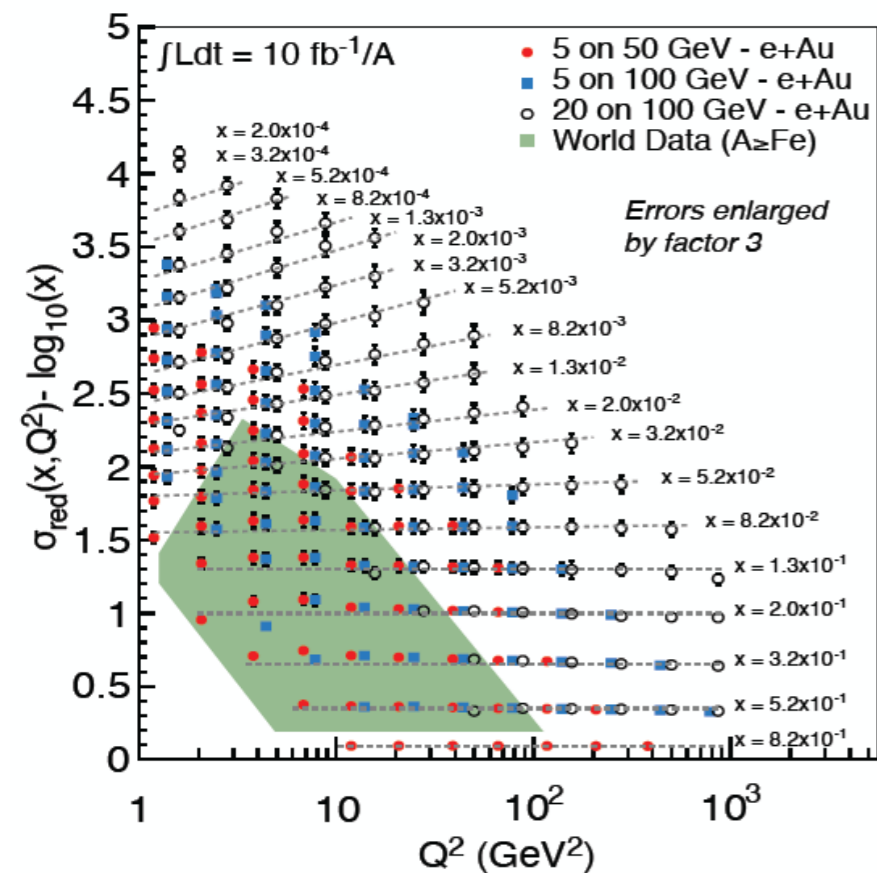
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ICs and uncertainties:

- Sensitivity to the mathematical form of the initial conditions is a well-known issue in proton PDFs: NNPDF, PDF4LHC recommendation of comparing different sets, HERAPDF2.0 studies,...
- In our case: determination of nPDFs beyond data...

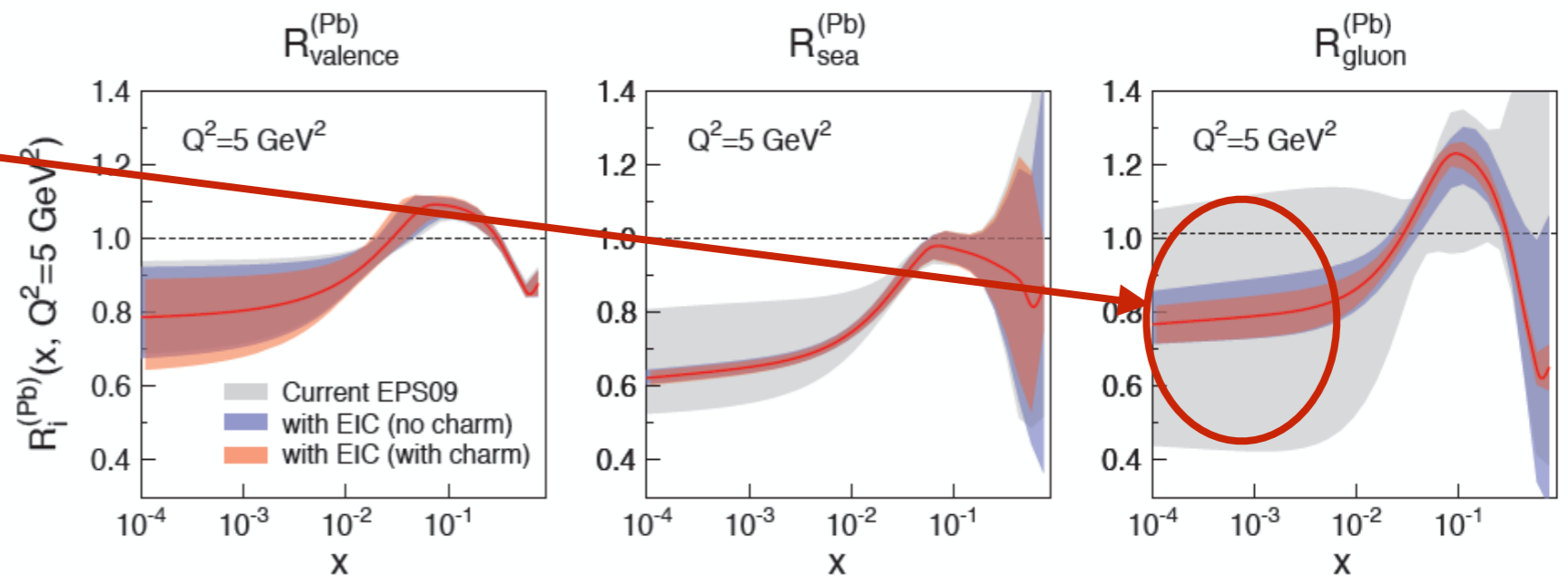
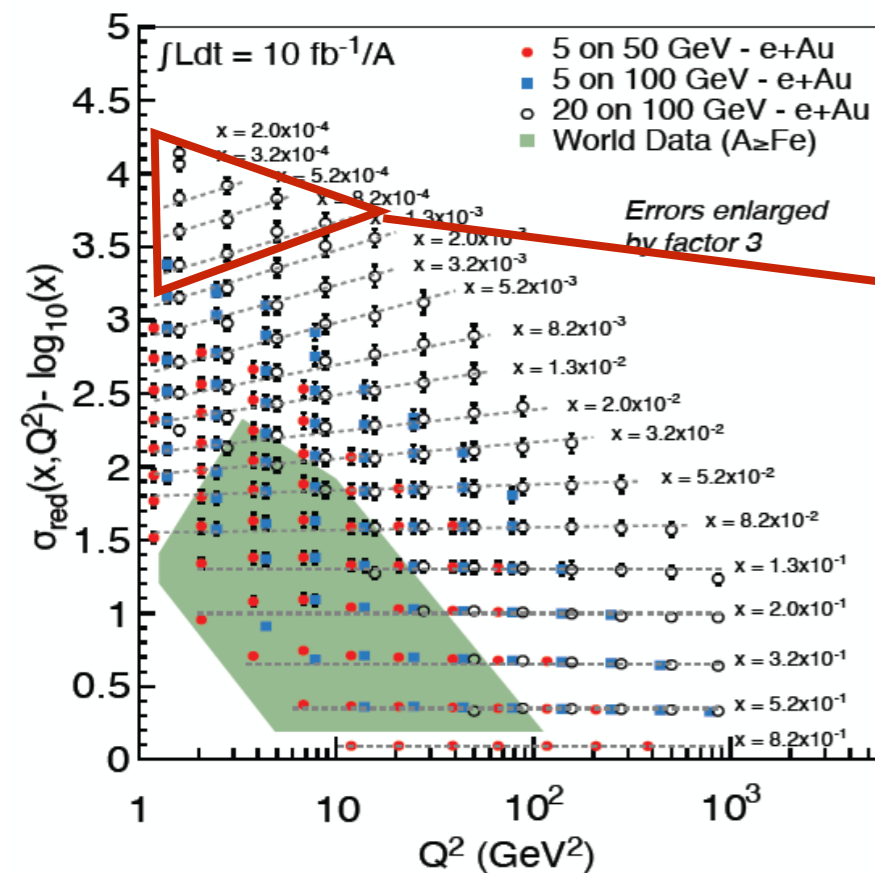


EIC example, Lamont at IS2014

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How?: mainly dictated by the shape of ICs



EIC example, Lamont at IS2014

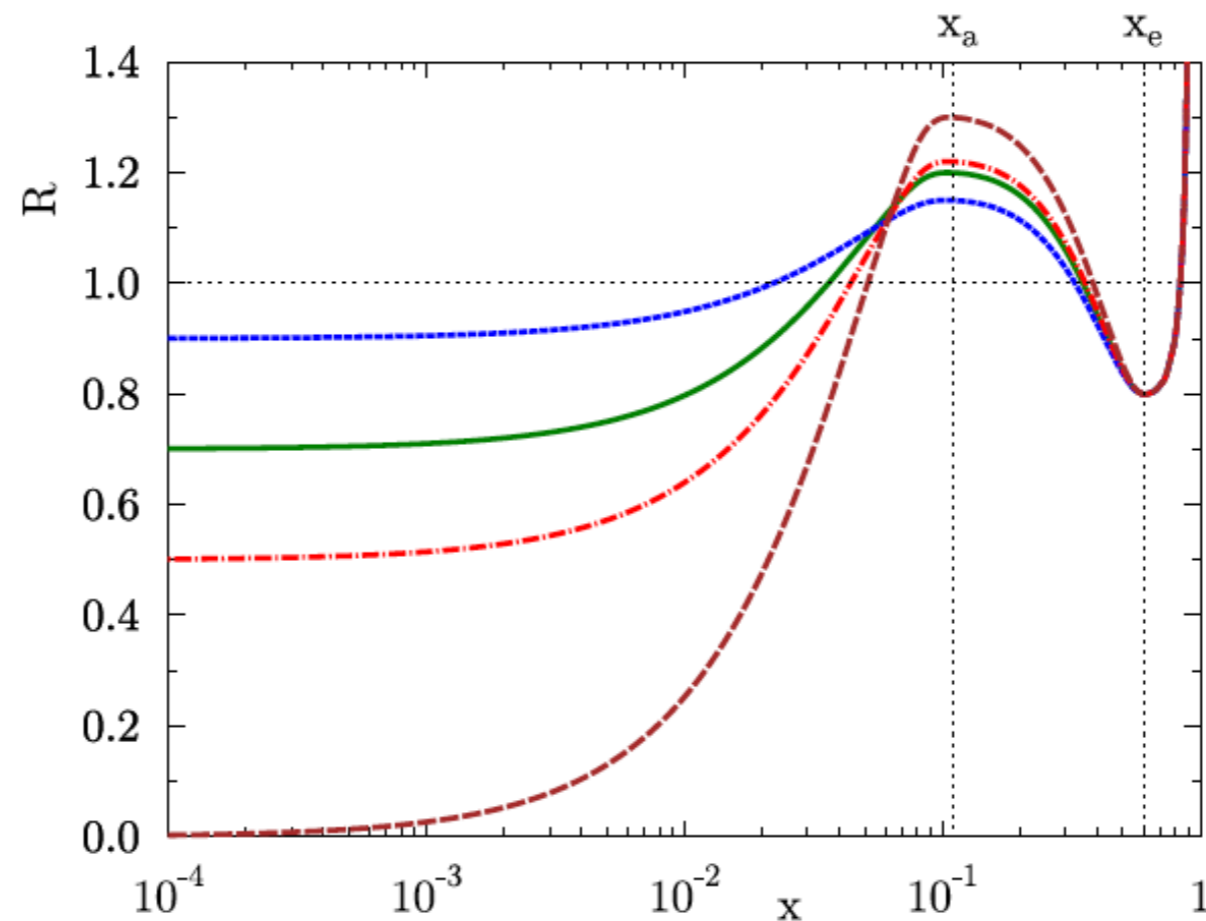
$$\frac{\partial R_{F_2}^A(x, Q^2)}{\partial \log Q^2} \approx \frac{10\alpha_s}{27\pi} \frac{xg(2x, Q^2)}{\frac{1}{2}F_2^D(x, Q^2)} \left\{ R_g^A(2x, Q^2) - R_{F_2}^A(x, Q^2) \right\} \quad \text{hep-ph/0201256}$$

- Very little freedom at small x .

The fit function in EPS09:

$$R^{\text{EPS09}}(x) = \begin{cases} a_0 + (a_1 + a_2 x) (e^{-x} - e^{-x_a}) & x \leq x_a \\ b_0 + b_1 x + b_2 x^2 + b_3 x^3 & x_a \leq x \leq x_e \\ c_0 + (c_1 - c_2 x) (1 - x)^{-\beta} & x_e \leq x \leq 1 \end{cases}$$

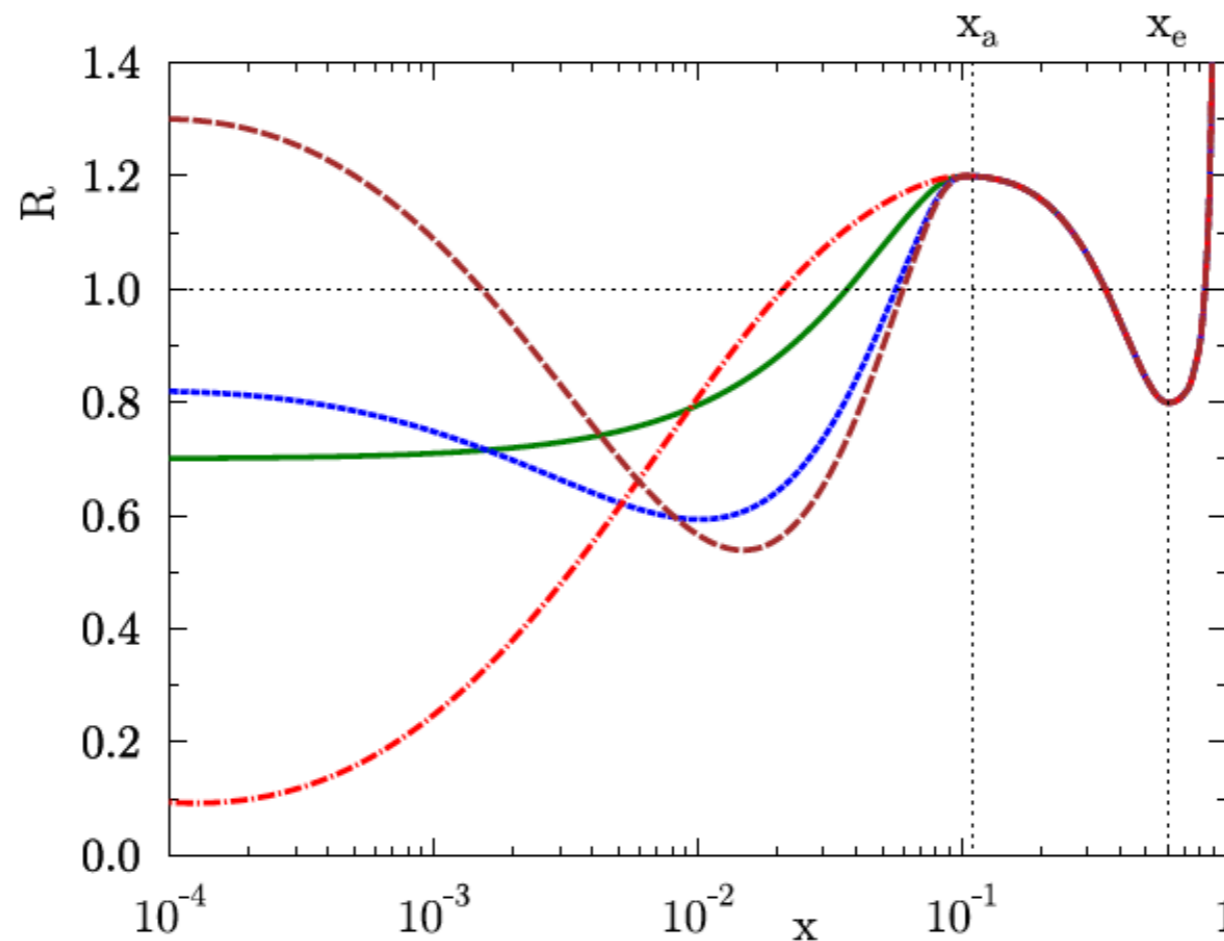
(power-law parametrization of A -dependence at x_a , x_e , and $x \rightarrow 0$)



New ICs:

- Use a far more flexible form to reduce the bias at small x :

$$R(x \leq x_a) = a_0 + a_1(x - x_a)^2 + \sqrt{x}(x_a - x) \left[a_2 \log\left(\frac{x}{x_a}\right) + a_3 \log^2\left(\frac{x}{x_a}\right) + a_4 \log^3\left(\frac{x}{x_a}\right) \right]$$



New fit framework:

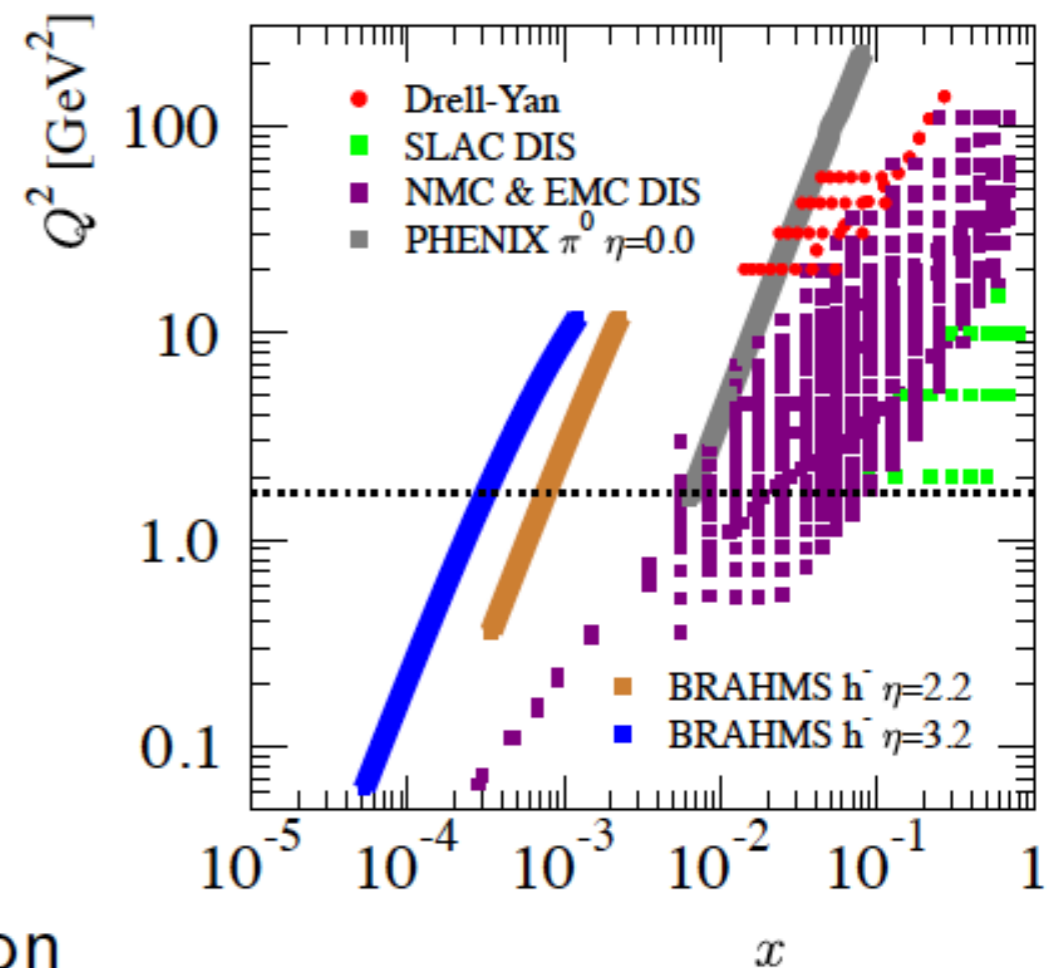
- Include the same data (DIS, Drell-Yan, inclusive π^0) as in EPS09 (no LHC data yet) plus LHeC (neutral current) pseudo data.
- CTEQ6.6 as baseline (doesn't really matter which one)
- Flavour-independent nuclear modifications at $Q_0 = 1.3 \text{ GeV}$

$R_V(x, Q_0)$ for both valence quarks

$R_S(x, Q_0)$ for light sea quarks

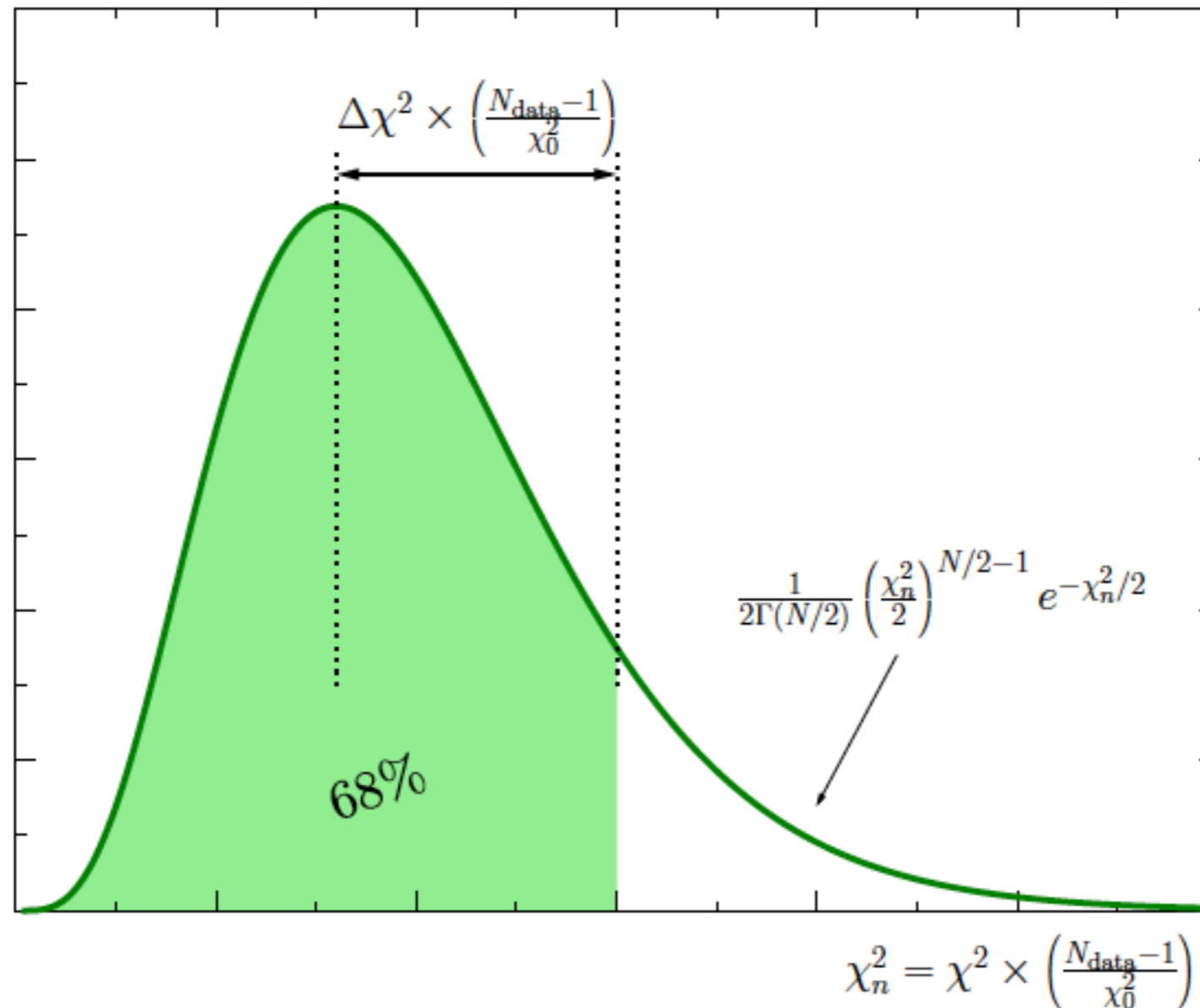
$R_G(x, Q_0)$ for gluons

- Charged-current data will be added later on to study the flavour dependence
- Cross-sections at NLO in the SACOT heavy-quark scheme (as CTEQ6.6)
- Robust Levenberg-Marquardt minimization method



New fit framework:

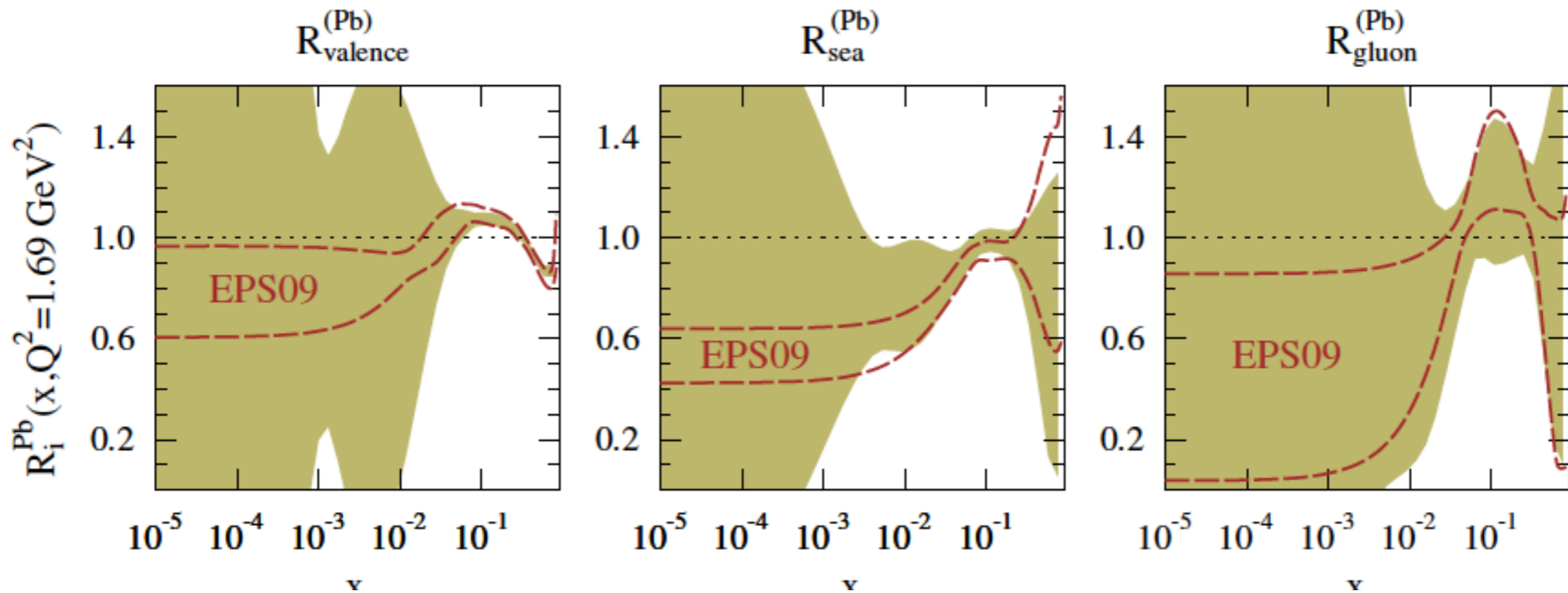
Standard Hessian uncertainty analysis (a la CTEQ, MSTW,...) with $\Delta\chi^2$ determined from the expected behaviour of probability distribution for the global χ^2



Gives $\Delta\chi^2 \approx 17$ (without or with the pseudodata)

New fit framework:

The baseline fit using the new fit functions: no control over small x !



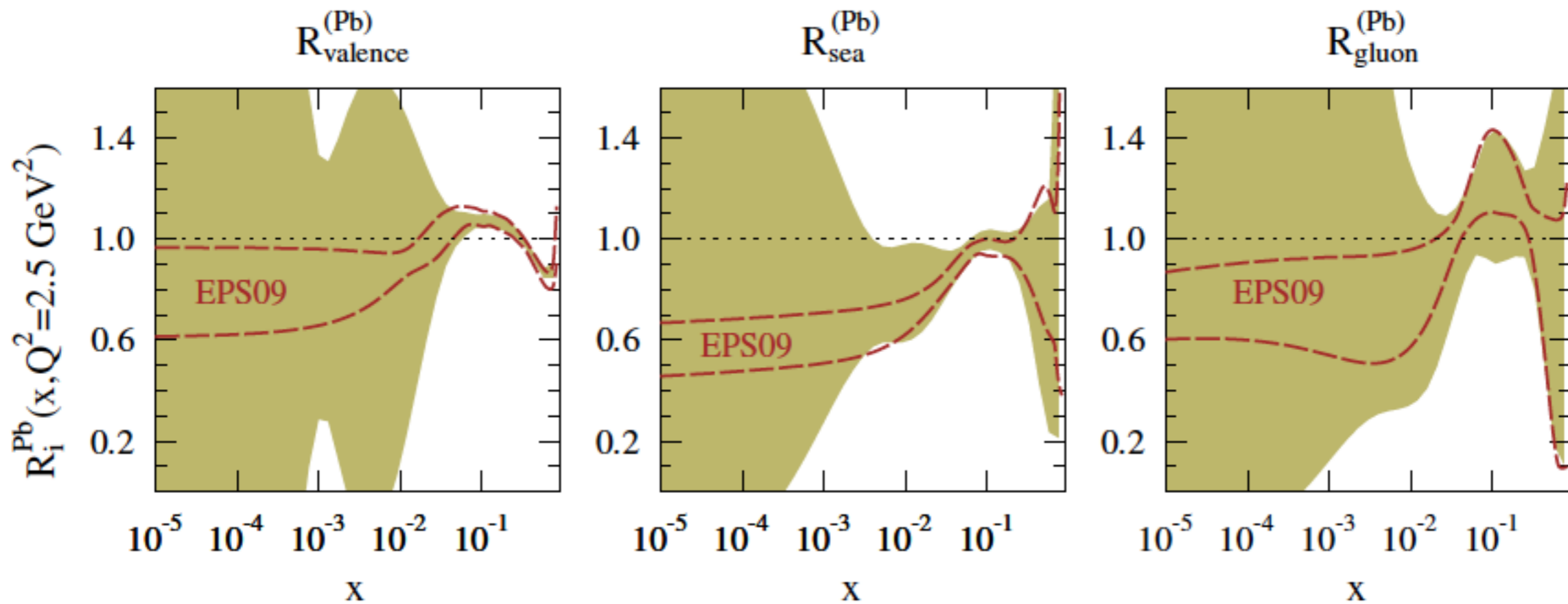
The lower bound restricted here by $F_L(Q^2 = 2 \text{ GeV}^2, x > 10^{-5}) > 0$

Maybe against “physical intuition” (small- x theory predicts shadowing, $R_i < 1$), but consistent with the data.

E.g. in EPS09, small- x shadowing was essentially built in

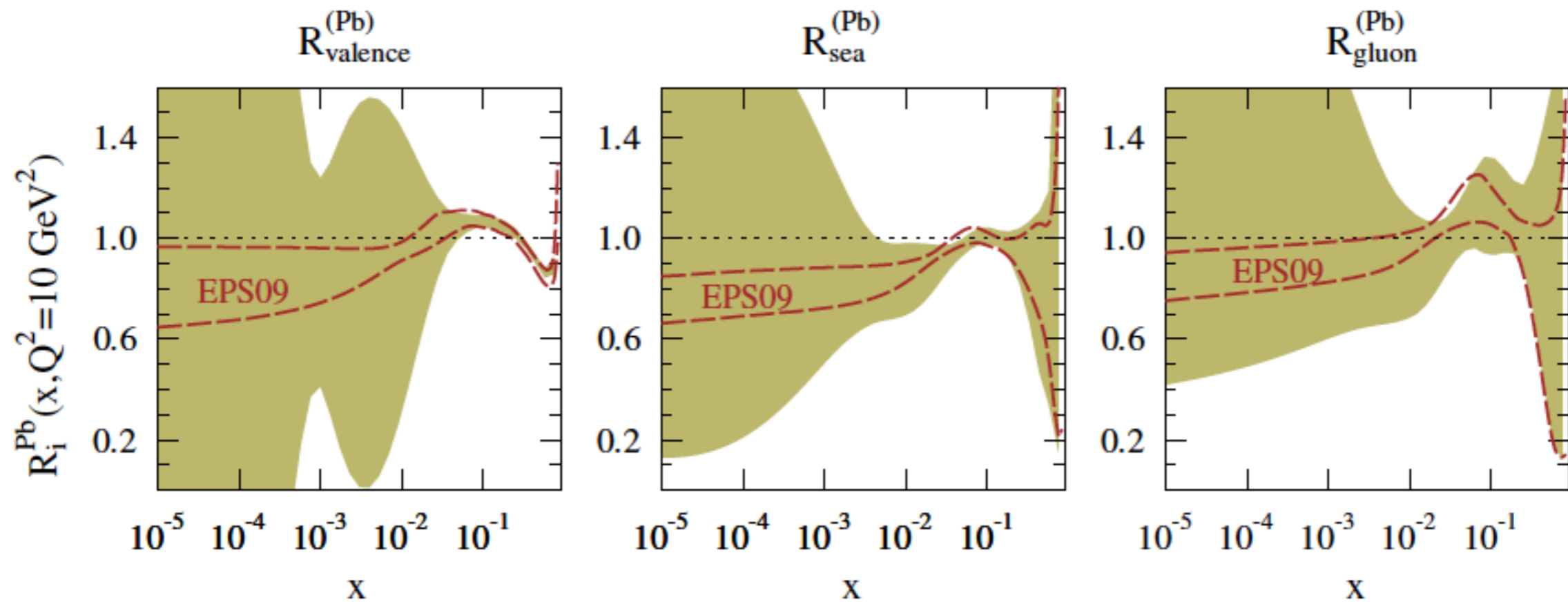
New fit framework:

The Q^2 dependence partly smooths out the differences in gluons



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1. Present status.

2. The issue of the initial conditions.

3. Results of the inclusion of LHeC pseudodata.

4. Conclusions and outlook.

Pseudodata:

- Assume $\mathcal{L}_{ep} = 10 \text{ fb}$, $\mathcal{L}_{e\text{Pb}} = 1 \text{ fb}$ (per nucleon)
- Top LHC energies: 7/2.75 TeV/nucleon.
- The pseudodata are obtained from ratios of reduced cross sections σ^i and relative uncertainties $\delta_{\text{uncor.}}^i$ and $\delta_{\text{norm.}}$ by

$$R_i = R_i(\text{EPS09}) \times [1 + \delta_{\text{uncor.}}^i r^i + \delta_{\text{norm.}} r^{\text{norm.}}]$$

where

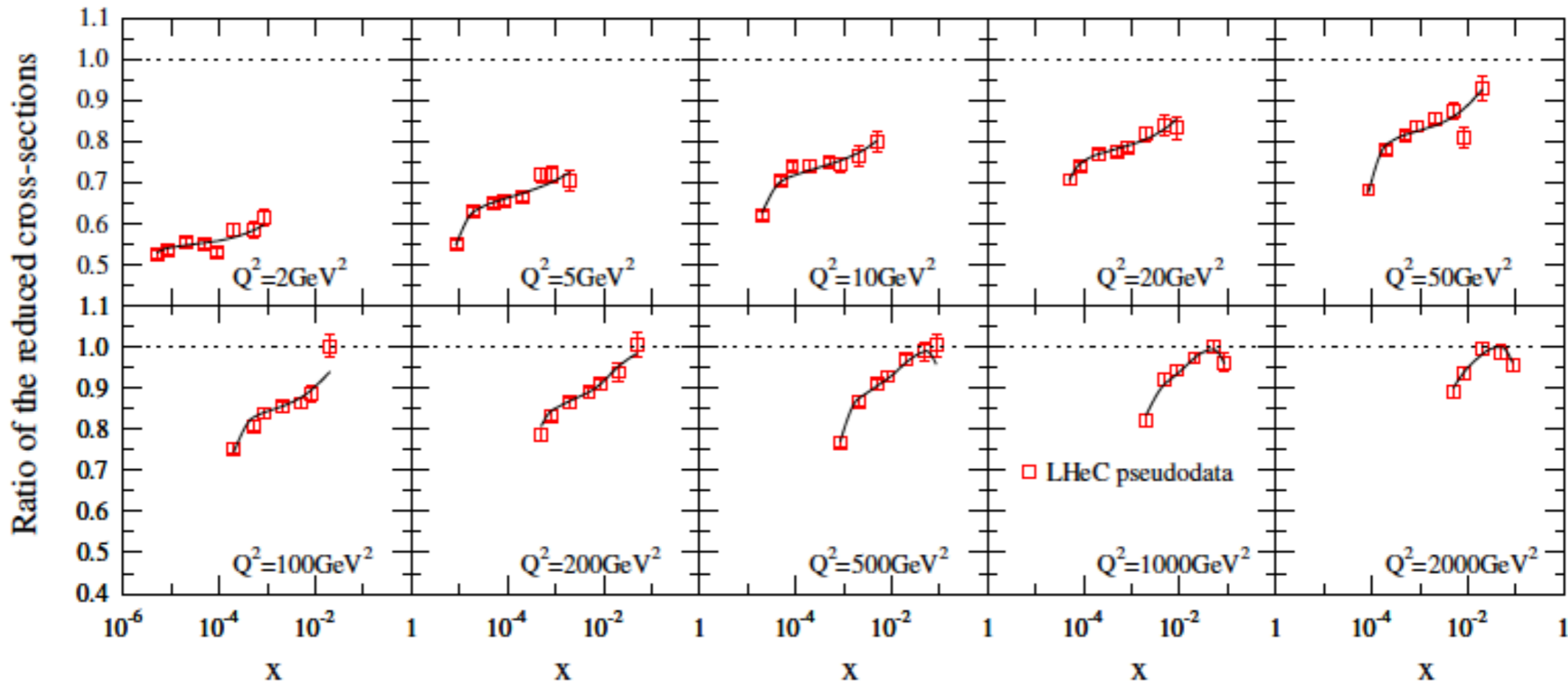
$$R_i(\text{EPS09}) = \frac{\sigma_{e\text{Pb}}^i(\text{CTEQ6.6} + \text{EPS09})}{\sigma_{ep}^i(\text{CTEQ6.6})},$$

and r^i and $r^{\text{norm.}}$ are Gaussian random numbers.

- Typically $\delta_{\text{uncor.}}^i < 2\%$ and $\delta_{\text{norm.}} = 1.4\%$ (assuming that the uncertainties in e-p and e-Pb are uncorrelated)

Pseudodata:

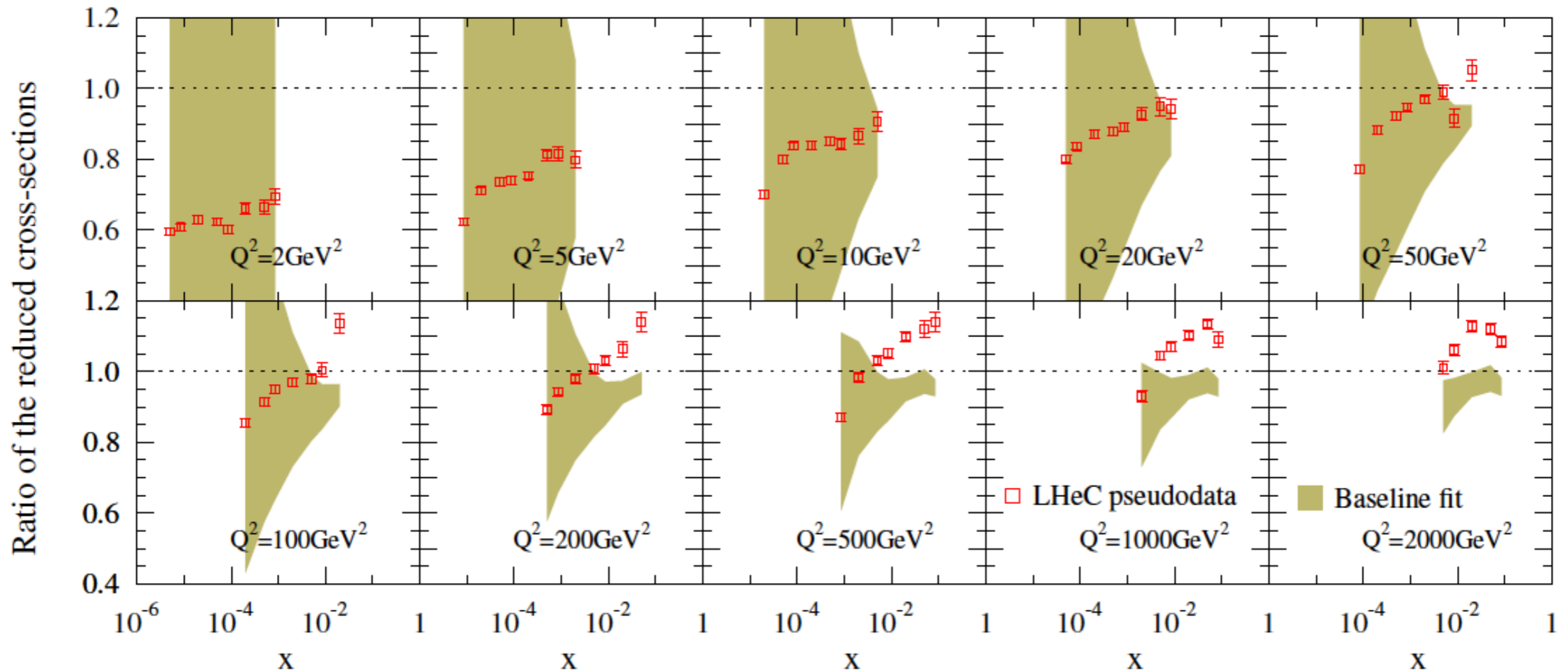
- **Complete, new simulation:** NC(+CC+c,b not yet used) with systematic uncertainties from a complete simulation.



Checked that χ^2/N_{data} to the underlying truth (=EPS09 ;)) fluctuates about unity depending on the random numbers that got chosen

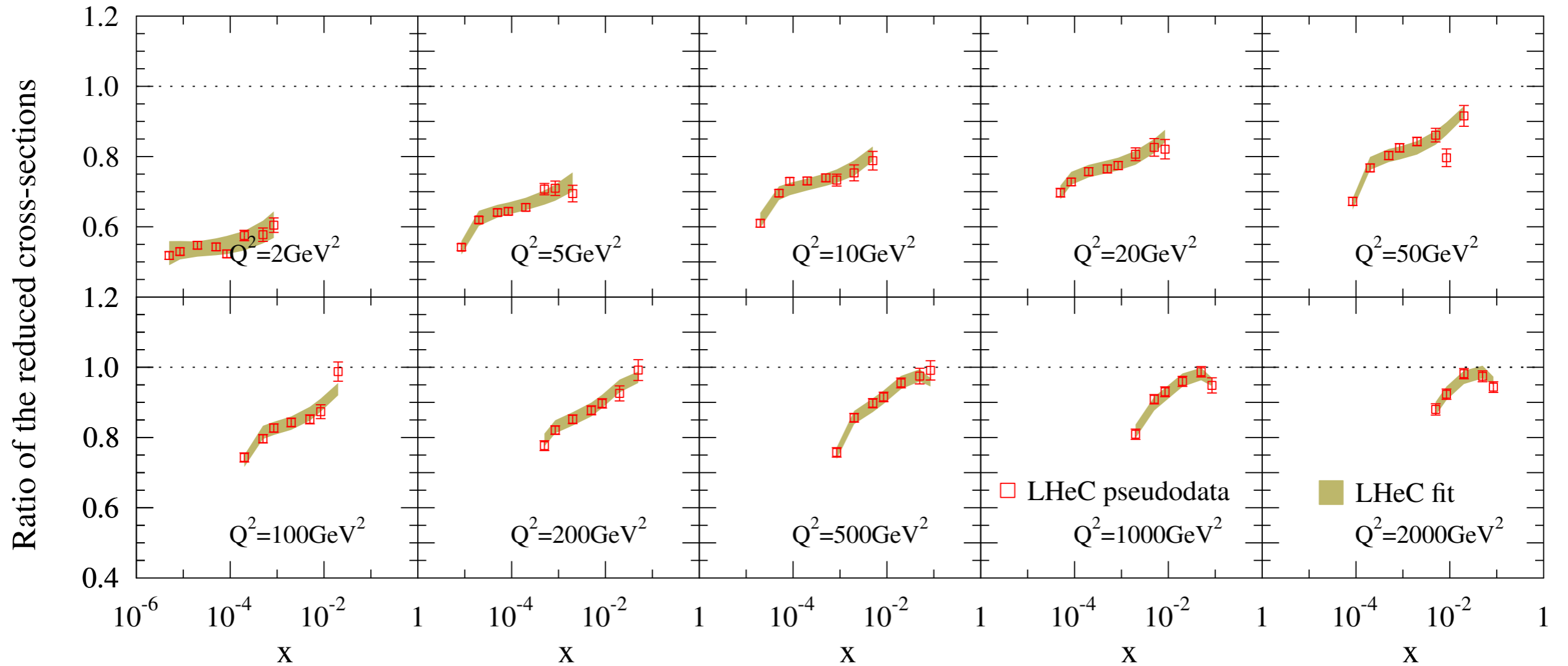
Pseudodata:

The error bands hugely exceed the data uncertainties

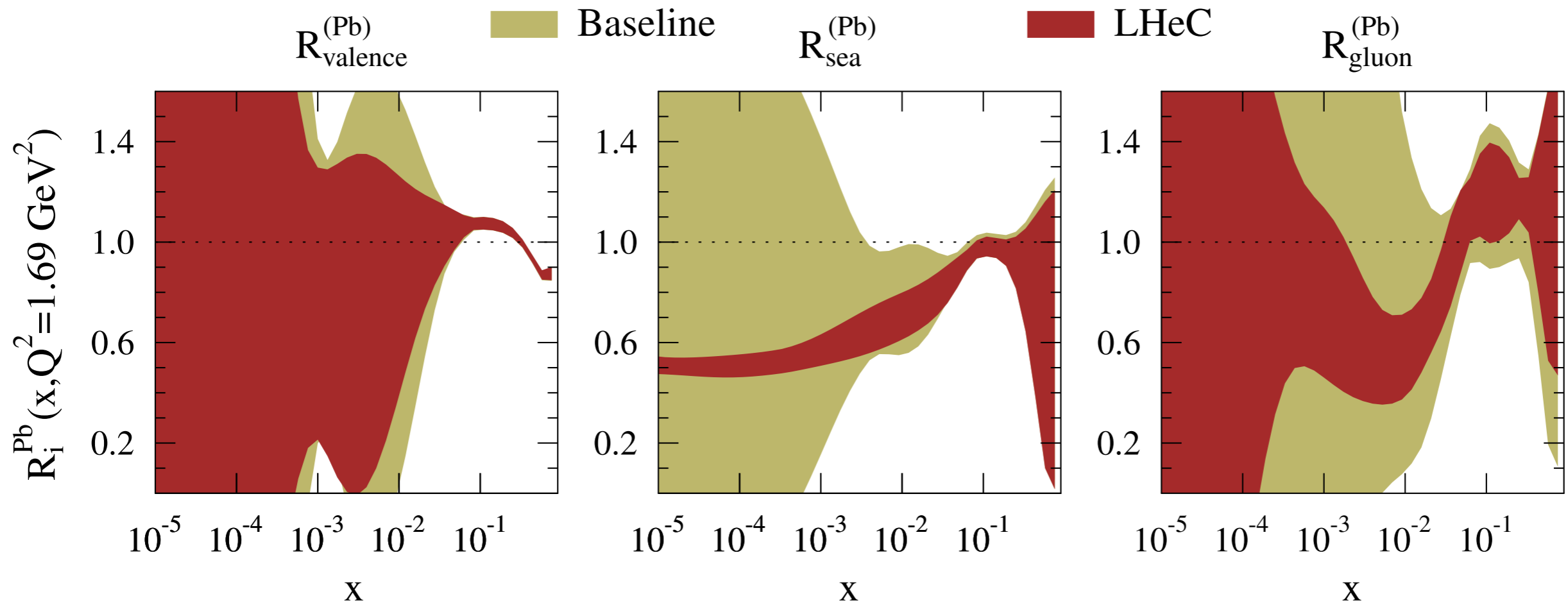


The “optimum” data normalization factor $f \sim 1.1$, hence the mismatch at large x

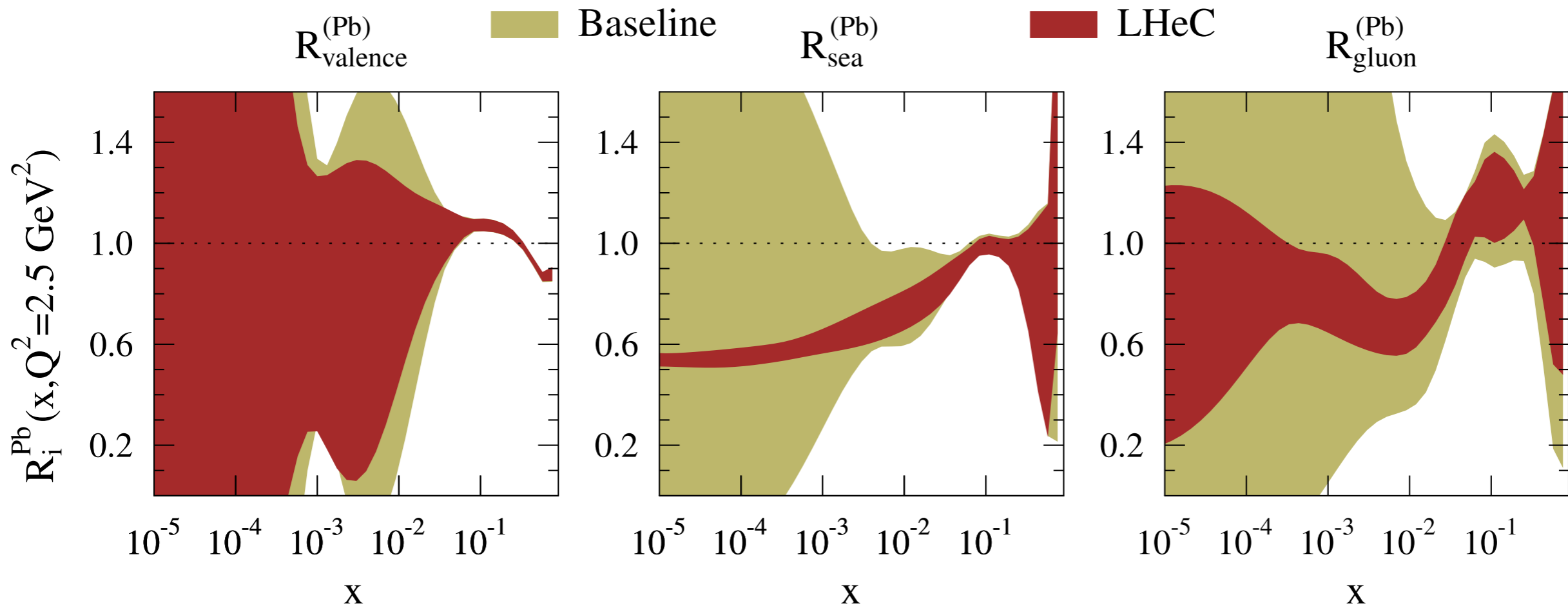
- **Uncertainties shrink!!!**



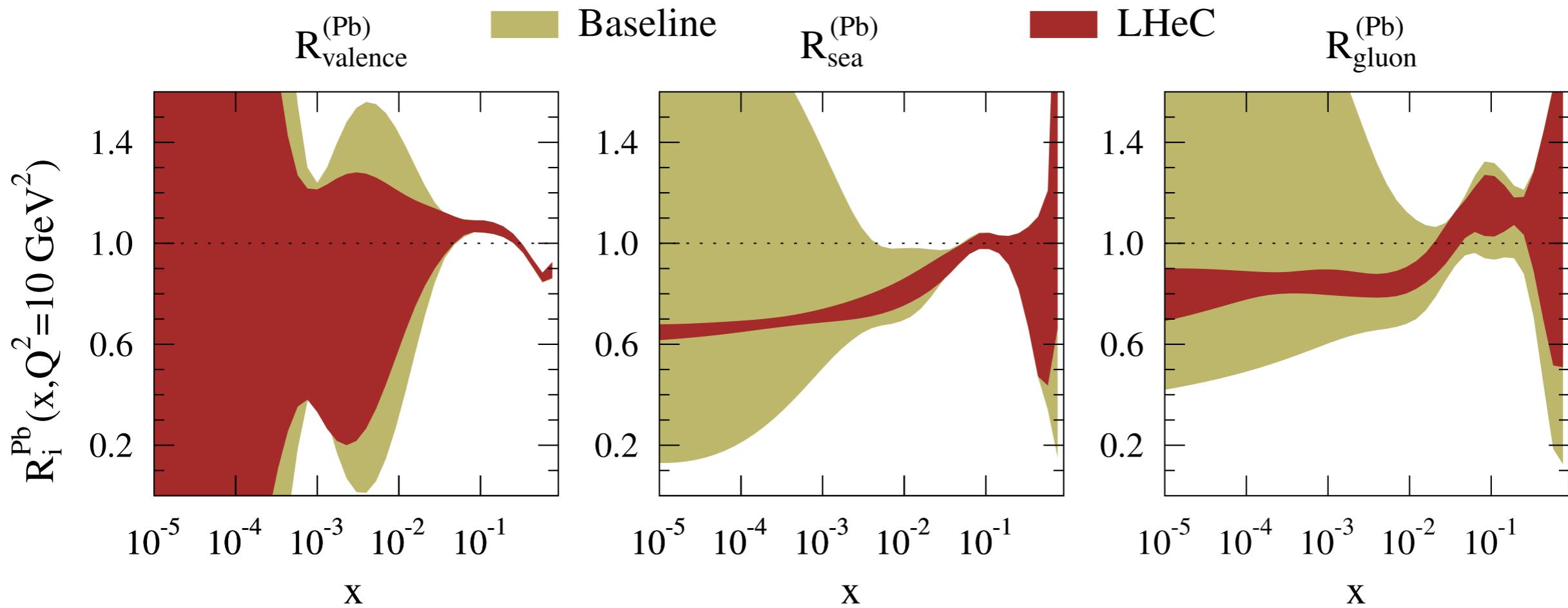
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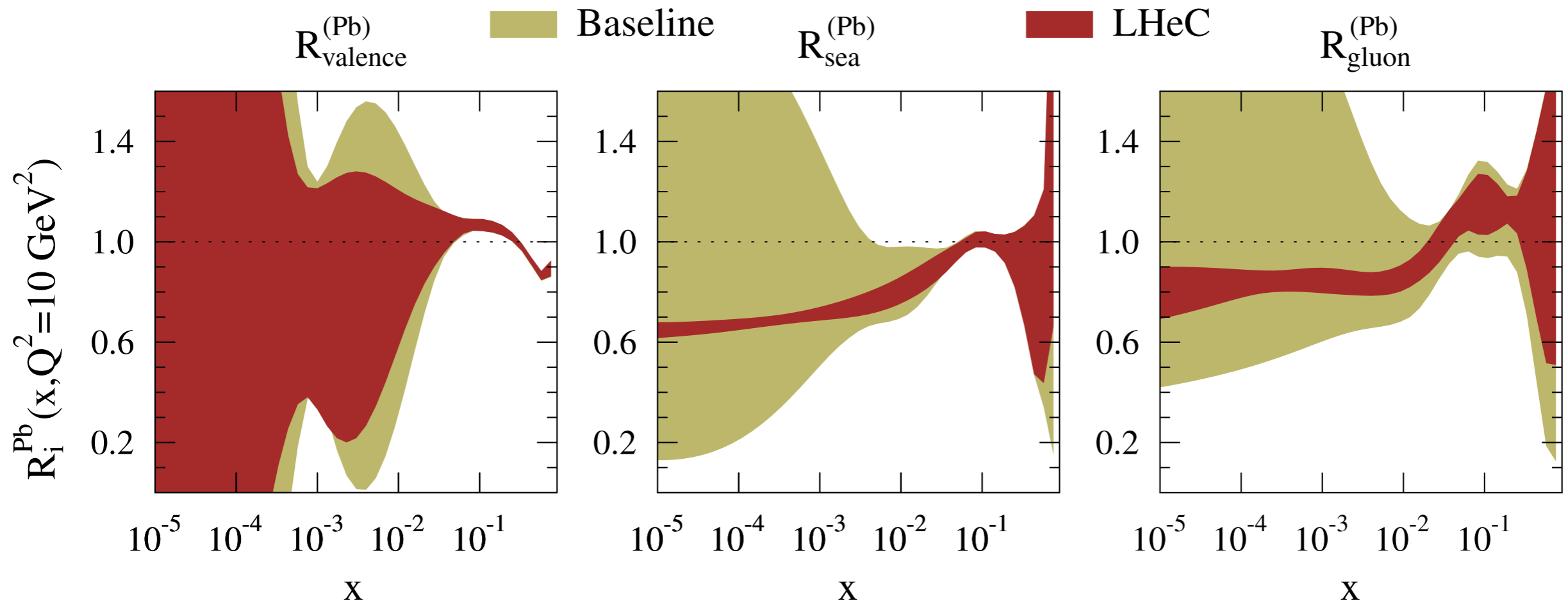
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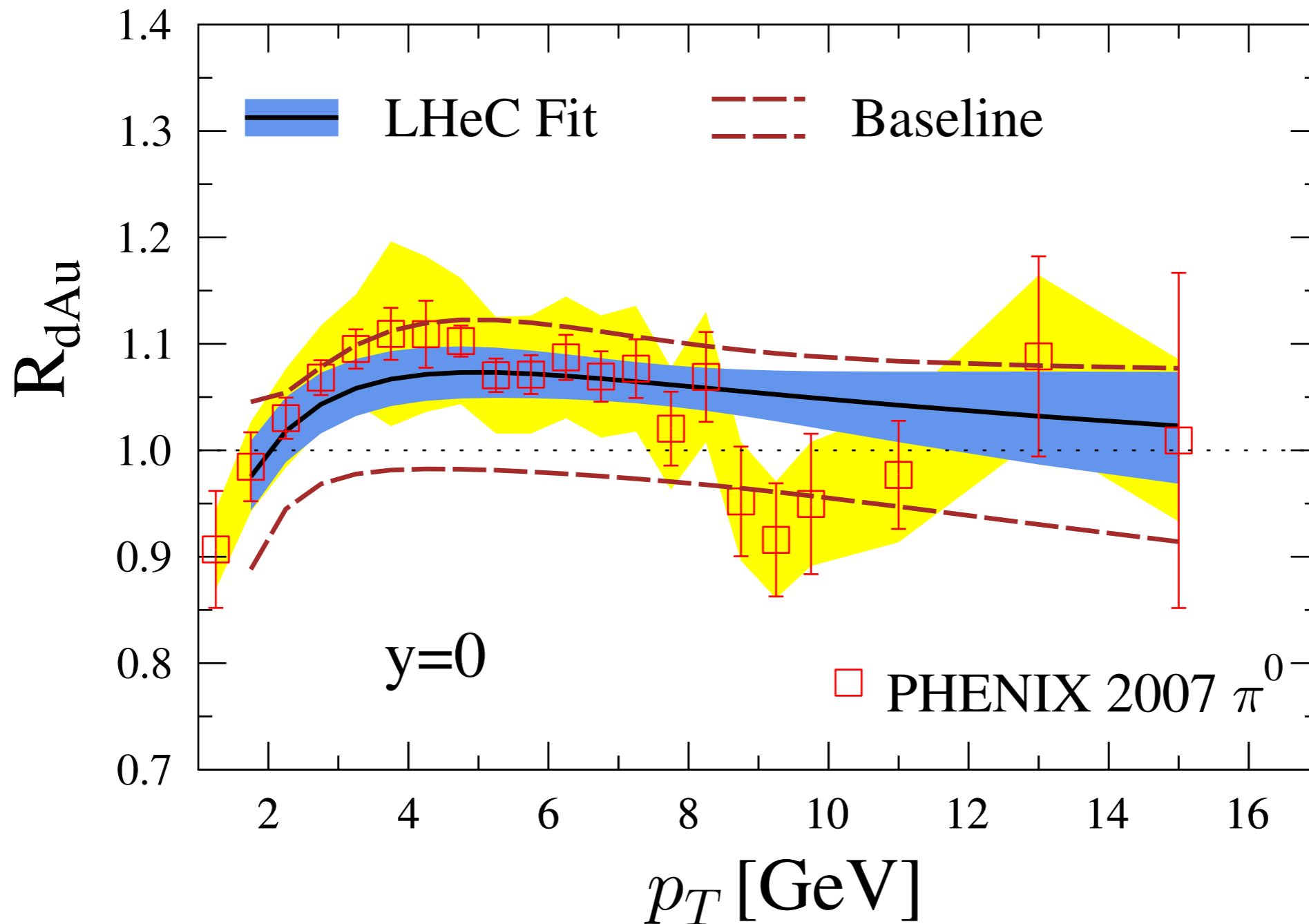


- **Uncertainties shrink!!!**



- **Kind of precision required for better understanding of HI data on hard probes.**

- Looking back to RHIC π^0 data - only direct constrain on glue at present (hopefully to be substituted by LHC jets):



Summary and outlook:

- Limitations of the uncertainty analysis in existing nPDF datasets due to the form of initial conditions explored: uncertainties actually much larger in the regions where data are absent.
- Results may challenge physical intuition, but the aim of fitting is an extraction of the information in data...
- Potential of LHeC is huge in this respect.
- Outlook will (would) be: add CC, study flavour decomposition, check different mass schemes, check tension with saturation, use Pb data alone.

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Thanks to Hannu and Max for a most nice collaboration!!!

Thanks a lot to Hannu - this talk is his!!!

Thank you very much for your attention!!!