

Double Higgs boson production in the Standard Model with extra scalar particles

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Motivation

- ▶ A scalar with mass 125 GeV has been discovered in 2012.
- ▶ In order to confirm that this is the Standard Model Higgs boson, its couplings have to be measured.
- ▶ Triple coupling: $g_{hhh} \sim \frac{m_h^2}{v}$. It can be measured in the $pp \rightarrow hh$ process.
- ▶ Standard Model prediction for the $pp \rightarrow hh$ cross section is 40 fb for $\sqrt{s} = 14$ TeV. That can only be measured at HL-LHC.
- ▶ What if there are other scalar particles?

Isosinglet

arXiv:1503.01618

Scalar sector:

$$\Phi = \begin{pmatrix} \phi^+ \\ \frac{1}{\sqrt{2}}(v_\Phi + \phi + i\eta) \end{pmatrix}, \quad X = v_X + \chi$$

Potential:

$$V_1(\Phi, X) = -\frac{1}{2}m_\Phi^2\Phi^\dagger\Phi + \frac{\lambda}{2}(\Phi^\dagger\Phi)^2 + \frac{1}{2}m_X^2X^2 + \mu\Phi^\dagger\Phi X$$

Mixing:

$$\begin{pmatrix} h \\ H \end{pmatrix} = \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} \phi \\ \chi \end{pmatrix}.$$

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1. $\left. \frac{\partial V_1}{\partial \phi} \right|_{\phi=0, \chi=0} = 0,$
2. $\left. \frac{\partial V_1}{\partial \chi} \right|_{\phi=0, \chi=0} = 0,$
3. $v_\Phi = 246$ GeV from the Fermi coupling in muon decay.
4. h is associated with the SM-like higgs, so $m_h = 125$ GeV.

Remaining model parameters: $\sin \alpha$ and m_H .

H decay widths:

$$\Gamma(H \rightarrow W^+ W^-) = \frac{m_H^3 \sin^2 \alpha}{16\pi v_\Phi^2} \left[1 - 4 \frac{m_W^2}{m_H^2} + 12 \frac{m_W^4}{m_H^4} \right] \sqrt{1 - \left(\frac{2m_W}{m_H} \right)^2}$$

$$\Gamma(H \rightarrow ZZ) = \frac{m_H^3 \sin^2 \alpha}{128\pi v_\Phi^2} \left[1 - 4 \frac{m_Z^2}{m_H^2} + 12 \frac{m_Z^4}{m_H^4} \right] \sqrt{1 - \left(\frac{2m_Z}{m_H} \right)^2}$$

$$\Gamma(H \rightarrow t\bar{t}) = \frac{3m_t^2 m_H \sin^2 \alpha}{8\pi v_\Phi^2} \left[1 - \left(\frac{2m_t}{m_H} \right)^2 \right]^{\frac{3}{2}}$$

$$\Gamma(H \rightarrow hh) = \frac{(2m_h^2 + m_H^2)^2}{32\pi v_\Phi^2 m_H} \sin^2 \alpha \cos^4 \alpha \sqrt{1 - \left(\frac{2m_h}{m_H} \right)^2}$$

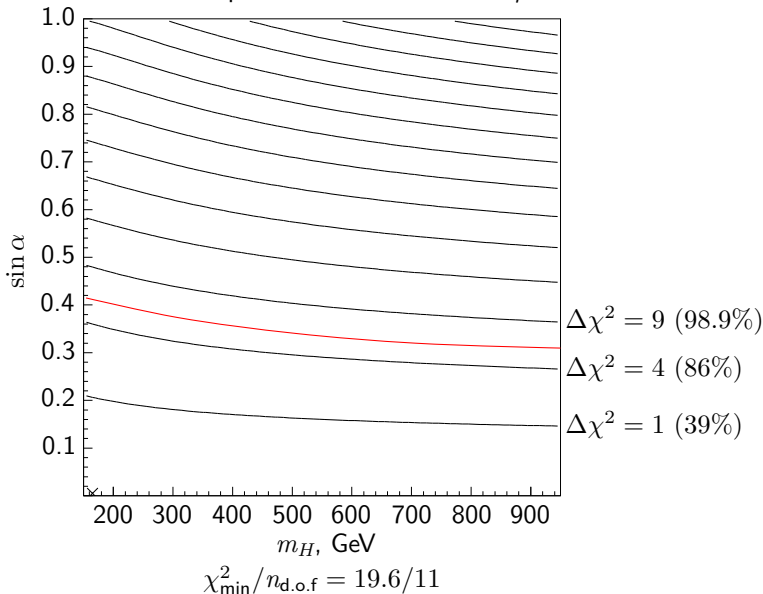
h double production cross section:

$$\sigma(pp \rightarrow H \rightarrow hh) = \sigma(pp \rightarrow h)_{\text{SM}} \cdot \sin^2 \alpha \cdot \text{Br}(H \rightarrow hh)$$

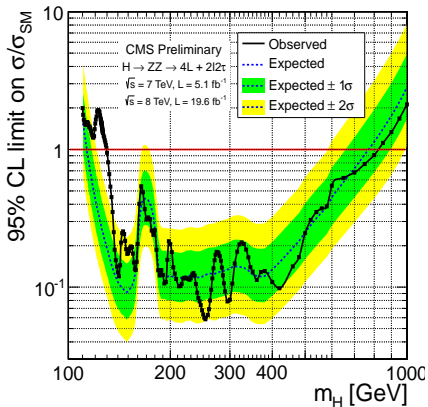
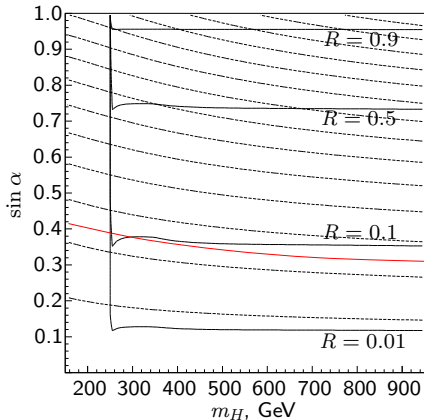
$$\mu_i = \frac{\sigma(pp \rightarrow h) \cdot \text{Br}(h \rightarrow f_i)}{(\sigma(pp \rightarrow h) \cdot \text{Br}(h \rightarrow f_i))_{\text{SM}}} = \cos^2 \alpha$$

$$\text{ATLAS: } \mu = 1.30_{-0.17}^{+0.18}, \quad \text{CMS: } \mu = 1.00_{-0.13}^{+0.14}$$

Bounds from electroweak precision observables and μ measurements:

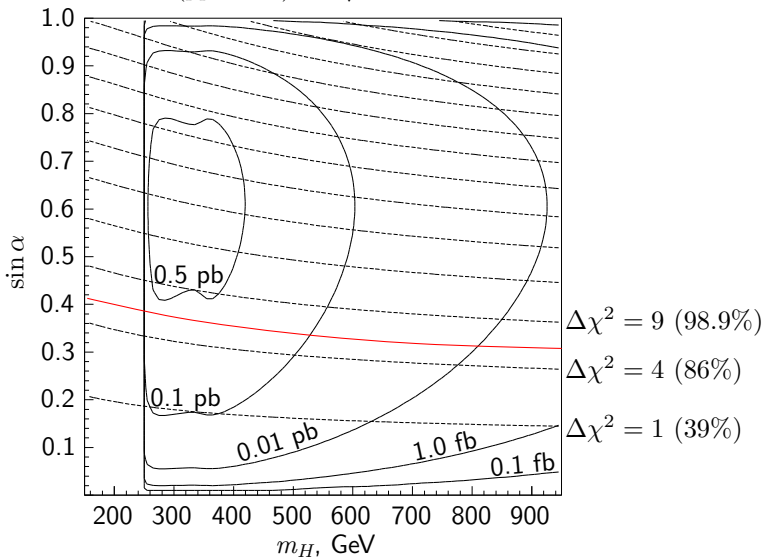


$$R \equiv \frac{\sigma(pp \rightarrow H) \text{Br}(H \rightarrow ZZ)}{(\sigma(pp \rightarrow h) \text{Br}(h \rightarrow ZZ))_{\text{SM}}} = \frac{\sin^4 \alpha}{\sin^2 \alpha + \frac{\Gamma(H \rightarrow hh)}{\Gamma_{\text{SM}}}}$$



Experiment: $R < 0.1$ for $200 \text{ GeV} < m_H < 400 \text{ GeV}$
(CMS PAS HIG-13-002).

$\sigma(pp \rightarrow hh)$ for $\sqrt{s} = 14$ TeV



Isotriplet

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Scalar sector:

$$\Phi = \begin{bmatrix} \phi^+ \\ \frac{1}{\sqrt{2}}(v_\Phi + \phi + i\eta) \end{bmatrix}, \quad \Delta = \frac{\vec{\Delta}\vec{\sigma}}{\sqrt{2}} = \begin{bmatrix} \delta^+/\sqrt{2} & \delta^{++} \\ \frac{1}{\sqrt{2}}(v_\Delta + \delta + i\rho) & -\delta^+/\sqrt{2} \end{bmatrix}$$

Potential:

$$V(\Phi, \Delta) = -\frac{1}{2}m_\Phi^2(\Phi^\dagger\Phi) + \frac{\lambda}{2}(\Phi^\dagger\Phi)^2 \\ + m_\Delta^2 \text{tr}[\Delta^\dagger\Delta] + \frac{\mu}{\sqrt{2}}(\Phi^T i\sigma^2 \Delta^\dagger\Phi + \text{h.c.})$$

Mixing:

$$\begin{pmatrix} h \\ H \end{pmatrix} = \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} \phi \\ \delta \end{pmatrix}.$$

$$m_h = 125 \text{ GeV}.$$

Custodial symmetry breaking:

$$\left. \begin{aligned} m_W^2 &= \frac{g^2}{4}(v_\Phi^2 + 2v_\Delta^2) \\ m_Z^2 &= \frac{\bar{g}^2}{4}(v_\Phi^2 + 4v_\Delta^2) \end{aligned} \right\} \Rightarrow \frac{m_W}{m_Z} \approx \left(\frac{m_W}{m_Z} \right)_{\text{SM}} \left(1 - \frac{v_\Delta^2}{v_\Phi^2} \right)$$

$$\left(\frac{m_W}{m_Z \cos \theta_W} \right)_{\text{SM}} = 1.00040 \pm 0.00024 \Rightarrow v_\Delta < 5 \text{ GeV (at } 3\sigma \text{ level)}$$

In the following we assume $v_\Delta = 5 \text{ GeV}$.

$$v_\Phi^2 + 2v_\Delta^2 = \frac{1}{\sqrt{2}G_F} = (246 \text{ GeV})^2 \Rightarrow v_\Phi \approx 246 \text{ GeV}.$$

With $v_\Delta \ll v_\Phi$ we get $\sin \alpha \approx \frac{2v_\Delta}{v_\Phi} \ll 1$.

Remaining model parameters: m_H . We will consider the case of $m_H = 300 \text{ GeV}$.

$$\Gamma(H \rightarrow ZZ) = \frac{v_\Delta^2}{v^4} \frac{m_H^3}{8\pi} \left[\frac{1 - 2 \left(\frac{m_h}{m_H} \right)^2}{1 - \left(\frac{m_h}{m_H} \right)^2} \right]^2 \left(1 - 4 \frac{m_Z^2}{m_H^2} + 12 \frac{m_Z^4}{m_H^4} \right) \sqrt{1 - \left(\frac{2m_Z}{m_H} \right)^2}$$

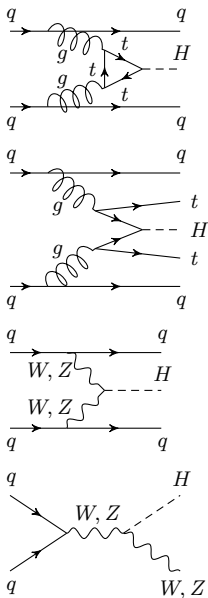
$$\Gamma(H \rightarrow WW) = \frac{v_\Delta^2}{v^4} \frac{m_H^3}{4\pi} \left[\frac{\left(\frac{m_h}{m_H} \right)^2}{1 - \left(\frac{m_h}{m_H} \right)^2} \right]^2 \left(1 - 4 \frac{m_W^2}{m_H^2} + 12 \frac{m_W^4}{m_H^4} \right) \sqrt{1 - \left(\frac{2m_W}{m_H} \right)^2}$$

$$\Gamma(H \rightarrow t\bar{t}) = \frac{v_\Delta^2}{v^4} \frac{3m_t^2 m_H}{2\pi} \left[\frac{1}{1 - \left(\frac{m_h}{m_H} \right)^2} \right]^2 \left(1 - \left(\frac{2m_t}{m_H} \right)^2 \right)^{\frac{3}{2}}$$

$$\Gamma(H \rightarrow hh) = \frac{v_\Delta^2}{v^4} \frac{m_H^3}{8\pi} \left[\frac{1 + 2 \left(\frac{m_h}{m_H} \right)^2}{1 - \left(\frac{m_h}{m_H} \right)^2} \right]^2 \sqrt{1 - \left(\frac{2m_h}{m_H} \right)^2}$$

$H \rightarrow WW$ decay is suppressed, $H \rightarrow ZZ$ is the “golden mode”.
 $\text{Br}(H \rightarrow hh) \approx 0.8$ for $m_H = 300$ GeV.

Heavy higgs production at the LHC:



$$\sigma(gg \rightarrow H) = \left[\frac{2v_{\Delta}}{v_{\Phi}} \frac{1}{1 - \left(\frac{m_h}{m_H}\right)^2} \right]^2 \sigma(gg \rightarrow h)_{\text{SM}}$$

$$= 2.4 \cdot 10^{-3} \cdot \sigma(gg \rightarrow h)_{\text{SM}}$$

$$\sigma(ZZ \rightarrow H) = \left[\frac{2v_{\Delta}}{v_{\Phi}} \frac{1 - 2\left(\frac{m_h}{m_H}\right)^2}{1 - \left(\frac{m_h}{m_H}\right)^2} \right]^2 \sigma(ZZ \rightarrow h)_{\text{SM}}$$

$$= 1.0 \cdot 10^{-3} \cdot \sigma(ZZ \rightarrow h)_{\text{SM}}$$

$$\sigma(WW \rightarrow H) = \left[\frac{2v_{\Delta}}{v_{\Phi}} \frac{\left(\frac{m_h}{m_H}\right)^2}{1 - \left(\frac{m_h}{m_H}\right)^2} \right]^2 \sigma(WW \rightarrow h)_{\text{SM}}$$

$$= 7.3 \cdot 10^{-5} \cdot \sigma(WW \rightarrow h)_{\text{SM}}$$

Higgs boson double production cross section at the LHC for $\sqrt{s} = 14$ TeV

Mass, GeV	the SM h		H
	125	300	300
$\sigma(gg \rightarrow h, H),^1$ pb	50(5)	11(1)	$25(2) \cdot 10^{-3}$
$\sigma(gg \rightarrow t\bar{t} + h, H),^1$ pb	0.61(6)	0.051(5)	$12(1) \cdot 10^{-6}$
$\sigma(W^+ W^- \rightarrow h, H),^2$ pb	3.272(4)	1.053(1)	$76.8(1) \cdot 10^{-6}$
$\sigma(ZZ \rightarrow h, H),^2$ pb	1.087(1)	0.365(1)	$365(1) \cdot 10^{-6}$
$\sigma(W^* \rightarrow Wh, WH),^2$ pb	0.150(6)	0.068(3)	$5.0(2) \cdot 10^{-6}$
$\sigma(Z \rightarrow Zh, ZH),^2$ pb	0.88(5)	0.042(2)	$42(2) \cdot 10^{-6}$

$$\begin{aligned} \sigma(pp \rightarrow hh) &= 40 \text{ fb (SM)} + 25 \text{ fb (} H \text{ production)} \cdot 0.8 \text{ (branching)} \\ &= 60 \text{ fb} \end{aligned}$$

¹For the SM higgs values are from *Handbook of LHC Higgs cross sections*, CERN-2011-002

²Obtained with the help of the program HAWK at LO + QCD without electroweak corrections

The Georgi-Machacek model

$$\Phi = \begin{bmatrix} \phi^{0*} & \phi^+ \\ -\phi^- & \phi^0 \end{bmatrix}, \quad \Delta = \begin{bmatrix} \delta^{0*} & \xi^+ & \delta^{++} \\ -\delta^- & \xi^0 & \delta^+ \\ \delta^{--} & -\xi^- & \delta^0 \end{bmatrix}.$$

$$\phi^0 = \frac{1}{\sqrt{2}}(v_\Phi + \phi + i\chi), \quad \delta^0 = \frac{1}{\sqrt{2}}(v_\Delta + \delta + i\eta),$$

$$\xi^0 = v_\xi + \xi.$$

$$m_W^2 = \frac{g^2}{4}(v_\Phi^2 + 2v_\Delta^2 + 2v_\xi^2)$$

$$m_Z^2 = \frac{\bar{g}^2}{4}(v_\Phi^2 + 4v_\Delta^2)$$

$$(v_\Phi^2 + 2v_\Delta^2 + 2v_\xi^2) = \frac{1}{\sqrt{2}G_F} = (246 \text{ GeV})^2$$

When $v_\xi = v_\Delta$ the bound on v_Δ from the gauge bosons mass ratio is relieved. LHC measurements allows v_Δ up to 50 GeV. In this case H production cross section can be as high as 2 pb depending on model parameters.

Thank you for your attention