

# Flavor Tagging TeV Jets for BSM and QCD

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In collaboration with **Zack Sullivan**  
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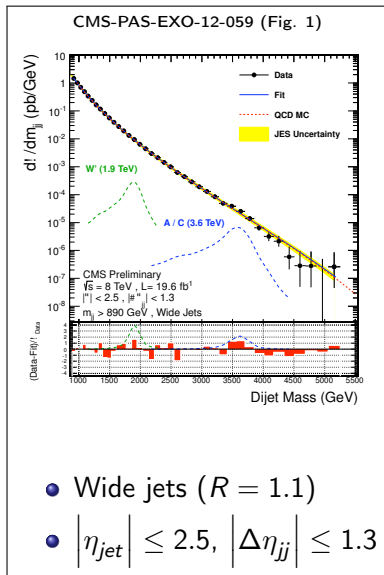
# $Z'$ Models

- One of the simplest BSM models is an additional  $U(1)$  symmetry, mediated by a neutral heavy boson ( $Z'$ ).
  - Experiments don't see heavy resonance in dilepton channels – what if the  $Z'$  is “leptophobic”?
  - **Dijets are discovery channel!**

- One of the simplest BSM models is an additional  $U(1)$  symmetry, mediated by a neutral heavy boson ( $Z'$ ).
  - Experiments don't see heavy resonance in dilepton channels – what if the  $Z'$  is “leptophobic”?
  - **Dijets are discovery channel!**
- *Dobrescu* and *Yu* [arXiv:1306.2629 and 1506.04435] outline simple, renormalizable, leptophobic  $Z'_B$ 
  - No tree-level couplings to SM leptons and bosons, only SM quarks are charged. This implies association with *baryon* number  $B$ .
  - Coupling to quarks is flavor independent,
    - $\frac{1}{6} g_B Z'_{B\mu} \bar{q} \gamma^\mu q$
  - Narrow width:
    - $\Gamma_{Z'}/M_{Z'} \approx \frac{1}{6} \alpha_B \left(1 + \frac{\alpha_S}{\pi}\right) \approx 1-5\%$  (depending on  $g_B$ )
  - Model needs vector-like fermions (anomalons); we assume they're “kinematically inaccessible”.

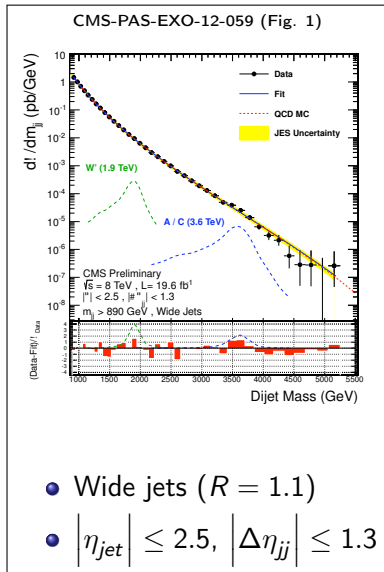
# Z' Dijet Searches

- Dijet search gives *lots of data*, but
  - Strong QCD BG (all quarks are “massless” at 2 TeV).
  - Precise reconstructing of radiation and  $t\bar{t}$  uses *wide* jets ... pileup smears mass resolution.



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- Leading processes at  $\alpha^2$ ?
  - $Z'$ :  $q\bar{q} \xrightarrow{s} q'\bar{q}'$
  - QCD heavy dijets (c**b**t):  
 $gg \xrightarrow{t} q\bar{q} \mid q\bar{q} \xrightarrow{s} q'\bar{q}'$
  - QCD light dijets (d**u**sg):  
 $gq \xrightarrow{t} gq \mid q\bar{q} \xrightarrow{t} q\bar{q} \mid gg \xrightarrow{s} gg$



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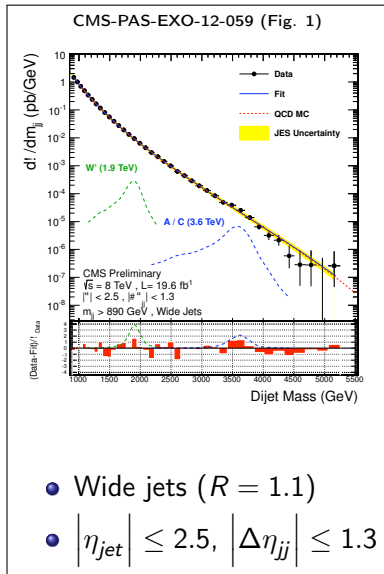
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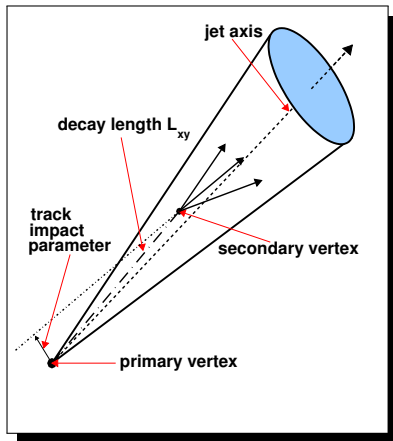
- $\frac{S}{\sqrt{BG}} \approx \frac{Z'}{\sqrt{QCD \text{ light}}}$

- *Tag b/c-jets to drive down light-jet QCD BG!*



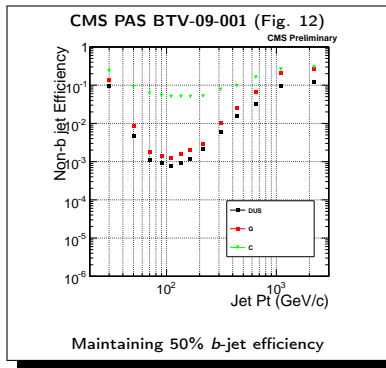
# Track-based $b$ -tag

- $b$ -hadrons have long lifetimes and decay at a secondary vertex (**SV**). Use tracks to find an **SV** inside a jet.
  - High efficiency for  $b$ -jets (.5-.8).
  - Also tag **charm** and **light** jets.



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  - Also tag **charm** and **light** jets.
- Probability to tag light jets increases severely as jet  $p_T$  approaches TeV.
  - $10^{-3}$  at 100 GeV  $\rightarrow 10^{-1}$  at 1 TeV

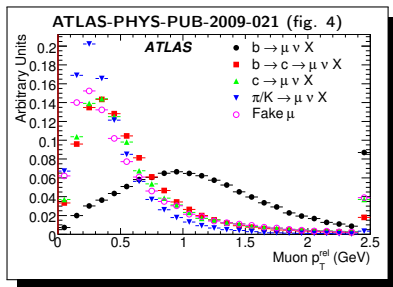


- Resolving **SV** inside high  $p_T$  jets is *limited by tracking performance*.
  - Tracks have higher  $p_T$  and bend less – harder to constrain.
  - Tracks are more collimated – increased sensitivity to tracker resolution.
  - Dense tracking environment – fake tracks *and* false duplicates.
- Gluons split ( $g \rightarrow b\bar{b}$ ) more often at high  $p_T$  – light flavor BG!



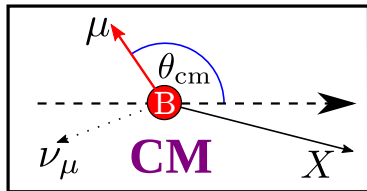
# Muon-based $b$ -tag

- $b/c$ -hadrons frequently decay semi-leptonically (where  $l \in \{e, \mu\}$ ):
  - $BR(b \rightarrow l\nu_l X) \approx 11\%$
  - $BR(c \rightarrow l\nu_l X) \approx 10\%$
  - 20% of  $b$ -jets have  $N_{muon} \geq 1$
- Hard to see electrons inside jets; we're lucky that someone ordered the *muon chamber*!
- The angle muons make with boost axis of mother should be larger if its mother had a high mass (and thus a heavy flavor).
  - Look at  $p_T^{rel}$  (muon momentum transverse to the centroid of its jet)
  - $p_T^{rel}$  loses efficiency for boosted decays because *the centroid of the entire jet* is too coarse a measure – need *subjet of decay*.



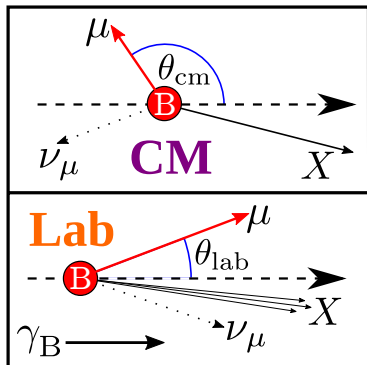
# Muon Emission vs. Semi-leptonic Subject

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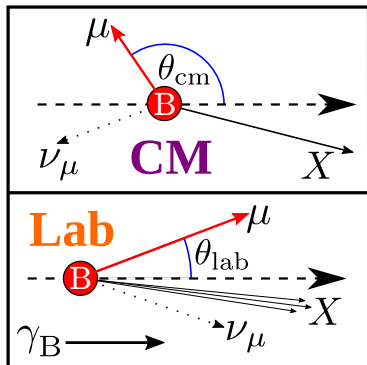
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- **Lab**: Muon is detected at angle  $\theta_{\text{lab}}$  w.r.t. the centroid of the subjet (which has boost  $\gamma_B$ ).
  - Define  $\kappa \equiv \beta_B/\beta_{\mu,\text{cm}}$



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$$x \equiv \gamma_B \tan(\theta_{\text{lab}}) = \frac{\sin(\theta_{\text{cm}})}{\kappa + \cos(\theta_{\text{cm}})} \quad (1)$$

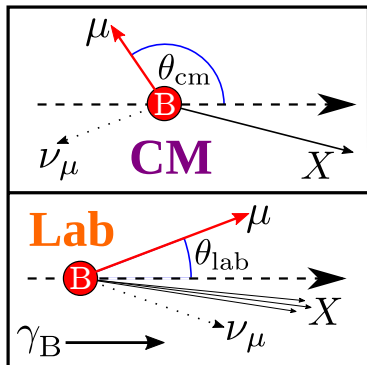


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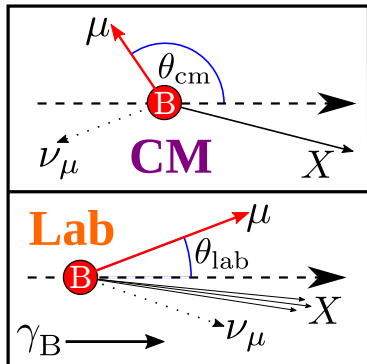


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$$\frac{dN}{dx} = 4\pi \frac{2x}{(x^2 + 1)^2} K(x, \kappa) \quad (\text{when } \gamma_B \gg \gamma_{\mu, \text{cm}} \rightarrow \kappa > 1) \quad (3)$$

## x Marks the Heavy Flavor tag

- We can calculate the **lab frame** region  $[0, x_\delta]$  which captures  $(1 - \delta)$  of the CM emission. It's not pretty

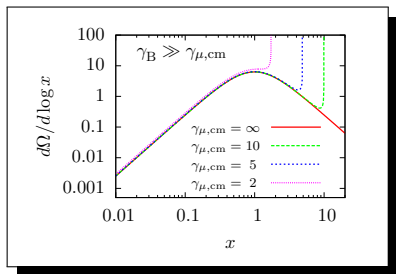
$$x_\delta = \sqrt{\frac{1 - \kappa^2 - 2\delta^2 + \sqrt{(\kappa^2 - 1)^2 + 4\kappa^2\delta^2}}{2\delta^2}} \quad (4)$$

- Taking the limit as  $\delta \rightarrow 0$  gives  $x_{\max} = 1/\sqrt{\kappa^2 - 1}$ .
- More important is the region which captures 90% of emitted muons

$$x_{90\%} \approx 3 \left( 1 - \frac{5}{2} \gamma_{\mu, \text{cm}}^{-2} \right) \approx 3 \quad (5)$$

- If you find a muon in a jet, ask:
  - “Is the muon consistent with a *very boosted emission* from the jet’s **primary hadron** (i.e. is  $x \leq x_{90\%}$ )?”
- If so, use the muon to tag the jet – *this is the  $\mu_x$  tag.*

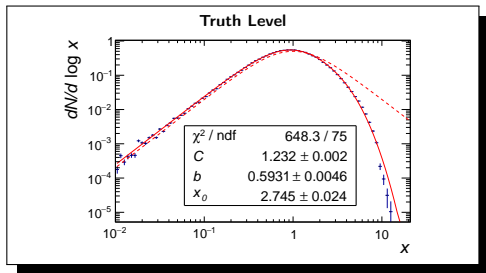
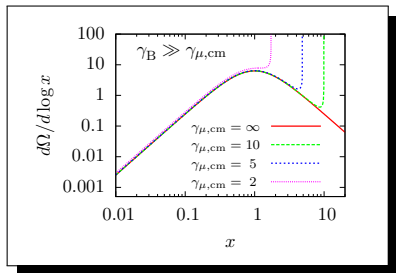
# Testing $dN/dx$



- Muons restricted to  $x_{\max}$ , defined by  $\gamma_{\mu,cm}$ .
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- **Exact:** Integrate over  $\gamma_{\mu,cm}$  and distribute asymptote.
- **Approximate:** apply cut-off function to asymptotic  $\frac{d\Omega}{d \log x}$ 
  - $\frac{2x^2}{(x^2+1)^2} \times C \frac{(1+\exp(-bx_0))}{(1+\exp(b(x-x_0)))}$

$$\mathbf{p}_{\text{subjet}} = \mathbf{p}_{\mu} + \mathbf{p}_{\text{core}} + \mathbf{p}_{\nu_{\mu}}$$

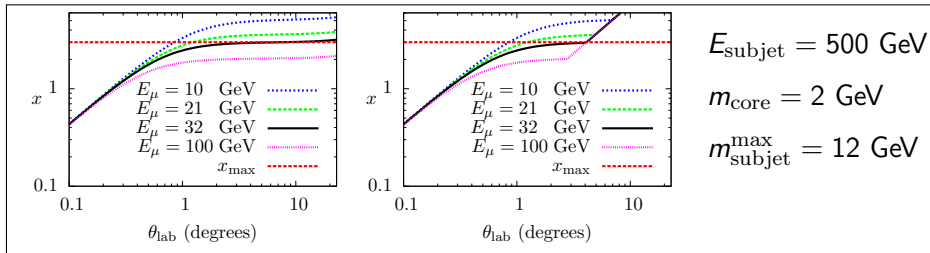
- Require **muons** to pass  $p_{T,\mu}^{\text{min}}$  (we use 10 GeV).
  - Allow them to participate in initial jet clustering (*hard muon seeds*).
- Isolate subjet's hadronic/EM energy (the **core**).
  - Re-cluster jets to find *extremely thin* core:
    - $R \approx 1/\gamma = \mathcal{O}(.01)$  (larger in practice)
  - $\gamma_{\text{subjet}}$  needs **mass** of core – very poorly measured.
    - Constrain mass to *best guess* (e.g.  $m_{D^{\pm}/D^0} \approx 2$  GeV).
  - Choose core which gets subjet mass closest to  $m_{B^{\pm}/B^0} \approx 5.3$  GeV.
- Subjet's **neutrino**:
  - System is under-determined. Simplest estimate: *add muon again to simulate neutrino*.

# What is $\mu_x$ Doing?

$$m_{\text{subject}} \approx \sqrt{m_{\text{core}}^2 + 4E_{\text{core}}E_{\mu}(1 - \cos(\theta_{\text{lab}}))} \quad (6)$$

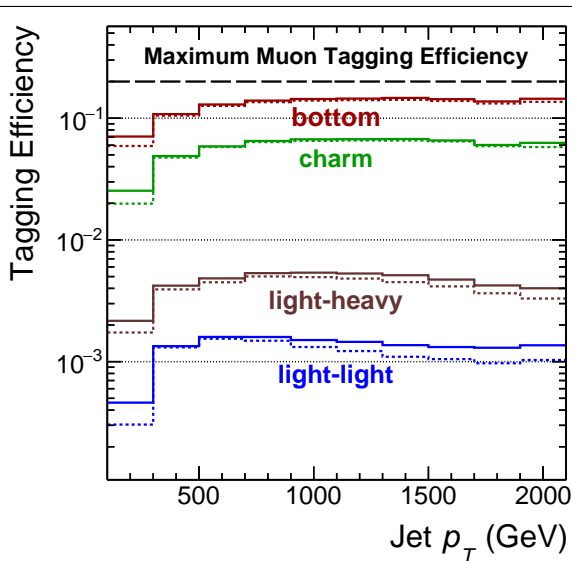
$$x \approx \frac{E_{\text{core}} + 2E_{\mu}}{\min(m_{\text{subject}}, m_{\text{subject}}^{\text{max}})} \tan(\theta_{\text{lab}}) \quad (7)$$

- When  $\theta_{\text{lab}}$  begins to dominate  $m_{\text{subject}}$ ,  $x$  flattens. If  $E_{\mu}$  is also large, it pushes the plateau *below*  $x_{\text{max}}$  — any  $\theta_{\text{lab}}$  causes tag.
- Using  $m_{\text{subject}}^{\text{max}}$  prevents arbitrarily large  $\theta_{\text{lab}}$  from passing the  $x$  cut.



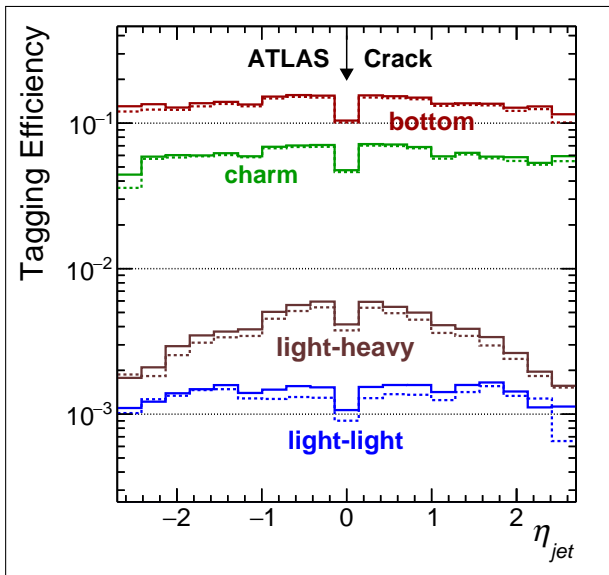
# Tagging Efficiency (Jet $p_T$ )

- All studies simulated at ATLAS at  $\sqrt{s} = 13$  TeV.
- Boosted kinematics turn on at 300 GeV.
- **light-heavy**:  
light jet fragments to heavy quark
- **light-light**:  
light jet stays light
- *Solid* line:  
no pileup
- *Dotted* line:  
 $\langle \mu \rangle = 40$



# Tagging Efficiency (Jet $\eta$ )

- Tag jets with  $x \leq 3$ 
  - $\sim 14\%$  of  $b$ -jets
  - $\sim 6.5\%$  of  $c$ -jets
  - Mis-tag  $\sim 0.65\%$  of light jets
- $\eta$  dependence  
*effectively flat* for bottom and charm.
  - Slight dip in endcap ( $\eta > 1$ ).
  - Large dip at ATLAS detector services crack.
- Light jets lose extra forward efficiency.



# Simulated $Z'$ Bump Hunt

MADGRAPH 5  $\rightarrow$  PYTHIA 8  $\rightarrow$  DELPHES 3 (with FastJet 3)

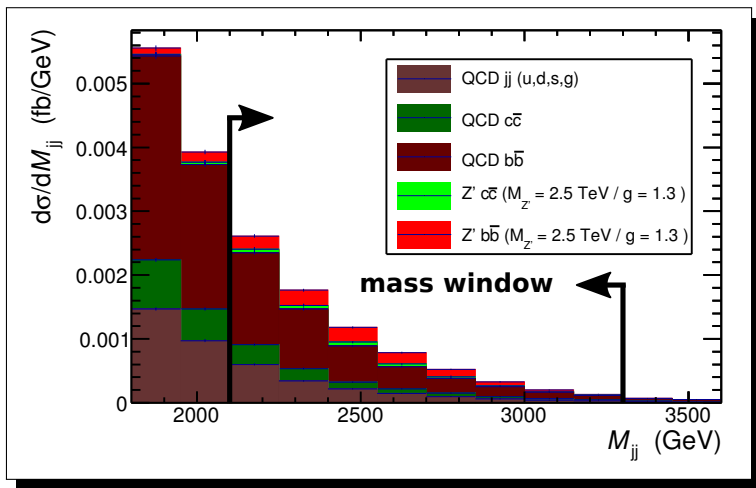
- Plot  $d\sigma/dM$  for dijet systems where *both* top jets are tagged.
  - Proof of concept for  $\mu_x$  tag; Delphes simulates a very simple detector.
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  - Need member of ATLAS or CMS to implement in  $\mu_x$  Geant4.
- Plenty of muons in **heavy** jets, good statistics for double-tagging.
- The double-tag rate for **light** jets  $\left( (\sim 6 \times 10^{-3})^2 \approx 4 \times 10^{-5} \right)$  is *too small* (he complained) — need  $10^9$  events for good statistics
  - When one jet is tagged, scale event weight by **one half times** the probability to tag the recoil jet (from tagging efficiency survey)
  - Either jet could produce the real tag (probabilistic OR):
$$(1 - (1 - \epsilon_j)^2) \times \frac{1}{2}\epsilon_j = \left( 2\epsilon_j - \cancel{\epsilon_j^2} \right) \frac{1}{2}\epsilon_j \approx \epsilon_j^2$$
  - **Reject** events with two real tags, otherwise double counting.

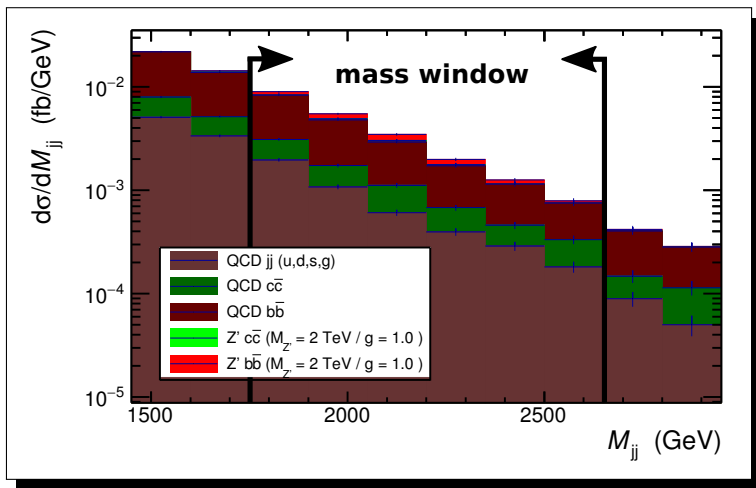
$$M_{Z'} = 2.5 \text{ TeV} \quad g_B = 1.3$$



- Require **both jets** to be tagged.
- Mass window:  $M_{Z'} \times [0.85, 1.25]$
- Narrow jets ( $R = 0.4$ )
- $|\eta_{jet}| \leq 2.7, |\Delta\eta_{jj}| \leq 1.5$



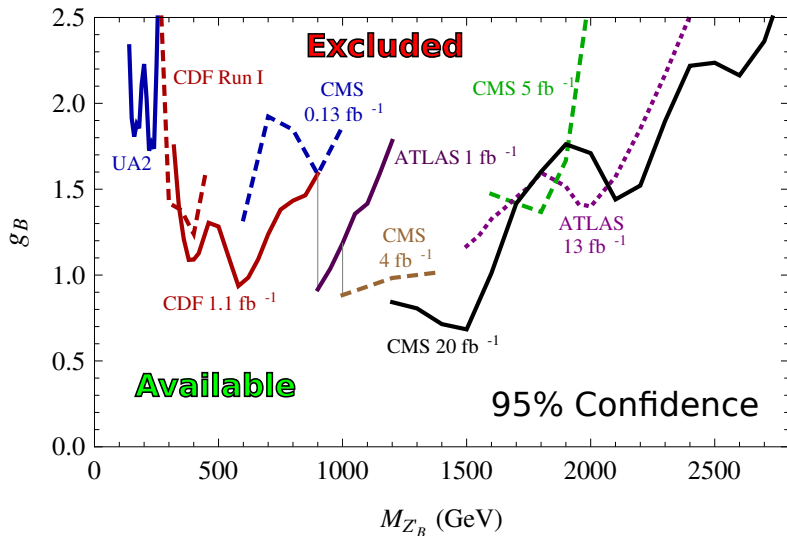
$$M_{Z'} = 2 \text{ TeV} \quad g_B = 1$$



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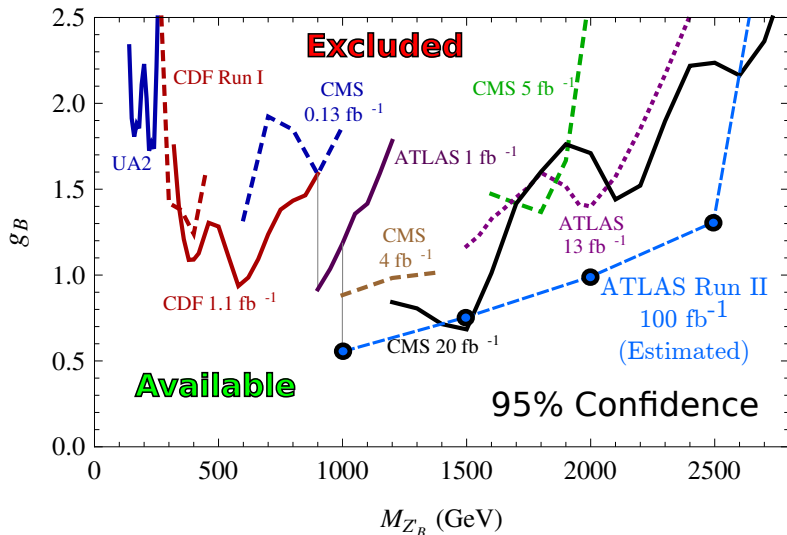
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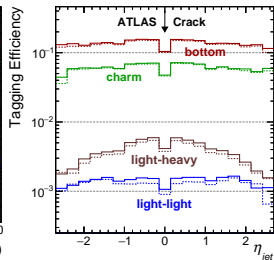
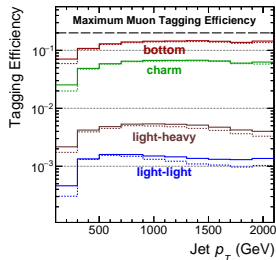
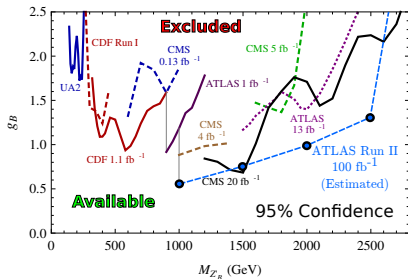


# Moving Forward

- Double-tagged exclusion is systematically limited — must detect an integer number of signal events.
  - A *single-tag* could offer a competitive (possibly better)  $S/\sqrt{BG}$ , with 15 times more signal.
- New paper by Dobrescu and Liu (arXiv: 1506.06736) proposes a  $Z'$  in 3.4–4.5 TeV range.
  - Heavy partner of possible  $W'$  seen at 1.8–2 TeV in ATLAS WZ channel.
- Seeing/excluding a bump in all three classes (0-tag / 1-tag / 2-tag) makes the strongest statement.

# Conclusion

- $\mu_x$  tags heavy flavor jets at the TeV scale.
  - **$b$ -jet:** 14%
  - **light-jet:**  $< 0.7\%$
- Flat signal response in  $p_T$  and  $\eta$ .
- Minimal pileup sensitivity.
- Should offer significant improvements in detecting/excluding  $Z'$  and other high energy phenomenon.



$$\frac{dN}{dx} = 4\pi \frac{2x}{(x^2 + 1)^2} K(x, \kappa) \quad (8)$$

where  $K(x, \kappa)$  corrects the shape

$$K(x, \kappa) = \frac{(1 + \kappa^2) + x^2(1 - \kappa^2)}{2\sqrt{1 + x^2(1 - \kappa^2)}} \Theta(x_{\max} - x) \quad (9)$$

We can calculate the maximum emission

$$x_{\max} = 1/\sqrt{\kappa^2 - 1} \approx \sqrt{\gamma_{\mu, \text{cm}}^2 - 1} \quad (10)$$

which, in our regime of interest ( $\gamma_B \gg \gamma_{\mu, \text{cm}} \gg 1$ ) is

$$x_{\max} \approx \sqrt{\gamma_{\mu, \text{cm}}^2 - 1} \quad (11)$$