

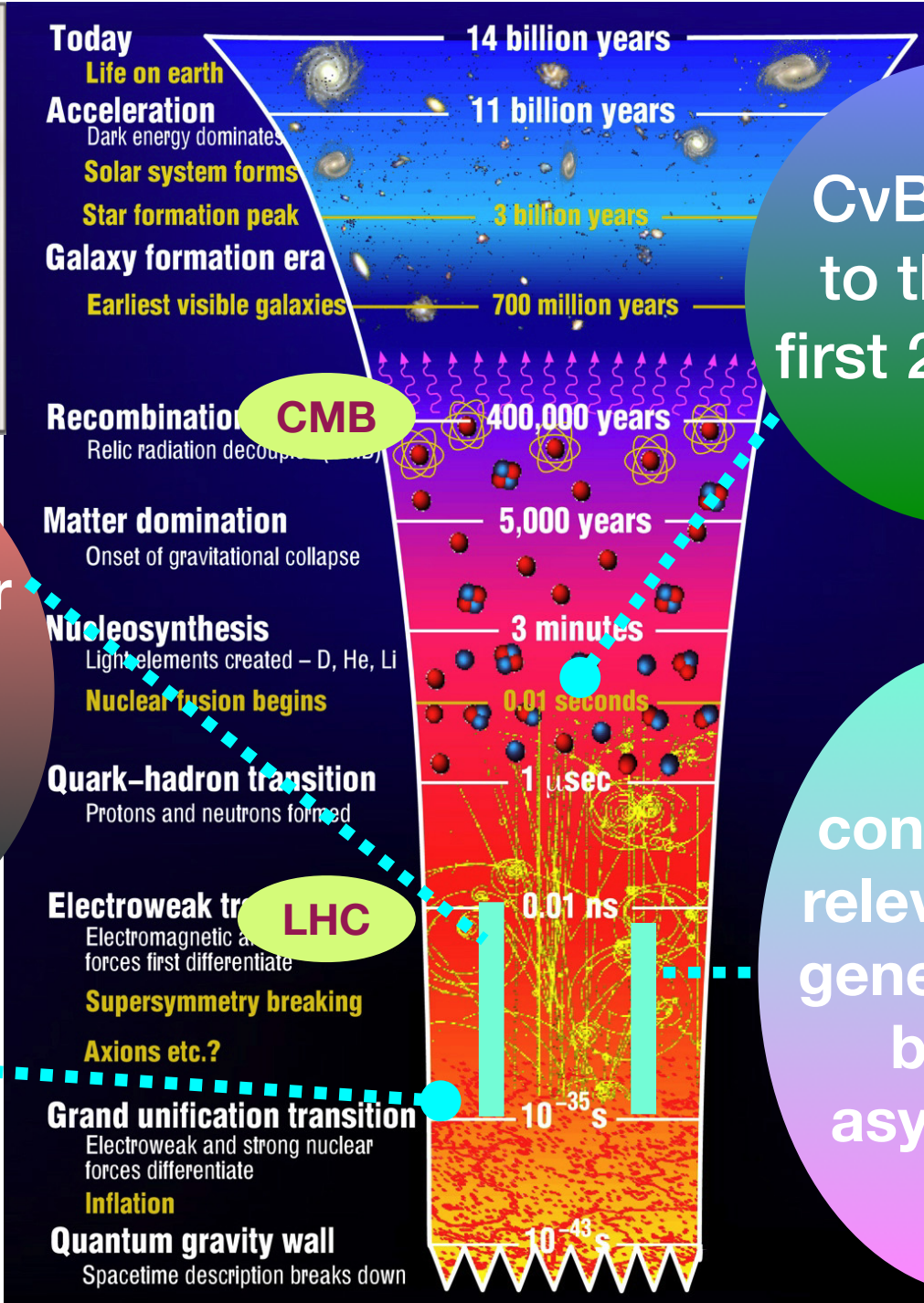
# Neutrinos and Physics beyond the Standard Model

---

Mu-Chun Chen, University of California at Irvine



DPF 2015, University of Michigan, Ann Arbor, August 7, 2015



CvB - back to the very first 2 second

operator for  $\nu$  mass generation unknown

unique window into GUT scale physics

conceivable relevance for generation of baryon asymmetry

# Where Do We Stand?

- Latest 3 neutrino global analysis (including recent results from reactor experiments and T2K):

Capozzi, Fogli, Lisi, Marrone, Montanino, Palazzo (2013, updated May 2014)

Parameter	Best fit	$1\sigma$ range	$2\sigma$ range	$3\sigma$ range
$\delta m^2/10^{-5} \text{ eV}^2$ (NH or IH)	7.54	7.32 – 7.80	7.15 – 8.00	6.99 – 8.18
$\sin^2 \theta_{12}/10^{-1}$ (NH or IH)	3.08	2.91 – 3.25	2.75 – 3.42	2.59 – 3.59
$\Delta m^2/10^{-3} \text{ eV}^2$ (NH)	2.43	2.37 – 2.49	2.30 – 2.55	2.23 – 2.61
$\Delta m^2/10^{-3} \text{ eV}^2$ (IH)	2.38	2.32 – 2.44	2.25 – 2.50	2.19 – 2.56
$\sin^2 \theta_{13}/10^{-2}$ (NH)	2.34	2.15 – 2.54	1.95 – 2.74	1.76 – 2.95
$\sin^2 \theta_{13}/10^{-2}$ (IH)	2.40	2.18 – 2.59	1.98 – 2.79	1.78 – 2.98
$\sin^2 \theta_{23}/10^{-1}$ (NH)	4.37	4.14 – 4.70	3.93 – 5.52	3.74 – 6.26
$\sin^2 \theta_{23}/10^{-1}$ (IH)	4.55	4.24 – 5.94	4.00 – 6.20	3.80 – 6.41
$\delta/\pi$ (NH)	1.39	1.12 – 1.77	0.00 – 0.16 $\oplus$ 0.86 – 2.00	—
$\delta/\pi$ (IH)	1.31	0.98 – 1.60	0.00 – 0.02 $\oplus$ 0.70 – 2.00	—

→ evidence of  $\theta_{13} \neq 0$

→ hints of  $\theta_{23} \neq \pi/4$

→ expectation of Dirac CP phase  $\delta$

→ no clear preference for hierarchy

→ Majorana vs Dirac

Recent T2K result  $\Leftrightarrow \delta \simeq -\pi/2$ , consistent with global fit best fit value

# Where Do We Stand?

---

- search for absolute mass scale:
  - end point kinematic of tritium beta decays

$$m_{\nu_e} < 2.2 \text{ eV (95\% CL) Mainz}$$

$$m_{\nu_\mu} < 170 \text{ keV}$$

$$m_{\nu_\tau} < 15.5 \text{ MeV}$$



**KATRIN: increase sensitivity ~ 0.2 eV**

- neutrinoless double beta decay

$$\text{current bound: } |\langle m \rangle| \equiv \left| \sum_{i=1,2,3} m_i U_{ie}^2 \right| < (0.14-0.38) \text{ eV (EXO, 2012)}$$

- Cosmology  $\sum(m_{\nu_i}) < 0.49 \text{ eV}$

$N_{\text{eff}} = 3.04 \pm 0.2$  [Planck 2015]  $\Rightarrow$  sterile neutrino **disfavored**

# Open Questions - Neutrino Properties



- 👉 Majorana vs Dirac?
- 👉 CP violation in lepton sector?
- 👉 Absolute mass scale of neutrinos?
- 👉 Mass ordering: sign of  $(\Delta m_{13}^2)$ ?
- 👉 Precision:  $\theta_{23} > \pi/4$ ,  $\theta_{23} < \pi/4$ ,  $\theta_{23} = \pi/4$  ?
- 👉 Sterile neutrino(s)?

a suite of current and upcoming experiments to address these puzzles

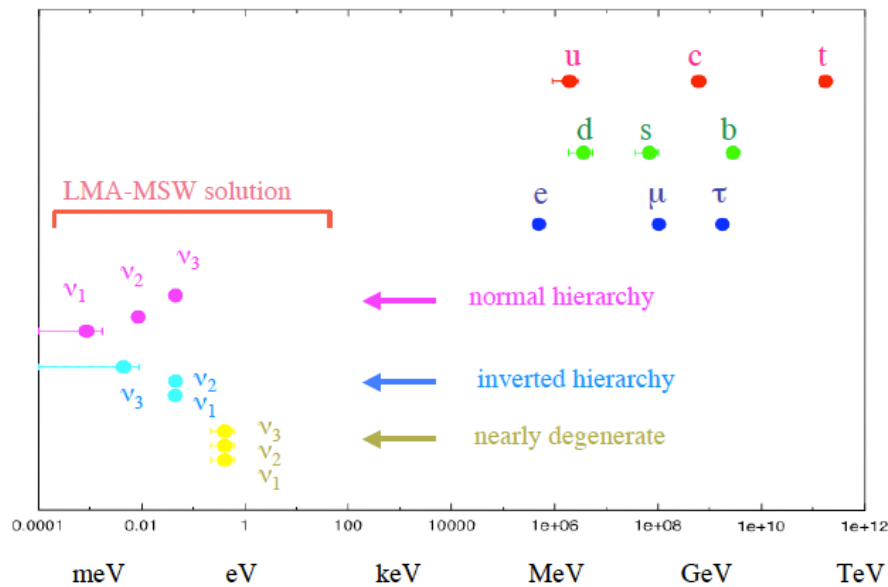
some can only be answered by oscillation experiments

# Open Questions - Theoretical

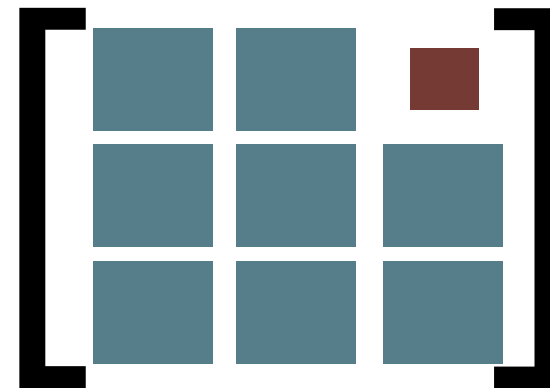


☞ Smallness of neutrino mass:

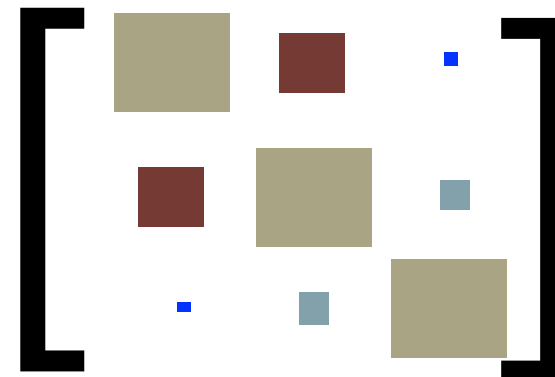
$$m_\nu \ll m_{e, u, d}$$



☞ Flavor structure:



leptonic mixing



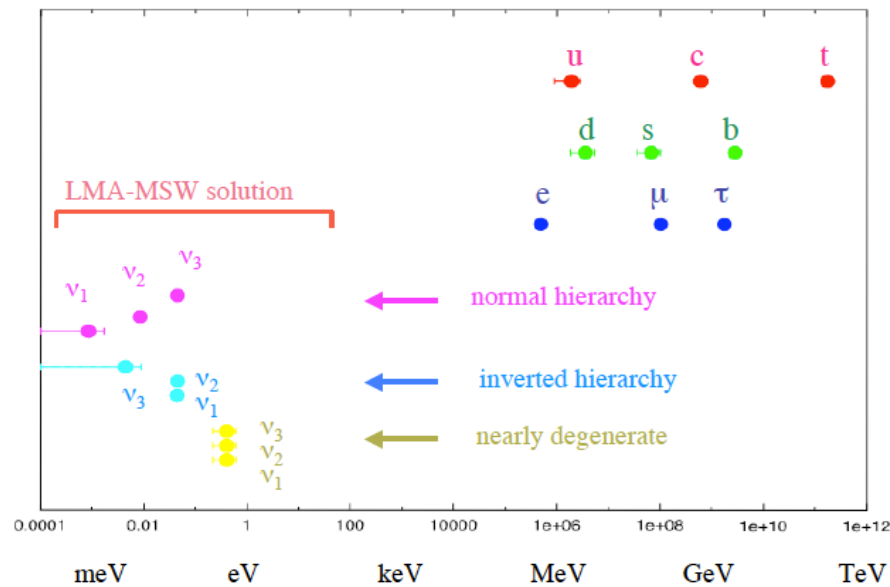
quark mixing

# Open Questions - Theoretical

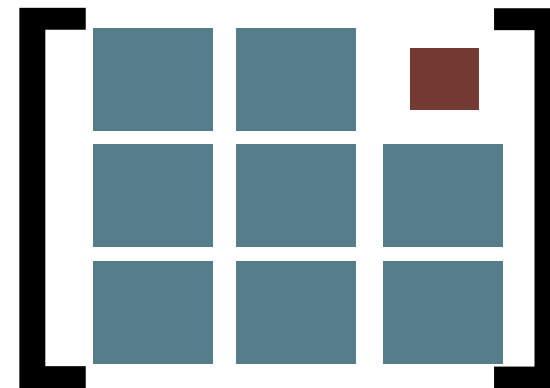


☞ Smallness of neutrino mass:

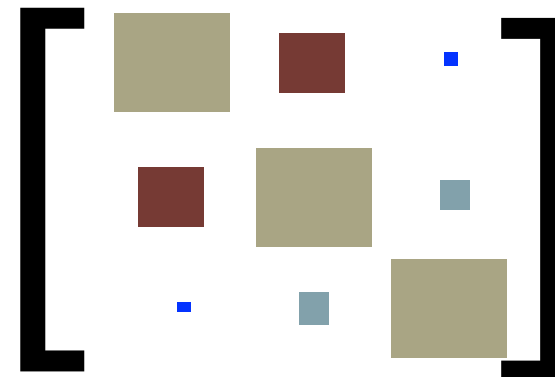
$$m_\nu \ll m_{e, u, d}$$



☞ Flavor structure:



leptonic mixing



quark mixing

**Fermion mass and hierarchy problem** ⇒ Many free parameters in the Yukawa sector of SM

# Smallness of neutrino masses

What is the operator for neutrino mass generation?

- Majorana vs Dirac
- scale of the operator
- suppression mechanism



# Neutrino Mass beyond the SM

---

- SM: effective low energy theory

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{\mathcal{O}_{5D}}{M} + \frac{\mathcal{O}_{6D}}{M^2} + \dots$$

→ new physics effects

- only one dim-5 operator: most sensitive to high scale physics

$$\frac{\lambda_{ij}}{M} H H L_i L_j \quad \Rightarrow \quad m_\nu = \lambda_{ij} \frac{v^2}{M}$$

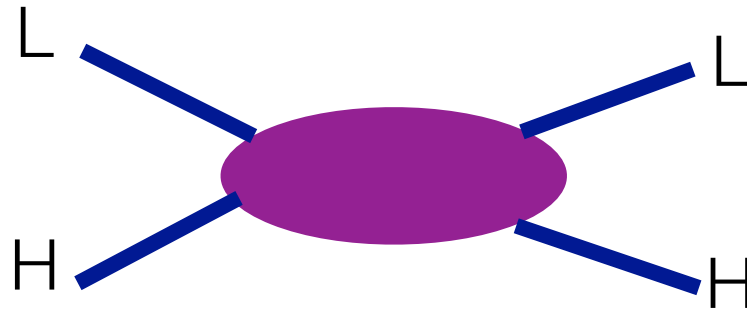
Weinberg, 1979

- $m_\nu \sim (\Delta m^2_{\text{atm}})^{1/2} \sim 0.1 \text{ eV}$  with  $v \sim 100 \text{ GeV}$ ,  $\lambda \sim O(1) \Rightarrow M \sim 10^{14} \text{ GeV}$

- Lepton number violation  $\Rightarrow$  Majorana fermions

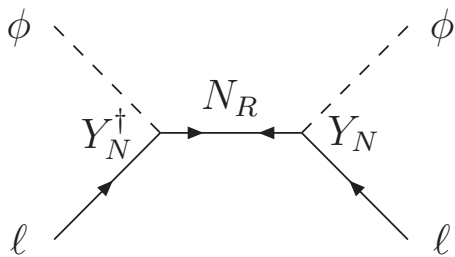
↕  
GUT scale

# Neutrino Mass beyond the SM



3 possible portals

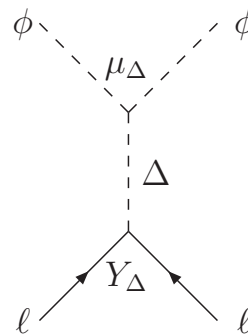
## Type-I seesaw



$$N_R: \text{SU}(3)_c \times \text{SU}(2)_w \times \text{U}(1)_Y \sim (1, 1, 0)$$

Minkowski, 1977; Yanagida, 1979; Glashow, 1979;  
Gell-mann, Ramond, Slansky, 1979;  
Mohapatra, Senjanovic, 1979;

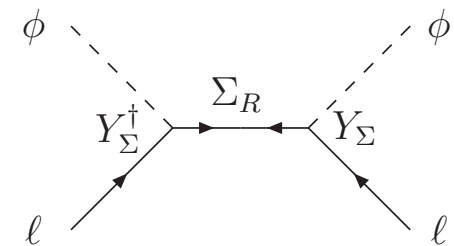
## Type-II seesaw



$$\Delta: \text{SU}(3)_c \times \text{SU}(2)_w \times \text{U}(1)_Y \sim (1, 3, 2)$$

Lazarides, 1980; Mohapatra, Senjanovic, 1980

## Type-III seesaw

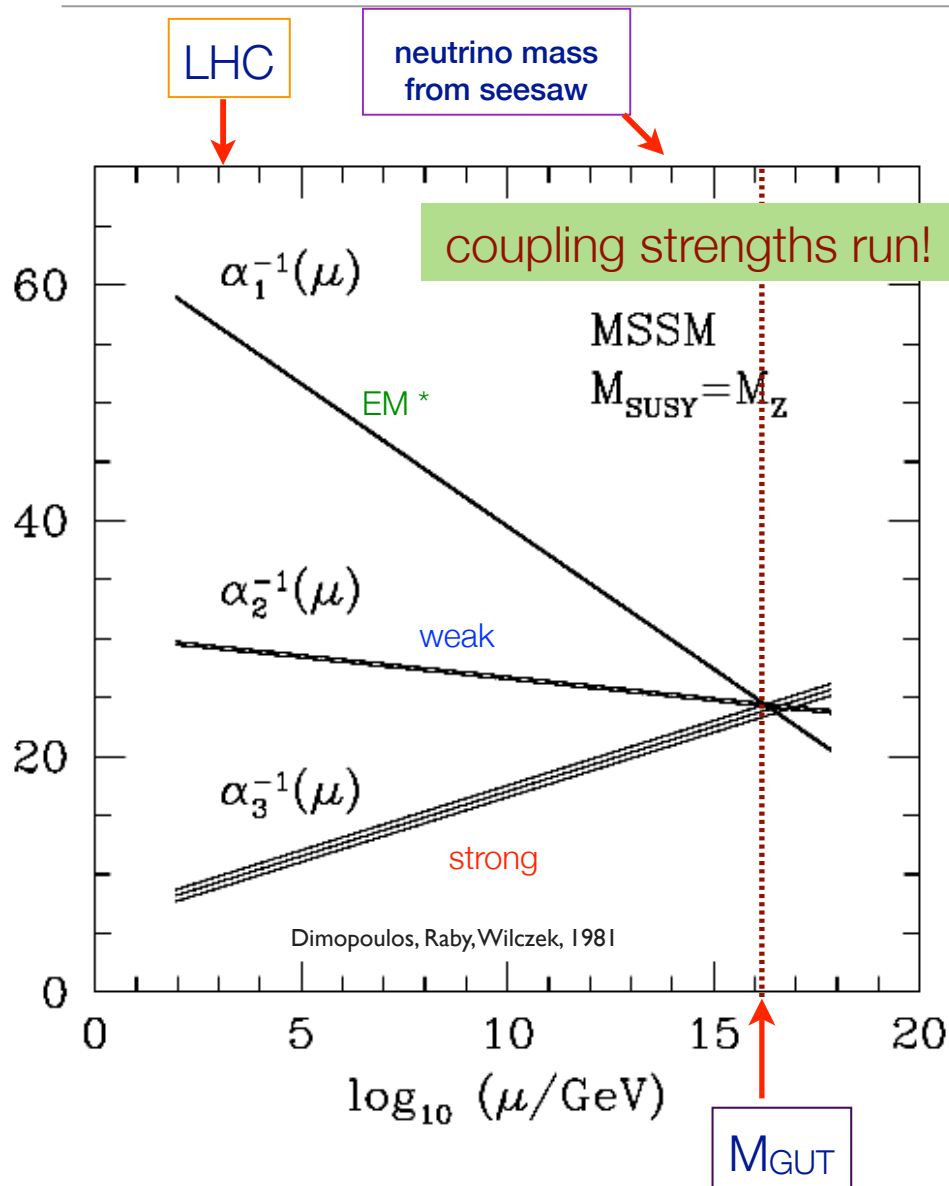


$$\Sigma = (\Sigma^+, \Sigma^0, \Sigma^-)$$

$$\Sigma_R: \text{SU}(3)_c \times \text{SU}(2)_w \times \text{U}(1)_Y \sim (1, 3, 0)$$

Foot, Lew, He, Joshi, 1989; Ma, 1998

# Grand Unification Naturally Accommodates Seesaw



- origin of the heavy scale  $\Rightarrow U(1)_{B-L}$
- exotic mediators  $\Rightarrow$  predicted in many GUT theories, e.g.  $SO(10)$

Fritzsch, Minkowski, 1975

$$16 = (3, 2, 1/6) \sim \begin{bmatrix} u & u & u \\ d & d & d \end{bmatrix}$$

$$+ (3^*, 1, -2/3) \sim (u^c \ u^c \ u^c)$$

$$+ (3^*, 1, 1/3) \sim (d^c \ d^c \ d^c)$$

$$+ (1, 2, -1/2) \sim \begin{bmatrix} \nu \\ e \end{bmatrix}$$

$$+ (1, 1, 1) \sim e^c$$

$$+ (1, 1, 0) \sim \nu^c$$

- exotic mediators in Type II, III: not easy to get in string theories

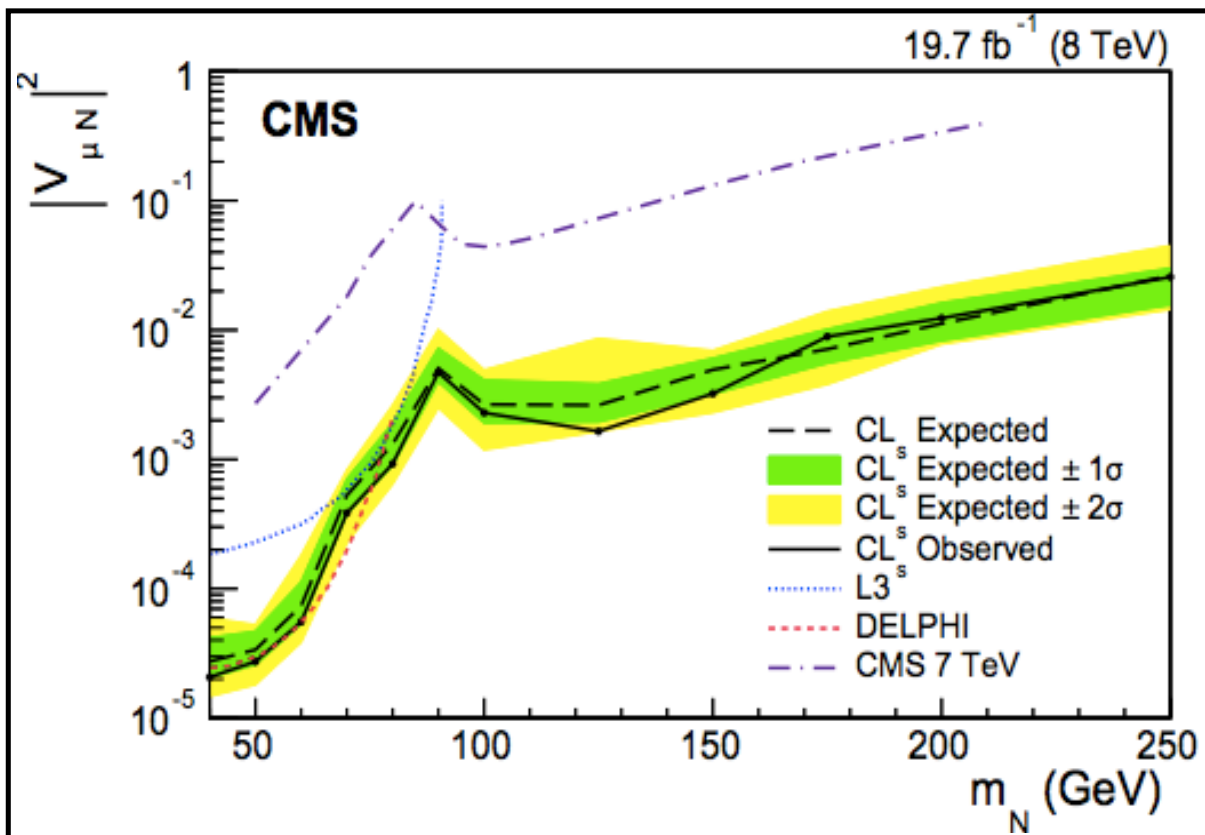
Dienes, March-Russell (1996)

# Low Scale Seesaws

---

- New particles:
  - Type I seesaw: generally decouple from collider experiments
  - Type II seesaw:  $\Delta^{++} \rightarrow e^+e^+, \mu^+\mu^+, \tau^+\tau^+$
  - Type III seesaw: observable displaced vertex Franceschino, Hambye, Strumia, 2008
  - inverse seesaw: non-unitarity effects
  - radiative mass generation: model dependent - singly/doubly charged SU(2) singlet, even colored scalars in loops
- New interactions:
  - LR symmetric model:  $W_R$
  - R parity violation:  $\tan^2 \theta_{\text{atm}} \simeq \frac{BR(\tilde{\chi}_1^0 \rightarrow \mu^\pm W^\mp)}{BR(\tilde{\chi}_1^0 \rightarrow \tau^\pm W^\mp)}$  Mukhopadhyaya, Roy, Vissani, 1998
  - .....

# Cautions!!! Is it really the $\nu_R$ in Type I seesaw?

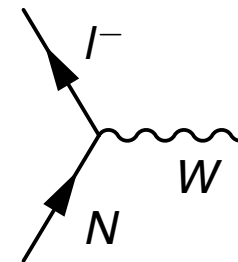


Expanded view of the region:

$40 \text{ GeV} < m_N < 250 \text{ GeV}$

Talk by E. Tiras

RH neutrino production thru active-sterile mixing:



$$\propto V = \frac{m_D}{M_R} \sim \frac{10^{-4} \text{ GeV}}{100 \text{ GeV}} = 10^{-6}$$

RH neutrino relevant for  $\nu$  mass generation

$$\Rightarrow |V_{\mu N}|^2 = 10^{-12}$$

unless extremely fine-tuned

Kersten, Smirnov (2007)

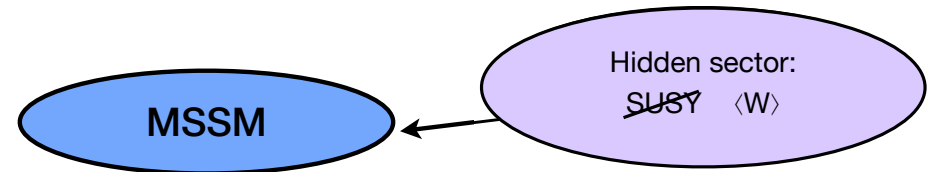
# Dirac Neutrinos and SUSY Breaking

---

- ▶ naturally small Dirac neutrino masses can arise
  - ▶ Randall-Sundrum model
  - ▶ Supersymmetry breaking
- ▶ before SUSY breaking: absence of Dirac neutrino masses (as well as Weinberg operator)
- ▶ after SUSY breaking: realistic effective Dirac neutrino masses generated

$$Y_\nu \sim \frac{m_{3/2}}{M_P} \sim \frac{\mu}{M_P}$$

Arkani-Hamed, Hall, Murayama, Tucker-Smith, Weiner (2001)



- ▶ similar to the Giudice-Masiero Mechanism for the mu problem

$$\mu \sim \langle \mathcal{W} \rangle / M_P^2 \sim m_{3/2}$$

Giudice, Masiero (1988)

- ▶ Need a symmetry reason for the absence of these operators before SUSY breaking

# Dirac Neutrinos and SUSY Breaking

- Simultaneous realization of these two scenarios can arise in MSSM with discrete R symmetries,  $\mathbb{Z}_M^R$  M.-C. C., M. Ratz, C. Staudt, P. Vaudrevange (2012)

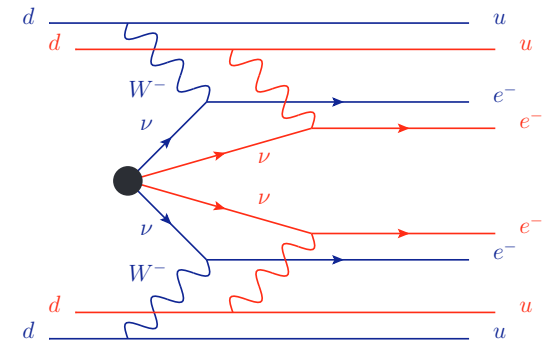
- ▶ neutrinos are of the Dirac type, with naturally small masses
- ▶  $\Delta L = 2$  operators forbidden to all orders  $\Rightarrow$  no neutrinoless double beta decay

- ▶ **New signature: lepton number violation  $\Delta L = 4$  operators,  $(\nu_R)^4$ , allowed  $\Rightarrow$  new LNV processes, e.g.** M.-C. C., M. Ratz, C. Staudt, P. Vaudrevange (2012)

- neutrinoless quadruple beta decay

Heeck, Rodejohann (2013)

- mu term is naturally small, simultaneously
- dangerous proton decay operators forbidden/suppressed
- may simultaneously explain the flavor structure with discrete generation dependent R symmetries (even with non-Abelian!) M.-C.C., M. Ratz, A. Trautner (2013)
- Dynamical generation of RPV operators with size predicted M.-C.C., M. Ratz, V. Takhistov (2014)

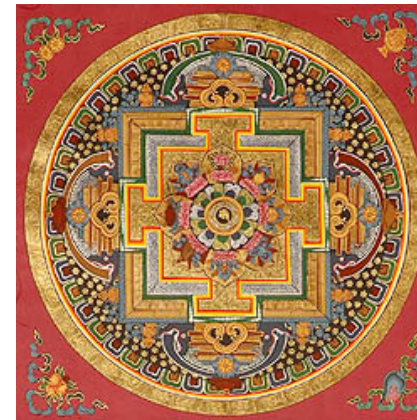


# Flavor structure

anarchy

vs

symmetry



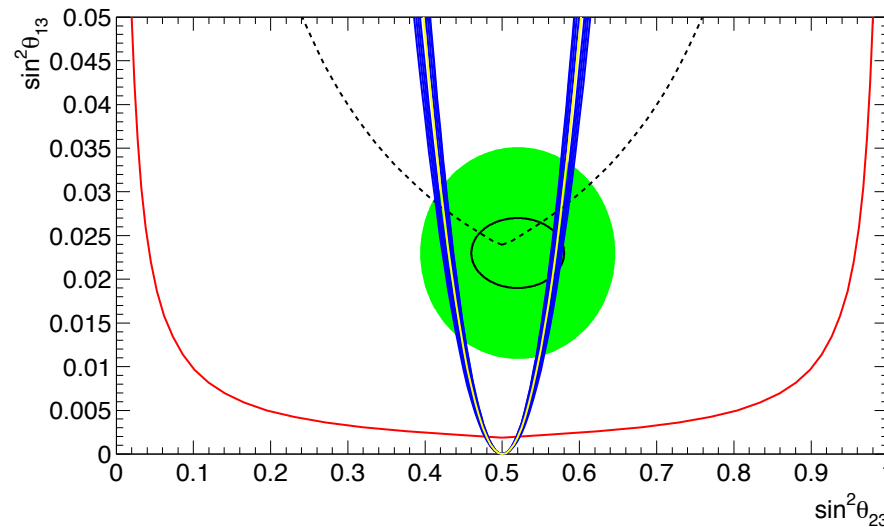


# Anarchy

Hall, Murayama, Weiner (2000);  
de Gouvea, Murayama (2003)



- there are no parametrically small numbers
- large mixing angle, near mass degeneracy statistically preferred



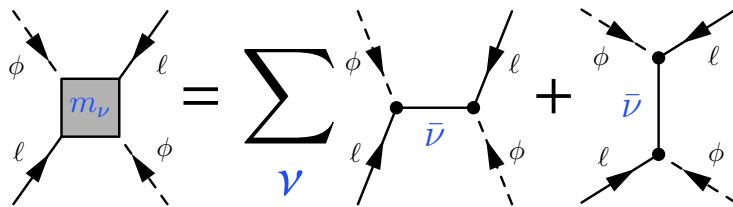
de Gouvea, Murayama (2012)

- UV theory prediction can resemble anarchy
  - warped extra dimensions
  - heterotic string theory

# Expectations from Heterotic String Theories

- heterotic string models: O(100) RH neutrinos

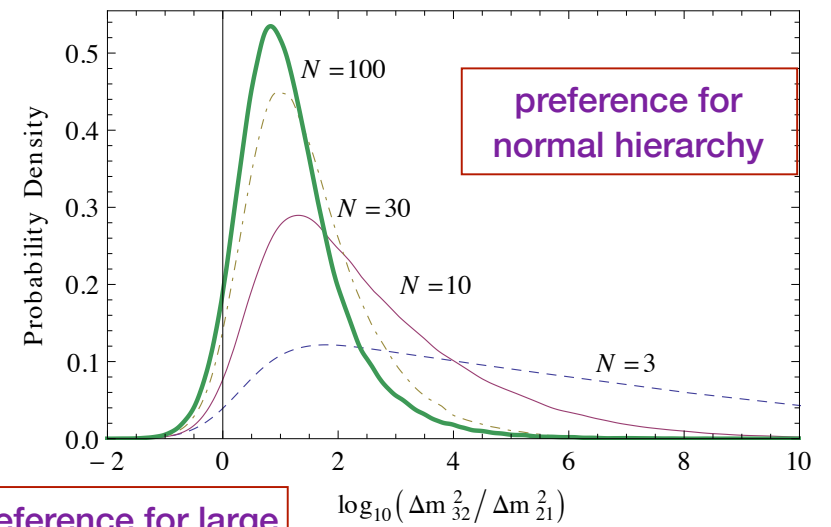
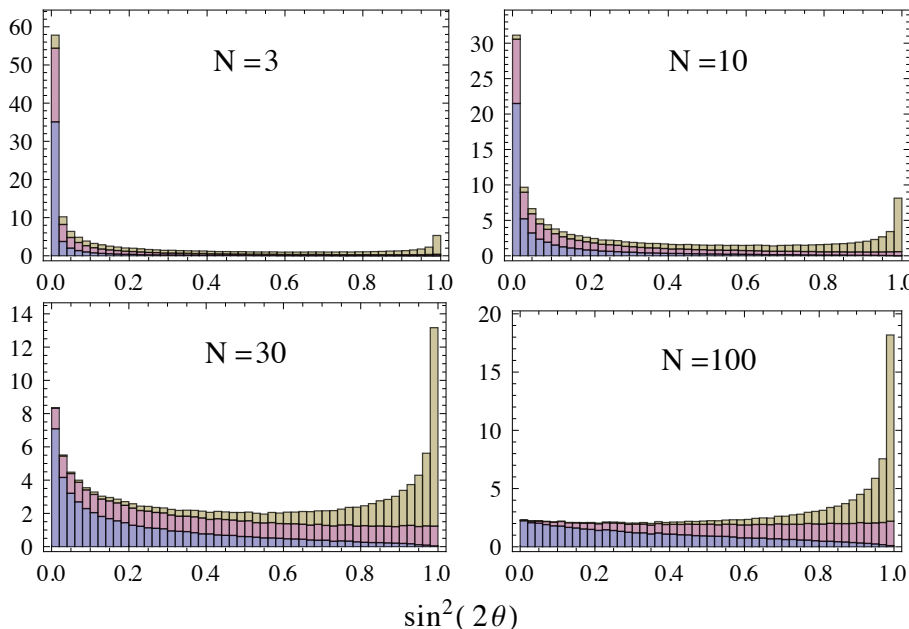
Buchmüller, Hamaguchi, Lebedev,  
Ramos-Sánchez, Ratz (2007)



$$m_\nu \sim \frac{v^2}{M_*} \quad \left( M_* \sim \frac{M_{\text{GUT}}}{10 \dots 100} \right)$$

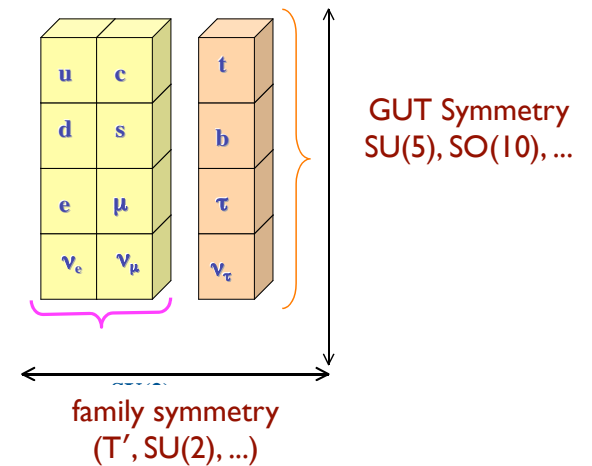
- statistical expectations with large N (= # of RH neutrinos)

Feldstein, Klemm (2012)



# Origin of Flavor Mixing and Mass Hierarchy

- Several models have been constructed based on
  - GUT Symmetry [SU(5), SO(10)]  $\oplus$  Family Symmetry  $G_F$
- Family Symmetries  $G_F$  based on continuous groups:
  - U(1)
  - SU(2)
  - SU(3)



- Recently, models based on discrete family symmetry groups have been constructed
  - $A_4$  (tetrahedron)
  - $T'$  (double tetrahedron)
  - $S_3$  (equilateral triangle)
  - $S_4$  (octahedron, cube)
  - $A_5$  (icosahedron, dodecahedron)
  - $\Delta_{27}$
  - $Q_6$



# Tri-bimaximal Neutrino Mixing

---

Capozzi, Fogli, Lisi, Marrone, Montanino, Palazzo (March 2014)

- Latest Global Fit ( $3\sigma$ )

$$\sin^2 \theta_{23} = 0.437 (0.374 - 0.626) \quad [\theta^{\text{lep}}_{23} \sim 41.2^\circ]$$

$$\sin^2 \theta_{12} = 0.308 (0.259 - 0.359) \quad [\theta^{\text{lep}}_{12} \sim 33.7^\circ]$$

$$\sin^2 \theta_{13} = 0.0234 (0.0176 - 0.0295) \quad [\theta^{\text{lep}}_{13} \sim 8.80^\circ]$$

- Tri-bimaximal Mixing Pattern

Harrison, Perkins, Scott (1999)

$$U_{TBM} = \begin{pmatrix} \sqrt{2/3} & \sqrt{1/3} & 0 \\ -\sqrt{1/6} & \sqrt{1/3} & -\sqrt{1/2} \\ -\sqrt{1/6} & \sqrt{1/3} & \sqrt{1/2} \end{pmatrix}$$

$$\sin^2 \theta_{\text{atm}, TBM} = 1/2$$

$$\sin^2 \theta_{\odot, TBM} = 1/3$$

$$\sin \theta_{13, TBM} = 0.$$

- Leading Order: TBM (from symmetry) + higher order corrections/contributions

- More importantly, corrections to the kinetic terms

Leurer, Nir, Seiberg (1993);  
Dudas, Pokorski, Savoy (1995)

M.-C.C., M. Fallbacher, M. Ratz, C. Staudt, (2012)

# Symmetry Relations

## Quark Mixing

mixing parameters	best fit	$3\sigma$ range
$\theta_{23}^q$	$2.36^\circ$	$2.25^\circ - 2.48^\circ$
$\theta_{12}^q$	$12.88^\circ$	$12.75^\circ - 13.01^\circ$
$\theta_{13}^q$	$0.21^\circ$	$0.17^\circ - 0.25^\circ$

## Lepton Mixing

mixing parameters	best fit	$3\sigma$ range
$\theta_{23}^e$	$41.2^\circ$	$35.1^\circ - 52.6^\circ$
$\theta_{12}^e$	$33.6^\circ$	$30.6^\circ - 36.8^\circ$
$\theta_{13}^e$	$8.9^\circ$	$7.5^\circ - 10.2^\circ$

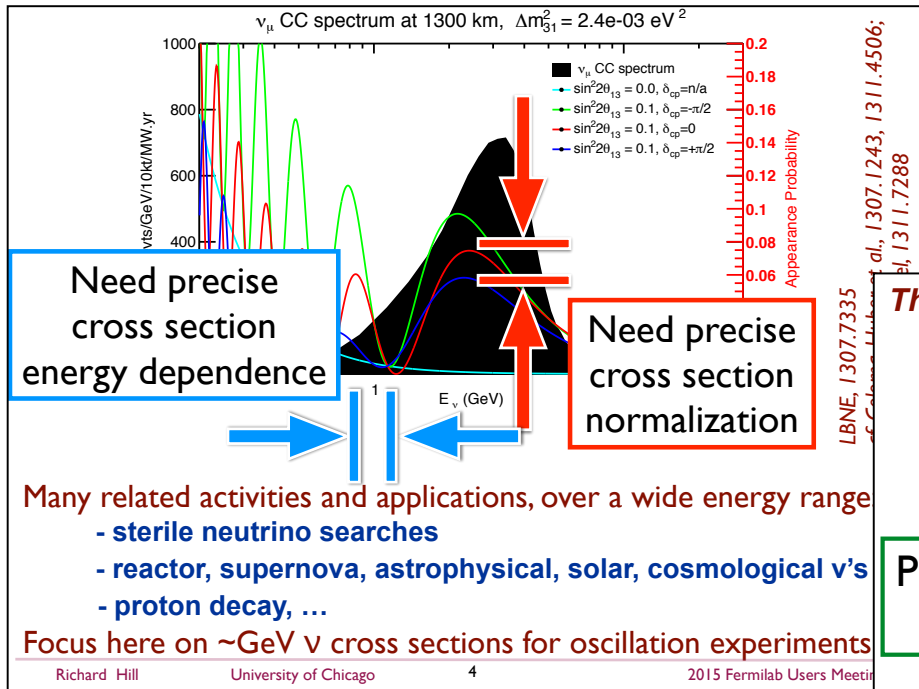
- **QLC-I**  $\theta_c + \theta_{\text{sol}} \cong 45^\circ$  Raidal, '04; Smirnov, Minakata, '04  
 (BM)  $\theta_{23}^q + \theta_{23}^e \cong 45^\circ$  ☞ **slight inconsistent**

- **QLC-II**  $\tan^2\theta_{\text{sol}} \cong \tan^2\theta_{\text{sol,TBM}} + (\theta_c / 2) * \cos \delta_e$  Ferrandis, Pakvasa; Dutta, Mimura; M.-C.C., Mahanthappa  
 (TBM)  $\theta_{13}^e \cong \theta_c / 3\sqrt{2}$  ☞ **Too small**

- testing symmetry relations: a *more* robust way to distinguish different classes of models

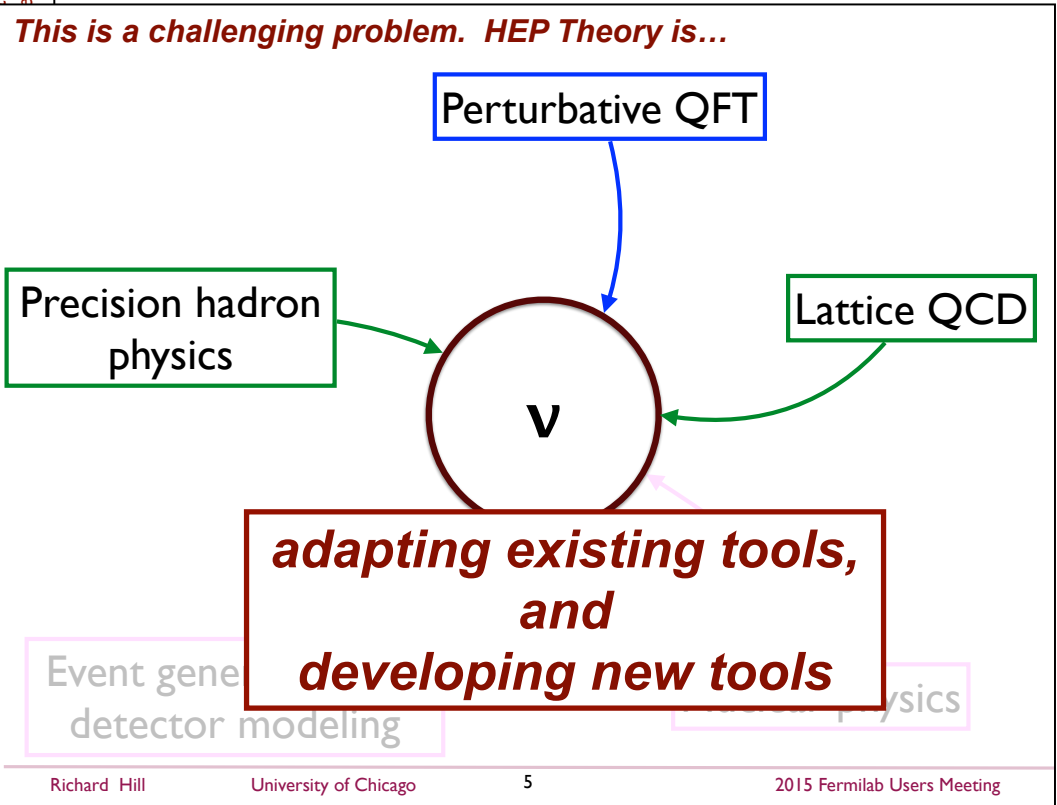
**measuring leptonic mixing parameters to the precision of those in quark sector**

# Aside: Precision Cross Section



See Talk by Richard Hill

HEP Theory can contribute!



# Origin of CP Violation

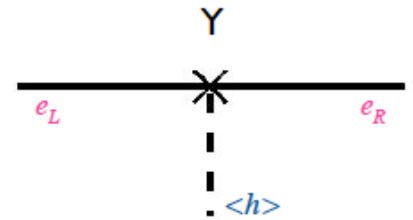
---

- CP violation  $\Leftrightarrow$  complex mass matrices

$$\bar{U}_{R,i}(M_u)_{ij}Q_{L,j} + \bar{Q}_{L,j}(M_u^\dagger)_{ji}U_{R,i} \xrightarrow{\text{CP}} \bar{Q}_{L,j}(M_u)_{ij}U_{R,i} + \bar{U}_{R,i}(M_u)_{ij}^*Q_{L,j}$$

- Conventionally, CPV arises in two ways:

- Explicit CP violation: complex Yukawa coupling constants  $Y$
- Spontaneous CP violation: complex scalar VEVs  $\langle h \rangle$



- **Complex CG coefficients in certain discrete groups  $\Rightarrow$  explicit CP violation**
  - CPV in quark and lepton sectors purely from complex CG coefficients

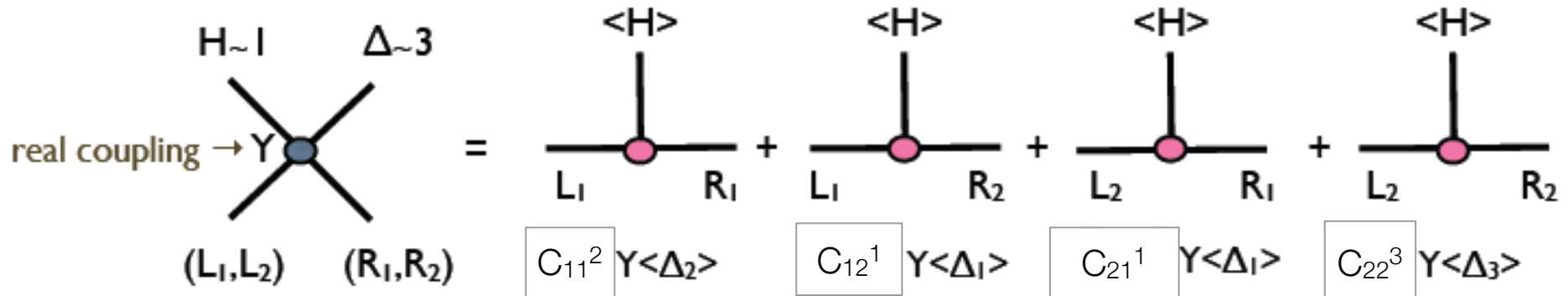
**CG coefficients in non-Abelian discrete symmetries**  
 $\Rightarrow$  relative strengths and phases in entries of Yukawa matrices  
 $\Rightarrow$  mixing angles and phases (and mass hierarchy)

# Group Theoretical Origin of CP Violation

M.-C.C., K.T. Mahanthappa  
Phys. Lett. B681, 444 (2009)

## Basic idea

Discrete  
symmetry  $G$



- Scalar potential: if  $Z_3$  symmetric  $\Rightarrow \langle \Delta_1 \rangle = \langle \Delta_2 \rangle = \langle \Delta_3 \rangle \equiv \langle \Delta \rangle$  real
- Complex effective mass matrix: **phases determined by group theory**

$C_{ij}^k$ :  
complex CG  
coefficients of  
 $G$

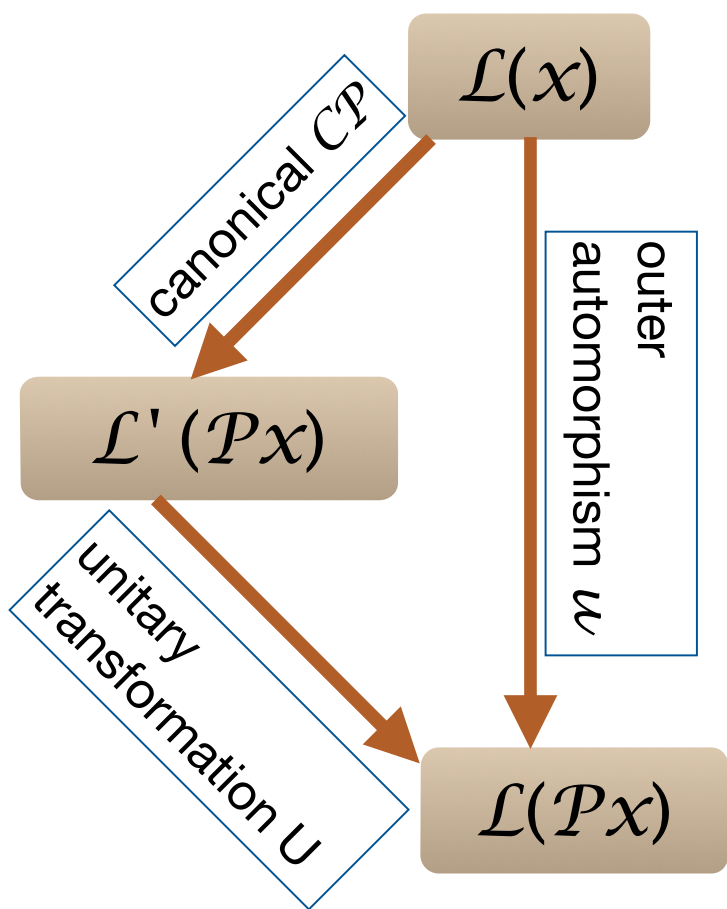
$$M = \begin{pmatrix} (L_1 & L_2) \\ C_{11}^2 & C_{21}^1 \\ C_{12}^1 & C_{22}^3 \end{pmatrix} Y \langle \Delta \rangle \begin{pmatrix} (R_1 \\ R_2) \end{pmatrix}$$



# Group Theoretical Origin of CP Violation

M.-C.C, M. Fallbacher, K.T. Mahanthappa,  
M. Ratz, A. Trautner, NPB (2014)

complex CGs  $\Leftrightarrow G$  and physical CP transformations do not commute



$$\Phi(x) \xrightarrow{\widetilde{CP}} U_{CP} \Phi^*(\mathcal{P} x)$$

$$\rho_{r_i}(u(g)) = U_{r_i} \rho_{r_i}(g)^* U_{r_i}^\dagger \quad \forall g \in G \text{ and } \forall i$$

**$u$  has to be a class-inverting,  
involuntary automorphism of  $G$**   
 $\Rightarrow$  **non-existence of such automorphism  
in certain groups**  
 $\Rightarrow$  **explicit physical CP violation in  
generic setting**

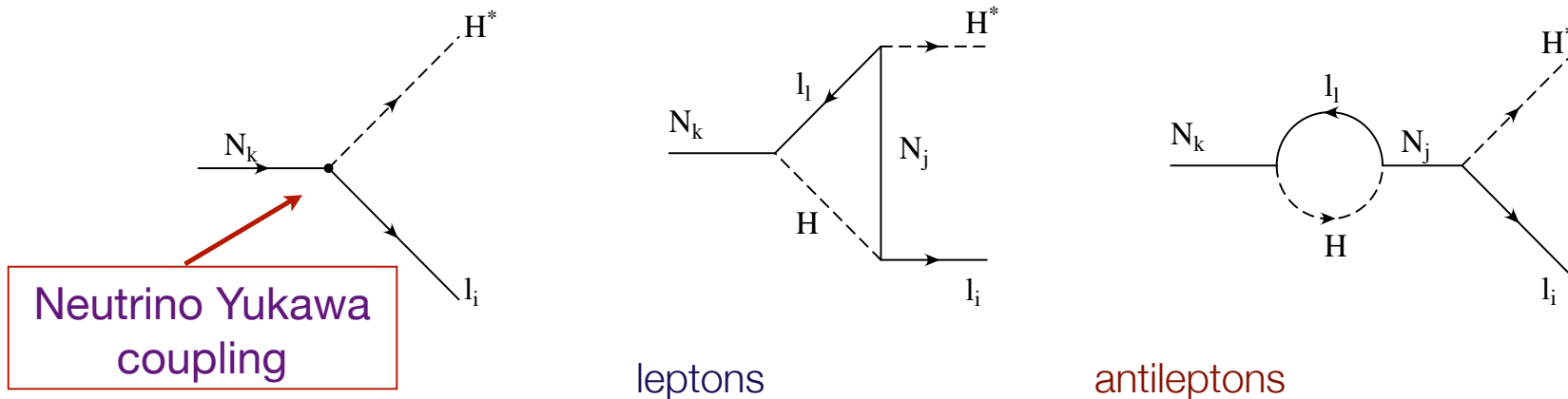
examples:  $T_7, \Delta(27), \dots$

# Cosmological Connection

# Standard Leptogenesis

Fukugita, Yanagida, 1986

- RH heavy neutrino decay:
  - quantum interference of tree-level & one-loop diagrams  $\Rightarrow$  primordial lepton number asymmetry  $\Delta L$



$$\epsilon_1 = \frac{\sum_{\alpha} [\Gamma(N_1 \rightarrow \ell_{\alpha} H) - \Gamma(N_1 \rightarrow \bar{\ell}_{\alpha} \bar{H})]}{\sum_{\alpha} [\Gamma(N_1 \rightarrow \ell_{\alpha} H) + \Gamma(N_1 \rightarrow \bar{\ell}_{\alpha} \bar{H})]}$$

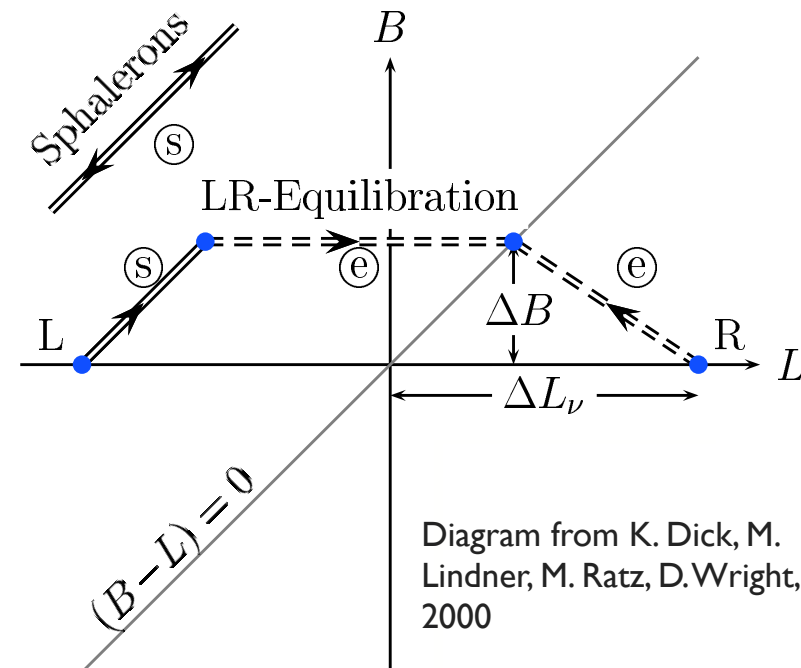
Leptonic CP violation  $\Rightarrow \Delta L \propto [\Gamma(N_1 \rightarrow \ell_{\alpha} H) - \Gamma(N_1 \rightarrow \bar{\ell}_{\alpha} \bar{H})] \neq 0$

# Dirac Leptogenesis

K. Dick, M. Lindner, M. Ratz, D. Wright, 2000;  
H. Murayama, A. Pierce, 2002

- Leptogenesis possible even when neutrinos are Dirac particles (no  $\Delta L = 2$  violation)
- Characteristics of Sphaleron effects:
  - only left-handed fields couple to sphalerons
  - sphalerons change  $(B+L)$  but not  $(B-L)$
  - sphaleron effects in equilibrium for  $T > T_{ew}$

late time LR equilibration of neutrinos making Dirac leptogenesis possible with primordial  $\Delta L = 0$



# Recent progress in Leptogenesis

---

## Toward the Theory of Leptogenesis:

Buchmuller, Fredenhagen, 2000;  
Simone, Riotto 2007;  
Lindner, Muller 2007

**Classical Boltzmann Equations**



**Quantum Boltzmann Equations**

**(Closed-time-path formulation for non-equilibrium QFT)**

Schwinger, 1961; Mahanthappa, 1962; Bakshi, Mahanthappa, 1963; Keldysh, 1965

Lots of progress, both quantitatively and qualitatively; still too early to see how big the impacts are

# Conclusions

---

- Fundamental origin of fermion mass hierarchy and flavor mixing still not known
- Neutrino masses: evidence of physics beyond the SM
- **Symmetries**: can provide an understanding of the pattern of fermion masses and mixing
  - correlations, correlations, correlations:
    - quark & lepton mixing parameters
    - lepton flavor violating charged lepton decays
    - proton (nucleon) decay, neutron-antineutron oscillation

