

# Muon Cooling Progress and Prospects for an S-channel Muon Collider Higgs Factory



M. A. Cummings ••• Muons, Inc. ••• August 5, 2015 ••• DPF 2015  
Ann Arbor, MI

...or, one highly possible, desirable facility that could illuminate the nature of the recently discovered Higgs Boson on the once and future path to the energy frontier that runs productively through the peculiar and unique capabilities of Fermilab:

- Muon storage rings as high precision neutrino sources.
- A Z' Factory
- **A Higgs Factory** ←
- A Muon Collider is an ideal technology for a TeV or multi-TeV collider.

# P5 Goals: Long-Range Accelerator R&D

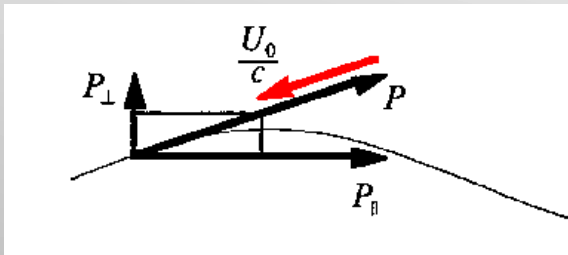
- “For  $e^+e^-$  Colliders the primary goals are:
  - Improving the gradient and lowering the power consumption”
    - **P5, Building for Discovery , p. 19 (May 2014)**
- Both goals are achieved by increasing the mass of the electrons
  - Higher mass electrons will not radiate ( $\sim m^{-4}$ ); enabling multipass acceleration; gradient is improved by number of turns
  - Non-radiating electrons, multipass acceleration, consume less power
- Changing the electron mass ... ( $m_e$  is quantized)
  - 0.511, **105.6**, 1777 MeV
- 105.6 MeV is optimum for next generation  $e^+e^-$  Colliders
  - requires  $E' \gg m_e / c\tau_e = 0.16$  MV/m

# High-Luminosity Lepton Colliders Need Cooling

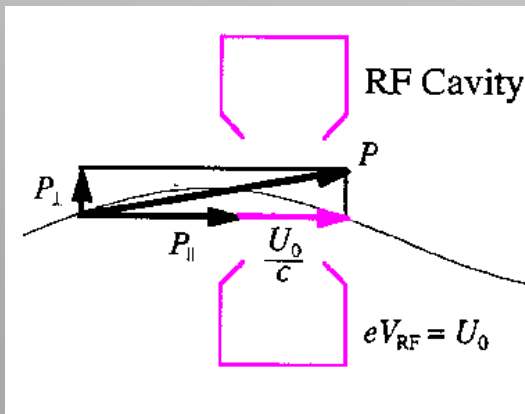
## Light $e^-$ :

– radiation damping

1. Lose  $P_{e,t}$  in bends - synchrotron radiation



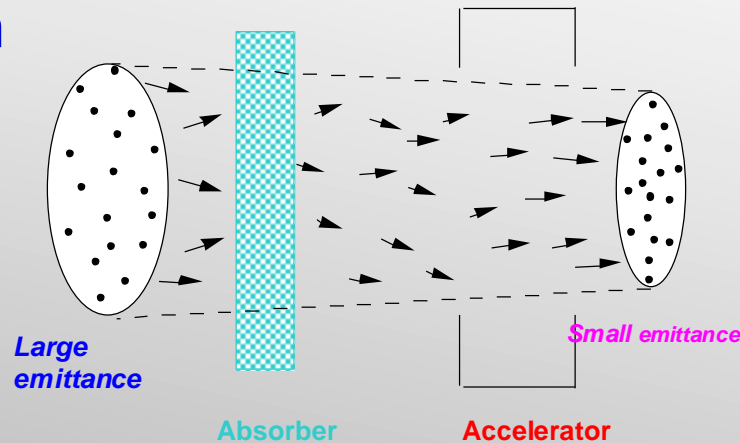
2. Regain only  $P_z$  in RF



## Heavy $e^-$ :

– “ionization cooling” ....

1. Lose  $P_{l,t}$  in material –



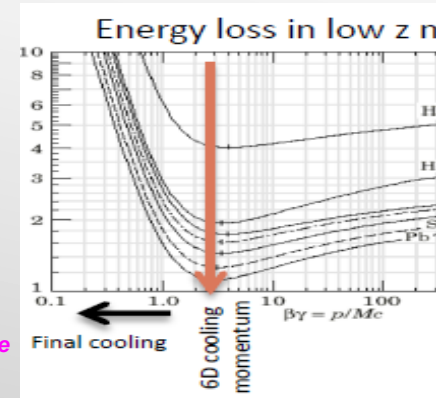
Momentum loss is opposite to motion,  $p_x, p_y, p_z, \Delta E$  decrease

Momentum gain is purely longitudinal

2. Regain only  $P_z$  in RF

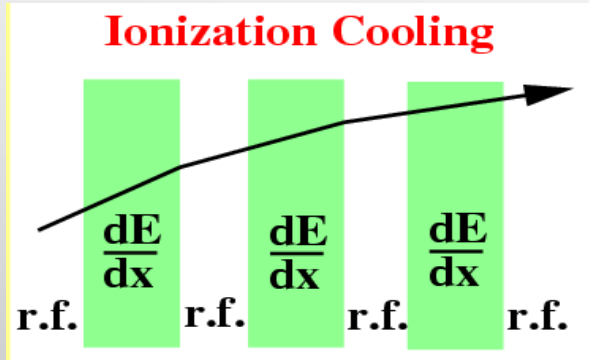
$$\frac{d\epsilon_N}{ds} = -\frac{1}{P_l} \frac{dP_l}{ds} \epsilon_N + \frac{\beta_{\perp} E_s^2}{2\beta^3 m_l c^2 L_R E}$$

Heating by multiple scattering

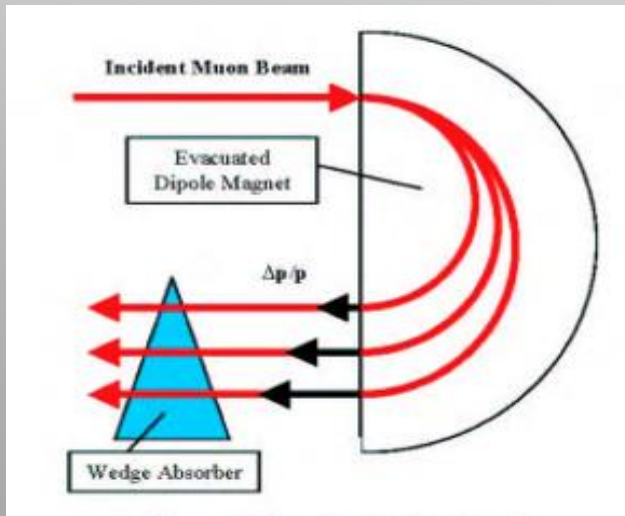


# 6 D Ionization Cooling and Emittance

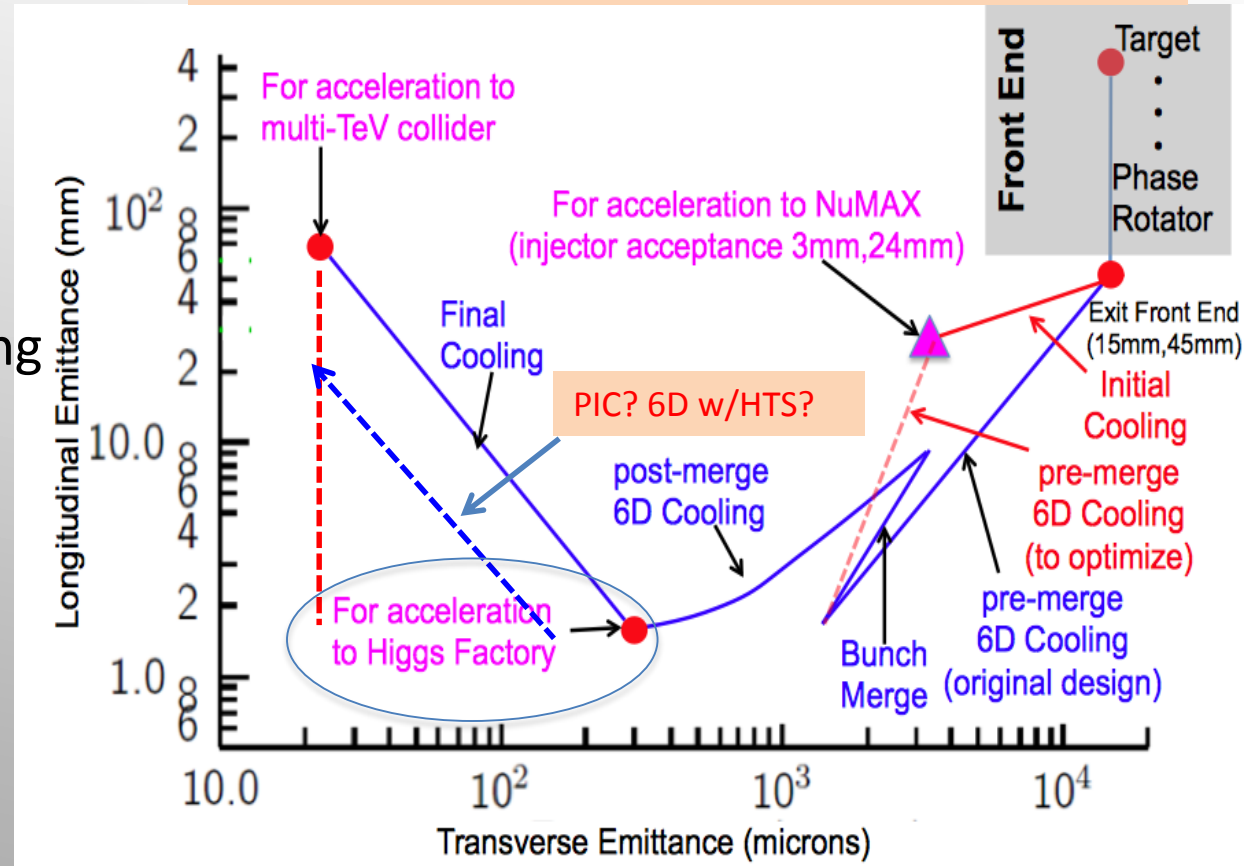
## 1. Neutrino source: 4-D cooling



## 2. Muon collider: 6-D cooling



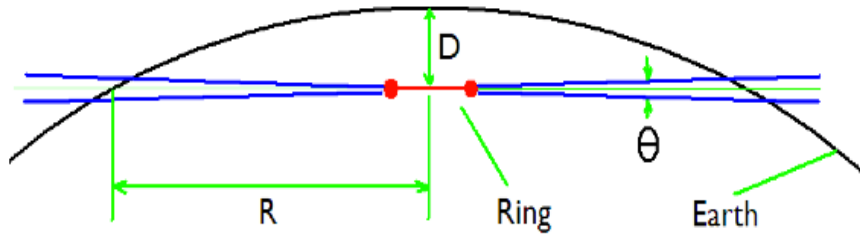
## Emittance evolution in a cooling channel



Emittance exchange:

exploits "dispersion":  $x(s) = D(s) * \Delta p/p$

# Neutrino Radiation Problem Inspires New Source



Bruce King, 2000

$$\text{Radiation} \propto \frac{E_\mu I_\mu \sigma_\nu}{\theta R^2} \propto \frac{P_{\text{beam}} \sigma_\nu}{\theta R^2}$$

Since

$$\mathcal{L} \propto B_{\text{ring}} P_{\text{beam}} \Delta\nu \frac{1}{\beta^*}$$

And we need

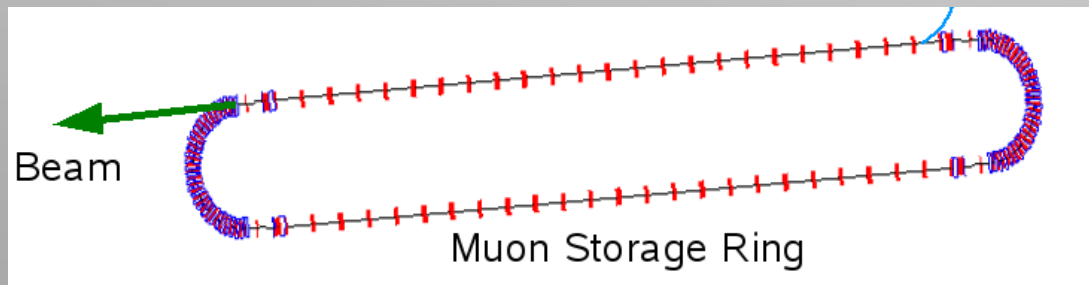
$$\mathcal{L} \propto E^2$$

$$\text{Radiation} \propto \left( \frac{\beta^*}{\Delta\nu B_{\text{ring}}} \right) \frac{\gamma^4}{D}$$

- Little problem at 1.5 TeV
- Required depth of order 200 m for 3 TeV  
and straight sections must be minimized or aimed at owned locations

Since muons live 100 times longer than charged pions, to be efficient a linear muon decay channel would have to be tens of km long, hence:

## Neutrino Factory



# “Heavy Electron” Accelerators

## Advantages

- Larger couplings to Higgs-like particles - possible low energy Higgs Factory, Z'
- Narrower energy spread – precision measurements
- Easier acceleration
- Smaller machine footprints

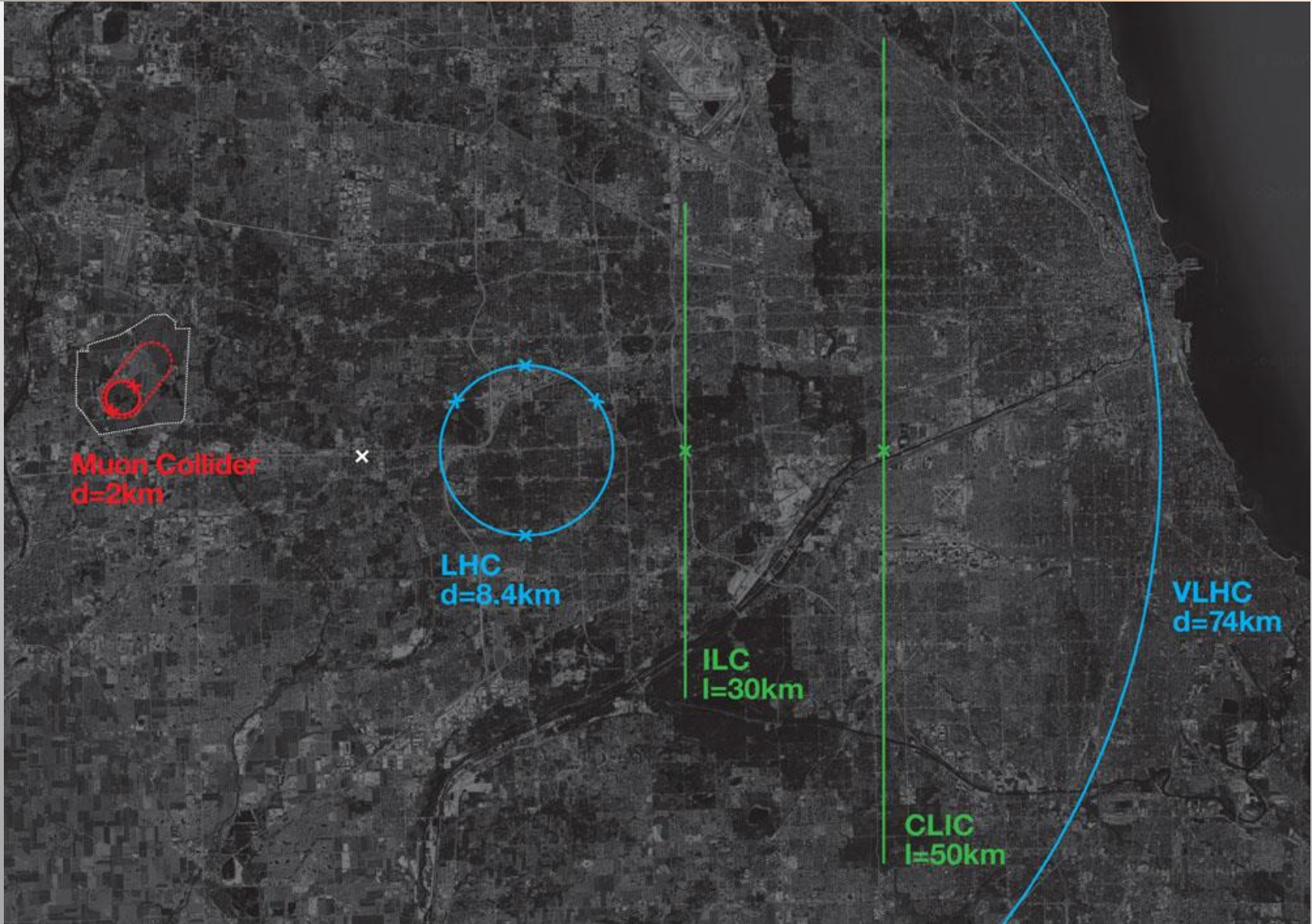
## Challenges

No show-stoppers...

- Production is into diffuse phase space
  - Tertiary beam:  $p \rightarrow \pi \rightarrow \mu \nu$
  - Need to capture and focus quickly
  - Ion. cooling necessary – but now a **developing technology**
- Have very short lifetimes:  $\mu \rightarrow e \nu_e \nu_\mu$ 
  - Acceleration must be rapid
  - Backgrounds from decays
  - Concern over neutrino radiation (**mitigated by extreme cooling, flat and or undulating beams...**)

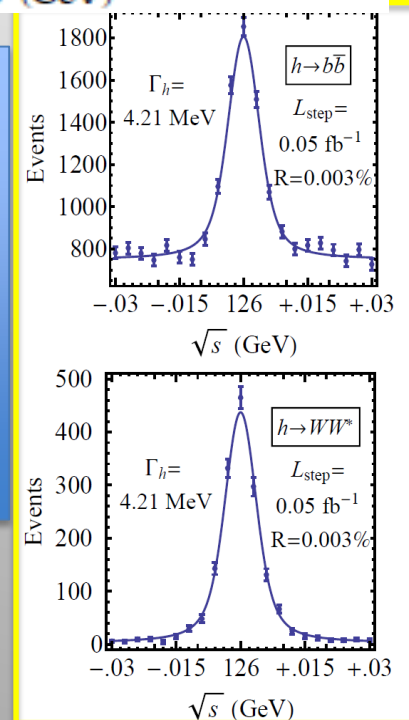
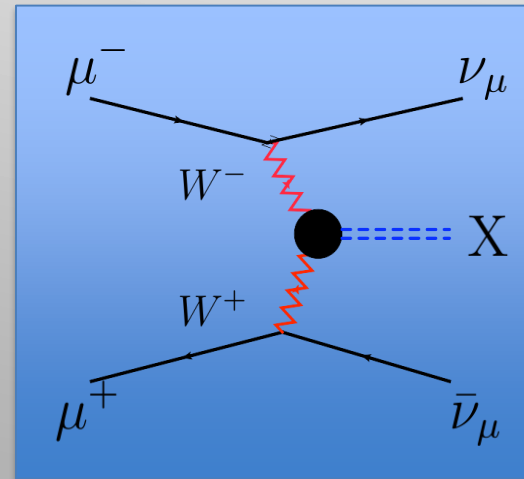
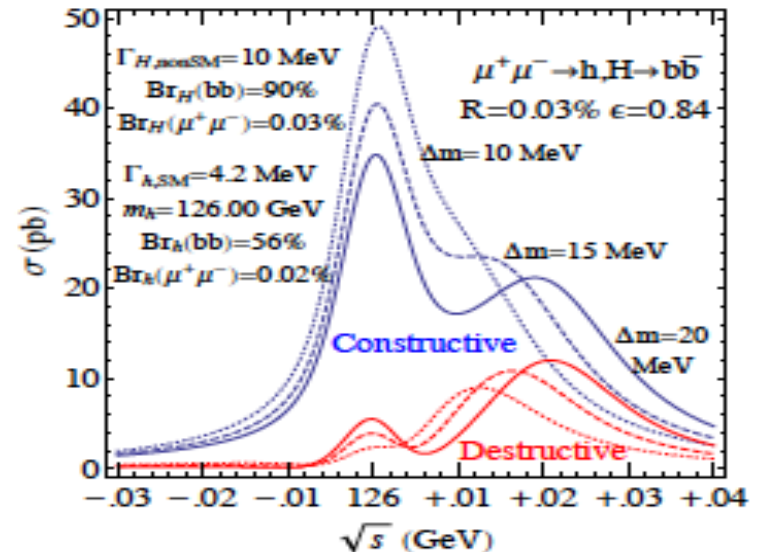


# Muon (heavy electron) Colliders are compact



# Features of the “Heavy Electron” Collider

- Superb Energy Resolution
  - SM Thresholds and s-channel Higgs Factory operation
- Multi-TeV Capability ( $\leq 10\text{TeV}$ ):
  - Compact & energy efficient machine
  - Luminosity  $> 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
  - Option for 2 detectors in the ring
- For  $\sqrt{s} > 1 \text{ TeV}$ : Fusion processes dominate
  - an Electroweak Boson Collider
  - a discovery machine complementary to a very high energy pp collider
  - 5TeV: Higgs self-coupling resolution  $< 10\%$



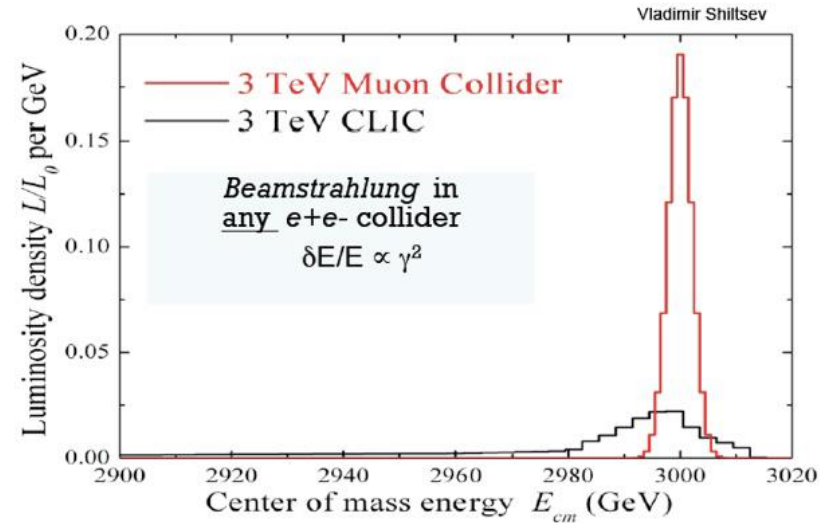
A 10 TeV  $\mu^+\mu^-$  collider has similar discovery reach as a 100 TeV pp machine!



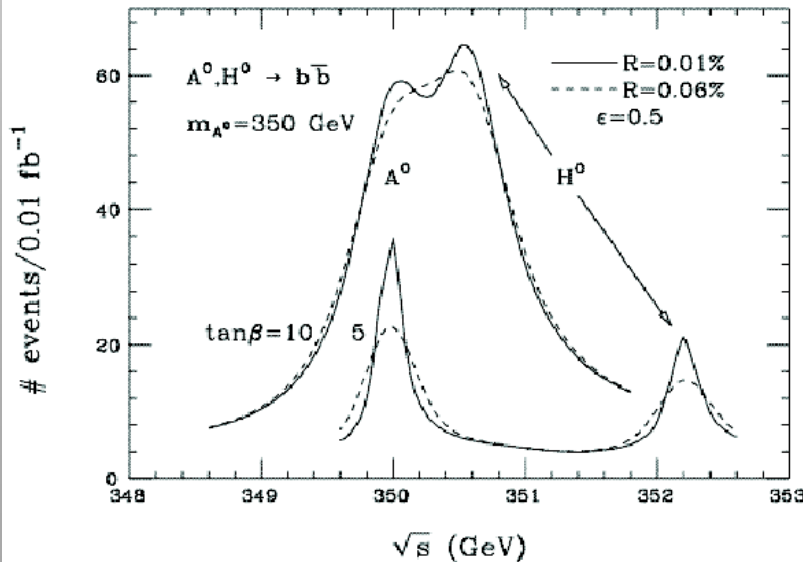
# Heavy vs. Light Lepton Physics Capability

## Superb Energy Resolution

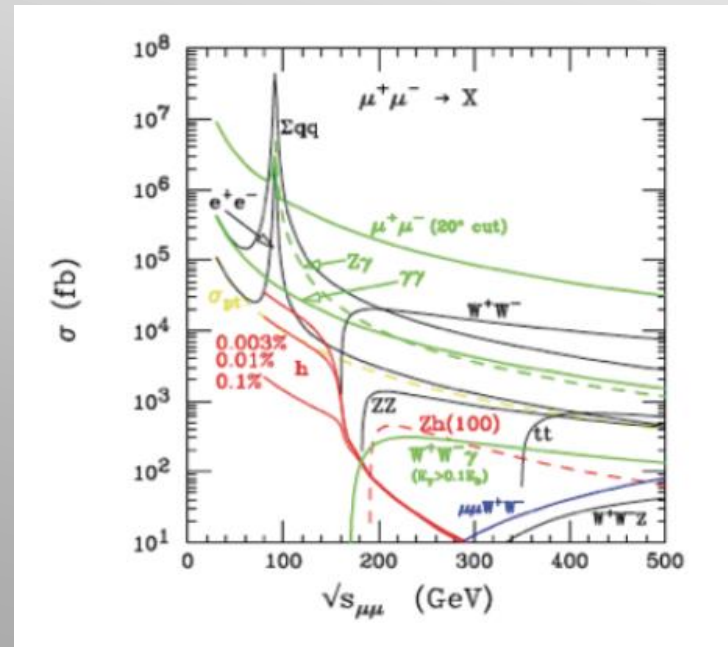
- MC: 95% luminosity in  $dE/E \sim 0.1\%$
- CLIC: 35% luminosity in  $dE/E \sim 1\%$



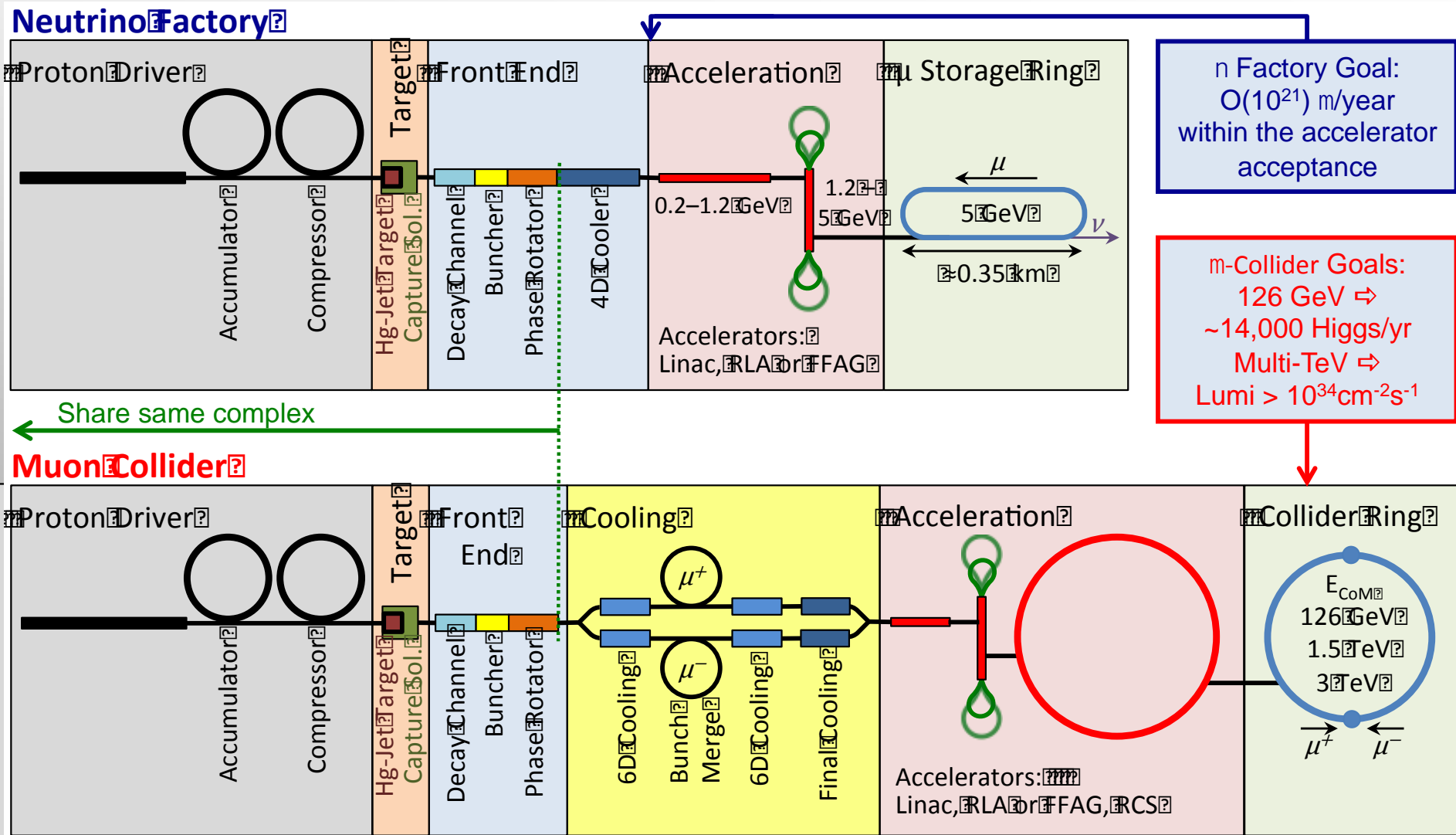
## Separation of $A^0$ & $H^0$ by Scanning



Gunion and Berger, 2000



# Muon Collider Functional Layout



Shared front ends - means a staged approach possible

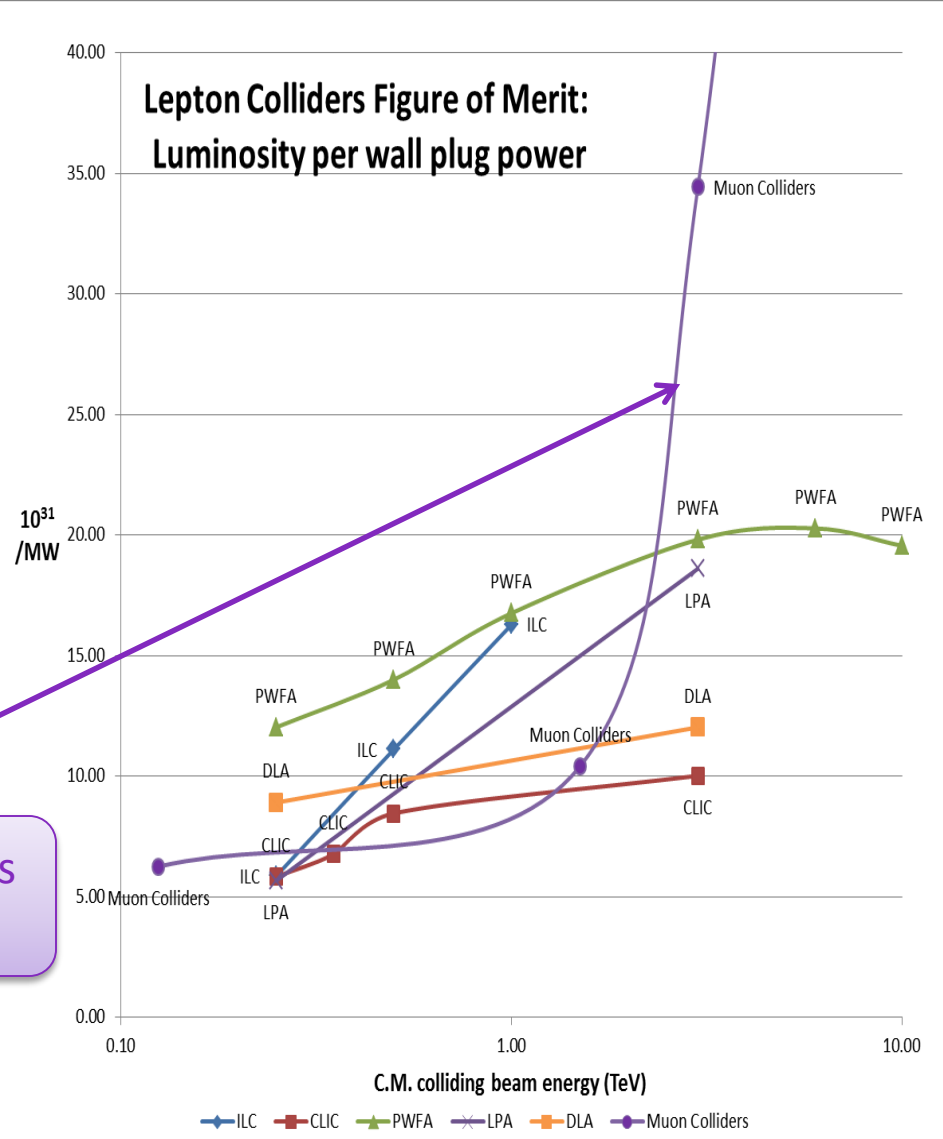
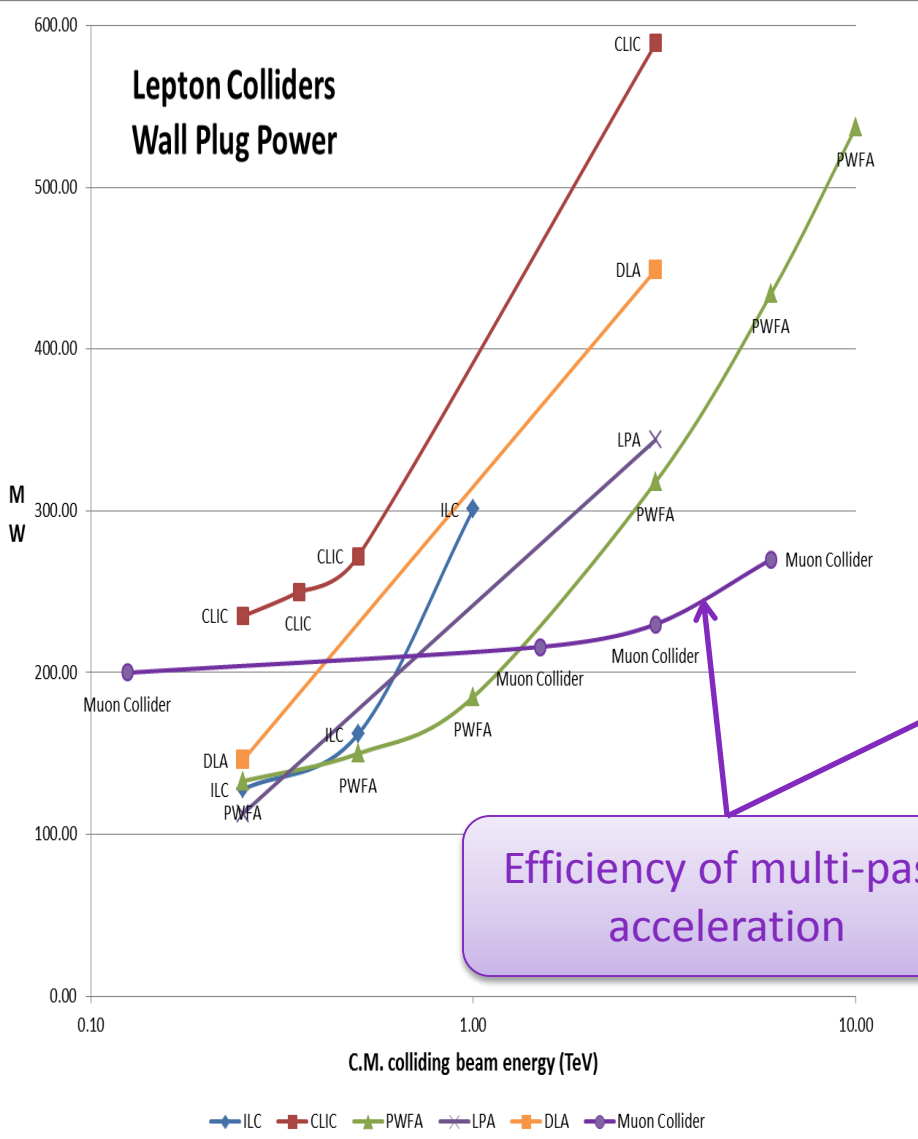
# Lepton (Muon) Collider Parameters

Parameter	Units	Higgs	Multi-TeV		
		Production Operation			Accounts for Site Radiation Mitigation
CoM Energy	TeV	<b>0.126</b>	<b>1.5</b>	<b>3.0</b>	<b>6.0</b>
Avg. Luminosity	$10^{34} \text{ cm}^{-2} \text{ s}^{-1}$	0.008	1.25	4.4	12
Beam Energy Spread	%	<b>0.004</b>	0.1	0.1	0.1
Higgs Production/ $10^7$ sec		13,500	37,500	200,000	820,000
Circumference	km	0.3	2.5	4.5	6
No. of IPs		1	2	2	2
Repetition Rate	Hz	15	15	12	6
$b^*$	cm	1.7	1 (0.5-2)	0.5 (0.3-3)	0.25
No. muons/bunch	$10^{12}$	4	2	2	2
Norm. Trans. Emittance, $\epsilon_{TN}$	$\mu \text{ mm-rad}$	0.2	0.025	0.025	0.025
Norm. Long. Emittance, $\epsilon_{LN}$	$\mu \text{ mm-rad}$	1.5	70	70	70
Bunch Length, $\sigma_s$	cm	6.3	1	0.5	0.2
Proton Driver Power	MW	4	4	4	<b>1.6</b>
Wall Plug Power	MW	<b>200</b>	<b>216</b>	<b>230</b>	<b>270</b>

Exquisite Energy Resolution  
Allows Direct Measurement  
of Higgs Width

Success of advanced cooling  
concepts  $\Rightarrow$  several  $\ll 10^{32}$

# Lepton Colliders – Efficiency at Multi-TeV Scale



# New Ideas from Muons, Inc.



Private company funded primarily through DOE SBIR/STTR program  
Rolland Johnson, founder and president

- 1. The idea of a gaseous energy absorber enables new technology to generate high accelerating gradients for muons by using the high pressure region of the Paschen curve: High Pressure RF Cavity (HPRF) **TESTED!****
- 2. Concept of a cooling channel filled with continuous homogenous absorber to provide longitudinal cooling by exploiting the path length correlation with momentum in a magnetic channel with positive dispersion: Helical Cooling Channel (HCC). **COMPLETE END-END SIMULATION.****
- 3. Parametric Resonance Ionization Cooling (PIC) concepts are being developed that can decrease emittance by factor of 10 beyond the “equilibrium emittance” of current cooling techniques. **STILL DEVELOPING****





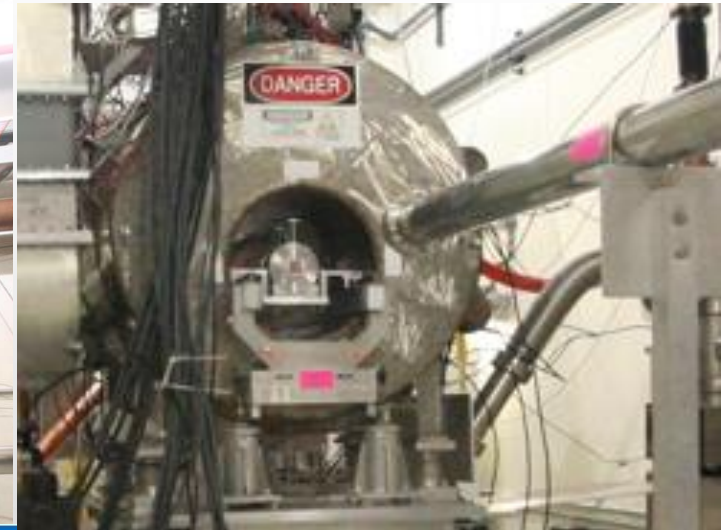
# Mucool Test Area (MTA)

MTA Hall

201 MHz cavity

SC magnet

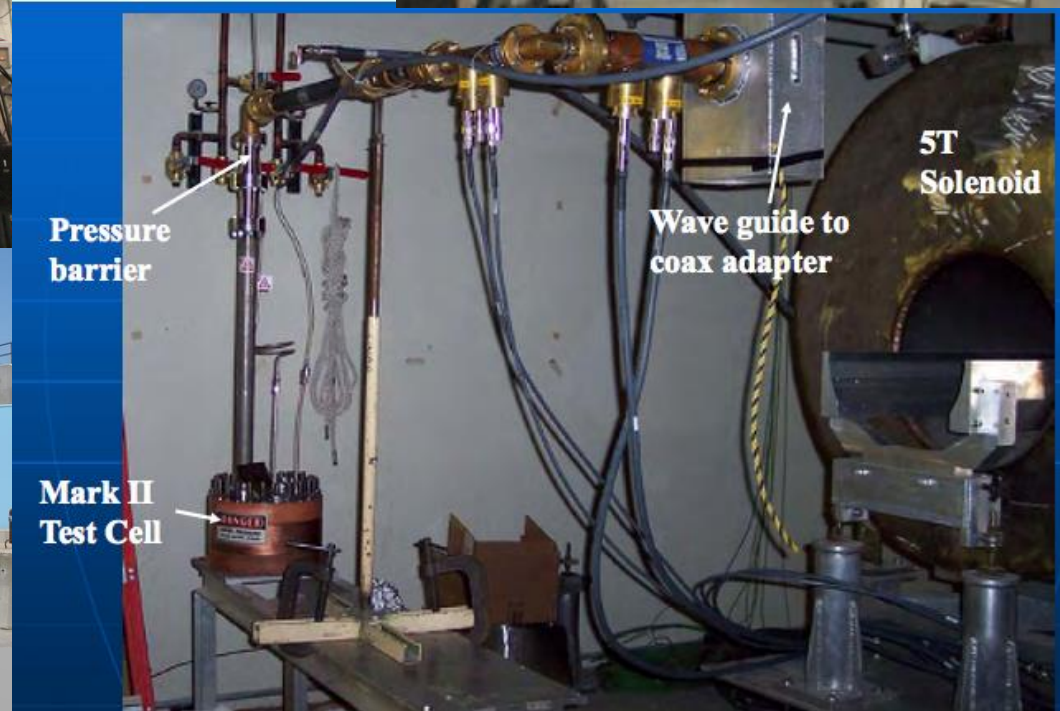
400 MeV H<sup>-</sup> beam



Entrance of MTA exp. hall



Compressor + refrigerator room



Pressure barrier

Wave guide to coax adapter

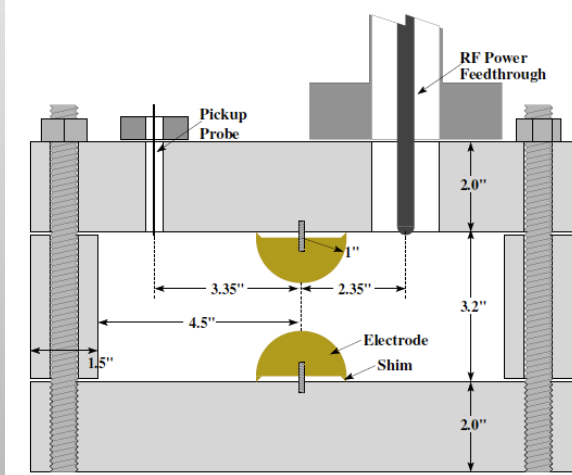
5T Solenoid

Mark II Test Cell



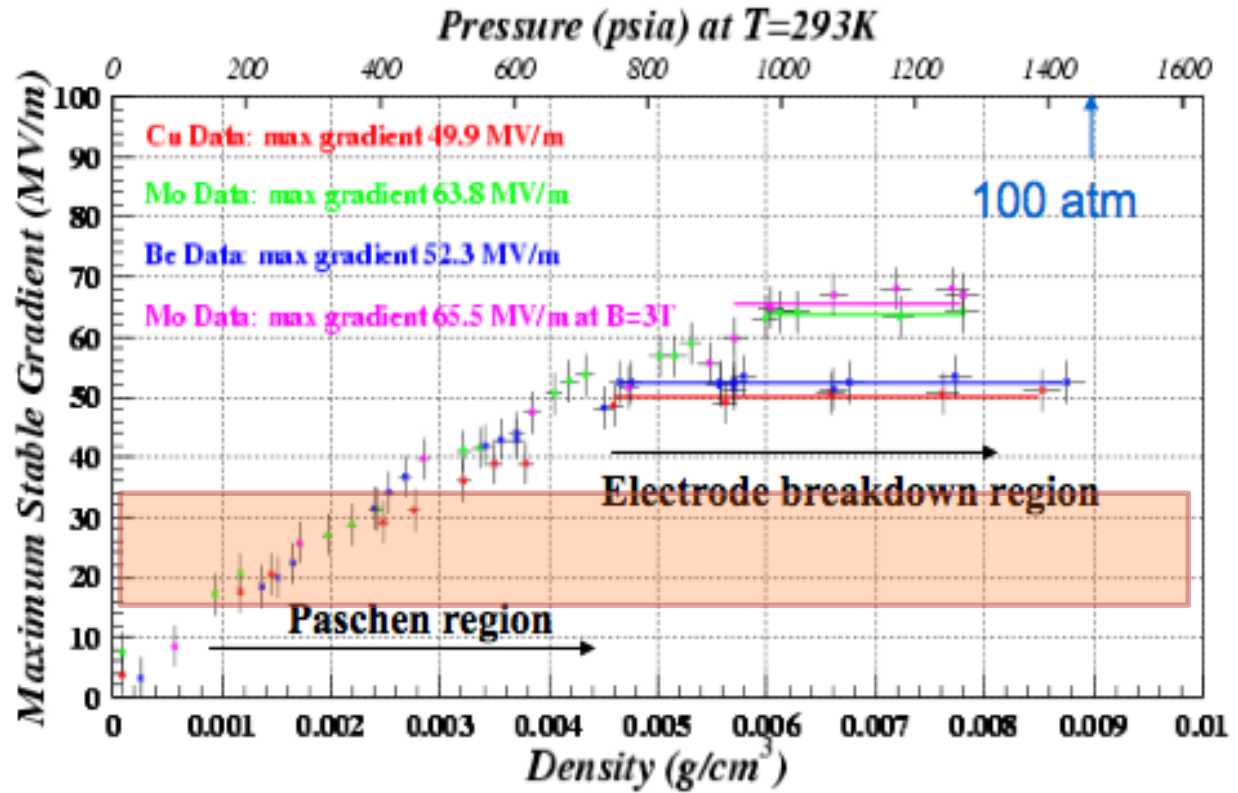
# High Pressure RF Test Cell

Can moderate dark current and breakdown currents in magnetic fields



Schematic view of HPRF cavity

Paschen curve verified!



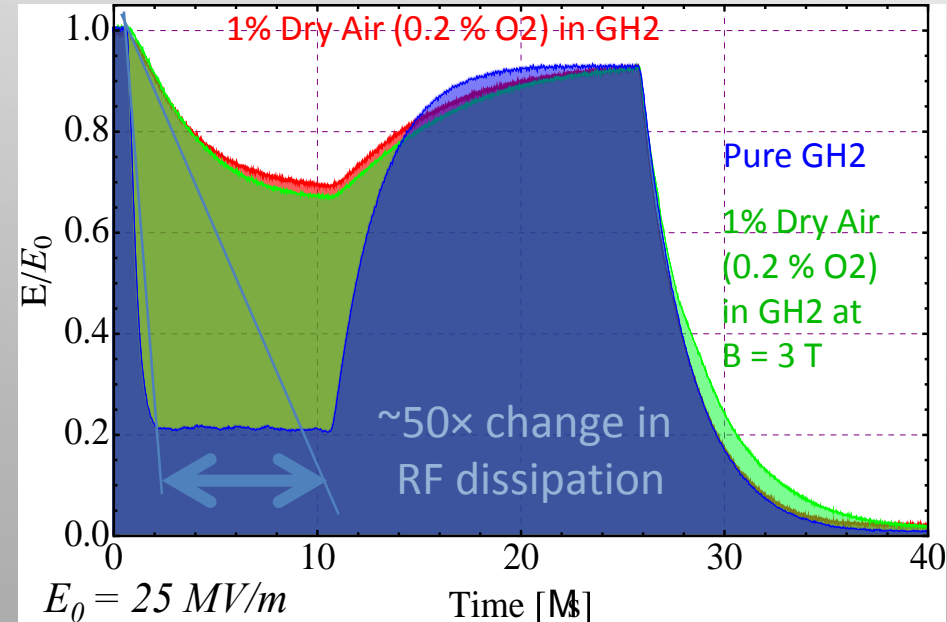
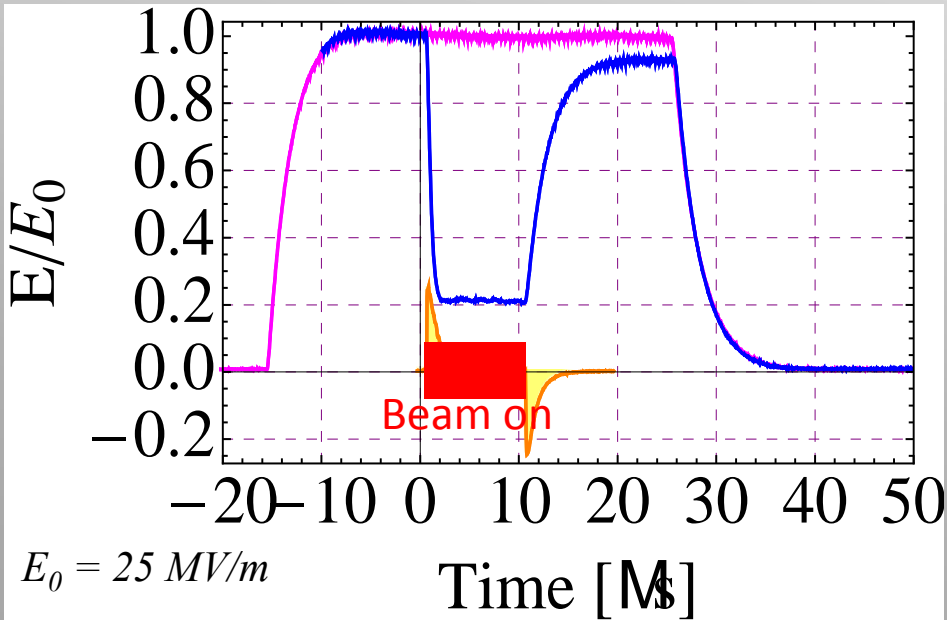
- Maximum gradient limited by breakdown of metal.
- Cu and Be have same breakdown limits (~50 MV/m), Mo(~63MV/m), W(~75MV/m).
- Results show no B dependence, much different metallic breakdown than for vacuum cavities.



# High Pressure RF with Beam

Does intense beam induce an electric breakdown? → **No!**

- Gas-filled cavity
  - Moderates dark current and breakdown currents in magnetic fields
  - Contributes to cooling
  - Is loaded, however, by beam-induced plasma
- Electronegative Species
  - Dope primary gas
  - Can moderate the loading effects of beam-induced plasma by scavenging the relatively mobile electrons





# Helical Cooling Channel Magnet

Dipole → Dipole + Solenoid (+Quad for stability)

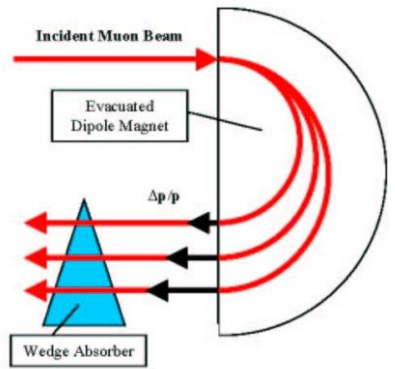


Figure 1. Use of a Wedge Absorber for Emittance Exchange

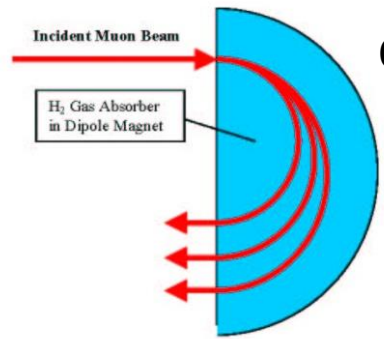


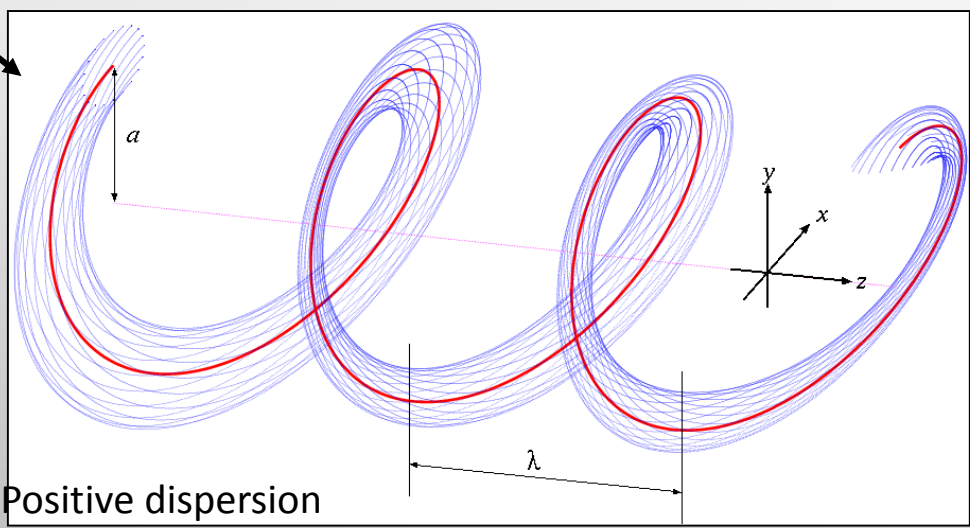
Figure 2. Use of Continuous Gaseous Absorber for Emittance Exchange

Opposing radial forces:

$$F_{h-dipole} \approx p_z \times B_{\perp}; \quad b \equiv B_{\perp}$$

$$F_{solenoid} \approx -p_{\perp} \times B_z; \quad B \equiv B_z$$

$$f_{central} = \frac{e}{m} (b_{\phi} \cdot p_z - b_z \cdot p_{\phi})$$



Positive dispersion

Red: Reference orbit

Blue: Beam envelope

Transforming to the frame of the rotating helical dipole leads to a time and z –independent Hamiltonian, can form relation:

$$p(a) = \frac{\sqrt{1 + \kappa^2}}{k} \left[ B - \frac{1 + \kappa^2}{\kappa} b \right]$$

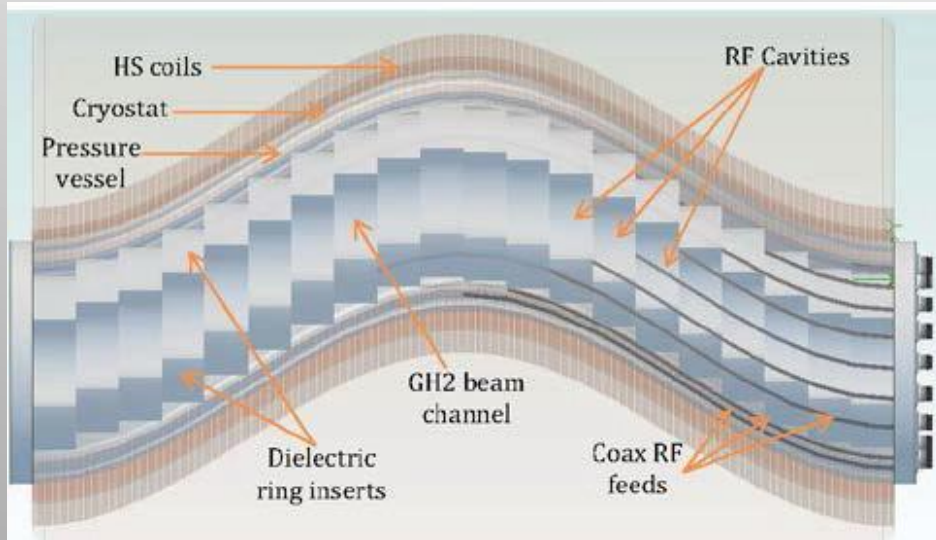
Manipulate values of parameters to change performance

Dispersive component makes longer path length for higher momentum particles and shorter path length for lower momentum particles.

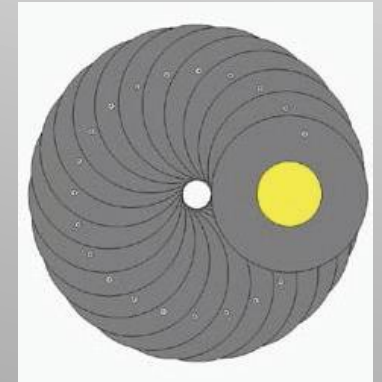
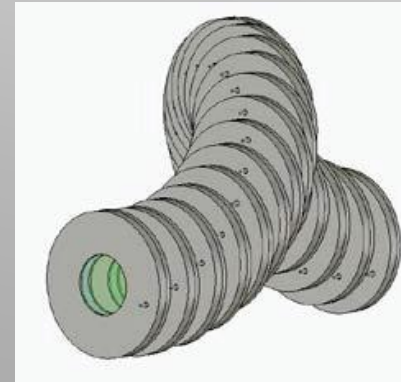
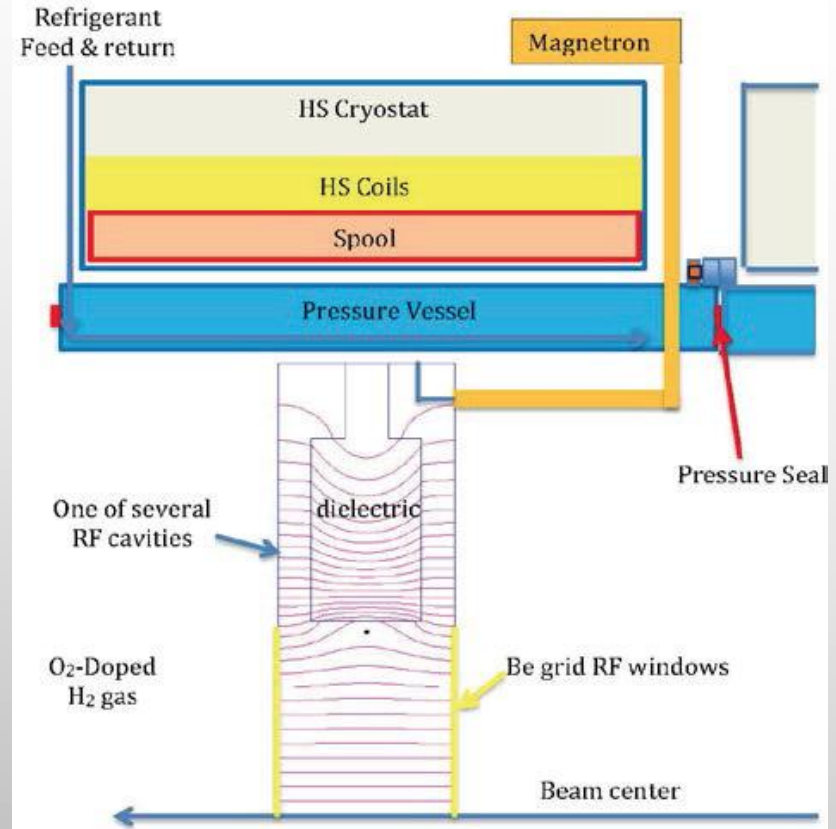
# HCC Engineering Design

## RF Cavities:

- 1 Pressurized
- 2 Dielectric Loaded
- 3 Positioned inside HS Coils
- 4 Powered by Magnetrons

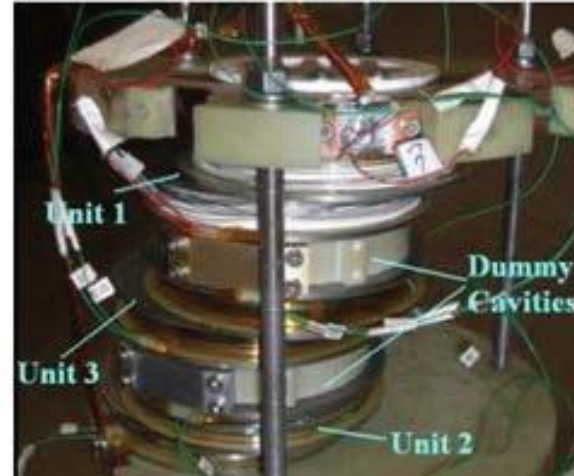
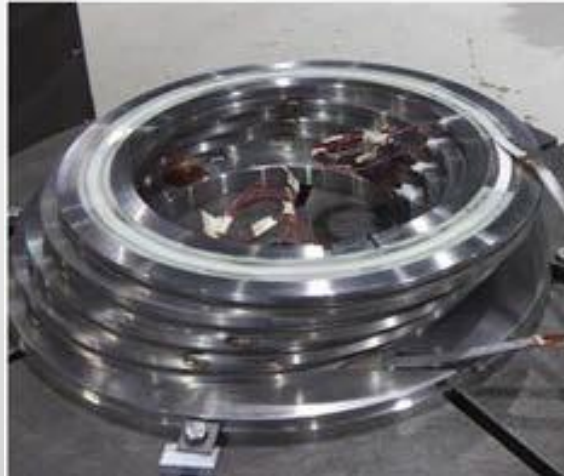


Conceptual diagram of an HCC module, showing dielectric-loaded RF cavities enclosed in a pressure vessel that “screws” into the HS cryostat. The pressure vessel contains tubes for water or LN2 refrigerant.

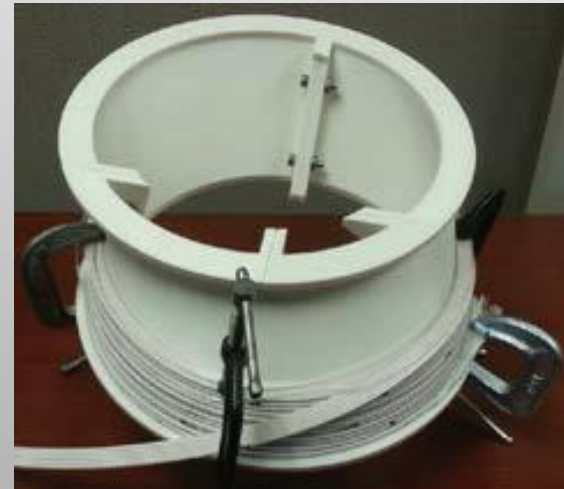
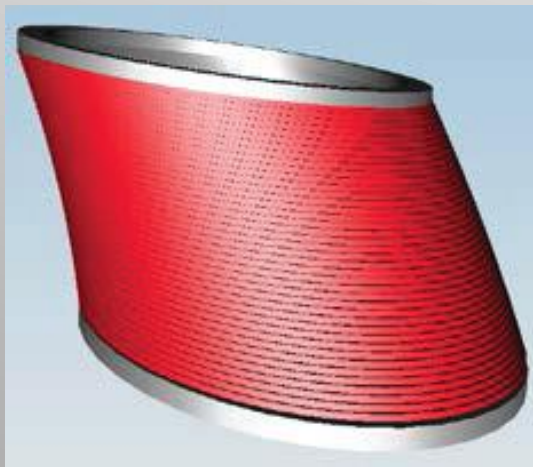




# Helical Solenoid Magnet – Muons, Inc. and Fermilab



Previous HS fabrication projects: (left) NbTi HS and (right) YBCO HS



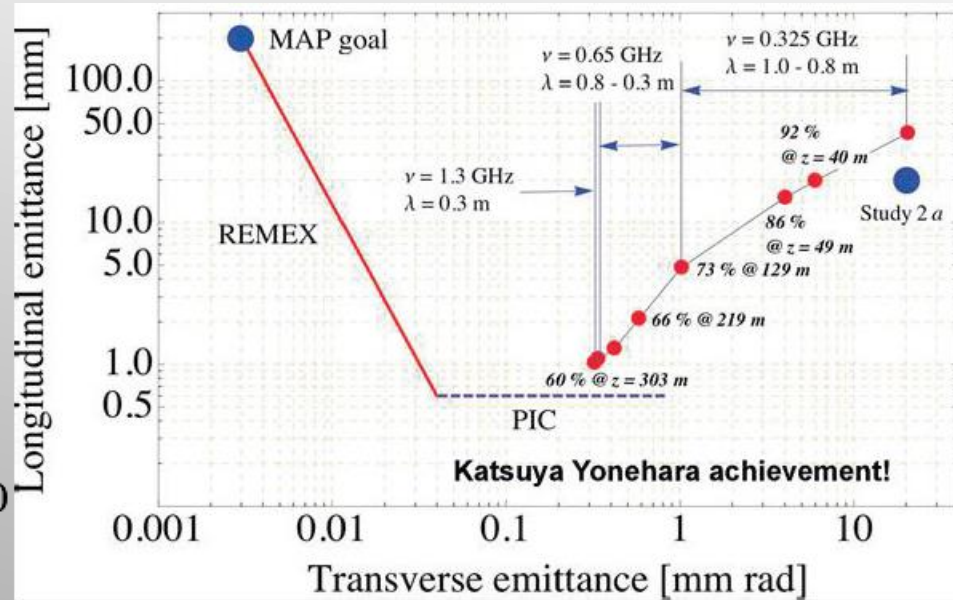
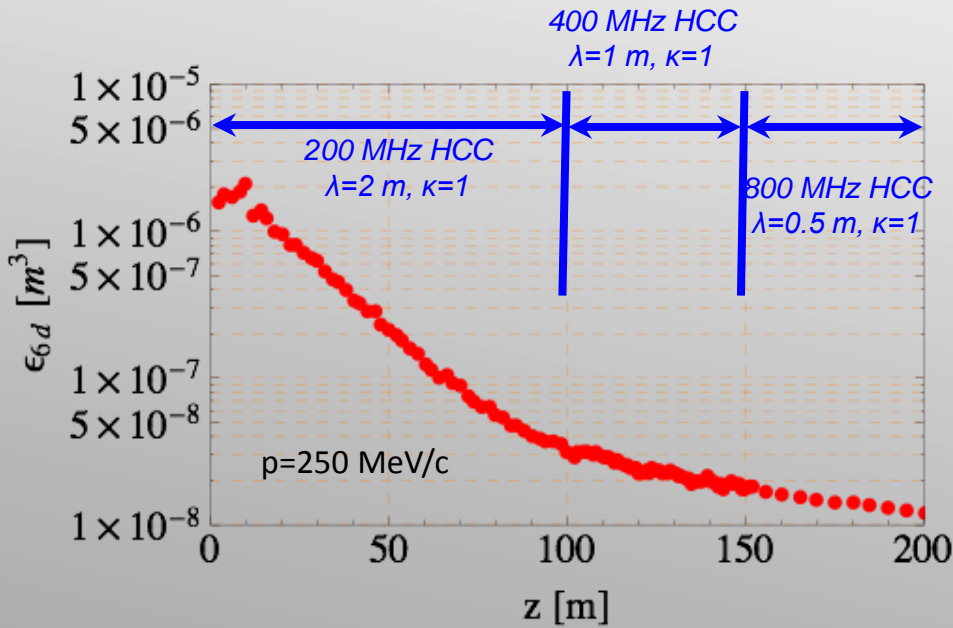
Conceptual drawing (left) and 3d printer version (right) of the Nb<sub>3</sub>Sn HS spool and conductor that will be fabricated and tested in the Fermilab Vertical Magnet Test Facility. The test will use two layers of cable.



# Simulation study of HCC for Muon Collider (MC)



Goal for low emittance MC design



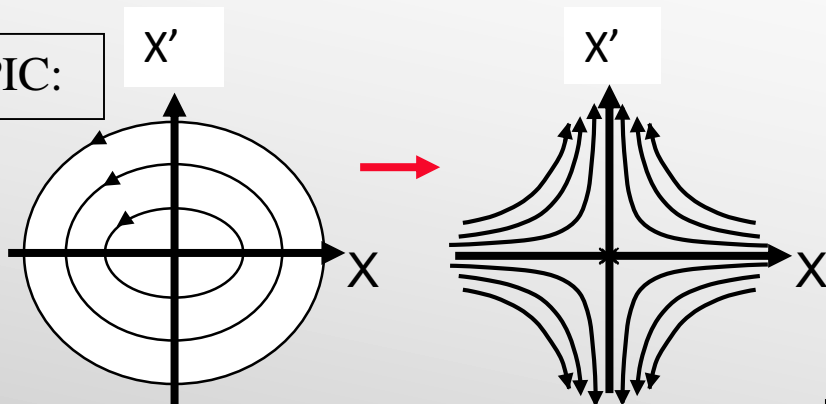
6D Phase space evolution in current HCC, by Katsuya Yonehara

Phase space evolution for Low Emittance Muon Collider (solid line: complete simulation, dashed line: in progress)



# Extreme Cooling: PIC and HCC

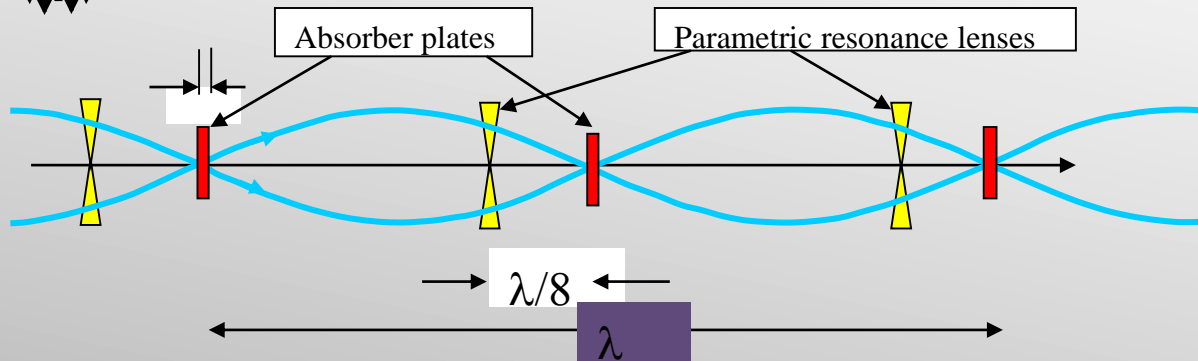
Old PIC:



$$M = \begin{pmatrix} e^{-\lambda\Lambda_d} \cos \psi & g \sin \psi \\ -\frac{1}{g} \sin \psi & e^{\lambda\Lambda_d} \cos \psi \end{pmatrix}$$

$\sin \Psi = 0$  decouples  $x$  and  $x'$

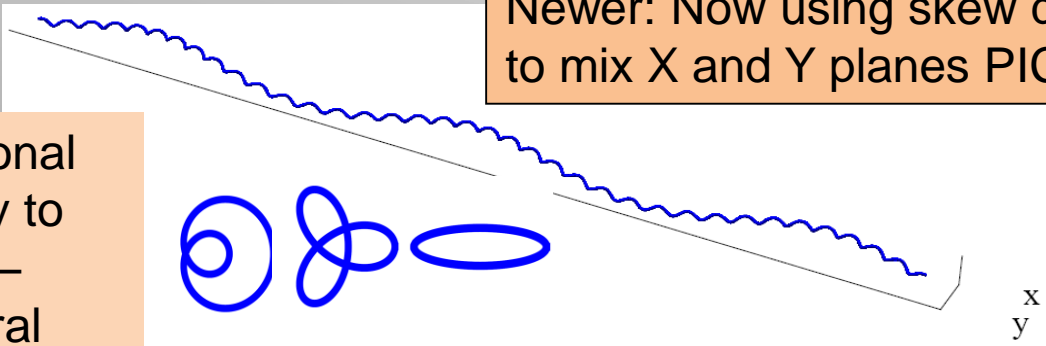
PS area is reduced in  $x$  due to the dynamics of the parametric resonance and reduced in  $x'$  by ionization cooling.



“epicycle HCC” PIC

HCC with 2 periods: an additional helical field of opposite helicity to create alternating dispersion – modified orbit from simple spiral

Newer: Now using skew quads to mix X and Y planes PIC

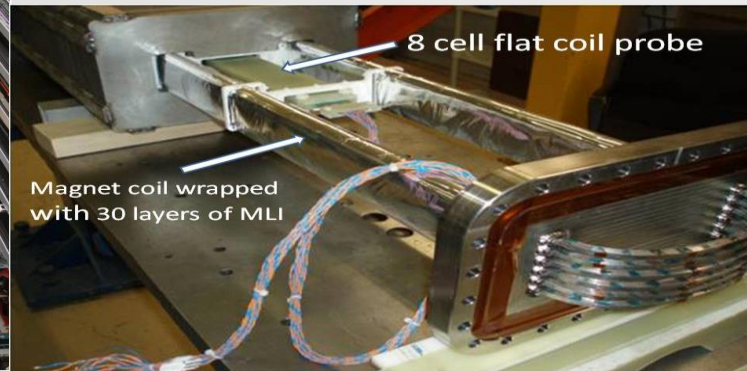
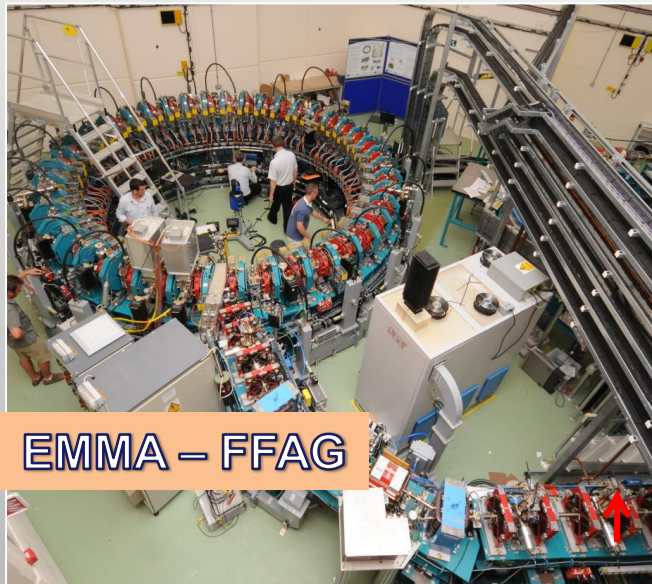




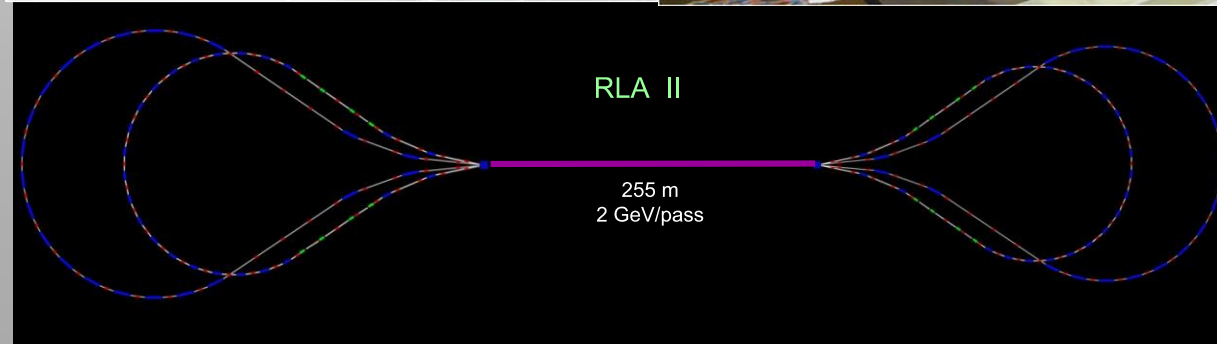
# Technology Challenges - Acceleration

- Muons require an ultrafast accelerator chain, that is just beyond “standard” machines

- Superconducting Linacs (NuMAX choice)
- Recirculating Linear Accelerators (RLAs)
- Fixed-Field Alternating-Gradient (FFAG) Rings
- Rapid Cycling Synchrotrons (RCS)



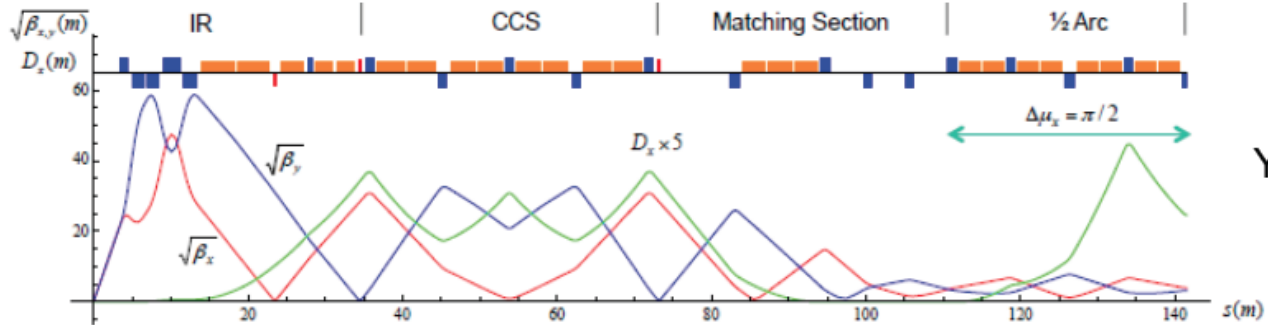
RCS requires  
2 T p-p magnets  
at  $f \geq 400$  Hz  
(U Miss, BNL &  
FNAL)



**JEMMRLA Proposal:**  
JLAB Electron Model of  
Muon RLA with Multi-pass  
Arcs

- RF power sources: Muons, inc. phase and frequency locked magnetrons can provide a cheaper, more robust alternative to klystrons

# Updated 63 x 63 GeV Lattice

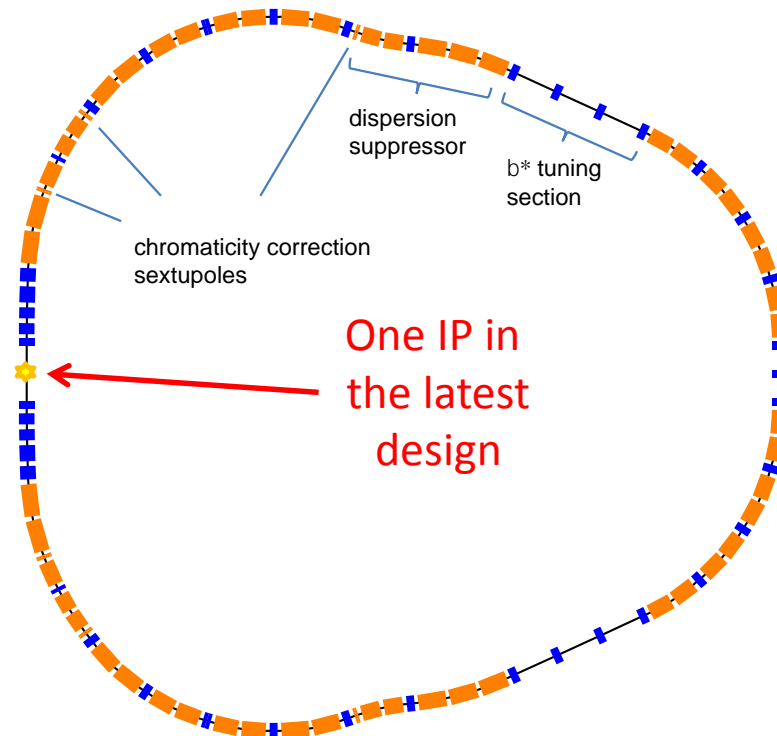


Y. Alexahin

Optics functions in half ring for  $\beta^*=2.5\text{cm}$

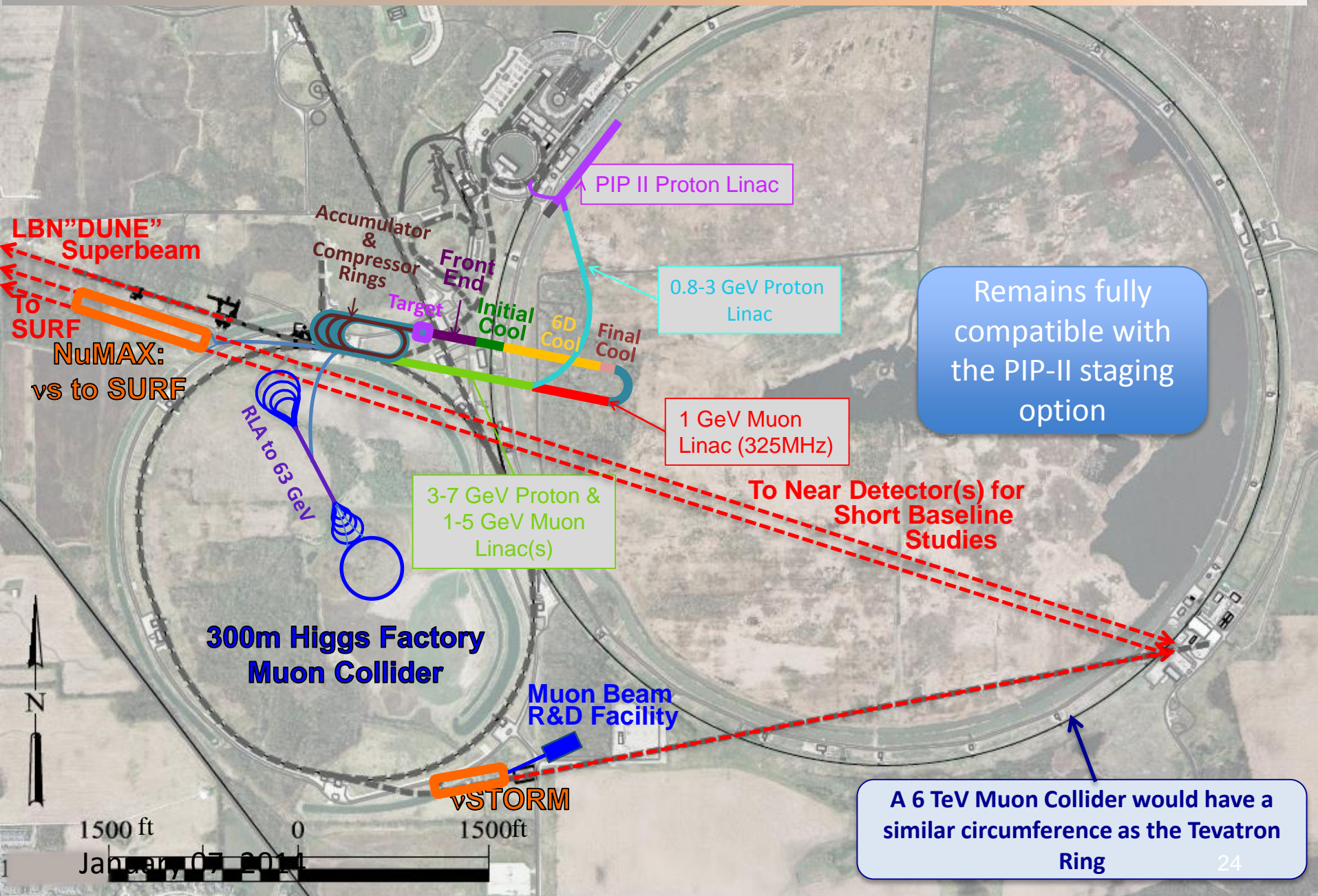
## Parameter

Beam energy	GeV	63	63
Average luminosity	$10^{31}/\text{cm}^2/\text{s}$	1.7	8.0
Collision energy spread	MeV	3	4
Circumference, C	m	300	300
Number of IPs	-	1	1
$\beta^*$	cm	3.3	1.7
Number of muons / bunch	$10^{12}$	2	4
Number of bunches / beam	-	1	1
Beam energy spread	%	0.003	0.004
Normalized emittance, $\epsilon_{\perp N}$	$\pi\text{-mm-rad}$	0.4	0.2
Longitudinal emittance, $\epsilon_{\parallel N}$	$\pi\text{-mm}$	1.0	1.5
Bunch length, $\sigma_s$	cm	5.6	6.3
Beam size at IP, r.m.s.	mm	0.15	0.075
Beam size in IR quads, r.m.s.	cm	4	4
Beam-beam parameter	-	0.005	0.02
Repetition rate	Hz	30	15
Proton driver power	MW	4	4





# Heavy Lepton Acceleration Program at Fermilab



# Parting Thoughts – Thinking Bigger



- Despite (consistent with) the current P5 priorities, a staged muon (heavy electron) acceleration program at Fermilab is a viable path to a Higgs factory and a possible energy frontier future. Starting with what we already have - planned and present.
- Cooling is a standard practice in accelerator science, ionization is settled physics and the **essential technology** for ionization cooling has now been proven **viable**. Necessary accelerator and magnetic field gradients have already been demonstrated.
- Some elements of these future machines will be built in the current “future” LBN(E,F,DUNE) neutrino program. A muon storage ring source of neutrinos could be a viable upgrade. Consistent with the “megascience”, international character of our aspirations at Fermilab.
- In particular, Muons, Inc. cooling and other accelerator technologies are making bright muon beams (and beams of any flavor) more **affordable** and **viable**.
- Great synergies with the Fermilab Program: Before the ultimate energy frontier machine, it offers possible upgrades to both current muon and neutrino programs. Staged implementation with **accruing** savings.



# Some Important Relationships

Hamiltonian Solution  $p(a) = \frac{\sqrt{1+\kappa^2}}{k} \left[ B - \frac{1+\kappa^2}{\kappa} b \right]$   $k = 2\pi/\lambda$   $\kappa = ka$

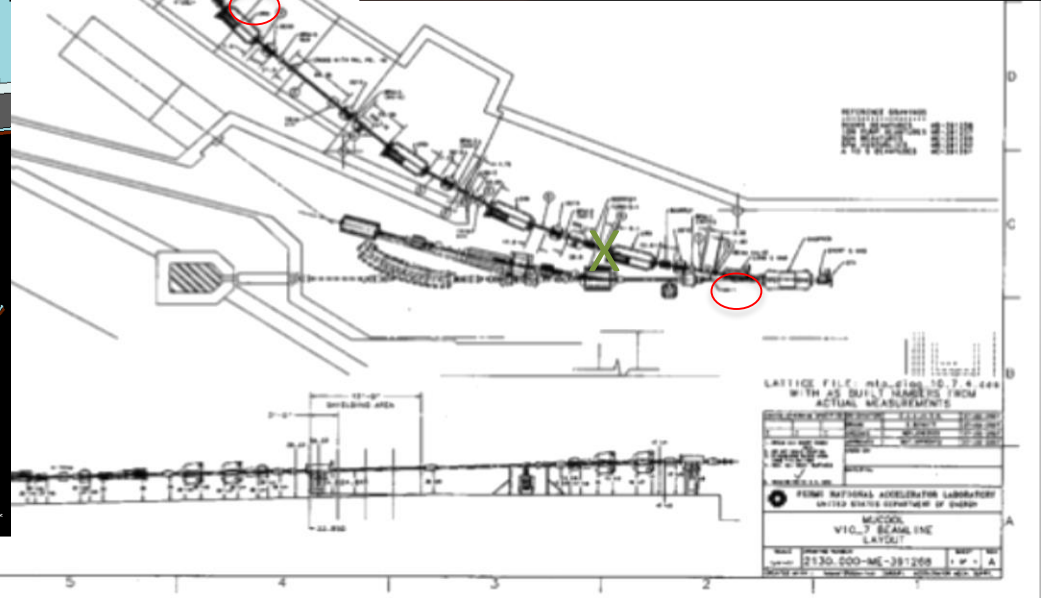
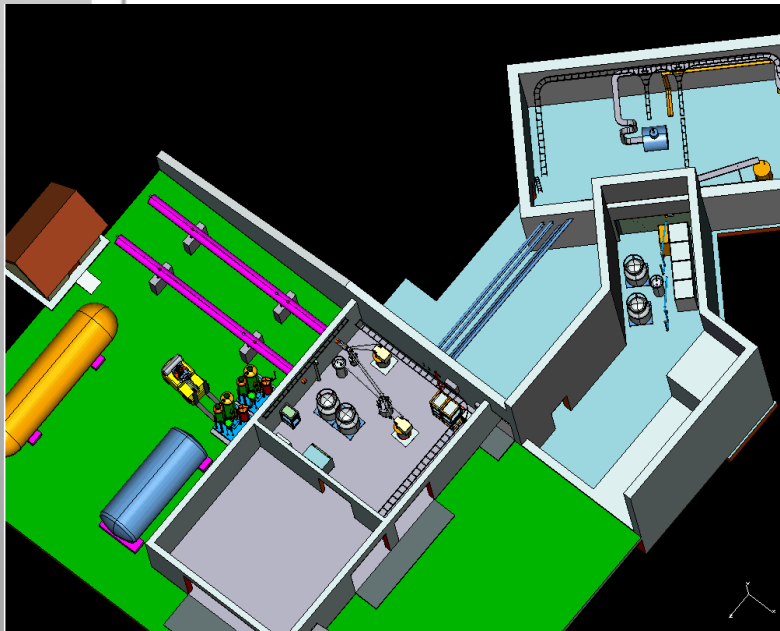
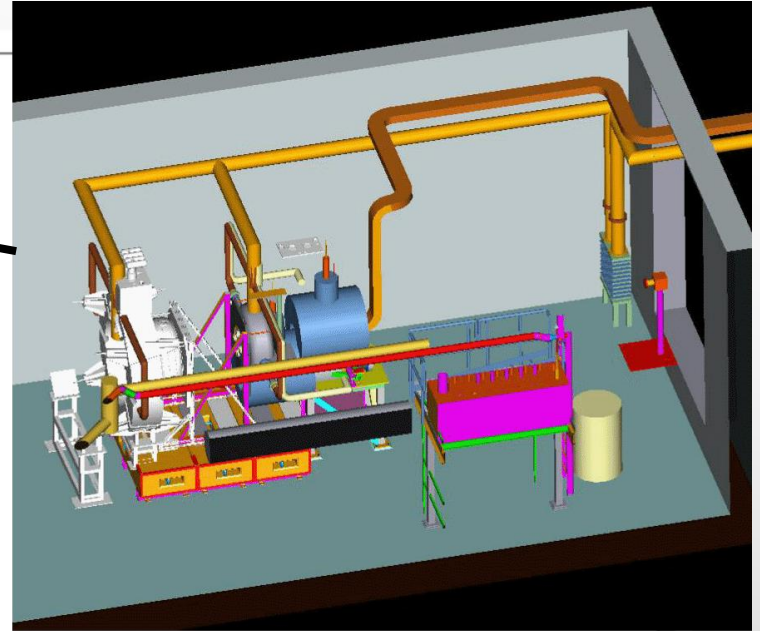
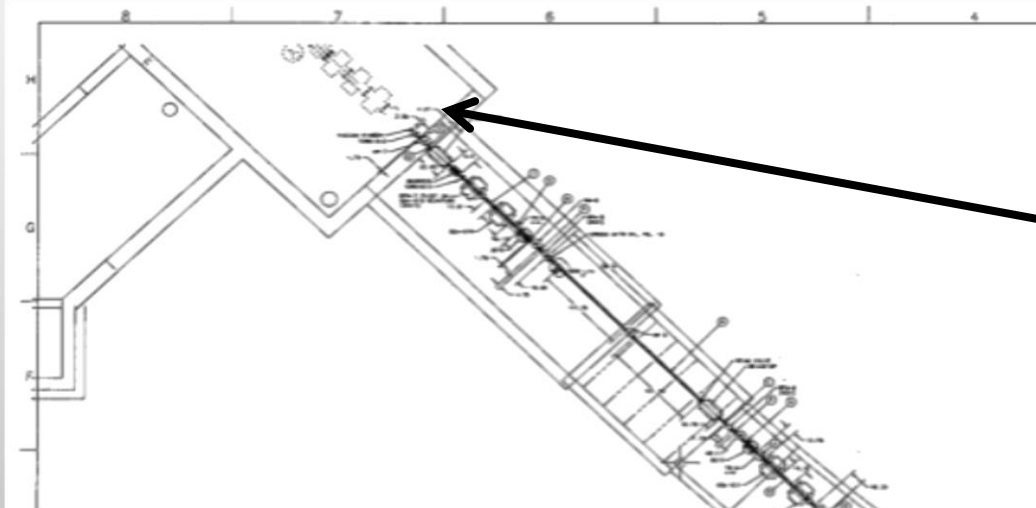
Equal cooling decrements  $q \equiv \frac{k_c}{k} - 1 = \beta \sqrt{\frac{1+\kappa^2}{3-\beta^2}}$   $k_c = B\sqrt{1+\kappa^2}/p$

Longitudinal cooling only  $\hat{D} \equiv \frac{p}{a} \frac{da}{dp} = 2 \frac{1+\kappa^2}{\kappa^2}$   $q = 0$

~Momentum slip factor  $\eta = \frac{d}{d\gamma} \frac{\sqrt{1+\kappa^2}}{\beta} = \frac{\sqrt{1+\kappa^2}}{\gamma\beta^3} \left( \frac{\kappa^2}{1+\kappa^2} \hat{D} - \frac{1}{\gamma^2} \right)$   $\frac{\kappa^2}{1+\kappa^2} \hat{D} \sim \frac{1}{\gamma_{transition}^2}$

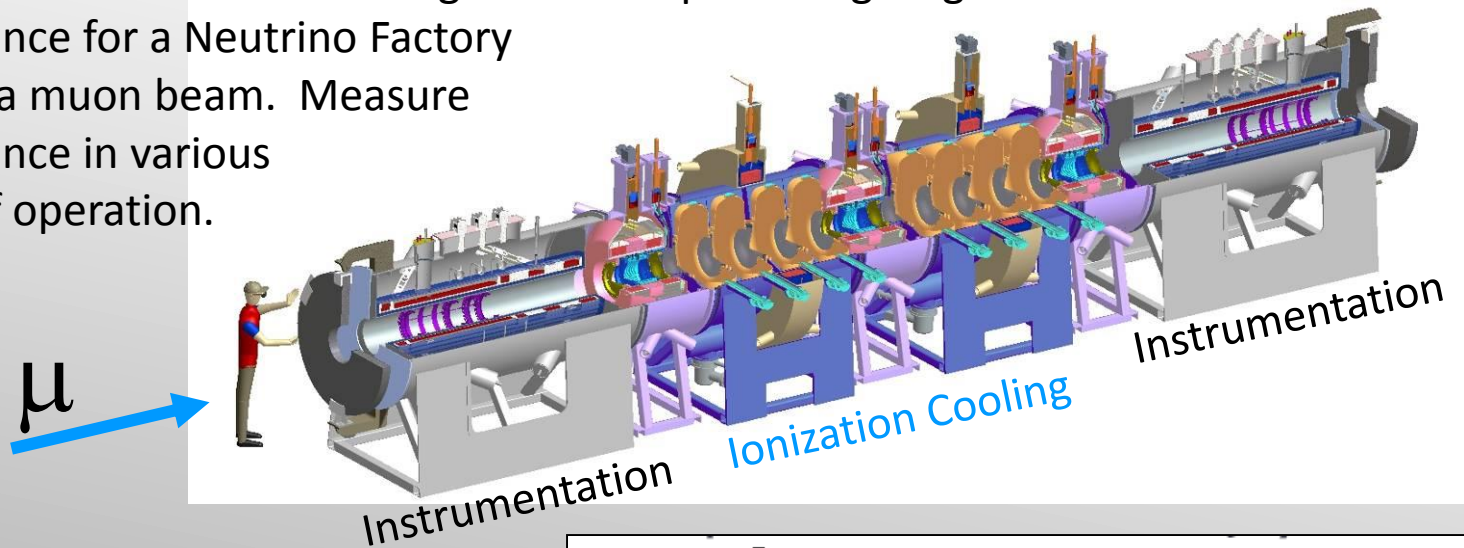


# MTA Beamline



# Ionization Cooling Experiment: MICE

GOALS: Build a section of cooling channel capable of giving the desired performance for a Neutrino Factory & test in a muon beam. Measure performance in various modes of operation.



- Multi-stage experiment.
- First stage being commissioned now.
- Anticipate final stage complete by ~2015

