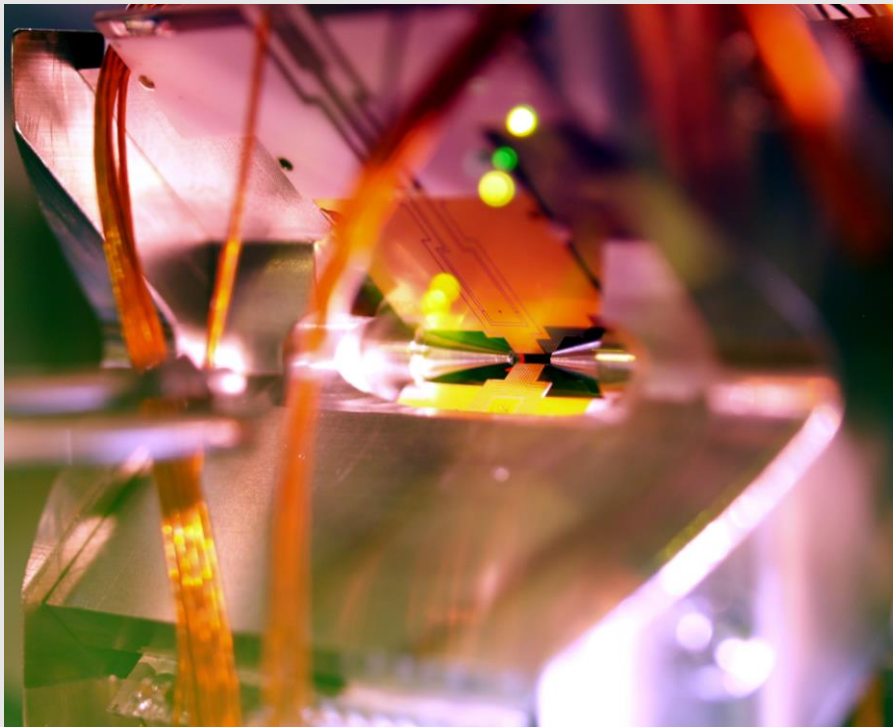


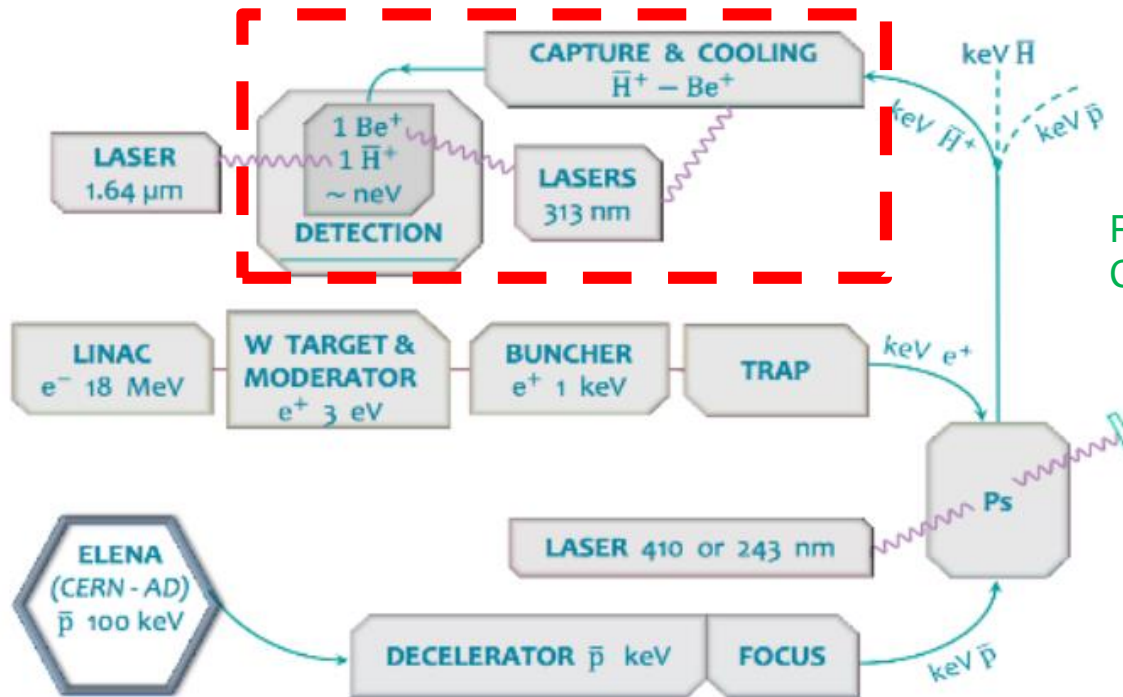
Techniques for Ground state cooling of anti-Hydrogen-ions



- Principle of GBAR experiment
- Sympathetic ground state cooling
- New trap production procedure
- Challenges of wavepacket expansion
- Temperature measurement via Young interferences
- Requirements and planing for the cryo trap

Sebastian Wolf, Andreas Koglbauer and Ferdinand Schmidt-Kaler, Johannes Gutenberg-University Mainz

GBAR experimental scheme



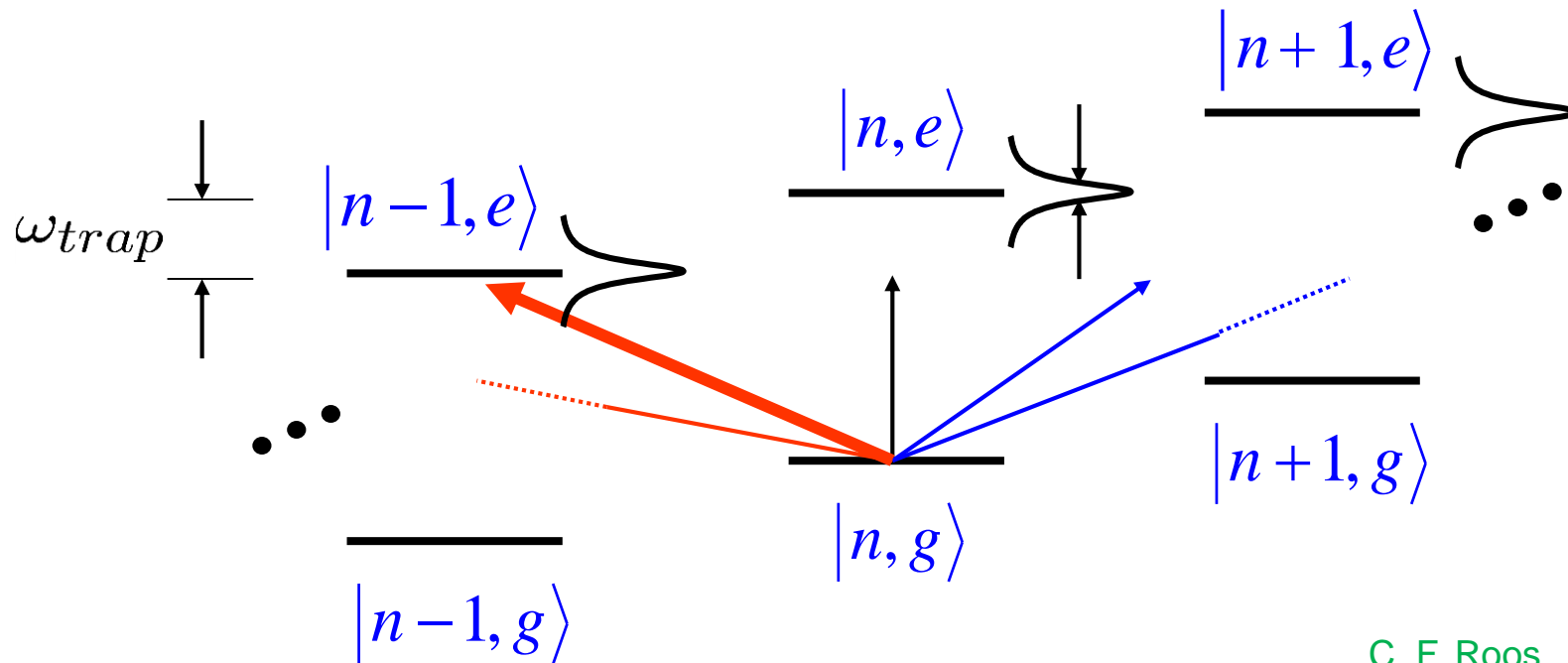
P. Perez and Y. Sacquin,
Class. Quantum Grav. **29**, 184008 (2012)

Doppler cooled ions $T \sim 1\text{mK}$
Rising height $h \sim 5\text{m}$

→ Ground State cooling
→ ($T \sim 10\ \mu\text{K}$, $h \sim 10\text{cm}$)

„Strong confinement“

$$\omega_{trap} \gg \gamma$$



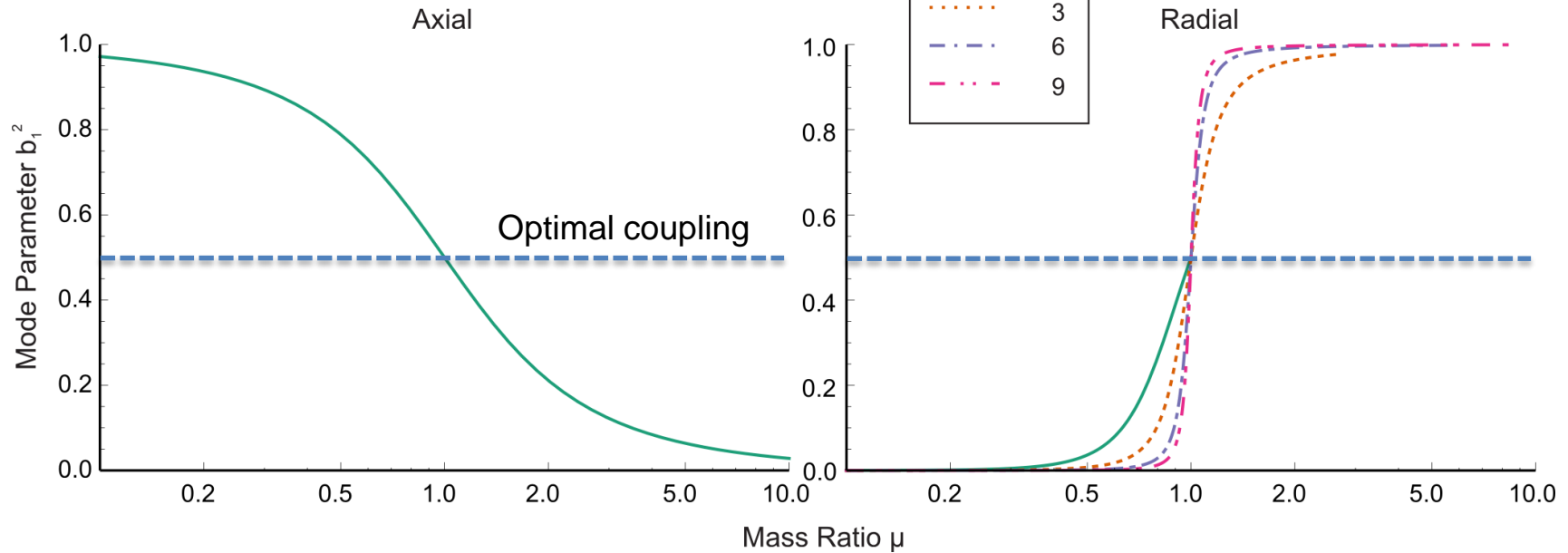
C. F. Roos,
Phys. Rev. Lett. **85**, 5547 (2000)

strong confinement – well resolved sidebands:
Selective excitation of a single sideband only,
e.g. here the red SB

Problem in high mass ratio

$$\varepsilon \sim \omega_{\text{rad}} / \omega_{\text{ax}}$$

J. Wübbena et al.,
PRA 85,043412 (2012)



Be:H = 9:1
Ca:Be = 4.4:1



COM (ax)



Stretch (ax)



Rocking (rad)

Increased coupling near ZigZag transitions



$$\alpha = \left(\frac{\omega_{ax}}{\omega_{rad}} \right)^2$$
$$\alpha_{krit} \approx 0.47$$

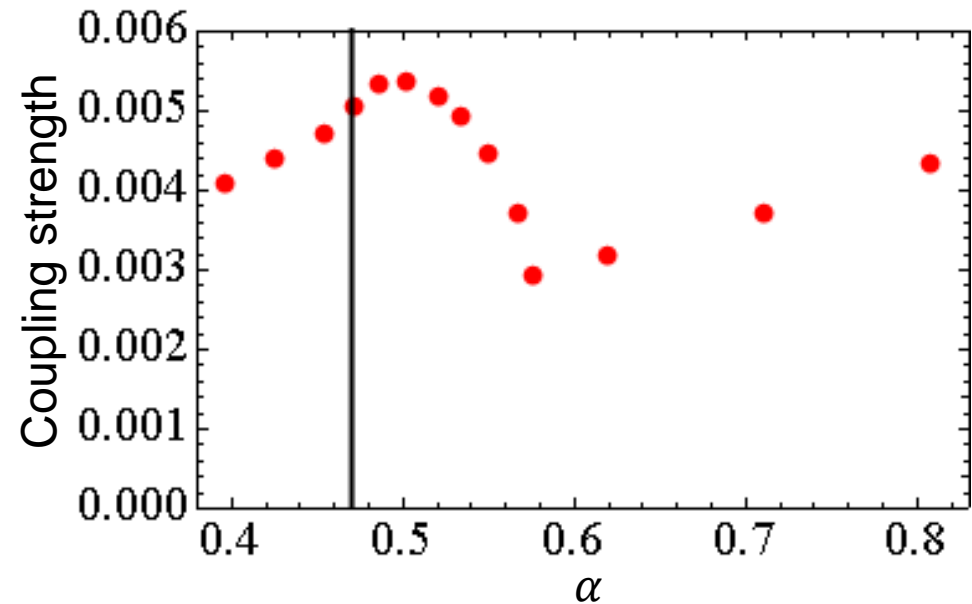
Calculation of oscillation modes and frequencies
equilibrium positions

oscillation modes and frequencies

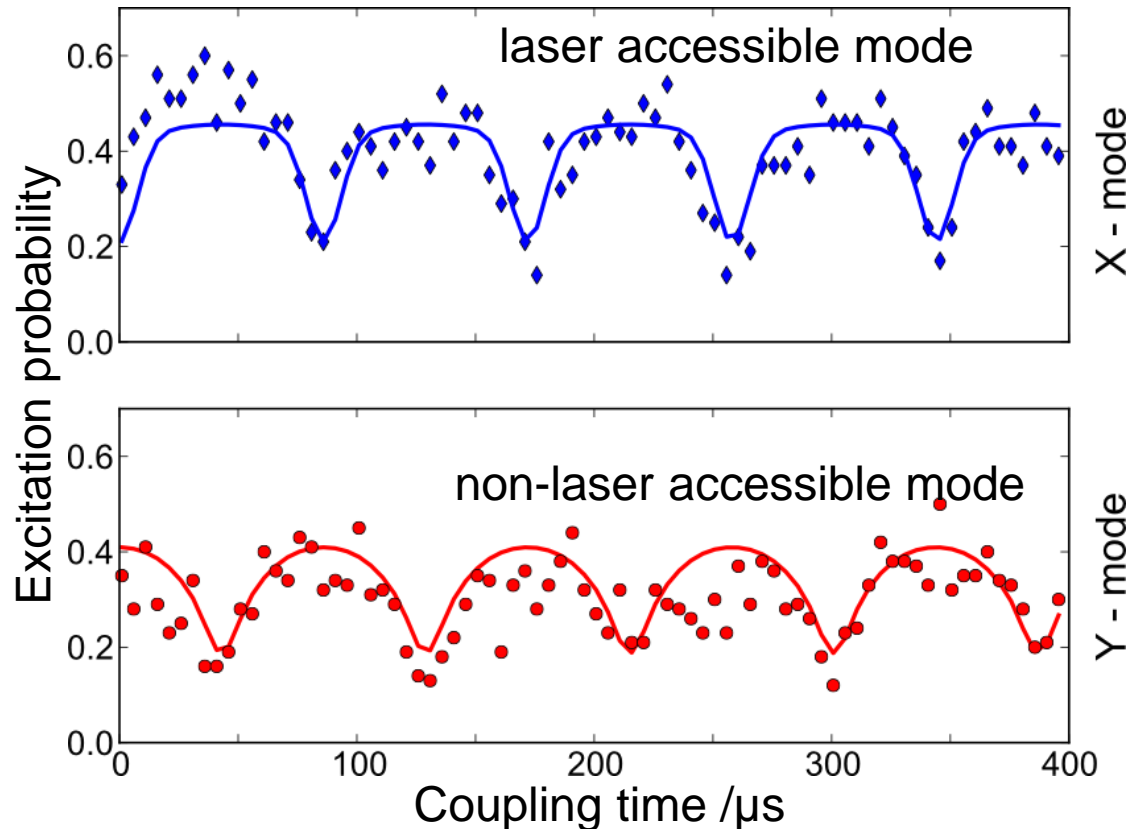
$$H_{i,j} = \frac{\partial}{\partial x_i} \frac{\partial}{\partial x_j} V.$$

$$\{\tilde{\omega}_j / \omega_z\} = \{\lambda \geq 0 \mid \det(M^{-1}H - \lambda^2 I) = 0\}$$

H. Kaufmann et al.,
Phys. Rev. Lett. 109, 263003 (2012)



Mode coupling by irradiation of difference frequencies



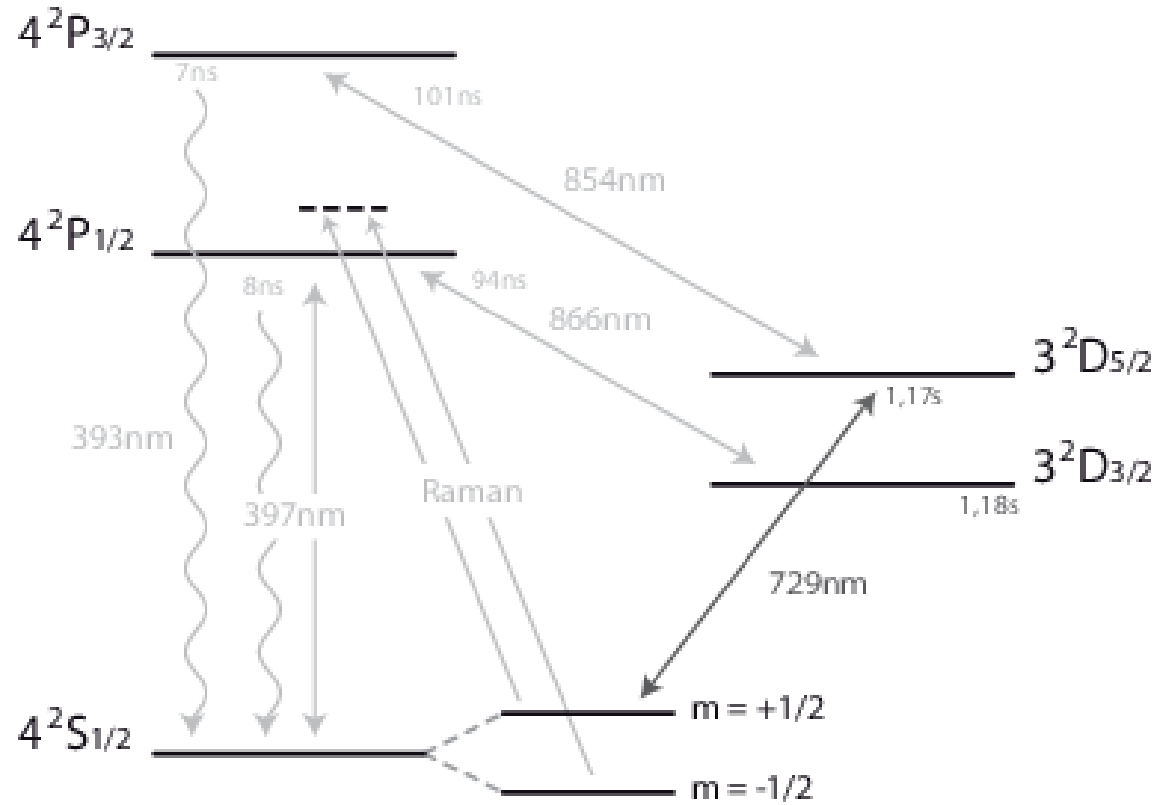
In this setup:
Not accessible due to geometric reasons

In Gbar:
Huge mass ratio results in low coupling

→ Ground state cooling despite low coupling

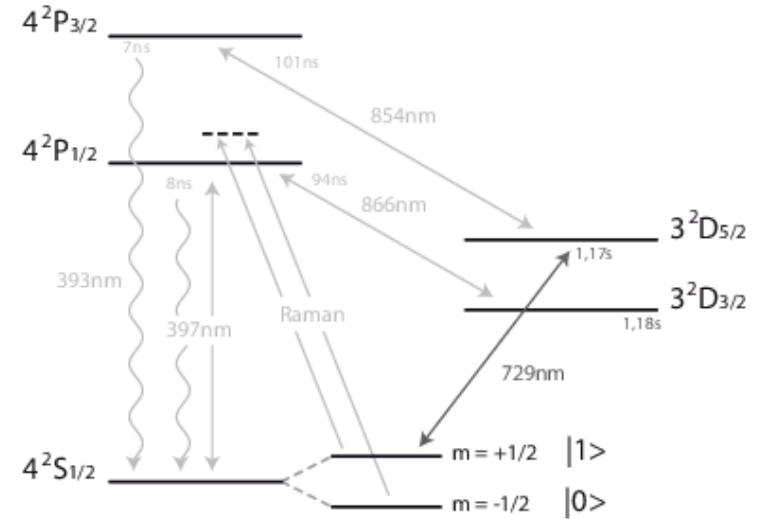
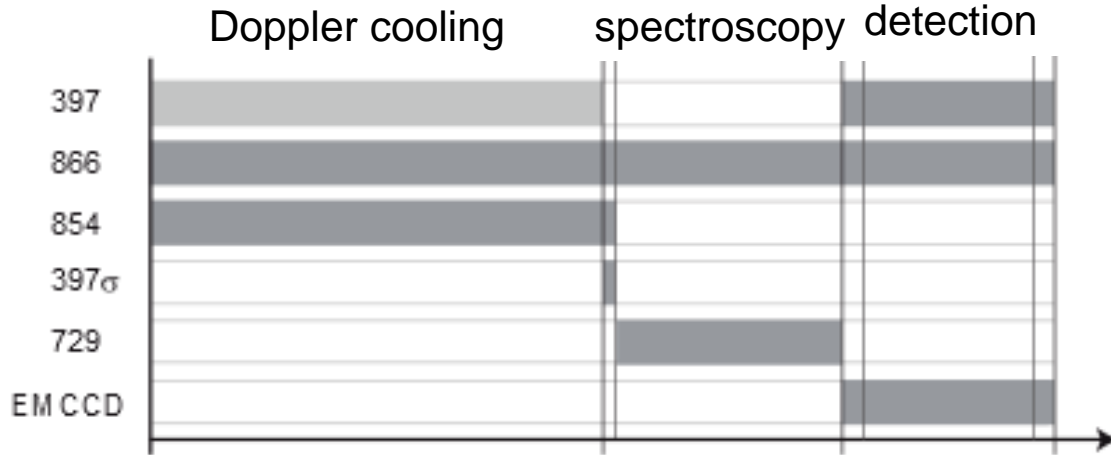
D. J. Gorman et al.,
Phys. Rev. A **89**, 062332 (2014)

Level scheme of $^{40}\text{Ca}^+$ ions

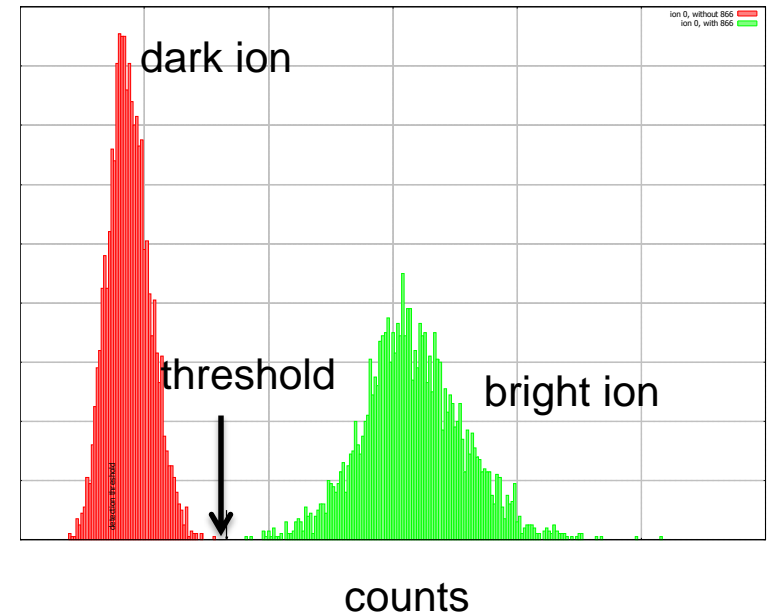
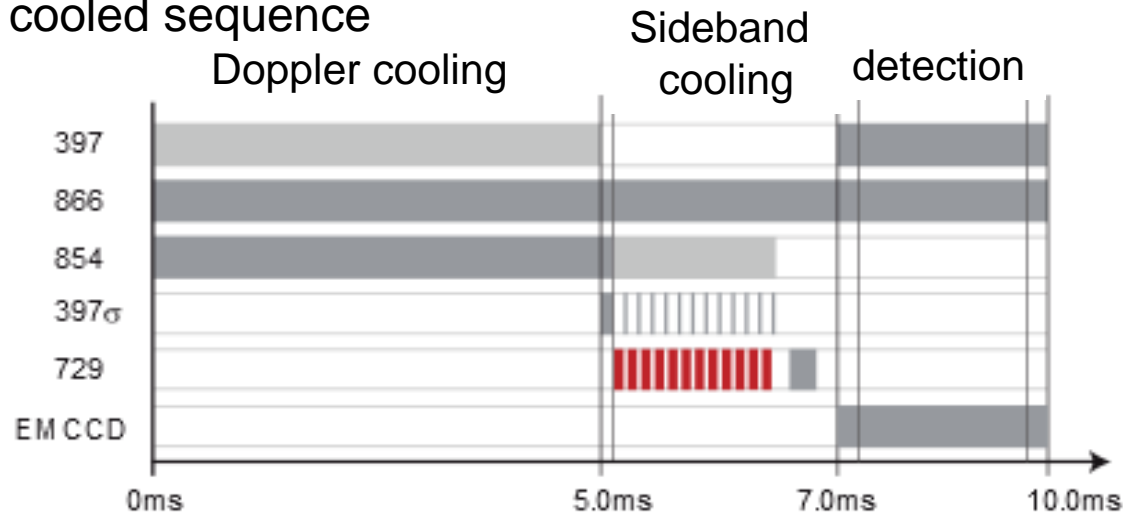


Sideband spectroscopy and cooling sequence

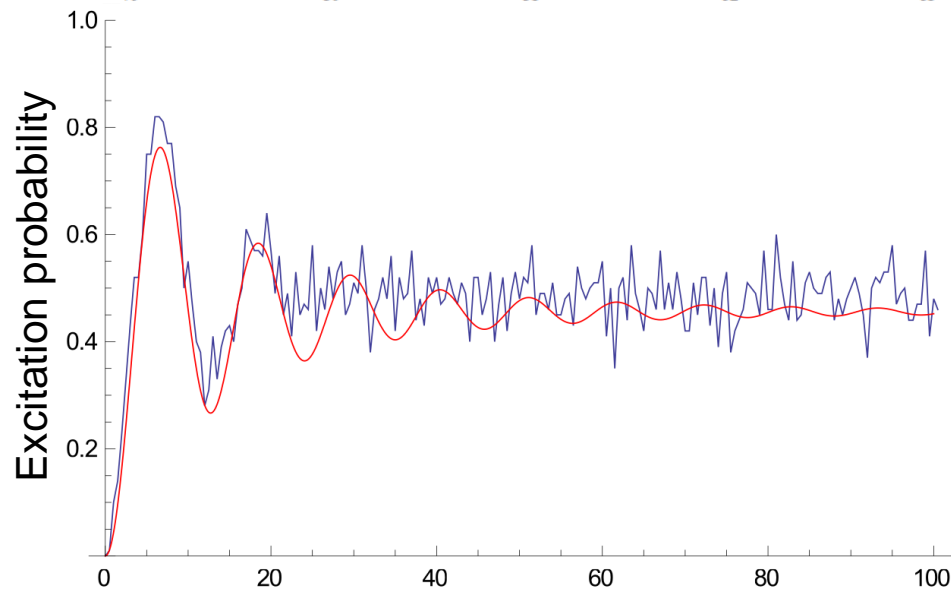
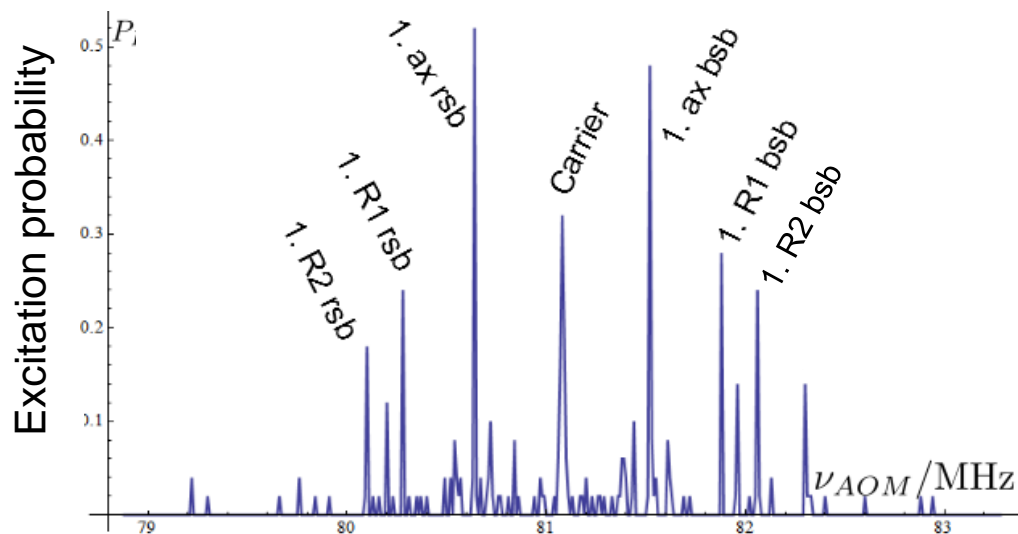
Doppler cooled sequence



Ground state cooled sequence



Sideband spectrum of single Ca⁺ ion



Axial heating rate in precision trap
 ~ 60 phonons/ms

Most probable due to floating electrode

\rightarrow ground state cooling not possible

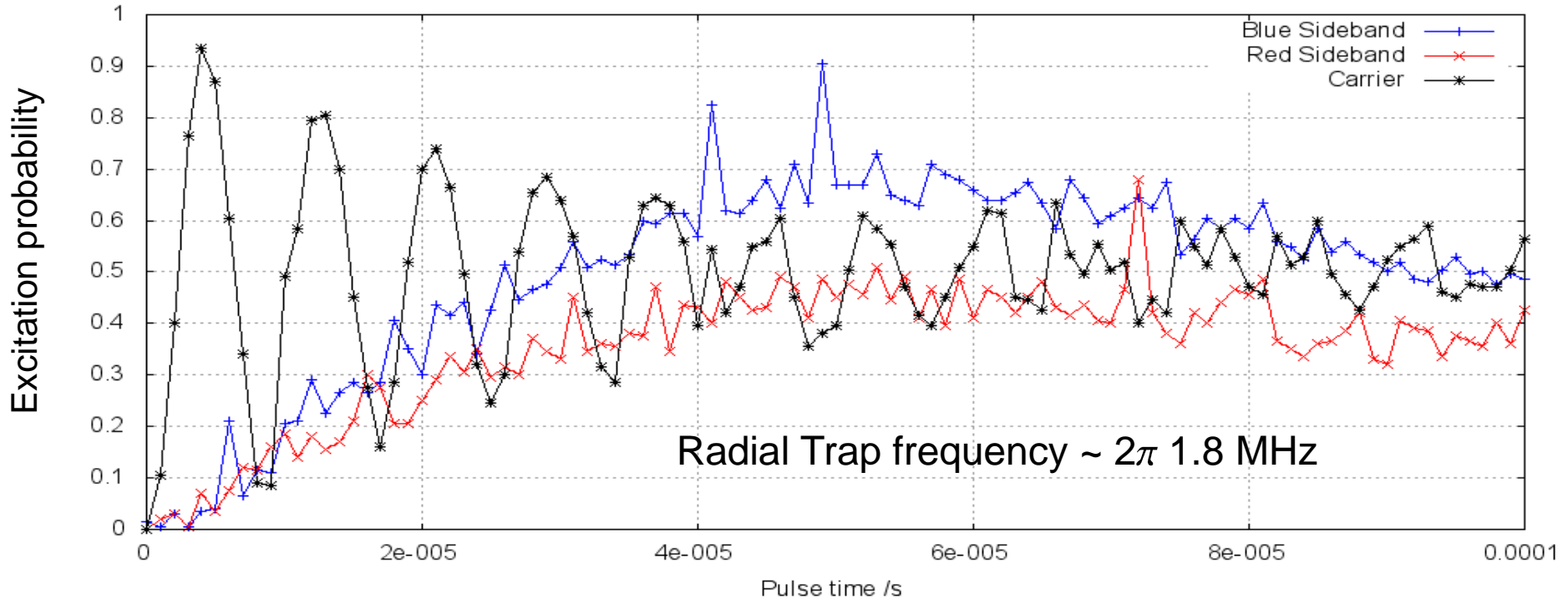
Sideband cooling to low phonon numbers

Results in identical trap in radial mode
(Implantation trap, Gerorg Jacob and Karin Groot-Berning)

$$\Omega_{car} \sim (1 - \eta^2 \bar{n}) \Omega_0$$

$$\Omega_{rsb} \sim \eta \sqrt{\bar{n}} \Omega_0$$

$$\Omega_{bsb} \sim \eta \sqrt{\bar{n} + 1} \Omega_0$$

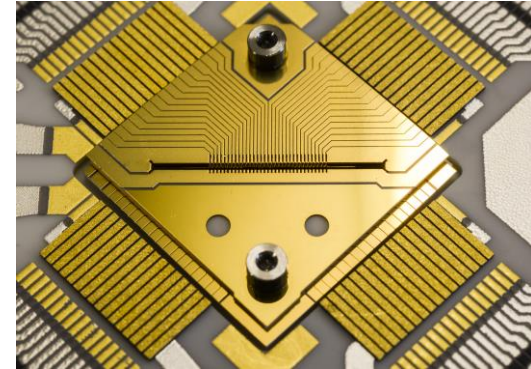
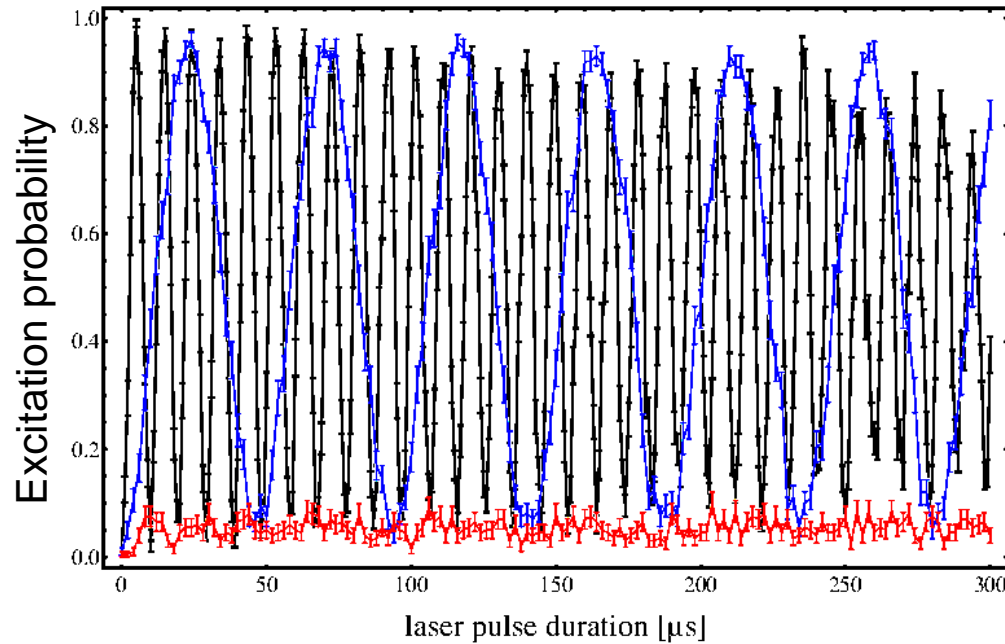


$$\bar{n} \sim 1.9$$

$$0.8 \text{ phonons/ms} < \dot{n} < 10 \text{ phonons/ms}$$



New trap design with electroplated electrodes

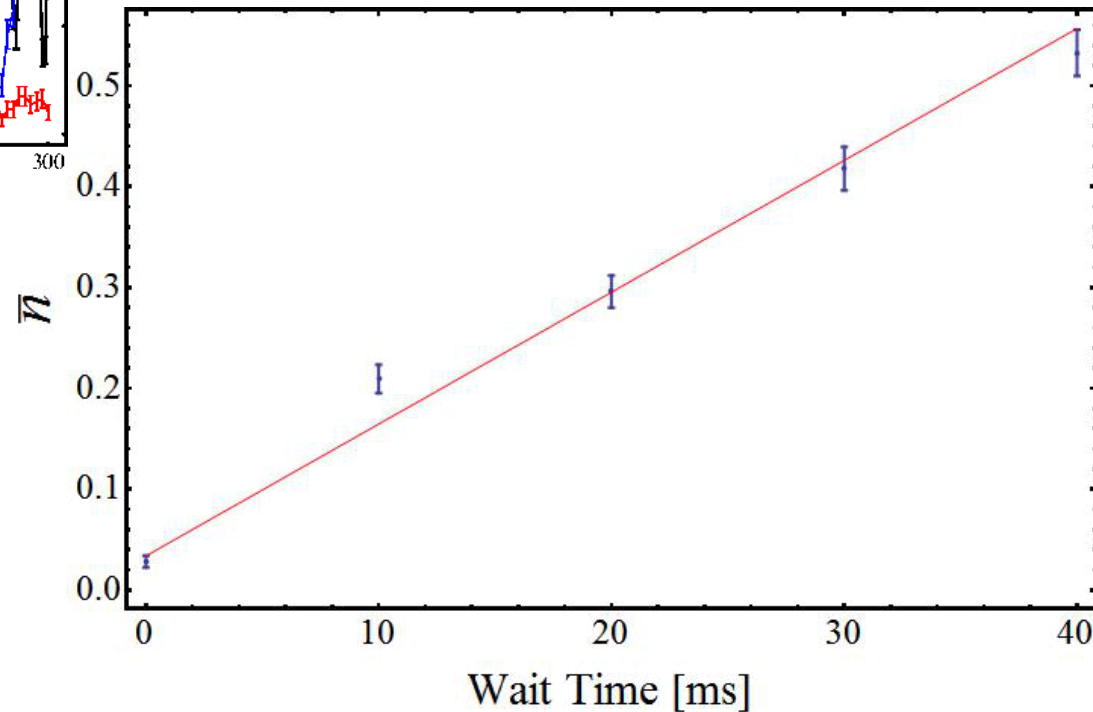


MicroTrap design with electroplating

$\bar{n} \sim 0.033$
 $\dot{n} \sim 13 \text{ phonons/s}$
 @ trap frequency $2\pi \cdot 1.7 \text{ MHz}$
 Distance ion \leftrightarrow electrodes: $d = 225 \mu\text{m}$

In GBAR trap $d = 475 \mu\text{m}$

$$\begin{aligned}
 \dot{n} &\propto d^{-4} \\
 \Rightarrow \dot{n}_{GBAR} &\sim 0.7 \text{ phonons/s}
 \end{aligned}$$



Adiabatic wavepacket expansion

Heisenberg limited ground state

$$\frac{\Delta \bar{g}}{\bar{g}} = \sqrt{\left(\frac{\Delta x}{2 \hbar}\right)^2 + \left(\frac{\hbar}{2 m \sqrt{2 \bar{g}} \hbar \Delta x}\right)^2}$$

Optimal position spread for g determination

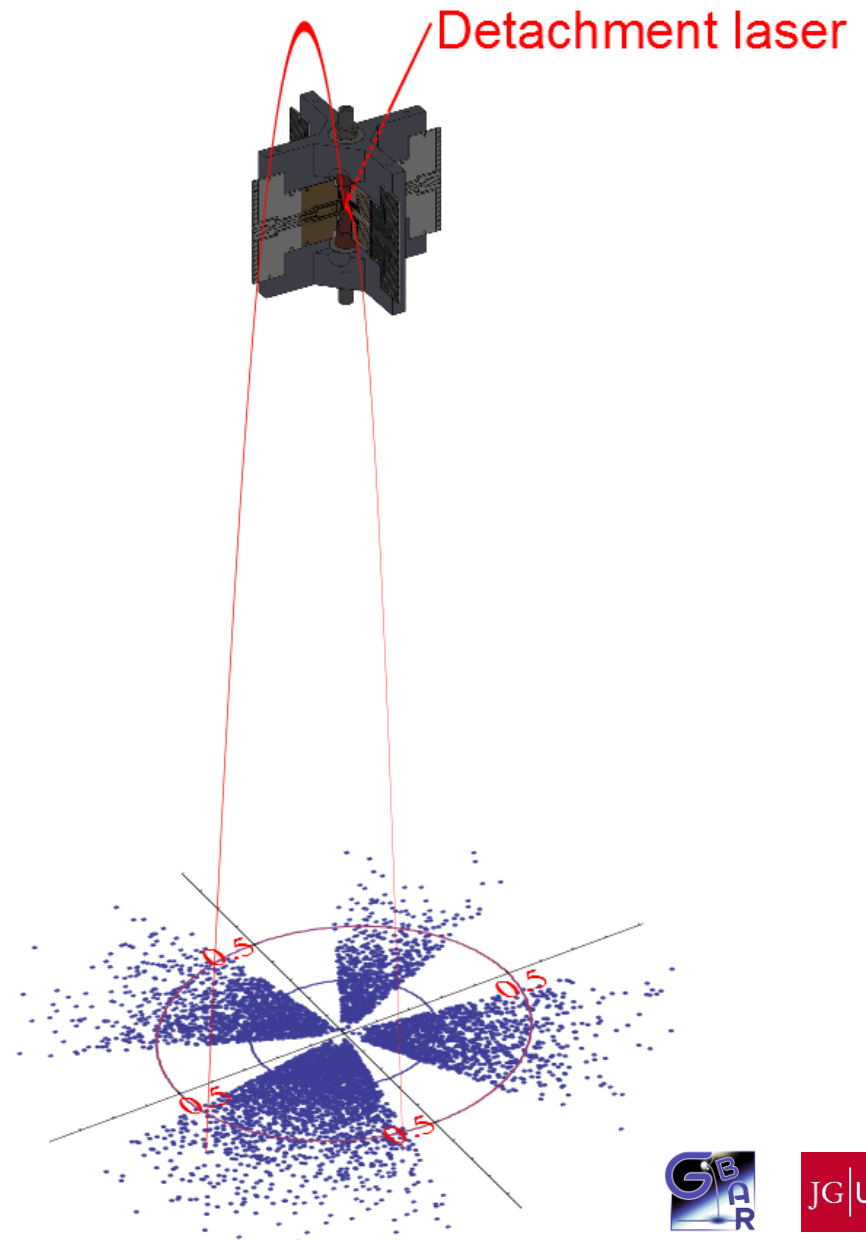
$$\rightarrow \omega_{ax} = 2\pi \text{ 1 Hz}; \Delta x_{min} = 88 \mu\text{m}$$

Main error from velocity spread

Solution:

Vertical trap and adiabatic opening of axial potential

G. Dufour et al.,
Eur. Phys. J. C, **74** 2731 (2014)



Adiabaticity vs. Heating rate

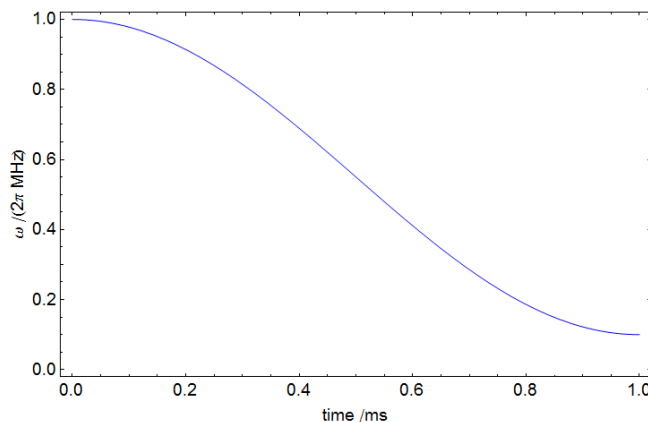
Axial adiabatic expansion $\omega_{ax} = 2\pi \text{ 1 MHz} \rightarrow 2\pi \text{ 0.1 MHz}$

Sin²-ramp

$$\frac{dn}{dt} \propto \omega^{-1}$$

Adiabaticity criterium

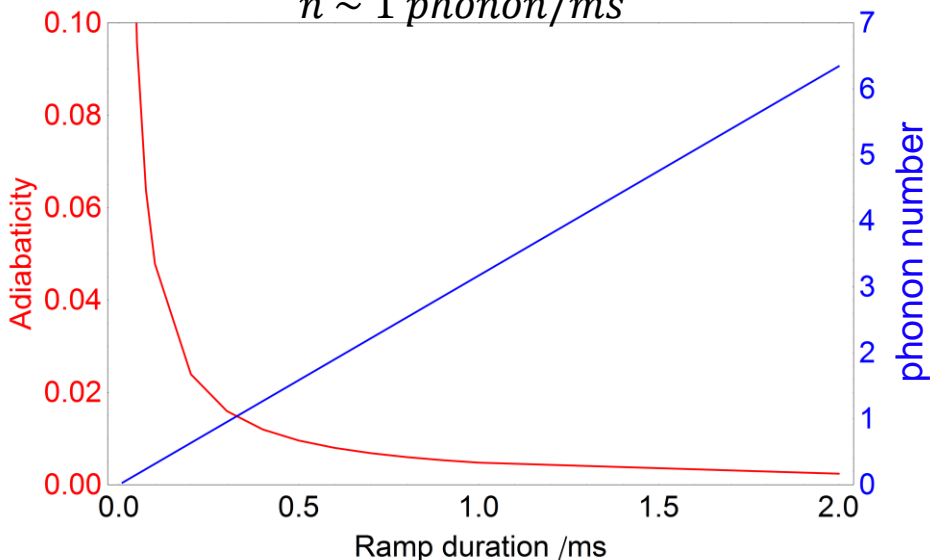
$$\frac{\dot{\omega}(t)}{\omega(t)^2} \ll 1, \forall t$$



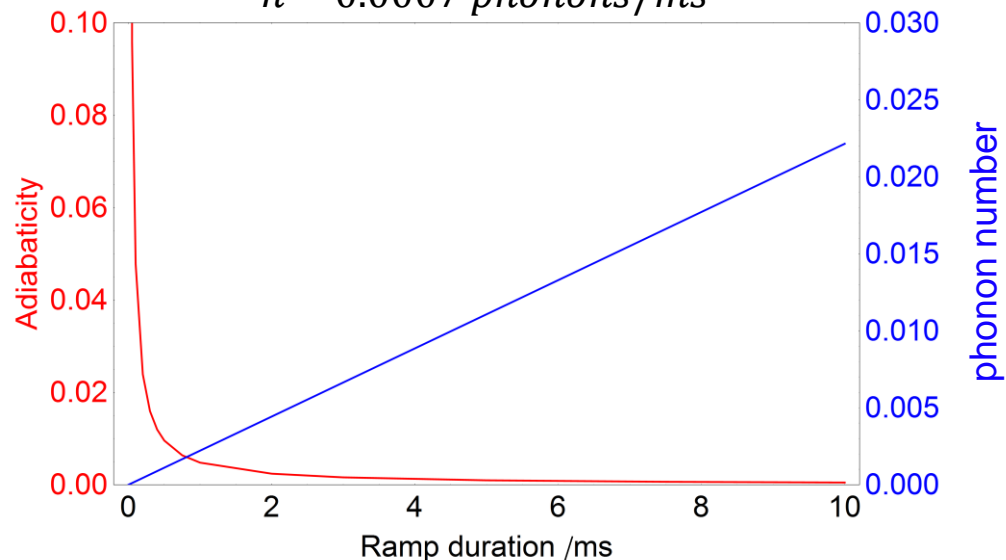
S. Schulz et al.,
Progress of Physics **54**, 648 (2006)

G. Poulsen et al.,
Phys. Rev. A **86**, 051402(R) (2012)

„old“ trap
 $\dot{n} \sim 1 \text{ phonon/ms}$



„new“ trap
 $\dot{n} \sim 0.0007 \text{ phonons/ms}$



Adiabaticity vs. Heating rate

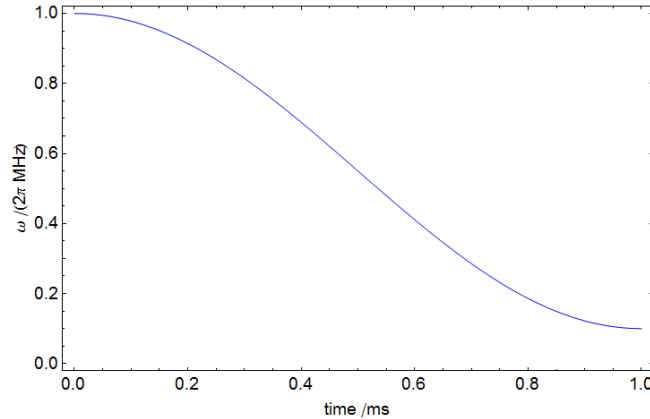
Axial adiabatic expansion $\omega_{ax} = 2\pi \text{ 1 MHz} \rightarrow 2\pi \text{ 0.1 MHz}$

Sin²-ramp

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Adiabaticity criterium

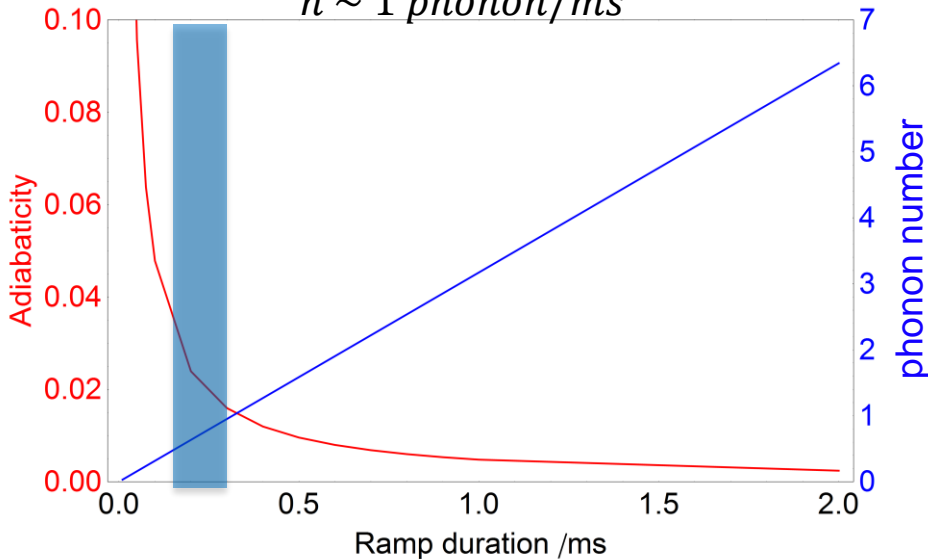
$$\frac{\dot{\omega}(t)}{\omega(t)^2} \ll 1, \forall t$$



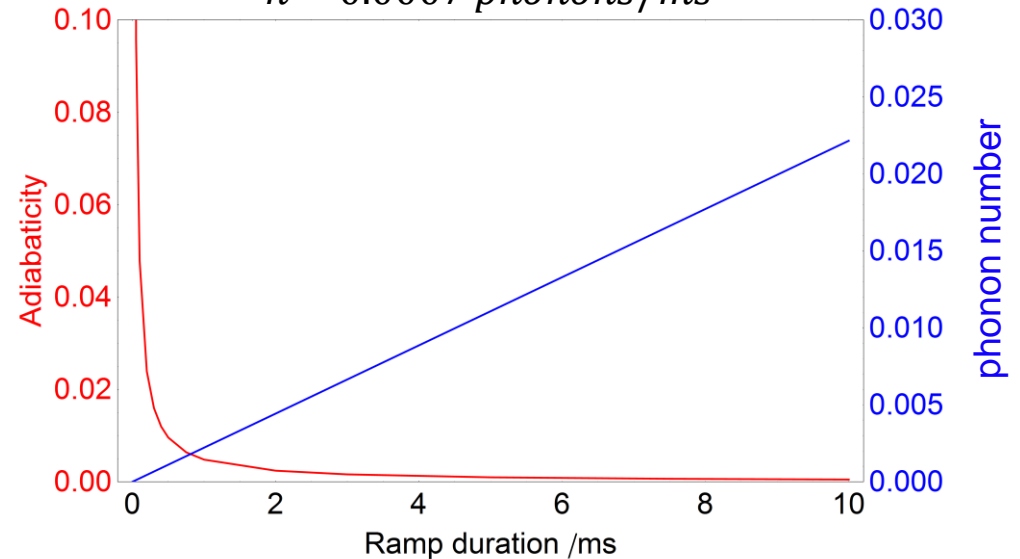
S. Schulz et al.,
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G. Poulsen et al.,
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Adiabaticity vs. Heating rate

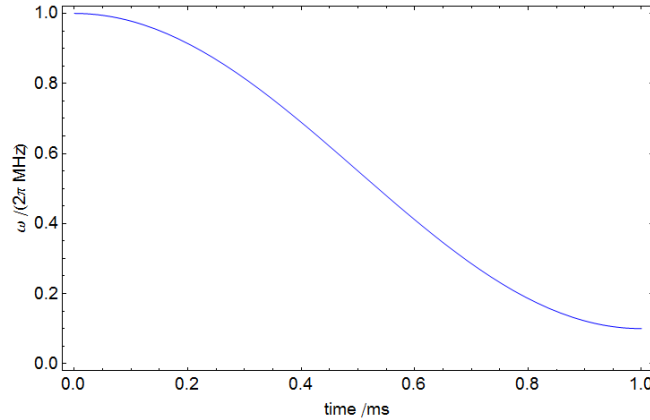
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Sin²-ramp

$$\frac{dn}{dt} \propto \omega^{-1}$$

Adiabaticity criterium

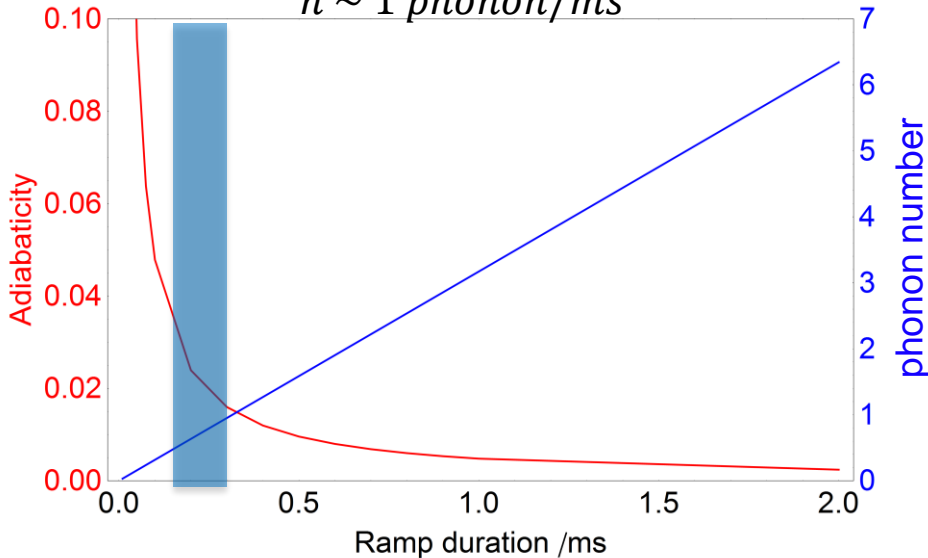
$$\frac{\dot{\omega}(t)}{\omega(t)^2} \ll 1, \forall t$$



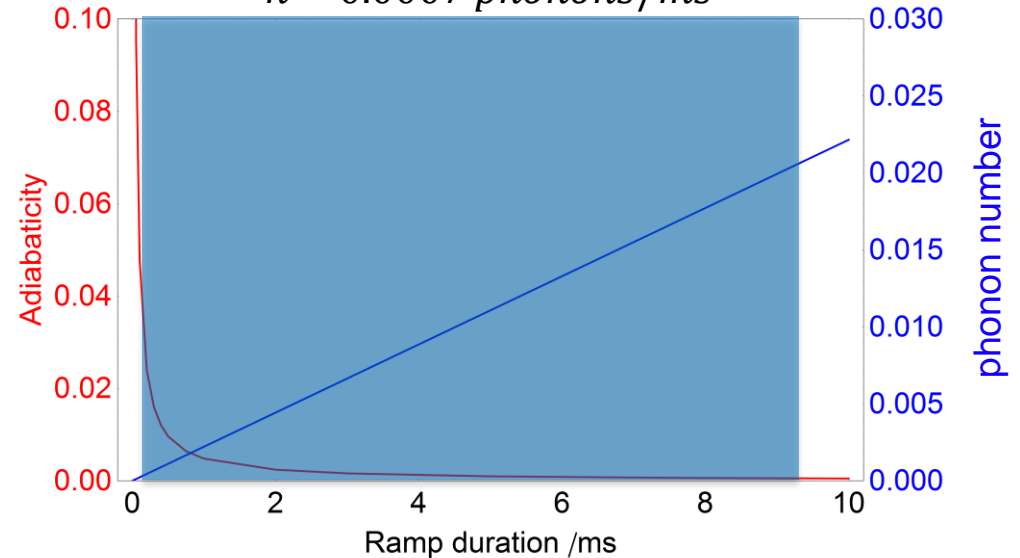
S. Schulz et al.,
Progress of Physics **54**, 648 (2006)

G. Poulsen et al.,
Phys. Rev. A **86**, 051402(R) (2012)

„old“ trap
 $\dot{n} \sim 1 \text{ phonon/ms}$



„new“ trap
 $\dot{n} \sim 0.0007 \text{ phonons/ms}$



Temperature measurement after expansion

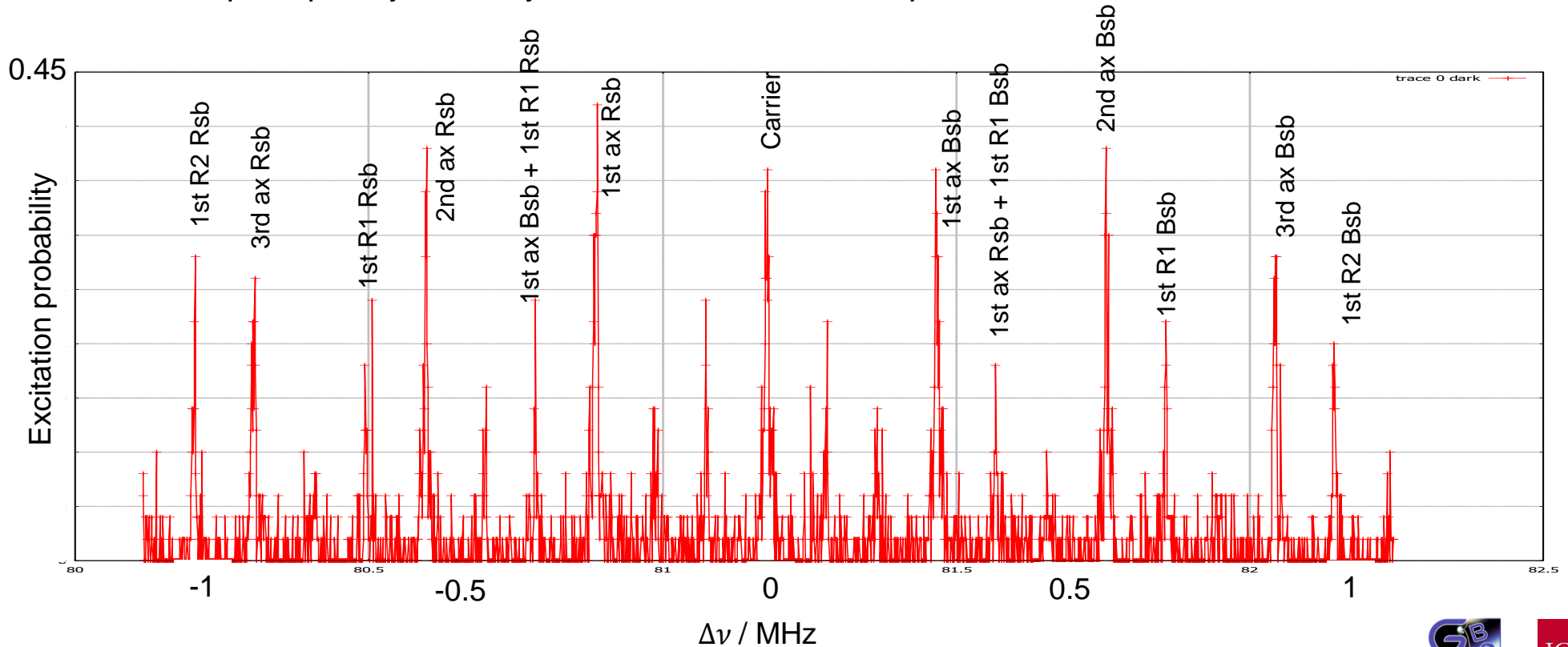
$$\eta = k \cos \phi \sqrt{\frac{\hbar}{2 m \omega}}$$

Lamb-Dicke parameter

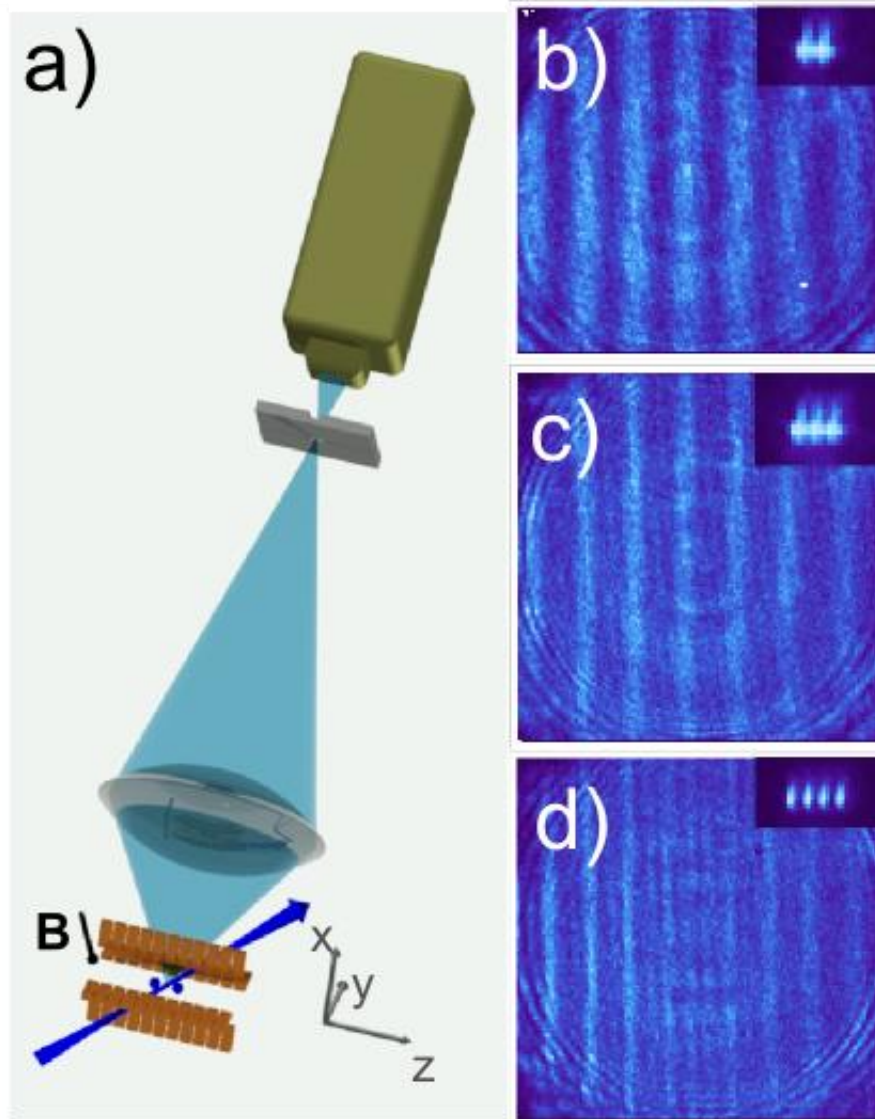
$$\Omega_{n+m,n} = \Omega_0 e^{-\frac{\eta^2}{2}} \eta^{|m|} L_{\min(n,n+m)}^{|m|}(\eta^2) \frac{(\min(n,n+m))!}{(\max(n,n+m))!}$$

Rabi frequency of sidebands

small trap frequency \rightarrow many sidebands, hard to interpret/address



Young-interference of ions in far-field



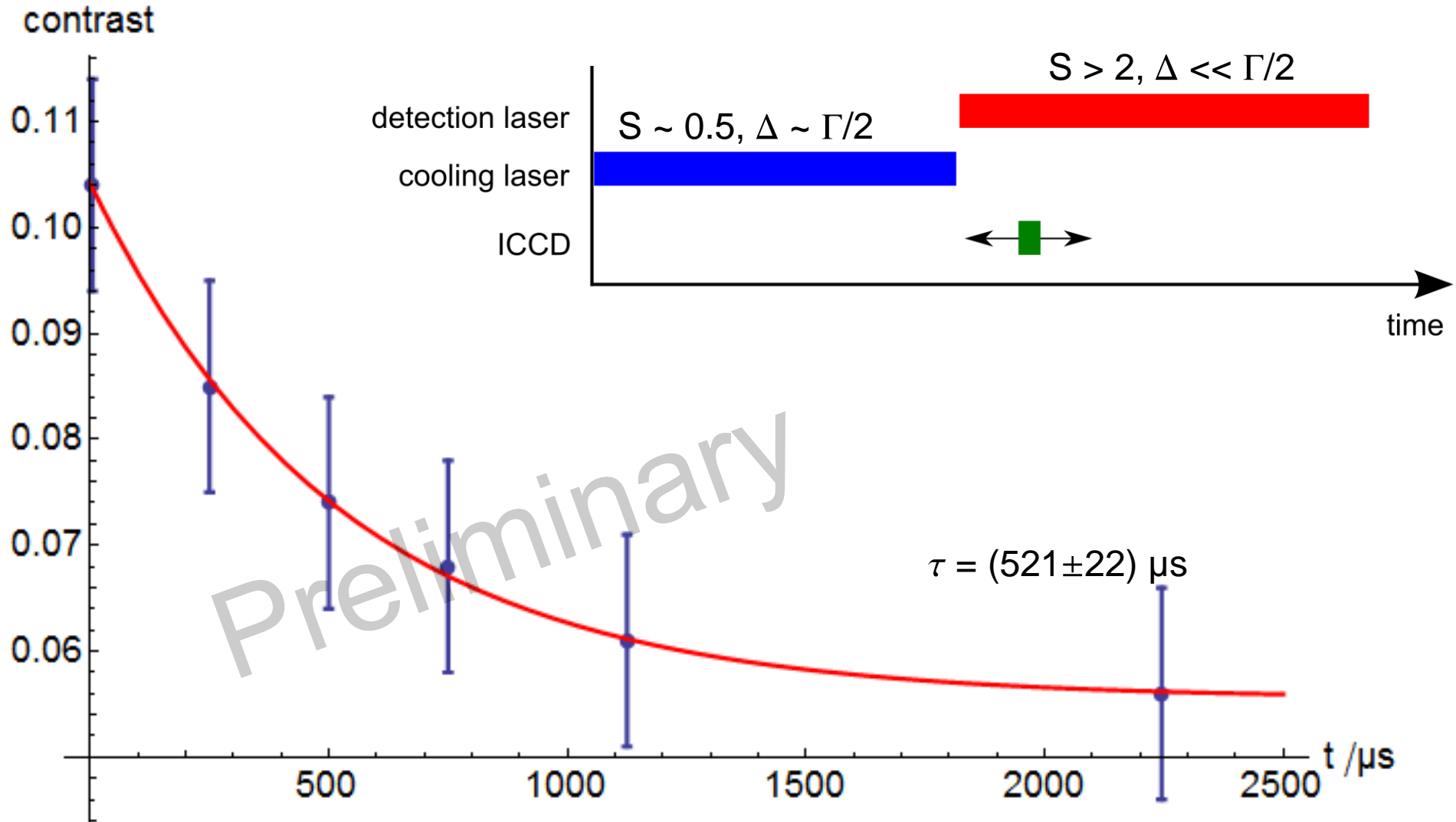
Debye-Waller factor

$$I(\mathbf{q}) = 2I_0(1 + \cos(q_z d) \exp\{-\langle[\mathbf{q} \cdot (\mathbf{u}_1 - \mathbf{u}_2)]^2\rangle/2\})$$

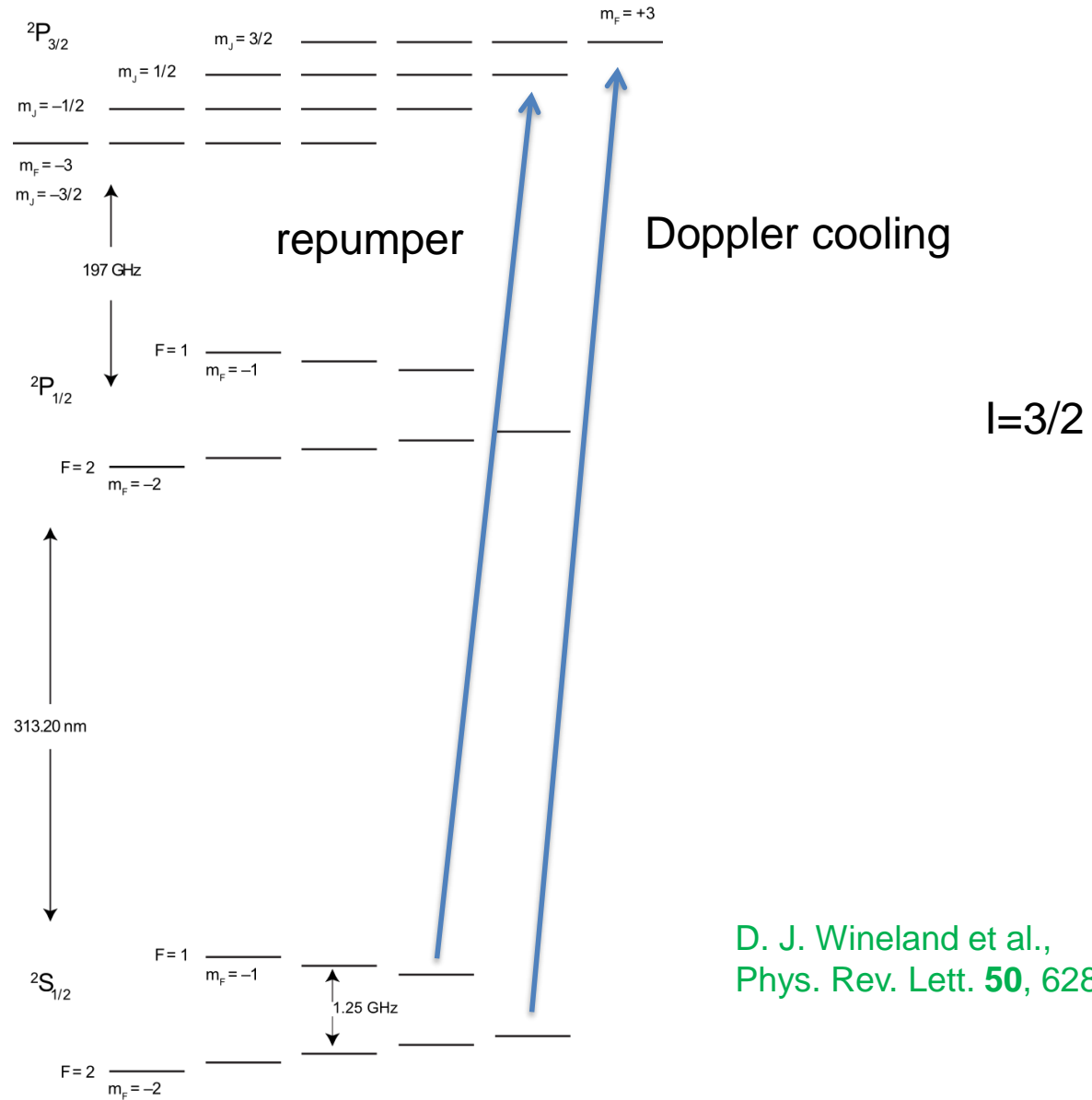
$$\mathbf{q} = \mathbf{k}_{out} - \mathbf{k}_{in}$$

→ Contrast is temperature dependant

Thermometry with two ion crystals

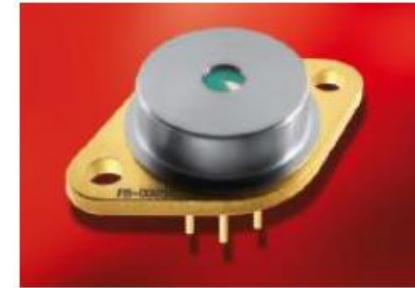


Level scheme of ${}^9\text{Be}^+$ ions

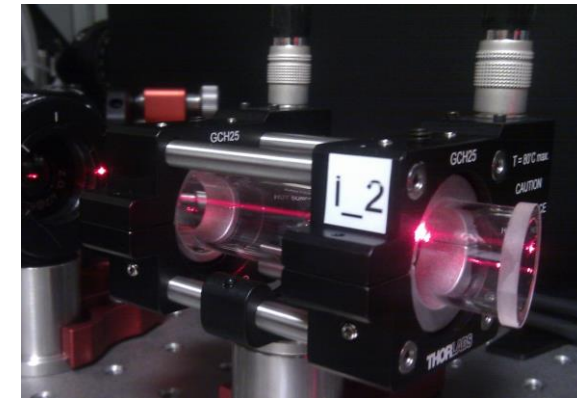
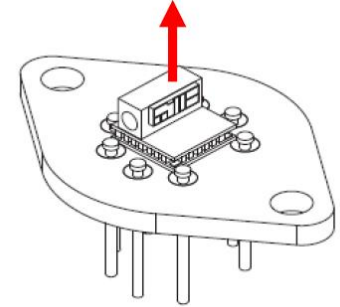


D. J. Wineland et al.,
 Phys. Rev. Lett. **50**, 628 (1983)

Distributed Bragg Reflector diode



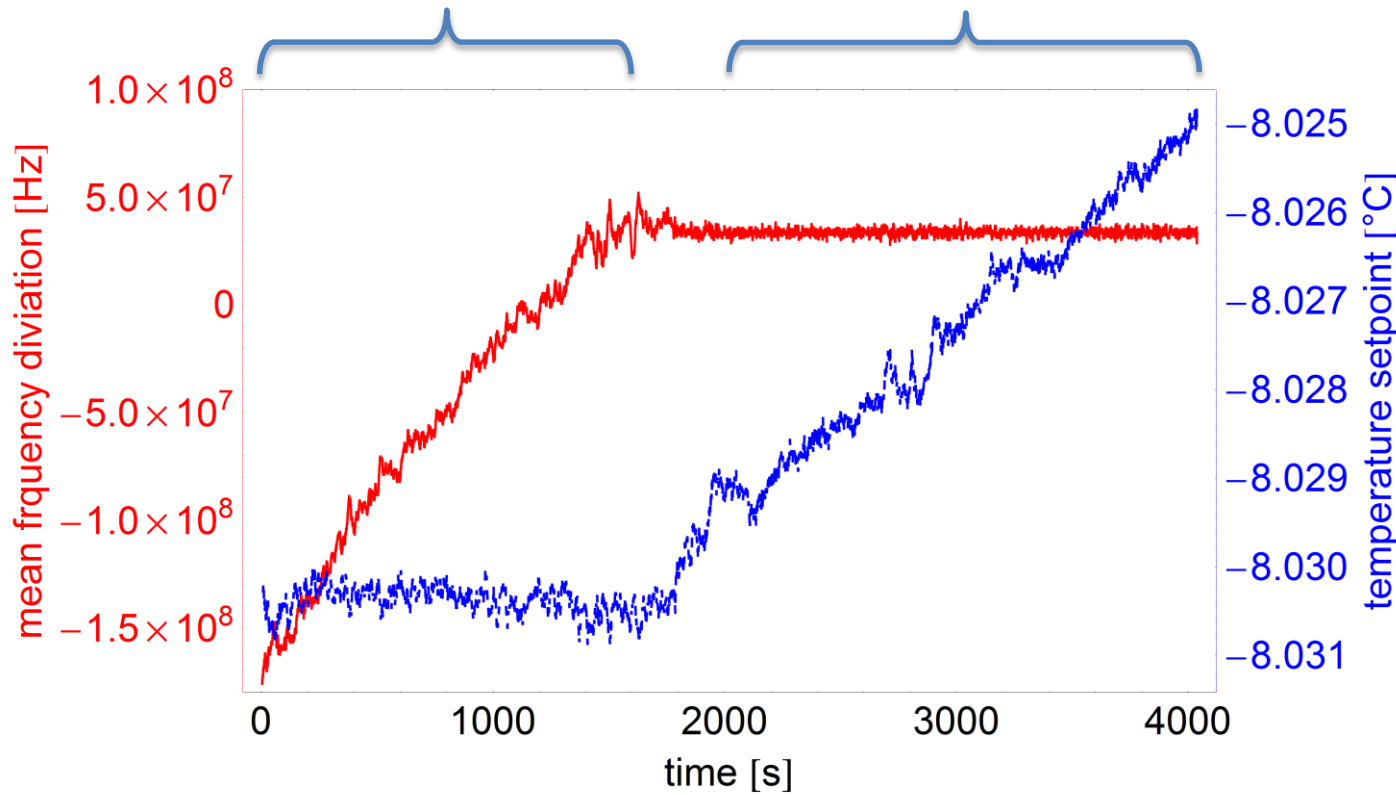
from Ferdinand-Braun-Institute Berlin



$\lambda = 626 \text{ nm}$

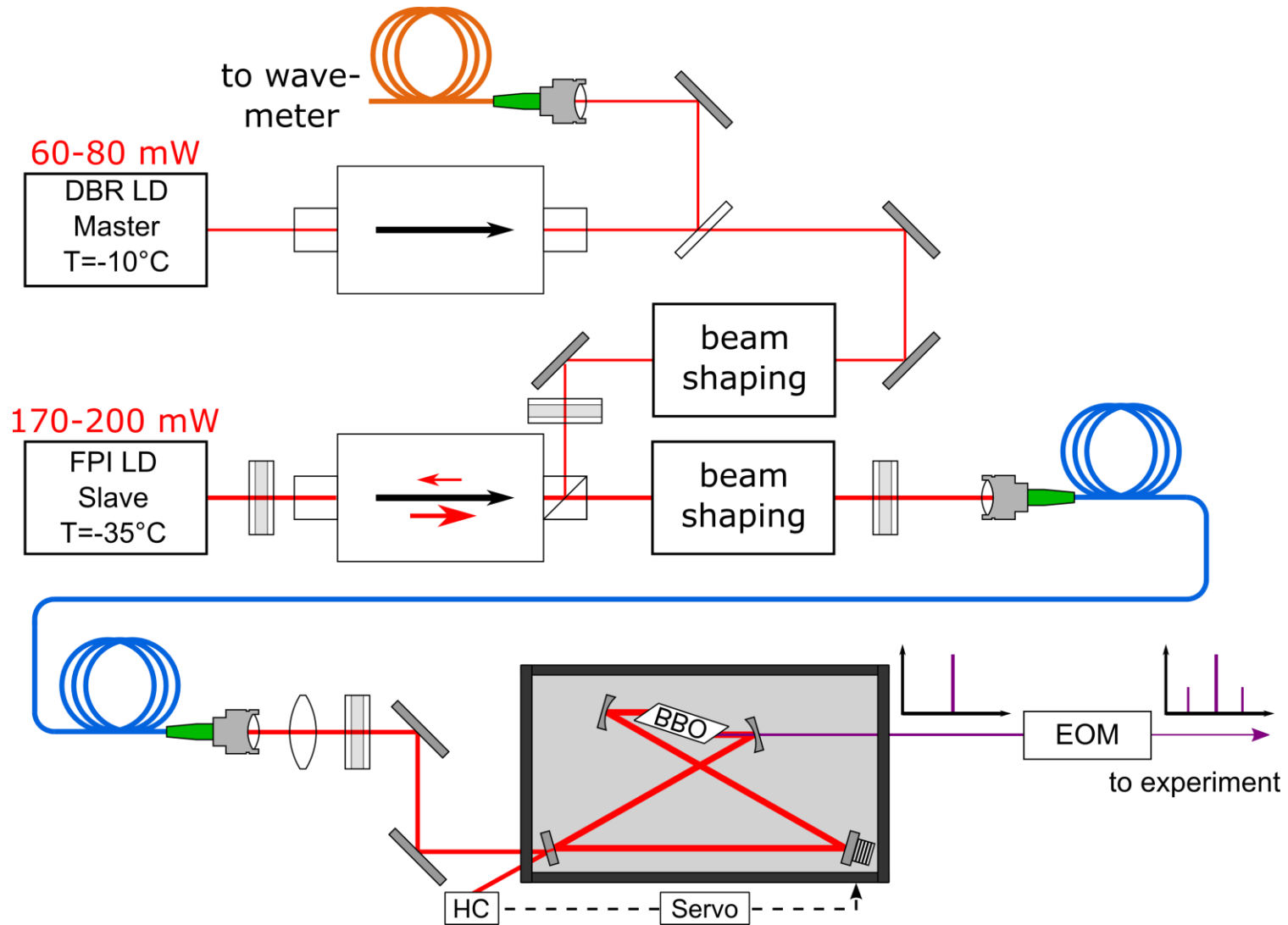
Only temperature stabilized

Locked on wavemeter
Frequency variation < 1.6 MHz

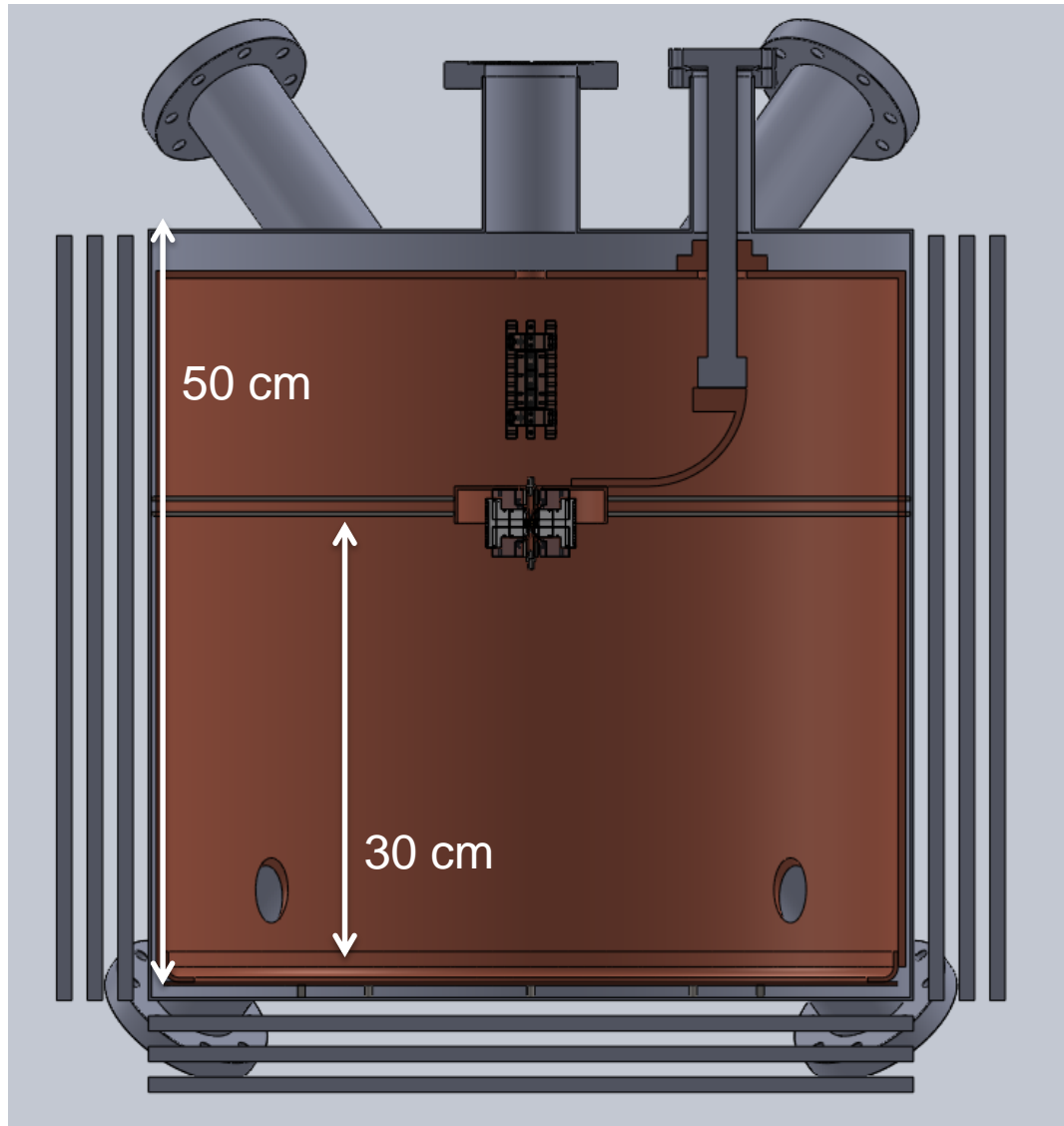


Currently setting up an Iodine spectroscopy cell

313nm Laser setup for Beryllium cooling

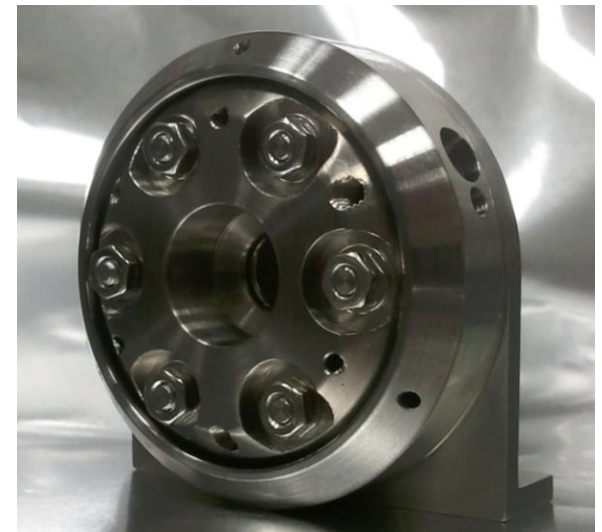


Cryogenic UHV setup

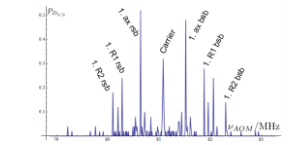


Design constraints

- Cryo (heating rate, pressure)
- Optical access (lasers, CCD)
- Thin walls (pion detection)
- Ion optics (\bar{H}^+ transport)
- Capture trap
- Velocity shaper

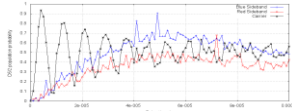


Conclusion and Outlook



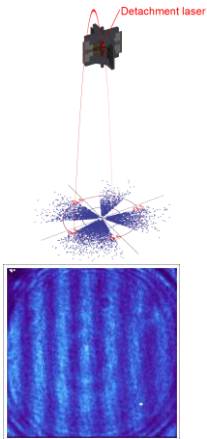
Sideband spectroscopy and cooling
Increased mode coupling required

2015



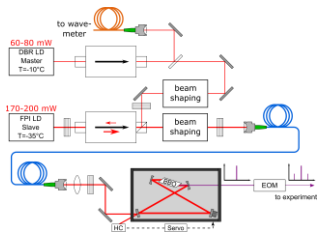
Adiabatic expansion for decreased momentum distribution

2016



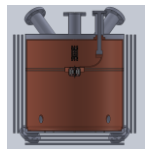
Interference contrast for temperature measurements

done



construction of Beryllium laser setup

2015



Cryo setup design

2016