

Mueller-Navelet jets at LHC: discriminating BFKL from DGLAP by asymmetric cuts

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based on

[F.G. C., D.Yu. Ivanov, B. Murdaca, A. Papa (2015)]

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Borgo, Corsica

Outline

- 1 Introduction
 - Mueller-Navelet jet production
- 2 Theoretical setup
 - BFKL resummation
 - BFKL vs high-energy DGLAP
 - BLM optimization procedure
- 3 Results
 - Numerical analysis
- 4 Conclusions

Outline

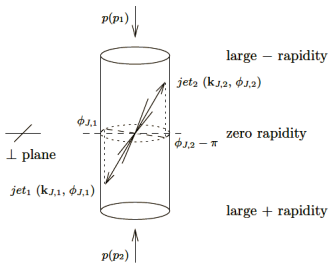
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Mueller-Navelet jets

Process: proton(p_1) + proton(p_2) \rightarrow jet $_1(k_1)$ + jet $_2(k_2)$ + X ...*LHC physics!*

$$\frac{d\sigma}{dx_{J_1} dx_{J_2} d^2k_{J_1} d^2k_{J_2}} = \sum_{i,j=q,\bar{q},g} \int_0^1 dx_1 \int_0^1 dx_2 f_i(x_1, \mu) f_j(x_2, \mu) \frac{d\hat{\sigma}_{ij}(x_1 x_2 s, \mu)}{dx_{J_1} dx_{J_2} d^2k_{J_1} d^2k_{J_2}}$$

- large jet transverse momenta: $\vec{k}_{J,1}^2 \sim \vec{k}_{J,2}^2 \gg \Lambda_{\text{QCD}}^2 \Rightarrow$ pQCD allowed
- large rapidity gap between jets (high energies) $\Rightarrow \Delta y = \ln \frac{x_{J,1} x_{J,2} s}{|\vec{k}_{J,1}| |\vec{k}_{J,2}|}$
 \Rightarrow BFKL resummation: $\sum_n \left(a_n^{(0)} \alpha_s^n \ln^n s + a_n^{(1)} \alpha_s^n \ln^{n-1} s \right)$



*Mueller-Navelet jets at LO:
a back-to-back di-jet reaction*

Picture from
[D. Colferai, F. Schwennsen, L. Szymanowski, S. Wallon (2010)]

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The BFKL resummation

pQCD, total cross section for $A + B \rightarrow X$: $\sigma_{AB}(s) = \frac{\text{Im}_s(\mathcal{A}_{AB}^{AB})}{s} \leftarrow$ optical theorem

- ◇ **Pomeron channel**: $t = 0$ + singlet colour representation in the t -channel
- ◇ **Regge limit**: $s \simeq -u \rightarrow \infty$, t not growing with s

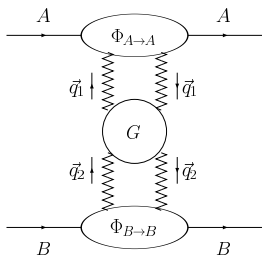
- **BFKL resummation**:

leading logarithmic approximation (LLA):

next-to-leading logarithmic approximation (NLA):

$$\alpha_s^n (\ln s)^n$$

$$\alpha_s^{n+1} (\ln s)^n$$



► $\text{Im}_s(\mathcal{A}_{AB}^{AB})$ factorization:

convolution of the **Green's function** of two interacting Reggeized gluons with the **impact factors** of the colliding particles.

$$\text{Im}_s(\mathcal{A}) = \frac{s}{(2\pi)^{D-2}} \int \frac{d^{D-2}q_1}{\vec{q}_1^2} \Phi_A(\vec{q}_1, \mathbf{s}_0) \int \frac{d^{D-2}q_2}{\vec{q}_2^2} \Phi_B(-\vec{q}_2, \mathbf{s}_0) \int_{\delta-i\infty}^{\delta+i\infty} \frac{d\omega}{2\pi i} \left(\frac{s}{s_0}\right)^\omega G_\omega(\vec{q}_1, \vec{q}_2)$$

- **Green's function** is **process-independent**

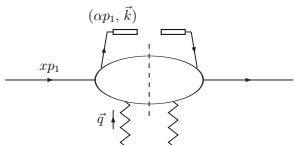
→ determined through the **BFKL equation**

[Ya.Ya. Balitsky, V.S. Fadin, E.A. Kuraev, L.N. Lipatov (1975)]

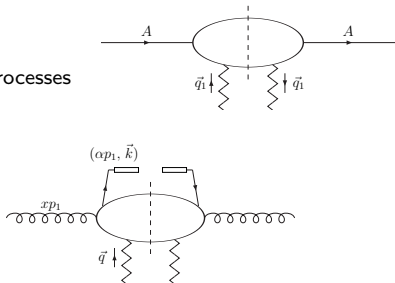
- **Impact factors** are **process-dependent**

→ known in the NLA just for few processes

- * forward jet production



quark jet vertex



gluon jet vertex

[J. Bartels, D. Colferai, G.P. Vacca (2003)]

[F. Caporale, D.Yu. Ivanov, B. Murdaca, A. Papa, A. Perri (2012)]

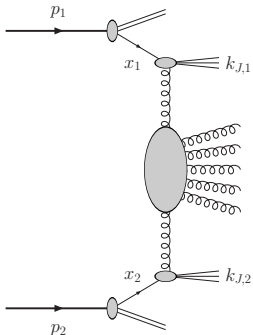
[D.Yu. Ivanov, A. Papa (2012)]

[D. Colferai, A. Niccoli (2015)]

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The cross section



Azimuthal correlation momenta

$$\langle \cos [n (\phi_{J_1} - \phi_{J_2} - \pi)] \rangle \equiv \frac{C_n}{C_0},$$

$$\mathcal{R}_{m,n} = \frac{\langle \cos (m\Delta\phi) \rangle}{\langle \cos (n\Delta\phi) \rangle}$$

$$\frac{d\sigma}{dx_{J_1} dx_{J_2} d|\vec{k}_{J_1}| d|\vec{k}_{J_2}| d\phi_{J_1} d\phi_{J_2}} = \frac{1}{(2\pi)^2} \left[C_0 + \sum_{n=1}^{\infty} 2 \cos(n\phi) C_n \right]$$

...useful definitions:

$$Y = \ln \frac{x_{J_1} x_{J_2} s}{|\vec{k}_{J_1}| |\vec{k}_{J_2}|}, \quad Y_0 = \ln \frac{s_0}{|\vec{k}_{J_1}| |\vec{k}_{J_2}|}$$

BFKL cross section...

$$\begin{aligned}
 C_n^{BFKL} &= \int_{-\infty}^{+\infty} dv e^{(Y-Y_0)[\bar{\alpha}_s(\mu_R)\chi(n,v)+\bar{\alpha}_s^2(\mu_R)K^{(1)}(n,v)]} \alpha_s^2(\mu_R) \\
 &\times c_1(n,v) c_2(n,v) \left[1 + \alpha_s(\mu_R) \left(\frac{c_1^{(1)}(n,v)}{c_1(n,v)} + \frac{c_2^{(1)}(n,v)}{c_2(n,v)} \right) \right]
 \end{aligned}$$

where

$$\chi(n,v) = 2\psi(1) - \psi\left(\frac{n}{2} + \frac{1}{2} + iv\right) - \psi\left(\frac{n}{2} + \frac{1}{2} - iv\right)$$

$$K^{(1)}(n,v) = \bar{\chi}(n,v) + \frac{\beta_0}{8N_c} \chi(n,v) \left(-\chi(n,v) + \frac{10}{3} + i \frac{d}{dv} \ln \left(\frac{c_1(n,v)}{c_2(n,v)} \right) + 2 \ln(\mu_R^2) \right)$$

...several NLA-equivalent expressions can be adopted for C_n !

→ ...we use the *exponentiated* one

[F. Caporale, D.Yu Ivanov, B. Murdaca, A. Papa, (2014)]

...high-energy DGLAP

- ◆ NLA BFKL expressions for the observables truncated to $\mathcal{O}(\alpha_s^3)$!

$$C_n^{DGLAP} = \int_{-\infty}^{+\infty} d\nu \alpha_s^2(\mu_R) c_1(n, \nu) c_2(n, \nu) \times \left[1 + \bar{\alpha}_s(\mu_R) (Y - Y_0) \chi(n, \nu) + \alpha_s(\mu_R) \left(\frac{c_1^{(1)}(n, \nu)}{c_1(n, \nu)} + \frac{c_2^{(1)}(n, \nu)}{c_2(n, \nu)} \right) \right]$$

Why asymmetric cuts?

- ▶ suppress Born contribution to ϕ -averaged cross section C_0 (back-to-back jets)

- ◆ avoid instabilities observed in NLO fixed-order calculations

[J.R. Andersen, V. Del Duca, S. Frixione, C.R. Schmidt, W.J. Stirling (2001)]

[M. Fontannaz, J.P. Guillet, G. Heinrich (2001)]

- ◆ **enhance effects of additional hard gluons** $\xrightarrow{\text{emphasize}}$ **BFKL effects**

- ▶ violation of energy-momentum in NLA strongly suppressed respect to LLA

[B. Ducloué, L. Szymanowski, S. Wallon (2014)]

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BLM method

NLO BFKL corrections to C_0 with opposite sign with respect to the leading order (LO) result and large in absolute value.

- ◇ ...call for some optimization procedure...
- ◇ ...choose scales to mimic the most relevant subleading terms
- **BLM** [S.J. Brodsky, G.P. Lepage, P.B. Mackenzie (1983)]
 - ✓ preserve the conformal invariance of an observable...
 - ✓ ...by making vanish its β_0 -dependent part
 - ✓ $\overline{MS} \rightarrow MOM$ + choose BLM scale + $MOM \rightarrow \overline{MS}$

* Partial (approximated) BLM:

$$a) \quad (\mu_R^{BLM})^2 = k_1 k_2 \exp \left[2 \left(1 + \frac{2}{3} l \right) - f(v) - \frac{5}{3} \right] \leftarrow \text{NLO IFs } \beta_0$$

$$b) \quad (\mu_R^{BLM})^2 = k_1 k_2 \exp \left[2 \left(1 + \frac{2}{3} l \right) - 2 f(v) - \frac{5}{3} + \frac{1}{2} \chi(v, n) \right] \leftarrow \text{NLO Kernel } \beta_0$$

[F. Caporale, D.Yu. Ivanov, B. Murdaca, A. Papa, (2015)]

$f(v) = 0$ for this process

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Observables and kinematics

- **Observables:**

$$\langle \cos [n (\phi_{J_1} - \phi_{J_2} - \pi)] \rangle \equiv \frac{C_n}{C_0}, \text{ with } n = 1, 2, 3$$

$$\frac{\langle \cos [2 (\pi - \Delta\phi)] \rangle}{\langle \cos (\pi - \Delta\phi) \rangle} = \frac{C_2}{C_1}, \quad \frac{\langle \cos [3 (\pi - \Delta\phi)] \rangle}{\langle \cos [2 (\pi - \Delta\phi)] \rangle} = \frac{C_3}{C_2}, \quad \text{with } \Delta\phi = \phi_{J_2} - \phi_{J_1}.$$

- ◇ *Integrated coefficients:*

$$C_n = \int_{y_{1,\min}}^{y_{1,\max}} dy_1 \int_{y_{2,\min}}^{y_{2,\max}} dy_2 \int_{k_{J_1,\min}}^{\infty} dk_{J_1} \int_{k_{J_2,\min}}^{\infty} dk_{J_2} \delta(y_1 - y_2 - Y) C_n(y_{J_1}, y_{J_2}, k_{J_1}, k_{J_2})$$

- **Kinematic settings:**

- ◇ $R = 0.5$ and $\sqrt{s} = 7$ TeV
- ◇ $-4.7 \leq y_i \leq 4.7$, with $i = 1, 2$
- ◇ $35 \text{ GeV} \leq k_{J_1} \leq 60 \text{ GeV}$
 $45 - 50 \text{ GeV} \leq k_{J_2} \leq 60 \text{ GeV}$

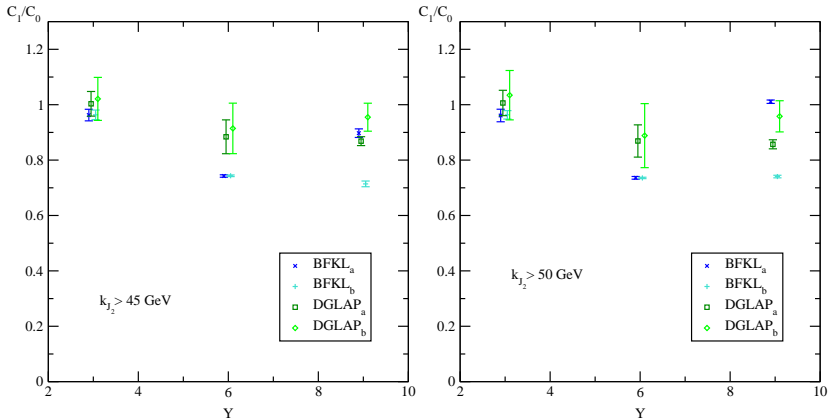
- **Numerical tools:** FORTRAN + NLO MSTW 2008 PDFs + CERLIB

→ weak time dependence on multidimensional integration ranges

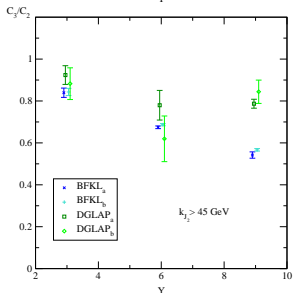
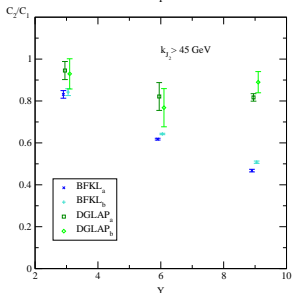
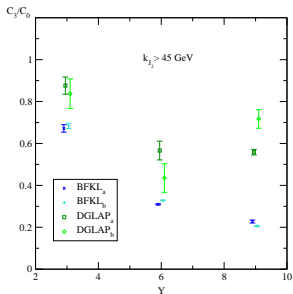
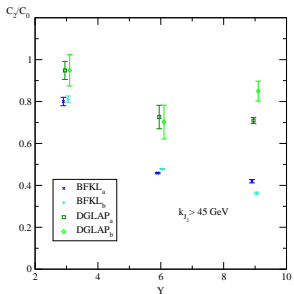
[A.D. Martin, W.J. Stirling, R.S. Thorne, G. Watt, (2009)]

<http://cernlib.web.cern.ch/cernlib>

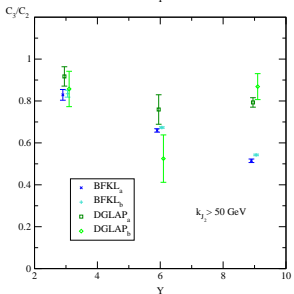
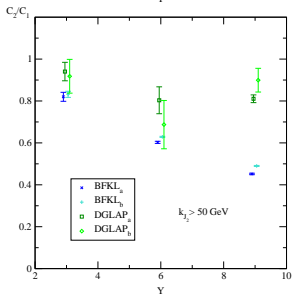
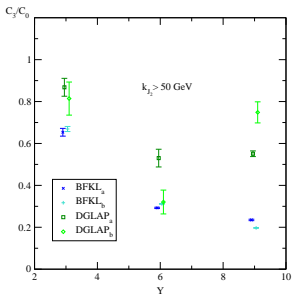
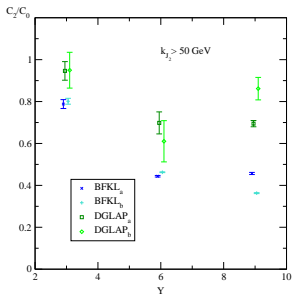
$$C_1/C_0$$



R_{nm} for $k_{J_2} > 45$ GeV



R_{nm} for $k_{J_2} > 50$ GeV



Conclusions

Comparison of predictions for several R_{nm} in full NLA BFKL approach and in NLO high-energy DGLAP.

- Implementation of a partial **BLM method** $\xrightarrow{\text{with}}$ two different optimized choices of scale!
- Asymmetric kinematics of detected jets:
 - $k_{J_1} > 35$ GeV and $k_{J_2} > 45$ GeV
 - $k_{J_1} > 35$ GeV and $k_{J_2} > 50$ GeV.

⇒ it exhibit a difference between **BFKL** and **DGLAP** growing with energy!



We strongly suggest experimentalist collaborations to consider also asymmetric kinematics in all future analyses of Mueller-Navelet jet production process!

**Thanks for your
attention!!**

BACKUP slides

The BFKL BLM cross section

$$a) \quad (\mu_R^{BLM})^2 = k_1 k_2 \exp \left[2 \left(1 + \frac{2}{3} l \right) - f(v) - \frac{5}{3} \right] \sim 5^2 k_1 k_2$$

$$b) \quad (\mu_R^{BLM})^2 = k_1 k_2 \exp \left[2 \left(1 + \frac{2}{3} l \right) - 2 f(v) - \frac{5}{3} + \frac{1}{2} \chi(v, n) \right] < (11.5)^2 k_1 k_2$$

$$\begin{aligned} C_n^{\text{BFKL}(a)} &= \frac{x_{J_1} x_{J_2}}{|\vec{k}_{J_1}| |\vec{k}_{J_2}|} \int_{-\infty}^{+\infty} dv e^{(Y-Y_0) \left[\bar{\alpha}_s(\mu_R) \chi(n, v) + \bar{\alpha}_s^2(\mu_R) \left(\bar{\chi}(n, v) - \frac{T^\beta}{C_A} \chi(n, v) - \frac{\beta_0}{8C_A} \chi^2(n, v) \right) \right]} \\ &\quad \times \alpha_s^2(\mu_R) c_1(n, v, |\vec{k}_{J_1}|, x_{J_1}) c_2(n, v, |\vec{k}_{J_2}|, x_{J_2}) \\ &\quad \times \left[1 - \frac{2}{\pi} \alpha_s(\mu_R) T^\beta + \alpha_s(\mu_R) \left(\frac{\bar{c}_1^{(1)}(n, v, |\vec{k}_{J_1}|, x_{J_1})}{c_1(n, v, |\vec{k}_{J_1}|, x_{J_1})} + \frac{\bar{c}_2^{(1)}(n, v, |\vec{k}_{J_2}|, x_{J_2})}{c_2(n, v, |\vec{k}_{J_2}|, x_{J_2})} \right) \right] \end{aligned}$$

$$\begin{aligned} C_n^{\text{BFKL}(b)} &= \frac{x_{J_1} x_{J_2}}{|\vec{k}_{J_1}| |\vec{k}_{J_2}|} \int_{-\infty}^{+\infty} dv e^{(Y-Y_0) \left[\bar{\alpha}_s(\mu_R) \chi(n, v) + \bar{\alpha}_s^2(\mu_R) \left(\bar{\chi}(n, v) - \frac{T^\beta}{C_A} \chi(n, v) \right) \right]} \\ &\quad \times \alpha_s^2(\mu_R) c_1(n, v, |\vec{k}_{J_1}|, x_{J_1}) c_2(n, v, |\vec{k}_{J_2}|, x_{J_2}) \\ &\quad \times \left[1 + \alpha_s(\mu_R) \left(\frac{\beta_0}{4\pi} \chi(n, v) - 2 \frac{T^\beta}{\pi} \right) + \alpha_s(\mu_R) \left(\frac{\bar{c}_1^{(1)}(n, v, |\vec{k}_{J_1}|, x_{J_1})}{c_1(n, v, |\vec{k}_{J_1}|, x_{J_1})} + \frac{\bar{c}_2^{(1)}(n, v, |\vec{k}_{J_2}|, x_{J_2})}{c_2(n, v, |\vec{k}_{J_2}|, x_{J_2})} \right) \right] \end{aligned}$$

The DGLAP BLM cross section

$$a) \quad (\mu_R^{BLM})^2 = k_1 k_2 \exp \left[2 \left(1 + \frac{2}{3} I \right) - f(v) - \frac{5}{3} \right] \sim 5^2 k_1 k_2$$

$$b) \quad (\mu_R^{BLM})^2 = k_1 k_2 \exp \left[2 \left(1 + \frac{2}{3} I \right) - 2 f(v) - \frac{5}{3} + \frac{1}{2} \chi(v, n) \right] < (11.5)^2 k_1 k_2$$

$$\begin{aligned} C_n^{\text{DGLAP(a)}} &= \frac{x_{J_1} x_{J_2}}{|\vec{k}_{J_1}| |\vec{k}_{J_2}|} \int_{-\infty}^{+\infty} dv \alpha_s^2(\mu_R) c_1(n, v, |\vec{k}_{J_1}|, x_{J_1}) c_2(n, v, |\vec{k}_{J_2}|, x_{J_2}) \\ &\quad \times \left[1 - \frac{2}{\pi} \alpha_s(\mu_R) T^\beta + \bar{\alpha}_s(\mu_R) (Y - Y_0) \chi(n, v) \right. \\ &\quad \left. + \alpha_s(\mu_R) \left(\frac{\bar{c}_1^{(1)}(n, v, |\vec{k}_{J_1}|, x_{J_1})}{c_1(n, v, |\vec{k}_{J_1}|, x_{J_1})} + \frac{\bar{c}_2^{(1)}(n, v, |\vec{k}_{J_2}|, x_{J_2})}{c_2(n, v, |\vec{k}_{J_2}|, x_{J_2})} \right) \right] \end{aligned}$$

$$\begin{aligned} C_n^{\text{DGLAP(b)}} &= \frac{x_{J_1} x_{J_2}}{|\vec{k}_{J_1}| |\vec{k}_{J_2}|} \int_{-\infty}^{+\infty} dv \alpha_s^2(\mu_R) c_1(n, v, |\vec{k}_{J_1}|, x_{J_1}) c_2(n, v, |\vec{k}_{J_2}|, x_{J_2}) \\ &\quad \times \left[1 + \alpha_s(\mu_R) \left(\frac{\beta_0}{4\pi} \chi(n, v) - 2 \frac{T^\beta}{\pi} \right) + \bar{\alpha}_s(\mu_R) (Y - Y_0) \chi(n, v) \right. \\ &\quad \left. + \alpha_s(\mu_R) \left(\frac{\bar{c}_1^{(1)}(n, v, |\vec{k}_{J_1}|, x_{J_1})}{c_1(n, v, |\vec{k}_{J_1}|, x_{J_1})} + \frac{\bar{c}_2^{(1)}(n, v, |\vec{k}_{J_2}|, x_{J_2})}{c_2(n, v, |\vec{k}_{J_2}|, x_{J_2})} \right) \right] \end{aligned}$$

Why BLM? MN jets - symmetric kinematics

